



# Improving Simulations of Zeeman Absorption Spectrum for Hyperspectral Microwave Sounding Applications

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5 **Abstract.** Accurate simulation of microwave oxygen absorption is critical for upper atmospheric remote sensing, yet traditional models suffer from biases due to simplified Zeeman splitting calculations. Two key advancements were presented to address this challenge. First, the 2024 RS-LBL model is updated with the Zeeman coefficients of Larsson et al. (2019), which capture higher-order rotational and anisotropic spin effects, thereby eliminating the 1 K bias in 7<sup>+</sup> line simulations caused by the Hund's case (b) approximation. Second, a full vector radiative transfer equation with a complex propagation matrix is implemented to rigorously model polarization under Zeeman splitting, integrated with hybrid Lorentz-Gaussian broadening. Systematic sensitivity experiments quantify the impacts of magnetic field intensity, propagation angle, and frequency shift on polarized brightness temperatures. Leveraging these insights, the Hyperspectral Microwave Atmospheric Sounder (HMAS) is designed: a 60-63 GHz linearly polarized instrument comprising 150 channels, optimized to 39 composite channels for noise reduction. Performance benchmarks against SSMIS UAS channels confirm that HMAS  
15 delivers unprecedented vertical resolution with reduced noise, establishing it as an optimal payload concept for next-generation space exploration missions targeting the near space atmosphere.  
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## 1 Introduction

Near space typically refers to the region between 20 and 100 km (60-0.0004 hPa) above sea level, encompassing the stratosphere, mesosphere, and lower thermosphere (Yang et al., 2023). Observation of near space is crucial for weather  
25 forecasting and climate analysis (Eckermann et al., 2018; Liu et al., 2007; Zhao et al., 2021). The accuracy of upper atmosphere forecasts can be improved by assimilating near space observations in numerical weather prediction (NWP) systems (Eckermann et al., 2009; Hoppel et al., 2013, 2008; Maurer et al., 2015; Nezhlin et al., 2009). However, observations of the middle to upper atmosphere are comparatively rare due to technological and scientific limitations (Dong et al., 2024). Satellite-based data used in NWP assimilation systems at altitudes above 1 hPa are typically from the Microwave Limb  
30 Sounder (MLS), the Sounding of the Atmosphere using Broadband Emission Radiometry (SABER), and the Special Sensor Microwave Imager/Sounder (SSMIS) on board the Defense Meteorology Satellite Program (DMSP) satellite (Hoppel et al.,



2008). The temperature analysis fields from assimilated SSMIS upper atmospheric sounding (UAS) channels are comparable to those from SABER and MLS data (Hoppel et al., 2013). However, SSMIS has only six UAS channels with low vertical resolution and significant noise. Increasing the amount of high-quality upper atmospheric observation data is critical for weather forecasting and climate analysis.

Infrared hyperspectral instruments have now reached maturity, and the radiance data have been proven to improve NWP forecast accuracy (Aires et al., 2015; Eresmaa et al., 2017; McNally et al., 2006). However, microwave sensors have significantly fewer detection channels compared to infrared instruments due to technological limitations (Boukabara and Garrett, 2011). With recent advancements in Fast Fourier Transform spectroscopy technology, microwave radiometers with high spectral resolution have become a more feasible component in remote sensing (Kummerow et al., 2022; Liu et al., 2007). This is highly beneficial because microwave hyperspectral sampling can achieve a high-density weighting function (WF), which facilitates the accurate retrieval of temperature and water vapor profiles and exerts a positive impact on weather forecasting (Aires et al., 2015; Zhang et al., 2025). In recent years, various studies have focused on specific hyperspectral microwave channels and their ability to provide valuable observations for retrieval or NWP systems (Bi et al., 2024; Blackwell et al., 2011; Boukabara and Garrett, 2011). However, most studies primarily reference the Advanced Microwave Sounding Unit (AMSU) or Advanced Technology Microwave Sounder (ATMS) temperature and water vapor detection channels (around 52.6-57.3 GHz and 183.31 GHz), which primarily provide information on tropospheric clouds, precipitation, and surface parameters, with limited upper atmospheric information.

Microwave oxygen ( $O_2$ ) absorption channel observations and simulations above 40 km are affected by Earth's magnetic field. The  $2 \times 2$  coherency matrix formed radiative transfer equation can describe the Zeeman splitting effect (Lenoir, 1967, 1968; Rosenkranz and Staelin, 1988). To fully investigate the influence of magnetic field parameters on brightness temperature (BT) simulation, Stogryn (1989) derived the magnetic field-related symmetry, systematically revealing the quantitative impact of Zeeman splitting on  $O_2$  absorption line simulations (Stogryn, 1989). However, previous research is based on the Hund's case (b) assumption, which has limitations for low quantum numbers. Larsson et al. (2019) provide a new Zeeman splitting coefficients database, improving the  $O_2$  fine-structure lines simulation accuracy (Larsson et al., 2019). This article provides a brief review of the computational and simulation differences between the Hund's case (b) and Larsson (2019) implementations in Rosenkranz and Staelin's microwave Line-by-Line (referred to as RS-LBL) model (Larsson et al., 2019; Rosenkranz and Staelin, 1988). The RS-LBL model (version 2024) update with Larsson (2019) Zeeman splitting coefficients is employed to analyze the oxygen line sensitivity and detection altitude in section 3. In section 4, the hyperspectral channel characteristics for a microwave sounder capable of high-resolution detecting near space temperature are proposed.



## 2 Microwave Propagation in Near Space O<sub>2</sub> Medium

### 2.1 Zeeman Splitting Coefficient

65 Under the influence of an external magnetic field, the Zeeman splitting effect causes energy levels to split, with the emitted  
or absorbed radiation originating from the molecule's magnetic dipole (Zeeman, 1897). The intensity and direction of the  
magnetic dipole moment are typically represented by the quantum mechanical matrix element  $\mu(N, M, \Delta J, \Delta M)$ , which  
denotes the transition strength when one quantum state transitions to another (Berdyugina and Solanki, 2002; Lenoir, 1968).  
70  $N$  represents the molecular quantum number for the end-over-end rotation. The magnetic quantum number  $M$  describes the  
quantum number of the electron's orbital angular momentum (or total angular momentum) component in the direction of a  
magnetic field within an atom. Its value is related to the total angular momentum quantum number  $J$ , expressed as  
 $M = -J, -J + 1, \dots, 0, \dots, J - 1, J$ , reflecting the spatial orientation of the atomic state within the magnetic field (Hill and  
Gordy, 1954).  $\Delta J$  denotes the total angular momentum quantum number change, describing the alteration in the atom's total  
angular momentum  $J$  before and after the transition.  $\Delta M$  denotes the difference between the final magnetic quantum  
75 number  $M'$  and the initial magnetic quantum number  $M$  during atomic transitions, i.e.,  $\Delta M = M' - M$ , serving as the core  
parameter for analyzing molecular radiation behavior and spectral splitting in magnetic fields. It determines the type of  
transition and directly correlates with the polarization characteristics of the emitted radiation:  $\Delta M = 0$  is commonly called  
the  $\pi$  component,  $\Delta M = \pm 1$  is called the  $\sigma^\pm$  component (Berdyugina and Solanki, 2002; Lenoir, 1968; Schadee, 1978).

80 A so-called 'g-factor' is commonly used to quantify the interaction intensity between a magnetic field and specific energy  
levels  $J_N$  of oxygen molecules. In an external magnetic field,  $g_{J_N}$  directly determines the energy perturbation of the  
Zeeman splitting (Hill and Gordy, 1954; Lenoir, 1968):

$$\Delta W = -g_{J_N} \mu_B M_J H \quad (1)$$

where  $\mu_B$  is the Bohr magneton,  $H$  represents the external field strength,  $M_J$  is the quantum number for the projection of  
85 total angular momentum on the magnetic field direction.

Previous microwave LBL models, such as the Millimeter-Wave Propagation Model (MPM) (Liebe, 1989) and RS-LBL  
(version 1988) (Rosenkranz and Staelin, 1988), as well as the Atmospheric Radiative Transfer Simulator (ARTS)  
calculations before 2014 (Larsson et al., 2014), employed Hund's case (b) basis wavefunctions to determine the Zeeman  
90 splitting coefficient:

$$g_{J_N}^{\text{Hund,b}} = \frac{g_S [J(J+1) - N(N+1) + S(S+1)]}{2J(J+1)} \quad (2)$$

where the  $S$  is the electronic spin-quantum number. This model is dominated by the electron spin  $g_s$  Zeeman effect, neglecting the fine-structure Hamiltonian off-diagonal elements and higher-order Zeeman effects (Larsson et al., 2014; Lenoir, 1968; Rosenkranz and Staelin, 1988).

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Recently, (Larsson et al., 2019) provide an updated Zeeman splitting coefficient calculation, which incorporates higher-order rotational  $g_r$  and anisotropic spin  $g_l^e$  Zeeman effects:

$$g_{J_N}^{\text{Larsson}} = g_s \cos^2 \phi + (g_s + 2g_l^e) \sin^2 \phi + 2g_r \cos \phi \sin \phi \quad (3)$$

where  $\phi$  is the diagonalization angle, determined by the ratio of the off-diagonal elements to the diagonal elements in the fine-structure Hamiltonians. For the derivation of the  $g_s$ ,  $g_r$ ,  $g_l^e$ , and  $g_{J_N}$  and the calculation results for  $g_{J_N=J-1}$ ,  $g_{J_N=J}$ , and  $g_{J_N=J+1}$ . Please refer to (Larsson et al., 2019).

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## 2.2 Oxygen Absorption

Oxygen absorption at microwave frequencies is a key element in atmospheric remote sensing and retrieval. The frequency characteristics and vertical sounding distribution provide critical data for retrieving atmospheric temperature profiles, pressure profiles, and dynamic processes. In practice,  $O_2$  absorption is not confined to a single frequency of a spectral line but is broadened by other influences (Tretyakov et al., 2005), primarily collisional or pressure broadening in the troposphere, which can typically be represented by Lorentz lines (Koshelev et al., 2015). In the upper atmosphere, the collisional broadening effect diminishes, and the absorption line broadening is now primarily caused by the relative motion of molecules (Doppler broadening), resulting in Gaussian line shapes (Ben-Reuven and Lightman, 1967; Koshelev et al., 2021; Van Vleck and Weisskopf, 1945).

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In mathematics, the  $O_2$  absorption coefficient is typically expressed as the per unit volume of oxygen molecules' power absorption efficiency for a specific microwave frequency (Unit: dB/km) (Liebe et al., 1977; Van Vleck, 1947):

$$\alpha(\nu) = n \sum_{j,i} S_{ji}(T) F(\nu, \nu_{ji}) \quad (4)$$

where  $n$  is the number of molecules per unit volume, and  $\nu$  is the incident electromagnetic wave frequency.  $j$  and  $i$  denote two distinct energy levels of an isolated molecule, where  $i$  represents the initial state energy level and  $j$  the final state. The absorption or emission process involves the molecule transitioning between energy levels  $i$  and  $j$ . The corresponding transition frequency is  $\nu_{ji} = (E_j - E_i) / h$ , where  $E_j$  and  $E_i$  are the final and initial states' energy, respectively,  $h$  is the Planck constant,  $S_{ji}(T)$  the monochromatic intensity of a single molecule at temperature  $T$ ,  $F(\nu, \nu_{ji})$  is the normalized line shape function, and the summation term  $\Sigma$  represents the sum over all possible energy level transition combinations.

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When performing microwave remote sensing and radiative transfer modeling at the atmosphere below 40 km, the  $O_2$  absorption coefficient  $\alpha$  is used in the scalar radiative transfer equation to express the absorption and emission of the medium. For this study, oxygen absorption lines above 40 km are also affected by the Zeeman splitting (Hill and Gordy, 1954; Meeks and Lilley, 1963). Only the vector radiative transfer equation can fully describe the radiation polarization characteristics at this complex condition. In the vector radiative transfer equation, the scalar  $\alpha$  is replaced by the complex propagation matrix  $\mathbf{G}$ , which incorporates  $O_2$  absorption properties (Lenoir, 1967):

$$\mathbf{G} = \begin{pmatrix} G_{11} & G_{12} \\ G_{21} & G_{22} \end{pmatrix} \quad (5)$$

with

$$G_{11} = \frac{1}{2}(1 + \cos \theta)^2 \cdot G_{\sigma_+} + \frac{1}{2}(1 - \cos \theta)^2 \cdot G_{\sigma_-} + \frac{1}{2}(1 - \cos^2 \theta) \cdot G_{\pi}$$

$$G_{22} = \frac{1}{2}(1 - \cos \theta)^2 \cdot G_{\sigma_+} + \frac{1}{2}(1 + \cos \theta)^2 \cdot G_{\sigma_-} + \frac{1}{2}(1 - \cos^2 \theta) \cdot G_{\pi}$$

$$G_{12} = G_{21} = \frac{1}{2}(1 - \cos^2 \theta) \cdot (G_{\sigma_+} + G_{\sigma_-} - G_{\pi})$$

where  $\theta$  is the angle between the magnetic field vector and the electromagnetic wave propagation direction. The calculation principles and formulas for  $G_{\pi}$ ,  $G_{\sigma_+}$ , and  $G_{\sigma_-}$  are analogous to those in Eq. (4), representing the product of the oxygen Zeeman relative intensities and line shape functions. The  $O_2$  line Zeeman component frequency shift and relative intensity calculation can be found in (Lenoir, 1968). The line shape is calculated using the complex error function (CERROR), as referenced in (Hui et al., 1978).

### 2.3 Radiative Transfer Transmittance Solution

The  $g_{J_N}$  determines the frequency shift and intensity of the oxygen line Zeeman components, influencing the absorption and radiance calculations. Therefore, this study calculates  $\mathbf{G}$  based on both  $g_{J_N}^{\text{hund,b}}$  and  $g_{J_N}^{\text{Larsson}}$  and determines the upward radiance. When dealing with the Zeeman effect radiance above 40 km, the BT coherence matrix can be solved directly. Incident radiance is calculated through the scalar radiative transfer model. The BT matrix is a  $2 \times 2$  matrix, with diagonal elements corresponding to linear-based or circular-based polarized brightness temperatures (Lenoir, 1968).

Alternatively, the total transmittance is calculated based on the oxygen absorption coefficient, and then the BT can be derived. Considering only oxygen absorption, the specific frequency transmittance  $\Gamma_v(z)$  of the  $O_2$  absorption line from



altitude  $z$  to the top of atmosphere relates to the optical depth  $\tau_v$  and  $O_2$  absorption coefficient  $\alpha(v, z)$  as follows (Meeks and Lilley, 1963; Weng, 2017):

$$\Gamma_v(z) = \exp\left(-\frac{\tau_v}{\mu}\right) = \exp\left(-\int_z^\infty \frac{\alpha(v, z)}{\mu} dz\right) \quad (6)$$

150 where  $\alpha(v, z)$  is the volumetric absorption coefficient in unit of  $\text{cm}^{-1}$ ,  $\mu = \cos(\beta)$ ,  $\beta$  is the zenith angle. For atmospheric detection, the integral term in Eq. (6) is obtained by summing all absorptions within each thin layer.

For the atmosphere above 40 km, the product matrix  $\mathbf{P}$  is solved through matrix diagonalization (Rosenkranz and Staelin, 1988).  $\mathbf{P}$  is a  $2 \times 2$  complex matrix that shares the same properties as  $\mathbf{G}$ . Based on  $\mathbf{P}$ , the transmittance matrix  $\mathbf{\Gamma}$  can be  
 155 calculated:

$$\mathbf{\Gamma} = \begin{pmatrix} \Gamma_{VV} & \Gamma_{VH} \\ \Gamma_{HV} & \Gamma_{HH} \end{pmatrix} \quad (7)$$

where the diagonal elements  $\Gamma_{VV}$  and  $\Gamma_{HH}$  represent the vertical and horizontal total transmittance, respectively, while the off-diagonal elements measure the coherence of the diagonal elements. The transmittance within each layer is multiplied by the atmospheric temperature, and then summed across the entire atmospheric column to obtain the brightness temperature  
 160 matrix.

The relation between the BT matrix diagonal element and the Stokes parameters is:

$$T_{B_{VV}} = (I + Q) / 2; \quad T_{B_{HH}} = (I - Q) / 2; \quad T_{B_{VH}} = (U - iV) / 2 \quad (8)$$

$$T_{B_{RC}} = (I - V) / 2; \quad T_{B_{LC}} = (I + V) / 2; \quad T_{B_{RL}} = (Q + iU) / 2 \quad (9)$$

165 where  $I$  is the total radiance intensity,  $Q$  is the difference between vertical and horizontal linear polarization,  $U$  is the difference between  $\pm 45^\circ$  linear polarization, and  $V$  is the difference between left- and right-hand circular polarization (Eriksson et al., 2011).

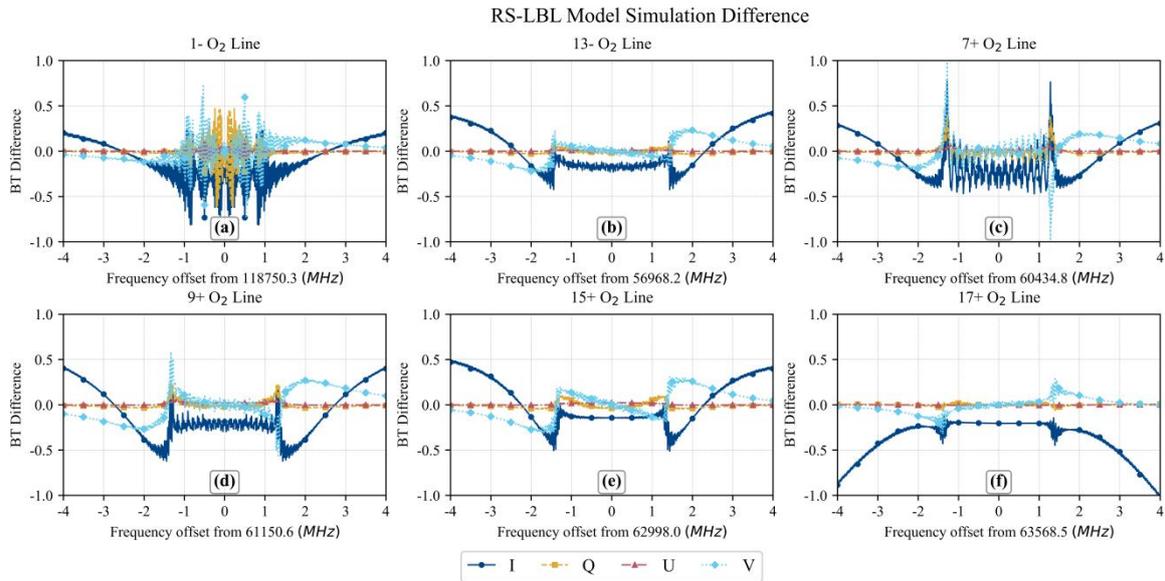
### 3 Simulation Results

#### 3.1 Microwave LBL Model Simulations

170 The BT matrix and Stokes vector for different oxygen absorption lines based on  $g_{J_N}^{\text{Hund,b}}$  and  $g_{J_N}^{\text{Larsson}}$  are calculated, respectively. Figure 1 shows the Stokes parameter differences between the Hund's case (b) and Larrson (2019) implementations for the different  $O_2$  lines. From Fig. 1, the  $7^+$  line  $V$  component exhibits the greatest absolute BT difference compared to other lines, approaching 1 K at a frequency shift of 1.3 MHz. The absolute differences of the  $1^-$  oxygen line in  $I$ ,



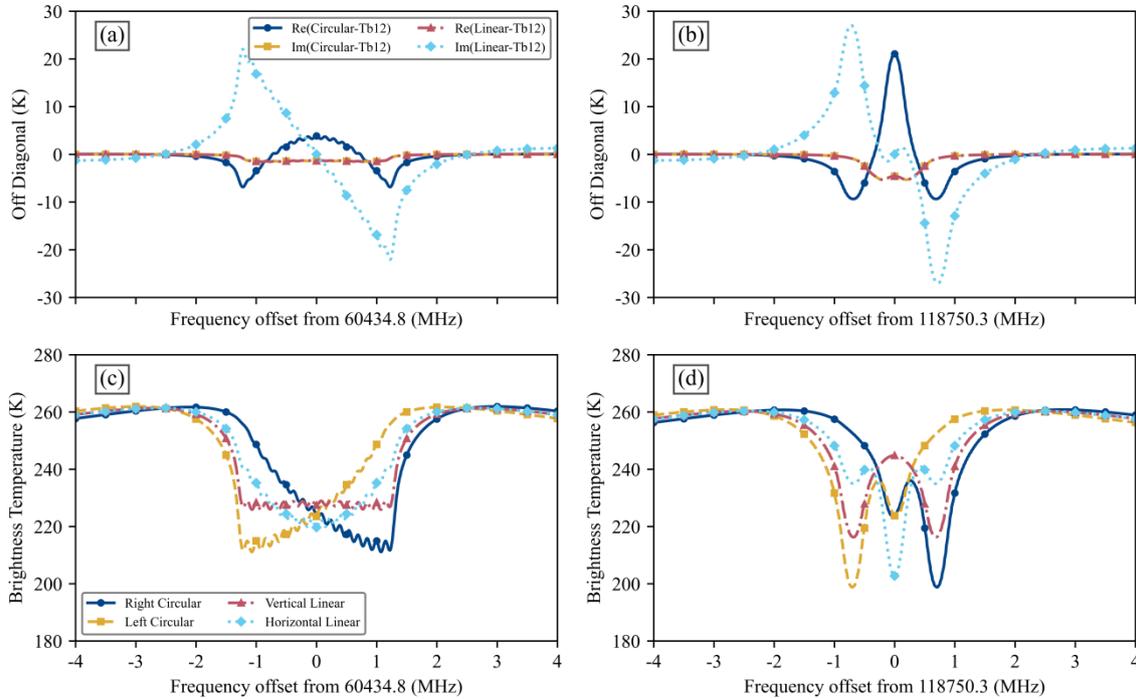
175  $Q$ , and  $V$  exceed 0.5 K within a frequency shift of 1 MHz. The differences are significant, and the newer Zeeman spectroscopy will hopefully improve the representation of upper atmosphere observations. Overall, the  $U$  component simulation differences of all oxygen lines are minimal, while the  $I$  and  $V$  components are more pronounced.



180 **Figure 1:** Stokes vector simulation differences between the Hund (b) and Larsson (2019) implementation of the microwave LBL model for total magnetic field strength  $B_e = 0.5$  Gauss,  $\theta = 135^\circ$ : (a)  $1^-$  (118.7503 GHz); (b)  $13^-$  (56.9682 GHz); (c)  $7^+$  (60.4348 GHz); (d)  $9^+$  (61.1506 GHz); (e)  $15^+$  (62.9980 GHz); and (f)  $17^+$  (63.5685 GHz) line (The dark blue (solid) line represents  $I$ , yellow (dashed) line represents  $Q$ , red (dashed-dotted) line represents  $U$ , and light blue (dotted) lines for  $V$ ).

185 Considering that  $g_{J_N}^{\text{Larsson}}$  primarily affects simulations at low  $J_N$  energy levels, where the  $7^+$  line intensity is the strongest, and the  $1^-$  line occupies a unique frequency position, these two lines are simulated using the RS-LBL model (version 1988) with improved Larsson (2019) implementation. Figure 2 shows the BT matrix elements distribution for the  $7^+$  line and the  $1^-$  line as a function of frequency for an input total magnetic field strength ( $B_e$ ) of 0.5 Gauss, and  $\theta$  of  $135^\circ$ . In Figures 2a and 2b, the BT matrix off-diagonal elements are used to describe the coherence of the diagonal elements. Figures 2c and 2d depict the BT matrix diagonal elements. From Figs. 2c and 2d, when the frequency offset between the  $7^+$  line and  $1^-$  line is around 1 MHz, the circularly-based polarization BT is lower than that of the linearly-based. When the frequency shift exceeds 2 MHz, the brightness temperatures of circular and linear polarization are comparable. Additionally, the left-hand and right-hand circular polarization brightness temperatures are the mirror of one another at the oxygen line center. The horizontal and vertical linear polarization brightness temperatures are symmetric about the oxygen absorption line center frequency.

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195 **Figure 2:** Brightness temperature matrix elements distribution as a function of frequency shift from  $7^+$  (left panel) and  $1^-$  (right panel) line center. In (a-b), the dark blue (solid) and yellow (dashed) lines represent the real and imaginary parts of circular polarization, respectively, and the red (dashed-dotted) and light blue (dotted) lines represent the real and imaginary parts of linear polarization, respectively. In (c-d), the dark blue (solid) and yellow (dashed) lines represent the right-hand and left-hand circular polarization simulated BT, respectively, and the red (dashed-dotted) and light blue (dotted) lines represent the vertical and horizontal linear polarization BT, respectively.

### 3.2 Dependence of $O_2$ Line on Magnetic Field

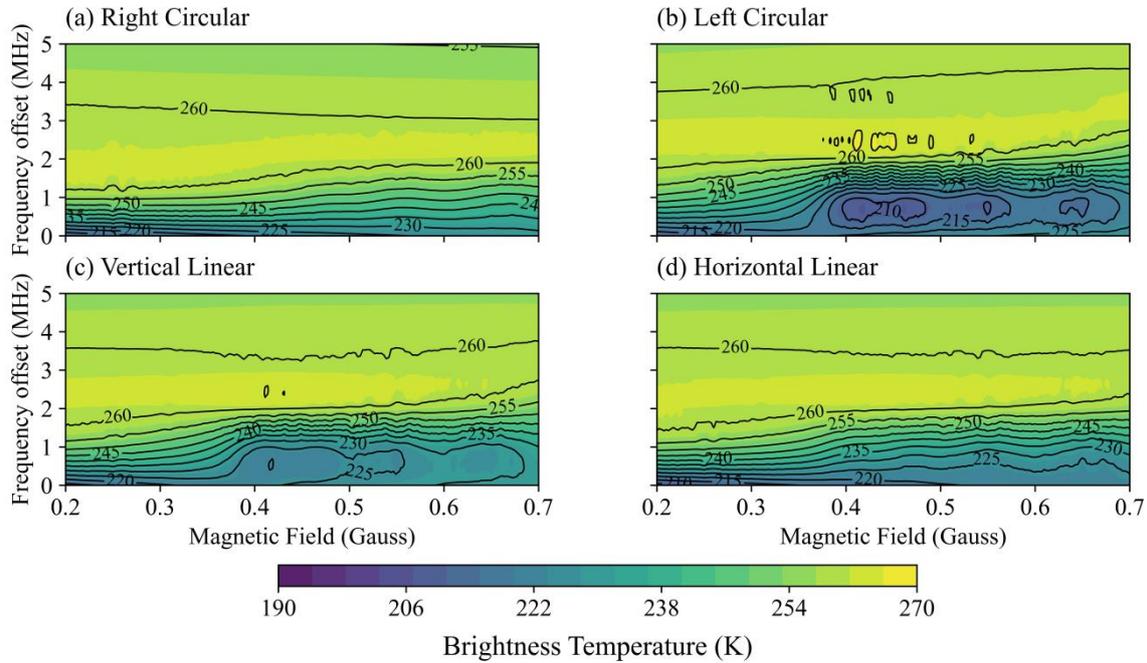
200 To evaluate the impact of the Earth's magnetic field on  $O_2$  absorption line simulations, two sets of experiments are conducted in this section. For experiment 1, the cosine of the angle between the magnetic field vector and the electromagnetic wave propagation direction ( $\cos(\theta)$ ) is set to a fixed value of 0.7, while  $B_e$  increases from 0.2 to 0.7 Gauss in steps of 0.01 Gauss. For experiment 2,  $B_e$  is fixed at 0.45 Gauss, while  $\theta$  ranges from  $0^\circ$  to  $180^\circ$  in steps of  $1^\circ$  ( $\cos(\theta)$  from 1 to -1). Figure 3 shows the  $7^+$  line simulated brightness temperatures for different polarizations, with the y-axis representing frequency shift from line center increases from 0 to 5 MHz in steps of 1 MHz. From Fig. 3, at the frequency shift of approximately 2-3 MHz, a distinct high-temperature region (260-270 K) appears across the entire magnetic field, exhibiting a relatively uniform distribution. When the frequency shift exceeds 3 MHz, the BT exhibits a highly uniform horizontal distribution, indicating that the polarization state and magnetic field exert a negligible influence at high frequency shifts. However, when the frequency shift is below 2 MHz, the BT varies significantly with magnetic field strength, exhibiting unique behavior across different polarization states.

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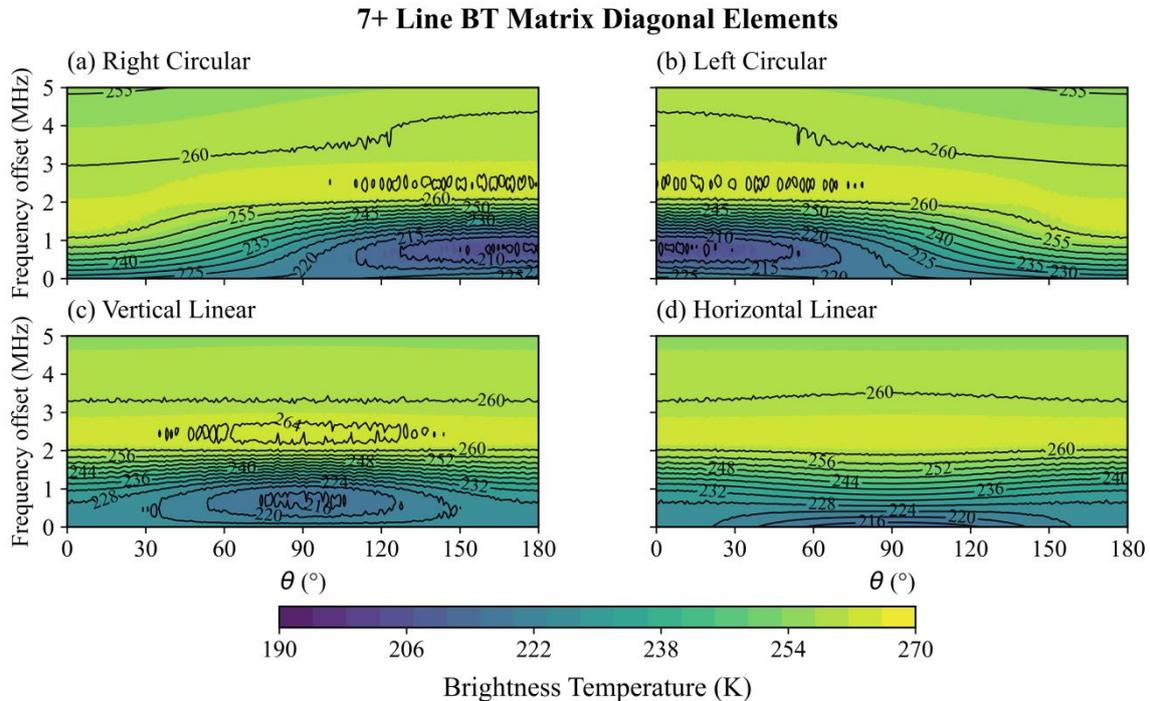
### 7+ Line BT Matrix Diagonal Elements



**Figure 3:** 7+ line center frequency shift from 0-5 MHz (step of 1 MHz) simulated brightness temperature distribution with  $B_e$  from 0.2-0.7 Gauss (step of 0.01 Gauss) at a fixed  $\cos(\theta)$  of 0.7 for (a) Right-hand circular polarization; (b) Left-hand circular polarization; (c) Vertical linear polarization; (d) Horizontal linear polarization.

215 The results of experiment 2 are presented in Fig. 4. Compared to the magnetic field strength distribution, the brightness temperature exhibits a more regular variation with  $\theta$ . From Fig. 4a, the low-temperature region is primarily concentrated in the frequency shift below 1.5 MHz and a  $\theta$  of  $90^\circ$ - $180^\circ$ , while the high-temperature region is mainly distributed in the frequency shift above 2 MHz. The left circular polarization (Fig. 4b) brightness temperature symmetry is to that of the right. Vertical linear polarization (Fig. 4c) shows low-temperature regions at frequency shifts below 1.5 MHz and within a  $\theta$  range of  $30^\circ$ - $150^\circ$ , with the lowest temperature occurring near  $\theta=90^\circ$ . The horizontal linear (Fig. 4d) polarization brightness temperature shows good uniformity. When the frequency shift exceeds 1.5 MHz, the contour lines for linear polarization are nearly parallel to the x-axis, indicating that linear polarization detection has greater advantages under this condition. Additionally, the linear polarization BT is symmetric about  $\theta=90^\circ$ .

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225 **Figure 4:** 7+ line center frequency shift from 0-5 MHz (step of 1 MHz) simulated brightness temperature distribution with  $\theta$  from 0-180° (step of 1°) at a fixed  $B_e$  of 0.45 Gauss for (a) Right-hand circular polarization; (b) Left-hand circular polarization; (c) Vertical linear polarization; (d) Horizontal linear polarization.

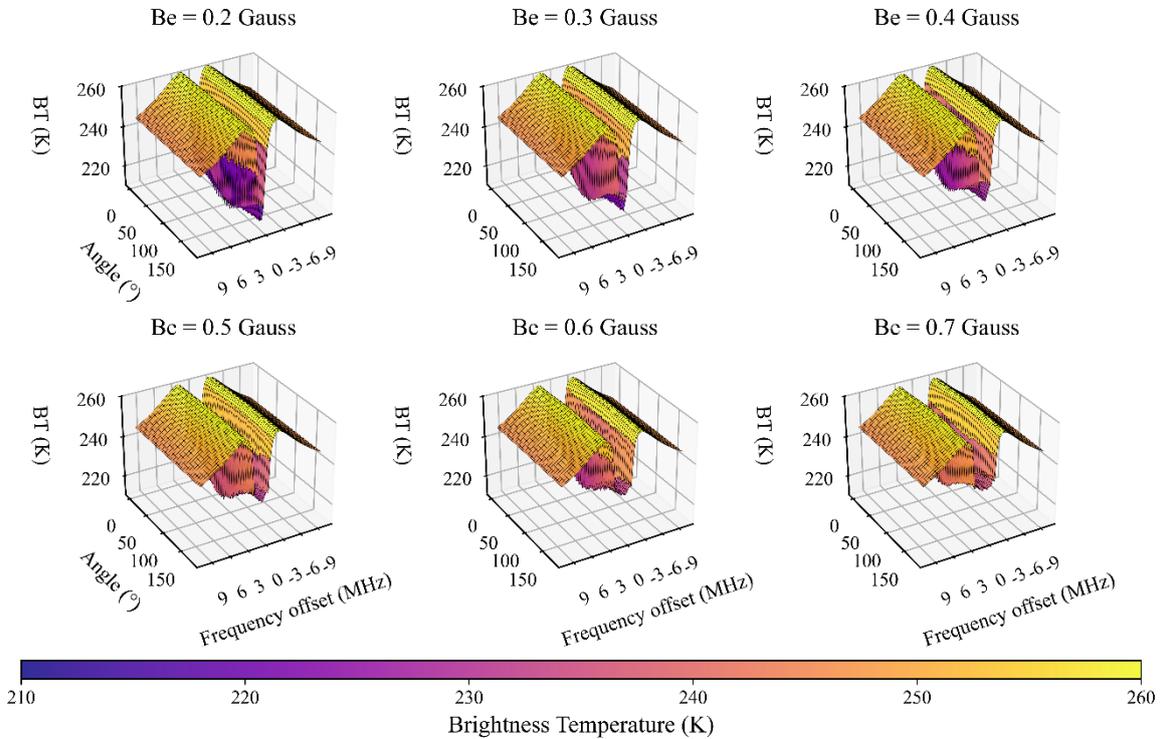
### 3.3 Analysis of Detection Altitude

Most past studies are based on fixed magnetic field strengths or angles, which are not sufficiently representative of the real Earth's atmospheric environment. This section performs three sets of cyclic calculations for  $B_e$ ,  $\theta$ , and frequency shift from the O<sub>2</sub> line center: 1.  $B_e$  ranges from 0.2-0.7 Gauss with steps of 0.1 Gauss. 2.  $\theta$  ranges from 0° to 180° in steps of 1°. 3. The frequency is determined by a 10 MHz shift from the O<sub>2</sub> absorption line center in steps of 0.1 MHz. The detection altitude of the 50-70 GHz oxygen absorption line under varying frequency and magnetic field conditions is analyzed, providing theoretical support for designing microwave sounder channels in near space environments. 7+ line vertical linear polarization BT is calculated and shown in Fig. 5, since past research focused more on circular polarization.

Each subplot of magnetic field strength in Fig. 5 displays two “peaks” (yellow high-BT) and one “valley” (purple low-BT). From Fig. 5, the “peaks” are primarily located near the 3 MHz frequency shift, with brightness temperatures reaching 260 K, while the “valleys” are mainly around the O<sub>2</sub> line center, with brightness temperatures as low as 220 K (corresponding to Fig. 3). When  $B_e$  increases from 0.2 Gauss to 0.7 Gauss, the “peaks” pattern remains virtually unchanged, but the “valleys” gradually contract upward, meaning that the brightness temperature upward with increasing magnetic field strength. The slope between “peak” and “valley” exhibits distinct temperature gradient variations (e.g., the boundary between yellow and

orange), which are nearly unchanged with  $\theta$  (consistent with the contour line structure in Fig. 4). This phenomenon indicates that the simulated brightness temperature increases with frequency shift and that the BT is unaffected by the observed angle. According to the standard atmospheric temperature profile distribution, the “peak” in Fig. 5 corresponds to an altitude of approximately 1 hPa. The simulated brightness temperature increases initially and then decreases with frequency shift, meaning the detection altitude gradually decreases.

### Vertical Linear Polarization Distribution



**Figure 5:**  $7^+$  line vertical linear polarization simulated brightness temperature distribution at 3 cyclic conditions: frequency shift of oxygen absorption line center from -10 MHz to 10 MHz in steps of 0.1 MHz,  $B_e$  ranges from 0.2-0.7 Gauss in steps of 0.1 Gauss, and  $\theta$  ranges from  $0^\circ$  to  $180^\circ$  in steps of  $1^\circ$ .

When quantitatively analyzing detection altitude, weighting functions are typically employed, with the peak height corresponding to the altitude where the radiation signal is strongest (Zhang et al., 2024). The WF is typically defined as a function of single-layer ( $l$ ) atmospheric pressure ( $P_l$ ) and the transmittance at specific frequencies ( $\nu$ ) (Rosenkranz and Staelin, 1988):

$$WF = (\Gamma_{l-1} - \Gamma_l) / [\ln(P_l) - \ln(P_{l-1})] \quad (10)$$

when  $l = 0$  (top of atmosphere):

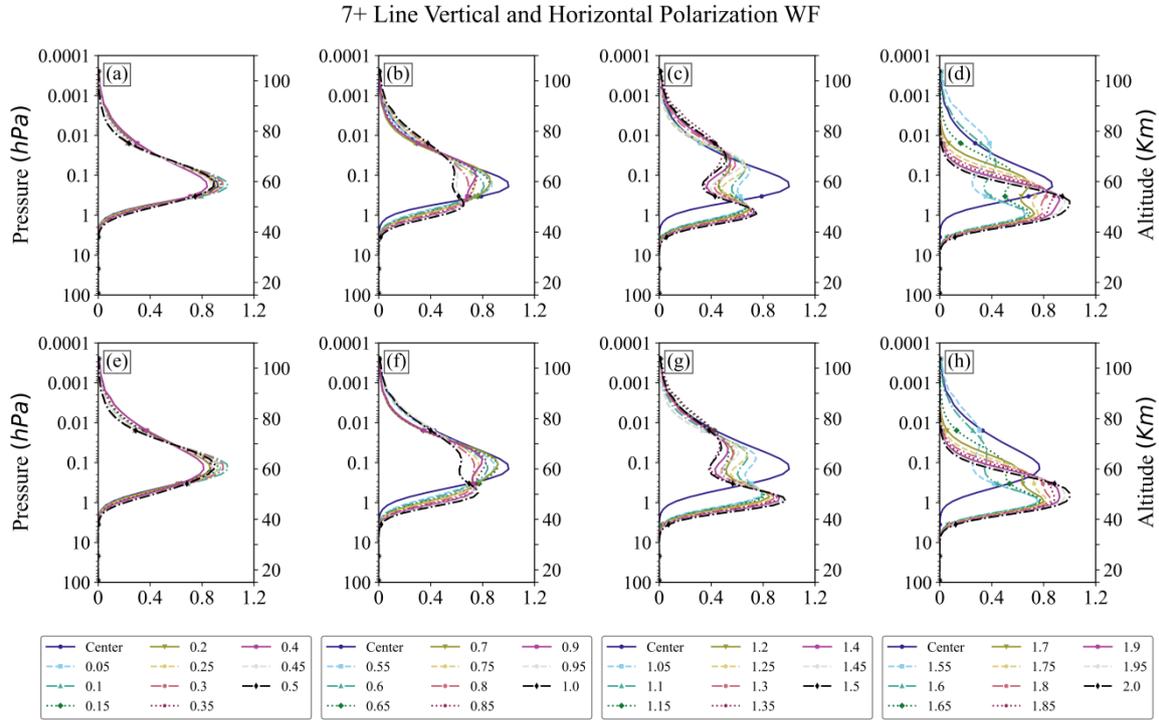
$$WF = (1 - \Gamma_l) / [\ln(P_{l+1}) - \ln(P_l)] \quad (11)$$



260 The avoidance of linear polarization in near space microwave remote sensing is largely due to its “double-peaked” WF  
(Rosenkranz and Staelin, 1988). According to Fig. 5, the locations where the WF exhibits “double-peaked” largely  
correspond to stronger magnetic field strength, meaning that linear polarization introduces uncertainty in observations and  
simulations of the polar regions or areas prone to electromagnetic storms. However, this “double-peaked” phenomenon  
changes with frequency shift. When the frequency shift exceeds 2 MHz, the magnetic field strength has a negligible effect on  
the temperature detection (Fig. 3). Furthermore, linear polarization offers significant symmetry advantages at the observed  
265 angle. It should be important for profiling the near space vertical atmosphere if the same oxygen absorption channel can be  
used for both linearly and circularly polarized detection.

To achieve full-polarization near space atmospheric detection, it is essential to investigate the distribution characteristics of  
the “double-peak” weighting function in linear polarization. The “double-peak” WF is more likely to appear at strong  $B_e$  (Fig.  
270 5). Therefore, this study fixed the magnetic field strength and  $\cos(\theta)$  at 0.63 Gauss and 0.9, respectively. The fine-structure  
weighting function for the  $7^+$  (60.4348 GHz) line and its 2 MHz frequency shift in 0.05 MHz is shown in Fig. 6. From Fig. 6,  
the WF is relatively narrow when the  $7^+$  line frequency shift is within 0.5 MHz, and the peak heights for both vertical (Figure  
6a) and horizontal (Fig. 6e) polarization are approximately 60 km (0.1 hPa). The weighting function starts to broaden at  
frequency shift 0.75 MHz, gradually exhibiting “double-peaked”. The altitudes of “double-peaked” are approximately 50  
275 and 65 km, with the lower-level signal being stronger, particularly in horizontal polarization. The “double-peak” structure  
gradually weakens as the frequency shift continues to increase, and the WF signal of the lower atmosphere gradually  
intensifies. At a frequency shift of 2 MHz, it exhibits a perfect narrow “single-peaked” WF.

Therefore, for linear polarization, oxygen line frequency shifts outside the range of 0.8-1.8 MHz can be selected to avoid the  
280 effects of the “double peak”. This selection of extreme cases aims to enable detailed simulation and analysis of oxygen lines  
under strong magnetic field conditions. Reality, not all oxygen absorption lines exhibit a “double peak” (such as  $17^+$ ) at high  
magnetic field strengths, which also depends on the intensity of the oxygen absorption line itself. In actual detection,  
multiple oxygen absorption lines are typically combined to diminish the influence of a single line.



285 **Figure 6:** Weighting Functions of 7+ line frequency shifts from 0.05-2 MHz at  $B_e$  of 0.63 Gauss and  $\cos(\theta)$  of 0.9 for the (a-d) vertical linear polarization, and (e-h) horizontal linear polarization. (a, e) represent frequency shifts of 0.05-0.5 MHz from the 7+ line center, (b, f) represent frequency shifts of 0.55-1.0 MHz, (c, g) represent shifts of 1.05-1.5 MHz, (d, h) represent shifts of 1.55-2.0 MHz. Colors denote the magnitude of the shift, with black lines indicating the 7+ line.

#### 4 Microwave Sounder in Near Space

##### 290 4.1 SSMIS UAS Channel Characteristics

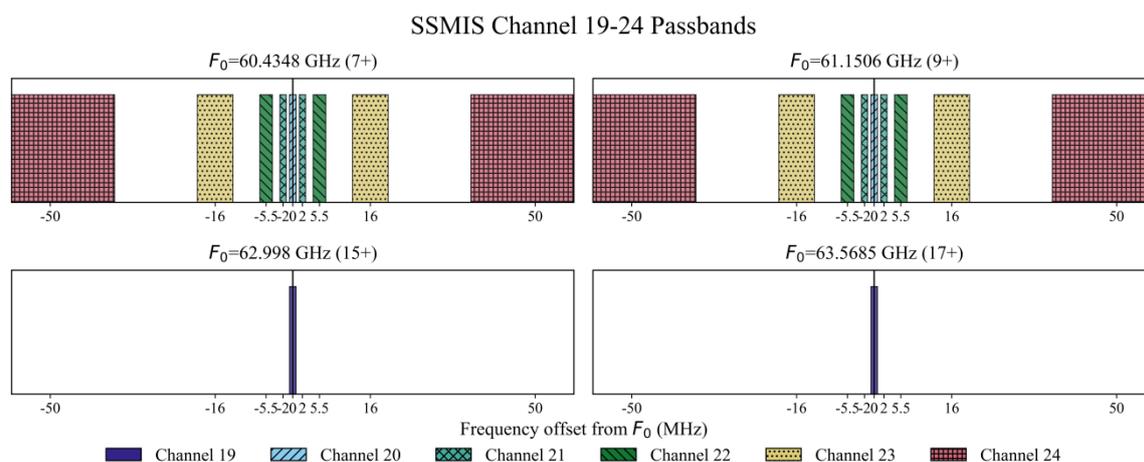
The SSMIS on board DMSP satellites, which features six channels capable of detecting altitudes from 20 to 100 km (Swadley et al., 2008). To achieve upper atmospheric detection, a narrow bandwidth is currently the preferred method (Lipton, 2003). However, a single narrow bandwidth often comes with significant channel noise, which may render the data unusable. The relationship between channel noise and bandwidth is as follows (Zhang et al., 2024):

295 
$$NEDT = (T_r + T_a) / \sqrt{BW \cdot t} \quad (12)$$

where  $NEDT$  denotes the channel noise,  $BW$  represents the channel bandwidth,  $T_r$  is the receiver equivalent noise temperature,  $T_a$  is the antenna temperature, and  $t$  is the integration time.



To reduce noise, channels are typically designed as a double- or quadruple-sideband, and multi-line cooperative detection  
 300 can significantly improve *NEDT* performance (Kunkee et al., 2008; Pardo et al., 1998). In SSMIS channel 19, the local  
 oscillator (LO) is positioned between the 15<sup>+</sup> and 17<sup>+</sup> line frequencies, while channels 20-24 are between the 7<sup>+</sup> and 9<sup>+</sup> lines  
 to achieve multiband detection. These UAS channels are designed for circular polarization. The SSMIS channel passband  
 distribution is shown in Fig. 7. SSMIS channel 20 has two passbands with bandwidths of approximately 1.35 MHz covering  
 the 7<sup>+</sup> and 9<sup>+</sup> lines, respectively. Channel 19 also features two passbands with bandwidths of approximately 1.35 MHz,  
 305 covering the 15<sup>+</sup> and 17<sup>+</sup> lines, respectively. Channel 21 has four passbands, each bandwidth of approximately 1.3 MHz,  
 positioned 2 MHz on either side of the 7<sup>+</sup> and 9<sup>+</sup> oxygen absorption lines. Channels 22-24 also feature four passbands  
 centered at the 7<sup>+</sup> and 9<sup>+</sup> oxygen line frequencies, with frequency shifts of ±5.5 MHz, ±16 MHz, and ±50 MHz, respectively.  
 Their respective bandwidths are 2.6 MHz, 7.35 MHz, and 26.5 MHz. The detection altitude of the channel decreases as the  
 oxygen line shift increases, enabling detection of near space environments (Swadley et al., 2008).



310

**Figure 7:** SSMIS channel 20-24 (upper panel) and channel 19 (bottom panel) passband distribution. The x-axis labels the passband frequency shift from the O<sub>2</sub> line, while the “rectangular” width indicates the bandwidth.

#### 4.2 HMAS Passband Distribution

The SSMIS is relatively mature, with remaining instruments approaching the end of their operational lifetimes. This study  
 315 proposes a high-resolution microwave sounder based on the same design principles as SSMIS, but with linear polarization.  
 Aiming to increase near space observations, with the new channels complementing and extending the existing SSMIS UAS  
 channels. To achieve high-resolution continuous detection, this study introduces channels that utilize new oxygen line  
 combinations around 11<sup>+</sup> and 13<sup>+</sup> based on the existing channel specifications. The first channel bandwidth centered on each  
 oxygen line is set to 1.8 MHz to reduce channel noise. Then a second channel with a bandwidth of 2 MHz is set near each  
 320 further oxygen line offset of 1.9 MHz. Thanks to recent microwave hyperspectral detection technology, the channels away  
 from the absorption line centers can all be set to narrow values, so the bandwidths of the remaining channels are all set to 2.2  
 MHz.



Based on these design principles, multiple channels with narrow bandwidth can be formed on either side of the 7<sup>+</sup>, 9<sup>+</sup>, 11<sup>+</sup>,  
 325 13<sup>+</sup>, 15<sup>+</sup>, and 17<sup>+</sup> oxygen lines. All these channel coverage or side of the oxygen absorption line can theoretically be  
 implemented on the same instrument named Hyperspectral Microwave Atmospheric Sounder (HMAS). Figure 8 shows the  
 HMAS partly channel distribution, where the top panel, middle panel, and bottom panel groups represent three sets of  
 detection channels designed with different oxygen line combinations, with the corresponding passbands for the SSMIS  
 channels overlaid. From Fig. 8, approximately 150 channels of the HMAS achieve continuous frequency coverage within the  
 330 7<sup>+</sup>, 9<sup>+</sup>, 11<sup>+</sup>, 13<sup>+</sup>, 15<sup>+</sup>, and 17<sup>+</sup> oxygen line offsets to  $\pm 26$  MHz with detection frequency from about 60-63 GHz.

To compare with SSMIS, the HMAS 150 channels are set to passband and combined into 39 composite channels. In HMAS  
 39 composite channels, there are 3 double-sideband and 36 quadruple-sideband composite channels. For microwave  
 radiometers, the  $T_a$  is typically assumed to be 290 K, and the  $T_r$  is calculated based on frequency, approximately 300 K at  
 335 60 GHz (Zhang et al., 2024). In this study, the system noise temperature is set to 800 K ( $T_r + T_a = 800\text{K}$ ). To reduce channel  
 noise, we plan to extend the integration time to approximately 44.3 ms. According to Eq. (12), the *NEDT* of HMAS  
 Composite Channel 1 is approximately 2 K. Table 1 gives the HMAS channel parameters.

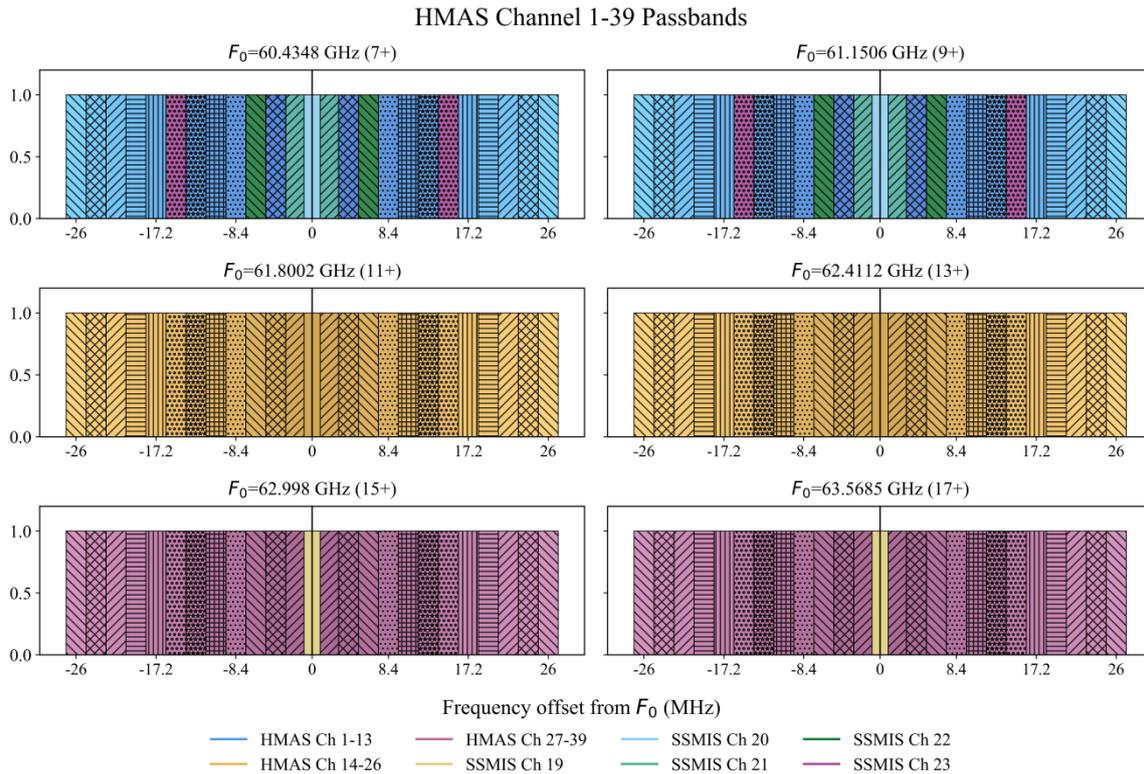
**Table 1** HMAS channel characteristics.

Channel	Center Frequency (GHz)	3-db Width (MHz)	NEDT (K)
1	60.7927±0.35790	1.8	2.00
2	60.7927±0.35790±0.0019	2.0	1.34
3	60.7927±0.35790±0.0040	2.2	1.28
4	60.7927±0.35790±0.0062	2.2	1.28
5	60.7927±0.35790±0.0084	2.2	1.28
6	60.7927±0.35790±0.0106	2.2	1.28
7	60.7927±0.35790±0.0128	2.2	1.28
8	60.7927±0.35790±0.0150	2.2	1.28
9	60.7927±0.35790±0.0172	2.2	1.28
10	60.7927±0.35790±0.0194	2.2	1.28
11	60.7927±0.35790±0.0216	2.2	1.28
12	60.7927±0.35790±0.0238	2.2	1.28
13	60.7927±0.35790±0.0260	2.2	1.28
14	62.1057±0.30550	1.8	2.00



15	$62.1057 \pm 0.30550 \pm 0.0019$	2.0	1.34
16	$62.1057 \pm 0.30550 \pm 0.0040$	2.2	1.28
17	$62.1057 \pm 0.30550 \pm 0.0062$	2.2	1.28
18	$62.1057 \pm 0.30550 \pm 0.0084$	2.2	1.28
19	$62.1057 \pm 0.30550 \pm 0.0106$	2.2	1.28
20	$62.1057 \pm 0.30550 \pm 0.0128$	2.2	1.28
21	$62.1057 \pm 0.30550 \pm 0.0150$	2.2	1.28
22	$62.1057 \pm 0.30550 \pm 0.0172$	2.2	1.28
23	$62.1057 \pm 0.30550 \pm 0.0194$	2.2	1.28
24	$62.1057 \pm 0.30550 \pm 0.0216$	2.2	1.28
25	$62.1057 \pm 0.30550 \pm 0.0238$	2.2	1.28
26	$62.1057 \pm 0.30550 \pm 0.0260$	2.2	1.28
27	$63.28325 \pm 0.28525$	1.8	2.00
28	$63.28325 \pm 0.28525 \pm 0.0019$	2.0	1.34
29	$63.28325 \pm 0.28525 \pm 0.0040$	2.2	1.28
30	$63.28325 \pm 0.28525 \pm 0.0062$	2.2	1.28
31	$63.28325 \pm 0.28525 \pm 0.0084$	2.2	1.28
32	$63.28325 \pm 0.28525 \pm 0.0106$	2.2	1.28
33	$63.28325 \pm 0.28525 \pm 0.0128$	2.2	1.28
34	$63.28325 \pm 0.28525 \pm 0.0150$	2.2	1.28
35	$63.28325 \pm 0.28525 \pm 0.0172$	2.2	1.28
36	$63.28325 \pm 0.28525 \pm 0.0194$	2.2	1.28
37	$63.28325 \pm 0.28525 \pm 0.0216$	2.2	1.28
38	$63.28325 \pm 0.28525 \pm 0.0238$	2.2	1.28
39	$63.28325 \pm 0.28525 \pm 0.0260$	2.2	1.28

340 The integration time for the SSMIS channel 19-23 is 25.2 ms, and for channel 24 is 12.6 ms (Swadley et al., 2008). For comparison, the system noise is also set to 800 K when calculating the *NEDT* for SSMIS in this study. From Eq. (12), the SSMIS Channels 19-20 *NEDT* is approximately 3 K, which is highly consistent with the reported (2.7 K) (Kunkee et al., 2008). The number of channels and vertical resolution in this study are significantly higher than those of SSMIS, allowing for an appropriate extension of the integration time.



345 **Figure 8:** HMAS all-channel passband distribution. The orange, pink, bright green, dark blue, and purple lines in the 7<sup>+</sup>, 9<sup>+</sup>, 15<sup>+</sup>, and 17<sup>+</sup> diagrams represent the SSMIS channels 19, 20, 21, 22, and 23 passbands, respectively.

Based on the same principle, high-resolution channels that do not utilize microwave hyperspectral detection technology are also proposed in this study. A double-sideband channel with a bandwidth of 1.8 MHz was set covering the oxygen absorption line. Four quadruple-sideband channels were established at frequencies progressively shifting away from the absorption line center: 1.9 MHz, 4.0 MHz, 6.5 MHz, 9.9 MHz, 15.5 MHz, and 26 MHz, with respective bandwidths of 1.9 MHz, 2.1 MHz, 2.7 MHz, 3.9 MHz, 7.1 MHz, and 13.7 MHz. Table 2 gives the Microwave Atmospheric Sounder (MAS) channel parameters suitable for conventional detection techniques. This is essentially an extension of SSMIS channels 19-23, incorporating the 11<sup>+</sup> and 13<sup>+</sup> lines. However, the most significant difference between MAS and SSMIS is its capability to perform linear or circular polarization detection. The MAS can be manufactured with reference to the structure of ATMS or AMSU to achieve end-to-end calibration.

**Table 2** MAS channel characteristics.

Channel	Center Frequency (GHz)	3-db Width (MHz)	NEDT (K)
1	60.7927±0.35790	1.8	2.00



2	60.7927±0.35790±0.0019	1.9	1.38
3	60.7927±0.35790±0.0040	2.1	1.31
4	60.7927±0.35790±0.0065	2.7	1.16
5	60.7927±0.35790±0.0099	3.9	0.96
6	60.7927±0.35790±0.0155	7.1	0.71
7	60.7927±0.35790±0.0260	13.7	0.51
8	62.1057±0.30550	1.8	2.00
9	62.1057±0.30550±0.0019	1.9	1.38
10	62.1057±0.30550±0.0040	2.1	1.31
11	62.1057±0.30550±0.0065	2.7	1.16
12	62.1057±0.30550±0.0099	3.9	0.96
13	62.1057±0.30550±0.0155	7.1	0.71
14	62.1057±0.30550±0.0260	13.7	0.51
15	63.28325±0.28525	1.8	2.00
16	63.28325±0.28525±0.0019	1.9	1.38
17	63.28325±0.28525±0.0040	2.1	1.31
18	63.28325±0.28525±0.0065	2.7	1.16
19	63.28325±0.28525±0.0099	3.9	0.96
20	63.28325±0.28525±0.0155	7.1	0.71
21	63.28325±0.28525±0.0260	13.7	0.51

### 4.3 Comparison of SSMIS and HMAS

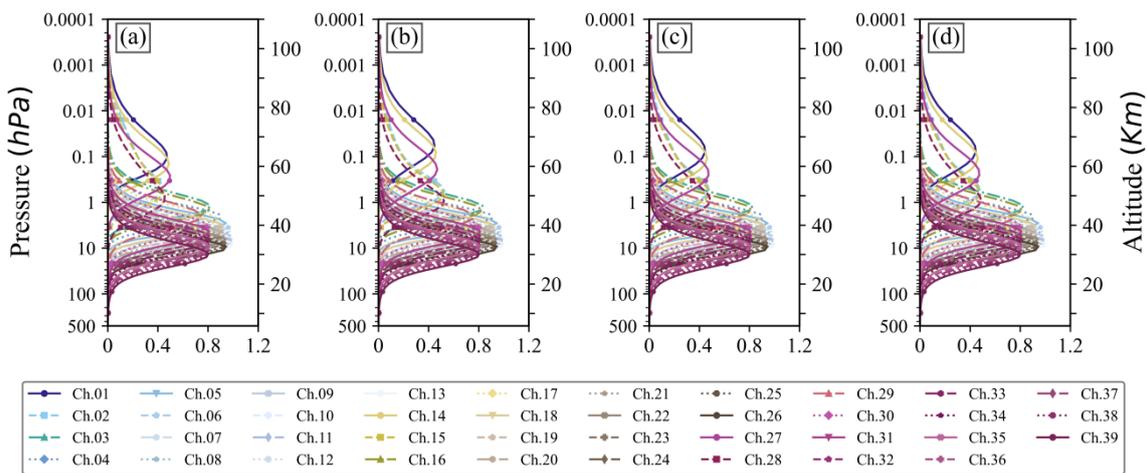
The atmospheric profile dataset used for SSMIS and HMAS simulation was developed by Peter Rayer (Met Office). It consists of 13,495 randomly sampled model profiles from the European Centre for Medium-Range Weather Forecasts (ECMWF), providing high vertical resolution (extending up to 0.0002 hPa). The key characteristics required for upper atmospheric simulations can be met by utilizing the average of this profile dataset. Figure 9 shows the HMAS weighting function distribution for different polarizations. The HMAS channels are grouped into three sets based on oxygen absorption line combinations: Group 1 (blue) comprises channels 1-13 centered around the 7<sup>+</sup> and 9<sup>+</sup> lines, Group 2 (yellow) includes channels 14-26 centered around the 11<sup>+</sup> and 13<sup>+</sup> lines, and Group 3 (pink) consists of channels 27-39 centered around the 15<sup>+</sup> and 17<sup>+</sup> lines. From Fig. 9, it is shown that the three double-sideband channels covering the respective oxygen absorption lines exhibit the highest peak with their respective WFs. Detection height gradually decreases as the passband moves further



370

from the oxygen line center, with every 13 channels exhibiting a similar pattern. Using only channels 1-2, 14-15, and 27-28 enables detection at upper altitudes of approximately 40-80 km, while the remaining channels complete the high-resolution coverage of about 20-55 km.

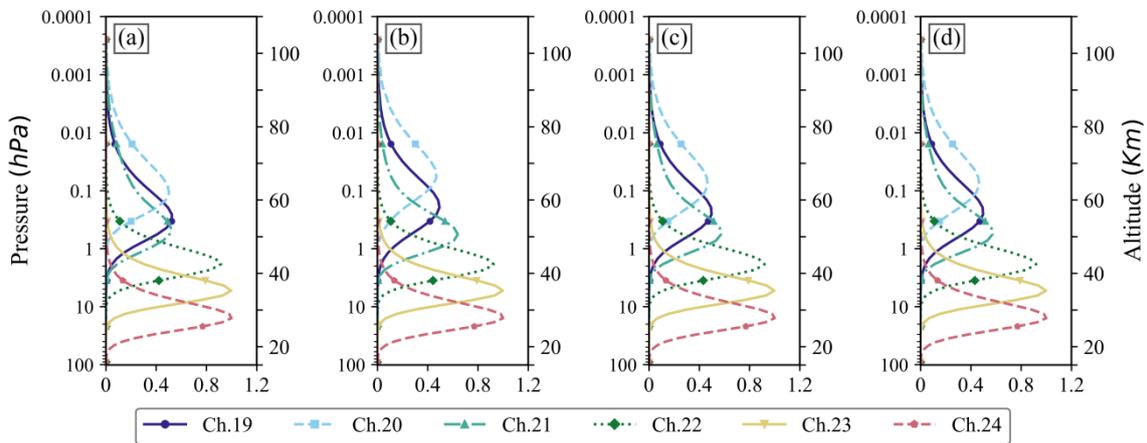
### HMAS Channel Weighting Functions Distribution



375

**Figure 9:** HMAS channel Weighting Functions (WF) for the (a) vertical-, (b) horizontal-, (c) right-, and (d) left-polarization. The first three channels in each group (channels 1-3, 14-16, and 27-29) are highlighted from the same color family.

### SSMIS Channel Weighting Functions Distribution



**Figure 10:** As Fig. 9, but for SSMIS channel 19-24.



## 380 5 Conclusions

In this study, recent developments in the modelling of the Zeeman effect on high-peaking oxygen ( $O_2$ ) absorption lines are incorporated into the microwave Line-by-Line (LBL) model to accurately simulate high-resolution satellite channels sensitive to these effects. The Stokes vector simulation differences for  $1^-$ ,  $13^-$ ,  $7^+$ ,  $9^+$ ,  $15^+$ , and  $17^+$  oxygen absorption lines are compared, and it is shown that the  $7^+$  line has the largest simulation difference for the  $V$  component. Brightness  
385 temperature (BT) is simulated for representative  $7^+$  and  $1^-$  oxygen lines using the Rosenkranz and Staelin's microwave Line-by-Line (RS-LBL) model updated with Larsson (2019) Zeeman splitting coefficients. The sensitivity of simulated BT to magnetic field strength ( $B_e$ ) and angle between the magnetic field vector and the electromagnetic wave propagation direction ( $\theta$ ) indicates that the  $O_2$  line center and frequency shift within 2 MHz are highly sensitive to  $B_e$ , particularly when it exceeds 0.4 Gauss, but above 2 MHz, there is negligible sensitivity. When the medium and magnetic field are uniformly distributed,  
390 and contributions from other absorption lines are neglected. The simulated BT exhibits symmetry with the  $\theta$ , specifically, the linearly polarized BT of oxygen absorption lines is symmetric about  $\theta=90^\circ$  ( $\cos(\theta)=0$ ), while left- and right-based circularly polarized BT are mirrors of each other.

The Special Sensor Microwave Imager Sounder (SSMIS) has six upper atmospheric sounding channels, which can  
395 potentially have a positive impact on assimilation (Hoppel et al., 2013). This study proposes both conventional and hyperspectral linear polarization channels parameters based on the simulation and analysis of oxygen absorption lines, aiming to complement and extend the capability of existing SSMIS observations, particularly as it reaches the end of its life. The channel configurations for both Hyperspectral Microwave Atmospheric Sounder (HMAS) and Microwave Atmospheric Sounder (MAS) are comparable to SSMIS, featuring double-sideband covering the oxygen line and quadruple-sideband  
400 channels on either side of the oxygen absorption line. To reduce channel noise, the bandwidth covering oxygen lines has been appropriately broadened. The study concludes by presenting the SSMIS and HMAS composite channel weighting function (WF) distributions. Overall, both the SSMIS and HMAS WFs achieve coverage from 100 to 0.001 hPa, but HMAS has a higher density, hence supported by hyperspectral detection technology, an instrument like HMAS is expected to obtain super high-resolution vertical atmospheric information from near space.

405 Since this study only focuses on the HMAS 150 channels at 60-63 GHz, with additional channels awaiting investigation. Meanwhile, the HMAS channel configuration is a conservative adaptation of existing techniques. In the future, channel setups can be fully adjusted based on technological capabilities, though all require simulation and analysis of the  $O_2$  fine-structure line. Temperature profile retrieval based on current channel parameters also enables comparison of differences  
410 between HMAS or MAS and SSMIS.



### **Code availability**

The microwave LBL code used in this article can be downloaded at: [https://cetemps.aquila.infn.it/mwrnet/lblmrt\\_ns.html](https://cetemps.aquila.infn.it/mwrnet/lblmrt_ns.html).

### **Author contributions**

415 CD and FW conceptualized and designed the experiments. CD, FW, and ET developed the methodology and performed the formal analysis, software development, data curation, and visualization. CD carried out the investigation and wrote the original draft. FW supervised the work and acquired funding. All co-authors contributed to writing, reviewing, and editing the final manuscript.

### **Competing interests**

The authors declare no conflicts of interest.

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### **Review statement**

430 The review statement will be added by Copernicus Publications listing the handling editor as well as all contributing referees according to their status anonymous or identified.



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