



1 **Integration of physics-informed deep learning with a distributed**
2 **hydrological model (PIDL-DHM): A hybrid model for runoff**
3 **simulation**

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20 **Abstract :** Climate change and vegetation restoration have altered hydrological
21 processes, but quantifying vegetation-runoff interactions remains challenging due to
22 complex feedback and data scarcity. We developed a physics-informed deep learning
23 hybrid model that couples process-based hydrology with deep learning to improve
24 runoff prediction in vegetation-altered basins. The model explicitly represents
25 transpiration, interception, snow dynamics, dual runoff generation, water-balance
26 constraints, and distributed spatial heterogeneity. Evaluations in three Chinese basins
27 spanning hydroclimatic and vegetation gradients show that the hybrid models
28 outperform pure deep learning, with the strongest improvements in semi-arid and
29 vegetation-transition basins. Correlation coefficients exceeded 0.8 at monthly/annual
30 scales and 0.75 at daily scales in the most responsive basins. Compared with GR4J,
31 the added complexity is most beneficial in heterogeneous semi-arid and ungauged
32 sub-basins. These results demonstrate that physical constraints improve extrapolation
33 reliability and support hybrid models for sustainable basin management under climate
34 change.

35 **Keywords :** Hybrid models; Deep learning; Vegetation–runoff interactions;
36 Climate change; Runoff prediction; Vegetation dynamics

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41 **Highlights**

42 1, This study proposed a physics-informed deep learning model that incorporates the
43 dual-regulation mechanisms of canopy and root systems as well as dynamic runoff
44 processes.

45 2, It demonstrated better transferability to ungauged basins compared to traditional
46 hydrological models.

47 3, Additionally, the model exhibited superior robustness under drought or hot climate
48 conditions relative to other modeling approaches.



49 1. Introduction

50 Runoff prediction models are essential tools for flood forecasting, drought assessment,
51 water allocation, and ecological restoration planning (Wang and Zeng, 2024). However, the
52 reliability of runoff prediction is increasingly challenged by non-stationary environmental
53 change (Konapala et al., 2020). Climate warming alters precipitation regimes, snow processes,
54 and soil moisture dynamics, while vegetation restoration, afforestation, agricultural expansion,
55 and land-cover change modify canopy interception, transpiration, and infiltration (Li et al.,
56 2018; Wang et al., 2019). These changes jointly reshape the partitioning of precipitation into
57 evapotranspiration, soil water storage, and surface runoff (Shen et al., 2018; Brient, 2020; Sit
58 et al., 2020). Consequently, hydrological models developed under historically stationary may
59 become unreliable when applied to basins undergoing rapid ecological or climate change (Li
60 et al., 2022).

61 Traditional runoff prediction models predominantly rely on process-based hydrological
62 models, such as the Soil and Water Assessment Tool (SWAT) (G. Arnold et al., 2012;
63 Hamman et al., 2018) and the Variable Infiltration Capacity (VIC) model (Liu et al., 2025; Li
64 et al., 2018), which offer physically-based representations of water and energy cycles (Bi et
65 al., 2023; Zhou et al., 2021; Du et al., 2022; Li et al., 2024). A key strength of these models is
66 their spatial discretization, which enables the representation of spatial heterogeneity (Shang et
67 al., 2023; Xue et al., 2024). However, a major limitation of these models remains their
68 vegetation-related parameters, rooting structures, phenological development, and stomatal
69 regulation are commonly simplified or prescribed (Chen et al., 2025; Gaur and Drewry, 2024;
70 Liu et al., 2020). Recent studies have shown that neglecting vegetation dynamics can lead to
71 substantial uncertainty in evapotranspiration and runoff simulations. For example,



72 incorporating remotely sensed vegetation phenology into SWAT improved the representation
73 of vegetation growth and ecohydrological processes, indicating that static phenological
74 assumptions can bias water-balance simulations (Chen et al., 2023). Similarly, studies on
75 land-surface and Earth-system models have shown that inaccurate sensitivity of
76 evapotranspiration to vegetation change can propagate into misleading hydrological and
77 climate feedbacks (Wang et al., 2024; Huang et al., 2016; Liu et al., 2025). These findings
78 suggest that these traditional models may fail to adequately represent such complex
79 interactions, leading to critical gaps in runoff prediction accuracy, especially during growing
80 seasons, droughts, and in regions with limited data (Lawrence et al., 2019; Li et al., 2015; Yao
81 et al., 2025; Barger et al., 2011; Xue et al., 2022).

82 These deficiencies are not merely theoretical. In a study of 156 Austrian catchments,
83 Duethmann et al. (2020) found that a conceptual semi-distributed HBV-type hydrological
84 model showed a mean gap of 95 mm yr⁻¹ per 35 years between simulated and observed
85 discharge trends. Accounting for vegetation dynamics using a satellite-derived vegetation
86 index in the calculation of reference evaporation reduced this gap by 36 mm yr⁻¹ per 35 years,
87 highlighting the role of missing vegetation processes in long-term hydrological simulations.
88 The challenge is particularly pronounced in basins where vegetation-water interactions vary
89 strongly across space. In semi-arid or transitional basins, shallow-rooted grasslands and
90 sparsely vegetated areas may respond rapidly to precipitation, whereas forested regions can
91 sustain transpiration and baseflow through deeper soil-water access (Luo et al., 2020; Gao et
92 al., 2022; Zhang et al., 2022). These contrasting mechanisms mean that a single lumped
93 parameter set may reproduce outlet discharge but still fail to represent internal hydrological
94 processes (Du et al., 2022; Camarero et al., 2024). Thus, evaluating models only by outlet



runoff can mask unrealistic spatial runoff generation patterns (Wei et al., 2021; Wood et al., 1992; Wang et al., 2007).

Deep learning models have recently achieved strong performance in rainfall-runoff prediction because of their ability to learn nonlinear relationships from large datasets (Ma et al., 2021; Van Katwyk et al., 2023). Models such as recurrent neural networks and long short-term memory networks can capture temporal dependence and complex hydroclimatic responses (Rumelhart et al., 1986). However, purely data-driven models are often difficult to interpret and may extrapolate poorly under conditions that differ from the training period, such as extreme droughts or ungauged subbasins (Khoshkalam et al., 2023; S. and Q., 2010). Their predictions may also violate water-balance consistency or produce hydrologically unreasonable internal fluxes (Sit et al., 2020). These limitations reduce their reliability for water-resource decision-making under climate and land-cover change.

Physics-informed deep learning provides a promising pathway to address these limitations by embedding hydrological process knowledge into differentiable neural network architectures (Tian et al., 2025; He et al., 2020; Shen et al., 2021). In such frameworks, physical equations, state variables, and process-based constraints can be integrated into neural networks, allowing model parameters to be optimized by gradient-based learning while maintaining physical interpretability (Lees et al., 2022; Li et al., 2024; Wang et al., 2018). Previous physics-informed hydrological models have demonstrated improved generalization by incorporating snow processes, soil-water dynamics, routing schemes, or water-balance constraints (Ji and Song et al., 2025; Shen & Lawson, 2021; Höge et al., 2022; Koppa et al., 2022). Following researches integrated more complex physical processes focusing on soil moisture dynamics (Konapala et al., 2020; Shang et al., 2023). However, most existing



118 physics-informed rainfall-runoff models still focus primarily on runoff generation and storage
119 dynamics, while vegetation physiological regulation, canopy interception, dynamic stomatal
120 resistance, and root-zone water uptake remain insufficiently represented (Zhong et al., 2023).
121 This limits their ability to simulate runoff under vegetation-altered or climate-stressed
122 conditions (Elghawi et al., 2023; Zhang et al., 2024; Wang et al., 2024; Xie et al., 2021). This
123 limitation shows the need to further refine PIDL (Physics-informed Deep Learning) models to
124 consider these critical processes (Dazzi, 2024; Vicente-Serrano et al., 2022; Niu et al., 2005).

125 This study focuses on the key questions: How can key ecological processes be
126 dynamically embedded within a PIDL framework? How can reliable predictive performance
127 be maintained in data-scarce regions? To address these challenges, this study develops a
128 distributed physics-informed deep learning hydrological model, referred to as PIDL-DHM
129 (Physics-informed Deep Learning with a Distributed Hydrological Model), that explicitly
130 couples hydrological process constraints with dynamic vegetation-water interactions. The
131 framework integrates three key components: (1) a physics-informed recurrent hydrological
132 module that represents water-balance dynamics, snow processes, runoff generation, and
133 baseflow; (2) a vegetation-process module that dynamically represents evapotranspiration,
134 canopy interception, and vegetation-mediated infiltration using learnable time-varying
135 parameters; and (3) a distributed routing and delay module that represents spatial
136 heterogeneity in runoff generation and translation to the basin outlet.

137 We systematically evaluated the model across three climatically and ecologically
138 contrasting Chinese basins from dry to wet climates to demonstrate its enhanced predictive
139 capability and generalization in ungauged basins. We provide a new runoff prediction method



140 in response to climate change and offer valuable insights for water resource management and
141 decision-making in these vulnerable regions.

142 **2. Methodologies and Data Sources**

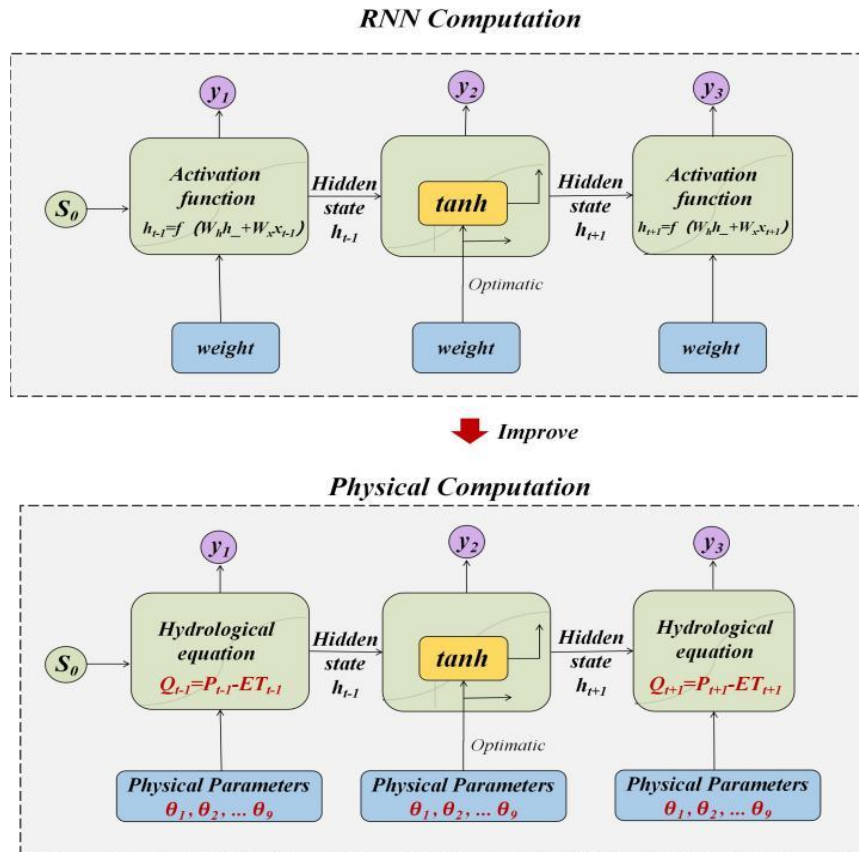
143 **2.1. Model Framework and major improvements**

144 **2.1.1. Foundational Architecture**

145 The integration of physics and DL in this study is built upon the open-source
146 contributions of Jiang (2020) and Zhong et al. (2023). Specifically, we adopt the core concept
147 of encoding physical dynamics directly within computational graph of RNN (Figure 1). To
148 implement this concept, we utilize a differentiable framework in PyTorch to rewrite the
149 physical model (Paszke et al., 2019; Patil and Stieglitz et al., 2014). The fundamental
150 innovation involves replacing the standard mathematical operations of RNN and LSTM cells
151 —the weights and bias matrices that transform inputs and hidden states (Figure 1a)—with
152 numerical solutions of physical governing equations and their parameters (Figure 1b). For
153 instance, the cell state update is governed by equations simulating soil moisture movement
154 (e.g., the soil water continuity equation) and runoff generation, while physical parameters
155 (e.g., saturated hydraulic conductivity) become learnable parameters within the network.
156 During the training process, the gradients of the loss function are backpropagated through
157 these physical equations through automatic differentiation in PyTorch, enabling the joint
158 optimization of both physical parameters and remaining network weights. Consequently, the
159 hidden state variable h_t is exclusively composed of the physical state variables s_0 (e.g. snow
160 water equivalent and soil moisture content), forming a physically interpretable “memory” of
161 the hydrological system carried between time steps. All the neural components are unified



162 within a single end-to-end architecture, facilitating joint optimization across physical and
 163 data-driven modules.



164
 165 **Figure 1.** (a) Schematic diagram of the pure neural network unit of RNN and LSTM. (b)
 166 Schematic diagram of hybrid models, which add physical information to the neural network
 167 units of RNN and LSTM. The hidden state and weight in a recurrent neural network can be
 168 replaced by physical equations and parameters (e.g., the soil water content) and physical
 169 parameters



170 2.1.2. Major Improvements

171 Beyond above approaches, our novel framework introduces major improvements in
172 representing runoff generation and vegetation processes. We rewrite the runoff generation and
173 vegetation processes model, which are encoded as differentiable components within the
174 PyTorch framework. Our key innovations within this framework include: (1)
175 Dual-mechanism runoff generation. Dry basins exhibit both infiltration excess runoff during
176 high-intensity storms and saturation-excess runoff when local soils reach field capacity after
177 prolonged wetting. Unlike Jiang's (2020) single-mechanism approach, our PRNN
178 incorporates a dynamic switching function that activates either infiltration-excess or
179 saturation-excess runoff mechanisms based on real-time climate inputs, allowing temporal
180 coexistence of both processes. (2) Plant-water interaction module. By incorporating a
181 dedicated LSTM network for vegetation processes, we explicitly represent memory effects in
182 plant-water interactions, including precipitation interception, stomatal transpiration, and root
183 water uptake.

184 2.1.3 Physical Mechanisms

185 (1) Precipitation and Snowmelt module

186 In our model, precipitation and snow are divided based on the temperature thresholds
187 T_{min} and T_{max} , and snow melt is modeled on the basis of the degree-day factor:

$$188 \quad P_{snow} = \begin{cases} 0 & T \geq T_{min} \\ P & T < T_{min} \end{cases} \quad (1)$$

$$189 \quad P_{rain} = \begin{cases} P & T > T_{min} \\ 0 & T \leq T_{min} \end{cases} \quad (2)$$



$$M = \begin{cases} \min[S_0, DDF \cdot (T - T_{max})] & T > T_{max} \\ 0 & T \leq T_{max} \end{cases} \quad (3)$$

where P and T are the precipitation and air temperature, respectively; DDF is the degree-day factor; P_{snow} and P_{rain} are the snowfall and precipitation, respectively; T_{min} is a training parameter representing the threshold temperature of the snowfall; T_{max} is a training parameter representing the snowmelt threshold temperature; and S_0 is the soil snow bucket content.

(2) Evapotranspiration

Evapotranspiration (ET) is calculated using the FAO56 Penman–Monteith (PM) Equation (5), which is a widely accepted method for estimating ET under various environmental conditions (Penman and Keen, 1997). Dynamic stomatal resistance is also used as a parameter, allowing for the incorporation of plant-specific responses to environmental stress (e.g., drought conditions).

$$ET = \begin{cases} ET_p \times (\frac{S_1}{S_{max}}) & 0 \leq S_1 \leq S_{max} \\ PET & S_1 > S_{max} \end{cases} \quad (4)$$

$$e_s = 0.611 \times \exp\left(\frac{17.3T}{T+237.3}\right) \quad (5)$$

$$ET_p = \frac{\Delta(R_n - G) + [\rho \cdot c_p \cdot (e_s - e_a)]/r_a}{\Delta + \gamma(1 + r_s/r_a)} \quad (6)$$

where S_1 and ET are water soil moisture content and actual evaporation, respectively, and where S_{max} is the storage capacity of the basin water bucket. R_n represents the net radiation, $MJ/m^2/day$. G is the soil heat flux density, which is set to 0 and is also measured in $MJ/m^2/day$. Δ is the slope of the saturation vapor pressure curve, expressed in $kPa/^\circ C$. e_s



209 represents the saturation vapor pressure; e_a represents the actual water vapor pressure; ρ
 210 represents the air density; cp represents the specific heat capacity; and γ represents the
 211 hygrometer constant. r_s and r_a are the stomatal resistance and aerodynamic resistance,
 212 respectively.

213 (3) Runoff and baseflow

214 By integrating the core ideas of the soil water storage curve (SWAT) and VIC
 215 (superinfiltration runoff) (Dunne and Black, 1970), the baseflow and surface runoff
 216 calculation formulas are as follows:

$$217 \quad q_{base} = \begin{cases} q_{max} \times (\frac{S_1}{S_{max}})^{-\beta} & 0 \leq S_1 \leq S_{max} \\ q_{max} & S_1 > S_{max} \end{cases} \quad (7)$$

$$218 \quad q_{sat} = \begin{cases} P_{rain} - (i_{max} - i_0) & P_{rain} > 0, P_a > i_{max} - i_0 \\ P_{rain} - \frac{i_{max}}{(1+b)} \times (1 - \frac{i_0}{i_{max}})^{(1+b)} & P_{rain} > 0, P_a \leq i_{max} - i_0 \end{cases} \quad (8)$$

$$219 \quad q_{unsat} = \begin{cases} P_{rain} - q_{sat} - f_{max} [1 - (1 - \frac{P_{rain} - q_{sat}}{f_{max}})^2] & P_{rain} > i_{max} - i_0 \\ S_1 - S_{max} & P_{rain} \leq i_{max} - i_0 \end{cases} \quad (9)$$

$$220 \quad q_{surf} = q_{unsat} + q_{sat} \quad (10)$$

$$221 \quad i_0 = i_{max} \times (1 - (1 - A)^{\frac{1}{b}}) \quad (11)$$

$$222 \quad i_{max} = (1 + b) \times S_{max} \quad (12)$$

$$223 \quad A = 1 - (1 - \frac{S_1}{S_{max}})^{\frac{b}{1+b}} \quad (13)$$



where q_{base} and q_{surf} are the baseflow and surface runoff, respectively. q_{unsat} and q_{sat} represent saturated runoff and unsaturated runoff, respectively. q_{max} , S_{max} and f are training parameters representing the maximum baseflow when the catchment bucket is fully saturated, the maximum water storage, and a decay factor for the decline rate of runoff. f_{max} is the maximum infiltration velocity. b is the shape parameter of the storage capacity curve details. i_{max} is the maximum infiltration capacity.

(4) Vegetation module

In this study, precipitation and temperature were used as additional inputs to the vegetation LSTM module to implicitly represent vegetation growth processes (Zhong et al., 2023; Gao et al., 2021). The dynamic vegetation LSTM module includes evapotranspiration, infiltration, and canopy interception. In the vegetation canopy interception and water storage module, vegetation canopy interception is represented using the Holton vegetation formula (Holton, 1961). The interception loss can be expressed as:

$$I_n = S_v + C_{sint} P_{rain} \quad (14)$$

where I_n represents the interception loss; S_v represents the water storage capacity of the vegetation in the canopy shelter area, $S_v=0$; and P_{rain} represents the precipitation in the vegetation cover area.

The evapotranspiration (ET) is calculated using the FAO56 Penman–Monteith (PM), but r_s used dynamic parameters for stomatal resistance. Additionally, the impact of vegetation on runoff is expressed using the Holton formula (Holton, 1961):

$$f(t) = GI \times A_a \times S_1^n + f_c \quad (15)$$



where $f(t)$ and f_c are the infiltration rate and stable infiltration rate, respectively, which are incorporated into the model to represent the physical properties of the soil and vegetation interaction. GI is the plant growth index, which is a dynamic parameter that represents the plant's growth stage. n is an empirical coefficient, and the experience value is 1.4. A_a is the ratio of the infiltration capacity and the soil surface water shortage, which represents the porosity connected with the surface and the vegetation root density index affecting infiltration. S_1 represents the water shortage capacity of the ground surface layer.

(5) Distributed delay kernel model equations

With the impact of spatial information on runoff modeling, the basin delay kernel model proposed by Sun et al. (2024) is like our fully distributed model but does not explicitly consider the runoff routing. Here we use a distributed hybrid-P-D configuration consider runoff generation move routing, so that land travel times are represented explicitly by a delay kernel. The delay kernel is a time-distribution operator applied after runoff generation, it reshapes timing while preserving mass at the daily step. Translation and dispersion from grid to the basin outlet are modeled by a learnable delay-kernel routing operator. The routed outlet discharge is computed as a discrete convolution:

$$Q = q_{surf} + q_{base} \quad (16)$$

$$Q_{basin, t} = \sum_{\tau=0}^{k-1} K(\tau) Q(t-\tau) \quad (17)$$

where Q_{basin} represents the runoff at the basin outlet. Q_i and α_i are the runoff and weighted calculations, respectively, which are based on the inverse distance of the distance from the grid point to the exit. N represents the total number of subbasins within the basin.



(6) Water balance constraint PRNNLayer

Mass conservation is enforced by construction through an explicit state-space update in the PRNN Layer, the mass conservation enforced by construction. At each time step, we enforced a basin-scale water balance residual using the model's internally simulated fluxes and storage:

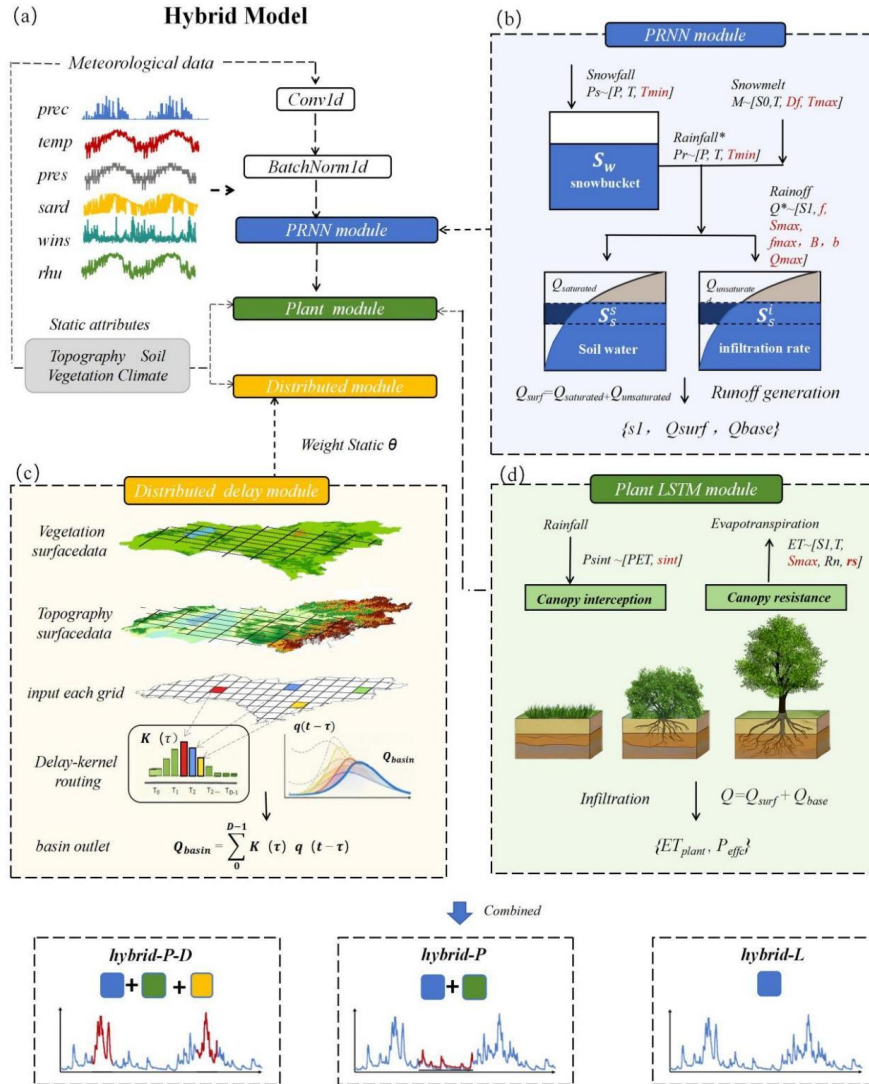
$$P+M=I+ET+Q_{sub}-Q_{surf}-\Delta S \quad (18)$$

Which is identically 0.

2.2. Model Implementation

2.2.1. Architectural Overview

The proposed PIDL framework couples three functionally distinct neural network blocks (Table 1): (1) Physics-Informed Recurrent Neural Networks module (PRNN module), which encodes basin-scale water-balance equations and runoff generation (Figure 2b); (2) Plant Long Short-Term Memory network module (Plant LSTM module), which learns nonlinear vegetation water-use processes (Figure 2d); and (3) Distribution delay kernel module (Distribution module), which is divided into a fully distributed grid (Figure 2c). The three blocks exchange fluxes at each simulation time step, and the PRNN module provides soil moisture surface runoff and basic runoff to the Plant LSTM module, which returns dynamic evapotranspiration, interception loss, and root uptake, and the distribution module generates runoff through each grid.



285

286 **Figure 2. Structure of the physics-informed deep learning distributed hydrological**
 287 **modeling framework (PIDL-DHM).** (a) Overview of the hybrid model architecture. (b)
 288 PRNN module diagram (highlighted in blue): The physics-informed recurrent neural network
 289 module combines DL with physical hydrological processes, including surface runoff and
 290 infiltration. For detailed formulations of these processes, refer to the main text (adapted from



291 S. Jiang, 2020). (c) Distributed delay module diagram (highlighted in yellow): This module
292 handles spatially distributed hydrological processes, and each grid includes a PRNN module
293 and a plant LSTM module. (d) Plant LSTM module diagram (highlighted in green): A long
294 short-term memory (LSTM) network that synergistically combines physical mechanisms with
295 vegetation processes. Meteorological inputs, including precipitation (prec), temperature
296 (temp), atmospheric pressure (pres), solar radiation (sard), wind speed (wins), and relative
297 humidity (rhu), drive the model. The figure depicts three model variations: hybrid-L: a hybrid
298 lumped hydrological process model integrating the PRNN module; hybrid-P: a hybrid model
299 that incorporates the Plant LSTM module; and hybrid-P-D: a fully distributed hybrid model
300 incorporating the PRNN, Plant LSTM, and distributed modules. BatchNorm1d: batch
301 normalization technique for stable training. Conv1D: extract spatial features from time series
302 data. FCNN: fully connected neural network for feature integration.

303 **Table 1. Architecture parameters of the hybrid physics-informed neural network model**

Item	Definitions
Network	Fully connected neural network
Hidden layer	1 LSTM layer (64 neurons); 2 CNN layers (25 filters)
Activation funtion	Tanh /ReLU/ Heaviside
Optimizer	Adam optimizer
Initial learning rate	0.01
training time	About 300s per 1 epochs

304 **2.2.2. Dynamic Parameterization**

305 To account for dynamic vegetation phenology and its impacts on hydrological processes,
306 we parameterize key vegetation-related coefficients as time-variant variables (Table 2).
307 Vegetation growth dynamically alters canopy interception, transpiration, and root water
308 uptake (Agnihotri et al., 2023), consequently modifying surface runoff generation and soil



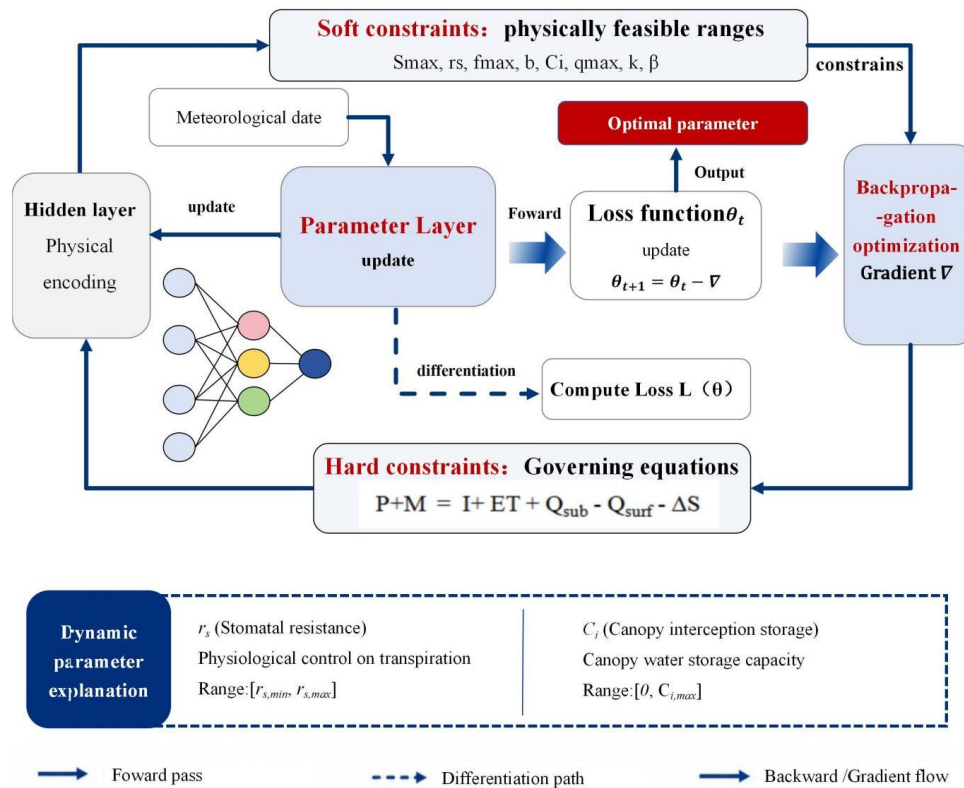
309 water transport velocities. Specifically, the canopy interception coefficient (C_i) is treated as a
310 dynamic parameter to capture these vegetation-mediated processes. To further extend this
311 dynamic framework, we also designate the maximum water storage capacity (S_{max}) and the
312 infiltration rate coefficient (f) governing the soil bucket model runoffs as time-dependent
313 parameters. For evapotranspiration (ET) processes, stomatal resistance (r_s) is similarly
314 implemented as a dynamic measure to mitigate the effects of vegetation phenology on ET
315 estimates. All remaining parameters maintain static representations. When implemented as
316 trainable variables, these parameters enable data-adaptive adjustments during model
317 calibration, ensuring accurate representation of observed vegetation characteristics.
318 Mechanistically, r_s modulates transpiration rates, whereas C_i controls canopy water retention
319 capacity. This dynamic parameterization significantly enhances model adaptability across
320 diverse climatic regimes and vegetation types. All physical mechanisms and their formulas
321 used in the model are in supplemental material 1.

322 2.2.3. Training Configuration

323 To achieve these innovations, The overall computational workflow began with
324 processing input data through the PRNN module (Figure 2b). Inputs include meteorological
325 forcing and static catchment attributes (Figure 3). To enhance training stability and accelerate
326 convergence, we applied batch normalization (BatchNorm1d) to the input features. For static
327 parameter learning, we deployed a 1D convolutional encoder (Conv1D) to extract spatial
328 features from time series data, which were subsequently integrated with other static features
329 using a fully connected neural network (FCNN) (Fukushima and Miyake, 1982; Botterill and
330 McMillan, 2023). The model was trained using the Adam optimizer with an initial learning
331 rate of 0.01. To prevent overfitting, early stopping was implemented with a patience of 80



epochs based on the Nash-Sutcliffe Efficiency (NSE) metric. The detailed architecture
 parameters are summarized in Table 1.



334

Figure 3. Updating of trainable hydrological parameters in the PIDL-DHM framework. Meteorological forcings and hydrological states are propagated through the differentiable physical model, while selected process parameters are dynamically updated within predefined physically feasible ranges. The governing hydrological equations impose hard physical constraints on model states and fluxes, whereas parameter bounds provide soft constraints on the optimization space. The loss gradient with respect to the trainable parameters is computed through automatic differentiation and backpropagated through the differentiable physical equations to iteratively update the parameters until the convergence criterion is satisfied.



344

Table 2. All the dynamic physical parameters and setting value ranges

Parameter	Range	Definitions
T_{min}	$[-3, 0]$	Critical freezing temperature
ddf	$[0, 5]$	Degree-day factor
T_{max}	$[0, 3]$	Snowmelt onset temperature
S_{max}	$[0, 1, 500]$	Soil water storage capacity
r_s	$[0, 500]$	Stomatal resistance
f_{max}	$[0, 50]$	Infiltration capacity
b	$[0, 5]$	Soil water retention curve shape parameter
C_i	$[0, 0.1]$	Canopy interception coefficient
q_{max}	$[0, 50]$	Maximum baseflow rate
β	$[0, 0.5]$	Baseflow shape coefficient

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2.3. Experimental Design and Evaluation

2.3.1. Study Areas and Data Sources

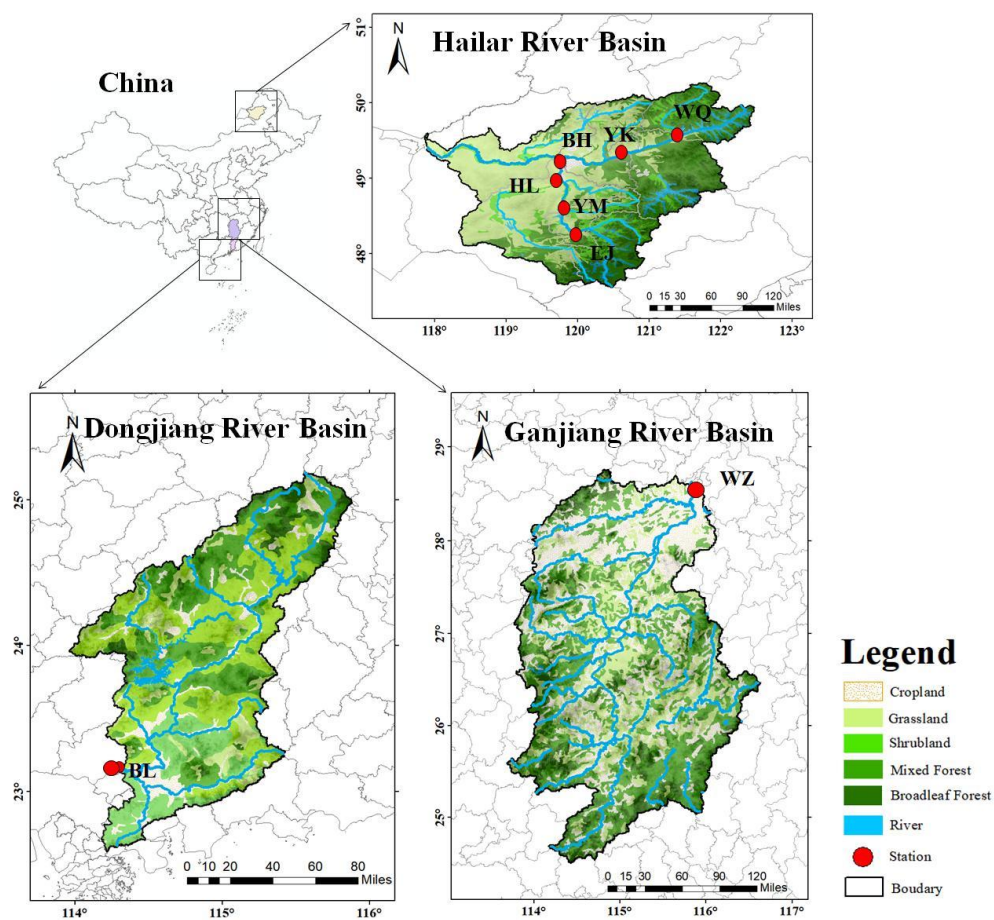


Figure 4. Location map of the Hailar River Basin (HRB), Dongjiang River Basin (DRB) and Ganjiang River (GRB). The distributions of the vegetation types and hydrological stations in the study area are shown, with different colors indicating various vegetation categories, including forests, shrublands, grasslands, and croplands. Two basins are in



southern China and one in northern China, representing wet and dry climates, respectively.

The runoff observation sites are BH, HL, YM, EJ, YK, WQ, BL, and WZ.

Table 3. Basin information for the Hailar River Basin (HRB), Dongjiang River Basin (DRB) and Ganjiang River Basin (GRB).

Station	HRB	DRB	GRB
Area	6.7×10^4	2.2×10^4	7.62×10^4
Vegetation	Grassland, forest	Forest	Forest, farmland
Temperature(°C)	-0.3	22.6	18.4
Precipitation(mm/year)	354.1	1,815.3	1,664.4
Station	BH	BL	WZ
Training year	2005-2014	2005-2009	2005-2014
Training data	1979-2004	1979-2004	1979-2004

The study was conducted in three contrasting river basins: the Hailar River Basin (HRB) in a semi-arid northern region, and the Dongjiang River Basin (DRB) and Ganjiang River Basin (GRB) in humid southern China (Figure 4, Table 3). The hydrological stations are the WZ station, the BL station and the BH station, respectively (Table 3). The vegetation types and areas across the three regions are diverse and exhibit distinct characteristics. Among the three basins, the largest basin, GRB, is 7.62×10^4 km² and is dominated by forest and farmland. The smallest basin, the Dongjiang River Basin, is 2.2×10^4 km² and is predominantly naturally forested. The Hailar River Basin is 6.7×10^4 km² and contains the



365 most varied vegetation types, including forests, shrubs, grasslands, and desertified grasslands.
366 Moreover, the three basins also have different climate types and runoff generation
367 mechanisms. The GRB and DRB are in humid areas, and the main runoff generation
368 mechanism is saturation excess runoff, whereas the HRB is located in semiarid areas, and the
369 main runoff generation mechanism is infiltration excess runoff.

370 We used daily meteorological data from the China Meteorological Forcing Dataset
371 (CMFD) and daily runoff observations from January 1, 1979, to December 31, 2014. The
372 CMFD was widely utilized in hydrological research throughout China. This dataset provides
373 six variables at daily temporal resolution and $0.1^{\circ} \times 0.1^{\circ}$ spatial resolution: near-surface air
374 temperature, surface pressure, specific humidity, wind speed, downward shortwave radiation,
375 and precipitation. The CMFD has been rigorously validated against station observations and
376 demonstrates strength in representing precipitation phase partitioning and radiation budgets
377 over complex terrain, making it suitable for driving process-based hydrological models in our
378 study regions with diverse climatic conditions. To ensure the reliability of the model inputs
379 and outputs, a systematic quality control procedure was applied to the raw hydrological data.
380 Streamflow values deemed hydrologically implausible (e.g., anomalously high outlier in
381 winter) were removed as outliers. These values are typically indicative of sensor errors or data
382 logging mistakes. In the Dongjiang River Basin, due to abnormal precipitation recorded in the
383 CMFD dataset, we evaluated model performance using daily runoff observation data from
384 January 1, 2005, to December 31, 2009. We trained the model using 25 years of daily runoff
385 observation data from January 1, 1979, to December 31, 2004, and evaluated its performance
386 on an additional ten years of observation data spanning January 1, 2005, to December 31,
387 2014.



388 To validate the simulated evapotranspiration, we further utilized flux tower from the
 389 Hulunbuir Grassland Ecosystem National Field Scientific Observation and Research Station,
 390 located in the Xiertala Ranch of Hulunbuir City, Inner Mongolia (next to BH station). This
 391 flux dataset has been widely employed in ecohydrological studies of temperate grasslands in
 392 northern China (Yan et al., 2021).

393 **2.3.2. Model Configurations**

394 Another important issue is whether the added complexity of hybrid models is justified.
 395 Increasing model flexibility may improve outlet-flow performance, but it does not necessarily
 396 imply better process realism. A meaningful assessment should therefore compare the
 397 proposed model not only with pure deep learning models, but also with a traditional
 398 hydrological benchmark such as GR4J. To quantify the contribution of each innovation on
 399 runoff simulation capability, we designed five different configuration schemes (Figure 2) (1)
 400 Deep Learning model (DL model): pure deep learning RNN without physical information. (2)
 401 Hybrid-L model: The base PRNN module with lumped water-balance equations (following
 402 Jiang et al., 2020). configured with basic processes such as precipitation snowmelt and
 403 superinfiltration full runoff modules. (3) Hybrid-P model: a vegetation module is added on the
 404 basis of the hybrid-L model, including the vegetation transpiration process, vegetation
 405 infiltration process, etc. (4) Hybrid-P-D model: a fully distributed module is added on the
 406 basis of the hybrid-P model, which is divided into $0.1^{\circ} \times 0.1^{\circ}$ grids, and the 6 parameters
 407 of vegetation LAI, canopy height, maximum LAI, slope, surface elevation, minimum LAI,
 408 and the LAI change rate for each grid are input. (5) GR4J model: a traditional lumped
 409 conceptual rainfall-runoff model used as a low-complexity benchmark. The model was



410 calibrated using the same meteorological forcing and runoff observations as the hybrid
411 models, with NSE as the objective function.

412 This progression enables tests that attribute performance gains to vegetation coupling
413 and spatial distribution. The four models (the DL model, hybrid-L model, hybrid-P model,
414 and hybrid-P-D model) share the same training parameters and loss function information and
415 are trained 150 times. To verify the migration ability of the model in data-deficient basins,
416 further research is necessary to determine whether models trained using basin exit points can
417 effectively simulate hydrological processes at any untrained location within the same basin.
418 We chose other runoff stations within the Hailar River Basin to validate the transferability of
419 the hybrid model.

420 2.3.3. Evaluation Metrics

421 Model performance was evaluated using the Nash-Sutcliffe Efficiency (NSE),
422 Kling-Gupta Efficiency (KGE), and Percent Bias (PBIAS). The statistical significance of
423 performance differences between models was assessed using Meng's Z-test for correlated
424 correlations (Meng et al., 1992; Nash and Sutcliffe, 1970, Legates and McCabe, 1999, Yilmaz
425 et al., 2008).

426 NSE can be defined in the following general form:

$$427 \quad NSE_{\alpha} = 1 - \frac{\sum_{i=1}^T |Q_{obs,i} - Q_{sim,i}|^{\alpha}}{\sum_{i=1}^T |Q_{obs,i} - \overline{Q_{obs}}|^{\alpha}} \quad (17)$$

428 where $Q_{obs,i}$ and $Q_{sim,i}$ are the simulated and observed runoff values, respectively, and
429 where $\overline{Q_{obs}}$ is the average observed value. NSE measures the overall fit-of-goodness of the
430 simulated and observed runoff data, with a NSE of 0.55 being the threshold for good
431 performance (Knoben et al., 2019, Newman et al., 2015).



The Pbias is defined as follows:

$$Pbias = 100 \times \left| \frac{\sum_1^n (Q_{sim} - Q_{obs})}{\sum_1^n Q_{obs}} \right| \quad (18)$$

where Q_{sim} and Q_{obs} are the observed and simulated runoffs sorted in descending order, respectively.

Kling Gupta efficiency (KGE) is an indicator that comprehensively evaluates the difference between simulated model results and observed data (Gupta et al., 2009). KGE combines measures of correlation, bias, and variability. The calculation formula is as follows:

$$KGE = 1 - \sqrt{(r - 1)^2 + (\alpha - 1)^2 + (\beta - 1)^2} \quad (19)$$

$$r = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2 \sum_{i=1}^n (Y_i - \bar{Y})^2}} \quad (20)$$

where the r Pearson correlation coefficient is used to measure the linear relationship between simulated values and observed values. $\alpha = \bar{X}/\bar{Y}$ represents the ratio of the average of the simulated and observed values, i.e., the ratio of the average of the simulated and observed values. $\beta = (\sigma_x/\bar{X})/(\sigma_y/\bar{Y})$ represents the ratio of the standard deviation σ_x , σ_y between the simulated and observed values, i.e., the ratio of the variability between the simulated and observed values. The closer the value is to 1, the better the model's performance in simulation is (Kling and Gupta, 2009).

The statistical significance of performance differences between models is assessed using Meng's Z-test for correlated correlations (Meng et al., 1992). Due to the interdependent (correlated) performance metrics, conventional tests like the t-test would be invalid here. Meng's test properly accounts for the high correlation between model forecasts, providing a more balanced and meaningful assessment of significance in the context of large hydrological



453 datasets. This method is particularly suitable for comparing dependent correlation coefficients
454 (e.g., KGE) derived from the same dataset. The test statistic is computed as:

$$z = \frac{1}{2} \ln\left(\frac{1+r}{1-r}\right)$$

$$Z = (z_1 - z_2) \times \sqrt{\frac{N-3}{2 \times (1-r_{12}) \times h}}$$

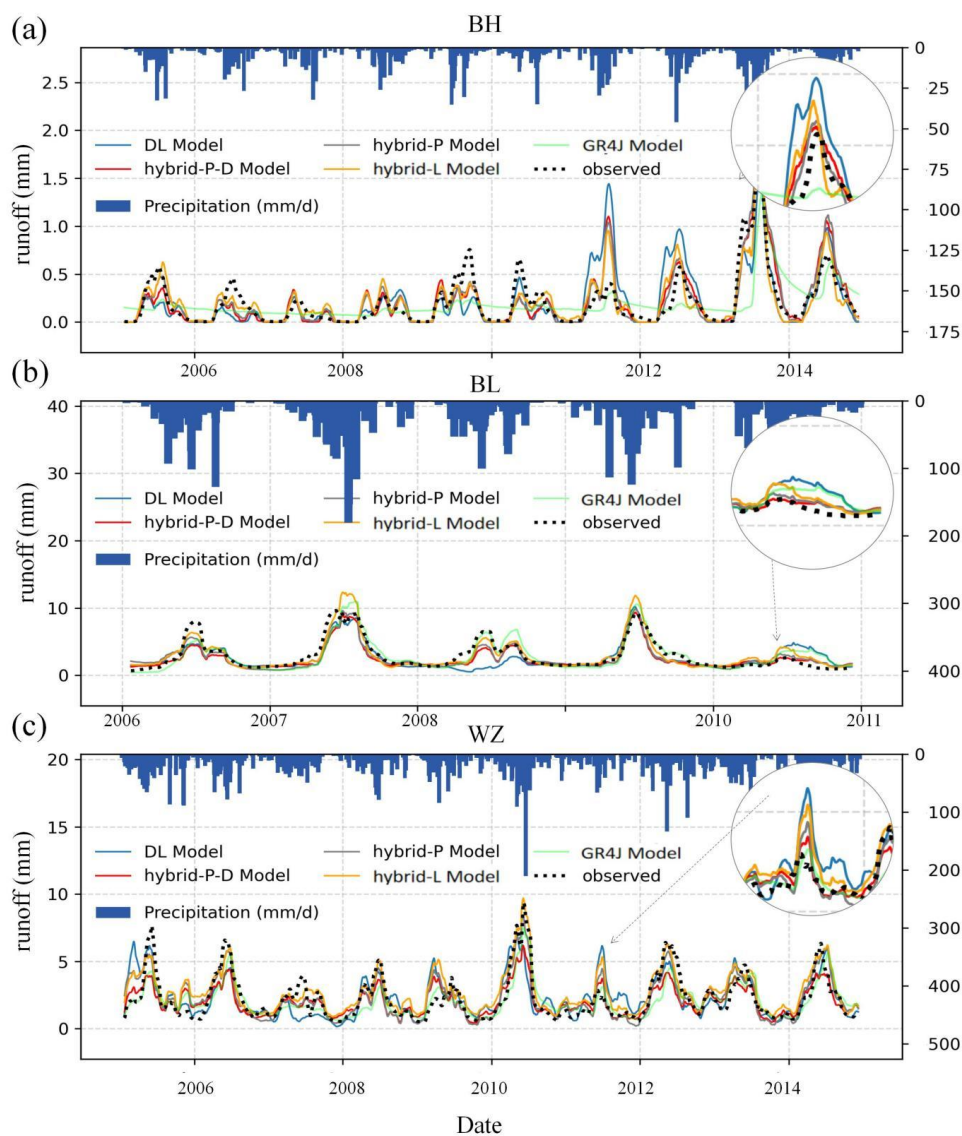
455 where: r is the Pearson correlation coefficient for a given model; z_1 and z_2 are Fisher's
456 z-transformations of the correlation coefficients for Data A and Data B, respectively; N is the
457 sample size; r_{12} is the correlation between the two sets of data predictions; h is a correction
458 factor accounting for the covariance structure

459



3. Results

3.1. Hybrid Model Evaluation Outlet Runoff in Trained Basins





463 **Figure 5. (a) (b) (c) Comparison of simulated and observed streamflows in the**
 464 **valid period.** The black dots represent observations, the blue dots represent the DL
 465 model, the red dots represent the hybrid-P-D model, the gray dots represent the hybrid-P
 466 model, the yellow dots represent the hybrid-L model, the green dots represent the
 467 Physical model (GR4J) and the blue bars represent precipitation. Partial detail enlarged
 468 image on the right side.

469 **Table 4. The results of 3 metrics (KGE, NSE and R^2) for five models (hybrid-L,**
 470 **hybrid-P, hybrid-P-D and DL models) in three study basins. Bold representation of the**
 471 **optimal model.**

Basin	Station	Model	KGE	NSE	R^2
HRB	BH	hybrid-L	0.766	0.551	0.774
		hybrid-P	0.820	0.655	0.823
		hybrid-P-D	0.821	0.650	0.822
		GR4J	0.440	0.356	0.359
		DL	0.687	0.340	0.715
DRB	BL	hybrid-L	0.767	0.713	0.845
		hybrid-P	0.785	0.736	0.858
		hybrid-P-D	0.784	0.735	0.858
		GR4J	0.783	0.622	0.622
		DL	0.702	0.600	0.781
GRB	WZ	hybrid-L	0.617	0.491	0.706
		hybrid-P	0.616	0.528	0.727
		hybrid-P-D	0.633	0.530	0.736
		GR4J	0.548	0.508	0.521



DL	0.607	0.379	0.644
----	-------	-------	-------

Overall, compared with the DL method, the three hybrid models perform well in accurately capturing runoff with appropriate amplitudes and times in the three study basins (Figure 5). At the BH station, the KGE values of the hybrid-P-D, hybrid-P and hybrid-L models are 0.821, 0.820 and 0.766, respectively (Table 4). At the WZ station, the KGE values of the hybrid-P-D, hybrid-P and hybrid-L models are 0.633, 0.616 and 0.617, respectively. The GR4J model provides a useful conceptual hydrological benchmark, but its simulations generally show weaker capability. The comparison results show that the hybrid-P-D and hybrid-P models perform better. Hybrid-P-D has the most significant improvement in the WZ station simulations. At the BH and BL stations, the performance of the hybrid-P models is significantly improved, indicating that plant LSTM modules can further enhance model performance. This enhancement is manifested in the R^2 and KGE values, with a significant increase of 0.056 at the BH station.

Table 5. Statistical significance of performance differences among five models (hybrid-L, hybrid-P, hybrid-P-D, GR4J and DL models) based on Meng's Z-test.

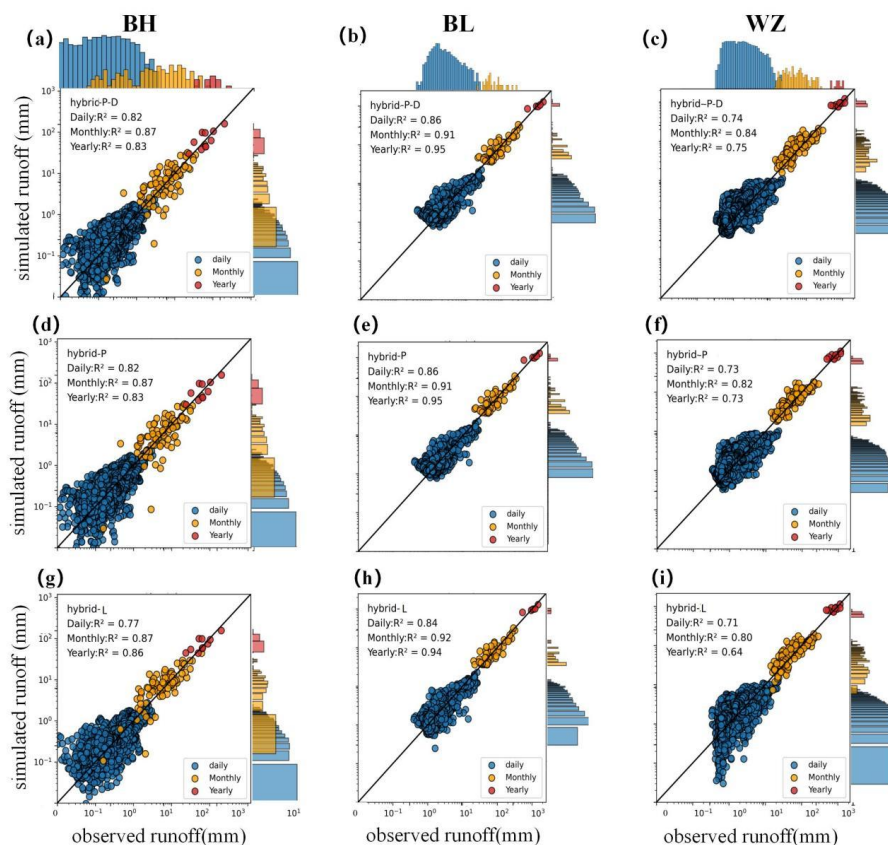
Note: Significance level: $p < 0.05$ (*), $p < 0.01$ (**), $p < 0.001$ (***). Performance direction based on NSE metric.

Model	hybrid-L	hybrid-P	hybrid-P-D	DL	GR4J
hybrid-L	-	<0.001***	<0.001***	<0.001***	<0.001***
hybrid-P	<0.001***	-	0.044*	<0.001***	<0.001***



hybrid-P-D	<0.001***	0.044*	-		<0.001***
DL	<0.001***	<0.001***	<0.001***	-	<0.001***
GR4J	<0.001***	<0.001***	<0.001***	<0.001***	-

488 The pairwise statistical comparisons using Meng's Z-test revealed that all model
 489 performance differences were statistically significant ($p < 0.05$), confirming good overall skill
 490 relative to the pure DL benchmark (Table 5). Among them, The hybrid-P-D models
 491 demonstrated significantly superior performance, improving the NSE and R^2 values by
 492 0.01-0.14. Its KGE spans 0.63-0.82, again surpassing the competing models. A comparison of
 493 the three models reveals that the plant LSTM module improves KGE most significantly at the
 494 BH station. The distribution module improved most significantly at the WZ station (Figure
 495 5b). This difference can be attributed to the BH being situated in a semiarid
 496 vegetation-transition zone, where the plant LSTM module excels at capturing
 497 vegetation-water processes with high accuracy. The WZ station spans the largest area within
 498 this zone, and the distribution module performs better in large basins. A detailed picture
 499 reveals that hybrid-P-D models excel under high-runoff events, whereas all the models
 500 perform similarly during low-runoff periods. Finally, incorporating explicit spatial
 501 heterogeneity clearly benefits runoff simulations. When the distributed module is applied to
 502 the three study basins, the NSE ranges from 0.53 to 0.7—up to 0.14 higher than its lumped
 503 counterparts — demonstrating that spatially resolved vegetation and runoff mechanisms
 504 enhance the predictive accuracy without sacrificing robustness.

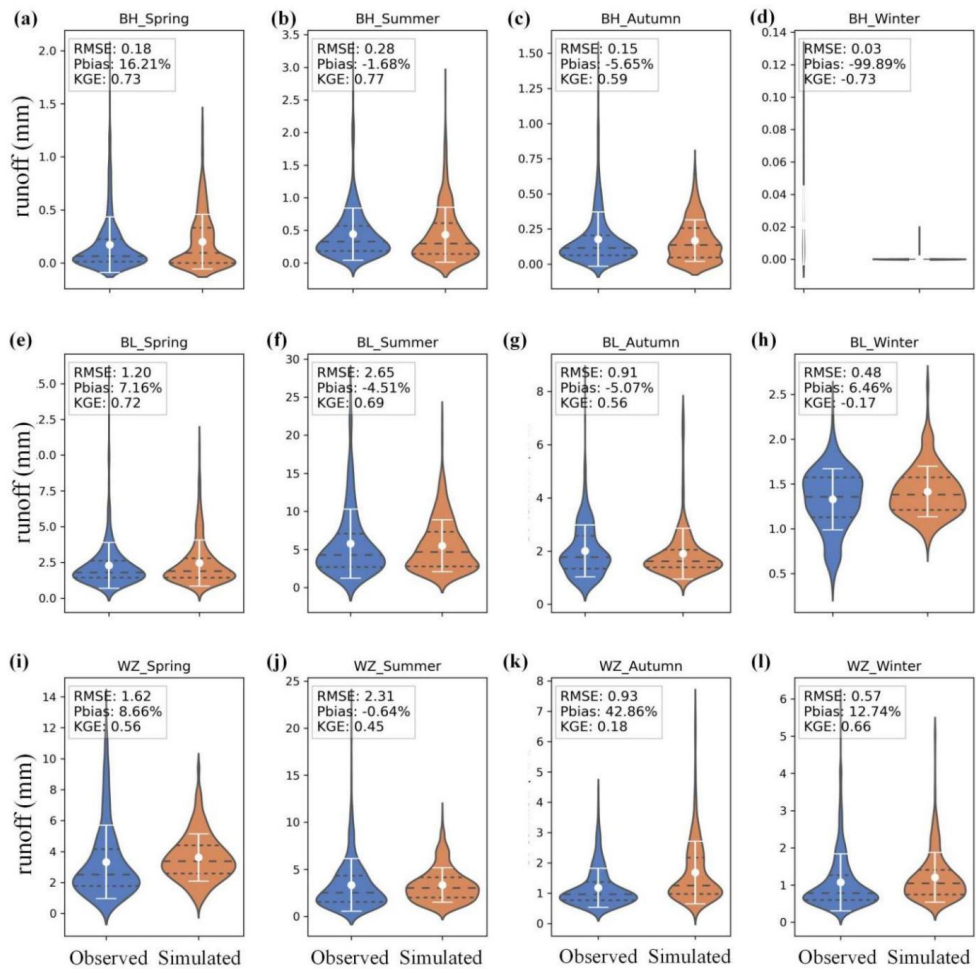


505

506 **Figure 6. Scatter plots depicting the simulated and observed runoff at daily,**
 507 **monthly, and annual timescales for three models (hybrid-L, hybrid-P and hybrid-P-D)**
 508 **across three stations (BH, BL and WZ).** The marginal histograms above and to the right of
 509 each scatter plot illustrate the frequency distributions of the observed (top) and simulated
 510 (right) runoff values at the three timescales. Each line represents the results for a specific
 511 model. Each column represents the results for a specific basin. The blue, yellow, and red
 512 markers denote daily, monthly, and yearly timescales, respectively. The solid 1:1 line
 513 indicates perfect agreement between the simulation and observation results.



514 **3.2. Comparison of Model Seasonal Performances across Three Basins**



516 **Figure 7. Violin plots comparing the distributions of observed (blue) and**
517 **hybrid-P-D simulated (orange) runoff values for each season.** From top to bottom: (a), (b),
518 (c), and (d) are the spring, summer, autumn and winter seasons, respectively, at the BH station;
519 (e), (f), (g), and (h) are the BL stations; and (i), (j), (k), and (l) are the WZ stations. Spring:
520 March–May; Summer: June–August; Autumn: September–November; Winter:
521 December–February. Each subplot displays statistical metrics, including the RMSE, NSE, and
522 KGE, reflecting the hybrid-P-D model’s performance in reproducing seasonal runoff.

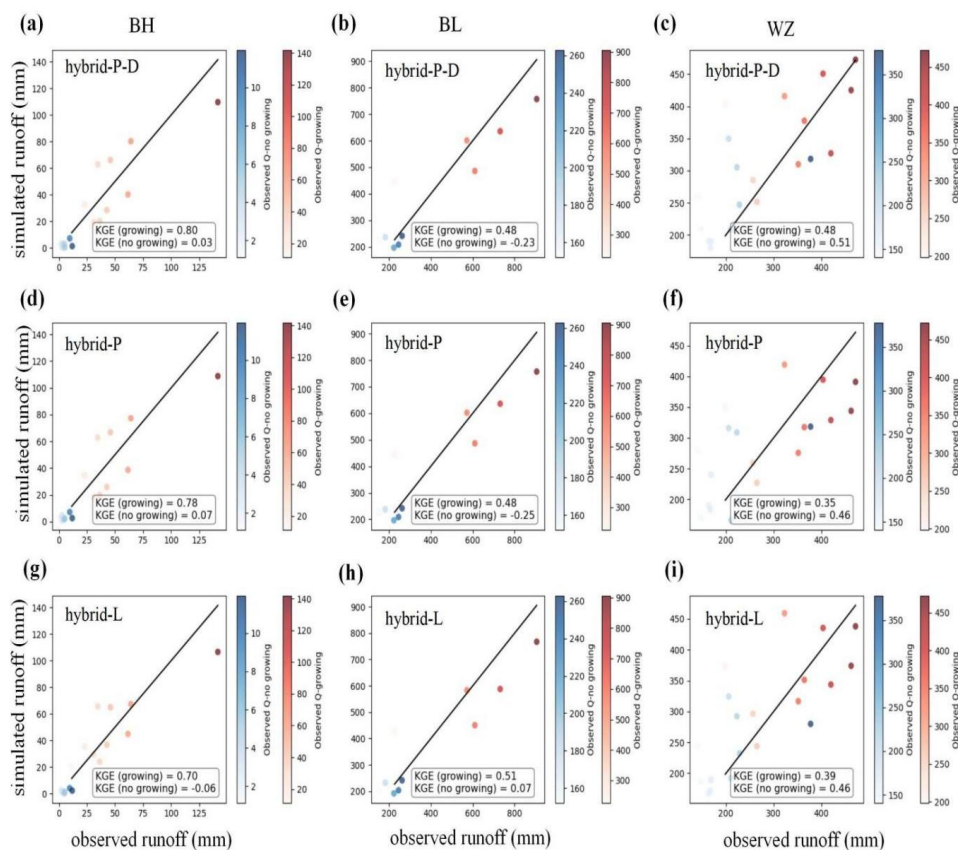


Figure 8. Scatter plot of the simulated and measured values for the growing season and nongrowing season. (a), (b), and (c) indicate the hybrid-P-D model; (d), (e), and (f) indicate the hybrid-P model; and (d), (e), and (f) indicate the hybrid-L model. Each line was evaluated at three stations (BH, BL and WZ). The growing season is from June to September, and the nongrowing season is from November to March of the following year. The blue color represents values during the nongrowing season, whereas the red color represents values during the growing season. Each point indicates the growing/nongrowing seasonally accumulated runoff, and the color intensity reflects the magnitude of the observed runoff.

For most stations, the “best” model of hybrid-P-D simulated distributions aligns with the observed distributions in terms of shape, mean, and variability during spring and summer. This is further supported by higher NSE and KGE values and lower RMSEs during these

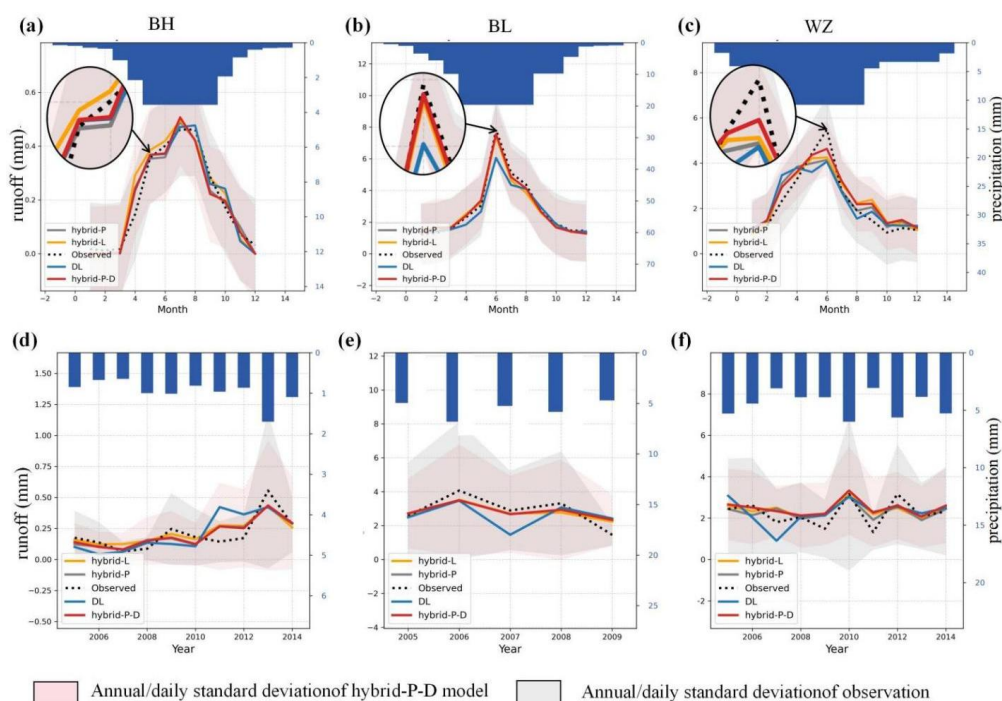


seasons. However, the model performance declines during winter at certain sites, particularly at the BH station (Figure 7d). At this site, the simulated runoff distribution is notably wider and more skewed than the observed distribution, as shown by the broader and asymmetrical violin shape. This indicates that the model overestimates the frequency of low-runoff events during winter. These results suggest that the hybrid-P-D model tends to overestimate low runoff under cold and drought conditions, resulting in highly skewed distributions and reduced NSE and KGE values. Overall, while the model demonstrates better performance during high-runoff seasons, larger deviations are observed during low-runoff conditions, as reflected in both the violin plot shapes and the performance metrics.

The scatter plot of runoff during the growing season and nongrowing season in the basin with measured values illustrates the extent to which vegetation influences runoff. Figure 8 shows the simulation of the Q-growing/Q-no growing scatter plots using the three models. Although the KGE values for both the hybrid-P-D and hybrid-P models are lower in low streamflow regions (Figure 8b, 8e), this mainly reflects the difficulty of simulating base flow, where the true discharge variations are so small that they are masked by measurement error and natural fluctuations. In contrast, the performance of the hybrid-P-D model (Figure 8c) slightly surpasses that of the hybrid-P model (Figure 8f), with a KGE increase of 0.13 at the WZ station. The hybrid-P-D model simulation is notably better during the growing season, as reflected by substantially higher KGE values than those during the nongrowing season. These findings indicate that the hybrid-P-D model is more effective at capturing runoff dynamics during periods of high vegetation activity. Notably, the improvement at the BH station was the most pronounced, increasing from 0.70 to 0.80, whereas at the WZ station, it increased from 0.35 to 0.48. In contrast, the improvement at the BL station was negligible. These results suggest that the hybrid-P-D model is particularly effective in larger basins such as the WZ and



559 in transitional vegetation zones such as the BH, where the interactions between vegetation and
 560 hydrology are more complex. Overall, the hybrid-P-D model outperforms the hybrid-P model
 561 in simulating Q-no growing.



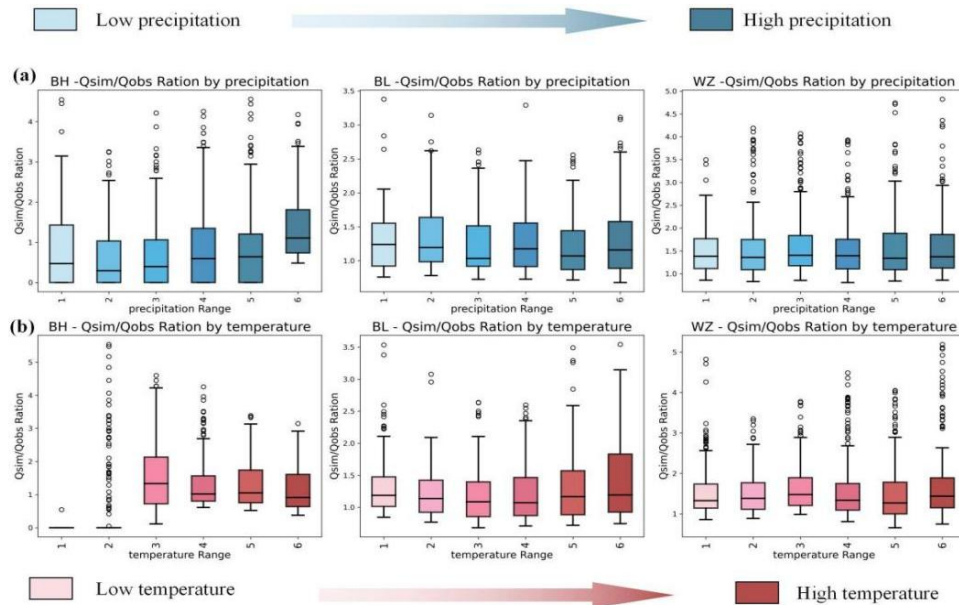
562 **Figure 9. (a)(b)(c) Multiyear average monthly runoff simulations for four models**
 563 **(hybrid-L in yellow, hybrid-P in gray, hybrid-P-D in red, and DL in blue) compared**
 564 **with observations (black dashed line), illustrating each model's ability to capture**
 565 **monthly patterns.** The red shaded area represents the variance in the hybrid-P-D simulation
 566 values, whereas the gray shaded area represents the variance in the hybrid-P simulation values.
 567 (d)(e)(f) Annual runoff simulations for the four models and observations, highlighting the
 568 interannual variability.
 569

570 Because the impact of vegetation on runoff is often masked by meteorology, the
 571 simulation accuracy for monthly runoff was extracted and compared separately. Overall,
 572 Figure 9 indicates that the hybrid-P-D and hybrid-P models outperform the DL model in



capturing monthly scale hydrological dynamics. The hybrid model and deep learning model successfully simulate the bimodal phenomenon at the BH station (Figure 9a). However, when simulating flood peaks, it is evident that in hybrid models, DL models anticipate the timing of the spring flood peak in advance. Among the models, the hybrid-P-D model provides the best simulation of the spring peak occurrence time (Figure 9c). However, Figure 9d, 9e and 9f shows that the DL, hybrid-P-D, hybrid-P and hybrid-L models perform poorly when simulating drought years (2007) with low precipitation, especially at the WZ station. A significant overestimation was observed in 2007, 2009, and 2011, which were the years with the least precipitation. However, based on the distribution of variance in the shaded areas, the hybrid-P-D model has a smaller variance than the hybrid-P model does, indicating higher accuracy in simulating peak runoff events.

Figure 10 shows boxplots of the ratio of simulated to observed runoff (Q_{sim}/Q_{obs}) according to different precipitation and temperature ranges. Q_{sim}/Q_{obs} is compared from low to high to analyze the model's adaptability to climate change. The results indicate that the "best" model of hybrid-P-D demonstrates good adaptability to climate change at both the WZ and BL stations, with no significant trend observed in the ratio of Q_{sim}/Q_{obs} as temperature and precipitation increase. In contrast, at the BH station, the ratio clearly increases with increasing temperature and precipitation, suggesting that the hybrid-P-D model tends to overestimate runoff under these conditions. These findings highlight the model's differential response to varying climates, with the hybrid-P-D model exhibiting a stronger tendency to overestimate runoff in dry and cold basins.



594

595 **Figure 10. Boxplots of simulated and observed runoff under different conditions. (a)**
 596 **Boxplots of hybrid-P-D simulations of observed runoff (Q_{sim}/Q_{obs}) under different**
 597 **precipitation conditions (blue).** It is classified into 6 equal parts to assess model
 598 performance across varying precipitation levels. The binned precipitation is classified as
 599 follows: for the BH site: <0.1, 0.1-0.2, 0.3-0.5, 0.6-1.3, 1.4-3.8, >3.9 mm/day; for the BL site:
 600 <0.1, 0.2-0.5, 0.6-2.0, 2.1-6.2, 6.3-16.2, >16.3 mm/day; for the WZ site: <0.1, 0.2-0.4, 0.5-1.4,
 601 1.5-4.3, 4.4-12.4, >12.5 mm/day. **(b) Boxplots of simulated and observed runoff under**
 602 **different temperature conditions (red).** The precipitation and temperature gradually
 603 increase from light to dark colors. The binned temperature is classified as follows: for the BH
 604 site: <-18.0, -18.1- -4.7, -4.8-8.5, 8.6-15.7, 15.8-19.4, >19.5°C; for the BL site: <17.6,
 605 17.7-22.8, 22.9-26.0, 26.1-27.4, 27.5-29.1, >29.2°C; for the WZ site: <8.1, 8.2-14.7, 14.8-20.7,
 606 20.8-24.8, 24.9-28.7, >28.8°C.

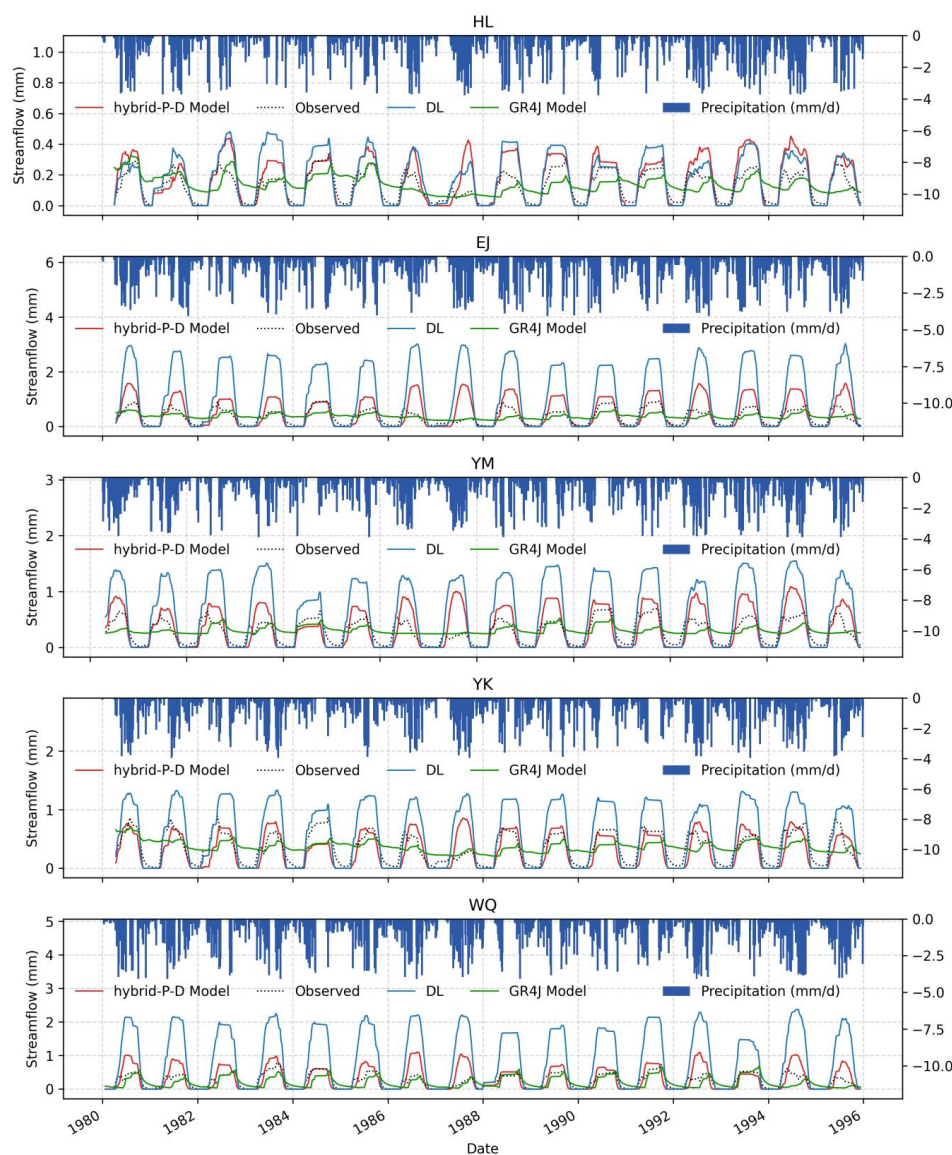
607 3.3. Evaluating Model Transferability in Nested Subbasins

608 To evaluate the model's transferability, we applied the parameters learned at the basin
 609 outlet (BH) directly to five nested catchments—HL, EJ, YK, YM, and WQ—without further
 610 training (Figure 11). We used a hybrid-P-D configuration for simulation because it demands



611 minimal local data and has the best calibration performance at the BH. A pure DL model with
612 identical hybrid-P-D model settings and training iterations was also employed for comparison.

613 The results show that hybrid-P-D achieved determination coefficients (R^2) between 0.56
614 and 0.76 across the five basins. Its PBIAS values were closer to zero than those of the DL
615 models were, indicating substantially lower systematic error. The results demonstrated that
616 the hybrid-P-D model, trained on data from basin outlet stations, performed impressively in
617 simulating the runoff process for nested basins. As shown in Figure 11, the hybrid-P-D model
618 also delivered a higher NSE than did the model based on the pure DL model, with the DL
619 model suffering the most pronounced performance degradation when transferred to ungauged
620 locations. Table 6 reveals that hybrid-P-D did not consistently outperform DL in terms of the
621 correlation coefficient R^2 . Instead, the key advantages of hybrid-P-D lie in the KGE and Pbias
622 — it substantially reduces systematic error, with Pbias values much closer to zero than those
623 of DL across all five transfer basins. However, the EJ station presented the lowest correlation
624 coefficient of 0.56. This can be attributed to the influence of human activities on the
625 hydrological processes in the basin above EJ station, such as the Honghuaerji Reservoir,
626 which plays a significant role in the runoff process. These activities complicate hydrological
627 simulation, leading to a decrease in model accuracy. To test spatial transferability, we applied
628 the parameters calibrated at the basin outlet (BH) directly to five nested subcatchments—HL,
629 EJ, YK, YM, and WQ — without any retraining. Under identical training conditions, the
630 hybrid-P-D model consistently outperformed the pure DL benchmark: R^2 increased to
631 0.56-0.76, KGE increased by up to 0.85, R^2 increased 0.07, and absolute Pbias decreased by
632 11.65% at the midstream and upstream stations (EJ, YK, WQ). These gains demonstrate that
633 hybrid-P-D can be generalized across space while requiring less calibration data.



634

635 **Figure 11. Comparison of simulated (hybrid-P-D, GR4J and DL models) and**
 636 **observed runoff during the valid period at the HL, EJ, YM, YK, and WQ stations in the**
 637 **HRB. The black dashed curve represents the observations, the blue line represents the DL**
 638 **model, the green line represents the GR4J model, the orange line represents the hybrid-P-D**
 639 **model, and the blue bars represent precipitation.**



640

641 **Table 6. Comparison of hybrid model performance in five transfer basins. Bold**
 642 **represents the optimal model.**

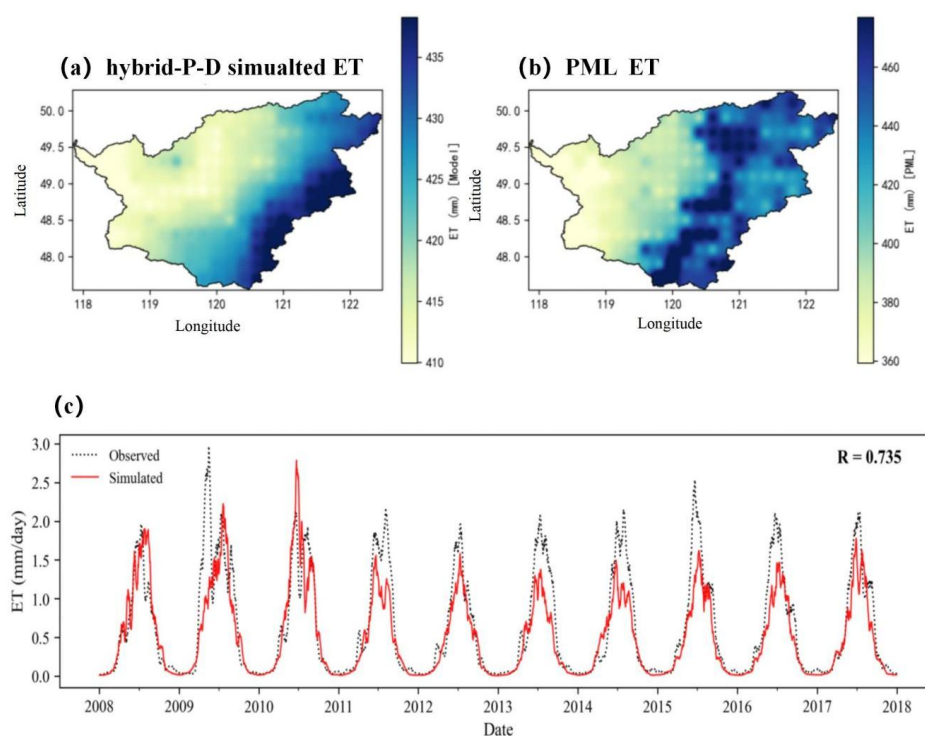
Station	Model	R ²	Pbias (%)	KGE
HL	hybrid-P-D	0.77	37.98	0.42
	GR4J	0.04	7.94	0.17
	DL	0.82	43.42	0.33
EJ	hybrid-P-D	0.57	37.35	0.35
	GR4J	0.09	-5.46	0.05
	DL	0.59	172.30	-1.34
YM	hybrid-P-D	0.62	15.86	0.58
	GR4J	0.10	-11.48	0.04
	DL	0.65	93.79	-0.21
YK	hybrid-P-D	0.60	-17.89	0.52
	GR4J	0.04	-1.14	0.03
	DL	0.66	49.35	0.33
WQ	hybrid-P-D	0.61	-7.35	0.49
	GR4J	0.41	-33.95	0.39
	DL	0.63	127.59	-0.38

643 3.4 Spatial and temporal validation of evapotranspiration

644 To verify whether the improved runoff predictions are physically consistent, we
 645 compared model-simulated evapotranspiration (ET) against satellite-based ET products
 646 (PML-V2) for the HRB, both spatially and temporally. Figure 12 presents the spatial



distribution of mean annual ET from the Hybrid-P-D model, the PML-V2 reference, and their difference. The Hybrid-P-D model reproduces the observed spatial gradient of higher ET in the downstream forested areas and lower ET in the upstream grasslands, with a pixel-wise RMSE = 45.5 mm yr⁻¹. The figure reveals slight underestimation in forest-grassland transition zones. Despite these localized discrepancies, the overall bias is evenly distributed, with no significant spatial clustering. This spatial consistency confirms that the distributed physical constraints translate land-surface heterogeneity into realistic ET patterns.



654

655 **Figure 12. Spatial and temporal validation of evapotranspiration in the HRB. (a)**
 656 **Hybrid-P-D simulated annual ET; (b) satellite-based annual ET (PML-V2); (c)**
 657 **Temporal comparison of daily evapotranspiration between Hybrid-P-D simulation and**
 658 **observations at the Hulunbuir flux tower in the HRB**



Figure 12(c) compares the temporal dynamics of daily ET between the Hybrid-P-D simulation and flux tower observations over the validation period. The model captures the seasonal cycle and interannual variability well, with a correlation coefficient of $R = 0.735$ between simulated and observed values. It reproduces the ET peak during the growing season and the low ET during winter dormancy, indicating that the dynamic vegetation module effectively tracks phenological water-use patterns.

4. Discussion

4.1. Comparison of Model Performance with Different Module Improvements

Accurate runoff simulations under climate change, particularly in data-scarce regions, are critical for effective water resource management. Our three hybrid models integrate dynamic vegetation–hydrological interaction mechanisms with distributed grid mechanisms by coupling deep learning and physical approaches. A validation across three Chinese basins representing dryness–wetness gradients revealed that the hybrid-P and hybrid-P-D models performed best. Notably, the hybrid-P-D model demonstrated superior performance in large basins with complex and heterogeneous underlying surface conditions. In contrast, the hybrid-P model, which does not rely on topographic or vegetation data, exhibited comparable accuracy to the hybrid-P-D model in medium- and small-sized basins, rendering it more suitable for regions with limited data availability (Figure 5). Compared with purely process-based or data-driven approaches, the hybrid-P-D model improved the KGE from 0.68 (DL model) to 0.82 (Table 4). By comparing the hybrid-P and hybrid-L models, we found that the plant LSTM module increased the KGE from 0.70 to 0.78 during the plant growing season. This indicates that the vegetation module improves the model’s ability to extrapolate to



681 ungauged basins and capture seasonal hydrological dynamics (Figure 11) (Li et al., 2022; A et
682 al., 2024; Bassani et al., 2024).

683 Although the fully distributed hybrid-P-D model achieved the best overall performance
684 in the semi-arid HRB, its advantage over the much simpler GR4J benchmark was limited in
685 the humid DRB, where both models produced comparable KGE values (GR4J:KGE=0.783 vs
686 Hybrid-P-D:KGE=0.784)(Table 4). This result suggests that the benefit of model complexity
687 is context dependent rather than universally required. In humid basins with relatively stable
688 runoff-generation conditions, a parsimonious conceptual model may already capture the
689 dominant hydrological response. By contrast, in the semi-arid HRB, particularly during
690 extreme low-flow periods such as the 2007 drought at the WZ station, the hybrid-P-D model
691 showed a more evident improvement over GR4J. For the ungauged sub-basins, including HL,
692 EJ, YM, YK, and WQ, the hybrid-P-D model was able to generate transferable simulations
693 using parameters learned from the basin outlet, whereas GR4J cannot be directly applied
694 without local calibration.

695 The performance gain stems from the vegetation module, which dynamically
696 parameterizes vegetation regulation within a distributed grid-based framework. Surface
697 evapotranspiration is modeled as a linear function of soil water content (*SWC*) coupled with a
698 dynamic stomatal resistance function (r_s), allowing accurate quantification of vegetation
699 transpiration responses under water stress. This approach effectively mitigates the
700 underestimation of runoff across multiple time scales (Figure 6) (Wu et al., 2024). The model
701 incorporates the spatial heterogeneity of vegetation types (e.g., LAI and canopy height) within
702 a $1 \times 1 \text{ km}^2$ grid, improving flood peak simulations and peak timing (Figure 5). Such



703 improvements are critical for accurately simulating the impacts of vegetation on hydrological
704 cycles across various land covers and climate regimes.

705 One of the key advantages of the hybrid-P-D model lies in its superior transferability
706 compared with traditional DL models (Figure 11). In regions where the soil depth and climate
707 closely resemble those in the training domain, the model performance has a correlation
708 coefficient (R^2) greater than 0.76. This enhanced transferability of the hybrid-P-D model
709 arises from its explicit integration of physical constraints and hydrological knowledge. Unlike
710 standard DL models, which rely solely on training data and often struggle when applied to
711 unseen environments, the hybrid-P-D model reduces this reliance by embedding physical
712 equations, such as dynamic infiltration capacity. These embedded processes serve as internal
713 priors that constrain model outputs within hydrologically reasonable ranges. As a result, the
714 hybrid-P-D model can capture transferable process representations that remain valid across
715 diverse climatic and ecohydrological regimes (Bindas et al., 2024; Feng et al., 2022). To
716 further improve the robustness and generalizability of hybrid models across climatic gradients,
717 we recommend extending the training durations and including larger catchments in future
718 studies.

719 Independent ET evaluation provides evidence for the hydrological plausibility of the
720 PIDL-DHM model. The comparison with PML-derived ET indicates that the model does not
721 exhibit a systematic basin-wide bias, suggesting that the overall magnitude and large-scale
722 spatial pattern of evapotranspiration are reasonably represented. However, relatively larger
723 errors occur in the transitional zones, where climatic gradients, vegetation structure, and
724 soil-moisture controls change more rapidly. These localized discrepancies imply that the
725 current model can capture the first-order spatial pattern of ET, but still has limitations in



726 representing fine-scale ecohydrological transitions. Future improvements should therefore
727 focus on strengthening the representation of spatially heterogeneous vegetation and soil-water
728 processes, for example by incorporating remote-sensing-based dynamic vegetation structural
729 parameters, canopy height, rooting depth, or soil-moisture constraints.

730 **4.2. Model performance influenced by different climates**

731 We validated the hybrid model across three diverse Chinese basins, which represent
732 gradients of dryness, wetness, and vegetation types, to assess its adaptability to varying
733 hydrological conditions. These basins, with distinct hydroclimatic characteristics, provide a
734 comprehensive test of the model's robustness in different environmental contexts. The
735 hybrid-P-D model exhibited strong adaptability to seasonal variations and dry–wet gradients,
736 showing its ability to capture seasonal fluctuations in vegetation–water interactions. The
737 simulations conducted for the spring, summer, and autumn seasons across these regions
738 revealed that the simulated runoff distributions closely aligned with the observed values
739 (Figure 8), reflecting good overall robustness and adaptability. These seasons correspond to
740 peak root activity and transpiration, during which the dual-runoff generation mechanism
741 module enhances simulation accuracy through soil moisture regulation (Figure 7).
742 Additionally, the model was able to simulate winter runoff accurately in nonfrozen basins,
743 such as the GRB and DRB, indicating its strong ability to handle seasonal shifts in runoff
744 generation.

745 Additionally, our hybrid framework captures long-term trends remarkably well across
746 most study basins. In dry years (such as 2007), low precipitation led to abnormal runoff
747 fluctuations, and the DL models tended to underestimate runoff (Figure 9), whereas the
748 hybrid-P-D model improved significantly. In the GRB and DRB basins, $Q_{\text{sim}}/Q_{\text{obs}}$ maintains



749 stable performance under gradually increasing temperature and precipitation conditions,
750 underscoring its ability to translate climatic signals into hydrological responses more
751 faithfully than conventional data-driven approaches do (Figure 10). Nevertheless, limitations
752 have emerged in semiarid grassland basins such as the HRB (Figure 8b). A significant
753 positive trend was observed in the Q_{sim}/Q_{obs} with increasing temperature and precipitation, a
754 pattern not observed in deep-rooted forest-dominated regions. This discrepancy suggests that
755 the vegetation module may inadequately represent long-term vegetation–climate–runoff
756 interactions in semiarid areas, potentially owing to the memory limitations of the RNN and
757 LSTM architectures over extended time series (Du et al., 2024; Wei et al., 2024). Grasslands,
758 characterized by shallow root systems and low water storage capacity, exhibit intensified
759 evapotranspiration under drought, exacerbating water loss (Wang et al., 2024). In contrast,
760 deep-rooted forests maintain stability during dry seasons by accessing deeper soil moisture,
761 thereby delaying runoff decline and maintaining baseflow (Wang et al., 2023; Jiang et al.,
762 2023). Explicit representations of dynamic rooting depth and moisture redistribution may help
763 improve model performance for basins with contrasting vegetation, such as the HRB.

764 To clarify these complexities in runoff generation, we propose an improved runoff
765 generation module that features dynamic switching between infiltration-excess (dry
766 conditions) and saturation-excess (wet conditions) mechanisms (Jiang et al., 2023). This
767 dual-mechanism approach allows the model to adaptively switch runoff generation
768 mechanisms based on real-time environmental conditions (Liang et al., 1994). Specifically,
769 parameters such as the infiltration curve shape factor (b) and maximum infiltration capacity
770 (I_{max}) are dynamically adjusted according to changing climatic and soil conditions (Table 2).
771 By dynamically modifying b and I_{max} , the model enables adaptive switching between
772 infiltration-excess runoff during dry periods and saturation-excess runoff under wet



773 conditions. One key advantage of this approach is its ability to capture the “crust formation”
774 of the soil surface, a phenomenon that often reduces infiltration capacity under climate stress.
775 Traditional static runoff schemes frequently underestimate this process, which leads to
776 inaccurate predictions, particularly under extreme climate conditions (Li et al., 2023; Patil et
777 al., 2014). By integrating this dynamic process, the model provides a more accurate
778 representation of the transitional dynamics between infiltration-excess and saturation-excess
779 runoff mechanisms (Steenhuis et al., 2013).

780 Overall, integrating the dual runoff generalization mechanism into the hybrid model
781 markedly enhances its ability to simulate key hydrological dynamics under climate change,
782 particularly across moisture gradients, seasonal transitions, and vegetation-mediated
783 responses. This improved simulation fidelity is not merely a statistical enhancement but holds
784 significant practical value for increasing the reliability of seasonal water supply forecasts and
785 refining climate change impact assessments in ecologically vulnerable regions. To further
786 strengthen the model’s utility, future work should focus on two key directions: (1)
787 incorporating more detailed parameterizations of frozen soil and root depth dynamics to
788 enhance physical realism, and (2) testing the generalizability of this framework by integrating
789 it with other established hydrological models (e.g., SWAT, VIC) or applying it to diverse
790 hydro-climatic regimes, such as arid basins or urbanizing catchments. These advancements
791 will solidify the model’s role as a robust tool for supporting adaptive water resource
792 management and ecological protection strategies (Wang et al., 2024; Wang et al., 2023; Jiang
793 et al., 2023).



794 5. Conclusions

795 This study develops a novel physics-informed deep learning framework that explicitly
796 integrates vegetation physiological processes and a dual runoff generation mechanism within
797 a fully distributed architecture. By coupling hydrological process representations with
798 vegetation parameterization, the model captures vegetation-hydrology feedbacks and spatially
799 heterogeneous runoff dynamics under changing climate conditions. The principal findings are
800 as follows.

801 (1) According to multiple evaluation metrics and time scales, both the hybrid-P and
802 hybrid-P-D models demonstrate relatively high accuracy ($R^2 > 0.74$ daily) and effectively
803 capture the temporal changes in runoff during the growing season. The hybrid-P-D model
804 performs better in large basins characterized by complex and heterogeneous surface
805 conditions, whereas the hybrid-P model requires less terrain or vegetation data and achieves
806 comparable accuracy in small- and medium-sized basins, making it more suitable for
807 data-limited regions.

808 (2) The hybrid-P-D and hybrid-P model frameworks exhibit strong transferability and
809 spatiotemporal generalizability by embedding unsaturated runoff processes. While the GR4J
810 achieved comparable performance in humid basins, the hybrid models demonstrate
811 advantages in more complex, data-scarce environments. The model more realistically captures
812 the transitional dynamics between the two runoff mechanisms, requiring only downstream
813 station data to simulate upstream and ungauged subbasin runoff satisfactorily. Augmenting
814 training with additional upstream stations improves localized simulations, areas where depth
815 and climate significantly deviate from the training domain.



816 (3) Spatial validation against PML-derived evapotranspiration indicates that the
817 hybrid-P-D model does not exhibit a systematic basin-wide ET bias and can reasonably
818 represent the overall magnitude and large-scale spatial pattern of evapotranspiration. However,
819 This study also revealed the shortcomings of current models in transitional zones where
820 climatic gradients, vegetation structure, and soil-moisture controls change rapidly. Future
821 work should therefore incorporate more detailed parameterizations of dynamic rooting depth,
822 canopy structure, frozen soil processes, and soil-moisture redistribution, as well as more
823 diverse training datasets, to further improve model generalization under extreme climate
824 events and seasonal edge conditions.

825 Future work should test the model on larger and more diverse datasets spanning broader
826 climate and vegetation zones to rigorously evaluate its generalization ability, strengthening
827 parameterization research on complex physical and physiological processes, such as
828 freeze–thaw cycles, root depth dynamics, and soil microstructure evolution, in the interaction
829 between vegetation and hydrology is necessary. Through these efforts, PIDL-DHM are
830 expected to become important tools for water resource management and ecological protection
831 in the context of climate change, providing solid scientific support for achieving sustainable
832 basin management.

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837 Credit Author Statement

838 **Junping Wang:** Data curation, Methodology, Writing - original draft. ; **Baolin Xue:**
839 Conceptualization, Writing - review & editing, Funding acquisition; **Guoqiang Wang:**
840 Project administration, Writing - review & editing, Supervision.

841 **Source code availability:** The source code is publicly available on Zenodo at record
842 18833916: <https://zenodo.org/records/18833916>. The archive includes the source code, model
843 training scripts, and a pre-trained model checkpoint, along with scripts for data preprocessing
844 and hydrological computations.

845 **Data availability:** The datasets used in this study are subject to confidentiality
846 restrictions and cannot be publicly shared. However, example data (HLE_BH_data.csv and
847 HLE_BH_surfacedata.csv) is available on Zenodo at record 18833916, :
848 <https://zenodo.org/records/18833916>.

849

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