



While highly desired, it remains a challenge for luminescence dating to determine high doses, hence high ages (e.g., >300 ka). When employing the single aliquot regenerative (SAR) dose measurement protocol, the challenge is to project a natural dose close to saturation to a dose-response curve



36 generated with high laboratory doses. The single-saturating exponential (SSE) function mostly
37 delivers poor fits to this type of dose responses and equivalent doses obtained from such fits are
38 likely inaccurate (Timar-Gabor and Wintle 2013). Other functions are employed, mostly the single
39 saturating exponential plus linear function (e.g. Tribolo et al. 2022) or the double exponential
40 function (e.g. Timar-Gabor et al. 2015). These functions include constants that have no direct
41 physical meaning and this, in turn, is inconsistent with the luminescence measurement parameters
42 (e.g. detection wavelength) by which the signal from a dosimeter's specific trap-hole pair is targeted
43 out of a broad light spectrum. It is therefore beneficial to employ a physically based model that
44 allows to interpret observations obtained from responses to high laboratory doses.

45 Dose-response curve fitting is critical to obtaining reliable equivalent doses (e.g. Grün and Rhodes
46 1992) and has been discussed accordingly in earlier studies (e.g. Bulur and Oezer 1992; Lyons et al.
47 1992). Since the SAR measurement protocol (Wintle and Murray 2000) was introduced, Bailey (2001)
48 and subsequent studies (e.g. Singarayer and Bailey, 2004) showed that the SSE is the appropriate fit
49 function for individual quartz OSL components. From this Wintle and Murray (2006) concluded that
50 for high natural doses the limit for determining reliably the equivalent dose (D_e) is at ca 86% of the
51 saturated value, hence the rule of thumb of $D_e < 2D_0$, where D_0 is 63% of the saturated value.
52 Although not explicitly stated, this recommendation implied the accurate determination of the
53 saturation intensity I_{sat} and, as a consequence, highly variable D_0 values are reported (e.g. Thomsen
54 et al 2016).

55 Alongside the difficulty to determine I_{sat} when using the SSE, underestimation of D_e was reported
56 frequently (e.g. Murray et al. 2007; Moska et al. 2012). Such underestimations are typically evident
57 by a suppressed laboratory-generated DRC relative to the natural dose response and explained by
58 the competition for free electrons from the R centre that is low during natural and high during
59 laboratory irradiation (Bailey 2004). The natural build-up of dose would therefore be different to
60 laboratory-induced build-up, resulting in a different shape of the dose-response curve (Chapot et al.
61 2012; Timar-Gabor and Wintle, 2013; Peng et al. 2022). Although empirically often not confirmed
62 (e.g. Chapot et al. 2012), the value of I_{sat} should be the same for natural and laboratory-induced
63 DRCs unless loss of trapped electrons occurred during burial (Peng et al. 2022). Chapot et al. (2012)
64 and Timar-Gabor and Wintle (2013) agree that the growth of the natural dose can be described by
65 the SSE and that the laboratory-induced DRC is best described using the sum of two exponential
66 functions. This is confirmed by Peng et al. (2022) who simulated quartz DRCs using the Bailey (2001)
67 kinetic model with slightly modified parameters. The results from the simulation suggest
68 competition for free electrons, either in the deep electron trap of the natural sample or in the
69 recombination centres of the irradiated sample (Peng et al. (2022). This well-known competition



70 between trap and recombination centre during irradiation (Bailey, 2004) has prompted different
71 statements: the competition for electrons in the deep trap is dose-dependent which should explain
72 the second saturating exponential component in the DRC (Peng et al. 2022) or, the competition
73 effects result in non-linear dose dependence of the luminescence signal, even at relatively low
74 laboratory doses depending on the trapping probability of electrons in traps, and the trapping
75 probability of holes in centres, as well as on the recombination probability of free electrons with
76 trapped holes in the centres (Lawless et al. 2009). For the latter case, D_0 may not be independent of
77 the range of regeneration doses in a SAR measurement protocol (Murray et al. 2021) and the
78 resulting D_e is then dependent on the model of luminescence response to dose.
79 Here we explore the analytical expression, *Lambert W*, developed by Pagonis et al. (2020) and the
80 OTORX function (Lawless and Timar-Gabor 2024). Both functions are an exact solution of the OTOR
81 (one trap and one recombination centre) model, with OTOTX allowing for an additional, deeper, trap
82 to take part in the irradiation process. The well-studied OTOR model (e.g., Kitis et al. 2019, 2025)
83 suggests that the shape of the dose-response curve (DRC) depends on A_n/A_m which is the ratio of the
84 recombination to retrapping rate constants. If $A_n/A_m \sim 1$, both the OTOR and the SSE functions agree
85 and the DRC shape is the same (Pagonis et al. 2020). For A_n/A_m , we establish values empirically for
86 quartz (see also Kitis et al. 2022) and for feldspar dosimeters, and we use the OTOR model to
87 understand the significance of the SSE-derived D_0 parameter and to find the reason for the often
88 reported D_e underestimation.

89

90 **2 Material and methods**

91 **2.1 Samples and luminescence measurements**

92 The samples used in this study are fine- and coarse-grained feldspar and quartz samples originating
93 from coastal or aeolian environments to ensure sufficient bleaching at time of deposition (Table 1).
94

95 Table 1. Characteristics and origin of samples used in this study.

Sample	Dosi- meter	Grain Size (μm)	Sample depositional environment	Sample reference
Sbg 426	Feldspar	4-11	Aeolian dust	This study
Sbg 452	Feldspar	4-11	Aeolian dust	This study
Sbg 453	Feldspar	180-300	Desert sand sheet	This study
Sbg 457	Feldspar	180-300	Desert sand sheet	This study
BAT1.19A	Feldspar	4-11	Aeolian dust	Avram et al. 2020
XY575	Feldspar	4-11	Aeolian dust	Avram et al 2022



XY575	Feldspar	4-11	Aeolian dust	Avram et al 2022
Love7	Feldspar	4-11	Aeolian dust	Avram et al. 2025
Love6	Feldspar	4-11	Aeolian dust	Avram et al. 2025
Stayky	Feldspar	4-11	Aeolian dust	Veres et al.2018
CAC_2.1	Quartz	4-11; 63-90	Aeolian dust	Timar-Gabor et al. 2017
CST _{inf}	Quartz	4-11; 63-90	Aeolian dust	Timar-Gabor et al. 2012
M#6#	Quartz	4-11; 63-90	carbonate aeolianite	Timar-Gabor et al. 2017
BT844	Quartz	4-11	Aeolian dust	Meszner et al. 2013
BT755	Quartz	4-11	Aeolian dust	Fuchs et al. 2013; Dataset: Fuchs et al. 2023
BT754	Quartz	4-11	Aeolian dust	Fuchs et al., 2013; Dataset: Fuchs et al., 2023
BT753	Quartz	4-11	Aeolian dust	Fuchs et al., 2013; Dataset: Fuchs et al. 2023
XF153_A	Quartz	4-11	Aeolian dust	Timar-Gabor et al. 2017
XY575	Quartz	4-11	Aeolian dust	Avram et al 2022
Stayky	Quartz	4-11; 63-90; 180-250	Aeolian sand	Veres et al.2018
Love5	Quartz	63-90	Aeolian sand	Avram et al. 2025
Love6	Quartz	63-90	Aeolian sand	Avram et al. 2025
BAT1.19_A	Quartz	4-11; 63-90	Aeolian sand	Avram et al. 2020
MV10	Quartz	4-11	Aeolian dust	Timar-Gabor et al. 2012
MST19	Quartz	4-11; 63-90	Aeolian dust	Timar-Gabor et al. 2012

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97 The L_x/T_x data, required to undertake the analysis, were obtained from published datasets (see Table
98 1 for references) or from samples currently analysed in our laboratory (see Sbg-samples in Table 1).

99 The latter were measured using the pIRIR₂₂₅ protocol (Thomsen et al. 2008) with integration
100 intervals of 0.06 s for the signal and last 60 s for the background to be subtracted. The detection
101 window used was 410±10 nm (BG39+HC414/46) in a *Lexyg Smart* reader equipped with a UV-VIS
102 photomultiplier tube (300-650 nm) and IR light stimulation (850±5 nm) delivering 100 mW/cm² at
103 sample position. The dose points selected followed doubling of the initial dose step (i.e. 1, 2, 4, 8...;
104 e.g. Grün and Rhodes 1991) with the maximum laboratory dose being around 5000 Gy. It is assumed
105 that the sensitivity change occurring during the measurement of the natural OSL is negligible and
106 that all sensitivity change occurring during the measurement of laboratory-dose induced OSL is
107 correctly monitored by the test dose OSL/IRSL.

108



109 2.2 Generating dose-response curves

110 The experimental data were fitted using the three fit functions SSE, OTOR, and OTORX, each
111 delivering the relevant fit parameters. These are $R=A_n/A_m$, D_{63} and c for OTOR(X) and D_0 for SSE (for
112 details see next paragraph). To avoid confusion, the characteristic saturation dose derived from the
113 OTOR functions is called D_{63} , the one derived from SSE is called D_0 , both representing 63% of the
114 saturation dose I_{sat} .

115 Two codes, one written in Python and the other one written in R (R Core STeam, 2026), were
116 employed. The Python code 3.13.5 (main, May 5 2026, GCC 14.2.0) uses the SciPy package version
117 1.15.3. The R implemented used the package 'Luminescence' (Kreutzer et al., 2026) and the function
118 `Luminescence::fit_DoseResponseCurve(..., fit.method = c("EXP", "OTOR",`
119 `"OTORX"))`. Both codes use to some extent the Fortran MINPACK library (Moré et al. 1980).

120 Both codes use standard approaches (non-linear least-squares and Levenberg-Marquardt algorithm
121 as discussed in Hayes et al. 1998) with the uncertainty being determined through weighting by the
122 inverse variance. This includes forcing the fit to go through the zero point (L_0/T_0 from a SAR
123 protocol). This value varies according to the sample's specific response to laboratory dosing and
124 according to the selection of the integration time intervals (Cunningham and Wallinga 2010).

125

126 3 Analysis of the dose-response curve functions

127 The dose response of dosimeters used in luminescence dating is the result of the trap-filling process
128 during irradiation followed by thermal or optical stimulation. The resulting luminescence signal is
129 proportional to the concentration of filled traps modified by the competition effects between traps
130 and recombination centres during thermal or optical stimulation (Pagonis et al. 2020). The simplest
131 model that describes the irradiation process, is the one trap one recombination centre (OTOR)
132 model (McKeever and Chen, 1997). This fundamental model is useful for SAR-derived data because it
133 can be described by a physics-based equation for the dose response, $n(D)/N$:

$$134 \quad \frac{n(D)}{N} = 1 + \frac{W\left\{(R-1)\exp\left(R-1-\frac{D}{D_c}\right)\right\}}{1-R} \quad (1)$$

135

136 where W is the Lambert function, $R = A_n/A_m$, D is the irradiation dose and D_c is a characteristic dose.
137 For details about the derivation of this equation see Lawless et al. (2009) and Pagonis et al. (2020).
138 Within the OTOR model, R is understood as the ratio of the trapping coefficient of the electron trap
139 to the recombination coefficient of the recombination centre. If measured in units of electron-hole
140 pairs created per volume, the characteristic dose $D_c = N/R$ where N is the total concentration of the
141 electron trap. If $R=1$, then D_c is the total dose, $D+D_i$ at which the OSL intensity is 63% of saturation,



just like the SSE formula. If $R=0.2$, as might be typical for quartz (Lawless and Timar-Gabor, 2024), then D_c is the total dose, $D+D_i$, at which the OSL intensity is 81% of saturation. In other words, the normalised OSL intensity (I/I_{sat}) is a function of R when the total dose is D_c (Fig. 1). On a DRC, small R values correspond to strong sublinearity. An important feature of the OTOR formula is that its DRCs are not self-similar, i.e. plots of I/I_{sat} versus $(D+D_i)/D_{63\%}$ do not overlap, unless they have the same R . In contrast, the same normalised plots produced through the SSE function overlap, because in the SSE formula $R=1$, hence the same for all plots. Thus, the OTOR-derived formula provides the flexibility to fit a wide variety of DRC.

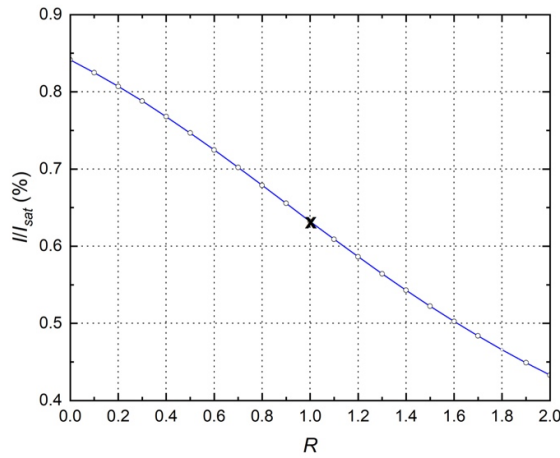


Fig. 1. The OSL intensity relative to the normalised saturation intensity as a function of R when total dose is D_c as derived from eq. 1. For $R=1$ $I/I_{sat} = 0.63\%$.

An alternative formulation of the OTOR model, called OTORX, is given by Lawless and Timar-Gabor (2024) where equations are modified to use $D_{63\%}$ as a fitting parameter:

$$I = I_{sat} \left[1 + \frac{1}{Q} \mathcal{W} \left(- (1-R) \exp \left[- \left(1 - \frac{e-1}{e} (1-R) \right) \frac{D+D_i}{D_{63\%}} - (1-R) \right] \right) \right] \quad (2)$$

where Q is

$$Q = \frac{A_m - A_n}{A_m} \frac{N}{N + N_D}$$

and $D_{63\%}$ is the dose at which $I = 0.63 I_{sat}$; all other factors are defined as in eq. 1.

For SAR-derived data, eq. 2 is normalised in the same way as it is done for SAR data:



$$\frac{L_x}{T_x} = c \frac{1 + \frac{1}{Q} \mathcal{W} \left(-(1-R) \exp \left[- \left(1 - \frac{e-1}{e} (1-R) \right) \frac{D + D_i}{D_{63\%}} - (1-R) \right] \right)}{1 + \frac{1}{Q} \mathcal{W} \left(-(1-R) \exp \left[- \left(1 - \frac{e-1}{e} (1-R) \right) \frac{D_T + D_i}{D_{63\%}} - (1-R) \right] \right)} \quad (3)$$

where D_T is the test dose and all other factors are defined as in eqs 1 and 2.

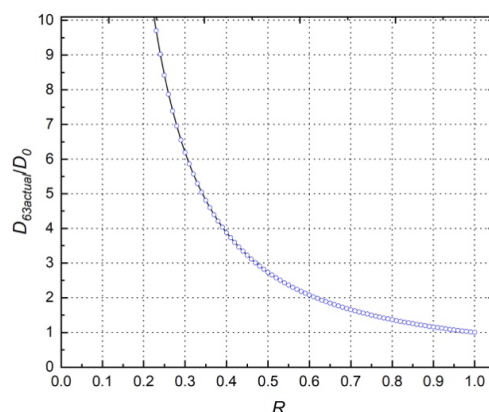
In eq. 3 I_{sat} no longer appears due to the normalisation, and is replaced by c to monitor the correction for sensitivity changes. If the sensitivity changes are corrected perfectly, c is 1. However, for most materials c is only within 20% of one.

Thus, eq. 3 involves 4 parameters:

- D_{63} (%) is the dose at which the luminescence intensity reaches 63% of the saturation dose, $I = 0.63 I_{sat}$
- R is the ratio of the trapping coefficient of the electron trap to the recombination coefficient of the recombination centre: $R = A_n/A_m$ called retrapping ratio
- c is the correction for a systematic change in sensitivity occurring during readouts of the regenerated dose OSL and subsequent test dose OSL. If c differs strongly from 1, then protocol and/or dosimeter are perhaps not appropriate
- D_i reflects the fact that OSL signal is measured even with zero applied dose, typically observed as recuperation signal.

Next, we examine the ability of the OTOR and SSE fit functions to determine the physical parameters R , D_{63} and D_0 , when the data to be fitted cover the low dose range, i.e., only the lower segment of a DRC composed of slope and curvature is covered by the data. By generating relevant mathematical formulation (see eqs A2 to A11 in Appendix), we find that error margins for D_{63} are large. To assess the error margins, the D_{63} value computed at value R ($D_{63\text{actual}}$) is compared to the D_0 value for $R=1$ (Fig. 2) using this equation:

$$\frac{D_{63\text{ actual}}}{D_0} = \frac{1 + (e-1)R}{eR^2}$$



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188 Fig. 2. The ratio $D_{63actual}/D_0$ plotted against R values ranging from 0.1 to 1, using eq. 4 (see

189 Appendix for details). For $R=1$ the ratio is 1.

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191 The plot in Fig. 2 shows that the ratio $D_{63actual}/D_0$ increases in a non-linear manner with decreasing R
192 values implying that for DRCs restricted to the low segment, the SSE model underestimates the
193 characteristic saturation dose D_0 when $R < 1$. When $R < 0.5$, the underestimation is significant .

194 Next, we test the control of the parameter R on the shape of the DRC by fitting the dose normalised
195 to the characteristic saturation dose against the luminescence intensity normalised to the saturation
196 intensity for various values of R using the OTOR function. In theory, the DRCs should not overlap and
197 should intersect at $I/I_{sat}=0.63$ and $(D+D_i)/D_{63}=1$. Using selected samples analysed in this study, we
198 plot I/I_{sat} vs D/D_{63} (Fig. 3): the lower segment of the curves appears to overlap due to generally small
199 L_0/T_0 values and the intersection point (see cross in Fig. 3) is a cluster of data points ranging from 0.6
200 to 0.7 at $D/D_{63}=1$ due to measurement uncertainty. Thus, the DRC shape is quasi-identical for
201 luminescence intensities up to D_{63} (or slightly below D_{63}) as long as the curves' zero-points are close
202 to zero. The DRC shape varies beyond D_{63} according to the sample's R value. This demonstrates that
203 the fit parameters R and D_{63} are key to accurately determine an equivalent dose from a sublinear
204 DRC.

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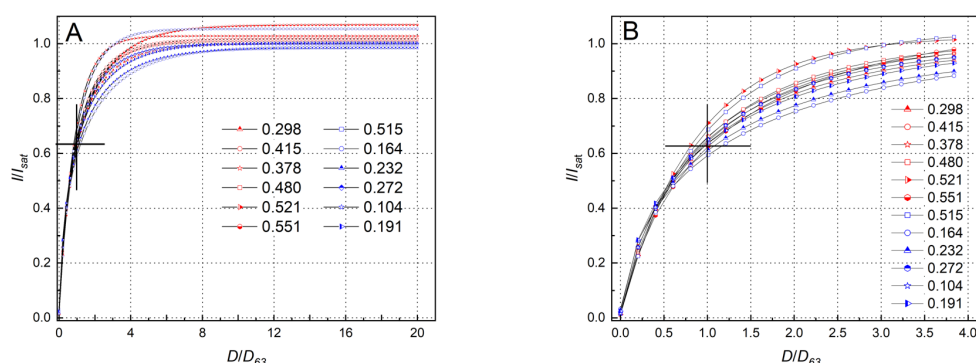


Fig. 3. The luminescence intensity (I) normalised by the intensity at saturation (I_{sat}) plotted against the laboratory dose (D) normalised by D_{63} for various values of R derived from quartz (blue) and feldspar (red) data. A – all data; B – lower segment of the curves shown in A. For values of R and D_{63} see Table 2.

In summary, our mathematical analysis reiterates what has been shown already by Pagonis et al. (2020), by Lawless and Timar-Gabor (2024) and by Kitis et al. (2025): (i) direct solutions of the OTOR model exist and these solutions are suitable to fit data derived from a SAR-based measurement protocol, (ii) the solutions provide fit parameters that are physically meaningful, (iii) the SSE function is a solution of OTOR for $R = 1$. Our mathematical analysis expand this knowledge by specifically analysing long versus short DRCs: when fitting a short DRC, the SSE function underestimates D_0 of those dosimeters for which R is actually smaller than 1. For the same short DRC, the OTOR model yields accurate D_{63} values with large error margins.

4 Results from experiments

Experiments were conducted to obtain fit parameters from SSE and OTOR(X) fit functions for a set of L_x/T_x data (for samples see Table 1), to obtain R values, examine fit parameters (D_0 , D_{63} and R) and to assess fit quality using the chi-squared test. The results are listed in Table 2.



246 Table 2. Fit parameter values for D_0 , D_{63} , R , c , and fit quality parameter ratio $\chi^2_{SSE}/\chi^2_{OTOR}$ obtained
 247 from the average of n measured aliquots using SSE, OTOR and OTORX fit functions where applicable.
 248 β_{max} is the maximum laboratory dose administered; *excluded from further examination.
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Sample	Protocol	n	β_{max} (Gy)	D_0 (SSE)	D_{63}	R	c	$\chi^2_{SSE}/\chi^2_{OTOR}$
Feldspar ($n=13$)								
Sbg 426	pIRIR ₂₂₅	3	4812	303	422	0.36	1.024	10.54
Sbg 452	pIRIR ₂₂₅	3	2355	318	454	0.424	0.936	12.25
Sbg 453	pIRIR ₂₂₅	3	2816	337	424	0.521	0.951	1.024
Sbg 457	pIRIR ₂₂₅	3	2816	311	383	0.551	0.936	1.052
BAT_1.19A	pIRIR ₂₉₀	3	5000	238	396	0.371	1.106	20.3
BAT_1.19A	pIRIR ₂₂₅	3	5000	321	519	0.301	1.062	198.9
XY575	pIRIR ₂₉₀	3	5000	249	521	0.315	1.015	152.4
XY575*	pIRIR ₂₂₅	3	5000	231	3213	0.061	0.914	134.9
Love7	pIRIR ₂₉₀	3	5000	562	878	0.378	0.972	172.1
Love7	pIRIR ₂₂₅	3	5000	634	971	0.364	0.976	69.4
Love6	pIRIR ₂₉₀	3	5000	490	805	0.497	0.956	100.3
Love6	pIRIR ₂₂₅	3	5000	490	912	0.415	0.969	38.7
Stayky*	pIRIR ₂₉₀	1	10000	283	1398	0.022	1.38	0.144
Quartz ($n=21$)								
BT844	SAR-OSL	3	1200	179	272	0.329	1.185	25.90
BT755	SAR-OSL	2	1200	179	272	0.328	1.202	38.1
BT754	SAR-OSL	2	1200	188	307	0.302	1.269	51.6
BT753	SAR-OSL	2	1200	202	332	0.305	1.215	31.3
XY575₄₋₁₁*	SAR-OSL	3	5000	241	660	0.191	0.376	71.3
Stayky₄₋₁₁	SAR-OSL	3	10000	237	688	0.223	1.046	39.6
Stayky₁₈₀₋₂₅₀	SAR-OSL	4	5000	50.8	91.2	0.256	1.180	107.5
Stayky₆₃₋₉₀	SAR-OSL	3	5000	50.1	102	0.222	1.182	230.4
Love6	SAR-OSL	3	5000	153	246	0.232	1.139	4.6



Love5	SAR-OSL	3	5000	134	244	0.216	1.216	19.8
BAT1.19A ₆₃₋₉₀	SAR-OSL	3	5000	54	111	0.323	1.144	171.3
CST_inf ₄₋₁₁	SAR-OSL	2	9984	302	668	0.184	1.056	23.6
CST_inf ₆₃₋₉₀	SAR-OSL	2	5245	143	187	0.376	1.082	15.0
CAC_2.1 ₄₋₁₁	SAR-OSL	1	5000	285	673	0.173	1.011	11.2
CAC_2.1 ₆₃₋₉₀	SAR-OSL	1	5000	99	184	0.153	1.137	11.9
M#6# ₄₋₁₁	SAR-OSL	3	6000	315	585	0.137	1.191	4.95
M#6# ₆₃₋₉₀	SAR-OSL	3	2060	105	158	0.343	1.251	737.6
MST19 ₄₋₁₁	SAR-OSL	1	5114	346	853	0.146	1.104	45.0
MST19 ₆₃₋₉₀	SAR-OSL	1	5002	172	294	0.167	1.101	20.5
MV10	SAR-OSL	1		314	808	0.110	1.091	52.1
XF_153_A ₄₋₁₁	SAR-OSL	2	5000	208	515	0.184	1.087	32.2

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251 For one quartz and one feldspar sample c deviates strongly from the expected value of 1. The values

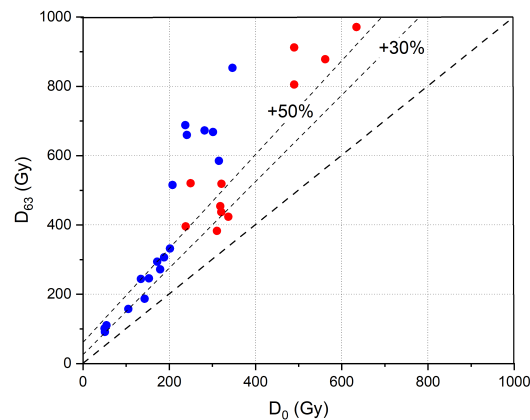
252 of D_0 , D_{63} and R obtained from these samples are therefore questionable and were excluded from

253 further examination. R -values obtained from the remaining samples are on average 0.26 ($\pm 27\%$) for

254 quartz and 0.41 ($\pm 20\%$) for feldspar. The ratio of D_0 (derived from SSE) and D_{63} (derived from OTOR)

255 is on average 0.54 for quartz and 0.65 for feldspar, i.e. D_0 is around 46% (quartz) and 35% (feldspar)

256 lower than D_{63} (Table 2; Fig. 4).



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258 Fig. 4. The D_{63} values plotted against the D_0 values for quartz (blue) and feldspar (red) samples. Lines

259 indicate the 1:1 relationship and the +30% and +50% deviation.



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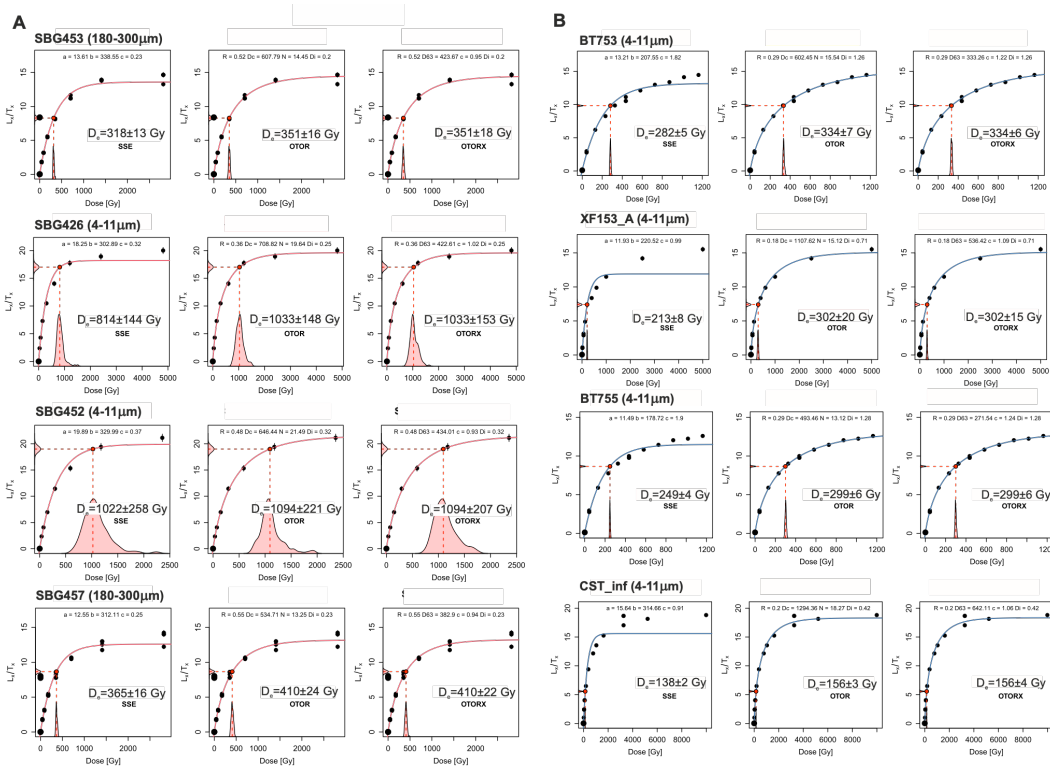
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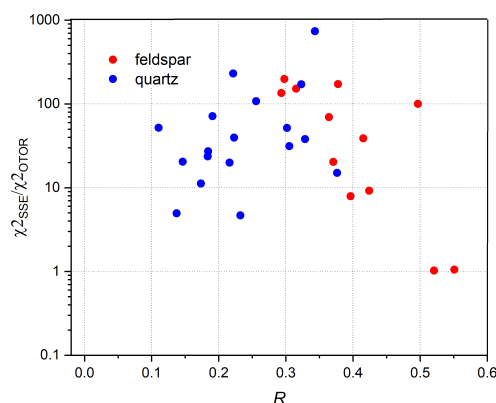
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Fig. 5. Interpolation of L_n/T_n onto DRCs generated using SSE, OTOR and OTORX functions; A - feldspar samples; B - quartz samples, both including grain size. Each panel shows the D_e value and the fit parameter values.

The quality of the SSE and OTOR(X) fits as shown in Fig. 5 is assessed using the chi-squared test with smaller χ^2 values indicating higher statistical significance. The ratio $\chi^2_{SSE}/\chi^2_{OTOR}$ is greater than 1 when the OTOR fit is more significant and hence, the poorer the SSE fit, the higher the ratio. Fig. 6 shows that most feldspar ratios and all quartz ratios are above 1, some by a factor of 10 or more (for data see Table 2).



288
 289 Fig. 6. The statistical significance of the SSE and OTOR fits for feldspar and quartz samples plotted
 290 against the OTOR fit parameter R . Note log scale of y-axis.

291

292 5 Discussion

293 In the empirical part of this study, the number of samples per dosimeter as well as the number of
 294 aliquots measured per sample, is small. The small number precludes a quantitative assessment of
 295 the experimental data, which is why uncertainties of individual parameter values are not meaningful
 296 and, hence, not listed in Table 2 and not shown in relevant figures. However, the empirical data
 297 compared with the mathematical analysis of the OTOR model (sec 3 and Appendix) allow us to infer
 298 usefulness and limitation of the OTOR fit functions for determining high natural doses using SAR
 299 protocols. This enables us to discuss the role of I_{sat} and A_n/A_m and thereby understand the D_e
 300 underestimation caused by the SSE.

301

302 5.1 DRC shape and quality of fit

303 The usefulness of the OTOR functions lies in the physical meaning of its parameters, where c allows
 304 to infer how suitable the measurement protocol and/or the sample is, R is a measure of the shape of
 305 the DRC and D_{63} is the characteristic saturation dose as is the parameter D_0 of the SSE function.
 306 The shape of the DRC is a function of experimental uncertainties, and the goodness of fit. Given the
 307 importance of the DRC shape for determining D_e , R provides a quality check for the D_e determined if
 308 its value can be predicted. Our R values for quartz (~ 0.26) are close to the ones published so far (e.g.
 309 Kitis et al., 2022; Lawless and Timar-Gabor, 2024) and slightly lower than those obtained from
 310 feldspars (~ 0.41). However, a statistically significant difference between the two dosimeters does
 311 not appear in our data: both dosimeters can show any R -value between 0.10 and 0.55 (Fig. 3) with



quartz tending to lower R -values, hence stronger sublinearity, than feldspar. Some R -values (Table 2) suggest dependence on measurement protocol where the pIRIR₂₉₀ protocol tends to deliver higher R values than the pIRIR₂₂₅ protocol. Similarly, larger grain sizes seem to deliver higher R -values than smaller grain sizes (Fig. 7). However, with the statistical noise not being quantifiable in our study, these trends remain untested.

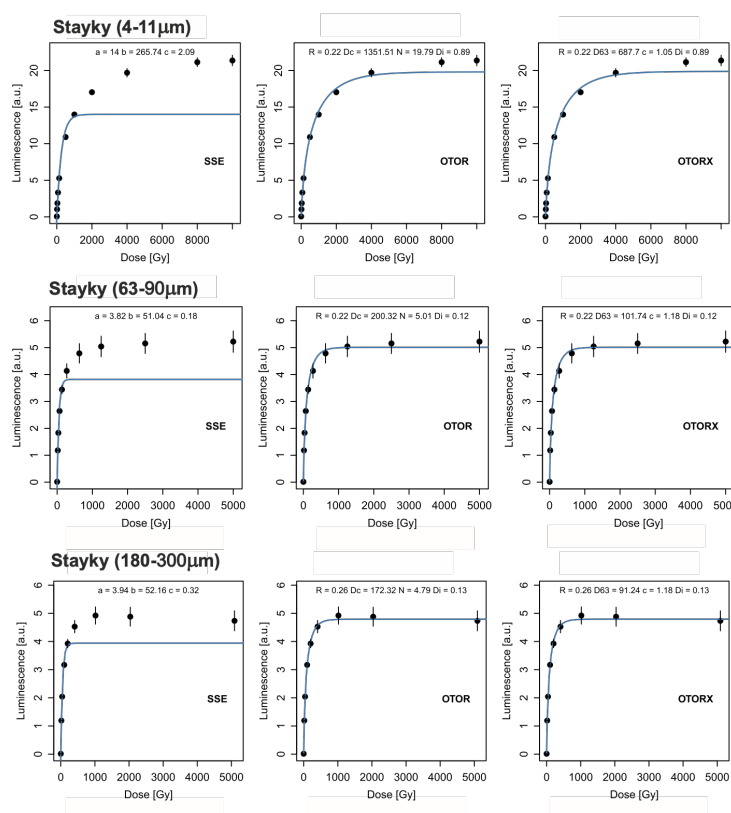


Fig. 7. DRCs of small and large quartz grains (sample Stayky).

The goodness of fit is quantified by the reduced chi-square (RCS) with $RCS < 5$ being regarded as indicating a satisfactory fit (Peng and Li, 2017). We examine the chi-squared ratio ($\chi^2_{SSE}/\chi^2_{OTOR}$; Table 2) as statistical significance of the SSE and OTOR fits and note that the OTOR functions improves the fit quality for almost all samples regardless the dosimeter (Fig. 6). Thus, the fit improvement compensates for the one extra degree of freedom that OTOR has compared to SSE. However, the improved fit quality is not independent of R : where R is outside the predicted value range, the OTOR fit quality is reduced (Fig. 6).



328 With the consistencies apparent so far, we can say that R is always smaller than 1, most probably
 329 smaller than 0.5. The impact of $R < 0.5$ is shown by the normalised D_{63} (Fig. 2) and by the normalised
 330 fit curves (Fig. 3): both the D_0 value and the shape of the DRC imply D_e underestimation where the
 331 inaccuracy of the D_e estimate becomes significant when projecting a natural dose onto the upper
 332 DRC segment, hence above $\sim D_0$. The empirical data confirm this by D_0 being 30-50% lower than D_{63}
 333 (Fig. 4). Unrealistic R values (e.g. 0.01..., 2.0...) indicate an irradiation process that cannot be
 334 described by the OTOR model. Conversely, natural doses projected onto a SSE-fitted DRC are reliable
 335 for the lower segment because this DRC segment is negligibly affected by the fact that R is actually
 336 smaller than 1 (Fig. 3) as long as the recuperated signal is small. With eq. 4 and eqs A2-A12 in mind,
 337 it is clear that this statement is valid for long DRCs only. If the DRC is short, D_0 is underestimated (Fig.
 338 2) and the separation between lower and upper DRC segment is difficult to quantify. This is evident
 339 from studies on standardised growth curves (e.g. Hu et al. 2019) demonstrating remarkably the
 340 variability of quartz DRCs, apparently caused by variable D_0 values of individual grains. Here, the
 341 OTOR functions are indeed useful, because they allow to double check fit parameters (e.g. D_0 , I_{sat})
 342 required to establish standardised growth curves.

343

344 **5.2 The role of the saturation intensity I_{sat}**

345 The value of I_{sat} is needed to accurately determine D_{63} and the value of D_{63} is required to assess the
 346 reliability of the saturation dose as shown by eq. 3 and Figs 2 and 3. Determining I_{sat} is a non-trivial
 347 task: quartz DRCs tend to show a non-monotonic shape (e.g. Duller 2012) which was explained with
 348 ‘dose quenching’, i.e. loss of recombination centres (Huntley et al. 1996) or with competition taking
 349 place during irradiation or during read-out (Lawless et al. 2005). The DRC of feldspar seem to reach a
 350 dose plateau (Fig. 5), but the corresponding dose is likely underestimated due to signal instability
 351 (Kars et al. 2008; King et al. 2018). Moreover, the study of Peng et al. (2022) suggests that there is a
 352 dose-dependent change of signal growth due to dose-dependent change in competition for free
 353 electrons in the deep trap. As dose grow, the efficiency of the trap in capturing free electrons
 354 diminishes while the recombination rate becomes stronger (Lawless et al. 2009), hence the sublinear
 355 dose response with $R < 1$. Thus, long DRCs are required to reliably determine the OTOR fit
 356 parameters. These long DRCs may or may not include I_{sat} but must be, at least, close to I_{sat} .

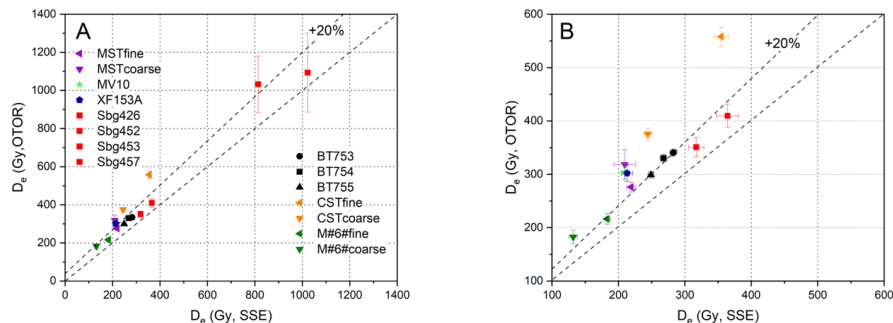
357

358 **5.3 Underestimation of high natural doses**

359 The data generated in this study suggest ca 10-30% underestimation of D_e in the dose range 100 –
 360 1000 Gy (Fig. 8) when using the SSE to construct the DRC. Our data echo the many age
 361 underestimations reported for quartz (e.g. Lowick and Preusser 2011; Timar et al. 2010; Timar-Gabor



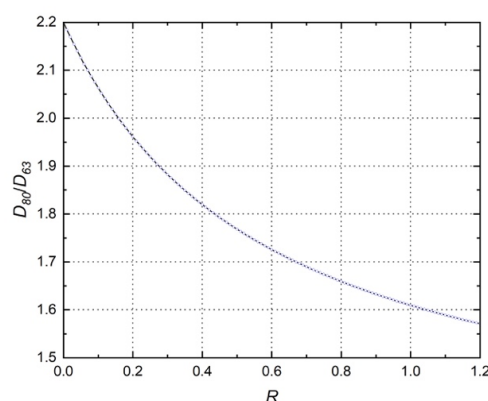
362 and Wintle 2013). Quantifying the underestimation for feldspars requires fading correction using the
363 OTOR function (e.g. Guralnik and King, 2025).



364
365 Fig. 8. Comparing D_e s obtained from OTOR and SSE fits. Feldspar data (red square) are not corrected
366 for fading. A – all samples analysed; B – detail of A for the dose range 150–450 Gy.

367
368 Approaches that circumvent the problem were proposed: selecting ‘supergrains’ out of the grain
369 population sampled (Yoshida et al. 2000), i.e. grains exhibiting D_0 values that are close to the
370 expected D_e value (e.g. Arnold et al 2016) or, the weighted mean natural dose (L_n/T_n) of all measured
371 grains is projected onto a standardised growth curve (Li et al. 2016). Both approaches rely on correct
372 estimation of the D_0 value. However, this value is underestimated for long DRCs (Fig. 4) and,
373 probably even more pronounced, for short DRCs (Figs. 2).
374 The often used alternative to the SSE is the double exponential (DSE) function. In fact, Pagonis et al.
375 (2020) show for a set of experimental data, that the DRCs obtained from OTOR and DSE fits are
376 indistinguishable. Earlier studies, albeit not referring to the OTOR model, demonstrate the
377 usefulness of the DSE function for determining high natural doses (e.g. Chapot et al. 2012; Timar-
378 Gabor et al. 2012; Berger and Chen 2011; Murray et al. 2007) and data displayed in Table A1 clearly
379 show agreement of D_e values obtained from OTOR and DSE fits. Thus, the DSE function likely delivers
380 reliable fits, with the only disadvantage being its less meaningful fit parameters and one extra
381 parameter that adds to the number of uncertainty components.

382
383



384

385 Fig. 9. The ratio D_{80}/D_{63} plotted vs R (see eq. A13 – A15 in Appendix for calculation).

386

387 Our study suggests that the dose range, for which the SSE offers reliable natural dose estimates, lies
 388 below $I=0.63I_{sat}$. From this follows that a D_e determined with a SSE fit is reliable when $D_{eSSE} < D_0$. As a
 389 consequence, the $D_e < 2D_0$ rule should be abandoned (see also King et al. 2018), because it does not
 390 take the parameter R into account which controls the shape of the DRC. Fig. 9, displaying the
 391 relationship between the ratio D_{80}/D_{63} and R confirms this: For $R=1$ the ratio is ~ 1.609 for OTOR, as
 it

392 is for SSE. For $R \sim 0.26$, which is the predicted value for quartz, the ratio is ~ 1.92 , hence $\sim 80\%$ higher
 393 than for SSE. For the calculation of these values see Appendix.

394

395 Conclusions

396 OTOR is a phenomenological model of the simplest form with the smallest number of parameters. It
 397 is well described for a number of dosimeters including quartz. For feldspars the application is
 398 justified by the simplicity of the model which captures the fundamental mechanisms of irradiation
 399 and readout in many insulators. We note that R values obtained experimentally are consistent, but
 400 are generally higher for feldspars than for quartz, which confirms the pronounced sublinearity
 401 observed with most quartz DRCs.

402 The OTOR fit functions are most useful for multi-grain aliquot data where the luminescence intensity
 403 is the sum of light emitted by multiple grains and detected in a narrow optical window. The results
 404 from the chi-square test show much better fit quality of OTOR compared to SSE, in particular for
 405 quartz, although OTOR involves one degree of freedom more than the SSE function.

406 The OTOR model does not necessarily describe all dose responses possible for dosimetric materials
 407 and may well be of limited use on the single-grain level. The OTOR solutions are unable to help with



complications that arise in the dosimeter due to chemical composition, crystal growth dimensions, defect locations in the crystal (e.g., Townsend et al. 2021) etc., all together making charge transfer via localised and delocalised mechanisms a complex recombination process. Moreover, using the OTOR functions to correct the DRC for fading is yet to be shown. Other functions should be taken into consideration, such as the GOK (General Order Kinetics, e.g. Guralnik et al. 2015) and the Broadly Applicable Function (Burbidge, 2015) both covering a wide range of dose responses. Our study suggests that reliable equivalent doses are obtained from a SSE fit only when the natural dose is smaller than the characteristic saturation dose while bearing in mind that the D_0 value is always underestimated if the DRC is short and $R < 0.5$. For high natural doses, i.e. $D_e > D_0$, the SSE is unable to describe the dose response data, and this leads automatically to D_e underestimation. To avoid D_e underestimation we recommend to replace the “ $2D_0$ ” rule with “ $1D_0$ ” when using the SSE function for generating a DRC.

420

421

422 **Appendix A**

423 SSE and OTOR

In luminescence dating the single-saturating exponential function (SSE) is typically used to fit a dose response curve (DRC) to the data points obtained from a SAR protocol. The relationship between the SSE and OTOR functions is as follows: for $R=1$, eq. 1 in the main text reduces to:

$$427 \quad F_1\left(\frac{D}{D_{63}}, 1\right) = 1 - \exp\left(\frac{-D}{D_{63}}\right) \quad (\text{A1a})$$

428 where F_1 is defined by:

$$429 \quad F_1\left(\frac{D}{D_{63}}, R\right) \equiv 1 + \frac{1}{(1-R)} \mathcal{W}\left\{-(1-R)\exp\left[-\left(1 - \frac{e-1}{e}(1-R)\right)\frac{D}{D_{63}} - (1-R)\right]\right\} \quad (\text{A1b})$$

430

431 OTOR and SSE for low-dose segment of the DRC

When the data obtained from a SAR measurement only cover the lower segment of a DRC composed of slope and curvature, the DRC is described by eq. S2 where, for reasons of simplicity, we assume no deep traps and no recuperation:

$$435 \quad I = I_{sat} F_1\left(\frac{D}{D_{63}}, R - 1\right) \quad (\text{A2})$$

The low-dose segment of the DRC is short enough to be accurately described by a quadratic polynomial which allows to expand eq. S2 into a Taylor series for low dose:

$$438 \quad I = \frac{[1 + (e-1)R]I_{sat}}{eRD_{63}} D - \frac{[1 + (e-1)R]^2 I_{sat}}{2e^2 R^3 D_{63}^2} D^2 + \mathcal{O}(D^3) \quad (\text{A3})$$

439



440 The same expansion is done for the SSE by setting $R=1$ in eq. S3 which yields:

$$441 \quad I = \frac{I_{sat}}{D_{63}} D - \frac{I_{sat}}{2D_{63}^2} D^2 + \mathcal{O}(D^3) \quad (A4)$$

442 We note that the OTOR expansion has three parameters (I_{sat} , D_{63} , R) and the SSE has two parameters

443 (I_{sat} , D_{63}).

444 By fitting the low segment of the DRC, the experimental constants c_1 and c_2 are obtained

445

$$446 \quad I = c_1 D - c_2 D^2 \quad (A5)$$

447 The next step is to match the experimentally determined correlation (eq. S5) to the OTOR model (eq.

448 S3) in a way that each corresponding coefficient in the two power series match. We consider that, if

449 two polynomials of a continuous variable (D in our case) are everywhere equal, the two polynomials

450 must have the same coefficient. Thus:

$$451 \quad c_1 = \frac{[1 + (e - 1)R]I_{sat}}{eRD_{63}} \quad (A6)$$

452

$$453 \quad c_2 = \frac{[1 + (e - 1)R]^2 I_{sat}}{2e^2 R^3 D_{63}^2} \quad (A7)$$

454

455 In eqs S6 and S7, c_1 and c_2 are known from experiment, $e \sim 2.718$ is the known constant and the

456 parameters D_{63} , R and I_{sat} are unknowns. Thus, we have two equations and three unknowns. As a

457 consequence, determining D_{63} (OTOR) from a low-dose segment of the DRC involves large error

458 margins. Conversely, D_0 (SSE) determined from a low-dose segment of the DRC, is precise when

459 assuming $R=1$ (see eq. S12 and Fig. 2 in main text for detail). To solve the problem of OTOR, we

460 assign a predicted value to R and solve eqs S6 and S7 to obtain I_{sat} and D_{63} in terms of the

461 experimental constants c_1 and c_2 :

$$462 \quad D_{63} = \frac{1 + (e - 1)Rc_1}{2eR^2c_2} \quad (A8)$$

$$463 \quad I_{sat} = \frac{eR}{[1 + (e - 1)R]} D_{63}c_1 = \frac{c_1^2}{2Rc_2} \quad (A9)$$

464

465 For SSE which assumes $R=1$, the above equations (S8 and S9) simplify to:

$$466 \quad D_{63} = \frac{1c_1}{2c_2} \quad A10$$

$$467 \quad I_{sat} = \frac{1c_1^2}{2c_2} \quad A11$$

468



Next, we analyse how much error is incurred when assuming a fixed R to use for fitting. We compare, for a given c_1 and c_2 , the D_{63} value (OTOR) computed at value R to the value of D_0 (SSE) computed for $R=1$. Taking the ratio of eq. S8 to eq. S9:

$$\frac{D_{63}}{D_0} = \frac{1 + (1 - e)R}{eR^2} \quad (\text{A12})$$

For the plot of eq. S12 see Fig. 2 in main text.

D_{63} and D_{80}

D_{63} is the dose at which the OSL response is 63.2% of its saturated value. D_{80} is the same for 80% of the saturated value. Excluding recuperation, the formulation is:

For OTOR:

$$D_{63} = \left[\frac{1}{e} - \left(1 - \frac{1}{e} \right) R \right] D_c \approx (0.367 + 0.633R) D_c \quad (\text{A13})$$

$$D_{80} = D_{63} \left[\frac{\ln(5) - \frac{4}{5}(1-R)}{1 - (1 - \frac{1}{e})(1-R)} \right] \approx D_{63} \left[\frac{0.809 + 0.800R}{0.368 + 0.632R} \right] \quad (\text{A14})$$

For SSE:

$$I = \left(1 - \frac{1}{e} \right) I_{sat} \quad \text{when } D = D_0 \quad (\text{A15})$$

$$D_{80} = D_0 \ln(5) \approx 1.609 D_0$$

For the relationship of D_0 or D_{63} to D_{80} for SSE and OTOR see Fig. 9 in main text.

Table A1. D_e values obtained for samples analysed in this study. DSE (double saturating exponential function) data with star (*) were obtained from Timar-Gabor et al. (2012).

Sample, Grain Size	Dosimeter	D_e (Gy; SSE)	D_e (Gy; OTOR)	D_e (Gy; DSE)
BT753 ₄₋₁₁	Quartz	286±5	341±7	344±7
BT754 ₄₋₁₁	Quartz	268±5	330±7	335±7
BT755 ₄₋₁₁	Quartz	249±4	299±11	301±6
CAC_2.1 ₄₋₁₁	Quartz	102±3	112±4	100±4
CAC_2.1 ₆₃₋₉₀	Quartz	90±2	127±4	129±5
CST_inf ₄₋₁₁	Quartz	360±9	558±20	650±20*
CST_inf ₆₃₋₉₀	Quartz	246±5	375±9	628±47*
M#6# ₄₋₁₁	Quartz	183±7	216±11	206±12
M#6# ₆₃₋₉₀	Quartz	133±7	183±12	187±14
MST19 ₄₋₁₁	Quartz	220±6	276±10	289±9*
MST19 ₆₃₋₉₀	Quartz	210±14	319±37	288±57*
MV10 ₄₋₁₁	Quartz	213±8	304±16	310±9*



XF_153_A ₄₋₁₁	Quartz	208±7	293±16	304±23
Sbg 426 ₄₋₁₁	Feldspar	814±144	1033±148	1090±152
Sbg 452 ₄₋₁₁	Feldspar	1022±258	1094±221	1075±235
Sbg 453 ₁₈₀₋₃₀₀	Feldspar	318±13	351±16	355±17
Sbg 457 ₁₈₀₋₃₀₀	Feldspar	365±16	410±24	404±25

491

492

493 **Code availability**

494 The R script is available at Zenodo (see link below).

495 The Python code written for OTORX is available at <https://github.com/jll2/LumDRC>

496

497 **Data availability**

498 Scripts used to generate the data as well as details of the data are available at Zenodo,

499 <https://doi.org/10.5281/zenodo.21226350>.

500

501 **Author contribution**

502 BM developed the idea of the study based on a suggestion obtained from SK. JL supported concept
503 and design and carried out computational work and mathematical formulation. SK carried out data
504 analysis and generated the empirical data. All authors contributed to interpretation of results, and to
505 text writing.

506

507 **Competing interests**

508 Sebastian Kreutzer is an associate editor of Geochronology. All other authors declare that they have
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510

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516

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525 **References**

- 526 Arnold, L. J., Duval, M., Demuro, M., Spooner, N. A., Santonja, M., and Pérez-González, A.: OSL dating
527 of individual quartz 'supergrains' from the Ancient Middle Palaeolithic site of Cuesta de la
528 Bajada, Spain, *Quaternary Geochronology*, 36, 78–101,
529 <https://doi.org/10.1016/j.quageo.2016.07.003>, 2016.
- 530 Avram, A., Constantin, D., Veres, D., Kelemen, S., Obreht, I., Hambach, U., Marković, S. B., and Timar-
531 Gabor, A.: Testing polymineral post-IR IRSL and quartz SAR-OSL protocols on Middle to Late
532 Pleistocene loess at Batajnica, Serbia, *Boreas*, 49, 615–633, <https://doi.org/10.1111/bor.12442>,
533 2020.
- 534 Avram, A., Constantin, D., Hao, Q., and Timar-Gabor, A.: Optically stimulated luminescence dating of
535 loess in South-Eastern China using quartz and polymineral fine grains, *Quaternary*
536 *Geochronology*, 67, 101226, <https://doi.org/10.1016/j.quageo.2021.101226>, 2022.
- 537 Avram, A., Mason, J. A., Del Valle Villalonga, L., Constantin, D., Grecu, S., Veres, D., Marković, S., and
538 Timar-Gabor, A.: Revisiting the chronology of a key loess section in North America using multiple
539 luminescence dating methods, *Geological Society of America Bulletin*, 137, 3207–3220,
540 <https://doi.org/10.1130/B38165.1>, 2025.
- 541 Bailey, R. M.: Towards a general kinetic model for optically and thermally stimulated luminescence
542 of quartz, *Radiation Measurements*, 33, 17–45, [https://doi.org/10.1016/S1350-4487\(00\)00100-](https://doi.org/10.1016/S1350-4487(00)00100-1)
543 1, 2001.
- 544 Bailey, R. M.: Paper I—simulation of dose absorption in quartz over geological timescales and its
545 implications for the precision and accuracy of optical dating, *Radiation Measurements*, 38, 299–
546 310, <https://doi.org/10.1016/j.radmeas.2003.09.005>, 2004.
- 547 Berger, G. W. and Chen, R.: Error analysis and modelling of double saturating exponential dose
548 response curves from SAR OSL dating, *ATL*, 29, 9–14, <https://doi.org/10.26034/la.atl.2011.444>,
549 2011.
- 550 Bulur, E. and Özer, A. M.: Comment on: A cautionary note: apparent sensitivity change resulting
551 from curve fitting, *ATL*, 10, 12–14, <https://doi.org/10.26034/la.atl.1992.191>, 1992.
- 552 Burbidge, C. I.: A broadly applicable function for describing luminescence dose response, *Journal of*
553 *Applied Physics*, 118, 044904, <https://doi.org/10.1063/1.4927214>, 2015.
- 554 Chapot, M. S., Roberts, H. M., Duller, G. A. T., and Lai, Z. P.: A comparison of natural- and laboratory-
555 generated dose response curves for quartz optically stimulated luminescence signals from
556 Chinese Loess, *Radiation Measurements*, 47, 1045–1052,
557 <https://doi.org/10.1016/j.radmeas.2012.09.001>, 2012.
- 558 Cunningham, A. C. and Wallinga, J.: Selection of integration time intervals for quartz OSL decay
559 curves, *Quaternary Geochronology*, 5, 657–666, <https://doi.org/10.1016/j.quageo.2010.08.004>,
560 2010.



- 561 Duller, G. A. T.: Improving the accuracy and precision of equivalent doses determined using the
562 optically stimulated luminescence signal from single grains of quartz, *Radiation Measurements*,
563 47, 770–777, <https://doi.org/10.1016/j.radmeas.2012.01.006>, 2012.
- 564 Fuchs, M., Kreutzer, S., Rousseau, D. D., Antoine, P., Hatté, C., Lagroix, F., Moine, O., Gauthier, C.,
565 Svoboda, J., and Lisá, L.: The loess sequence of Dolní Věstonice, Czech Republic: A new OSL-
566 based chronology of the last climatic cycle, *Boreas*, 42, 664–677, [https://doi.org/10.1111/j.1502-](https://doi.org/10.1111/j.1502-3885.2012.00299.x)
567 [3885.2012.00299.x](https://doi.org/10.1111/j.1502-3885.2012.00299.x), 2013.
- 568 Fuchs, M., Kreutzer, S., Rousseau, D.-D., Antoine, P., Hatté, C., Lagroix, F., Moine, O., Gauthier, C.,
569 Svoboda, J., & Lisá, L. (2023). [Luminescence Dataset] The loess sequence of Dolní Věstonice,
570 Czech Republic: A new OSL-based chronology of the last climatic cycle [Data set]. In *Boreas*
571 (1.0.0, Vol. 42, pp. 664–667). Zenodo. <https://doi.org/10.5281/zenodo.8246533>
- 572 Grün, R. and Rhodes, E. J.: Simulations of saturating exponential ESR/TL dose response curves -
573 weighting of intensity values by inverse variance, *ATL*, 10, 50–56,
574 <https://doi.org/10.26034/la.atl.1992.202>, 1992.
- 575 Guralnik, B. and King, G. E.: Anomalous fading correction in luminescence dating – a mathematical
576 reappraisal. *Geochronology*, preprint, <https://doi.org/10.5194/egusphere-2025-4186>, 2025.
- 577 Guralnik, B., Li, B., Jain, M., Chen, R., Paris, R. B., Murray, A. S., Li, S.-H., Pagonis, V., Valla, P. G., and
578 Herman, F.: Radiation-induced growth and isothermal decay of infrared-stimulated
579 luminescence from feldspar, *Radiation Measurements*, 81, 224–231,
580 <https://doi.org/10.1016/j.radmeas.2015.02.011>, 2015.
- 581 Hayes, R. B., Haskell, E. H., and Kenner, G. H.: An assessment of the Levenberg-Marquardt fitting
582 algorithm on saturating exponential data sets., *Ancient TL*, 16, 57–62,
583 <https://doi.org/10.26034/la.atl.1998.294>, 1998.
- 584 Hu, Y., Li, B., and Jacobs, Z.: Single-Grain Quartz OSL Characteristics: Testing for Correlations within
585 and between Sites in Asia, Europe and Africa, *MPs*, 3, 2, <https://doi.org/10.3390/mps3010002>,
586 2019.
- 587 Huntley, D.J., Short, M.A., Dunphy, K., 1996. Deep traps in quartz and their use for optical dating.
588 *Can. J. Phys.* 74, 81-91.
- 589 Kars, R. H., Wallinga, J., and Cohen, K. M.: A new approach towards anomalous fading correction for
590 feldspar IRSL dating — tests on samples in field saturation, *Radiation Measurements*, 43, 786–
591 790, <https://doi.org/10.1016/j.radmeas.2008.01.021>, 2008.
- 592 King, G. E., Burow, C., Roberts, H. M., and Pearce, N. J. G.: Age determination using feldspar:
593 Evaluating fading-correction model performance, *Radiation Measurements*, 119, 58–73,
594 <https://doi.org/10.1016/j.radmeas.2018.07.013>, 2018.
- 595 Kitis, G., Polymeris, G. S., and Pagonis, V.: Stimulated luminescence emission: From
596 phenomenological models to master analytical equations, *Applied Radiation and Isotopes*, 153,
597 108797, <https://doi.org/10.1016/j.apradiso.2019.05.041>, 2019.



- 598 Kitis, G., Peng, J., Li, B., and Pagonis, V.: Testing new analytical expression for dose response curves
599 originating from the OTOR model, *Journal of Luminescence*, 244, 118747,
600 <https://doi.org/10.1016/j.jlumin.2022.118747>, 2022.
- 601 Kitis, G., Polymeris, G. S., and Peng, J.: Determining equivalent dose for optically stimulated
602 luminescence (OSL) dating with physically meaningful dose response curves, *Quaternary*
603 *Geochronology*, 88, 101671, <https://doi.org/10.1016/j.quageo.2025.101671>, 2025.
- 604 Kreutzer, S., Burow, C., Dietze, M., Fuchs, M. C., Schmidt, C., Fischer, M., Friedrich, J., Mercier, N.,
605 Philippe, A., Riedesel, S., Autzen, M., Mittelstrass, D., Gray, H. J., Galharret, J.-M., Colombo, M.,
606 Steinbuch, L., de Boer, A.-M., and Bluszcz, A.: Luminescence: Comprehensive luminescence
607 dating data analysis (1.2.1), <https://doi.org/10.32614/CRAN.package.Luminescence>, 2026.
- 608 Lawless, J. L. and Timar-Gabor, A.: A new analytical model to fit both fine and coarse grained quartz
609 luminescence dose response curves, *Radiation Measurements*, 170, 107045,
610 <https://doi.org/10.1016/j.radmeas.2023.107045>, 2024.
- 611 Lawless, J. L., Chen, R., and Pagonis, V.: Sublinear dose dependence of thermoluminescence and
612 optically stimulated luminescence prior to the approach to saturation level, *Radiation*
613 *Measurements*, 44, 606–610, <https://doi.org/10.1016/j.radmeas.2009.03.003>, 2009.
- 614 Lawless, J. L., Chen, R., Lo, D., and Pagonis, V.: A model for non-monotonic dose dependence of
615 thermoluminescence (TL), *J. Phys.: Condens. Matter*, 17, 737–753,
616 <https://doi.org/10.1088/0953-8984/17/4/016>, 2005.
- 617 Li, B., Jacobs, Z. and Roberts, R. G.: Investigation of the applicability of standardised growth curves
618 for OSL dating of quartz from Haua Fteah cave, Libya. *Quaternary Geochronology* 35, 1–15,
619 <http://dx.doi.org/10.1016/j.quageo.2016.05.001>, 2016.
- 620 Lowick, S. E. and Preusser, F.: Investigating age underestimation in the high dose region of optically
621 stimulated luminescence using fine grain quartz, *Quaternary Geochronology*, 6, 33–41,
622 <https://doi.org/10.1016/j.quageo.2010.08.001>, 2011.
- 623 Lyons, R. G., Brennan, B. J., Hosking, P. L., and Brennan, B. J.: Estimation of accumulated dose and its
624 uncertainties: potential pitfalls in curve fitting, *ATL*, 10, 42–49,
625 <https://doi.org/10.26034/la.atl.1992.201>, 1992.
- 626 Moré, J. J., Garbow, B. S., and Hillstom, K. E.: User Guide for MINPACK-1,
627 <https://cds.cern.ch/record/126569/files/CM-P00068642.pdf> (last access: 23 May 2026), 1980.
- 628 McKeever, W. S. and Chen, R.: Luminescence models. *Radiation Measurements* 27, 625–661,
629 [https://doi.org/10.1016/S1350-4487\(97\)00203-5](https://doi.org/10.1016/S1350-4487(97)00203-5), 1997.
- 630 Meszner, S., Kreutzer, S., Fuchs, M., and Faust, D.: Late Pleistocene landscape dynamics in Saxony,
631 Germany: Paleoenvironmental reconstruction using loess-paleosol sequences, *Quaternary*
632 *International*, 296, 94–107, <https://doi.org/10.1016/j.quaint.2012.12.040>, 2013.



- 633 Moska, P., Adamiec, G., and Jary, Z.: High resolution dating of loess profile from Biały Kościół, south–
634 west Poland, *Quaternary Geochronology*, 10, 87–93,
635 <https://doi.org/10.1016/j.quageo.2012.04.003>, 2012.
- 636 Murray, A. S. and Wintle, A. G.: Luminescence dating of quartz using an improved single-aliquot
637 regenerative-dose protocol, *Radiation Measurements*, 32, 57–73,
638 [https://doi.org/10.1016/S1350-4487\(99\)00253-X](https://doi.org/10.1016/S1350-4487(99)00253-X), 2000.
- 639 Murray, A. S., Svendsen, J. I., Mangerud, J., and Astakhov, V. I.: Testing the accuracy of quartz OSL
640 dating using a known-age Eemian site on the river Sula, northern Russia, *Quaternary*
641 *Geochronology*, 2, 102–109, <https://doi.org/10.1016/j.quageo.2006.04.004>, 2007.
- 642 Murray, A., Arnold, L. J., Buylaert, J.-P., Guerin, G., Qin, J., Singhvi, A. S., Smedley, R. and Thomsen, K.
643 J.: Optically stimulated luminescence dating using quartz. *Nature Reviews, Methods Primers* 1–
644 72, <https://doi.org/10.1038/s43586-021-00068-5>, 2021.
- 645 Pagonis, V., Kitis, G., and Chen, R.: A new analytical equation for the dose response of dosimetric
646 materials, based on the Lambert W function, *Journal of Luminescence*, 225, 117333,
647 <https://doi.org/10.1016/j.jlumin.2020.117333>, 2020.
- 648 Peng, J. and Li, B.: Single-aliquot Regenerative-Dose (SAR) and Standardised Growth Curve (SGC)
649 Equivalent Dose Determination in a Batch Model Using the R Package ‘numOSL’. *Ancient TL*
650 35(2): 32–53, <https://doi.org/10.26034/la.atl.2017.516>, 2017.
- 651 Peng, J., Wang, X., and Adamiec, G.: The build-up of the laboratory-generated dose-response curve
652 and underestimation of equivalent dose for quartz OSL in the high dose region: A critical
653 modelling study, *Quaternary Geochronology*, 67, 101231,
654 <https://doi.org/10.1016/j.quageo.2021.101231>, 2022.
- 655 R1 Core Team: R: A language and environment for statistical computing (v4.6.0),
656 <https://r-project.org/> (last access: 23 May 2026), 2026.
- 657 Singarayer, J. S. and Bailey, R. M.: Component-resolved bleaching spectra of quartz optically
658 stimulated luminescence: preliminary results and implications for dating, *Radiation*
659 *Measurements*, 38, 111–118, [https://doi.org/10.1016/S1350-4487\(03\)00250-6](https://doi.org/10.1016/S1350-4487(03)00250-6), 2004.
- 660 Thomsen, K. J., Murray, A. S., Jain, M., and Bøtter-Jensen, L.: Laboratory fading rates of various
661 luminescence signals from feldspar-rich sediment extracts, *Radiation Measurements*, 43, 1474–
662 1486, <https://doi.org/10.1016/j.radmeas.2008.06.002>, 2008.
- 663 Thomsen, K. J., Murray, A. S., Buylaert, J. P., Jain, M., Hansen, J. H., and Aubry, T.: Testing single-grain
664 quartz OSL methods using sediment samples with independent age control from the Bordes-Fitte
665 rockshelter (Roches d’Abilly site, Central France), *Quaternary Geochronology*, 31, 77–96,
666 <https://doi.org/10.1016/j.quageo.2015.11.002>, 2016.
- 667 Timar, A., Vandenberghe, D., Panaiotu, E. C., Panaiotu, C. G., Necula, C., Cosma, C., and Van Den
668 Haute, P.: Optical dating of Romanian loess using fine-grained quartz, *Quaternary*
669 *Geochronology*, 5, 143–148, <https://doi.org/10.1016/j.quageo.2009.03.003>, 2010.



- 670 Timar-Gabor, A., Vasiliniuc, Ș., Vandenberghe, D. A. G., Cosma, C., and Wintle, A. G.: Investigations
671 into the reliability of SAR-OSL equivalent doses obtained for quartz samples displaying dose
672 response curves with more than one component, *Radiation Measurements*, 47, 740–745,
673 <https://doi.org/10.1016/j.radmeas.2011.12.001>, 2012.
- 674 Timar-Gabor, A. and Wintle, A. G.: On natural and laboratory generated dose response curves for
675 quartz of different grain sizes from Romanian loess, *Quaternary Geochronology*, 18, 34–40,
676 <https://doi.org/10.1016/j.quageo.2013.08.001>, 2013.
- 677 Timar-Gabor, A., Constantin, D., Buylaert, J. P., Jain, M., Murray, A. S., and Wintle, A. G.:
678 Fundamental investigations of natural and laboratory generated SAR dose response curves for
679 quartz OSL in the high dose range, *Radiation Measurements*, 81, 150–156,
680 <https://doi.org/10.1016/j.radmeas.2015.01.013>, 2015.
- 681 Townsend, P. D., Wang, Y., and McKeever, S. W. S.: Spectral evidence for defect clustering:
682 Relevance to radiation dosimetry materials, *Radiation Measurements*, 147, 106634,
683 <https://doi.org/10.1016/j.radmeas.2021.106634>, 2021.
- 684 Tribolo, C., Mercier, N., Dumottay, C., Cantin, N., Banks, W. E., Stratford, D., De La Peña, P., Backwell,
685 L., Wadley, L., and Francesco d’Errico: Luminescence dating at Border Cave: attempts, questions,
686 and new results, *Quaternary Science Reviews*, 296, 107787,
687 <https://doi.org/10.1016/j.quascirev.2022.107787>, 2022.
- 688 Veres, D., Tecsá, V., Gerasimenko, N., Zeeden, C., Hambach, U., and Timar-Gabor, A.: Short-term soil
689 formation events in last glacial east European loess, evidence from multi-method luminescence
690 dating, *Quaternary Science Reviews*, 200, 34–51,
691 <https://doi.org/10.1016/j.quascirev.2018.09.037>, 2018.
- 692 Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., Burovski, E.,
693 Peterson, P., Weckesser, W., Bright, J., van der Walt, S. J., Brett, M., Wilson, J., Millman, K. J.,
694 Mayorov, N., Nelson, A. R. J., Jones, E., Kern, R., Larson, E., Carey, C. J., Polat, İ., Feng, Y., Moore,
695 E. W., VanderPlas, J., Laxalde, D., Perktold, J., Cimrman, R., Henriksen, I., Quintero, E. A., Harris,
696 C. R., Archibald, A. M., Ribeiro, A. H., Pedregosa, F., van Mulbregt, P., and SciPy 1.0 Contributors:
697 SciPy 1.0: Fundamental algorithms for scientific computing in python, *Nature Methods*, 17, 261–
698 272, <https://doi.org/10.1038/s41592-019-0686-2>, 2020.
- 699 Wintle, A. G. and Murray, A. S.: A review of quartz optically stimulated luminescence characteristics
700 and their relevance in single-aliquot regeneration dating protocols, *Radiation Measurements*, 41,
701 369–391, <https://doi.org/10.1016/j.radmeas.2005.11.001>, 2006.
- 702 Yoshida, H., Roberts, R.G., Olley, J.M., Laslett, G.M. and Galbraith, R.F.: Extending the age range of
703 optical dating using single ‘supergrains’ of quartz. *Radiation Measurements* 32, 439–446,
704 [https://doi.org/10.1016/S1350-4487\(99\)00287-5](https://doi.org/10.1016/S1350-4487(99)00287-5), 2000