



1 **Ice–ice collisional breakup enhances secondary ice production but**
2 **reduces surface hailfall in a simulated pulse hailstorm**

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Abstract

Secondary ice production (SIP) can substantially modify the ice-phase structure of mixed-phase clouds, but its role in short-lived pulse hailstorms remains unclear. Here, an ice – ice collisional breakup (BR) parameterization is implemented in the NSSL two-moment scheme within Cloud Model 1 (CM1), and seven sensitivity experiments are conducted for an idealized pulse hailstorm to examine the effects of droplet shattering during freezing (DS) and BR on ice-phase evolution and surface hailfall. The results show that BR has a much stronger effect than DS on the cloud-ice structure and surface hail mass. Relative to CNTL, the experiments including BR show a marked reduction in the peak total hail mass at the surface, with the largest decrease reaching 41.94 %. BR increases the ice crystal number concentration by about two orders of magnitude between approximately 5 and 9 km, accompanied by reduced supercooled liquid water above 4 km, lower graupel mixing ratio, and weakened graupel riming growth. These changes reduce the size of potential hail embryos, weaken graupel-to-hail conversion at some heights, and limit subsequent hail growth. The decomposition of BR collision pairs shows that, during the mature hail-producing stage, collisions of ice crystals with graupel and hail become the main sources of BR fragments. Overall, BR can substantially reduce surface hail mass in this idealized pulse-hailstorm case by restructuring the ice phase and enhancing competition for supercooled liquid water.

Keywords: Hail; Numerical simulation; Pulse storm; Secondary ice production; Collisional breakup.

1. Introduction

In situ observations in many mixed-phase and deep convective clouds have shown that ice crystal number concentrations (ICNCs) often exceed ice-nucleating particle (INP) concentrations by several orders of magnitude, a discrepancy that cannot be explained by primary ice nucleation alone (Hobbs and Rangno, 1985; Cantrell and Heymsfield, 2005; Field et al., 2017; Korolev and Leisner, 2020). This discrepancy indicates the presence of secondary ice production (SIP). Various SIP mechanisms have been proposed, but their specific roles in clouds remain uncertain owing to observational limitations, making numerical models an important tool for investigating SIP processes (Korolev et al., 2017; Sullivan et al., 2017; Huang et al., 2017). Among these



mechanisms, the Hallett–Mossop (H–M) process has been the most widely implemented in numerical models. However, its active temperature range is limited to approximately -8 to -3 °C, and its contribution is therefore limited in the colder mixed-phase regions of deep convective clouds (Hallett and Mossop, 1974; Saunders and Hosseini, 2001). Droplet shattering during the freezing of supercooled raindrops (DS) and ice–ice collisional breakup (BR) can operate over broader temperature ranges and may therefore contribute in colder mixed-phase regions where the H–M process is inactive (Vardiman, 1978; Takahashi et al., 1995; Yano and Phillips, 2011; Phillips et al., 2017a, b; Phillips et al., 2018; Sullivan et al., 2018a; James et al., 2021). However, the relative importance of these SIP mechanisms also depends on the specific cloud microphysical conditions. In recent years, several modeling studies have incorporated SIP mechanisms into microphysics schemes. These studies indicate that in-cloud ICNCs, phase partitioning, and precipitation characteristics can change substantially due to SIP, although the dominant SIP mechanism in different cloud types remains debated (Huang et al., 2022; Qu et al., 2022, 2025; Han et al., 2024).

Previous modeling studies of SIP have considered a range of cloud types, including polar stratiform clouds, orographic mixed-phase clouds, and tropical deep convection (Sotiropoulou et al., 2020, 2021; Georgakaki et al., 2022; Huang et al., 2022), but relatively few have focused on hailstorms. Hail is a form of solid precipitation produced in severe convective storms and poses serious risks to agricultural production, property, and public safety (Prein and Holland, 2018; Allen et al., 2020). In China, hailstorms have caused substantial economic losses, with reported losses reaching hundreds of millions to several billion Chinese yuan in some periods or severe years (Tian et al., 2022). Recent studies have also shown long-term changes in hailstorm activity in China and suggested further changes under future climate warming (Zhang et al., 2025). Hail occurrence is particularly frequent in mountainous and plateau regions (Zhang et al., 2008; Li et al., 2018; Ni et al., 2020). Hail growth primarily occurs within updraft regions rich in supercooled liquid water. Additional ice crystals generated by SIP may intensify competition for this liquid water and accelerate its depletion, thereby influencing hail growth. Cloud water competition has also been identified as an important microphysical process affecting precipitation development in aerosol–cloud interactions (Zhao et al., 2024). However, how this pathway varies among different types of hailstorms remains unclear. Supercell, multicell, and pulse storms differ



83 markedly in their dynamical structures and hail growth conditions. Pulse storms are
84 characterized by short lifetimes, weak vertical wind shear, and relatively simple
85 dynamical backgrounds (Miller and Mote, 2017; Dong et al., 2024), making them
86 suitable for mechanistic studies of how SIP affects hail growth. At the same time, hail
87 growth in pulse storms is time-limited. Whether SIP-induced changes in the ice phase
88 can be effectively transferred to hail growth and subsequently affect hailfall at the
89 surface during this short period is a key question.

90 Based on a representative pulse hailstorm that occurred in Weining, Guizhou Province,
91 China, on 27 July 2022, this study examines the effects of multiple SIP mechanisms,
92 namely H–M, BR (based on Phillips et al. (2017a), hereafter PH17), and DS (based on
93 Lawson et al. (2015) and Sullivan et al. (2018b)), on hail. In addition, the BR fragment
94 source is quantitatively decomposed by collision pair to examine how the contribution
95 of each collision pair changes during storm evolution. By combining this
96 decomposition with microphysical conversion-rate diagnostics, this study assesses how
97 SIP-driven restructuring of the ice phase is translated into changes in hail growth and
98 hailfall at the surface within the short life cycle of a pulse storm. The results provide a
99 reference for understanding the microphysical mechanisms by which SIP affects hail
100 growth in rapidly evolving convection.

101 The paper is organized as follows. Sect. 2 describes the case background, model
102 configuration, SIP parameterizations, and experimental design. Sect. 3 presents the
103 storm evolution, microphysical responses, and contributions of BR collision pairs in
104 each experiment. Sect. 4 summarizes the main conclusions and discusses their
105 implications for hail growth mechanisms and SIP parameterization studies.

106 **2. Data and Methods**

107 **2.1 Case overview and observational basis**

108 This study is based on a pulse hailstorm that occurred in Weining, Guizhou Province,
109 China, on 27 July 2022. The storm developed in an environment characterized by high
110 CAPE and weak vertical wind shear and exhibited a short lifetime, rapid development,
111 and rapid onset of hailfall, consistent with the basic features of a representative pulse
112 storm. It therefore provides a suitable case for examining SIP mechanisms in rapidly



113 evolving convection.

114 The observation data used in this study are primarily from the National Hail
115 Suppression Field Experiment conducted by the China Meteorological Administration
116 in Guizhou Province, China, since 2021. Radar echo data were obtained from two X-
117 band, fully solid-state, dual-polarization phased-array radars (ETWS-X02), located in
118 Xueshan Town (104.09° E, 27.05° N) and Xinming Village (103.94° E, 26.98° N),
119 respectively. Each radar operates at a wavelength of 3.2 cm, has 128 array antenna
120 elements, supports horizontal and vertical polarization measurements, and has a
121 maximum detection range of 60 km, a horizontal resolution of 30 m, and a minimum
122 volume scan time of 30 s.

123 Hydrometeor classification was performed using a fuzzy logic identification framework
124 based on polarimetric observables, including horizontal reflectivity factor (Z_H),
125 differential reflectivity (Z_{DR}), specific differential phase (K_{DP}), and the copolar
126 correlation coefficient (ρ_{hv}), which were used to assign weighted hydrometeor
127 categories according to their radar signatures. Comparable fuzzy logic and X-band
128 polarimetric hydrometeor classification methods have been described in previous
129 studies (Park et al., 2009; Dolan and Rutledge, 2009; Al-Sakka et al., 2013; Ribaud et
130 al., 2019).

131 **2.2 Model configuration**

132 Idealized numerical simulations were conducted using the three-dimensional
133 nonhydrostatic cloud model CM1 (Cloud Model 1, version 20.3; Bryan and Fritsch,
134 2002), initialized with an intensive radiosonde sounding collected at 0600 UTC on 27
135 July 2022. The initial wind field was prescribed as zero to suppress the dynamical
136 influence of environmental wind shear, so that SIP-related microphysical mechanisms
137 in this type of pulse storm and their effects on hail formation and evolution could be
138 examined more directly.

139 The total integration time was 180 min, with a time step of 3 s and an output interval of
140 60 s. The model grid contained $201 \times 201 \times 96$ points, corresponding to a horizontal
141 domain of $35.1 \text{ km} \times 35.1 \text{ km}$ and a vertical extent of 18 km. The horizontal grid
142 spacing was 100 m within 10.1 km of the domain center and was then uniformly



143 stretched to 400 m toward the lateral boundaries. The vertical grid spacing was 100 m
144 below 6 km, uniformly stretched from 100 to 400 m between 6 and 10 km, and fixed at
145 400 m above 10 km. The simulations were performed in a large-eddy simulation (LES)
146 configuration, and random potential temperature perturbations were introduced at the
147 initial time.

148 Following Morrison et al. (2022), moist convection was initiated using perturbations in
149 surface heat and moisture fluxes. The perturbations in surface sensible heat flux and
150 moisture flux are denoted by H_s and H_l , respectively, and are given by

$$\begin{aligned} 151 \quad H_s &= \begin{cases} U_s, t < 3600 \\ U_s + M_s e^{-r^2/L_H^2}, t \geq 3600 \end{cases} \\ 152 \quad H_l &= \begin{cases} U_l, t < 3600 \\ U_l + M_l e^{-r^2/L_H^2}, t \geq 3600 \end{cases}, \end{aligned} \quad (1)$$

153 where r is the horizontal distance from the domain center and L_H is the horizontal length
154 scale of the enhanced fluxes. During the first 60 min of the simulation, spatially uniform
155 background surface heat and moisture fluxes were applied over the domain, with
156 magnitudes of $U_s = 0.03 \text{ K m s}^{-1}$ and $U_l = 1.2 \times 10^{-5} \text{ kg kg}^{-1} \text{ m s}^{-1}$, corresponding to
157 sensible and latent heat fluxes of approximately 35 and 35 W m^{-2} , respectively. After
158 60 min, Gaussian-shaped enhanced fluxes were superimposed at the domain center. In
159 Eq. (1), $M_s = 0.3 \text{ K m s}^{-1}$ and $M_l = 1.2 \times 10^{-4} \text{ kg kg}^{-1} \text{ m s}^{-1}$, corresponding to sensible
160 and latent heat fluxes of approximately 350 and 350 W m^{-2} , respectively. Based on
161 independent sensitivity tests, L_H was set to 2000 m to trigger and maintain the
162 development of a single-cell pulse storm.

163 Cloud microphysical processes were represented using the NSSL two-moment bulk
164 scheme (Mansell et al., 2010). The scheme predicts the mass mixing ratios and number
165 concentrations of six hydrometeor categories: cloud water, rain, cloud ice, snow,
166 graupel, and hail. It also allows the bulk densities of graupel and hail to evolve during
167 the simulation, making it well suited for hailstorm simulations. In all experiments, the
168 original Hallett–Mossop (H–M) process in the NSSL scheme was retained. On this
169 basis, two DS configurations were tested, and a BR parameterization was introduced to
170 examine the effects of different SIP mechanisms on storm development and hail
171 characteristics.



172 2.3 SIP parameterizations

173 2.3.1 Droplet shattering configurations

174 DS represents the fragmentation of supercooled raindrops during freezing and the
175 release of secondary ice crystals. To enable a consistent comparison among different
176 DS schemes, the additional source term for secondary ice crystals produced by DS is
177 written as

$$178 \quad \frac{\partial N_{ice}}{\partial t} |_{DS} = N_{DS} \cdot \frac{\partial N_{freeze}}{\partial t}, \quad (2)$$

179 where $\frac{\partial N_{freeze}}{\partial t}$ is the number concentration tendency of freezing raindrops, and N_{DS} is
180 the mean number of ice fragments produced by a single freezing raindrop. In addition
181 to the CNTL experiment, two DS configurations are compared in this study. DS_LAW
182 uses the empirical expression of Lawson et al. (2015), for which the additional source
183 term for secondary ice crystals is

$$184 \quad \frac{\partial N_{ice}}{\partial t} |_{LAW} = N_{LAW} \cdot d^4 \cdot \frac{\partial N_{freeze}}{\partial t}, \quad (3)$$

185 where $N_{LAW} = 2.5 \times 10^{-11}$, and d is the equivalent-volume diameter of the raindrop in
186 μm .

187 DS_SUL follows the parameterization of Sullivan et al. (2018b), in which the additional
188 source term of secondary ice crystals is expressed as

$$189 \quad \frac{\partial N_{ice}}{\partial t} |_{SUL} = (p_{DS} \cdot N_{DS}) \frac{\partial N_{freeze}}{\partial t}, \quad (4)$$

190 where p_{DS} is the probability that a freezing raindrop shatters, given by

$$191 \quad p_{DS} = \frac{p_{max}}{\max\{\mathcal{N}(T_{\mu}, \sigma)\}} \mathcal{N}(T_{\mu}, \sigma), \quad (5)$$

$$192 \quad \mathcal{N}(T_{\mu}, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{(T-T_{\mu})^2}{2\sigma^2}\right]. \quad (6)$$

193 This parameterization represents the shattering probability as a normal distribution
194 function of temperature, where T_{μ} is the temperature at which the probability reaches



its maximum, set here to $T_\mu = 258$ K; σ is the distribution width; and p_{max} is the maximum shattering probability. Following the formulation of Sullivan et al. (2018b), σ , p_{max} , and N_{DS} were set to 3 K, 20 %, and 10, respectively, to obtain a relatively pronounced DS response. The two DS configurations are included in parallel to test the sensitivity to the DS formulation and to examine the different influences of raindrop size and thermodynamic control in a pulse hailstorm.

2.3.2 Implementation of the BR parameterization

Within the original microphysical framework of the NSSL scheme, a PH17-type ice–ice collisional breakup (BR) parameterization was coupled online. The four ice-phase hydrometeor categories in NSSL, namely hail, graupel, snow, and cloud ice, were mapped to the hail, graupel, snow, and crystal types in PH17, respectively. This category mapping was kept fixed during the BR calculation, whereas particle mass, density, terminal velocity, and number concentration were diagnosed from the prognostic NSSL state.

Because the NSSL two-moment scheme predicts only the mass mixing ratio and number concentration of each hydrometeor category, it does not directly provide the particle size spectra or particle properties required by PH17. A bin-emulation approach was therefore adopted. At each physical time step and for each grid point with temperature below 273.15 K and at least one ice-phase category present, discrete size spectra were temporarily reconstructed for hail, graupel, snow, and cloud ice. Here q_x is the mass mixing ratio and c_x is the volume number concentration. The mean particle mass of category x is therefore defined as

$$\bar{m}_x = \frac{\rho_{air} q_x}{c_x}, \quad (7)$$

where ρ_{air} is the air density. For each ice-phase category, the particle size distribution was assumed to follow a gamma distribution in diameter space. The shape parameter was set to $\mu = 0.5$ for hail and $\mu = 0$ for graupel, snow, and cloud ice. The slope parameter was determined using the NSSL mass–diameter relationship for each category and the diagnosed mean particle mass. Spherical mass relationships were used for hail and graupel, whereas the corresponding NSSL mass–diameter relationships were used for snow and cloud ice. This treatment allows the reconstructed size spectra



225 to remain consistent with the mass mixing ratio and number concentration predicted by
226 the NSSL scheme.

227 The diagnostic diameter range for each hydrometeor category was specified according
228 to the native physical range used for that category in the NSSL scheme, rather than
229 being uniformly constrained to the PH17 valid diameter range during spectrum
230 reconstruction. Each diameter range was divided into logarithmically spaced bins, and
231 the representative diameter of each bin was taken as the geometric mean of the two bin
232 edges. The initial number fraction in each bin was obtained by integrating the gamma
233 distribution over the corresponding diameter interval. The bin weights were then
234 adjusted so that the reconstructed spectrum satisfied both the total volume number
235 concentration and total mass density constraints:

$$236 \quad \sum_i n_{x,i} = c_x, \quad (8)$$

$$237 \quad \sum_i n_{x,i} m_{x,i} = \rho_{air} q_x, \quad (9)$$

238 Here $n_{x,i}$ and $m_{x,i}$ are the volume number concentration and particle mass of bin i for
239 category x , respectively. The particle mass and terminal velocity in each bin were then
240 calculated using the corresponding NSSL mass–diameter and fall-speed relationships.
241 The PH17 diameter range of 0.5–5 mm was not used to constrain the reconstructed
242 spectra, but was applied only later in the calculation of empirical parameters in the
243 fragment-number formula.

244 For any two bins i and j , the collision kinetic energy was calculated using the reduced-
245 mass form:

$$246 \quad K_0 = \frac{1}{2} \left(\frac{m_i m_j}{m_i + m_j} \right) (v_i - v_j)^2, \quad (10)$$

247 where m_i and m_j are the particle masses of the two bins, and v_i and v_j are their terminal
248 velocities. The collision rate between any two bins i and j was estimated using a
249 gravitational collision kernel:

$$250 \quad R_{ij} = \frac{1}{4} n_i n_j \cdot \pi (D_i^{phys} + D_j^{phys})^2 |v_i - v_j| E_c, \quad (11)$$

251 Here, n_i and n_j are the volume number concentrations of the two bins, D_i^{phys} and D_j^{phys}



are the corresponding diagnosed physical diameters, E_c is the collision efficiency. For self-collisions within the same particle category, only bin combinations with $j \geq i$ were evaluated. A factor of 1/2 was applied for same-bin self-collisions.

For ice-phase collision pairs already represented in the native NSSL scheme, the corresponding collision efficiencies were retained. For pairs not explicitly treated in NSSL, simplified values were assigned based on the native ice-phase collision treatments: $E_c = 1.0$ for H–H, H–G, and G–G collisions, and $E_c = 0.5$ for S–S and I–I collisions. Additional sensitivity experiments using $E_c = 0.5$ for H–H, H–G, and G–G collisions produced qualitatively similar results, indicating that the main conclusions are not sensitive to this simplified choice. Here, H, G, S, and I denote hail, graupel, snow, and cloud ice, respectively. For example, H–G represents hail–graupel collisions, and G–I represents graupel–cloud ice collisions.

The number of fragments generated by a single collision was then calculated following PH17:

$$N_{BR} = \min\{N_{max}, \alpha A(M)[1 - \exp(-(\frac{CK_0}{\alpha A(M)})^\gamma)]\}, \quad (12)$$

where K_0 is the collision kinetic energy of the bin pair. The term $\alpha = \pi D_{calc}^2$ represents the characteristic area scale of the breaking particle, consistent with PH17. Here D_{calc}

denotes the representative diameter used only in the PH17 fragment-number formula. The physical diameters diagnosed from the bin-emulation spectra were still used to calculate the collision kernel, particle mass, terminal velocity, and collision kinetic energy. For collisions between particles of the same category, the physical representative diameter was first taken as the smaller of the two particle diameters. For collisions between different categories, it was taken as the diameter of the more fragile particle. This physical representative diameter was then constrained to the PH17 valid range of 0.5–5 mm to obtain D_{calc} . The parameters A , C , γ , N_{max} , and related coefficients were specified according to the collision type, temperature, and particle characteristics in PH17. Additional implementation settings are summarized in Appendix A1.

For any two bins i and j , the number source of BR fragments was calculated as



$$N_{ij} = N_{BR} \times R_{ij}, \quad (13)$$

where R_{ij} is the collision rate estimated from the gravitational collision kernel. The BR calculation was performed after the NSSL process of ice multiplication from snow. The BR fragment number source was accumulated as a cloud-ice number source, and the corresponding fragment mass transfer was passed to the mass-conserving feedback step. The parent-category adjustment, mass transfer, and number concentration updates are described in Sect. 2.3.3.

To diagnose the dominant sources of BR, the calculated BR fragment number source was further accumulated separately for each ice-phase collision pair. The four ice-phase categories correspond to 10 unordered collision pairs: H–H, G–G, S–S, I–I, H–G, H–S, H–I, G–S, G–I, and S–I. In the following analysis, the “BR collision-pair contribution” refers to the percentage contribution of each collision pair to the total BR fragment number source.

2.3.3 Category adjustment and mass-conserving feedback

At the particle scale, ice–ice collisional breakup generally removes only part of the mass of the colliding particles as fragments rather than completely removing the parent particles. In the NSSL two-moment scheme, however, adding only the fragments produced by BR without adjusting the mass and number concentration of the colliding ice-phase particles may introduce artificial changes in total ice mass and mean particle size. To avoid this effect, the BR-related mass loss was accumulated diagnostically over all bin pairs for each fragile hydrometeor category x at every time step and grid point before the feedback update:

$$L_x^{BR} = \sum_{i,j} \Delta q_{x,ij}^{BR}, \quad (14)$$

where $\Delta q_{x,ij}^{BR}$ is the mass loss assigned to category x from the bin combination (i, j) , and the summation is taken over all relevant collision pairs within the current time step. The mass loss actually applied was constrained by the available mass:

$$\tilde{L}_x^{BR} = \min(L_x^{BR}, q_x), \quad (15)$$

where q_x is the mass mixing ratio of category x . For hail, graupel, and snow as the



309 fragile parent category, the mass mixing ratio and number concentration of the parent
310 category were then adjusted using the same fractional reduction:

$$311 \quad f_x = \frac{\tilde{L}_x^{BR}}{q_x}, \quad (16)$$

$$312 \quad q_x^{new} = q_x - \tilde{L}_x^{BR}, \quad (17)$$

$$313 \quad N_x^{new} = (1 - f_x)N_x. \quad (18)$$

314 Here, N_x denotes the number concentration of category x . For hail, graupel, and snow,
315 the removed mass was transferred to cloud ice, and the cloud ice number concentration
316 was increased according to the corresponding BR fragment number source. When cloud
317 ice was the fragile category, the fragments were still assigned to cloud ice; therefore,
318 no inter-category mass transfer was applied, and only the cloud ice number
319 concentration was increased.

320 **2.4 Experimental design and diagnostics**

321 All sensitivity experiments used the same CM1 configuration and NSSL two-moment
322 microphysics scheme described in Sect. 2.2, with only the SIP-related settings varied
323 among the experiments. A total of seven sensitivity experiments were designed (Table
324 1). CNTL is the control experiment, in which only the default H–M process in the NSSL
325 scheme is retained. All other experiments are configured relative to CNTL. DS_LAW
326 and DS_SUL activate the two DS configurations separately. BR_PH_1 and BR_PH_2
327 include the BR process in addition to the default H–M process, using the 5-bin and 20-
328 bin configurations, respectively, with DS deactivated. SIP_ALL_1 and SIP_ALL_2
329 combine DS_LAW with BR, also using the 5-bin and 20-bin configurations,
330 respectively. DS_LAW is used in the combined SIP experiments because the Lawson
331 et al. (2015) formulation is directly based on observationally inferred fragment
332 production during freezing. Except for the SIP-related settings, the dynamical and
333 thermodynamic conditions are identical across all experiments; therefore, differences
334 among the experiments are primarily attributable to the SIP parameterizations.

335 The main diagnostics include cloud-ice structural characteristics, hail characteristics at
336 the surface, the evolution of in-cloud microphysics, and BR sources. Unless otherwise



337 stated, all diagnostics are calculated within a horizontal analysis box centered on the
 338 domain center, extending 5.95 km from the center in both the x and y directions.
 339 “Surface” refers to the lowest model level. Vertical profiles and microphysical process
 340 rates are averaged within the main updraft region, which is further defined as grid points
 341 with $w > 2 \text{ m s}^{-1}$ within this horizontal analysis area. The mature-stage mean cloud-ice
 342 volume is calculated within the same horizontal analysis box and is defined as the
 343 volume of grid cells satisfying $N_i > 10^5 \text{ kg}^{-1}$. In this paper, “supercooled liquid water”
 344 refers to the sum of cloud water and rainwater at temperatures below 0°C . The BR
 345 source analysis is based on the diagnostic BR fragment number source from different
 346 collision pairs, as defined in Sect. 2.3.2. Based on the simulated evolution of hail aloft
 347 and surface hailfall in CNTL, the rapid development stage and mature hail-producing
 348 stage are defined as 90–107 min and 108–120 min, respectively.

349 **Table 1.** Overview of the numerical sensitivity experiment design. All experiments
 350 retain the default NSSL H–M process. BR_PH_1 and BR_PH_2 denote PH17-type
 351 BR calculations using 5 and 20 emulated size bins, respectively.

Experiment Name	H–M process	Droplet Shattering (DS)	Collisional Breakup (BR)	Description
CNTL	ON	OFF	OFF	Control experiment, retaining only the default NSSL H–M process
DS_LAW	ON	ON (Lawson et al., 2015)	OFF	Uses an empirical DS parameterization based on raindrop size
DS_SUL	ON	ON (Sullivan et al., 2018b)	OFF	Uses a temperature-dependent DS parameterization with a prescribed breakup probability
BR_PH_1	ON	OFF	ON (PH17; 5 bins)	BR only; bin emulation uses 5 bins
BR_PH_2	ON	OFF	ON (PH17; 20 bins)	BR only; bin emulation uses 20 bins
SIP_ALL_	ON	ON (Lawson	ON (PH17; 5	Combined experiment with



1		et al., 2015)	bins)	DS_LAW and BR_PH_1
SIP_ALL_	ON	ON (Lawson	ON (PH17; 20	Combined experiment with
2		et al., 2015)	bins)	DS_LAW and BR_PH_2

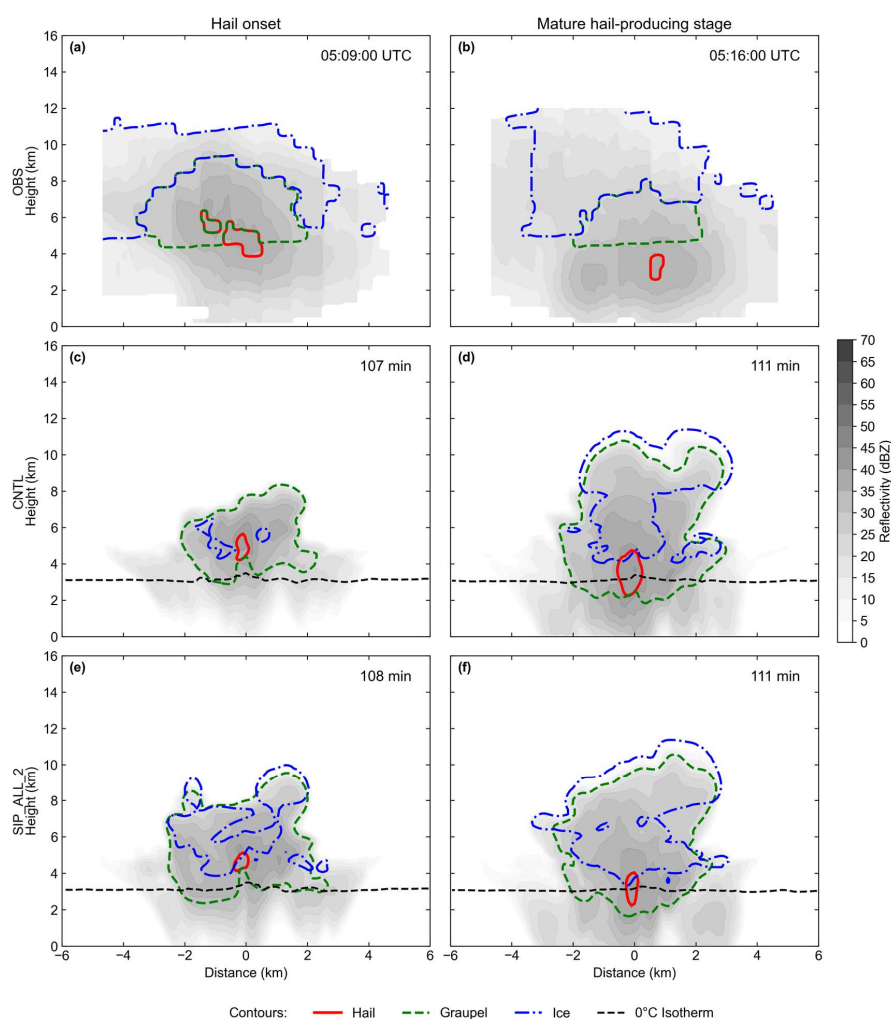
352



3. Results

3.1 Observed storm structure and responses to SIP

Previous work has shown that the CNTL experiment can reasonably reproduce the convective initiation height, the 35 dBZ echo top height, the echo width, and the rapid onset of hailfall of this case (Dong et al., 2024). Figure 1 further compares the reflectivity structure and the main ice-phase particle distributions among observational retrievals, the CNTL experiment, and the SIP_ALL_2 experiment at two representative stages.



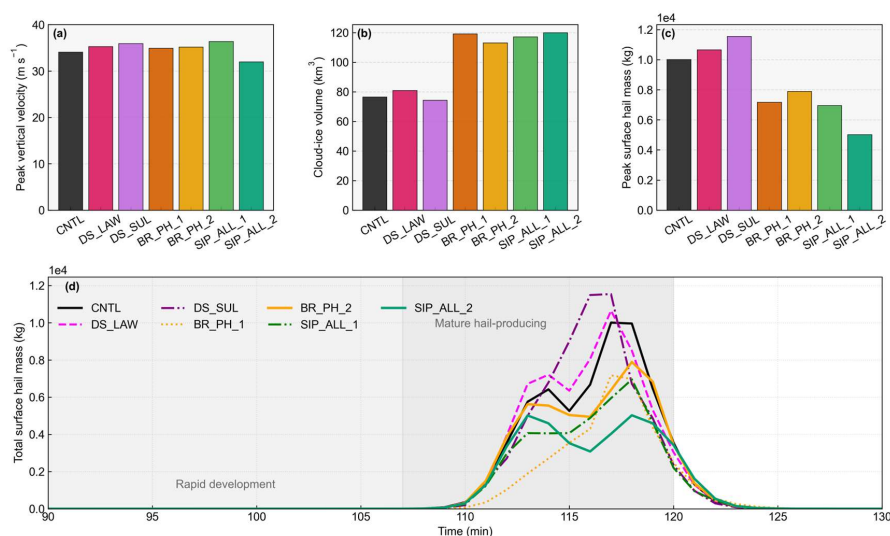


362 **Figure 1.** Observed and simulated storm structure at hail onset and during the mature
363 hail-producing stage. The first column corresponds to the end of the rapid development
364 stage, when hail first appears aloft ($q_h > 1 \text{ g kg}^{-1}$), and the second column shows a
365 representative time during the mature hail-producing stage. The grayscale shading
366 shows reflectivity. Red, green, and blue contours denote hail, graupel, and ice crystals,
367 respectively, and the black dashed line indicates the 0°C isotherm.

368 The observational retrievals show that the pulse storm had already developed a clear
369 vertical stratification of the ice phase during the rapid development stage (Fig. 1a). Ice
370 crystals extended upward to approximately 11 km, graupel was concentrated between
371 about 4.5 and 8 km, with the hail core located in the lower part of the graupel region,
372 near 4–6 km. During the mature hail-producing stage (Fig. 1b), the hail core descended
373 to approximately 2.5–4 km, while upper-level ice crystals remained above 10 km.

374 The CNTL experiment generally reproduces the main altitude ranges of graupel and
375 hail. However, at the time when hail first appears aloft, CNTL underestimates the upper-
376 level ice crystal region, with both the horizontal coverage and vertical extent being
377 markedly smaller than those indicated by the observational retrievals (Fig. 1c). This
378 bias is reduced during the mature hail-producing stage, but notable differences in the
379 spatial distribution of ice crystals remain.

380 Compared with CNTL, SIP_ALL_2 produces only minor changes in the overall echo
381 morphology but yields a more extensive mid- and upper-level ice crystal field. At the
382 time when hail first appears aloft, the ice crystal distribution in SIP_ALL_2 is more
383 continuous and has a broader horizontal extent than in CNTL (Fig. 1e). During the
384 mature hail-producing stage, the upper boundary of the ice crystal field reaches around
385 12 km, with a broader horizontal distribution; meanwhile, the position of the hail core
386 is also closer to that retrieved from observations (Fig. 1f). To assess whether these
387 differences are accompanied by systematic changes in storm dynamics, cloud-ice extent,
388 and surface hailfall, Fig. 2 compares storm-scale characteristics across the seven
389 sensitivity experiments.



390

391 **Figure 2.** Storm-scale dynamical, cloud-ice, and surface hailfall responses across the
 392 sensitivity experiments. (a) Peak domain-maximum vertical velocity, (b) mature-stage
 393 mean cloud-ice volume, (c) peak total hail mass at the surface, and (d) time series of
 394 total surface hail mass. Cloud-ice volume is calculated with $N_i > 10^5 \text{ kg}^{-1}$ during the
 395 mature hail-producing stage. The light and dark gray shading in (d) denotes the rapid
 396 development and mature hail-producing stages, respectively.

397 The peak domain-maximum vertical velocity varies only weakly among the
 398 experiments, remaining roughly within $34\text{--}36.5 \text{ m s}^{-1}$ (Fig. 2a). The two DS
 399 experiments are close to CNTL, and the BR-only and combined SIP experiments do not
 400 show a systematic enhancement. For cloud-ice volume (Fig. 2b), the DS-only
 401 experiments remain close to CNTL, whereas the BR-only and combined SIP
 402 experiments produce larger cloud-ice volumes of about $105\text{--}120 \text{ km}^3$. This is consistent
 403 with the broader cloud-ice region shown in the SIP_ALL_2 cross section in Fig. 1.

404 The peak total hail mass at the surface shows a clearer response (Fig. 2c). The two DS-
 405 only experiments produce slightly larger peak values than CNTL. In contrast, all
 406 experiments including BR markedly reduce the peak surface hail mass. Relative to
 407 CNTL, the reduction is 21.15 % in BR_PH_2, while SIP_ALL_2 produces the largest
 408 reduction among all sensitivity experiments, reaching 41.94 %. The following analysis
 409 therefore uses BR_PH_2 and SIP_ALL_2 as representative BR experiments.

410 Figure 2d shows the temporal evolution of total surface hail mass. In all experiments,
 411 total surface hail mass increases rapidly after about 110 min and reaches its peak shortly



thereafter. The peak timing is similar among the experiments, occurring between 116 and 118 min, whereas the main difference lies in the peak magnitude. The microphysical changes responsible for these differences are examined in the following section.

3.2 SIP-induced restructuring of the ice phase and liquid water competition

Figure 3 shows the mean vertical profiles of key hydrometeor properties in the five representative experiments during the mature hail-producing stage. The largest differences among the experiments occur in the ice crystal number concentration.

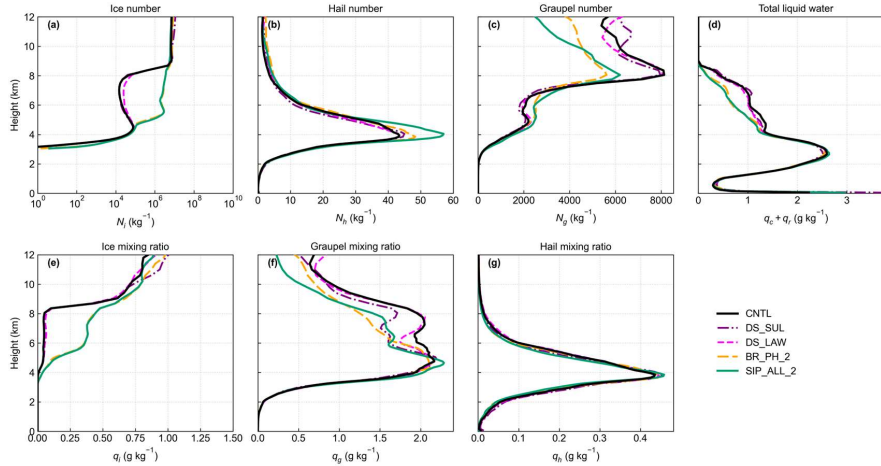


Figure 3. Mean vertical profiles of key hydrometeor properties in the analysis region during the mature hail-producing stage for representative experiments. (a) Ice crystal number concentration, (b) hail number concentration, (c) graupel number concentration, (d) total liquid water, (e) cloud ice mixing ratio, (f) graupel mixing ratio, and (g) hail mixing ratio.

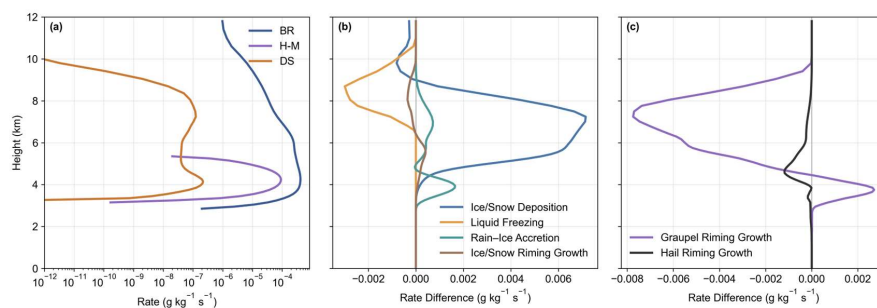
Between about 5 and 9 km, N_i in BR_PH_2 and SIP_ALL_2 increases to approximately 10^6 – 10^7 kg⁻¹, whereas CNTL and the two DS-only experiments remain at about 10^4 – 10^5 kg⁻¹. At other altitudes, the differences among the experiments are smaller. This indicates that the increase in ICNC in the mid- to upper-level mixed-phase region during the mature hail-producing stage is mainly associated with BR, while the effect of DS alone is weak.

Corresponding to the increase in ICNC, the cloud ice mixing ratio in BR_PH_2 and



434 SIP_ALL_2 also increases below about 9 km, although the increase is relatively limited
435 (Fig. 3e). The total supercooled liquid water is reduced above 4 km, especially in the
436 mid-level mixed-phase region (Fig. 3d). The response of graupel number concentration
437 varies with height: it increases between about 4 and 7 km but decreases above 7 km
438 (Fig. 3c). At the same time, the graupel mixing ratio decreases overall.

439 For hail, the number concentration in BR_PH_2 and SIP_ALL_2 increases near 4 km,
440 with SIP_ALL_2 showing an increase of about 30 % (Fig. 3b). The hail mixing ratio,
441 however, does not show a clear overall change (Fig. 3g). These results indicate that BR
442 mainly modifies the number and mass distributions of ice crystals and graupel, together
443 with a local increase in hail number, and is accompanied by a reduction in supercooled
444 liquid water above 4 km. To further identify the microphysical processes associated
445 with these hydrometeor changes, Fig. 4 compares the main microphysical process rates
446 during the mature hail-producing stage.



447

448 **Figure 4.** Mean vertical profiles of microphysical process rates in the analysis region
449 during the mature hail-producing stage. (a) Secondary ice mass source rates associated
450 with the three SIP processes in SIP_ALL_2. (b) Differences in the main ice-phase and
451 liquid-water-related process rates between SIP_ALL_2 and CNTL. (c) Differences in
452 the riming growth rates of graupel and hail between SIP_ALL_2 and CNTL. Positive
453 values indicate larger process rates in SIP_ALL_2 than in CNTL. Detailed definitions
454 of the process labels are provided in the Appendix.

455 Figure 4a shows the vertical distribution of the secondary ice mass source rates
456 associated with the three SIP processes in SIP_ALL_2 during the mature hail-producing
457 stage. BR contributes above approximately 3 km and reaches its maximum near 4 km,
458 with a peak value close to $10^{-4} \text{ g kg}^{-1} \text{s}^{-1}$. The H-M process is mainly confined to a
459 layer between about 3 and 5.5 km, whereas DS is generally weaker but extends to higher
460 altitudes. Overall, BR is the dominant SIP mass source during this stage. It should be



461 noted that, although BR still has a non-negligible contribution at upper levels, its largest
462 source rates are mainly located below 9 km, consistent with the ICNC enhancement in
463 Fig. 3 being concentrated mainly between about 5 and 9 km.

464 The changes in ICNC, supercooled liquid water, and graupel mixing ratio in Fig. 3
465 suggest that the BR response is concentrated mainly between 4 and 9 km. To identify
466 the processes responsible for these differences, Fig. 4b shows the differences in the
467 main microphysical process rates between SIP_ALL_2 and CNTL. The most
468 pronounced positive difference occurs in the depositional growth of ice crystals and
469 snow, mainly between about 5 and 9 km, with the maximum in the mid- to upper mixed-
470 phase region. Rain–ice accretion also increases between about 4 and 7 km. In contrast,
471 the contribution of direct liquid freezing to ice-phase growth is reduced between about
472 7 and 9 km, while the riming growth of ice crystals and snow changes only weakly.

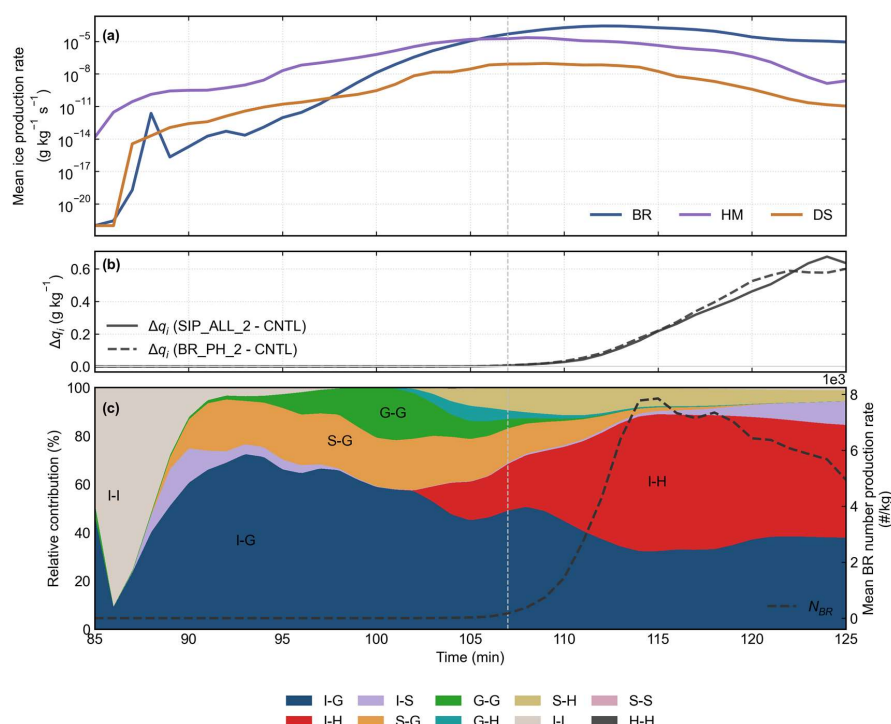
473 Relative to CNTL, the riming growth of graupel in SIP_ALL_2 is substantially
474 weakened between about 5 and 9 km, especially near 7–8 km (Fig. 4c), despite a weak
475 local enhancement near 3.5–4 km. The change in hail riming growth is smaller than that
476 of graupel and is mainly characterized by a decrease between 4 and 7 km. These features
477 indicate that the BR-related increase in ice crystals mainly affects liquid-water
478 competition and graupel growth in the mid-level mixed-phase region, thereby
479 influencing subsequent hail growth.

480



3.3 Temporal evolution of BR and its decomposition by collision pair

Figure 5a reveals the temporal evolution of the different SIP processes.



483

Figure 5. Temporal evolution of SIP rates, cloud ice responses, and BR collision pair contributions in SIP_ALL_2. (a) Region-mean secondary ice mass production rates from BR, H-M, and DS. (b) Region-mean cloud ice mass mixing ratio differences (Δq_i) in SIP_ALL_2 and BR_PH_2 relative to CNTL. (c) Relative contributions of the main ice-phase collision pairs to the BR fragment number source; the black dashed line denotes the region-mean BR fragment number source on the right-hand axis. The gray vertical dashed line marks 107 min, corresponding to the end of the rapid development stage.

Before 100 min, the BR mass production rate remains relatively low and is clearly smaller than that of the H-M process. BR then increases rapidly and exceeds H-M at 107 min, becoming the main SIP mass source thereafter. DS remains weak throughout the period, consistent with the vertical process-rate diagnostics in Fig. 4a.

The Δq_i values of SIP_ALL_2 and BR_PH_2 relative to CNTL both increase after 107 min (Fig. 5b). The two experiments show similar variations during 107–125 min,



498 indicating that the increase in q_i in the combined SIP experiment, relative to CNTL, is
499 mainly attributable to BR.

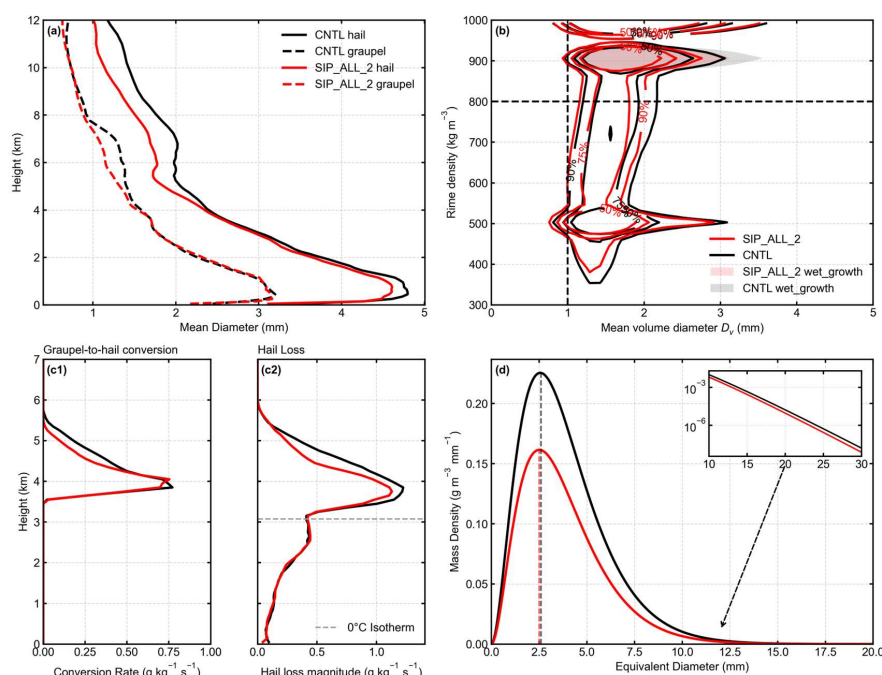
500 To further identify the source of the BR enhancement, Fig. 5c decomposes the BR
501 fragment number source into contributions from different ice-phase collision pairs. It
502 should be noted that the shaded areas in Fig. 5c represent relative contributions;
503 therefore, when the total BR number source is very small, a large percentage does not
504 necessarily correspond to a large absolute number of fragments. Before 90 min, I–I
505 accounts for a large fraction, but the total BR fragment number source is extremely low.
506 As the storm develops, I–G becomes the dominant contributor during 90–103 min,
507 accounting for more than 50 %, while S–G and G–G also make appreciable
508 contributions. During the mature hail-producing stage, the relative contribution of I–H
509 increases markedly, and I–H together with I–G becomes the main source of BR
510 fragments. In contrast, I–I and the other collision types contribute less during the period
511 of strong BR activity. These features indicate that the enhancement of BR is mainly
512 maintained by collisions between ice crystals and larger ice-phase particles, especially
513 graupel and hail.

514



3.4 Consequences for hail growth, hail embryos, and surface hail spectrum

The preceding results show that SIP enhancement occurs mainly during the mature hail-producing stage and is accompanied by reduced supercooled liquid water and weakened graupel riming growth in the mid- to upper-level mixed-phase region. Figure 6 further examines how these microphysical changes affect hail growth and the surface hail mass.



521

Figure 6. Region-averaged hail and graupel size responses, hail source and loss terms, and surface hail mass spectrum during the mature hail-producing stage. (a) Vertical profiles of the mean diameters of hail and graupel; (b) graupel mean volume diameter-rimed density phase space, with the dashed lines denoting the NSSL graupel-to-hail conversion thresholds of $D_v = 1$ mm and rimed density = 800 kg m^{-3} , and the shaded areas indicating the wet-growth regions; (c) hail source and loss terms, including (c1) graupel-to-hail conversion and (c2) melting plus shedding loss, with the gray dashed line denoting the mean 0°C isotherm; and (d) surface hail mass spectrum, with the inset showing the 10–30 mm diameter range.

Figure 6a shows that the mean hail diameter in SIP_ALL_2 is generally smaller than that in CNTL above about 4 km, corresponding to the 4–8 km layer where hail growth is suppressed. The mean graupel diameter also decreases between about 4 and 8 km. In



534 the NSSL scheme, graupel can be converted to hail only when it is in the wet-growth
535 regime, its mean volume diameter D_v exceeds 1 mm, and its rimed density exceeds 800
536 kg m^{-3} . In SIP_ALL_2, the graupel population shifts toward smaller diameters, and this
537 shift is particularly evident at the large-particle end within the wet-growth region (Fig.
538 6b). In other words, compared with CNTL, the potential hail embryos in SIP_ALL_2
539 move farther away from the conditions favorable for efficient conversion to hail. This
540 is consistent with the source-term diagnostics in Fig. 6c1: although the conversion peak
541 near 4 km is close to that in CNTL, the graupel-to-hail conversion rate in SIP_ALL_2
542 is clearly reduced between about 4.5 and 5.5 km.

543 For hail loss, Fig. 6c2 shows that the loss caused by melting and shedding in
544 SIP_ALL_2 is close to that in CNTL below the 0 °C level and is even smaller between
545 about 3.5 and 5.5 km. This indicates that the reduction in surface hail mass is only
546 weakly related to hail loss and should be mainly attributed to smaller graupel particles,
547 weakened graupel-to-hail conversion, and limited subsequent hail growth. Could the
548 reduced surface hail mass be caused directly by BR-induced hail mass removal? Direct
549 mass removal from the hail category can occur only through H–H collisions, because
550 hail is treated as the least fragile ice-phase category. However, Fig. 5c shows that the
551 H–H contribution is negligible during the period of strong BR activity, suggesting that
552 this direct-removal pathway is unlikely to dominate in the present implementation.
553 Similarly, H–G and G–G collisions, which could directly remove mass from the graupel
554 category, also contribute little during the mature hail-producing stage, while the
555 moderate G–G contribution occurs earlier when the total BR source is still weak.

556 The surface hail mass spectrum is shown in Fig. 6d. Compared with CNTL,
557 SIP_ALL_2 has a smaller peak diameter and a markedly lower mass density over the
558 0–10 mm diameter range, which provides the dominant contribution to the surface hail
559 mass. Although the difference is smaller at diameters larger than 10 mm, the mass
560 density in SIP_ALL_2 also remains lower than in CNTL in this large-particle range.

561 Taken together, the SIP processes, especially BR, reduce the surface hail mass through
562 a linked set of microphysical changes. The large number of secondary ice crystals
563 enhances competition for liquid water in the 4–8 km mixed-phase region, weakens
564 graupel riming growth, reduces the mean size of potential hail embryos, weakens
565 graupel-to-hail conversion over part of the layer, and suppresses the riming growth of



566 hail itself. These processes jointly lead to the reduction in surface hail mass.

567 **4. Summary and Discussion**

568 This study examines how different secondary ice production mechanisms affect ice-
569 phase evolution, hail growth, and surface hailfall in a short-lived pulse hailstorm.
570 Idealized numerical experiments were conducted using CM1 with the NSSL two-
571 moment microphysics scheme. Two droplet-shattering configurations, an ice-ice
572 collisional breakup parameterization, and their combined effects were tested. The main
573 conclusions are as follows.

574 (1) Among the SIP mechanisms examined here, BR has a much stronger effect than DS
575 on the simulated cloud-ice structure and surface hailfall. The experiments that include
576 BR produce larger cloud-ice volumes during the mature hail-producing stage. However,
577 BR does not lead to a systematic increase in the domain-maximum vertical velocity,
578 and the peak updraft intensities remain broadly similar among the experiments.
579 Therefore, the changes in cloud-ice volume and surface hail mass cannot be simply
580 attributed to stronger storm-scale dynamics. The peak total hail mass at the surface is
581 also more sensitive to BR: relative to CNTL, it decreases by 21.15 % in BR_PH_2 and
582 by 41.94 % in SIP_ALL_2, which shows the largest reduction. These results suggest
583 that the main effect of BR is likely to reduce surface hail mass through changes in the
584 ice-phase structure.

585 (2) In the experiments including BR, the ice crystal number concentration during the
586 mature hail-producing stage increases by about two orders of magnitude between
587 approximately 5 and 9 km, from about 10^4 – 10^5 kg^{-1} in CNTL and the DS-only
588 experiments to about 10^6 – 10^7 kg^{-1} . This layer corresponds to the region where
589 supercooled liquid water decreases above 4 km and the graupel mixing ratio is reduced.
590 Process-rate diagnostics further show that the depositional growth of ice crystals and
591 snow is enhanced in SIP_ALL_2, and rain-ice accretion also increases, whereas
592 graupel riming growth is markedly weakened between about 5 and 9 km. The response
593 of hail itself is weaker: the hail mixing ratio shows little overall change, but the mean
594 hail diameter is smaller and graupel-to-hail conversion is suppressed at some heights.
595 Hail loss is not enhanced, indicating that the reduction in surface hail mass is mainly
596 associated with smaller graupel particles, smaller potential hail embryos, weakened



597 graupel-to-hail conversion, and suppressed subsequent hail riming growth. The surface
598 hail mass spectrum also shows that SIP_ALL_2 is markedly lower than CNTL over the
599 0–10 mm diameter range, which provides the dominant contribution to total surface
600 hail mass.

601 (3) The contributions of different BR collision pairs vary distinctly during storm
602 evolution. In the early stage, I–I collisions can account for a large relative fraction, but
603 the BR fragment number source is very small at that time. As the storm develops, I–G
604 becomes the dominant contributor during about 90–103 min, while S–G and G–G also
605 make appreciable contributions. After the storm enters the mature hail-producing stage,
606 the relative contribution of I–H increases markedly, and I–H together with I–G becomes
607 the main source of BR fragments. In contrast, I–I and the other collision types
608 contribute less during the mature hail-producing stage. This indicates that, in this pulse
609 hailstorm case, the enhancement of BR is mainly maintained by collisions between ice
610 crystals and larger ice-phase particles, especially graupel and hail. As BR produces
611 more ice crystals, the frequency of collisions involving ice crystals may further increase,
612 helping to maintain or enhance the BR fragment number source.

613 These results show that SIP can substantially regulate hail growth even in a short-lived
614 pulse hailstorm. BR begins to increase rapidly near the end of the rapid development
615 stage and becomes the main SIP mass source during the mature hail-producing stage.
616 The large number of secondary ice crystals produced by BR expands the cloud-ice
617 region and enhances competition for liquid water in the mid-level mixed-phase region.
618 At the same time, graupel riming growth and graupel-to-hail conversion at some heights
619 are suppressed, and subsequent hail growth is limited. As a result, the storm shows a
620 marked reduction in surface hail mass without an evident change in dynamical intensity.

621 The BR response in this study is subject to uncertainties related to the PH17
622 parameterization and its implementation within the NSSL two-moment scheme,
623 including the category mapping, reconstructed particle size spectra, and several
624 simplified parameter settings. Although sensitivity experiments using different bin
625 numbers and collision efficiencies produced qualitatively similar results, a bulk
626 microphysics scheme cannot fully represent the diversity of ice-particle properties in
627 real hailstorms. In addition, the simulations represent an idealized pulse hailstorm
628 environment. Therefore, the BR response and its impacts on hail growth and surface



629 hailfall may vary among different storm types and microphysics schemes, and the
630 associated microphysical mechanisms should be further evaluated under a broader
631 range of storm conditions.

632 In addition, BR can markedly increase in-cloud ice crystal number and strengthen the
633 competition among ice-phase particles for supercooled liquid water. This has
634 implications for numerical simulations of hail suppression by cloud seeding. When BR
635 is included in a model, the simulated storm may already contain many small ice crystals,
636 resembling a relatively strong “natural seeding” state. Under such conditions, the
637 assessment of artificial seeding effects may differ from traditional simulation studies
638 that do not fully account for SIP processes (Atlas, 1977; Garstang et al., 2005). The
639 presence of BR may affect the optimal timing, dosage, and location of hail-suppression
640 seeding, as well as the criteria used to evaluate seeding effectiveness (Lu et al., 2023).
641 However, this study also shows that the rapid increase in BR occurs mainly from the
642 end of the rapid development stage to the mature hail-producing stage. It therefore
643 remains unclear whether the small ice crystals produced by BR are already abundant
644 before the key time window in which artificial seeding may be most effective. Future
645 work should combine different storm types and seeding scenarios to systematically
646 assess how SIP affects conclusions drawn from numerical simulations of hail
647 suppression.

648

649

650 Appendix A

651 A1. Supplementary settings for the PH17-type BR parameterization in the NSSL bulk
652 scheme

653 Sects. 2.3.2 and 2.3.3 describe the main implementation of the PH17-type BR
654 parameterization in the NSSL scheme. Here, additional details are provided on the
655 PH17 parameter settings and simplifying assumptions.

656 The empirical parameters A , C , γ and N_{max} , together with the fragment mass fraction
657 ζ , in the PH17 formula for fragment number were assigned according to Table 1 of
658 PH17. For particle fragility, the following order from most to least fragile is assumed:



cloud ice, snow, graupel, and hail.

For the rimed mass fraction Ψ in PH17, the NSSL scheme does not explicitly predict the corresponding variable required by PH17. Therefore, Ψ is fixed at 0.2, corresponding to the PH17 estimate for lightly to moderately rimed particles. Han et al. (2024) likewise prescribed the rimed fraction as a constant when implementing a PH17-type BR scheme in a bulk microphysics framework; although their default value was 0.4, additional sensitivity tests with values of 0.2, 0.3, and 0.4 produced different BR responses, although the differences among these sensitivity tests were not significant. Nevertheless, using a fixed Ψ introduces uncertainty, and its influence could be further assessed through dedicated sensitivity experiments.

Table A1. Main supplementary settings of the PH17-type BR parameterization used in this study.

Item	Setting in this study	Description
PH17 empirical parameters	A , C , γ , N_{max} , and ζ are taken from Table 1 of PH17	Original PH17 parameter values are used.
Category mapping	I, S, G, and H correspond to the PH17 categories of crystal, snow, graupel, and hail, respectively.	Consistent with the four ice-phase categories in the NSSL scheme.
Representative diameter D	Limited to 0.5–5 mm	Values outside this range are truncated to the nearest bound.
Ice/snow habit	Dendritic between -12 and -17 °C; spatial planar at other subzero temperatures	Following PH17 guidance for models that do not explicitly predict ice habit.
Rimmed fraction Ψ	Fixed at $\Psi = 0.2$	Represents lightly to moderately rimed particles.

A2. Microphysical process labels in Fig. 4

Table A2 lists the process labels used in the microphysical conversion-rate diagnostics



674 in Fig. 4 and their physical meanings.

675 **Table A2.** Meanings of the microphysical process labels used in Fig. 4.

Label in Fig. 4	Physical meaning
Ice/Snow Deposition	Depositional growth of cloud ice and snow by water vapor deposition
Liquid Freezing	Freezing of liquid hydrometeors
Rain–Ice Accretion	Freezing of raindrops collected by ice particles
Ice/Snow Growth	Growth of cloud ice and snow by riming supercooled liquid water
Graupel Riming Growth	Growth of graupel by riming supercooled liquid water
Hail Riming Growth	Growth of hail by riming supercooled liquid water

676 *Code and data availability.*

677 The data and code used in this study are available from Zenodo at
 678 <https://doi.org/10.5281/zenodo.20556202> (Dong et al., 2026). The archive contains the
 679 CM1 input sounding and namelist files for all sensitivity experiments, the modified
 680 CM1/NSSL-BR source-code files and patch, the processed figure-source data and
 681 selected NetCDF slices for Figs. 1–6, metadata files, and the Python plotting scripts.
 682 Complete raw CM1 history files are not included because of their large size, but the
 683 provided files are sufficient to reproduce the manuscript figures and rerun the
 684 simulations.

685

686 *Author contribution.*

687 YD conceptualized the study, curated the data, developed the methodology,
 688 implemented the model modifications, performed the simulations and analysis, and
 689 wrote the original manuscript draft. SH contributed to the investigation, project
 690 administration, interpretation of the results, and manuscript review and editing. BC
 691 contributed to the investigation, project administration, interpretation of the results, and
 692 manuscript review and editing. TH contributed to manuscript review and editing. All
 693 authors discussed the results and contributed to the final version of the manuscript.

694



695 *Competing interests.*

696 The authors declare that they have no conflict of interest.

697

698 *Financial support.*

699 This work was supported by the National Natural Science Foundation of China (grant
700 no. 42405091), the CMA Key Innovation Team (grant no. CMA2022ZD10), and the
701 S&T Development Fund of CAMS (grant no. 2025KJ022).

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References

- 704 Allen, J. T., Giammanco, I. M., Kumjian, M. R., Punge, H. J., Zhang, Q., Groenemeijer, P.,
705 Kunz, M., and Ortega, K.: Understanding Hail in the Earth System, *Reviews of*
706 *Geophysics*, 58, e2019RG000665, <https://doi.org/10.1029/2019RG000665>, 2020.
- 707 Al-Sakka, H., Boumahmoud, A.-A., Fradon, B., Frasier, S. J., and Tabary, P.: A New Fuzzy
708 Logic Hydrometeor Classification Scheme Applied to the French X-, C-, and S-Band
709 Polarimetric Radars, *Journal of Applied Meteorology and Climatology*, 52, 2328 – 2344,
710 <https://doi.org/10.1175/JAMC-D-12-0236.1>, 2013.
- 711 Atlas, D.: The Paradox of Hail Suppression: Under different circumstances, cloud seeding may
712 result in either increased or decreased hail., *Science*, 195, 139 – 145,
713 <https://doi.org/10.1126/science.195.4274.139>, 1977.
- 714 Bryan, G. H. and Fritsch, J. M.: A Benchmark Simulation for Moist Nonhydrostatic Numerical
715 Models, *Mon. Wea. Rev.*, 130, 2917 – 2928, [https://doi.org/10.1175/1520-0493\(2002\)130<2917:ABSFMN>2.0.CO;2](https://doi.org/10.1175/1520-0493(2002)130<2917:ABSFMN>2.0.CO;2), 2002.
- 717 Cantrell, W. and Heymsfield, A.: Production of Ice in Tropospheric Clouds: A Review, *Bull.*
718 *Amer. Meteor. Soc.*, 86, 795 – 808, <https://doi.org/10.1175/BAMS-86-6-795>, 2005.
- 719 Dolan, B. and Rutledge, S. A.: A Theory-Based Hydrometeor Identification Algorithm for X-
720 Band Polarimetric Radars, *Journal of Atmospheric and Oceanic Technology*, 26, 2071 –
721 2088, <https://doi.org/10.1175/2009JTECHA1208.1>, 2009.
- 722 Dong, Y., Hua, S., Chen, B., Wang, H., and Hou, T.: Numerical simulation of a pulse hailstorm
723 in the plateau region in southwestern China, *Atmospheric Research*, 299, 107218,
724 <https://doi.org/10.1016/j.atmosres.2023.107218>, 2024.
- 725 Dong, Y., Hua, S., Chen, B., and Hou, T.: Data and code for “Ice–ice collisional breakup
726 enhances secondary ice production but reduces surface hailfall in a simulated pulse
727 hailstorm”, Zenodo [data set and code], <https://doi.org/10.5281/zenodo.20556202>, 2026.
- 728 Field, P. R., Lawson, R. P., Brown, P. R. A., Lloyd, G., Westbrook, C., Moisseev, D.,
729 Miltenberger, A., Nenes, A., Blyth, A., Choularton, T., Connolly, P., Buehl, J., Crosier, J.,
730 Cui, Z., Dearden, C., DeMott, P., Flossmann, A., Heymsfield, A., Huang, Y., Kalesse, H.,
731 Kanji, Z. A., Korolev, A., Kirchgaessner, A., Lasher-Trapp, S., Leisner, T., McFarquhar,
732 G., Phillips, V., Stith, J., and Sullivan, S.: Chapter 7. Secondary Ice Production - current
733 state of the science and recommendations for the future, *Meteorological Monographs*,
734 *AMSMONOGRAPHS-D-16-0014.1*, <https://doi.org/10.1175/AMSMONOGRAPHS-D-16-0014.1>, 2017.
- 736 Garstang, M., Brientjes, R., Serafin, R., Orville, H., Boe, B., Cotton, W., and Warburton, J.:
737 Weather Modification: Finding Common Ground, *Bull. Amer. Meteor. Soc.*, 86, 647 – 656,
738 <https://doi.org/10.1175/BAMS-86-5-647>, 2005.
- 739 Georgakaki, P., Sotiropoulou, G., Vignon, É., Billault-Roux, A.-C., Berne, A., and Nenes, A.:
740 Secondary ice production processes in wintertime alpine mixed-phase clouds, *Atmos.*
741 *Chem. Phys.*, 22, 1965 – 1988, <https://doi.org/10.5194/acp-22-1965-2022>, 2022.
- 742 Hallett, J. and Mossop, S. C.: Production of secondary ice particles during the riming process,
743 *Nature*, 249, 26 – 28, <https://doi.org/10.1038/249026a0>, 1974.
- 744 Han, C., Hoose, C., and Dürlich, V.: Secondary Ice Production in Simulated Deep Convective
745 Clouds: A Sensitivity Study, *Journal of the Atmospheric Sciences*, 81, 903 – 921,
746 <https://doi.org/10.1175/JAS-D-23-0156.1>, 2024.
- 747 Hobbs, P. V. and Rangno, A. L.: Ice Particle Concentrations in Clouds, *J. Atmos. Sci.*, 42,
748 2523 – 2549, [https://doi.org/10.1175/1520-0469\(1985\)042<2523:IPCIC>2.0.CO;2](https://doi.org/10.1175/1520-0469(1985)042<2523:IPCIC>2.0.CO;2), 1985.



- 749 Huang, Y., Blyth, A. M., Brown, P. R. A., Choularton, T. W., and Cui, Z.: Factors controlling
750 secondary ice production in cumulus clouds, *Quart J Royal Meteorol Soc*, 143, 1021 –
751 1031, <https://doi.org/10.1002/qj.2987>, 2017.
- 752 Huang, Y., Wu, W., McFarquhar, G. M., Xue, M., Morrison, H., Milbrandt, J., Korolev, A. V.,
753 Hu, Y., Qu, Z., Wolde, M., Nguyen, C., Schwarzenboeck, A., and Heckman, I.:
754 Microphysical processes producing high ice water contents (HIWCs) in tropical
755 convective clouds during the HAIC-HIWC field campaign: dominant role of secondary
756 ice production, *Atmos. Chem. Phys.*, 22, 2365 – 2384, [https://doi.org/10.5194/acp-22-](https://doi.org/10.5194/acp-22-2365-2022)
757 2365-2022, 2022.
- 758 James, R. L., Phillips, V. T. J., and Connolly, P. J.: Secondary ice production during the break-
759 up of freezing water drops on impact with ice particles, *Atmos. Chem. Phys.*, 21, 18519 –
760 18530, <https://doi.org/10.5194/acp-21-18519-2021>, 2021.
- 761 Korolev, A. and Leisner, T.: Review of experimental studies of secondary ice production, *Atmos.*
762 *Chem. Phys.*, 20, 11767 – 11797, <https://doi.org/10.5194/acp-20-11767-2020>, 2020.
- 763 Korolev, A., McFarquhar, G., Field, P. R., Franklin, C., Lawson, P., Wang, Z., Williams, E.,
764 Abel, S. J., Axisa, D., Borrmann, S., Crosier, J., Fugal, J., Krämer, M., Lohmann, U.,
765 Schlenczek, O., Schnaiter, M., and Wendisch, M.: Mixed-Phase Clouds: Progress and
766 Challenges, *Meteorological Monographs*, 58, 5.1-5.50,
767 <https://doi.org/10.1175/AMSMONOGRAPHS-D-17-0001.1>, 2017.
- 768 Lawson, R. P., Woods, S., and Morrison, H.: The Microphysics of Ice and Precipitation
769 Development in Tropical Cumulus Clouds, *Journal of the Atmospheric Sciences*, 72,
770 2429 – 2445, <https://doi.org/10.1175/JAS-D-14-0274.1>, 2015.
- 771 Li, X., Zhang, Q., Zou, T., Lin, J., Kong, H., and Ren, Z.: Climatology of Hail Frequency and
772 Size in China, 1980 – 2015, *Journal of Applied Meteorology and Climatology*, 57, 875 –
773 887, <https://doi.org/10.1175/JAMC-D-17-0208.1>, 2018.
- 774 Lu, Y., Zhou, Y., Zou, S., Yang, Z., and Zeng, Y.: The Macro- and Microphysical Response
775 Characteristics of the Multicell Hailstorm Hail-Suppression Operation: Case Study,
776 *Journal of Applied Meteorology and Climatology*, 62, 1243 – 1262,
777 <https://doi.org/10.1175/JAMC-D-22-0129.1>, 2023.
- 778 Mansell, E. R., Ziegler, C. L., and Bruning, E. C.: Simulated Electrification of a Small
779 Thunderstorm with Two-Moment Bulk Microphysics, *Journal of the Atmospheric*
780 *Sciences*, 67, 171 – 194, <https://doi.org/10.1175/2009JAS2965.1>, 2010.
- 781 Miller, P. W. and Mote, T. L.: Standardizing the Definition of a “Pulse” Thunderstorm,
782 *Bulletin of the American Meteorological Society*, 98, 905 – 913,
783 <https://doi.org/10.1175/BAMS-D-16-0064.1>, 2017.
- 784 Morrison, H., Peters, J. M., Chandrakar, K. K., and Sherwood, S. C.: Influences of
785 Environmental Relative Humidity and Horizontal Scale of Subcloud Ascent on Deep
786 Convective Initiation, *Journal of the Atmospheric Sciences*, 79, 337 – 359,
787 <https://doi.org/10.1175/JAS-D-21-0056.1>, 2022.
- 788 Ni, X., Muehlbauer, A., Allen, J. T., Zhang, Q., and Fan, J.: A Climatology and Extreme Value
789 Analysis of Large Hail in China, *Monthly Weather Review*, 148, 1431 – 1447,
790 <https://doi.org/10.1175/MWR-D-19-0276.1>, 2020.
- 791 Park, H. S., Ryzhkov, A. V., Zrnić, D. S., and Kim, K.-E.: The Hydrometeor Classification
792 Algorithm for the Polarimetric WSR-88D: Description and Application to an MCS,
793 *Weather and Forecasting*, 24, 730 – 748, <https://doi.org/10.1175/2008WAF2222205.1>,
794 2009.
- 795 Phillips, V. T. J., Yano, J.-I., and Khain, A.: Ice Multiplication by Breakup in Ice – Ice Collisions.



- 796 Part I: Theoretical Formulation, *Journal of the Atmospheric Sciences*, 74, 1705 – 1719,
797 <https://doi.org/10.1175/JAS-D-16-0224.1>, 2017a.
- 798 Phillips, V. T. J., Yano, J.-I., Formenton, M., Ilotoviz, E., Kanawade, V., Kudzotsa, I., Sun, J.,
799 Bansemmer, A., Detwiler, A. G., Khain, A., and Tessoroff, S. A.: Ice Multiplication by
800 Breakup in Ice – Ice Collisions. Part II: Numerical Simulations, *Journal of the*
801 *Atmospheric Sciences*, 74, 2789 – 2811, <https://doi.org/10.1175/JAS-D-16-0223.1>, 2017b.
- 802 Phillips, V. T. J., Patade, S., Gutierrez, J., and Bansemmer, A.: Secondary Ice Production by
803 Fragmentation of Freezing Drops: Formulation and Theory, *Journal of the Atmospheric*
804 *Sciences*, 75, 3031 – 3070, <https://doi.org/10.1175/JAS-D-17-0190.1>, 2018.
- 805 Prein, A. F. and Holland, G. J.: Global estimates of damaging hail hazard, *Weather and Climate*
806 *Extremes*, 22, 10 – 23, <https://doi.org/10.1016/j.wace.2018.10.004>, 2018.
- 807 Qu, Z., Korolev, A., Milbrandt, J. A., Heckman, I., Huang, Y., McFarquhar, G. M., Morrison,
808 H., Wolde, M., and Nguyen, C.: The impacts of secondary ice production on microphysics
809 and dynamics in tropical convection, *Atmos. Chem. Phys.*, 22, 12287 – 12310,
810 <https://doi.org/10.5194/acp-22-12287-2022>, 2022.
- 811 Qu, Z., Korolev, A., Milbrandt, J. A., Heckman, I., Cholette, M., Nguyen, C., and Wolde, M.:
812 The impacts of secondary ice production on the microphysics and dynamics of mid-
813 latitude cold season convection, *Atmos. Chem. Phys.*, 25, 17845 – 17868,
814 <https://doi.org/10.5194/acp-25-17845-2025>, 2025.
- 815 Ribaud, J.-F., Machado, L. A. T., and Biscaro, T.: X-band dual-polarization radar-based
816 hydrometeor classification for Brazilian tropical precipitation systems, *Atmos. Meas.*
817 *Tech.*, 12, 811 – 837, <https://doi.org/10.5194/amt-12-811-2019>, 2019.
- 818 Saunders, C. P. R. and Hosseini, A. S.: A laboratory study of the effect of velocity on Hallett –
819 Mossop ice crystal multiplication, *Atmospheric Research*, 59 – 60, 3 – 14,
820 [https://doi.org/10.1016/S0169-8095\(01\)00106-5](https://doi.org/10.1016/S0169-8095(01)00106-5), 2001.
- 821 Sotiropoulou, G., Sullivan, S., Savre, J., Lloyd, G., Lachlan-Cope, T., Ekman, A. M. L., and
822 Nenes, A.: The impact of secondary ice production on Arctic stratocumulus, *Atmos. Chem.*
823 *Phys.*, 20, 1301 – 1316, <https://doi.org/10.5194/acp-20-1301-2020>, 2020.
- 824 Sotiropoulou, G., Vignon, É., Young, G., Morrison, H., O’ Shea, S. J., Lachlan-Cope, T., Berne,
825 A., and Nenes, A.: Secondary ice production in summer clouds over the Antarctic coast:
826 an underappreciated process in atmospheric models, *Atmos. Chem. Phys.*, 21, 755 – 771,
827 <https://doi.org/10.5194/acp-21-755-2021>, 2021.
- 828 Sullivan, S. C., Hoose, C., and Nenes, A.: Investigating the contribution of secondary ice
829 production to in - cloud ice crystal numbers, *JGR Atmospheres*, 122, 9391 – 9412,
830 <https://doi.org/10.1002/2017JD026546>, 2017.
- 831 Sullivan, S. C., Hoose, C., Kiselev, A., Leisner, T., and Nenes, A.: Initiation of secondary ice
832 production in clouds, *Atmos. Chem. Phys.*, 18, 1593 – 1610, <https://doi.org/10.5194/acp-18-1593-2018>, 2018a.
- 834 Sullivan, S. C., Barthlott, C., Crosier, J., Zhukov, I., Nenes, A., and Hoose, C.: The effect of
835 secondary ice production parameterization on the simulation of a cold frontal rainband,
836 *Atmos. Chem. Phys.*, 18, 16461 – 16480, <https://doi.org/10.5194/acp-18-16461-2018>,
837 2018b.
- 838 Takahashi, T., Nagao, Y., and Kushiya, Y.: Possible High Ice Particle Production during
839 Graupel – Graupel Collisions, *J. Atmos. Sci.*, 52, 4523 – 4527,
840 [https://doi.org/10.1175/1520-0469\(1995\)052<4523:PHIPPD>2.0.CO;2](https://doi.org/10.1175/1520-0469(1995)052<4523:PHIPPD>2.0.CO;2), 1995.
- 841 Tian, Y., Yao, W., Sun, Y., Wang, Y., Liu, X., Jiang, T., Zhang, L., Meng, L., Wang, L., Sun, X.,



- 842 and Wang, H.: A method for improving the performance of the 2σ lightning jump
843 algorithm for nowcasting hail, *Atmospheric Research*, 280, 106404,
844 <https://doi.org/10.1016/j.atmosres.2022.106404>, 2022.
- 845 Vardiman, L.: The Generation of Secondary Ice Particles in Clouds by Crystal – Crystal
846 Collision, *J. Atmos. Sci.*, 35, 2168 – 2180, [https://doi.org/10.1175/1520-0469\(1978\)035<2168:TGOSIP>2.0.CO;2](https://doi.org/10.1175/1520-0469(1978)035<2168:TGOSIP>2.0.CO;2), 1978.
- 848 Yano, J.-I. and Phillips, V. T. J.: Ice – Ice Collisions: An Ice Multiplication Process in
849 Atmospheric Clouds, *Journal of the Atmospheric Sciences*, 68, 322 – 333,
850 <https://doi.org/10.1175/2010JAS3607.1>, 2011.
- 851 Zhang, C., Zhang, Q., and Wang, Y.: Climatology of Hail in China: 1961 – 2005, *Journal of*
852 *Applied Meteorology and Climatology*, 47, 795 – 804,
853 <https://doi.org/10.1175/2007JAMC1603.1>, 2008.
- 854 Zhang, Q., Li, R., Li, W., Li, X., Ng, C.-P., Zhang, S., and Zhao, C.: Climate impacts and future
855 trends of hailstorms in China based on millennial records, *Nat. Commun.*, 16, 8000,
856 <https://doi.org/10.1038/s41467-025-63028-7>, 2025.
- 857 Zhao, C., Sun, Y., Yang, J., Li, J., Zhou, Y., Yang, Y., Fan, H., and Zhao, X.: Observational
858 evidence and mechanisms of aerosol effects on precipitation, *Sci. Bull.*, 69, 1569–1580,
859 <https://doi.org/10.1016/j.scib.2024.03.014>, 2024.