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Exploring the influence of wind stress and ocean stratification on sea surface temperature variability in the central tropical Pacific

by

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25 **Abstract.**

26 The El Niño-Southern Oscillation (ENSO) is a climate oscillation in the tropical Pacific sustained by a positive
27 feedback between sea surface temperature (SST) gradient and the Walker circulation, known as the Bjerknes
28 feedback. This results in an oscillation in the SST anomaly between warm (El Niño) and cold (La Niña) phases.
29 In traditional ENSO theories, the Bjerknes feedback amplifies an initial disturbance to produce a full El Niño or
30 La Niña, while the Sverdrup transport, caused by off-equatorial wind stress (WS) curl, determines the slow
31 charging of the equatorial Pacific through deepening of the thermocline. However, recent research has emphasized
32 the role played by the WS divergence in generating Kelvin waves that initiate El Niño. To account for changes in
33 the action of the WS over a varying ocean stratification, we introduce a dimensionless WS (DWS) and use the
34 Helmholtz decomposition to break it down into an irrotational (curl-free) and solenoidal (divergence-free)
35 component to study ENSO variability over the interannual-to-interdecadal time scale. We show that the irrotational
36 component of the DWS drives the thermocline dynamics on interannual time-scales, while the solenoidal
37 component, which drives Sverdrup transport, determines off-equatorial internal waves, referred to as q-waves, that
38 induce changes in the thermocline depth over longer time-scales. Furthermore, we develop an integral relation that
39 links the variability of the thermocline depth anomaly across the tropical Pacific to the Niño-3.4 index variability.
40 We conclude that the DWS irrotational component determines the Niño-3.4 index interannual variability, while
41 the solenoidal component determines its long-term variability.

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43



44 1. Introduction

45 Since the 17th century, Peruvian fishermen have observed a recurring anomalously warm current
46 along the Peruvian coast near Christmas. They named this phenomenon "El Niño" (the little boy) or
47 "Niño de Cristo" (Christ child). The first scientific mention of "El Niño" dates back to the early 1890s
48 (Carrillo, 1892). However, until the first half of the 20th century, it was believed to be a local occurrence
49 limited to the coasts of Peru and Ecuador. Since then, significant discoveries have been made about the
50 structure and time-space scales involved in El Niño. It is now understood to be a manifestation of the
51 strongest year-to-year climate fluctuation on our planet known as El Niño Southern Oscillation (ENSO).
52 A crucial aspect of the ENSO cycle is the positive feedback relationship between the zonal sea surface
53 temperature (SST) gradient and the Walker circulation, referred to as the Bjerknes feedback (e.g.,
54 Bjerknes, 1969; Wyrtki, 1975). The surface easterly winds of the Walker circulation cause the
55 thermocline to sink in the west and rise in the east, resulting in the formation of the western warm pool
56 and the upwelling cold tongue in the eastern part of the basin. This zonal SST gradient further reinforces
57 the easterly winds. El Niño and La Niña are extreme events that occur when the Walker circulation
58 weakens (El Niño) or strengthens (La Niña), leading to a decrease or increase in upwelling in the eastern
59 tropical Pacific. This process results in an irregular oscillation between warm (El Niño) and cold (La
60 Niña) phases, with peaks occurring in boreal winter and recurring every 2-5 years (Rasmusson et al.,
61 1990; Jiang et al., 1995).

62 Our understanding of the oscillatory nature of ENSO relies on recognizing the relationship between
63 changes in internal ocean dynamics and changes in the wind stress pattern. By interpreting the tropical
64 Pacific Ocean as a double-layer system, the heat stored in the water column depends on the depth of the
65 interface that separates the surface and bottom layers. The zonal deformation of this interface (i.e. the
66 dynamical ocean subsurface memory) is sustained by the dynamical balance between the fluid internal
67 zonal pressure gradient and zonal winds (Cane and Zebiak, 1985; Philander, 1990; Jin, 1997; Burgers et
68 al., 2005; Jin et al., 2006).

69 Therefore, the SST anomaly, depth of the interface separating the surface and bottom layers, whose
70 fluctuations from a reference depth are often assumed to coincide with fluctuations in the depth of a
71 sentinel isotherm (typically the 15 °C, 17 °C, or 20 °C isotherm depth referred to as Z_{15} , Z_{17} , Z_{20}), and
72 zonal wind stress are a natural set of "state variables" that can be used to infer the basic physics
73 underlying ENSO. In a broad sense, and assuming that over the interannual time-scale the tropical Pacific
74 climate system can be approximated by a linear system, the dynamics underlying ENSO is described by
75 linear or non linear models that relate the evolution of the state variables to each other (Penland and
76 Sardeshmukh, 1995; Newman et al., 2009; Newman et al., 2011; Capotondi and Sardeshmukh, 2015).



77 Over the past 25 years, the linear recharge/discharge oscillator (LRDO) model, proposed by Jin
78 (1997), Burgers et al. (2005), and Jin et al. (2006), has served as a robust conceptual framework for
79 interpreting the interannual variability of SST anomalies in the tropical Pacific, despite some
80 discrepancies with observations. In this model, wind stress curl plays a fundamental role in the
81 preconditioning and evolution of ENSO. During the recharge phase, easterly wind (EW) anomalies
82 generate off-equatorial anticyclonic wind stress curls, resulting in a net equatorward Sverdrup transport
83 that deepens the equatorial thermocline. Conversely, during the discharge phase, westerly wind (WW)
84 anomalies produce off-equatorial cyclonic wind stress curls, causing a poleward Sverdrup transport that
85 moves warm water away from the equator and shallows the equatorial thermocline. The
86 recharge/discharge model describes ENSO as a self-sustained cycle driven by the slow buildup and
87 drainage of warm water towards and from the equator. From a mathematical perspective, the ocean is
88 represented as a two-layer system, in which the deepening of the interface between the layers represents
89 the charging phase, while the shoaling of this interface represents the discharge. In the original
90 formulation (Jin, 1997), the thermocline variability is separated into two components: the zonal tilt (i.e.
91 the difference in thermocline depth between the east and west), which responds quickly to winds, and
92 the mean equatorial heat content (the average depth of the thermocline across the entire equator), which
93 changes slowly through Sverdrup transport. The "oscillation" is related to the lag between these two
94 components. The zonal wind stress immediately affects the tilt, but it takes time for the Sverdrup transport
95 to change the mean depth of the thermocline (the recharge/discharge).

96 The Bjerknes feedback is represented in the recharge/discharge model as a growth mechanism that
97 turns an initial disturbance into a full El Niño or La Niña event. While Sverdrup transport determines
98 the slow charging of the equatorial Pacific providing the "memory" (i.e. the mean depth of the equatorial
99 thermocline) of the equatorial Pacific climate system, the Bjerknes feedback amplifies an initial
100 disturbance into a full El Niño or La Niña event. In this study, we discuss the relationship between
101 changes in the wind stress curl and divergence, and tilting of the thermocline to explain ENSO variability
102 over the interannual-to-interdecadal time scale.

103 Other studies have emphasized the importance of equatorial Kelvin waves (KW) forced by westerly
104 wind (WW) events. Picaut and Delcroix (1995) investigated equatorial wave sequences during the 1986–
105 1987 El Niño and showed that anomalous zonal advection was closely associated with KWs excited by
106 a succession of local WW events in the western and central tropical Pacific. These findings underscore
107 the central role of WWs in triggering SST anomalies on interannual timescales (see also Wang and
108 Fiedler, 2006; Santoso et al., 2017).



109 More recently, Eusebi Borzelli and Carniel (2023) examined the zonal displacements of the
110 convergence region between westerly and easterly winds (EWs). They demonstrated that internal KWs
111 are systematically generated beneath the WW/EW convergence zone and that the zonal position of this
112 convergence is highly correlated with the Southern Oscillation Index (SOI). In their terminology, the
113 WW/EW convergence corresponds to the region of minimum wind stress divergence (i.e., the maximum
114 absolute value of wind stress divergence), emphasizing the critical role of wind stress divergence in
115 controlling interannual SST anomaly variability.

116 Overall, these studies indicate that both wind stress curl and wind stress divergence are key
117 dynamical factors governing the initiation and evolution of El Niño events.

118 Over the long term, time series of ENSO indexes exhibit a “regime shift” from 1976, first noted by
119 Quinn and Neal (1984, 1985). Subsequent studies (Trenberth, 1990; Trenberth and Hurrell, 1994;
120 Graham, 1994), have emphasized the importance of this feature in relation to interdecadal climate
121 variability over the North Pacific. Since then, several studies have concentrated on the interdecadal or
122 longer ENSO variability. In this context, it is important to note that the behavior and characteristics of
123 ENSO are closely linked to the slowly changing background mean climate conditions of the equatorial
124 Pacific. These conditions impact ENSO initiation and growing (Fedorov and Philander, 2001; An et al.,
125 2008; Collins et al., 2010). It is projected that the mean climate state of the tropical Pacific will change
126 due to global warming, with a faster rate of warming in the equatorial Pacific compared to off-equatorial
127 regions (Liu et al., 2005; Collins et al., 2010). This warming is expected to be more pronounced in the
128 eastern and western equatorial Pacific compared to the central region (Xie et al., 2010). Additionally, the
129 surface of the ocean is expected to warm more quickly than the subsurface (An et al., 2008). This surface
130 warming pattern is responsible for an increase in rainfall, particularly in the eastern part of the basin,
131 which is a defining characteristic of extreme El Niño events (Zhong et al., 2025). Accordingly, Cai et al.
132 (2015; 2022) observed that El Niño events are becoming more frequent and intense under global
133 warming.

134 From a slightly different perspective, some research has focused on the effect of meridional mean-
135 state change on low frequency variability of El Niño. It is well known that the intertropical convergence
136 zone (ITCZ) is typically located north of the equator for most of the year, resulting in climatological
137 cross-equatorial southerly winds across the eastern equatorial Pacific. The relaxation of these southerly
138 winds crossing the equator leads to a weakening of the cold and westward currents south of the equator,
139 contributing to the thermocline downwelling and SST warming in the eastern equatorial Pacific, which
140 in turn modulates El Niño intensity (Philander and Pacanowski, 1981; Périgaud et al., 1997; Hu and
141 Fedorov, 2018; Peng et al., 2020). This observation has led some authors to investigate ENSO variability



142 over interdecadal or longer time scales in relation to low frequency variability of the ITCZ and meridional
143 cross-equatorial southerly winds (Xie et al., 2018; Capotondi and Ricciardulli, 2021; Wang and Zheng,
144 2023).

145 Here, to account for the modulation of wind stress forcing caused by the slowly varying surface
146 density and related changes in the reduced gravity (g'), we introduce a dimensionless wind stress (DWS).
147 The DWS is defined as the ratio between the wind stress and the product of the surface-layer density and
148 the square of the first baroclinic mode velocity. The first baroclinic mode velocity, denoted by c_1 , is given
149 by $(g'H)^{1/2}$, where H is the depth of the surface layer and g' is the reduced gravity (see appendix B for
150 details).

151 To investigate the relative contributions of DWS curl and divergence to SST anomaly variability in
152 the tropical Pacific on interannual to interdecadal timescales, we decompose the DWS into irrotational
153 (curl-free) and solenoidal (divergence-free) components using the Helmholtz decomposition. Assuming
154 the tropical Pacific as a two-layer ocean, we follow Capotondi and Sardeshmukh (2015) and use
155 variations in Z_{15} as a proxy for fluctuations in the depth of the interface layer. This allows us to derive an
156 integral relationship linking basin-wide changes in the Z_{15} anomaly to the Niño-3.4 index (N_{34}). The N_{34}
157 is defined as the five-month median-filtered mean SST anomaly over the region 5°S–5°N, 190°E–240°E
158 (the Niño-3.4 region). Our results indicate that interannual variability in N_{34} is primarily driven by the
159 coupling between the irrotational component of the DWS and thermocline depth fluctuations. In addition,
160 we find that differential temperature changes between the surface and subsurface ocean layers (An et al.
161 2008) induce variations in the reduced gravity field (g'), thereby modulating the background ocean
162 dynamics. We show that the interaction between the solenoidal component of the DWS and these slow
163 changes in ocean stratification provides a mechanistic explanation for the long-term modulation of El
164 Niño intensity.

165 2. The data

166 Surface winds and SST were obtained from the Copernicus data archive. Copernicus provides
167 parameters over a regular spatial grid of $0.25^\circ \times 0.25^\circ$. This study utilized ERA5 monthly surface zonal
168 winds and SST over the region 160°E–270°E, 20°S–20°N in the period Jan 1960–Dec 2020.

169 The wind stress was calculated from surface wind components using the standard formula
170 $\boldsymbol{\tau} = \rho_{air} \cdot c_D \cdot (v_x^2 + v_y^2)^{1/2} \cdot \mathbf{v}$, where $\mathbf{v} = (v_x, v_y)$ is the surface wind, ρ_{air} is the air density at the ocean surface
171 (taken as 1.2 kg/m^3) and c_D is the drag coefficient (taken as $1.2 \cdot 10^{-3}$ if $(v_x^2 + v_y^2)^{1/2} < 11 \text{ m/s}$ and
172 $[0.49 + 0.065 \cdot (v_x^2 + v_y^2)^{1/2}] \cdot 10^{-3}$ if $(v_x^2 + v_y^2)^{1/2} \geq 11 \text{ m/s}$, for details see Large and Pond, 1981).



173 SST data were used to compute the N_{34} . Monthly SST data from January 1960 to December 2020,
174 were extracted from the Copernicus database over the Niño-3.4 region. The SST anomaly was computed
175 using as a reference climatological baseline, the period January 1991-December 2020.

176 The Institute of Atmospheric Physics (IAP) at the Chinese Academy of Sciences (CAS) has provided
177 salinity and temperature (TS) data for the water column. These data consist of monthly objective maps
178 covering the entire global ocean from January 1960 to December 2020, sampled over a regular spatial
179 grid of $0.5^\circ \times 0.5^\circ$. The data includes TS profiles from the surface to a depth of 2000 m (for more
180 information, refer to Cheng et al. 2017). In this study, data from the region (160°E - 270°E , 20°S - 20°N)
181 were extracted to compute the Z_{15} and seawater density profiles.

182 The velocity of the first baroclinic mode and the depth of the main thermocline were calculated
183 using sea water density profiles, as described in Appendix B. It should be noted that the CAS-IAP data
184 is sampled on a $0.5^\circ \times 0.5^\circ$ grid, while the Copernicus wind data is sampled on a $0.25^\circ \times 0.25^\circ$ grid. To
185 calculate the DWS, we used a "nearest neighborhood" interpolation method to undersample the wind
186 stress data.

187 3. The Z_{15} - N_{34} integral relationship

188 Our objective is to explain the variability of N_{34} by utilizing an integral relationship that connects
189 the variability of the Z_{15} anomaly across the entire observation region (160°E - 270°E , 20°S - 20°N) to N_{34} .
190 This relationship can be expressed as

$$N_{34}(t) = \int_{(S)} \frac{dx}{S} w(x) Z(x, t) = \sum_{m=1}^M Z(x_m, t) \cdot w(x_m) \quad (1)$$

191
192 In this equation $Z(x_m, t)$ represents the Z_{15} anomaly at point x_m on date t , and $N_{34}(t)$ represents the N_{34} on
193 date t . The unknowns $w(x_m)$ define the linear model that links Z and N_{34} . We determine $w(x_m)$ by requiring
194 that the representation (1) is "optimal" in the least-square sense, namely we require that the Root Mean
195 Square (RMS) between N_{34} and its representation on the right-hand side of (1) is minimum, i.e.

$$\min \left\{ \left[\left| N_{34}(t) - \sum_{m=1}^M Z(x_m; t) \cdot w(x_m) \right|^2 \right] \right\}_{w(x_1), w(x_2), \dots, w(x_M)} \quad (2)$$



196 where the bra-ket symbol denotes temporal averaging. By computing the derivative with respect to $w(x_k)$
197 of the RMS, and requiring the minimum condition, we obtain a system of linear equations for the
198 unknowns $w(x_m)$ ($m=1\dots M$), i.e.

$$\sum_{m=1}^M A(x_k, x_m) \cdot w(x_m) = n(x_k) \quad (3)$$

199 where

$$\begin{aligned} n(x_k) &= \int_0^T \frac{dt}{T} N_{34}(t) \cdot Z(x_k, t) \\ A(x_k, x_m) &= \int_0^T \frac{dt}{T} Z(x_k, t) \cdot Z(x_m, t) \end{aligned} \quad (4)$$

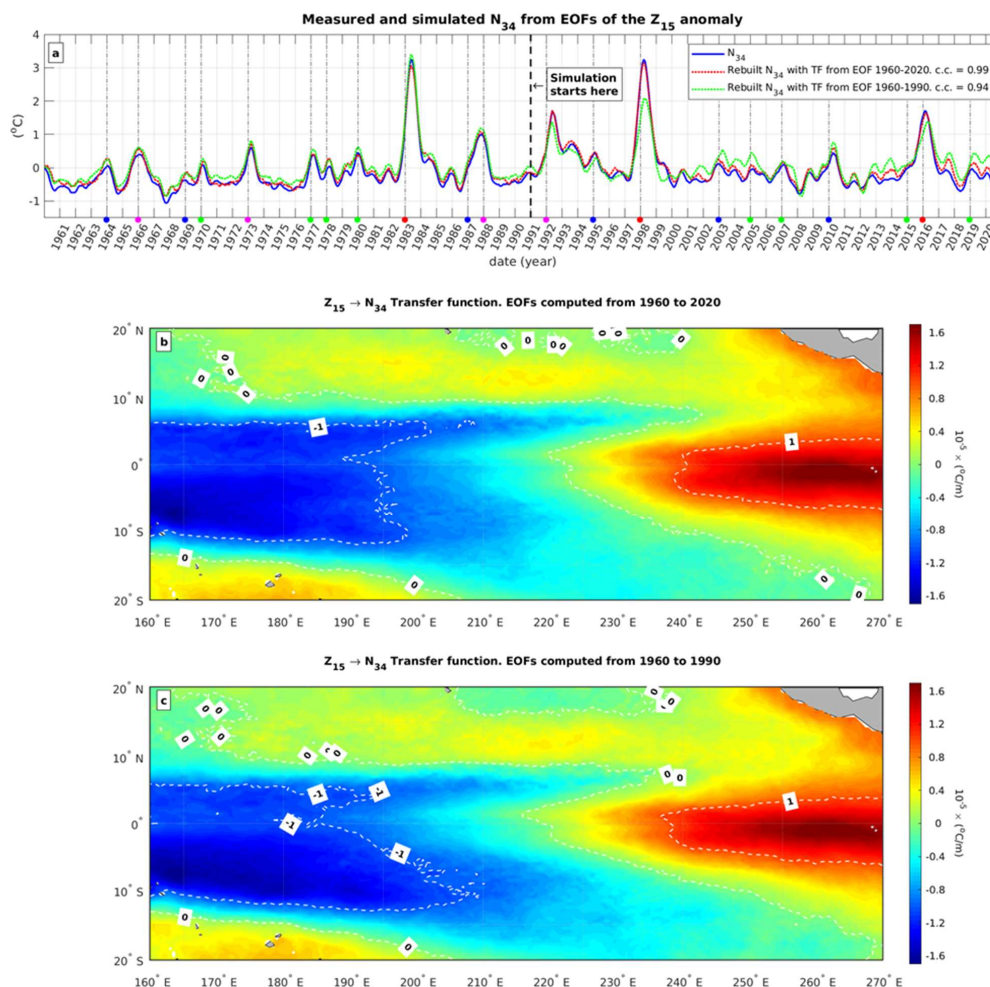
200 The matrix \mathbf{A} , with elements $(\mathbf{A})_{km} = A(x_k, x_m)$, is the autocorrelation matrix of Z . Taking this in to
201 account, denoting with λ_n the variance explained by n^{th} Empirical Orthogonal Function (EOF) of Z , with
202 Y_n the n^{th} dimensionless EOF, and with α_n its corresponding dimensionless Principal Component (PC),
203 we have (see Appendix A for the calculation)

$$w(x_m) = \sum_n \frac{c_n}{\sqrt{\lambda_n}} \cdot Y_n(x_m) \quad (5)$$

204 where the sum is extended to all EOFs of Z , and c_n is the projection of the N_{34} along the direction of the
205 n^{th} PC, i.e.

$$c_m = \int_0^T \frac{dt}{T} \alpha_m(t) \cdot N_{34}(t) \quad (6)$$

206 Note that $w(x)$ is a transfer function that maps the Z_{15} anomaly over the entire tropical Pacific to the
207 average SST anomaly over the central tropical Pacific. In Figure 1a, we show the measured N_{34} (blue
208 solid line) and the N_{34} rebuilt from the Z_{15} anomaly using equation (1) and transfer function $w(x)$ given
209 by equations (5) and (6). To rebuild the N_{34} , we have truncated the sum (5) to the first four EOFs, which
210 cumulatively explain 84% of the overall Z_{15} data set variance. The two dashed lines represent the
211 estimates of the transfer function obtained from the EOF analysis of the Z_{15} anomaly performed using
212 data from the entire observation period (i.e. 1960-2020, red dashed line) and the sub-period 1960-1990
213 (green dashed line). In both cases, the N_{34} is accurately reconstructed, indicating the stability of the
214 method in relation to the period over which the EOF analysis is performed. This is further supported by
215 the similarity between the transfer functions estimated from the EOF analysis of the Z_{15} anomaly over



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Figure 1: a) The blue solid line represents the measured N_{34} values, while the dashed lines represent the simulated N_{34} values from the first four EOFs of the Z_{15} anomaly. The red dashed line shows the N_{34} values simulated from the transfer function calculated using EOF analysis from 1960 to 2020, while the green dashed line shows the N_{34} values simulated from the transfer function calculated from EOF analysis from 1960 to 1990. Colored dots on the bottom horizontal axis represent El Niño events obtained from <https://ggweather.com/enso/oni.htm>. Color of the dots represent El Niño event intensity, with the following legend: red, extreme; magenta, strong; blue, moderate; green, weak. b) Z_{15} anomaly- N_{34} transfer function calculated from the first four EOFs of the Z_{15} over the period 1960-2020. c) Z_{15} anomaly- N_{34} transfer function calculated from the first four EOFs of the Z_{15} over the period 1960-1990.

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226 the entire observation period and the period 1960-1990 (see Figures 1b and 1c). A general analysis of the
 227 transfer function's spatial structure indicates that it is characterized by values significantly different from
 228 zero in the region comprised approximately between 10°S and 10°N. This suggests that variations in the
 229 Z_{15} anomaly outside of this region have minimal impact on changes in the N_{34} . Within the region 10°S-



230 10°N, the transfer function displays significantly positive values in the eastern part of the basin, notably
 231 negative values in the western, and values close to zero in the central area. This highlights a key
 232 geographical feature of the tropical Pacific climate system: the zonal tilting of the thermocline, which
 233 drives the atmospheric response related to the Bjerknes feedback. In the eastern Pacific, the thermocline
 234 is shallow and upwelling is strong, so even small vertical movements of the Z_{15} determine changes in the
 235 SST. In the western Pacific, the thermocline is deep, and its variations are critical for generating eastward
 236 propagating KWs. On the other hand, the central Pacific acts as a buffer zone where the thermocline is
 237 at an intermediate depth. In this region, there is no upwelling, and even a large vertical shift in the Z_{15}
 238 anomaly does not necessarily result in SST changes.

239 **4. Wind stress and Z_{15} : “quasi-balance” and residual mean dynamics**

240 We start with the full double layer, linearized shallow water equations, in which the term
 241 $\boldsymbol{\tau}/(g' \cdot H \cdot \rho) = \boldsymbol{\tau}/(c_1^2 \cdot \rho)$ is expressed as the sum of a solenoidal (i.e. divergence-free) and irrotational (curl-
 242 free) vector field, as prescribed by the Helmholtz decomposition (see e.g Morse and Feshbach 1953), i.e.

$$\frac{\boldsymbol{\tau}}{g' \cdot H \cdot \rho} = \frac{\boldsymbol{\tau}}{c_1^2 \cdot \rho} = \nabla \phi + \nabla \times \mathbf{A} \quad (7)$$

243 In equation (7), $\boldsymbol{\tau}$ represents the wind stress, g' the reduced gravity, H and ρ the thickness and density
 244 of the surface layer, and $c_1 = (g'H)^{1/2}$ the velocity of the first baroclinic mode. The terms ϕ and \mathbf{A} are
 245 commonly referred to as the scalar and vector potential, respectively. Note that the vector $\boldsymbol{\tau}/(c_1^2 \cdot \rho)$ is
 246 dimensionless, and will be referred to as DWS in the following. Note also that ϕ and \mathbf{A} have dimensions
 247 of length. Furthermore, note that since the DWS lies in the x-y plane, $\mathbf{A}=(0,0,S)$. The function S , is
 248 typically referred to as the DWS stream-function.

249 Using the Helmholtz decomposition of the DWS and the definitions above, the linear shallow water
 250 equation can be written in terms of ϕ and S as

$$\begin{cases} \frac{1}{g'} \left(\frac{\partial u}{\partial t} - f v \right) = \frac{\partial h}{\partial x} + \frac{\partial \phi}{\partial x} + \frac{\partial S}{\partial y} \\ \frac{1}{g'} \left(\frac{\partial v}{\partial t} + f u \right) = \frac{\partial h}{\partial y} + \frac{\partial \phi}{\partial y} - \frac{\partial S}{\partial x} \\ - \frac{\partial h}{\partial t} + D \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) = 0 \end{cases} \quad (8)$$

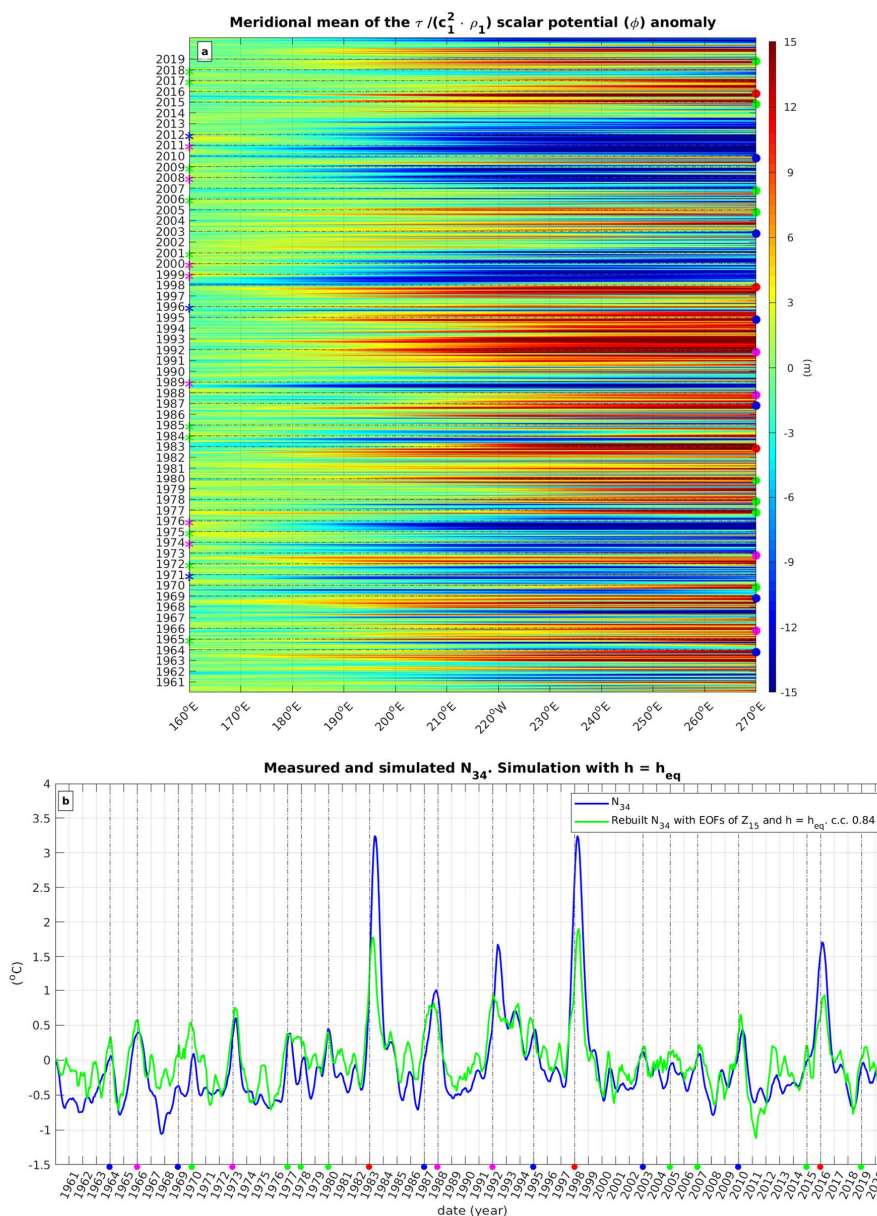
251 where D is a reference depth set to 120 m, h is the departure of the interface layer from D (i.e. $H=D-h$)
 252 and the continuity equation has been linearized around D as in Jin (1997). Jin (1997) sought for solutions
 253 of the quasi-geostrophic equations, in which h is in equilibrium with the zonal wind stress, and assumed



254 the meridional wind stress to be zero. Here we seek for solutions of (8) around the interface layer
255 computed by setting the ocean at the hydrostatic state (i.e. $u=v=0$). It is important to note that at this
256 state, the zonal and meridional components of the DWS are in equilibrium with the zonal and meridional
257 derivatives of the interface layer. We denote this interface as h_{eq} , and we will refer to this layer to as
258 quasi-equilibrium layer. The momentum equations in (8) at the hydrostatic state are $\nabla h_{eq} + \nabla \phi + \nabla \times \mathbf{A} = 0$,
259 where we have used the definition (7) of scalar and vector potential. By extracting the divergence of this
260 equation, we get $-\nabla^2 h_{eq} = \nabla^2 \phi$. It is therefore natural to set $-h_{eq} = \phi$. This means that the divergence of the
261 DWS, forces the “equilibrium” part of the dynamics. We indicate with $-q$ the displacement of the interface
262 layer from its shape at the equilibrium state (h_{eq}), namely $h(x,y,t) = h_{eq}(x,y,t) - q(x,y,t)$. The DWS was
263 decomposed in to irrotational and solenoidal components using the Helmholtz decomposition. The
264 irrotational component (i.e. ϕ) was used to represent $-h_{eq}$.

265 In Figure 2a, the meridional mean of the h_{eq} anomaly is shown in relation to El Niño (indicated by
266 the dots on the right vertical axis) and La Niña (indicated by the squares on the left vertical axis) events.
267 It is evident that the deformation of the interface layer induced by h_{eq} is consistent with both El Niño and
268 La Niña events.

269 In Figure 2b, we present the N_{34} obtained from equation (1) using the h_{eq} anomaly instead of the Z_{15}
270 anomaly and the transfer function of Figure 1b. The correlation coefficient between the measured N_{34}
271 and N_{34} reconstructed from the quasi-equilibrium dynamics (h_{eq}) is high (0.83), indicating that the quasi-
272 equilibrium dynamics accurately capture the main features of the N_{34} variability. However, upon closer
273 examination of Figure 2b, it is evident that the N_{34} deduced from the quasi-equilibrium dynamics
274 underestimates N_{34} values during some strong (1965-66, 1972-73) and all extreme (1982-83, 1997-98,
275 2015-2016) El Niño events. As shown in Figure 2b (red and magenta bullets on the bottom axis),
276 successive strong or extreme El Niño events occur over time scales longer than the interannual,
277 suggesting that while the equilibrium dynamic accurately captures the interannual variability of SST
278 anomalies in the central tropical Pacific, it only partially resolves the fluctuations of the N_{34} over longer
279 time scales. This leads us to hypothesize that q , which is forced by the rotational part of the DWS,
280 encapsulates the long-term variability of the Z_{15} anomaly and, thus, of the N_{34} . From equation (8), it is
281 possible to derive an equation for q . However, a great simplification can be made by using the geostrophic
282 approximation. A reasonable strategy to use this approximation is to exclude the equatorial belt between
283 2°S-2°N and derive an equation for q in the two strips between 2°N-20°N and 2°S-20°S. The geostrophic
284 approximation appears reasonable because we are interested in the long-term, basin-scale variability of
285 q . Using this approximation we find



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Figure 2: a) Meridional mean of the dimensionless wind stress potential anomaly. Colored dots on the right vertical axis represent El Niño events classified as discussed in the legend of Figure 1a. Colored rectangles on the left vertical axis represent La Niña events obtained from <https://ggweather.com/enso/oni.htm>, with the following legend: magenta, strong; blue, moderate; green, weak. b) Measured (blue line) and rebuilt N_{34} (green line) obtained with the transfer function of Figure 1b and substituting, in place of the Z_{15} anomaly, the anomaly of h_{eq} . Colored dots on the horizontal bottom axis represent El Niño events classified as discussed in the legend of Figure 1a.



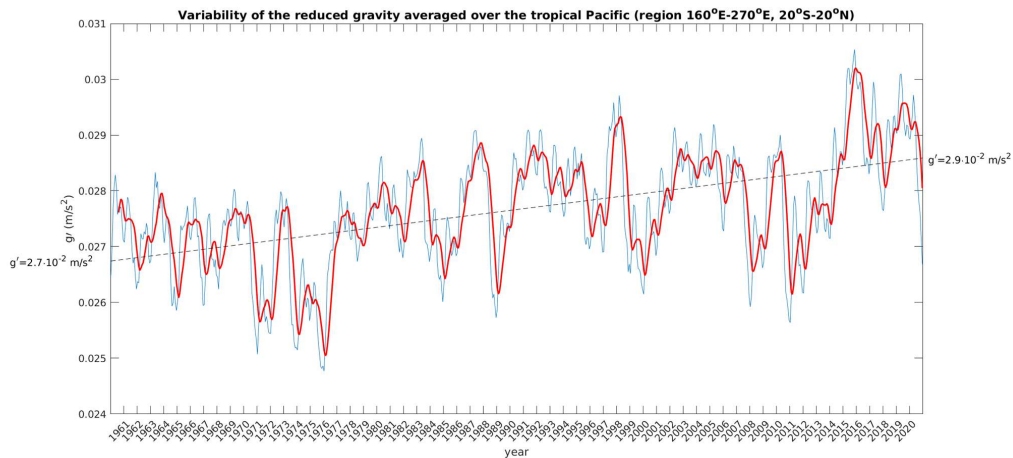
$$\begin{cases} v = -\left(\frac{g'}{f}\right) \cdot \left(\frac{\partial S}{\partial y} - \frac{\partial q}{\partial x}\right) \\ u = -\left(\frac{g'}{f}\right) \cdot \left(\frac{\partial S}{\partial x} + \frac{\partial q}{\partial y}\right) \end{cases} \quad (9)$$

293 and, observing that $\partial h_{eq}/\partial t \approx 0$, substituting equation (9) in the continuity equation, we get

$$\frac{\partial q}{\partial t} - D\left(\frac{g' \cdot \beta}{f^2}\right) \cdot \frac{\partial q}{\partial x} = D\left(\frac{g'}{f}\right) \nabla^2 S - D\left(\frac{g' \cdot \beta}{f^2}\right) \frac{\partial S}{\partial y} \quad (10)$$

294 where $\beta = df/dy$.

295 To account for the slowly changing background mean climate conditions of the equatorial Pacific,
 296 we have considered $g' = g'(t)$, with $g'(t)$ representing the average spatial reduced gravity field over the
 297 region 20°S-20°N, 160°E-270°W. This was computed from TS data, as discussed in Appendix B. Figure
 298 3 shows $g'(t)$ and illustrates that the reduced gravity field in the entire tropical Pacific is characterized
 299 by a trend of increase of approximately $0.33 \cdot 10^{-4} \text{ m/s}^2$ per year, in addition to oscillations over the sub-
 300 decadal time-scale. This increase in reduced gravity is a result of an increase in the stability of the water
 301 column, which is consistent with an increase of the stratification of the water column due to the uneven
 302 increase in temperature of the surface and bottom layers (An et al. 2008).



303

304 **Figure 3:** Spatial average of the reduced gravity field over the region 20°S-20°N, 160°E-270°E. The blue line represents raw
 305 data; the red line represents 5-month median filtered data; the black dashed line is the linear fit.

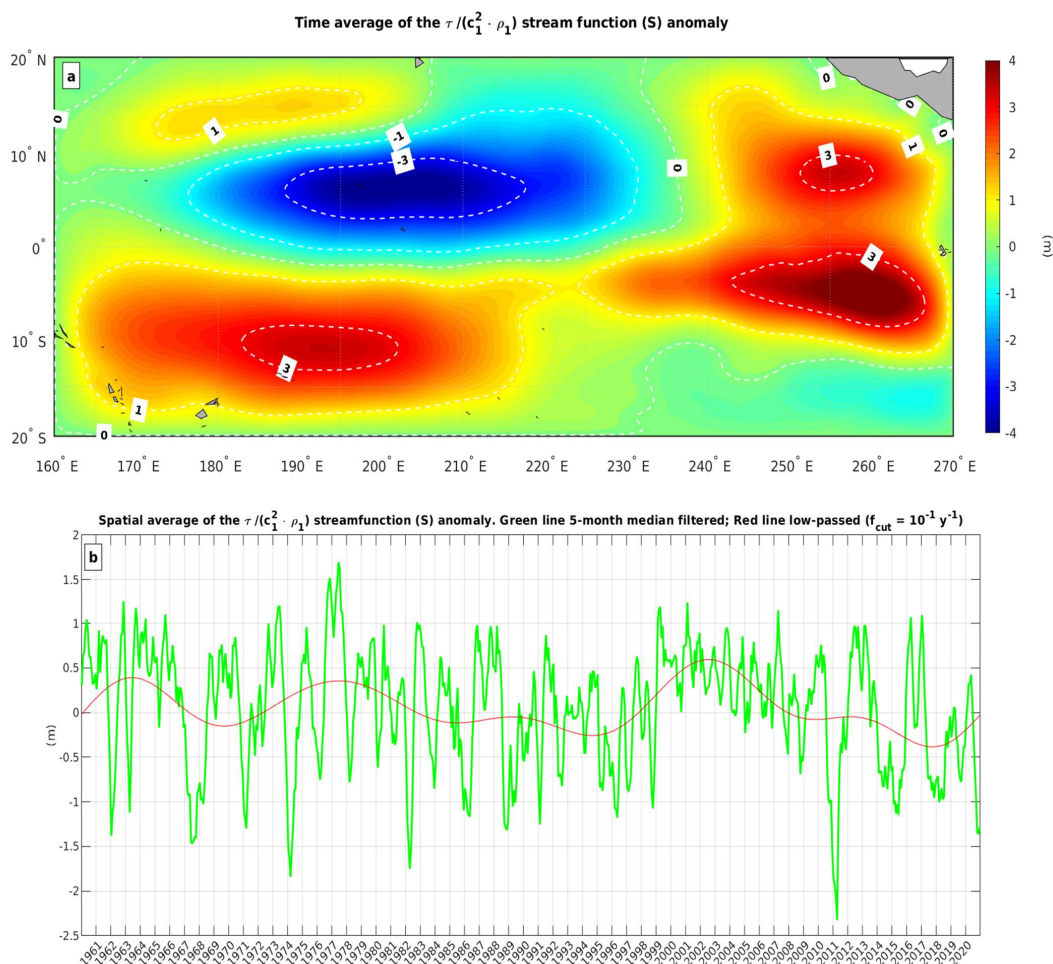
306



307 With the above observation, equation (10) describes an internal wave (q -wave in the following)
308 forced by the rotational component of the DWS that propagates westward over the equilibrium
309 thermocline (i.e. h_{eq}) with a velocity $c = D \cdot (g' \cdot \beta / f^2)$ that depends on time and latitude.

310 Figure 4a displays the time-averaged spatial distribution of the DWS streamline function (S)
311 anomaly, while Figure 4b depicts the temporal variability of the space-averaged S anomaly. In the western
312 part of the basin, the S anomaly is characterized by a positive-value region south of the equator and a
313 negative-valued region north of it. In contrast, the eastern tropical Pacific shows two regions with positive
314 values both south and north of the equator. The spatial pattern of the S anomaly in the western tropical
315 Pacific is consistent with mass redistribution towards the equator due to Sverdrup transport. However, in
316 the eastern part of the basin, the spatial structure of the S anomaly is consistent with Sverdrup transport
317 towards the equator in the south and Sverdrup transport away from the equator in the north. This suggests
318 that in the eastern tropical Pacific, wind stress curl is not as effective in transporting mass towards the
319 equator as it is in the western part of the basin. This asymmetry could be related to ENSO asymmetry,
320 but further, focused research is necessary to clarify this issue. The temporal variability of the spatially
321 averaged S anomaly (Figure 4b, green line) does not appear to be dominated by specific frequencies.
322 However, the residual signal obtained after applying a low-pass filter with a cut-off frequency of 10^{-1}
323 years⁻¹ (Figure 4b, red line) is weak, suggesting that the S anomaly is only minimally affected by
324 interdecadal variability.

325 The q -wave field was calculated separately for the northern and southern regions of the equator by
326 solving equation (10) with an initial condition of zero, using the technique outlined in Appendix C. In
327 order to provide the reader with a better understanding of the spatial and temporal variability of the q -
328 wave field, the q -wave time series was decomposed into EOFs. The q -wave field is primarily described
329 by two EOF modes, which together explain 98% of the variance. Figure 5a displays the first EOF of the
330 q -wave field, while Figure 5b shows its corresponding PC. Similarly, Figure 5c and 5d depict EOF2 and
331 its corresponding PC, respectively. Both EOFs demonstrate that the q -wave field is primarily
332 concentrated in the subtropical region between 2°S-7°S and 2°N-7°N. Along the zonal direction, EOF1
333 describes two negative patterns located in the western and eastern parts of the basin, and another region
334 of positive values that fills the entire central part of the tropical Pacific. The corresponding PC1, describes
335 a linear trend which transits from negative to positive values by the beginning of 1990. This implies that,
336 from 1960 to 1990, q -waves contributed to the rise (note that $h = h_{eq-q}$) of the thermocline from its
337 equilibrium position, while in the subsequent period they contributed to the deepening of the thermocline
338 in these regions. Conversely, in the central tropical Pacific during 1960-1990, q -waves contributed to the
339 deepening of the thermocline and the rise of it in the period 1990-2020.



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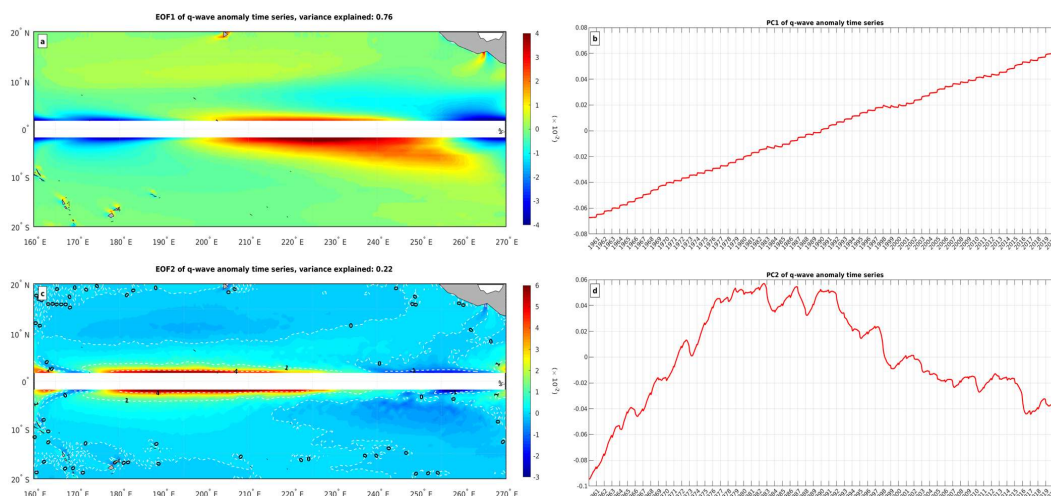
341 **Figure 4:** a) Time average of the dimensionless wind stress stream-function anomaly. b) Spatial average over the region
 342 20°S-20°N, 160°E-270°E of the dimensionless wind stress stream-function anomaly.

343

344 In the zonal direction, EOF2 is characterized by three distinct regions: two with positive values in
 345 the western and central parts of the basin, and one with negative values in the eastern tropical Pacific.
 346 The temporal variability of this spatial pattern is represented by PC2, as shown in Figure 5d. A visual
 347 inspection of Figure 5d reveals that PC2 of the q-wave field is characterized by a strong long-term
 348 variability, with a weak interannual variability.

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Figure 5: EOF analysis of the q -wave anomaly field obtained with initial condition $q_0 = 0$. a) EOF1. b) PC1. c) EOF2. d) PC2.

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To analyze the effect of q -wave interdecadal variability on SST anomalies in the central tropical Pacific, we reconstructed the N_{34} using equation (1) and replacing the Z_{15} anomaly with the h_{eq-q} anomaly, with q computed with the initial condition set to zero. The results are shown in Figure 6, where we have plotted, beside the estimate of N_{34} obtained by replacing the Z_{15} anomaly with h_{eq-q} anomaly, the measured N_{34} (blue line) and the estimated N_{34} using the h_{eq} anomaly (green line, same as Figure 2a) for comparison. It is evident that the inclusion of the q -wave significantly improves the accuracy of the N_{34} estimate. In particular, the addition of the q -wave allows for a more precise representation of strong and extreme El Niño events, compared to using only h_{eq} .

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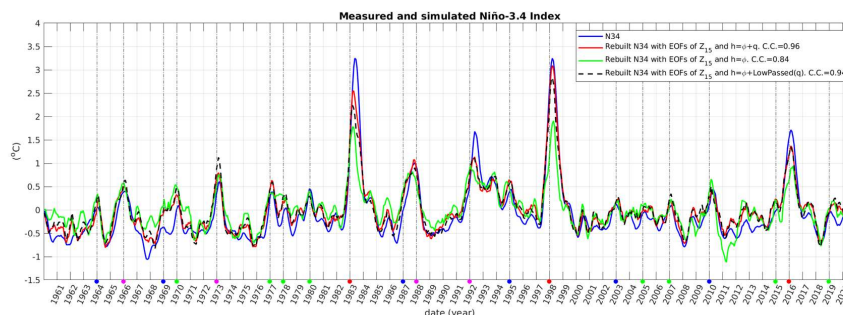
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To demonstrate that the improvement in the N_{34} estimate is a result of low frequency signals encapsulated in q , which are filtered out by the "quasi-equilibrium" assumption, in Figure 6 we have also plotted the N_{34} estimate obtained by replacing the Z_{15} anomaly with the residual signal of the h_{eq} minus the low-passed q (represented by a black dashed line). The low pass filtering was performed with a frequency cut of 10^{-1} years $^{-1}$. It can be observed that the low-pass filtering of q results in a N_{34} estimate that is similar to that obtained using the unfiltered q -signal (compare the red and black dashed line). This demonstrates that the interannual variability of the SST anomaly in the central tropical Pacific can be explained by the equilibrium dynamics, which encapsulates the variability of the interface layer over time scales shorter than 10 years, and is associated with the divergence of the DWS. On the other hand, q -waves are responsible for the long-term variability of SST anomalies, as they reflect the non-



373 equilibrium dynamics of the thermocline. These waves are driven by the rotational component of the
 374 DWS. Mathematically, they represent deviations of the thermocline from its shape at the hydrostatic
 375 state, caused by the curl of the DWS. Physically, q -waves are a result of the thermocline accommodation
 376 due to mass redistribution caused by the Sverdrup transport. As mass in the surface layer is displaced
 377 meridionally by the Sverdrup transport, the thermocline responds by generating q -waves that propagate
 378 zonally.



379

380 **Figure 6:** Measured (blue solid line) and simulated N_{34} . Red solid line: N_{34} simulated using the transfer function of Figure
 381 1b and substituting, in place of the Z_{15} anomaly, the anomaly of the interface layer computed as $h = h_{eq} - q$. Green line: N_{34}
 382 simulated using the transfer function of Figure 1b and substituting, in place of the Z_{15} anomaly, the anomaly of the interface
 383 layer computed as $h = h_{eq}$ (same as green line of Figure 2). Black dashed line: N_{34} obtained from low passed q . Colored dots
 384 on the horizontal bottom axis represent El Niño events classified as discussed in the legend of Figure 1a.

385 5. Discussion and Conclusion

386 In this study, we have investigated the relationships between the thermocline depth anomaly, and
 387 wind stress in the entire tropical Pacific, and changes in the average SST anomaly in the central part of
 388 the basin over both interannual and interdecadal time scales. Our results indicate that the variability in
 389 the SST anomaly in the central tropical Pacific can be accurately represented by an integral relationship,
 390 which links the variability in the thermocline depth anomaly to the Niño-3.4 index. This integral
 391 relationship is defined by a transfer function derived from an EOF analysis of the thermocline depth
 392 anomaly, which we have assumed to be represented by the 15° isotherm depth anomaly. The spatial
 393 structure of the transfer function indicates that even small variations in the thermocline depth anomaly
 394 in the western or eastern parts of the tropical Pacific can have significant impacts on the SST anomaly in
 395 the central part of the basin, while large variations in the thermocline depth anomaly in the central Pacific
 396 have minimal influence on SST variation in this region. This result is consistent with Zhong et al. (2025),
 397 who demonstrated, using a different approach, that El Niño is more predictable in the eastern and western
 398 parts of the tropical Pacific compared to the central part of the basin.



399 Our analysis has shown that the transfer function's structure remains stable regardless of the chosen
400 period for EOF analysis of the thermocline depth anomaly. However, the effectiveness of the transfer
401 function in capturing the interdecadal variability of the N_{34} may vary depending on the specific period
402 selected for the EOF analysis. To definitively address this issue, a systematic sensitivity test would be
403 necessary. We have only performed a few spread tests, which suggest that in order to accurately capture
404 the long-term variability of the N_{34} in relation to changes in the thermocline depth anomaly, the EOF
405 analysis of the thermocline depth anomaly must be conducted over a sufficiently long period to include
406 a range of El Niño and La Niña events with varying intensities. This is evident in the period 1960-1990,
407 which includes 11 El Niño events (four weak, three moderate, three strong, and one extreme) and 14 La
408 Niña events (eight weak, one moderate, and five strong).

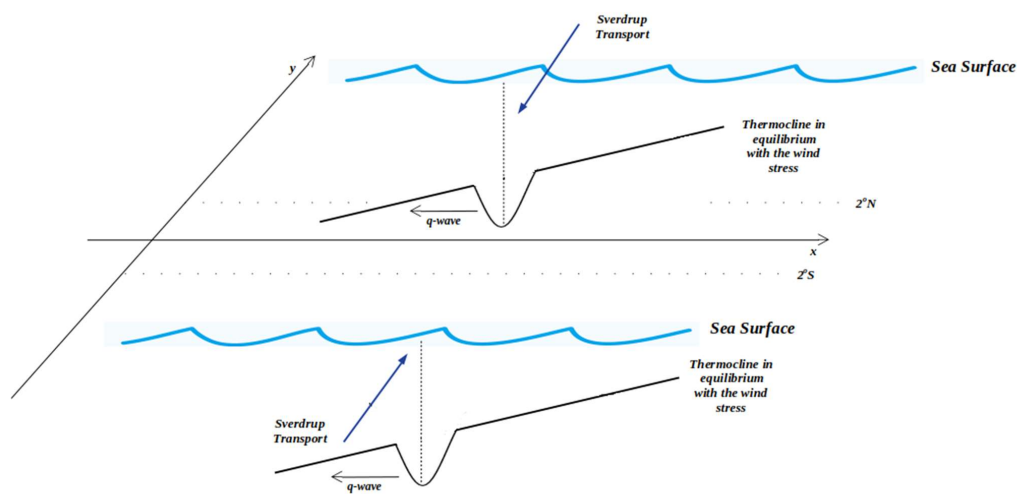
409 To analyze the impact of wind stress variability on SST anomalies in the central tropical Pacific, we
410 examined the coupling between changes in the depth of the thermocline and the irrotational (curl-free)
411 and solenoidal (divergence-free) components of the DWS. The use of the DWS is necessary because,
412 even a wind stress without divergence or curl, can provide divergence or vorticity to the horizontal ocean
413 dynamics through spatial changes of the first baroclinic mode velocity and/or surface density. Our
414 findings indicate that the irrotational component of the DWS, which is related to the divergence of the
415 DWS and drives the quasi-equilibrium dynamics, is the main factor influencing the interannual
416 variability of SST anomalies in the central tropical Pacific. This is consistent with the findings of Eusebi
417 Borzelli and Carniel (2023), who observed that the region of maximum wind convergence in the tropical
418 Pacific shifts along the zonal direction in phase with the SOI. This suggests that the divergence of the
419 wind field can explain the variability of the tropical Pacific climate system on the ENSO time-scale.

420 In this research, we have demonstrated that the equilibrium dynamics can be described by an
421 equation between the DWS scalar potential and the deformation of the interface layer. This equation
422 takes the form $-\nabla^2 h_{eq} = \nabla^2 \phi$ and we have set $-h_{eq} = \phi$. Although the most natural, this solution is not
423 the most general and this choice could be questioned. A more general solution could be, for instance,
424 $-h_{eq} = \phi + \alpha \cdot x + \beta \cdot y$, where the linear components represent the average slope over the entire observation
425 period of the thermocline in the zonal and meridional directions. However, this signal does not contribute
426 to the h_{eq} anomaly, and for the sake of simplifying the formalism, we have chosen to set $h_{eq} = -\phi$.

427 Non-equilibrium dynamics associated with the solenoidal component of the DWS, which represents
428 its rotational contribution, becomes important on timescales longer than a decade. This solenoidal
429 component drives the generation of internal waves, referred to as q -waves, which propagate westward
430 and induce large-scale deformations of the thermocline. In physical terms, q -waves describe the
431 thermocline response to Sverdrup transport due to wind stress curl. Figure 7 shows schematically the



432 generation process of q -waves. It should be noted that the propagation speed of q -waves is formally
 433 similar to that of long, off-equatorial, internal Rossby waves. Therefore, q -waves can be classified as
 434 Rossby-like waves. However, there are some notable differences between the two. Specifically, Rossby
 435 waves travel over a flat thermocline, while q -waves are caused by the rotational (solenoidal) component
 436 of wind stress and result in a deviation of the thermocline from its shape at hydrostatic equilibrium. As a
 437 result, q -waves propagate over a more complexly shaped thermocline. Furthermore, unlike ordinary
 438 Rossby waves, the propagation speed of q -waves depends explicitly on time due to the temporal
 439 variability of reduced gravity.



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Figure 7: Schematical representation of q -waves.

443 By modulating thermocline depth, q -waves contribute to SST anomaly variability in the central
 444 tropical Pacific and provide a dynamical pathway through which non-equilibrium ocean processes
 445 influence surface temperature. Although the solenoidal component of the DWS itself exhibits limited
 446 variability on interdecadal time scales, it acts on a background ocean state whose stratification evolves
 447 slowly over time. Such long-term changes in stratification are captured by variations in the reduced
 448 gravity field (g'), which reflects uneven temperature changes between the upper and lower ocean layers.

449 Our results indicate that interdecadal variability of SST anomalies in the central tropical Pacific
 450 arises from the coupling between the slowly varying reduced gravity field and the solenoidal component
 451 of the DWS. In this framework, changes in surface ocean density modulate the efficiency of Sverdrup



452 transport associated with wind stress curl, thereby controlling the long-term thermocline response and its
453 imprint on SST variability. This mechanism complements the equilibrium dynamics dominant at
454 interannual timescales and highlights the role of rotational wind forcing in shaping the long-term ENSO
455 variability.

456 The uneven heating of the surface and bottom layers of the tropical Pacific under greenhouse
457 warming described by An et al. (2008) has the obvious consequence of increasing the stability of the
458 water column and, therefore, increasing the reduced gravity. However, the role of surface salinity in
459 determining changes in the reduced gravity field is less certain, although some authors have emphasized
460 the importance of including sea surface salinity records to improve El Niño forecasting (e.g. Wang et al.,
461 2024). In addition to the redistribution of salt by ocean currents, the acceleration of the hydrological
462 cycle under greenhouse warming also contributes to regional means and long-term trends in sea surface
463 salinity (Durack et al., 2012). However, it has been shown that estimates of long-term trends in sea
464 surface salinity in the tropical Pacific are regionally dependent (Zhi et al., 2025). While our research did
465 not specifically address the impact of long-term surface salinity trends on the variability of the reduced
466 gravity field, a focused analysis using the methods presented here could provide insight into the role of
467 salinity changes in the interdecadal variability of SST anomalies in the tropical Pacific.

468 As a final remark, some authors have noted that the 2023-24 El Niño event was unusual due to its
469 significant oceanic warming, but relatively subdued Southern Oscillation and wind anomalies over the
470 tropical Pacific (Pang et al., 2025). This suggests that the event was not influenced by the traditional
471 Bjerknes feedback mechanism. According to these authors, the intense oceanic warming was mainly
472 caused by the accumulation of heat content in the western Pacific during the preceding prolonged La
473 Niña period, and they attributed the event to oceanic processes. In the terminology of this research, an
474 increased heat piled up in the western tropical Pacific is expected to contribute to increasing the stability
475 of the water column and, in turn, increase the reduced gravity. According to Pang et al. (2025), the 2023-
476 24 El Niño was dominated by interannual variability and the geostrophic approximation used here is only
477 able to capture variability over a time-scale longer than 3-4 years. However, it is interesting to note that,
478 according to equation (10), an increased reduced gravity determines a more efficient forcing of q -waves
479 by the rotational component of the dimensionless wind stress. In order to clarify this issue, more specific
480 approximations that allow for the derivation of an equation capable of capturing the interannual
481 variability of q -waves, based on, for instance, the quasi-geostrophic approximation used in Jin (1997),
482 are necessary.

483



484 **Appendix A: solution of equation (3) and derivation of equation (5)**

485 We have used dimensionless EOF analysis of the Z_{15} anomaly. This EOF algorithm is summarized
486 by the following equations

$$\begin{aligned} \mathbf{Z}(t) &= \sum_{m=1}^M \sqrt{\lambda_m} \alpha_m(t) \cdot \mathbf{Y}_m(x_i) \\ \alpha_n(t_j) &= \frac{1}{\sqrt{\lambda_n}} [\mathbf{Z}(t)]^T \cdot \mathbf{Y}_n(x_m) \end{aligned} \quad (\text{A.1})$$

487 that, for convenience we have rewritten in vector form defining the column vectors $\mathbf{Z}(t)$, whose i^{th}
488 element is $Z(x_i, t)$ ($i=1..M$), and \mathbf{Y}_m , whose i^{th} element is the value of the m^{th} ($m=1..M$) EOF at point x_i .
489 In equation (A.1), the suffix T indicates the transpose. After rewriting equation (3) in matrix form,
490 observing that \mathbf{Y}_k are eigenvectors of \mathbf{A} , with an obvious notation, expressing $\mathbf{w} = q_1 \mathbf{Y}_1 + \dots + q_M \mathbf{Y}_M$
491 $\mathbf{n} = b_1 \mathbf{Y}_1 + \dots + b_M \mathbf{Y}_M$ we have $q_k = b_k / \lambda_k$, where b_k is the projection of \mathbf{n} along the direction of the k^{th} EOF,
492 i.e. $b_k = \mathbf{n}^T \cdot \mathbf{Y}_k$. Therefore, $b_k = \mathbf{n}^T \cdot \mathbf{Y}_k = \int_0^T \frac{dt}{T} N_{34}(t) \cdot [\mathbf{Z}(t)]^T \cdot \mathbf{Y}_k = \sqrt{\lambda_k} \int_0^T \frac{dt}{T} N_{34}(t) \cdot \alpha_k(t)$ or

$$\mathbf{w} = \sum_{n=1}^M \frac{\mathbf{Y}_n}{\sqrt{\lambda_n}} \cdot \int_0^T \frac{dt}{T} N_{34}(t) \cdot \alpha_n(t) \quad (\text{A.2})$$

493 which is equation (5).

494 **Appendix B: determination of the reduced gravity field and first baroclinic mode velocity**

495 To compute the reduced gravity and the velocity of the first baroclinic mode we used the strategy
496 suggested by Eusebi Borzelli and Carniel (2023) and Eusebi Borzelli et al. (2024). Firstly, the ocean's
497 vertical structure was assumed to consist of two layers, and the density profiles were fitted with a step
498 function. This involved dividing each profile into two sub-segments of varying length and calculating
499 the average density for each segment. The resulting step function representations were then compared to
500 the original profile, and the one with the lowest root-mean-square was selected as the best step function
501 representation of the water column. This process was repeated for each date of the observation period,
502 providing spatial distributions of density in the surface ($\rho(x,y,t)$) and bottom ($r(x,y,t)$) layers and a “first
503 approximation” depth of the surface layer ($H^0(x,y,t)$). In the calculation of the velocity of the first
504 baroclinic mode, we excluded all points in which $H^0(x,y,t)$ was less deep than 60 m (with 60 m supposed
505 to be the maximum depth of the mixed layer) and $\rho(x,y,t) \geq r(x,y,t)$. This was done to avoid spurious results
506 due to density changes in the mixed layer and instabilities in the water column. The velocity of the first
507 baroclinic mode was obtained by solving the vertical mode equation (Wusch and Stammer, 1997), namely



$$\frac{d}{dz} \left[\frac{1}{N^2(x, y, z, t)} \cdot \frac{dP_n}{dz} \right] + \frac{1}{c^2_n(x, y, t)} P_n = 0 \quad (\text{B.1})$$

508 subject to rigid upper and lower boundary conditions, at each date of the observation period, in each point
 509 of the observation domain. In equation (B.1), $N^2(x, y, z, t)$ is the buoyancy frequency, $n=0, 1, \dots$, with $n=0$
 510 indicating the barotropic mode, and $1/c^2_n$ are real-valued, positive eigenvalues, with c_n indicating the
 511 velocity of the n^{th} baroclinic mode. In the final calculation of the depth of the surface layer, we excluded
 512 all points in which $H^{\theta}(x, y, t)$ was less deep than 60 m (with 60 m supposed to be the maximum depth of
 513 the mixed layer) and $\rho(x, y, t) \geq r(x, y, t)$. This was done to avoid spurious results due to density changes in
 514 the mixed layer and instabilities in the water column. **Appendix C: Solution of equation (10).**

515 Equation (1) was transformed in to a system of ordinary independent differential equations using
 516 the Fourier method. Observing that in equation (10) the latitude is a parameter, at every latitude it can be
 517 rewritten as

$$\frac{\partial q}{\partial t} - c_y(t) \cdot \frac{\partial q}{\partial x} = b_y(x, t) \text{ where } \begin{cases} c_y(t) = D \left(\frac{g' \cdot \beta}{f^2} \right) \\ b_y(x, t) = D \left(\frac{g'}{f} \right) \nabla^2 S - D \left(\frac{g' \cdot \beta}{f^2} \right) \frac{\partial S}{\partial y} \end{cases} \quad (\text{C.1})$$

518 Fixing the latitude, indicating with $Q(k, t)$ and $B(k, t)$ the Fourier transforms along the zonal directions of
 519 $q(x, t)$ and $b_y(x, t)$, we get a system of decoupled ordinary differential equation of the form

$$\frac{dQ}{dt} - ik \cdot c_y(t) Q = B(k, t) \text{ with initial condition } Q(k, t = 0) = Q_0(k) \quad (\text{C.2})$$

520 where $Q_0(k)$ is the Fourier transform of the initial condition $q(x, t=0) = q_0(x)$.

521 We solved equation (C.2) using the integrating factor. Namely, setting $\mu(t) = \exp \left[-ik \int_0^t c_y(s) \cdot \right.$
 522 $\left. ds \right]$ we have

$$Q(k, t) = \frac{Q_0(k) + \int_0^t ds B(k, s) \cdot \mu(s)}{\mu(t)} \quad (\text{C.3})$$

523

524 Code availability

525 Matlab scripts, developed for this research under Matlab release 2018a, can be downloaded at

526 <https://doi.org/10.6084/m9.figshare.30609104>



527

528 **Data availability**

529 Data used in this research can be downloaded succumbing to European Union (EU) regulations on
530 geophysical data exchange (see [https://www.copernicus.eu/en/international-cooperation-area-data-](https://www.copernicus.eu/en/international-cooperation-area-data-exchange)
531 [exchange](https://www.copernicus.eu/en/international-cooperation-area-data-exchange)).

532 Original ERA5 wind and SST data can be downloaded from the Copernicus data archive by
533 registered users at

534 [https://cds.climate.copernicus.eu/datasets/reanalysis-era5-single-levels-monthly-](https://cds.climate.copernicus.eu/datasets/reanalysis-era5-single-levels-monthly-means?tab=overview)
535 [means?tab=overview](https://cds.climate.copernicus.eu/datasets/reanalysis-era5-single-levels-monthly-means?tab=overview)

536 Original monthly T-S data were made available by the Institute of Atmospheric Physics (IAP) of the
537 Chinese Academy of Sciences (CAS) and can be downloaded the at the following web site

538 <http://www.ocean.iap.ac.cn/pages/dataService/dataService.html?navAnchor=dataService>

539

540 **Authors' contributions**

541 All the authors contributed equally to the work. G.L.E.B. and S.C. proposed the original idea and
542 designed the research. All authors contributed to analyze the data and to interpret the results. G.L.E.B.
543 and C.E.C. provided the figures. G.L.E.B. wrote the initial version of the manuscript, S.C., C.E.C. and
544 M.S. provided corrections and comments.

545

546 **Competing Interests**

547 The authors declare no competing interest.

548

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552

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557 **References**

- 558 An, S.-I., Kug, J.-S., Ham, Y.-G., Kang, I.-S.: Successive modulation of ENSO to the future greenhouse warming. *J.*
559 *Clim.*, 21, 3–21, doi: <https://doi.org/10.1175/2007JCLI1500.1>, 2008
- 560
561 Bjercknes, J.: Atmospheric teleconnections from the equatorial Pacific, *Mon. Wea. Rev.*, 97, 163–172, 1969
- 562
563 Burgers, G., Jin, F.-F., van Oldenborgh, G. J.: The simplest ENSO recharge oscillator, *Geophys. Res. Lett.*, 32,
564 L13706, doi: <https://doi.org/10.1029/2005GL022951>, 2005
- 565
566 Cai, W. et al.: ENSO and greenhouse warming, *Nat. Clim. Change*, 5, 849–859, doi:
567 <https://doi.org/10.1038/NCLIMATE2743>, 2015
- 568
569 Cai, W. et al.: Changing El Niño–Southern Oscillation in a warming climate, *Nature Reviews Earth & Environment*,
570 2(9), 628–644, doi: <https://doi.org/10.1038/s43017-021-00199-z>, 2022
- 571
572 Collins, M. et al.: The impact of global warming on the tropical Pacific Ocean and El Niño, *Nat. Geosci.*, 3, 391–
573 397, doi: <https://doi.org/10.1038/ngeo868>, 2010
- 574
575 Cane, M. A., Zebiak, S.: A Theory for El Niño and the Southern Oscillation, *Science*, 228, 4703, 1085–1087, doi:
576 <https://doi.org/10.1126/science.228.4703.108>, 1985
- 577
578 Capotondi, A., and P. D. Sardeshmukh, P. D.: Optimal precursors of different types of ENSO events, *Geophys. Res.*
579 *Lett.*, 42, 9952–9960, doi: <https://doi.org/10.1002/2015GL066171>, 2015
- 580
581 Capotondi, A., Ricciardulli, L.: The influence of pacific winds on ENSO diversity, *Sci. Rep.*, 11, 18672. doi:
582 <https://doi.org/10.1038/s41598-021-97963-4>, 2021
- 583
584 Carrillo, C. N.: Desertacion sobre las corrientes y estudios de la corriente Peruana de Humboldt, *Bol. Soc. Geogr.*
585 *Lima*, 11, 72–110, 1892
- 586
587 Cheng L., Trenberth, K., Fasullo, J., Boyer, T., Abraham, J., Zhu, J. : Improved estimates of ocean heat content from
588 1960 to 2015, *Science Advances*, 3, e1601545, doi: <https://doi.org/10.1126/sciadv.1601545>, 2017
- 589
590 Durack, P. J., Wijffels, S. E., Matear, R. J.: Ocean salinities reveal strong global water cycle intensification during
591 1950 to 2000, *Science*, 336(6080), 455–458. doi: <https://doi.org/10.1126/science.1212222>, 2012
- 592
593 Eusebi Borzelli, G. L., Carniel, S.: Where the winds clash: what is really triggering El Niño initiation?, *npj Clim.*
594 *Atmos. Sci.*, 6, 119, doi: <https://doi.org/10.1038/s41612-023-00445-9>, 2023
- 595
596 Eusebi Borzelli, G. L., Napolitano, E., Carillo, A., Struglia, M.V., Palma, M. and Iacono, R.: Hydrographic vs.
597 Dynamic Description of a Basin: The Example of Baroclinic Motion in the Ionian Sea, *MDPI-Oceans*, 5, 2, 383–
598 397, doi: <https://doi.org/10.3390/oceans5020023>, 2024
- 599
600 Fedorov, A. V., Philander, S. G.: A stability analysis of tropical ocean-atmosphere interactions: Bridging
601 measurements and theory for El Niño, *J. Clim.*, 14, 3086–3101. doi: [https://doi.org/10.1175/1520-0442\(2001\)014<3086:ASAOTO>2.0.CO;2](https://doi.org/10.1175/1520-0442(2001)014<3086:ASAOTO>2.0.CO;2), 2001
- 602
603
604 Graham, N. E.: Decadal-scale climate variability in the 1970s and 1980s: Observations and model results. *Climate*
605 *Dyn.*, 10, 135–162. doi: <https://doi.org/10.1007/BF00210626>, 1994
- 606
607 Hu, S., Fedorov, A. V.: Cross-equatorial winds control El Niño diversity and change, *Nat. Climate Change*, 8, 798–
608 802, doi: <https://doi.org/10.1038/s41558-018-0248-0>, 2018
- 609
610 Jiang, N., Neelin, J. D., Ghil, M.: Quasi-quadrennial and quasi-biennial variability in the equatorial Pacific, *Climate*
611 *Dynamics*, 12, 101–112, doi: <https://doi.org/10.1007/BF00223723>, 1995
- 612
613 Jin, F. F.: An equatorial ocean recharge paradigm for ENSO. Part I: conceptual model, *J. Atmos. Sci.*, 54, 811–829,
614 doi: [https://doi.org/10.1175/1520-0469\(1997\)054<0811:AEORPF>2.0.CO;2](https://doi.org/10.1175/1520-0469(1997)054<0811:AEORPF>2.0.CO;2), 1997



615
616 Jin, F.-F., Kim S. T., Bejarano, L.: A coupled-stability index for ENSO, *Geophys. Res. Lett.*, 33, L23708, doi:
617 <https://doi.org/10.1029/2006GL027221>, 2006
618
619 Large, W. G., and Pond, S.: Open ocean momentum flux measurements in moderate to strong winds. *Journal of*
620 *physical oceanography*, 11(3), 324-336. doi: [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0485(1981)011<0324:OOMFMI>2.0.CO;2)
621 [0485\(1981\)011<0324:OOMFMI>2.0.CO;2](https://doi.org/10.1175/1520-0485(1981)011<0324:OOMFMI>2.0.CO;2), 1981
622
623 Liu, Z., Vavrus, S., He, F., Wen, N. & Zhong, Y.: Rethinking tropical ocean response to global warming: the enhanced
624 equatorial warming, *J. Clim.* 18, 4684–4700, doi: <https://doi.org/10.1175/JCLI3579.1>, 2005
625
626 Morse, P. M., Feshbach, H.: *Methods of Theoretical Physics*, McGraw-Hill, 1953
627
628 Newman, M., Sardeshmukh, P. D. Penland C.: How important is air-sea coupling in ENSO and MJO evolution, *J.*
629 *Clim.*, 22, 2958–2977, doi: <https://doi.org/10.1175/2008JCLI2659.1>, 2009
630
631 Newman, M., Shin, S.-I., and M. A. Alexander M. A.: Natural variation in ENSO flavors, *Geophys. Res. Lett.*, 38,
632 L14705, doi: <https://doi.org/10.1029/2011GL047658>, 2011
633
634 Peng, Q., S.-P. Xie, D. Wang, Y. Kamae, H. Zhang, S. Hu, X.-T., Zheng, Wang, W.: Eastern Pacific wind effect on
635 the evolution of El Niño: Implications for ENSO diversity, *J. Climate*, 33, 3197–3212, doi:
636 <https://doi.org/10.1175/JCLI-D-19-0435.1>, 2020
637
638 Peng, Q., Xie, S. P., Miyamoto, A., Deser, C., Zhang, P., Luongo, M. T.: Strong 2023–2024 El Niño generated by
639 ocean dynamics, *Nat. Geosci.*, 18, 471–478, doi: <https://doi.org/10.1038/s41561-025-01700-9>, 2025
640
641 Penland, C., Sardeshmukh P. D.: The optimal growth of tropical sea surface temperature anomalies, *J. Clim.*, 8,
642 1999–2024, doi: [https://doi.org/10.1175/1520-0442\(1995\)008<1999:TOGOTS>2.0.CO;2](https://doi.org/10.1175/1520-0442(1995)008<1999:TOGOTS>2.0.CO;2), 1995
643
644 Périgaud, C., Zebiak, S. E., Mélin, F., Boulanger, J.-P., and Dewitte, B.: On the role of meridional wind anomalies
645 in a coupled model of ENSO, *J. Climate*, 10, 761–773, doi: [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0442(1997)010,0761:OTROMW.2.0.CO;2)
646 [0442\(1997\)010,0761:OTROMW.2.0.CO;2](https://doi.org/10.1175/1520-0442(1997)010,0761:OTROMW.2.0.CO;2), 1997
647
648 Philander, S. G. H., Pacanowski, R. C.: The oceanic response to cross-equatorial winds (with application to coastal
649 upwelling in low latitudes), *Tellus*, 33A, 201–210, doi: <https://doi.org/10.3402/tellusa.v33i2.10708>, 1981
650
651 Philander, S. G.: *El Niño, La Niña and the Southern Oscillation*, Academic Press, New York, 289 pp., 1990
652
653 Picaut, J., Delcroix, T.: Equatorial wave sequence associated with warm pool displacements during the 1986-1989
654 El Niño-La Niña, *J. Geophys. Res.*, **100**(C9), 18393-18408. doi: <https://doi.org/10.1029/95JC01358>, 1995
655
656 Quinn, W. H., Neal, V.T.: Recent climate change and the 1982–83 El Niño, *Proc. Eighth Annual Climate Diagnostic*
657 *Workshop*, Downsview, ON, Canada, NOAA, 148–154, 1984
658
659 Quinn, W. H., Neal, V.T.: Recent long-term climate change over the eastern tropical and subtropical Pacific and its
660 ramifications, *Proc. 9th Annual Climate Diagnostic Workshop*, Corvallis, OR, NOAA, 101–109, 1985
661
662 Rasmusson, E. M., Wang, X., Ropelewski, C. F.: The biennial component of ENSO variability, *J. Mar. Systems*, 1,
663 71-96, doi: [https://doi.org/10.1017/0924-7693\(90\)90153-2](https://doi.org/10.1017/0924-7693(90)90153-2), 1990
664
665 Santoso, A., Mcphaden, M. J., Cai, W.: The defining characteristics of ENSO extremes and the strong 2015/2016
666 El Niño, *Rev. Geophys.*, **55**(4), 1079-1129. doi: <https://doi.org/10.1002/2017RG000560>, 2017
667
668 Trenberth, K. E.: Recent observed interdecadal climate changes in the Northern Hemisphere, *Bull. Amer. Meteor.*
669 *Soc.*, 71, 988–993, 1990
670
671 Trenberth, K. E., and J. W. Hurrell, J. W.: Decadal atmospheric–ocean variations in the Pacific, *Climate Dyn.*, 9,
672 303–309. doi: <https://doi.org/10.1007/BF00204745>, 1994
673



- 674 Wang, C. and Fiedler, P.C.: ENSO Variability and the Eastern Tropical Pacific: A Review, *Progress in Oceanography*,
675 69, 239-266. doi: <https://doi.org/10.1016/j.pocean.2006.03.004>, 2006
676
- 677 Wang, H., Zheng, X. T.: Interdecadal Variability of the Meridional Wind across the Eastern Equatorial Pacific and
678 Its Relationship with ENSO, *Journal of Climate*, 36(12), 4189-4202, doi: <https://doi.org/10.1175/JCLI-D-22-0516.1>,
679 2023
680
- 681 Wang, H., Hu, S., Guan, C., Li, X.: The role of sea surface salinity in ENSO forecasting in the 21st century, *npj Clim.*
682 *Atmos. Sci.*, 7, 206. doi: <https://doi.org/10.1038/s41612-024-00763-6>, 2024
683
- 684 Wyrski, K.: El Niño—The dynamic response of the equatorial Pacific Ocean to atmospheric forcing, *J. Phys.*
685 *Oceanogr.*, 5, 572–584, 1975
686
- 687 Wusch, C., Stammer, D.: Atmospheric loading and the oceanic “inverted barometer” effect, *Rev. Geophys.*, 35, 1,
688 79-107, doi: <https://doi.org/10.1029/96RG03037>, 1997
689
- 690 Xie, S.-P. et al.: Global warming pattern formation: Sea surface temperature and rainfall, *Journal of Climate*, 23,
691 966–986, doi: <https://doi.org/10.1175/2009JCLI3329.1>, 2010
692
- 693 Xie, S. P., Peng, Q., Kamae, Y., Zheng, X. T., Tokinaga, H., Wang D.: Eastern Pacific ITCZ dipole and ENSO
694 diversity, *Journal of Climate*, 31(11), 4449-4462, doi: <https://doi.org/10.1175/JCLI-D-17-0905.1>, 2018
695
- 696 Zhong, W., Sullivan, A., Eusebi Borzelli, G.L., Li, Z.: Early signs of strong El Niño–Southern Oscillation episodes,
697 *Sci. Rep.*, 15, 17225, doi: <https://doi.org/10.1038/s41598-025-01809-2>, 2025
698
- 699 Zhi, H., Zhang, R.H., Dong, M., Wu, M.: Upper ocean salinity and temperature changes and their contributions to
700 the stratification in the tropical Pacific under global warming, *Clim. Dyn.*, 63, 93, doi:
701 <https://doi.org/10.1007/s00382-024-07570-y>, 2025