



2 **First Alps-wide reconstruction of LGM glacial sediment transport enabled by GPU-accelerated particle tracking**

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12 **Abstract.** Reconstructing the transport histories and provenances of glacial sediments and ice-contact
14 deposits (e.g. tills, moraines) in formerly glaciated regions remains a major challenge, particularly at icefield-
to ice-sheet scales and over multi-millennial timescales. Yet such reconstructions are central to key questions
in Quaternary science, including estimates of past glacial erosion rates and sediment fluxes, the role of
16 subglacial sediment storage in erosion buffering, or the reconstruction of past ice-flow dynamics, ice divides,
and confluences. While numerical modelling can enable one to reproduce past glacial sediment transport
18 via coupling glacier models with Lagrangian particle tracking, this becomes computationally unfeasible over
large spatial domains and paleo timescales using traditional computing. As a result, no study to date has
20 simulated glacial sediment transport using large particle numbers (tens of millions) across continental-scale
icefields such as the European Alps during the Last Glacial Maximum (LGM): a pre-requisite given the
22 ubiquitous nature of sediments in glacier systems. In this study, we overcome this limitation through a new
coupling of 3D Lagrangian particle tracking with Graphics-Processing-Units (GPU)-accelerated, high-
24 resolution glacier simulations based on the deep-learning-enhanced Instructed Glacier Model (IGM). Our
approach unlocks the ice advection of tens of millions of particles at minimal additional computational cost,
26 allowing simulations of glacial sediment transport across the European Alps over multi-millennial timescales
(40-18 ka) and at an unprecedented spatial resolution of 300 m. In doing so, we produce the first Alps-wide
28 modelling reconstruction of glacial sediment transport during the LGM, using process-based particle seeding
schemes to represent both subglacial (e.g. abrasion, plucking) and supraglacial (e.g. rockfall, landslides)
30 sediment sourcing. Results are analysed through complementary ‘sink-to-source’ (deposit provenance) and
‘source-to-sink’ (potential depositional pathways) analyses, enabling us to reconstruct the LGM glacial
32 transport of numerous ice-contact deposits and surface lithologies across the Alps. We find that
supraglacially sourced glacial sediments are typically eroded earlier, experience longer glacier residence
34 times, and undergo greater cumulative ice-free exposure than those of subglacial origin, with implications
for the interpretation of cosmogenic nuclide inheritance in glacial deposits. Our new coupled glacier-particle
36 modelling framework opens avenues for quantitative model-data comparisons using glacial geomorphology
and provides a powerful tool for reconstructing paleo ice dynamics, sediment provenance, and Quaternary
38 glacial landscape evolution.



40 **1 Introduction**

42 In the early 1800s, pioneering naturalists argued certain sediments found in mountain forelands evidenced
widespread past glacier expansions, an idea commonly known as the ‘glacier theory’ (e.g. Esmark, 1824;
44 Venetz, 1830; Agassiz, 1840; Lyell, 1840). Their hypotheses were later validated by investigations
characterizing deposits emplaced at the lateral, frontal, or subglacial margins of former glaciers, icefields,
46 and ice sheets (Sugden & John, 1976). These so-called ‘ice-contact deposits’ include erratic boulders,
lateral and terminal moraines, till units, drumlins, eskers, lineations, and various other glacio-depositional
48 landforms (Evans & Benn, 2004). Over the last two centuries, glacial geologists have studied these
features across formerly glaciated landscapes to reconstruct the extent, duration, style, and timing of past
50 glacier advances and retreats (e.g. Penck & Brückner, 1909; Evans et al., 2006; Ehlers et al., 2011; Davies
et al., 2012; Clark et al., 2022). In the European Alps, a long tradition of such work has focused on
52 reconstructing Quaternary glaciations of the Alpine Ice Field (AIF) (e.g. Geikie, 1910; van Husen, 1997;
Kelly et al., 2004; Preusser et al., 2010, 2011; Graf et al., 2015; Ivy-Ochs, 2015; 2022). Consequently, the
54 processes of ice-contact sediment deposition and post-depositional disturbance are often well documented
in many regions.

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By contrast, the pre-depositional histories of ice-contact deposits are often poorly constrained. The
58 inaccessibility and complexity of glacial sediment erosion/transport processes challenge empirical
characterization in modern glacier systems, and even more so in paleo settings (Boulton, 1996). Field
60 studies attempting to quantify pre-depositional histories in active glacier systems use techniques such as
mineralogical provenance analyses (e.g. Herman et al., 2015), detrital and *in situ* low-temperature
62 thermochronology (e.g. Enkelmann & Ehlers, 2015), terrestrial cosmogenic nuclide concentrations (e.g.
Guillon et al., 2015), morainic soil material’s fingerprinting analysis (e.g. Mohammadi et al., 2024), or
64 luminescence rock surface burial dating (Margirier et al., 2025). However, these studies are rare, often
limited to individual deposits or catchments, and difficult to extend to paleo glacier events. As a result, the
66 provenance, erosion histories, transport distances, durations, and pathways of ice-contact deposits remain
highly challenging to constrain at larger spatial and temporal scales.

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Yet understanding glacial sediment erosion/transport history and their provenance is critical for multiple
70 research questions. Such insights can, for instance, improve estimates of Quaternary glacial erosion rates
and sediment fluxes, complementing studies of glaciofluvial sediment export dynamics (e.g. Koppes et
72 al., 2015; Herman et al., 2015; Lane et al., 2017; Overeem et al., 2017; Delaney et al., 2023). They also
inform mechanisms and timescales of debris cover and subglacial sediment storage, involved in bedrock
74 shielding and erosion buffering (Delaney & Anderson, 2022). Pre-depositional sediment histories can also
reveal past ice dynamics, including interactions with topography and the mechanisms of flow

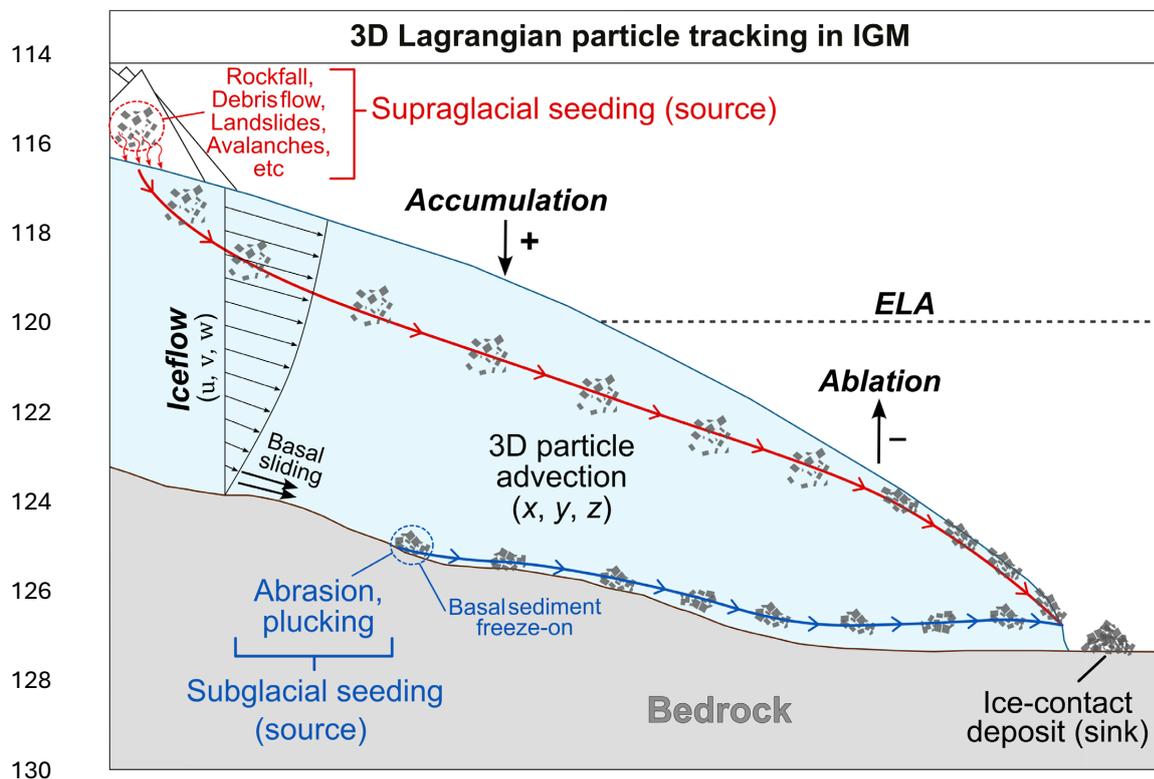


76 convergence/divergence associated with tributary glaciers merging or separating during waxing and
waning cycles of ice sheets or icefields (Jouvet et al., 2017). These reconstructions aid in identifying
78 former ice-flow regimes and the position or migration of ice divides, key to interpreting sedimentary
archives of past ice-flow directionality (e.g. Hughes et al., 2010; Kamleitner et al., 2024) and to mapping
80 former ice transfluences (e.g. Reitner et al., 2010). Moreover, knowing whether a deposit reached glacier
ice supraglacially or subglacially, and its glacial transport history, supports the application of
82 geochronological methods (e.g. cosmogenic exposure or luminescence dating), where prior exposure to
sunlight or the atmosphere can affect age interpretations (e.g. Heyman et al., 2011). Quantifying glacial
84 sediment routing and export in formerly glaciated landscapes is also crucial to inform industries for
instance concerned with aggregate resources or the geological disposal of nuclear waste (e.g. Fischer et
86 al., 2015; 2021). Lastly, tracking the transport history of iconic glacial erratics, some of which have
cultural significance (Reynard, 2004; Coutterand, 2018), offers an opportunity to bridge scientific
88 understanding with public engagement. Thus, while it represents a substantial challenge, characterizing
the pre-depositional history of glacial sediments and ice-contact deposits yields widespread implications
90 for numerous research fields.

92 Numerical modelling offers a means to address the above knowledge gaps by generating spatially
distributed, time-evolving estimates of glacial sediment transport which can be compared against
94 empirical point data (e.g. Veness et al., 2025). A robust and established method consists in coupling a
glacier evolution model with Lagrangian particle tracking to simulate the time-transient advection of
96 sediment-like particles by ice-flow (e.g. Rybak & Huybrechts, 2003; Rowan et al., 2015; Bernard et al.,
2020; Scherler & Egholm, 2020). When modelled glacier geometries are somewhat consistent with
98 empirical evidence, and when particle seeding is parameterised to mimic real sediment erosion processes,
this method can produce first-order estimates of glacial sediment transport pathways (Margirier et al.,
100 2025). However, no studies have yet coupled Lagrangian tracking of large particle numbers ($>10^6$) to
multi-millennial-scale simulations of past Alpine Ice Field (AIF) glaciations. This is largely due to two
102 constraints. First, previous AIF simulations exhibited potent mismatches in ice thickness compared to field
data, limiting confidence in inferred ice-flow dynamics (Mey et al., 2016; Seguinot et al., 2018; Jouvet et
104 al., 2023). Second, standard numerical approaches impose a high computational cost and high memory
requirement when conducting Lagrangian tracking of large particle numbers: i.e. tens to hundreds of
106 millions of particles. Given the highly ubiquitous nature of sediments in glacier systems, such high particle
numbers are essential if one wants to realistically depict some of the natural processes involved (Rowan
108 et al., 2015). Consequently, no studies to date have simulated glacial sediment transport using large particle
numbers across continental-scale icefields like the AIF at any timescale, let alone over thousands of years.

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131 Figure 1. Simplified schematic diagram illustrating the Graphics-Processing-Units (GPU) - based, 3D
132 Lagrangian particle advection scheme of both supraglacially seeded (red) and subglacially seeded (blue)
133 particles coupled with our Instructed Glacier Model (IGM) setup and implemented in this study. 'ELA'
134 stands for 'Equilibrium Line Altitude'.

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Here we show that these bottlenecks can be overcome. Leger et al. (2025) produced an ensemble of 100
152 high-resolution (300 m) simulations of the AIF during the Last Glacial Maximum (LGM), whose best-
performing simulations improved model-data agreement in both ice thickness and extent compared to
154 previous efforts (e.g. Seguinot et al., 2018; Jouvét et al., 2023). These advances were enabled by the
Instructed Glacier Model (IGM), a high-order, thermo-mechanically coupled glacier evolution model
156 (Jouvét et al., 2021; Jouvét & Cordonnier, 2023). IGM leverages physics-informed machine learning and
computation on Graphics Processing Units (GPU) to reduce the computational cost of traditional glacier
158 modelling by several orders of magnitude. Here we show that IGM's novel GPU-based architecture also
enables efficient parallelization of Lagrangian particle tracking, permitting to couple the advection of
160 millions of particles within our AIF model framework at minimal additional cost (see Results section) and
consequently track the glacial-transport trajectories of individual particles from their location of origin
162 (the source) to their final deposition site (the sink).

164 To this end, we conduct a new set of Alps-wide simulations of the last glaciation of the European Alps
using the same data-consistent IGM setup as Leger et al. (2025) with the additional coupling of 3D
166 Lagrangian tracking of large particle numbers. Ultimately, we produce the first Alps-wide model estimates
of time-transient and 3D glacial sediment trajectories between 40 and 18 ka, the period bracketing the
168 LGM. We design a new particle advection module and seeding scheme that simulates both the subglacial
(e.g. via abrasion, plucking) and supraglacial (e.g. via rockfall, debris flow) origins of glacially transported
170 sediments (Fig. 1). By introducing this new method, we can simulate the complex glacial-transport
trajectories of LGM ice-contact deposits (e.g. terminal moraines) across the Alps at high spatial (300 m)
172 and temporal (10 yr) resolutions, and estimate their provenances, glacial transport time, erosion timing,
and cumulative ice-free time during their source-to-sink journey. With this experiment, we also model the
174 possible LGM source-to-sink trajectories of certain surface lithologies (i.e. sources) throughout the Alps,
which we subsequently compare against empirical data on LGM-dated erratics of known location and
176 lithology (e.g. Kamleitner et al., 2022).

178 The Alps-wide results of this study are presented below and under the form of figure catalogues and
trajectory shapefiles accessible via the Zenodo repository attached to this paper (link:
180 <https://doi.org/10.5281/zenodo.18374156>). They provide the means to compare our spatially distributed
modelling estimates against empirical evidence on, for instance, deposited LGM erratics and their
182 lithologies/provenance, former ice-flow direction during the LGM, documented ice transfluences, and
preserved post-retreat deposits and mapped moraines. We believe this first Alps-wide reconstruction of
184 LGM glacial sediment transport will prove useful to glacial geologists, geomorphologists,
sedimentologists, and industries studying ice-contact sediments related to the last glaciation of the
186 European Alps. This new ability to conduct coupled glacier-particle modelling over continental and multi-
millennial scales opens the door to new model-data comparisons which, in turn, can further improve the



188 accuracy of future AIF models. We provide examples showing how such model estimates can address
empirical debates and raise new hypotheses that can be tested via future field campaigns. Finally, this
190 study provides a novel, computationally efficient modelling workflow which opens the possibility to
produce high-resolution estimates of the erosion, transport, and deposition dynamics of glacial sediments
192 in numerous glaciated or formerly glaciated regions of the world.

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2 Methods

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2.1 Model setup

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IGM is a thermo-mechanical 3D glacier evolution model enhanced with physics-informed deep learning
200 using a convolutional neural network emulator (Jouvet & Cordonnier, 2023) of the high-order
'Blatter-Pattyn' ice-flow solver (Blatter, 1995). In this study, we build on the results of Leger et al. (2025)
202 and use the exact same IGM model version (2.2.1), spatial resolution (300 m), input parameters, and
forcings as used for their ensemble's (n=100) best-scoring simulation, i.e. simulation 37 (see Figs. 1, 6 in
204 Leger et al., 2025). We also run our simulations using the same GPU (Nvidia RTX 4090). In Leger et al.
(2025), a perturbed-parameter ensemble of 100 simulations was performed, covering 35-18 ka at 300 m
206 spatial resolution across the European Alps, an order-of-magnitude improvement over previous 1-2 km
models (Seguinot et al., 2018; Jouvet et al., 2023). Their model setup (and thus also ours) integrates
208 modules for ice-enthalpy (after Aschwanden et al., 2012), surface mass balance (after Calov & Greve,
2005), isostatic adjustment (after Wickert, 2015), and avalanching. The climate forcing was produced by
210 Russo et al. (2024) (also used by Jouvet et al., 2023), who conducted regional downscaling over Europe
(2 km resolution) of global Earth-system model outputs using the Weather Research and Forecasting
212 model, providing gridded fields of temperature and precipitation for both the LGM (24 ka) and the pre-
industrial era (1850 AD). A glacial index scheme generates continuous climate forcing interpolating these
214 two states using independent local proxy climate data that combines pollen and speleothem records (Fig.
2e in Leger et al., 2025; Luetscher et al., 2015; Duprat-Oualid et al., 2017). Basal sliding is parameterized
216 following a nonlinear Weertman friction condition (e.g. Schoof & Hewitt, 2013) with a sliding coefficient
also influenced by enthalpy-driven basal meltwater content and elevation-dependent basal materials'
218 strength, following Bueler & van Pelt (2015) and the Mohr-Coulomb law (Cuffey & Paterson, 2010). For
the bed topography, as in Leger et al. (2025)'s simulation 37, we use the digital elevation model from Mey
220 et al. (2016) which includes the removal of (1) present-day glacier thicknesses and lake depths, and (2)
reconstructed present-day valley-fill sediment thicknesses in main overdeepenings throughout the Alps.
222 More detailed methods and model descriptions are presented in Leger et al. (2025).



224 Here, we employ this model setup to run two new simulations featuring the additional coupling of 3D
Lagrangian particle tracking. The first simulation is parameterised for subglacial particle seeding whilst
226 the second for supraglacial particle seeding (Fig. 1). We run all simulations between 40 and 18 ka, thus
starting 5 kyr earlier than the original setup. While Leger et al. (2025) showed that starting the simulation
228 before 35 ka had no noticeable impact on the modelled AIF geometry during the LGM (~24.8 ka in their
simulations), preliminary tests showed that it does affect the diversity of modelled particle trajectories
230 (more details in Results section).

232 2.2 Particle seeding schemes

234 For each model time step (every 0.01-0.04 yr) and domain cell ($n = 6,030,036$), we implement a set of
conditions to determine whether to ‘seed’ (i.e. create) a new particle or not. We exclusively focus on
236 estimating glacial sediment trajectories and transport statistics, and do not address the volumes of glacial
sediments, erosion, or deposits. Therefore, seeding of a new particle can be interpreted as the creation of
238 a new glacial ‘sediment entity’ within the glacier system, possibly ranging in size from grains to large
boulders. Note that throughout this paper, we use the terms ‘glacial sediment’ and ‘glacial transport’ to
240 describe all sediments that are transported by glacier ice, thus combining supraglacial, englacial, and
subglacial debris/transport. Below, we describe the set of conditions required for both subglacial seeding
242 and supraglacial seeding to occur in our model (Fig. 2).

244 The frequency and spatial distribution of subglacial seeding is here set to be a function of basal ice velocity,
as frequently observed (Humphrey & Raymond, 1994; Herman et al., 2015; Cook et al., 2020; Herman et
246 al., 2021). Here, we use the subglacial erosion law obtained by Koppes et al. (2015) from results on
sediment export volumes from several outlet glaciers of the Patagonian and Antarctic Peninsula icefields.
248 This non-linear erosion law assumes the erosion rate \dot{e} is proportional to the sliding velocity u_s raised
to a power, using an erodibility constant $K_g = 5.2 \times 10^{-11}$ and a sliding velocity exponent of $l = 2.34$:

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$$\dot{e} = K_g |u_s|^l \quad 1)$$

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We follow Seguinot & Delaney (2021) and assume glacier systems studied by Koppes et al. (2015) likely
254 yield similar dynamics to former outlet glaciers of the AIF during the LGM. Using this law, our model
computes an erosion rate and cumulative erosion over time for each grid cell (Fig. 2). Computed erosion
256 is not used to modify the bed topography dynamically but rather only as a quantitative proxy for particle
seeding. Once this artificial cumulative erosion reaches a certain threshold (here set to 4 cm), seeding
258 occurs and the erosion value is reset to 0, thus adding a new particle to the system (Fig. 2). This value (4
cm) is arbitrary and represents a parameter to control the total number of advected particles. To add
260 stochasticity to the modelled creation and freeze-on of subglacial sediment, seeding further requires



meeting a condition of time delay since last seeding occurred. This time delay is set to randomly vary
262 between 10 and 60 yrs during the simulation following a uniform probability distribution (Fig. 2). Thus,
even though erosion is positively correlated to basal ice velocity, some randomness is here introduced in
264 whether seeding will occur shortly or with some delay after the cumulative erosion threshold is reached.
Note that with this scheme, we do not model the glaciofluvial transport of subglacially eroded materials,
266 as our model setup is not yet coupled to a subglacial hydrological-routing module. Instead, we exclusively
focus on subglacially eroded materials which freeze on and are subsequently advected by glacier ice (Alley
268 et al., 1998). The limitations of this assumption are further mentioned in the Discussion section.

270 For supraglacial seeding, our scheme was conceived to simulate mechanisms generating supraglacial
debris on glaciers, i.e. gravitational mass wasting events including rockfall, rock avalanches, debris flow,
272 avalanches, or landslides (Benn et al., 2012). We assume these events require both no (or little) ice cover
and steep slopes to occur. We define all slopes steeper than 45° as susceptible to mass wasting (Fig. 2),
274 following recommendations from Fischer et al. (2012). However, our 300 m model resolution still smooths
high-elevation peaks and steep slopes resulting in fewer locations $>45^\circ$ steep than in reality. To avoid this
276 bias, we use a higher-resolution digital elevation model (30 m resolution; Tadono et al., 2014) to produce
a mask of pixels meeting a $>45^\circ$ slope condition. We consider all modelled ice that is <20 m thick and
278 located in pixels meeting the high-resolution $>45^\circ$ slope mask to be an artifact of our 300 m resolution,
thus representing regions that would have no (or negligible) ice cover in reality. As a result, in our setup,
280 a given grid cell needs to both satisfy the $>45^\circ$ slope condition (in the high-resolution mask) and display
modelled ice thickness <20 m, for supraglacial seeding to occur (Fig. 2).

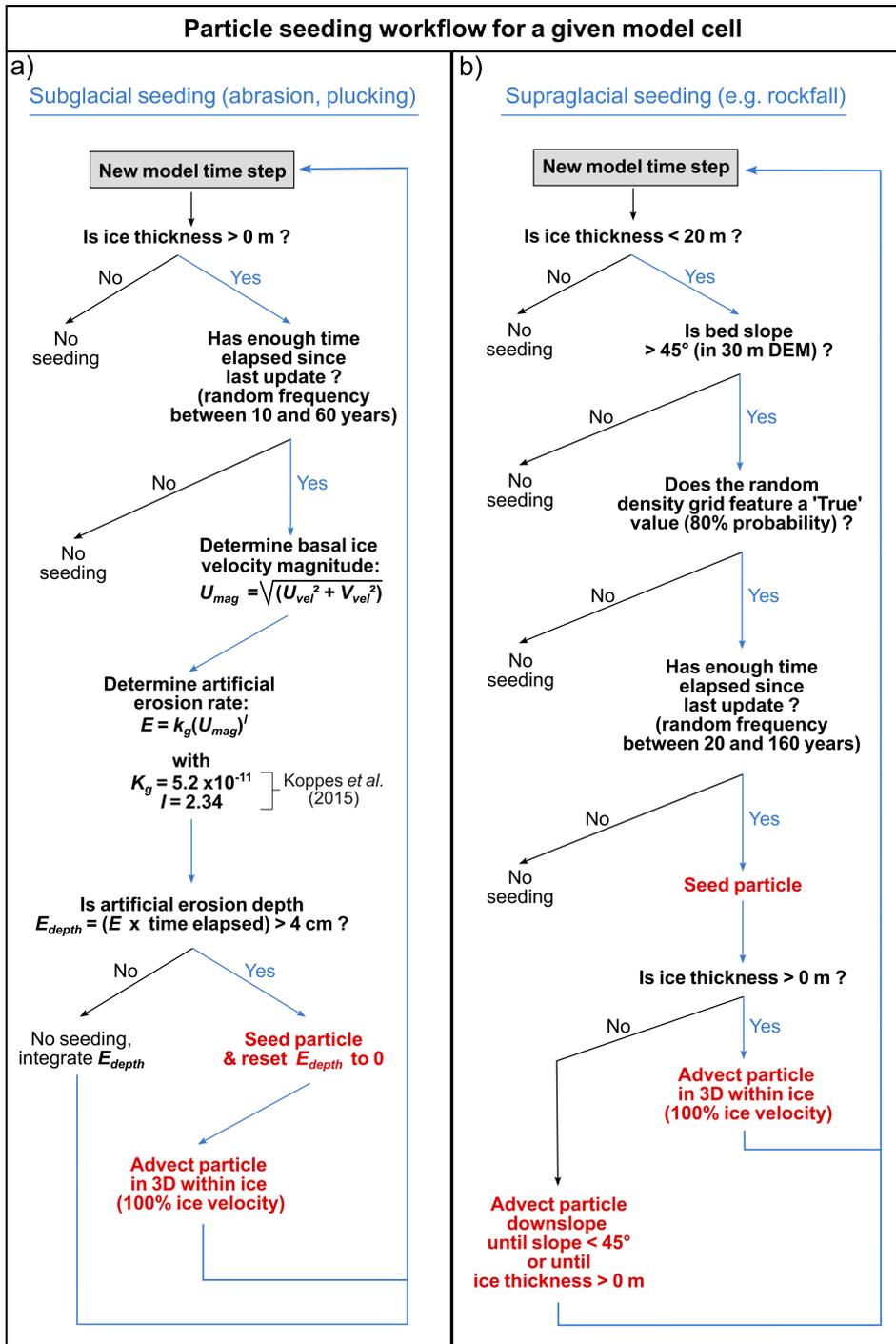
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As with subglacial seeding (see above), we introduce stochasticity in supraglacial debris production.
284 Firstly, supraglacial seeding only occurs when meeting a Boolean mask condition (True/False array)
randomly shuffled for all domain cells (at every time step) with a True-value likelihood of 80%. Following
286 this, seeding also only occurs when meeting a time delay set to randomly vary between 20 and 160 yrs
during the simulation (Fig. 2). All random sampling follows a uniform probability distribution. These
288 additional conditions separately add temporal and spatial randomness to supraglacial seeding, thus
applying a probabilistic algorithm; common in mass-wasting event modelling (e.g. Champel et al., 2002).
290 Therefore, while gravitational mass wasting events are highly likely where/when the model features steep
slopes ($>45^\circ$) and a lack of ice cover, they are not necessarily going to occur at every time step and always
292 in the same locations (Fig. 2). Once seeded, particles are advected downslope following the steepest
descent until slope angle $<45^\circ$, or until reaching cells with modelled ice, in which case ice advection will
294 take over (Fig. 2).

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338 **Figure 2.** Decision chart indicating the model workflow specific to our particle seeding schemes for a given
 340 model cell ($n = 6,030,036$), and for the two cases of (a) subglacial seeding (abrasion, plucking) and (b)
 342 supraglacial seeding (e.g. rockfall, rock avalanche, debris flow, landslides, etc.). This chart summarizes the
 set of conditions and parameters applied to every model cell and at every model timestep (every 0.01-0.04 yr)
 during the simulation in order to seed, or not seed, a new particle within the model system.



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2.3 Particle Lagrangian advection scheme

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To track the movement of particles in 3D within the evolving glacier geometry, we use a Lagrangian advection scheme which computes the space-time trajectory of particles created from seeding and resolves the precise 3D positions of particles at sub-grid resolution. At each model timestep, IGM computes the 3D ice-flow based on a high-order stress-balance model referred to as the ‘Blatter-Pattyn’ model (Blatter, 1995) and thus outputs a 3D velocity field. Each particle’s horizontal (x, y) and vertical (z) positions are thus updated according to ice velocity components u, v, w , respectively, integrated over a model timestep, Δt , using an explicit Euler scheme.

$$354 \quad x^{n+1} = x^n + \Delta t \cdot \bar{u}, \quad 2)$$

$$y^{n+1} = y^n + \Delta t \cdot \bar{v},$$

$$356 \quad z^{n+1} = z^n + \Delta t \cdot \bar{w},$$

358 where $\bar{u}, \bar{v}, \bar{w}$ represent the bilinearly interpolated horizontal and vertical velocities, respectively, at a particle’s current location (x^n, y^n). We ensure no particles artificially leave the ice column due to numerical integration errors or transient velocity fluctuations by clipping their relative (normalized) vertical positions to between 0 (bed) and 1 (ice surface). The bilinear interpolation for a scalar field f at a sub-grid location (x, y) is computed using:

$$364 \quad \bar{f}(x, y) = \sum_{i,j} f_{i,j} \cdot (1 - |x - i|) \cdot (1 - |y - j|) \quad 3)$$

366 where the summation runs over the four grid nodes surrounding the particle’s horizontal position, and the weights $(1 - |x - i|)$ and $(1 - |y - j|)$ ensure a smooth linear interpolation based on the distances to these nodes.

370 We assume all particles are advected at the velocity of the ice. The limitations of this assumption are assessed in the Discussion section below. When a particle reaches the modelled ice margin and is deposited, i.e. when ice thickness at its position becomes 0 m, it is prescribed the bed elevation. If local slope is $<45^\circ$ this particle will remain stagnant (Fig. 2). If the modelled glacier re-advances and local ice thickness is >0 m again, the particle gets re-entrained and 3D ice advection computations restart. We thus assume that all temporarily deposited sediments freeze-on and get re-entrained by a re-advancing ice margin. Although reality is more complex whereby former deposits can be overridden and survive younger glacier advances, the process of re-entrainment is here considered to dominate (Cogez et al., 2018). This assumption is supported by the general rarity, in formerly glaciated landscapes, of preserved older moraines inboard of younger and more extensive terminal moraines (Gibbons et al., 1984).



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Although particle positions are computed at every timestep (0.01-0.04 yr), they are saved every 10 model
382 years, which for our simulated timeframe (40-18 ka) generates 2200 data frames for each of the millions
of advected particles (20.5 million at maximum). The data saved for each particle include its x and y
384 coordinates, relative height in ice column, seeding year, and cumulative glacial transport time since
seeding. 10 years is the highest output frequency achieved while ensuring the particle database (~1.22 TB)
386 can be post-processed at a manageable computational cost. At that output temporal frequency, the post-
processing mapping of particle trajectories fully reflects the simulated ice-flow and particle advection in
388 most cases, except where modelled ice velocities are both high (e.g. $>1000 \text{ m yr}^{-1}$) and towards highly
sinuous glacier motion (e.g. around valley bends), where mapping particle positions every 10 years can
390 result in unrealistically straight trajectories. This will however only impact the mapped trajectory towards
the bend and not reduce the accuracy of its modelled provenance nor destination.

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2.4 Reconstructing glacial sediment trajectories

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After running the glacier-particle coupled IGM simulations, we use the output database of particle
396 coordinates to map the time-transient trajectories of certain particles. This is conducted within the frame
of two analyses. The first one, hereafter referred to as the ‘sink-to-source’ analysis, aims at reconstructing
398 the provenance and glacial transport pathways of specific LGM terminal ice-contact deposits. The second
analysis, called ‘source-to-sink’, addresses the opposite question. Its objective is to estimate the possible
400 transport pathways and deposition locations of glacial sediments eroded from a pre-determined source.

402 The sink-to-source analysis consists in finding all particles that end up within the area of a mapped deposit
at the end of the simulation (18 ka), after final glacier retreat, and trace back their glacial transport
404 trajectories. Although this can be achieved for any user-defined polygon, we focus on ice-contact deposits
located towards the terminal margins of main AIF outlet glaciers during the LGM (e.g. LGM moraines).
406 To follow a consistent methodology across the Alps, we map a series of 49 polygons (Fig. 3a) covering
the area between our most extensive time-independent modelled ice margin and the empirical LGM outline
408 of the AIF originally produced by Ehlers et al. (2011) and improved by several studies since (Gianotti et
al., 2008; 2015; Ravazzi et al., 2012; Monegato et al., 2017; Federici et al., 2017; Ivy-Ochs et al., 2018;
410 Braakhekke et al., 2020; Kamleitner et al., 2022; 2023; Ribolini et al., 2022). Tracing polygons over that
area between ensures to isolate all particles deposited at the LGM margins even where model-data fit in
412 ice extent is not perfect, which is still the case despite improvements relative to former AIF-wide LGM
models (Seguinot et al., 2018; Jouvét et al., 2023; see Fig. 4a in Leger et al., 2025).

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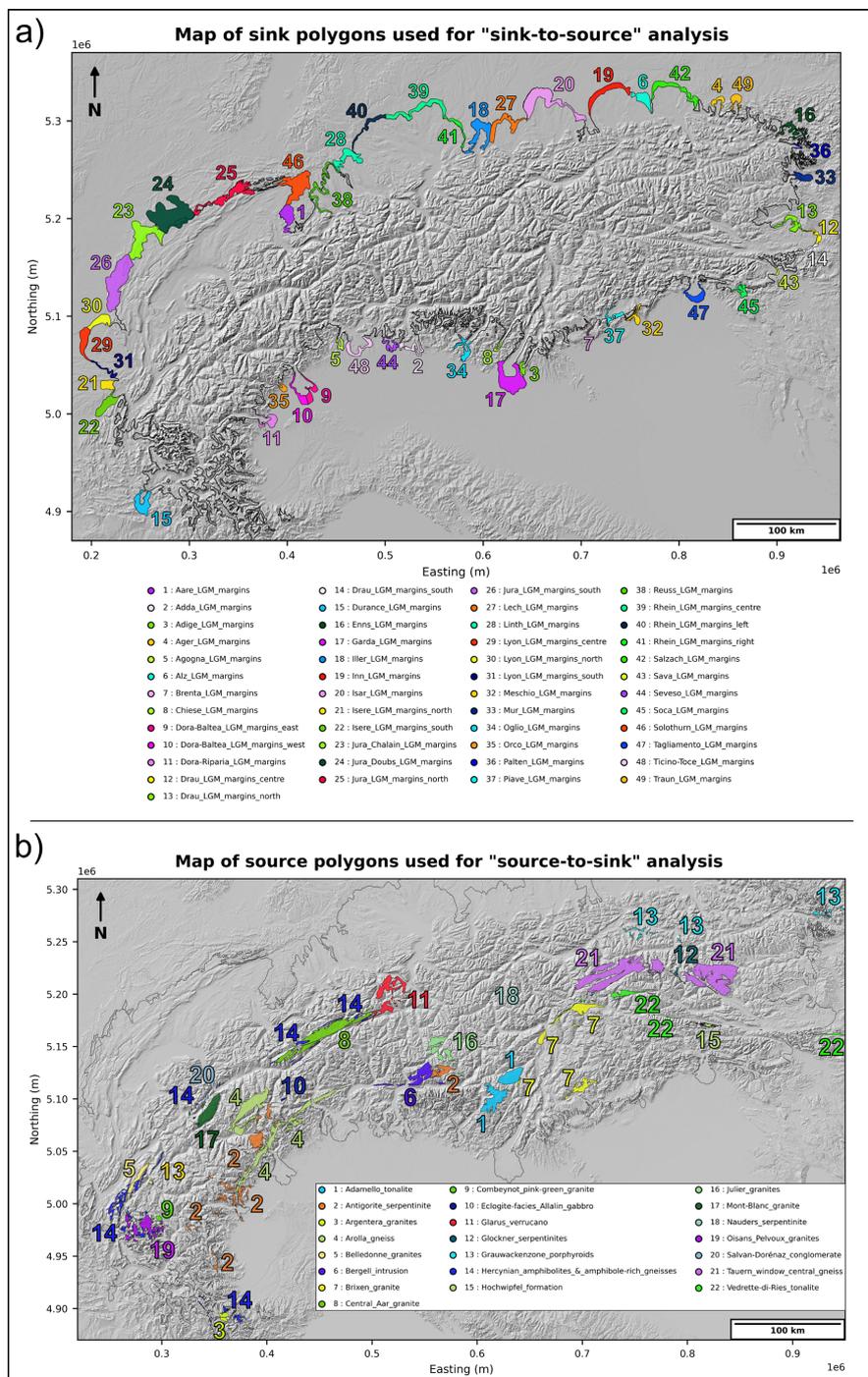


Figure 3. Maps of all sink and source polygons used for producing both catalogues of (a) sink-to-source and (b) source-to-sink analyses and their resulting particle trajectories. Sink polygons (a; n = 49) were selected and mapped to represent terminal ice-contact deposits for all major outlet glaciers of the Alpine Ice Field (AIF) during the Last Glacial Maximum (LGM), while source polygons (b; n = 22) were selected and mapped from geological data on surface outcrops for key lithologies across the Alps (more details in section 2.4). In this and all subsequent paper figures displaying geo-spatial data, X and Y coordinates are displayed as projected (unit: m) in the WGS 84 / UTM zone 32N (EPSG:32632) coordinate reference system.



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Importantly, our 49 sink polygons (Fig. 3a) are not a precise map of terminal LGM ice-contact deposits preserved in the Alps. However, they are useful to produce a first-order estimation of possible LGM glacial trajectories for deposits located towards major outlet glacier margins, pre-erosion. Producing an Alps-wide, digital and open-access map of all preserved terminal ice-contact deposits dating to the LGM (e.g. Clark et al., 2018; Davies et al., 2020) has yet to be achieved in the Alps and is beyond the scope of this study. To estimate the relative contributions of various provenances to the total particle number found in a sink deposit, we divide our Alps-wide domain in 241 present-day hydrological catchments; obtained from the global HydroBASINS database (Lehner & Grill, 2013), and named based on catchment-specific river names (Figure S1). Our sink-to-source analysis produces a catalogue of modelled particle trajectories, estimated provenance fractions per basin, and statistics including glacial transport time and particle age (i.e. seeding year), for all particles found in each of the 49 sink polygons shown in Figure 3a. All results are produced separately for subglacial and supraglacial particle seeding, enabling us to compare the impacts of different sourcing mechanisms on glacial sediment transport histories and provenances.

470

For the source-to-sink analysis, we select sources that represent mapped outcrops of specific alpine surface lithologies, to estimate the glacial transport pathways of sediments from specific rock types between 40 and 18 ka, across the Alps. We focus on rock type as this enables us to compare modelled estimates against empirical data on ice-contact deposits (e.g. erratic boulders) of known lithologies and locations post-retreat (e.g. Braakhekke et al., 2020; Monegato et al., 2022). This requires identifying surface lithologies specific enough to be associated with mapped outcrops and uniquely recognisable through geological assessment of ice-contact deposits. The outcrops moreover need to cover a large-enough area for enough particle seeding to overlap them, given that a single grid cell is 90,000 m². To identify such lithologies, we use the open-access 1:500,000-scale geological map sheets 1 and 2 from the ‘Structural model of Italy’ (Bigi et al., 1990a; b). These maps present a relatively high spatial resolution, are easily accessible online and georeference-able, and provide a consistent naming convention of lithologies across the entire Alps. We also use geodata derived from the Geological Map of Austria 1:50.000 sheets 197 Kötschach and 198 Weißbriach for one extra lithology (i.e. the Hochwipfel formation) (Geologische Bundesanstalt Österreich, 2021a, b). We then isolate a subset of 22 surface lithologies referred to as our ‘source polygons’ (Fig. 3b). While these are not a comprehensive list satisfying the above criteria, they are spatially widespread and cover the main rock types described by investigations on LGM erratic boulders in the Alps. They include Mont-Blanc granite (Bussien Grosjean et al., 2018), Glarus Verrucano (Letsch et al., 2015), or Salvan-Dorénaz conglomerate (Capuzzo et al., 2003), for instance (Fig. 3b).

490 The source-to-sink analysis consists in finding all particles seeded within our 22 source polygons during the AIF simulations, and in mapping their glacial transport pathways. Due to existing mechanisms of sediment melt-out and lodgement at the ice-bed interface (Alley et al., 1997), we consider any location



along the resulting trajectories to be a possible destination for glacial sediment of the studied lithology.
494 Thus, the source-to-sink analysis produces a catalogue of maps displaying modelled trajectories of
particles seeded within each of the 22 selected surface lithologies shown in Figure 3b. The maps are
496 produced for both subglacial and supraglacial particle seeding allowing for a direct comparison between
the two.

498

Consequently, the main outputs of this study are the ‘sink-to-source’ and ‘source-to-sink’ analyses, i.e.
500 two catalogues of model results shared under the form of maps displaying source and sink particle
trajectories, pie charts of deposit provenance fractions, histograms showing data from sink particles, and
502 polyline shapefile data for visualization in GIS softwares. These data are all accessible from the Zenodo
repository attached to this paper (link: <https://doi.org/10.5281/zenodo.18374156>).

504

506 **3 Results**

508 **3.1 GPUs reduce the computational cost of particle tracking**

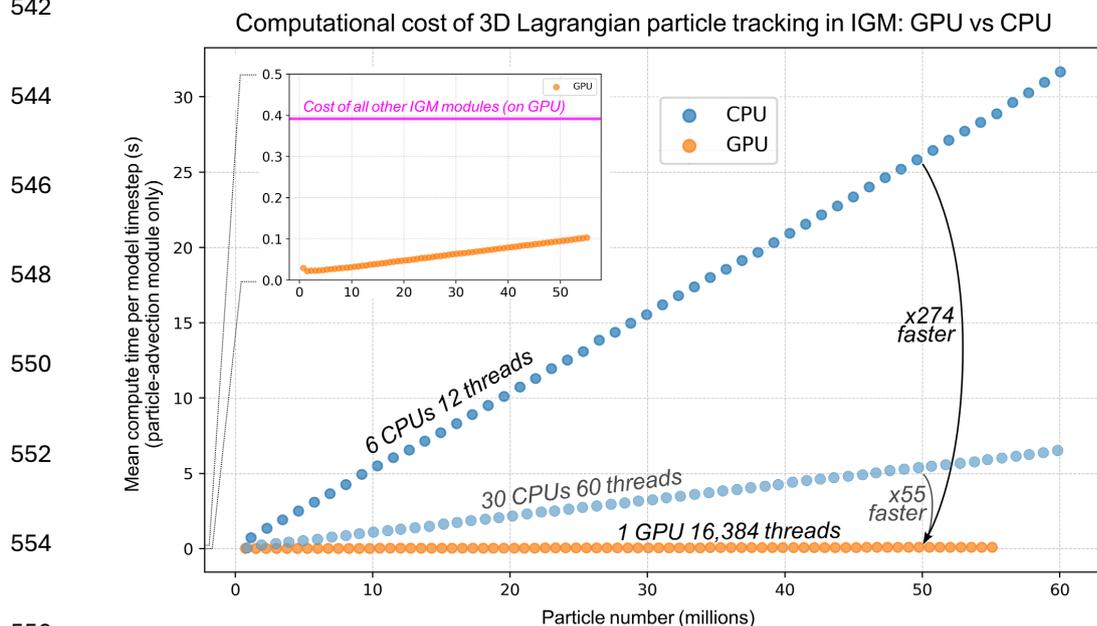
510 GPUs are particularly well-suited for particle-based numerical modelling, such as Lagrangian particle
tracking, due to their architecture optimized for massively parallel execution of small, independent
512 computations, ideal for processing individual particles concurrently. This contrasts with traditional
computing on Central Processing Units (CPU) which restricts the parallelization of such small operations
514 on much fewer cores. Consequently, GPU-accelerated algorithms for particle-based modelling have been
extensively developed in fields as varied as fluid mechanics, graphics, or geosciences (e.g. Wang et al.,
516 2022; Aaron, 2023). In our specific application, we find that transferring all computation on the GPU
makes 3D Lagrangian particle advection highly efficient, with a computational cost that remains small
518 even when tracking tens of millions of particles within a modelled glacier (Fig. 4).

520 To quantify this gain, we ran a test simulation over the majority of the European Alps and, after initializing
an LGM Alpine Ice Field (AIF), seeded new particles in all grid cells of the glacier accumulation area
522 every two model years, thus quickly multiplying the total particle number. When operating on a single
GPU (Nvidia RTX 4090), raising the number of particles from 0 to 50 million increases the mean cost of
524 computing their advection linearly between 0.02 and 0.1 seconds per timestep (Fig. 4). Even with 50
million particles in the system, the computational cost of particle tracking remains below 26% of the mean
526 cost (i.e. ~0.39 seconds per timestep) of all other IGM processes and modules in our Alps-wide simulation
of the LGM at 300 m resolution. When running the same test using multiple CPUs instead, the mean costs
528 of tracking 50 million particles reach approximately 26 and 5.5 seconds per timestep using 12 and 60 CPU
threads, respectively (Fig. 4). These computational costs are between 274 and 55 times greater than those



530 obtained with a single GPU, respectively. For 10 million advected particles, the costs are still 200 and 42
532 times greater than with the GPU, respectively. This shows that when using any traditional CPU-based
534 glacier evolution model, coupling Lagrangian tracking of large particle numbers ($>10^7$) would
536 substantially increase the simulation's computational cost. The alternative of accurately computing
538 particle trajectories using post-processing only (after simulations are run), although not computationally
540 restrictive, would be made impossible by the data volume of transient 3D velocity fields that would need
542 to be saved at every time step (0.01-0.04 yr), which in our case would quickly exceed the hundreds of
544 Terabytes. Contrastingly, when using IGM and a GPU-based approach, 3D particle tracking of large
546 particle numbers can be coupled to simulations with only a small additional cost relative to the ice-flow
548 model (Fig. 4). This enables us to run, for the first time, IGM simulations at high (300 m) spatial
550 resolutions with millions of particles tracked over Alps-wide and multi-millennial scales, an experiment
552 that would be unfeasible using traditional CPU-based computing.

542



558 **Figure 4. Mean computational time/cost (in seconds) of computing the Lagrangian 3D advection of particles**
560 **in ice during a single model timestep of our Alpine-Ice-Field simulations with the Instructed Glacier Model**
562 **(IGM), as a function of particle number. The data shown here allows one to compare the computational**
564 **cost of Lagrangian particle tracking on a single GPU (orange dots; Nvidia RTX 4090) relative to computing it on**
566 **multiple CPU cores (blue dots; Intel(R) Xeon(R) CPU E5-2620 v3). The difference between blue and orange**
568 **dotted lines highlights the significant computational gain of parallelizing particle advection operations on the**
570 **GPU. The intermediate line of blue dots (30 CPUs, 60 threads) is shown with slight transparency as numbers**
were calculated assuming linear proportionality to the real computational costs obtained with a 6 CPU (12
threads) setup. The inset graph changes the Y scale and zooms inside compute time values <0.5 seconds,
allowing one to visualize the linear increase in cost with increasing numbers of advected particles when using
the single GPU (otherwise invisible). The inset also compares this particle-module cost against the average
computational cost (~ 0.39 s; pink line) of a single model timestep when combining all other GPU-based IGM
modules used when running the Alps-wide 300 m best-fit simulation of Leger et al. (2025): i.e. the same
simulation we re-run in this study.



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3.2 Alps-wide patterns of glacial sediment sourcing

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Our coupled glacier-particle simulations output a database of 3D particle coordinates and other statistics from the moment of seeding until the end of the glacier simulation (i.e. 18 ka). Thus, for both simulations with subglacial and supraglacial particle seeding, a map of seeding locations for each of the ~20.5 million advected particles can be produced. To visualize the spatial heterogeneity of particle seeding, we transform the seeding location data into normalized seeding density maps (Fig. 5). In Figure 5, bright colours (normalized density closer to 1) show regions with relatively more particle seeding events during the simulations. For subglacial seeding, these regions are associated with high basal ice velocities modelled during extended periods of the simulation, spanning 40-18 ka. These can be interpreted as likely to produce the largest volumes of glacial sediments of subglacial origin (e.g. abrasion and plucking) during the LGM. Potent subglacial sediment sourcing regions include the Rhône valley between Montreux and Sion (Switzerland), the Dora Baltea valley between Aosta and Ivrea (Italy), the Romanche valley between Le Bourg-d'Oisans and Grenoble (France), or the Rhein valley between Domat/Ems (Switzerland) and Bregenz (Austria), for instance (Fig. 5a).

588

For supraglacial seeding, regions of high seeding densities are those presenting steep topographies ($>45^\circ$) and ice-free conditions (or thin ice covers: <20 m) during extended time-periods of the simulation. These regions also need to be near dynamic modelled glaciers for seeded particles to eventually get transported by glacier ice. These regions are interpreted as likely to have produced the largest volumes of supraglacial sediments (e.g. from rockfall, debris flow, landslides, avalanches) during the LGM. Our results suggest that high supraglacial sediment sourcing regions are widespread (Fig. 5b) but include, for instance, the Écrins Massif (France), the Lepontine Alps (Switzerland), the Dolomiti Bellunesi Massif (Italy), the Triglav Massif (Slovenia), or the Bernese Alps (Switzerland). During the LGM, these regions are most concentrated within a narrow band located towards the northern and southern peripheries of the alpine arc, where high topographies (> 2500 m a.s.l.) combined with thin/no ice cover maximize the likelihood of nunatak occurrence (Fig. 5b). Contrastingly, supraglacial sediment sourcing is lower further towards the Alps' interior, where the model produces greater ice thicknesses and topographic ice covers for extended periods, thus reducing nunatak occurrence.

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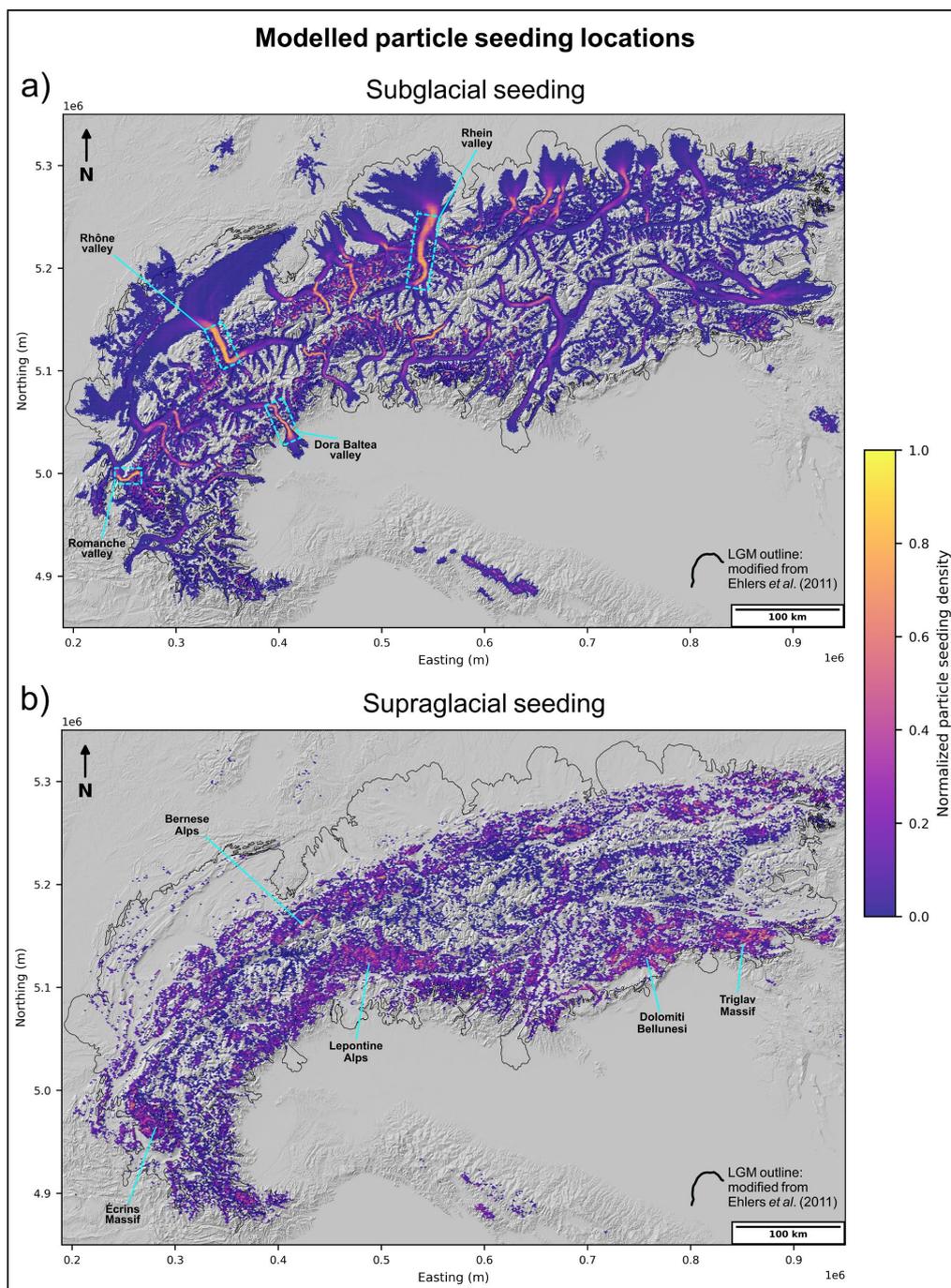
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642 **Figure 5. Maps showing the seeding locations of all modelled particles (~20.5 million at maximum) in both**
644 **simulations with (a) subglacial and (b) supraglacial particle seeding. The maps are divided into small**
646 **hexagons in which the total number of seeded particles is computed. Hexagons are colored based on this total**
648 **number normalized across the entire dataset, resulting in a density map of particle seeding locations, with**
brighter yellow colors indicating relatively more seeding, and darker purple colors indicating relatively less
seeding. A lack of colors (grey hillshade background) indicates no particle seeding occurred at any time
during simulations.



650 3.3 The sink-to-source analysis and catalogue

652 With the sink-to-source analysis, we produce a catalogue of modelled time-transient trajectories for
terminal LGM ice-contact deposits mapped across the Alps, hereafter referred to as our ‘sinks’ (see section
654 2.4). Sink-to-source trajectories reveal the modelled pathways of ice-advected particles ending up within
these sinks after final glacier retreat. For each sink polygon mapped ($n = 49$; Fig. 3a), we provide a high-
656 resolution map of particle trajectories, along with an estimation of particle provenance fractions. For each
sink and particle in this sink, we also produce statistics on total particle glacial transport distance,
658 cumulative glacial transport time, cumulative time in ice-free conditions during source-to-sink journey,
and seeding year (i.e. timing of erosion). These data are produced for both cases of subglacial and
660 supraglacial seeding, enabling us to quantify differences in glacial transport dynamics between the two.
We consider the sink-to-source catalogue to be a main result of this study and encourage readers to
662 download it from the Zenodo repository attached to this paper (link:
<https://doi.org/10.5281/zenodo.18374156>). All particle trajectory data for each seeding type and sink are
664 also available as polyline shapefiles for visualization in GIS software.

666 3.3.1 A sink-to-source case study: the Inn glacier LGM margins

668 As a case study, we here describe the results of our sink-to-source analysis for a single ice-contact deposit,
i.e. the Inn glacier LGM margins (sink 19; Fig. 6). We chose this outlet glacier as its modelled ice-flow
670 during the LGM originates from a large variety of catchments, produces numerous transfluences, has been
the subject of several studies (e.g. Reitner, 2007; van Husen, 1997), and produces a good ice-extent fit
672 during maximum expansion with empirical data (see Fig. 1a in Leger et al., 2025). In our subglacial and
supraglacial seeding simulations, totals of 53,797 and 36,945 particles end up within this ice-contact
674 deposit, respectively (Fig. 6). The sink particles originate from 15 (for subglacial seeding) and 12 (for
supraglacial seeding) different hydrological basins. Our modelling suggests the basin contributing the
676 most ice-contact sediments of subglacial origin is the Inn-Simsee basin (basin 44; Figure S1), with an
estimated provenance fraction of 42.5% (Fig. 6). For supraglacial seeding, the distribution of provenance
678 fractions is different. The basin estimated to provide the most sediments of supraglacial origin is the Ziller
basin (basin 191; Figure S1), although its provenance fraction (32%) is tied with the Alz-Traun basin
680 (basin 63, 29.5%). On average, our modelling suggests that ice-contact deposits of the LGM Inn glacier
margins spent $3,021 \pm 4,114$ yrs (median \pm interquartile range) in glacier ice for those of subglacial origin.
682 This median number is approximately twice greater for ice-contact deposits of supraglacial origin, with a
cumulative glacial transport time of $6,361 \pm 3,641$ yrs (see section 3.3.2 for why). At maximum, particles
684 are modelled to spend up to 12,644 and 14,613 yrs in ice for subglacial and supraglacial seeding,
respectively (Fig. 6e, f). Particles yielding such high glacial transport times are few (<300) and frequency



686 distributions tail off, which indicates that starting our simulations at least 15 kyr before the local LGM
688 (~24.8 ka) is both important and adequate (Fig. 6e, f). On average, ice-contact deposits of the Inn LGM
690 margins are modelled to have travelled over 78 ± 80 and 138 ± 81 km for sediments of subglacial and
692 supraglacial origin, respectively. Ice-contact deposits of subglacial origin are estimated to have spent, on
694 average, a total of 353 ± 1936 yrs in ice-free conditions during their source-to-sink journey. This time in
696 ice-free conditions occurs when particles are deposited following temporary ice retreat, prior to re-
entrainment by subsequent advances (see videos in supplement). This median number increases fivefold
to 1885 ± 3719 yrs for sediments of supraglacial origin, suggesting a greater potential for atmospheric
exposure during their transport (assuming they remain at the Earth's surface). In line with these
estimations, the results suggest that ice-contact deposits of the Inn LGM margins and of supraglacial origin
are on average eroded 5090 yrs earlier than those of subglacial origin (Fig. 6).

698 For these Inn glacier LGM margin deposits, the modelled trajectories of subglacially-seeded sediments
display similar pathways than those of supraglacial origin. However, we find that glacial sediments of
700 supraglacial origin, due to reaching glacier surfaces from nunataks and valley/glacier sides, are more likely
to produce trajectories resembling well-defined medial moraines (e.g. Fig. 6b, basins 170, 150). We find
702 this is rarely the case for modelled trajectories of subglacially-seeded particles, which can originate from
across the glacier bed, including from valley/glacier centres where basal velocities are highest. This
704 difference also explains why subglacially seeded particles spread over the entire terminal perimeter of the
Inn glacier's piedmont lobe during the LGM. However, particles of supraglacial origin rarely reach the
706 glacier's centreline and are pushed sideways by flow divergence within the piedmont lobe, causing
preferential advection to both the left and right lateral margins of the terminal lobe, but not to its centre
708 (Fig. 6). We observe a similar trajectory differentiation between ice-contact deposits of subglacial versus
supraglacial origin for the Garda (sink 17) and the Ticino-Toce (sink 48) outlet glaciers, towards their
710 modelled piedmont lobes (see 'sink-to-source' catalogue). This mechanism has important implications for
sampling frontal moraines for detrital thermochronology and linking sampling locations to catchment
712 provenances (e.g. Bernard et al., 2020).

714 These results focus on a single LGM ice-contact deposit, or 'sink', as an example. The same data were
obtained for all 49 mapped sinks (Fig. 3a) and can be viewed via the sink-to-source analysis catalogue
716 (link: <https://doi.org/10.5281/zenodo.18374156>).

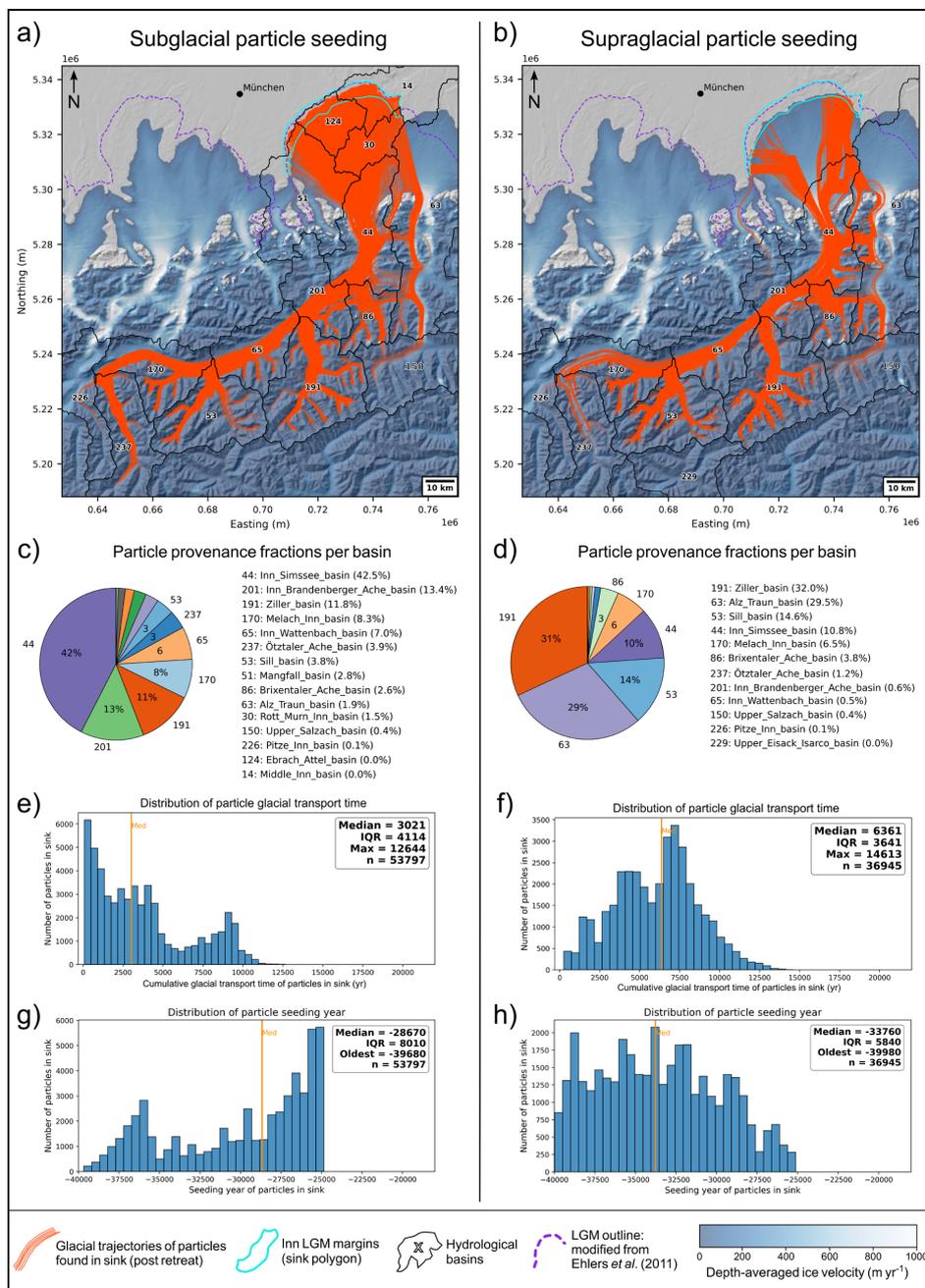
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Figure 6. Sink-to-source analysis and resulting modelled particle trajectories (a, b) and transport statistics (c-h) for subglacially (a, c, e, g) and supraglacially (b, d, f, h) seeded particles ending up in the chosen sink (cyan polygon) following final glacier retreat. Here, results are shown for a single example sink (or ice-contact deposit) from our sink-to-source catalogue (n=49 sinks in total), i.e. the Inn glacier LGM margins (sink 19: see Fig. 3a for location). The pie charts (c, d) and associated legends indicate the provenance fractions of all particles ending up in this sink for each hydrological basin (mapped and numbered in black on panels a, b) in which they were seeded (see Figure S1). Histograms (e-h) display the resulting distributions of sink particle cumulative glacial transport times and seeding years (i.e. particle age). ‘IQR’ stands for ‘Interquartile Range’: i.e. the spread of middle 50% of the dataset: 75th – 25th percentiles.



762

3.3.2 *Ice-contact deposits of subglacial versus supraglacial origin*

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As described above for Inn glacier LGM deposits, we find notable differences in glacial transport histories and characteristics between ice-contact deposits of subglacial versus supraglacial origin. Similar differences hold true when analysing all 49 sinks and the 3.1 million particles deposited within them (Fig. 7). For the majority of these sinks (41 out of 49), cumulative glacial transport time is on average greater for particles of supraglacial origin. When averaging over all sinks, the particle glacial transport time is higher by approximately 1925 years, i.e. a factor of 1.9 increase. The total ice-free time (pre-deposition) of sink particles during their source-to-sink journey is also higher for those of supraglacial origin in 41 out of 49 cases, and on average by 1519 yrs, a factor of ~ 2.74 increase (Fig. 7). We find a similar pattern for the age (i.e. the seeding year) of sink particles, which is older (on average by 4640 yrs) for those of supraglacial origin in 46 out of 49 cases. Thus, our modelling suggests that in the Alps, LGM terminal ice-contact deposits of supraglacial origin were likely to be eroded earlier in time, spend more time in or on glacier ice, and spend more time exposed in ice-free conditions during their full source-to-sink journey (Fig. 7). This is likely caused by glacial sediment of supraglacial origin reaching the glacier surface mainly in accumulation areas, where steep topographies protrude, and where ice velocities are lower.

Unlike subglacially-eroded materials which are preferentially produced in fast-flowing areas often located closer to terminal deposits, supraglacial debris requires (on average) more time to be advected to lower glacier elevations and areas of faster-flowing ice and, in turn, to the terminus. Moreover, glacial sediments of supraglacial origin tend to reach contact with ice towards slope-adjacent glacier sides, making them likely to remain near lateral ice margins during glacial transport. This increases their chances of deposition during temporary periods of ice retreat and thinning, which can increase their cumulative ice-free time during their source-to-sink journey. In contrast, subglacially-eroded sediments will preferentially be concentrated towards the faster-flowing centreline of glaciers, further away from lateral glacier margins. These results have implications for terrestrial cosmogenic nuclide exposure dating of moraine sediments deposited by alpine glaciers and other topographically constrained icefields (Heyman et al., 2011). Indeed, they imply that ice-contact deposits of supraglacial origin are more likely to yield cosmogenic nuclide inheritance signals relative to those of subglacial origin, not only because of pre-transport exposure, but also due to potentially longer and more complex glacial transport histories. However, one must note that clast erosion during glacial transport can counterbalance this mechanism and instead remove nuclide inheritance signals (Matthews et al., 2017) (more details in Discussion).

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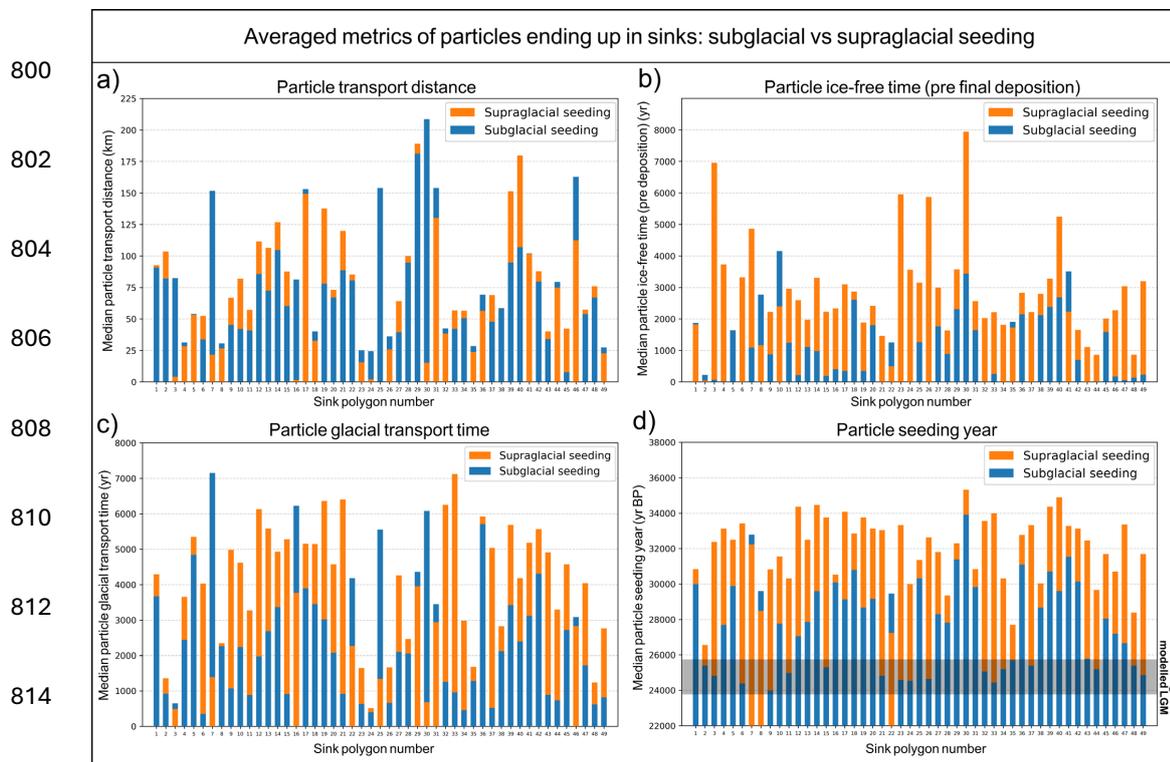


Figure 7. Overlapping bar plots (non-stacked) indicating particle statistics averaged over all sink particles (median) for each of the 49 sinks (or ice-contact deposits) in our catalogue (x axis), shown separately for both subglacial seeding (blue bars) and supraglacial seeding (orange bars). See Fig. 3a (or catalogue) to visualize the locations and names of these 49 sinks. The data are shown for four distinct particle metrics, i.e. the median sink particle transport distance (a), the median cumulative time a particle spent in ice-free conditions during its full source-to-sink journey (b), the median cumulative particle glacial transport time (c), and the median particle seeding year (i.e. the particle age) (d). For all metrics except transport distance, modelled sink particles of supraglacial origin tend to display higher median values (orange bars taller than blue bars), suggesting that, on average, they tend to be older (i.e. seeded earlier), spend more time in glacier ice, and spend more time in ice-free conditions during their source-to-sink journey, relative to sink particles of subglacial origin.

3.3.3 Addressing ‘sink-to-source’ debates: The Mont Salève erratics case study

To demonstrate that our modelled glacial sediment trajectories can help address tangible research questions and scientific debates in the Alps, we conduct a specific analysis for the example of the Mont Salève erratics. The Mont Salève, located 10 km to the south of Geneva, is a ~600 m tall, ~16 km long, and ~2.5 km wide limestone mountain part of the Jura Massif. The Salève features a flat plateau-like summit (~1300 m a.s.l.) displaying approximately 400 preserved erratic boulders (1200 pre-exploitation) officially protected since 1877 and subject to investigations since (e.g. Coutterand, 2010). Some of the erratics were geologically identified as Gneiss from the Siviez-Michabel nappe (Valais, Switzerland) while

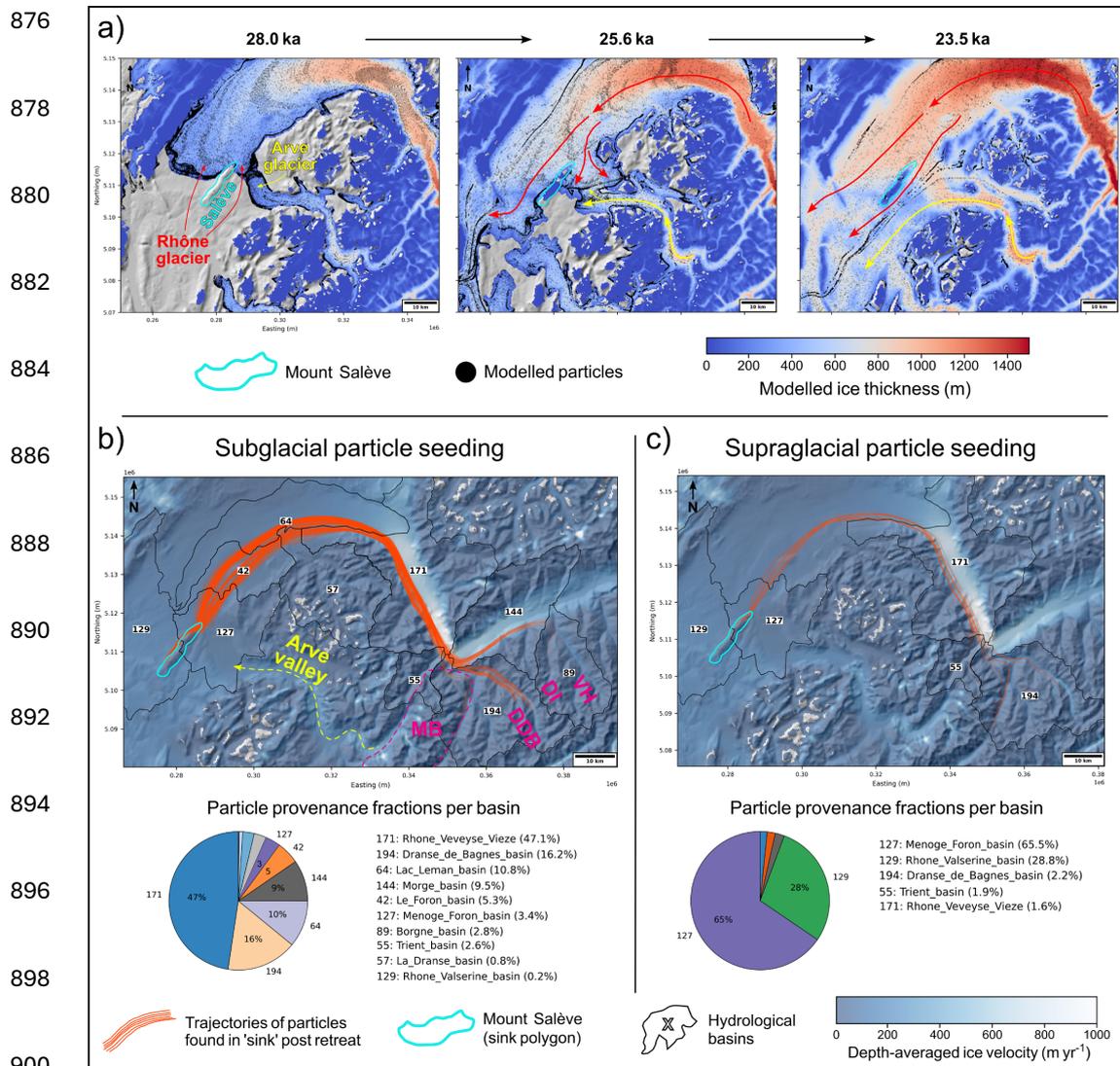


840 others as Mont-Blanc granite. They were hypothesised to have been deposited during retreat phases and
842 thinning from the largest Late-Pleistocene glaciations of the AIF. More specifically, Coutterand (2010)
844 attributed their glacial transport and deposition to two separate glacier systems; i) the Rhône glacier
846 flowing along the Rhône valley and Geneva Lake basin thus reaching the Salève from the northeast, and
848 ii) the Arve glacier flowing along the Arve valley and originating from the Mont-Blanc Massif thus
850 reaching the Salève from the southeast. Our study enables to compare these hypotheses against modelled
852 estimates for the first time. Firstly, our results suggest the Mont Salève summit was covered by a thin (~30
854 - 100 m) layer of ice during the LGM, when peak AIF extent and volume was reached (~24.8 ka; Leger et
856 al., 2025) (Fig. 8). When tracking the trajectories of all particles deposited on the Mont Salève following
deglaciation, we find that no particles are modelled to be deposited by the Arve glacier (Fig. 8). Instead,
between 40 and 18 ka, 100% of modelled ice-contact deposits on the Salève are deposited by the Rhône
glacier, with glacial sediment travelling exclusively along the western side of the Rhône valley and the
southern side of the Geneva Lake basin (Fig. 8). The seeding locations of particles deposited on the Salève
trace back to the northeastern sectors of the Mont-Blanc Massif, thus overlapping Mont-Blanc granite
outcrops, but also to the Dranse de Bagnes, Dixence, and Val-d'Hérens valleys (Vallais, Switzerland) thus
overlapping the Siviez-Michabel gneiss nappe (Bigi et al., 1990) (Fig. 8). Thus, in our simulations, the
geographical origin of both subglacially- and supraglacially seeded particles can explain the lithologies of
erratic boulders found on the Salève plateau (Fig. 8).

858 The lack of Salève-deposit trajectories associated with the Arve glacier is related to the modelled dynamics
of confluence between the Rhône and Arve glaciers. Our simulations suggest that during the last AIF
860 advance preceding the LGM (~28-26 ka), a branch of the more voluminous and thicker Rhône glacier
862 expanded southward from the Geneva Lake basin into the Arve valley and around the southeastern flanks
864 of the Salève. This modelled expansion generates enough driving stress to push the thinner Arve glacier,
forced to redirect its flow south-westward due to its lower ice discharge rate (Fig. 8). Consequently, our
866 simulations suggest the Mont Salève remained surrounded by ice exclusively from the Rhône glacier
868 during the LGM and until final deglaciation from the area (~20 ka in our simulations). More empirical
investigations and dating of the Salève erratics are needed to either validate or discard this new model-
derived hypothesis, which differs from the previous empirical hypothesis (Coutterand, 2010). Regardless,
this study case of the Mont Salève erratics is a prime example demonstrating how Alps-wide modelling
of glacial sediment transport can help address questions on past glacier flow dynamics and the former
transport history of certain ice-contact deposits.

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902 **Figure 8. Instructed Glacier Model (IGM) output, sink particle trajectory maps, and sink particle provenance**
 904 **fractions per hydrological basin, for the Mont Salève erratics case study (see section 3.3.3). The three ice-**
 906 **thickness model output snapshots (a) at 28, 25.6, and 23.5 ka display the modelled ice thickness fields in the**
 908 **region of the Mont Salève indicating how the Rhône and Arve glaciers interact in our model. More**
 910 **specifically, they show how, in our simulation, the Rhône glacier pushes the ice from the Arve glacier towards**
 912 **the southwest forcing it to redirect its flow: causing the Mont Salève to be surrounded by modelled ice**
 914 **exclusively from the Rhône glacier during the entire Last Glacial Maximum (LGM). This in turn explains**
 916 **the resulting particle glacial-transport trajectories (b, c), highlighted by orange lines, shown for particles**
ending up on and around the Mont Salève following final ice retreat. These suggest no ice-contact deposits of
the Mont Salève are modelled to be transported by the Arve glacier. They are instead all exclusively
transported by the Rhône glacier. Note particle seeded within Basin 129 (28% of particles for supraglacial
seeding) are only local to Mont Salève: i.e. particles from near the summit moved downslope and which still
end up within the mapped polygon following final ice retreat. On panel b; ‘MB’, ‘DDB’, ‘DI’, and ‘VH’ stand
for the ‘Mont-Blanc Massif’, and the ‘Dranse de Bagnes’, ‘Dixence’, and ‘Val-d’Hérens’ valleys, respectively,
enabling to locate places mentioned in main text (section 3.3.3).



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3.4 The source-to-sink analysis and catalogue

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With the source-to-sink analysis, we produce a second catalogue of time-transient (40-18 ka) glacial
922 sediment trajectories for a selection of key surface lithologies across the Alps, hereafter referred to as our
'sources' (see section 2.4) (link: <https://doi.org/10.5281/zenodo.18374156>). These trajectories reveal the
924 pathways of particles seeded either subglacially or supraglacially within source polygons ($n = 22$; Fig.
3b). For each source polygon and seeding type, we provide a high-resolution map of source particle
926 trajectories. We interpret these source-to-sink trajectories as model estimates of possible locations (along
the modelled trajectories) where sediments of a specific surface lithology may have been transported to
928 and deposited by ice between 40 and 18 ka. These locations can then be compared against the coordinates
of documented deposits (e.g. erratic boulders) of known lithology, which may help assess the accuracy of
930 our modelling.

932 3.4.1 A source-to-sink case study: the 'Arolla Gneiss' trajectories

934 As an example from our catalogue, we here describe our source-to-sink analysis for a single lithology, i.e.
Arolla Gneiss (source number 4 in the catalogue: Fig. 9). This lithology is part of the Austroalpine system
936 of the western Alps and, more specifically, of the Dent Blanche and Sesia Lanzo composite nappe-system
of Paleoafrican provenance (Manzotti, 2011). It was formed during the Early-Alpine and Lepontine
938 tectonometamorphic events and is mainly composed of greenschist orthogneisses from Late-Hercynian
granitoids (Bigi et al., 1990a). This lithology outcrops mainly within the Dent Blanche, Dent d'Hérens
940 and Weisshorn Massifs (Swiss Alps), and along a narrow band of the southern Italian Alps stretching for
~160 km from the Valle di Viù to the Melezza valley and Locarno (Ticino, Switzerland) (Fig. 9). Numerous
942 erratics deposited in the Swiss and Italian alpine forelands are of Arolla-Gneiss lithology (e.g. Graf et al.,
2015).

944

In our simulations, Arolla Gneiss is modelled to be eroded and transported by ice into vastly different
946 valleys and outlet glacier catchments following diverse and complex trajectories (Fig. 9). It is for instance
modelled to be transported by the Rhône outlet glacier reaching the Lyon outlet glacier (France), but also
948 by the Solothurn outlet glacier (Switzerland), the Dora Baltea outlet glacier reaching the Ivrea morainic
arc (Italy), and the Ticino-Toce outlet glacier (Italy) (Fig. 9). Arolla Gneiss trajectories enable us to
950 visualize how modelled ice flux from the upper Rhône glacier diverges over the northern Lake Geneva
flanks during the LGM, as previously modelled (e.g. Juvet et al., 2017). Indeed, it reveal how modelled
952 ice flowing along the true right side of the Rhône valley (between Martigny and Montreux, Switzerland)
bends eastwards and heads towards Solothurn, while ice flowing along the true left side of the Rhône
954 valley bends south-westwards along the Geneva Lake and heads towards the Lyon outlet glacier (Fig. 9).



956 Interestingly, some of the particles heading towards Solothurn are pushed against the southeastern Jura
flanks in locations of modelled ice transfluences causing glacial transport through the Jura mountains, into
958 the Doubs valley and towards the northern margins of the Jura icecap (France) (Fig. 9). Our simulations
thus produce transfluences of alpine ice overflowing the Jura mountains during peak LGM extent and
960 volume (~24.8 kyr). These transfluences are modelled in three broad locations, firstly towards the Vallorbe
pass and the valley of the Jougne (46°43'N; 6°23'E), secondly towards Baulmes and Sainte-Croix (East
962 of the Mount Suchet: 46°48'N; 6°30'E), and thirdly directly West of Vallorbe over the 'Grotte aux Fées'
cave and the Combe du Puits area (46°42'N; 6°19'E). Former expansions of alpine glaciers overflowing
964 the Jura mountains are thought to have occurred during pre-LGM maximum Late-Quaternary glaciations
such as during Marine Isotope Stage (MIS) 12, 10, 8, or 6 (Keller and Krayss, 2011; Preusser et al., 2011;
966 Graf et al., 2015). However, no published evidence yet exists for such transfluences during the LGM (MIS
2) (Campy, 1992; Buoncristiani & Campy, 2011). Our model may either slightly overestimate ice thickness
968 over the Rhône and Solothurn glaciers during the LGM, or may be correct but sedimentological evidence
for such momentary transfluence may be rare and not yet documented/dated. The modelled Arolla-Gneiss
970 trajectories reveal other surprising and complex pathways, such as possible transport of glacial sediments
up into the Aulps valley (Morzine river valley, France) by ice from the Rhône glacier which, in our model,
972 generates southward ice-flow upvalley from the Geneva Lake basin (Fig. 9). Key differences can be
observed between modelled Arolla-Gneiss trajectories of particles seeded subglacially versus
974 supraglacially. Within the Rhône glacier catchment, Arolla-Gneiss outcrops are confined to high-elevation
topographies located towards the glacier's upper accumulation zone, where nunatak occurrence and
976 rockfall potential are high, and where modelled basal ice velocities remain relatively low (<50 m yr⁻¹).
Thus, within the Rhône glacier catchment, supraglacially seeded particles from Arolla-Gneiss outcrops
978 yield a higher number and diversity of modelled trajectories, relative to subglacially-seeded particles (Fig.
9). In the southern Italian Alps, particle trajectories show the opposite, with numerous outcrops located in
980 fast-flowing ice regions leading to higher numbers of trajectories and ice-contact deposit locations for
particles of subglacial origin.

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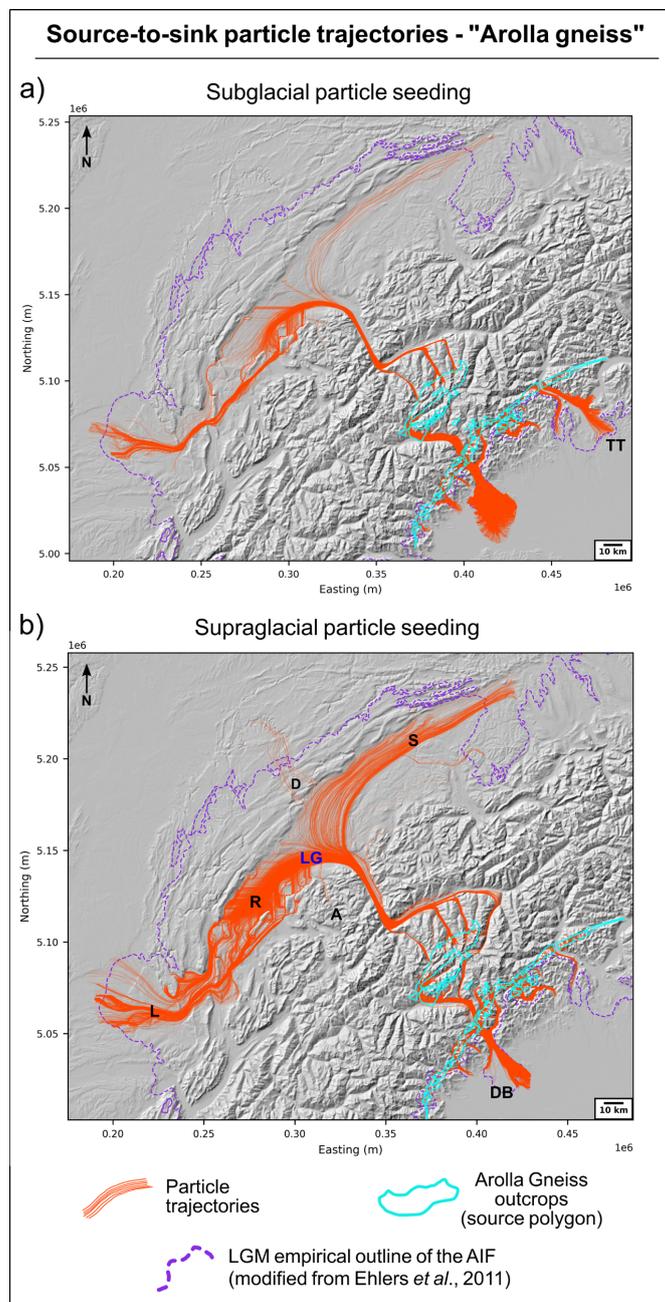
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Figure 9. Source-to-sink analysis and resulting particle glacial-transport trajectories for all particles seeded within an example source polygon; in this case a single surface lithology from our source-to-sink catalogue (n=22 surface lithologies), i.e. the Arolla Gneiss (originally mapped by Bigi *et al.*, 1990). Particle trajectories are shown for both subglacial (a) and supraglacial (b) seeding. We interpret these source-to-sink trajectories as model estimates of possible locations (along the entire trajectories) where ice-contact deposits of the Arolla-gneiss lithology may have been transported to and deposited by glaciers between 40 and 18 ka (time frames of simulations). The labels ‘A’, ‘DB’, ‘D’, ‘L’, ‘LG’, ‘R’, ‘S’, ‘TT’ stand for: ‘Aulps valley’, ‘Dora-Baltea outlet glacier’, ‘Doubs valley’, ‘Lyon outlet glacier’, ‘Lake Geneva’, ‘Rhône glacier’, ‘Solothurn outlet glacier’, ‘Ticino-Toce outlet glacier’, respectively, and relate to places/features mentioned in the main text (section 3.4.1).



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3.4.2 Model-data comparison with dated erratics

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Our ‘source-to-sink’ analysis provides the opportunity to test model agreement against data from ice-
1036 contact deposits of known provenance. Here, we conduct such a model-data comparison by compiling
peer-reviewed publications which dated erratic boulders in the Alps to the time range of our simulations
1038 (40-18 ka) using terrestrial cosmogenic nuclide exposure dating (Table S1). The compiled erratics need to
feature a lithological description that is specific enough (e.g. ‘Central Aar granite’) to be associated to a
1040 well-defined and spatially restricted lithology (unlike ‘limestone’, for instance). Moreover, only one
sample per location (i.e. a sampling site in original studies) is considered for this test, to reduce statistical
1042 biases. A total of 38 erratic boulders were found to match these requirements, published in 13 separate
studies (Ivy-Ochs et al., 2004; Gianotti et al., 2008; Reber et al., 2014; Graf et al., 2015; Bichler et al.,
1044 2016; Wüthrich et al., 2018; Ivy-Ochs et al., 2018; Boxleitner et al., 2019; Prud’homme et al., 2020;
Braakhekke et al., 2020; Kamleitner et al., 2022; Kamleitner et al., 2023; Roattino et al., 2023). Exposure
1046 ages were re-calculated consistently as part of the AlpIce geochronological database (Kamleitner et al., *in
prep*). Modelled particle trajectories (subglacial and supraglacial seeding combined) for the relevant
1048 source lithology successfully overlap the locations of erratic boulders of that lithology in 26 out of 38
cases (Table S1). The trajectories thus fit empirical data in 68% of cases. This number would moreover
1050 increase to 81% would we tolerate a small (<4 km) increase in ice extent in locations where our model
slightly underestimates ice extent during the LGM, relative to mapped terminal moraines (see Fig. 1a, 4a
1052 in Leger et al., 2025). Thus, clear model-data misfit is only observed in 18% of cases (10 boulder samples).
These results suggest our LGM model of the AIF coupled with our particle-seeding and 3D tracking
1054 schemes can transport particles to appropriate locations, for the majority of the compiled erratics (Table
S1).

1056

3.5 Detecting LGM ice transfluences across the Alps

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As shown above with the example of Arolla Gneiss ‘source-to-sink’ trajectories overflowing the Jura
1060 Massif, the coupling of 3D particle tracking enables us to estimate, for the first time, the precise locations
and time span of ice transfluences in the Alps during the LGM (Fig. 10). Ice transfluences occur when the
1062 growth of ice sheets and/or icefields cause the formation of topographically uncoupled ice domes, i.e.
which accumulate away from summits and hydrological catchment divides. If the surface elevation of
1064 these domes exceeds the altitude of neighbouring cols, uncoupling from main hydrological catchments
occurs causing ice-flow to cross main hydrological divides (Linton, 1949). This can result in glacial
1066 sediment transport over high-elevations ridges/cols and into different catchments (Monegato et al., 2022)
(Fig. 10). Reconstructing LGM transfluences can thus help understand former ice-flow dynamics and
1068 unravel the puzzling lithologies/provenances of certain ice-contact deposits in the Alps (e.g. Reitner et al.,



2010). Here, we loaded our modelled particle trajectories and thus 3D ice-flow lines into a geographic
1070 information software (ArcGIS Pro 3.4) to detect the occurrence of ice transfluences in our simulations,
focusing only on the 11 largest hydrological catchments of the Alps (Rhône, Aare, Rhein, Isar, Inn, Enns,
1072 Drau, Piave, Brenta, Adige, Po) (Lehner & Grill, 2013). We present this analysis' results in a series of
maps (Figures S8-14) highlighting the locations of modelled ice domes, flowlines, and ice transfluences
1074 across the Alps. Figure 10 shows one of these maps for the example region of the upper Inn catchment.
There, the build-up of the 'Engadin' ice dome centred towards Zernez (46°41'N, 10°05' E, 1465 m a.s.l.)
1076 and reaching a modelled maximum ice surface elevation of ~3100 m a.s.l. leads to a complex network of
topographically uncoupled flowlines causing a high concentration of ~30 ice transfluences into the
1078 adjacent Rhein, Adda, Adige, and Isar catchments (Fig. 10). This causes, for instance, modelled ice from
the Inn valley between St.-Moritz (46°29'N; 9°50'E) and Zernez (a 45 km stretch) flowing south-
1080 westwards over the Maloja pass (46°24'N; 9°41'E) into the Val Bregaglia, Como Lake basin, and feeding
the Adda and Seveso outlet glaciers (sinks 2 and 44 in 'sink-to-source' catalogue). As another example,
1082 we note that our model reproduces the well-documented Simplon pass transfluence (e.g. Florineth &
Schlüchter, 1998; Kelly et al., 2004; Dielforder & Hetzel, 2014), with ice possibly transporting sediments
1084 from the Eiger-Mönch-Jungfrau mountains (e.g. Aar granites) across the Rhône valley, over the Simplon
pass, and into the Ticino-Toce glacier system during the LGM (sink 48 in 'sink-to-source' catalogue,
1086 Figure S11). In our simulations, we also find that modelled ice is nearly always warm-based towards the
main ice domes and transfluences occurring during the LGM (see Fig. 6b in Leger et al., 2025). Moreover,
1088 the modelled time span of transfluence occurrence is highly case-specific and can vary from 1-3 kyr, thus
only during peak LGM conditions, to up to nearly the full simulation time frame (i.e. 22 kyr) and LGM
1090 period (e.g. the Engadin ice dome, Fig. 10). Consequently, our results show that coupling 3D Lagrangian
particle tracking to glacier evolution modelling can also help identify the detailed events of complex and
1092 momentary topographic uncoupling of ice-flow during major Quaternary glaciations of the Alps.

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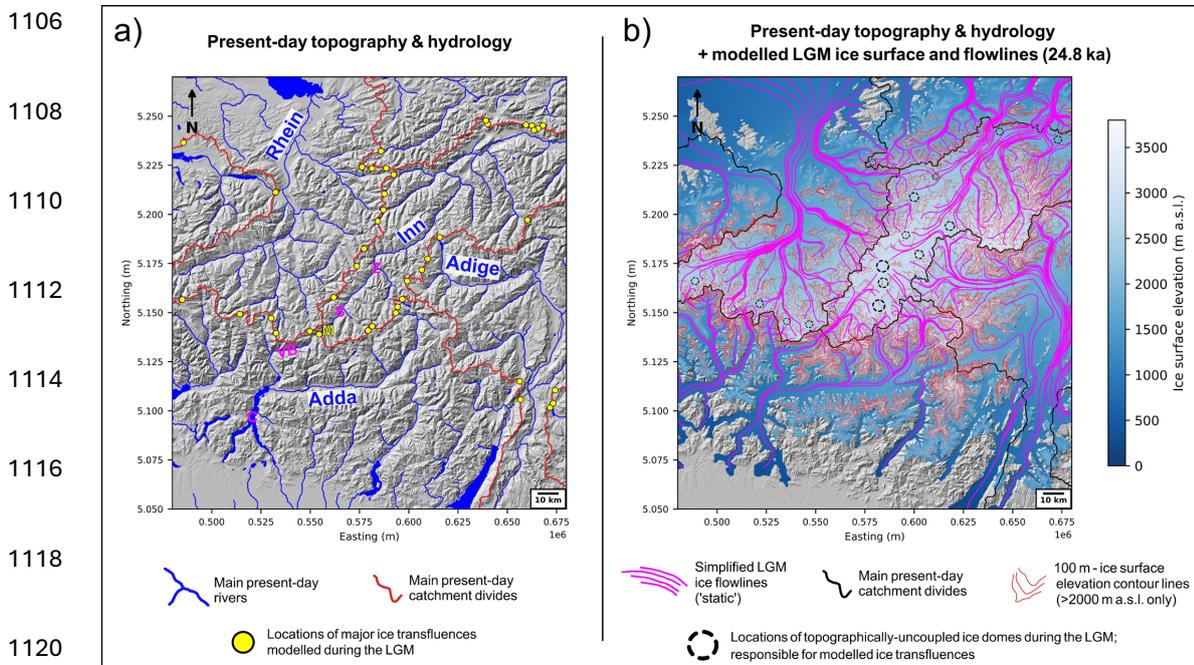
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1122 **Figure 10. Map of modelled ice surface elevations and simplified ‘static’ ice flowlines (pink lines) during the**
1124 **LGM (~24.8 ka) in the region of the Engadin ice dome, with locations of modelled ice transfluences (yellow**
1126 **dots on panel a). These transfluences can explain the complex provenance of certain ice-contact deposits. We**
1128 **quantified them for the 11 largest river catchments of the Alps, whose divides are shown in red on panel a,**
1130 **and black on panel b. A series of six figures displaying the same ice-transfluence analysis for five other regions**
1132 **of the Alpine Ice Field (AIF) are available in the Supplementary Materials. Note that whilst useful for the**
1134 **visual purpose of this figure, the simplified glacier flowlines (pink lines) shown here (panel b) are drawn from**
1136 **so-called ‘static’ flowlines, which are non-time-transient and only obtained from the depth-averaged ice**
1138 **velocity field modelled during a single time frame: i.e. the maximum AIF volume; at 24.8 ka. These should**
only be considered useful to visualize the modelled flow direction of ice at the precise locations of
transfluences and only during peak LGM. The substantially more complex and accurate time-transient flow
trajectories obtained from our 3D Lagrangian particle tracking, displayed in Figures 6 and 9 for example,
are more diverse and representative of the modelled time-transient ice-flow trajectories, but would make
visualizing transfluences on this figure impossible given the large number of modelled particles and resulting
cross-cutting trajectories (see Figure S7). On panel a, the ‘C’, ‘M’, ‘S’, ‘VB’, and ‘Z’ labels stand for ‘Lake
Como’, ‘Maloja pass’, ‘St. Moritz’, ‘Val Breglaglia’, and ‘Zernez’, respectively, and relate to locations
mentioned in main text (section 3.5).

1140

3.6 Particle trajectory sensitivity to model parameters

1142

1144 To assess the sensitivity of our particle trajectories to both the seeding scheme and model parameters, we
1146 conduct two additional AIF simulations that differ from the original setup presented above like so: i) The
first sensitivity test uses a ‘simple’ seeding scheme, which is not process-based and instead creates
particles supraglacially in a spatially- and temporally-regular manner, i.e. with seeding occurring in 20%
of grid cells exclusive to the accumulation zone, and regularly every 300 yrs. ii) The second sensitivity



1148 test uses the same ‘complex’ seeding as the original scheme (Fig. 2) but employs the parameter values of
a different ensemble simulation (i.e. number 24) within the set of 8 Not-Ruled-Out-Yet simulations
1150 obtained by Leger et al. (2025). Whilst featuring different ensemble-varying parameter values (see Table
S1 in Leger et al., 2025), simulation 24 produces Alps-wide model-data agreements in LGM ice extent
1152 and thickness that are indistinguishable from simulation 37 (used throughout this study). Input parameter
differences (n=10) however generate changes in SMB, the basal sliding parameterization, ice rheology,
1154 and the magnitude of isostatic deflection. Importantly, simulation 24 uses a different bed topography than
simulation 37, with no removal of valley-fill sediments.

1156

In the first sensitivity test, which uses ‘simple’ seeding instead, model agreement with the locations of
1158 dated erratics presented above (section 3.4.2), using our source-to-sink analysis, decreases from 81-68%
to 74-58%. These two ranges represent whether we tolerate the small (<4 km) increase in ice extent
1160 mentioned above (section 3.4.2). Whilst not substantial, this decrease in model-data agreement is
noticeable and suggests that a less process-based particle seeding scheme leads to a worse model-data fit
1162 on the provenance, glacial transport, and deposition histories of ice-contact deposits during the LGM. In
the second sensitivity test, as the seeding scheme is unchanged from the original (see section 2.2), we can
1164 use provenance fractions (%) per hydrological basin (n=241) for each sink (see section 2.4) to quantify
inter-simulation differences. Here, when using parameters from Leger et al. (2025)’s ensemble simulation
1166 24 instead of 37, we find that particle provenance fractions per hydrological basin (e.g. percentages in
Figs. 6, 8) remain identical in ~72% of cases, on average (median difference: 28.5%). When comparing
1168 particles’ provenance basins irrespective of fraction percentages, we find sink particles originate from the
same basins in 88.5% of cases. Thus, running a simulation which yields a similar LGM model-data fit but
1170 uses different sensitive parameter values causes sink particles to originate from different basins in 11.5%
of cases and provenance fractions to vary by 28.5% on average. These results show a non-negligible inter-
1172 simulation variability highlighting a noticeable sensitivity of particle trajectories and provenances to
modelled ice dynamics and/or bed topography changes. However, this test also shows that the majority of
1174 particle trajectories, provenances, and glacial transport histories remain unchanged relative to the original
simulation.

1176

1178 **4 Discussion**

1180 **4.1 Limitations and future work**

1182 The computational gains of GPU-based glacier modelling coupled with 3D Lagrangian particle tracking
enabled us to produce, for the first time, an Alps-wide estimation of transient glacial sediment pathways
1184 during the last glaciation (40-18 ka). Although our model-data comparison of source-to-sink trajectories



1186 yields promising results with between 81% and 68% model fit with dated erratics' locations (section 3.4.2,
1187 Table S1), this study should be considered a first-order attempt yielding limitations and room for
1188 improvement. We here describe the main limitations of the assumptions made in this experiment,
1189 providing suggestions for improvement in future modelling work of similar nature.

1190 In this study, we assume passive particle glacial transport with no interaction with ice rheology and flow
1191 dynamics. In reality, supraglacial debris can influence glacier surface mass balance through insulation
1192 (e.g. Rowan et al., 2015) while basal ice sediments can alter basal friction and thus glacier sliding
1193 velocities (Hallet, 1981; Iverson et al., 2003). Our modelling also assumes all glacial sediment to move at
1194 the same velocity as the ice. Whilst this is a common modelling assumption (e.g. Rowan et al., 2015;
1195 Jouvét et al., 2017; Bernard et al., 2020; Margirier et al., 2025), the drag force in Stokes Law can cause
1196 resistance and lower velocities for clasts advected within highly viscous fluids (e.g. ice; Byers et al., 2012).
1197 Moreover, complex mechanisms of sediment storage occur (e.g. lodgement tills) at partially coupled ice-
1198 bed interfaces causing sediment advection speeds below ice velocity (Alley et al., 1997; Evans et al.,
1199 2006). On the contrary, gravitational and fluvio-glacial transport within glacier systems can generate
1200 sediment advection speeds greater than ice velocity (Walder and Fowler, 1994). Gravitational englacial
1201 transport also occurs when a glacier features numerous fractures in which debris can fall, a mechanism
1202 that is not yet modelled in glacier-wide simulations. Sediment transport by rivers (proglacial) and
1203 subglacial drainage, whilst not modelled in this study, can also complexify deposits' transport histories by
1204 moving large sediment volumes further down-river prior to glacier re-entrainment (Lane et al., 2017). In
1205 future work, modelling these complex mechanisms would require full coupling of both subglacial
1206 hydrology and sediment-transport modules to glacier-evolution models (Delaney et al., 2023).

1208 We assume all sediment to be fully preserved during glacial transport, and that variability in ice-contact
1209 deposit provenance is exclusively controlled by variations in seeding and glacial transport histories.
1210 However, clast erosion during glacial transport also plays an important role. Indeed, glacial sediments
1211 transported over greater distances are more likely to spend time at the ice-bed interface where they
1212 typically undergo abrasion, crushing, or truncation (Boulton, 1978). With increasing time and transport
1213 distance, this can generate rounding and comminution of coarse sediments (e.g. boulders, cobbles) into
1214 finer fractions (e.g. silts, sands and gravels) which can be mobilized by subglacial hydrology and
1215 evacuated downstream. Subsequently, the likelihood of finding sediments from a specific source in ice-
1216 contact deposits tends to decrease with increasing distance from that source (Humlum, 1985). In future
1217 modelling work, more realistic provenance fractions may thus be obtained through parameterizations that
1218 reduce particle preservation as glacial transport time and distances increase.

1220 Our particle seeding scheme assumes that all bed surfaces are equally susceptible to subglacial erosion
1221 and production of supraglacial debris via gravitational mass wasting. This is a simplification as different



1222 lithologies yield different hardnesses and varying susceptibilities to abrasion, plucking, frost shattering,
1224 weathering, and other erosion mechanisms (Moosdorf et al., 2018). The subglacial erosion susceptibility
1226 of distinct outcrops is also often dependent on local tectonic pre-conditioning (e.g. degree of rock faulting
1228 and fracturing). The accuracy of future coupled glacier-particle modelling may thus be increased by adding
an erodibility index parameter controlling the seeding likelihood based on rock hardness, faulting,
temperature-driven rock-permafrost conditions, and resistance to erosion, constrained by present-day
geological observations and/or reconstructed past erosion rates (Gallach et al., 2021).

1230 Soft beds under temperate glaciers can become saturated with meltwater, leading to reduced effective
1232 pressure, lower basal yield stress, and faster sliding velocities (Iverson et al., 1995). While a meltwater
1234 feedback on sliding is included in our thermo-mechanically coupled glacier model setup (Leger et al.,
2025), we consistently assume a positive correlation between sliding velocities and subglacial particle
seeding through abrasion and plucking (Fig. 2). However, this may not always be the case as water
saturation of soft beds and reduced effective pressure can instead shield bed material from
abrasion/plucking reducing sediment mobilization or causing local soft bed deformation to instead
dominate (Boulton, 1979).

1238

Finally, while our GPU-based approach enables us to track an unprecedented number of particles in ice
1240 (~20.5 million) given our simulations' spatio-temporal scales, sediments are ubiquitous in real glaciers.
Therefore, our modelling, which also does not include the re-mobilization by glaciers of pre-LGM
1242 sediment deposits, likely still underestimates the diversity of pathways glacial sediments may follow
within a glacier system as complex as the former AIF during Late-Quaternary glaciations. However, as
1244 shown with this work, GPU-computing enables coupled glacier-particle modelling to become orders-of-
magnitude cheaper and more computationally efficient. This should motivate new modelling studies of
1246 this nature to include the tracking of large particle numbers, thus helping to identify the particle numbers
that more fully represent the ubiquitous nature of glacial sediments within icefield and ice-sheet systems.

1248

Given the limitations summarized above, it is clear our modelling does not fully capture the complexity
1250 of glacial sediment sourcing and transport on multi-millennial, Alps-wide scales. Therefore, the diversity
of 1) provenances and glacial transport pathways for a given ice-contact deposit, and 2) possible ice-
1252 contact deposit locations for a given source lithology, are likely underestimated by our 'sink-to-source'
and 'source-to-sink' analyses (e.g. Figs. 6, 9). However, we believe that our simulations still capture the
1254 majority of former glacial sediment transport pathways, as evidenced by the relatively good model-data
fit obtained (81-68%) when comparing modelled particle trajectories for a given lithology with data on
1256 LGM-dated erratic locations (section 3.4.2, Table S1).



1258 As described above (section 2.4), our sink-to-source analysis uses a subjective set of 49 sink polygons
1260 (Fig. 3a) covering the space between maximum time-independent margins of the modelled AIF and the
1262 updated LGM empirical outline of Ehlers et al. (2011). Our sink polygons thus result from a consistent yet
1264 highly simplified Alps-wide separation of large regions containing the LGM margins of former AIF outlet
1266 glaciers. An obvious future improvement would be to produce a similar sink-to-source analysis for a more
1268 detailed map of individual glacio-terminal landforms and ice-contact deposits that remain preserved to
1270 this day, thus enabling a more accurate model-data comparison. However, this would require producing a
1272 digital (e.g. GIS database), open-access, Alps-wide map of preserved glacial geomorphology with
1274 geochronological constraints and a consistent naming convention (e.g. Glasser & Jansson, 2008; Clark et
1276 al., 2018). To our knowledge, such a valuable product is not yet available for the European Alps.

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4.2 Coupled glacier-particle modelling; wider implications and perspectives

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4.2.1 New perspectives for paleo glacier model-data comparisons

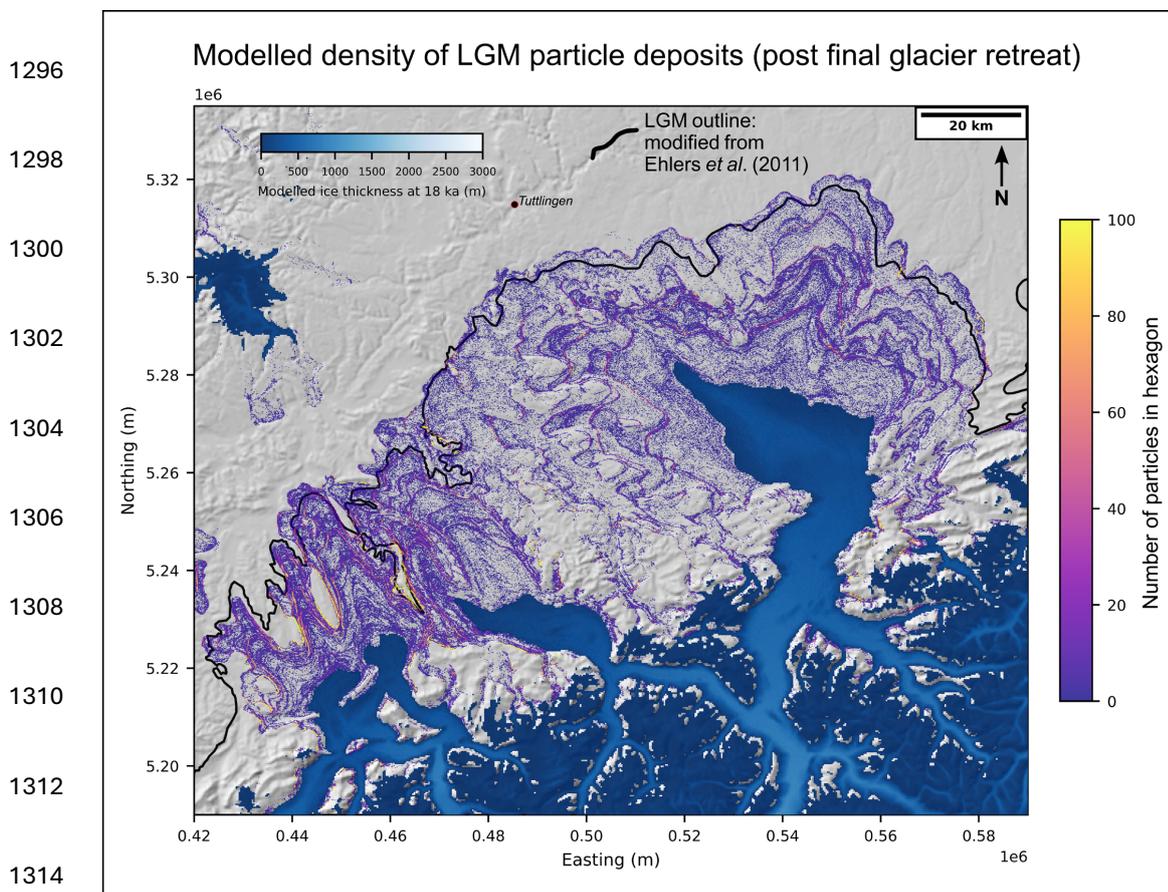
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1274 After modelling the final retreat of the AIF from its LGM margins (24-18 ka), our particle advection
1276 scheme deposits static particles in deglaciated regions which form moraine-like shapes (e.g. Fig. 11,
1278 Figures S3-6). The resulting spatial densities and shapes of these particle deposits are controlled by; 1) the
1280 modelled ice-margin shape and location at a given time, 2) the modelled ice margin retreat rate and
1282 residence time during maximum glacier extent, still-stands, and/or smaller re-advances, and 3) the supply
1284 of ice-advected particles to the glacier margins at a given model location and time. To improve the
1286 accuracy of the model regarding these three mechanisms, one could compare the spatial patterns of
1288 modelled particle deposits against the preserved glacio-geomorphological record (Fig. 11, Figures S3-6).
Although this is not within the scope of this study, we believe this work opens the possibility to design
new post-processing tools to automatically quantify the agreement between modelled particle deposits
(post deglaciation) and preserved landforms such as terminal and lateral moraines. This could represent a
novel approach to paleo model-data comparison that may complement existing tools (e.g. Ely et al., 2019;
Archer et al., 2023, Veness et al., 2025) designed to automatically score transient paleo simulations and
quantitatively evaluate model sensitivities to - and the adequacy of - input parameterizations and climate
forcings (Fig. 11). Such comparison may also help identify mechanisms controlling the spatial
heterogeneity of preserved ice-contact deposits found across deglaciated forelands and valleys today (Ivy-
Ochs et al., 2022).

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1316 **Figure 11.** Map of modelled particle deposit densities located in modelled ice-free regions at 18 ka, the final
1318 timestep of our Alpine Ice Field (AIF) simulations of the Last Glacial Maximum (here 40–18 ka), and for the
1320 foreland region of the Rhein, Linth, and Reuss outlet glaciers. The AIF model output is displayed using
1322 modelled ice thickness at 18 ka. The particle deposit data shown here combines both datasets of particles
1324 seeded subglacially and supraglacially and is expressed as a spatial density map. Each colored dot is a small
1326 hexagon in which the total number of deposited particles is computed. Bright yellow colors indicate hexagons
1328 holding the highest concentrations of deposited particles. This model output clearly highlights periods of
outlet glacier advances and/or margin stabilization during our AIF simulations through formation of
moraine-shaped particle deposits. We argue the novel ability to produce such results over large spatio-
temporal scales with our GPU-based Lagrangian particle tracking coupled to glacier evolution modelling
may provide room for future model-data comparison exercises that quantify the fit between modelled particle
deposits and the preserved glacio-geomorphological record (see Discussion section).

1330 4.2.2 A method to investigate complex internal ice-flow dynamics

1332 Lagrangian particle tracking coupled with glacier modelling essentially offers a mechanism to better
1334 visualize the time-transient 3D flow trajectories of simulated glacier motion (Figure S7). As a result, it can
help to better understand contemporary and past internal glacier dynamics, including vertical ice motion,



1336 flow convergence and divergence, and the complex behaviours of merging glaciers. Such processes can
1337 be especially complicated in topographically constrained glacier complexes such as the former AIF. For
1338 instance, when two glaciers converge, their respective ice masses will become separated by a suture zone
1339 sometimes visible through formation of medial moraines (Small et al., 1979). Reconstructing the precise
1340 locations and, importantly, the lateral migrations of such suture zones in paleo glaciers, which result from
1341 disequilibrium in the magnitudes of confronting driving stresses from two glaciers, can be crucial to
1342 explain: 1) the formation of specific subglacial landforms and their locations (e.g. lineations, drumlins and
1343 their orientations), 2) the lack or instead over-abundance of ice-contact deposits in specific locations, or
1344 3) the puzzling provenances of specific sediments deposited at glacier margins. While such complex ice
1345 dynamics can be well-represented in glacier evolution models solving high-order ice-flow physics, particle
1346 tracking offers a means to easily visualize and quantify these processes (otherwise invisible) in model
1347 outputs. Our Mont Salève case study (section 3.3.3) is a good example for which understanding the
1348 location and migration of the suture zone separating the Rhône and Arve glaciers, easily visible with
1349 particles on Figure 8 (panel a), is key in understanding the modelled provenance and transport pathways
1350 of specific ice-contact deposits in this region (e.g. the Mont Salève erratics).

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1351 *4.2.3 Implications for research on glacial landscape evolution*

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1353 By combining our results with those of Leger et al. (2025), we demonstrate that GPU-parallelization can
1354 substantially decrease the computational cost of glacier evolution modelling coupled with Lagrangian
1355 particle tracking (Fig. 4). Besides helping to estimate glacial sediment transport trajectories over multi-
1356 millennial and continental spatio-temporal scales, we believe this new approach opens the door to a range
1357 of earth-surface modelling capabilities that may prove useful in addressing research questions in the fields
1358 of glaciology and mountain geomorphology. As an example, we believe there is potential for future model-
1359 data comparison studies to better characterize the role of glacial erosion on the relief development of
1360 mountain belts during Quaternary glaciations (e.g. Bernard et al., 2025), but also on more contemporary
1361 timescales (e.g. Delaney et al., 2023). Open questions remain, for instance, regarding the relative
1362 proportions of glacial erosion materials evacuated as glaciofluvial bed/suspended load versus frozen-on
1363 englacial debris, their role in controlling sediment export and deposition rates in the lowlands, and the
1364 spatio-temporal variability of these different processes under changing hydro-climatic conditions (Alley
1365 et al., 1998; Zhang et al., 2022; Fedotova & Magnani, 2024; Delaney et al., *in press*). Large uncertainties
1366 remain also regarding subglacial mechanisms of sediment storage and resulting shielding of bedrock
1367 erosion, introducing sediment evacuation delays that are challenging to quantify, and which may bias
1368 current understandings of subglacial erosion's correlation with basal glacier conditions including ice
1369 velocity and temperature (Herman et al., 2021; Delaney & Anderson, 2022). These challenging questions
1370 would benefit from new model-data comparison studies that bridge spatio-temporal gaps in empirical



1372 observations, thus making more holistic and fully coupled model frameworks involving particle tracking
valuable tools for future investigations addressing these questions (Delaney et al., 2023).

1374 To this day, one of the most advanced and efficient models coupling glacier-flow simulations with
1376 processes of fluvial and hillslope erosion, subglacial erosion, subglacial hydrology, and sediment transport
over multi-millennial timescales, is the integrated second-order shallow ice approximation model
(iSOSIA; Egholm et al., 2011). However, it remains computationally unfeasible to run such a CPU-based
1378 model over entire mountain ranges (e.g. the Alps), Quaternary-glaciation timescales (10^4 - 10^6 yr), and at
the high spatial resolutions (<500 m) required to accurately resolve steep mountain topographies (Bernard
1380 et al., 2025). On the other hand, recent advances in GPU-optimized modelling and physics-informed
machine learning have enabled to overcome such computational bottlenecks whilst in some cases
1382 respecting high-order 3D physics (e.g. Jouvét & Cordonnier, 2023; Cordonnier et al., 2023; Jain et al.,
2024; Leger et al., 2025). The efficient GPU-parallelization of Lagrangian tracking will enable
1384 incorporating end-to-end advection of large particle numbers within fully coupled glacier-and-landscape
evolution models. Therefore, it seems plausible that over the next few years, GPU-based modelling
1386 approaches permit high-resolution simulations whose outputs can be directly compared against empirical
data on, for instance, Quaternary glacier incision rates and timing (e.g. Valla et al., 2011) or sediment
1388 export volumes and provenance data (e.g. Herman et al., 2015; Koppes et al., 2015; Overeem et al., 2017).
Such model-data comparisons may shed light on the complex mechanisms influencing the dynamics of
1390 glacial erosion and its interaction with climate and topographic change over various spatio-temporal
scales.

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5. Conclusion

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This study presents the first modelling reconstruction of sediment transport by glaciers across the entire
1398 European Alps during the Last Glacial Maximum (LGM). This is achieved via the new coupling of 3D
Lagrangian particle tracking within the Graphics Processing Units (GPU)-accelerated, high-resolution
1400 glacier simulations of Leger et al. (2025) using the Instructed Glacier Model (IGM). Our modelling
computes the 3D ice advection of tens of millions of particles, enabling us to simulate complex, time-
1402 transient glacial sediment transport trajectories across the Alps over multi-millennial timescales (40-18
ka), and at an unprecedentedly high spatial resolution (300 m). Here, a key methodological innovation is
1404 the development of process-based particle seeding schemes for both subglacial and supraglacial sediment
origins over large spatial scales, attempting to capture distinct erosion and debris entrainment dynamics.
1406 Our GPU-based approach significantly reduces the computational cost of Lagrangian tracking, making it



feasible to track tens of millions of particles within glacier evolution models ran over continental domains,
1408 which represents a computational breakthrough for glacial sediment modelling.

1410 Our two complementary sets of results, i.e. the sink-to-source (reconstructing ice-contact deposit
provenance) and source-to-sink (mapping potential depositional locations) analyses, yield Alps-wide
1412 estimates of LGM glacial sediment routing, transport times, erosion timing, and cumulative ice-free
exposure. The full results of these analyses are presented in two catalogues accessible via the Zenodo
1414 repository attached to this publication. We find particles of supraglacial origin are typically eroded earlier
in time (i.e. are older), experience longer glacier residence times, and more cumulative ice-free exposure,
1416 with implications for interpreting cosmogenic nuclide inheritance signals in surface exposure dating for
instance.

1418

By presenting case studies such as the Mont Salève erratics transport histories, we also show how our
1420 modelling can address empirical hypotheses by reconstructing detailed particle trajectories consistent with
known lithologies, which can in certain cases suggest revised paleo ice-flow interpretations. After
1422 comparing model results against empirical data, we find that sediment trajectories overlap with dated
erratic boulders in 81-68% of cases, supporting the reliability of the approach and validating the use of
1424 process-based particle seeding schemes over simpler methods. Furthermore, our results enable us to
precisely detect and map multiple LGM ice transfluences, including previously unreported overflow
1426 pathways, and estimate their occurrence durations, thus offering new perspectives on complex internal
ice-flow and topographically uncoupled glacier dynamics across the Alps.

1428

We believe this first Alps-wide modelling of LGM glacial sediment transport and ice-flow dynamics
1430 provides a range of predictions that will prove useful to glacial geologists, geomorphologists,
sedimentologists and industries studying ice-contact sediments related to Late-Quaternary glaciations of
1432 the European Alps. Finally, the computationally efficient (GPU-based) coupled glacier-particle modelling
framework developed here opens new avenues for quantitative model-data comparisons using preserved
1434 glacial geomorphology and provides a powerful tool to study and better constrain paleo ice dynamics,
sediment provenance, and Quaternary glacial landscape evolution.

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1444 **Code and data availability.**

1446 The data that represent the main findings of this study: namely the ‘sink-to-source’, ‘source-to-sink’, ‘ice-
1448 transfluence’ data catalogues and their corresponding particle-trajectory polyline shapefiles are available
1450 from the following Zenodo open-access online repository: <https://doi.org/10.5281/zenodo.18374156>. This
1452 repository also features a series of videos displaying Alps-wide results from our Instructed Glacier Model
1454 (IGM) simulations including the visual rendering of particle advection and deposition for both subglacial
1456 and supraglacial seeding and zoomed in for 10 different regions of the Alps. These videos are also
accessible via the IGM YouTube channel: <https://www.youtube.com/@IGMGlacierModel/playlists>. Finally,
this repository also features codes, files and detailed instructions required to reproduce this study’s specific
IGM simulations using the correct IGM version (2.2.1.). Note that whilst the full modelled particle
database produced in this study is too large to be stored online and shared (~1.22 TB), readers are
encouraged to contact the corresponding author if wishing to compute and display particle trajectories for
specific sinks or sources.

1458 The IGM source code (Python programming language) which now includes the fully GPU-optimized
particle-tracking module (in IGM versions $\geq 2.2.3$) is open access and available from the GitHub repository
1460 at <https://github.com/instructed-glacier-model/igm.git>. IGM’s documentation is available from its official
website at <https://igm-model.org/>.

1462

Supplement.

1464 The supplement related to this article is available online at:

1466 **Author contributions.**

T.P.M.L., G.J., and M.B. conceived and designed the study with input ideas from S.K., A.V., A.H., F.H.
1468 and S.N. G.J. developed the original version of IGM, including the Lagrangian particle-tracking module
in IGM, whose code was then modified and improved by B.F. within the context of this study to become
1470 fully GPU-optimised, with tests and compute-time diagnostics from T.P.M.L. T.P.M.L. designed and coded
the particle seeding schemes and carried out the IGM simulations. T.P.M.L. created the post-processing
1472 coding workflow for particle trajectory extraction and mapping, with help from B.A. who optimized the
Python code for efficient search of the large output particle database. T.P.M.L. compiled and generated the
1474 hydrological basin, ice-contact deposit, and surface lithology databases required for running the ‘sink-to-
source’ and ‘source-to-sink’ analyses presented above. S.K. contributed to the extraction and mapping of
1476 certain surface lithologies. T.P.M.L. conducted the model-data comparison against erratic boulder data
leveraging prior literature data mining and exposure-age recalculations from S.K. T.P.M.L. ran model
1478 sensitivity analyses, wrote the manuscript, and produced all figures and supplementary materials. All co-
authors contributed to the discussions, interpretations and gave feedback on the final manuscript and
1480 figures.



1482 **Competing interests.**

The contact author has declared that none of the authors have any competing interests.

1484

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