

Parameter estimation of river incision models of soft sedimentary rocks — a case study on the Kamikita Coastal Plain, northeast Japan

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Abstract. ~~To predict long-term future landscape evolution, u~~Understanding of the river incision model, ~~which is crucial~~ ~~the m~~ ~~for predicting long-term landscape evolution~~ ~~ain driver of continental erosion, is especially important.~~ For the bedrock channel incision model (detachment-limited (DL) model: erosion rate $E = KA^mS^n$ where A is drainage area, S is channel gradient, ~~and~~ ~~K , m , n are parameters~~), parameters (K , m , and n) can be estimated ~~by the~~ ~~via~~ slope-area analysis if E is known. ~~Based on the worldwide basin-averaged denudation rates of~~ ~~Using~~ ¹⁰Be ~~denudation rate~~ ~~concentrations~~, previous studies ~~globally~~ compiled the parameter values for variable lithology. However, ~~the scarcity of~~ ~~limited~~ data ~~availability~~ for ~~the~~ soft sedimentary rock ~~restricts~~ ~~limits~~ the applicability of global ~~seale~~ compilation. In addition, measuring the ¹⁰Be concentration in sedimentary rock is ~~difficult~~ ~~challenging~~ in humid and tectonically active regions ~~like~~ Japan. To address this, slope-area analysis was conducted ~~in the Kamikita Coastal Plain, Japan, where~~ ~~bedrock~~ lithology (~~sedimentary rocks of~~ Miocene to Pleistocene ~~sedimentary rocks~~) and uplift rate ($\sim 0.2 \text{ mm y}^{-1}$ for the past 300 ka) are assumed to be uniform. ~~Parameter values were estimated based on~~ ~~River incision rates were~~ ~~approximately~~ derived ~~approximately~~ from ~~widely distributed~~ marine terraces (MIS 5e, 7, 9, and 11) ~~which are widely distributed in the area.~~ For six target rivers, DL-like behaviour was confirmed in the limited ~~upstream and midstream~~ areas located upstream of the alluvium distribution. ~~Except for small rivers of~~ ~~$A < 25 \text{ km}^2$,~~ ~~†~~ ~~The~~ ~~reference~~ ~~concavity index~~ ~~m/n was~~ ~~0.44 ± 0.10~~ ~~between~~ ~~0.35 and 0.6,~~ ~~which is the~~ ~~typical~~ ~~range~~ for steady-state channels. ~~Across the~~ ~~m/n range of 0.4–0.6,~~ ~~the~~ ~~The~~ ~~estimated~~ ~~exponent~~ ~~n~~ ~~consistently~~ ~~exhibited~~ ~~nonlinearity~~ ~~was~~ ~~nonlinear~~, ranging between 1.14 to 1.34 ~~and 2~~, which is consistent with the previous global compilations. ~~This~~ ~~This~~ ~~observed~~ ~~nonlinearity~~ ~~can~~ ~~be~~ ~~explained~~ ~~by~~ ~~likely~~ ~~reflects~~ ~~transient~~ ~~landscape~~ ~~responses~~ to past sea-level changes, ~~which~~ ~~generated~~ ~~causing~~ ~~slope-break~~ knickpoints at similar elevations. Finally, the ~~estimated~~ erosion coefficient K ~~was~~ ~~estimated~~ ~~to~~ ~~be~~ ~~$(10^{-5} \text{--} 10^{-6}) \text{ m}^{0.1} \text{ y}^{-1}$~~ . ~~For the main lithology of late Pliocene and early Pleistocene sedimentary rock,~~ the estimated K almost agreed with the global relationship ~~between~~ ~~K~~ ~~and~~ ~~with~~ unconfined compressive strength q_u ($K \propto 1/q_u^2$), supporting the significant influences of bedrock lithology on K .

1 Introduction

Prediction of long-term ~~future~~ landscape evolution is indispensable for social planning ~~and~~ ~~infrastructure management~~, such as radioactive waste ~~repositories~~ ~~disposal~~, ~~and~~ mine waste ~~disposal~~ ~~deposits~~, and landfills. ~~In several fields, long-term assessments spanning~~ ~~10^4 – 10^5 years are required to confirm geological stability;~~ for instance, carbon dioxide capture and storage ($\sim 10,000$ years: IPCC, 2005; Alcalde et al., 2018) and radioactive waste disposal (100,000 years for intermediate-level waste: e.g., SSM, 2008; NRA, 2021). To ensure reliable risk assessment for these facilities, including the evaluation of future erosion depths and their effects on groundwater flow systems, past landscape evolution since the Late Quaternary (i.e., the last glacial–interglacial cycle since 125 ka) must be elucidated. ~~For example, the disposal facility for intermediate or high level radioactive waste must be evaluated to ensure that it will remain isolated from the biosphere and humans for at least several thousand years (IAEA, 2011) to one million years (STUK, 2013).~~ Among various landscape processes, river incision is one of the main drivers of landscape evolution and can cause ~~large~~ ~~considerable~~ vertical erosion (e.g., Whipple, 2004). Therefore, a quantitative understanding of river incision models and their parameters is essential for ~~robust~~ ~~making~~ long-term projections of erosion depth.

40 River incision models are broadly classified into two types: the detachment-limited (DL) model and the transport-limited (TL) model. The DL model assumes that all particles eroded by the river are immediately removed from the system. The long-term river incision rate E [$L T^{-1}$] is controlled by shear stress or stream power per unit width on the bed (e.g., Howard and Kerby, 1983; Howard, 1994; Whipple and Tucker, 1999). Under idealized circumstances, E is described as a simple function of both channel slope S [-] and upstream drainage area A [L^2] as follows:

$$45 \quad E = KA^m S^n, \quad (1)$$

where m and n are positive constants ($\theta = m/n$ is the concavity index). K [$L^{1-2m} T^{-1}$] is the erosion coefficient reflecting the combined influences of bed erodibility, climate and downstream changes in channel hydraulic geometry. On the other hand, the TL model assumes that sediment flux Q [$L^2 T^{-1}$] transported by the river is limited by its transport capacity (Henderson, 1966; Hergarten, 2020):

$$50 \quad Q \propto A^{m+1} S^n. \quad (2)$$

The values of S and A can be easily calculated based on digital elevation model (DEM). Therefore, if E is known and the environment (i.e., tectonics, lithology, and climate) is uniform, the river incision parameters (m , n , and K) can be estimated from the field data and the DL model (e.g., Kirby and Whipple, 2012; Lague, 2014). When using data from rivers with different drainage areas, a reference concavity θ_{ref} , generally the regional mean of observed θ , is used for comparison purposes.

55 In recent decades, river incision parameters have been estimated in various regions (e.g., Kirby and Whipple, 2012; Lague, 2014; Harel et al. 2016; Hilley et al., 2019; Adams et al., 2020; Desormeaux et al., 2022; Hu et al., 2023; Marder and Gallen, 2023; Ott et al., 2023) and global compilations have been conducted using this data. For example, Lague (2014) estimated the parameters for 10 basins globally distributed and found that $n \sim 2$ (ranging from 1 to 4) using $\theta_{ref} = 0.45$. Harel et al. (2016) compiled the parameter values at 59 study areas of various lithology, climatic, and tectonic settings. Using $\theta_{ref} = 0.5$, a mean ($\pm 1\sigma$) n of 2.7 (± 2.9) was suggested. Moreover, Haag and Schoenbohm (2025) indicated that the global compiled K in Harel et al. (2016) is inversely proportional to the square of unconfined compressive strength q_u : $K \propto 1/q_u^2$.

60 However, there are two problems with the above studies. First, previous research ($q_u \geq 15$ MPa: Haag and Schoenbohm, 2025) lacks data of soft sedimentary rocks. This is especially important for tectonically active regions like Japan where over 50% of the surface geology consists of Paleogene and Neogene sedimentary rocks (NUMO, 2021). Nevertheless, river incision parameters and its relationship with q_u have not been discussed for soft sedimentary rocks with $q_u = 1-10$ MPa. Second, previous parameter estimations have primarily relied on basin average denudation rates derived from cosmogenic radionuclides (CRN), such as beryllium-10 (^{10}Be) in quartz grains from river sediments. However, it is difficult to measure the ^{10}Be concentration for sedimentary rocks in humid and tectonically active regions like Japan due to the lack of quartz and the diversity of topographic deformation and sedimentation-erosion processes (AIST, 2016). In such regions, the ^{10}Be measurement is appropriate for quartz-rich rocks, such as granite (e.g., Takahashi et al., 2023). Furthermore, CRN-derived denudation rates typically reflect relatively short-term durations, which are roughly inversely proportional to the incision rate (Lague, 2014). Therefore, CRN-derived denudation rates reflect average timescales of 10^5 years in active regions with erosion rates of several $mm\ ky^{-1}$, but only 10^2-10^3 years in tectonically active regions with several $m\ ky^{-1}$ erosion (von Blanckenburg, 2006). Another conventional approach is to~~Parameter estimations have been also conducted~~ assuming a topographic steady state (e.g., Snyder et al., 2000; Kirby and Whipple, 2001; Duvall et al., 2004). However, many environments have not yet attained a steady state (Bishop et al., 2005; Campforts and Govers, 2015; Vanacker et al., 2015; Armitage et al., 2018). Especially in coastal areas, ~~which are preferable for geological disposal in terms of safe waste transportation (METI, 2017),~~ the landscape has been drastically changed due to periodic sea-level change. Thus, as Lague (2014) noted, deriving locally measured incision rates from dated terraces remains one of the least potentially biased methods for quantifying long-term incision. However, only~~Very~~ a few studies (e.g., Lague, 2014) address this issue by using reach incision rates based on fluvial strath terraces.

To address these issues, we performed slope-area analysis in the Kamikita Coastal Plain, Japan, where bedrock lithology (sedimentary rocks of Miocene to Pleistocene) and uplift rate are assumed to be uniform. Parameter values were estimated based on river incision rates approximately derived from marine terraces (Marine Isotope Stages (MIS) 5e, 7, 9, and 11) widely distributed in the area. First, we estimated the validity range of the DL model and θ for six target rivers. Then, we estimated the river incision parameters using the erosion rates approximately evaluated from the marine terraces. Finally, we confirmed the validity of the estimated parameter values by comparing them with those from previous global compilations.

2 Study area

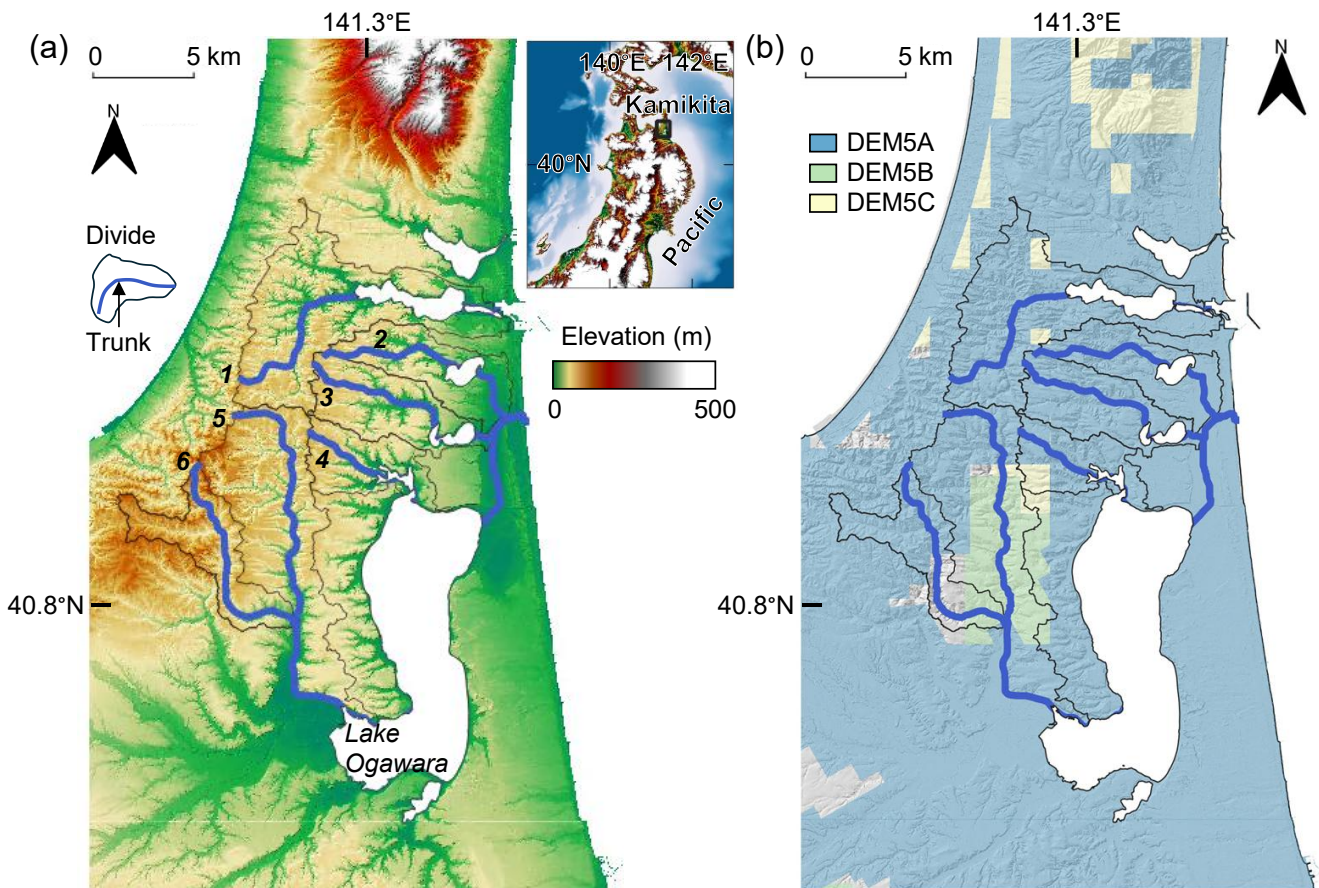


Figure 1: (a) Topography and (b) provided area of 5 m DEM by Geospatial Information Authority of Japan. For area where 5 m DEM is not provided, 10 m DEM was used.

The Kamikita Plain in northeast Japan is a vast coastal plain approximately $30 \times 50 \text{ km}^2$, located along the coastline of Pacific Ocean (Fig. 1a). In this region, Middle and Late Pleistocene marine terraces are widely preserved at multiple levels (Fig. 2a): the Takadate terrace (MIS 5e), the Tengudai terrace (MIS 7), the Shichihyaku terrace (MIS 9), and the higher terrace (MIS 11) (AIST, 2016). The chronology has been estimated using various techniques: sediment rate chronology (Miyachi, 1985; Koike and Machida, 2001), optically stimulated luminescence (AIST, 2015, 2016), and tephra and phytolith stratigraphy (Kuwabara, 2004, 2007, 2009; Matsu'ura et al., 2019). Based on these previous studies, Matsu'ura et al. (2019) concluded that the uplift rate of the Kamikita Plain (around Lake Ogawara) has been constant at approximately 0.2 mm y^{-1} over the last 300 ka. Geological units of the Kamikita Plain are summarised by Kudo et al. (2020) (Fig. 2b). Bedrock was formed in the early to middle Miocene: the Takahoko Formation, sedimentary rock (16.6–13.1 Ma), which is mainly composed of pumice tuff, sandstone, and mudstone (Inohara et al., 2008), and the Tomari Formation, volcanic rock (16.6–15 Ma), characterized by basaltic to andesitic lavas and pyroclastic rocks (Kudo et al., 2020). Sedimentary rock units of late Pliocene to early Pleistocene,

105 the Hamada ~~formation~~ Formation and the Katchi ~~formation~~ Formation, which primarily consist of sandstone and siltstone (Nemoto and Ujiie, 2009), ~~overlies~~ overlay the bedrock. These sedimentary rocks are covered by terrace deposits of middle to late Pleistocene and alluvium. The mean annual rainfall in this region is around 1,300 mm (JMA, 2026).

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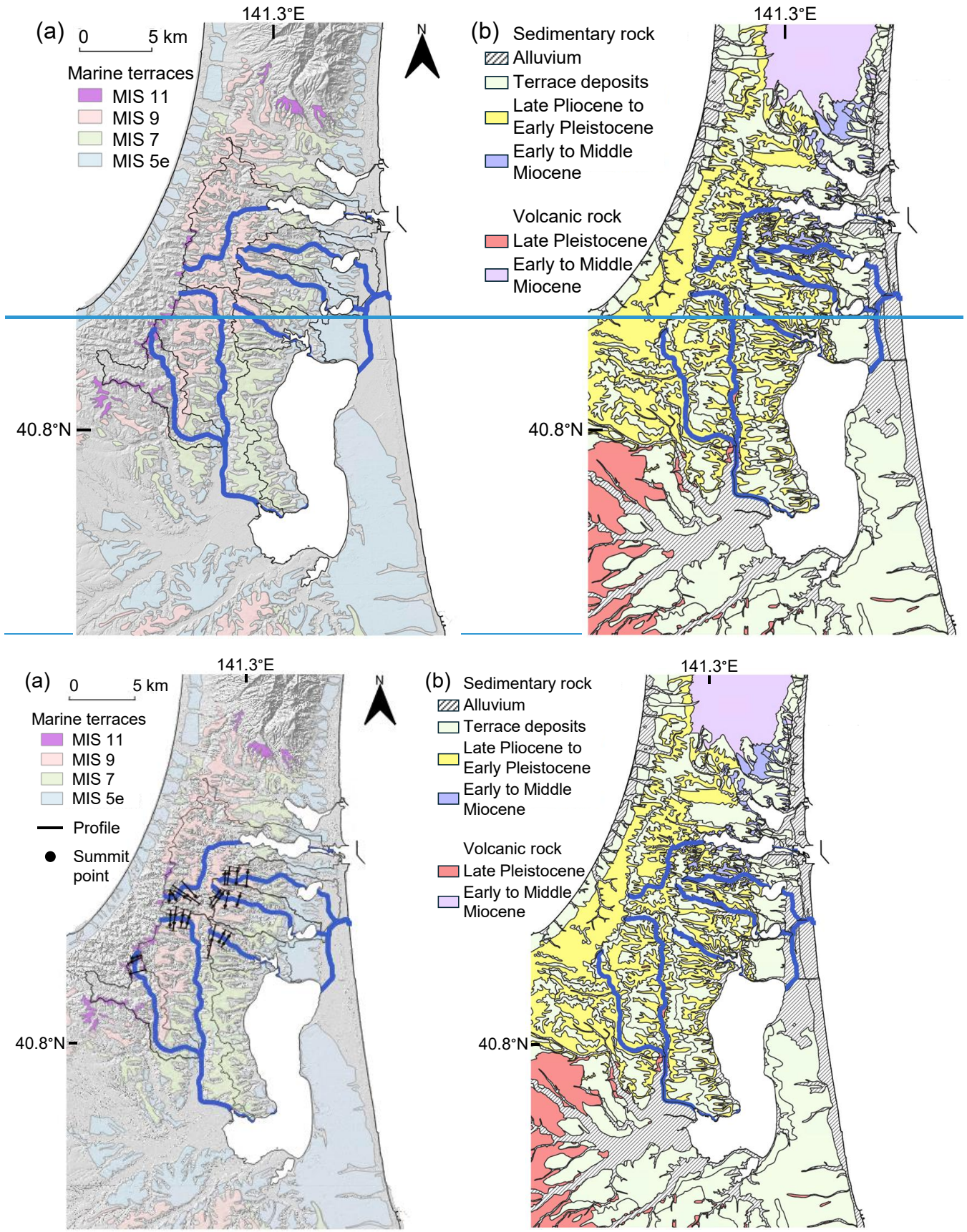


Figure 2: (a) Marine terraces and (b) geology of the study area. Marine terraces are based on Koike and Machida (2001). Geological map is based on the 1:200,000 scale geologic map (AIST, 2025). The summit levels extracted from profiles of the marine terrace surfaces were used for erosion rate estimates. Geological units are based on Kudo et al. (2020).

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The Continental Divide is located in the western part of the study area. The valley is deep on the west side of the divide and shallow on the east side. The rivers on the east side dissect the marine terraces and flow into the Pacific Ocean. Downstream the rivers, coastal lagoons such as Lake Ogawara are located, which were formed by sea-level fall during the Last Glacial Maximum and by subsequent development of sandbanks during the post-glacial period. In this study, we examined six streams flowing into the Pacific Ocean (1: the Togusari River, 2: the Ishiwatari River, 3: the Hiranuma River, 4: the Uchinuma River, 5: the Doba River, 6: the Gandosawa River) (Table 1), whose lithologic (sedimentary rock of Miocene to Pleistocene) and tectonic conditions (uplift rate $\sim 0.2 \text{ mm y}^{-1}$) can be assumed to be uniform. Note that the rivers No. 2–6 are tributaries of the Takase River, which has a drainage area of 867 km² (MLIT, 2006) and flows from the Hakkoda Mountains located west of the study area. Volcanic rocks are distributed throughout the region and the tectonics differ from that of the Kamikita Plain; therefore, the Takase River was excluded from the scope of this study.

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Table 1: Target rivers. Drainage area and length include coastal lagoons.

No.	River	Drainage Area (km ²)	Length (km)	Valley-head elevation (m)
1	Togusari River	55.9	18.7	64.8
2	Ishiwatari River	23.0	12.9	67.9
3	Hiranuma River	24.6	12.7	74.7
4	Uchinuma River	16.2	7.1	63.7
5	Doba River	74.4	22.2	73.5
6	Gandosawa River	74.4	20.2	93.5

3 Methods

As previous research has shown (e.g., Whipple and Tucker, 2002; Whipple, 2004), most bedrock channels are mixed bedrock-alluvial channels partially covered by alluvium. In this case, the river profile consists of colluvial, bedrock, and alluvial sections (Fig. 3a). In the bedrock section where the DL model holds, Eq. (1) can be rewritten as the stream power law (Hack, 1957; Flint, 1974):

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$$S = k_s A^{-\theta}, \quad (3)$$

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where $k_s = (E/K)^{1/n} [L^{2\theta}]$ is the steepness index. This means that in the DL model, the log-transformed slope-area plot can be fitted with a linear regression (Fig. 3b). Since channel transitions from bedrock to alluvial (i.e., DL to TL) or colluvial processes typically cause changes in channel slope (e.g., Whipple and Tucker, 1999, 2002; Stock et al., 2005), sections can be identified using the slope-area plot (Wang et al., 2017). Above a critical drainage area (A_c), colluvial processes, such as debris flows and land sliding, are dominant (Wobus et al., 2006). Below A_c , the fluvial processes dominate. Both the bedrock and alluvial sections exhibit a descending gradient with increasing drainage areas (Whipple and Tucker, 2002). However, the transition to alluviated conditions cause a sudden reduction in channel gradient (Wobus et al., 2006).

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Channels may contain knickpoints, which can be classified into two categories: vertical-step knickpoints and slope-break knickpoints (Fig. 3c). Vertical-step knickpoints correspond to sudden changes in elevation, such as waterfalls, and can be identified as spikes on the slope-area plot. These knickpoints are generally caused by channel-scale heterogeneities such as bounding faults (e.g., Kirby and Whipple, 2012; Liu et al., 2020).

145 Herein, we focused on ~~S~~slope-break knickpoints because they represent channel response to, ~~on the other hand, develop~~
~~spatially or temporally, which corresponds to~~ regional-scale perturbations, such as ~~trends of~~ lithologic heterogeneity and sea-
 level fall (e.g., Haviv et al., 2010; Kirby and Whipple, 2012; Boulton et al., 2020). Unlike vertical-step knickpoints, these
features mark a fundamental shift in the channel gradient~~In this study, we focused on the slope-break knickpoints, which~~
~~cause leading to an~~ abrupt changes in flow conditions. By identifying these slope-break knickpoints, we can evaluate how
 150 regional-scale factors influence river incision parameters.

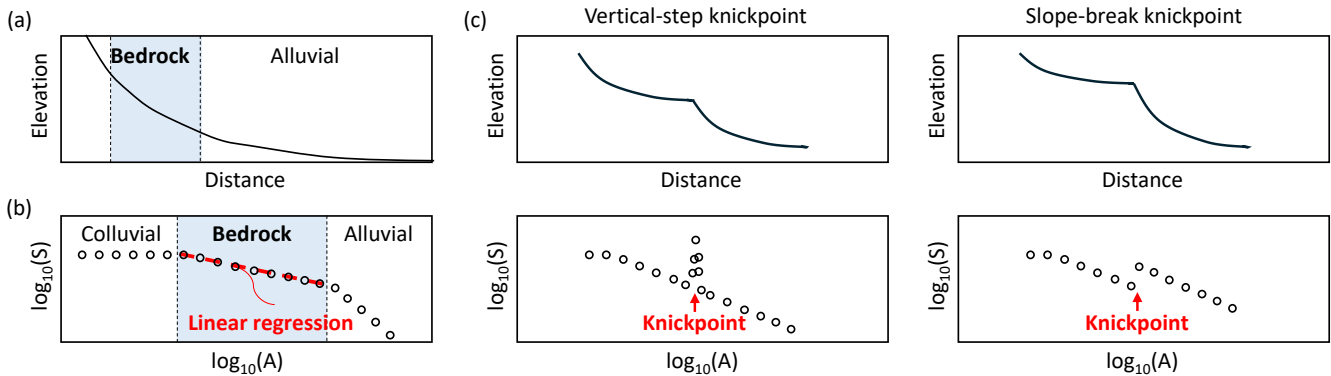


Figure 3: Schematic of (a) river profile, (b) slope-area plot, and (c) knickpoints (revised from Snyder et al. (2000) and Whipple (2013)).

155 This study estimated river incision parameters in three consecutive steps. First, sections exhibiting DL-like behaviours were identified from slope-area plots. Their validity was confirmed by comparing them with the alluvium distribution. We used a 5 m gridded digital elevation model (DEM), which is provided by the Geospatial Information Authority of Japan (Fig. 1b). Three types of 5 m DEM collected by different methods were combined: DEM5A (airborne LiDAR measurements), DEM5B and
 160 DEM5C (photogrammetry). There is also a 10 m DEM covering the entire country, which is created by interpolating topographic contour map with 10 m intervals. However, such a DEM can cause problems, such as artificial knickpoints due to interpolation errors or short-circuit meander bends in a river profile (Wobus et al., 2006). Therefore, we used the higher-resolution 5 m DEM. In areas where 5 m DEM is not available, such as the southeastern part of the Doba River and the middle of the Gandosawa River, 10 m DEM was bilinearly resampled to 5 m point spacing. Using the ArcHydrology toolbox (Tarboton
 165 et al., 1991), streams were extracted by applying a D8 flow routing algorithm and the trunk was defined from the Horton-Strahler number. To circumvent noise, previous research (Wobus et al., 2006; Whipple et al., 2007) has indicated that DEM-derived river profiles require the implication of some smoothing algorithms, such as a moving-window average. Furthermore, calculating the averaged channel slopes at a certain elevation interval or logarithmic bins of drainage area (log-bin averaging) was suggested (e.g., Snyder et al., 2000; Wobus et al., 2006). In previous studies utilizing the USGS 10m DEM (root mean
 170 square error = 2.44 m; Gesch, 2007), Wobus et al. (2006) used moving-window sizes of 200 or 400 m, whereas Whipple et al. (2007) suggested an optimal window size of 250 m. The DEM datasets used herein possess a maximum measurement error (standard deviation) of 5 m, with specific accuracies ranging from~~The measurement error (standard deviation) of the DEM is~~
~~0.3 m (DEM5A), 0.7 m (DEM5B), 1.4 m (DEM5C), and to 5 m (10m DEM) (GIA, 2026). To ensure analytical consistency across the entire catchment and account for the largest measurement error, we smoothed elevation data using a 500-m moving
 175 window~~~~In this study, we smoothed elevation data over a 500-m moving window~~ and calculated averaged slopes on 5 m contours and log-bin averaged slopes. We verified that no artificial knickpoints were generated at DEM tile boundaries.
 In the second step, we calculated the channel concavity index from the integral approach within the detachment-limited reaches (Perron and Royden, 2013):

$$\chi = \int_{x_b}^x \left(\frac{A_0}{A(x)} \right)^\theta dx, \quad (4)$$

$$180 \quad z(x) = z(x_b) + \left(\frac{E}{KA_0^m} \right)^{1/n} \chi, \quad (5)$$

where x [L] is the horizontal upstream distance from an outlet; x_b [L] is the distance at the outlet (in this study, $x_b = 0$); and z [L] is elevation. The validity of the bedrock sections identified by slope-area plots is confirmed again by the linearity of χ plot. Using a reference basin area of $A_0 = 1 \text{ m}^2$, the concavity index (θ) and knickpoint locations were estimated using a statistical segment-fitting algorithm (Mudd et al., 2014). In this algorithm, the optimal θ is evaluated in χ space by minimizing the corrected Akaike Information Criterion (AICc) across all possible contiguous channel segments.

$$185 \quad \text{AICc} = \text{AIC} + \frac{2k(k+1)}{N-k-1}, \quad \text{AIC} = 2k + \frac{\text{RSS}}{\sigma_z^2} \quad (6)$$

where N is the number of channel nodes, s is the number of segments ($k = 2s$), RSS is the residual sum of squares between data points and regression lines, and σ_z is the standard deviation of elevation measurements, including geomorphic noise. In this study, we used DEM5A (standard deviation: 0.3 m) in detachment-limited reaches, and σ_z was conservatively set to 0.6 m. A bootstrapping method was employed with 1,000 independent trials to evaluate the robustness of the results. In this method, channel nodes were randomly skipped using a uniform distribution ranging from 0 to $2 \times n_{sk}$. Following Gailleton et al. (2019), n_{sk} was set to 1. θ_{ref} was determined using a collinearity test that minimized the sum of AICc values across all analyzed rivers. Knickpoints were defined as boundaries between adjacent segments. Knickpoint type was classified using the slope ratio of regression lines (S_{ratio}) and elevation difference (Z_{jump}) across these boundaries: large Z_{jump} with a minimal change in S_{ratio} indicates a vertical-step knickpoint, whereas a significant change in S_{ratio} with negligible Z_{jump} indicates a slope-break knickpoint. In accordance with Gailleton et al. (2019), knickpoints were extracted using the optimal θ specific to each river. we estimated θ as the value providing the best linear fit between χ and z . $k_{sn} = SA^{\theta_{ref}}$ was calculated using θ_{ref} , the regional mean of θ . Knickpoints were extracted as the local minimum points of k_{sn} with respect to χ (Gailleton et al., 2019).

In the third step, the values of n and K were estimated. Within the detachment-limited reaches, the relationship between E and k_{sn} is expressed as:

$$200 \quad E = K k_{sn}^n \quad (7)$$

Taking the natural logarithm of Eq. (7) allows n and K to be estimated via the regression analysis of E and k_{sn} (e.g., Leonard et al., 2023):

$$\ln(E) = n \ln(k_{sn}) + \ln(K), \quad (8)$$

205 where n and $\ln(K)$ represent the slope of the regression line and the intercept, respectively. by regression analysis of logarithms of E and k_{sn} ($\ln(E) = a \ln(k_{sn}) + b$ where $a = n$, $b = \ln(K)$). River terraces are not identified in the study area (Koike and Machida, 2001). Since the target rivers incising marine terraces have smooth and concave-up profiles, long-term incision rate E was approximately calculated based on the height of marine terraces:

$$E = (z_t - z_r - d)/T_t, \quad (9)$$

210 where z_t [L] is the summit level of the marine terrace; z_r [L] is the present river profile; d [L] is the thickness of tephra and loess; and T_t [T] is the formation age of the river. The summit level of the marine terrace was reconstructed by interpolating the highest elevations from multiple topographic profiles extracted from preserved marine terrace surfaces (Fig. 2a; see Figs. S1–S6 for detailed maps and profiles). Where summit levels were comparable on both banks of the river, their average value was used. T_t was approximated as the terrace age where valley head is located.

215 To ensure spatial consistency, E and k_{sr} were compared at equal intervals of 200 m along the river channels, following the
 approach for parameter estimation using strath terraces by Lague (2014). To account for uncertainties in E (Eq. (9)), a Monte
 Carlo simulation with 10,000 iterations was performed based on the inherent probability distribution of all input parameters
 (Table 2). Elevation uncertainty was modeled as a Gaussian distribution based on DEM precision (0.3 m for DEM5A) in the
 detachment-limited reaches. The uncertainties in terrace age (T_i) and tephra thickness (d) were represented using uniform
 220 distributions derived from field observations.
 T_i values were adapted from those reported by Matsu'ura et al. (2019) for the Kamikita Coastal Plain: 398 to 410 ka (MIS 11),
 318 to 324 ka (MIS 9c), 230 to 235 ka (MIS 7e), 212 to 220 ka (MIS 7c), and 116 to 132 ka (MIS 5e). Furthermore, d values
 were derived from ~~Due to volcanoes in the nearby districts, observed data of tephra layers and loam (tephric loess) interealated~~
~~with tephra layers of various ages are observed~~ in the study area. The main tephra layers are as follows (Kudo, 2023): Hakkoda
 225 second-stage (Hkd2: 0.19–0.29 Ma) and White Pumice (WP: 210 ka) erupted ~~from~~ the Hakkoda Volcano; Orange Pumice
 (OrP: 166 ka) and Towada-Ofudo (To-Of: 36 ka) erupted from the Towada Volcano; and Toya (106 ka) erupted from the Toya
 Volcano. Based on outcrop observations at seven locations, AIST (2015, 2016) has identified the tephra and loam thickness
 as 11.4 m (sampled at Onadesawa) and 10.5 m at Kanaya for MIS 11; 14 m at Shichihyaku and 7 m at Kamiyoshita for MIS
 9; 6 m at Hotozawa for MIS 7; 2 m or 4 m at Neinuma for MIS 5e (the outcrop locations: Fig. S7). For the MIS 5e marine
 230 terraces, Koike and Machida (2001) indicated that the thickness of cover deposit layers ~~are is~~ 2 m at four points to 3 m at one
 point. ~~Based on previous research, d is assumed to be 12 m for MIS 11, 10 m for MIS 9, 5 m for MIS 7, and 2 m for MIS 5e~~
~~terraces.~~ Note that Kudo (2023) provides an approximate estimate of the spatial distribution of tephra thickness for the Towada
 Volcano. However, this information is not provided for other volcanoes. ~~Therefore~~ Accordingly, we a uniform thickness was
~~assigned to each terrace stage (Table 2) did not consider regional differences in the thickness of covering layers.~~ This Monte
 235 Carlo approach enables the evaluation of the parameter reliability by accounting for uncertainties in summit level, riverbed
elevation, tephra thickness, and marine terrace age.

Table 2: Probability distribution used for uncertainty analysis of erosion rate.

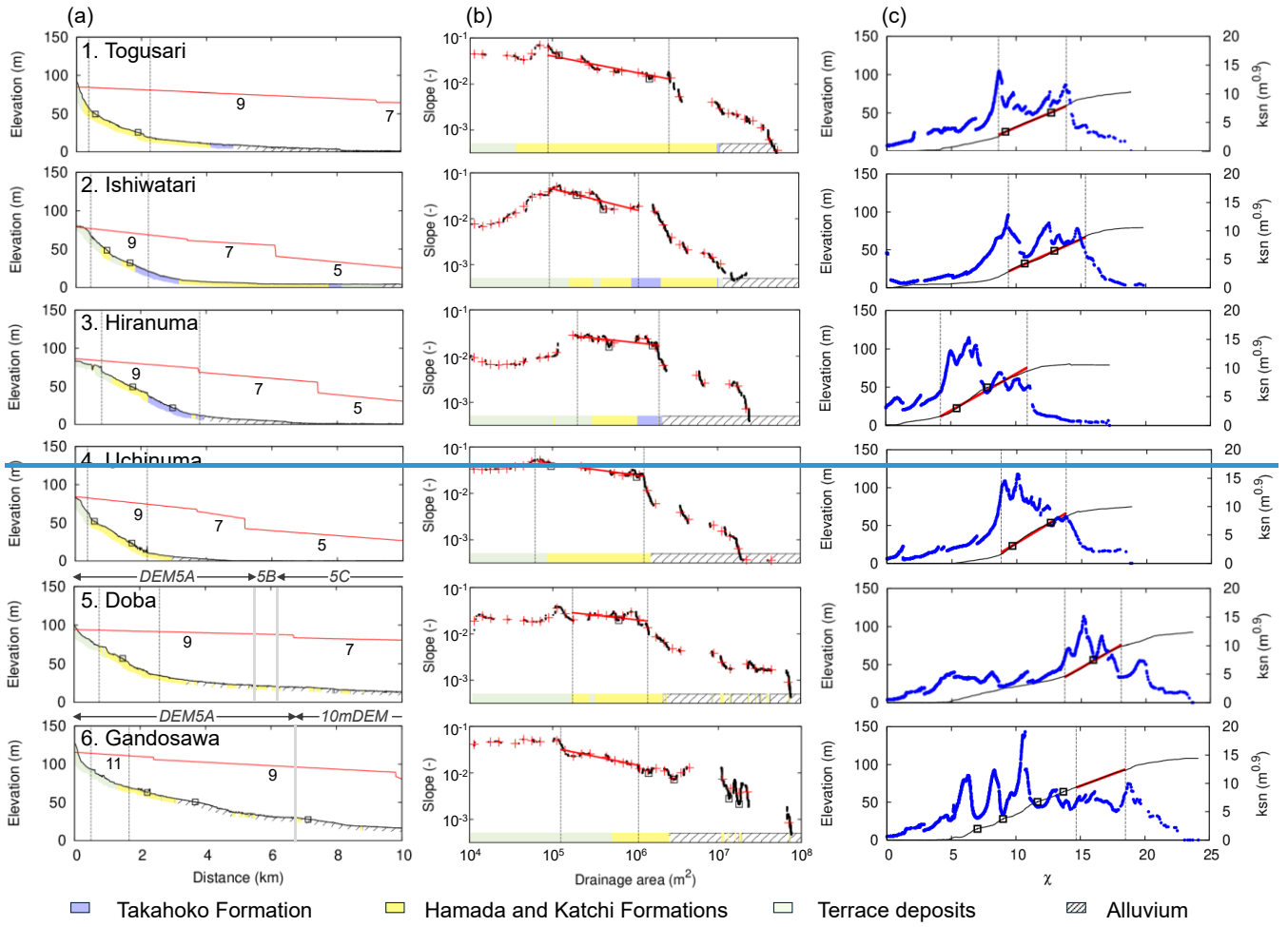
Parameter	Assigned distribution	Values
z_t Summit level (m)	Gaussian	Mean: reconstructed summit level σ : standard deviation within 200 m interval
z_r Riverbed (m)	Gaussian	Mean: elevation extracted from DEM σ : 0.3 m (standard error of DEM5A)
d Tephra thickness (m)	Uniform	MIS 9: [7.0, 14.0], MIS 11: [10.5, 11.4]
T_i Marine terrace age (ka)	Uniform	MIS 9c: [318, 324], MIS 11: [398, 410]

240 4 Results

4.1 Channel profiles

Longitudinal river profiles, slope-area plots, and χ plots for six rivers are shown in Fig. 4. A_{cr} is confirmed at ~ 0.1 km² for all
 rivers, which is consistent with earlier studies (e.g., Montgomery and Foufoula-Georgiou, 1993; Stock and Dietrich, 2003;
 Wobus et al., 2006). In the slope-area plots (Fig. 4b), all rivers exhibit an approximately linear descending gradient with
 245 increasing drainage areas. The gradients suddenly reduce around $A = 1$ –10 km² upstream of the alluvium distribution. This is
 consistent with previous research on mixed bedrock and alluvial channels (Snyder et al., 2000; Wobus et al., 2006, Wang et
 al., 2017), reflecting a transition to alluviated conditions due to the sea level rise during the Holocene. Therefore, the studied

rivers are considered to be mixed bedrock and alluvial channels, and the sudden decrease in the channel gradient corresponds to the transition from erosive bedrock channels (DL) to depositional alluvial channels (TL).



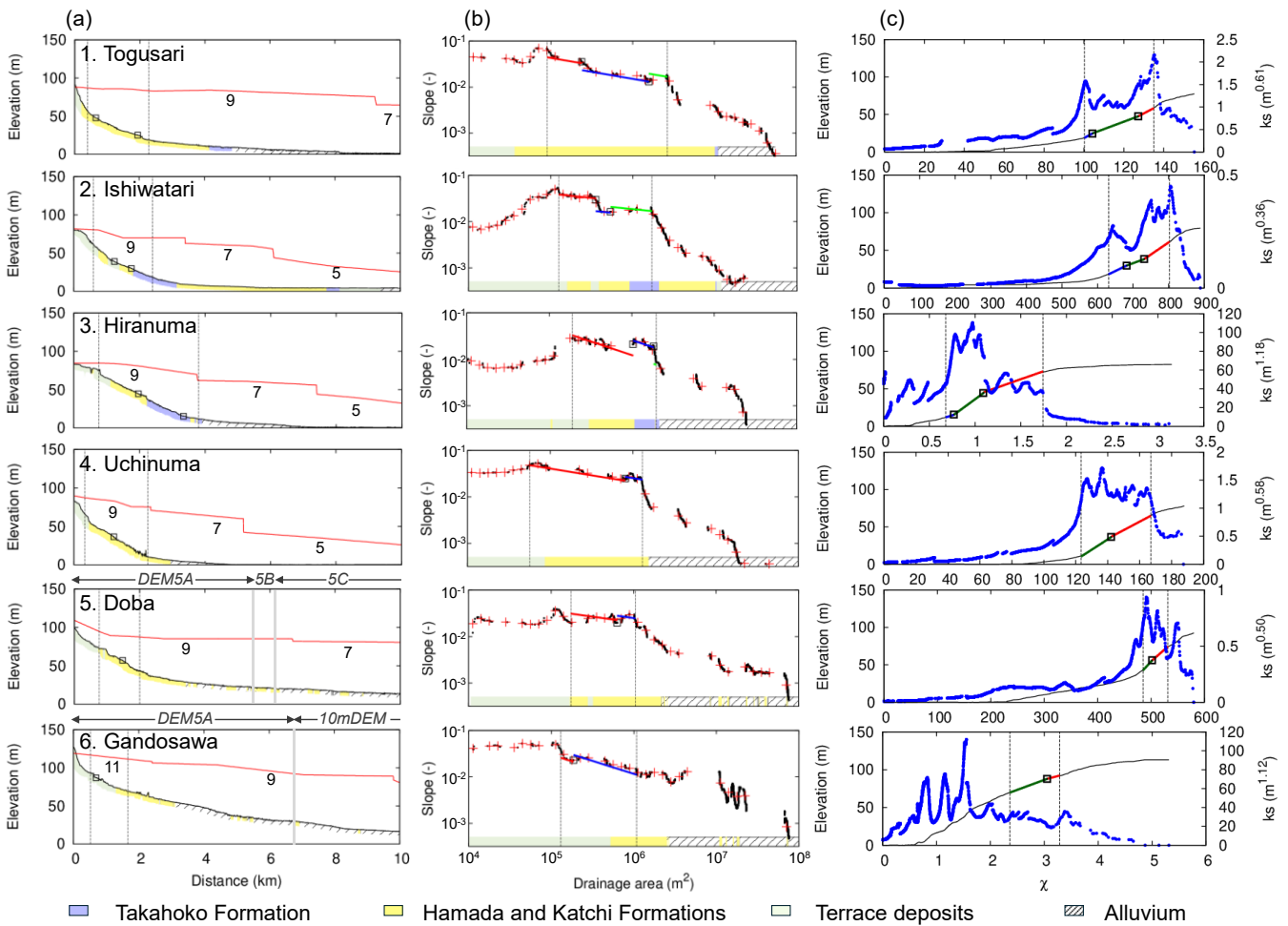


Figure 4: Stream profile analysis of the study area. (a) Longitudinal profile (black line) and the elevation of marine terraces (red line) with Marine Isotope Stages. Squares denote knickpoints. Gray lines for rivers No. 5 and 6 indicate the boundaries of DEMs other than DEM5A (LiDAR 5m DEM). (b) Slope-area plot. Average channel slopes are calculated on 5-m contours (black point) and by the log-bin averaging method (red mark). (c) χ plot (black line) with k_s (blue point) based on the reference concavity of each river ($\theta = 0.45$) with k_{sn} (blue point). In all graphs, dashed lines and red color bold lines (red, blue, and green) correspond to the bedrock section and its regression line.

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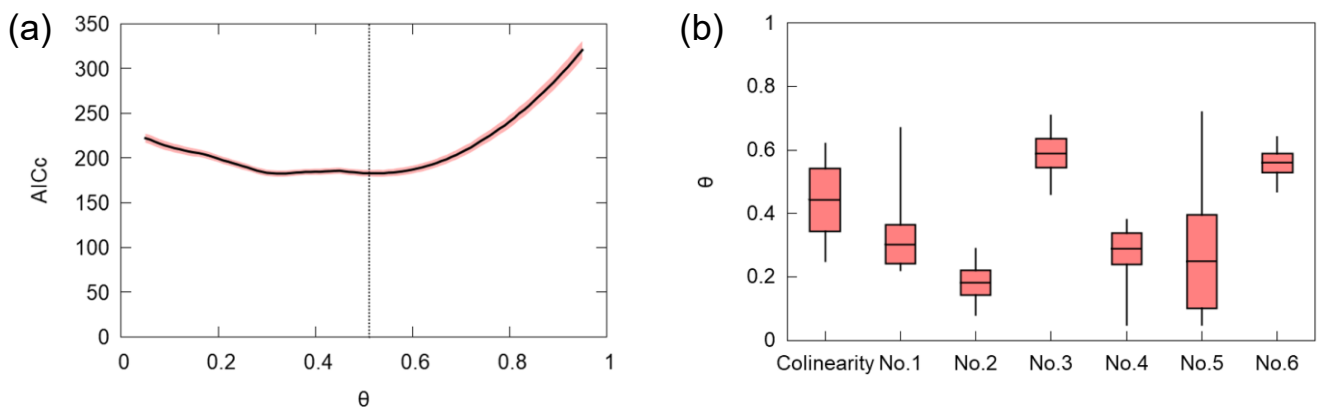
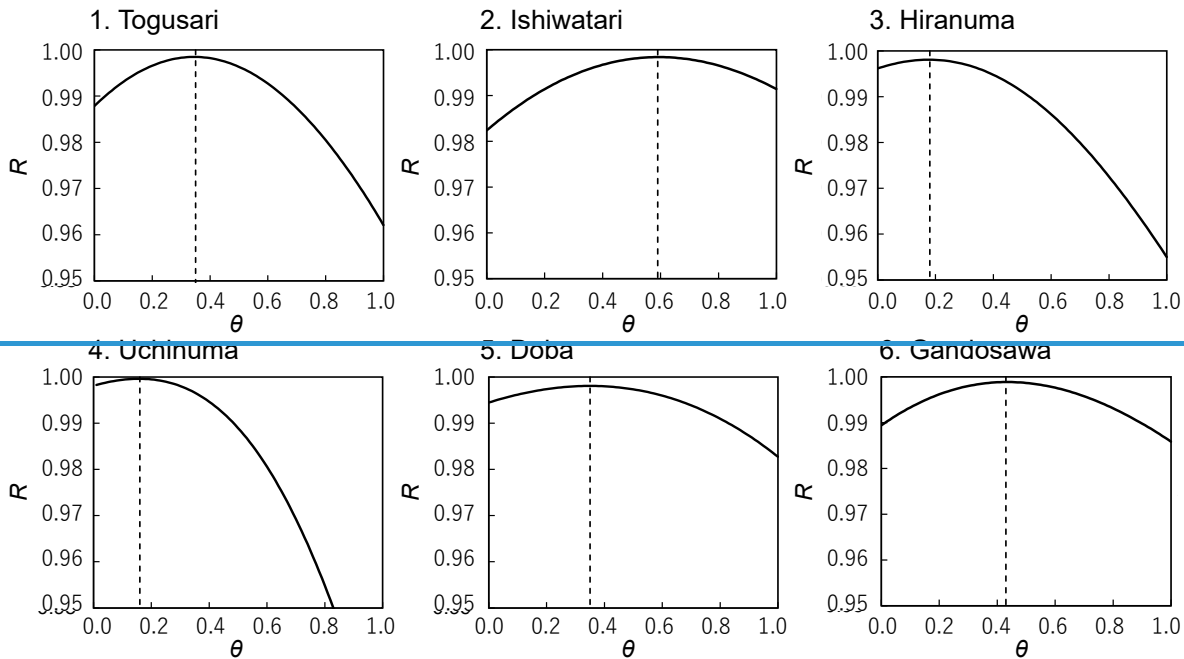
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Estimated values of concavity index θ . The θ values estimated for detachment-limited reaches are summarised in Table 23 and Fig. 5. The optimal θ values for each river range from 0.18 to 0.59 (Fig. S8 shows the AICc values). Meanwhile, θ_{ref} was estimated to be 0.44 ± 0.10 (standard deviation) using the collinearity test (Fig. 5b). For all rivers, optimal θ achieved the linear regression of χ plots with high correlation coefficients of $R \sim 1$ (Fig. 5), which manifests DL-like behaviour in the upstream and midstream sections. Although θ ranges from 0.11 to 0.59, θ is approximately 0.4 except for small rivers of $A < 25 \text{ km}^2$ (No. 2, 3, 4), which lies within the general range of steady-state channels ($\theta = 0.35\text{--}0.6$; Kirby and Whipple, 2012). Notably, θ of river No. 6, whose formation age (MIS 11) is the oldest, is and closely aligns with close to 0.45, at the typical value for reference concavity of 0.45 index (e.g., Wobus et al., 2006). Snyder et al. (2003) indicates that even considering sea-level changes, a quasi-steady-state condition has been achieved in the upper parts of the channel. Therefore, although small channels the target rivers tend to fluctuate from their mouths to their divides reflecting sea-level change, it can be assumed that the other rivers they have approached to the quasi-steady state in the upstream section. However, as θ_{ref} can impact the estimation of river incision parameters, in subsequent calculations, we evaluate analyzed k_{sn} using based on θ_{ref} values of 0.45, 0.4, 0.5, and 0.6 to ensure robustness.

275

Table 23: Formation ages and concavity indices (with standard deviation).

No.	1	2	3	4	5	6
Formation Age	MIS 9	MIS 9	MIS 9	MIS 9	MIS 9	MIS 11
θ	<u>0.30</u> \pm <u>0.06</u>	<u>0.18</u> \pm <u>0.04</u>	<u>0.59</u> \pm <u>0.04</u>	<u>0.29</u> \pm <u>0.05</u>	<u>0.25</u> \pm <u>0.15</u>	<u>0.56</u> \pm <u>0.03</u>
	0.35	0.59	0.18	0.16	0.35	0.44



280 **Figure 5: (a) AICc values for the regional collinearity test and (b) the distribution of optimal θ for regional and individual river basins. In (a), the solid line and shaded red area indicate the mean and $\pm 1\sigma$ (standard deviation) interval for 1,000 bootstrap trials. In (b), the whiskers indicate the range between minimum and maximum values, while the boxes represent the mean and $\pm 1\sigma$ interval. Correlation coefficients of χ plots based on a range of θ .**

285 **Table 4 and Figure 6 shows a map of the extracted knickpoints and their locations on the map from the χ plots (Fig. 4c). All knickpoints are classified as slope-break knickpoints and do not correspond to the boundaries between different DEM datasets. Except for the second knickpoint of river No.2, the knickpoints are not located near lithological boundaries. Instead, they are distributed at similar elevations (around E.L. 25 m and 50 m), which do not correspond to the lithology or the boundary of the different DEMs. This suggests that they can be base-level-fall related upstream-migrating knickpoints. In the Sanriku Coast,**

290 **approximately 50 km south of the study area, Ogami (2015) indentified upstream-migrating knickpoints in multiple rivers which were formed during the sea-level highstands during MIS 5e, 7, 9, and 11. The knickpoints in the study area may have**

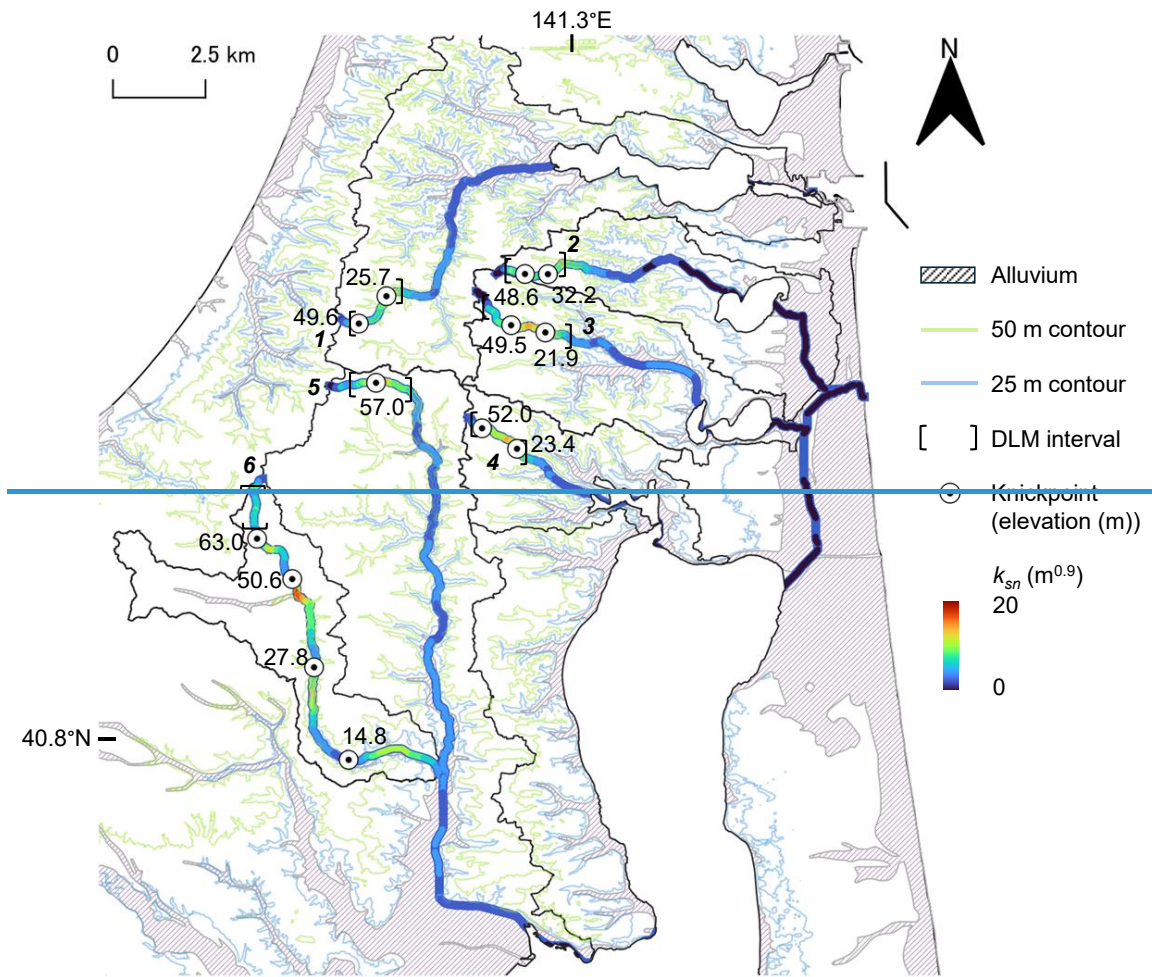
been formed for the same reason. Note that in river No. 6, which formed earlier than the other rivers (MIS11), a knickpoint is observed at a higher elevation of 88 m. This knickpoint could have been formed during a preceding sea-level cycle.

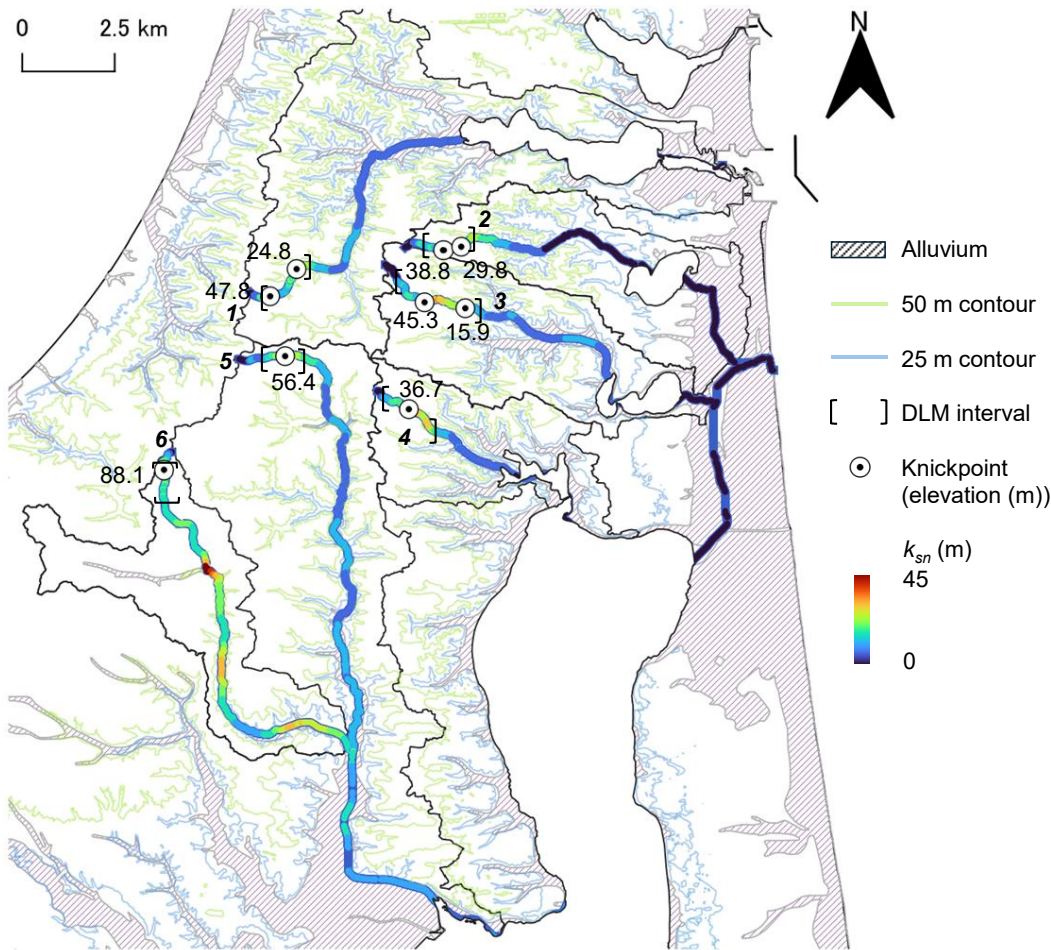
The second knickpoint of river No.2 is located near the boundary between the Hamada and Katchi Formations and the Takahoko Formation (Fig. 4a). As discussed in Sect. 5.2, the Takahoko Formation exhibits higher N -values (80–137) compared with the Hamada and Katchi Formations (50–63). This contrast in rock hardness likely contributed to the formation of this lithological knickpoint. The same boundary is also located near the first knickpoint of river No.3; however, because its elevation is close to 50 m, this knickpoint might be affected by both the lithological difference and sea-level changes.~~Note that lithological boundaries do not correspond to the knickpoints (Fig. 4). This is in agreement with the small difference in q_u of the bedrock, around several MPa, as discussed in Sect. 5.2. Another possible reason is sediment cover and tool effects (Yamanashi and Naruse, 2025). However, while the influence of the sediment requires further investigation, the cover and tool effects by riverbed gravel is considered to be insignificant for the target soft sedimentary rocks with $q_u = 1–10$ MPa.~~

Table 4: Extracted knickpoints.

<u>River No.</u>	<u>Knickpoint</u>	<u>Elevation (m)</u>	<u>Z_{jump} (m)</u>	<u>S_{ratio} (-)</u>
<u>1</u>	<u>Slope-break</u>	<u>47.8</u>	<u>-0.05</u>	<u>0.71</u>
	<u>Slope-break</u>	<u>24.8</u>	<u>0.05</u>	<u>1.49</u>
<u>2</u>	<u>Slope-break</u>	<u>38.8</u>	<u>-0.13</u>	<u>0.53</u>
	<u>Slope-break[†]</u>	<u>29.8</u>	<u>0.02</u>	<u>1.34</u>
<u>3</u>	<u>Slope-break</u>	<u>45.3</u>	<u>-0.71</u>	<u>2.10</u>
	<u>Slope-break</u>	<u>15.9</u>	<u>-0.04</u>	<u>0.44</u>
<u>4</u>	<u>Slope-break</u>	<u>36.7</u>	<u>-0.50</u>	<u>1.22</u>
<u>5</u>	<u>Slope-break</u>	<u>56.4</u>	<u>0.11</u>	<u>1.24</u>
<u>6</u>	<u>Slope-break</u>	<u>88.1</u>	<u>0.01</u>	<u>1.41</u>

[†]This knickpoint is located approximately 50 m upstream from the lithological boundary (Hamada/Katchi and Takahoko Formations) along the river channel.





310 **Figure 6: Knickpoints (points with elevation (m)) and 25 m and 50 m contours (blue and green lines) within the detachment-limited reaches. Color along the rivers demonstrates k_{sn} ($\theta_{ref}=0.5$).**

4.2 River incision parameters

315 We then compared the long term river incision rate E and the river steepness k_{sn} were compared based on log bin averaged data at 200-m intervals along the river channels (Figs. 7a–c). Using the data of all the rivers A, we confirmed that there is a positive correlation between E and k_{sn} was observed across all θ_{ref} values. The with a correlation coefficient ($\text{of } R$) increased with increasing θ_{ref} , ranging from = 0.37 to 0.5946. Across the range of $\theta_{ref}=0.4$ –0.6, the estimated n values consistently indicated a nonlinear relationship ($n > 1$) and fell within a narrow range from 1.14 to 1.34. In contrast, the estimated K varied over a considerably wider range from 4.2×10^{-7} to 1.3×10^{-5} . The 90% confidence intervals for these parameters were n parameter = values were obtained as n of [0.94, 1.28], 1.54 [0.86, 1.15], 2.22 [1.46], and [1.10, 1.36], (90% confidence interval) and K of = [1.0 $\times 10^{-6}$, 2.9 $\times 10^{-6}$], 2.4 $\times 10^{-6}$ [5.61.1 $\times 10^{-7}$], 1.02.9 $\times 10^{-5}$] ($\text{m}^{\text{0+}} \text{y}^{\text{-1}}$) and [2.5 $\times 10^{-7}$, 7.8 $\times 10^{-7}$] for $\theta_{ref}=0.4, 0.5$ and 0.6, respectively (Fig. 8 shows the results obtained at $\theta_{ref}=0.5$).

325 Table 3–5 shows the parameter values obtained for each river. Although a relatively high correlation could be confirmed for rivers No. 3–6 ($R \geq 0.65$), values of K vary by almost nearly one order of magnitude. Similarly, the values of n exhibited inter-river variability; $n > 1$ for rivers Nos. 3–6, whereas $n < 1$ for rivers Nos. 1 and 2. This variation may have been caused by the uncertainty of marine terrace surface z , along the rivers; high level marine terraces used for estimation of E (MIS 9 and MIS 11) are dissected by river and stream erosion (Fig. 2a). This can cause the large scatter in Fig. 7 for small incision rate, which correspond to upstream sections.

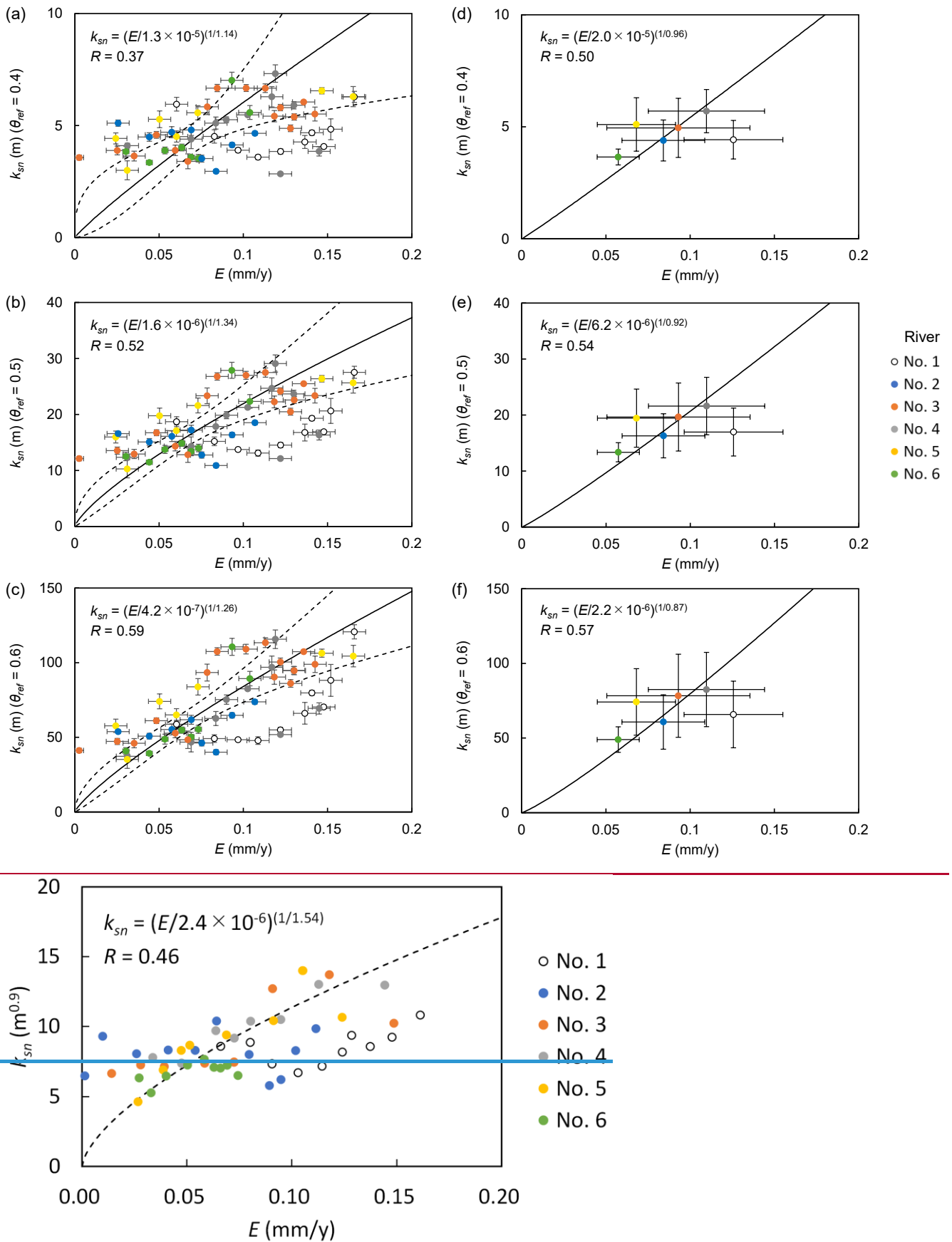


Figure 7: River incision rate versus channel steepness index k_{sn} within the detachment-limited reaches: (a-c) sampled at 200 m intervals and (d-f) averaged for each reach, both for $\theta_{ref} = 0.4, 0.5,$ and 0.6 . Error bars denote $\pm 1\sigma$. The bold and dashed lines indicate the regression lines and their 90% confidence intervals.

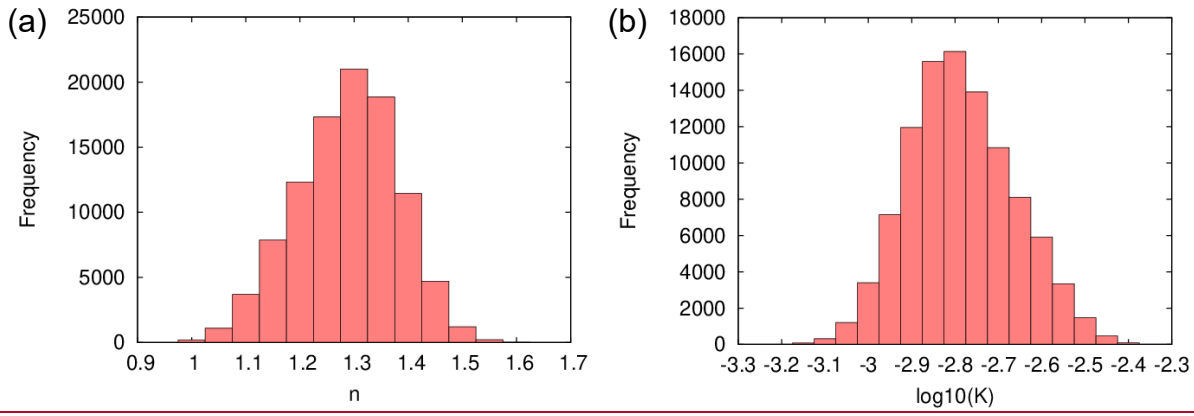


Figure 8: Probability distributions of n and K values estimated from 10,000 Monte Carlo simulations ($\theta_{ref} = 0.5$).

Table 35: River incision parameters (n and K) and correlation coefficient estimated for each river ($\theta_{ref} = 0.5$).

No.	1	2	3	4	5	6
n (-)	0.650.82	0.721.14	1.792.10	1.571.59	1.361.48	2.392.07
K ($m^{0.1}y^{-1}$)	1.8×10^{-5} 1.9 × 10 ⁻⁵	9.9×10^{-6} 3.7 × 10 ⁻⁶	3.6×10^{-7} 5.9 × 10 ⁻⁷	8.2×10^{-7} 2.5 × 10 ⁻⁷	1.1×10^{-6} 2.5 × 10 ⁻⁶	1.1×10^{-7} 1.0 × 10 ⁻⁶
R	0.440.41	0.310.16	0.570.76	0.920.94	0.790.92	0.660.65

5 Discussions

5.1 The value of n

In Sect. 4.2, the ~~results~~ estimated values of n (1.14 to 1.34) ~~indicate~~ show a nonlinear relationship ($n > 1$) between ~~incision rate E and river steepness k_{sn} across θ_{ref} of 0.4–0.6.~~ Specifically, for $\theta_{ref} = 0.5$ and 0.6 where $R \geq 0.5$, the 90% confidence interval for n lie entirely above 1.1. This nonlinear relationship is consistent with previous research conducted in various regions, where most estimates of n are between 1 and 2 (e.g., Ouimet et al., 2009; DiBiase et al., 2010; Lague, 2014; Harel et al., 2016; Campforts et al., 2020; Gallen and Fernandez-Blanco, 2021; Leonard et al., 2023). Additionally ~~In addition,~~ slope-break knickpoints occurred ~~we confirmed that the target rivers are impacted by eustatic sea level change at similar elevations across multiple rivers, which do not correspond to boundaries of lithology or different DEM datasets.~~

Meanwhile, when we compared the averaged E and k_{sn} values within detachment-limited reaches, n was approximately 1 across all θ_{ref} values ($n = 0.96, 0.92$, and 0.87 for $\theta_{ref} = 0.4, 0.5$, and 0.6 ; Figs. 7d-f). Furthermore, when river No.1 was excluded and only tributaries within the same drainage area (the Takase River) were compared, n was 1.05 with a higher R of 0.79.

These results suggest that the observed nonlinearity is likely an apparent effect caused by the presence of migrating knickpoints triggered by sea-level change (Pavano, 2025), rather than reflecting the intrinsic physics of river incision processes. Although most rivers yield $n > 1$, river Nos.1 or 2 exhibited $n < 1$. For river No.1, $n < 1$ possibly reflects the differences in watershed and downstream boundary conditions. Unlike other tributaries that flow into the large Lake Ogawara within the Takase River basin (867 km²), river No.1 has a small drainage area (55.9 km²) and flows into the small Takahoko pond. These contrasting base-level conditions can lead to different transient response at the catchment scale, causing fluctuations in n values. For river No.2, the presence of a lithological boundary, where the downstream lithology is more erodible than upstream lithology, may result in a lower n value.

Nevertheless, the intrinsic physics of river incision processes may also contribute to the observed nonlinearity. Such physical factors include shear stress thresholds, abrasion, plucking, and channel-width effects (Whipple et al., 2000), as well as tool and cover effects (Yamanashi and Naruse, 2025). The main target lithology comprises soft sedimentary rocks ($q_u \leq 3$ MPa,

as discussed in Sect. 5.2), where the tool and cover effects of riverbed gravel are likely minimal due to rapid disintegration into fine sediments; however, two possibilities remain: shear stress threshold and abrasion. In the small-scale catchments, the base flow discharge may be insufficient to exceed the critical shear stress required for bedrock incision. In addition, the abundance of sand derived from soft bedrock may cause suspended-load abrasion, which theoretically supports n values of $\sim 5/3$ (Whipple et al., 2000). The migration of fluvial knickpoints migration due to sea level change can cause the nonlinearity ($n > 1$) (Pavano, 2025). To reduce the effect of sea level change (i.e., fluctuation caused by the knickpoints), we compared k_{sn} and E averaged for each river in common with Pavano et al. (2016). As a result, an almost linear value of $n = 1.01$ was obtained (Fig. 8). In particular, the trend of rivers in the same basin (No. 2–6) are quite similar, with a correlation factor of $R = 0.97$. Even excluding river No.1, the estimated parameter value is similar: $n = 1.02$ [0.86, 1.18]. This suggests that past sea level fluctuations may account for the nonlinear relationship between k_{sn} and E . Note that the neglected effect of channel width is limited, since parameter estimation was performed in the limited upstream and midstream areas (Fig. 6). While the relative contributions of these transient responses and physical processes require further comprehensive investigation, the estimated parameters represent robust time-averaged behavior integrated over multi glacial–interglacial cycles.

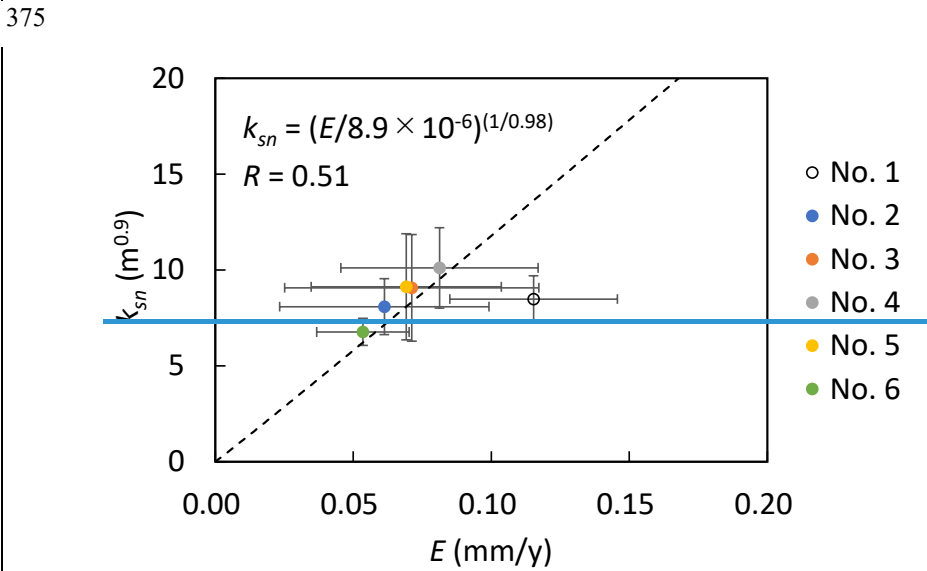


Figure 8: River incision rate versus channel steepness index k_{sn} (averaged for each river section). Error bars denote $\pm 1\sigma$.

5.2 The value of K

The value of K can vary by orders of magnitude due to lithology, climate, tectonics, hydraulic processes, and other environmental conditions (e.g., Murphy et al., 2016; Dibiase et al., 2018; Chen et al., 2019; Seybold et al., 2021). Among them, Haag and Schoenbohm (2025) confirmed a strong correlation ($R^2 = 0.89$) between global estimates for K based on ^{10}Be erosion rates (Harel et al., 2016) and Schmidt hammer-derived lithologic erodibility ($K \propto L_E$, $L_E = q_u^{-2}$: Sklar and Dietrich, 2001; Turowski et al., 2023); where L_E is the lithologic erodibility (Campforts, 2020) and q_u is unconfined compressive strength (Fig. 9).

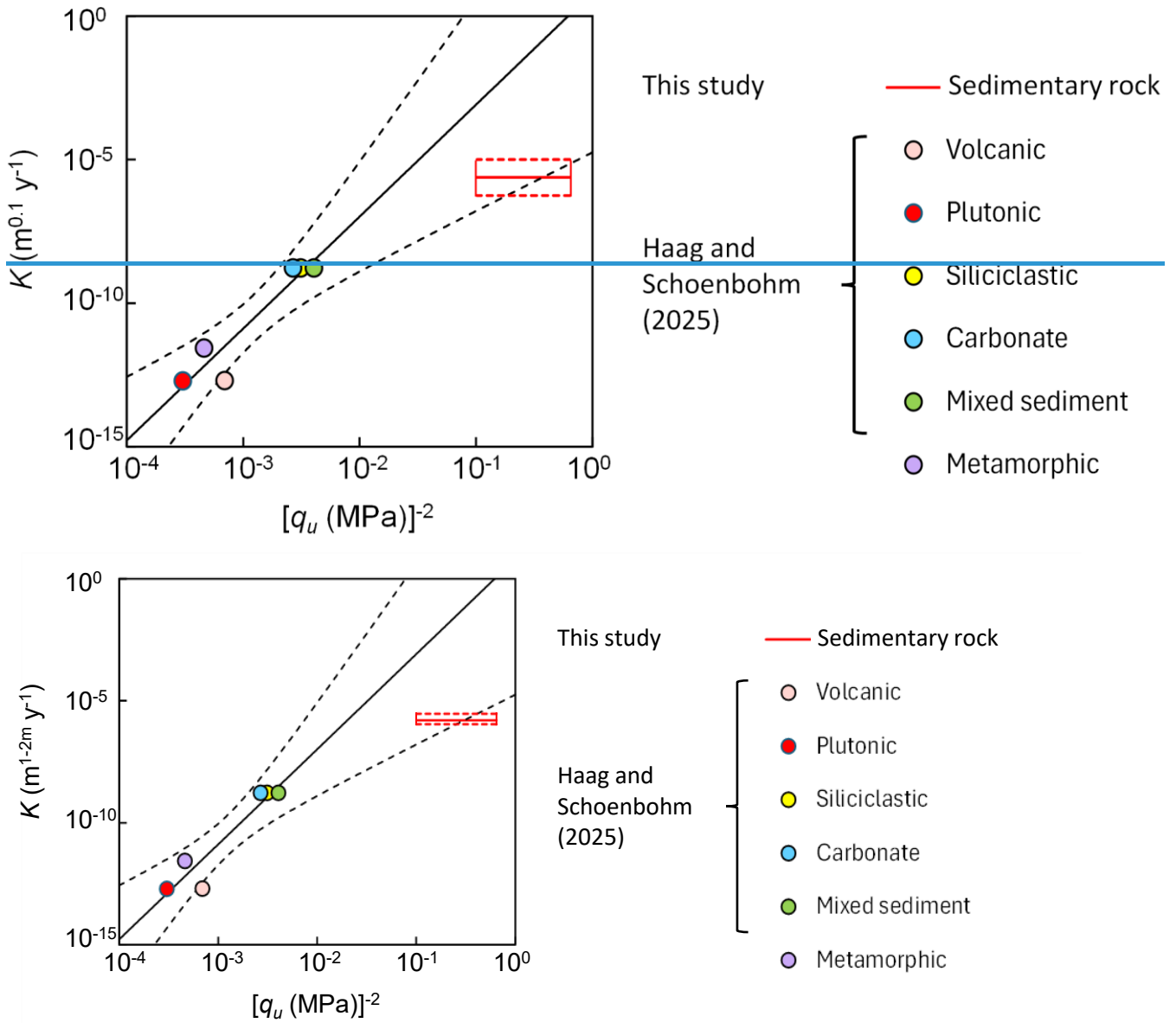
In this section, estimates for K for this study and the relationship between K and q_u in Haag and Schoenbohm (2025) were compared at the same θ_{ref} of 0.5. In the study area, measured N -values from previously studies for each lithology are as follows (Onuma, 1972; Planning Bureau, Ministry of Construction, Japan, 1997): 25–41 for the terrace deposits, 50–63 for the Hamada and Katchi formations, and 80–137 for the Takahoko formation. We then converted the N -values to q_u ($q_u = 25\text{--}50 N$ MPa: Japanese Geotechnical Society, 2015): 0.6–2.0 MPa for the terrace deposits, 1.2–3.1 MPa for the Hamada and Katchi formations, and 2.0–6.8 MPa for the Takahoko formation. For the Hamada and Katchi formations of which the studied rivers mainly consist, estimated values are almost within the 90% confidence interval of the regression line of Haag and Schoenbohm (2025) (Fig. 9). In Sect. 4.2, the estimated K value was 1.6×10^{-6} [1.1×10^{-6} , 2.9×10^{-6}]. Although rock strength in this study

is out of range of the previous study ($q_u = 10\text{--}100$ MPa), a strong correlation was observed between the results of this study and the data in Haag and Schoenbohm (2025) with $R^2 = 0.8584$. This highlights the significant influence of bedrock lithology on K , as indicated by previous research (e.g., Campforts et al., 2020; Haag and Schoenbohm, 2025).

However, the results of this study underestimate K (the regression line) in the work of Haag and Schoenbohm (2025). This discrepancy is likely caused by three potential reasons. First, as discussed in Sect. 5.1, the influence of sea-level changes may lead to an underestimation of K . One possible reason for this discrepancy is the effect of sea level change, which is discussed in Sect. 5.1. When comparing the average k_{sn} and E in the river section, which effectively smooths the transient knickpoint migration due to sea-level changes, the estimated K value increased to a larger K of 8.962×10^{-6} [4.777×10^{-78} , 1.751×10^{-4}], approaching $m^{0.1} y^{-1}$ was obtained (Fig. 8). Although the estimation uncertainty is large, the estimated K value is consistent with the relationship described by Haag and Schoenbohm (2025) (Fig. 9).

Second, another possible reason for the discrepancy may arise from is that we compared the use of present values of k_{sn} to compare with long-term average erosion rates. Since the target rivers have been formed gradually by incising the flat marine terraces, long-term average k_{sn} should be less than the present value. If the long-term average k_{sn} is half of present k_{sn} , the estimated K doubles without changing the n value.

Third, the cohesion of the main riverbed lithologies (the Hamada and Katchi Formations), which are semi-consolidated sedimentary rocks with $q_u = 1.2\text{--}3.1$ MPa that primarily consist of sandstone and siltstone (see Sect. 2), may function as a resistive factor. This cohesion increases the shear stress threshold and leads to the dissipation of stream power. Since standard mechanical indicators such as N -values often fail to fully capture the cohesive resistance inherent in these semi-consolidated units, the resulting K values may fall near the lower bound of the global relationship.



415 **Figure 9: Comparison between the results of this study and data of Haag and Schoenbohm (2025) for unconfined compressive strength q_u and erosional coefficient K . The box plot shows the best estimate and 90% confidence interval of our results based on the log-bin averaged data for all the rivers. The black line and dashed lines are the best estimate and 90% confidence interval shown in Haag and Schoenbohm (2025).**

6 Conclusions

420 This study estimated the river incision parameters for soft sedimentary rock, which are lacking in previous global compilations. The study targeted the Kamikita Coastal Plain, where bedrock lithology (sedimentary rocks of Miocene to Pleistocene) and uplift rate (approximately 0.2 mm y^{-1} over the past 300 ka) are assumed to be uniform. Parameter values were estimated using slope-area analysis based on river incision rates approximately derived from marine terraces (MIS 5e, 7, 9, and 11) widely distributed in the area. A summary of the main results is as follows.

- 425 (1) DL-like behaviour was confirmed in the limited upstream and midstream area ($A \geq 10^{-5} \text{ km}^2$) located upstream of the alluvium distribution for all rivers. Although the optimal θ value varied from 0.18 to 0.59 for each river, θ_{ref} was estimated to be 0.44 ± 0.10 . Except for small rivers of $A < 25 \text{ km}^2$, the concavity index m/n was between 0.35 and 0.6, which is falls within the typical range for steady-state channels (0.35–0.6).

- 430 (2) ~~Across the θ_{ref} range of 0.4 to 0.6, Exponent n was consistently exhibited a nonlinear relationship, ranging between 1.14 and 1.34~~ and 2, which ~~is consistent~~ aligns with the ~~previously~~ global compilation of 1 to 2. This nonlinearity can be due to past sea-level changes, causing slope-break knickpoints at similar elevations.
- 435 (3) For target rivers consisting mainly of late Pliocene and early Pleistocene sedimentary rock, erosion coefficient K was estimated to be $10^{-5-6} \text{ m}^{0.1} \text{ y}^{-1}$. Estimated K is almost within 90% confidence interval of the previous global relationship with unconfined compressive strength q_u ($K \propto 1/q_u^2$). This supports the significance of bedrock lithology on K , as previously reported (e.g., Campfort et al. (2020) and Haag and Schoenbohm (2025)).

These results represent long-term average erosion trends integrated over multiple glacial–interglacial cycles (since MIS 9 or 11). Consequently, the estimated n and K values are considered to reflect integrated values that account for past temporal variations in external forcing, such as climate and sea-level changes. For long-term safety assessments, such as those required for radioactive waste disposal, these parameters serve as a basis for time-dependent simulations of future landscape evolution over a glacial–interglacial cycle ($\sim 10^4$ to 10^5 years). Such simulations can be implemented using mixed DL and TL models, incorporating these time-varying external forcing and additional geomorphic processes, such as hillslope and coastal sediment transport (e.g., Salles et al., 2018). Using the estimated n and K values as the baseline, this approach could enable the reliable prediction of not only the maximum erosion depth, but also the spatial distribution of erosion across the site and its subsequent effects on groundwater flow systems. ~~Although the estimation of long term k_{sn} and E includes uncertainty (i.e., the formation age of river and the marine terrace surface), this study shows a similar trend of incision parameters for soft sedimentary rocks to more consolidated rocks in the previous global compilations. These results show the average trend of long term erosion after MIS 9 or MIS 11. The obtained parameters are beneficial to perform predictions of long term landscape evolution in the safety assessment of such as radioactive waste disposal. However, as we mentioned earlier, there is uncertainty due to the past sea level change and the estimation error of marine terrace elevations.~~ To further verify the estimated parameters, our next

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450 step will be the reproduction of past landscape evolution by numerical landscape evolution models using mixed DL and TL models.

Data availability

The DEM data is available at Geospatial Information Authority of Japan (<https://service.gsi.go.jp/kiban/>). The geological data is available at National Institute of Advanced Industrial Science and Technology (<https://gbank.gsj.jp/seamless/>).

455 Supplement

The supplement related to this article is available online at XXX.

Author contributions

S. Takai and T. Sanga designed research. S. Takai and T. Sanga performed research and analyzed data. S. Takai wrote the original manuscript draft and led editing. All authors reviewed and revised the manuscript and approved the final version.

460 Competing interests

The authors declare that they have no conflict of interest.

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