



1 **Milankovitch Forcing and Nonlinear Climate Variability during the**
2 **Late Givetian (Appalachian Basin, New York, USA)**

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10 **Key Points:**

- 11 - High- and low-latitude climatic and hydrological teleconnections shaped Late Givetian
12 climate variability
- 13 - Linear and nonlinear (half)precession-obliquity interactions governed climate-
14 sediment responses in the pantropical belt
- 15 - Astronomical forcing paced regional events and the timing of the Frasnian Crisis in the
16 Appalachian Basin



17 **Abstract**

18 Astronomical forcing is a major driver of Earth's climate variability, yet the linear and
19 nonlinear climate responses to this forcing under warmer-than-present conditions remain
20 poorly constrained. We use cyclostratigraphy of the Sherburne Formation, a Givetian record
21 from the Appalachian Basin, to characterize Milankovitch cyclicity and evaluate the complex
22 climatic behavior inferred from the sedimentary record. A new cyclostratigraphic age model
23 refines the timing of the regional Fir Tree, Hubbard Quarry and Lodi events and places the
24 onset of the global Frasnian Crisis (represented by the regional Lodi Event) into an
25 astronomically calibrated framework. Our results reveal precession-eccentricity-paced detrital
26 influx, obliquity amplification, precession-obliquity interference patterns, half-precessional
27 cyclicity, and nonlinear climate-sediment dynamics. These findings show how pantropical late
28 Givetian climate variability is shaped by high- and low-latitude climatic and hydrologic
29 teleconnections and highlight the sensitivity of Devonian climate to orbital variability.

30 **Keywords:** Cyclostratigraphy, Devonian, Orbital Forcing, Nonlinear, Half Precession



31 **Plain Language Summary**

32 Earth's climate is influenced by predictable changes in its orbit around the Sun and
33 variations in its rotational axis. These are known as Milankovitch cycles (precession, obliquity
34 and eccentricity) and shape climate patterns over tens of thousands to millions of years. We
35 studied rocks from the Sherburne Formation in the Appalachian Basin (New York State, USA)
36 to see how these orbital cycles affected climate during the late Givetian, about 380 million
37 years ago, when Earth's climate was in a warmer-than-present state. We show that the late
38 Givetian climate responded strongly to changes in the Earth's orbit. The rocks recorded clear
39 signals of precession, obliquity, and eccentricity, including complex interactions and amplified
40 responses that point to nonlinear climate behavior. Using these patterns, we built a new
41 timeline for several important events during the investigated interval. Overall, our results reveal
42 that the late Givetian climate was highly sensitive to orbital variations, and that these
43 astronomical rhythms played a key role in shaping environmental change and biological
44 turnover.



45 **1. Introduction**

46 Earth's climate system is fundamentally shaped by interactions among astronomical
47 forcing, large-scale atmospheric and oceanic circulation, the hydrological cycle, and internal
48 feedbacks (e.g., Saltzman, 2002). Astronomical forcing refers to the modulation of incoming
49 solar radiation (insolation) caused by quasi-periodic variations in Earth's orbital parameters –
50 precession, obliquity, and eccentricity (Milankovitch 1941). These 'predictable' Milankovitch
51 cycles alter both the amount and latitudinal distribution of insolation (Berger, 1987; 1988;
52 Laskar et al., 2004), strongly influencing seasonality and long-term climate patterns, and they
53 form a cornerstone of our understanding of past climate change (e.g., Hays et al., 1976).
54 However, the climatic expression of astronomical forcing is rarely a simple linear response to
55 insolation changes (Rial et al., 2004). Complex Earth-system dynamics can modulate, amplify
56 or reshape orbital signals across a wide range of timescales (e.g., Imbrie and Imbrie, 1980;
57 Paillard, 1998). Such relationships are increasingly well understood in more recent Cenozoic
58 records (e.g., Lourens et al., 2005; Sullivan et al., 2023) but less so in the Paleozoic (De
59 Vleeschouwer et al., 2024). Recent work has documented the influence of orbitally forced
60 climatic cycles on Devonian paleoenvironmental patterns (e.g., De Vleeschouwer et al., 2012;
61 2014; Da Silva et al., 2020; Wichern et al., 2024; Gérard et al., 2025; 2026; Huygh et al.,
62 2026), but with a focus on major anoxic or extinction intervals (e.g., the Kellwasser Crisis).
63 Typically, cyclostratigraphic studies apply linear time-series analysis and spectral tools, such
64 as bandpass filtering and continuous wavelet transforms (e.g., De Vleeschouwer et al., 2012;
65 Laurin et al., 2015; Arts et al., 2024; Spiering et al., 2024), to detect Milankovitch pacing of
66 sedimentary cyclicity. Such approaches, however, are not designed to resolve the nonlinear
67 feedbacks which may be responsible for the observed variability. Consequently, their influence
68 on the expression of orbital forcing in Paleozoic climate records remains poorly constrained.

69 In this work, we investigate how astronomical forcing shaped late Givetian
70 paleoclimate using an approach that allows us to detect both linear and potential nonlinear
71 expressions of Milankovitch cyclicity preserved within the Sherburne Formation (lower

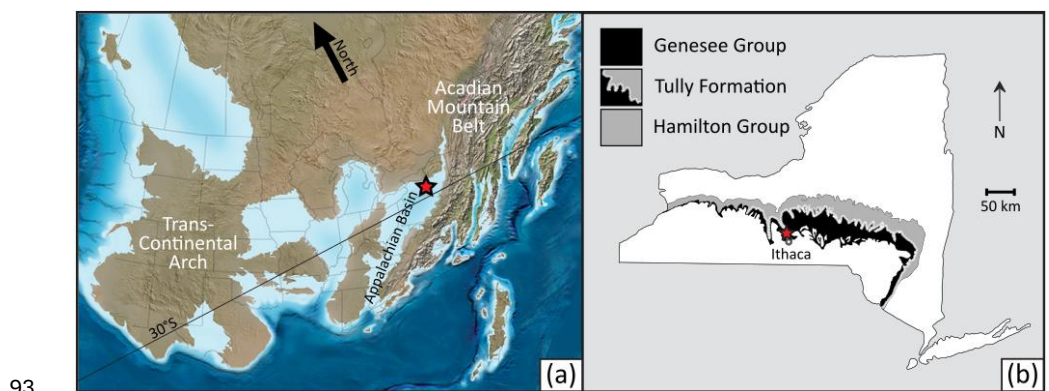


72 Genesee Group) of central New York State (Baird et al., 2023). The Sherburne Formation
73 represents a well-preserved archive of late the Givetian subtropical Appalachian Basin,
74 making it well suited for evaluating the expression of orbital forcing outside major extinction
75 intervals. Within this framework, we employ high-resolution proxies for detrital input, to analyze
76 the character and frequency structure sedimentary cycles observed within the Sherburne
77 Formation and develop two complementary floating astrochronologies. In addition, we put the
78 regional Fir Tree, Hubbard Quarry and Lodi eustatic and hypoxic events into an integrated
79 sequence- and cyclostratigraphic framework and assess phase relationships between
80 astronomical forcing and paleoclimatic response. Together, these analyses illustrate a
81 workflow that may be broadly applicable to Paleozoic climate archives and show how
82 astronomical forcing and internal Earth-system dynamics interacted to shape the late Givetian
83 paleoclimate.



84 **2. Geological Setting**

85 The Cargill Salt Company Test Core #17 (hereafter Cargill #17 Core) was drilled in
86 1977 near Lansing, Tomkins County, southern Cayuga Lake area in central New York State,
87 USA (42°31'22.9" N, 76°30'17.5" W) and spans ~847 m of strata, providing a detailed
88 sedimentary record through the upper Silurian to Middle Devonian strata of the northern
89 Appalachian Basin. Deposition of the Sherburne Formation (uppermost Givetian) occurred in
90 a foredeep setting of this foreland basin, which developed during early Tectophase 4 of the
91 Acadian Orogeny and lay within an expanded subtropical zone at approximately 30° S
92 paleolatitude (Fig. 1; Ver Straeten, 2010; Baird et al., 2023; Ver Straeten et al., 2023).



93
94 **Fig. 1. Geological setting of the Cargill #17 Core.** a) Middle Devonian paleogeographic map adapted from
95 Blakey, 2014 (~380 Ma). b) Outcrop belt for the Genesee, Tully and Hamilton in the Appalachian Basin of New York
96 State. Location of the Cargill #17 Core, just north of Ithaca, is indicated by a red star. Figure adapted from Zambito
97 et al. (2016).

98 The depositional setting of the Sherburne has been interpreted in various ways,
99 traditionally characterized as part of the northern Appalachian Basin Portage Magnafacies that
100 formed on the distal shelf, slope, and proximal basin through turbiditic processes (Rickard,
101 1975; deWitt and Colton, 1978; see summary in Baird et al., 2023). However, recent work by
102 Wilson and Schieber (2014; 2015; 2017) has interpreted the turbidites of the Sherburne
103 Formation in the Cargill #17 core to more specifically represent fluvial-discharge events
104 deposited in a storm-dominated proximal shale setting through hyperpycnal processes with a



105 high sedimentation rate. Importantly for this study, hyperpycnites are dependent on flood
106 frequency and magnitude, and therefore climate (Mulder et al., 2003).

107 The uppermost part of the Cargill #17 Core covers ~41.3 m of the Upper Givetian
108 Sherburne Formation, attributed to the upper portion of the third-order sequence Giv-5 (Brett
109 et al., 2011). Lithostratigraphic correlations and conodont biostratigraphy date the Sherburne
110 Formation from 379.2 to 380.0 Ma (*K. disparilis* to *S. norrisi* zones) (Kirchgasser, 1994; Brett
111 et al., 2011; Becker et al., 2020). Stratigraphically, the Sherburne Formation in the southern
112 Cayuga Lake area comprises the Fir Tree, Hubbard Quarry, and Lodi members, as well as an
113 upper, unnamed Penn Yan Formation-equivalent that is not present in the Cargill #17 Core
114 (Fig. 2; Zambito et al., 2009; Baird et al., 2023). The Sherburne Formation is a time
115 transgressive unit, the base of which generally gets older to the east and south along the
116 outcrop belt in the northern Appalachian Basin and replaces the basinal shale of the Penn Yan
117 Formation through progradation (Baird et al., 2023). The Fir Tree Member (lower *K. disparilis*
118 conodont Zone) in this core consists of medium gray calcareous siltstones to laminated silt
119 and dark shales, marking the onset of subsequence Giv-5D and representing a 3rd order late
120 highstand systems tract (LHST) (previously designated as Giv-5C Brett et al., 2011; but
121 elevated to Giv-5D in Baird et al., 2023). The base of the Fir Tree (subsequence Giv-5D
122 boundary; Fig. 2) is a widely recognized erosion surface marked in cratonic successions by
123 deep incision, for example at the base of the Coralville Formation of the Cedar Valley Group
124 in Iowa (Witzke et al., 1988; Witzke and Bunker, 1996, 1997). The Fir Tree Event therefore
125 represents a regionally recognized event in at least eastern North America, however this event
126 is poorly characterized and not recognized in most recent tabulations of Devonian events (e.g.,
127 Becker et al., 2016, 2020; Baird et al., 2023) and may have been conflated with the Genesee
128 Event of the Taghanic Crisis in studies outside of the Appalachian basin (the Genesee Event
129 is now understood to have been earlier in the *S. hermanni* Zone). However, some workers
130 have noted the beginnings of decline of reefal organisms associated with widespread anoxia
131 toward the end of the *K. disparilis* or *P. dengleri* Zone, with reefal collapse noted at the end of



132 the Givetian (Copper and Scotese, 2003); it also marks the end of most trilobites in the
133 Appalachian Basin, notably *Dipleura* (Zambito et al., 2015; Baird et al., 2023).

134 The contact between the Fir Tree and the overlying Hubbard Quarry Member (at 38.3
135 m depth; Fig. 2) marks a maximum starvation surface (MSS) and minor discontinuity (Brett et
136 al., 2011; Baird et al., 2023); using the sequence stratigraphic model proposed by Zambito et
137 al. (2009) for these strata, the transgression continues through to the base of the middle
138 Hubbard Quarry, which is identified as the maximum flooding surface (MFS) at 28.3 m depth
139 (Fig. 2). While in more distal settings within the Appalachian Basin the deepest, most anoxic
140 conditions of the Hubbard Quarry occur at or near the contact with the Fir Tree, progradation
141 into the study location means the environmental expression of the Hubbard Quarry occurs
142 closer to the MFS (Fig. 2). The Fir Tree – Hubbard Quarry Member succession (*K. disparilis*
143 to *P. dengleri saggita* conodont zones) therefore represents a 3rd order transgressive to
144 highstand to falling stage systems tracts (TST-HST-FSST) (Brett et al., 2011; Baird et al.,
145 2023). It comprises: (i) lower Hubbard Quarry dark gray shales with light gray silty stringers,
146 (ii) a middle subunit composed of alternating dark and lighter gray shales containing crinoids
147 and, (iii) upper Hubbard Quarry gray calcareous siltstones. From 17.7 m upwards, thin traces
148 of cross-lamination are visible, suggesting a higher-energy environment, interpreted as storm-
149 influenced hyperpycnites by Wilson and Schieber (2014; 2015; 2017). After an initial
150 deepening (lower Hubbard Quarry through lowest middle Hubbard Quarry Member), the
151 middle-upper Hubbard Quarry Member displays a significant regressive phase of sediment
152 aggradation (Fig. 2; Baird et al., 2023).

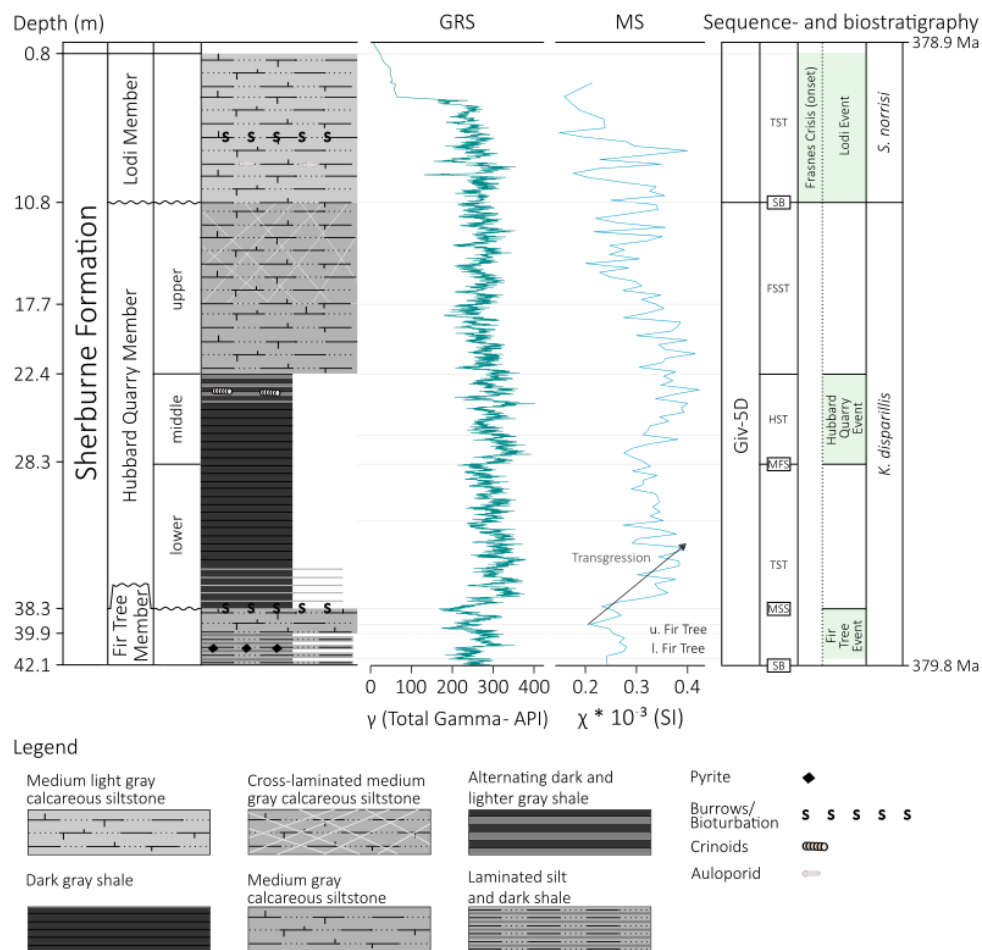
153 The Lodi Member (10.8 m to 0.8 m depth, *P. dengleri dengleri* to *S. norrisi* conodont
154 zones) consists of medium light gray, slightly bioturbated, calcareous siltstone with abundant
155 *Aulopora* and represents a 3rd order transgressive systems tract (TST) (Brett et al., 2011). The
156 onset of the Frasnian Crisis (Becker et al., 2020) coincides with the base of the Lodi Member
157 and is marked by the regional Lodi Event, which represents another major lowstand sequence
158 boundary. Indeed, a major incised erosion surface of up to 18 meters is observed at the base



159 Lithograph City Formation (middle Cedar Valley Group) in Iowa (Witzke et al., 1988; Witzke
160 and Bunker, 1996, 1997). The uppermost Lodi Member (*S. norrisi* conodont Zone, uppermost
161 Givetian) is absent in the Cargill #17 Core, so the Givetian-Frasnian boundary is most likely
162 not recorded. The uppermost ~3.8 m of the core are fragmented, with multiple missing
163 intervals.

164 The Frasnian Crisis was multi-phased with three pulses of extinction, each associated
165 with a transgression and widespread dysoxic-anoxic events. The first phase occurred at the
166 later *P. dengleri* to *S. norrisi* zone, the age of the Lodi Member and just prior to the Givetian-
167 Frasnian boundary. The largest phase is associated with black shales of the early Frasnian
168 MN-1 zone and a final event in the lower MN-2 zone (see e.g., Klapper, 1989 regarding
169 Montagne Noire (MN) conodont zonation). The early phase, which is regionally called the Lodi
170 Event, includes major ammonoid extinction and termination of reef growth in many areas
171 (Becker et al., 2016, 2020).

172 The Sherburne Formation records environmental characteristics of the late Givetian.
173 This interval is broadly regarded as a warm-temperate greenhouse world (Becker et al., 2020),
174 although recent work by Dahl et al. (2022) challenges this view: CO₂ reconstructions and
175 climate-sensitivity modeling suggests that the Givetian climate may have been cooler and
176 more variable than previously thought. The Givetian was marked by the expansion of tree-like
177 terrestrial vegetation (e.g., *Archaeopteris*; Stein et al., 2020), and considerable faunal turnover
178 that shaped evolutionary steps in the marine realm (Raup and Sepkoski, 1982; House 2002;
179 Brett et al., 2020; Becker et al., 2020; Ver Straeten et al., 2023). Regionally, the Sherburne
180 Formation captures environmental variability following the major, second-order Taghanic
181 Crisis and leading into the onset of the second-order Frasnian Crisis (Brett et al., 2011; 2020;
182 Zambito et al., 2012, 2016; Becker et al., 2016, 2020; Baird et al., 2023). These broader
183 climatic and biotic conditions provide the environmental backdrop against which the
184 Sherburne Formation's cyclicity is evaluated.



185

186 **Fig. 2. Integrated stratigraphy of the Sherburne Formation in the Cargill #17 Core.** Stratigraphy, lithological
 187 column, gamma ray spectrometry (GRS, total gamma – API), magnetic susceptibility (MS, SI – Kappa * 10⁻³),
 188 sequence stratigraphy; subsequence Giv-5D, sequence boundary (SB), maximum starvation surface (MSS),
 189 highstand systems tract (HST), falling stage systems tract (FSST), transgressive systems tract (TST) from Brett et
 190 al. (2011) and Baird et al. (2023), event stratigraphy, conodont zonation (Kirchgasser, 1994), and numerical ages
 191 based on the conodont zonation (Becker et al., 2020).



192 **3. Materials and Methods**

193 **3.1. Gamma-ray Spectrometry**

194 High-resolution gamma ray spectrometry (GRS) total gamma ‘ γ ’ (API units) was
195 acquired at ± 0.013 m spacing using a Core Lab Instruments Gamma Logger at the
196 Department of Geosciences at the University of Cincinnati (Ohio, USA). The γ -signal is
197 proportional to the naturally occurring γ -radiation of the sample and integrates contributions
198 primarily from ^{40}K , ^{232}Th and ^{238}U (Killeen, 2015). It represents an amalgamated signal
199 dominated by ^{40}K (and to a lesser extent by ^{232}Th), typically associated with clay-rich, detrital
200 material, and by ^{238}U , which is often enriched in organic-rich intervals. Across most of the
201 Sherburne Formation, the γ -signal is a reliable proxy for detrital input, with minor organic
202 contributions restricted mostly to dark gray shales of the lower and middle Hubbard Quarry
203 members.

204 **3.2. Magnetic Susceptibility**

205 Magnetic susceptibility (MS; ‘ χ ’ in SI-units Kappa 10^{-3}) was measured at ± 0.3 m
206 spacing using Beloit College’s handheld Terraplus KT-10R v2 meter while the core was on
207 loan at the University of Cincinnati. The χ -signal represents the degree of magnetization of a
208 material in response to an applied external magnetic field, which is commonly dominated by
209 paramagnetic and ferromagnetic minerals which are typically enriched in detrital fractions of
210 sedimentary rocks (Ellwood et al., 2000). When primary, the χ -signal also serves as a proxy
211 for detrital input (Da Silva et al., 2009; 2012; De Vleeschouwer et al., 2012).

212 **3.3. Statistical Approaches**

213 Data treatment and statistical testing were performed in R Studio (version
214 2025.05.0+496). Time series and spectral analyses used “Astrochron” (Meyers, 2014) and
215 “WaverideR” (Arts, 2023). GRS γ - and MS χ -signals were linearly interpolated and detrended
216 using the `detrend()` or `noLow()` functions. Power spectral density was estimated via the multi-
217 taper method (MTM; Thomson, 1982; Meyers, 2012). Significance testing employed AR(1)



218 models with a Bonferroni correction at the 90 %, 95 %, and 99 % confidence levels, assuming
219 an AR(1) process as the null hypothesis. Evolutive spectral analysis was carried out primarily
220 using continuous wavelet transforms (CWT; Arts, 2023; Arts et al., 2024), suited for capturing
221 both frequency and depth/time localization in non-stationary signals, across a range of
222 cyclicities, though with limited frequency resolution. Normalized evolutive harmonic analysis
223 (EHA) and evolutive power spectral analysis (EPSA) ('eha' function, Meyers et al., 2001)
224 tracked spectral features through time, highlighting oscillation magnitude and frequency
225 strength. Taner bandpass filters isolated components of interest. Hilbert transforms were
226 applied to filtered signals to assess envelopes, allowing for assessment of amplitude
227 modulation patterns. Focus was placed on amplitude modulation patterns of precession,
228 obliquity and short eccentricity cycles by extracting higher-order cycles from the envelope of
229 hierarchically shorter cycles. To avoid convoluted phrases, for example, SE(i) is used to
230 denote the '100-kyr short eccentricity cycle, recovered indirectly (i.e., 'i') from the envelope of
231 precession'.

232 TimeOpt, an inverse modeling approach designed primarily for the evaluation of
233 eccentricity-related amplitude modulation and bundling, was used to estimate sedimentation
234 rates. This method enables astronomical tuning by identifying an optimal sedimentation rate
235 that simultaneously optimizes (i) amplitude modulation of precession (or short eccentricity) by
236 eccentricity, and (ii) concentration of spectral power at target orbital frequencies (Meyers,
237 2015). An average climatic precession target frequency of 0.0525 kyr^{-1} ($\sim 19.1 \text{ kyr}$) was
238 calculated based on estimates by Waltham (2015) at 380 Ma.

239 Nonlinear interactions were assessed using bicoherence analysis, a high-order
240 spectral method capable of identifying quadratic phase coupling (Hasselmann et al., 1963;
241 Kim and Powers, 1979; Hinich, 1982; Choudhury et al., 2008; Sullivan et al., 2023). This
242 approach detects a third, new frequency that arises from Milankovitch combination tones; sum
243 ($f_3 = f_1 + f_2$) and difference ($f_3 = f_1 - f_2$) tones (e.g., Hagelberg et al., 1991; von Döbeneck and
244 Schmieder, 1999; Da Silva et al., 2018; Sullivan et al., 2023).



245 **4. Results**

246 4.1. *Gamma-ray Spectrometry*

247 The γ -values fluctuate between 200-350 API across the Sherburne Formation, except
248 in the fragmented upper Lodi Member, which is excluded from further analysis. The lowest
249 values occur in the laminated siltstones to shales and calcareous siltstones of the Fir Tree
250 Member, oscillating strongly around a \sim 250 API baseline. A pronounced shift to higher γ -values
251 marks the base of the overlying Hubbard Quarry Member at 38.3 m, followed by fluctuations
252 around a slightly declining \sim 300 API baseline. The transition from the lower to middle Hubbard
253 Quarry Member (28.3 m) is marked by the highest γ -values, reaching approximately 400 API
254 (MSS; Fig. 2), after which values progressively decrease through the upper Hubbard Quarry
255 Member. In the Lodi Member, γ -values fluctuate around 250-300 API (Fig. 2). Superimposed
256 on these larger-scale trends are prominent 0.5-1.5 m bundles, in turn grouped into meter- to
257 decameter-scale rhythmic packages.

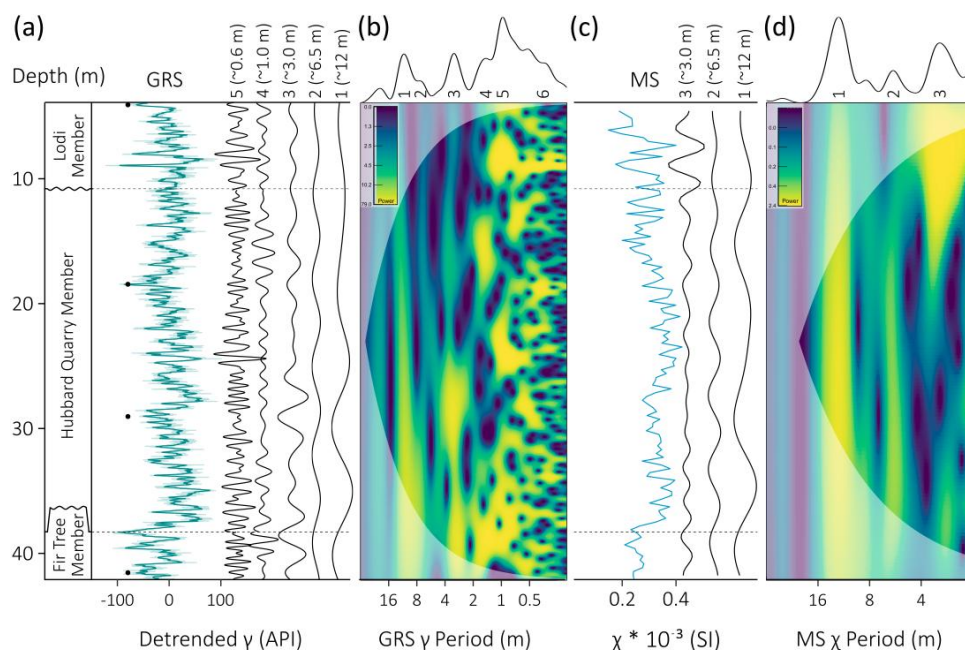
258 4.2. *Magnetic Susceptibility*

259 The Fir Tree Member shows consistently low χ -values (\sim 0.25 SI). A pronounced
260 increase marks the transition to the overlying lower Hubbard Quarry Member, followed by a
261 gradual decline toward the middle Hubbard Quarry Member (28.3 m; Fig. 2). χ -values rise
262 again to \sim 0.40 SI near the base of the upper Hubbard Quarry Member, then decrease to \sim 0.20
263 SI in its middle portion. From the middle of the upper Hubbard Quarry Member into the
264 overlying Lodi Member, χ -values display strongest variability, ranging from 0.2 to 0.4 SI in the
265 middle part of the Lodi Member (Fig. 2). Similar to the γ -signal, meter- to decameter-scale
266 rhythmicity is superimposed on these larger-scale trends in the χ -signal.



267 **5. Cyclostratigraphy**

268 **5.1. Depth-domain Cyclostratigraphy**



269

270 **Fig. 3. Depth-domain cyclostratigraphy of the Sherburne Formation.** a) Stratigraphy, detrended GRS γ -signal
 271 (light cyan) and 7-running average γ -signal (cyan), and bandpass filter output of key components 1 to 5 (black) and
 272 their corresponding mean periodicities (m). Components 3 to 5 were extracted separately for each member. Black
 273 dots indicate interpreted local minima in long-term cyclicity. b) GRS γ continuous wavelet transform and average
 274 wavelet power spectrum. c) MS χ -signal (blue) and bandpass filter output of key components 1 to 3 (black) and
 275 their corresponding mean periodicities (m). d) MS χ continuous wavelet transform and average wavelet power
 276 spectrum.

277 A CWT applied to the detrended γ -signal (Fig. 3a) reveals about six significant
 278 components exhibiting elevated wavelet power that appear significant versus 90 % AR(1)
 279 confidence level (MTM in Fig. S1). Although spectral power varies locally, mean periods
 280 remain relatively stable throughout the Sherburne Formation (Fig. 3b). Taner bandpass
 281 filtering extracted five components from the detrended γ -signal: 1 (~12 m), 2 (~6.5 m), 3 (~3.0
 282 m), 4 (~1.0 m) and 5 (~0.6 m) (Fig. 3a). To account for minor mean frequency shift of



283 components 4 and 5, filtering was applied separately to each member, centering the window
284 around intervals of highest spectral power. At the Fir Tree-Hubbard Quarry and Hubbard
285 Quarry-Lodi contacts, a discrepancy in these components (Fig. 3) is interpreted as the
286 expression of the minor discontinuities present (Baird et al., 2023).

287 A similar approach applied to the MS χ -signal (Fig. 3d) identified three key components
288 with mean periodicities of ~ 12 , ~ 6.5 , ~ 3.0 , and ~ 1 m. Of these, component 1 is statistically
289 significant (90 % AR(1); Fig. S1). A fourth ~ 1.0 -m component was also detected (Fig. S1) but
290 excluded from interpretation due to low signal resolution. Taner bandpass filtering was used
291 to extract three key signals (Fig. 3c).



292 5.2. *Cyclostratigraphic Age Models*

293 Milankovitch cycles are essential for constructing astronomical age models, and a key
294 characteristic is their well-defined hierarchical structure, expressed through time-dependent
295 frequency ratios. For the late Givetian (~380 Ma), average durations are: 405-kyr long
296 eccentricity, 173-kyr long obliquity, ~100-kyr short eccentricity, 34.3-kyr obliquity, and ~19.1-
297 kyr precession, yielding ratios of 1.0:1.8:5.2:9.1:21.2 that reflect their hierarchical structure.
298 Components 1 to 5 in the γ -signal (Fig. 3b) exhibit ratios of 1.0:1.7:5.0:10.0:20.0, strongly
299 suggesting the imprint of Milankovitch cyclicity. Similar periodicities in components 1 to 3 of
300 the χ -signal further support this interpretation. Accordingly, the Sherburne Formation spans
301 ~1.2 Myr at an average sedimentation rate of ~3 cm/kyr.

302 TimeOpt (0.2 to 4.0 cm/kyr; Meyers, 2015) was applied to test for amplitude modulation
303 of precession by eccentricity and of short eccentricity by long eccentricity. For the γ -signal,
304 average sedimentation rates of 3.29 and 3.39 cm/kyr were obtained, respectively (r^2_{opt} ; Fig.
305 S2 and S3). In complement, TimeOpt testing for amplitude modulation of short eccentricity by
306 long eccentricity, applied to the χ -signal, yielded an average sedimentation rate of 3.71 cm/kyr
307 (r^2_{opt} ; Fig. S4). These estimates agree closely with the frequency-ratio estimates,
308 strengthening the cyclostratigraphic interpretation. Conodont biostratigraphy (*K. disparilis* and
309 *S. norrisi*; ~900 kyr; Becker et al., 2020) suggest comparable rates, well within the same order
310 of magnitude (Fig. 2).

311 For the Late Givetian, the 405-kyr eccentricity 'metronome' remains the most stable
312 and reliable Milankovitch cycle, even when considering the possibility that it could have been
313 temporarily disrupted (Zeebe and Lantink, 2024). Accordingly, minimal tuning to the 405-kyr
314 eccentricity was applied to the γ -signal (see black dots on Fig. 3a), guided by four local minima
315 in the bandpass filter output of component 1 (Fig. 3b), interpreted to reflect 405-kyr long
316 eccentricity. In the absence of an astronomical solution due to solar system chaos (Laskar,
317 2020), this approach provides the most reliable duration estimate. Using only four depth-time
318 tie-points minimizes manipulation of the original γ -signal and preserves frequency modulation



319 (e.g., precession frequency modulation by eccentricity). This age model (hereafter AM1) yields
320 a floating astrochronology ~ 1238 kyr and is ideal for investigating longer-term processes ($\sim 10^5$
321 yr).

322 Recovery of all identified Milankovitch cycles (Fig. 3) from the time-domain γ -signal
323 (Fig. 4) enabled a second, complementary tuning approach based on precession. Guided by
324 the bandpass filter output of component 5 (Fig. 3a) and assuming a fixed 19.1-kyr precession
325 period, a second age model (hereafter AM2) was constructed. The resulting floating
326 astrochronology spans ~ 1267 kyr. Although the use of 67 depth-tie points at fixed 19.1-kyr
327 intervals sacrifices information on the different frequency components of precession, this
328 approach corrects more effectively for small-scale sedimentation rate variations. This is most
329 crucial when investigating processes on sub-Milankovitch timescales, for which such a high-
330 resolution age model is most ideal.

331 Finally, the estimated duration of the Cargill #17 Core Sherburne Formation is
332 calculated by averaging AM1 and AM2, yielding 1252 ± 29 kyr (Fig. S5). The uncertainty
333 associated with this estimate reflects the difference in relative time between AM1 and AM2
334 and is a realistic error margin equivalent to nearly two precession cycles. Both γ - and χ -signals
335 were tuned using both AM1 and AM2 prior to subsequent cyclostratigraphic analysis.

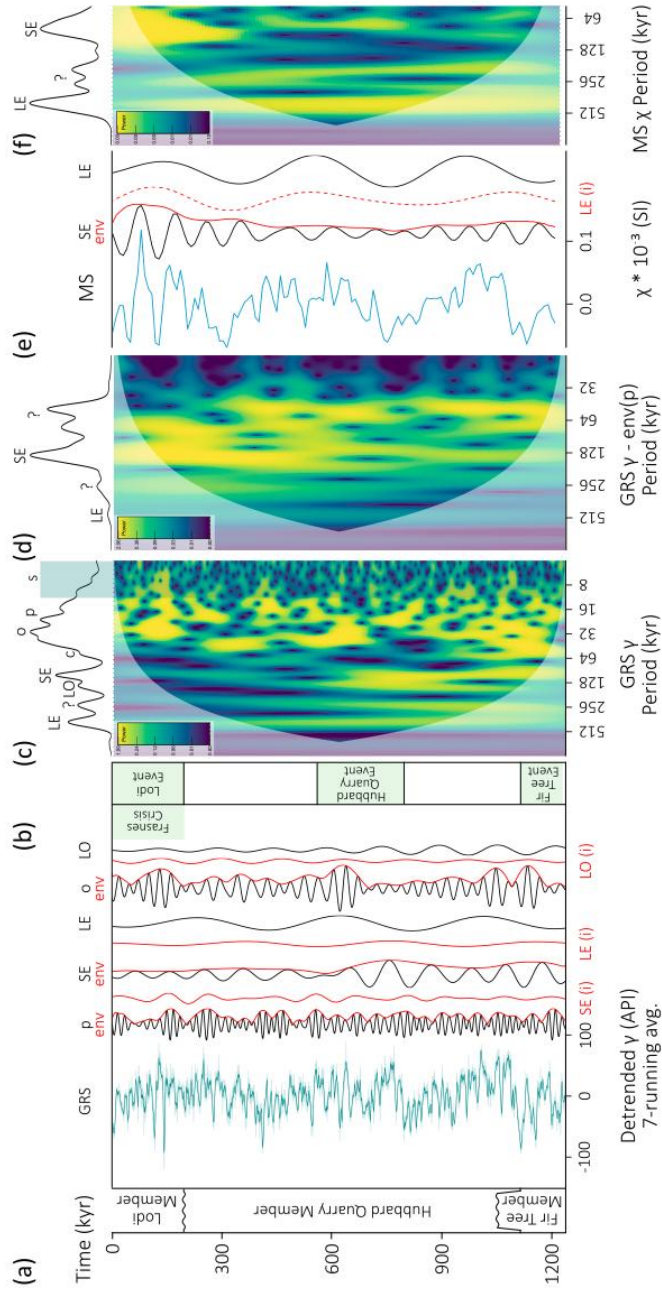


Fig. 4. Time-domain (AM1) cyclostratigraphy of the Sherburne Formation. a) Stratigraphy, detrended GRS y-signal (light cyan) and 7-running average y-signal (cyan), and bandpass filter output of precession (p; black) and its envelope (SE; black) extracted from the envelope of precession (SE(i); red), short eccentricity (SE; black) and its envelope (red), long eccentricity extracted from the envelope of short eccentricity (LE(i); red), long obliquity (LO; black), obliquity (o; black) and its envelope (red), long obliquity extracted from the envelope of obliquity (LO(i); red), long obliquity (LO; black). b) Bio-event stratigraphy. c) GRS y CWT and average wavelet power spectrum, combination tones (c), and sub-Milankovitch cyclicity (s) highlighted in light blue. d) GRS y CWT of the envelope of precession and average wavelet power spectrum. e) MS x-signal (blue) and bandpass filter output of short eccentricity (SE; black) and its envelope (red), long eccentricity extracted from the short eccentricity envelope (LE(i); dashed red), long eccentricity (black). f) MS x CWT and average wavelet power spectrum.

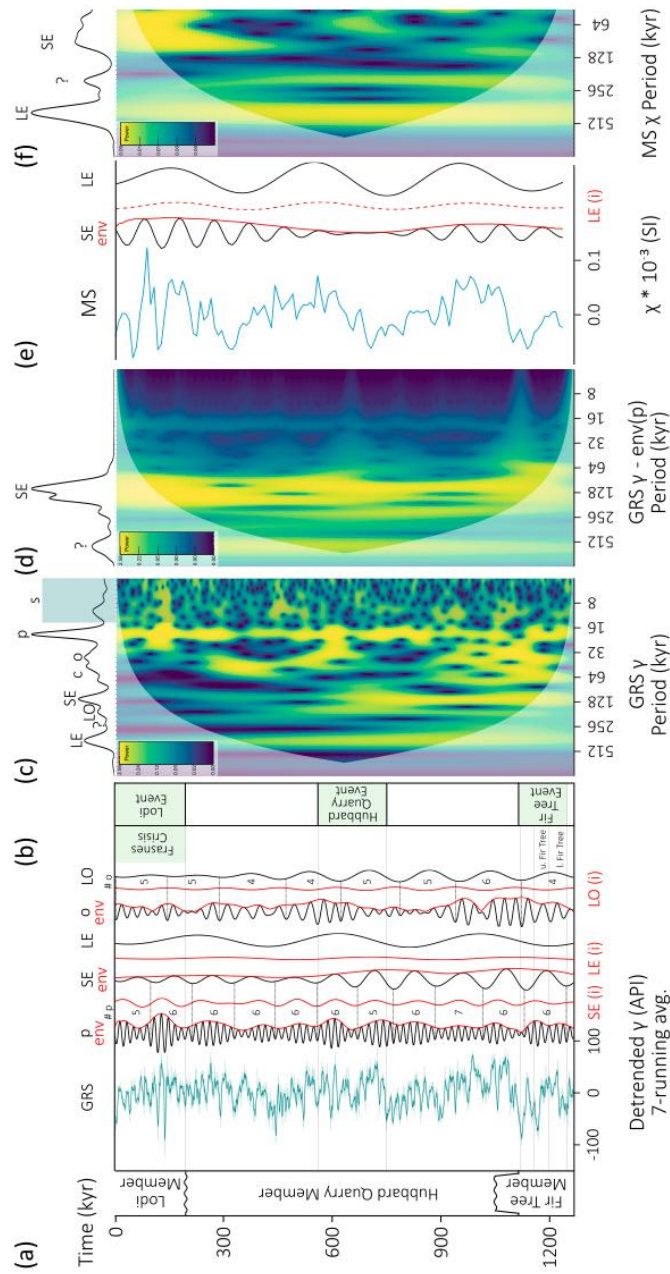


Fig. 5. Time-domain (AM2) cyclostratigraphy of the Sherburne Formation. a) Stratigraphy, detrended GRS γ -signal (light cyan) and 7-running average γ -signal (cyan), and bandpass filter output of precession (p; black) and its envelope (SE; black) extracted from the envelope of precession (SE(i); red), short eccentricity (SE; black) and its envelope (red), long eccentricity extracted from the envelope of short eccentricity (LE(i); red), long obliquity (LO; red), long obliquity (LO; black), obliquity (o; black) and its envelope (red), long obliquity extracted from the envelope of obliquity (LO(i); red), long obliquity (LO; black). Numbers indicate counted precession (#p) cycles per interpreted SE cycle and obliquity (#o) per interpreted LO cycle. b) Bio-event stratigraphy. c) GRS γ CWT and average wavelet power spectrum, sub-Milankovitch cyclicity (s) highlighted in light blue. d) GRS γ CWT of the envelope of precession and average wavelet power spectrum. e) MS χ -signal (blue) and bandpass filter output of short eccentricity (SE; black) and its envelope (red), long eccentricity extracted from the short eccentricity envelope (LE(i); dashed red), long eccentricity (black). f) MS χ CWT and average wavelet power spectrum.



352 5.3. *Time-domain Cyclostratigraphy*

353 The Devonian lies beyond the interval for which astronomical solutions remain reliable,
354 as chaotic divergence limits the precision of deep-time orbital calculations (Laskar, 2020;
355 Zeebe and Lantink, 2024). We therefore assess the Milankovitch imprint through time-series
356 and spectral analyses of the GRS γ - and MS χ -signals, tuned using two complementary age
357 models: AM1 (405-kyr eccentricity) and AM2 (19.1-kyr precession). Both age models offer
358 specific advantages and limitations that complement one another. Due to the long-term
359 stability of the 405-kyr LE cycle, AM1 provides the most accurate temporal estimation and
360 preserves frequency modulation, but it performs poorly in correcting for high-frequency
361 sedimentation rate changes. In contrast, AM2 offers the highest temporal resolution and
362 effectively accounts for sedimentation rate changes – thereby also more faithfully capturing
363 amplitude modulation patterns – though it sacrifices precession frequency modulation.
364 Consequently, while analyses targeting the linear Milankovitch imprint should yield
365 comparable results across both models, higher-order spectral methods (e.g., bicoherence
366 analysis) may produce divergent outputs, as they are more sensitive to phase structure and
367 nonlinear interactions, whose detection can be affected by the tuning.

368 5.3.1. *Long Eccentricity-based Age Model (AM1)*

369 CWT analysis of the γ -signal tuned to AM1 reveals imprints of 405-kyr long eccentricity
370 (LE), as well as ~173-kyr long obliquity (LO), ~100-kyr short eccentricity (SE), obliquity and
371 precession cycles (Fig. 4c). These Milankovitch components were filtered, and their amplitude
372 modulation (i.e., envelope) was obtained via Hilbert transform. About 5 to 7 precession cycles
373 occur per short eccentricity cycle (Fig. 4a), matching predictions for the late Givetian (~380
374 Ma; Waltham, 2015). The amplitude modulation patterns of precession align satisfactorily with
375 SE extrema. A second CWT of the precession envelope (Fig. 4d) shows dominant SE power,
376 with only minor LE power, as expected for such a relatively short record (~3 LE cycles).



377 Sub-Milankovitch spectral power (s; Fig. 4c) suggests half-precession cycles and/or
378 high-frequency combination tones (i.e., millennial-scale variability), statistically significant at
379 the 90 % AR1 level (MTM; Fig 6a, Fig. S1c, d). Additional wavelet power appears between 35-
380 65 kyr periods (Fig. 4c), which is also present in the envelope of precession (Fig. 4d) and half-
381 precession, as shown later. These may reflect localized sedimentation rate changes, linear
382 Milankovitch interferences (affecting the envelope of precession) or nonlinear interactions.

383 To explore the origin of cyclic components that deviate from canonical Milankovitch
384 frequencies, bicoherence analysis was performed, with a focus on nonlinear interactions
385 between precession and obliquity (Fig. 6c). In several regions of the spectrum, quadratic
386 coupling between precession and obliquity is evident, producing sum tones (10.3 to 13.9 kyr)
387 and/or difference tones (~36 to 128 kyr). Additional coupling occurs between sub-Milankovitch
388 components and precession and obliquity components (Fig. 6c).

389 5.3.2. *Precession-based Age Model (AM2)*

390 Spectral analyses similar to those described in the previous section confirm LE, LO,
391 SE and obliquity in addition to the precession cyclicity in the γ -signal that was tuned according
392 to AM2 (i.e., precession-based; Fig. 5). This equally serves as a cross-check of the proposed
393 cyclostratigraphic interpretation. Precession counts consistently yield 5-7 cycles per SE cycle
394 (Fig. 5a). Similarly, obliquity counts reveal 4-6 cycles per LO cycle (Fig. 5a), equally in-line
395 with astronomical predictions (~150 to 177 kyr in the ZB23 solutions; Zeebe and Lantink,
396 2024). These counts suggest the Fir Tree-Hubbard Quarry discontinuity represents only a
397 minor hiatus, most likely shorter than one obliquity cycle. Similarly, the sequence boundary
398 (SB) at the base of the Lodi Member also appears to represent only a minor hiatus of about
399 the same duration. From this SB onwards, the precession envelope shifts slightly out of phase
400 with the extracted SE cycle, possibly reflecting either the influence of the hiatus, edge effects
401 introduced by bandpass filtering and subsequent Hilbert transform, or a change in the
402 paleoclimatic response. A similar but weaker effect occurs in the lower Fir Tree Member.
403 Conversely, the envelope of obliquity and LO does exhibit a consistent anti-phased

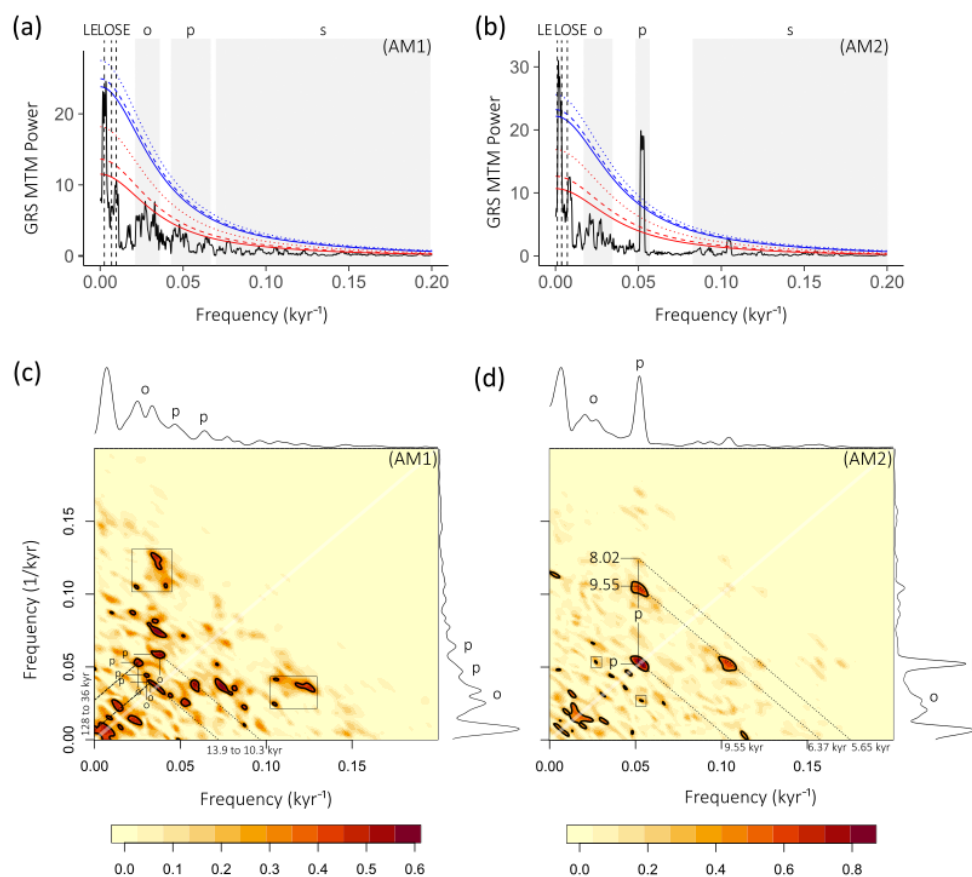


404 relationship, which may in part be due to the tendency of bandpass filtering and the Hilbert
405 transform to impose smoother, more regular phase behavior when signal amplitudes are low
406 (Fig. 4a, Fig. 5a).

407 Tuning to 19.1-kyr precession enhances sub-Milankovitch power (Fig. 5c), suggesting
408 half-precession and/or nonlinear interactions. Bicoherence analysis reveals strong diagonal
409 coupling at 19.1 kyr (Fig. 6d), consistent with (mathematical) harmonic generation producing
410 a ~9.55 kyr component. Quadratic coupling between precession and this component in turn
411 yields a ~6.37-kyr component, suggesting involvement of a harmonic cascade. Tuning to
412 precession can generate a harmonic cascade as an artefact, because it forces variations in
413 the sedimentation rate that effectively result in frequency modulation of the signal. However,
414 we observe that a ~9.55-kyr component is recovered through spectral analysis (Fig. 4) and it
415 also appears on the bicoherence spectrum of the γ -signal tuned according to AM1 (Fig. 6c),
416 where it couples with precession and obliquity components. This strongly suggests that the
417 detected sub-Milankovitch cyclicity (incl. the ~9.55-kyr component) is not only a tuning artifact
418 (Fig. 8).

419 5.3.3. *Magnetic Susceptibility*

420 Spectral and time series analyses of the χ -signal tuned to AM1 and AM2 yield highly
421 similar results and are therefore treated together. CWT analysis shows increased wavelet
422 power at LE and SE periodicities (Fig. 4), which are extracted using Taner bandpass filtering
423 (Fig. 4) to facilitate comparison of phase relationship between γ and χ . Crucially, the extracted
424 SE and LE components appear broadly in-phase with those recovered from the γ -signal (Fig.
425 4, 5), indicating that both proxies exhibit a similar response to astronomically forced insolation
426 changes. This reinforces their interpretation as reflecting detrital input variations.



427

428 **Fig. 6. Bicoherence analysis of the tuned GRS γ -signal.** a) Time-domain γ (AM1) MTM spectrum. b) Time-
 429 domain γ (AM2) MTM spectrum. Classical significance testing at 90, 95 and 99 % confidence levels using an
 430 autoregressive model of order 1 (AR(1)) is included for each spectrum (red full, dashed and dotted red lines,
 431 respectively) and Bonferroni corrections (blue). c) Weighted overlap segment averaging (WOSA) power spectrum
 432 and bicoherence spectrum of γ (AM1). Obliquity and precession marked by 'o' and 'p', respectively. Increased
 433 bicoherence indicates quadratic coupling, revealing nonlinear Milankovitch combination (dotted diagonals) and
 434 difference (dashed diagonals) tones. Black squares indicate quadratic coupling of 9.55-kyr and sub-Milankovitch
 435 components. d) WOSA and bicoherence spectra of γ (AM2), black squares indicate regions of precession-obliquity
 436 coupling. Obliquity and precession marked by 'o' and 'p', respectively. Nonlinear Milankovitch combination tones
 437 (dotted diagonals). Key sub-Milankovitch durations highlighted on the bicoherence spectrum in kyr.



438 *5.3.4. Phase Relationship of Proxies to Astronomical Forcing*

439 Interpretation of proxy dynamics and their phase relationships with astronomical
440 forcing is critical for understanding proxy responses and assessing the timing of regional
441 events relative to Milankovitch cycle extrema. Cyclostratigraphy of γ - and χ -signals
442 demonstrates that deposition of the Sherburne Formation strata within the Appalachian Basin
443 was strongly influenced by astronomically paced changes in detrital input. Because both
444 proxies represent an amalgamated signal (e.g., Da Silva et al., 2009; 2012; Killeen, 2015), it
445 remains uncertain whether these variations represent changes in the total amount of detrital
446 input or its composition. The dominant driver is most plausibly the hydrological cycle,
447 influencing detrital delivery through variations in weathering, erosion, runoff, and/or
448 astronomically paced eustatic sea-level fluctuations (Da Silva et al., 2009; 2012; Zhang et al.,
449 2022). This is in agreement with the interpretation of the Sherburne Formation strata as
450 hyperpynites (Wilson and Schieber, 2014; 2015; 2017).

451 Intervals characterized by stronger γ precession-scale amplitude variation are
452 interpreted to correspond to maxima in SE (Fig. 4, 5). The in-phase relationship between
453 eccentricity signals extracted from both γ and χ indicates that both proxies respond
454 synchronously to changes in insolation forcing. This is reinforced by the in-phase relationship
455 between SE and SE(i) extracted from the γ -signal, suggesting maximal precession amplitude
456 modulation during SE maxima (Fig. 4, 5). Accordingly, high γ - and χ -values are interpreted to
457 reflect periods of strong climatic precession at the paleodepositional site. Similarities in proxy
458 responses suggest that shared processes influenced χ in the same way, although its lower
459 resolution limits detailed analysis. Although a 405-kyr LE imprint is recognizable in both proxy
460 signals, its expression is less clear in the precession envelopes (Fig. 4, 5). This is attributed
461 primarily to the presence of obliquity, combination tones (Fig. 6) and interferences involving
462 precession and obliquity (Fig. 7), which affect the amplitude of the γ -signal and may hamper
463 indirect recovery of eccentricity cycles from the envelopes of hierarchically shorter cycles.



464 *5.3.5. Duration of Regional Events and their Phase-relationship to Astronomical Forcing*

465 The durations of the Fir Tree, Hubbard Quarry, and Lodi events can be estimated with
466 age model AM1, tuned to the stable 405-kyr eccentricity metronome. The Fir Tree Event lasted
467 108 ± 29 kyr, broadly equivalent to the duration of one short eccentricity cycle. The error
468 margin of 29 kyr is estimated based on the difference between AM1 and AM2. The succeeding
469 Hubbard Quarry Event, representing highstand conditions and associated low oxygen
470 conditions inferred from the black shale facies (Fig. 2), is more protracted; its duration is 214
471 ± 29 kyr, equivalent to two SE cycles. Finally, the Lodi Event, which also marks the onset of
472 the Frasnian Crisis, has an estimated duration of at least 200 ± 29 kyr.

473 The Fir Tree, Hubbard Quarry and Lodi events share a notable similarity: their onset
474 occurs near a minimum in precession and short eccentricity (Fig. 5). Although this pattern is
475 not explicitly diagnostic of the underlying causal mechanisms, it does indicate that
476 astronomical forcing exerted a strong control on the timing of their initiation. Based on the 405-
477 kyr long eccentricity cycle extracted directly from the γ - and χ -signals, the temporal position of
478 these events can be placed within the broader long-eccentricity framework. Both the Fir Tree
479 and Hubbard Quarry events appear to occur shortly after a minimum in 405-kyr eccentricity,
480 initiating on the rising limb of the long-eccentricity cycle. Conversely, the Lodi Event appears
481 to occur shortly after a maximum in 405-kyr eccentricity and unfolds on the decreasing limb of
482 the long-eccentricity cycle.

483 Yet, while the Lodi and Fir Tree events are both interpreted to occur during a TST after
484 a SB, the hypoxic Hubbard Quarry Event develops during a HST (Fig. 2). These differences –
485 closely tied to eustatic sea-level variations – cannot be entirely reconciled with the eccentricity-
486 paced forcing identified above. Although the timing of these events appears dictated by
487 precession-eccentricity minima, their expression and relationship to sea-level variations likely
488 involved additional controls. Given that the three events occur over slightly more than 1.2 Myr,
489 we hypothesize that the s_4 - s_3 1.2-Myr obliquity cycle (Laskar, 2020) may represent the
490 additional pacing mechanism required to explain their differing sea-level contexts.



491 Astronomically controlled sea-level variability on such timescales was already reported by
492 Huygh et al. (2026) for the Appalachian Basin during the Frasnian. Although the Sherburne
493 Formation record is too short to resolve the s_4 - s_3 cycle directly, the spacing of the Fir Tree,
494 Hubbard Quarry and Lodi events is consistent with their development near successive
495 extrema of this long-period obliquity modulation.

496 Whether the Fir Tree and Lodi event occur during a s_4 - s_3 minimum or maximum – and,
497 conversely, whether the Hubbard quarry corresponds to the opposite extremum – cannot be
498 inferred from the available data. This uncertainty arises because the phase relationship
499 between obliquity and sea-level change is mechanism-dependent: glacio-eustasy and
500 limno/aquifer-eustasy respond in opposite phase to obliquity forcing (Lourens and Hilgen,
501 1997; Li et al., 2018), and the dominant mechanism depends on the prevailing climatic regime.
502 Although the presence of substantial (continental) ice during the cooler Givetian (Becker et
503 al., 2020) remains debated, integrated stratigraphy and oxygen-isotope evidence does
504 suggest that glacio-eustatic processes may have operated on < 1.7 -Myr timescales (Elrick et
505 al., 2009). Hence, we propose that glacio-eustasy may have contributed to the observed
506 eustatic sea-level variations. As noted above, the Fir Tree and Lodi events correspond with
507 substantial incision of up to 18 meters in Iowa that is difficult to explain without glacio-eustasy,
508 which could be substantial under relatively cool and variable climate conditions (cf. Dahl et al.,
509 2022). Taken together, we hypothesize that obliquity-scale climate variability modulated the
510 sea-level context in which the Fir Tree, Hubbard Quarry and Lodi events unfolded,
511 superimposed on their precession-eccentricity-paced timing.



512 *5.3.6. Milankovitch Interference Patterns and Nonlinearities*

513 Insolation at a given latitude depends, among other factors (e.g., solar cycles), on
514 climatic precession and obliquity (e.g., Milankovitch, 1941; Berger et al., 2006). Because
515 different paleodepositional settings and proxies can respond to these orbital cycles through
516 distinct mechanisms, their interplay may be recorded in multiple ways. Within the scope of this
517 study, two types of interactions between astronomical frequencies are therefore relevant for
518 understanding climate responses to insolation forcing.

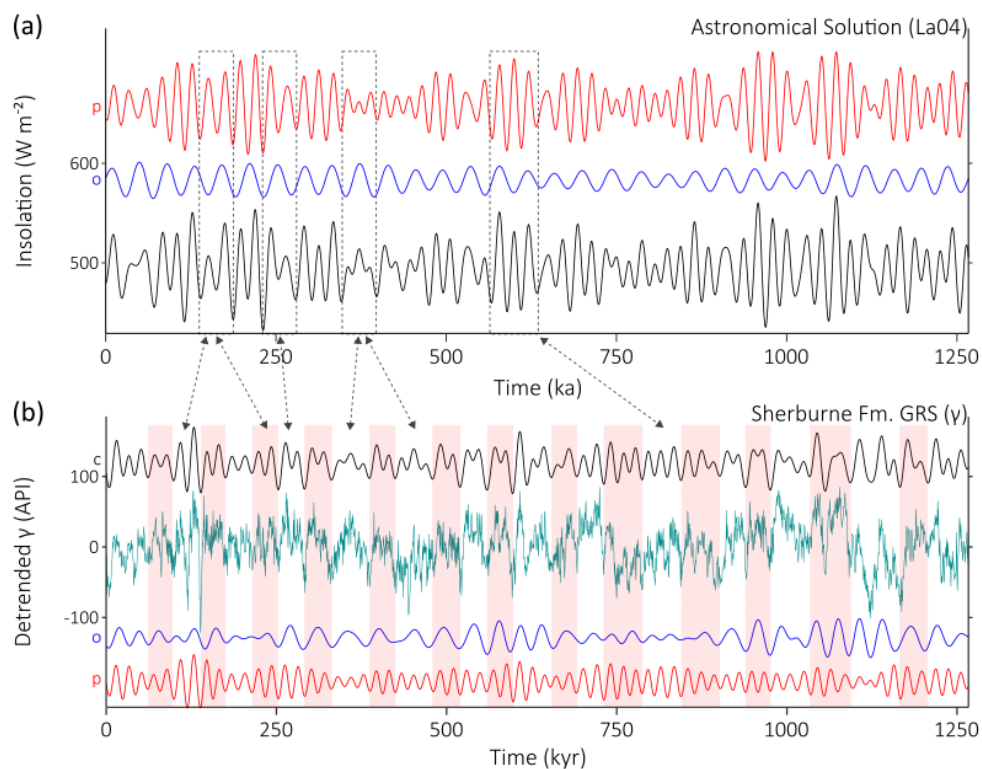
519 The first involves linear interference between carrier frequencies such as precession
520 and obliquity, which does not generate new frequencies in the underlying forcing (Fig. 8a, c;
521 Laskar et al., 2004). Because precession and obliquity are not phase-locked, their extrema
522 may coincide regularly but not periodically, and their combined linear effect generates time-
523 dependent interference patterns manifested as amplitude modulation and beating patterns
524 (Fig. 8b, d). The resulting amplitude envelope – extractable using a Hilbert transform (Fig. 8a,
525 c) – contains frequency variability associated with the modulation itself (i.e., new frequencies;
526 Fig. 8b, d). Depending on the sensitivity of the proxy system, a purely linear response may
527 therefore record either the carrier frequencies and/or the amplitude envelope produced by
528 their interference (Imbrie and Imbrie, 1980; Meyers and Hinnov, 2010). For completeness,
529 certain processes, such as bioturbation, may mimic an envelope-type response (Meyers,
530 2014).

531 A second class of interactions involves nonlinear responses to astronomical forcing,
532 leading the Earth system to generate new frequencies that are not present in the original
533 insolation signal. Such behavior can occur in a range of contexts, including threshold-
534 controlled climate-sediment interactions such as runoff-driven erosion and sediment
535 accumulation (Tucker and Slingerland, 1997) as well as nonlinear sediment-transport
536 dynamics (Jerolmack and Paola, 2010). This is conceptually illustrated in Fig. 8e, where a
537 hyperbolic tangent $f(x) = \tanh[2(x-1)]$ acts as a nonlinear operator that produces mixed
538 frequencies ($f_3 = f_1 \pm f_2$), such as ~50-kyr components (see Fig. 8f, g). Note that processes



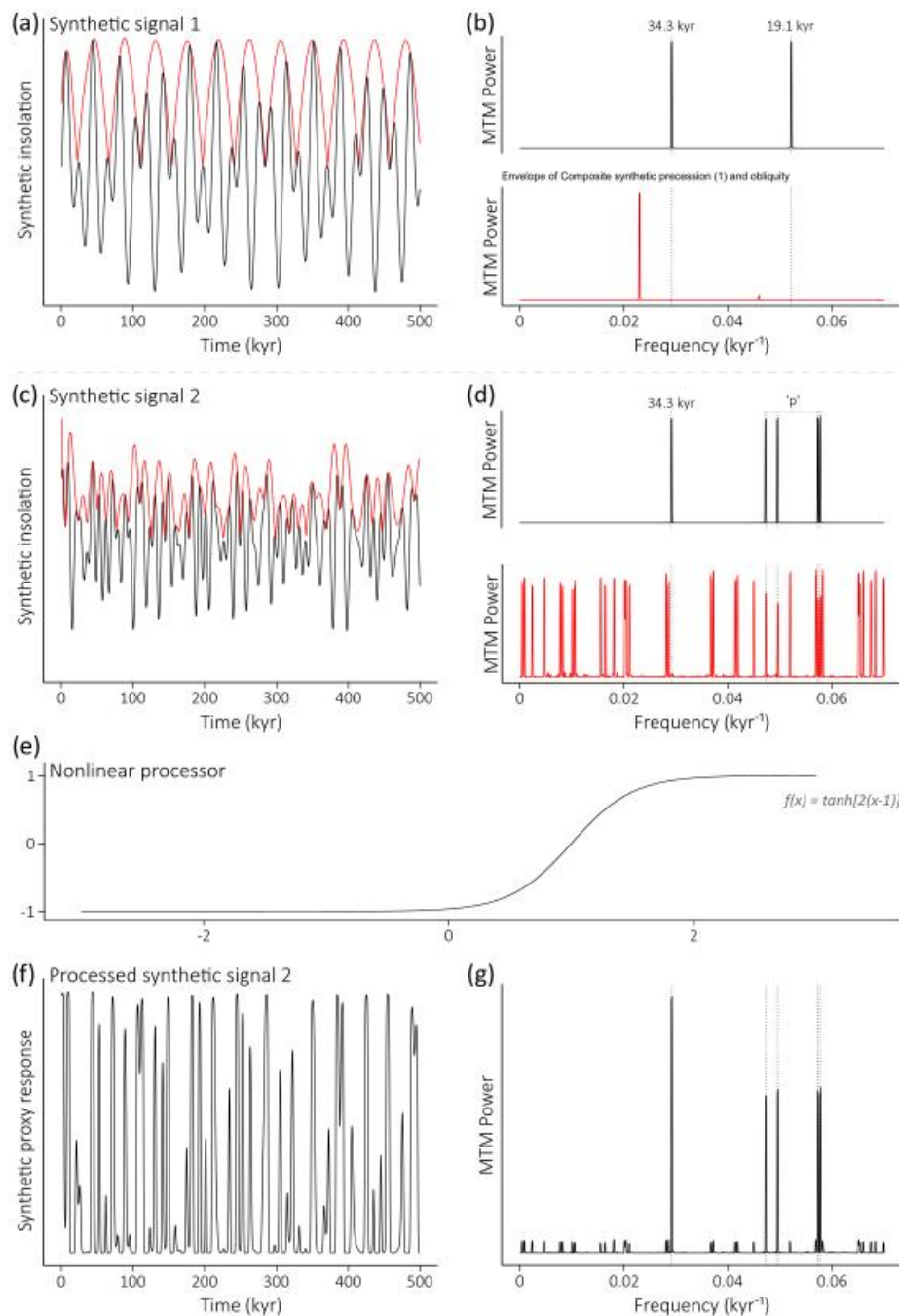
539 that appear to track the amplitude envelopes of higher-frequency carriers may also be
540 nonlinear in their underlying dynamics (e.g., Huybers and Wunsch, 2004). Quantifying the
541 linear proxy response to the envelope of the carrier frequencies (e.g., to total insolation
542 variability) and a nonlinear proxy response in inherently noisy sedimentary proxy series is
543 challenging, especially because neither amplitudes nor frequencies are entirely diagnostic.

544 The framework presented above clarifies how new frequency components – such as
545 those observed in the Sherburne Formation γ -signal – may arise and provides the basis for a
546 qualitative interpretation of their origin. For example, a ~50-kyr component is present in
547 obliquity (Laskar et al., 2004), but it is relatively weak and is not expected to contribute
548 substantially (Spiering et al., 2024). Alternatively, such a component (Fig. 4-6) can result either
549 from a linear response to the amplitude envelope of higher-frequency insolation components
550 (Fig. 8d) or from nonlinear interactions involving, for example, precession and obliquity (Fig.
551 8g). A third possibility is that these components represent harmonics of the ~100-kyr short-
552 eccentricity cycle. However, this pathway is readily evaluated: in the Sherburne Formation γ -
553 signal, the extracted short-eccentricity component shows no stable phase relationship with the
554 40-60 kyr variability (Fig. S6), making a harmonic origin unlikely (Spiering et al., 2024).
555 Moreover, this framework also highlights the limitations of time-series and spectral analysis in
556 elucidating a proxy response to climatic variability as a result of insolation forcing. Although
557 new frequency components arising from a response to the insolation envelope may exhibit
558 higher amplitudes than those generated through nonlinear interactions (Fig. 8d, f), the
559 amplitudes preserved in sedimentary proxy series may be muted, amplified, or overprinted by
560 noise and other non-cyclic contributions (Mudelsee, 2010; Meyers, 2014), complicating their
561 interpretation.



562

563 **Fig. 7. Milankovitch interference patterns in the Sherburne Formation γ -signal.** a) Insolation series (La04 at
 564 65°N; Laskar et al., 2004) from 0 to 1267 ka (black), filtered precession (p; red) and obliquity (o; blue). Red bands
 565 and black dashed arrows highlight and indicate similar precession-obliquity interference patterns – not correlation.
 566 b) Detrended γ -signal (cyan) tuned according to AM2 and bandpass filter output of precession (p; red), obliquity (o;
 567 blue) and a linear superposition (i.e., sum) of the precession and obliquity filter output (c; black). Vertical red bars
 568 highlight interference patterns between precession and obliquity. Black dashed boxes and arrows indicate similar
 569 interference patterns.





571 **Fig. 8. Conceptual illustration of synthetic insolation forcing, proxy responses, and their MTM spectra.** a)
572 Synthetic insolation of linearly superimposed 19.1 and 34.3-kyr signals (black) and Hilbert-derived envelope (red),
573 zoom-in on 0-500 kyr. b) MTM power spectra of the signals in a); upper: synthetic insolation (black), lower: its
574 envelope (red). c) Synthetic insolation of linearly superimposed 17.34, 17.47, 20.2, 21.2 and 34.3-kyr signals
575 (black) and Hilbert-derived envelope (red), zoom-in on 0-500 kyr. b) MTM power spectra of the signals in d); upper:
576 synthetic insolation (black), lower: its envelope (red). e) nonlinear processor $f(x) = \tanh[2(x-1)]$. f) Synthetic proxy
577 response after nonlinear processing using $f(x) = \tanh[2(x-1)]$ of the time series plotted in panel e. g) MTM power
578 spectrum of the synthetic proxy response (f). Note that the prominence of envelope-derived or nonlinear frequency
579 components is sensitive to the chosen input parameters of the conceptual experiment.

580

581 Building on this framework, the cyclicity observed in the Sherburne Formation γ -signal
582 is interpreted here as reflecting a nonlinear proxy response to climatic variability with
583 substantial contributions from a linear response to insolation and its envelope. Integration of
584 bandpass filtering (Fig. 3, 4, 5, 7) with CWT (Fig. 4, 5) and bicoherence analysis (Fig. 6)
585 supports this dual-mechanism interpretation. Apparent interference patterns, resulting from
586 linear superposition of precession and obliquity appear to dominate the γ -signal (Fig. 7) and
587 reflect a response to changes in total insolation (Laskar et al., 2004). The similarity between
588 these precession-obliquity interference patterns and the La04 solution (Fig. 7a) is highly
589 suggestive of a dominant contribution by a linear proxy response to insolation variability.
590 Because no unique astronomical solution exists for the Givetian, these interference patterns
591 are compared with the La04 insolation series for illustration purposes (from 0 to 1267 ka;
592 Laskar et al., 2004; Fig. 7). Note that direct comparison may be somewhat limited due to the
593 shorter Givetian precession and obliquity durations (Laskar et al., 2004; Waltham, 2015;
594 Laskar, 2020).

595 In addition to these interference patterns, the Sherburne Formation γ -signal also
596 exhibits features that cannot be produced by linear superposition alone; significant
597 bicoherence between astronomical components (Fig. 6) demonstrates that the climate-
598 sediment system introduces nonlinear interactions, generating new frequencies through



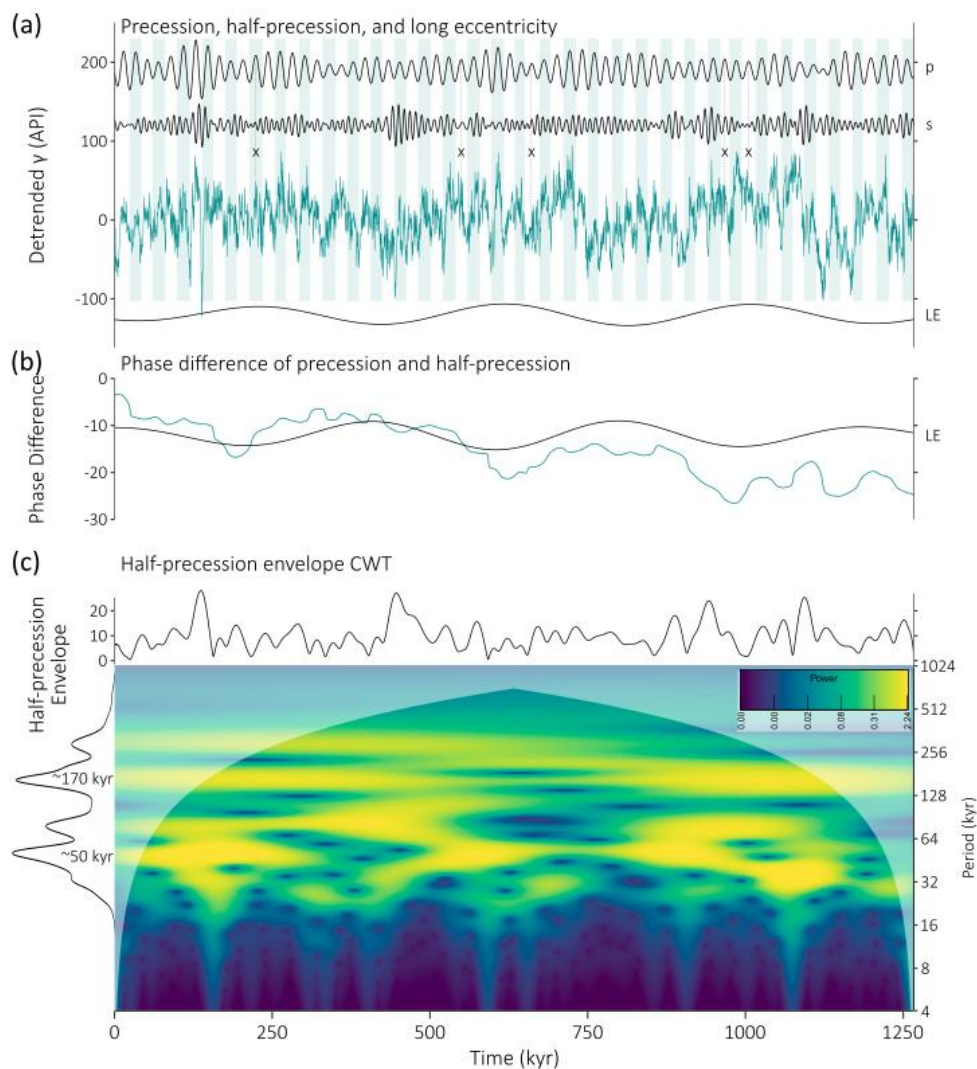
599 quadratic phase coupling (Sullivan et al., 2023) and likely further modifying the amplitude
600 structure of the proxy response. Such nonlinear interactions may give rise to both lower-
601 frequency (i.e., sum tones) and higher-frequency (i.e., difference tones) components
602 (Hagelberg et al., 1991; von Dobeneck and Schmieder, 1999). Although nonlinear interactions
603 can generate similar frequencies, for example, in the 40-60 kyr band (Fig. 6), climate-sediment
604 nonlinearities are typically state-dependent and not expected to generate persistent, well-
605 defined patterns (Tucker and Slingerland, 1997; Jerolmack and Paola, 2010) such as those
606 arising from a response to total insolation variability (Fig. 7a, b). While bicoherence analysis
607 does not allow discrimination between sum and difference tones, our integrated spectral (Fig.
608 4-7) and conceptual (Fig. 8) results indicate that both types of nonlinear products were likely
609 captured by the γ -signal. Although additional cyclicity is evident at eccentricity timescales (Fig.
610 4-6), the summed precession-obliquity signal appears to account for the majority of variability
611 observed in the γ -signal (Fig. 7), while non-cyclic contributions and sedimentary noise likely
612 also contributed. The considerations outlined above are equally relevant for interpreting
613 variability in the sub-Milankovitch band, where both half-precession and nonlinear frequency
614 generation can produce similar spectral expressions, which is addressed in the next section.



615 *5.3.7. Half-precession Cycles*

616 In the intertropical belt, in particular at the equator, the Sun culminates at the zenith of
617 both equinoxes (Berger et al., 2006). If climate responds predominantly to the largest of these
618 twice-annual insolation maxima (Berger and Loutre, 1997), then the precessional modulation
619 of equinox intensity produces two insolation peaks per precession cycle, giving rise to
620 variability at approximately half the precession period (i.e., mean ~9.5 kyr for the Givettian).
621 Thus, half-precession does not represent a harmonic of precession; rather, it is a geometric
622 consequence of how equatorial insolation responds to climatic precession (Berger and Loutre,
623 1997; Berger et al., 2006; Wu et al., 2025). However, distinguishing half-precession is not
624 straightforward, because nonlinear interactions between precession and obliquity (Fig. 6;
625 Table E1) or a proxy response to the total-insolation envelope (Fig. 8d) can generate
626 frequencies that fall within the same band, complicating the elucidation of a true half-
627 precessional signal.

628 The γ -signal consistently shows splitting of precession-scale cycles (Fig. 9a),
629 suggesting a half-precession-like imprint. In addition, the γ CWT spectra reveal prominent
630 power centered around a ~9.5 kyr period (Fig. 4, 5). MTM and EPSA analyses (Fig. S7) show
631 that this band comprises multiple components (7.8 to 12.3 kyr) across the Sherburne
632 Formation (see MTM spectrum, Fig. S1). Moreover, elevated bicoherence (Fig. 6) suggests
633 the presence of similar frequencies resulting from nonlinearities and their involvement in
634 quadratic coupling.



635

636 **Fig. 9. Half-precession cyclicity in the Sherburne Formation γ -signal.** a) Detrended γ -signal (cyan) tuned
637 according to AM2 and bandpass filter output of ~ 9.5 -kyr sub-Milankovitch 'half-precession' cycles (s; black),
638 precession (p; black) and 405-kyr long eccentricity (LE; black). Intervals where a 2:1 s:p-structure breaks down are
639 marked using 'x', for which dashed vertical lines demarcate the temporal location of interpreted half-precession
640 cycles. b) The phase difference between extracted precession and half-precession cycles (cyan) and filtered 405-
641 kyr component (LE; black). c) Half-precession envelope (black) and continuous wavelet spectrum of the half-
642 precession envelope revealing pronounced ~ 50 -kyr and ~ 170 -kyr cyclicity.



643 Using Taner bandpass filters, precession and the ~9.5-kyr sub-Milankovitch
644 components were isolated from the γ -signal (AM2), enabling direct comparison of bundling
645 patterns and phase coherency (Fig. 9). The robustness of the ~9.5-kyr bandpass filter was
646 verified to exclude artefacts arising from filter-window parameters. Throughout the formation,
647 two ~9.5-kyr cycles consistently occur per precession cycle (Fig. 9a). Only four intervals (~6
648 %) deviate from this 1:2 ratio, which may reflect localized sub-precession sedimentation-rate
649 changes, sedimentary noise (e.g., traditional slope-derived turbidites) or, more likely,
650 interference from combination tones (Fig. 6). Such tones are absent from the insolation
651 spectrum (e.g., Laskar et al., 2004) and instead reflect state-dependent climate-sediment
652 feedbacks (Hagelberg et al., 1991; Tucker and Slingerland, 1997; Jerolmack and Paola,
653 2010), rather than a consistent half-precession response. The persistent ~9.5-kyr frequencies
654 (Fig. 6; Fig. S7) and repeated two-per-precession bundling (Fig. 9a) strongly suggest half-
655 precession cyclicity as the dominant source of sub-Milankovitch variability, with secondary
656 contributions from nonlinear interactions. Therefore, while the identified ~9.5-kyr components
657 cannot be interpreted as reflecting half-precession alone, we consider half-precession to be
658 the dominant contributor and use this term as shorthand for this frequency band in the
659 following discussion. Sub-7-kyr cyclicity is attributed to either Milankovitch combination tones
660 or harmonics of (half-) precession (Fig. 6; Fig. S7). To further assess the relative contributions
661 of half-precession and nonlinear sub-Milankovitch imprints, we examine the phase and
662 amplitude modulation patterns of half-precession.

663 Visual inspection of the extracted precession and half-precession shows that their local
664 extrema do not align, suggesting that the two signals are not phase locked. Such behavior is
665 expected given the identified presence of nonlinearities (Fig. 6). To test this visual observation,
666 the 1:2 phase-locking signal at a given time index (t) was calculated (Fig. 9b) using the
667 instantaneous phases (using a Hilbert transform) of filtered precession and half-precession,
668 according to:

$$669 \quad \Delta\phi(t) = 2\phi_{pre}(t) - \phi_{hpre}(t) \quad (1)$$



670 where $\Delta\phi(t)$ represents the phase difference between the instantaneous phase of
671 precession $\phi_{pre}(t)$ and ‘half-precession’ $\phi_{hpre}(t)$ (Rosenblum et al., 1996). The phase locking
672 value (PLV) was calculated to quantify the consistency of the phase difference over (t) , with
673 values of 0 indicating random phase difference (i.e., no locking) and 1 indicating perfect phase
674 locking:

$$675 \quad PLV = \left| \frac{1}{N} \sum_{t=1}^N e^{i\Delta\phi(t)} \right| \quad (2)$$

676 where N represents the number of datapoints and the $e^{i\Delta\phi(t)}$ term expresses the phase
677 difference as a unit-length complex vector (Lachaux et al., 1999). A PLV of ~ 0.28 indicates
678 that the phase difference between precession and half-precession is not entirely random, but
679 highly unstable. This behavior is illustrated in Fig. 9b, which shows a steadily decreasing
680 baseline in $\Delta\phi(t)$ with a superimposed ~ 405 -kyr fluctuation that strongly resembles long
681 eccentricity and is consistently anti-phased to the 405-kyr LE extracted from the γ -signal (Fig.
682 9). From this, we infer that eccentricity influenced the phase evolution of precession and half-
683 precession.

684 To further investigate the origin of sub-Milankovitch cyclicity, the envelope of the
685 extracted half-precession, obtained through a Hilbert transform, was examined to assess the
686 longer-period amplitude modulation of this band. A CWT shows that the resulting envelope is
687 dominated by ~ 50 -kyr and ~ 170 -kyr variability. At first glance, this appears unexpected,
688 because eccentricity modulates precession and one might therefore anticipate ~ 100 -kyr (short
689 eccentricity) and ~ 405 kyr (long eccentricity) modulation in the envelope of the half-precession
690 signal. Such a ~ 170 kyr component is intriguing given it broadly corresponds to the s_3 - s_6
691 “metronome” (Laskar, 2020), which has a periodicity of 150 to 177 kyr (Zeebe and Lantink,
692 2024) but, given that the 173-kyr component extracted from the γ -signal is relatively weak (Fig.
693 4, 5), we refrain from attempting to further interpret this feature.



694 **6. Paleoclimatic and Paleodepositional Response**

695 We now set insights obtained through cyclostratigraphic analysis of the Sherburne
696 Formation γ - and χ -signals into a broader paleoclimatic perspective, providing new constraints
697 on how astronomical forcing shaped the late Givetian paleoclimate and depositional
698 processes in the Appalachian Basin. The cyclic variability points to a complex interplay among
699 precession, obliquity, and eccentricity, reflecting a climate system responding to changes in
700 total insolation, for example through precession-obliquity interferences, in combination with
701 nonlinear climate-sediment interactions.

702 An obliquity imprint is – at first glance – somewhat surprising at a $\sim 30^\circ$ S paleolatitude
703 because the direct effect of obliquity on insolation is strongest at high latitudes and is less
704 pronounced near the equator (Milankovitch 1941, Berger et al., 1993, 2006; Laskar et al.,
705 2004). Indeed, focusing on a Belgian record, De Vleeschouwer et al. (2012) suggested that
706 the influence of high-latitude climate variability was very limited (or absent) at $\sim 7^\circ$ S
707 paleolatitude during the Middle Devonian. Yet, the detected combination tones involving
708 obliquity (Fig. 6) and the clear precession-obliquity interference patterns in the γ -signal (Fig.
709 7A) unmistakably reaffirm the imprint of obliquity on the Sherburne Formation γ -signal,
710 identified through spectral analysis (Fig. 4, 5). This suggests that obliquity was also transmitted
711 into the subtropics through climate-system pathways – rather than direct insolation forcing
712 alone – consistent with a dynamically coupled tropical-subtropical climate system. Dynamic
713 variations of, for example, the Intertropical Convergence Zone (ITCZ) net precipitation (De
714 Vleeschouwer et al., 2012) are expected to respond to both precession and obliquity, which
715 modulate seasonal and annual-mean temperature gradients, respectively (Schneider et al.,
716 2014). This interplay between tropical hydrology and higher-latitude forcing is consistent with
717 modeling results of Tuenter et al. (2003), who demonstrated – for the modern African summer
718 monsoon – that obliquity-driven high-latitude climate variability can be transmitted into the
719 tropics and subtropics through large-scale atmospheric circulation. Moreover, Zhang et al.
720 (2022) reported combined precession and obliquity forced ITCZ migration at $5\text{--}20^\circ$ N during



721 the Early Cambrian as a result of interhemispheric pressure contrasts, thereby influencing the
722 lower-latitude hydrological cycle.

723 Recovery of a relatively strong obliquity imprint could suggest climatic teleconnections
724 from high latitudes (e.g., Meyers, 2012; Zeeden et al., 2019) involving changes in ice volume
725 (c.f. De Vleeschouwer et al., 2014). Although direct evidence of continental ice during the
726 Middle Devonian is absent, the potential presence of continental ice during this cooler interval
727 (Becker et al., 2020) has long been pondered (Elrick et al., 2009; Dahl et al., 2022) and on
728 eustatic sea-level fluctuations. Although a glacio-eustatic regime could strongly contribute to
729 the amplification of obliquity, it should be stated that a relatively strong obliquity imprint does
730 not *per se* reflect the presence of continental ice (Gérard et al., 2026). Moreover, Bosmans et
731 al. (2015) reported that “*obliquity-induced changes in tropical climate can occur without high-*
732 *latitude ice sheet fluctuations*” and that tropical circulation changes (in their climate model) are
733 consistent with obliquity-induced changes in the cross-equatorial insolation gradient. The
734 effect of changes in insolation on high-latitude productivity in combination with ocean
735 circulation changes influenced by obliquity at higher latitudes (i.e., thermohaline circulation)
736 offer alternative or additional explanations for the translation and amplification of obliquity at
737 lower latitudes (Gérard et al., 2025; 2026). As currently reconstructed (Fig. 1), the
738 paleogeography of the northern Appalachian Basin is restricted and therefore prone to ocean
739 circulation changes (see Zambito et al., 2012, for discussion of circulation changes in the
740 Sherburne-preceding Tully Formation). Ultimately, the Sherburne Formation record
741 underscores that subtropical climate during the Middle Devonian was not isolated from high-
742 latitude forcing, but dynamically linked via a combination of teleconnection, circulation
743 dynamics and, potentially, ice-volume variability.

744 Half-precession is generally considered unique to equatorial insolation forcing (Berger
745 and Loutre, 1997; Berger et al., 2006). Recovery of such frequencies from detrital influx at
746 relatively high latitudes (~30° S) therefore suggests considerable interactions with tropical
747 climate variability, likely mediated through the hydrological cycle (*cf.*, western equatorial



748 Pacific; Wu et al., 2025). During the Middle Devonian, one of the most potent drivers of
749 hydrological cycle variability was the precession-forced monsoonal circulation over the
750 Euramerican continent within the pantropical belt (De Vleeschouwer et al., 2012). Migration of
751 the intertropical convergence zone (ITCZ) modulated monsoonal activity, producing wet-dry
752 cycles that governed detrital input and composition (De Vleeschouwer et al., 2012; 2014;
753 Zhang et al., 2022; Wichern et al., 2024). Yet, the Sherburne Formation was deposited at an
754 estimated paleolatitude of $\sim 30^{\circ}\text{S}$ – potentially beyond the latitudinal range typically reached
755 by the ITCZ. Although De Vleeschouwer et al. (2014) inferred a substantial southward ITCZ
756 displacement toward the Appalachian Basin during the Late Devonian SH summer (see also
757 Wichern et al., 2024), such migration was likely part of a broader dynamical framework. In
758 particular, ITCZ position should be viewed in conjunction with Hadley-cell behavior, which
759 governs the large-scale redistribution of heat and moisture across the tropics and subtropics
760 (e.g., Bian et al., 2025). Given the sensitivity of the hydrological cycle to astronomical forcing,
761 it is hypothesized that similar mechanisms contributed to amplification of half-precession at
762 higher latitudes, alongside ocean-circulation-driven teleconnections (Wu et al., 2025).
763 Fundamentally, climatic precession and half-precession cycles are both driven by eccentricity-
764 modulated precession (Berger and Loutre, 1997; Berger et al., 2006). Even though two half-
765 precession cycles occur per precession cycle (Berger et al., 2006), their insolation expression
766 in terms of amplitude and phase may differ depending on latitude and geometry (e.g., Wu et
767 al., 2025). This would, in addition to high-frequency sedimentation rate changes, and the
768 presence of combination tones as a result of nonlinearities in the climate-sediment system,
769 explain why the extracted half-precession cycles are not phase-locked with precession (Fig.
770 9). Additionally, climate simulations show that the presence of ice sheets can further modulate
771 the amplitude and phase of half-precession responses by altering the background climate
772 state (Wu et al., 2025). Together, these mechanisms offer an explanation that accounts for the
773 modulated, non-phase-locked half-precession signal recovered from the Sherburne
774 Formation.



775 **7. Conclusions**

776 The cyclostratigraphic framework developed for the Sherburne Formation, guided by
777 the 405-kyr long-eccentricity metronome, reveals substantial astronomical forcing of detrital
778 influx in the late Givetian Appalachian Basin at ~30°S. Our results support a precession-
779 dominated hydrological regime with a distinct obliquity imprint and persistent half-precession
780 cycles. Based on the recognized Milankovitch imprint, the new cyclostratigraphic age model
781 constrains the duration of the Sherburne Formation in the Cargill #17 core to 1252 ± 29 kyr,
782 and constrains the durations of the regional Fir Tree, Hubbard Quarry, and Lodi events to 108
783 ± 29 kyr, 214 ± 29 kyr, and at least 200 ± 29 kyr, respectively – consistent with one to two short
784 eccentricity cycles. The onset of the global Frasnian Crisis unfolds during a 405-kyr long
785 eccentricity maximum and, possibly, during an extremum of the 1.2-Myr s_4 - s_3 obliquity-
786 modulation cycle governing eustatic sea-level variations.

787 The recovery of half-precession and obliquity in the pantropical belt highlights a
788 complex interplay of equatorial and high-latitude dynamics, shaping changing climatic
789 conditions. Nonlinear climate-sediment dynamics further influenced how these astronomical
790 rhythms were transmitted into the basin, affecting their expression in the detrital record. This
791 interplay can be understood in terms of the broader climatic mechanisms at work: climatic
792 teleconnections, monsoonal dynamics, ITCZ and Hadley-cell migration, ocean-circulation
793 changes, and possibly glacio-eustasy, collectively exerted considerable control over the
794 paleodepositional environment. Together, these mechanisms exerted strong control over
795 sediment supply to the Appalachian Basin, underscoring the strong and complex influence of
796 astronomical forcing on the late Givetian climate.



797 **Conflict of Interest**

798 The authors declare there are no conflicts of interest in this manuscript.

799 **Acknowledgements**

800 This is a contribution to the "Projet de Recherche" funded by the Belgian National Fund of
801 Scientific Research (FNRS), contract T.0037.22 "WarmAnoxia". Thomas J. Algeo is
802 acknowledged for supervising the GRS measurements of the Cargill #17 Core at the University
803 of Cincinnati, Ohio (USA) by Kyleigh Hope, A.J. Kmetz, and Thomas Gott. Magnetic
804 susceptibility data collection was undertaken by Beloit College undergraduates May Willison
805 and Olivia Farbarik; this work was supported by the donors of ACS Petroleum Research Fund
806 under Undergraduate Research Grant 60525-UR2 to J. Zambito.



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825 **Data and Code Availability Statement**

826 All data and R-code can be found via [10.5281/zenodo.19483389](https://doi.org/10.5281/zenodo.19483389)



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