



CLIMATE MODUS OPERANDI

Anastasios A. Tsonis¹ and Geli Wang²

1. Department of Mathematical Sciences, University of Wisconsin-Milwaukee,
Milwaukee, WI 53201, USA
2. Laboratory of Middle Atmosphere and Global Environment Observation (LAGEO),
Institute of Atmospheric Physics, Chinese Academy of Sciences, Beijing, China

Abstract

This overview paper is a culmination of decades of research into climate, chaos, and nonlinear dynamics. It is a voyage of work done since the early 1980's in nonlinear dynamics in climate. As an expected extension, in 2004 networks introduced into atmospheric sciences (Tsonis and Roebber, 2004). Ever since it is realized that at longer time and space scales climate operates with its major modes interacting with each other, and that rules and randomness co-exist. Here we present an overview of what we have learned so far.

Correspondence: Anastasios A. Tsonis (aatsonis@uwm.edu)

1. Introduction

Imagine that you would like to have a general idea of your health. What do you think your doctor does? They would not test how every little cell is doing. They will take samples of your blood and urine (and maybe others) and performs tests that would give indications of what is the state of your major body parts (heart, liver, kidneys, etc.). When we talk about climate, we basically do the same thing. We test the major signals.



30 This is the main idea behind the theory of networks. A network is defined by a set of nodes and
31 their links, where any pair of nodes is connected according to some rule. Usually, a node is a
32 time series of some variable and its connection to the other nodes is defined by some
33 deterministic/statistical measure (for example, cross-correlation). The architecture of a network
34 (set of connections between the nodes), can reveal important and novel features of the system it
35 represents (Albert and Barabasi 2002; Strogatz 2001; da F. Costa et al. 2007). One such feature
36 is communities (Newman and Girvan 2004). Communities represent subsets in the network of
37 densely connected nodes, with a few connections between the subsets which help the
38 communities influence each other (Arenas et al. 2006). Identification of these communities can
39 offer useful insights about the dynamics of the system under investigation.

40 Climate networks were introduced in the atmospheric sciences in 2004 (Tsonis and Roebber,
41 2004). In the climate system, network communities have been identified to correspond to major
42 climate modes, such as the Pacific North America (PNA) pattern, the North Atlantic Oscillation
43 (NAO), and other major climate modes, all connected to climate teleconnections (Tsonis et al.
44 2008, Tsonis et al. 2011). Since then, network theory was applied to climate with impressive
45 results, for example, the discovery of a new dynamical mechanism for major climate shifts
46 (Tsonis et al. 2006; Tsonis et al. 2007; Tsonis et al. 2008; Tsonis and Swanson 2008; Yamasaki
47 et al. 2008; Gozolchiani et al. 2008; Swanson and Tsonis 2009). As we list below, many studies
48 followed, using major climate modes, where interaction between climate modes from several
49 fields (pressure, temperature etc.) was investigated using various mathematical methods such as
50 nonlinear prediction, causality, convergence cross mapping, slow-feature analysis, and others.
51 The following are major examples of causality and interaction between major climate modes.
52 The list of the major climate modes referred in this work is shown in Appendix 1. For detail
53 references of these indexes see Wyatt et al. (2011), Lin et al. (2005), Zhang et al. (2026) and
54 references therein.

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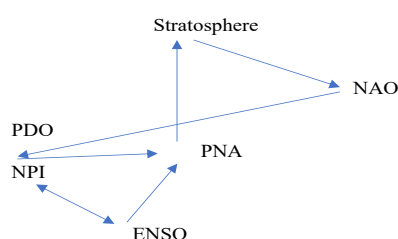
56 **2. Results**

57 1) According to Tsonis et al. (2007) study, NAO, PDO (and NPI), PNA, and ENSO interact with
58 each other and the stratosphere in a way that determines climate shifts. As Figure 1 shows, NAO



59 influences PDO and NPI, ENSO affects NPI and PNA, and through the stratosphere the cycle
60 closes back to NAO. If during this interaction the modes synchronize, and the coupling between
61 the modes increases, climate shifts from a positive (negative) to a negative (positive) global
62 temperature regime. This study explained for the first time all global temperature trend changes
63 in the global temperature record.

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66 *Figure 1: Tsonis et al. (2007), Wang et al. 2009. Method: Network Synchronization and coupling*
67 *strength between modes.*

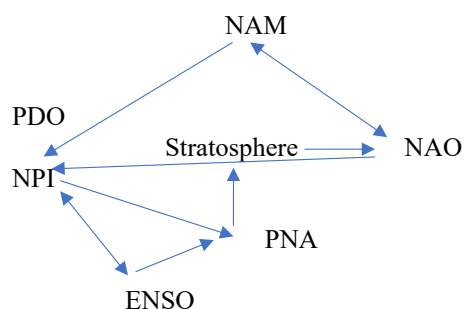
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69 This study provided the grounds for investigating the interaction of several major climate modes.
70 Many studies followed this development, where interaction between climate modes was
71 investigated using the mathematical methods mentioned above. The following are several major
72 examples of causality and interaction between major climate modes.

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74 2) An extension of the above study including NAM and using a different method is shown next.

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79 *Figure 2: Pan et al. (2020). Method: Slow Feature Analysis (Blaschke et al. 2006). Main results:*

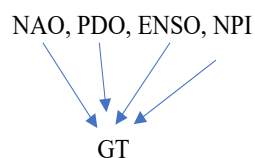
80 *Results suggest that the base periods and their harmonic oscillations related to stratosphere*

81 *and ENSO, act as key connections among other climatic modes with synchronous behaviors,*

82 *highlighting the important roles of these oscillations in the variability of the Earth's climate.*

83

84 3) Directional influences



85

86 *Figure 3: Wang et al. (2012): Method: Nonlinear Prediction on actual (not filtered) data. Main*

87 *results: Prediction of Global Temperature improves as we add more and more dominant modes.*

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90 4) Stadium wave



NHT->AMO->AT->NAO->ENSO-> NPO/PDO-> ALPI



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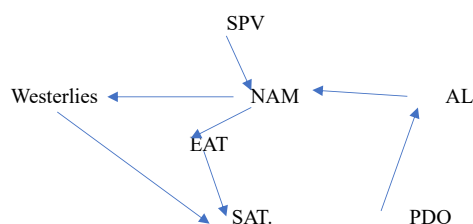
92 *Figure 4: Wyatt et al. (2011). Method: Synchronization, Multichannel Singular Spectrum*

93 *Analysis. Main results: Initial changes in the North Atlantic temperature anomaly associated*
94 *with AMO culminate in an oppositely signed hemispheric signal about 30 years later. Results*
95 *presented there support the hypothesis that AMO plays a significant role in hemispheric and,*
96 *by inference, global climate variability.*

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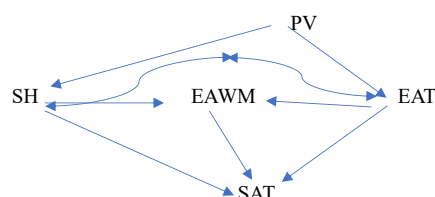
99 5) Including Asian modes



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101 *Figure 5: Lin et al. (2025). Method: Convergence Cross Mapping (Sugihara et al. 2012). Main*
102 *results: The relationship between NAM and SAT during winter is strongly modulated by PDO*
103 *phase shifts, which affect the intensity of the Aleutian Low, thereby impacting the Pacific center*
104 *of NAM and altering its influence on Northeast Asia.*

105 6) Including another set of Asian modes



106

107 *Figure 6: Zhang et al. (2026). Method: Convergence Cross-Mapping (Sugihara et al. 2012).*

108 *Main results: The above network applies to both positive and negative NAM phases. Findings*

109 *reveal that interactions between the modes vary on interannual and interdecadal scales. On*

110 *interannual scales, NAM (in both positive and negative phase) and EAWM show similar influence*

111 *patterns on winter surface air temperature (SAT). NAM plays a pivotal role in the EAWM's*

112 *decadal influence on SAT through quasi-stationary planetary wave activity. Moreover, EAT exerts*

113 *a consistently positive influence on SH.*

114

115 Other studies have added to these connections, including (among others): 1) CR → GT, Tsonis

116 et al. (2015), Method: Convergence Cross-Mapping (Sugihara et al. 2012), 2) NAM → SAT,

117 Zhang et al. (2018), Method: Convergence Cross-Mapping (Sugihara et al. 2012), 3) the effect of

118 8-yr information flow from larger to smaller scales in long term SAT records from European

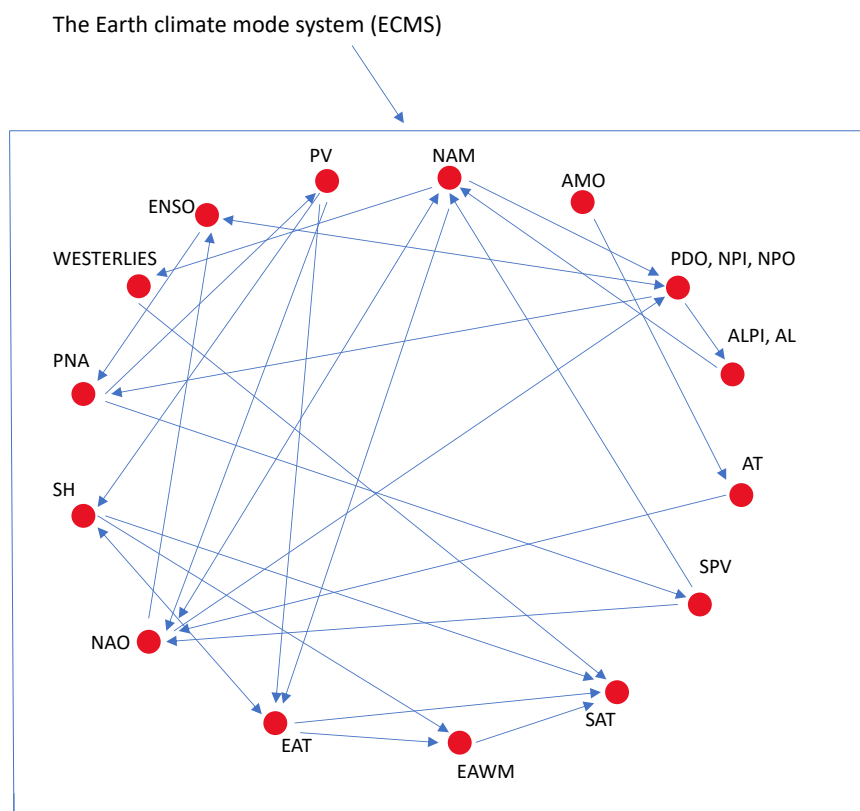
119 stations (Jajcay et al 2016), 4) the effect of phase low frequency interannual processes on quasi-

120 annual variability of amplitude and phase of extreme ENSO events (Jajkay et al. 2018), 5) the

121 strong relation of climate networks to climate teleconnections and how teleconnections stabilize

122 climate (Tsonis and Roebber, 2004, Tsonis et al. 2008). Figure 7 combines the above presented

123 results.



124

125 *Figure 7: This figure represents a picture of causality in climate dynamics of the “Earth system”*
 126 *based on the studies mentioned above. It is by no means the complete picture of climate modes*
 127 *interactions, but it serves as an idea of what is the background of climate mode interactions.*
 128 *Note that in some cases, causality is bidirectional. The location of the nodes is arbitrary.*

129

130 The above figure of causality in climate dynamics is by no means the final picture, as many other
 131 connections may be identified in future studies, or that some modes may exhibit
 132 “commonalities” to other modes, but the general picture remains very coherent. We are dealing
 133 with a complex network, which is also a “small-world” network, in the sense that communication
 134 between modes in the network is very efficient (we can go from one mode to any other mode in
 135 just a few steps). This provides a new perspective of how climate may be operating and how
 136 climate teleconnections manifest themselves. However, the picture is not complete unless the



137 extraterrestrial influence (solar output, and cosmic rays), which affect global temperature, are
138 included, as it is shown in Figure 8. This Figure points to the fact that we are dealing with a “3-
139 body problem” with nonlinear components (CR, SUN, Earth Climate Mode System), which by
140 definition is complex and chaotic, and thus quite unpredictable.



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142 *Figure 8: As an addition to Figure 7, here we show that possible connections to extraterrestrial*
143 *forces and climate.*

144
145 When we are dealing with data where “noise” is present, the validity of the results is based on
146 statistical significance. Therefore, (as we all know), while a result from a solid mathematical
147 method may be statistically significant, it does not guarantee that “noise” sometimes will not
148 take over and “ruin” the predictions based on the mathematical projections. Rules and
149 randomness co-exist and when rules prevail, prediction are reliable, but when randomness
150 (noise) becomes more dominant, predictions fail, as we all know from personal experience with
151 climate predictions (not to mention weather predictions).

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154 **3) Instead of Conclusions**

155 Major signals or modes emerge in the complex climate system and their interactions provide
156 unique clues and insights into the dynamics of climate, long-range correlation/teleconnections,
157 and climate shifts, over time scales closely related to our experiences of weather, climate
158 changes, and extremes.

159 Digging deeper in this idea of causality in climate, noise (randomness), and unpredictability, one
160 has to wonder what is the bigger picture. Climate may be thought as being just an isolated part in



161 our universe, but could there be a bigger picture? In the general sense of the Universe, there is
162 the physical system (the laws of nature) and the formal mathematical system (the language of the
163 physical system). How does complexity and randomness connect to it? Is there randomness in
164 the physical system? As it has been known for years, randomness in the physical system, through
165 the second law of thermodynamics (irreversibility), through the sensitivity in initial conditions
166 (chaos), through quantum-mechanics, and through stochasticity (the interaction of infinite
167 agents), is an inherited property of nature. At the same time, due to theories by Gödel, Cantor,
168 Chaitin, Kolmogorov and others (Hofstadter, 1979, Tsonis, 2007, Tsonis, 2024), it is clear that in
169 the pure mathematical system (not statistics) there is plenty of randomness. This may not be
170 surprising if we assume that the formal mathematical system is the language of nature.

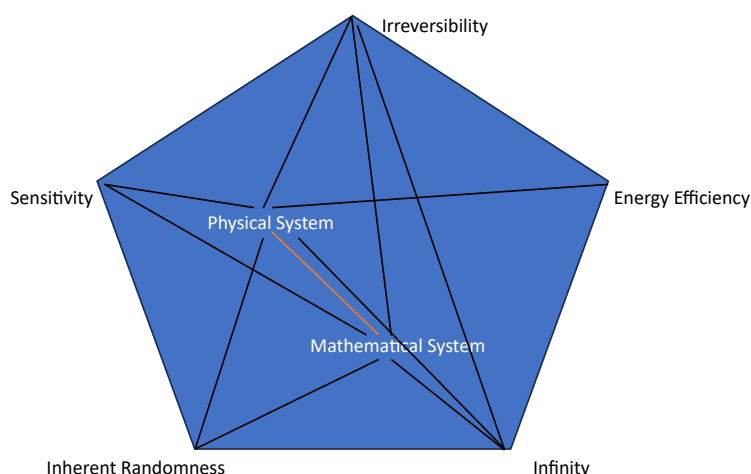
171 Rules alone or randomness alone do not produce networks that are both stable and efficient.
172 What makes them both stable and efficient is the co-existence of rules and randomness. As an
173 example, let's consider cumulus cloud formations. Even though, this example refers to a small-
174 scale phenomenon, it demonstrates the co-existence of rules and randomness at all scales. Given
175 a rather uniform surface, the air at the surface gets warm during the day, then it rises, and as it
176 rises, it expands and cools. This increases the relative humidity. At some point the relative
177 humidity reaches 100% and then the cloud bases form, basically at the same level everywhere in
178 the area. Up to this point everything is determined by physics. But once the bases are formed the
179 cloud development is rather random. Given the fact that cubic or spherical clouds have never
180 been observed, the formation of a rather well-defined cloud bases is followed by irregular
181 vertical structures. But why? One could imagine that once the cloud bases are formed, rules
182 could dictate that each molecule in the original rising air moves and interacts with the other
183 molecules in such a way as to always form a cube or a sphere. But can you imagine the effort
184 and energy that the atmosphere will have to make in order for this to happen? Clearly this will
185 basically require infinite power and energy. But, does nature want to use infinity and infinite
186 power for every little process? Nature reserves infinity for bigger purposes. Instead, after the
187 rules are set, randomness comes into picture, and molecules are left to move randomly, thus
188 generating irregular cloud shapes, while minimizing effort. This is in accordance with the
189 principle of the least possible energy consumption (least effort, energy efficiency) as has been
190 suggested by George Zipf (Zipf, 1949), and mathematically and physically demonstrated by the



191 work of Ilya Prigogine (Prigogine 1980), which won him the Nobel prize in Chemistry in 1997.
192 Thus, randomness emerges as a property of nature. Even though the above example refers to a
193 small-scale phenomenon, it demonstrates the co-existence of rules and randomness. This
194 “inherited” randomness (which involves the free interaction of many agents- otherwise referred
195 to as stochasticity) becomes a property of nature.

196 This co-existence is the main recipe for basically all processes in the Universe and life, including
197 most natural processes, Darwinian evolution (random variations and natural selection), life, DNA
198 structure, languages, music, and as we show here, climate(Tsonis, 2008, Tsonis 2024). And, as
199 the random deviations of the Cosmic Microwave Radiation (the relic of Big Bang, Fixsen, 2009)
200 would suggest, this co-existence is present since the beginning of time. Therefore, while the
201 notion of infinity appears abstract, infinity, irreversibility, sensitivity to the initial conditions, too
202 many interacting agents (stochasticity, or inherited randomness), and energy efficiency may be
203 the key players in the dynamics of the Universe. These ideas are summarized in Figure 9, which
204 indicates the possible connections between the physical and mathematical system and the five
205 main ingredients of rules and randomness in both systems. Again, we need to mention that this is
206 not by any means a final answer, but just a perspective based on what we understand right now.

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208

209 *Figure 9: This figure shows the possible connections between the physical and mathematical*
 210 *system and the five main ingredients of rules and randomness in both systems. The position of*
 211 *the nodes in this figure is strictly arbitrary. The actual physical position of the “actors” involved*
 212 *in this picture remains open to debate. This is not by any means the complete picture of how*
 213 *the universe works, but just a suggestion of where we are at right now.*

214

215 **Authors contributions:** AAT designed the paper, with all the figures, and wrote the first
 216 version. GW was part of most of networks included in this paper, and contributed to interpreting
 217 results and improving this paper.

218 **Competing interests:** The authors declare that they have no conflict of interest.

219 **Code and data availability:** All codes and data availability have been cited in the references
 220 and are available by the authors

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314 APPENDIX

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316 The list of the major climate modes referred in this work. For detail references of these indexes
317 see Wyatt et al. (2011), Lin et al. (2005), Zhang et al. (2026) and references therein.

318

319 1. NAM (Northern Hemisphere Annual Mode). Note that NAM is also referred to as AO

320 (Arctic Oscillation)

321 2. SAT (Wintertime Surface Air Temperature Over NE Asia)

322 3. NAO (North Atlantic Oscillation)

323 4. PDO, NPI, NPO (Pacific Decadal Oscillation, North Pacific Index, North Pacific

324 Oscillation)

325 5. ENSO (El Nino Southern Oscillation)

326 6. PNA (Pacific North American pattern index)

327 7. SPV (Strength of Stratospheric Polar Vortex)

328 8. AMO (Atlantic Multi Decadal Oscillation)

329 9. AT (Atmospheric-Mass Transfer Anomalies)

330 10. ALPI, AL (Aleutian Low-Pressure Index)



331 11. PV (Index relating to total air mass in NH between 500-hPa isobaric surface and the

332 boundary of polar vortex)

333 12. SH (Siberian High)

334 13. EAWM (East Asian Winter Monsoon)

335 14. EAT (East Asian Trough)

336 15. Westerlies (mid-to high-latitude westerly jet intensity)

337 16. Extraterrestrial forces (Solar activity and Cosmic Rays)

338 17. GT/NHT (Global Temperature, North Hemisphere Temperature)

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340 Note that, some modes may have “commonalities” to other modes but they all have distinct
341 “ingredients” associated with them. For example, PV refers to the intensity of the tropospheric
342 polar vortex calculated as the total air mass in NH between 500-hPa isobaric surface and the
343 boundary of polar vortex, while SPV represents the strength of arctic stratospheric polar vertex
344 calculated as the mean zonal wind averaged over 600-900 N and 50-10 hPa. SPV is also related
345 to Quasi-Biennial-Oscillation (QBO).

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