



1 **Mechanical interaction of geometrically linked cracks and faults**

2 Ludovico Manna^{1*}, Matteo Maino^{1,2}, Leonardo Casini³, Marcin Dabrowski⁴

3 ¹ Department of Earth and Environmental Sciences, University of Pavia, Pavia, Italy

4 ² Institute of Geosciences and Earth Resources of Pavia, C.N.R., Pavia, Italy

5 ³ Department of Chemical, Physical, Mathematical and Natural Sciences, University of Sassari, Sassari, Italy

6 ⁴ Computational Geology Laboratory, Polish Geological Institute – National Research Institute, Wrocław,
7 Poland

8

9 **Corresponding author:**

10 Ludovico Manna, ludovico.manna01@universitadipavia.it

11

12 **ORCID:**

13 Ludovico Manna: <https://orcid.org/0009-0003-7952-157X>

14 Matteo Maino: <https://orcid.org/0000-0001-8766-8027>

15 Leonardo Casini: <https://orcid.org/0000-0002-6157-1865>

16 Marcin Dabrowski: <https://orcid.org/0000-0003-0309-8050>

17

18 **Abstract**

19 Understanding how macroscopic fractures develop from interacting cracks is essential for describing brittle
20 deformation in upper-crustal rocks. Although empirical failure criteria successfully describe fracturing in
21 laboratory experiments, they do not explain how microcracks distributed within deforming rocks interact,



22 coalesce and organize into through-going fracture networks. In this study, we examine how the geometrical
23 distribution of pre-existing cracks controls the local stress perturbations that may influence fracture
24 formation. We use two-dimensional Finite Element Method-based numerical simulations to quantify the
25 elastic stress field around isolated cracks, *en echelon* crack arrays and randomly distributed crack systems
26 undergoing simple shear. The results show that crack orientation, and spacing strongly control the
27 distribution of reduced compression, effective cohesion, and localized strain around crack tips, and
28 determine whether local stress perturbations may promote or inhibit crack linkage. Favorably arranged crack
29 arrays produce overlapping lobes of reduced compression and local principal stress trajectories that
30 effectively connect neighboring crack tips, defining potential linkage paths oblique to the far-field maximum
31 principal stress. These findings suggest that shear fractures primarily develop from the overlap of tensile
32 stress perturbation regions around pre-existing cracks rather than being controlled solely by the far-field
33 stress or the geometry of mode I cracks formed during early stages of deformation. In highly anisotropic crack
34 configurations, the distribution forces shear fracture evolution and fault configurations along limited paths.
35 Conversely, rocks with isotropic crack distributions tend to preferentially activate *en echelon* arrays oriented
36 approximately at 30° relative to the far-field maximum principal stress, as predicted by the Coulomb criterion.
37 This research demonstrates that the distribution, and orientation of the pre-existing cracks exert a first-order
38 control over the mechanical evolution of shear fractures and faults, as well as the impact of crustal and
39 hydrostatic pressure variations on the conditions for failure and crack opening in upper-crustal rocks.

40

41 **1. Introduction**

42 Brittle deformation is common in the upper crust, where both temperature and effective pressure are low.
43 It typically occurs when stress exceeds rock strength (Segall and Pollard, 1983; Reches and Lockner, 1994;
44 Price, 1966), although brittle creep may operate under subcritical stress levels (Brantut et al., 2013). Under
45 brittle conditions, deformation is commonly accommodated by the development and propagation of
46 fractures (Sibson, 1986). Fractures are generally classified into two main categories: shear fractures or faults,



47 dominated by offset parallel to the walls, and extension fractures or joints, with opening displacement
48 perpendicular to their plane (e.g., Bahat, 1991; Bahat et al., 2005; Van der Pluijm and Marshak, 2004;
49 Atkinson, 2015; Scholz, 2019). While the terms shear and extension fractures are primarily used by
50 experimentalists to identify laboratory-scale structural discontinuities, the terms faults and joints are
51 commonly used to describe the corresponding large-scale structures observed in the field (Fossen, 2016).
52 Understanding the mechanisms of joint and fault formation is fundamental for predicting the mechanical
53 evolution and permeability structure of the upper crust (e.g., Sibson, 1977; Handy et al., 2007; Wibberley et
54 al., 2008). In particular, faults may act either as conduits or barriers to fluid transport, depending on their
55 geometry (Chester and Logan, 1986; Hooper, 1991; Hickman et al., 1995; Caine et al., 1996; Gudmundsson
56 et al., 2001). Moreover, since faults govern strain localization in the upper crust and play a key role in
57 earthquake nucleation, understanding their formation is essential for seismic risk assessment (Thatcher,
58 1975; Carlson et al., 1994; Harris, 2017).

59

60 **1.1 Introducing microcracks**

61 Early theoretical calculations of tensile strength based on the breaking of crystal lattice yielded values several
62 orders of magnitude higher than those required to fracture rock samples in laboratory tests (Orowan, 1949;
63 Scholz, 2019 and references therein). This apparent paradox was resolved by recognizing that polycrystalline
64 materials like rocks are largely inhomogeneous and, in particular, contain numerous microscopic, randomly
65 distributed structural flaws such as pores and grain boundaries (Griffith, 1920; 1924). When these flaws have
66 a planar geometry and lengths of millimeters or less, they are referred to as microcracks (Anders et al., 2014).
67 Microcracks are typically saturated with liquids or gases (Brace et al., 1968; Zoback and Byerlee, 1976). Due
68 to a prominent effect of stress concentration around favorably oriented cracks, failure can initiate locally and
69 develop into a macroscopic fracture even if the far-field stress remains below the strength of the intact rock
70 (Griffith, 1924; Pollard and Fletcher, 2005). When multiple cracks are closely spaced within a rock, they may
71 interact, either promoting or inhibiting crack growth depending on their relative orientation and separation



72 (Nabavi et al., 2017; Healy et al., 2006; McBeck et al., 2021). Therefore, microcracks play a crucial role in
73 controlling fracture nucleation and growth and, consequently, the macroscopic strength of rocks (Brace and
74 Bombolakis, 1963; Vermilye and Scholz, 1998; Paterson and Wong, 2005; Healy et al., 2006; Anders et al.,
75 2014; McBeck et al., 2023). The evolution and mechanical interaction of microcracks, however, strongly
76 depend on the stress conditions, particularly on confining pressure (e.g., Brace et al., 1966).

77 At low confining pressures, multiple tensile (mode I) cracks and resulting macroscopic extension fractures
78 parallel to the direction of $\vec{\sigma}_1^\infty$ accommodate most of the deformation, promoting axial splitting in uniaxial
79 experiments (Tapponnier and Brace, 1976; Martel et al., 1988; Twiss and Moores, 1992; Bobet and Einstein,
80 1998; Moir et al., 2010; Renard et al., 2017; Renard et al., 2018; McBeck et al., 2021). As lithostatic pressure
81 increases with depth, cracks tend to close and undergo frictional sliding along their contacting walls, marking
82 the transition toward the formation of shear rather than extension fractures (Ramsey and Chester, 2004; Liu
83 et al., 2022). At higher confining pressures, shear mode (mode II) cracks dominate microscopic brittle
84 deformation, especially when the deforming rock is on the verge of macroscopic failure, as indicated by
85 studies based on acoustic emission analysis (e.g., Stanchits et al., 2006; Graham et al., 2010).

86 1.2 Extension fractures

87 Laboratory observations show that extension fractures develop parallel to the far-field maximum principal
88 stress $\vec{\sigma}_1^\infty$ (e.g., Lawn, 1993; Pollard and Fletcher, 2005; Jaeger et al., 2009). Extension fractures may form
89 through the growth of mode I cracks (Tapponnier and Brace, 1976; Martel et al., 1988; Bobet and Einstein,
90 1998) under effective tensile stress, a condition that is rare and confined to the upper part of the Earth's
91 crust (e.g., Nur, 1982). Under a tensile stress regime, mode I cracks can propagate in-plane, a process that
92 has been extensively studied, both for subcritical (Obreimoff, 1930; Liebowitz, 1968; Evans, 1972; Atkinson,
93 1982) and dynamic conditions (Cook and Erdogan, 1972; Siegmund et al., 1997).

94 However, extension fractures can also form and propagate under remotely applied compressive stresses
95 (Griffith, 1920; 1924; Nemat-Nasser and Horii, 1982). Theoretical (e.g., Hoek and Bieniawski, 1965; Maugis,
96 1992) and experimental (Orowan, 1949; Brace and Bombolakis, 1963) studies have shown that tensile



97 stresses may locally develop and concentrate at the tips of microcracks oriented obliquely to the direction of
98 the major in-plane principal stress $\vec{\sigma}_1^\infty$. As a result of the local tension conditions in the microcrack tip zone,
99 new cracks can initiate and develop into the so-called wing cracks (e.g., Ashby and Hallam, 1986; Cannon et
100 al., 1990), which typically grow stably along curved paths, until their growth ceases once they align with the
101 direction of $\vec{\sigma}_1^\infty$ (Brace and Bombolakis, 1963; Pollard and Fletcher, 2005; Price, 1966). The linkage of multiple
102 oblique cracks through wing crack propagation can ultimately lead to the formation of macroscopic extension
103 fractures parallel to $\vec{\sigma}_1^\infty$ (Nicholson and Pollard, 1985). The development of extension fractures under a
104 compressive regime dominates brittle deformation at low confining pressure (up to ≈ 10 MPa), for which pore
105 fluid pressure can sufficiently reduce the effective pressure (Paterson and Wong, 2005) and promote crack
106 opening as well as lead to substantial tensile stress concentrations at the tips of favorably oriented cracks.

107

108 1.3 Shear fractures

109 Unlike opening cracks, shear cracks cannot grow through in-plane propagation (Brace and Bombolakis, 1963;
110 Erdogan and Sih, 1963; Liu, 1985). The linkage of wing cracks developing from the tips of multiple pre-existing
111 cracks has been suggested as the most plausible mechanism leading to crack coalescence into larger, system-
112 spanning shear fractures (e.g., Brace et al., 1966; Scholz, 1968; Hallbauer et al., 1973; Horii and Nemat-
113 Nasser, 1985; Petit and Barquins, 1988; Vermilye and Scholz, 1998; Healy et al., 2006; Renard et al., 2018;
114 McBeck et al., 2026). Experimental observations indicate that shear fractures typically form in conjugate pairs
115 and are oriented obliquely (typically at about $30\text{--}35^\circ$) relative to the direction of $\vec{\sigma}_1^\infty$ (e.g., Lawn, 1993; Pollard
116 and Fletcher, 2005; Jaeger et al., 2009). These observations are formalized mathematically in the Mohr-
117 Coulomb failure criterion, which applies in compressive stress regimes and adopts a linear relationship
118 between shear and normal stress on a critically stressed failure plane. It is valid at high confining pressures
119 ($>3\text{--}4$ MPa; Twiss and Moores, 1992) and predicts shear fractures oriented at approximately $\theta \approx \pm 30^\circ$ to $\vec{\sigma}_1^\infty$.
120 These angles are related to a material parameter, the angle of internal friction ϕ , which experimentally yields
121 values of $\approx 30\text{--}35^\circ$, according to the following relation:



122
$$\theta = \frac{\pi}{4} - \frac{\phi}{2} \quad (1)$$

123 A fundamental theoretical attempt to describe the formation of shear fractures through the coalescence of
124 mode I cracks, based on earlier theoretical studies (e.g., Brace et al., 1966; Scholz, 1968) was proposed by
125 Reches and Lockner (1994). They suggested that in an intact rock without pre-existing flaws, tensile cracks
126 form parallel to $\vec{\sigma}_1^\infty$ during the early stages of loading, and that tensile stress lobes elongating at
127 approximately $\pm 30^\circ$ relative to the crack direction emanate from their tips. When cracks cluster at
128 separations comparable to their lengths, the overlap of high local tensile stress regions between adjacent
129 crack tips promotes the development of fracture arrays oriented at $\approx \pm 30^\circ$ relative to $\vec{\sigma}_1^\infty$, thereby providing
130 a fundamental theoretical explanation for the observed macroscopic internal friction angles.

131 A related study was conducted by Vermilye and Scholz (1998), who interpreted fault growth as the
132 progressive development of tensile microfractures around propagating shear fracture tips. According to this
133 study, brittle shear fractures do not advance simply as in-plane mode II cracks. Instead, fault-tip stress
134 perturbations promote the nucleation, interaction and coalescence of mode I microfractures within the
135 process zone. The accumulation of these tensile cracks provides a mechanism by which distributed
136 microcracking can localize into a macroscopic shear fracture.

137 Healy et al. (2006) extended this concept proposing a three-dimensional model in which brittle shear
138 fractures form through the interaction and coalescence of many tensile microcracks. Their results show that
139 the geometry of the microcrack population and the elastic stress perturbations around individual cracks can
140 control the position and orientation of the resulting shear fracture surfaces. Their model suggests that tensile
141 crack interaction can generate more complex fracture patterns than those predicted by classical Mohr–
142 Coulomb theory, particularly under three-dimensional stress states. This highlights the importance of
143 considering not only the far-field stress, but also the geometry, orientation and spacing of interacting cracks.

144 However, all these models mainly consider the interaction between cracks parallel to $\vec{\sigma}_1^\infty$ and neglect
145 differently oriented pre-existing flaws. Consequently, only a single possible orientation for shear fractures
146 formed through crack coalescence is predicted, which contradicts field and laboratory observations



(Anderson, 1905; Peacock and Sanderson, 1995; Bobet and Einstein, 1998; Tang et al., 2001; Wong et al., 2001; Kim et al., 2003; 2004; Crider and Peacock, 2004; Chang et al., 2015; Zhou et al., 2015; Kanaya and Hirth, 2024). Moreover, recent work has shown that if clustered, interacting cracks parallel to $\vec{\sigma}_1^\infty$ are arranged in alternating left-right steps, the stress interference at their tips should favor the formation of new fractures parallel to $\vec{\sigma}_1^\infty$, rather than oblique shear fractures (McBeck et al., 2023). This underlines the importance of considering simplified but realistic geometrical arrangements of interacting cracks in brittle rocks, such as *en echelon* cracks.

1.4 *En echelon* cracks

En echelon arrays, consisting of closely-spaced cracks in a stepped configuration, are common features in upper-crustal rocks (Cosgrove and Engelder, 2004; de Joussineau and Aydin, 2007; Peacock et al., 2016; Sanderson and Peacock, 2019; Beach, 1975; Segall and Pollard, 1980; La Pointe and Hudson, 1985; Rothery, 1988). The regular geometry of *en echelon* crack arrays enables inferences regarding the tectonic stress during their formation (Roering, 1968; Jackson, 1991; Wiltschko et al., 2009). These interpretations mostly derive from field observations of vein and crack arrays mapped at the outcrop scale (Roering, 1968; Beach, 1975; Jackson, 1991; Peacock and Sanderson, 1995; Willemse, 1997; Kelly et al., 1998; Wiltschko et al., 2009). In shear zones, *en echelon* arrays progressively rotate and stretch during deformation producing sigmoidal vein geometries that serve as valuable kinematic indicators (Bons et al., 2012; Lisle, 2013). Nevertheless, kinematic analysis is not sufficient to explain the spacing, lengths, and geometry of *en echelon* cracks (Pollard and Fletcher, 2005; Seyum and Pollard, 2016). In fact, the magnitude of the near-tip stress of each crack in the array is perturbed by the neighboring cracks, to a degree which mainly depends on their overlap and orientation (Pollard et al., 1982; Du and Aydin, 1991; Mandal, 1995; Chau and Wang, 2001; Seyum and Pollard, 2016), and the interactions may lead to curved crack trajectories (Pollard et al., 1982; Du and Aydin, 1991; Chau and Wang, 2001; Seyum and Pollard, 2016). In *en echelon* crack arrays, bridges of wall rock experience highly concentrated strains and may ultimately fail, leading to the linkage of neighboring cracks (Nicholson and Pollard, 1985). These regular crack systems may therefore act as precursory structures to faults (de Joussineau and Aydin, 2007; Crider, 2015). Both in crystalline and sedimentary rocks, faults typically



173 develop through the linkage of pre-existing features such as cracks, mineral cleavages, veins and other types
174 of discontinuities (Shipton and Cowie, 2001; de Joussineau and Aydin, 2007; Faulkner et al., 2010). This
175 indicates that regular crack arrays play a crucial role in the incipient stages of macroscopic fault zone
176 development (Kranz, 1979; Wong, 1982; Gottschalk et al., 1990; Moore and Lockner, 1995; Crider, 2015).
177 Conversely, propagating faults control the growth and linkage of cracks in a highly-stressed process zone
178 ahead of the fault tip (Granier, 1985; Cox and Scholz, 1988; Lockner et al., 1991; Moore and Lockner, 1995;
179 Reches and Lockner, 1994).

180

181 **1.5 Step faults**

182 Step faults may be viewed as macro-scale analogues to the *en echelon* crack arrays observed at the micro-
183 scale (Segall and Pollard, 1983; Pollard and Segall, 1987; Kim and Sanderson, 2005; Aydin et al., 2006; de
184 Joussineau and Aydin, 2007; Nabavi et al., 2017; Faulkner et al., 2010). Although strike-slip faults may be
185 observed as linear, continuous features at large scales, they typically consist of multiple, subparallel
186 segments, separated by step-like bridges (Childs et al., 2009; Faulkner et al., 2010). These bridging segments
187 interact producing local stress field perturbations, similarly to systems of *en echelon* cracks (Segall and
188 Pollard, 1983; Pollard and Segall, 1987; Dasgupta and Mukherjee, 2017). The geometry of the steps is the key
189 parameter governing fault segment interactions. Depending on the orientation of the fault segments relative
190 to the direction of regional tectonic compression, extensional or contractional stepovers develop respectively
191 for the step sense matching or opposite to the sense of fault slip (Biddle and Christie-Blick, 1985; Christie-
192 Blick and Biddle, 1985; Woodcock and Fischer, 1986; Sylvester, 1988; Woodcock and Schubert, 1994;
193 Westaway, 1995; Cunningham and Mann, 2007; Mann, 2007). Field, analytical, analogue, and numerical
194 studies consistently demonstrated that the evolution of step faults depends on the overlap between fault
195 segments, and their relative orientation (Rodgers, 1980; Mann et al., 1983; Pollard and Segall, 1987;
196 Bürgmann and Pollard, 1994; Willemse et al., 1996; Kim and Sanderson, 2005; Li et al., 2009; Kristensen et
197 al., 2008; Childs et al., 2009; Strijker et al., 2013; Nevitt et al., 2014; Nevitt, 2015).



198

199 **1.6 Linear Elastic Fracture Mechanics**

200 The mechanical description of crack growth is commonly addressed using Linear Elastic Fracture Mechanics
201 (LEFM), which derives conceptually from Griffith's energy balance approach (Griffith, 1920; Atkinson, 2015
202 and references therein). Loading a crack embedded in an elastic medium results in stress diverging as $r^{-\frac{1}{2}}$ in
203 the near-tip zone, where r is the distance from the crack tip (Irwin, 1957; Rice, 1968; Pollard and Fletcher,
204 2005; Atkinson, 2015; Price, 1966). To address the problem of this unphysical stress singularity inherent in
205 linear elastic models of cracks, the stress intensity factor K is introduced in LEFM, a mode-sensitive quantity
206 which remains finite and depends on loading conditions and crack geometry. Specifically, the near-tip stress
207 tensor components σ_{ij} are defined as follows:

$$208 \quad \sigma_{ij} = \frac{K f_{ij}(\vartheta)}{\sqrt{2\pi r}} \quad (2)$$

209 The indices i and j identify spatial components, σ_{ij} are stress tensor components at a (small) distance r from
210 the tip and f_{ij} are angular functions of the polar angle ϑ measured from the crack tip. The mode I stress
211 intensity factor K_I , for example, is:

$$212 \quad K_I = \frac{\sigma_{ij} \sqrt{2\pi r}}{f_{ij}(\vartheta)} \quad (3)$$

213 In the framework of LEFM, crack propagation intensifies when K approaches the fracture toughness (K_C), a
214 material parameter typically ranging between 1 and 3 $\text{MPa} \cdot \text{m}^{\frac{1}{2}}$ for rocks. In this case, crack growth is stable
215 and is referred to as subcritical crack growth, where propagation velocity is proportional to the stress
216 intensity factor (Brantut et al., 2013). If the stress intensity factor exceeds the fracture toughness, unstable
217 growth occurs at velocities often comparable to the speed of sound in the medium (Irwin and de Wit, 1983,
218 Atkinson, 2015).

219



220 1.7 Macroscopic failure criteria

221 Although LEFM provides a solid framework for the description of stress near a crack tip and subsequent crack
222 growth, an alternative approach relies on macroscopic failure criteria to predict fracture nucleation. In this
223 framework, a fracture is assumed to initiate when stresses satisfy a given mathematical criterion. The
224 simplest is the tensile criterion, according to which failure occurs when the minimum principal stress exceeds
225 tensile strength T_0 of the rock, that is:

$$226 \quad \sigma_2 \leq -T_0 \quad (4)$$

227 The Mohr-Coulomb criterion, which relates the shear strength τ of a rock to the applied normal stress σ_n , is
228 expressed as:

$$229 \quad \tau = C + \mu \sigma_n = C + \tan \phi \sigma_n \quad (5)$$

230 where C is the cohesion, μ is the coefficient of internal friction and ϕ is the angle of internal friction of the
231 rock. As introduced above, the Mohr-Coulomb criterion predicts failure on planes oriented at $\theta = \frac{\pi}{4} - \frac{\phi}{2}$ with
232 respect to $\vec{\sigma}_1^\infty$. If the resolved shear stress on such planes exceeds the shear strength for the given stress
233 state, a fracture is expected to nucleate. Both these macroscopic failure criteria allow the identification of
234 potential fracture nucleation sites and fault orientations (e.g., Pollard and Fletcher, 2005; Jaeger et al., 2009;
235 Fossen, 2016). Macroscopic failure criteria have been widely applied to large-scale geological problems, such
236 as the prediction of dyke propagation paths and fault geometries (e.g., Pollard and Fletcher, 2005;
237 Gudmundsson, 2011). If the rock contains a distribution of pre-existing flaws, these approaches can also be
238 relevant at the meso- and micro-scale, where the failure criteria can be interpreted as an effective description
239 of the collective behavior of interacting microcracks (e.g., Ashby and Sammis, 1990; Amitrano, 2003;
240 Schmittbuhl et al., 2003).

241

242 1.8 Outlook



243 In this study, we examine the tendency for fracture formation in regions of reduced stress (potential effective
244 tensile stress) due to the presence of preexisting cracks, under the hypothesis that large fracture networks,
245 including faults, are controlled by stress perturbations generated by pre-existing cracks during elastic
246 deformation. Using Finite Element Method-based simulations, we analyze stress and strain fields in systems
247 containing *en echelon* and randomly distributed cracks, relying on macroscopic failure criteria to evaluate
248 potential favorable conditions for brittle deformation.

249

250 **2. Methods**

251 We used a Matlab-based implementation of the Finite Element Method (FEM) for plane strain 2D linear
252 elasticity to study the stress and strain fields around pre-existing cracks approximated by elliptical voids. We
253 developed two different types of models: i) *en echelon* arrays of aligned cracks with varying separation and
254 orientation relative to the major in-plane principal stress $\vec{\sigma}_1^\infty$, and ii) randomly located cracks with variable
255 length and degree of their alignment. The second-order shape functions (interpolation space in the FEM
256 formulation) (Hughes, 2003; Bathe, 2006) combined with unstructured, body-fitting triangular meshes allow
257 for highly accurate solutions even in complex computational domains, including systems with internal
258 discontinuities (Moës et al., 1999; Dabrowski et al., 2008; Chen, 2012; Zhao et al., 2018). We used six-node
259 triangular elements, and the computational meshes were generated using the Triangle mesh generator,
260 developed by Shewchuk (1996, 2002). The linear elastic models are formally scale-independent, and the
261 spatial dimensions are non-dimensionalized using the crack length. The models and the obtained stress and
262 strain fields can be upscaled or downscaled to the scale of interest in a straightforward manner (e.g., Goodier
263 & Hodge Jr., 2016). Other studies (e.g., Chinnery, 1963; Resor and Flodin, 2010; Atkinson, 2015; Castelletto
264 et al., 2017; Menegoni et al., 2024) have demonstrated that linear elastic models can be useful for evaluating
265 stress conditions that are critical for localizing permanent strains, thereby contributing to the formation of
266 geological structures at various scales, from small to large. All reported results are normalized: each stress



267 and strain component locally computed using FEM is normalized by the representative background value,
268 i.e., the principal value of stress and strain that would be attained in the absence of cracks.

269 The approach of using highly-elongated elliptical voids to approximate friction-less cracks in rocks has been
270 adopted in multiple studies (e.g., Yang and Soh, 2002; Bertoldi et al., 2007; Niu et al., 2024). An analytical
271 solution for the displacement and stress fields around an isolated and highly elongated elliptical void
272 embedded in a medium undergoing homogeneous elastic deformation in the far field (e.g., Pollard, 1987;
273 Meguid et al., 1991; Schmid and Podladchikov, 2003; Jaeger et al., 2009) provides valuable insights into the
274 slip magnitude and stress concentration around friction-less cracks as well as an opportunity to test
275 numerical codes. Although representing two-dimensional slit cracks as ellipses rather than sharp lines using
276 the approach of contact elements (Johnson, 1987) is convenient for numerical modeling, caution must still
277 be exercised against element interpenetration and overlap.

278 Slit cracks offer a versatile way to study different types of discontinuous structures within rocks. For example,
279 multiple colinear cracks may represent rough fractures, which can be modeled as a series of thin voids
280 representing the alternation of non-contacting wall patches and contact asperities (Feng and Gross, 2000;
281 Myer, 2000). Models with randomly distributed but aligned cracks can be used to simulate mechanical effects
282 related to bedding and schistosity in sedimentary and metamorphic rocks, respectively (e.g., Nicksiar and
283 Martin, 2013). Similarly, a distribution of microscopic cracks that are randomly positioned and oriented can
284 be used to model grain boundaries in granular and polycrystalline media or the random distribution of crystal
285 lattice defects in undeformed magmatic rocks (Graham et al., 2010; Fattaruso et al., 2022).

286 The number of points used for discretizing input ellipses in each model was selected to optimize geometric
287 resolution while avoiding excessive computational cost. The nodal coordinates are defined using an elliptic
288 parametrization, such that all points on the ellipse satisfy $x_i = a \cos \eta_i$ and $y_i = b \sin \eta_i$, with $\eta_i = i * 2\pi/1000$, $i = 0, 1, 2, \dots, N_{ell} - 1$. In the *en echelon* crack models, which contain a limited number of cracks
290 (10), the perimeter of each crack is discretized using $N_{ell}=1000$ nodal points. In contrast, in the randomly
291 distributed crack models, which include a much larger number of cracks (500), each crack perimeter is



292 discretized using $N_{ell}=360$ nodes to limit computational cost while preserving sufficient numerical resolution
293 (computational meshes exceeding 5 million triangular elements were used for the random models). The
294 aspect ratio of the ellipses is set to 10000 in the *en echelon* crack models and to 1000 in the randomly
295 distributed crack models.

296

297 **3. Model setup**

298 The structural geology and rock mechanics sign convention, in which compressive stresses are taken as
299 positive, is adopted in this study. All the studied strain and stress distributions are obtained from two-
300 dimensional, plane-strain numerical simulations, where the xy plane represents the modelled cross-section.
301 The local magnitudes of the major and minor in-plane principal stresses are denoted as σ_1 and σ_2 ,
302 respectively. Under plane strain conditions, the out-of-plane principal stress typically acts as the intermediate
303 component, its magnitude depending on the Poisson's ratio and the nature of the far-field loading. The
304 vectors indicating the local orientation of the principal stresses are labeled as $\vec{\sigma}_1$ and $\vec{\sigma}_2$, respectively.

305 We use P^∞ to denote the far-field hydrostatic stress, which represents the action of the lithostatic pressure
306 due to overburden weight. Because our objective is to investigate the stress perturbation due to the presence
307 of cracks, the results are expressed in terms of reduced stresses, which are calculated by subtracting the
308 lithostatic pressure, thus representing the non-lithostatic stress component. We assume sufficiently high
309 pore fluid pressure in the cracks to maintain their aperture open. For pore fluid pressure approaching the
310 lithostatic pressure, the reduced stress would directly correspond to the effective stress. The key stress
311 quantity analyzed in each model is the reduced and normalized magnitude of the minor in-plane principal
312 stress $\tilde{\sigma}_2 = (\sigma_2 - P^\infty)/(\sigma_1^\infty - P^\infty)$. Negative values of $\tilde{\sigma}_2$ indicate sublithostatic stress states, or potentially
313 effective tension, whereas positive values correspond to elevated compression, with the least compressive
314 principal stress locally exceeding the background lithostatic load. For crack systems that produce strongly
315 negative local values of $\tilde{\sigma}_2$, we identify regions where the minor in-plane principal stress potentially
316 approaches or exceeds the tensile strength of the rock. Therefore, it may lead to nucleation and growth of



317 tensional fractures, facilitating the coalescence of the pre-existing cracks or faults into either macroscopic
318 fractures or larger-scale faults, respectively.

319 To evaluate the potential conditions for nucleation of shear fractures under different confining pressures P^∞
320 and pore fluid pressures P_f , we rely on the following formulation of the Mohr-Coulomb macroscopic failure
321 criterion:

$$322 \quad \tau_m - (\sigma_m - P^\infty) \sin(\phi) = (P^\infty - P_f) \sin(\phi) + C \cos(\phi) \quad (6)$$

323 where C is the cohesion, ϕ is the angle of internal friction (which is set to 35° in our models, a value consistent
324 with experimental results for unweathered rocks),

$$325 \quad \tau_m = \frac{\sigma_1 - \sigma_2}{2} \quad (7)$$

326 is half the local in-plane differential stress and

$$327 \quad \sigma_m = \frac{\sigma_1 + \sigma_2}{2} \quad (8)$$

328 is the local in-plane mean stress. The calculation of the in-plane principal stress components allows us to
329 evaluate the confining pressure- and fluid pressure-dependent normalized effective cohesion $\tilde{C}$, defined as:

$$330 \quad \tilde{C} = [C + (P^\infty - P_f) \tan(\phi)] / (\sigma_1^\infty - P^\infty) = [\frac{\tau_m}{\cos(\phi)} - (\sigma_m - P^\infty) \tan(\phi)] / (\sigma_1^\infty - P^\infty) \quad (9)$$

331 $\tilde{C}$ represents the stress threshold for activating shear fractures between pre-existing cracks for specific values
332 of P^∞ and P_f . If the rock cohesion for a specific stress state is not sufficiently high for the local value of $\tilde{C}$,
333 conjugate shear fractures may develop at angles

$$334 \quad \theta = \pm \left(\frac{\pi}{4} - \frac{\phi}{2} \right) \quad (10)$$

335 with respect to the local orientation of $\vec{\sigma}_1$.

336 We also analyze the distributions of the normalized first invariant of the strain tensor $\bar{I}_1 = tr(\vec{\epsilon})$ and of the
337 normalized shear strain $\bar{\epsilon}_{xy}$, to estimate local volumetric deformation and the local amplification of the far-



338 field shear deformation, respectively. Positive values of $\bar{I}_1$ represent dilation, whereas negative values
339 represent contraction.

340 In all models, right-lateral simple shear deformation is applied to the system by prescribing a shear strain
341 value of $\gamma = 10^{-3}$. Any initial stress variations due to the difference between the pore fluid pressure in the
342 cracks and background lithostatic pressure are discarded. The material parameters representing the bulk
343 properties of the rock undergoing elastic deformation were taken from Tal et al. (2018), which focuses on
344 the nucleation of earthquakes on rough faults. The Young's modulus of the rock is set to 60 GPa, and the
345 Poisson's ratio is 0.25. These values fall within the range of experimentally determined elastic parameters
346 for the most common crustal rocks such as granite and limestone. The simple shear loading generates a 48
347 MPa differential stress $\sigma_1^\infty - \sigma_2^\infty$ in the far field, which corresponds to a 24 MPa deviatoric stress $\sigma_1^\infty - P^\infty$
348 that is equal to the reduced major in-plane principal stress. Nevertheless, the obtained stress magnitudes
349 are presented as normalized and reduced stresses that are independent, for the analyzed setup, from the
350 specific value of the Young's modulus and Poisson's ratio.

351 Elastic deformation and stress distributions in rocks with pre-existing cracks are simulated for two distinct
352 geometries: i) *en echelon* array of cracks, and ii) randomly distributed cracks.

353

354 **3.1 En echelon cracks**

355 In the first model, we examine *en echelon* systems consisting of multiple slit cracks of the same orientation
356 ϑ and a constant half-length a , whose centers are aligned along a straight line inclined at an angle φ . All
357 angles are measured counterclockwise from the horizontal orientation that corresponds to the shear
358 direction. The crack array is placed in the center of a square computational domain, with the side length L
359 set to $1000 \cdot a$ to minimize the boundary effects (Fig. 1A). 10 cracks are used to form the array and the stress
360 distributions are analyzed around the centrally located ellipses that are expected to approximate conditions
361 for periodic *en echelon* crack arrays.



362 We performed four sets of parametric experiments. In the first set, we varied the normalized projected
363 overlap d , defined as:

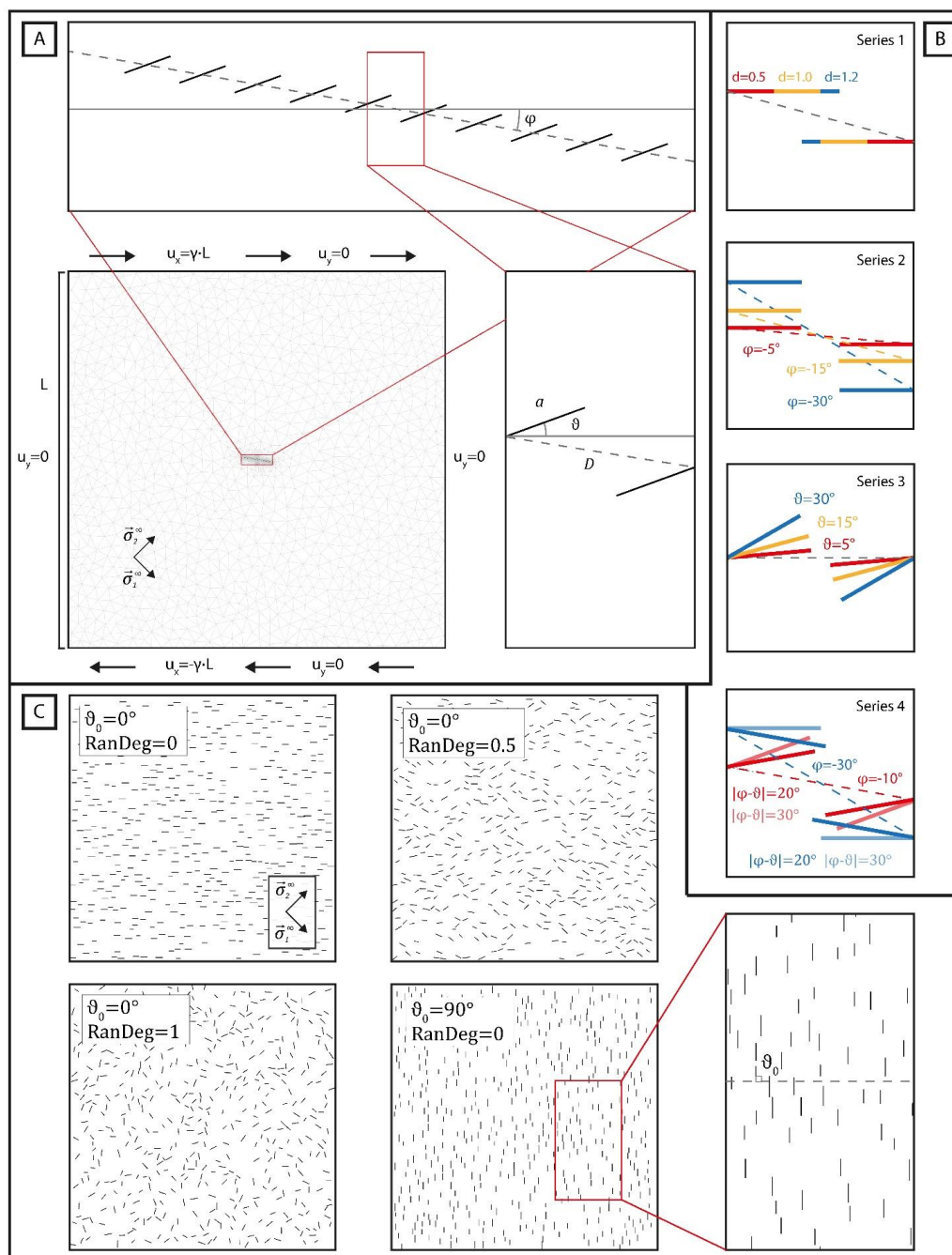
364
$$d = \frac{2a}{D|\cos(\varphi - \vartheta)|} \quad (11)$$

365 where D denotes the distance between the centers of adjacent cracks. In this set of experiments, we
366 considered models with d ranging from 0.5 (minimum crack overlap, corresponding to a configuration, in
367 which the projection of the distance between adjacent crack centers onto the crack direction equals twice
368 the crack length) to 1.2 (Fig. 1A). A configuration with $d=1$ corresponds to the case where the projections of
369 the crack tips onto the crack direction coincide into a single point, or, equivalently, the projected distance
370 between the crack centers along the same direction equals the crack length. The crack orientation ϑ is set to
371 0° , and two symmetrical configurations with $\varphi=\pm 15^\circ$ are considered. In the second set of experiments, we
372 varied the inclination φ of the crack array over the ranges -45° to -5° (Fig. 1A) and, symmetrically, 5° – 45° ,
373 including the collinear crack configuration ($\varphi=0^\circ$). In this set, ϑ was fixed at 0° and d was set to 0.8 (Fig. 1A).
374 In the third set, we varied the crack orientation ϑ between -45° and -5° and, symmetrically, 5° – 45° , with φ
375 fixed at 0° and d set to 0.9 (Fig. 1A). In the fourth set of experiments, we varied d between 0.8 (underlapping
376 cracks) and 1.2 (overlapping cracks), and simultaneously varied ϑ and φ such that their difference ranged
377 between -30° and 30° in 10° steps, while φ was set to 0° , $\pm 10^\circ$, $\pm 20^\circ$ (Fig. 1B).

378



379



380

381 Fig. 1: (a) A square domain of width L with an embedded array of *en echelon* cracks in the center subject to

382 simple shear. In the first inset, the *en echelon* array of 10 cracks is illustrated. The array forms an angle φ



383 with respect to the horizontal shear direction. In the second inset, the two central cracks in the system are
384 shown. The crack half-length is a , the distance between their centers is D and their orientation with respect
385 to the horizontal is ϑ . (b) Representative examples of model setups for the four sets of simulations with *en*
386 *echelon* cracks. Series 1: variable projected overlap d . Series 2: variable array inclination φ . Series 3: variable
387 crack orientation ϑ . Series 4: variable φ and $\varphi - \vartheta$. (c) Representative configurations of models with
388 randomly distributed slit cracks. Both the crack orientation ϑ_0 and the degree of randomness in crack
389 orientation *RanDeg* are varied. In the inset, a local crack distribution in the model with $\vartheta_0 = 90^\circ$ and
390 *RanDeg* = 0 is illustrated.

391

392 3.2 Randomly distributed cracks

393 The second set of models consists of multiple, non-intercepting slit cracks of varying sizes, with crack half-
394 length a randomly drawn from a uniform distribution spanning $0.5 \cdot 10^{-3}L$ to $10^{-2}L$. The cracks are
395 randomly distributed in terms of their positions, and their orientations are either randomized to a varying
396 degree or fully aligned (Fig. 1C). In the numerical procedure used for generating the input model, the crack
397 length and orientation are first drawn from their distributions, and then the crack is randomly placed within
398 the domain. If it overlaps with the previously added cracks or intersects the domain boundaries, a new
399 random position for its center is generated. This random sequential addition procedure may result in a bias
400 between the intended and resulting distribution of crack lengths and orientations. For example, longer cracks
401 are more likely to be rejected due to the non-intersection constraint. However, this effect is expected to be
402 small for the studied crack densities. The geometry of several model realizations is illustrated in Fig. 1C.

403 The geometrical distribution of cracks within the domain is controlled using two key parameters:

- 404 • Crack orientation
- 405 • Degree of randomness in crack orientation

406 When the degree of randomness is set to zero, all cracks are aligned in a specific direction, representing rocks
407 with a strong structural anisotropy due to crack alignment. Slightly increasing the randomness parameter



408 results in a more realistic model, in which cracks maintain a preferred orientation but include small random
409 deviations from the mean orientation (Fig. 1C). A maximum randomness value of 1 represents a fractured
410 rock with an isotropic structure (Fig. 1C), or, if crack density is low, an intact rock with randomly distributed
411 microcracks. The relationship between the trial orientation of the i -th crack ϑ_i and the degree of randomness
412 of the system $RanDeg$ is described by the following equation:

$$413 \quad \vartheta_i = \vartheta_0 + RanDeg \cdot \left(\pi \cdot RN_i(0,1) - \frac{\pi}{2} \right) \quad (12)$$

414 In this equation, ϑ_0 is a fixed angle representing the orientation of all cracks when $RanDeg$ is set to zero.
415 $RN_i(0,1)$ is a random number uniformly distributed in the interval (0,1), varying for each crack. If $RanDeg=0$,
416 all cracks are aligned and $\vartheta_i = \vartheta_0$ for all i (Fig. 1C). As $RanDeg$ increases, the angles ϑ_i are allowed to vary
417 randomly within an interval proportional to $RanDeg$. When $RanDeg=1$, each ϑ_i is a completely random
418 angle in the range $\left[\vartheta_0 - \frac{\pi}{2}, \vartheta_0 + \frac{\pi}{2} \right]$ (Fig. 1C).

419 Different models were analyzed by keeping the domain area fixed while varying the number of cracks. Here,
420 we present the results for the models with the highest crack concentration, which embedded 500 cracks (Fig.
421 1C). The average crack non-dimensional density P_{22} of these models can be defined as (Sanderson and Nixon,
422 2015):

$$423 \quad P_{22} = \frac{N l_c^2}{L^2} \quad (13)$$

424 where l_c is the mean crack length:

$$425 \quad l_c = \frac{\sum_{i=1}^N 2a_i}{N} \quad (14)$$

426 and L is the length of a side of the domain. $P_{22}=0.055$. Despite the low crack density, mechanical interactions
427 between cracks remain significant, meaning they cannot be treated as isolated cracks (Kachanov, 1992).

428 We analyzed a total of 16 configurations, varying the angle ϑ_0 over 0° , 45° , 90° , and -45° and $RanDeg$ over
429 the values 0, 0.25, 0.5 and 1. The four configurations with $RanDeg=1$, although differing in details, effectively
430 produce the same model, therefore the number of unique configurations is 13.



431

432 **4. Results**

433 In this section, we present the results of our numerical simulations. The first subsection revisits the classical
434 results for isolated cracks. The second subsection presents the results for models with *en echelon* systems of
435 slit cracks. In the third subsection, we examine the results of models with randomly distributed cracks.

436

437 **4.1 Isolated crack**

438 In this subsection, we examine the classical results on the distribution of the least compressive stress around
439 an isolated crack with characteristic orientations, such as mode I and II. To isolate from the effects due to
440 lithostatic load and the specific level of simple shear, we use the reduced and normalized minor in-plane
441 principal stress magnitude $\tilde{\sigma}_2$. The results show that the mode I and II crack orientations generate
442 distinctively shaped regions of reduced compressive stress, which may potentially correspond to sites of
443 effective tensile stress.

444 Fig. 2 illustrates the stress distributions around two classes of cracks defined by their orientation: cracks
445 parallel (Fig. 2A) and oblique (Fig. 2B) to the principal stress axes. Cracks parallel to the direction of major in-
446 plane far-field principal stress $\vec{\sigma}_1^\infty$ are referred to as mode I cracks, whereas those oriented at $\pm 45^\circ$ are named
447 mode II cracks.

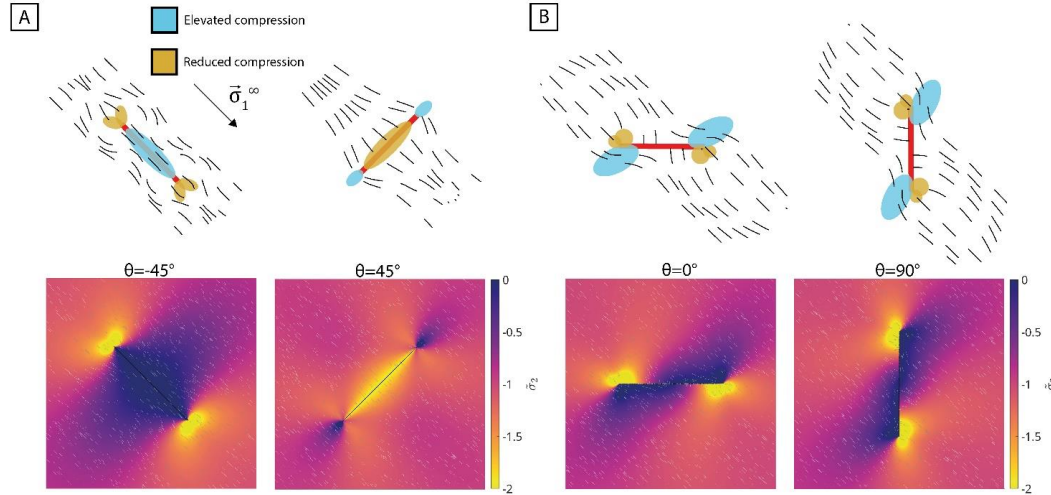
448 For mode I cracks, regions of reduced compression, which could be associated with effectively tensile stress,
449 preferentially occur in two symmetrical lobes emanating from the crack tips at a low angle relative to the
450 crack elongation. For cracks oriented perpendicular to $\vec{\sigma}_1^\infty$, the effective tensile stress may develop within an
451 elliptically shaped region located around their centers (Fig. 2A). Elevated compressive stresses concentrate
452 within elliptically shaped regions enveloping mode I cracks and occur in single lobes radiating from the tips
453 along the crack direction for cracks oriented perpendicular to $\vec{\sigma}_1^\infty$ (Fig. 2A).



In mode I orientation, we observe that the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$ fan out around the crack tips, then progressively reconverge toward the crack and align with its major axis next to it (Fig. 2A). In contrast, for cracks oriented perpendicular to the far-field compression direction $\vec{\sigma}_1^\infty$, the local trajectories of the major in-plane principal stress curve toward the tips, while remaining perpendicular to the crack around its center (Fig. 2A).

459

460



461

Fig. 2: Top: Schematic illustrations of reduced and elevated compressive stress regions around isolated mode I and II cracks. Bottom: Distributions of the minor in-plane principal stress magnitude $\bar{\sigma}_2$. White and black lines indicate the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$. (a) Mode I cracks oriented at 0° and 90° (left to right) relative to the direction of the far-field principal compression axis $\vec{\sigma}_1^\infty$. (b) Mode II cracks oriented at $\pm 45^\circ$ relative to $\vec{\sigma}_1^\infty$.

467

For the mode II cracks, which are oriented at $\pm 45^\circ$ relative to the direction of $\vec{\sigma}_1^\infty$, zones of reduced compression or potentially effective tensile stress concentrate in paired lobes that emanate asymmetrically from each crack tip towards the compressive quadrants of the far-field simple shear. The lobes are oriented at $\pm 30^\circ$ relative to $\vec{\sigma}_1^\infty$, forming angles of -15° and -75° relative to the crack direction (Fig. 2B). Single lobe-



472 shaped regions of elevated compression, elongating at approximately $\pm 90^\circ$ relative to $\vec{\sigma}_1^\infty$ are located on the
473 opposite sides of the tip regions (Fig. 2B).

474 The local trajectories of the major in-plane principal stress $\vec{\sigma}_1$ deflect around mode II cracks, aligning with
475 their orientation in the regions characterized by elevated compression and becoming sub-perpendicular to
476 the crack in areas of reduced compressive stress (Fig. 2B).

477

478 **4.2 En echelon cracks**

479 In this set of numerical experiments, we simulated stress perturbation around *en echelon* crack arrays to
480 assess their mechanical interaction and tendency for reactivation and potential coalescence into macroscopic
481 fractures. We again focus on the reduced and normalized minor in-plane principal stress magnitude $\tilde{\sigma}_2$. We
482 analyze how (i) the spatial distribution of potential sites of effective tension $\tilde{\sigma}_2$ (i.e., negative $\tilde{\sigma}_2$ values)
483 between neighboring cracks, (ii) the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$, (iii) normalized
484 effective cohesion $\tilde{C}$, (iv) the normalized first invariant of the strain tensor $\bar{I}_1$ and (v) the normalized shear
485 strain $\bar{\epsilon}_{xy}$ vary as a function of three geometric parameters: the projected overlap between neighboring
486 cracks along their major axis d , the orientation of the *en echelon* array φ with respect to the far-field major
487 compression direction, and the inclination of the cracks ϑ within the array.

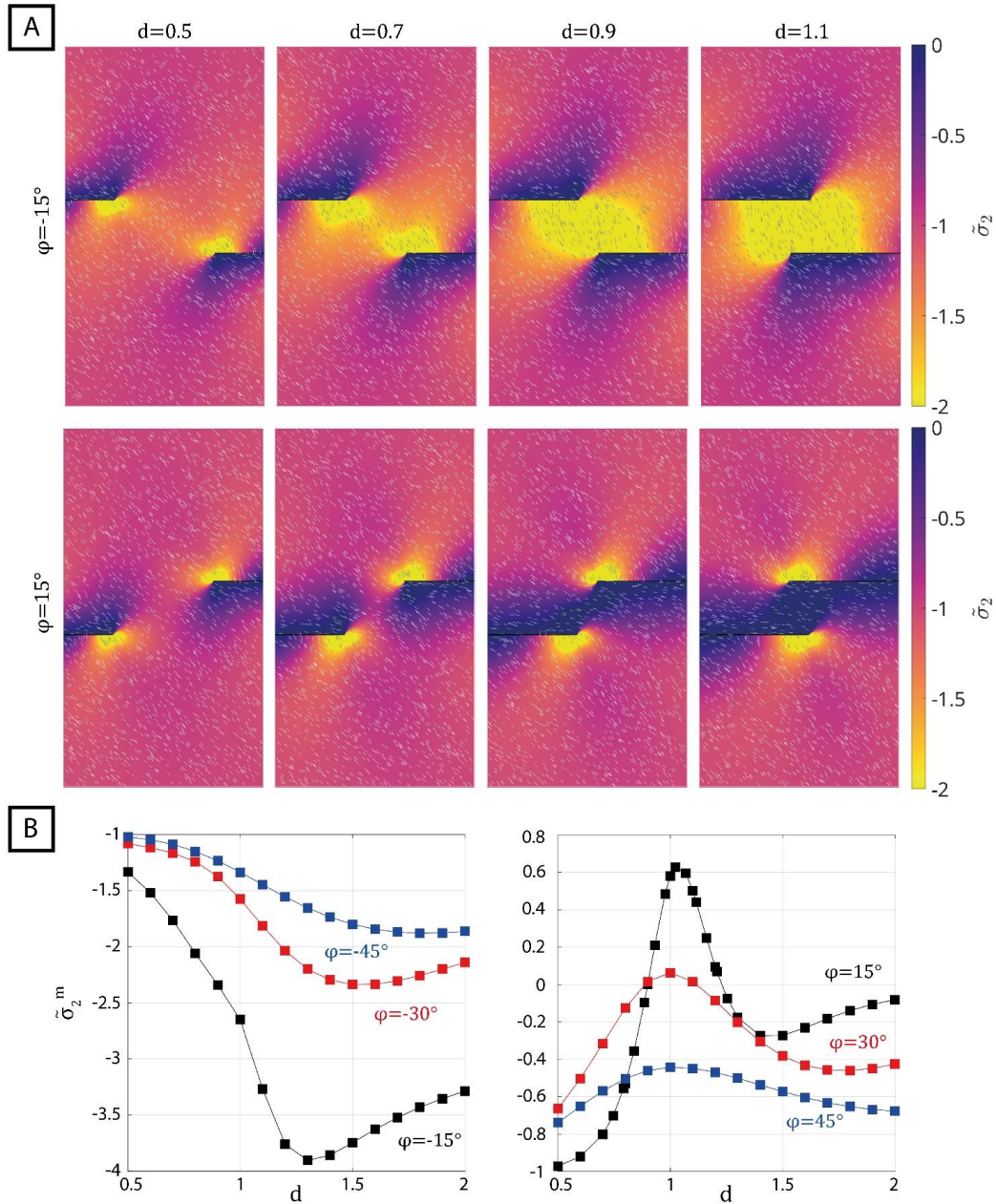
488 Fig. 3A illustrates the distribution of $\tilde{\sigma}_2$ around horizontally oriented cracks ($\vartheta=0^\circ$; mode II with respect to
489 simple shear applied in the far field) arranged in arrays oriented at $\varphi=\pm 15^\circ$ relative to the shearing direction,
490 for d values ranging from 0.5 to 1.1. Equivalent configurations for vertical mode II cracks and for collinear
491 model-oriented cracks are shown in Fig. A1. A systematic trend emerges: for $\varphi=-15^\circ$, decreasing crack
492 separation promotes the coalescence of reduced compressive stress zones between the crack tips (Fig. 3A).

493 In contrast, for $\varphi=15^\circ$, regions of elevated compression merge and amplify between adjacent crack tips (Fig.
494 3A).

495



496



497

498 Fig. 3: (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$ for different geometric configurations of *en*
 499 *echelon* crack arrays. Only the central unit cell is shown. Crack orientation: $\vartheta=0^\circ$ (mode II cracks relative to
 500 far-field simple shear). In each row, the array orientation φ is fixed: -15° (top) and 15° (bottom). Along each



row, d varies from 0.5 to 1.1. White and black lines indicate the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$. (b) Normalized and reduced minor in-plane principal stress magnitude $\vec{\sigma}_2^m$ calculated at the midpoint between the neighboring crack tips in an array of *en echelon* cracks oriented at $\vartheta=0^\circ$ as a function of the projected overlap d . Different colors represent different crack array orientations φ . The symmetrical configurations with $\varphi = \pm 15^\circ$, $\pm 30^\circ$, and $\pm 45^\circ$ are illustrated in the right and left panel, respectively.

507

For the $\varphi=-15^\circ$ configuration, mechanical interaction between neighboring cracks is weak at $d=0.5$ (Fig. 3A). The shapes of the reduced compression lobes are similar to those of isolated cracks described in the previous section, and the deflection of $\vec{\sigma}_1$ is mostly limited to the immediate vicinity of the crack tips. At $d=0.7$, mechanical interaction between the neighboring cracks strengthens, and partial overlap of strongly depressed compressive stress regions ($\vec{\sigma}_2 < -2$) is observed (Fig. 3A). In this configuration, the trajectories of $\vec{\sigma}_1$ slightly deflect between adjacent tips, particularly near the boundaries of the reduced compression regions, where they follow the contours of the $\vec{\sigma}_2$ perturbation. The configuration with $d=0.9$ represents the most effective geometric arrangement for overlap of reduced compression (potentially effective tension) regions around individual crack tips, which merge into regular, elliptically shaped areas connecting adjacent tips (Fig. 3A). In this configuration, the trajectories of $\vec{\sigma}_1$ within the regions of reduced stress tend to align along the line linking neighboring crack tips. For $d=1.1$, interaction remains significant and strongly reduced compression regions are observed between adjacent tips. The local trajectories of $\vec{\sigma}_1$ are approximately perpendicular to the cracks within the reduced compression regions and parallel to them in the elevated stress zones. For this configuration, the trajectories of $\vec{\sigma}_1$ no longer align with the line connecting the neighboring crack tips (Fig. 3A).

For $\varphi=15^\circ$, interaction between reduced stress regions at adjacent crack tips is weak for d between 0.5 and 0.7 (Fig. 3A). Between the cracks, the local trajectories of $\vec{\sigma}_1$ are nearly perpendicular to the line connecting their neighboring tips, indicating conditions unfavorable for potential linkage development (Fig. 3A). As d



526 increases, elevated compression zone progressively builds and broadens between neighboring crack tips.
527 Thus, for the array orientation of $\varphi=15^\circ$, increasing crack clustering promotes elevated compression between
528 their tips and creates unfavorable conditions for crack linkage (Fig. 3A).

529 Fig. 3B illustrates the dependence of $\tilde{\sigma}_2$ calculated at the midpoint between the tips of neighboring cracks
530 ($\tilde{\sigma}_2^m$) on the projected overlap d for different values of φ . In the configurations with $\varphi<0^\circ$ (Fig. 3B, left panel),
531 the obtained curves show that with increasing d $\tilde{\sigma}_2^m$ decreases super-linearly down to a minimum value and
532 then gradually increases. The value of d that corresponds to the minimum $\tilde{\sigma}_2^m$ increases as array orientation
533 departs from the horizontal shear direction (decreasing φ) (Fig. 3B). For $\varphi=-30^\circ$, the minimal $\tilde{\sigma}_2^m$ value is
534 attained for the projected overlap d equal to about 1.5. The arrays that align into the horizontal shear
535 direction produce more pronounced minimum values of $\tilde{\sigma}_2^m$ (approximately -3.9).

536 For configurations with $\varphi>0^\circ$, $\tilde{\sigma}_2^m$ increases as d increases, reaching a maximum at about $d=1$ for all the
537 studied cases (Fig. 3B). The maximum values of $\tilde{\sigma}_2^m$ in the configurations with $\varphi=15^\circ$ and 30° are positive,
538 indicating elevated compression at the midpoint between the tips of adjacent cracks (Fig. 3B). As d further
539 increases, $\tilde{\sigma}_2^m$ decreases to a local minimum at a value of d that depends on the array orientation, and then
540 increases again asymptotically to 0 (Fig. 3B). The local minimum of $\tilde{\sigma}_2^m$ stays above -1 in all configurations,
541 indicating that the normalized and reduced minor in-plane principal stress magnitude in this region is higher
542 than its background value.

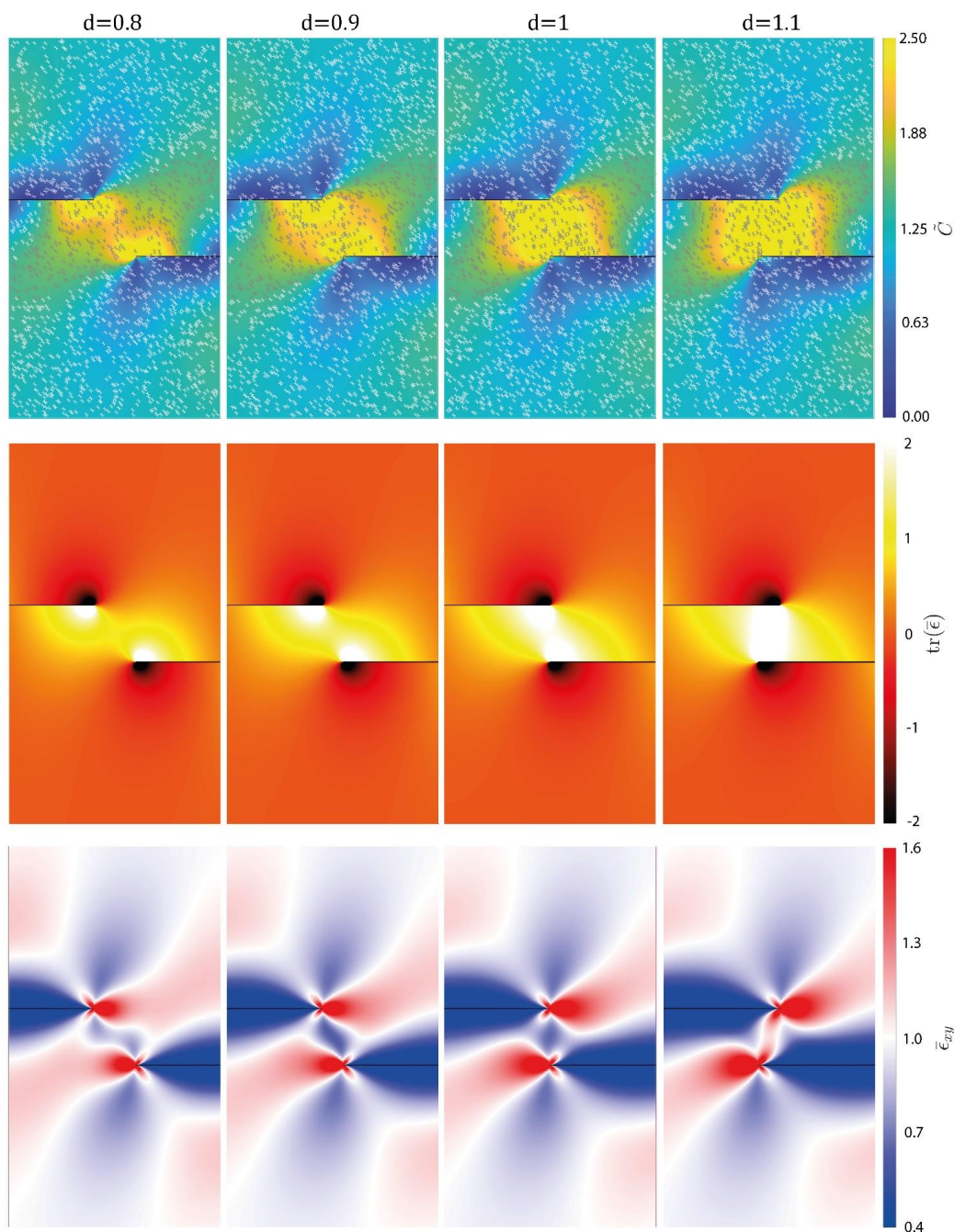
543 Fig. 4 illustrates the distribution of the normalized effective cohesion $\tilde{C}$, the normalized first invariant of the
544 strain tensor, $\bar{I}_1 = tr(\bar{\epsilon})$, and the normalized shear strain $\bar{\epsilon}_{xy}$ around cracks oriented at $\vartheta=0^\circ$ and arranged
545 in arrays oriented at $\varphi=-15^\circ$, for d values ranging from 0.8 to 1.1. The distribution of $\tilde{C}$ is asymmetrical around
546 the crack tips. In the interior region between neighboring cracks, $\tilde{C}$ attains its highest values (over 60 MPa)
547 within two lobe-shaped regions, while the lowest values are distributed in the exterior areas between the
548 cracks. At $d=0.8$, the regions of high $\tilde{C}$ at the tips of individual cracks do not overlap, and $\tilde{C}\approx 45$ MPa at the
549 midpoint between neighboring crack tips (Fig. 4). The lobe-shaped regions still do not overlap at $d=0.9$, but
550 the interaction is stronger and $\tilde{C}\approx 55$ MPa at the midpoint (Fig. 4). At higher values of d , overlap between the



551 lobes of high $\tilde{C}$ is observed, and the entire region between the crack tips is characterized by values of $\tilde{C}$ that
552 exceed 60 MPa (Fig. 4). In all configurations, one of the potential fracture directions is oriented at $\theta \approx 90^\circ$,
553 indicating potential linkage between the tips of neighboring cracks in the neutral overlap configuration ($d=1$).
554 The conjugate fracture orientation is $\theta \approx -35^\circ$.
555



556



557

558 Fig. 4: Normalized effective cohesion $\tilde{C}$, normalized first strain invariant $\bar{I}_1$ and shear strain component $\bar{\epsilon}_{xy}$

559 for different geometric configurations of *en echelon* crack arrays (from top to bottom row). The array



orientation is fixed at $\varphi=-15^\circ$, and the crack orientation is set at $\vartheta=0^\circ$. The projected overlap d is varied in columns between 0.8 and 1.1. White and black lines in the first row indicate the potential orientations of conjugate shear fractures.

563

The first invariant $\bar{I}_1$, which represents the local volumetric strain, exhibits positive values corresponding to local dilation distributed within lobe-shaped regions between the tips of neighboring cracks, and negative values corresponding to local contraction distributed symmetrically with respect to the crack orientation. At $d=0.8$ the lobes of local dilation do not overlap (Fig. 4). A weak interaction is observed at $d=0.9$, and overlap between the lobes occurs at $d=1.0$ (Fig. 4). At $d=1.1$, the lobes completely overlap and merge into an elongated elliptical-rectangular region connecting the tips, where $\bar{I}_1$ reaches high positive values (Fig. 4).

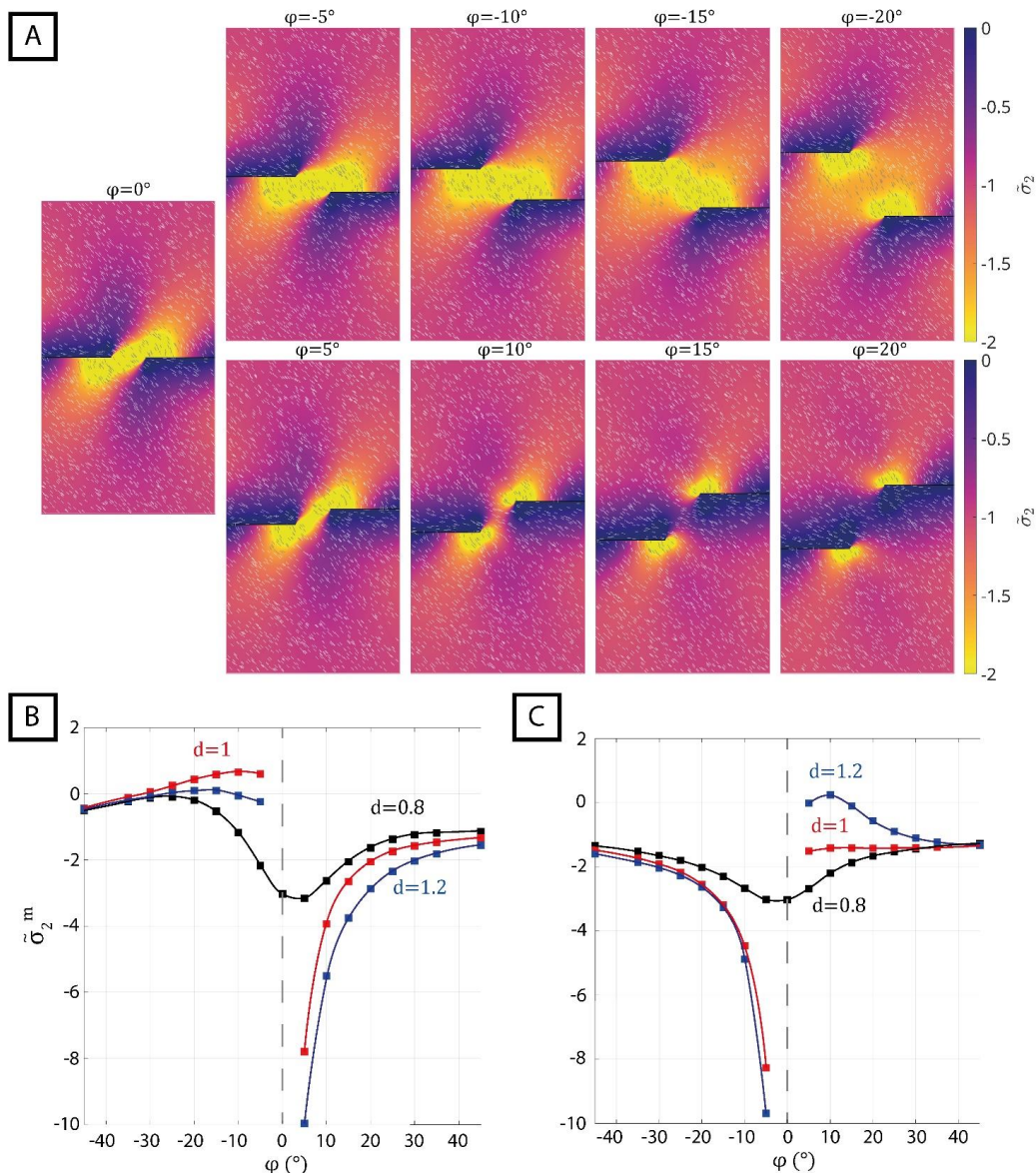
The distribution of the shear strain component $\bar{\epsilon}_{xy}$ is characterized by high values concentrated within lobes emanating from the crack tips and elongating in the crack direction, as well as two symmetrical, smaller lobes elongating obliquely relative to the crack and pointing towards the crack center. For underlapping cracks $d=0.8$, a weak interaction can be observed between the major lobes of high shear strain at the individual crack tips (Fig. 4). At increasing values of d between 0.9 and 1.0, regions of strain shadowing overlap, leading to the formation of a sigmoidal zone, where $\bar{\epsilon}_{xy}$ is lower than its unit background value (Fig. 4). For overlapping cracks $d=1.1$, the smaller lobes of high $\bar{\epsilon}_{xy}$ interact, and sigmoidal regions of high shear strain linking neighboring crack tips are observed (Fig. 4).

Fig. 5A presents the perturbation of $\bar{\sigma}_2$ around cracks for configurations with the crack inclination fixed at $\vartheta=0^\circ$ and the projected overlap between the cracks set to $d=0.8$, while the inclination of the crack array φ is varied. Fig. 5A shows configurations with φ ranging from -5° to -20° (top row) and the corresponding symmetrical configurations around $\bar{\sigma}_1^\infty$, with φ ranging from 5° to 20° (bottom row). The left-most panel displays the collinear crack configuration. Additional examples showing the effect of array orientation for vertical mode II cracks and collinear mode I-oriented cracks are reported in Fig. A2.

584



585



586

587 Fig. 5: (a) Normalized and reduced minor principal stress magnitude $\tilde{\sigma}_2$ for different geometric configurations
 588 of *en echelon* crack arrays. Only the central unit cell is shown. The crack orientation is fixed at $\vartheta=0^\circ$. The
 589 projected overlap is fixed at $d=0.8$. The crack array orientation φ is first set to 0° and then ranges from -5° to
 590 -20° (top row) and from 5° to 20° (bottom row). White and black lines indicate the local trajectories of the
 591 major in-plane principal stress $\tilde{\sigma}_1$. B-C) Normalized and reduced minor in-plane principal stress magnitude
 592 $\tilde{\sigma}_2^m$ calculated at the midpoint between the two innermost cracks in an array of *en echelon* cracks. Different



593 colors represent different values of the projected overlap d : underlapping cracks ($d=0.8$), neutral cracks
594 ($d=1$), and overlapping cracks ($d=1.2$). (b) The crack orientation is fixed at $\vartheta=0^\circ$, and the dependence of $\tilde{\sigma}_2^m$
595 on φ is illustrated. (c) The array orientation is fixed at $\varphi=0^\circ$, and the dependence of $\tilde{\sigma}_2^m$ on ϑ is presented.

596

597 When the crack array is aligned with $\tilde{\sigma}_1^\infty$, the distance between adjacent tips is increased and the interaction
598 between regions of reduced compression near the crack tips is weakened. For $\varphi=-5$ to -10° , strong overlap
599 of reduced compression regions is observed, but the local trajectories of $\tilde{\sigma}_1$ are not favorable for the linkage
600 between the adjacent tips (Fig. 5A). For $\varphi=-15$ to -20° , the reduced compression regions overlap and the
601 local trajectories of $\tilde{\sigma}_1$ tend to connect neighboring tips (Fig. 5A).

602 Reduced compression between adjacent crack tips is also observed for $\varphi=5-10^\circ$, but in these configurations
603 the local trajectories of $\tilde{\sigma}_1$ are nearly perpendicular to the elongation of the discussed regions (Fig. 5A). The
604 $\tilde{\sigma}_1$ trajectories prominently deflect between the tips and tend to align with the crack orientation. As φ
605 increases from 15° to 20° , regions of elevated compression develop between neighboring crack tips, with the
606 local trajectories of $\tilde{\sigma}_1$ aligning with the direction of $\tilde{\sigma}_1^\infty$ (Fig. 5A).

607 For the $\varphi=0^\circ$ case, the lobe-shaped regions of reduced compression partially overlap within a zone elongating
608 at approximately 30° , where the $\tilde{\sigma}_1$ trajectories are roughly aligned with the direction of $\tilde{\sigma}_1^\infty$ (Fig. 5A). The
609 deflection of $\tilde{\sigma}_1$ is more pronounced near the tips of the individual crack tips. The $\tilde{\sigma}_1$ trajectories are
610 approximately perpendicular to the cracks in the regions of reduced compression and parallel to them within
611 regions of elevated compression.

612 Fig. 5B and C illustrate the dependence of $\tilde{\sigma}_2$ calculated at the midpoint between the tips of neighboring
613 cracks, denoted by $\tilde{\sigma}_2^m$, for different values of d on the array orientation φ (Fig. 5B, with $\vartheta=0^\circ$), and on the
614 crack orientation ϑ (Fig. 5C, with $\varphi=0^\circ$). In the configurations with $\vartheta=0^\circ$ (Fig. 5B), $\tilde{\sigma}_2^m$ increases gradually as
615 φ increases from -45° to about -25° to -10° (depending on the projected overlap), reaching a maximum which,
616 in the configurations with high overlap, is positive and therefore indicates local elevated compression.
617 Beyond the maximum, $\tilde{\sigma}_2^m$ decreases as the array direction approaches the horizontal (Fig. 5B). For

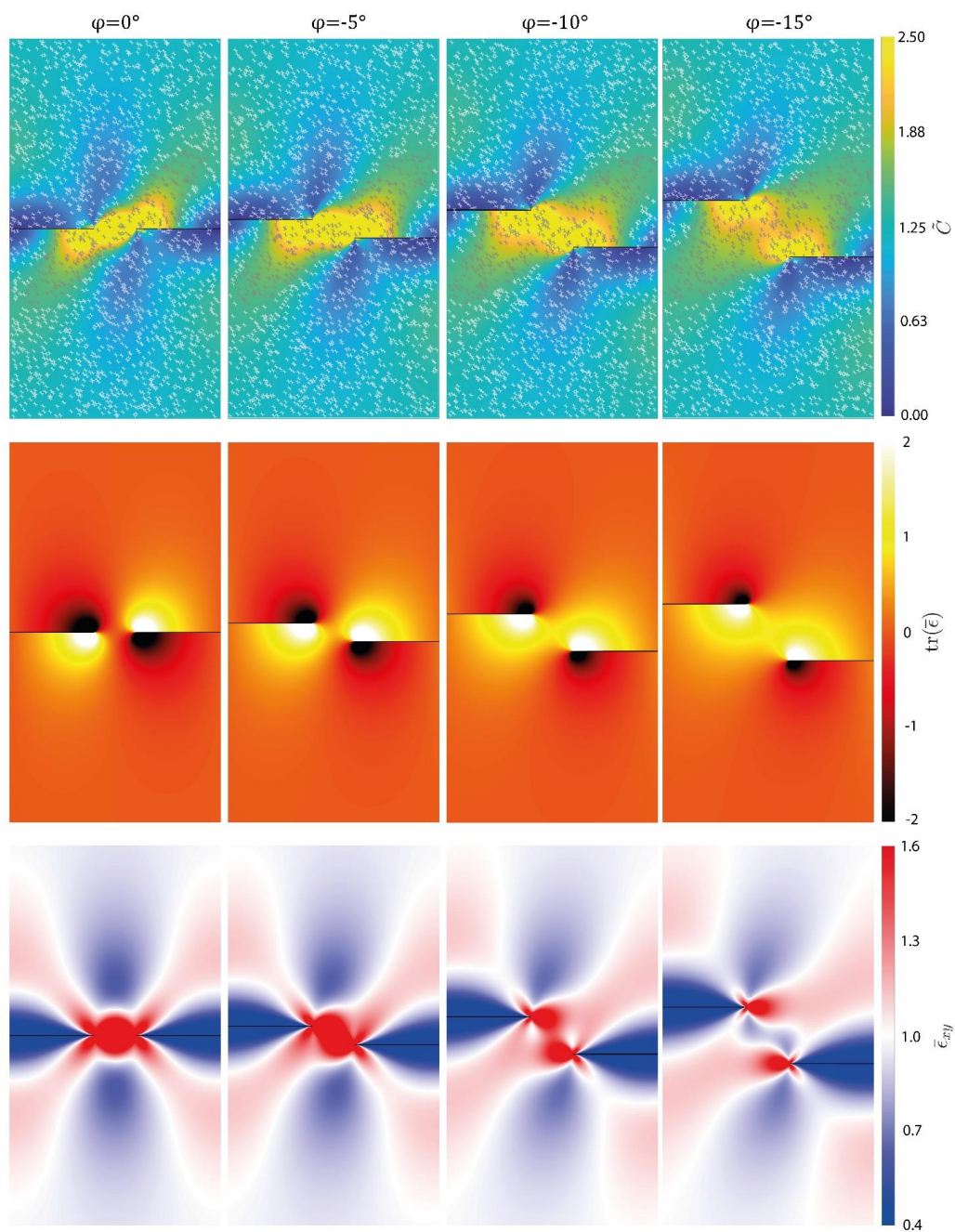


underlapping cracks ($d=0.8$), the minimum $\tilde{\sigma}_2^m$ is reached at $\varphi \approx 5^\circ$ (Fig. 5B). In the neutral and overlapping configurations ($d=1.0$ and $d=1.2$, respectively), $\tilde{\sigma}_2^m$ diverges to negative values as the cracks are brought towards contact, at low positive values of φ (Fig. 5B). For all the curves corresponding to different d values, $\tilde{\sigma}_2^m$ increases as φ increases, approaching its background value as φ approaches 45° (Fig. 5B).

In the configurations with $\varphi=0^\circ$ and variable ϑ , $\tilde{\sigma}_2^m$ decreases steeply as ϑ increases from -45° and approaches 0° (Fig. 5C). For low negative values of ϑ $\tilde{\sigma}_2^m$ diverges to $-\infty$, especially in the configurations with neutral and high overlap. As ϑ increases from 0° to higher positive values, $\tilde{\sigma}_2^m$ reaches a maximum in the configurations with $d=1.0$ and $d=1.2$ (in the latter case, the maximum is positive, indicating elevated compression) (Fig. 5C). For all configurations with different values of d , $\tilde{\sigma}_2^m$ approaches its background value as ϑ approaches 45° (Fig. 5C).

Fig. 6 illustrates the distribution of $\tilde{C}$, $\bar{I}_1$ and $\bar{\epsilon}_{xy}$ around underlapping cracks ($d=0.8$) oriented at $\vartheta=0^\circ$ and arranged in arrays oriented at φ angles ranging from 0° to -15° . Additional examples are illustrated in Figures A3, A4. For φ ranging from 0° to -10° , the lobe-shaped regions where $\tilde{C}$ exceeds 60 MPa at the tips of neighboring cracks overlap, merging into elliptical regions of high $\tilde{C}$ elongating along the line connecting the crack tips (Fig. 6). In these regions, the potential conjugate fracture orientations are $\theta \approx -15^\circ$ and -70° (Fig. 6). This indicate that potential crack linkage would be facilitated at low negative values of φ , where the line connecting the tips of neighboring cracks is approximately oriented at -15° . At $\varphi=-15^\circ$, the regions of high $\tilde{C}$ do not overlap, although strong interaction is still observed (Fig. 6).

636



637

638 Fig. 6: Normalized effective cohesion $\tilde{C}$, normalized first strain invariant $\bar{I}_1$ and shear strain component $\bar{\epsilon}_{xy}$

639 for different geometric configurations of *en echelon* crack arrays. The crack orientation is set at $\vartheta=0^\circ$, and the



640 projected overlap is fixed at $d=0.8$. The array orientation is varied between $\varphi=0^\circ$, -5° , -10° , and -15° . White
641 and black lines in the first row indicate the potential orientations of conjugate shear fractures.

642

643 In all four configurations, the lobe-shaped regions characterized by high volumetric dilation are confined to
644 the tips of the individual cracks and show no evident overlap, although weak interaction is observed at $\varphi=-$
645 10° and -15° (Fig. 6).

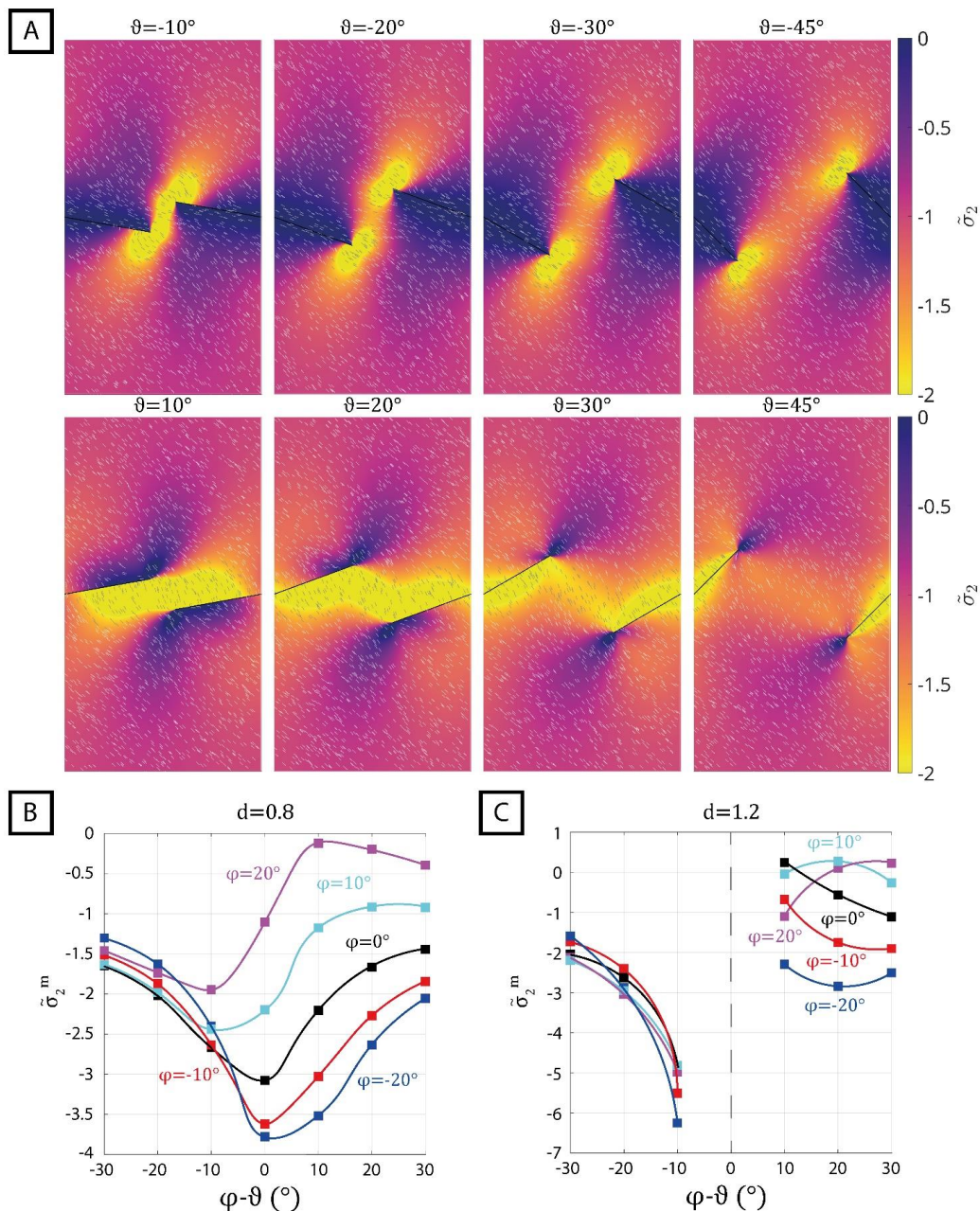
646 At $\varphi=0^\circ$, the lobes characterized by high shear strain merge into an elliptical region (Fig. 6). This region of
647 high $\bar{\varepsilon}_{xy}$ elongates between the tips of neighboring cracks at $\varphi=-5^\circ$; in this configuration, it exhibits a
648 sigmoidal shape (Fig. 6). At $\varphi=-10^\circ$, the major lobes of concentrated $\bar{\varepsilon}_{xy}$ show no overlap, although
649 interaction is still observed. At $\varphi=-15^\circ$ shear strain is low between the crack tips, and a clear overlap between
650 areas of strain shadowing can be observed (Fig. 6).

651 Fig. 7A illustrates the dependence of $\bar{\sigma}_2$ perturbation on the crack orientation ϑ in *en echelon* arrays with
652 $\varphi=0^\circ$ and $d=0.9$. The values of ϑ range from -10° to -45° (top row) and, symmetrically with respect to the
653 shearing direction, from 10° to 45° (bottom row). Further configurations illustrating the effect of crack
654 orientation for selected array orientations are shown in Fig. A5.

655



656



657

658 Fig. 7: (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$ for different geometric configurations of *en*

659 *echelon* crack arrays. The crack array orientation is fixed at $\varphi=0^\circ$ and the projected overlap at $d=0.9$. The

660 crack orientation ϑ ranges from -10° to -45° along the top row and from 10° to 45° along the bottom row.

661 White and black lines represent the local trajectories of the major in-plane principal stress $\tilde{\sigma}_1$. B-C)



662 Experimental curves describing the dependence of the normalized effective minor in-plane principal stress
663 $\bar{\sigma}_2$ calculated at the midpoint between the two innermost cracks ($\bar{\sigma}_2^m$) in arrays of *en echelon* cracks on the
664 difference between the array orientation φ and the crack orientation ϑ . Different colors represent different
665 array orientations: $\varphi=0^\circ$, 10° , 20° , -20° , and -10° . (b) The results for underlapping cracks ($d=0.8$), are
666 illustrated. (c) The results for overlapping cracks ($d=1.2$) are presented.

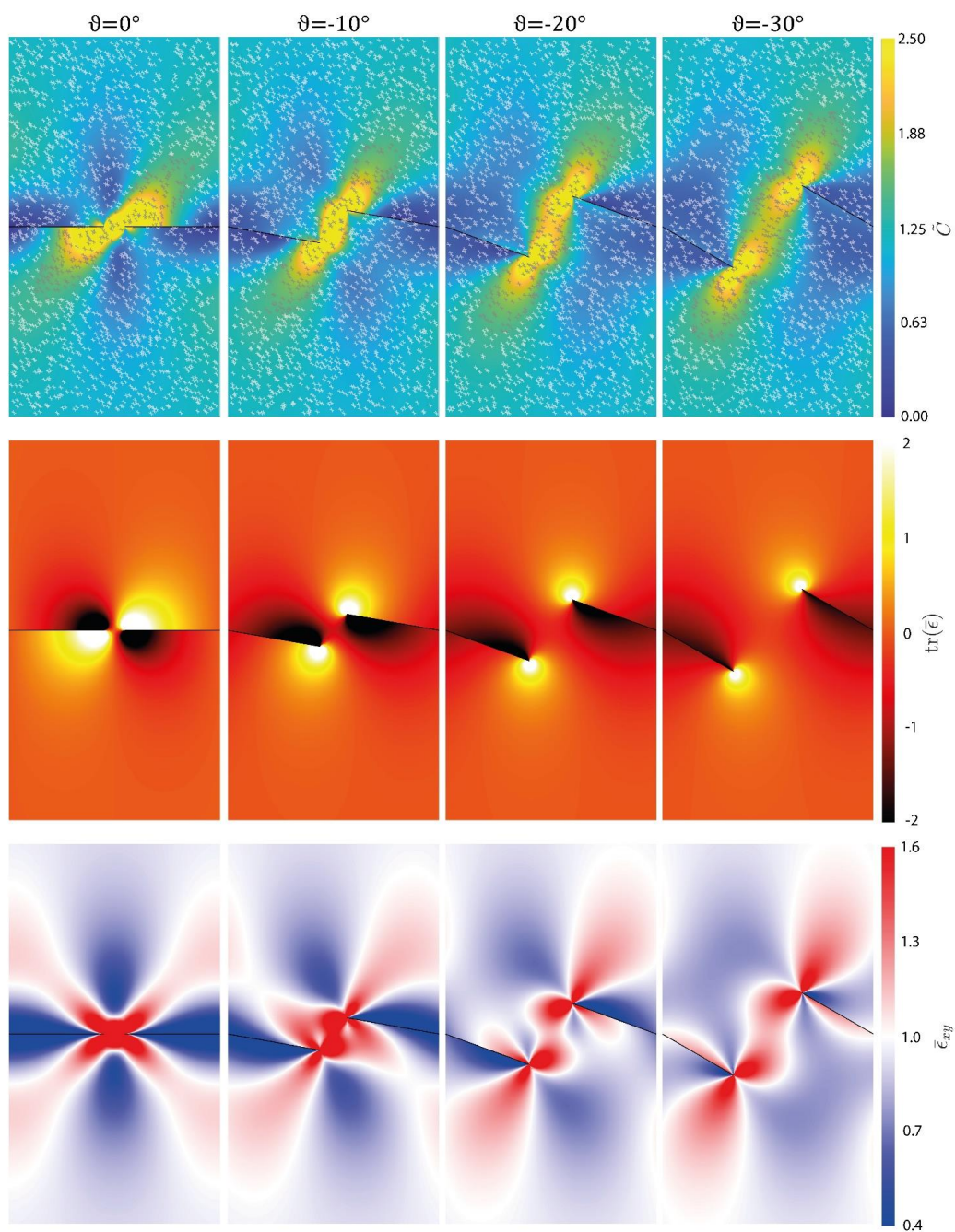
667

668 For ϑ ranging from -10° to -20° , the regions of depressed compression between adjacent crack tips overlap,
669 forming elongated areas oriented approximately between 35° and 45° (Fig. 7A). Although these crack
670 orientations promote overlap of reduced compression regions, the trajectories of major principal stress $\bar{\sigma}_1$
671 tend to align with the cracks rather than in orientations favorable for linkage development between the
672 neighboring tips (Fig. 7A). At $\vartheta=-30^\circ$ and -45° , the reduced compression lobes cease to overlap, but oblique
673 zones of weaker interaction persist, within which the local trajectories of $\bar{\sigma}_1$ are oriented at -45° (Fig. 7A).

674 In the counterpart symmetrical configurations, for $\vartheta=10^\circ$ the reduced compression lobes overlap, but the
675 local trajectories of $\bar{\sigma}_1$ show no alignment with the line connecting adjacent crack tips (Fig. 7A). For ϑ values
676 between 20° and 30° , both the overlap of reduced compression regions and the orientation of $\bar{\sigma}_1$ suggest
677 that these geometries are potentially favorable for crack linkage via tensile mechanism (Fig. 7A). For ϑ values
678 over 30° , the separation between adjacent crack tips becomes too large for reduced compression lobes to
679 overlap, although weak interactions can still be observed (Fig. 7A).

680 Fig. 8 illustrates the distribution of $\tilde{C}$, $\bar{I}_1$ and $\bar{\varepsilon}_{xy}$ around underlapping cracks ($d=0.9$) arranged in arrays
681 oriented at $\varphi=0^\circ$, with ϑ ranging between 0° and -30° . At $\vartheta=0^\circ$ and -10° , overlap between regions of high $\tilde{C}$
682 is observed, within elliptical areas elongating between the crack tips, although in both configurations the
683 local orientations of the potential conjugate fractures do not effectively connect the neighboring tips (Fig. 8).
684 At $\vartheta=-20^\circ$, interaction is weaker, and $\tilde{C}\approx 50$ MPa at the midpoint between the tips (Fig. 8). At $\vartheta=-30^\circ$, the
685 interaction is further weakened, with $\tilde{C}\approx 40$ MPa at the midpoint (Fig. 8).

686



687

688 Fig. 8: Normalized effective cohesion $\tilde{C}$, normalized first strain invariant $\tilde{I}_1$ and shear strain component $\tilde{\epsilon}_{xy}$

689 for different geometric configurations of *en echelon* crack arrays. The array orientation is set at $\varphi=0^\circ$, and



690 the projected overlap is fixed at $d=0.9$. The crack orientation is varied between $\vartheta=0^\circ$, -10° , -20° , and -30° .

691 White and black lines in the first row indicate the potential orientations of conjugate shear fractures.

692

693 No clear overlap between regions of localized dilation or contraction are observed, except for the
694 configuration with $\vartheta=-10^\circ$, where weak overlap between compaction regions occurs (Fig. 8). At $\vartheta=-30^\circ$,
695 approaching the configuration in which the cracks are aligned with the far-field orientation of the major
696 principal stress, the lobes of high dilation tend to elongate from the tips in the crack direction, while
697 contraction localizes along the major dimension of the cracks (Fig. 8).

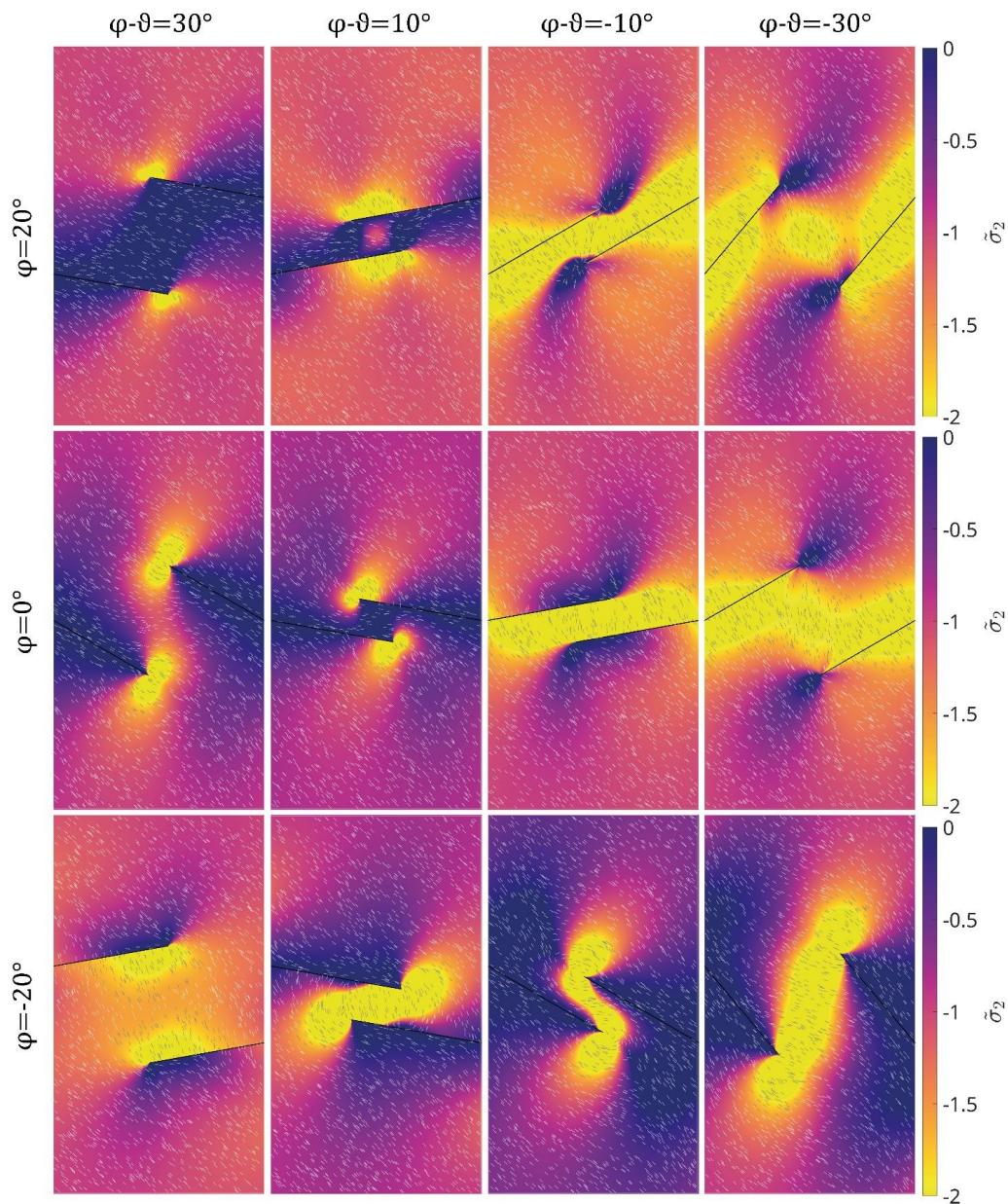
698 At $\vartheta=0^\circ$, the lobes characterized by high $\bar{\epsilon}_{xy}$ component of shear strain merge into an elliptical region (Fig.
699 8). At $\vartheta=-10^\circ$, the overlap is partial, and high $\bar{\epsilon}_{xy}$ values concentrate within a figure-eight-shaped region (Fig.
700 8). For configurations with $\vartheta=-20^\circ$ and -30° , the interaction weakens and relatively high shear strain localizes
701 within a sigmoidal region connecting neighboring crack tips (Fig. 8).

702 Fig. 9 illustrates the dependence of the perturbation of $\bar{\sigma}_2$ on the alignment between the crack orientation
703 ϑ and the array orientation φ for overlapping crack configurations ($d=1.2$). Three array orientations are
704 considered: $\varphi=0^\circ$, 20° , and -20° (the latter two configurations are symmetrical with respect to the horizontal).
705 For each array orientation, ϑ is varied accordingly, resulting in four configurations with $\varphi-\vartheta=30^\circ$, 10° , -10°
706 and -30° .

707



708



709

710 Fig. 9: Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$ for different geometric configurations of *en*
 711 *echelon* crack arrays. The crack array orientation varies between $\varphi=20^\circ$ (top row), $\varphi=0^\circ$ (middle row), and
 712 $\varphi=-20^\circ$ (bottom row). The projected overlap is fixed at $d=1.2$. The difference between φ and the crack
 713 orientation ϑ varies between 30° , 10° , -10° , -30° . White and black lines represent the local trajectories of the
 714 major in-plane principal stress $\tilde{\sigma}_1$.



715

716 In the configuration with $\varphi=20^\circ$, regions characterized by reduced compression are confined near the tips of
717 the individual cracks for $\varphi-\vartheta=30^\circ$ and 10° , while elevated compression occurs in the interior region between
718 the cracks (Fig. 9). Within the high compression regions, the trajectories of major in-plane principal stress $\vec{\sigma}_1$
719 deflect and tend to align with the cracks. In the configuration with $\varphi-\vartheta=10^\circ$, a small circular region in which
720 $\vec{\sigma}_2$ is approximately equal to its background value is observed, because the lobes of elevated compression at
721 the tips of neighboring cracks do not overlap effectively (Fig. 9). At $\varphi-\vartheta=-10^\circ$, the entire inner region between
722 the overlapping cracks is characterized by strongly reduced compression (Fig. 9). Low values of $\vec{\sigma}_2$ are also
723 observed along the major dimension of the cracks. In this configuration, the local trajectories of $\vec{\sigma}_1$ connect
724 the tips of neighboring cracks. At $\varphi-\vartheta=-30^\circ$, a similar stress distribution occurs, although the interacting lobes
725 of elevated compression at the tips of the individual cracks break the continuity of the reduced compression
726 region, which effectively localizes near the crack tips and within a circular region between them (Fig. 9). The
727 local trajectories of $\vec{\sigma}_1$ align with the line connecting the tips of adjacent cracks.

728 In the configuration with $\varphi=0^\circ$ and $\varphi-\vartheta=30^\circ$, the lobes of reduced compression show no overlap, although
729 weak interaction occurs (Fig. 9). At $\varphi-\vartheta=10^\circ$, elevated compression occurs in the inner region between the
730 cracks. In both these configurations, the local trajectories of $\vec{\sigma}_1$ tend to align with the crack array. At $\varphi-\vartheta=-$
731 10° and -30° , the inner region between the cracks is characterized by reduced compression (Fig. 9). In the
732 first configuration, the region of high $\vec{\sigma}_2$ is rectangular, and the local trajectories of $\vec{\sigma}_1$ are approximately
733 perpendicular to the crack orientations within it. In the latter configuration, the region of low $\vec{\sigma}_2$ is less
734 continuous and exhibits a sigmoidal shape (Fig. 9). In this case, the trajectories of $\vec{\sigma}_1$ connect the tips of
735 neighboring cracks.

736 For $\varphi=-20^\circ$ and $\varphi-\vartheta=30^\circ$, the inner region between the tips of neighboring cracks is characterized by relatively
737 low $\vec{\sigma}_2$, although the lobes where it reaches its lowest values do not overlap (Fig. 9). The crack tips are not
738 connected by the local trajectories of $\vec{\sigma}_1$, which tend to orient perpendicular to the cracks. At $\varphi-\vartheta=10^\circ$, the
739 lobes of strongly reduced compression overlap, merging into an elliptical region that connects the tips of

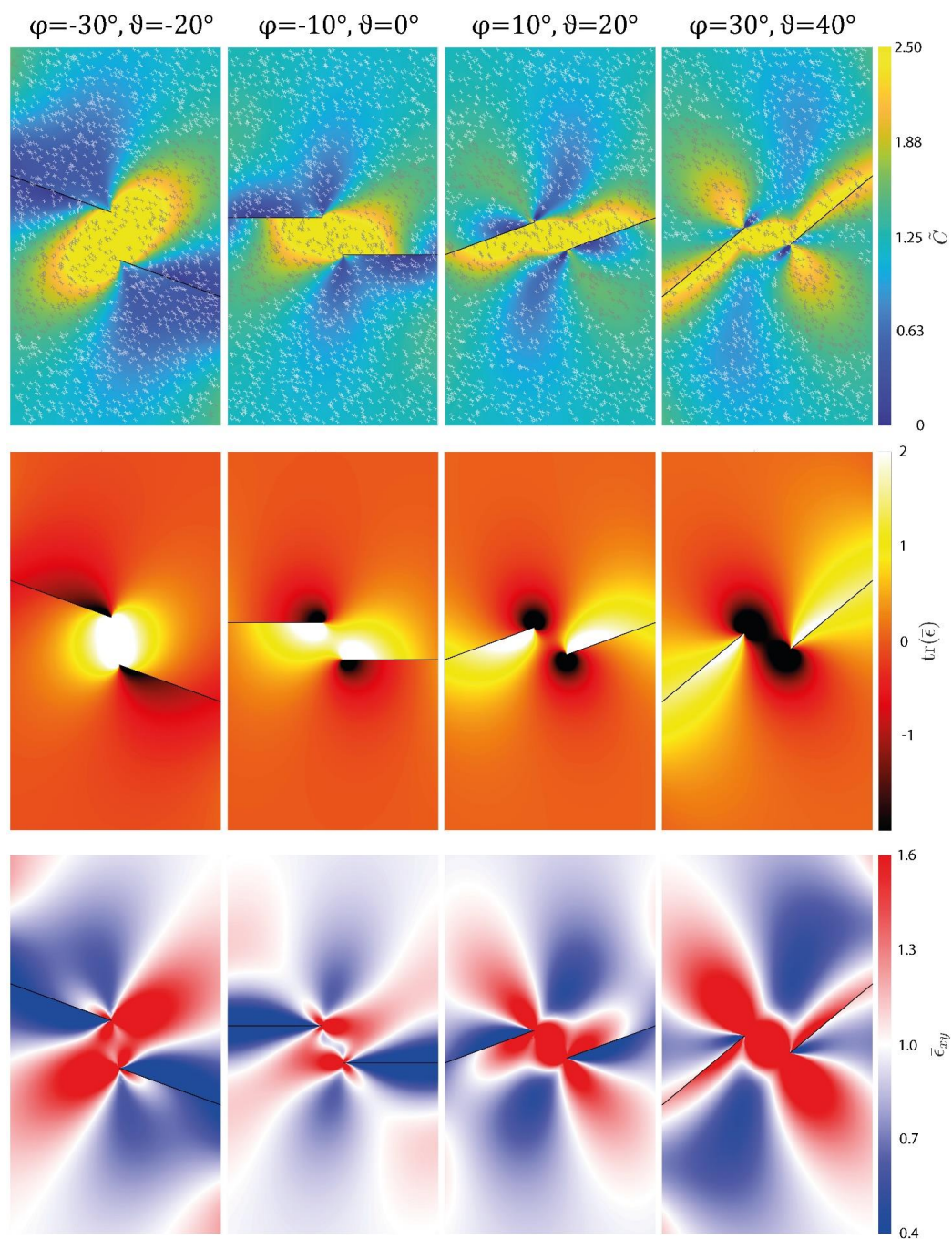


740 neighboring cracks (Fig. 9). However, these tips are not effectively connected by the local trajectories of $\vec{\sigma}_1$.
741 At $\varphi - \vartheta = -10^\circ$ and -30° regions of reduced compression occur between the crack tips, in elliptical regions
742 elongating approximately along the line connecting the tips (Fig. 9). In these configurations, the local
743 trajectories of $\vec{\sigma}_1$ tend to align with the crack array.

744 Fig. 7B-C illustrate the dependence of $\tilde{\sigma}_2^m$ ($\tilde{\sigma}_2$ calculated at the midpoint between the tips of neighboring
745 cracks) for different values of d and φ on the alignment between the array orientation and the crack
746 orientation, that is, on the difference $\varphi - \vartheta$. In both the underlapping $d=0.8$ (Fig. 7B) and overlapping $d=1.2$
747 (Fig. 7C) configurations, $\tilde{\sigma}_2^m$ decreases steeply as $\varphi - \vartheta$ increases from -30° to 0° . For $d=0.8$, $\tilde{\sigma}_2^m$ reaches a
748 minimum at a value of $\varphi - \vartheta$ that depends on φ , and then increases as $\varphi - \vartheta$ approaches 30° for all
749 configurations with different φ (Fig. 7B). The configuration with $\varphi = -20^\circ$ yields the lowest values of $\tilde{\sigma}_2^m$. For
750 $d=1.2$, at low positive values of $\varphi - \vartheta$, $\tilde{\sigma}_2^m$ gradually decreases as $\varphi - \vartheta$ increases in the configurations with
751 $\varphi = 0^\circ$, -10° and -20° , and increases to positive $\tilde{\sigma}_2^m$ values, corresponding to elevated compression, in the
752 configurations with $\varphi = 10^\circ$ and 20° (Fig. 7C).

753 Fig. 10 illustrates the distribution of $\tilde{C}$, $\tilde{I}_1$ and $\bar{\epsilon}_{xy}$ around underlapping cracks ($d=0.9$) arranged in arrays
754 oriented at $\varphi = -30^\circ$, -10° , 10° and 30° , with $\varphi - \vartheta$ fixed at -10° . At $\varphi = -30^\circ$, an elliptical region where $\tilde{C}$ exceeds
755 60 MPa elongates approximately perpendicular to the crack direction (Fig. 10). Within this region, one of the
756 potential conjugate fracture orientations, $\theta \approx -75^\circ$, is approximately aligned with the line connecting the
757 neighboring crack tips. At $\varphi = -10^\circ$ the region of overlap between the lobes of high $\tilde{C}$ exhibits an elliptical
758 shape and elongates between the crack tips (Fig. 10). In this configuration as well, one of the orientations,
759 $\theta \approx -50^\circ$, effectively connects the crack tips. At $\varphi = 10^\circ$ and 30° , the lobes of high $\tilde{C}$ overlap and merge into
760 sigmoidal-shaped regions, within which one of orientations $\theta \approx -40^\circ$ and -25° , respectively, are consistent with
761 potential linkage between the cracks (Fig. 10).

762



763

764 Fig. 10: Normalized effective cohesion $\tilde{C}$, normalized first strain invariant $\bar{I}_1$ and shear strain component $\bar{\epsilon}_{xy}$

765 for different geometric configurations of *en echelon* crack arrays. The relative orientation between the array



766 and the cracks is set at $\varphi - \vartheta = -10^\circ$, and the projected overlap is fixed at $d=0.9$. The array orientation is varied
767 between $\varphi = -30^\circ, -10^\circ, 10^\circ$, and 30° . White and black lines in the first row indicate the potential orientations
768 of conjugate shear fractures.

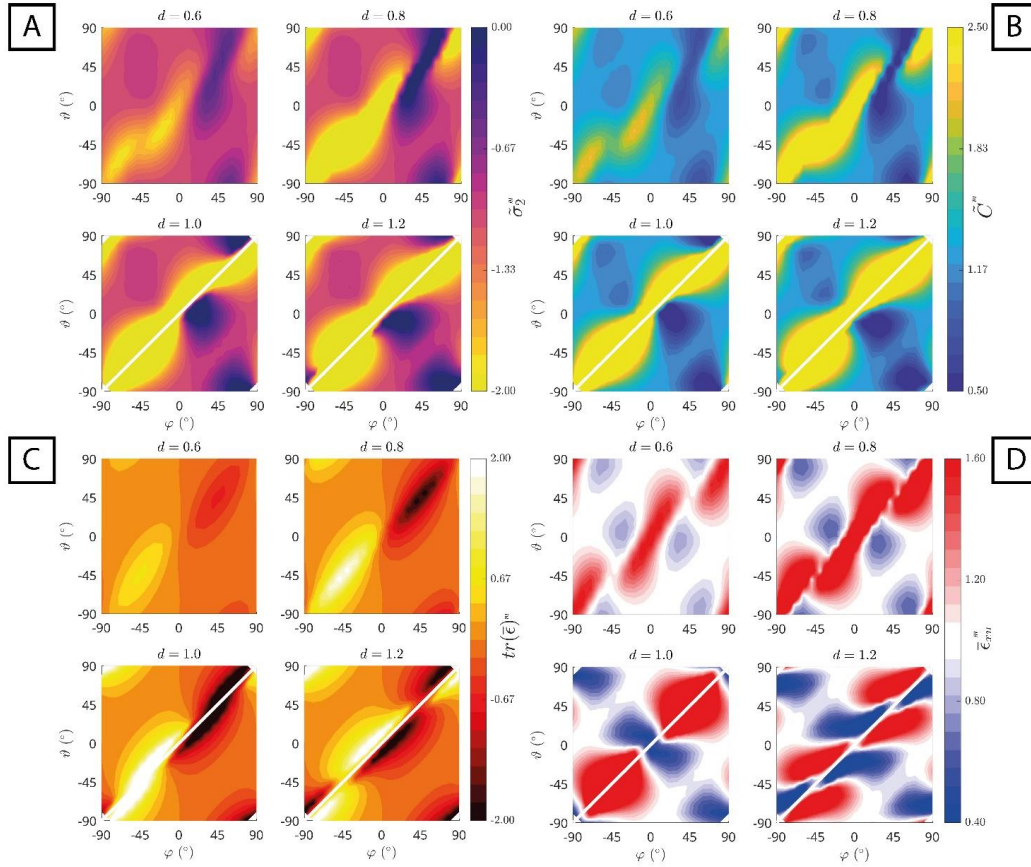
769

770 An elliptical region of overlap between regions of localized dilation is observed at $\varphi = -30^\circ$, while weaker
771 interaction is observed at $\varphi = -10^\circ$ (Fig. 10). At $\varphi = 10^\circ$, weak contraction occurs in the region between the crack
772 tips. A region of stronger contraction between the tips is observed at $\varphi = 30^\circ$. In the two latter configurations,
773 dilation is confined near the tips of individual cracks, in the exterior region between them (Fig. 10).

774 At $\varphi = -10^\circ$ and -30° , the lobes of high $\bar{\varepsilon}_{xy}$ do not fully overlap, although large areas of $\bar{\varepsilon}_{xy}$ are observed in the
775 exterior region between them (Fig. 10). Conversely, at $\varphi = 10^\circ$ and 30° , a region of high $\bar{\varepsilon}_{xy}$ connects the tips
776 of neighboring cracks. In these configurations, other lobe-shaped areas of high $\bar{\varepsilon}_{xy}$ occur, elongating in the
777 direction of $\bar{\sigma}_1^\infty$ (Fig. 10).

778 Fig. 11 summarizes the results for the numerical experiments with *en echelon* crack arrays. The first general
779 observation is that all the analyzed stress and strain quantities reach the highest values at the midpoints
780 between neighboring crack tips in configurations with $d \geq 1$ (Fig. 11). Secondly, for overlapping cracks ($d >$
781 1), we observe similar magnitudes of $\bar{\sigma}_2^m$, $\bar{C}^m$, $\bar{I}_1^m$, and $\bar{\varepsilon}_{xy}^m$ compared to the neutral overlap configuration
782 ($d = 1$), but the dependence of these quantities on φ and ϑ changes. As an example, $\bar{I}_1^m$ reaches its maximum
783 value for $\varphi \approx \vartheta \approx -45^\circ$ when $d = 1$, while it reaches the same values for $\varphi \approx \vartheta \approx 0^\circ$ for $d = 1.2$ (Fig. 11C).
784 The third general result from this set of experiments is that both the highest and lowest values of all the
785 quantities we considered are reached when the cracks are aligned with the array orientation ($\varphi - \vartheta \approx$
786 $0^\circ, \pm 180^\circ$; Fig. 11).

787



788

789 Fig. 11: Normalized magnitudes measured at the midpoint between the tips of neighboring cracks in the *en*
 790 *echelon* array of (a) the reduced minor in-plane principal stress $\tilde{\sigma}_2^m$, (b) the effective cohesion $\tilde{C}^m$, (c) the
 791 first invariant of the strain tensor $\tilde{I}_1^m$, and (d) the shear strain component $\tilde{\epsilon}_{xy}^m$, for different values of φ , ϑ ,
 792 and d .

793

794 4.3 Randomly distributed cracks

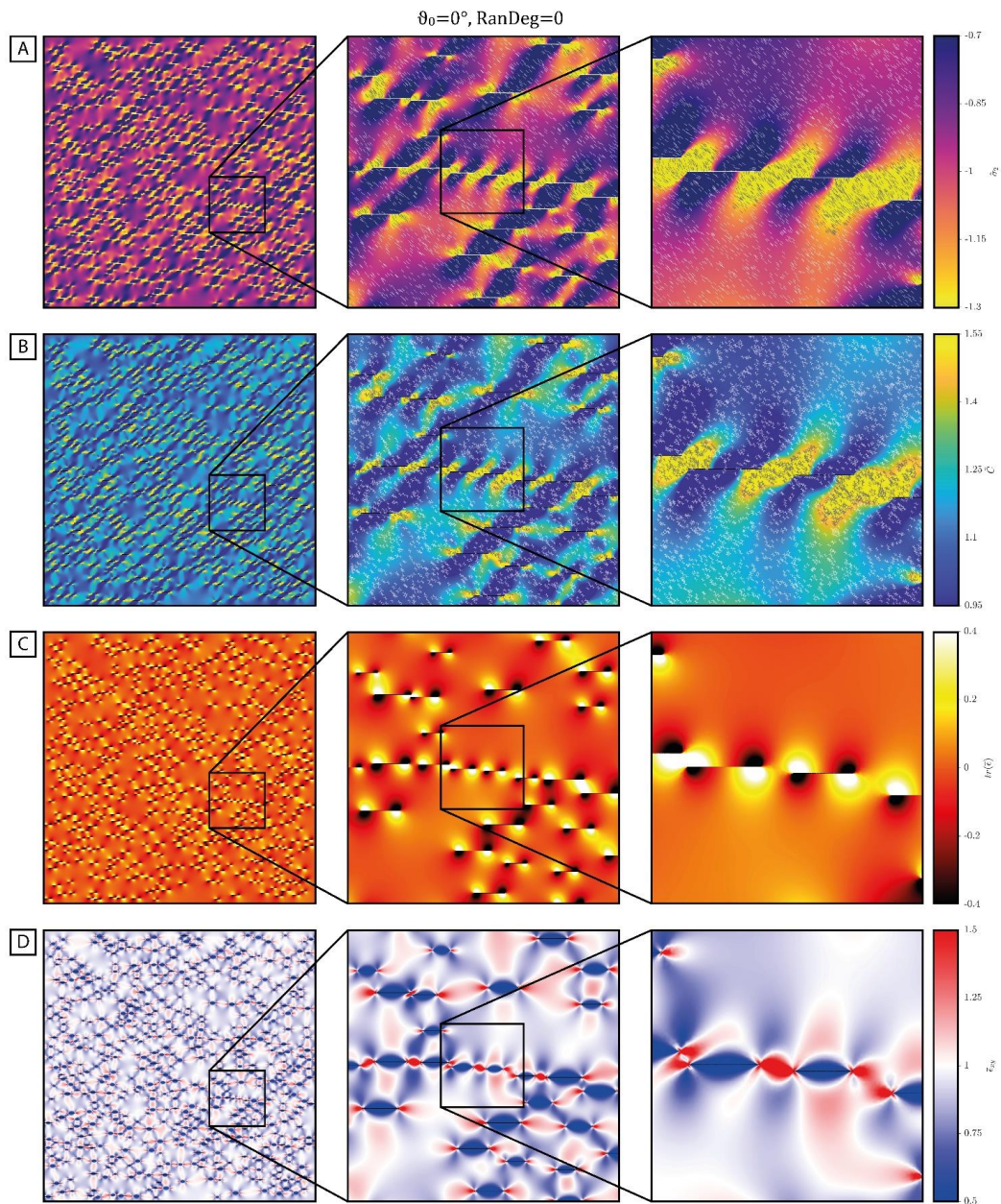
795 In this set of numerical experiments, we analyzed the spatial distribution around 500 cracks with random
 796 locations of the following quantities, each one normalized by its far-field value: the reduced minor in-plane
 797 stress magnitude $\tilde{\sigma}_2$, the effective cohesion $\tilde{C}$, the first strain tensor invariant $\tilde{I}_1$, and the shear strain



798 component $\bar{\epsilon}_{xy}$. We also analyzed the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$ and the local
799 orientations of the potential conjugate shear fractures inclined at $\theta = \pm \left(\frac{\pi}{4} - \frac{\phi}{2}\right) = \pm 27.5^\circ$ relative to $\vec{\sigma}_1$.
800 Among the 13 configurations that we simulated, we selected two for detailed analysis: (i) the configuration
801 in which all cracks are horizontally aligned ($\vartheta_0 = 0^\circ$ and $RanDeg = 0$), and (ii) the configuration in which all
802 crack orientations are random ($RanDeg = 1$). For each model, we assess the mechanical interaction
803 between cracks at three different scales: (i) the domain scale, (ii) an intermediate scale at which mechanical
804 interactions between multiple cracks can be resolved and subsets of *en echelon* cracks can be analyzed, and
805 (iii) the crack-length scale, at which interactions between a few cracks and the resulting perturbations of the
806 stress and strain fields between adjacent crack tips can be investigated.

807 Fig. 12 illustrates the distributions of $\tilde{\sigma}_2$, $\tilde{C}$, $\tilde{I}_1$, and $\bar{\epsilon}_{xy}$ in the system with $\vartheta_0 = 0^\circ$ and $RanDeg = 0$.
808 Additional configurations with vertically and obliquely aligned cracks are shown in Figures A6 and A7.
809 Inspection of the $\tilde{\sigma}_2$ distribution across the entire domain reveals regions of elevated compression elongating
810 at angles of $40\text{--}45^\circ$ (Fig. 12A). Smaller regions of reduced compression at the tips of individual crack tips
811 overlap, elongating at angles between -10° and -18° (Fig. 12A). This type of mechanical interaction, caused
812 by the overlap between the reduced-compression lobes at the crack tips that elongate at low angles relative
813 to the crack direction, produces arrays of mechanically linked cracks oriented at approximately -15° (Fig.
814 12A). Due to the overlap between the reduced-compression lobes at the tips of individual cracks elongating
815 at high angles relative to the crack direction, additional regions of potentially tensile stress develop at angles
816 of $45\text{--}60^\circ$, connecting cracks in arrays oriented between -55° and -75° (Fig. 12A). However, we observe that
817 only in arrays of cracks oriented at approximately -15° the local trajectories of $\vec{\sigma}_1$ effectively connect the tips
818 of adjacent cracks, suggesting that extension fractures may promote crack coalescence in these regions (Fig.
819 12A, insets). In contrast, between cracks in arrays oriented at approximately -70° , the trajectories of $\vec{\sigma}_1$ tend
820 to align with the direction of $\vec{\sigma}_1^\infty$, and fail to connect the tips of neighboring cracks (Fig. 12A, first inset).

821



822

823 Fig. 12: Stress and strain fields in a system with 500 horizontally aligned cracks ($\vartheta_0 = 0^\circ$ and $\text{RanDeg} = 0$)

824 with random locations. In the first inset, a subdomain containing an *en echelon* array of cracks is illustrated.

825 The second inset shows the interactions between the tips of a few cracks in the *en echelon* array. (a)

826 Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent the local trajectories of



827 the major in-plane principal stress $\bar{\sigma}_1$. (b) Normalized effective cohesion $\bar{C}$. White and black lines indicate the
828 potential orientations of conjugate shear fractures. (c) Normalized first strain invariant $\bar{I}_1$. (d) Normalized
829 shear strain $\bar{\epsilon}_{xy}$.

830

831 Similarly, analysis of the $\bar{C}$ distribution in this system reveals elongated regions of low $\bar{C}$ values oriented at
832 angles of 35-45° (Fig. 12B). We observe that the orientations of the regions formed by the overlap of high- $\bar{C}$
833 lobes concentrated at the tips of individual cracks are similar to those associated with reduced compression.
834 Lobes of high $\bar{C}$ elongating at low angles relative to the crack direction link multiple cracks arranged in arrays
835 oriented at approximately -15°, whereas lobes of high $\bar{C}$ elongating at high angle relative to the crack
836 direction mechanically link crack tips at angles of 60-70° (Fig. 12B). In this case, we also observe that the
837 interaction associated with the high-angle lobes of elevated $\bar{C}$ extends farther from the crack tips, connecting
838 cracks separated by distances of 3-4 times the crack half-length (Fig. 12B). The local trajectories of potential
839 shear fractures effectively connect the tips of adjacent cracks arranged in arrays oriented at approximately -
840 10° to -15°, and those in arrays oriented at -60 to -70° when the crack separation is small (Fig. 12B, insets).

841 High values of $\bar{I}_1$ concentrate between cracks arranged in arrays oriented at angles between -10° and -40°
842 (Fig. 12C). In this case, due to the different geometry of the regions of high volumetric dilation at the tips of
843 individual cracks compared to those observed for $\bar{\sigma}_2$ and $\bar{C}$, interactions between cracks in arrays oriented
844 at lower negative angles are much weaker (Fig. 12C). Symmetrically, volumetric contraction is observed
845 between cracks arranged in arrays oriented at angles between 10° and 40° (Fig. 12C). The perturbation to the
846 strain field appears to affect smaller regions around cracks than those observed for the stress field.
847 Consequently, interactions between regions of high $\bar{I}_1$ require small crack separations and high overlap to
848 occur (Fig. 12C, insets).

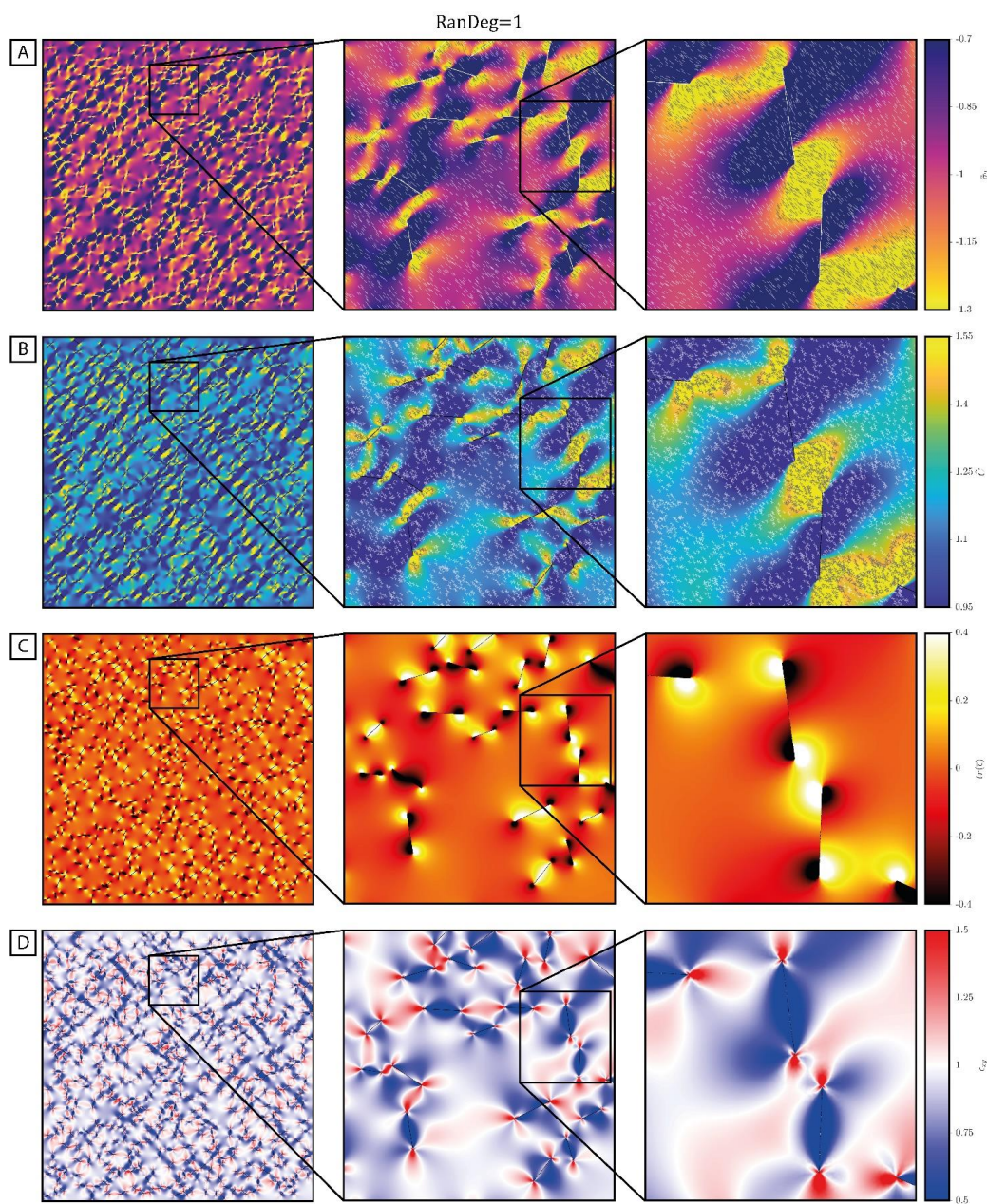
849 Elliptical regions of low $\bar{\epsilon}_{xy}$ are observed along the major axes of the individual cracks (Fig. 12D). These
850 regions of strain shadowing do not merge into longer regions with distinct orientations. In contrast, shear
851 strain reaches high values between approximately collinear cracks arranged in arrays oriented between -10°



852 and 10° , forming long chains of mechanically interacting cracks (Fig. 12D). This observation is consistent with
853 the fact that the largest regions of elevated $\bar{\epsilon}_{xy}$ are shaped as lobes elongating parallel to the crack direction
854 (Fig. 12D, insets). Because of the orientation of the two smaller, symmetrical lobes of high $\bar{\epsilon}_{xy}$ that extend
855 from the crack tips opposite to the crack direction, crack arrays oriented at $\pm 45^\circ$ can also interact through
856 the development of narrower regions of elevated shear strain (Fig. 12D, insets).

857 Fig. 13 illustrates the distribution of $\tilde{\sigma}_2$, $\tilde{C}$, $\tilde{I}_1$, and $\bar{\epsilon}_{xy}$ in the system containing randomly located and
858 randomly oriented cracks ($RanDeg = 1$). Additional configurations with intermediate degrees of crack
859 alignment ($RanDeg = 0.25, 0.5$) are illustrated in Figures A8 and A9. In this configuration, analysis of the $\tilde{\sigma}_2$
860 distribution reveals multiple interference patterns. Sub-horizontally aligned cracks ($\vartheta_i \approx 0^\circ$) arranged in
861 arrays oriented at approximately -15° , and sub-vertically aligned cracks ($\vartheta_i \approx 90^\circ$) arranged in arrays
862 oriented at approximately -75° , interact through the overlap of regions of elevated $\tilde{\sigma}_2$ that emanate
863 asymmetrically from their tips relative to the crack direction (Fig. 13A; see also Fig. 2B, Fig. 3A, and Fig. 5A).
864 Cracks aligned with the orientation of $\vec{\sigma}_1^\infty$ and arranged in arrays oriented at angles ranging from -30° to -60°
865 interact through the overlap of the symmetrical lobes at their tips, forming chains subparallel to the far-field
866 maximum compressive stress (Fig. 13A; see also Fig. 2A). Cracks oriented at 45° , owing to the geometry of
867 the regions of elevated $\tilde{\sigma}_2$ surrounding them (Fig. 2A), do not interact efficiently within long arrays. However,
868 in some regions of the domain, the stress perturbations they induce may act as bridges that facilitate the
869 overlap of regions of elevated $\tilde{\sigma}_2$ around differently oriented cracks (Fig. 13A). Analysis of the principal stress
870 trajectories reveals that, in arrays of cracks with $\vartheta_i \approx 90^\circ$ oriented at approximately -75° , the tips of adjacent
871 cracks are effectively connected by the local trajectories of $\vec{\sigma}_1$, similarly to the arrays of cracks with $\vartheta_i \approx 0^\circ$
872 oriented at approximately -15° discussed in the previous section (Fig. 13A, insets). In contrast, for cracks with
873 $\vartheta_i \approx -45^\circ$, the local trajectories connect neighboring crack tips only when cracks are nearly collinear, such
874 that only arrays oriented at approximately -45° appear geometrically favorable for coalescence (Fig. 13A,
875 insets).

876



877

878 Fig. 13: Stress and strain fields in a system containing 500 randomly oriented cracks ($RanDeg = 1$) with
 879 random locations. In each row, the first inset illustrates a subdomain containing mechanically interacting
 880 cracks with different orientations. The second inset shows the interaction between the tips of two aligned
 881 cracks. (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent the local



882 trajectories of the major in-plane principal stress $\tilde{\sigma}_1$. (b) Normalized effective cohesion $\tilde{C}$. White and black
883 lines indicate the potential orientations of conjugate shear fractures. (c) Normalized first strain invariant $\tilde{I}_1$.
884 (d) Normalized shear strain $\tilde{\epsilon}_{xy}$.

885

886 The distribution of $\tilde{C}$ is essentially similar to that of $\tilde{\sigma}_2$. Arrays of sub-horizontally and sub-vertically aligned
887 cracks oriented at -15° and -75° , respectively, as well as arrays of nearly collinear cracks oriented at
888 approximately -45° produce the greatest overlap between regions of elevated $\tilde{C}$ (Fig. 13B). We observe that
889 the tips of cracks oriented at -45° and arranged in arrays oriented at approximately -15° and -75° are
890 effectively connected by the orientations of the potential shear fractures that may develop within regions of
891 elevated $\tilde{C}$ (Fig. 13B). In addition, horizontally oriented arrays of cracks with $\vartheta_i \approx 30^\circ$ mechanically interact
892 through the development of sigmoidal regions of elevated $\tilde{C}$, within which the orientations of potential shear
893 fractures connect the tips of the neighboring cracks (Fig. 13B, first inset).

894 Volumetric dilation occurs in arrays of cracks with $\vartheta_i \approx \pm 45^\circ$ oriented at approximately -45° . However, for
895 arrays of cracks with $\vartheta_i \approx -45^\circ$, the narrow, circular geometry of the regions of elevated dilation at their
896 tips requires the cracks to be nearly collinear for the regions of high $\tilde{I}_1$ to overlap effectively (Fig. 13C). In
897 contrast, the regions of high $\tilde{I}_1$ surrounding cracks with $\vartheta_i \approx 45^\circ$ exhibit broader, elliptical shapes, producing
898 wider perturbation regions in which the cracks do not need to be perfectly aligned within a straight array to
899 interact mechanically (Fig. 13C). We also observe patterns similar to those identified for $\tilde{\sigma}_2$ and $\tilde{C}$: sub-
900 horizontal cracks arranged in arrays oriented at approximately -15° , and sub-vertical cracks arranged in arrays
901 oriented at approximately -75° , mechanically interact through overlap of regions of high $\tilde{I}_1$ at their tips (Fig.
902 13C).

903 Shear strain tends to concentrate within single-lobe-shaped regions elongating in the crack direction from
904 the tips of sub-horizontal and sub-vertical cracks. Therefore, these concentrations of $\tilde{\epsilon}_{xy}$ at the individual
905 crack tips overlap efficiently when the cracks are arranged in sub-horizontal and sub-vertical arrays,
906 respectively (Fig. 13D). Because the regions of elevated $\tilde{\epsilon}_{xy}$ at the tips of cracks oriented at $\vartheta_i \approx \pm 45^\circ$ are



907 shaped as double lobes symmetrical with respect to the crack direction, the geometrically favorable array
908 orientations for mechanical interaction are -15° and -75° for cracks with $\vartheta_i \approx -45^\circ$, and 15° and 75° for
909 cracks with $\vartheta_i \approx 45^\circ$ (Fig. 13D).

910

911 5. Discussion

912 The presented numerical results provide valuable insight into how the mechanical interaction between pre-
913 existing cracks depends on their geometry, orientation and spacing. In the following, we discuss the
914 implications of local stress and strain perturbations for potential fracture nucleation, crack linkage and fault
915 development in upper-crustal rocks. First, we consider how confining pressure and pore fluid pressure affect
916 the conditions for crack closure and brittle failure. Then, we examine how geometrically controlled stress
917 perturbations may promote or inhibit crack coalescence, and how crack-scale interactions can be related to
918 the development of larger fracture networks and faults. Finally, we compare some of the model results with
919 geological structures observed in nature.

920

921 5.1 From reduced to normalized effective stresses: the potential for tensile failure under crustal lithostatic 922 and pore pressure conditions

923 In the presented models, stress values are reduced and normalized, allowing the results to be interpreted
924 independently of a specific ambient stress magnitude. The confining lithostatic pressure component is
925 subtracted to isolate the stress perturbation due to the presence of cracks under an increment of the far-
926 field simple shear. Negative values of the reduced minor in-plane principal stress correspond to regions of
927 reduced compression, which may embed sites of effective tension depending on the balance between
928 confining pressure, local pore pressure and the applied far-field deviatoric stress. However, to assess whether
929 a given value of reduced stress is sufficient to promote tensile crack growth or fracture nucleation, the
930 normalized values must be converted into dimensional effective stresses based on the crustal depth ranges
931 of interest.



932 A first-order conversion can be obtained by assuming a lithostatic pressure state, according to Heim's rule
933 (Milnes, 1979), and upper-crustal rock densities of approximately $2600\text{--}2800\text{ kg/m}^3$, that correspond to a
934 lithostatic gradient of about 27 MPa/km. For a homogeneous hydrostatic pore pressure increasing at
935 approximately 10 MPa/km, the background effective confining pressure is

936
$$P_{eff} [\text{MPa}] = P^\infty - P_f \approx 17 \cdot z [\text{km}] \quad (15)$$

937 Where z is depth expressed in kilometers and the resulting P_{eff} in MPa. This background effective pressure
938 is independent of crack orientation, and the effective stresses at a given depth can be obtained by adding
939 P_{eff} to the calculated reduced stresses upon scaling them with the postulated far-field shear stress.

940 For the elastic parameters and boundary conditions used in the present work, the prescribed increment of
941 far-field simple shear produces a dimensional differential stress of 48 MPa. Therefore, a normalized reduced
942 stress of a negative unit value ($\tilde{\sigma}_2 = -1$) corresponds to a local reduction of the minor in-plane principal
943 stress of 24 MPa relative to the unperturbed background value due to the ambient lithostatic pressure. In
944 contrast, positive values of $\tilde{\sigma}_2$ indicate elevated compression. Depending on the presumed depth and pore
945 pressure conditions, the same reduced and normalized stress value may correspond to different effective
946 stresses and mechanical outcomes.

947 Threshold values of $\tilde{\sigma}_2$ within regions of reduced compression include -2, -4, and -10. The value $\tilde{\sigma}_2 \approx -2$
948 corresponds to the threshold commonly used in maps of the spatial distribution of $\tilde{\sigma}_2$ magnitudes. Values
949 around $\tilde{\sigma}_2 \approx -4$ represent the approximate minimum reached at the midpoint between neighboring
950 underlapping cracks, $\tilde{\sigma}_2^m$, whereas values approaching $\tilde{\sigma}_2 \approx -10$ correspond to the strongest midpoint
951 minima obtained for overlapping crack configurations. With the presumed far-field tectonic shear stress,
952 which dictates the dimensional scaling adopted here, these values of $\tilde{\sigma}_2$ correspond to local reductions of
953 the minor in-plane principal stress of approximately 48, 96 and 240 MPa, respectively.

954 Tensile failure can occur without fluid overpressure only where the local stress reduction is sufficiently large
955 to overcome both the hydrostatic effective confining pressure and the tensile strength of the rock (Brace et
956 al., 1968; Paterson and Wong, 2005; Brantut et al., 2013). Here, fluid overpressure refers to pore fluid



pressure exceeding the hydrostatic pressure at a given depth (Osborne and Swarbrick, 1997). Assuming a tensile strength of $T_0 = 10$ MPa representative for intact rocks (Miskovsky, 2011), the approximate condition for tensile failure under hydrostatic pore fluid pressure is

$$17 \cdot z \text{ [km]} + 24\tilde{\sigma}_2 \text{ [MPa]} < -T_0 \text{ [MPa]} \quad (16)$$

Accordingly, a stress reduction of $\tilde{\sigma}_2 \approx -2$ may be sufficient to exceed the tensile strength only within the top 2 km of the crust (Fig. 14A). Values around $\tilde{\sigma}_2 \approx -4$, and especially $\tilde{\sigma}_2 \approx -10$, which are locally reached at the midpoints between cracks, may remain sufficient to promote tensile failure to greater depths (Fig. 14A). Between 5 and 10 km, values of $\tilde{\sigma}_2 \approx -2$ would require significant pore fluid overpressure, whereas values around $\tilde{\sigma}_2 \approx -4$ may induce tensile failure mainly in the shallower part of this interval (Fig. 14A). In contrast, values around $\tilde{\sigma}_2 \approx -10$ still exceed the tensile strength under hydrostatic conditions (Fig. 14A). At depths greater than 10 km, within typical upper-crustal seismogenic conditions (Faulkner et al., 2010), only values close to $\tilde{\sigma}_2 \approx -10$ would allow the stress state between cracks to approach effective tension without substantial overpressure, although some degree of overpressure would certainly be required below depths of approximately 12 km.

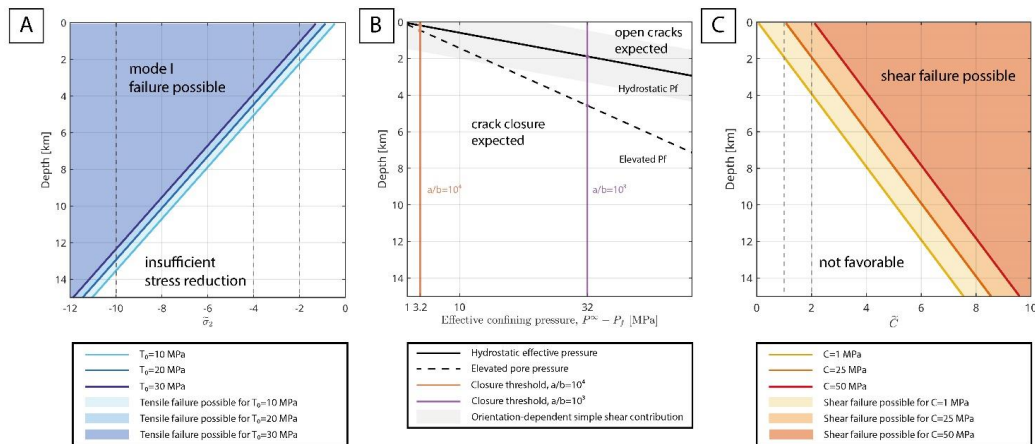


Fig. 14: Mechanical conditions for tensile failure, crack closure and shear failure under upper-crustal effective pressure conditions. (a) Critical magnitude of reduced and normalized minor in-plane principal stress, $\tilde{\sigma}_2$,



975 required for mode I tensile failure for $T_0 = 10, 20, 30$ MPa. The shaded regions represent stress conditions
976 where tensile failure is possible, and vertical dashed lines show representative model outputs of $\tilde{\sigma}_2$. (b)
977 Effective confining pressure ($P^\infty - P_f$) as a function of depth for hydrostatic pore pressure and for a possible
978 elevated pore pressure gradient. The grey band illustrates the orientation-dependent simple shear
979 contribution to the effective stress component acting normal to the crack walls. Vertical lines represent
980 normal stress thresholds for crack closure (for cracks with aspect ratios $\frac{a}{b} = 10^4, 10^3$). (c) Critical reduced
981 and normalized cohesion $\tilde{C}$ required for shear failure for rocks with cohesion of $C=1, 25$, and 50 MPa. Shaded
982 regions indicate conditions where shear failure is possible. Vertical dashed lines mark representative model
983 ranges of $\tilde{C}$.

984

985 In the shallow upper crust, or in deeper regions affected by elevated pore fluid pressure, the local reduction
986 of the least compressive stress observed in the models may locally result in effective tensile stresses
987 exceeding rock tensile strength, which promotes tensile fracture growth. For typical tectonic stress values up
988 to a few tens of MPa, the moderate values of reduced $\tilde{\sigma}_2$ between -2 and -4 are mainly relevant at shallow
989 depths, whereas the strongest local minima, approaching -10, may produce sites prone to tensile failure over
990 a broader depth range. Since the values of $\tilde{\sigma}_2$ discussed here are evaluated at the midpoints between
991 neighboring cracks, where the influence of individual crack-tip singularities is reduced, the analyzed potential
992 for tensile linkage between multiple cracks is underestimated.

993

994 **5.2 Crack closure and pore fluid pressure**

995 A key assumption of the presented models is that cracks are represented as highly elongated, frictionless
996 elliptical voids. This approximation builds on the classical framework of an elliptical hole in an infinite
997 medium, in which local stress perturbations are controlled by the aspect ratio of the cavity and the far-field
998 loads (Pollard and Segall, 1987; Jaeger et al., 2009). Elliptical voids approximate slit cracks in the limit of high
999 aspect ratio, while avoiding the stress singularity associated with an ideal sharp crack tip, which is generally



1000 difficult to resolve accurately in standard numerical models. In our study, this numerical approach is used to
1001 investigate the stress perturbations and interference introduced by persistently open cracks away from the
1002 immediate near-tip region. We therefore avoid directly addressing challenging processes such as partial or
1003 complete crack closure, contact mechanics between rough crack walls, frictional slip, and mineral sealing.
1004 Nonetheless, natural cracks in the upper crust may be voids, open and fluid-filled, closed or sealed by
1005 minerals, as well as undergoing frictional sliding, depending on the far-field loads and pore fluid pressure that
1006 determine the effective normal stress acting on the crack walls (Brace et al., 1968; Kranz, 1983; Brantut et
1007 al., 2013; Anders et al., 2014). The present results therefore describe the elastic stress field around
1008 mechanically open, traction-free cracks, but not around closed or partially closed cracks that can transmit
1009 normal stress and experience frictional slip. In the following, we inspect the limitations introduced by this
1010 assumption.

1011 At first order, crack closure is governed by the effective normal stress acting across the crack walls:

1012
$$\sigma'_n = \sigma_n - P_f \quad (17)$$

1013 where σ_n is the total normal stress resolved across the crack and P_f is the internal pore fluid pressure. If
1014 $\sigma'_n > 0$, the crack is under effective compression and tends to close. If $\sigma'_n < 0$, pore fluid pressure exceeds
1015 the compression resolved at the crack walls, and hydraulic fracturing may occur at the crack tip. Thus, the
1016 simplest idealized condition to ensure crack opening would be the state of hydraulic overpressure $P_f > \sigma_n$
1017 for all the cracks in the considered system, even though an elliptical crack with a finite initial aperture (aspect
1018 ratio) does not require the effective normal stress to vanish completely to remain partially open.

1019 A more realistic condition for complete crack closure under the plane strain approximation builds on the
1020 elastic model (Jaeger et al., 2009):

1021
$$\sigma_1^\infty = \frac{G}{1-\nu} \frac{b}{a} \quad (18)$$



1022 where $\sigma_{\perp}^{\infty}$ is the far-field normal stress acting perpendicular to the crack walls that is sufficient for closing a
1023 slit crack of aspect ratio a/b , which is embedded in an elastic medium with shear modulus G and Poisson's
1024 ratio ν .

1025 For the common elastic parameters of rocks that are invoked in this study, ($E=60$ GPa, $\nu=0.25$), the shear
1026 modulus is $G=24$ GPa. Microcracks in rocks are typically highly elongated and under vanishing effective loads
1027 exhibit aspect ratios b/a in the range between 10^{-4} and 10^{-3} (Feves and Simmons, 1976; Kranz, 1983).
1028 Hence, the estimated far-field effective normal stress acting perpendicular to the crack walls needed for
1029 complete (all cracks within the postulated range of aspect ratios) crack closure yields:

1030
$$\sigma_{\perp c}^{\infty} \approx 32 \text{ MPa} \quad (19)$$

1031 Before considering the effects due to a tectonic increment of simple shear, this threshold can be compared
1032 with the background effective pressure introduced in Section 5.1. Under lithostatic loading and hydrostatic
1033 pore fluid pressure (Eq. 15), closure thresholds of 3.2 and 32 MPa are reached at approximate depths of

1034
$$z_c \approx \frac{3.2}{17} \approx 0.2 \text{ km} \quad (20)$$

1035 and

1036
$$z_c \approx \frac{32}{17} \approx 1.9 \text{ km} \quad (21)$$

1037 respectively. Thus, under hydrostatic pore pressure conditions, very thin cracks with $\frac{b}{a} \approx 10^{-4}$ are expected
1038 to close within the upper few hundred meters, whereas cracks with $\frac{b}{a} \approx 10^{-3}$ may remain partially open up
1039 to depths approaching 2 km (Fig. 14B). Cracks with larger apertures would require greater effective
1040 compression for complete closure.

1041 At greater depths, maintaining open cracks requires pore fluid pressure above hydrostatic values, such that

1042
$$P^{\infty} - P_f < \frac{G}{1-\nu} \frac{b}{a} \quad (22)$$

1043 or equivalently,



1044
$$P_f > P^\infty - \frac{G}{1-\nu} \frac{b}{a} \quad (23)$$

1045 Fluid overpressure may occur if fractures are hydraulically isolated, permeability is reduced, or fluid
1046 production exceeds drainage (Brace et al., 1968; Kranz, 1983; Paterson and Wong, 2005; Brantut et al., 2013).
1047 This limitation is particularly relevant for *en echelon* crack systems, because mechanical models of *echelon*
1048 veins show that vein spacing, the relative orientation between veins and arrays, elastic stiffness, internal
1049 crack pressure, and the closing of intersecting pressure-solution seams can all influence crack opening and
1050 near-tip stress fields (Seyum and Pollard, 2016). In particular, the closing of pressure-solution seams may
1051 modify the mechanical interaction between adjacent open veins, alter the opening distribution along the
1052 veins, and promote straighter propagation paths.

1053 In the present models, which simulate the stress field due to a simple shear increment of $\gamma=10^{-3}$, the induced
1054 far-field shear stress is approximately $\tau^\infty = G\gamma \approx 24 \text{ MPa}$.

1055 The normal stress increment acting perpendicular to a crack is

1056
$$\sigma_\perp^\infty = \sigma_1^\infty \cos^2 \beta + \sigma_2^\infty \sin^2 \beta \quad (24)$$

1057 where σ_1^∞ and σ_2^∞ are the reduced major and minor in-plane far-field principal stresses, equal to 24 and -24
1058 MPa, respectively, and β is the angle between the ellipse minor-axis direction, normal to the crack walls, and
1059 the far-field maximum compressive stress direction $\vec{\sigma}_1^\infty$.

1060 Since $\vec{\sigma}_1^\infty$ is oriented at -45° under right-lateral simple shear, the angle ϑ between the major axis of the cracks
1061 and the horizontal is related to β as follows:

1062
$$\beta = \vartheta - 45^\circ \quad (25)$$

1063 The tectonic normal-stress increment can therefore be written as

1064
$$\sigma_\perp^\infty = G\gamma \sin 2\vartheta \quad (26)$$

1065



1066 For the $\frac{b}{a} \approx 10^{-4}$ cracks used in the *en echelon* models, and considering only the reduced far-field stress
1067 generated by the prescribed simple shear, and neglecting both confining pressure and pore fluid pressure,
1068 the closure threshold is exceeded for:

1069
$$3.8^\circ \lesssim \vartheta \lesssim 86.2^\circ \quad (27)$$

1070 When the depth-dependent background effective pressure is also included, the condition required to prevent
1071 complete closure becomes:

1072
$$P_f > P^\infty + \sigma_\perp^\infty(\vartheta) - \frac{G}{1-\nu} \frac{b}{a} = P^\infty + G\gamma \sin 2\vartheta - \frac{G}{1-\nu} \frac{b}{a} \quad (28)$$

1073 This relation shows that the pressure required to keep a crack open depends not only on depth and pore
1074 fluid pressure, but also on crack orientation, aspect ratio and elastic parameters of the rock undergoing
1075 deformation.

1076 This distinction is important because open and closed cracks produce different near-tip stress fields. Open
1077 cracks concentrate tensile stresses and promote mode I crack propagation, whereas closed cracks may
1078 reactivate by frictional sliding or mixed-mode propagation, generating different wing crack angles (Brace and
1079 Bombolakis, 1963; Pollard and Fletcher, 2005; Lee et al., 2022).

1080 It is also important to distinguish the role of pore pressure in macroscopic failure criteria from its role at the
1081 individual crack scale. In macroscopic failure criteria, pore pressure is usually treated as an isotropic
1082 contribution to the stress tensor σ' :

1083
$$\sigma' = \sigma - P_f \mathbf{I} \quad (29)$$

1084 where $\mathbf{I}$ is the identity tensor. In this framework, pore pressure decreases the mean stress and shifts Mohr
1085 circles toward lower effective normal stress, without directly affecting the deviatoric stress tensor.

1086 At the crack scale, pore fluid pressure acts as a normal traction on discrete crack walls, inducing elastic strain
1087 in the surrounding medium. Unless pore fluid pressure in all cracks exactly matches the ambient lithostatic
1088 pressure, producing purely volumetric deformation in a homogeneous material, this results in an elastic



1089 perturbation in the surrounding medium which includes deviatoric components. Directly including internal
1090 crack pressure in the future models would allow for assessing the closure of individual cracks as well as
1091 quantifying the local stress perturbation associated with the difference between the pore fluid pressure and
1092 the overall lithostatic pressure.

1093

1094 **5.3 Cohesion and pressure-dependent shear failure**

1095 As confining pressure increases, cracks tend to close, and frictional sliding is likely to occur. Shear failure is
1096 controlled by the balance between differential and normal stress, pore fluid pressure, cohesion and angle of
1097 internal friction (Brace and Bombolakis, 1963; Paterson and Wong, 2005; Brantut et al., 2013; Lee et al.,
1098 2022). The dependence of shear failure on pressure is consistent with laboratory observation showing that
1099 shear fracturing becomes increasingly important at higher confinement, particularly on the verge of
1100 macroscopic failure (Stanchits et al., 2006; Graham et al., 2010; McBeck et al., 2023). The interpretation of
1101 the obtained results depends on the comparison between the estimated local effective cohesion threshold
1102 values and realistic values of rock cohesion.

1103 To evaluate potential shear failure in regions located between the cracks, we used the Mohr-Coulomb
1104 criterion with a representative angle of internal friction of $\phi = 35^\circ$, consistent with typical values for
1105 unweathered upper-crustal rocks. The model output $\tilde{C}$ may be interpreted as the reduced and normalized
1106 value of the cohesion that a rock would need to avoid shear failure under a specific local stress state.
1107 Therefore, if the cohesion of the rock is lower than the dimensional value of $\tilde{C}$ for a given set of lithostatic
1108 and pore fluid pressures, shear fracture nucleation may occur along the orientations predicted by the Mohr-
1109 Coulomb criterion. Therefore, high values of $\tilde{C}$ identify regions where the local stress perturbation strongly
1110 favors shear failure.

1111 Given the boundary conditions used in the present study, the conversion of $\tilde{C}$ to a dimensional cohesion
1112 threshold C_{eff} (in MPa) is performed as follows:



1113
$$C_{eff}(z)[MPa] = 24 \cdot \tilde{C} [MPa] - (P^{\infty}(z) - P_f(z)) \tan \phi [MPa] \quad (30)$$

1114 Where z is depth. Assuming, as in the previous section, an internal friction angle $\phi = 35^\circ$, a lithostatic
1115 gradient of 27 MPa and hydrostatic pore fluid pressure of approximately 10 MPa, the expression for C_{eff}
1116 becomes:

1117
$$C_{eff}(z)[MPa] \approx 24 \cdot \tilde{C} [MPa] - 12 \cdot z [km] \quad (31)$$

1118 In the *en echelon* crack models, about 11% of the considered geometrical configurations lead to a value of
1119 $\tilde{C} < 1$ at the midpoint between neighboring cracks. These values correspond to local stress states that may
1120 be unfavorable for shear failure. In these configurations, the stress perturbation induced by the presence of
1121 the cracks tends to inhibit shear failure activation, particularly when confining pressure is considered. In most
1122 configurations (about 70% of the studied setups), $1 < \tilde{C} < 2$. These values of $\tilde{C}$ correspond to local stress
1123 states which may be moderately favorable for the activation of shear failure. These configurations may
1124 promote shear failure, especially where confinement is low, pore fluid pressure is elevated, or the host rock
1125 is poorly consolidated. The remaining configurations have $\tilde{C} > 2$, reaching values of up to 8 in a few
1126 configurations. These high values correspond to local stress states that may be favorable for shear failure
1127 development due to stress perturbations between the interacting microcracks. In these cases, the stress
1128 perturbation may promote shear failure even in rocks with relatively high cohesion, although effective
1129 pressure still controls the feasible depth range.

1130 These ranges of $\tilde{C}$ can be compared with representative values of cohesion for different lithologies. Weak or
1131 highly damaged rocks may have cohesion values of the order of 1 MPa, as reported for low-strength wet
1132 mudstones (Winn et al., 2017). Moderately strong rocks may be represented by $C \approx 25$ MPa, consistent with
1133 cohesion values measured for intact mudstone, pyroclastic rocks or granite. Strong rocks may reach $C \approx 50$
1134 MPa, as reported for measured values of high strength crystalline or diabase samples (Winn et al., 2017; Chen
1135 et al., 2023). These values are taken as reference cohesion levels to assess the possibility of shear failure at
1136 confining pressures and ranges of $\tilde{C}$.



1137 In the shallow upper crust, between 0 and 5 km depth (corresponding to an increase of effective pressure
1138 from 0 to about 60 MPa under hydrostatic pore fluid pressure), for very weak or highly damaged rocks with
1139 $C \approx 1$ MPa, even model configurations that yield values of $\tilde{C} < 1$ may promote shear failure down to
1140 approximately 2 km depth, whereas the range $1 < \tilde{C} < 2$ may remain favorable down to approximately 4
1141 km (Fig. 14C). For rocks of moderate cohesion ($C \approx 25$ MPa), configurations with $\tilde{C} < 1$ are insufficient to favor
1142 shear failure near the surface, whereas configurations with $1 < \tilde{C} < 2$ may promote it down to about 2 km
1143 (Fig. 14C). Stronger rocks ($C \approx 50$ MPa) generally require $\tilde{C} > 2$ to generate stress states favorable enough for
1144 shear failure within this depth range (Fig. 14C).

1145 Between 5 and 10 km depth, the effective pressure term increases from about 60 to 120 MPa under
1146 hydrostatic pore fluid pressure. Therefore, configurations with $\tilde{C} < 1$ are not favorable for shear failure
1147 development, even in very weak rocks, whereas most configurations within the range $1 < \tilde{C} < 2$ become
1148 effective only if the rock is very weak, or for pore fluid pressure above hydrostatic values (Fig. 14C). For rocks
1149 of moderate cohesion, in this depth range, shear failure requires values close to $\tilde{C} \approx 2$ or even higher (Fig.
1150 14C). Stronger rocks, with $C \approx 50$ MPa, require $\tilde{C} \gtrsim 4 - 7$, unless pore fluid pressure approaches lithostatic
1151 pressure (Fig. 14C).

1152 At depths higher than 10 km, which correspond to the base of the typical seismogenic zone in the upper
1153 crust, the effective pressure correction is larger than 120 MPa. Therefore, configurations with $\tilde{C} < 4$ are not
1154 favorable for shear fracture nucleation under hydrostatic pore pressure and the presumed level of tectonic
1155 load (Fig. 14C). At these depths, shear failure in weak to moderately cohesive rocks requires either
1156 substantially higher values of $\tilde{C} > 5 - 6$ or pore fluid pressure significantly above hydrostatic values (Fig.
1157 14C). Strong rocks, with $C \approx 50$ MPa, require values of $\tilde{C}$ close to the highest values observed in the models,
1158 approximately $\tilde{C} > 7$ at 10 km depth (Fig. 14C). At greater depths, even these configurations would require
1159 elevated pore fluid pressure, potentially approaching lithostatic pressure, to remain favorable for shear
1160 failure.



1161 The dependence of the Mohr-Coulomb shear failure estimates on depth can be compared with that for mode
1162 I failure in Section 5.1. Under hydrostatic pore-pressure conditions, increasing depth corresponds to
1163 increased effective confining pressure, so larger stress perturbations are required to induce either tensile or
1164 shear failure (Brace and Bombolakis, 1963; Paterson and Wong, 2005; Jaeger et al., 2009; Brantut et al.,
1165 2013). For example, at 5 km, tensile failure for $T_0 = 10 \text{ MPa}$ requires approximately $\tilde{\sigma}_2 \lesssim -4$, whereas shear
1166 failure requires $\tilde{C} \gtrsim 2.5$ for a very weak rock with ($C \approx 1 \text{ MPa}$) and $\tilde{C} \gtrsim 3.5$ for a rock with ($C \approx 25 \text{ MPa}$).
1167 At 10 km, the corresponding thresholds increase to approximately $\tilde{\sigma}_2 \lesssim -7.5$, $\tilde{C} \gtrsim 5$, and $\tilde{C} \gtrsim 6$,
1168 respectively. Thus, the commonly observed range ($1 < \tilde{C} < 2$) is mainly relevant for shallow depths and
1169 rocks with low cohesion, whereas only the highest values of $\tilde{C}$ obtained in the models remain sufficient for
1170 shear failure near the base of the upper-crustal seismogenic zone under hydrostatic conditions. Poor fluid
1171 pressure above hydrostatic values reduces the effective normal stress and expands the depth range over
1172 which both tensile and shear failure may occur.

1173

1174 **5.4 Geometry-controlled stress interference and crack coalescence**

1175 Our numerical results indicate that the geometry of pre-existing cracks strongly influences the location,
1176 magnitude and orientation of stress perturbations that may promote fracture nucleation and crack linkage.
1177 This is consistent with the general view that brittle failure in rocks is not controlled only by the far-field stress,
1178 but also by the local stress concentrations generated by flaws, pores, grain boundaries, cracks and other
1179 discontinuities (Griffith, 1920; Brace and Bombolakis, 1963; Pollard and Fletcher, 2005; Anders et al., 2014).
1180 This interpretation is also consistent with studies of fault process zones, where microfracture density and
1181 orientation are interpreted as records of altered stress fields around propagating fault tips (Vermilye and
1182 Scholz, 1998; Wilson et al., 2003; Mitchell and Faulkner, 2009).

1183 The analysis of the *en echelon* models shows that arrays inclined at equal but opposite angles relative to the
1184 crack direction produce significantly different stress interactions between neighboring crack tips. For some
1185 geometries, decreasing separation promotes the overlap of regions of reduced compression between



1186 adjacent crack tips. In these cases, the local stress state may approach effective tension if the reduction in
1187 the minor in-plane principal stress is sufficiently large relative to the confining and pore pressure conditions
1188 (see Sec. 5.1). This behavior agrees with the general crack interaction framework proposed by Reches and
1189 Lockner (1994), who argued that macroscopic shear fractures may originate from the overlap of tensile stress
1190 concentrations between cracks originated in mode I. However, our results extend this concept by
1191 demonstrating that favorable stress conditions are not restricted to cracks initially parallel to $\vec{\sigma}_1^\infty$. Instead,
1192 we argue that cracks with different orientations, especially mode II-oriented cracks, may generate
1193 asymmetric lobes of reduced compression, which are particularly effective in generating linking paths oblique
1194 relative to the direction of $\vec{\sigma}_1^\infty$. These regions of reduced compression are particularly important because
1195 they can define potential pathways for local mode I crack growth leading to macroscopic fracture linkage.
1196 This interpretation is consistent with experimental and theoretical studies in which macroscopic shear
1197 fractures develop through the interaction and coalescence of tensile microcracks, while in-plane mode II
1198 propagation is strongly inhibited (Brace et al., 1966; Scholz, 1968; Petit and Barquins, 1988; Reches and
1199 Lockner, 1994; Healy et al., 2006). Besides the magnitude of reduced compression that controls the potential
1200 of locally shifting the effective stress into the tensile regime, the orientation of the local principal stress
1201 trajectories is also essential to infer crack linkage, because mode I fractures are expected to propagate
1202 perpendicular to the local least compressive principal stress (parallel to the local maximum compressive
1203 principal stress). Therefore, direct tensile crack coalescence could be problematic within overlapping lobes
1204 of reduced compression with local $\vec{\sigma}_1$ trajectories that do not connect adjacent crack tips. This is consistent
1205 with Healy et al. (2006), who showed that the elastic interaction between finite three-dimensional mode I
1206 cracks may produce tensile linkage paths oblique to $\vec{\sigma}_1^\infty$. Our models show that comparable conditions may
1207 also develop around mode II-oriented cracks. A specific example is provided by horizontal cracks arranged in
1208 *en echelon* arrays at $\varphi = -15^\circ$, for which overlapping lobes of reduced compression and local $\vec{\sigma}_1$ trajectories
1209 connect adjacent tips at intermediate values of crack separation (Figs. 3, 5).

1210 The opposite behavior occurs in geometries where the region between adjacent cracks is characterized by
1211 elevated compression. In these configurations, decreasing crack separation does not necessarily promote



linkage. Instead, the interaction between crack tips may inhibit coalescence because of locally increased compression across the potential linkage region. This demonstrates that crack clustering is not automatically favorable for fault formation. Depending on their relative arrangement and orientation, closely spaced cracks may form mechanically linked arrays or represent regions of increased resistance to brittle deformation.

Models with randomly distributed cracks extend these observations to more realistic systems. Even in these models, in which cracks are not arranged into periodic arrays, favorable mechanical interactions emerge, where local crack subsets resemble *en echelon* geometries. In the models with aligned cracks, overlapping reduced-compression lobes define arrays oriented predominantly at approximately -10° to -18° relative to the crack direction, with additional alignments at higher angles. These orientations are compatible with common macroscopic shear-fracture orientations relative to $\vec{\sigma}_1^\infty$. This result provides a micro-mechanical analogue for field observations of faults initiating from sheared joints, *en echelon* joint zones, splays and discontinuous slip surfaces that progressively link with increasing deformation (Shipton and Cowie, 2001; Shipton and Cowie, 2003; de Joussineau and Aydin, 2007). These models suggest that apparently disordered crack systems may contain local geometrical arrangements that favor the early localization of fractures.

In the models with randomly oriented cracks, the most perturbed regions are associated with specific crack orientations and arrangements. In particular, regions of reduced compression surrounding the crack tips form around each isolated crack, but overlaps between these regions and pathways for potential macroscopic fracture coalescence ultimately only develop if multiple of these cracks are aligned and arranged in oriented arrays. In addition, only in a subset of these configurations also the local deflected trajectories of $\vec{\sigma}_1$ connect the tips of neighboring cracks, thus suggesting possible direct linkage. This is consistent with field studies of damage zones, which show that fracture density and fracture orientation vary systematically with distance from fault cores and with proximity to fault tips, auxiliary faults and geometrical irregularities (Wilson et al., 2003; Mitchell and Faulkner, 2009). It is also consistent with numerical models of off-fault damage, which show that local slip gradients and stress concentrations can lead to the formation of tensile fractures at some distance from the main fault surface (Savage and Cooke, 2010). Therefore, within an apparently disordered crack system, only subsets of favorably oriented and favorably positioned cracks may



1238 control the initial localization of fracture growth. This may explain why macroscopic fault zones emerge from
1239 distributed damage while preserving preferred orientations.

1240 These results suggest that the orientation of an emerging macroscopic fracture may be controlled by the
1241 spatial arrangement of mechanically interacting cracks and by the stress perturbations that they generate.
1242 The Mohr-Coulomb criterion can then be applied to the locally perturbed stress field to identify favorably
1243 oriented planes for shear failure or frictional sliding. The subsequent macroscopic fracture orientation may
1244 result from the progressive linkage of these locally favorable planes and pre-existing cracks, rather than being
1245 determined exclusively by the homogeneous far-field stress. This is compatible with the observation that
1246 shear fractures commonly form at angles predicted by frictional failure criteria, while supporting the
1247 interpretation that the underlying mechanisms may involve tensile stress concentration and crack
1248 coalescence (Reches and Lockner, 1994; Petit and Barquins, 1988; Healy et al., 2006; Vermilye and Scholz,
1249 1998).

1250 Regions of sufficiently reduced compression may promote mode I fracture growth, whereas regions with high
1251 values of $\tilde{C}$ identify locations where the local stress state may satisfy the Mohr–Coulomb criterion. The
1252 potential orientations of shear failure are defined relative to the local, rather than far-field, principal stress
1253 trajectories. Crack interaction may therefore control both where shear failure is possible and how the locally
1254 favorable failure planes are oriented between neighboring tips. Depending on crack geometry, effective
1255 pressure and rock strength, tensile and shear failure may act as alternative or complementary linkage
1256 mechanisms.

1257

1258 **5.5 Bridging crack-scale linkage and step fault growth**

1259 The obtained results can be interpreted within a broader framework in which faults progressively develop
1260 from the interaction and linkage of structural discontinuities. Natural faults are not simple planar surfaces,
1261 but instead usually segmented slip surfaces separated by relay zones, crossed by Riedel shears, and
1262 surrounded by damage zones characterized by heterogeneous strain (Faulkner et al., 2010). In this context,



1263 the crack interactions modelled in the present study may be regarded as a simplified mechanical analogue of
1264 composite fault zones. Local stress perturbations around the tips of discontinuities may promote the
1265 progressive linkage of initially isolated fractures into interconnected structures that accommodate large
1266 displacement.

1267 At the process zone scale, the distribution of microfractures around natural faults provides an important
1268 analogue for the stress perturbation models presented here. Vermilye and Scholz (1998) showed that
1269 densities and orientations of fault-related microfractures are different from those of background
1270 microfractures, and interpreted them as products of the perturbed stress field around fault tips. Similarly,
1271 Wilson et al. (2003) reported analyses of samples from the Punchbowl fault, in the San Andreas system, and
1272 similarly showed that microfracture density and orientation anisotropy increases towards the fault core,
1273 suggesting that the fabric of damage zone records both early growth stages and later deformation associated
1274 with slip. In the study of Mitchell and Faulkner (2009), several possible mechanical processes contributing to
1275 off-fault damage are compared, including Andersonian microcrack coalescence and interaction between
1276 faults through wing-crack growth. These studies describe the decay of fault-related damage away from fault
1277 cores and tips, providing a field-scale analogue to the decay of stress perturbations away from isolated cracks
1278 or crack arrays illustrated in the present models.

1279 The results can also be compared with numerical models in which off-fault damage is driven by local stress
1280 concentrations. Savage and Cooke (2010) showed that tensile fracture may form where tangential hoop
1281 stresses exceed the tensile strength of the rock, especially near rupture tips where slip gradients are elevated.
1282 It was also demonstrated that pre-existing damage contributed to localizing subsequent fracture growth. This
1283 is relevant to the present models because pre-existing cracks generate local stress perturbations that may
1284 promote either the nucleation of new fractures or the linkage of existing defects into larger structures. These
1285 newly formed structures may then further modify the stress field and create favorable pathways for
1286 subsequent deformation.



1287 At the mesoscale, a bridge between distributed discontinuities to localized faults is illustrated in two studies
1288 by Shipton and Cowie (2001; 2003) about deformation bands and slip surfaces in sandstone. In faults
1289 surrounded by damage zones containing deformation bands and unconnected slip surfaces, measurable
1290 throw initiates when the connection between individual slip surfaces develops. Stress concentrations may
1291 develop around slipping surfaces, increasing shear stress on adjacent regions of the fault and ultimately
1292 favoring off-fault damage. In our models, we present stress perturbations around crack arrays, which may
1293 define favorable regions for linkage. In both the natural fault systems described by Shipton and Cowie (2001,
1294 2003) and the crack arrays examined here, localized brittle structures do not form as continuous propagating
1295 structures, but emerge from the progressive connection of initially scattered discontinuities.

1296 At larger scales, segmented faults and step fault systems show similarities with the presented *en echelon*
1297 models, especially in terms of the interaction between fault tips within regions of stress perturbation. Field
1298 studies indicate that faults may initiate from sheared joints, *en echelon* vein arrays and discontinuous slip
1299 surfaces, before these discrete sets of isolated discontinuities are linked into through-going faults (de
1300 Joussineau and Aydin, 2007; Peacock et al., 2017). Numerical models of step faults further show that spacing
1301 between fault segments and their degree of overlap strongly control stress perturbations, strain localization,
1302 and the development of damage zones between interacting faults (Nabavi et al., 2017; Nunes et al., 2025).
1303 These observations are consistent with our results, which demonstrate that crack linkage is controlled not
1304 only by their spacing, but by the combined effect of crack-tip separation and the orientation of individual
1305 cracks as well as their arrays.

1306 The role of initial structure geometry in the evolution of fault zones and relay zones between fault segments
1307 has been discussed in multiple studies. Kristensen et al. (2008) framed the relay zone evolution as a process
1308 involving displacement transfer, breaching and eventual incorporation into fault-bounded lenses. Childs et
1309 al. (2009) proposed that segmentation and relay-zone geometry partly control the fault zone thickness. This
1310 is consistent with the present results, especially with the observation that even small variations in crack
1311 orientation, degree of overlap and array orientation strongly affect whether linkage between multiple cracks



1312 is promoted or inhibited. At larger scales, similar geometrical variations may play a crucial role in the
1313 development of continuous faults from isolated segments through relay zones.

1314 Comparison with geological structures suggests that different crack linkage mechanisms may be relevant to
1315 different fault-zone geometries. Where lobes of effective tensile stress overlap between neighboring
1316 discontinuities, linkage may occur through the formation of extensional bridges, pull-apart structures or
1317 breached relay zones, as observed in echelon vein arrays and segmented fault systems (Peacock and
1318 Sanderson, 1995; Kim et al., 2003; Sanderson and Peacock, 2019). In contrast, in regions where elevated
1319 compression concentrates, elevated shear stress may promote linkage through nucleation of shear fractures,
1320 for example along pressure-solution seams, cleavage surfaces or phyllosilicate-rich shear fabrics (Seyum and
1321 Pollard, 2016; Tesei et al., 2012; Sánchez-Roa et al., 2017).

1322 Overall, the models show that the orientation and spacing of neighboring discontinuities control whether
1323 local stress perturbations promote or inhibit their linkage. At larger scales, progressive linkage of
1324 mechanically favorable discontinuities may contribute to the development of segmented fault zones and to
1325 their progressive evolution into continuous fault structures.

1326

1327 **5.6 The role of geometry of pre-existing structures in the fault initiation**

1328 The obtained numerical results allow us to speculate on how pre-existing discontinuities influence the brittle
1329 faulting process. Rocks constituting the uppermost crust commonly exhibit dominant elastic and brittle
1330 (plastic) behavior as opposed to viscous flow of the lower crust (e.g., Nabavi et al., 2017; Casini et al., 2023).

1331 The stress field due to elastic deformations in rock media with pre-existing microcracks has a significant
1332 impact on the coalescence and growth of macroscopic fractures and, ultimately, faults (Reches and Lockner,
1333 1994; Bobet and Einstein, 1998; Tang et al., 2001; Wong et al., 2001; Aydin and Schultz, 1990; Peacock and
1334 Sanderson, 1996; Crider and Peacock, 2004; Chang et al., 2015; Zhou et al., 2015; Scholz, 2019; Zhang et al.,
1335 2021; McBeck et al., 2023). Using the different synthetic crack network geometries modeled in this work, we
1336 demonstrated that the shape and extent of stress concentration regions are strongly influenced by the



1337 arrangement of the cracks, as well as by their relative size and separation. Different crack array orientations
1338 result in variable patterns of stress and strain concentrations, the combination of which may control crack
1339 linkage and coalescence into larger fractures.

1340 Fig. 15 compares different crack configurations identified in the numerical models with characteristic linking
1341 patterns observed in common geological structures. The rock architecture comprises a range of multi-scale
1342 discontinuities that can be approximated by the cracks in our model. These discontinuities span from the
1343 micro- to macro-scale, including mineral fabrics, grain boundaries and intragranular microfractures, cleavage
1344 and twins, veins and solution seams, bedding, joints and faults.

1345 In *en echelon* arrays where the pre-existing crack set is aligned parallel to $\vec{\sigma}_1^\infty$, significant positive interference
1346 between regions of reduced compression occurs at angles oriented between 30° and 45° with respect to $\vec{\sigma}_1^\infty$,
1347 depending on the degree of crack overlap. Typical examples include extensional bridges between faults
1348 linked by wing cracks (Fig. 15A; Kim et al., 2003). If the pre-existing cracks are oriented perpendicular to $\vec{\sigma}_1^\infty$,
1349 the *en echelon* configurations broaden the region of reduced compression across the array, favoring the
1350 development of through-going fractures or faults within the pre-existing sets of veins or joints, possibly
1351 involving the rotation of these structures (Fig. 15B; e.g., Crider and Peacock, 2004).

1352 However, the largest reductions in compression occur when cracks oriented at $\pm 45^\circ$ relative to $\vec{\sigma}_1^\infty$ are aligned
1353 along arrays at approximately 20-30° relative to σ_1 (Fig. 15C,D). Tensile linkage through these arrays may
1354 significantly enhance the likelihood of failure and fracture propagation. It should be emphasized that these
1355 new fractures opening within regions of reduced compression should be classified as mode I, even if their
1356 orientation (ca. 20-30° relative to $\vec{\sigma}_1^\infty$) is typical of mode II shear fractures. In other words, fractures forming
1357 at 30–35° from the $\vec{\sigma}_1^\infty$ direction, as commonly observed in experimental analyses (e.g., Paterson and Wong,
1358 2005; McBeck et al., 2023), cannot be defined a priori as shear fractures. This suggests that mode I
1359 microcracks with variable orientations may contribute to the development of mode II macroscopic fractures,
1360 which are the most typical structures developing in rock media. The geometry of conjugate (Anderson, 1905)
1361 strike-slip, normal, and reverse fault zones represent excellent examples of this process (Fig. 15D). Because

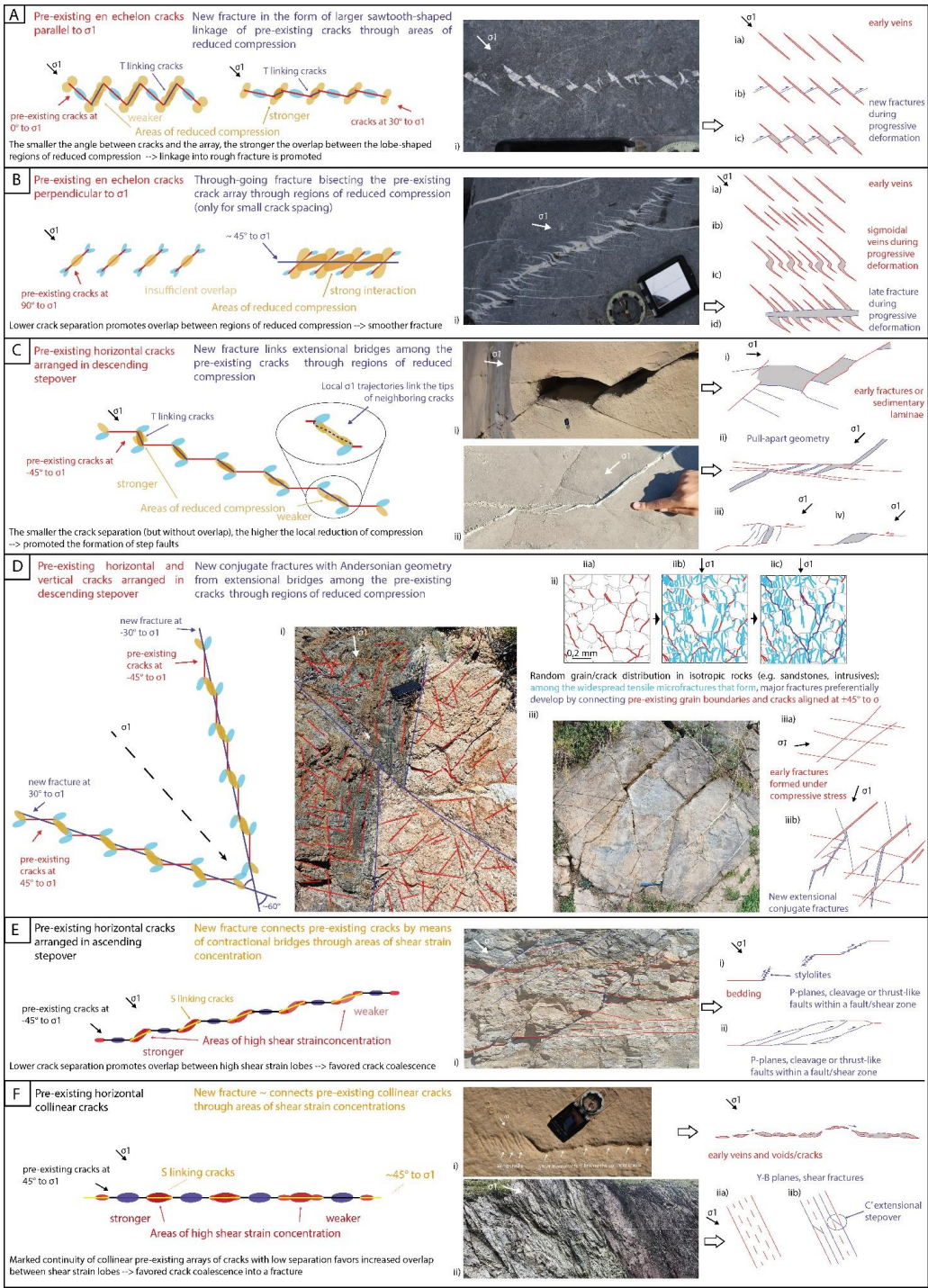


1362 regions of reduced compression appear to be favorable sites for crack opening and linkage, under a random
1363 distribution of pre-existing cracks, these geometrically arranged crack arrays are statistically more likely to
1364 initiate failure, thereby increasing the probability of fracture formation along these preferential directions.
1365 This provides a possible rationale for why, in rocks with a nearly isotropic distribution of discontinuities, the
1366 orientation of brittle structures tend to obey the Mohr-Coulomb criterion.

1367 Although regions of reduced compression may represent favorable sites for crack opening and linkage,
1368 configurations that are unfavorable for the formation of extensional bridges may still promote fracture
1369 development through shear strain localization. Shear strain concentration may become important in
1370 contractional bridges or within dense arrays of planar discontinuities that are typical in rocks with strong
1371 planar anisotropies. Examples of contractional bridges include cleavage, stylolite, P-planes solution seams
1372 and faults with reverse motion bridging low-angle discontinuities (Fig. 15E,F). The overlap of shear strain
1373 lobes at these connections may promote rupture. Shear strain amplification can occur both in ascending
1374 stepover configurations or, more efficiently, along collinear cracks. The strongest amplification occurs in
1375 elongated lobes that branch out parallel to the crack, starting from its tips (Fig. 15E). It follows that the most
1376 favorable paths connecting high shear strain areas are vertical and horizontal collections of collinear cracks,
1377 along which rupture may be facilitated. Examples of these configurations include mode II fractures linking
1378 sets of pre-existing aligned cracks or grain boundaries, or B and Y plane shear zones (Fig. 15E, F). It should be
1379 noted that Y planes preferentially develop in phyllosilicate-rich shear zones (e.g., Tesei et al., 2012; Sanchez-
1380 Roa et al., 2017; Volpe et al., 2022), as these are dominated by minerals with platy morphologies, where the
1381 grain boundaries are commonly aligned along collinear layers.



1382



1383



Fig. 15: Comparison between numerical simulations with field examples of fault zones developed through the coalescence of crack networks. (a) Overlap of reduced-compression lobes around *en echelon* cracks parallel to $\vec{\sigma}_1^\infty$ may promote rupture connecting crack tips, resulting in the possible formation of a sawtooth-shaped fracture. A similar geometry is shown in the photograph and associated evolutionary model of an array of calcite-filled pull-aparts linked by shear fractures in the Liassic limestones of Somerset, UK (Peacock and Sanderson, 1995; note that the fault zone is sinistral, but the image is mirrored vertically for an easier comparison; photograph courtesy of D.C.P. Peacock). (b) Overlap of reduced-compression lobes around *en echelon* cracks perpendicular to $\vec{\sigma}_1^\infty$ may promote coalescence through the middle of the crack array. A similar geometry is shown in the photograph (courtesy of D.C.P. Peacock), accompanied by an evolutionary model of an array of rotated *en echelon* calcite-filled veins in the Liassic limestones of Somerset, UK (Peacock and Sanderson, 1995). (c), (d) Overlap of reduced-compression lobes may locally weaken the rock, inducing potential rupture connecting neighboring crack tips. In (c) the configuration of reduced-compression bridges in a step fault is represented by the formation of pull-apart structures; photographs i) and iii) are from Gozo Island, Malta (Kim et al., 2003), ii) from the Ligurian Alps, Italy (Mueller et al., 2023), iv) from Cantil Valley, California, USA (Kim et al., 2004). In (d) the possible formation of conjugate fractures with the typical shear fracture orientation ($\pm 30^\circ$ to $\vec{\sigma}_1^\infty$) but with mode I origin is shown. Bridges with reduced compression arise from random distribution of the pre-existing cracks, from where the arrays of cracks aligned at $\pm 45^\circ$ to $\vec{\sigma}_1^\infty$ are the most favorable geometrical configurations for the formation of conjugate fault systems following the Anderson (1905) rules. Examples are from a composite fabric of a dike intrusion within a metagranite (photograph from Tenda massif, Corsica, France), ii) a sequential mapping of grain-scale microfractures forming in samples experimentally deformed (modified from Kanaya and Hirth, 2024); tensile fracture (light blue lines) and the pre-existing favorably oriented grain boundaries (red lines) control the formation of the conjugate macroscopic shear fractures. iii) Another field example of sandstones from the Ligurian Alps, Italy (Mueller et al., 2023) showing the development of high-angle conjugate normal faults from the connection of pre-existing sets of conjugate thrust faults through calcite filled veins. Overlap of the shear strain lobes is displayed in (e), with the possible formation of shear fractures ($\pm 60^\circ$ to $\vec{\sigma}_1^\infty$) linking contractional bridges in



1410 limestones of the Ligurian Alps (Manna et al., 2023; Perozzo et al., 2024). (f) Arrays of collinear shear fractures
1411 ($\pm 45^\circ$ to $\vec{\sigma}_1^\infty$) are shown in the photograph of a right-lateral fault from the west of Marsalforn, Gozo Island,
1412 Malta (courtesy of D.C.P. Peacock; Kim et al., 2003) and from a reverse fault in metapelites from the Ligurian
1413 Alps (Maino et al., 2020). In all schemes and photographs the pre-existing cracks or bedding are indicated
1414 with red lines, the linking new fractures with blue lines, except for the schemes illustrating the shear strain
1415 patterns, where pre-existing cracks are indicated with black lines and new fractures with yellow lines.

1416

1417 6. Conclusions

1418 We used two-dimensional FEM-based linear elastic simulations to investigate how different geometries of
1419 pre-existing crack networks perturb the local stress and strain fields in a rock undergoing an increment of
1420 simple shear deformation. The models show that changes in shape, spacing and orientation of crack
1421 arrangements control the spatial distribution of stress and strain perturbations in the regions between
1422 neighboring cracks, determining mechanically favorable or unfavorable conditions for crack interaction and
1423 potential linkage. In fact, the numerical stress analysis reveals patterns of potentially tensile stress
1424 concentration that are closely related to the orientation of pre-existing cracks and may lead to the linkage of
1425 cracks into larger fractures. These patterns emerge in two classes of geometrical configurations: (i) *en echelon*
1426 cracks and (ii) randomly distributed cracks. From our study, we find that:

1427 1. *En echelon* crack arrangements exhibit local trajectories of the major in-plane principal stress that
1428 effectively connect neighboring crack tips in specific configurations: approximately collinear mode I-oriented
1429 cracks, and conjugate mode II-oriented crack arrays in which horizontal cracks are arranged in arrays inclined
1430 at -15° and vertical cracks along arrays inclined at -75° . In the reference simple shear configuration
1431 considered here, where $\vec{\sigma}_1^\infty$ is oriented at -45° , these correspond in both cases to array orientations of about
1432 30° from $\vec{\sigma}_1^\infty$. These configurations may be favorable for tensile failure-driven crack linkage and suggest that
1433 orientations typically associated with shear fractures, approximately $\pm 30^\circ$ relative to $\vec{\sigma}_1^\infty$ as prescribed by the
1434 Mohr–Coulomb criterion, may be explained through the preferential activation of crack arrangements that



1435 most effectively reduce the far-field compression. In contrast, their symmetric counterparts relative to the
1436 crack orientation, such as horizontal cracks arranged in arrays oriented at 15° and vertical cracks arranged in
1437 arrays oriented at 75° , produce elevated compression between neighboring tips and local $\vec{\sigma}_1$ trajectories that
1438 do not connect the tips, thereby inhibiting linkage.

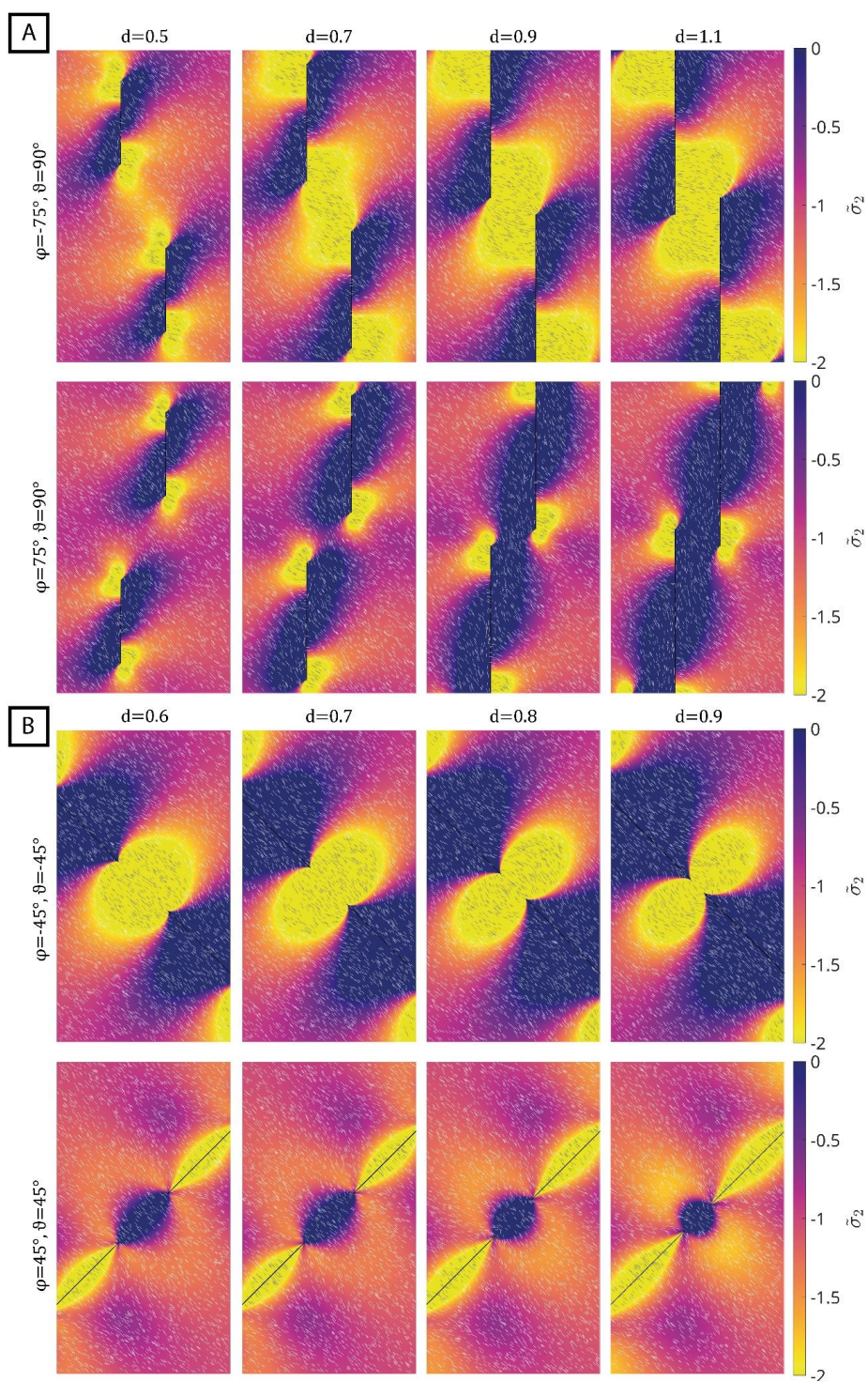
1439 2. In randomly distributed crack systems, potential fracture pathways do not arise uniformly throughout the
1440 crack population. Instead, they emerge from subsets of cracks with orientation, spacing and relative position
1441 that promote the overlap of stress perturbation regions around their tips. This suggests that macroscopic
1442 fracture orientation may develop through the linkage of mechanically favorable crack clusters rather than
1443 from the homogeneous response of the entire crack population.

1444 3. When the normalized and reduced stress perturbation values recorded for each geometrical configuration
1445 are converted to crustal pressure conditions, the depth range over which tensile failure, shear failure and
1446 open-crack conditions are possible depends on effective pressure, tensile strength, cohesion, pore fluid
1447 pressure and crack aspect ratio. Under hydrostatic pore-pressure conditions, increasing depth progressively
1448 restricts the conditions for tensile failure and crack opening, whereas elevated pore fluid pressure expands
1449 the depth range over which crack interaction may promote brittle failure. We argue that, under common
1450 upper-crustal pressure conditions, only the highest calculated stress perturbations may produce local
1451 effective tension. Therefore, the configurations in which compression is most effectively reduced may be the
1452 first to reactivate during deformation, leading to crack linkage and, ultimately, to the formation of shear
1453 fractures.

1454 Overall, the results show that the orientation, spacing and spatial distribution of pre-existing cracks in a rock
1455 undergoing elastic deformation determine whether local stress perturbations promote or inhibit crack
1456 linkage. The geometrical arrangement of pre-existing cracks therefore is the dominant factor controlling how
1457 fracture networks develop, orient and evolve mechanically in the upper crust.

1458

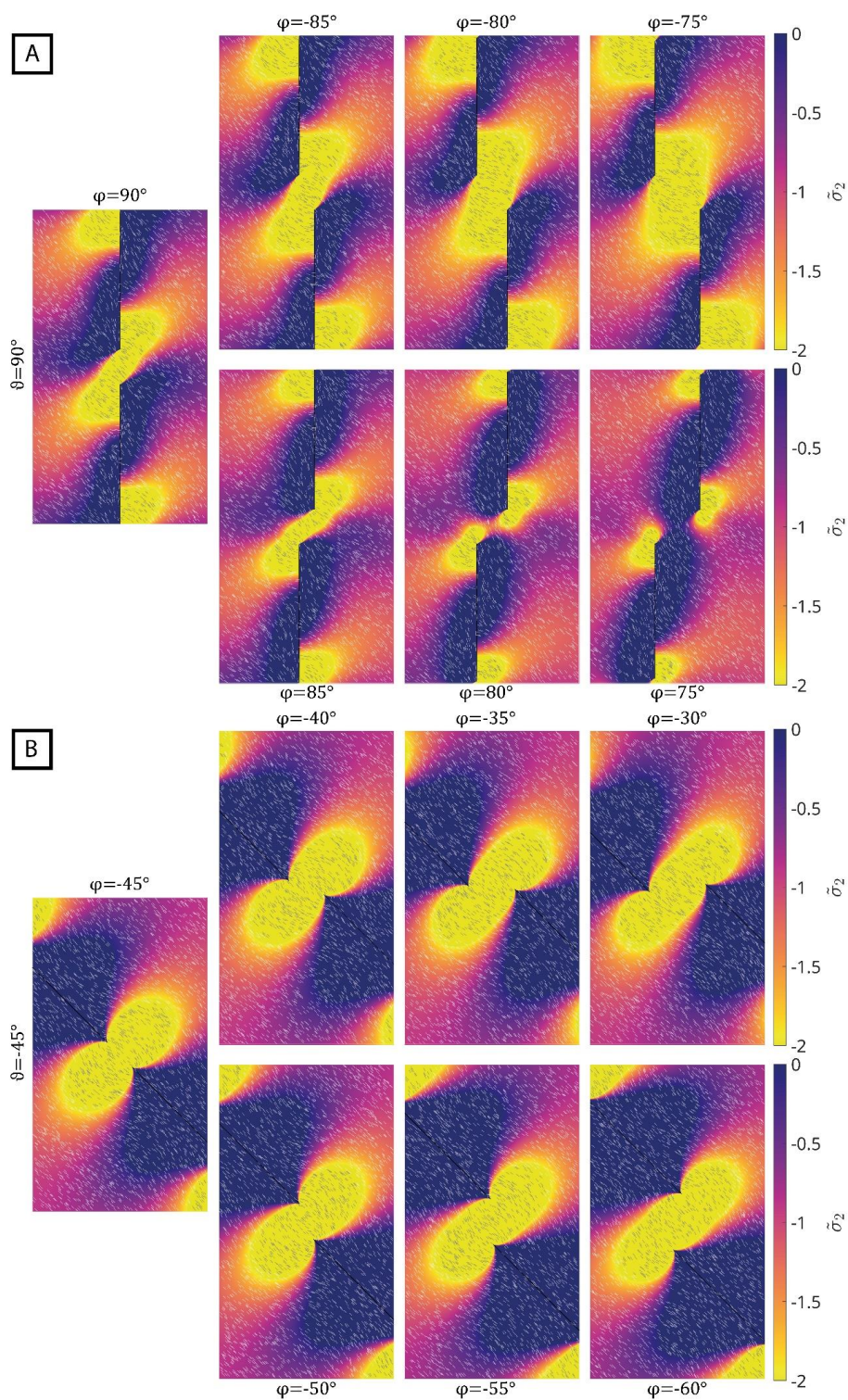
1459 **Appendix A**





1462 **Fig. A1:** Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$ for different geometric configurations of *en*
1463 *echelon* crack arrays. Only the central unit cell is shown. White and black lines indicate the local trajectories
1464 of the major in-plane principal stress $\tilde{\sigma}_1$. (a) Crack orientation: $\vartheta=90^\circ$ (mode II cracks relative to far-field
1465 simple shear). In each row, the array orientation φ is fixed: -75° (top) and 75° (bottom). Along each row, d
1466 varies from 0.5 to 1.1. B) Crack orientation: $\vartheta=-45^\circ$ (top row, mode I cracks relative to far-field simple shear),
1467 and $\vartheta=45^\circ$ (bottom row). The array orientation φ is -45° (top) and 45° (bottom). Along each row, d varies
1468 from 0.6 to 0.9.

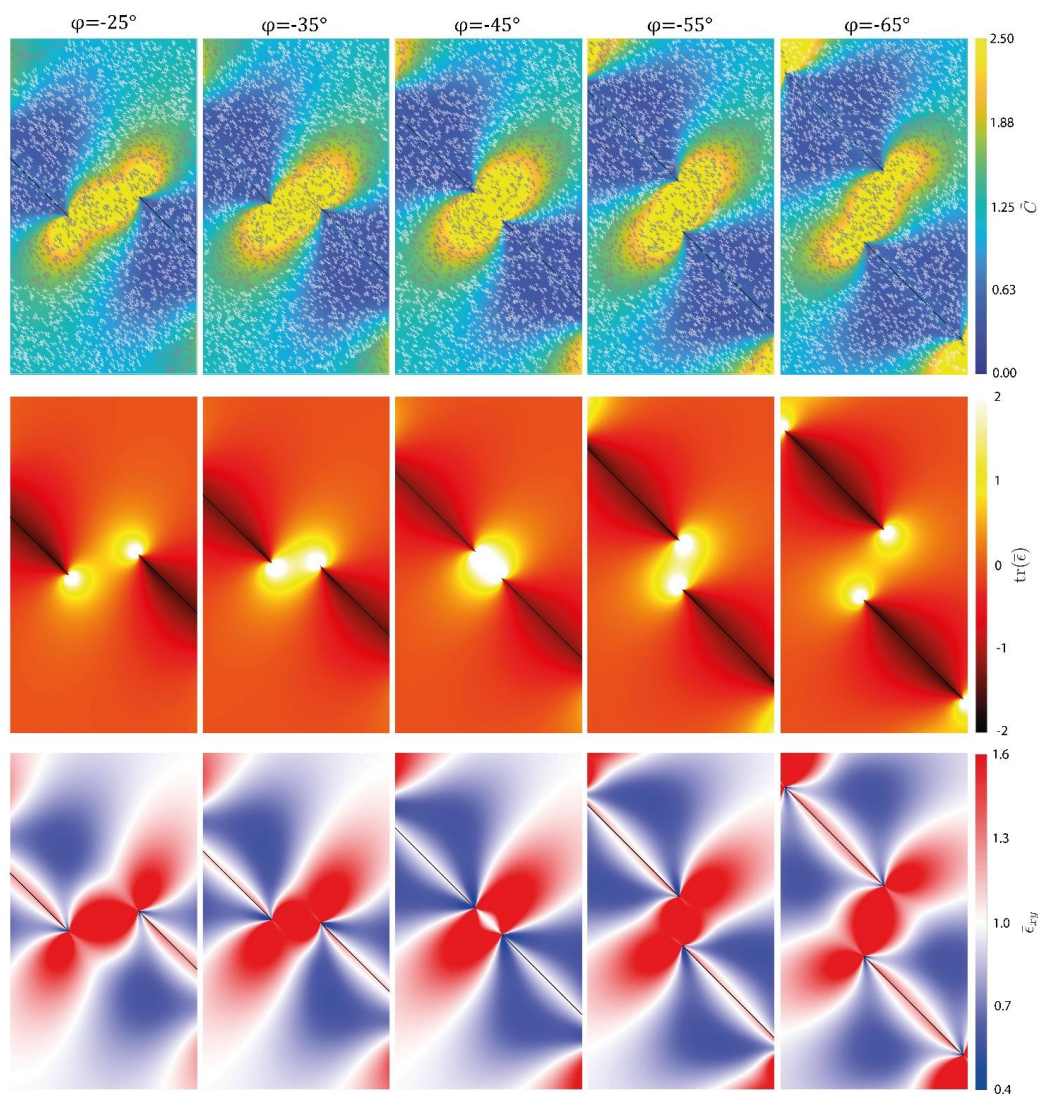
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1471 **Fig. A2:** Normalized and reduced minor principal stress magnitude $\tilde{\sigma}_2$ for different geometric configurations
1472 of *en echelon* crack arrays. Only the central unit cell is shown. White and black lines indicate the local
1473 trajectories of the major in-plane principal stress $\tilde{\sigma}_1$. (a) The crack orientation is fixed at $\vartheta=90^\circ$. The projected
1474 overlap is fixed at $d=0.8$. The crack array orientation φ ranges from -90° to -75° (top row) and from 90° to
1475 75° (bottom row). B) The crack orientation is fixed at $\vartheta=-45^\circ$. The projected overlap is fixed at $d=0.8$. The
1476 crack array orientation φ ranges from -30° to -60° .

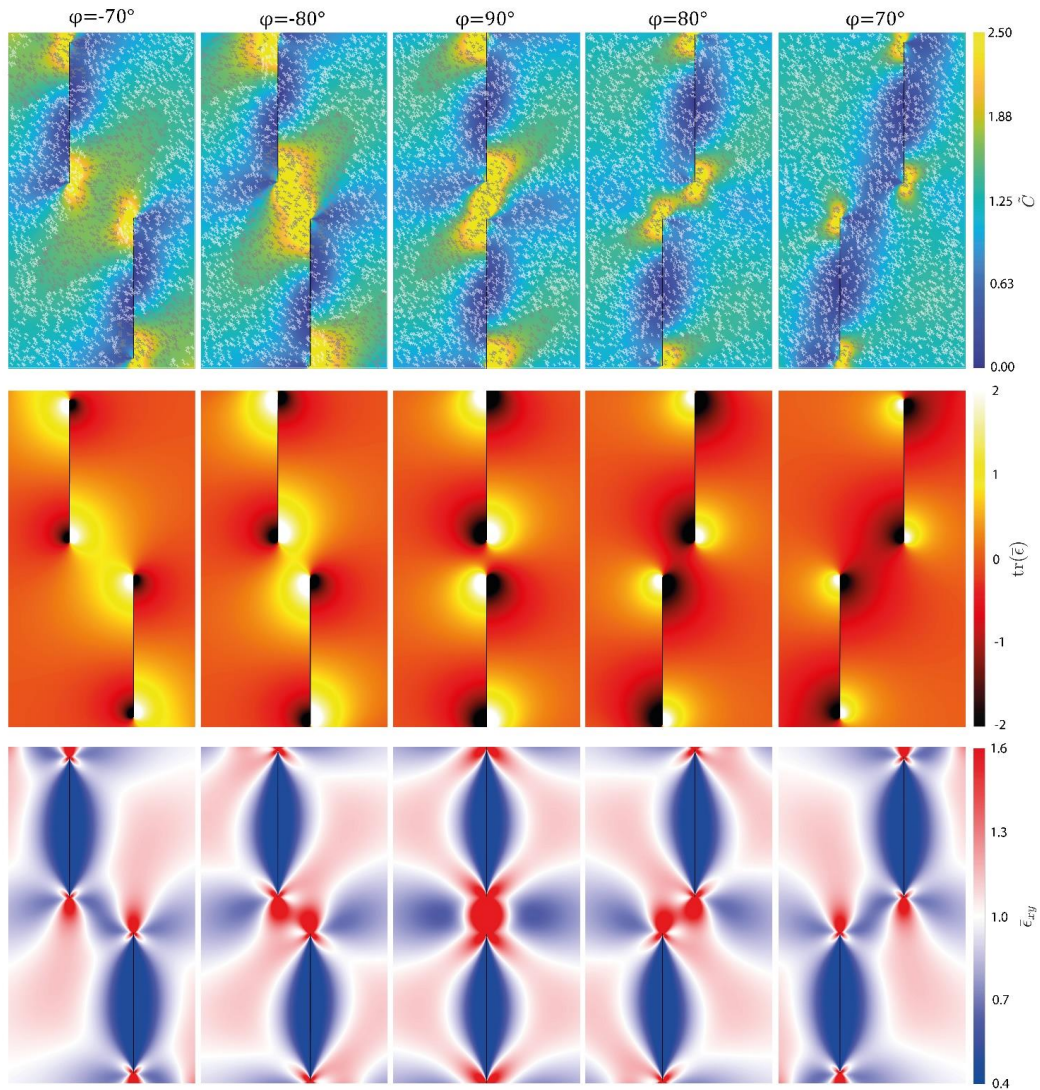
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1479 **Fig. A3:** Normalized effective cohesion $\bar{C}$, normalized first strain invariant $\bar{I}_1$ and shear strain component $\bar{\epsilon}_{xy}$
 1480 for different geometric configurations of *en echelon* crack arrays. The crack orientation is set at $\vartheta = -45^\circ$, and
 1481 the projected overlap is fixed at $d = 0.8$. The array orientation φ is varied between -25° and -65° . White and
 1482 black lines in the first row indicate the potential orientations of conjugate shear fractures.

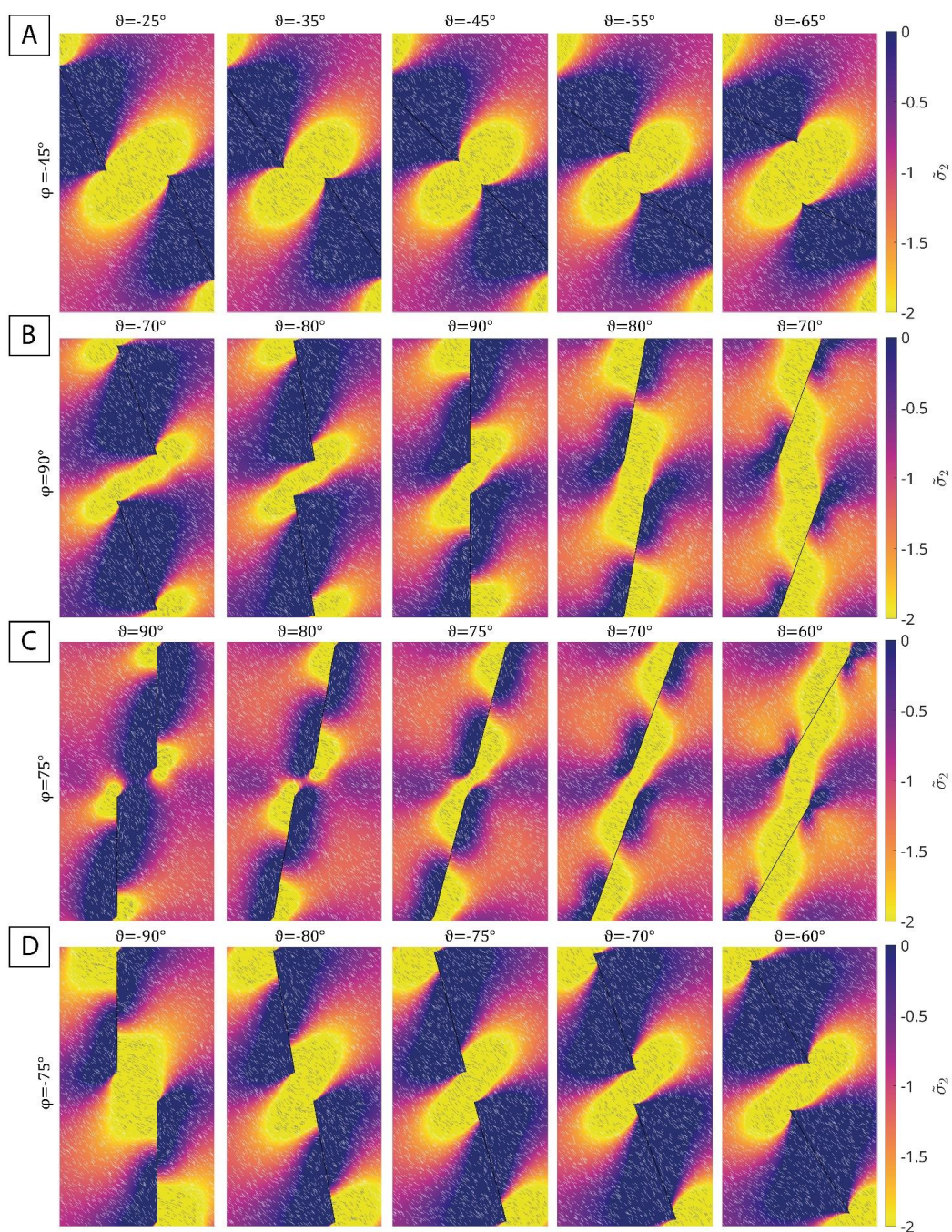
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1484

1485 **Fig. A4:** Normalized effective cohesion $\bar{C}$, normalized first strain invariant $\bar{I}_1$ and shear strain component $\bar{\epsilon}_{xy}$
 1486 for different geometric configurations of *en echelon* crack arrays. The crack orientation is set at $\vartheta=90^\circ$, and
 1487 the projected overlap is fixed at $d=0.8$. The array orientation φ is varied between -70° and -90° and,
 1488 symmetrically, between 90° and 70° . White and black lines in the first row indicate the potential orientations
 1489 of conjugate shear fractures.

1490



1491

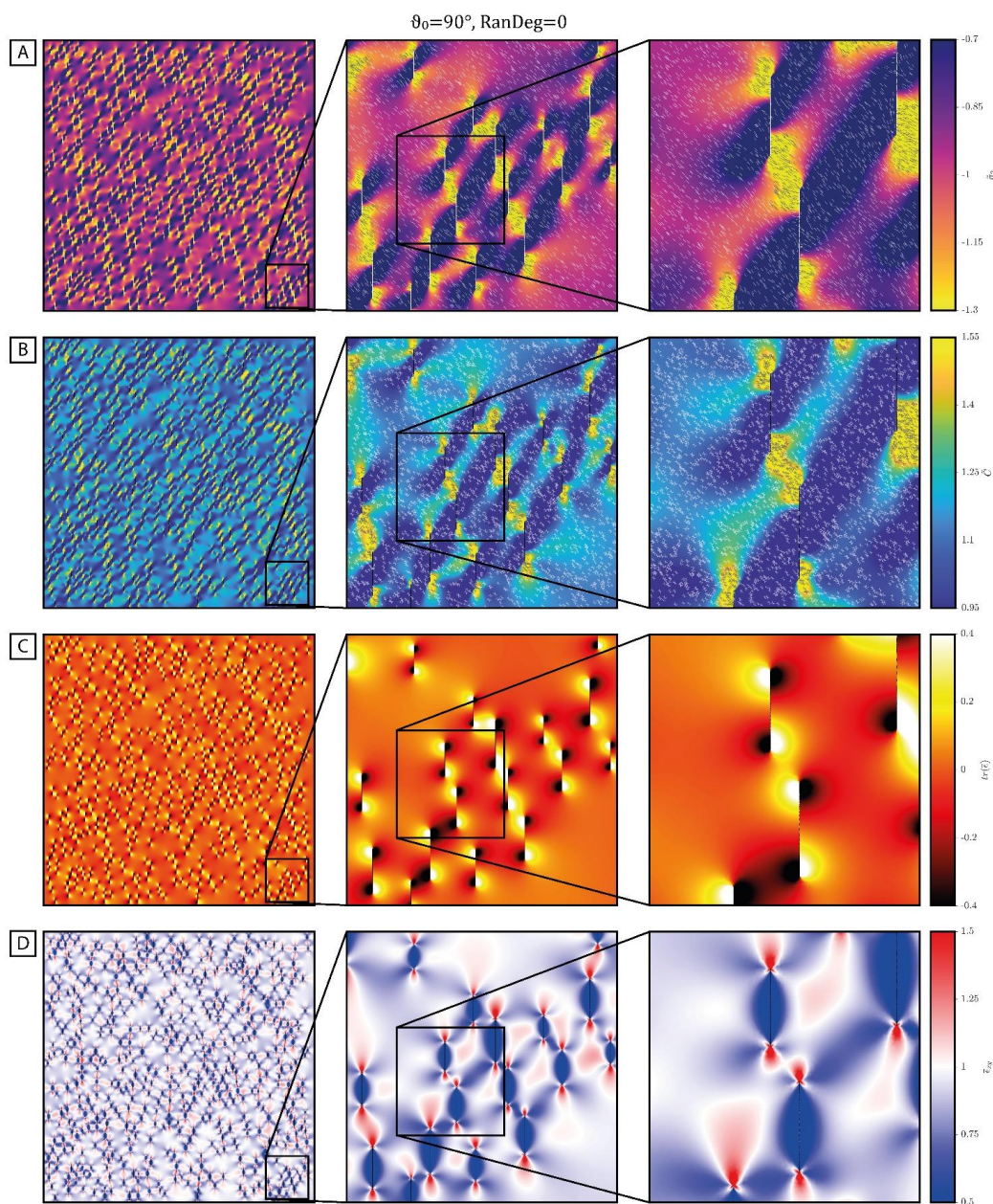
1492 **Fig. A5:** Magnitude of the minor in-plane principal stress $\bar{\sigma}_2$ for different geometric configurations of *en*

1493 *echelon* crack arrays. The projected overlap is fixed at $d=0.8$. White and black lines represent the local



1494 trajectories of the major in-plane principal stress $\vec{\sigma}_1$. (a) The crack array orientation is fixed at $\varphi=-45^\circ$. The
1495 crack orientation ϑ ranges from -25° to -65° . B) The crack array orientation is fixed at $\varphi=90^\circ$. The crack
1496 orientation ϑ ranges from -70° to -90° and, symmetrically, from 70° to 90° . C) The crack array orientation is
1497 fixed at $\varphi=75^\circ$. The crack orientation ϑ ranges from 90° to 60° . D) The crack array orientation is fixed at $\varphi=-$
1498 75° . The crack orientation ϑ ranges from -90° to -60° .

1499



1500

1501 **Fig. A6:** Stress and strain fields in a system with 500 vertically aligned cracks ($\vartheta_0 = 90^\circ$ and $RanDeg = 0$)

1502 with random locations. In the first inset, a subdomain containing multiple *en echelon* arrays of cracks is

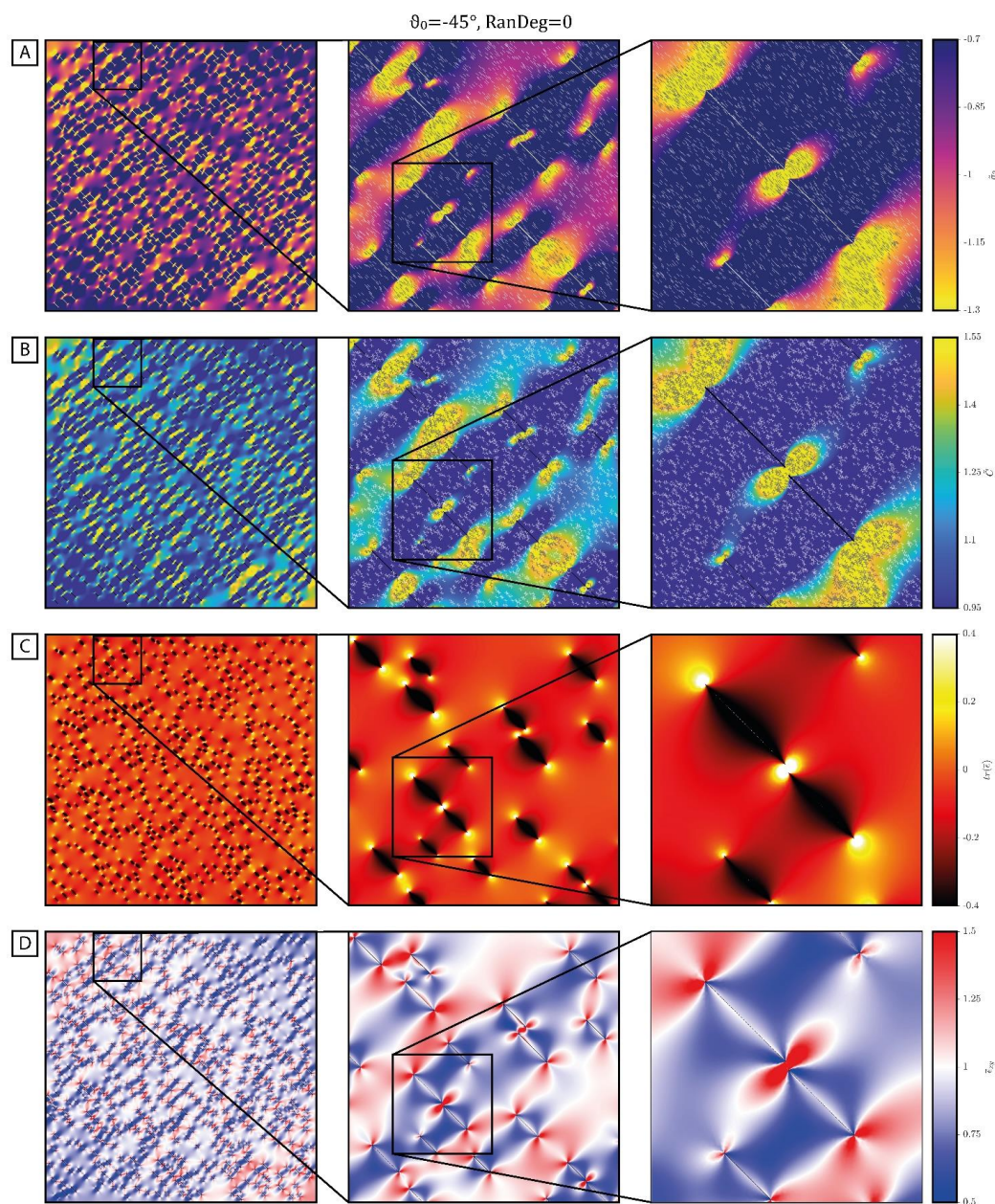
1503 illustrated. The second inset shows the interactions between the tips of two cracks in an *en echelon* array.

1504 (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent the local trajectories



1505 of the major in-plane principal stress $\bar{\sigma}_1$. B) Normalized effective cohesion $\bar{C}$. White and black lines indicate
1506 the potential orientations of conjugate shear fractures. C) Normalized first strain invariant $\bar{I}_1$. D) Normalized
1507 shear strain $\bar{\epsilon}_{xy}$.

1508



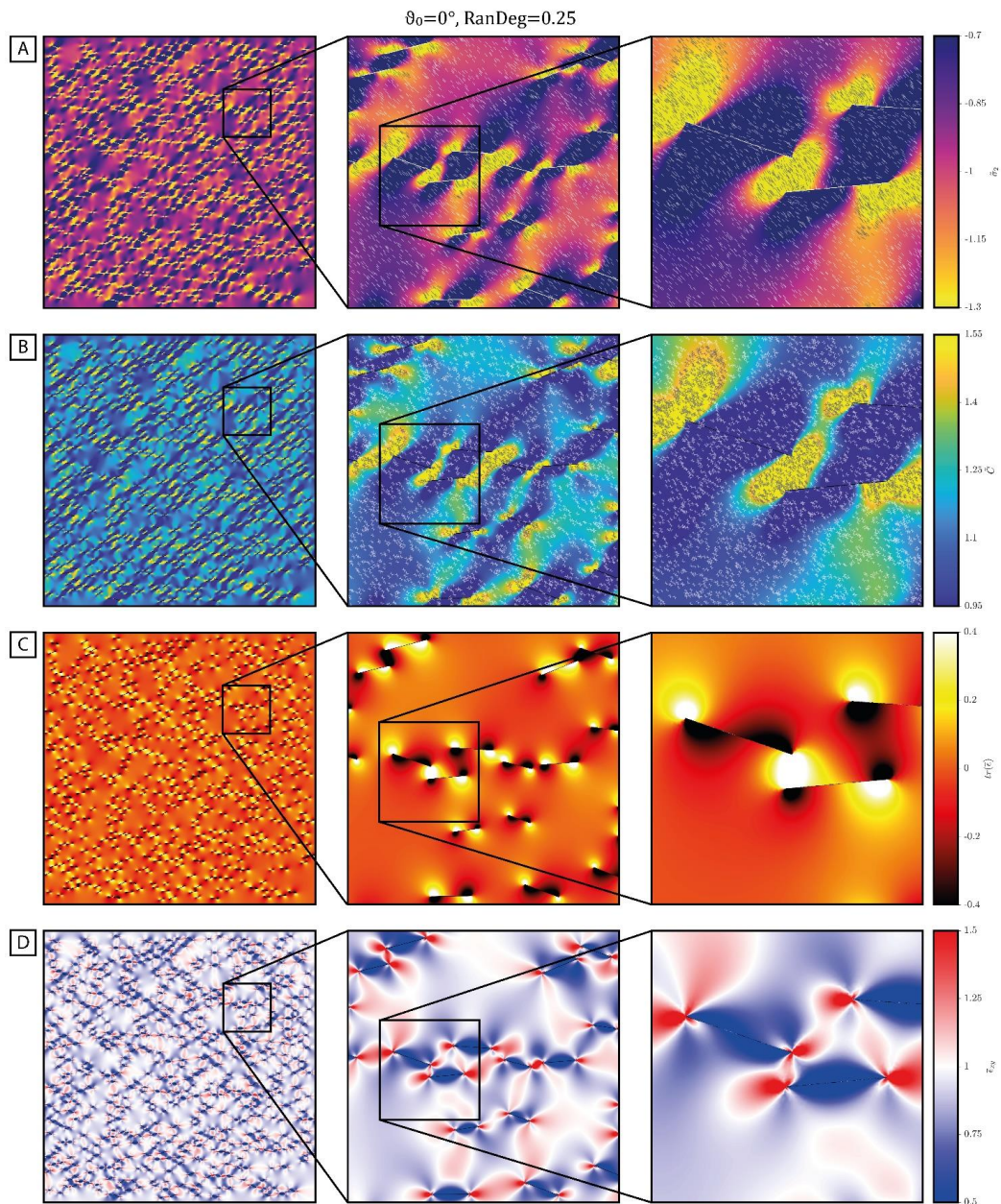
1509

1510 **Fig. A7:** Stress and strain fields in a system with 500 obliquely aligned cracks ($\theta_0 = -45^\circ$ and $RanDeg = 0$)
 1511 with random locations. In the first inset, a subdomain containing multiple *en echelon* arrays of cracks is
 1512 illustrated. The second inset shows the interactions between the tips of two interacting cracks in an *en*
 1513 *echelon* array. (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent the



1514 local trajectories of the major in-plane principal stress $\vec{\sigma}_1$. B) Normalized effective cohesion $\tilde{C}$. White and
1515 black lines indicate the potential orientations of conjugate shear fractures. C) Normalized first strain invariant
1516 $\bar{I}_1$. D) Normalized shear strain $\bar{\epsilon}_{xy}$.

1517



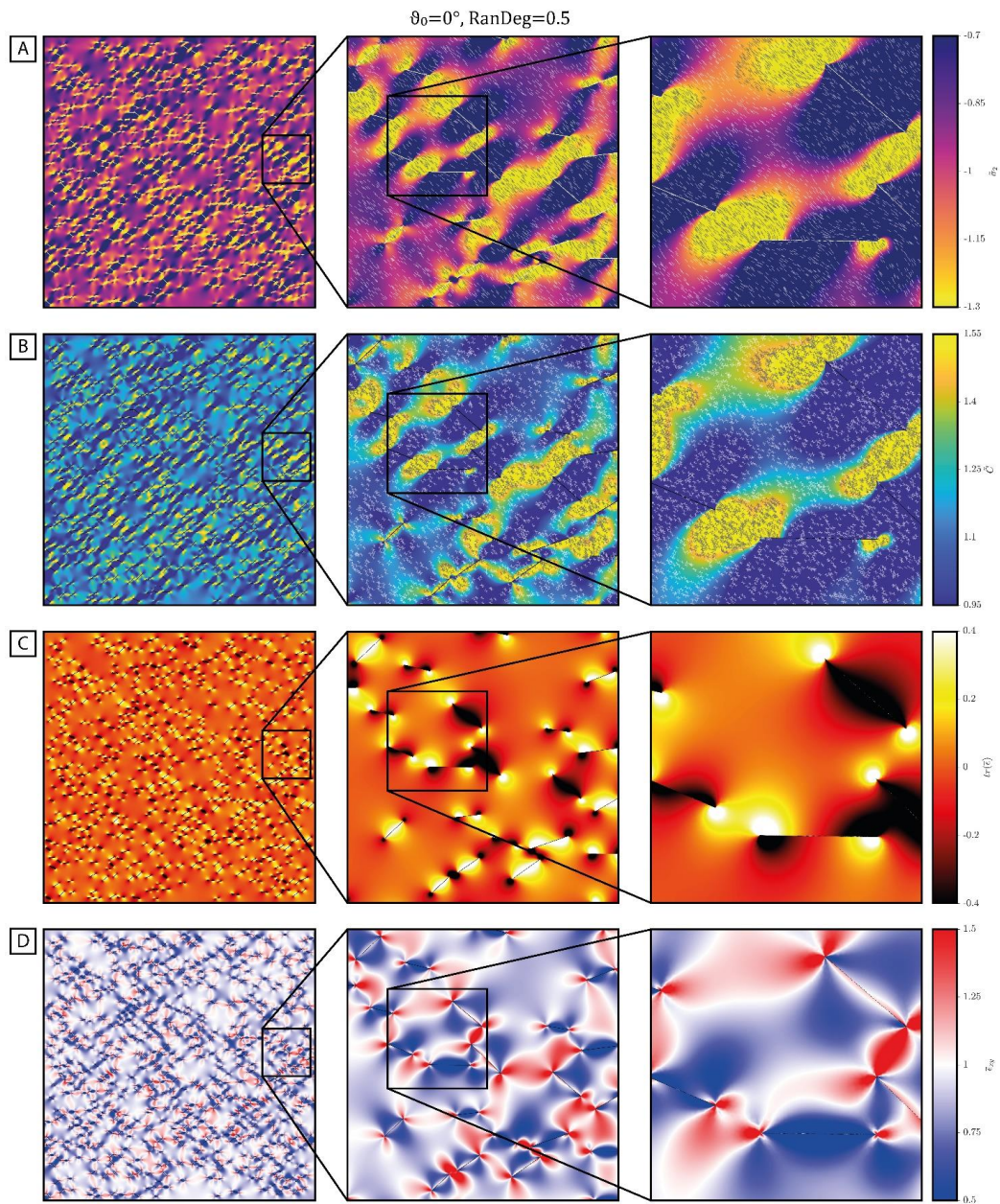
1518

1519 **Fig. A8:** Stress and strain fields in a system containing 500 cracks with base orientation $\vartheta_0 = 0^\circ$ and
 1520 $RanDeg = 0.25$ with random locations. In each row, the first inset illustrates a subdomain containing
 1521 mechanically interacting cracks with different orientations. The second inset shows the interaction between
 1522 the tips of two cracks. (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent



1523 the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$. B) Normalized effective cohesion $\tilde{C}$. White and
1524 black lines indicate the potential orientations of conjugate shear fractures. C) Normalized first strain invariant
1525 $\bar{I}_1$. D) Normalized shear strain $\bar{\epsilon}_{xy}$.

1526



1527

1528 **Fig. A9:** Stress and strain fields in a system containing 500 cracks with base orientation $\vartheta_0 = 0^\circ$ and
 1529 $\text{RandDeg} = 0.5$ with random locations. In each row, the first inset illustrates a subdomain containing
 1530 mechanically interacting cracks with different orientations. The second inset shows the interaction between
 1531 the tips of two cracks. (a) Magnitude of the minor in-plane principal stress $\tilde{\sigma}_2$. White and black lines represent



1532 the local trajectories of the major in-plane principal stress $\vec{\sigma}_1$. B) Normalized effective cohesion $\tilde{C}$. White and
1533 black lines indicate the potential orientations of conjugate shear fractures. C) Normalized first strain invariant
1534 $\bar{I}_1$. D) Normalized shear strain $\bar{\epsilon}_{xy}$.

1535

1536 **Data availability**

1537 The numerical results presented in this study are generated from the finite element model code and input
1538 parameters described in the manuscript. The full set of raw output files is not deposited in a public
1539 repository because the study involves a large parametric exploration of hundreds of geometric
1540 configurations, each producing separate numerical output files, and the complete dataset would be large
1541 and largely redundant with the reproducible model outputs. The data underlying the figures can be
1542 regenerated using the publicly available code provided in the Code availability section. Additional
1543 processed output files are available from the corresponding author upon reasonable request.

1544

1545 **Code availability**

1546 To improve the reproducibility of this experiment, the codes used for FEM analysis are available at a
1547 Zenodo (Manna, 2025; retrievable at <https://doi.org/10.5281/zenodo.15681017>) and GitHub repository
1548 (<https://github.com/LudoManna/CrackSystems.git>).

1549

1550 **Author contribution**

1551 LM conceived the work, developed numerical models, analyzed and interpreted the data. MM conceived
1552 the work and interpreted the data. LC developed numerical models. MD conceived the work, developed
1553 numerical models, and interpreted the data.

1554



1555 **Competing interests**

1556 The authors declare that they have no conflict of interest.

1557

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1562 manuscript. All scientific content, interpretations, and wording were made by the authors.

1563

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1567

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