

The manuscript proposes a coupled soil radiative transfer model by integrating the improved Hapke-HSR model with the MARMIT-2 model to simulate soil spectral reflectance under varying moisture conditions. The topic is relevant, and the study demonstrates promising results across multiple datasets. The manuscript shows clear novelty, with a well-organized structure and generally good writing quality. I recommend publication after major revisions. I encourage the authors to address the following comments.

We sincerely thank the reviewer for the positive and encouraging assessment of our manuscript. We appreciate the recognition of the relevance, novelty, and overall quality of the work, as well as the constructive suggestions for improvement.

In response, we have thoroughly revised the manuscript to address all comments. The main revisions include clarifying the novelty and model contribution, improving the description of the coupling strategy and parameter estimation, strengthening the discussion of model applicability and limitations, and expanding comparisons with existing approaches.

We believe these revisions have improved the clarity of the manuscript. All comments are addressed in detail below, and we hope the revised version meets the reviewer's expectations.

1. Although the proposed coupled model shows promising performance, the novelty of the study could be further clarified. It is recommended to explicitly highlight the key innovations of the proposed approach in comparison with existing models (e.g., Hapke or MARMIT-2) in the Introduction, to strengthen the overall contribution of the manuscript.

Response 1: We sincerely thank the reviewer for this insightful and constructive suggestion. We fully agree that the novelty of the proposed framework should be more explicitly highlighted, particularly in comparison with existing soil radiative transfer models.

In the revised manuscript, we have substantially strengthened the Introduction to clearly articulate the key innovations and scientific contributions of this study.

Specifically, the novelty of the proposed Hapke-HSR + MARMIT-2 model framework can be summarized as follows:

(1) A physically consistent unified modeling framework:

Unlike existing models that separately describe either dry soil scattering (e.g., Hapke model) or moisture-induced absorption (e.g., MARMIT-2 model), the proposed approach establishes a unified formulation that explicitly integrates particle scattering and moisture-dependent absorption/refraction processes within a single radiative transfer framework.

(2) Elimination of the dependency on externally prescribed dry soil reflectance:

The MARMIT-2 model requires prior knowledge of dry soil reflectance, which is often unavailable in practical applications. In this study, the improved Hapke-HSR model dynamically generates dry reflectance under varying observation geometries, thereby removing this limitation and improving model applicability.

(3) Joint spectral–directional simulation capability under varying moisture conditions:

By inheriting the angular formulation of the Hapke model and incorporating moisture effects via MARMIT-2 model, the proposed model enables consistent simulation of soil reflectance across both spectral and directional domains, which is not achievable with either model alone.

(4) Improved performance under high soil moisture conditions:

The coupled framework significantly enhances model accuracy and stability at high soil moisture levels ($SMC \geq 30\%$), where existing models typically exhibit systematic biases, particularly in strong water absorption regions.

We believe that these revisions have clarified the novelty and strengthened the overall contribution of the manuscript.

Please see p. 3, lines 87-94, in the revised manuscript.

2. Several models are listed in Table 1; however, it is not entirely clear why the Hapke-HSR and MARMIT-2 models were selected for coupling instead of other possible combinations (e.g., BSM with Hapke-HSR). A brief justification for this choice would improve the clarity of the study design.

Response 2: We thank the reviewer for this important comment. We agree that the rationale for selecting the Hapke-HSR and MARMIT-2 models should be clarified.

In the revised manuscript, we have added a concise justification based on the complementary physical characteristics of the two models. The Hapke-HSR model provides a physically based description of directional scattering and enables simulation of dry soil reflectance, whereas the MARMIT-2 model explicitly represents moisture-related absorption and refraction processes but does not account for angular effects and requires prescribed dry reflectance.

Compared with semi-empirical models such as BSM, which lack explicit directional representation, the Hapke-HSR model offers a stronger physical basis for angular reflectance, while MARMIT-2 provides a more physically interpretable treatment of moisture effects. Their coupling therefore enables a physically consistent integration of directional and moisture-related processes.

Please see p. 2-3, lines 63-86, in the revised manuscript.

3. The manuscript should provide clearer references or methodological explanations regarding how the optimal values of parameters such as B_0 , h , b' , c , and c' are determined. In addition, since both b and c influence the BRDF shape in the Hapke model, it would be helpful to clarify why the discussion primarily focuses on parameter b .

Response 3: We thank the reviewer for this insightful comment. We agree that the determination of model parameters and their physical interpretation should be clarified.

In the revised manuscript, we have explicitly stated that the parameters B_0 , h , b' , c , and c' are adopted from previous studies and represent commonly used or empirically optimized values for soil surfaces (e.g., Hapke, 2012; Ding et al., 2022). These parameter values have been shown to provide stable and physically reasonable representations of soil reflectance across a wide range of conditions. To improve clarity, we have added appropriate references and briefly described their physical meaning and typical value ranges. Regarding the roles of parameters b and c , we have added further clarification in Section 4.1. Although both parameters influence the

BRDF shape through the phase function, their sensitivities and physical effects differ. The parameter b primarily controls the width and anisotropy of the scattering lobe, and exhibits a stronger and more stable influence on reflectance across viewing geometries. In contrast, the parameter c mainly affects the asymmetry between forward and backward scattering and generally shows lower sensitivity under the observational configurations considered in this study.

Therefore, this study focuses primarily on parameter b in the discussion, as it plays a dominant role in shaping the directional reflectance characteristics under the given conditions. We have added this explanation to the manuscript to improve the transparency and physical interpretation of the model parameters.

Please see p. 3, lines 99-105, in the revised manuscript.

References

Ding, A., Ma, H., Liang, S., and He, T.: Extension of the Hapke model to the spectral domain to characterize soil physical properties, *Remote Sensing of Environment*, 269, 112843, 2022.

Hapke, B.: Bidirectional reflectance spectroscopy 7: the single particle phase function hockey stick relation, *Icarus*, 221, 1079–1083, 2012.

4. In the current manuscript, the distinction between input parameters and retrieved parameters is not always clear, particularly in some tables. It is recommended to clearly differentiate these parameter types and ensure consistent terminology throughout the manuscript.

Response 4: We thank the reviewer for this helpful suggestion. In the revised manuscript, we have clarified the distinction between input and retrieved parameters throughout the text. Specifically, input parameters refer to variables prescribed in the forward simulations, whereas retrieved parameters are estimated through inversion.

To improve clarity, we have revised the relevant tables and descriptions to explicitly distinguish these parameter types. In addition, Table 1 provides a summary of the input parameters for each soil model, ensuring a consistent and transparent presentation. We have also ensured consistent terminology across the manuscript. These revisions improve the clarity and reproducibility of the modeling framework.

Table 1. Input parameters of each soil model.

Models	Input parameters
Hapke-HSR (Ding et al., 2022)	SZA, VZA, RAA, b , A_0 , A_1 , A_2 , A_3 , and f
Improved Hapke-HSR (dry soil)	SZA, VZA, RAA, b , M , and χ_{soil}
MARMIT-2 (Dupiau et al., 2022)	δ , L and ε
Hapke-HSR model and MARMIT-2	SZA, VZA, RAA, b , M , χ_{soil} , δ , L and ε

The meanings of the parameters

- (1) Solar zenith angle (SZA)
- (2) View zenith angle (VZA)
- (3) Relative azimuth angle (RAA)
- (4) Coefficient of the scattering phase function (b)
- (5) Soil spectral fitting parameters (A_0 , A_1 , A_2 and A_3)
- (6) Equivalent water thickness (f)
- (7) Soil particle size and shape-dependent parameter (M)
- (8) The imaginary component of the soil complex refractive index (χ_{soil})
- (9) Volume fraction of the soil particles (δ)
- (10) Thickness of the water layer (L)
- (11) Surface coverage fraction of water (ε)

Please see p. 8, lines 201-208, in the revised manuscript.

References

- Ding, A., Ma, H., Liang, S., and He, T.: Extension of the Hapke model to the spectral domain to characterize soil physical properties, *Remote Sensing of Environment*, 269, 112843, 2022.
- Hapke, B.: Bidirectional reflectance spectroscopy 7: the single particle phase function hockey stick relation, *Icarus*, 221, 1079–1083, 2012.

5. The study is mainly conducted under a fixed observation geometry. It would be beneficial to further discuss how this assumption may influence the model results, as well as the applicability of the model under different viewing and illumination conditions.

Response 5: We thank the reviewer for this valuable comment. We agree that the assumption of a fixed observation geometry should be further discussed in terms of its influence on the results and the applicability of the proposed model.

In the revised manuscript, we have added a clarification regarding this aspect. In this study, a fixed observation geometry is adopted primarily because the available datasets do not provide multi-angular measurements. This simplification allows us to focus on evaluating the spectral performance of the model under controlled conditions. We note that the proposed Hapke-HSR + MARMIT-2 framework is not restricted to a fixed geometry. The Hapke-HSR component explicitly accounts for viewing and illumination angles, and therefore the coupled model can be directly extended to simulate soil reflectance under varying geometries. However, the use of fixed geometry in this study may limit the characterization of angular effects and the full assessment of BRDF behavior.

We have added a discussion to clarify that future work will incorporate multi-angular datasets to further evaluate and validate the model under varying observation conditions. This extension will allow a more comprehensive assessment of the model's applicability in real remote sensing scenarios. We appreciate the reviewer's suggestion, which has helped improve the discussion of model applicability and limitations.

Please see p. 8, lines 201-208, in the revised manuscript.

6. Although the validation results are generally convincing, the study could be further strengthened by including comparisons with additional models (e.g., GSV or similar approaches), or by providing more discussion on the differences between the proposed model and existing methods.

Response 6: We thank the reviewer for this constructive suggestion. We agree that additional comparisons and discussion with existing models would further strengthen the manuscript.

In the revised version, we have expanded the discussion to provide a clearer comparison between the proposed Hapke-HSR + MARMIT-2 model framework and other representative soil reflectance models. Specifically, we discuss the differences

in model structure, physical assumptions, and applicability, with particular emphasis on models such as GSV and BSM models. We note that models such as GSV and BSM are primarily semi-empirical or hybrid approaches, which are effective in describing spectral reflectance variability but do not explicitly represent directional scattering processes. In contrast, the proposed framework is based on a physically consistent coupling of directional scattering (Hapke-HSR model) and moisture-related absorption processes (MARMIT-2 model), enabling joint simulation across both spectral and angular domains. In addition, we clarify that the primary objective of this study is to develop and validate a unified physically based framework. Therefore, the comparison focuses on models that explicitly represent moisture processes (e.g., MARMIT-2 model), which provides a more direct and meaningful benchmark for evaluating model improvements.

We have incorporated this discussion into the manuscript to improve the positioning of the proposed model relative to existing approaches. We appreciate the reviewer's suggestion, which has helped enhance the completeness and clarity of the study.

Please see p. 20, lines 489-492, in the revised manuscript.

7. The coupling strategy between the improved Hapke-HSR model and the MARMIT-2 model is not entirely clear. It would be useful to clarify whether the parameters (b , M , δ , L , ϵ) are retrieved sequentially or simultaneously, and to provide a clearer description of the integration workflow.

Response 7: We thank the reviewer for this insightful comment. We agree that the coupling strategy and parameter estimation procedure should be described more clearly.

The coupling between the improved Hapke-HSR and MARMIT-2 models is implemented in a sequential manner at the model level. Specifically, the improved Hapke-HSR model is first used to simulate dry soil reflectance under different observation geometries, based on scattering-related parameters (e.g., b , M). The resulting dry soil reflectance is then used as input to the MARMIT-2 model, which simulates wet soil reflectance by accounting for moisture-related parameters (e.g., δ , L , ϵ). This structure follows the physical process in which scattering from dry soil is

subsequently modified by moisture-related absorption and refraction effects. Regarding parameter estimation, two strategies can be applied depending on the application scenario. In this study, the parameters can be retrieved simultaneously using the coupled Hapke-HSR + MARMIT-2 model, allowing all five parameters (b , M , δ , L , ϵ) to be jointly optimized. Alternatively, a sequential inversion strategy can also be adopted, in which the dry soil parameters (b , M) are first estimated using the Hapke-HSR model, followed by the inversion of moisture-related parameters (δ , L , ϵ) using the MARMIT-2 model.

To improve clarity, we have revised the manuscript to explicitly describe this integration workflow and to clarify the relationship between the sequential coupling of the models and the flexible parameter inversion strategies (Figure 1). These revisions make the modeling framework more transparent and easier to interpret. We appreciate the reviewer’s suggestion, which has helped improve the clarity of the methodological description.

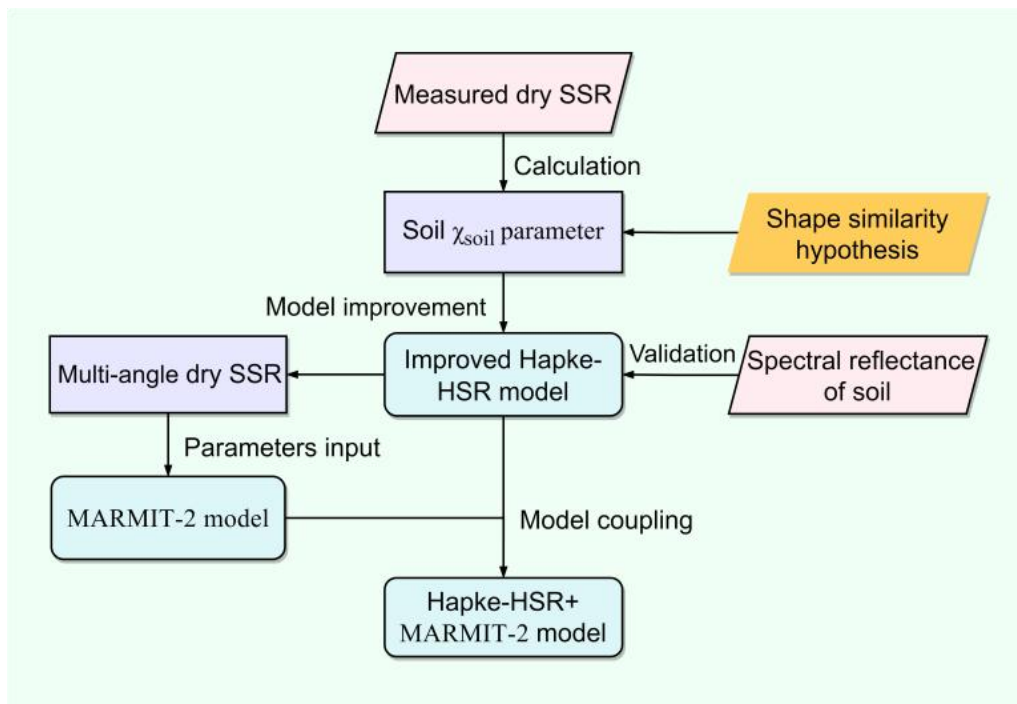


Figure 1: The workflow of the improved Hapke-HSR model and the coupled MARMIT-2 model.

Please see p. 6, lines 178-181, in the revised manuscript.

8. In the Discussion, the manuscript attributes the decrease in model accuracy (when using averaged χ_{soil}) mainly to differences in soil types. However, soil properties (e.g., organic carbon content, texture) can vary significantly even within the same soil type and may strongly affect spectral absorption. It is suggested to consider incorporating soil property variability or grouping spectrally similar soils when defining χ_{soil} , which may further improve model performance.

Response 8: We thank the reviewer for this valuable suggestion. We agree that soil properties such as organic carbon content and texture can vary significantly within the same soil type and may influence spectral absorption characteristics.

In the current study, the use of an averaged χ_{soil} is intended as a simplified representation to evaluate the overall performance of the coupled model under varying moisture conditions. While this approach captures the general behavior across different soils, it does not explicitly account for within-type variability, which may contribute to the observed decrease in accuracy. We agree that incorporating soil property variability or grouping spectrally similar soils represents a promising direction for improving model performance. In the revised manuscript (Section 5.X), we have added a discussion to clarify this limitation and to highlight potential improvements. In particular, defining χ_{soil} based on soil-specific properties or spectral similarity classes could provide a more accurate representation of absorption behavior. However, implementing such a strategy requires detailed soil property information or clustering analyses, which are beyond the scope of the present study. Our primary objective is to establish a unified physical framework, and the use of averaged χ_{soil} serves as a first-order approximation. We have revised the manuscript to explicitly acknowledge this limitation and to outline future work aimed at incorporating soil-specific or spectrally grouped parameterization strategies.

We appreciate the reviewer's suggestion, which has helped improve the discussion of model applicability and future development.

Please see p. 17, lines 408-416, in the revised manuscript.