



RiverGraphNet: Physics-Aware Routing of Gridded Runoff Through Directed River Networks

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Key Points:

- A physics-aware graph neural network framework (RiverGraphNet) was developed to route physically-generated gridded-runoff through directed river-network topology.
- *RiverGraphNet* substantially improved streamflow-routing performance relative to RAPID across a heterogeneous semi-arid watershed, particularly in headwater and intermediate tributaries.
- Temporal memory representation and training objective strongly shaped routing behavior, highlighting tradeoffs between predictive skill, recession dynamics, and hydrologic realism.



42 Abstract

43 River routing provides the critical link between runoff generation and downstream streamflow prediction,
44 yet conventional routing models often rely on simplified hydraulic assumptions, fixed parameters, and
45 conservative transport formulations that may limit performance in heterogeneous river systems. Here,
46 we introduce *RiverGraphNet*, a physics-aware graph-based routing framework designed to route
47 physically generated gridded runoff through directed river networks. The framework explicitly isolates
48 routing from runoff generation by coupling *Noah-MP* runoff with a directed river-network graph derived
49 from the *NextGen* hydrofabric for the *Salt–Verde* watershed (Arizona, USA). Gridded runoff is transferred
50 from the *Noah-MP* domain to graph nodes representing hydrologic routing elements, while streamflow
51 propagation is learned using a *Graph Attention Network* (GAT) informed by physically meaningful node
52 and edge attributes describing drainage structure, terrain, and hydraulic-routing proxies.

53 *RiverGraphNet* was evaluated against observed daily streamflow at 23 USGS gauges and compared with
54 RAPID, a widely used physics-based routing benchmark forced with identical *Noah-MP* gridded runoff
55 inputs. Experiments examined the influence of temporal routing memory (3–30 day runoff lags), temporal
56 convolution, and alternative loss functions (MSE, weighted MSE, and JKGE-based objectives).
57 *RiverGraphNet* consistently outperformed RAPID across nearly all gauges and configurations. The best-
58 performing experiment (14-day lag weighted MSE) achieved a median $KGE_{\{ss\}}$ of 0.72, substantially
59 exceeding RAPID performance (median $KGE_{\{ss\}}$ of 0.0). Event-scale hydrographs and flow-duration
60 analyses demonstrated improved representation of *peak timing*, *event magnitude*, and *long-term*
61 *streamflow distributions*. Attention analysis further revealed that routing improvements were most
62 strongly associated with channel-width and dominant-pathway metrics rather than travel-time proxies
63 alone, suggesting that adaptive representation of network influence provides predictive value beyond
64 conventional travel-time parameterization. These results demonstrate the potential of physics-aware,
65 topology-constrained graph learning as a flexible alternative for routing gridded hydrologic runoff through
66 complex river networks.

67

68 Plain Language Summary

69 Predicting how water moves through river networks is essential for flood forecasting, reservoir
70 management, and water-resource planning. Traditional river-routing models use simplified physical
71 equations to move runoff downstream, but their performance can be limited in complex watersheds
72 where flow behavior varies across space and time. In this study, we developed *RiverGraphNet*, a new
73 routing framework that uses artificial intelligence to learn how water moves through connected river
74 networks while preserving the physical structure of the watershed.

75 Instead of predicting streamflow directly from weather data, *RiverGraphNet* focuses only on the routing
76 problem. We first generated runoff using a physics-based land surface model (*Noah-MP*), then transferred
77 that runoff into a digital representation of the *Salt–Verde* river network in Arizona. The model uses graph
78 neural networks, a type of machine learning designed for connected systems, to learn how runoff
79 propagates from upstream tributaries to downstream river gauges.

80 *RiverGraphNet* consistently outperformed a widely used traditional routing model (RAPID), producing
81 more accurate streamflow predictions across nearly all river gauges. It better reproduced *flood peaks*,
82 *timing of streamflow events*, and *long-term streamflow behavior*. The results show that combining
83 physically generated runoff with machine learning that respects river-network connectivity can
84 significantly improve routing predictions. This work demonstrates a promising new approach for
85 hydrologic modeling and suggests that future hybrid models combining artificial intelligence with physical
86 conservation laws could further improve realism and reliability.



87

88 **1 Introduction**

89 **1.1 Background**

90 Hydrologic and land surface models are widely used to characterize the terrestrial water cycle, and to
91 support applications such as flood forecasting, reservoir operation, climate impact assessment and water
92 resources management (*Cortés-Salazar et al., 2023; Salvati et al., 2024; Farmani et al., 2025; Agnihotri et*
93 *al., 2023b; Farmani et al., 2024; Tavakoly et al., 2016*). However, realistic streamflow prediction using
94 such models requires not only the partitioning of precipitation into evapotranspiration and runoff, but
95 also the transport routing of runoff through interconnected river networks. River routing models
96 therefore provide the critical link between runoff production and the discharge observed at stream gages,
97 by transforming runoff into spatially and temporally distributed streamflow estimates (*Cortés-Salazar et*
98 *al., 2023; Salvati et al., 2024; David et al., 2011*).

99 Physical routing processes govern the timing, attenuation, accumulation, and downstream propagation
100 of runoff signals, strongly influencing hydrograph shape, flood-wave behavior, peak discharge, and
101 baseflow representation (*Salvati et al., 2024; Fenton, 2019; Cortés-Salazar et al., 2023*). Because
102 streamflow depends on both upstream hydrologic conditions and downstream flow propagation through
103 connected river networks, a wide range of routing approaches have been developed for hydrologic
104 application, including Muskingum routing, Muskingum–Cunge routing, kinematic-wave schemes,
105 diffusive-wave formulations, dynamic-wave models, and large-scale vector-based systems such as Routing
106 Application for Parallel Computation of Discharge (RAPID), mizuRoute, CaMa-Flood, and the Model for
107 Scale Adaptive River Transport (MOSART) (*Seo et al., 2026; David et al., 2011; Salvati et al., 2024;*
108 *Mizukami et al., 2016; Yamazaki et al., 2013; Li et al., 2013*). These approaches are widely used because
109 they provide interpretable representations of flow propagation while preserving mass conservation and
110 maintaining the computational efficiency required for operational hydrologic applications. (*David et al.,*
111 *2011*). Previous studies have shown that explicitly representing river-network routing can substantially
112 influence streamflow simulations relative to modeling approaches in which runoff transport through river
113 networks is treated implicitly or represented using simplified basin-response functions (*Cortés-Salazar et*
114 *al., 2023; David et al., 2011*).

115 Despite these advantages, simplified river-routing approaches such as RAPID and mizuRoute necessarily
116 rely on assumptions and parameterizations that may limit their performance in heterogeneous or highly
117 nonlinear river systems. For example, Muskingum-based and related routing formulations approximate
118 flow translation and attenuation using prescribed routing parameters, which may become less effective
119 under rapidly rising floods, fluctuating hydrographs, highly diffusive flow conditions, or spatially variable
120 channel and floodplain behavior (*Fenton, 2019; Cortés-Salazar et al., 2023*). Many routing frameworks
121 also do not explicitly represent evaporation, seepage, reinfiltration, channel transmission losses, and
122 other runoff–streamflow transformation processes that can be important in semi-arid river systems (*Lima*
123 *et al., 2025; Nijssen et al., 2001*). In addition, existing routing systems can be difficult to adapt to human
124 regulation, including reservoir operations, diversions, irrigation withdrawals, and managed releases,
125 without additional site-specific parameterization or operational rules (*Cortés-Salazar et al., 2023; Salvati*
126 *et al., 2024*). These limitations motivate routing approaches that retain physically meaningful river-
127 network structure while allowing more flexible, spatially adaptive representation of runoff propagation
128 through connected river systems.

129 **1.2 The Potential of Graph Neural Networks**

130 Limitations of conventional routing frameworks, and the increasing availability of large hydrologic
131 datasets, have motivated growing interest in artificial intelligence (AI)-based and data-driven approaches
132 for river-network modeling (*Lees et al., 2021; Slater et al., 2025; Moshe et al., 2020; Wang et al., 2025*).



133 Among these approaches, *graph neural networks* (GNNs) have emerged as a particularly promising
134 approach, because river systems naturally form directed spatial graphs in which upstream conditions
135 influence downstream hydrologic responses through structured connectivity pathways. [Sun et al. \(2022\)](#)
136 demonstrated that GNNs provide a physically meaningful framework for basin-scale river-network
137 learning by explicitly incorporating river connectivity into streamflow prediction systems. Similarly, [Moshe
138 et al. \(2020\)](#) leveraged river-network topology to improve hydrologic prediction across connected basins,
139 while [Xiang and Demir \(2021\)](#) showed that distributed runoff pathways and flow-direction relationships
140 can be naturally represented using directed graph structures. Recent studies have further emphasized
141 that river-network structure, hydrological distance, and directional connectivity strongly influence
142 streamflow prediction skill and spatial dependency representation across hydrologic systems ([Seo et al.,
143 2026](#); [Liu et al., 2023](#)).

144 Building upon these developments, GNN-based hydrologic frameworks have increasingly been applied to
145 streamflow forecasting and spatiotemporal hydrologic prediction. Existing studies have incorporated
146 graph-based river-network learning for streamflow forecasting ([Sun et al., 2022](#); [Moshe et al., 2020](#)),
147 graph neural rainfall–runoff models using flow-direction and spatial attributes ([Xiang and Demir, 2021](#)),
148 graph attention networks for flood propagation and hydrodynamic prediction ([Acosta et al., 2025](#); [Sarkar
149 et al., 2025](#)), recurrent graph architectures such as GNN–GRU models for flood prediction ([Kazadi et al.,
150 2024](#)), and spatiotemporal graph neural networks for streamflow prediction across connected river basins
151 ([Akkala et al., 2025](#)). [Jia et al. \(2020\)](#) further proposed *physics-guided recurrent graph networks* that
152 combine graph-based spatial learning with hydrologic process constraints to improve prediction
153 robustness and physical consistency.

154 Recent STGNN and graph-based flood prediction studies have demonstrated that graph-learning
155 architectures can effectively capture complex spatiotemporal interactions and improve streamflow
156 forecasting performance relative to conventional machine-learning approaches ([Akkala et al., 2025](#);
157 [Roudbari et al., 2024](#); [Sarkar et al., 2025](#); [Wan et al., 2024](#)). More broadly, recent reviews of deep-learning
158 applications in hydrology have identified GNNs as promising tools for representing non-Euclidean spatial
159 dependencies and distributed hydrologic interactions that cannot be adequately represented using
160 conventional grid-based or independent time-series approaches ([Slater et al., 2025](#); [Zhao et al., 2024](#)).

161 More recent studies have begun extending graph-based hydrologic learning beyond streamflow
162 forecasting toward explicit runoff routing and topology-aware flow propagation. [Mosaffa et al. \(2026\)](#)
163 introduced a GNN-based routing module designed specifically to represent runoff transport through river
164 networks and argued that many existing deep-learning-based hydrologic models focus primarily on runoff
165 generation while treating routing processes only implicitly. Similarly, [Lima et al. \(2025\)](#) and Bindas et al.
166 (2024) explored differentiable routing frameworks for land surface models and highlighted growing
167 interest in machine-learning-based routing emulators capable of approximating traditional routing
168 behavior while reducing computational complexity. In this regard, [Taghizadeh et al. \(2025\)](#) and [Acosta et
169 al. \(2025\)](#) illustrated the potential of *physics-aware* graph learning for flood propagation and
170 hydrodynamic prediction across spatially-distributed river systems. [Wang et al. \(2025\)](#) additionally
171 emphasized the importance of graph topology for improving large-scale flood forecasting and efficient
172 information propagation across river networks while also highlighting challenges associated with long-
173 range graph interactions in large river trees.

174 Together, these studies demonstrate the growing potential of GNNs for routing-oriented hydrologic
175 modeling and motivate continued development of topology-aware and physics-guided routing
176 frameworks. However, despite recent progress, important scientific gaps remain in graph-based
177 hydrologic routing. Many existing graph-based hydrologic studies focus primarily on direct streamflow
178 forecasting using graph connectivity to improve predictive skill rather than explicitly representing runoff



transport through river networks (Sun et al., 2022; Akkala et al., 2025). More recent routing-oriented frameworks have combined machine-learning-based runoff generation with graph-based routing modules, such as long short-term memory (LSTM)–GNN architectures in which runoff is generated directly at subbasin or graph-node units prior to routing (Mosaffa et al., 2026). Other studies have explored recurrent neural networks (RNNs) to route runoff inputs derived from hydrologic models, but typically without explicitly addressing the transfer of physically generated gridded runoff into directed river-network graphs or isolating routing behavior independently from runoff generation processes (Lima et al., 2025). Consequently, relatively few studies have investigated how physically generated gridded runoff propagates through topology-aware graph-routing frameworks while evaluating routing realism, upstream–downstream consistency, and agreement with established physics-based routing models.

1.3 Scope of this Investigation

To address these gaps, we developed a physics-aware GNN-based routing framework for hydrologic streamflow prediction and evaluate (for the Salt-Verde river system in Arizona) whether GNNs can effectively route physically-generated gridded runoff through a directed river-network topology. The framework is designed as a standalone routing operator that isolates runoff transport from runoff generation. Runoff fields are generated externally by the physically-based Noah-Multi-Parameterization (Noah-MP, citation?) land surface model and transferred to a river-network topology specified using routing elements provided by the NextGen Water Resources Modeling Framework. The runoff is then propagated through a directed graph using topology-aware GNN message passing. The framework incorporates physically meaningful node and edge attributes describing river geometry, drainage structure, terrain characteristics, and hydraulic routing behavior. Together, these components define a physically structured graph-routing system for evaluating graph-based runoff propagation and streamflow prediction across heterogeneous river networks.

Unlike many existing graph-based hydrologic studies that directly predict streamflow or generate runoff at graph nodes, the proposed framework explicitly isolates the routing component by transferring gridded Noah-MP runoff into a physically structured river-network graph prior to routing. GNN-based routing through directed river-connectivity-networks is then used to predict daily streamflow at USGS gauge locations while preserving physically meaningful upstream–downstream flow structure. Model performance is evaluated against both observed and physics-based RAPID-generated streamflow, with RAPID selected as the physics-based routing benchmark because it is a widely used, computationally efficient river-network routing model that has been extensively developed, evaluated, and applied across regional to global domains, including operational and quasi-operational streamflow forecasting, flood-inundation mapping, water-resources assessment, and hydrologic modeling applications (Tavakoly et al., 2023).

By separating runoff generation from routing and explicitly bridging physically generated runoff fields with graph-based river routing, this study evaluates whether topology-aware graph learning can provide an effective and hydrologically meaningful framework for large-scale runoff routing and streamflow prediction.

2 Methods

Figure 1 provides an overview of the RiverGraphNet workflow. The framework consists of four primary components: (1) transfer of gridded Noah-MP runoff to river-network graph nodes, (2) graph-based spatial message passing along the Next Generation Water Model (NGen) river-network topology, (3) learned temporal processing of lagged runoff-response behavior, and (4) extraction of streamflow predictions at graph nodes corresponding to USGS gauge locations.

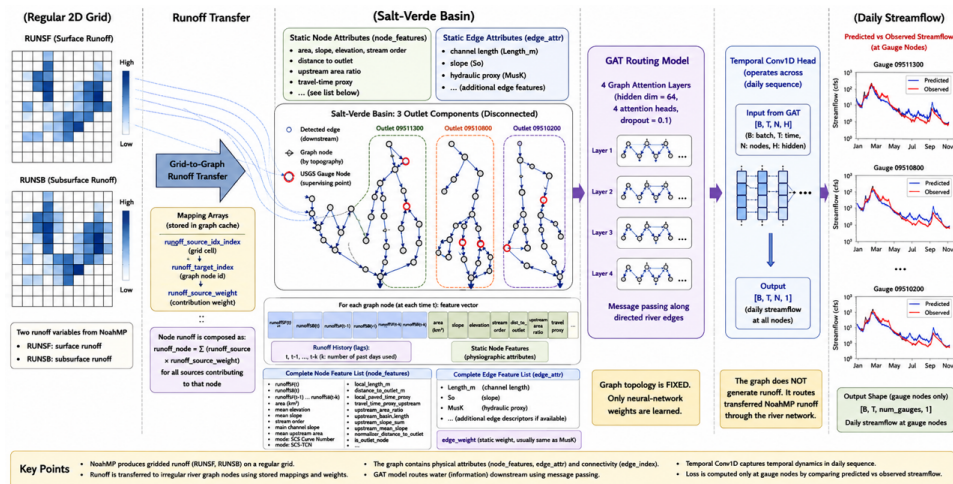


223 Unlike conventional deep-learning approaches that treat each gauge as an independent time-series
224 prediction problem, the proposed framework explicitly represents the river network as a graph. Nodes
225 represent NGen routing elements associated with flow paths/divides, and directed edges represent
226 hydrologic connectivity between upstream and downstream river elements. This structure constrains
227 information exchange to physically connected routing pathways, allowing the model to learn runoff
228 propagation and streamflow-routing relationships while preserving watershed connectivity.

229 Gridded Noah-MP runoff is first transferred from the Noah-MP grid to the graph domain. In the divide-
230 based mapping approach, each active runoff grid cell is assigned to the corresponding NGen divide or
231 routing element based on spatial overlap membership, and runoff contributions are aggregated to
232 produce node-aligned runoff inputs. These transferred runoff values provide the local water input to each
233 graph node before graph message passing is applied.

234 The following sections describe each component of the RiverGraphNet framework in detail. Sections 2.1–
235 2.2 introduce the study area and Noah-MP runoff simulations used to generate gridded runoff forcing.
236 Sections 2.3–2.6 describe the RAPID benchmark, river-network graph construction, grid-to-graph runoff
237 transfer, and graph features. Section 2.7 presents the GAT-based routing model, followed by the training
238 strategy, loss functions, and evaluation procedures in Sections 2.8–2.9.

239



240

Figure 1. Overview of the proposed graph-based routing framework. Gridded Noah-MP surface and subsurface runoff are transferred to NGen river-network graph nodes using divide-based runoff aggregation. The directed river graph preserves upstream–downstream hydrologic connectivity through graph edges representing river-network flowpaths. A GAT performs topology-aware spatial message passing using graph connectivity and physical node/edge attributes, while lagged runoff features and an optional temporal Conv1D head are used to learn delayed runoff-response behavior. Daily streamflow predictions are extracted at graph nodes corresponding to mapped USGS gauge locations and evaluated against observed streamflow and RAPID routing simulations.



241 **2.1 Study Area**

242 The Salt–Verde watershed located in central Arizona, USA (**Figure 2**) is formed by the Salt and Verde River
243 systems that originate in the mountainous regions of northern and eastern Arizona and flow southwest
244 toward the Phoenix metropolitan area. The watershed spans strong topographic and hydroclimatic
245 gradients, with elevations ranging from approximately 300 to 3,450 m above sea level. High-elevation
246 headwater regions are characterized by forested and snow-influenced environments, whereas lower
247 elevations transition into semi-arid and desert landscapes. The watershed contains complex tributary
248 structures and heterogeneous drainage characteristics, providing a challenging setting for streamflow
249 routing applications.

250 The Salt–Verde watershed plays a critical role in central Arizona water supply and reservoir operations.
251 Streamflow generation is influenced by both winter snow accumulation and summer monsoon
252 precipitation, resulting in highly variable seasonal runoff dynamics. Snowmelt-driven flows from higher
253 elevations contribute substantially to spring runoff, while short-duration convective storms associated
254 with the North American Monsoon can generate rapid hydrologic responses and localized flooding in
255 lower-elevation areas. These mixed runoff-generation mechanisms produce heterogeneous spatial and
256 temporal flow behavior across the watershed. Strong hydroclimatic variability, heterogeneous terrain,
257 and complex river topology make the Salt–Verde watershed a scientifically relevant and challenging
258 testbed for graph-based streamflow routing models.

259 A total of 26 United States Geological Survey (USGS) streamflow gauges at which 30+ years of observed
260 daily discharge records are available were selected for analysis. These gauges span a wide range of
261 drainage areas, from 36.4 to 6,615 mi², with a median drainage area of 499.5 mi². Of those, to reduce
262 anthropogenic regulation effects, three gauges that are substantially affected by major reservoir
263 operations were excluded from the primary evaluation. The remaining 23 gauges represent
264 predominantly natural flow conditions and provide broad spatial coverage across the watershed.

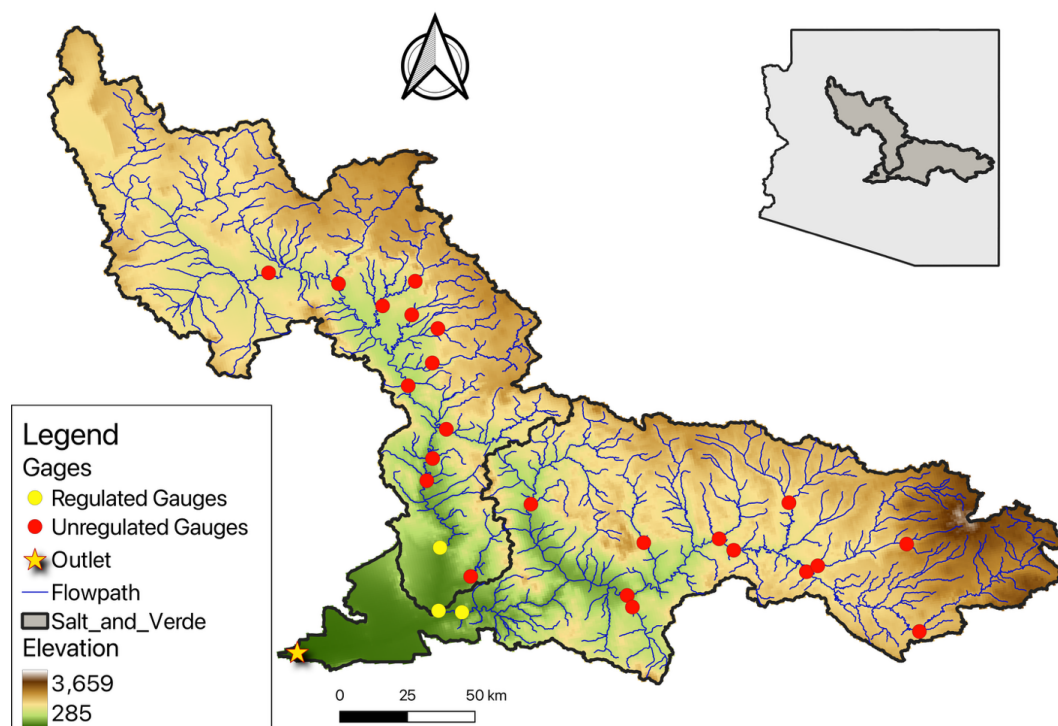


Figure 2. Study area of the Salt–Verde watershed in central Arizona, USA. The figure shows watershed boundaries, elevation distribution, NGen river-network flow paths (Strahler order > 2), and locations of USGS streamflow gauges used in this study. Red markers indicate unregulated gauges used for model training and evaluation, while yellow markers represent gauges affected by reservoir regulation that were excluded from the primary analysis. The inset map shows the location of the watershed within the state of Arizona.

265

266 2.2 Noah-MP Runoff Simulations

267 Runoff inputs for the graph-routing framework were generated using the Noah-MP land surface model
 268 (Niu et al., 2011). Noah-MP simulations were performed over the Salt–Verde river system driven by hourly
 269 Analysis Of Record for Calibration (AORC) meteorological forcing data at approximately 1-km spatial
 270 resolution for the 1981–2022 period (Fall et al., 2023). The AORC dataset provides gridded meteorological
 271 forcing variables including precipitation, temperature, radiation, humidity, wind speed, and surface
 272 pressure, and has been widely used for hydrologic and land-surface modeling applications.

273 The Noah-MP configuration used in this study incorporates an advanced soil hydrology representation
 274 that includes the mixed-form *Richards'* equation solver, representation of preferential-flow, and the *Van*
 275 *Genuchten* soil hydraulic parameterization (Niu et al., 2020a; Niu et al., 2024). Soil and vegetation
 276 characteristics were derived from the STATSGO soil dataset and the USGS 24-category vegetation
 277 classification dataset, while bedrock-depth information was obtained from Shangguan et al. (2017).
 278 Additional Noah-MP configuration options used in this study are summarized in Table 1. Daily surface



runoff (RUNSF) and subsurface runoff (RUNSB) generated by Noah-MP were subsequently used as runoff inputs for both the graph-routing framework and RAPID routing simulations. Identical runoff inputs and simulation periods were used for both routing experiments to ensure a consistent comparison between the physics-based and graph-learning routing frameworks.

Table 1: Noah-MP parameterization schemes used for runoff simulations.

Process	Schemes
Dynamic vegetation	Dynamic vegetation
Canopy stomatal resistance	Ball-Berry type
Moisture factor for stomatal resistance	Plant water stress
Runoff and groundwater	TOPMODEL with groundwater
Surface layer exchange coefficient	Monin-Obukhov similarity theory (MOST)
Radiation transfer	Modified two-stream
Ground snow surface albedo	Two-stream radiation scheme (Wang et al., 2022)
Precipitation partitioning	Wet bulb temperature (Wang et al., 2019)
Lower boundary condition for soil temperature	2-m air temperature climatology at 8m
Snow/soil temperature time scheme	Semi-implicit
Surface evaporation resistance	Sakaguchi and Zeng (2009)
Root profile	Dynamic root (Niu et al., 2020b)
Soil hydrology	Mixed-form Richards equation (Niu et al., 2024)
Soil hydraulics	Van Genuchten parameterization (Niu et al., 2024)
Preferential flow	Dual-permeability representation (Niu et al., 2024)

2.3 RAPID Routing Benchmark

We used a physics-based routing benchmark, namely the *Routing Application for Parallel computation of Discharge* (RAPID; [David et al. \(2011\)](#)) method. RAPID is a vector-based river routing model that applies a matrix formulation of the *Muskingum* routing method to efficiently simulate streamflow propagation across large river networks. The model has been widely used in large-scale hydrologic applications and operational streamflow forecasting systems because of its computational efficiency and ability to preserve flow continuity across connected river reaches ([Agnihotri et al., 2023a](#)).

Daily Noah-MP surface runoff and subsurface runoff generated from the land-surface simulations were used as lateral inflow inputs to the RAPID routing model. A vector-based river network for the *Salt-Verde* watershed was developed using the NHDPlus dataset to maintain consistency between routing experiments and graph-network construction ([Tavakoly, 2017](#)). RAPID simulations were subsequently used as a benchmark for evaluating graph-based streamflow routing performance and routing realism across the river network.

2.4 River-Network Graph Construction

The graph-routing framework was constructed using the NGen hydrofabric representation of the *Salt-Verde* watershed ([Ogden et al., 2026](#)). The NGen hydrofabric represents the river system as a connected set of hydrologically linked flow paths, nexus elements, and catchment divides that explicitly preserve upstream–downstream network topology across the watershed. In this study, the hydrofabric was converted into a directed graph structure in which graph nodes represent routing elements associated with river reaches, and graph edges represent directed hydrologic connectivity between upstream and



304 downstream routing elements (**Figure 3**). The resulting graph preserves the spatial organization and
305 topological structure of the physical river system while enabling graph-based message passing for
306 streamflow routing.

307 The graph was constructed from three outlet systems corresponding to the major downstream outlets
308 within the Salt–Verde watershed: USGS gauges 09511300, 09510000, and 09510200. These outlet
309 systems were merged into a single routing graph containing three disconnected graph components.
310 Directed graph connectivity was represented using upstream-to-downstream edge pairs defining flow
311 propagation through the river network. Gauge locations were mapped onto graph nodes using projected-
312 coordinate matching between USGS gauge locations and NGen routing elements.

313 The graph cache additionally stores node attributes, edge attributes, and runoff-transfer mapping arrays
314 used during graph-routing simulations. These datasets include static physiographic descriptors, hydraulic
315 edge characteristics, and source-to-target runoff-transfer relationships linking gridded Noah-MP runoff
316 fields to graph-routing elements. The final graph contained 4,118 graph nodes and 4,115 directed edges
317 representing the Salt–Verde routing system used throughout all routing experiments.

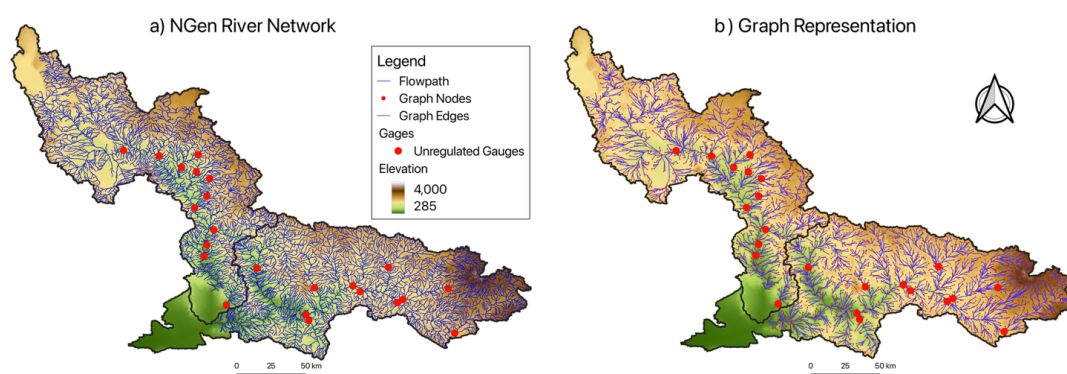


Figure 3. Representation of the Salt–Verde watershed river system and its graph-based routing structure. Panel (a) shows the original NGen hydrofabric flow path network and locations of USGS streamflow gauges used in this study. Panel (b) shows the corresponding directed graph representation used by the routing framework, where hydrologically connected routing elements are represented as graph nodes and directed edges defining upstream–downstream flow connectivity. The graph preserves the spatial organization and topology of the physical river network while enabling graph-based runoff routing and message passing.

318 2.5 Grid-to-Graph Runoff Transfer

319 Runoff generated by Noah-MP is produced on a regular gridded domain, whereas the routing framework
320 operates on an irregular river-network graph derived from the NGen hydrofabric. Consequently, a grid-
321 to-graph runoff-transfer procedure is required to transform gridded runoff fields into graph-node runoff
322 inputs prior to routing (**Figure 4**). In this study, runoff transfer was performed using the NGen divide
323 structure, where runoff generated within each divide was aggregated and assigned to the corresponding
324 routing element within the directed graph network.

325 The runoff-transfer framework uses precomputed source-to-target mapping arrays stored within the
326 graph cache, including $runoff_{source_lat_index}$, $runoff_{target_index}$, and $runoff_{source_weight}$. These
327 arrays define the relationship between active Noah-MP runoff grid cells and NGen hydrologic divides



328 associated with graph nodes. For each divide, runoff contributions from intersecting runoff grid cells were
 329 aggregated using predefined spatial weights, defined by area, to produce node-level runoff inputs
 330 consistent with the routing topology. For runoff grid cells located along divide boundaries, runoff
 331 contributions were assigned to the divide containing the largest fractional coverage of the corresponding
 332 grid cell.

333 Daily Noah-MP surface runoff (RUNSF) and subsurface runoff (RUNSB) were used as dynamic runoff inputs
 334 for the routing framework. For each simulation day, runoff generated on the regular Noah-MP grid was
 335 transferred into divide-based graph-node runoff signals prior to graph routing. The resulting runoff tensor
 336 therefore represents spatially aggregated runoff inputs aligned with the directed river-network graph
 337 used by the graph neural network routing framework.

338 The divide-based runoff-transfer method provides an efficient mechanism for coupling physically
 339 generated gridded runoff fields with graph-based river routing while preserving consistency between
 340 hydrologic catchment structure and river-network connectivity. Unlike many graph-based hydrologic
 341 studies that directly generate runoff at graph nodes or subbasin units, the proposed framework explicitly
 342 bridges gridded land-surface model runoff with topology-aware river-network routing.

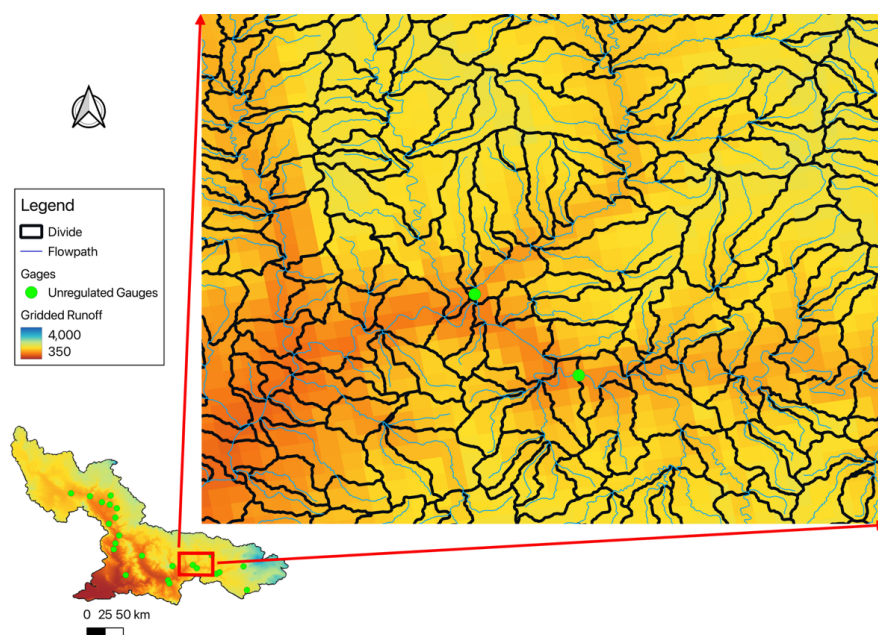


Figure 4 Illustration of the grid-to-graph runoff-transfer procedure used in the routing framework. Black polygons represent NGen hydrologic divides, blue lines indicate river-network flow paths, and the colored raster background represents Noah-MP grids. Runoff generated within each divide is spatially aggregated and transferred to the corresponding graph-routing element prior to graph-based routing. Green markers indicate USGS streamflow gauges used for model training and evaluation.



2.6 Graph Features and Topology Attributes

The graph-routing framework incorporates both node and edge attributes derived from the NGen hydrofabric and associated physiographic datasets to provide physically meaningful information for graph-based routing. Node features describe the local hydrologic, geomorphic, and topologic properties of individual routing elements within the river network. These attributes included river-segment length, local and upstream drainage area, stream order, terrain elevation, terrain slope, impervious fraction, dominant soil type, dominant vegetation type, distance to outlet, upstream contributing-area metrics, and travel-time descriptors representing relative routing behavior throughout the watershed.

Several node attributes were specifically designed to provide information related to hydrologic connectivity and flow-transport behavior within the river system. For example, *totalrainageareaskm*, *upstreamareaatio*, and *upstreamflowpathcount* help distinguish headwater routing elements from downstream integrating reaches, while *distanceoutletm*, *localtraveltimeproxy*, and *traveltimeproxyoutlet* provide relative measures of routing distance and flow-travel behavior across the network. Additional features describing soil and vegetation properties allow the routing framework to incorporate spatial physiographic variability throughout the watershed.

Edge attributes describe hydraulic and geomorphic relationships between connected routing elements and provide physically meaningful information governing runoff propagation between upstream and downstream graph nodes. Edge features included channel length, slope, Manning-type roughness parameters, channel-width descriptors, Muskingum-style hydraulic proxies, travel-time proxies, storage-related metrics, and conveyance descriptors. These attributes allow graph message passing to depend not only on graph topology but also on hydraulic and geomorphic characteristics influencing runoff transport through the river network.

The combination of directed graph topology, static node attributes, and hydraulic edge descriptors enables the graph-routing framework to represent heterogeneous routing behavior across the watershed. Consequently, graph message passing is informed not only by upstream–downstream connectivity but also by local *terrain*, *drainage structure*, *hydraulic characteristics*, and *network position* within the river system. Table 2 summarizes the primary node and edge features used in the graph-routing framework.

Table 2. Graph topology, runoff-transfer, and physical feature variables stored in the graph cache.

Category	Variables	Description
Graph topology	edge_source, edge_target	Directed upstream-to-downstream graph connectivity
Node location / indexing	flat_index, node_x, node_y	Node location on the runoff/forcing grid
Gauge mapping	gauge_id, gauge_index	USGS gauge identifiers and corresponding graph-node indices
Runoff transfer	runoff_source_flat_index, runoff_target_index, runoff_source_weight, runoff_source_fraction	Mapping between Noah-MP runoff grid cells and NGen divide/graph nodes



Runoff-source attributes	elevation, cell_area_m2, distance_to_flowpath_m	Attributes of runoff-contributing grid cells
Node features	node_dem_elevation_m, lengthkm, areasqkm, tot_drainage_areasqkm, order, mean.elevation, mean.slope, mean.impervious, mode.ISLTYP, mode.IVGTYPE, local_length_m, distance_to_outlet_m, local_travel_time_proxy, travel_time_proxy_to_outlet, incremental_area_fraction, upstream_area_ratio, upstream_flowpath_count, upstream_area_km2_topologic, normalized_stream_order, is_outlet_node	Static physiographic, topologic, and routing-position descriptors for each graph node
Edge features	Length_m, So, n, nCC, BtmWidth, TopWidth, TopWidthCC, MusX, MusK, travel_time_proxy, velocity_proxy, manning_travel_time_proxy, inverse_manning_travel_time_proxy, storage_proxy, conveyance_proxy, width_ratio_proxy	Hydraulic, geomorphic, and routing-proxy attributes for each directed edge

372

373 2.7 Graph Neural Network Routing Framework

374 The routing model uses a *Graph Attention Network* (GAT) to perform topology-aware message passing
 375 over the river graph. During message passing, connected upstream routing elements do not contribute
 376 equally. Instead, the attention mechanism learns adaptive weights for graph edges based on node states
 377 and edge attributes such as flow path length, slope, hydraulic roughness/channel descriptors, travel-time
 378 proxies, upstream drainage attributes, and other derived hydrologic features. This allows the model to
 379 learn spatially variable routing influence across headwaters, steep channels, low-gradient reaches, and
 380 downstream integrating segments.

381 For each graph node i , the GAT computes attention coefficients describing the relative influence of
 382 neighboring upstream nodes j during graph message passing

$$383 \quad \alpha_{ij} = \frac{\exp\left(\text{LeakyReLU}\left(a^T [W h_i || W h_j]\right)\right)}{\sum_{k \in \mathcal{N}(i)} \exp\left(\text{LeakyReLU}\left(a^T [W h_i || W h_k]\right)\right)} \quad (\text{Eq 1})$$

384 where h_i and h_j represent node-feature vectors for connected routing elements, W is a learnable linear
 385 transformation, a is the attention vector, and $\mathcal{N}(i)$ denotes neighboring upstream nodes connected to
 386 node i . The resulting attention coefficient α_{ij} represents the learned routing influence of upstream
 387 node j on downstream node i .

388 The updated node representation is then computed through weighted aggregation of neighboring
 389 upstream information:

$$390 \quad h'_i = \sigma\left(\sum_{j \in \mathcal{N}(i)} \alpha_{ij} W h_j\right) \quad (\text{Eq 2})$$

391 where σ denotes a nonlinear activation function. Through this message-passing procedure, runoff and
 392 hydrologic information propagate through the directed river network while allowing the model to learn
 393 spatially varying routing behavior across heterogeneous river segments.

394 Temporal behavior is represented in two complementary ways. First, for each graph node and each
 395 prediction day, the model receives lagged runoff inputs from previous days. For example, a configuration
 396 may use runoff lags such as 0, 1, 2, 3, 7, and 14 days, meaning that the node feature vector for a given day



includes runoff from the current day and selected previous days. The dataset provides a routing-lag context period before each prediction window, so these lagged values come from real runoff data rather than zero padding. Second, when enabled, a temporal Conv1D head is applied after graph message passing to learn short-term temporal smoothing and delayed response patterns across the daily output sequence. Therefore, temporal routing memory is learned from lagged runoff features and temporal convolution, rather than imposed as an explicit mass-conserving hydrologic routing equation

During training, the graph topology, gauge-node mapping, and runoff-transfer mapping remain fixed. The learned parameters are the neural-network weights controlling node-feature transformation, graph attention/message passing, and optional temporal convolution. Streamflow predictions are extracted only at graph nodes mapped to USGS gauge locations using the predefined gauge-index arrays. The resulting predictions are daily routed streamflow estimates informed by Noah-MP runoff, constrained by the NGen river-network structure, and calibrated against observed gauge streamflow.

2.8 Training Strategy and Loss Functions

The graph-routing framework was trained using supervised learning with observed daily USGS streamflow as the prediction target. Training samples were constructed from daily Noah-MP runoff and gauge streamflow using fixed-length temporal windows. In the primary experiments, each sample contained a 180-day streamflow prediction window. An additional routing-lag context period was included before the prediction window so that lagged runoff inputs at the beginning of the sequence were derived from real antecedent runoff values rather than artificial zero padding. The context period was used only to construct lagged runoff features; training losses and reported metrics were computed over the prediction window. In addition to the standard routing configuration, the study evaluated multiple temporal-routing-memory configurations based on different runoff-lag representations. To investigate the influence of antecedent runoff information on graph-routing performance, separate experiments were conducted using lag windows of 3, 7, 14, and 30 days in order. To isolate the contribution of learned temporal sequence processing relative to graph-based spatial routing alone, additional ablation experiments were performed without the temporal convolutional (CNN) head. These experiments allowed systematic evaluation of how temporal-memory representation influences streamflow-routing behavior across the Salt–Verde river network.

Training, validation, and testing datasets were constructed using distribution-balanced temporal block splitting to reduce distributional mismatch between data partitions and provide a robust evaluation of model generalization under heterogeneous hydroclimatic conditions (Figure S1). The continuous streamflow record (1981–2022) was first divided into non-overlapping 180-day temporal blocks, and those blocks were assigned to training, validation, and testing partitions so that observed streamflow distributions were as similar as possible across the splits. This differs from purely chronological splitting and from random day-level sampling. This strategy was adopted because the Salt–Verde watershed exhibits strong interannual hydroclimatic variability, seasonal runoff differences, vegetation and watershed-condition changes over recent decades, and nonstationary streamflow behavior. Consequently, purely random day-level sampling could artificially mix hydrologically distinct periods and introduce unrealistic distribution leakage between training and evaluation datasets. By preserving contiguous temporal blocks while balancing streamflow distributions across the data partitions, the proposed splitting strategy reduces this risk and provides a more robust evaluation of model generalization under heterogeneous hydroclimatic conditions. The resulting training, validation, and testing partitions are summarized in **Figure S1** of the Supplementary Material, which shows the cumulative distribution functions (CDFs) of observed streamflow for each partition.



Model training used masked loss functions so that missing streamflow observations did not contribute to optimization. Losses were computed only at graph nodes corresponding to mapped USGS gauge locations. Several loss formulations were evaluated during model development, including *Mean Squared Error* (MSE), *weighted MSE*, and *Jawad Kling–Gupta Efficiency* (JKGE)-based losses (Jawad et al, 2026).

For the standard masked MSE loss, missing streamflow observations were excluded using a validity mask. For gauge g , the loss was computed as:

$$\text{MSE}_g = \frac{\sum_{t=1}^T m_{g,t} (Q_{g,t}^{\text{pred}} - Q_{g,t}^{\text{obs}})^2}{\sum_{t=1}^T m_{g,t}} \quad (\text{Eq 3})$$

where $Q_{g,t}^{\text{pred}}$ and $Q_{g,t}^{\text{obs}}$ denote predicted and observed streamflow at gauge g and time step t , respectively, and $m_{g,t}$ a binary mask equal to 1 for valid observations and 0 for missing values. The final MSE loss was computed by averaging MSE_g over valid gauges in the batch.

The weighted MSE formulation extends this by including optional gauge or time-dependent weights:

$$\text{WMSE}_g = \frac{\sum_{t=1}^T w_{g,t} (Q_{g,t}^{\text{pred}} - Q_{g,t}^{\text{obs}})^2}{\sum_{t=1}^T w_{g,t}} \quad (\text{Eq 4})$$

where $w_{g,t} = m_{g,t} a_g$ combines the missing-data mask and any optional gauge-specific weighting (a_g). Gauges without a specified curriculum weight were assigned $a_g = 1$, while selected gauges received larger weights between 1.25 and 1.5 to increase their contribution during optimization. This formulation prevents gauges with more valid observations from dominating the optimization and allows selected gauges to receive higher or lower training emphasis.

The framework also evaluated JKGE-based losses. For observed discharge y_g and predicted discharge q_g at gauge g , a benchmark operator $B(\cdot)$ defines the time-varying baselines $b_{y,g} = B(y_g)$ and $b_{q,g} = B(q_g)$, from which the anomaly components $\psi_{y,g} = y_g - b_{y,g}$ and $\psi_{q,g} = q_g - b_{q,g}$ are computed. Next the anomaly correlation, anomaly variability and normalized benchmark mismatch components C_g , V_g and M_g are determined as:

$$C_g = \frac{\psi_{q,g}^T \psi_{y,g}}{|\psi_{q,g}| \cdot |\psi_{y,g}|}$$

$$V_g = \frac{|\psi_{q,g}|}{|\psi_{y,g}|}$$

$$M_g = \frac{|b_{q,g} - b_{y,g}|}{|b_{y,g} - \bar{y}_g \mathbf{1}|}$$

where $\bar{y}_g$ is the mean observed discharge, and $\mathbf{1}$ is a vector of ones. From these, the JKGE score for gauge g is computed as:

$$\text{JKGE}_g = 1 - \sqrt{(C_g - 1)^2 + (V_g - 1)^2 + M_g^2} \quad (\text{Eq 5})$$

The JKGE loss was then defined as: $L_{\text{JKGE}} = 1 - \overline{\text{JKGE}}$, where JKGE is the average JKGE over valid gauges. In the section-average JKGE variants, the benchmark operator $B(\cdot)$ was implemented using fixed non-overlapping temporal sections, so that each section had its own local benchmark mean. This allowed



the loss to evaluate both low-frequency streamflow behavior and anomaly dynamics within each temporal section.

The routing framework also supports curriculum-style gauge training. The model always operates on the complete fixed river-network graph, but the loss was computed only for gauges active within the current curriculum stage. The curriculum progressively increased routing complexity by beginning with upstream and headwater gauges and gradually incorporating more downstream and hydrologically integrated gauges. This staged strategy was intended to stabilize optimization by first learning simpler local routing behavior before requiring the model to reproduce more complex downstream routing responses.

Model optimization was performed using backpropagation on the fixed directed river-network graph. During training, graph topology, runoff-transfer mappings, gauge-node mappings, and graph feature definitions remained fixed throughout all experiments. The learned parameters consisted of neural-network weights controlling node-feature transformations, graph message passing and attention weighting, and optional temporal convolution operations. Stage-best checkpointing and validation-based model selection were used to preserve stable routing solutions and reduce destructive transitions between curriculum-training stages.

2.9 Evaluation Metrics

Model performance was evaluated using multiple hydrologic metrics designed to assess streamflow *magnitude, temporal dynamics, variability, and routing consistency* across the *Salt–Verde* river system. Performance evaluation focused not only on prediction accuracy at individual gauges, but also on the ability of the routing framework to reproduce physically meaningful upstream–downstream flow behavior throughout the directed river network. Routing performance was evaluated independently at each USGS gauge using observed daily streamflow records and corresponding routed streamflow predictions.

The primary evaluation metrics included the *Kling–Gupta Efficiency* (KGE). The KGE metric is defined as:

$$KGE = 1 - \sqrt{\{(1 - \alpha)^2 + (1 - \beta)^2 + (1 - \rho)^2\}} \quad (\text{Eq 6})$$

where ρ is the Pearson correlation coefficient between observed and predicted streamflow, α is the variability ratio, and β is the bias ratio.

In this study, we report the KGE skill score (KGE_{ss}), which provides a normalized version of KGE relative to a benchmark model, Following the formulation discussed by *Knoben et al. (2019)*:

$$KGE_{ss} = 1 - \frac{1 - KGE}{\sqrt{2}} \quad (\text{Eq 7})$$

Using this formulation ensures that $KGE_{ss} \leq 0$ means that the model performs no better than a trivial benchmark model that corresponds to simulated values at every time step being set to the observed long-term-mean, while a perfect model yields $KGE_{ss} = 1$. All reported evaluation metrics are computed over the independent test period. Additional diagnostics including *Root-Mean-Square Error* (RMSE), and *Percent Bias* (PBIAS) were also computed for each gauge. To quantify improvement relative to the RAPID benchmark, we additionally computed the KGE_{ss} improvement as

$$\Delta KGE_{ss} = KGE_{ss}^{model} - KGE_{ss}^{RAPID} \quad (\text{Eq 8})$$

where positive values indicate that the evaluated model outperforms RAPID. Percent improvement relative to RAPID was computed



511

$$512 \quad \% \Delta KGE_{ss} = 100 \times \frac{KGE_{ss}^{model} - KGE_{ss}^{RAPID}}{|KGE_{ss}^{RAPID}|} \quad (Eq\ 8)$$

513 Because KGE_{ss}^{RAPID} can be zero or negative at some gauges, percent improvements were interpreted
 514 cautiously and were not emphasized when the RAPID denominator was near zero.

515 Since a primary objective of this study was to evaluate graph-based routing behavior relative to a widely
 516 used physics-based routing framework, all graph-routing simulations were directly compared against
 517 RAPID routing simulations generated using the same Noah-MP runoff forcing inputs. Because both routing
 518 systems used identical runoff inputs, differences between routed streamflow predictions primarily reflect
 519 differences in routing representation rather than runoff-generation uncertainty. This configuration
 520 allowed the study to isolate graph-based routing behavior and evaluate whether topology-aware graph
 521 learning can reproduce or improve upon physically based routing behavior.

522 3 Results

523 3.1 Overall Routing Performance

524 Results show that the graph-based routing framework demonstrates strong streamflow-routing skill
 525 across the *Salt–Verde* watershed by consistently outperforming the RAPID routing benchmark at most of
 526 the evaluation gauge locations. Performance comparisons across routing configurations show that graph-
 527 based routing substantially improves streamflow representation relative to RAPID while preserving
 528 physically meaningful upstream–downstream routing structure. **Figure 5** summarizes KGE_{ss}
 529 improvements relative to RAPID for all routing configurations, including different temporal-routing-
 530 memory experiments and loss-function formulations.

531 Among all evaluated experiments, the best-performing configuration corresponds to the 14-day lag
 532 weighted-MSE experiment (*lag14_{w,mse}*), which achieved the highest mean KGE_{ss} value (0.70) and the
 533 highest median KGE_{ss} value (0.72) across the evaluation gauges (**Table 3**). Several additional weighted-
 534 MSE configurations also ranked among the strongest-performing experiments, indicating that graph-
 535 based routing performance remained robust across multiple training configurations. Although the 14-day
 536 lag produced the best results for the *Salt–Verde* watershed, the optimal temporal-memory representation
 537 is likely basin dependent and influenced by factors such as watershed size, flow-regime characteristics,
 538 snowmelt processes, and subsurface storage dynamics. Consequently, temporal-memory sensitivity
 539 analyses similar to those conducted here may be necessary when applying the framework to other river
 540 systems.

541 JKGE-based training configurations produced more variable routing behavior across the watershed.
 542 Although several JKGE experiments achieved competitive routing skill, the standard *lag14_{j,kge}*
 543 configuration showed lower overall performance than the *weighted-MSE* and *standard-MSE* experiments.
 544 Nevertheless, even the weaker JKGE configurations still produced predominantly positive KGE_{ss}
 545 improvements relative to RAPID, indicating that the graph-routing framework remained competitive
 546 across nearly all gauges regardless of loss formulation.

547 **Figure 5** demonstrates that nearly all routing configurations produce positive KGE_{ss} improvements
 548 relative to RAPID across essentially the entire gauge network. For most experiments, all gauges show
 549 positive improvement over RAPID. Even the *lag14_{j,kge}* configuration, which exhibits the weakest overall
 550 performance among the evaluated experiments, produces only a single gauge with slight negative KGE_{ss}
 551 change relative to RAPID. The consistent positive improvement distributions indicate that the graph-



routing framework robustly improves routing behavior across a wide range of hydrologic conditions, drainage areas, and river-network structures within the Salt–Verde watershed.

For the best-performing configuration (lag14_wmse), the mean KGE_{ss} increased from -0.29 for RAPID to 0.70 for RiverGraphNet, and all 22 gauges with valid RAPID comparisons exhibited positive improvement. A one-sided paired Wilcoxon signed-rank test comparing gauge-level KGE_{ss} values between RiverGraphNet and RAPID indicates that the improvement was highly significant ($p = 2.38 \times 10^{-7}$), providing statistical support that the observed performance gains are unlikely to arise from random variation across gauges.

Additional examination of the gauge-level improvement distributions using violin plots (Figure S2) reveals patterns consistent with the boxplot results shown in Figure 5. The distributions remained predominantly positive across routing configurations and does not exhibit substantial multimodal structure, indicating that the observed performance gains were broadly distributed throughout the gauge network rather than being driven by a small number of highly improved locations.

To provide additional context beyond the RAPID benchmark, RiverGraphNet performance was also compared against the National Water Model (NWM) streamflow simulations (Figure 6). RAPID was selected as the primary benchmark throughout this study because it generally achieved higher KGE_{ss} values and more stable performance across the evaluation network than NWM. Consequently, RAPID represents the more challenging benchmark for assessing routing performance within the Salt–Verde watershed. RiverGraphNet nevertheless outperforms both RAPID and NWM across most evaluation gauges, indicating that the observed performance gains are not simply relative to a weak benchmark but extend to a widely used operational hydrologic modeling framework. This comparison provides additional confidence that the improvements reflect meaningful advances in routing representation rather than advantages relative to a particular benchmark model.

The overall results suggest that graph-based routing provides a flexible, robust, and physically meaningful alternative to traditional routing approaches when physically-generated runoff inputs and physically-structured river-network topology are incorporated into the learning framework. The strongest routing performance emerges from configurations that combined graph-based spatial message passing, antecedent runoff memory, and balanced gauge-aware optimization within the directed routing graph framework.

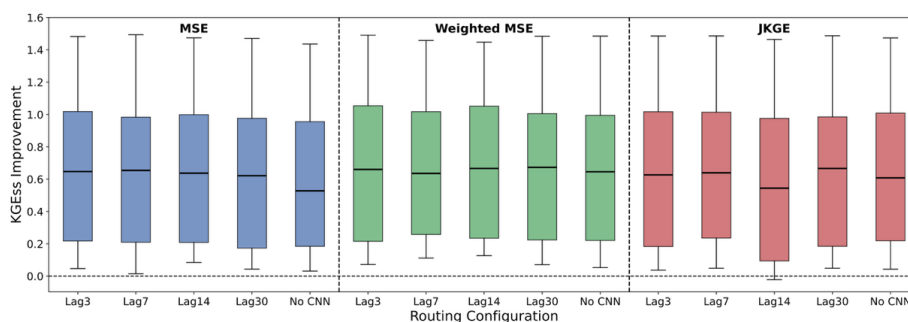


Figure 5. Distribution of KGE_{ss} improvements relative to the RAPID routing benchmark across all graph-routing configurations evaluated in this study. Boxplots summarize gauge-level KGE_{ss} improvement distributions for different temporal-routing-memory configurations (3-, 7-, 14-, and 30-day runoff lags), loss formulations (MSE, weighted MSE, and JKGE), and experiments without the temporal convolutional (CNN) head.



Table 3. Summary statistics of gauge-level KGE_{ss} values for RAPID and all graph-routing configurations across the Salt–Verde watershed. Reported statistics include the mean, median, minimum, maximum, and standard deviation of KGE_{SS} computed across all evaluation gauges. Routing configurations include different temporal-routing-memory experiments, loss-function formulations, and ablation experiments without the temporal convolutional (CNN) head. The weighted-MSE configurations generally produced the highest overall routing performance and the most stable gauge-level behavior.

scenario	mean	median	minimum	maximum	standard deviation
RAPID	-0.29	-0.01	-4.88	0.65	1.30
lag14_wmse	0.70	0.72	0.34	0.84	0.11
lag14_no_cnn_jkge	0.67	0.71	0.30	0.81	0.12
lag7_jkge	0.68	0.71	0.32	0.83	0.11
lag14_no_cnn_wmse	0.68	0.71	0.33	0.82	0.12
lag7_wmse	0.69	0.71	0.38	0.84	0.11
lag3_wmse	0.69	0.69	0.30	0.84	0.12
lag3_mse	0.68	0.69	0.29	0.82	0.11
lag14_mse	0.67	0.69	0.32	0.83	0.13
lag30_wmse	0.68	0.69	0.31	0.86	0.13
lag3_jkge	0.67	0.68	0.31	0.84	0.12
lag7_mse	0.66	0.68	0.30	0.82	0.12
lag14_no_cnn_mse	0.65	0.68	0.30	0.83	0.12
lag30_jkge	0.65	0.67	0.32	0.83	0.12
lag30_mse	0.66	0.67	0.33	0.85	0.11
lag14_jkge	0.61	0.64	0.27	0.80	0.13

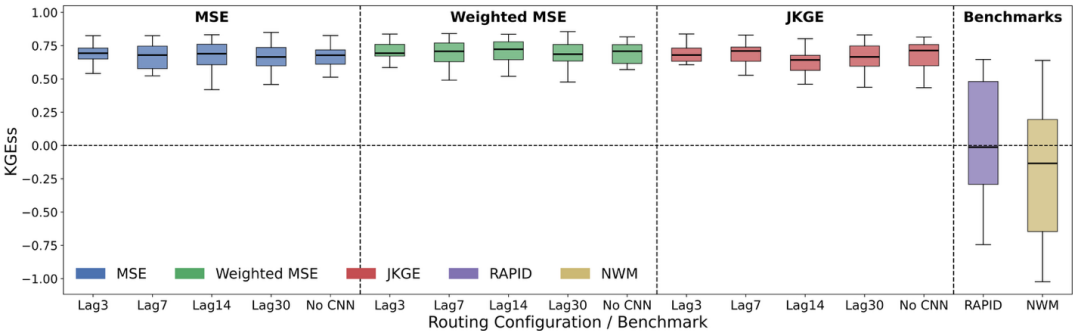




Figure 6. Distribution of KGE_{ss} across evaluation gauges for all RiverGraphNet routing configurations compared with RAPID and National Water Model (NWM) benchmarks. RiverGraphNet configurations consistently achieve higher median performance and smaller performance variability than both benchmark systems. The comparison demonstrates that performance gains are not limited to improvements over RAPID but also extend to a widely used operational hydrologic modeling framework.

590

591 3.2 Spatial Routing Performance Across the Watershed

592 Spatial evaluation of routing performance reveals substantial variability in streamflow-routing skill across
593 the *Salt–Verde* watershed for both the RAPID and graph-based routing frameworks. **Figure 7** compares
594 gauge-level KGE_{ss} values for the RAPID benchmark and the best-performing graph-routing configuration
595 (*lag14_{wmse}*). The spatial distributions demonstrate that routing performance is strongly influenced by
596 *watershed position, drainage structure, and local hydrologic characteristics*.

597 The RAPID routing benchmark produces highly variable routing performance across the watershed, with
598 several gauges exhibiting relatively low or even negative KGE_{ss} values. The weakest RAPID performance
599 generally occurs in smaller headwater tributaries and intermediate nested basins characterized by
600 steeper terrain and more heterogeneous runoff-generation behavior. These regions often exhibit highly
601 nonlinear hydrologic responses, short runoff concentration times, and stronger sensitivity to localized
602 precipitation variability, which may be difficult to fully represent using fixed-parameter routing
603 approaches.

604 In contrast, the graph-based routing framework produced consistently positive and spatially stable routing
605 performance across nearly all evaluation gauges. The best-performing graph-routing configuration
606 substantially reduced the occurrence of low-skill gauges and produced improved routing behavior
607 throughout both upstream tributaries and downstream integrating river reaches. The graph-routing
608 framework achieved particularly strong performance in mountainous and hydrologically complex regions
609 where upstream connectivity, local drainage structure, and variable flow-transport behavior play
610 important roles in streamflow propagation.

611 **Figure 8** shows the spatial distribution of KGE_{ss} improvements relative to RAPID. Gains are not uniform,
612 with the strongest benefits being concentrated in *headwater* and *intermediate* tributaries. These
613 improvements suggest that topology-aware graph message passing and adaptive attention weighting
614 allows the routing framework to better represent heterogeneous runoff propagation and nonlinear
615 upstream–downstream interactions compared to the fixed routing representation used in RAPID.

616 The spatial improvement patterns additionally indicate that graph-based routing is able to effectively
617 integrate physically meaningful node and edge attributes describing river geometry, drainage structure,
618 and hydraulic-routing proxies. Because the framework explicitly represents river-network connectivity
619 through directed graph topology, upstream runoff contributions can influence downstream routing
620 behavior through learned spatial interactions rather than fixed routing equations alone. This flexibility
621 likely contributes to the improved routing behavior observed across complex tributary systems and nested
622 watershed structures within the *Salt–Verde* river network.

623 Although graph-based routing generally outperforms RAPID throughout the watershed, the magnitude of
624 improvement varies spatially across gauges. Smaller improvements at several downstream gauges may
625 reflect the increased influence of integrated watershed-scale dynamics, routing accumulation uncertainty,
626 and potential anthropogenic flow regulation effects that are not fully represented within the current
627 graph-routing framework. Nevertheless, the consistently positive improvement patterns demonstrate



628 that graph-based routing provides a robust and spatially transferable alternative for routing physically
629 generated runoff through complex river-network systems.

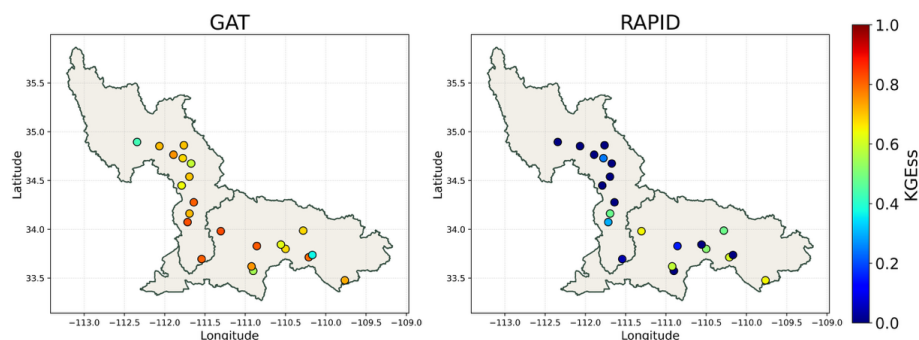


Figure 7. Spatial distribution of gauge-level KGEss values across the Salt-Verde watershed for (a) the RAPID routing benchmark and (b) the best-performing graph-routing configuration (lag14_wmse). Circle colors represent KGEss values at each USGS evaluation gauge. The graph-based routing framework produced more spatially consistent and uniformly positive routing performance across the watershed relative to RAPID, particularly within upstream and intermediate tributary systems.

630

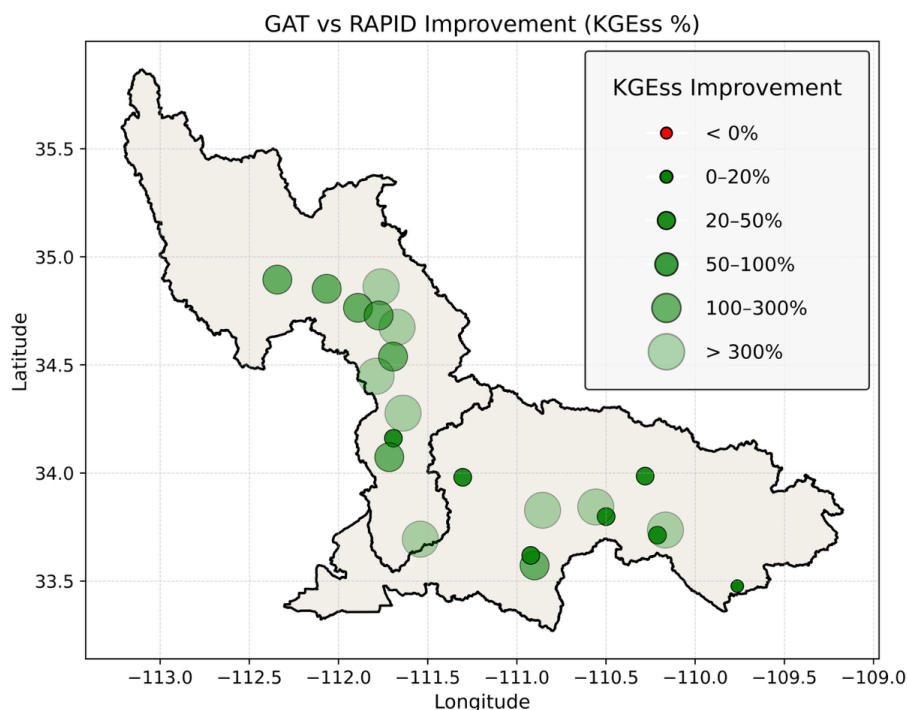




Figure 8. Spatial distribution of KGEss improvement relative to RAPID for the best-performing graph-routing configuration (lag14_wmse). Positive values indicate improved routing performance of the graph-based framework compared to the RAPID routing benchmark. Circle size and color intensity increase with larger positive improvement magnitude. The strongest improvements generally occurred within upstream and intermediate tributaries characterized by complex river-network topology and heterogeneous hydrologic behavior.

631

632 3.3 Influence of Temporal Routing Memory

633 The influence of temporal-routing-memory representation was evaluated using multiple lag
634 configurations and temporal-processing experiments. To investigate how antecedent runoff information
635 influences graph-based streamflow routing behavior, routing experiments were conducted using runoff-
636 lag windows of 3, 7, 14, and 30 days. Additional ablation experiments were performed without the
637 temporal convolutional (CNN) head to isolate the contribution of learned temporal sequence processing
638 relative to graph-based spatial routing alone. **Figure 5** and **Table 3** summarize routing performance across
639 all temporal-routing-memory configurations.

640 The results indicate that the routing performance is relatively insensitive to the selected runoff-lag
641 representation over the range of lag windows evaluated. Differences among lag configurations are
642 generally modest, with most experiments producing similar gauge-level KGE_{ss} distributions (**Figure 5**).
643 Nevertheless, the 7-day and 14-day lag experiments consistently ranked among the strongest-performing
644 configurations. In particular, the 14-day lag weighted-MSE configuration (*lag14_wmse*) achieves the
645 highest mean and median KGE_{ss} values among all evaluated experiments.

646 Although differences among lag configurations are relatively small, the consistently strong performance
647 of the intermediate-lag experiments suggests that antecedent hydrologic information over multi-day
648 timescales may provide useful routing context within the *Salt–Verde* watershed. Streamflow generation
649 in the basin is influenced by the travel time of snowmelt runoff, subsurface-flow persistence, and multi-
650 day runoff accumulation from tributary systems. Lag windows spanning approximately one to two weeks
651 therefore appear sufficient to capture much of the antecedent information relevant for daily routing
652 prediction.

653 Extending the lag window from 14 to 30 days did not produce additional performance gains despite
654 providing substantially larger antecedent runoff context. This suggests that, for the *Salt–Verde* watershed,
655 incorporating runoff information beyond approximately two weeks provides limited additional benefit for
656 routing performance. However, the optimal temporal-memory representation is likely basin dependent
657 and may vary with watershed size, river-network length, flow-regime characteristics, and dominant
658 hydrologic processes. The similarity of the results across lag configurations further indicates that the
659 graph-routing framework remains robust across a range of temporal-memory representations.

660 The “no-CNN” ablation experiments demonstrate that the graph-routing framework remains highly
661 competitive even without the temporal convolutional processing head, with several experiments
662 achieving routing performance comparable to, or exceeding, many of the CNN-enabled configurations.
663 These results indicate that much of the routing information is already captured through graph-based
664 spatial message passing together with lagged runoff inputs. The results suggest that the temporal
665 convolutional head serves mainly as an additional refinement mechanism for short-term temporal
666 smoothing and delayed-response representation, rather than as the dominant source of routing memory
667 within the framework.



Overall, the temporal-routing-memory experiments indicate that incorporating antecedent runoff information is beneficial for graph-based routing, but that routing performance remains relatively stable across the range of lag windows evaluated. The results further suggest that physically structured graph topology and lagged runoff inputs together capture much of the runoff-propagation behavior required for streamflow prediction within the *Salt-Verde* river network.

3.4 Influence of Loss Functions

The influence of objective functions on graph-routing performance was evaluated by comparing models trained using *standard MSE*, *weighted MSE*, and *JKGE-based loss* formulations. While the previous section focused on temporal-routing-memory representation, this section examines how different training objectives shape routing behavior and hydrologic prediction characteristics. **Figure 5** and **Table 3** summarize watershed-wide performance differences across routing configurations, while representative event-scale hydrograph comparisons in **Figure 9** provide insight into how the loss formulations influence specific hydrologic behaviors.

Weighted-MSE-based configurations consistently produced the strongest overall routing performance across the watershed. Multiple *weighted-MSE* experiments ranked among the top-performing configurations, with the *lag14_{wmse}* experiment achieving the highest overall mean and median $KGE_{\{ss\}}$ values (**Table 3**). This behavior suggests that gauge-balanced weighted optimization improves routing robustness across the heterogeneous gauge network by preventing the optimization from becoming dominated by a small subset of gauges with larger flows, longer records, or stronger gradients. Because the *weighted-MSE* formulation combines missing-data masking with optional gauge-specific weighting, the training process remained spatially balanced while allowing additional emphasis on strategically important gauges.

Event-scale hydrograph comparisons (Figure 9) reveal clear behavioral differences among the loss formulations. Models trained using standard MSE and weighted MSE generally reproduces event timing and peak magnitudes more effectively than the JKGE-based configuration, contributing to their superior aggregate performance metrics. In contrast, the JKGE-based configuration often produced closer agreement with observed recession behavior and low-flow recovery following major runoff events. RAPID frequently exhibited delayed response and substantial overestimation during several large runoff events. This suggests that squared-error optimization tends to prioritize reducing errors during high-flow conditions, where absolute deviations are largest, while placing less emphasis on accurately representing recession dynamics and sustained low-flow behavior.

To further quantify these differences, hydrologic-signature metrics were computed for each routing framework (**Figure S3**). Consistent with the hydrograph comparisons, the loss functions emphasized different aspects of watershed response. The weighted-MSE configuration generally produces smaller errors for mean flow (7.7%), high-flow magnitude (18.7%), and peak flow (6.1%), substantially outperforming RAPID, which exhibits errors of 52.5%, 56.2%, and 293.7%, respectively. In contrast, the JKGE configuration produces the lowest errors for low-flow magnitude (38.8% versus 77.3% for weighted MSE), recession behavior (91.9% versus 99.0%), and baseflow index (18.9% versus 27.0%). These results support the event-scale hydrograph analysis by showing that JKGE training better preserves selected low-flow and recession characteristics, whereas weighted-MSE training tends to reduce errors in mean-flow, high-flow, and peak-flow signatures. The results highlight tradeoffs among loss formulations rather than a universally superior objective function.

In contrast, *JKGE-based* training produces a different routing behavior profile. Although JKGE configurations generally achieves lower overall $KGE_{\{ss\}}$ performance than the MSE-based formulations, both the hydrograph comparisons and hydrologic-signature analysis indicate that JKGE often produces



713 closer agreement with observed recession behavior, low-flow recovery, and baseflow characteristics
714 following major events (**Figure 9**). Because the JKGE objective explicitly incorporates anomaly correlation,
715 variability consistency, and benchmark mismatch rather than relying solely on squared-error
716 minimization, the resulting routing behavior tends to better preserve selected hydrograph-shape
717 characteristics and temporal variability structure. However, this broader optimization objective may also
718 complicate training across highly heterogeneous routing conditions, contributing to weaker aggregate
719 predictive performance.

720 These results indicate that loss-function choice influences not only overall routing skill but also the
721 hydrologic behavior emphasized during optimization. *Weighted-MSE* formulations appear most effective
722 for maximizing overall predictive skill and peak-event routing performance, whereas *JKGE-based*
723 objectives may better preserve recession dynamics and low-flow behavior in selected situations. This
724 tradeoff highlights the importance of aligning optimization objectives with the hydrologic behaviors most
725 relevant to the intended routing application.

726

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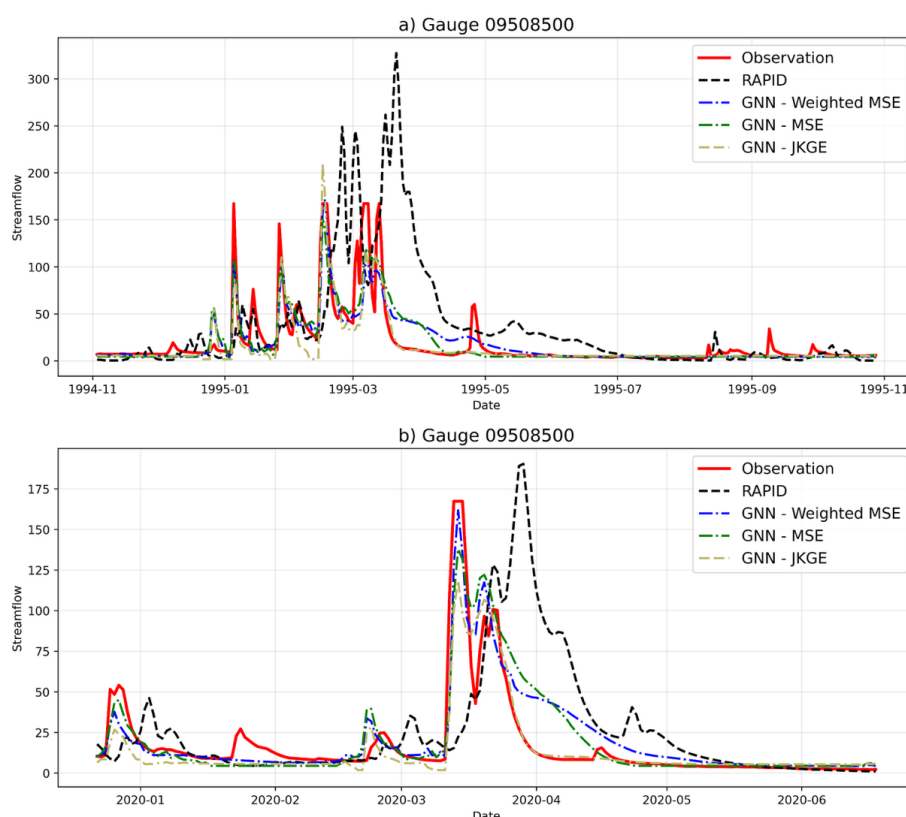


Figure 9. Representative event-scale hydrograph comparisons illustrating the influence of training loss functions on routing behavior at USGS gauge 09508500. Results are shown



for observed streamflow, RAPID routing, and graph-routing models trained using weighted MSE, standard MSE, and JKGE objectives.

728 3.5 Hydrologic Behavior and Event-Scale Routing Evaluation

729 In addition to aggregate performance metrics, the hydrologic realism of the routing framework was
730 evaluated using representative event-scale hydrographs and flow-duration-curve (FDC) analysis across
731 multiple gauges spanning different portions of the *Salt–Verde* watershed. While KGE_{ss} -based metrics
732 provide an overall measure of predictive skill, hydrograph and FDC analyses provide complementary
733 insight into the ability of the routing models to reproduce hydrologically meaningful behaviors, including
734 *event timing, peak attenuation, recession dynamics, and long-term streamflow distributions*.

735 **Figure 10** compares representative event-scale hydrographs at four evaluation gauges spanning different
736 hydrologic settings within the watershed. Across all locations, the graph-based routing framework
737 produced substantially more realistic streamflow responses than the RAPID benchmark. In the
738 representative events examined, RAPID exhibits delayed peak timing, exaggerated event magnitudes, and
739 prolonged recession tails following major runoff events. These behaviors are particularly evident at
740 intermediate and downstream gauges, where routing accumulation errors propagate into substantial
741 overestimation of peak discharge and unrealistically persistent post-event flows.

742 In contrast, the graph-based routing framework reproduced observed hydrograph timing and event
743 magnitude substantially more accurately across the evaluated gauges. The best-performing *weighted-*
744 *MSE* configuration captured rapid event responses in flashy tributaries while also maintaining
745 hydrologically plausible attenuation behavior in larger integrating basins. Improvements are especially
746 pronounced during multi-peak runoff events, where the graph-routing framework more effectively
747 reproduces the timing and separation of sequential runoff responses. Some smoothing and elevated
748 recession behavior remains in selected cases, but the graph-based routing framework consistently
749 reduces the extreme overestimation and delayed routing behavior observed in RAPID.

750 Flow-duration-curve analysis further confirms the improved hydrologic realism of the graph-based routing
751 framework (Figure 11). Across representative gauges, RAPID frequently overestimates high-flow
752 magnitudes and exhibited prolonged recession behavior, producing unrealistic streamflow distributions
753 relative to observations. These deviations should be interpreted in the context of the RAPID configuration
754 used in this study, which relied on an existing CONUS-scale routing parameterization and was not
755 recalibrated specifically for the *Salt–Verde* watershed. Therefore, the comparison should not be
756 interpreted as a general limitation of RAPID, but rather as evidence that fixed large-scale routing
757 parameterizations and standard routing assumptions may require local adaptation or modification to
758 better represent the full range of streamflow conditions in heterogeneous semi-arid river systems.

759 In contrast, the graph-based routing configurations reproduce observed streamflow distributions much
760 more consistently across high-, intermediate-, and low-flow conditions. The *weighted-MSE* configuration
761 generally provides the closest overall agreement with observed FDC behavior, particularly across the mid-
762 range and high-flow portions of the distribution. The *JKGE-based* configuration occasionally produces
763 improved low-flow agreement, consistent with the recession-behavior patterns discussed in Section 3.4,
764 but generally shows weaker agreement during higher-flow conditions. The improved FDC behavior
765 indicates that the graph-based routing framework better preserves long-term hydrologic variability while
766 maintaining physically meaningful event-scale routing behavior.

767 Taken together, the hydrograph and FDC analyses demonstrate that the graph-based routing framework
768 improves not only aggregate performance metrics but also hydrologically meaningful streamflow
769 behavior across diverse watershed conditions. By combining physically generated runoff inputs with
770 topology-aware graph routing, the framework more effectively represents *peak timing, event*



771 *attenuation, recession dynamics, and long-term flow distributions* than the conventional RAPID routing
772 benchmark.
773

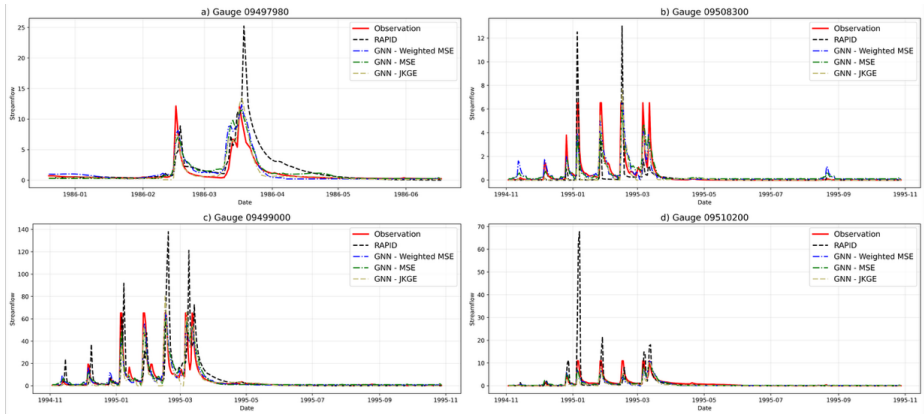


Figure 10. Representative event-scale hydrograph comparisons across four USGS evaluation gauges within the Salt-Verde watershed, showing observed streamflow, RAPID routing, and graph-based routing results using weighted MSE, standard MSE, and JKGE training objectives. The graph-based routing framework generally reproduces event timing, peak magnitude, and recession behavior more realistically than RAPID across diverse hydrologic settings. In the representative cases examined, RAPID frequently exhibits delayed peak response, exaggerated discharge magnitudes, and prolonged recession tails, particularly during multi-peak runoff events and at hydrologically integrated downstream locations.

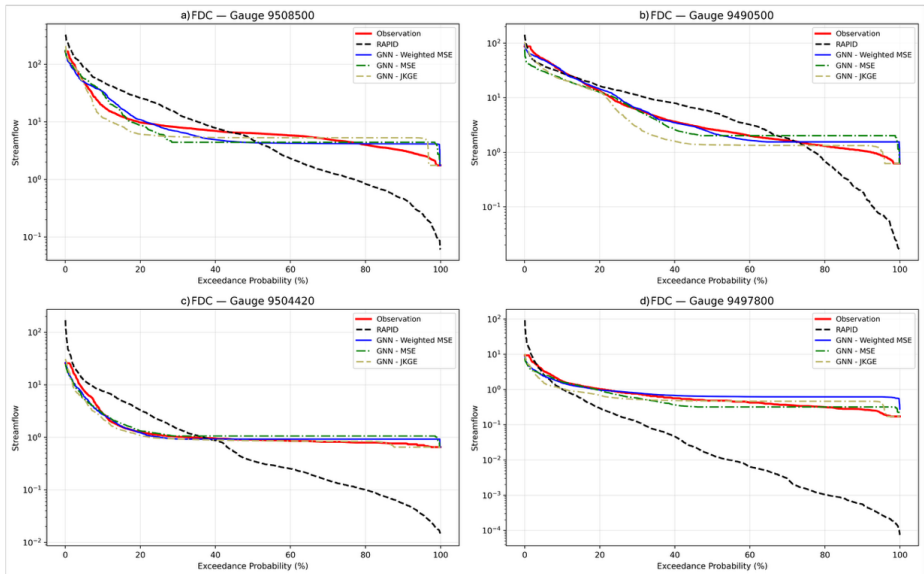




Figure 11. Flow-duration-curve (FDC) comparisons at four representative USGS gauges within the Salt–Verde watershed for observed streamflow, RAPID routing, and graph-based routing configurations trained using weighted MSE, standard MSE, and JKGE objectives. The graph-based routing framework more consistently reproduces observed streamflow distributions across high-, intermediate-, and low-flow conditions compared to RAPID. Weighted-MSE configurations generally provide the closest overall agreement with observed FDC behavior, while JKGE-based training occasionally improves low-flow representation through sharper recession behavior.

775

776 3.6 Hydrologic Plausibility and Streamflow–Runoff Consistency

777 In addition to predictive performance metrics and event-scale hydrograph evaluation, the
778 hydrologic plausibility of the routing frameworks was examined using a watershed-scale streamflow–
779 runoff consistency diagnostic. For each evaluation gauge, the ratio between streamflow and cumulative
780 upstream Noah-MP runoff was computed and compared for RAPID, the graph-based routing framework,
781 and observations (**Figure S4**). This diagnostic provides a relative measure of how well the routed
782 streamflow compares with the runoff volume generated upstream of each gauge and offers insights into
783 whether the routing behavior remains hydrologically consistent across the watershed.

784 The RAPID routing benchmark produces streamflow-to-upstream-runoff ratios clustered near unity across
785 most evaluation gauges, reflecting the expected conservative behavior of a physics-based routing
786 framework that primarily redistributes runoff through the river network without introducing substantial
787 transformation of the upstream runoff signal. This behavior indicates internally consistent routing relative
788 to the Noah-MP runoff forcing, although agreement with observed watershed response depends on the
789 realism of the underlying runoff-generation inputs.

790 In contrast, observed streamflow exhibits substantially greater spatial variability in streamflow–runoff
791 ratios across the *Salt–Verde* watershed. Many gauges show ratios below unity, while others exhibit more
792 moderate deviations depending on watershed location and drainage structure. These deviations likely
793 reflect the combined influence of *runoff-generation uncertainty* in Noah-MP, *transmission losses*,
794 *evapotranspiration effects*, *groundwater interactions*, *anthropogenic regulation*, and other *watershed-*
795 *scale hydrologic processes* that are not explicitly represented in the runoff-routing comparison.

796 The graph-based routing framework produces streamflow–runoff ratios that more closely resemble the
797 spatial variability observed in the gauge record than the nearly uniform conservative behavior exhibited
798 by RAPID (**Figure S4**). In particular, the graph-based framework captures the heterogeneous spatial
799 structure of runoff–streamflow relationships across both headwater and downstream basins, suggesting
800 that the learned routing transformations better reproduce effective watershed response behavior rather
801 than simply preserving the upstream runoff signal through fixed conservative routing.

802 These results suggest that graph-based routing improves not only predictive skill but also the realism of
803 watershed-scale runoff–streamflow relationships relative to observations. However, this diagnostic
804 should not be interpreted as a strict mass-conservation evaluation, since discrepancies between observed
805 streamflow and upstream Noah-MP runoff may reflect both routing behavior and biases in the runoff-
806 generation model itself. Nevertheless, the analysis provides an informative hydrologic plausibility check,
807 although it does not by itself distinguish routing-process improvements from compensation for biases in
808 the Noah-MP runoff forcing.

809



810 3.7 Interpretation of Learned Routing Behavior

811 To better understand the routing behavior learned by RiverGraphNet, we analyzed the spatial
812 distribution of graph-attention coefficients and their relationships with physical river-network
813 characteristics. **Figure S5a** shows the mean attention coefficients aggregated across the *Salt-Verde* river
814 network. Attention values exhibited substantial spatial variability rather than remaining uniformly
815 distributed throughout the network, indicating that the model learned heterogeneous routing influence
816 among connected river reaches. This behavior suggests that upstream contributions were not treated
817 equally during message passing and that the routing framework selectively emphasized specific flow
818 pathways within the watershed.

819 Relationships between attention coefficients and physical routing attributes are shown in **Figure S5b**.
820 Mean attention exhibited positive associations with channel width metrics, including both top width ($p =$
821 0.247) and bottom width ($p = 0.247$), as well as a weaker positive relationship with travel-time proxy ($p =$
822 0.169). In contrast, attention was negatively associated with channel slope ($p = -0.190$) and Manning
823 roughness ($p = -0.244$), while channel length showed little relationship with attention ($p = 0.043$). These
824 patterns indicate that the model preferentially assigned greater routing influence to wider, lower-
825 gradient, and lower-roughness river reaches, which generally correspond to more hydraulically efficient
826 flow pathways within the network.

827 Additional insight is provided by the stream-order analysis shown in **Figure S5c**. First-order reaches
828 exhibited the highest median attention values, while attention generally decreased with increasing stream
829 order. This pattern suggests that the routing framework placed greater emphasis on information
830 originating from headwater tributaries and progressively distributed that information through
831 downstream portions of the network. Because headwater reaches represent the locations where runoff
832 signals first enter the river system, the elevated attention assigned to these reaches suggests that accurate
833 propagation of headwater runoff is a critical control on downstream routing performance. The decreasing
834 attention with stream order further indicates that the model progressively integrates information as flow
835 accumulates downstream through the river hierarchy.

836 To place the stream-order results in the context of the underlying river-network structure, we additionally
837 examined network topology as a function of stream order (**Figure S6**). The number of graph edges does
838 not increase monotonically toward lower stream orders, with second-order reaches representing the
839 most common stream-order class in the network. Similarly, upstream contributing area increases
840 systematically with stream order, indicating that higher-order reaches integrate progressively larger
841 portions of the watershed. Therefore, the elevated attention assigned to first-order reaches cannot be
842 explained solely by network abundance or drainage-area magnitude. Instead, the results suggest that
843 RiverGraphNet preferentially emphasizes headwater runoff signals despite their relatively small
844 contributing areas, highlighting the importance of accurately propagating local runoff generation through
845 the downstream routing hierarchy. This behavior further suggests that routing errors originating in
846 headwater tributaries may accumulate downstream, making accurate representation of upstream runoff
847 signals particularly important for overall routing performance.

848 To investigate which learned routing behaviors were most strongly associated with performance gains,
849 gauge-level reductions in RMSE relative to RAPID were compared against several attention-derived
850 routing metrics (**Table 4**). The strongest relationships were observed for attention-weighted channel-
851 width metrics, with correlations of $p = 0.736$ for top width and $p = 0.725$ for bottom width. Moderate
852 relationships were also observed for concentration of attention within dominant upstream pathways ($p =$
853 0.545) and attention-weighted travel-time metrics ($p = 0.502$). These results indicate that the largest
854 improvements over RAPID occurred where the learned routing behavior most strongly emphasized major
855 conveyance pathways and hydraulically efficient portions of the river network.



Table 4. Spearman correlations between learned routing metrics and gauge-level RMSE reduction relative to RAPID.

scenario	Spearman ρ
Attention-weighted top channel width shift	0.736
Attention-weighted bottom channel width shift	0.725
Top-10% upstream attention concentration	0.545
Attention-weighted travel-time proxy	0.502

4 Discussion

4.1 Implications for Graph-Based Runoff Routing

The results demonstrate that GNNs can provide an effective framework for routing physically-generated runoff through directed river-network topology. Unlike direct streamflow-forecasting models, the proposed framework isolates the routing component by transferring Noah-MP runoff from gridded model space into NGen river-network graph elements before applying graph-based message passing. This separation is important because it allows the learned model to be evaluated specifically as a routing operator rather than as a combined runoff-generation and streamflow-prediction system.

The strong performance gains relative to RAPID suggest that topology-aware graph learning can capture routing behavior that is difficult to represent using fixed routing assumptions alone. The directed graph structure constrains information propagation to hydrologically-connected pathways, while node and edge attributes allow the model to learn spatially-variable routing relationships across heterogeneous channel and watershed conditions. This provides a flexible routing framework that remains physically structured through the river graph while allowing learned adaptation to local hydrologic behavior.

4.2 Why Graph Routing Improves Performance Relative to RAPID

The largest improvements occurred in headwater and intermediate tributary systems, where runoff responses are often more nonlinear, spatially heterogeneous, and sensitive to local terrain and drainage structure (Bain et al., 2023). In these regions, fixed-parameter routing assumptions may be less able to represent variable travel times, local attenuation behavior, and multi-peak runoff responses. By contrast, the GAT framework learns adaptive upstream–downstream influence weights across the graph, allowing routing behavior to vary across river-network position and physiographic setting.

The hydrograph and FDC results further indicate that the graph-based framework reduces the delayed peaks, exaggerated event magnitudes, and prolonged recession behavior observed in RAPID for representative events. This does not imply that RAPID is generally unsuitable; rather, it suggests that in this application, the combination of Noah-MP runoff forcing and fixed routing assumptions produced systematic mismatch at several gauges. The learned graph-routing framework was able to partially correct these routing-response errors while maintaining consistency with the physical river-network structure.



888 4.3 Temporal Memory and Loss-Function Tradeoffs

889 The temporal-memory experiments show that intermediate-lag windows, especially the 14-day runoff-lag
890 configuration, provide the strongest overall routing performance. This suggests that graph-based routing
891 benefits from antecedent runoff information over multi-day timescales consistent with snowmelt
892 response, subsurface-flow persistence, and tributary accumulation processes in the *Salt-Verde*
893 watershed. Longer 30-day-lag configurations did not improve performance, indicating that excessive
894 antecedent information may introduce noise or temporal complexity that is less directly relevant to daily
895 routing behavior.

896 The loss-function experiments revealed an additional tradeoff. *Weighted-MSE* training produced the
897 strongest aggregate routing performance, likely because gauge-balanced optimization stabilized learning
898 across a heterogeneous gauge network. However, *JKGE-based* training occasionally improved recession
899 and low-flow behavior, even though it performed less well overall. This indicates that different loss
900 functions emphasize different hydrologic behaviors. For operational peak-flow prediction in the *Salt-Verde*,
901 *weighted MSE* may be preferable, whereas objectives that better preserve recession dynamics may
902 be useful when low-flow behavior or hydrograph shape is the primary focus.

903 4.4 Hydrologic Plausibility and Limits of Learned Routing

904 The streamflow–runoff consistency diagnostic provides an informative hydrologic plausibility check for
905 evaluating how each routing framework transforms upstream runoff into downstream discharge. In this
906 diagnostic, routed streamflow at each gauge is compared with the cumulative Noah-MP-generated runoff
907 originating upstream of that gauge. For a routing framework that primarily redistributes runoff through
908 the river network without substantial transformation, streamflow-to-upstream-runoff ratios would be
909 expected to remain relatively close to unity, subject to numerical losses or routing approximations. This
910 behavior was observed for RAPID, which produced nearly uniform ratios across most gauges, consistent
911 with its physically conservative routing formulation.

912 In contrast, observed streamflow exhibited substantially greater spatial heterogeneity in these ratios
913 across the watershed. This variability reflects the fact that real watershed response is not governed solely
914 by conservative channel transport of generated runoff. Instead, effective runoff-to-streamflow
915 transformation integrates multiple interacting processes, including runoff-generation uncertainty,
916 transmission losses in ephemeral or semi-arid channels, evapotranspiration losses, infiltration and
917 groundwater recharge, delayed subsurface return flow, channel storage effects, and local anthropogenic
918 influences such as diversions or regulated releases. Consequently, the observed watershed response
919 represents the combined outcome of both runoff production and subsequent hydrologic transformation
920 processes rather than idealized conservative routing alone.

921 The graph-based routing framework produced streamflow–runoff ratios that more closely resembled the
922 spatial variability exhibited by the observation-based diagnostic than the nearly uniform conservative
923 behavior exhibited by RAPID. This suggests that the learned routing operator does not simply emulate
924 conservative runoff translation, but instead learns effective transformations that better reproduce the
925 integrated watershed-scale response reflected in the observations. From a predictive perspective, this
926 behavior is beneficial because the objective of the routing framework is to reproduce observed discharge
927 rather than merely preserve the raw runoff signal.

928 However, this interpretation requires caution. Because the diagnostic uses Noah-MP-generated runoff as
929 the upstream forcing reference, discrepancies between routed streamflow and observations cannot be
930 attributed uniquely to routing behavior. Errors in precipitation forcing, snow accumulation and melt
931 timing, soil moisture dynamics, infiltration partitioning, groundwater exchange, or runoff generation
932 within Noah-MP may all propagate into this comparison. As a result, the apparent improvement in



933 hydrologic realism achieved by the graph-based framework may arise from multiple mechanisms:
934 improved representation of routing dynamics, implicit compensation for systematic runoff-generation
935 biases, or a combination of both. Future diagnostic frameworks should seek to separate these effects
936 explicitly, for example by evaluating the routing model using multiple runoff-generation products,
937 synthetic runoff experiments with known routing characteristics, or conservation-constrained routing
938 formulations that limit compensatory adjustments.

939 This distinction is scientifically important because the current graph-routing framework is designed as a
940 predictive routing emulator rather than a strictly mass-conserving hydrodynamic solver. Although the
941 model remains physically structured through explicit river-network topology, directed connectivity, and
942 physically meaningful node and edge attributes, it does not impose explicit water-balance constraints
943 during optimization. Consequently, the framework is capable of learning effective transformations that
944 improve agreement with observations, but those transformations are not guaranteed to correspond to
945 physically conservative routing behavior.

946 This highlights an important tradeoff between predictive accuracy and strict physical interpretability in
947 learned hydrologic routing systems. The current framework demonstrates that topology-aware graph
948 learning can substantially improve streamflow prediction relative to conventional routing benchmarks,
949 but future work should investigate hybrid architectures that explicitly incorporate conservation
950 constraints, flow continuity requirements, or differentiable hydrodynamic priors. Such approaches would
951 help distinguish true routing-process improvement from compensatory correction of runoff-generation
952 errors while preserving the predictive flexibility of graph-based learning.

953 **4.5 What Did RiverGraphNet Learn About Routing?**

954 Beyond improving predictive performance, the attention analysis provides insight into the routing
955 behavior learned by RiverGraphNet and offers clues regarding limitations of conventional routing
956 formulations. Unlike RAPID, which routes runoff using prescribed hydraulic relationships and fixed routing
957 parameters, RiverGraphNet learned spatially heterogeneous routing influences throughout the river
958 network. Importantly, the observed relationships should not be interpreted as direct physical flow
959 partitioning. Graph-attention coefficients describe how information is propagated through the learned
960 routing model rather than how water is physically distributed among river reaches. Nevertheless, the
961 attention analysis provides insight into which physical attributes were most influential in the learned
962 routing process. Although hydraulic descriptors such as channel width, slope, roughness, and travel-time
963 metrics were explicitly provided to the model, the learned attention mechanism did not utilize them
964 equally. Instead, systematic preferences emerged across the river network, indicating that certain channel
965 characteristics exerted a stronger influence on information propagation and routing performance than
966 others. This provides a physically interpretable view of how the model routes runoff through the network.

967 Attention coefficients were positively associated with channel-width metrics and travel-time proxies,
968 while negative relationships were observed with channel slope and Manning roughness. These patterns
969 indicate that the model preferentially emphasized wider, hydraulically efficient flow pathways while
970 reducing the influence of steeper or hydraulically resistant reaches. Such behavior is physically intuitive
971 because wider channels generally provide greater conveyance capacity and also represent locations
972 where runoff contributions from multiple upstream tributaries have already been integrated.
973 Consequently, channel width may serve not only as a hydraulic descriptor but also as an indicator of the
974 relative importance of a pathway within the river-network hierarchy.

975 More importantly, the routing characteristics most strongly associated with performance improvement
976 were not travel-time metrics alone. Gauge-level reductions in routing error relative to RAPID were most
977 strongly correlated with attention-weighted channel-width metrics, with correlations of $p = 0.736$ and $p =$



0.725 for top and bottom channel width, respectively. Weaker but still substantial relationships were observed for dominant upstream-pathway attention concentration ($p = 0.545$) and attention-weighted travel-time metrics ($p = 0.502$). These results suggest that routing performance depends not only on estimating travel time and attenuation correctly, but also on determining which upstream pathways exert the strongest control on downstream flow. Channel width likely acts as a proxy for major conveyance pathways and accumulated upstream drainage structure, indicating that the model learned where the most influential runoff signals originate and become concentrated within the network, rather than simply how rapidly water propagates downstream. This finding suggests that accurate routing depends not only on representing travel-time and attenuation processes, but also on identifying which upstream tributaries exert the greatest control on downstream discharge. In this sense, the largest performance gains appear to arise from improved representation of network influence and upstream contribution weighting in addition to conventional routing dynamics.

Additional context is provided by the underlying river-network structure (Figure S6). Upstream contributing area increases systematically with stream order, indicating that higher-order reaches integrate progressively larger portions of the watershed. However, the attention analysis showed the opposite pattern, with the highest attention values occurring in first-order reaches and progressively lower attention assigned to higher-order channels. Because first-order reaches are not associated with the largest contributing areas, this result suggests that RiverGraphNet is not simply emphasizing the largest rivers or the most aggregated portions of the network. Instead, the model appears to recognize that routing errors originating in headwater tributaries can propagate and accumulate downstream, making accurate representation of headwater runoff signals particularly important for overall routing performance.

An important observation is that RAPID already incorporates substantial spatial variability through reach-specific Muskingum K parameters, which represent travel-time differences throughout the river network (Figure S7). Therefore, if travel-time representation alone were the dominant limitation, one would expect the strongest performance gains to be associated with travel-time metrics. Instead, the strongest relationships were observed with attention-weighted channel-width metrics and pathway-concentration measures. This suggests that a key limitation may not be the estimation of travel time itself, but rather the assumption that routing influence is fully determined by predefined hydraulic relationships. Channel width may partially reflect processes not explicitly represented in the routing formulation, including changes in hydraulic conveyance, channel storage, floodplain interaction, transmission losses, and riparian evapotranspiration. In semi-arid systems such as the Salt–Verde watershed, wider channel sections may therefore reflect locations where effective runoff propagation differs from that predicted by travel-time relationships alone. The RiverGraphNet results indicate that allowing routing influence to vary according to channel geometry and network context may provide additional predictive value beyond conventional travel-time parameterization.

This finding provides a useful perspective on why graph-based routing improved performance relative to RAPID. Conventional routing frameworks primarily focus on propagating water through predefined hydraulic relationships, whereas the learned graph-routing framework additionally adapts the relative importance of upstream tributaries according to local channel geometry, network position, and accumulated watershed structure. In other words, the largest improvements were associated with the model’s ability to selectively emphasize dominant conveyance pathways rather than treating all upstream contributions according to a fixed routing formulation.

The learned routing behavior suggests a specific limitation of conventional routing formulations: travel-time and attenuation parameters alone may not fully describe how information propagates through complex river networks. In RiverGraphNet, the largest improvements occurred when routing influence



was adaptively concentrated along dominant conveyance pathways. This suggests that future versions of RAPID could potentially benefit from routing formulations that allow effective routing influence or attenuation behavior to vary according to channel geometry, stream order, drainage structure, or other network attributes. More generally, hybrid frameworks that retain physically based Muskingum routing while incorporating learned, spatially adaptive weighting of upstream contributions may provide a promising pathway toward improving routing performance without sacrificing physical consistency.

4.6 Limitations and Future Work

Several limitations remain. First, reservoir operations and managed releases are not explicitly represented. Although dam-affected gauges were excluded from the primary training loss, regulated reaches remain an important challenge for applying graph-routing models in operational river systems. Incorporating reservoir storage, release rules, diversions, and irrigation withdrawals would improve applicability in human-influenced basins. One potential approach is to augment the river graph with reservoir-state nodes or self-loop connections that allow information and storage effects to persist locally over time, enabling the model to learn delayed release behavior and operational controls in regulated systems.

Second, the current framework relies on observed streamflow records for supervised training and evaluation. This dependence on gauge observations may limit direct applicability in ungauged or data-sparse regions, where long-term discharge records are unavailable or where the gauge network does not adequately represent spatial variability in runoff-routing behavior. Future work could address this limitation through regional transfer learning, pretraining across multiple well-gauged basins, parameter sharing among hydrologically similar watersheds, and hybrid training strategies that combine limited observations with physics-based routing simulations or conservation-based regularization. These approaches could improve model transferability while reducing dependence on dense local streamflow observations.

Third, the framework depends on the quality of Noah-MP runoff inputs and the accuracy of the grid-to-graph runoff-transfer procedure. Errors in runoff generation, precipitation forcing, soil moisture dynamics, or divide-based runoff aggregation can propagate into the routing model. Future studies should evaluate the framework using multiple runoff forcings, alternative runoff-transfer schemes, and additional basins with contrasting hydroclimatic regimes.

Fourth, the current RiverGraphNet framework does not explicitly enforce mass conservation at individual graph nodes or along river-network edges. Although the model is physically structured through directed river-network topology and physically meaningful node and edge attributes, the learned message-passing operation is not constrained to conserve incoming runoff volume during downstream propagation. As a result, the model may improve agreement with observed streamflow partly by learning effective corrections to biases in Noah-MP runoff generation, precipitation forcing, or grid-to-graph runoff transfer, rather than only by representing conservative river-routing processes. This flexibility can improve predictive skill, but it also limits physical interpretability and makes it difficult to distinguish true routing-process improvements from compensation for runoff-generation errors. Future work should incorporate conservation-aware graph architectures, water-balance regularization, differentiable routing constraints, or hybrid physics-machine learning formulations that preserve mass continuity while retaining the adaptive capacity of graph-based learning.

Fifth, although GAT-attention provides adaptive graph connectivity weighting, attention weights should not automatically be interpreted as physical flow partitioning without additional analysis. Future work should examine whether learned attention patterns correspond to meaningful hydrologic controls such as drainage area, slope, travel time, and upstream contributing structure.



Overall, this study demonstrates that topology-aware graph learning can serve as a promising routing framework for converting physically generated gridded runoff into daily streamflow predictions. By explicitly separating runoff generation from routing, the framework provides a useful testbed for evaluating learned river-network routing behavior and for developing future hybrid models that combine physical consistency, mass conservation, and adaptive graph-based learning.

5 Conclusions

This study has developed and tested a standalone graph-based hydrologic routing framework designed to explicitly isolate runoff routing from runoff generation by coupling physically generated Noah-MP runoff with topology-aware graph neural network routing over a directed river-network representation of the *Salt–Verde* watershed. Unlike many existing graph-based hydrologic studies that directly forecast streamflow or generate runoff at graph nodes, the proposed framework focuses specifically on the routing problem by transferring gridded land-surface runoff into a physically-structured river graph derived from the NGen hydrofabric and learning runoff propagation through Graph Attention Network (GAT)-based message passing.

The results demonstrate that graph-based routing can substantially improve streamflow prediction relative to the RAPID physics-based routing benchmark. Across all experimental configurations, the graph-routing framework consistently produced positive performance gains relative to RAPID at almost all gauges, with the strongest configuration achieving a mean $KGE_{\{ss\}}$ of 0.70 compared with a mean $KGE_{\{ss\}}$ of -0.29 for RAPID. Spatial analysis showed that improvements were particularly pronounced in headwater and intermediate tributaries, where hydrologic response is highly nonlinear and routing behavior is strongly influenced by heterogeneous drainage structure, terrain complexity, and localized upstream–downstream interactions.

The temporal-routing-memory experiments indicated that routing performance was relatively insensitive to lag length over the range evaluated. Although intermediate runoff-memory representations (7–14 days) consistently produced among the strongest results, differences among lag configurations were generally modest. The no-CNN ablation experiments further indicated that much of the predictive routing skill emerged from the combination of graph topology and lagged runoff inputs, with the temporal convolutional module serving primarily as an additional refinement mechanism rather than the dominant source of temporal routing memory.

Loss-function experiments revealed important tradeoffs between aggregate predictive skill and hydrologic behavior. *Weighted-MSE* optimization produced the strongest overall performance, likely because gauge-balanced optimization improves stability across the heterogeneous evaluation network while preventing dominant gauges from disproportionately influencing training. In contrast, *JKGE-based* objectives often better preserved recession dynamics and low-flow recovery, but generally produced weaker overall predictive performance. These findings highlight that optimization objective selection can meaningfully shape the hydrologic behavior learned by graph-based routing models.

Event-scale hydrograph and flow-duration-curve analyses confirmed that the graph-based routing framework improved not only aggregate performance metrics but also hydrologically meaningful streamflow behavior. Compared with RAPID, the learned routing framework more effectively reproduced *peak timing*, *event magnitude*, *hydrograph shape*, *attenuation behavior*, and *long-term streamflow distributions* across diverse hydrologic settings. These improvements suggest that topology-aware graph message passing provides a flexible mechanism for representing heterogeneous runoff propagation across complex river systems.



1112 Attention analysis provided additional insight into the routing behavior learned by RiverGraphNet. The
1113 model preferentially emphasized headwater runoff signals and dominant conveyance pathways, while
1114 routing improvements were most strongly associated with channel-width metrics rather than travel-time
1115 proxies alone. This suggests that identifying which upstream pathways exert the strongest influence on
1116 downstream discharge may be as important as representing travel-time and attenuation processes
1117 themselves.

1118 At the same time, the hydrologic plausibility analysis highlighted an important scientific limitation.
1119 Although the graph-based routing framework produced watershed-response patterns more consistent
1120 with observations than conservative routing alone, the framework does not explicitly enforce mass
1121 conservation. Consequently, improved agreement with observed streamflow may reflect both enhanced
1122 routing representation and implicit compensation for errors in the Noah-MP runoff-generation forcing.
1123 This distinction is important because predictive success does not necessarily imply physically conservative
1124 routing realism.

1125 Overall, this study demonstrates that graph neural networks provide a promising framework for
1126 hydrologic routing when physically-generated runoff and explicit river-network topology are incorporated
1127 into the learning architecture. The results suggest that graph-based routing can outperform conventional
1128 routing frameworks, particularly in heterogeneous systems where fixed routing assumptions may be
1129 limiting. Future work should focus on hybrid graph-routing architectures that incorporate explicit water-
1130 balance constraints, differentiable hydrodynamic priors, reservoir regulation processes, and multi-basin
1131 evaluation in order to improve physical interpretability while preserving the predictive flexibility of graph-
1132 based learning. More broadly, the results demonstrate that graph neural networks can serve not only as
1133 accurate routing models but also as valuable tools for investigating how hydrologic information
1134 propagates through complex river networks.

1135

1136 **Data and Code Availability**

1137 The streamflow observations used in this study were obtained from the U.S. Geological Survey (USGS)
1138 National Water Information System (NWIS). River-network topology, hydrofabric attributes, and routing
1139 elements were derived from the Next Generation Water Model (NGen) hydrofabric.

1140 Noah-MP runoff simulations used as routing inputs were generated using the modeling framework
1141 described in Section 2. The RiverGraphNet source code, training configurations, graph-cache files,
1142 evaluation scripts, and supporting analysis workflows are publicly available at
1143 [https://github.com/mfarmani95/LSTM_GNN_routing-].

1144

1145 **Author Contribution**

1146 Mohammad A. Farmani developed the RiverGraphNet framework, implemented the graph-based
1147 modeling workflow, performed the graph-routing experiments, analyzed the results, prepared the figures,
1148 and wrote the initial manuscript draft. Sadaf Moghisi performed the Noah-MP simulations and RAPID
1149 routing experiments, contributed to result analysis, and reviewed the manuscript. Andrew Bennet
1150 contributed to the conceptualization of the study, interpretation of the results, and manuscript review.
1151 Muhammad Jawad reviewed the manuscript and contributed to interpretation of the results. Hoshin
1152 Gupta, Ali Behrangi, and Ahmad A. Tavakoly contributed to manuscript review, interpretation of the
1153 results, and refinement of the hydrologic and methodological framing. Guo-Yue Niu contributed to the
1154 Noah-MP modeling framework, hydrologic interpretation, supervision, and manuscript review. All authors
1155 discussed the results and contributed to the final manuscript.



1156

1157 **Competing interest**

1158 The contact author has declared that none of the authors has any competing interests.

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