



1 Process-based evaluation of green roof models for
2 assessment of heat mitigation efficacy in WRF (v4.3.1) and
3 EnergyPlus (v8.6.0)

4 Maria Martinez Mendoza¹, Alireza Saeedi², James A. Voogt¹, E. Scott Krayenhoff²

5 ¹Department of Geography and Environment, The University of Western Ontario, London,
6 Ontario, Canada.

7 ²School of Environmental Sciences, University of Guelph, Guelph, Ontario, Canada.

8 *Correspondence to:* Maria Martinez Mendoza (mmart376@uwo.ca)

9 **Abstract.** Green roofs mitigate urban heat, but to fully assess their impact, green roof models must
10 be integrated into urban climate models, where they provide critical surface boundary conditions.
11 Ensuring their reliability requires evaluation, yet such efforts remain limited in the literature. This
12 study addresses that gap by evaluating two configurations of EcoRoof, the green roof module from
13 EnergyPlus (ER_o for the original version of the model, and ER_m for a modified version), and a
14 multilayer green roof parametrization for WRF (WRF-MLGR) (Heusinger et al., 2018; Sailor,
15 2008; Zonato et al., 2021). These models were tested against field observations from a monitored
16 green roof in London, Ontario, focusing on latent heat flux (Q_e), surface temperature (T_{surf}), storage
17 heat flux (Q_g) and soil water content (SWC). Model performance varied by variable. The two
18 EcoRoof versions showed similar performance, with mean RMSE across study periods of
19 approximately 56-60 W m⁻² for Q_e , 3-4 °C for T_{surf} , 22 W m⁻² for Q_g , and 0.03 m³ m⁻³ for SWC.
20 Performance for Q_e was comparable across models; however, WRF-MLGR exhibited much larger
21 errors for Q_g (with mean RMSE exceeding 100 W m⁻²) and SWC (0.06 m³ m⁻³), along with higher
22 T_{surf} deviations (~5 °C). Overall, EcoRoof provided a more consistent representation of the daytime
23 energy balance, whereas WRF-MLGR showed structural biases in surface heating. These findings
24 highlight the importance of process-level evaluation for urban climate applications and underscore
25 the need for continued model development to address the structural limitations in green roof
26 parametrizations.



27 **1. Introduction**

28 Green roofs have emerged as a promising technology to enhance urban resilience. They consist of
29 vegetation on the rooftops of buildings and offer numerous environmental benefits, such as
30 mitigating urban heat, reducing building energy use, reducing stormwater runoff and contributing
31 to biodiversity and urban livability (Berardi et al., 2014; Oberndorfer et al., 2007; Shafique et al.,
32 2018). Their ability to influence the surface energy balance makes them particularly valuable as
33 an urban heat adaptation strategy. Vegetation and moist growing media redirect energy into the
34 latent heat flux through evapotranspiration, thereby reducing sensible heat flux to the atmosphere,
35 while the soil's thermal mass dampens diurnal temperature extremes (Li et al., 2014) and acts as a
36 layer of insulation providing year round benefit to the host building.

37 To capture these effects at the city scale, green roofs must be incorporated into urban canopy
38 models, where reliable parameterizations can provide critical surface boundary conditions for
39 simulations of urban climate adaptation. Rigorous evaluation of their underlying energy-balance
40 schemes is essential for reliable integration into city-scale applications (Krayenhoff et al. 2021).
41 While many studies include green roofs as an adaptation measure (Berardi, 2016; He et al., 2020;
42 Heusinger and Weber, 2017; Jaffal et al., 2012; Kim et al., 2024; Krayenhoff et al., 2003; Liu and
43 Minor, 2005; Martens et al., 2008; Seo et al., 2023; Silva et al., 2016; Zheng et al., 2022), most
44 rely on parameterizations without thoroughly assessing model performance. Furthermore, when
45 evaluation is performed, it usually focuses on outcome variables such as surface or soil
46 temperature. Krayenhoff et al. (2021) emphasize that evaluating surface energy fluxes (i.e., the
47 physical processes) offers a more robust insight and is essential to ensure accurate and dependable
48 results.

49 As part of ongoing efforts to improve green-roof representation in urban canopy models (Siddiqui
50 et al., 2022), we evaluate two existing green-roof models: EcoRoof included in EnergyPlus (Sailor,
51 2008) and a green roof model coupled in the multi-layer urban canopy model BEP-BEM (Martilli
52 et al. 2002) within the Weather and Research Forecasting model (WRF), hereafter referred to as
53 WRF-MLGR (Zonato et al. 2021). These models were selected based on their availability,
54 exportability, and potential integration into the GEM-TEB urban climate modelling framework.
55 They represent contrasting levels of structural complexity and are embedded within widely used



56 building and atmospheric modelling systems, making them strong candidates for comparative
57 assessment.

58 Despite their widespread use, both models have rarely been subject to comprehensive evaluation.
59 For EcoRoof, most applications emphasize thermal behavior or energy savings without model
60 evaluation (e.g. Cascone et al. 2018; Zheng & Weng 2020; Costanzo et al. 2016). Studies that do
61 include some form of evaluation, such as Silva et al. (2016) and Karachaliou et al. (2016), do not
62 explicitly assess surface energy fluxes. Similarly, WRF-MLGR was first introduced by Zonato et
63 al. (2021) within the WRF-BEP-BEM framework (Martilli et al., 2002; Salamanca et al., 2010),
64 and its implementation rather than evaluation was emphasized. Applications of other WRF
65 configurations (e.g. Kalogeri et al. 2023; and Imran et al. 2018) follow the same pattern of focusing
66 on implementation rather than evaluation, and while some efforts at evaluation exist (e.g. Khan et
67 al. 2023; Sun et al. 2016), these remain limited in scope.

68 Taken together, these examples highlight a common trend in literature: while these models are
69 widely applied to estimate cooling potential, energy performance or inform design and policy
70 decisions, their predictive accuracy is rarely scrutinized. This underscores the need for systematic
71 evaluation of green roof models. To address this gap, we evaluate EcoRoof and WRF-MLGR
72 against observations from a green roof test array. Specifically, we ask: (a) how well does each
73 model reproduce fluxes (Q_e , Q_g) and T_{surf} during multi-month periods? (b) How does model
74 performance change across different moisture regimes and radiative forcing conditions? and (c)
75 how accurately do they simulate soil water content dynamics during and after precipitation events?

76 2. Methods

77 2.1 Site and experimental setup

78 The study site for this research is a green roof located on the rooftop of the Talbot College building,
79 at Western University, London, Ontario, Canada. The green roof plot is composed of individual
80 modules placed side by side, with dimensions of 0.3 m x 0.3 m and depths of 0.10 m and 0.15 m.
81 The green roof does not completely cover the roof area; Fig. 1 shows a photograph of the green
82 roof setting. It has three different types of vegetation: *Sedum spurium*, *Aquilegia canadensis*, and
83 *Sporobolus heterolepis*.

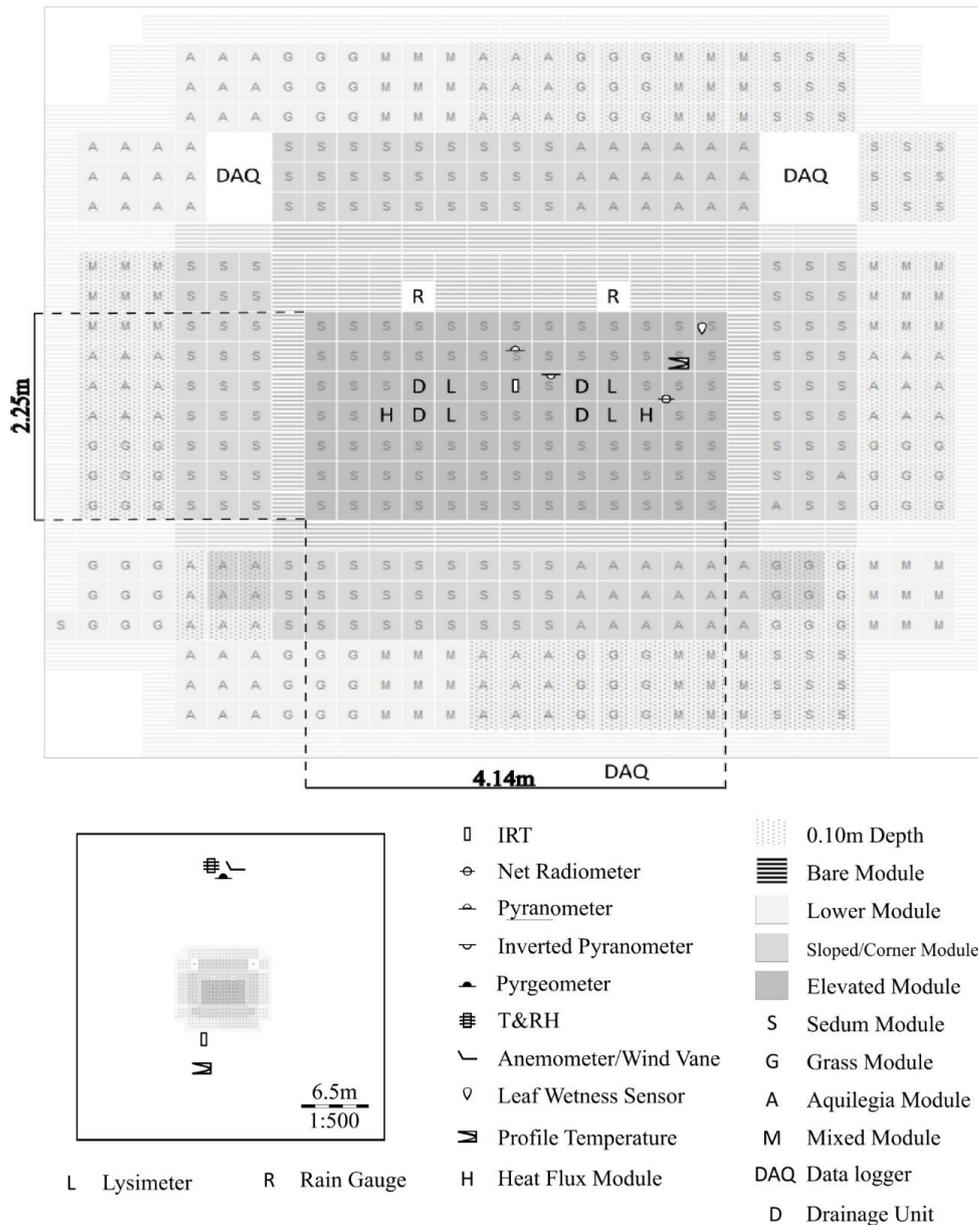


Figure 1: The green roof test array on Talbot College at Western University. Photo credit: J. Voogt

84 For this study, the observational data comes from a central array within the green roof which is
85 elevated from the roof surface to allow the installation of lysimeters. The array consists of modules
86 planted exclusively with *Sedum spurium*. The growing media was previously characterized by
87 Perelli (2014) and was constructed as a homogeneous 0.15 m layer, with no intentional vertical
88 differentiation in material composition. For analysis purposes, however, the substrate was treated
89 analytically as a 2.5 cm surface layer and a 12.5 cm subsurface layer, reflecting sensor placement
90 and root distribution rather than distinct physical layers within the growing medium.

91 **2.2 Data collection and observed variables**

92 This research uses observational data from the summer and fall seasons of 2014, collected from
93 July 1st to October 31st, 2014. Details about the measured variables and instrumentation used can
94 be found in Sect. S1 of the supplementary materials and on Kurukulaarachchi (2017). Energy-
95 balance components and microclimate variables were sampled at 1-second intervals and
96 subsequently averaged and stored at 5-minute resolution, lysimeters, rain gauges and drainage
97 units were averaged (or totaled, as appropriate) over 1-minute intervals. A conceptual diagram of
98 the green roof instrumentation set up is shown in Fig. 2.



99

100 **Figure 2: Green roof conceptual diagram (Kurukulaarachchi, 2017)**

101 **2.3 Selection of study periods and evaluation criteria**

102 **2.3.1 Selection of analysis periods**



103 To evaluate model performance, two analysis periods of 62 days were selected, each encompassing
104 multiple precipitation events interspersed with drying intervals. Period selection was guided by a
105 monthly stratification of the dataset, for which summary statistics (mean, standard deviation, and
106 25th, 50th, and 75th percentiles) were computed for net radiation, air temperature, vapor pressure
107 deficit (VPD), and wind speed. Based on similarities in these environmental characteristics, July–
108 August was grouped as ‘summer’ and September–October as ‘fall’. These labels are used only for
109 descriptive convenience and do not correspond to full meteorological seasons.

110 Two additional subsets were defined to isolate model performance under contrasting
111 environmental conditions: dry versus rainy days and low versus high net radiation (Q^*). For the
112 moisture-based classification, a daily rainfall threshold of > 5 mm was used to identify rainy days,
113 while dry days were defined as having < 0.2 mm of rainfall on the target day and during the
114 preceding two days. This classification yielded 15 rainy days in summer and 11 in fall, and 13 dry
115 days in summer and 14 in fall.

116 For the radiation-based classification, high- and low-net radiation days were identified using
117 percentile thresholds: days below the 25th percentile of daytime mean net radiation were classified
118 as low-net radiation conditions, and days above the 75th percentile were classified as high-net
119 radiation conditions. This procedure resulted in 31 low-net radiation days and 31 high-net radiation
120 days across the analysis periods.

121 **2.3.2 Evaluation criteria and data exclusions**

122 Although the model simulates energy balance continuously, the focus of the evaluation is not on
123 the accuracy of fluxes during precipitation itself, but rather on how well the model responds to
124 rainfall inputs over time. To isolate this response, time steps with active precipitation (rainfall $>$
125 0.2 mm) were excluded at the analysis stage. This approach is consistent with the study objectives,
126 as Q_e cannot be reliably estimated from lysimeters measurements during rainfall and moreover,
127 evapotranspiration is minimal under these conditions due to high humidity and reduced vapor
128 pressure gradients.

129 The evaluation was restricted to daytime conditions ($Q^* > 0$), when surface energy exchanges are
130 dominated by radiative forcing and turbulent fluxes are most pronounced. In addition, time steps



131 affected by instrument malfunction, calibration activities, or missing data were removed. All
132 exclusions were applied only to the observed and modeled outputs used for evaluation; the
133 simulations themselves were performed using the complete forcing datasets.

134 **2.4 Derivation of observed energy balance**

135 **2.4.1 Energy balance framework and assumptions**

136 The experimental green roof used in this study occupies only a portion of the roof surface (Fig. 1),
137 surrounded by conventional roofing material, introducing potential for advective effects, as
138 thermal gradients between the vegetated and bare roof surfaces may influence heat exchange.
139 Kurukulaarachchi (2017) analyzed selected drying periods from 2014 and found that only 2.8% of
140 the data showed possible signs of advection, with strong evidence present in just 1.2% of the cases.
141 Advection in that study was identified under specific conditions—such as temperature inversions,
142 wind directions associated with a large fetch across the bare roof surface, and large temperature
143 differences between the green roof and surrounding surfaces—indicating the movement of warm,
144 dry air across the vegetated modules.

145 Based on these findings, advective influences are expected to be minimal in the present dataset.
146 Accordingly, the observational surface energy balance is formulated under the assumption of
147 negligible horizontal energy fluxes, and is expressed as:

$$148 \quad Q^* = Q_e + Q_h + Q_g \quad (1)$$

149 Before calculating observed Q_e and Q_g , the raw data underwent processing steps to ensure physical
150 consistency and compatibility among variables. These steps included computing lysimeter weight
151 changes, converting precipitation and drainage data into equivalent depths, deriving soil water
152 content from lysimeter measurements, and estimating a soil heat capacity that accounts for changes
153 in moisture. Observed Q_e was taken as the average of the two lysimeter-derived (northeast and
154 southeast) estimates, whereas Q_g was derived from one module only (west module) due to
155 extensive missing data in the other module. In addition, the radiative measurement of T_{surf} was
156 corrected using an emissivity of 0.96 (Kurukulaarachchi, 2017), and the measured incident
157 longwave radiation to represent kinetic temperature. Detailed derivations and processing steps for
158 all variables are provided in Sect. S2 of the supplementary materials.



159 **2.5 Green Roof Energy Balance Models**

160 **2.5.1 Comparison of Model Approaches**

161 The models to be compared are stand-alone versions of ER—an original version of the model, as
 162 found withing EnergyPlus v8.6.0 (Sailor, 2008), and a modified configuration following
 163 Heusinger et al. (2018)—and a stand-alone version of the green roof parametrization embedded in
 164 WRF v.4.3.1 (Zonato et al., 2021). Table 1 provides an overview of each model.

165 **Table 1: Green roof model overview.**

Characteristic	Model		
	ER _o (Sailor, 2008)	ER _m Heusinger et al. (2018)	WRF-MLGR (Zonato et al., 2021)
Dimensionality	One dimension (vertical).	One dimension (vertical).	One dimension (vertical).
Number of Layers	Two soil layers (a surface layer and a subsurface layer).	Two soil layers (a surface layer and a subsurface layer).	Ten layers (four corresponding to the built roof below six corresponding to the green roof soil).
Energy balance calculation	Separate assessment of energy balance for the foliage layer and for the soil surface.	Separate assessment of energy balance for the foliage layer and for the soil surface.	Lumped energy processes for foliage and soil surface with no explicit separation of canopy.
Radiative exchange	Accounts for long-wave and short-wave radiative exchange between plant canopy and soil.	Accounts for long-wave and short-wave radiative exchange between plant canopy and soil.	Calculates net radiation but does not detail intra-canopy or canopy-soil radiative exchanges.



Convective heat transfer	Two-layer resistance-based model with explicit canopy air space	Two-layer resistance-based model with explicit canopy air space	Bulk aerodynamic method without soil-vegetation flux partitioning.
Evapotranspiration	Accounts for soil evaporation and plant transpiration, with stomatal resistance being influenced by environmental factors.	Accounts for soil evaporation, plant transpiration (influenced by environmental factors), and evaporation of intercepted rainfall.	Includes only plant transpiration influenced by environmental conditions; no soil evaporation.
Heat conduction and storage	Fourier's law.	Fourier's law.	Fourier's law.
Soil thermal properties	Moisture-dependent.	Moisture-dependent.	Moisture-dependent.
Runoff/drainage	Occurs when rainfall exceeds a fixed infiltration threshold and when layers exceed saturation; drainage from the subsurface layer conductivity-based.	Includes canopy interception with drip to the soil and replaces fixed infiltration threshold with moisture-dependent surface runoff calculation.	Drainage occurs from the bottom layer using a moisture-dependent conductivity function. Does not include explicit surface runoff or canopy interception.

166 **2.5.2 Model set up**

167 In addition to input parameters, which need to be specified in the program, the models require an
 168 input file with atmospheric forcing data, which is common to both models. It consists of time series
 169 measurements of eight variables: incoming solar radiation, incoming longwave radiation, wind
 170 speed, air temperature, humidity, precipitation, air pressure and irrigation. Most variables were
 171 directly measured on site, except air pressure, which was retrieved from London A weather station
 172 (WMO ID: 71623), located at London International Airport. The models also require certain



173 variables to be initialized, the specific variables vary according to the model and are specified in
174 Sect. S5 of the supplementary materials, along with the input parameters required by the models.
175 The models are initialized (forcing file starts) at 03:00 LT on the first day of the period and end at
176 23:00 LT on the last day of the period. The timesteps are 5 minutes long and the values used for
177 the initialization correspond to the value at the 03:00 time step for all variables except albedo,
178 which is an average.

179 **2.6 Evaluation metrics**

180 For the model evaluation a quantitative analysis was performed to compare modeled and observed
181 values. The statistical metrics calculated are Mean Absolute Error (MAE), Mean Bias Error (MBE)
182 and Root Mean Square Error (RMSE); along with the statistical method for model evaluation
183 outlined by Willmott (1982), Willmott et al. (1985) and Willmott et al. (2012). This includes the
184 separation of RMSE into its systematic (RMSE_s), and unsystematic (RMSE_u) components, and the
185 Index of agreement. For this study the refined version of the Index of agreement (d_r) is used (Eq.
186 2 and Eq. 3), given that it includes improvements from the original version.

$$187 \quad 1 - \frac{\sum_{i=1}^n |\hat{y}_i - y_i|}{C \sum_{i=1}^n |y_i - \bar{y}|}, \text{ when} \quad (2)$$

$$188 \quad \sum_{i=1}^n |\hat{y}_i - y_i| \leq C \sum_{i=1}^n |y_i - \bar{y}|, \text{ or}$$

$$189 \quad \frac{C \sum_{i=1}^n |y_i - \bar{y}|}{\sum_{i=1}^n |\hat{y}_i - y_i|} - 1, \text{ when} \quad (3)$$

$$190 \quad \sum_{i=1}^n |\hat{y}_i - y_i| > C \sum_{i=1}^n |y_i - \bar{y}|$$

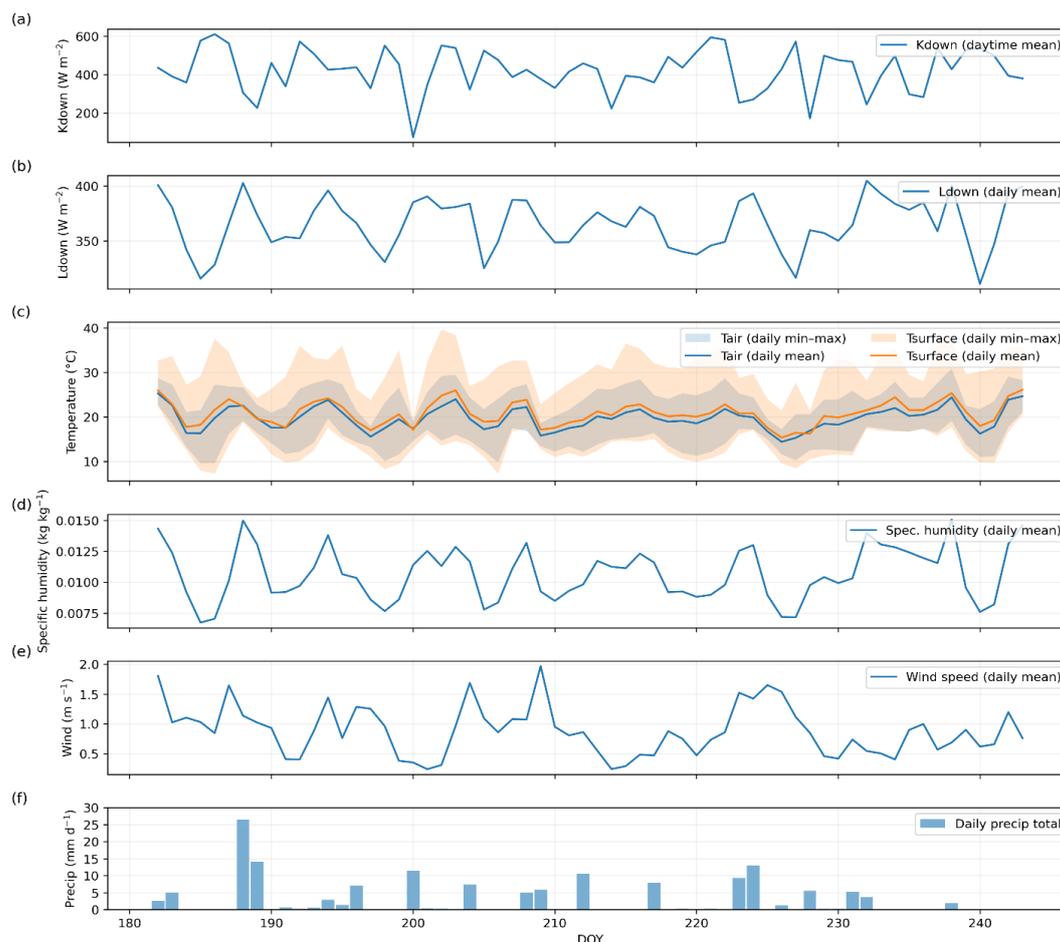
191 where n is the number of observations of y , y_i is the i th observation, \bar{y} is the mean, \hat{y}_i represents
192 the modeled value and C is a constant, equal to 2. The improvements of this version include an
193 index range that is double of the original (range from -1 to 1), which provides greater separation
194 when comparing models that perform relatively well, and the use of absolute rather than squared
195 differences, which makes the index less sensitive to outliers (Willmott et al., 2012). The better
196 performing green roof model should have lower values of RMSE and higher RMSE_u relative to
197 RMSE_s; and a d_r value closer to 1 (Comer et al., 2000; Willmott et al., 2012).



198 **3. Results**

199 **3.1 Weather conditions**

200 During the summer period (DOY 182–243), conditions show persistently high daytime mean
201 incoming shortwave radiation and relatively stable daily mean incoming longwave radiation. Daily
202 mean air and surface temperatures remain elevated throughout the period, with surface
203 temperatures consistently exceeding air temperatures, and exhibiting a relatively wide daytime
204 temperature range as indicated by the min–max envelopes. Specific humidity shows moderate
205 variability, with lower daily mean values generally coinciding with warmer, clearer days. Daily
206 mean wind speeds remain low to moderate and vary mainly from day-to-day, indicating variability
207 driven by changing synoptic conditions. Precipitation occurs on a limited number of days, with
208 most events near 10 mm (Fig. 3).



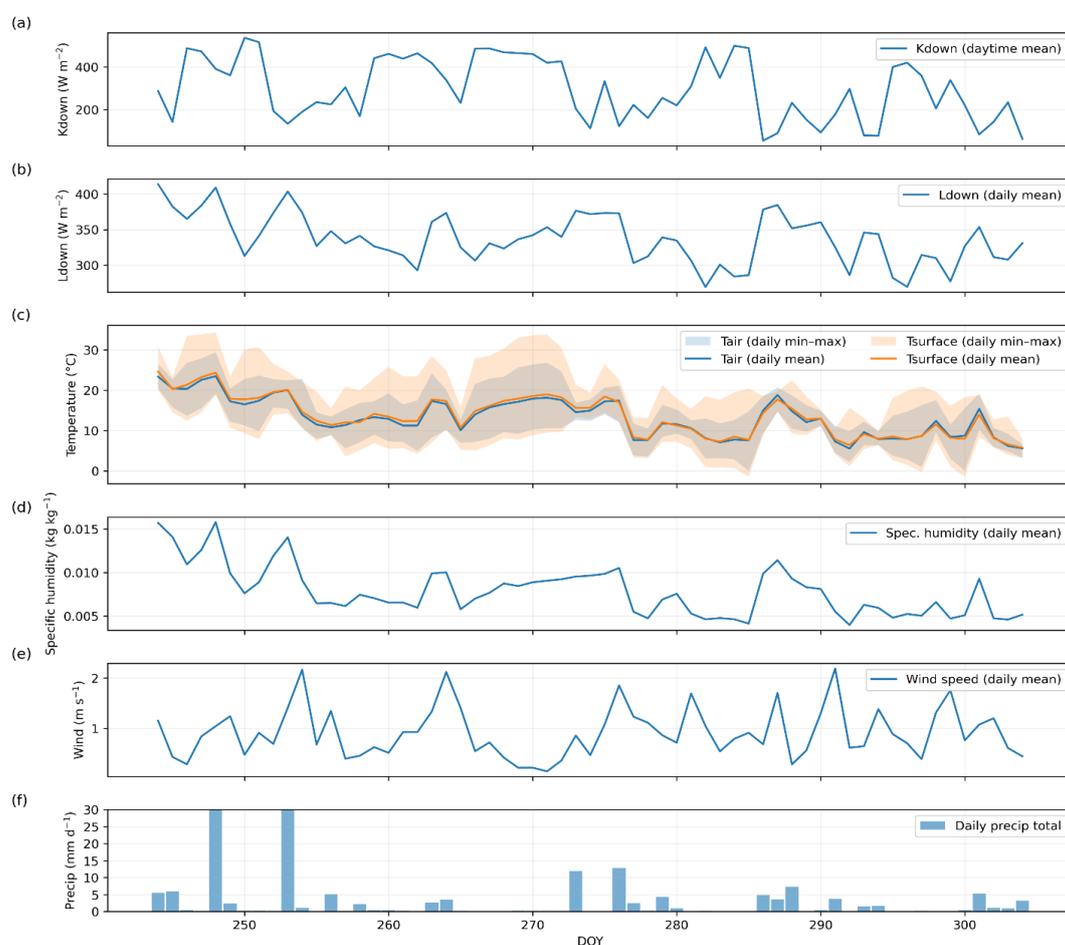
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210 **Figure 3: Weather conditions during the summer period. Panels a) and b) show daytime**
211 **mean incoming shortwave (Kdown) and daily mean longwave (Ldown) radiation,**
212 **respectively; panel c) shows daily mean air and surface temperatures with shaded envelopes**
213 **indicating the daily minimum–maximum temperature range.; panel d) shows daily mean**
214 **specific humidity; panel e) shows daily mean wind speed; and panel f) shows daily**
215 **precipitation totals.**

216 During the fall period (DOY 244–304), daytime mean incoming shortwave radiation decreases
217 relative to summer and shows greater day-to-day variability, while daily mean incoming longwave
218 radiation remains comparatively stable. Daily mean air and surface temperatures decline over the



219 period, and the daily temperature range becomes narrower. Daily mean specific humidity is
220 generally lower than during summer, consistent with cooler atmospheric conditions, while daily
221 mean wind speeds show increased day-to-day variability. Precipitation occurs on a similar number
222 of days as in summer, with most events below 10 mm and two significant larger rainfall events
223 (Fig. 4).



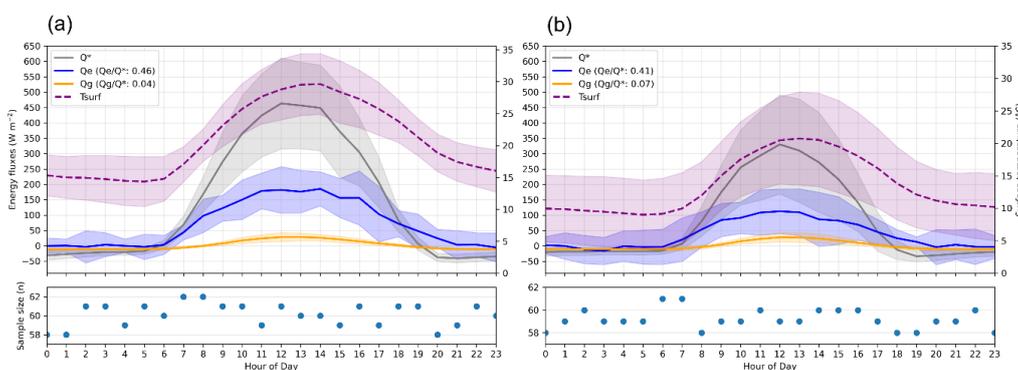
224
225 **Figure 4: Weather conditions during the fall period. Panels a) and b) show daytime mean**
226 **incoming shortwave (Kdown) and daily mean longwave (Ldown) radiation, respectively;**
227 **panel c) shows daily mean air and surface temperatures with shaded envelopes indicating**
228 **the daily minimum–maximum temperature range.; panel d) shows daily mean specific**



229 humidity; panel e) shows daily mean wind speed; and panel f) shows daily precipitation
230 totals.

231 3.2 Observed energy balance

232 To characterize the surface energy exchange at the study site, we first examined the observed
233 energy balance (Fig. 5). The hourly composites show a similar overall structure. In summer (Fig.
234 5a) mean Q^* peaks around $\sim 450 \text{ W m}^{-2}$ and is partitioned primarily into Q_h (50%), while Q_e
235 accounts for 46% of daytime energy and Q_g for roughly 4%. T_{surf} peaks near $\sim 30 \text{ }^\circ\text{C}$. In fall (Fig.
236 5b), all components decrease seasonally: midday mean Q^* is $\sim 300 \text{ W m}^{-2}$, Q_e represents 41% of
237 the energy and Q_g contributes 7% of the energy. T_{surf} peaks around $20 \text{ }^\circ\text{C}$.



238
239 **Figure 5: a) Hourly composite diurnal cycle of the observed energy balance components for**
240 **the summer period (June-August), and b) the fall period (September-October), lower panels**
241 **indicate the number of samples contributing to each hourly mean.**

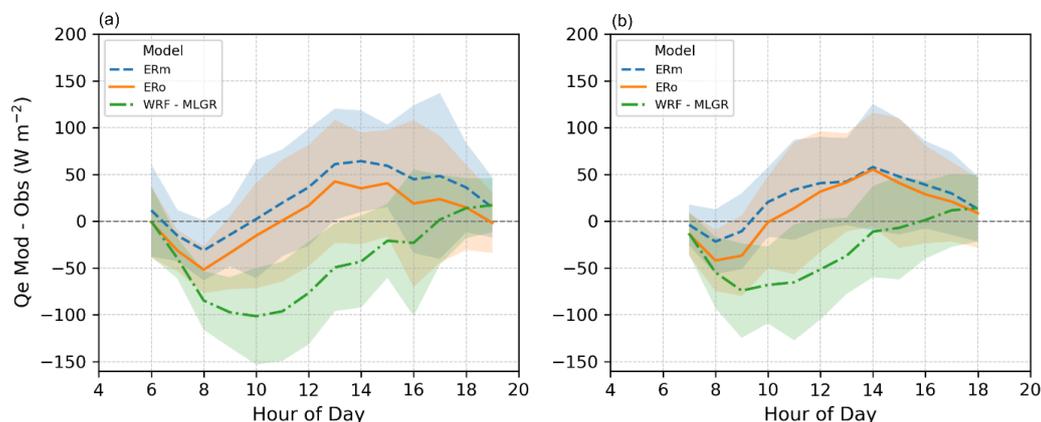
242 These composites illustrate how the green-roof energy balance evolves between periods, providing
243 a reference framework for the subsequent model evaluation. Observed uncertainties were
244 quantified using standard error propagation methods (Taylor, 1997), yielding mean daytime
245 uncertainties of $\pm 39 \text{ W m}^{-2}$ for Q_e and $\pm 14 \text{ W m}^{-2}$ for Q_g . This helps contextualize the significance
246 of the model–observation differences discussed below. Further details on the uncertainty
247 propagation are provided in Sect. S3 and S4 of the supplementary materials.



248 3.3 Comparative model evaluation

249 3.3.1 Latent heat flux

250 The hourly composites (Fig. 6) shows the two ER configurations (ER_o and ER_m) exhibiting early-
251 morning underestimations and an afternoon positive bias, peaking around $\sim 50 \text{ W m}^{-2}$. In contrast,
252 WRF-MLGR consistently underestimates Q_e during the morning, and most of the afternoon, with
253 biases reaching 100 W m^{-2} , later in the afternoon the model switches to overestimations. The
254 shaded envelopes show larger variability for ER than for WRF-MLGR. In the summer period (Fig.
255 6a), ER_o shows stronger early-morning underestimations but smaller midday overestimation than
256 ER_m , while WRF-MLGR maintains its predominantly negative bias, particularly in the morning.
257 In the fall period (Fig. 6b) all models show reduced amplitudes, but the same general patterns
258 persist: ER transitions from morning underestimation to afternoon overestimation and WRF-
259 MLGR remains negatively biased.



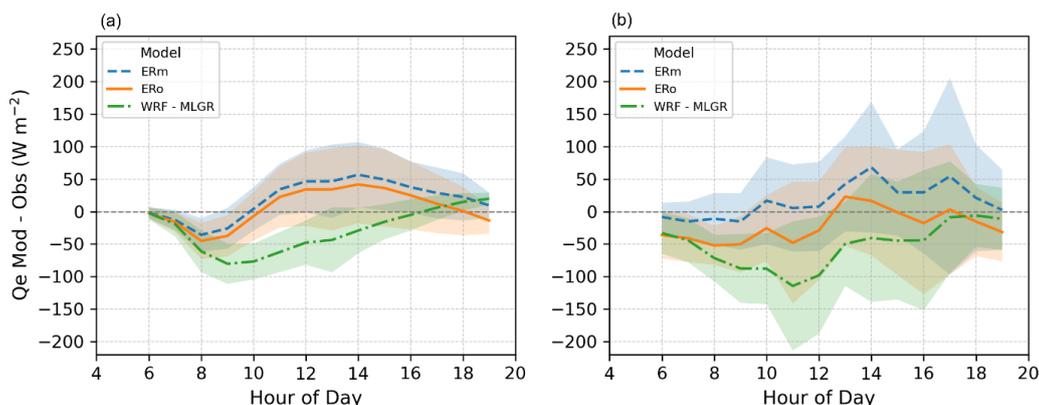
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261 **Figure 6: Hourly composite of the difference between modeled and observed Q_e for a) the**
262 **summer period and b) the fall period.**

263 Figure 7 presents the composite differences between modeled and observed Q_e —during daytime
264 hours without active precipitation—, separated into dry days ($< 0.2 \text{ mm}$ of rainfall on the target
265 day and during the preceding two days.; Fig. 7a) and rainy days (daily rainfall $> 5 \text{ mm}$; Fig. 7b).
266 On dry days, model behavior closely resembles that of the full-period composites and shows
267 relatively small variability. In contrast, rainy days exhibit substantially larger variability across all
268 models. The ER configurations retain the morning-to-afternoon bias reversal but with less

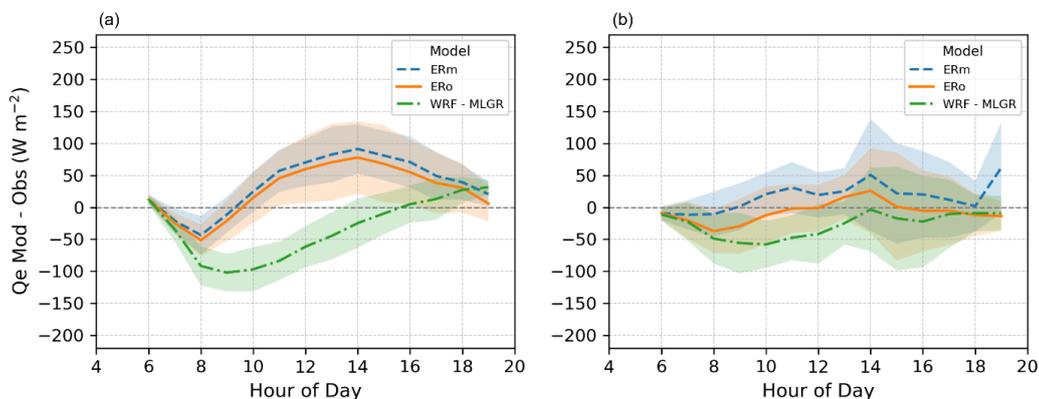


269 consistent timing and a wider spread, whereas WRF-MLGR shows strong and persistent
270 underestimation accompanied by a pronounced spread.



271
272 **Figure 7: Hourly composite of the difference between modeled and observed Q_e for a) dry**
273 **days and b) rainy days.**

274 Days with high net radiation (Fig. 8a) reproduce the full-period diurnal pattern, with both ER
275 configurations showing slightly larger mean differences, and all models exhibiting a relatively
276 narrow spread. In contrast, low net radiation days (Fig. 8b) display a markedly different behavior,
277 characterized by substantially increased variability and much smaller mean biases across all
278 models.



279
280 **Figure 8: Hourly composite of the difference between modeled and observed Q_e for a) high**
281 **net radiation days and b) low net radiation days.**



282 The statistical metrics (Table 2) are consistent with these patterns. ER shows slightly superior
 283 performance during the summer period: both ER versions retain positive MBE yet achieve
 284 marginally lower MAE than WRF-MLGR and higher d_r values (both ER_o and $ER_m \approx 0.60$ vs 0.50).
 285 For the fall season MAE and d_r are very similar between ER_o and WRF-MLGR, while ER_m shows
 286 slightly lower MAE and higher d_r . RMSE decomposition shows that ER errors are dominated by
 287 unsystematic errors. WRF-MLGR shows the opposite behavior, with systematic underestimation
 288 dominating.

289 **Table 2: Statistical evaluation metrics for the Q_e for ER_o , ER_m , and WRF-MLGR models.**
 290 **Metrics include the Mean Absolute Error (MAE), Mean Bias Error (MBE), Root Mean**
 291 **Squared Error (RMSE), its unsystematic (RMSEu) and systematic (RMSEs) components,**
 292 **all in $W m^{-2}$ and refined index of agreement (d_r).**

	<i>ER - original</i>		<i>ER - modified</i>		<i>WRF-MLGR</i>	
	Summer	Fall	Summer	Fall	Summer	Fall
MAE	47.0	46.2	46.9	41.0	58.8	44.1
MBE	2.8	13.2	20.5	22.7	-48.8	-35.7
d_r	0.60	0.50	0.60	0.56	0.50	0.52
RMSE	60.7	60.0	59.3	53.0	77.6	61.6
RMSEu	60.5	58.2	55.4	47.8	47.4	38.6
RMSEs	4.6	14.5	21.2	22.8	61.4	48.0

293 3.3.2 Surface temperature

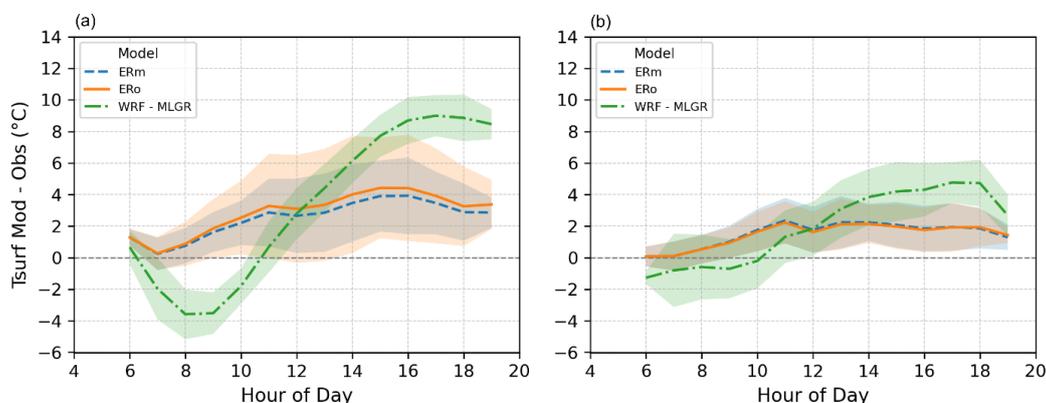
294 Both ER configurations show a persistent warm bias throughout the day, with the largest
 295 differences occurring in the afternoon. In contrast, WRF-MLGR shows a different pattern,
 296 characterized by morning underestimation followed by substantial afternoon overestimation.
 297 During the summer period both ER configurations maintain this warm bias and exhibit greater
 298 day-to-day variability than WRF-MLGR, particularly during the warmest hours. In the fall period,
 299 bias magnitudes are reduced for all models and variability decreases for ER, reflecting the overall
 300 weaker radiative forcing and more moderate surface temperatures (see Fig. S1 of supplementary
 301 materials).

302 Mean surface temperature biases are generally amplified under dry conditions and reduced on
 303 rainy days. This contrast is modest for the ER configurations, which maintain a similar warm bias
 304 across both moisture regimes, but is much more pronounced for WRF-MLGR. Under wetter



305 conditions, bias magnitudes and diurnal range are dampened, and variability decreases (see Fig.
306 S2 of supplementary materials).

307 High net radiation conditions (Fig. 9a) accentuate both diurnal temperature biases and variability.
308 Under these conditions, ER exhibits increased daytime variability, while WRF-MLGR shows a
309 comparatively narrower spread. Mean bias magnitudes remain comparable to those of the full
310 evaluation periods, although morning underestimation in WRF-MLGR is slightly enhanced under
311 strong radiative forcing. In contrast, low net-radiation conditions (Fig. 9b) are characterized by
312 substantially reduced mean temperature differences for all models, most notably for WRF-MLGR.
313 While variability in WRF-MLGR increases slightly under low net radiation conditions, the ER
314 configurations show more stable behavior.



315
316 **Figure 9: Hourly composite of the difference between modeled and observed T_{surf} for a)**
317 **high net radiation days and b) low net radiation days.**

318 Table 3 summarizes the statistical metrics for T_{surf} and reinforces the patterns seen in the diurnal
319 composites. All models exhibit positive MBE, confirming T_{surf} warm biases. ER shows lower MAE
320 values and higher d_r than WRF-MLGR in both periods, indicating smaller overall deviations from
321 observations. The RMSE decomposition shows that ER's errors are dominated by their systematic
322 component, consistent with the stable warm bias seen in the diurnal plots. WRF-MLGR, in
323 contrast, exhibits a greater contribution from the unsystematic component. However, this statistical
324 partitioning should not be interpreted as random variability. Rather, it reflects the consistent shift
325 from morning underestimation to afternoon overestimation within the daytime period. These



326 opposing biases partly offset each other in the MBE but remain large in magnitude, leading to
 327 elevated RMSE. Therefore, the large error components in WRF-MLGR indicate a structural timing
 328 and magnitude error in surface heating rather than random variability.

329 **Table 3: Statistical evaluation metrics for T_{surf} for ER_o, ER_m, and WRF-MLGR models.**
 330 **Metrics include the Mean Absolute Error (MAE), Mean Bias Error (MBE), Root Mean**
 331 **Squared Error (RMSE), its unsystematic (RMSE_u) and systematic (RMSE_s) components,**
 332 **all in °C, and refined index of agreement (d_r).**

	<i>ER - original</i>		<i>ER - modified</i>		<i>WRF-MLGR</i>	
	Summer	Fall	Summer	Fall	Summer	Fall
MAE	3.3	2.1	2.8	2.2	4.4	3.6
MBE	3.2	2.0	2.7	2.1	2.9	2.6
d_r	0.66	0.82	0.71	0.81	0.54	0.68
RMSE	4.4	2.6	3.6	2.7	5.4	4.6
RMSE _u	2.9	1.5	2.3	1.6	4.2	3.7
RMSE _s	3.3	2.1	2.8	2.2	3.3	2.7

333 3.3.3 Soil Heat Flux

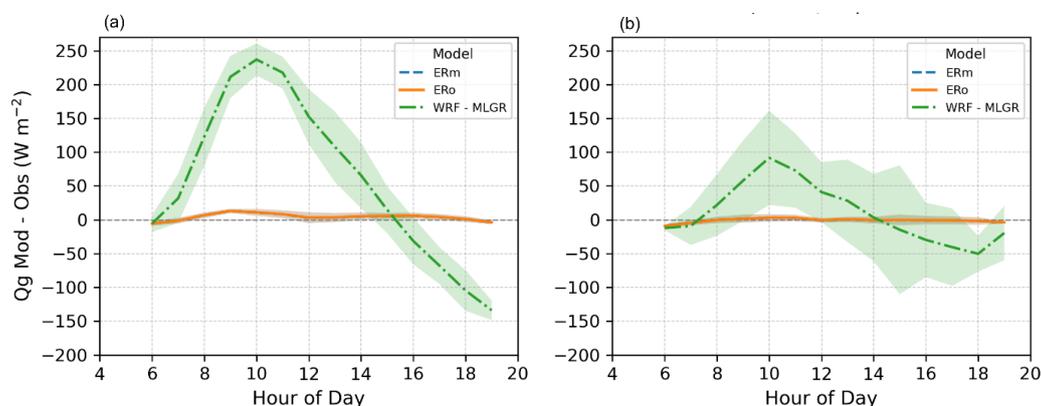
334 Q_g exhibits the largest model–observation discrepancies for WRF-MLGR in both evaluation
 335 periods. Bias magnitudes are substantially larger than for the ER configurations, with peak
 336 overestimations exceeding 200 W m^{-2} , followed by a reversal to substantial underestimation in the
 337 late afternoon. In contrast, both ER configurations remain close to observations, with small
 338 consistently positive biases and low variability. Seasonal differences are modest: WRF-MLGR
 339 errors are larger in summer, while ER shows similarly stable behavior across both seasons, with
 340 reduced variability during fall (see Fig. S3 of supplementary materials).

341 Mean Q_g differences are generally reduced during rainy days relative to dry conditions. Under
 342 rainy conditions, the ER configurations remain close to zero throughout the day, while WRF-
 343 MLGR shows a marked reduction in bias magnitude but a substantially wider spread, indicating
 344 increased variability and less consistent timing (see Fig. S4 of supplementary materials).

345 High net-radiation conditions (Fig. 10a) strongly amplify Q_g biases, particularly for WRF-MLGR,
 346 which exhibits large midday overestimations that peak near $\sim 250 \text{ W m}^{-2}$ and a relatively narrow



347 spread. In contrast, the ER configurations remain close to observations with limited variability.
348 Under low net radiation conditions (Fig. 10b) the magnitude of Q_g biases decreases for all models.
349 For WRF-MLGR, mean differences are substantially reduced, however, the spread widens
350 substantially, reflecting increased day-to-day variability under weaker radiative forcing.



351
352 **Figure 10: Hourly composite of the difference between modeled and observed Q_g for a)**
353 **high net radiation days and b) low net radiation days.**

354 Table 4 reinforces these contrasts. ER performs well, with both configurations showing nearly the
355 same performance during both seasons, in the fall they show modest MAE values ($\sim 7 \text{ W m}^{-2}$),
356 relatively high RMSE ($\sim 35 \text{ W m}^{-2}$) and high index of agreement ($d_r = 0.77$ for ER_o and 0.78 for
357 ER_m). The summer period shows a small MAE for both configurations ($\sim 7 \text{ W m}^{-2}$) and relatively
358 low RMSE ($\sim 9 \text{ W m}^{-2}$), these errors were dominated by the systematic component during the fall
359 period, and by the unsystematic component during the summer period.

360 In contrast, WRF-MLGR performs very poorly, showing very large MAE (83 W m^{-2} for the fall
361 and 103 W m^{-2} for the summer), RMSE (110 and 128 W m^{-2}), and strongly negative d_r values
362 (-0.64 and -0.75), indicating poor temporal agreement. As observed for T_{surf} , the RMSE
363 decomposition attributes a large portion of the error to the unsystematic component; however, the
364 diurnal composites display a consistent phase pattern. The large error magnitudes in WRF-MLGR
365 therefore reflect a systematic mismatch in the timing and magnitude of Q_g rather than random
366 variability.



367 **Table 4: Statistical evaluation metrics for the Q_g for ER_o, ER_m, and WRF-MLGR models.**
 368 **Metrics include the Mean Absolute Error (MAE), Mean Bias Error (MBE), Root Mean**
 369 **Squared Error (RMSE), its unsystematic (RMSE_u) and systematic (RMSE_s) components all**
 370 **in $W m^{-2}$, and refined index of agreement (d_r).**

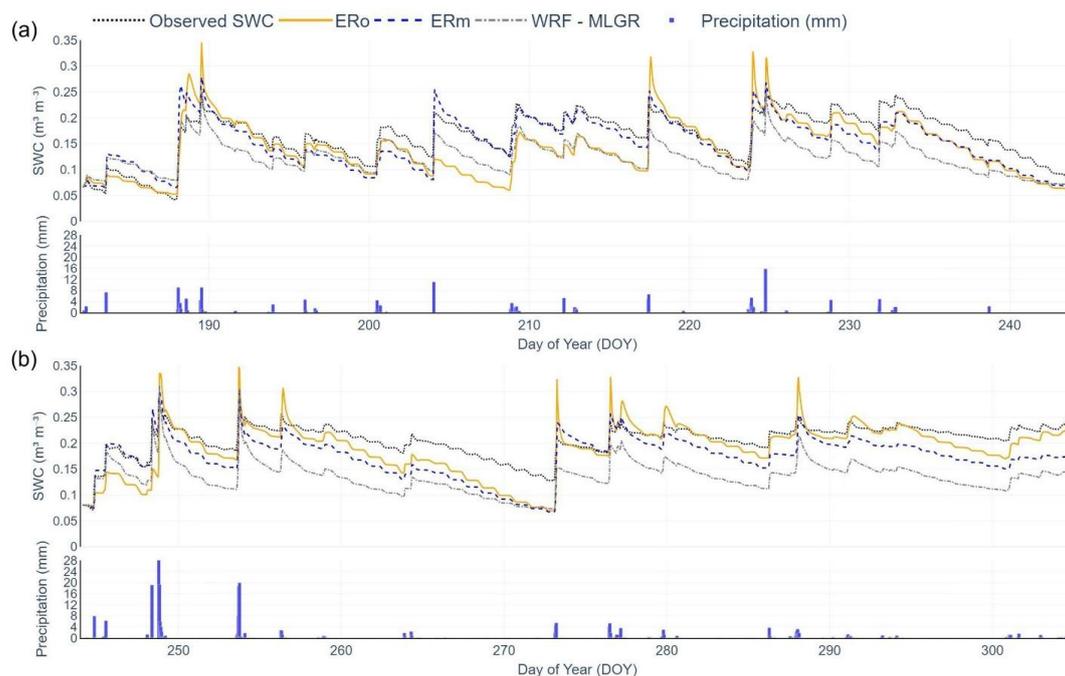
	<i>ER - original</i>		<i>ER - modified</i>		<i>WRF-MLGR</i>	
	Summer	Fall	Summer	Fall	Summer	Fall
MAE	7.0	6.9	7.3	6.7	103.3	82.9
MBE	4.2	3.8	4.3	3.6	63.9	46.6
d_r	0.73	0.77	0.72	0.78	-0.75	-0.64
RMSE	8.7	34.6	8.9	34.6	127.6	109.5
RMSE _u	7.3	16.2	7.4	15.9	97.6	99.0
RMSE _s	4.7	30.6	5.0	30.8	82.3	46.9

371 **3.3.4 Moisture content**

372 Figure 11 shows the evolution of observed and modeled water content throughout summer (Fig.
 373 11a) and fall (Fig. 11b). All models reproduce the timing of rainfall events, showing sharp
 374 increases in SWC after precipitation. However, the magnitude of these responses differs
 375 substantially across models.

376 During the summer period (Fig. 11a), ER_m shows the closest agreement with the observed peaks
 377 and subsequent dry-down trajectories. ER_o responds well to rainfall but generally produces larger
 378 peak values and drains more rapidly, leading to underestimation between events. WRF-MLGR
 379 consistently underpredicts SWC, with peak magnitudes consistently lower than observed and with
 380 faster post-rainfall declines.

381 In the fall period (Fig. 11b), the two ER configurations converge, producing very similar dynamics,
 382 with ER_o slightly closer to observations, particularly during the later part of the dry-downs. WRF-
 383 MLGR continues to reproduce the correct timing of wetting and drying but maintains well below
 384 observed magnitude.



385

386 **Figure 11: Time series of observed and modeled water content, with precipitation for a) the**
 387 **summer period and b) the fall period. Solid lines represent the model simulations (ER_o, ER_m,**
 388 **and WRF-MLGR), the dashed line shows the observations, and red bars indicate precipitation.**

389 Table 5 highlights the contrast in model performance for water content. All models show negative
 390 MBE, confirming overall underestimation. The MAE values for the ER configurations are
 391 relatively small ($0.030 \text{ m}^3 \text{ m}^{-3}$ in the summer and 0.022 in the fall for ER_o; $0.021 \text{ m}^3 \text{ m}^{-3}$ in the
 392 summer and 0.035 in the fall for ER_m), when compared with WRF-MLGR, which shows larger
 393 errors, with MAE reaching $0.045 \text{ m}^3 \text{ m}^{-3}$ in the summer and 0.070 in the fall. Model agreement
 394 follows the same trend: ER achieves moderate d_r values, with the original configuration
 395 performing more consistently. In contrast, WRF-MLGR yields d_r values near zero (or negative),
 396 indicating poor agreement in magnitude despite reproducing event timing; its strong systematic
 397 dry bias (relatively large negative MBE) and damped storage response dominate the agreement
 398 score. RMSE values also favor ER ($0.038 \text{ m}^3 \text{ m}^{-3}$ and 0.029 for ER_o; $0.025 \text{ m}^3 \text{ m}^{-3}$ and 0.039 for
 399 ER_m) over WRF-MLGR (0.048 and $0.073 \text{ m}^3 \text{ m}^{-3}$). For ER_o, RMSE reflects a balance of systematic
 400 and unsystematic components, while ER_m shows larger unsystematic errors during summer but



401 larger systematic errors in the fall. WRF-MLGR errors are dominated by systematic
 402 underestimation, consistent with its low storage representation.

403 **Table 5: Statistical evaluation metrics for the moisture content for ER_o, ER_m, and WRF-**
 404 **MLGR models. Metrics include the Mean Absolute Error (MAE), Mean Bias Error (MBE),**
 405 **Root Mean Squared Error (RMSE), its unsystematic (RMSE_u) and systematic (RMSE_s)**
 406 **components all in m³ m⁻³ and refined index of agreement (*d_r*).**

	<i>ER - original</i>		<i>ER - modified</i>		<i>WRF-MLGR</i>	
	Summer	Fall	Summer	Fall	Summer	Fall
MAE	0.030	0.022	0.021	0.035	0.045	0.070
MBE	-0.024	-0.018	-0.012	-0.032	-0.039	-0.070
<i>d_r</i>	0.601	0.514	0.719	0.234	0.397	-0.356
RMSE	0.038	0.029	0.025	0.039	0.048	0.073
RMSE _u	0.029	0.020	0.021	0.023	0.017	0.018
RMSE _s	0.025	0.021	0.013	0.032	0.045	0.071

407 **4. Discussion**

408 **4.1 Green roof observed energy balance**

409 Relatively few studies report all surface energy balance components for green roofs
 410 simultaneously; however, many report individual components. As a result, reported observational
 411 energy balance values span a wide range, reflecting differences in climate, vegetation type,
 412 substrate moisture conditions, roof configuration, and measurement approach.

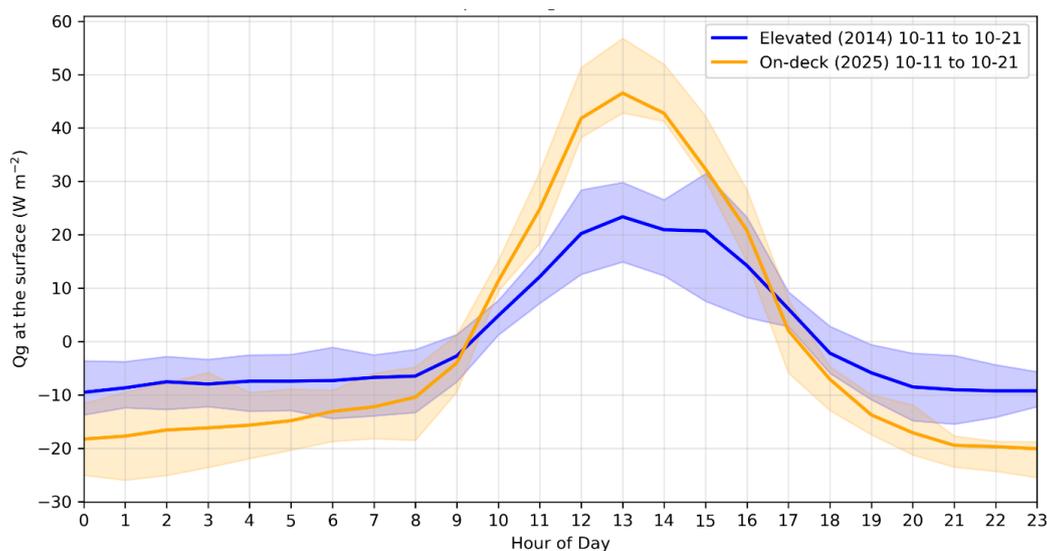
413 Q_e and/or evapotranspiration rate, is the most frequently evaluated component in the green-roof
 414 literature, given it plays an important role in the cooling potential and hydrology of green roofs.
 415 At our study site, Q_e represents approximately 46 % of the net radiation during the summer period
 416 and 41% during fall. These fractions correspond to a daily mean of 71 W m⁻² for the summer, and
 417 36 W m⁻² in the fall. These values are comparable in magnitude to those reported by in other green
 418 roof studies. Marasco et al. (2015), for example, observed daily mean Q_e values of approximately
 419 44–55 W m⁻² for two full-scale extensive Sedum roofs in New York City, averaged over multiple
 420 years. Gößner et al. (2025) similarly reported daily mean evapotranspiration rates equivalent to a
 421 Q_e of approximately 49 W m⁻² for ground-level extensive green roof systems in southern Germany,
 422 based on two years of observations. Despite differences in climate and experimental setup, the



423 similarity in daily mean Q_e magnitudes across studies indicates that the observed fluxes at our site
424 are consistent with those reported for green roofs elsewhere. The seasonal separation applied in
425 the present study likely explains the higher summer and lower fall daily means relative to the multi-
426 year averages reported in these studies. In contrast, other studies report higher Q_e for systems with
427 denser vegetation or garden-style rooftops, such as the rooftop garden examined by Dong et al.
428 (2025) where daily mean Q_e reached approximately 209 W m^{-2} .

429 Observational estimates of Q_g for green roof surfaces are less commonly reported. Heusinger &
430 Weber (2017), who evaluated the surface energy balance of a full-scale extensive Sedum roof,
431 reported a daytime mean Q_g values of 36 W m^{-2} during June-August and 19 W m^{-2} during
432 September-November. In contrast, our measurements indicate lower daytime mean Q_g — 12 W m^{-2}
433 in the summer (July-August) and 13 W m^{-2} in the fall (September-October). This difference is
434 likely related to the configuration of our green roof system, which is elevated above the rooftop
435 surface, creating an air gap between the module and the roof deck that acts as an additional
436 insulating layer.

437 To assess the influence of this configuration, one heat flux module (Fig. 2) was temporarily
438 relocated to a location on the roof where it was in direct contact with the roof surface, and Q_g was
439 then measured over a short period in October (Fig. 12). Under these conditions, the daytime mean
440 Q_g increased to 23 W m^{-2} , better aligning with the September-November values reported by
441 Heusinger & Weber (2017). Although this relocation experiment was conducted over a relatively
442 short period in fall, the results suggest that the elevated configuration of our modules reduces
443 conductive heat transfer. A longer evaluation period, particularly including summer conditions,
444 would likely yield higher Q_g values, as suggested by the larger June–August means reported by
445 Heusinger & Weber (2017).



446

447 **Figure 12: Hourly composite diurnal cycle of the observed soil heat flux (Q_g) for the elevated**
448 **green roof on-deck configurations, data ranges from Oct. 11 to Oct 21 for both 2014 and**
449 **2025. Solid lines show the mean Q_g , while the shaded bands indicate ± 1 standard deviation.**

450 4.2 Physical behavior of the models

451 Because the two ER configurations (ER_o and ER_m) produced very similar results, the discussion
452 focuses on the general physical behavior of the ER model rather than on version-specific
453 differences. The refinements introduced in the modified version did not fundamentally alter the
454 model's energy-partitioning behavior. As a result, the dominant contrasts in model performance
455 arise not between the ER versions but between ER and WRF-MLGR, which differ structurally in
456 vegetation representation, stomatal and aerodynamic resistance formulations, and soil hydrology.
457 Thus, the discussion refers to “ER” generically when examining the physical basis of model
458 behavior.

459 4.2.1 Latent heat flux

460 ER consistently overestimated Q_e , whereas WRF-MLGR produced negative deviations. The ER
461 bias can be traced to the model's simplified representation of vegetation controls on transpiration.
462 Because ER computes latent heat flux as the sum of soil evaporation, transpiration—and
463 evaporation of intercepted water, in the case of ER_m—transpiration dominates under vegetated



464 conditions and is strongly scaled by LAI. The relatively high LAI observed led ER to treat Sedum
465 as fully active, despite the fact that CAM species typically maintain low transpiration rates through
466 conservative stomatal regulation even under favorable environmental conditions (Gravatt and
467 Martin, 1992; Huang et al., 2024).

468 The ER model's stomatal resistance formulation does not capture this conservative behavior. In
469 ER, minimum stomatal resistance is adjusted only by radiation-, moisture-, and VPD-based stress
470 functions, which allows stomata to remain relatively open until VPD becomes high. CAM plants,
471 however, exhibit earlier stomatal closure, responding directly to atmospheric demand through a
472 “feed-forward” mechanism that is not represented in the model (Males & Griffiths; 2017). As a
473 result, ER overestimates transpiration during conditions under which Sedum would
474 physiologically restrict water loss.

475 WRF-MLGR represents latent heat flux solely through transpiration, as the current version does
476 not include a soil evaporation term. This structural limitation causes systematic underestimation
477 of Q_e . In addition, WRF-MLGR places greater emphasis on aerodynamic resistance and applies
478 strong atmospheric controls on stomatal resistance, including air temperature. While this yields
479 behavior more consistent with the conservative water-use strategy of CAM vegetation, it can also
480 amplify the underestimations by suppressing transpiration prematurely under rising temperature
481 and VPD, reinforcing the negative biases seen in the statistical evaluation. Thus, although WRF-
482 MLGR represents Sedum's conservative stomatal behavior more realistically than ER, the absence
483 of a soil evaporation component and the strong atmospheric regulation of stomatal resistance
484 contribute to underestimations over the diurnal cycle.

485 **4.2.2 Surface temperature and soil heat flux**

486 Both models overestimate daytime T_{surf} and Q_g , though for different reasons and with different
487 magnitudes. ER shows a modest but systematic warm bias ($\approx 1-3$ °C), possibly because the model
488 lacks vegetation heat capacity and therefore cannot buffer short-term fluctuations in net radiation.
489 Combined with small energy misallocations among Q_e , Q_h , and Q_g , this causes excess energy to
490 accumulate at the surface, producing a consistent warm bias despite the model's tendency to
491 overestimate latent heat flux. Correspondingly, ER produces small but systematic overestimations
492 of Q_g , which primarily stem from biases in the near-surface temperature gradient. Although the

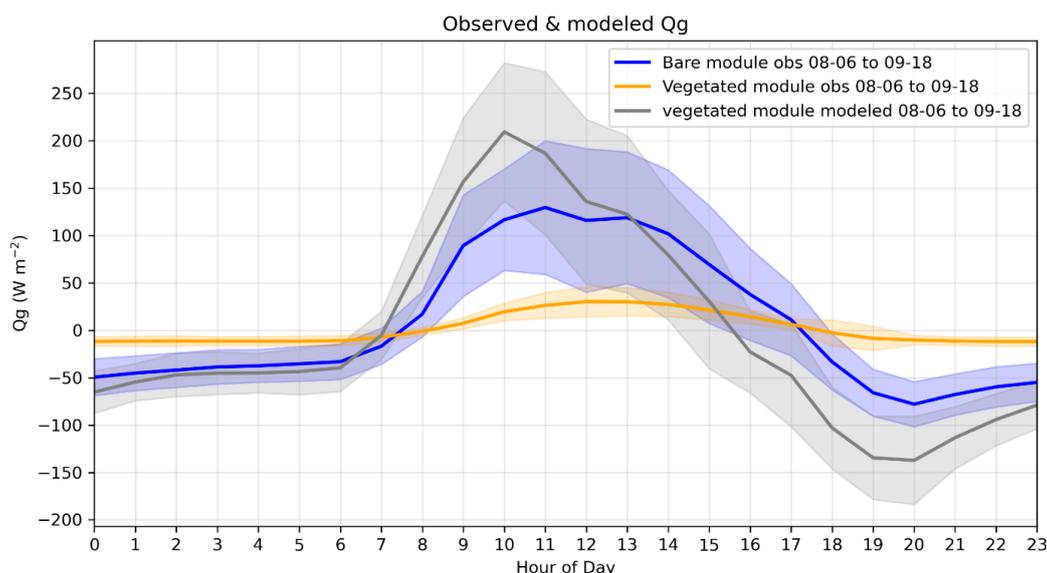


493 model includes a moisture-dependent conductivity formulation, this representation does not fully
494 capture the observed variation in k for the studied substrate (Perelli, 2014). Nevertheless, retaining
495 the original formulation results in realistic Q_g magnitudes because the smaller conductivity
496 partially offsets the warm bias in the simulated surface and shallow soil temperatures. As a result,
497 the residual errors in Q_g remain modest and consistent throughout the day, as reflected in the small
498 RMSE values and the relatively flat diurnal difference curves for both ER versions.

499 In contrast, WRF-MLGR exhibits a much larger positive bias in T_{surf} , particularly during the
500 afternoon, along with very large Q_g errors, and failure to reproduce the observed Q_g diurnal cycle.
501 The most likely reason for this bias is the lack of vegetation radiative representation, meaning all
502 shortwave and longwave radiation is absorbed at the “combined soil-vegetation” surface, with
503 effectively no shading of the soil surface, canopy heat storage, or radiative interactions to moderate
504 surface warming. As a result, incoming radiation is applied directly to the soil rather than to the
505 vegetation that shades the substrate. Because soil has a much higher thermal admittance than
506 foliage, a large fraction of the radiative forcing is initially stored as ground heat, leading to elevated
507 morning values of Q_g as the energy accumulates in the upper soil layers. This stored energy
508 governs the subsequent evolution of T_{surf} and delays the development of Q_h and Q_e , causing Q_g to
509 dominate the diurnal partitioning of surface fluxes. This behavior contrasts with real vegetated
510 surfaces, where the vegetation enables rapid adjustment of sensible and latent heat fluxes under
511 increasing radiative forcing (Curtis, 1936; Tadeu et al., 2021). As part of the experimental green
512 roof system tests, an unvegetated module was also instrumented and installed to monitor Q_g . Figure
513 13 illustrates how, as a consequence of this soil-dominated energy storage, the modeled Q_g
514 presents a diurnal pattern that is more consistent with that of a bare substrate than with observations
515 from the vegetated module.



516



517

518 **Figure 13: Hourly composite of the observed bare (non-vegetated) module (blue), observed**
519 **vegetated module (yellow) and modeled vegetated module from WRF-MLGR (green) Q_g .**
520 **Solid lines represent the mean value and the shaded areas represent ± 1 standard deviation.**
521 **Legend also includes the plotted dates.**

522 4.2.3 Moisture Content

523 ER_o captures the timing of rainfall inputs but often produces larger post-rain increases in water
524 content and a faster early decline than observed. This reflects the model structure in which
525 precipitation is applied directly to the surface layer, producing an immediate increase in SWC in
526 the upper layer. These peaks are followed by a rapid initial decline driven as internal redistribution
527 transfers water from the surface layer to the subsurface layer, where it becomes available for
528 gravitational drainage and transpiration. Redistribution also contributes directly to an early
529 decrease in the depth-averaged water content by relaxing the unrealistically high surface-layer
530 moisture. Although evapotranspiration is overestimated by the model, the early post-rain decrease
531 is dominated by redistribution and drainage rather than an immediate enhancement of Q_e . Once
532 soil moisture decreases, modeled and observed drying rates become more similar, however ER_o



533 remains persistently drier because early post-rain redistribution and drainage reduce stored water
534 more rapidly than in the observed system.

535 ER_m alters the water balance primarily through canopy interception and a moisture-dependent
536 runoff formulation. A fraction of rainfall is temporarily stored on the foliage and evaporated
537 directly, so only the remaining drip reaches the soil. This dampens the sharp post-rain increases in
538 soil water content seen in ER_o and, for many events, brings the modeled peaks closer to
539 observations. The new runoff parameterization also removes water from the surface layer as a
540 function of saturation, providing an explicit drainage pathway when the soil is wet. Together, these
541 changes reduce the magnitude of storage peaks and promote faster loss of excess water, so ER_m
542 tracks the observed dry-down more closely but often remains slightly drier than ER_o between
543 rainfall events.

544 In WRF-MLGR, the soil hydraulic parameters and free-drain bottom boundary allow water to
545 percolate out of the soil column very efficiently when the profile is wet. Hydraulic conductivity in
546 the deeper soil exhibits a strong nonlinear dependence on soil moisture, and the multilayer
547 diffusion scheme rapidly transfers infiltrated water downward toward this drainage sink. As a
548 result, the deeper layers tend to dry quickly following precipitation. Because these lower layers
549 represent a substantial fraction of the total soil depth and the simulated bulk water content is
550 computed as a depth-weighted average across all layers, their rapid drying strongly influences the
551 overall column moisture. Consequently, the model exhibits a persistent dry bias relative to the
552 lysimeter-derived bulk water content.

553 **4.3 Model performance under different moisture regimes and radiative forcing conditions**

554 **4.3.1 Influence of moisture regime**

555 Model performance exhibits a clear sensitivity to moisture regime across all evaluated variables.
556 Under dry conditions, model behavior is generally more stable, with limited variability in all
557 variables and more consistent biases in T_{surf} and Q_g . These conditions correspond to a moisture-
558 limited regime in which surface energy partitioning is more predictable. In contrast, during the dry
559 daytime hours of rainy days, mean differences are reduced, but variability in Q_e and Q_g and T_{surf}
560 increase. This indicates that elevated substrate moisture and residual surface wetness increase the



561 complexity of surface–atmosphere exchanges and introduce greater uncertainty in modeled fluxes
562 and temperatures.

563 **4.3.2 Influence of radiative forcing**

564 Separating days by net radiation shows that radiative forcing primarily scales existing model biases
565 rather than altering their structure. Under high net radiation, biases in Q_e , T_{surf} and Q_g are amplified,
566 as greater available energy intensifies the expression of errors associated with each model's
567 representation of vegetation and soil processes, leading to more consistent error patterns. Under
568 low net radiation, error magnitudes are reduced but become more variable, as limited energy
569 availability constrains fluxes and increases sensitivity to day-to-day atmospheric variability. These
570 results indicate that radiative forcing does not introduce new sources of error but instead governs
571 how strongly underlying model assumptions are expressed.

572 **4.4 Implications for modeling and research**

573 The findings of this study suggest that past applications of ER and WRF-MLGR should be
574 interpreted with some caution. For ER, the systematic overestimation of Q_e implies that earlier
575 studies may have overstated the evaporative cooling potential of green roofs, especially under high
576 radiation and low moisture availability. Nevertheless, ER performed comparatively well in
577 simulating Q_g and T_{surf} , indicating that it may be more reliable for studies focused on subsurface
578 thermal dynamics or building-energy performance.

579 In contrast, WRF-MLGR exhibits structural limitations across all major components of the surface
580 energy balance. Although the model shows an overall moderate agreement for Q_e , the lack of a
581 soil-evaporation term, means Q_e is represented solely through transpiration, leading to persistent
582 underestimations. The absence of an explicit vegetation canopy also allows incoming radiation to
583 interact directly with the soil, increasing the radiative load on this (relatively) high thermal
584 admittance surface (instead of the low thermal admittance vegetation) and amplifying surface heat
585 storage and release. T_{surf} , which is tightly coupled to Q_g , consequently exhibits pronounced daytime
586 warm biases. Taken together, these highlight areas where WRF-MLGR would benefit from further
587 refinement to improve its suitability for green roof applications. Our team has further developed



588 this model to address these main limitations and its performance against observations is much
589 improved, particularly for Q_g (Saeedi et al., 2026).

590 More broadly, this study underscores the importance of rigorous, process-level evaluation in
591 modeling of green roofs and of urban heat adaptation strategies more generally (Krayenhoff et al.
592 2021). Users of ER or WRF-MLGR should be aware of each model’s structural assumptions and
593 characteristic biases and should evaluate outputs against local green roof energy balance
594 observations whenever possible. Accurate representation of the surface energy balance is essential
595 for credible assessments of green roof performance. Ultimately, selecting an appropriate model—
596 and clearly acknowledging its limitations—will be key to producing robust, policy-relevant
597 assessments of green roof performance in urban environments.

598 **5. Conclusion**

599 This research presented a detailed evaluation of two green roof energy balance models—EcoRoof
600 (EnergyPlus) and WRF-MLGR—using observational data collected from a *Sedum*-covered green
601 roof test array. By comparing simulated and observed values of Q_e , Q_g , and T_{surf} across multiple
602 environmental conditions, this study provided insights into model behavior, limitations, and
603 applicability. The results revealed that both models exhibit biases, though for different reasons
604 rooted in their structure and assumptions. EcoRoof consistently and modestly overestimated Q_e
605 and T_{surf} , partly due to vegetation parameter sensitivity and simplified representations of surface–
606 atmosphere exchanges. In contrast, WRF-MLGR underestimated Q_e , and strongly overestimated
607 T_{surf} and Q_g , likely due to its lack of an explicit vegetation layer and consequent primary site of
608 radiation exchange being a hybrid “soil-vegetation” layer with substantial thermal admittance.

609 Beyond reporting performance metrics, this study highlights the importance of comprehensive,
610 process-level model evaluation—an aspect often lacking in prior green roof modeling studies—
611 and underscores the need for future model developments that ensure physically consistent flux
612 formulations. In particular, vegetation-specific physiology, canopy and substrate heat storage,
613 radiative absorption, and the distinct evaporation and transpiration pathways. These findings are
614 particularly relevant for the integration of green roof schemes into urban canopy and building



615 energy models, where accurate representation of surface energy partitioning is critical for assessing
616 heat mitigation potential and informing strategies to improve urban climate resilience.

617 **Code and data availability.** The exact stand-alone versions of the green roof model
618 configurations used to produce the results presented in this study are archived in a persistent public
619 repository at Zenodo: <https://doi.org/10.5281/zenodo.18688590> (Martinez Mendoza et al., 2026).
620 The archived release corresponds to the precise versions of the codes, input forcing data,
621 observational datasets and post processing scripts used in this research, ensuring reproducibility
622 of the results.

623 The stand-alone WRF-MLGR implementations are derived from the WRF source code and are
624 distributed under the GNU General Public License v2.0 or later (GPL v2+). The stand-alone
625 EcoRoof implementations (original configuration ER_o and modified configuration ER_m), derived
626 from EnergyPlus, are distributed under the BSD 3-Clause License. The observational datasets and
627 post-processing scripts are distributed under the Creative Commons Attribution 4.0 International
628 (CC BY 4.0) license.

629 The ER model is based on the green roof module originally described by Sailor (2008) and
630 implemented within EnergyPlus; the modified ER configuration follows the developments
631 described by Heusinger (2018) and the WRF-MLGR green roof parameterization is based on the
632 scheme described by Zonato et al. (2021). The observed data used for the evaluation were collected
633 as part of a long-term field experiment conducted at Western University, London, ON, Canada.

634 **Author contribution.** MMM designed and implemented the evaluation methodology, performed
635 all simulations, conducted all analyses, interpreted results and prepared the manuscript. AS
636 extracted and implemented the green roof models, adapting components originally embedded
637 within larger modeling frameworks. JAV supervised the work, assisted with the interpretation of
638 results, suggested additional analyses, and reviewed and edited the manuscript. ESK contributed
639 to the acquisition and implementation of the model codes, assisted with the interpretation of
640 results, and reviewed and edited the manuscript.

641 **Competing interests.** The authors declare that they have no conflict of interest.



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