



# Towards a Remote Sensing Solution to Quantify Nitrous Oxide Emissions by Integrating Shortwave and Thermal Infrared Bands

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**Abstract.** Nitrous oxide ( $N_2O$ ) is a potent greenhouse gas whose emissions are dominated by natural and agricultural soils and are highly heterogeneous and episodic, yet existing observational techniques lack the spatial coverage and near-surface sensitivity needed to resolve this variability. In this study, we evaluate a remote sensing framework that integrates shortwave infrared (SWIR) and thermal infrared (TIR) spectral bands to enhance the detectability of column-integrated  $N_2O$  mixing ratio ( $X_{N_2O}$ ).

5 To implement this, we expand the capacity of the SPLAT-VLIDORT radiative transfer model to jointly simulate both spectral regions and apply linear sensitivity analysis to quantify the  $X_{N_2O}$  measurement error and vertical sensitivity under realistic environmental conditions and instrumental designs. This framework is applied to both airborne and spaceborne instruments to evaluate the influence of platform characteristics on retrieval performance. The joint SWIR–TIR setting improves near-surface sensitivity relative to the TIR band alone while maintaining the low  $X_{N_2O}$  measurement error. It achieves single-sounding  
10 measurement error of approximately 3.2 ppb for an airborne instrument with a ground footprint size of 20 m and 1.1 ppb for spaceborne instrument with a footprint size of 0.7 km, while retaining sensitivity to the near-surface layers. Assuming  $X_{N_2O}$  variability is observable at twice the precision, natural  $X_{N_2O}$  variability inferred from in situ aircraft  $N_2O$  observations in the US Midwest becomes observable beyond spatial aggregation scales of  $\sim 2.5$  km for airborne and  $\sim 22$  km for spaceborne instruments, subject to significant  $X_{N_2O}$  variation between flights. An independent, emission-based detectability analysis indicates that  $X_{N_2O}$  variability induced by uniform emissions of  $5 \text{ nmol m}^{-2} \text{ s}^{-1}$  becomes observable beyond spatial averaging  
15 of about 2.1 km for airborne and 8.4 km for spaceborne instruments. Together, these results constitute a quantitative basis for



N<sub>2</sub>O detectability using a joint SWIR–TIR setting, with a focus on diffuse soil emissions that are more difficult to detect yet dominate the global N<sub>2</sub>O budget, and they provide practical guidance for future N<sub>2</sub>O dedicated missions.

## 1 Introduction

20 Nitrous oxide (N<sub>2</sub>O) is the third most important anthropogenic greenhouse gas after carbon dioxide (CO<sub>2</sub>) and methane (CH<sub>4</sub>)  
(Weber et al., 2024; Feng and Li, 2023), currently accounting for approximately 7% of the net anthropogenic radiative forcing  
(3.22 W m<sup>-2</sup>) of the Earth’s climate system (Feng and Li, 2023; IPCC, 2021). It has a global warming potential of roughly 273  
times greater than CO<sub>2</sub> over a 100-year timescale (Weber et al., 2024) and an atmospheric lifetime of 116 ± 9 years (Prather  
et al., 2015), primarily due to its slow removal via photolysis in the stratosphere (Tian et al., 2020). Anthropogenic activities  
25 including fuel combustion, agriculture, and industrial processes have substantially increased the N<sub>2</sub>O emissions (Smith, 2017;  
Jovani-Sancho et al., 2023), with nitrogen-based fertilizers used in agriculture being the major contributor (Thompson et al.,  
2019; Tian et al., 2020). In the global N<sub>2</sub>O budget at about 19 TgN yr<sup>-1</sup>, natural soil emissions dominate the N<sub>2</sub>O sources  
at about 6–7 TgN yr<sup>-1</sup>, followed by agricultural emissions ranging from 4.3 to 5.8 TgN yr<sup>-1</sup> (Syakila and Kroeze, 2011).  
Atmospheric N<sub>2</sub>O concentrations have already exceeded those projected under the most pessimistic scenario of the Shared  
30 Socioeconomic Pathway (SSP5-8.5), suggesting that current emission trajectories surpass both policy expectations and model  
projections (Tian et al., 2024). This is further reinforced by Microwave Limb Sounder (MLS) observations from 2005–2021,  
which reveal a growing stratospheric sink for N<sub>2</sub>O, implying that actual emissions may be higher than those inferred from  
concentration data alone (Prather et al., 2023).

A variety of observational techniques have been used to quantify N<sub>2</sub>O emissions and characterize their spatiotemporal  
35 variability. Chambers are widely employed for agricultural field-scale studies (Zhang et al., 2024; Kong et al., 2025; Zimbron  
et al., 2025), offering high precision at fine temporal resolution, but they are effectively point measurements and are not  
representative of broader heterogeneous landscapes. Ground-based Eddy Covariance (EC) systems provide continuous flux  
measurements over larger footprints (~ 1 km<sup>2</sup> scale), capturing ecosystem-scale dynamics, but their fixed-point nature limits  
spatial coverage (Murphy et al., 2022; Pan et al., 2022; Rana et al., 2025; Tikkasalo et al., 2025). Airborne EC campaigns  
40 overcome this limitation by measuring fluxes over tens to hundreds of kilometers and have been particularly effective in  
agricultural regions, although their deployment remains logistically complex and resource-intensive (Wilkerson et al., 2019;  
Waldmann et al., 2025). Similarly, airborne or tall tower-based in situ measurements combined with atmospheric transport  
and inversion models provide valuable top-down estimates of regional emissions, offering a complement to inventory-based  
approaches (Kort et al., 2017; Dacic et al., 2024; Gvakharia et al., 2020; Xiang et al., 2013; Griffis et al., 2019; Haszpra et al.,  
45 2018; Kort et al., 2011; Chen et al., 2016b). Despite these advances, accurately capturing soil N<sub>2</sub>O emissions, complicated by  
their episodic and spatially heterogeneous nature (Molodovskaya et al., 2012; Ackett et al., 2025; Zhang et al., 2024; Zhou  
et al., 2022; Shrestha and Wang, 2018), remains a major challenge, underscoring the need for scalable observational strategies  
with improved spatial resolution.



Remote sensing of greenhouse gases on spaceborne or airborne platforms offers a powerful alternative to overcome these  
50 spatiotemporal limitations, by providing coverage up to the global scale and allowing the detection of long-term trends and  
multiscale emission patterns (Jacob et al., 2016). Remote sensing instruments typically observe the dry air column-integrated  
mixing ratio of greenhouse gases, conventionally denoted as “ $X$ ” followed by the molecule name, e.g.,  $X_{N_2O}$  for  $N_2O$ . These  
column amounts are insensitive to the vertical distributions of trace species and thus more closely related to emissions than  
point-based volume mixing ratios (Chen et al., 2016a). Over the recent decade, missions such as the Orbiting Carbon Observa-  
55 tories (OCO-2 & OCO-3) (Crisp, 2015; Crisp et al., 2017; Eldering et al., 2019; Taylor et al., 2023), TROPOspheric Monitoring  
Instrument (TROPOMI) (Lorente et al., 2021), Greenhouse Gases Observing Satellite (GOSAT) series (Butz et al., 2011; Suto  
et al., 2021), and MethaneSAT (South, 2024) deliver high-precision  $CO_2$  and  $CH_4$  retrievals and have demonstrated the ability  
to detect and quantify emissions from global to sub-kilometer scales. Airborne platforms provide complementary capabilities  
by targeting high-resolution observations at finer spatial scales. For example, MethaneAIR, an airborne precursor to Methane-  
60 SAT, provides a fine spatial resolution of  $20 \times 20 \text{ m}^2$  with overall  $X_{CH_4}$  retrieval accuracy within  $\sim 1\%$  when validated against  
ground-based spectrometers (Chan Miller et al., 2024; Chulakadabba et al., 2023).

In contrast, there exists no dedicated remote sensing mission for  $N_2O$  (Ricaud et al., 2021). In the shortwave infrared (SWIR)  
spectral region, where  $CO_2$  and  $CH_4$  instruments have achieved remarkable success, the most detectable  $N_2O$  band near  $2.3 \mu\text{m}$   
is weak and subject to significant interference from  $CH_4$  bands. Stronger  $N_2O$  features are found in the thermal infrared (TIR)  
65 near  $4.4$  or  $7.8 \mu\text{m}$ , but TIR observations have limited sensitivity to near-surface layers, which matter the most for emission  
detection. In addition, the relative emission-induced enhancements to the  $N_2O$  column are generally lower than those of  $CH_4$   
and  $CO_2$ , and in this regard,  $N_2O$  has been proposed as a light-path proxy for  $CH_4$  and  $CO_2$  retrievals (Frankenberg et al.,  
2025). For example, the peak-to-peak variability of  $N_2O$  volume mixing ratio observed in the planetary boundary layer (PBL)  
over a source region is only a few ppb (Dacic et al., 2024), which translates to an  $X_{N_2O}$  variability of about 1 ppb, or 0.3% of  
70 the  $X_{N_2O}$  background. This makes  $N_2O$  sources more difficult to detect than  $CO_2$  or  $CH_4$  even given comparable instrument  
sensitivity. As secondary products,  $N_2O$  abundance has been retrieved from existing satellite-observed spectra in both SWIR  
and TIR bands. The SCanning Imaging Absorption SpectroMeter for Atmospheric CHartography (SCIAMACHY) offered  
one of the first  $N_2O$  detection capabilities in SWIR region. With a target precision of approximately 10% in the retrieved  
 $N_2O$  column amount, the SCIAMACHY  $N_2O$  product is insufficient for detecting localized enhancements (Dils et al., 2006).  
75 Infrared sounders primarily designed for numerical weather prediction, such as the Atmospheric Infrared Sounder (AIRS) and  
the Infrared Atmospheric Sounding Interferometer (IASI), have improved upon SCIAMACHY with typical  $N_2O$  precision  
close to 1% (Xiong et al., 2014; Vandenbussche et al., 2022). However, their coarse spatial resolution and limited near-surface  
sensitivity make them poorly suited for detecting localized  $N_2O$  emission sources. For the first time, the GOSAT-2 satellite  
covers both SWIR and TIR  $N_2O$  bands with the same instrument, but its coarse footprint diameter of  $\sim 10 \text{ km}$  and sparse  
80 sampling geometry limit its ability to resolve localized and spatially heterogeneous  $N_2O$  enhancements (Suto et al., 2021).  
Using only the SWIR  $N_2O$  band of GOSAT-2, Noël et al. (2022) provided the first  $X_{N_2O}$  product from GOSAT-2 with single-  
sounding precisions of about 4–9 ppb. Still, current spaceborne  $N_2O$  instrumentation cannot be used to study agricultural  
emissions, which triggers attempts to use other high-resolution nitrogen species as a proxy (Adams et al., 2025).



Leveraging the heritages of existing greenhouse gas instruments, especially MethaneAIR and MethaneSAT, this study presents a dual SWIR–TIR band concept applicable for both airborne and spaceborne N<sub>2</sub>O remote sensing instruments. Similar to MethaneAIR and MethaneSAT, this concept employs high spatial resolution (footprint sizes of about 20 m for airborne and 0.7 km for spaceborne instruments), wide swath imaging grating spectrometer designs for the ability to detect both emission hot spots (Warren et al., 2025) and dispersed sources (MacKay et al., 2026). The coverage of the SWIR N<sub>2</sub>O band at 2.3 μm offers near-uniform vertical sensitivity desirable for emission quantification. The stronger TIR N<sub>2</sub>O band at 7.8 μm provides crucial observational constraints to  $X_{N_2O}$ , additional to the weak SWIR band. For the first time, we enhance the Smithsonian Planetary Atmosphere–Vector Linearized Discrete Ordinate Radiative Transfer (SPLAT–VLIDORT), the radiative transfer model underpinning the MethaneAIR and MethaneSAT retrieval algorithms (Chan Miller et al., 2024), to enable a joint SWIR–TIR retrieval. Linear sensitivity analysis based on this enhanced radiative transfer framework demonstrates that the integration of SWIR and TIR bands yields significantly improved N<sub>2</sub>O precision and PBL sensitivity relative to the limiting single-band case, an advantage similarly seen in the multispectral CO retrieval in the Measurements of Pollution in the Troposphere (MOPITT) instrument (Worden et al., 2010).

To assess the N<sub>2</sub>O detectability by the proposed instruments under realistic conditions, we approximate real-world  $X_{N_2O}$  variability in two complementary ways. The first is to assume  $X_{N_2O}$  covaries with PBL N<sub>2</sub>O mixing ratio, which was extensively sampled by an aircraft during the Measurement of Agriculture Illuminating farm-Zone Emissions of N<sub>2</sub>O (MAIZE) campaign over the US Midwest. The second is to transform a range of hypothetical N<sub>2</sub>O emissions that are informed by autochamber flux data to  $X_{N_2O}$  enhancements at various spatial scales. These  $X_{N_2O}$  variabilities are then compared with  $X_{N_2O}$  measurement error at common spatial scales to infer detectability. Together, these results establish the scientific basis for N<sub>2</sub>O remote sensing missions dedicated to detect and quantify agricultural soil N<sub>2</sub>O emissions at spatial scales relevant to emissions monitoring and management, providing practical guidance for instrument design aimed at closing existing gaps in N<sub>2</sub>O monitoring. By treating agricultural N<sub>2</sub>O emissions as the primary design case, the proposed instrument capable of resolving the most challenging sources will also be well suited for other stronger emission sectors such as industrial.

## 2 Data

This section presents the three observational datasets used in this study. First, satellite-retrieved atmospheric state data from the Cross-track Infrared Sounder (CrIS) provide profiles of temperature and key absorbers (N<sub>2</sub>O, CH<sub>4</sub>, and H<sub>2</sub>O) in the SWIR and TIR bands, which define the atmospheric and surface conditions for forward radiative transfer modeling (Section 3.1.4) and allow estimation of prior error structures (Section 3.1.2). In combination with the instrument noise characteristics (Section 3.1.3), these lead to the  $X_{N_2O}$  measurement error estimation for the proposed instruments. Second, airborne in-situ measurements from the MAIZE campaign (Section 2.2) capture high-resolution N<sub>2</sub>O variability within the PBL over a major agricultural region, shedding light on the  $X_{N_2O}$  spatial heterogeneity using semivariograms (Section 3.2). Third, hourly N<sub>2</sub>O flux measurements by autochambers distributed in a commercial farm in Illinois (Section 2.3) provide realistic spatiotemporal variability of soil N<sub>2</sub>O emissions, putting the detectability of N<sub>2</sub>O emissions into a real-world context (Section 3.3).

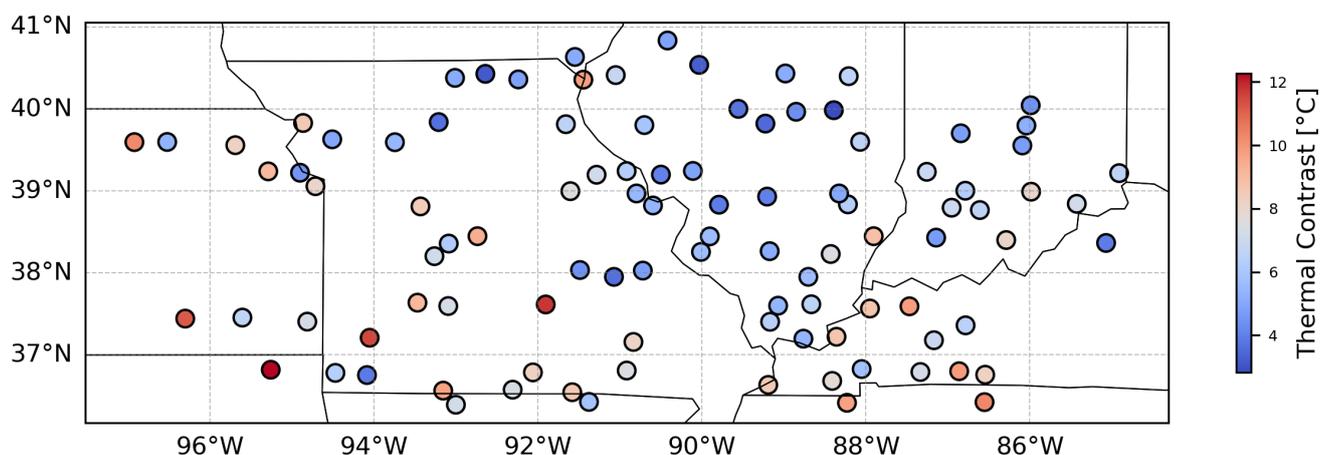


## 2.1 Realistic geophysical quantities from CrIS Level 2 product

Level 2 data from the CrIS instrument onboard NOAA’s JPSS satellites are used to construct realistic profiles of trace gases ( $N_2O$ ,  $CH_4$ ,  $H_2O$ ) and temperature as well as surface temperature and emissivity useful for the TIR radiative transfer modeling.

120 This study leverages 100 CrIS soundings over the US Midwest acquired on 23 August 2023. Figure 1 shows the spatial distribution of the selected CrIS pixels, color-coded by thermal contrast, which is defined as the difference between retrieved surface temperature and that of the lowest atmospheric layer. These soundings span a wide range of thermal contrast (2–12 K), providing a representative sample of summer conditions for evaluating retrieval sensitivity. Thermal contrast is most important for the TIR band, as it governs the strength of the upwelling signal and thus influences vertical sensitivity. The prior error

125 matrices for  $H_2O$  and temperature profiles available in the CrIS Level 2 data are used to set a priori constraints in the linear sensitivity study (see Section 3.1.2).



**Figure 1.** Spatial distribution of 100 CrIS soundings over the US Midwest on 23 August 2023, color-coded by thermal contrast. These pixels span a wide range of thermal contrast from 2–12 K.

## 2.2 MAIZE aircraft campaign in situ measurements

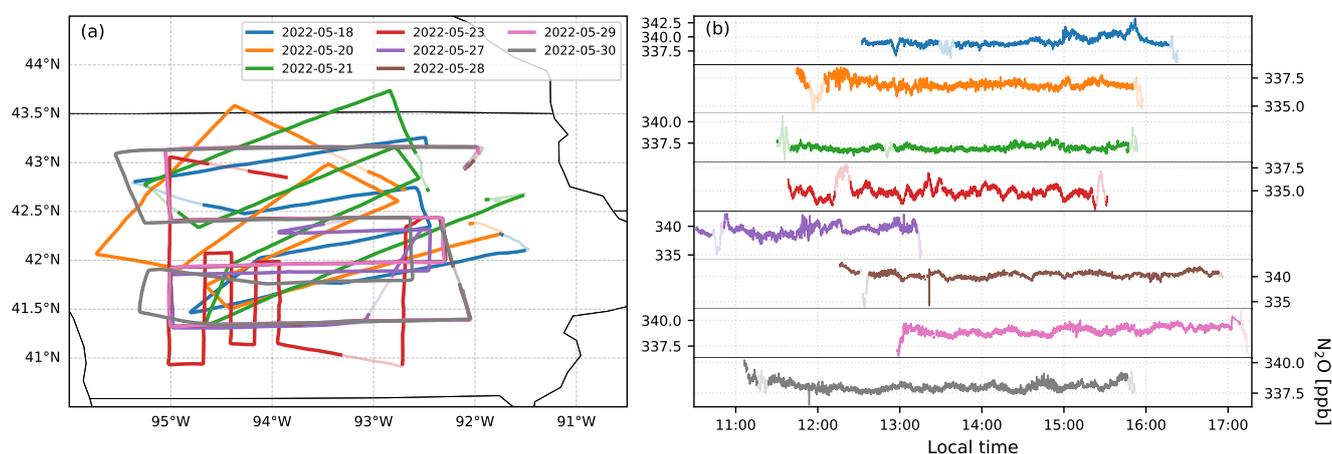
Airborne in-situ measurements of  $N_2O$  were conducted over the state of Iowa, located within the corn belt of United States (41° to 43.5°N and 92° to 95°W), in 2022 as part of the MAIZE campaign. A total of eight research flights took place between

130 18 and 30 May 2022 using a Mooney aircraft operated by Scientific Aviation, Inc. Flights were conducted during growing season under fair weather conditions, avoiding active precipitation, low visibility events, and on days with steady winds. This period, characterized by recent fertilizer application and warm and moist conditions was conducive to elevated  $N_2O$  emissions from cropland soils. Each flight lasted around 5–6 hours and was conducted between 11:00 and 18:00 local time to ensure sampling within a well-developed PBL. The aircraft flew at an average altitude of  $\sim 475$  m above ground level (AGL), with

135 transects oriented perpendicular to the prevailing wind direction to enhance sensitivity to surface fluxes. Two vertical profiles



were captured during each flight to characterize the PBL structure. The primary target species,  $N_2O$ , was measured using a Los Gatos Research (LGR)  $N_2O/CO$  Analyzer (model 916-0015), which also recorded  $H_2O$  and  $CO$ . In addition,  $CH_4$  and  $CO_2$  were measured using a Picarro G2401-m analyzer (Dacic et al., 2024). The  $N_2O$  in situ measurements are used to approximate column-integrated mixing ratio of  $N_2O$  and analyze its spatial variability. Figure 2a shows the area coverage for each flight and Fig. 2b indicates the corresponding in situ  $N_2O$  mixing ratios measured during each flight. The faint lines indicate vertical profile segments and bold lines mark the horizontal PBL transects used to quantify  $X_{N_2O}$  variability for the semivariogram-based detectability analysis.



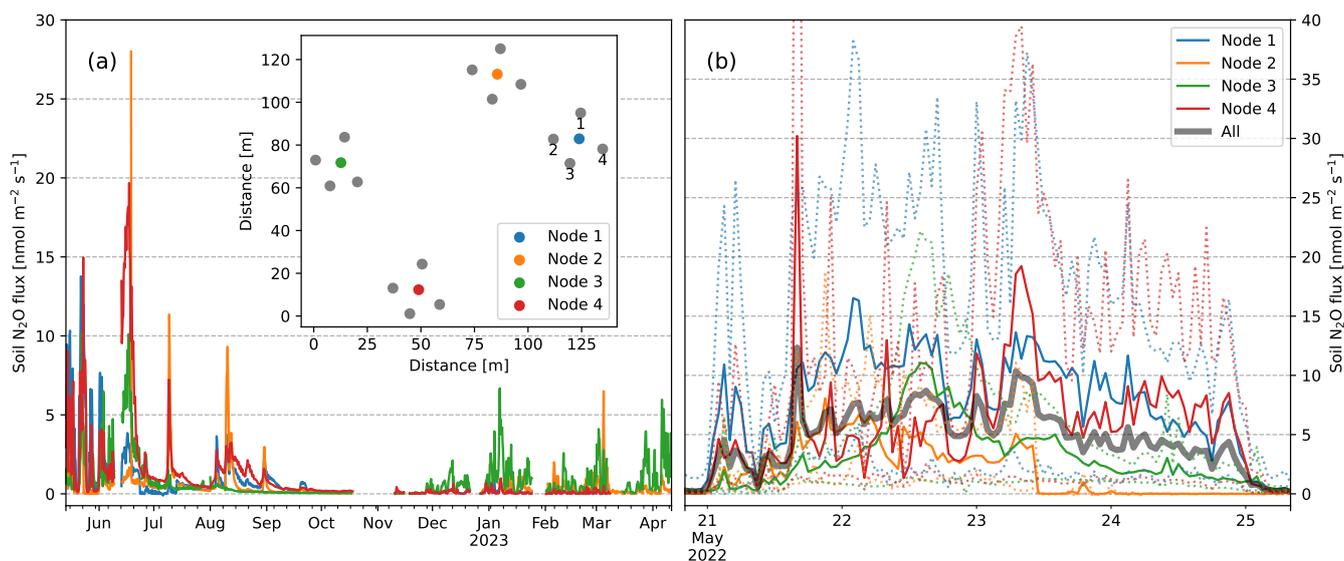
**Figure 2.** (a) Flight tracks during the MAIZE campaign over the state of Iowa in May 2022. (b) Corresponding time series of in situ  $N_2O$  mixing ratios. Faint lines represent vertical profile segments, while bold lines highlight horizontal flight path within the PBL used to calculate  $X_{N_2O}$  variability for detectability analysis. Colors distinguish individual flight days and are consistent between panels.

### 2.3 Autochamber flux data

Hourly  $N_2O$  fluxes were measured from May 2022 to April 2023 in a conventionally-tilled maize field near Villa Grove, Illinois, using 16 automated chambers. To capture spatial and temporal variability of emissions, the chambers were distributed across four sampling nodes within  $\sim 5$  ha area, with nodes spaced 50–100 m apart (Fig. 3a inset). Each node contained four chambers radially positioned 12 m from a central  $N_2O$  gas analyzer (LI-7820, LI-COR Biosciences), which sequentially sampled the fluxes using an automated multiplexer (LI-8250). Chamber collars (20 cm diameter) were permanently installed adjacent to crop rows, ensuring that no vegetation was present within the chamber footprint and that chambers remained fully open between measurements in order to avoid shading or disturbance. Figure 3a shows the spatiotemporal variation of measured  $N_2O$  flux across four nodes, where chambers in the same node are averaged and then aggregated to 6-hour intervals to enhance visualization. Data are missing for approximately three weeks in October–November 2022 due to instrument maintenance and crop harvest (Stuchiner et al., 2025). Figure 3b zooms in over a high emission event of 21–25 May 2022 to highlight the hourly



155 variability of N<sub>2</sub>O emissions. The node-wise average time series are shown as solid lines, while the maximum and minimum chamber values within each node are shown as dashed lines. The thick grey line represents the overall hourly flux averaged over all nodes which remain mostly above 5 nmol m<sup>-2</sup> s<sup>-1</sup> and occasionally exceed 10 nmol m<sup>-2</sup> s<sup>-1</sup> in this period.



**Figure 3.** Time series of soil N<sub>2</sub>O flux (nmol m<sup>-2</sup> s<sup>-1</sup>) measured from May 2022 to April 2023 using automated chambers deployed at four nodes in a conventionally tilled maize field near Villa Grove, Illinois. (a) Node-averaged fluxes at 6-hourly resolution showing the temporal and spatial variability, with distinct emission pulses during the early growing season. The inset shows the spatial arrangement of nodes and chambers within an area of ~5 ha. (b) Expanded view of 21–25 May 2022, highlighting the hourly flux variability. Solid lines represent node-averaged fluxes, dashed lines denote the minimum and maximum chamber values within each node, and the thick grey line represents the average across all nodes.

### 3 Measurement Methodology

This section combines theoretical analysis and empirical data to evaluate the capability of potential dual-band remote sensing instruments for detecting N<sub>2</sub>O emissions on both airborne and spaceborne platforms. Section 3.1 introduces the linear sensitivity analysis framework, which takes a Bayesian approach to quantify  $X_{N_2O}$  measurement error and vertical sensitivity based on instrument design parameters, a priori constraints, and radiative transfer simulations. Section 3.2 leverages in situ airborne N<sub>2</sub>O measurements from the MAIZE campaign to approximate spatial variability of  $X_{N_2O}$  and characterize how this variability compares with measurement error at different spatial scales. Finally, Section 3.3 compares emission-driven column enhancement against measurement error. Both Sections 3.2 and 3.3 aim to provide a quantitative basis for the detectability of N<sub>2</sub>O emissions by the proposed instruments.



### 3.1 Linear sensitivity analysis

#### 3.1.1 Theory

As articulated in Rodgers (2000), the linear sensitivity analysis framework assumes that the perturbations to a vector of observations  $\mathbf{y}$  are linear relative to the perturbations of a state vector  $\mathbf{x}$ . In other words, the Jacobian

$$170 \quad \mathbf{K} = \frac{\partial \mathbf{y}}{\partial \mathbf{x}} \quad (1)$$

is approximately constant within the error range of  $\mathbf{x}$ . Here,  $\mathbf{y}$  is the expected values of a spectrum observed by a remote sensing instrument with Gaussian error covariance matrix  $\mathbf{S}_o$ , and the state vector consists of the volume mixing ratio profiles of  $\text{N}_2\text{O}$ ,  $\text{CH}_4$ , and  $\text{H}_2\text{O}$ , atmospheric temperature profile, and the surface temperature. We assume a priori knowledge of  $\mathbf{x}$  as a Gaussian distribution with mean value  $\mathbf{x}_a$  and a covariance matrix of  $\mathbf{S}_a$ . Within the Bayesian framework,  $\mathbf{S}_a$  represents the prior uncertainty of the state vector. Practically, it also acts as a regularization whose strength can be controlled by multiplying  $\mathbf{S}_a$  by a scaling factor, as implemented in Section 4.1. The a priori profiles are adopted from CrIS Level 2 products as mentioned in section 2.1. The prior error matrices are constructed in a similar manner to those deployed in the MethaneAIR/GOSAT algorithms for  $\text{N}_2\text{O}$  and  $\text{CH}_4$  profiles and extracted from CrIS Level 2 product for  $\text{H}_2\text{O}$  and atmospheric temperature profiles (see section 3.1.2). The observation error  $\mathbf{S}_o$  is constructed based on the instrument specification given in section 3.1.3. The Jacobian  $\mathbf{K}$  is calculated using the radiative transfer model detailed in section 3.1.4.

Applying the Bayes' theorem, the state vector can be retrieved from the observation and the prior:

$$\hat{\mathbf{x}} = \mathbf{x}_a + \mathbf{G}(\mathbf{y} - \mathbf{K}\mathbf{x}_a), \quad (2)$$

where

$$\begin{aligned} \mathbf{G} &= \frac{\partial \hat{\mathbf{x}}}{\partial \mathbf{y}} \\ &= \mathbf{S}_a \mathbf{K}^T (\mathbf{K} \mathbf{S}_a \mathbf{K}^T + \mathbf{S}_o)^{-1} \end{aligned} \quad (3)$$

185 is the gain matrix. Here, T denotes matrix transpose. The measurement error is linearly propagated from the observation to the retrieved state vector:

$$\mathbf{S}_m = \mathbf{G} \mathbf{S}_o \mathbf{G}^T. \quad (4)$$

Our goal is to retrieve  $X_{\text{N}_2\text{O}}$ , which can be written as a function of the retrieved state vector:

$$X_{\text{N}_2\text{O}} = \mathbf{h}^T \hat{\mathbf{x}}. \quad (5)$$

190 Currently, we assume  $X_{\text{N}_2\text{O}}$  only depends on the retrieved  $\text{N}_2\text{O}$  mixing ratio profile, so the weighting vector  $\mathbf{h}$  is the fractional dry air column at the corresponding layer of the  $\text{N}_2\text{O}$  profile and zero otherwise. The measurement error of  $X_{\text{N}_2\text{O}}$  is then linearly propagated from the state vector measurement error:

$$\sigma_{X_{\text{N}_2\text{O}}} = \mathbf{h}^T \mathbf{S}_m \mathbf{h}. \quad (6)$$



195 This measurement error, or precision of  $X_{N_2O}$ , is a fundamental design parameter for any  $N_2O$  instrument as it limits the observable variability of  $X_{N_2O}$  by instrument noise. However,  $\sigma_{X_{N_2O}}$  does not inform the different detectability at different part of the atmosphere. When the a priori is dominant, the retrieval precision mostly reflects the a priori uncertainty. As such, we will leverage the averaging kernel matrix, which represents the sensitivity of the retrieved state to the true atmosphere state and is given by

$$\begin{aligned} \mathbf{A} &= \frac{\partial \hat{\mathbf{x}}}{\partial \mathbf{x}} \\ &= \mathbf{G}\mathbf{K}. \end{aligned} \quad (7)$$

200  $X_{N_2O}$  as a derived quantity from the retrieved state can then be evaluated using the column averaging kernel vector  $\mathbf{a}$ . The element of the column averaging kernel for the  $l$ th  $N_2O$  layer is

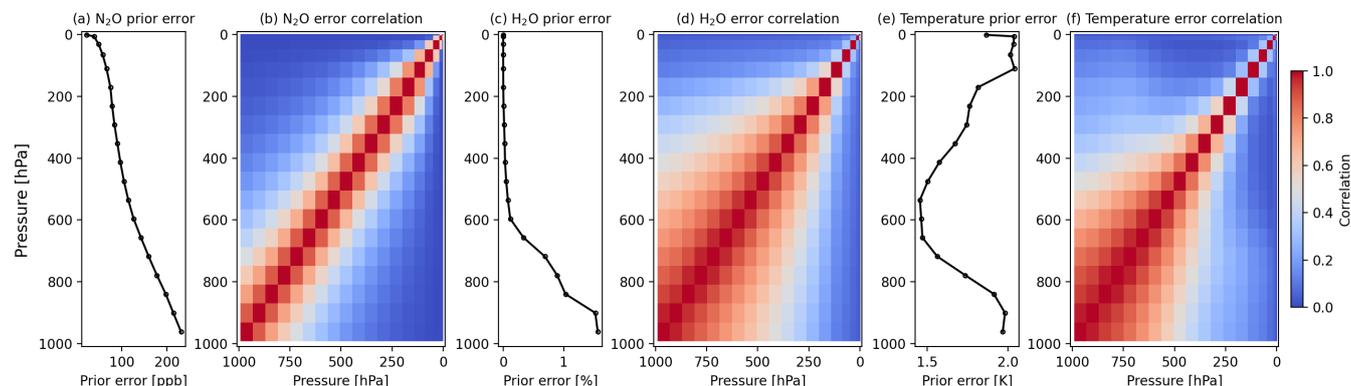
$$\mathbf{a}_l = \frac{1}{\mathbf{h}_l} (\mathbf{h}^T \mathbf{A})_l, \quad (8)$$

205 in which the subscript  $l$  only indexes the elements related to the  $N_2O$  profile. For a particular layer, a column averaging kernel value equaling 1 represents the ideal case, where the retrieved  $X_{N_2O}$  responds to changes in  $N_2O$  mixing ratio profile exactly as the true value of  $X_{N_2O}$ . A column averaging kernel value smaller than 1 indicates that the retrieved  $X_{N_2O}$  is less sensitive to  $N_2O$  in that layer, and that the a priori  $N_2O$  profile element is a significant contributor. We use the mean column averaging kernel values of the bottom two layers (roughly the bottom 1 km) as the indicator of the retrieved  $X_{N_2O}$ 's sensitivity to near-surface  $N_2O$ . A desirable instrument design should have a low  $X_{N_2O}$  measurement error and a near-surface column averaging kernel value close to 1.

### 210 3.1.2 A priori constraint

The prior error covariance matrix  $\mathbf{S}_a$  is a crucial element in the regularization of the retrieval, as it balances the contributions from the observation and the prior. To capture realistic variability, we adopt the MethaneAIR  $CH_4$  a priori error matrix (Chan Miller et al., 2024), which originates from the GOSAT  $CH_4$  algorithm developed by University of Leicester (Parker et al., 2020), for both  $N_2O$  and  $CH_4$  profiles. Similar to Chan Miller et al. (2024), we decompose the error covariance matrix 215 into a standard deviation profile and an error correlation matrix. The  $N_2O$  standard deviation profile, shown in Fig. 4a, is scaled down from the original  $CH_4$  standard deviation profile by a factor of 5.76, reflecting the lower atmospheric abundance of  $N_2O$ . The error correlation matrix is the same for  $N_2O$  and  $CH_4$  and is shown in Fig. 4b. This choice is justified by the fact that both  $N_2O$  and  $CH_4$  are long-lived, well-mixed gases with similar vertical distribution patterns in the troposphere and stratosphere.

220 For  $H_2O$  and temperature, the prior error covariance matrices are adopted from the CrIS Level 2 product (Section 2.1) and similarly decomposed into standard deviation profiles and error correlation matrices in Fig. 4c-f. The CrIS Level 2 algorithm operates in logarithmic space for trace gases, so the  $H_2O$  profile standard deviation is converted from relative error to absolute error, in mixing ratio unit, using the CrIS posterior  $H_2O$  profile. In addition to atmospheric profiles, the surface temperature is included in the state vector, along with a loose 10% prior error.



**Figure 4.** Prior error covariance matrices, decomposed to standard deviation profiles and error correlation matrices, for atmospheric profiles in the state vector. Panels a, c, and e show the error standard deviation profiles for N<sub>2</sub>O, H<sub>2</sub>O, and temperature, respectively. Panels b, d, and f present the corresponding error correlation matrices. The N<sub>2</sub>O prior error is constructed by scaling down the CH<sub>4</sub> standard deviation from the MethanAIR and GOSAT algorithms while keeping the same correlation matrix. H<sub>2</sub>O and temperature priors are adopted from the CrIS Level 2 product.

### 3.1.3 Instrument design parameters and observational constraints

225 For potential airborne and spaceborne N<sub>2</sub>O-observing instruments, we assume push-broom, imaging grating spectrometer designs similar to those in MethaneAIR and MethaneSAT (Staebell et al., 2021; Chan Miller et al., 2024). The instrument specifications are chosen from currently available technologies and detailed in Table 1. The instruments possess two separate spectrometers for the SWIR and TIR N<sub>2</sub>O bands. Due to limited space in the target aircraft, we choose smaller focal plane arrays (FPA) for the airborne instrument, which contain 1280 × 1024 pixels for the SWIR spectrometer and 640 × 512 pixels  
 230 for the TIR spectrometer. The FPA dimension for the spaceborne instrument is 2048 × 2048 pixels for both bands. The along-track ground pixel size  $dy$  is determined by the ground speed of the platform  $v$  and the exposure time  $dt$  as  $dy = v dt$ . The swath width for the airborne instrument is about 2.5 km at a representative aircraft altitude of 9.25 km, and for the spaceborne instrument, about 320 km at an orbit height of 600 km. The native across-track ground pixel size, or ground sampling distance (GSD, denoted as  $dx_0$ ), reflects how the swath is sampled by the spatial dimension of the FPA, which at maximum contains  
 235 1024 SWIR and 512 TIR pixels for the airborne instrument and 2048 pixels for the spaceborne instrument. To collocate the footprints of two bands and make them square-like, the native across-track pixels are binned by a factor  $B$ , such that the final across-track ground pixel size  $dx$  is

$$dx = B dx_0. \quad (9)$$

The combination of SWIR and TIR spectra associated with a common ground footprint with dimension  $dx \times dy$  is referred to  
 240 as a “sounding” of N<sub>2</sub>O. For further analysis of the detectability of  $X_{N_2O}$  variability, it is helpful to define a footprint size  $d_0$



for an N<sub>2</sub>O sounding as the edge size of a square having the same area of the ground footprint:

$$d_0 = \sqrt{dx dy}. \quad (10)$$

**Table 1.** Instrument design parameters for airborne and spaceborne instruments.

Parameter	Symbol [unit]	Airborne	Airborne	Spaceborne	Spaceborne
		SWIR	TIR	SWIR	TIR
Observation altitude	$h_t$ [km]		9.25		600
Swath width	[km]		2.5		320
Exposure time	$dt$ [s]		0.1		0.1
Ground speed	$v$ [m s <sup>-1</sup> ]		200		7010
Along-track size	$dy = v dt$ [m]		20		701
Across-track size	$dx = B dx_0$ [m]		20		640
Footprint size	$d_0 = \sqrt{dx dy}$ [m]		20		670
Wavelength range	[nm]	2240–2300	7820–8000	2240–2300	7600–8000
Spectral sampling	$d\lambda$ [nm]	0.0575	0.3	0.0575	0.25
Slit width <sup>a</sup>	$n_{sample} [\times d\lambda]$	3	3	3	3
Detector pixel size	$dp$ [ $\mu$ m]	12	15	18	18
f-number	$f$	2	2	2	2
System efficiency	$\eta$	0.46	0.35	0.5	0.5
Readout noise	$N_r$ [electrons]	210	200	60	60
Dark current	$D$ [electrons s <sup>-1</sup> ]	$1.8 \times 10^5$	$7 \times 10^6$	100	100
GSD	$dx_0$ [m]	2.5	5	160	160
Across-track binning	$B$	8	4	4	4

<sup>a</sup> Gaussian slit function (i.e., instrument spectral response function, ISRF) is assumed.

The observation error covariance matrix ( $\mathbf{S}_o$ ) is assumed to be diagonal; in other words, the noise of individual detector pixels follows independent Gaussian distributions. The standard deviation of observation error is calculated by multiplying each single-channel radiance  $r$  with a signal-to-noise ratio (SNR):

$$SNR = \frac{S}{N}, \quad (11)$$

where the signal  $S$  and noise  $N$  are measured by number of electrons. The signal is computed as

$$S = \frac{\pi}{4} \cdot r \cdot \frac{dp^2}{f^2} \cdot n_{sample} \cdot d\lambda \cdot dt \cdot \eta, \quad (12)$$

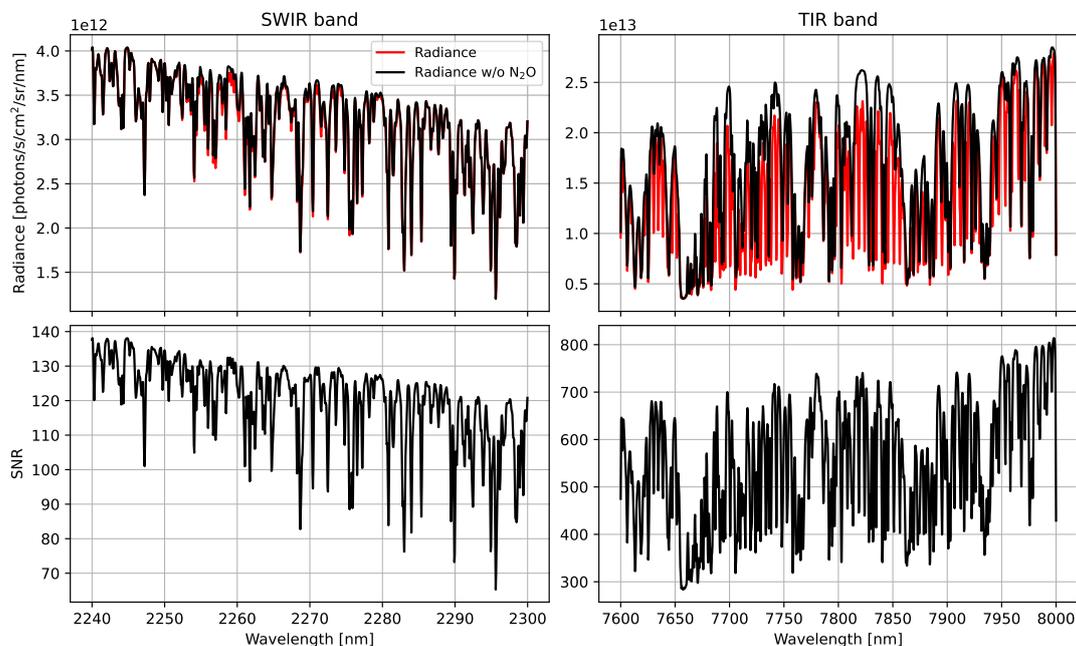
where  $r$  is the observed radiance at a specific wavelength (photons · s<sup>-1</sup> · cm<sup>-2</sup> · nm<sup>-1</sup> · sr<sup>-1</sup>),  $dp$  is detector pixel size,  $f$  is f-number,  $n_{sample}$  is slit width measured as the ratio between the full width at half maximum of the instrument spectral response



function (ISRF) and the spectral sampling interval,  $d\lambda$ ,  $dt$  is exposure time, and  $\eta$  is system efficiency. All parameters except the radiance are listed in Table 1. The total noise per exposure is computed as the quadrature sum of readout noise ( $N_r$ ) and shot noise, the latter having contributions from both the signal and the cumulative dark current ( $D$ ) over the exposure time. Considering the across-track binning factor  $B$ , the noise for each sounding is

$$255 \quad N = \sqrt{\frac{S + Ddt + N_r^2}{B}}. \quad (13)$$

Figure 5 (top row) shows the simulated radiance spectra of a typical sounding at the spectral ranges and resolutions of the spaceborne instrument, with and without  $N_2O$ , by the radiative transfer model detailed in section 3.1.4. In the SWIR band, differences with and without  $N_2O$  are small, owing to weak absorption lines, whereas the TIR  $N_2O$  features are much more prominent. The other spectral lines are mostly due to  $CH_4$  and  $H_2O$  absorption with minor contributions from solar Fraunhofer lines for the SWIR. Figure 5 (bottom row) shows the corresponding SNR estimates calculated using Eq. 11 for the spaceborne instrument. The SNR for the SWIR band is significantly lower than that for the TIR due to lower radiance levels and finer spectral sampling. The SNR for the airborne instrument (not shown) appears similar but is slightly lower due to higher readout noise.



**Figure 5.** Top row shows simulated radiance spectra at the spectral ranges and resolutions of the spaceborne instrument, and bottom row shows corresponding signal-to-noise ratio (SNR). The left column shows the SWIR band (2240–2300 nm), and the right column shows the TIR band (7600–8000 nm). In the top panels, the black curves represent simulated radiance with  $N_2O$  abundance set to zero, highlighting the absorption features attributable to  $N_2O$ . Radiance is expressed in units of  $\text{photons s}^{-1} \text{cm}^{-2} \text{nm}^{-1} \text{sr}^{-1}$ . SWIR band shows weaker  $N_2O$  line strengths while the TIR band exhibits stronger absorption features and higher SNR due to strong signals.



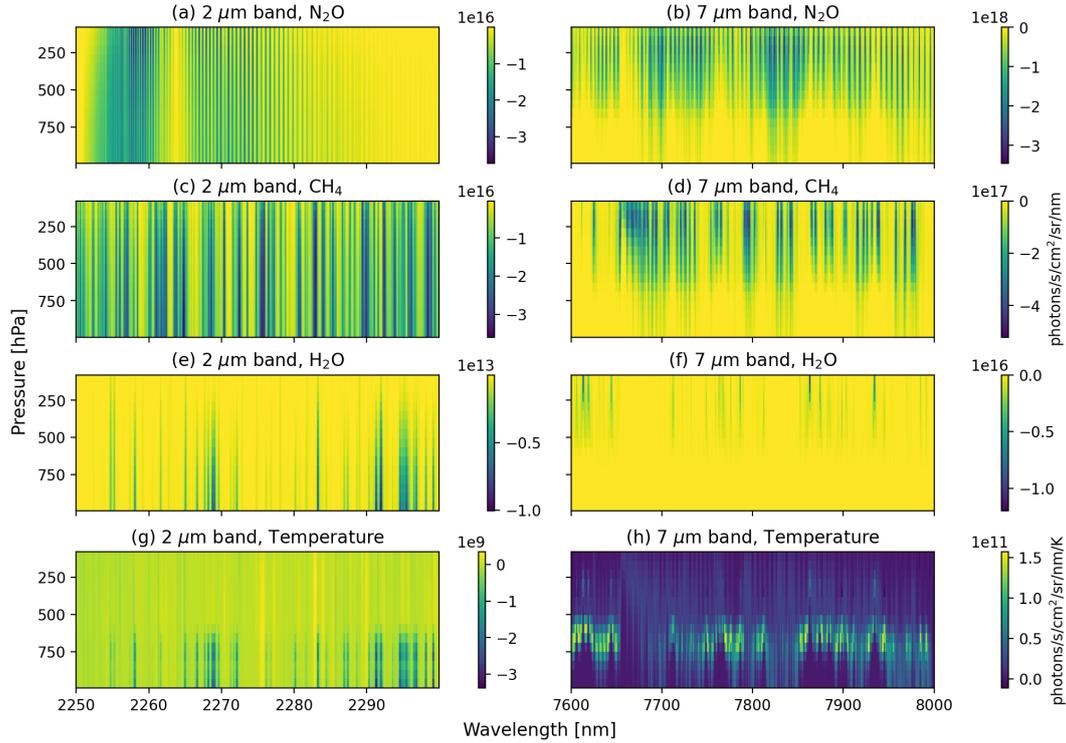
### 3.1.4 Radiative transfer simulation

265 For radiative transfer, this study leverages the VLIDORT radiative transfer model (Spurr, 2006), a discrete-ordinate multiple scattering code for a stratified multi-layer atmosphere. The great advantage for the present N<sub>2</sub>O application is VLIDORT's ability to generate not only radiances (in scalar mode without polarization) or (for polarized light calculations) Stokes 3-vectors, but also any group of analytically-calculated Jacobians with respect to any atmospheric profile variable (temperature and trace gas mixing ratios) and any surface quantity (e.g., albedo, temperature, and emissivity).

270 The SPLAT environment compiles atmospheric meteorological and constituent profiles, along with reference datasets to generate the linearized inputs required by VLIDORT to simulate both radiance and analytically derived Jacobian with respect to atmospheric state variables. For gases, the input absorption cross sections are based on look-up tables derived from HITRAN 2020 (Gordon et al., 2022), while aerosol optical properties are represented using Mie and T-matrix calculation. For more on these setups and specific use on MethaneAIR retrieval, see Spurr and Christi (2014) and Chan Miller et al. (2024).

275 Although more widely used in radiative transfer of solar radiations (e.g., Liu et al., 2010; O'Dell et al., 2012), VLIDORT can operate in both solar and thermal regimes and has been used in joint ultraviolet-TIR ozone retrieval from separate instruments (Cuesta et al., 2013). In the thermal regime, VLIDORT's radiative transfer is driven by blackbody thermal emission, treated in the atmosphere as a piecewise-continuous linear function of layer optical thickness. VLIDORT ingests a set of Planck functions, specified for the atmosphere at all layer boundaries, and again at the surface. Thermal emission is unpolarized and is  
280 assumed isotropic. The Planck functions at layer boundaries are linearized in order to determine temperature-profile Jacobian contributions additional to those arising from the temperature dependencies in the optical thicknesses (Spurr and Christi, 2019). This study marks the first application of the SPLAT-VLIDORT framework on the joint solar and thermal radiative transfer of the same instrument.

Figure 6 shows the Jacobians of the SWIR (left column) and TIR bands (right column) with respect to atmospheric N<sub>2</sub>O,  
285 CH<sub>4</sub>, H<sub>2</sub>O, and temperature profiles simulated by SPLAT-VLIDORT over a typical Midwest summer environmental conditions. These Jacobians are convolved with the ISRF and sampled at the spectral intervals of the spaceborne instrument specified in Table 1. Each panel represents a matrix, quantifying the change in observed radiance due to a unit perturbation in the state variable at given pressure level and wavelength. For N<sub>2</sub>O (Fig. 6a-b), the SWIR band exhibits weak absorption but relatively uniform sensitivity throughout the column, while the TIR band provides stronger sensitivity in the mid- and upper troposphere,  
290 but less near-surface response. This complementary behavior reinforces the benefit of combining SWIR and TIR observations for improved N<sub>2</sub>O retrievals.



**Figure 6.** Jacobians with respect to  $N_2O$ ,  $CH_4$ ,  $H_2O$ , and temperature profiles for SWIR (a,c,e,g) and TIR (b,d,f,h) bands respectively. Each panel shows the sensitivity of observed radiance to a unit perturbation in the corresponding state variable as a function of pressure and wavelength. Only altitudes up until 100 hPa are shown to emphasize the troposphere and lower stratosphere, where most  $N_2O$  variability occurs. The distinct vertical sensitivity patterns between SWIR and TIR bands highlight their complementary roles in  $N_2O$  remote sensing.

### 3.2 Detectability of $X_{N_2O}$ variability at different spatial scales

When spatially aggregating  $X_{N_2O}$  observations, the measurement error decreases with the target length scale  $d$ , assuming independent sounding errors:

$$295 \quad \sigma_{X_{N_2O}}(d) = \sigma_{X_{N_2O}}(d_0) \frac{d_0}{d}, \quad (14)$$

where  $\sigma_{X_{N_2O}}(d_0)$  is the native measurement error at sounding footprint size  $d_0$ , obtained from the linear sensitivity analysis (Section 3.1). At a length scale  $d \geq d_0$ , it is meaningful to compare the aggregated measurement error  $\sigma_{X_{N_2O}}(d)$  with the real-world  $X_{N_2O}$  variability  $\delta_{X_{N_2O}}(d)$ . With a known  $X_{N_2O}$  spatial distribution, its spatial variability can be quantified through a semivariogram (Matheron, 1963; Souri et al., 2022):

$$300 \quad \delta_{X_{N_2O}}(d) = \sqrt{\frac{1}{2} \langle (\Delta_d X_{N_2O})^2 \rangle}, \quad (15)$$



where  $\delta_{X_{N_2O}}(d)$  is the standard deviation that represents variability at length scale  $d$ .  $\Delta_d$  is an operator that differentiates all  $X_{N_2O}$  values separated by distances in a range of  $d \pm \varepsilon$ , where  $\varepsilon$  controls the granularity of the distance binning. The angular brackets  $\langle \rangle$  average all point pairs within the specified bin.

In reality, spatially distributed  $X_{N_2O}$  measurements that can support semivariogram calculation are very rare. Nonetheless, we can approximate the semivariogram of  $X_{N_2O}$  using the semivariogram of in situ measured  $N_2O$  mixing ratio in the PBL:

$$\Delta_d X_{N_2O} = \frac{1 - \exp(-h_b/H)}{1 - \exp(-h_t/H)} \Delta_d \mu_{N_2O}, \quad (16)$$

where  $h_b$  is PBL height,  $h_t$  is observation altitude as in Table 1,  $H = 7.5$  km is the assumed atmospheric scale height, and  $\Delta_d \mu_{N_2O}$  is the spatial differentiation of PBL  $N_2O$  mixing ratio, denoted as  $\mu_{N_2O}$ . Because  $h_t$  is significantly larger than  $h_b$ , the variability of  $X_{N_2O}$  is smaller than that of  $\mu_{N_2O}$ . Equation 16 holds when the variability of  $X_{N_2O}$  is dominantly driven by the variability in the PBL, and the PBL  $N_2O$  mixing ratio is approximately uniform in the vertical direction. Combining Eq. 15 and 16, we obtain:

$$\delta_{X_{N_2O}}(d) = \frac{1 - \exp(-h_b/H)}{1 - \exp(-h_t/H)} \sqrt{\frac{1}{2} \langle (\Delta_d \mu_{N_2O})^2 \rangle}. \quad (17)$$

Here, the semivariogram is directly calculated from extensively measured PBL  $N_2O$  mixing ratios during the MAIZE campaign, and the PBL height is inferred from collocated spiral profiles. The semivariograms are calculated for each flight from 0 to 50 km with 0.25 km bin width.

Since  $X_{N_2O}$  measurement error decreases with  $d$  (Eq. 14), and  $X_{N_2O}$  variability typically increases with  $d$  (Eq. 17), a critical spatial scale for variability can be numerically solved from the following equation:

$$q \times \sigma_{X_{N_2O}}(d^*) = \delta_{X_{N_2O}}(d^*), \quad (18)$$

where  $q$  is a positive scalar. The solution  $d^*(q)$  is the aggregated spatial scale beyond which  $X_{N_2O}$  variability exceeds  $q$  times the measurement error.  $q = 1$  means the variability equals the measurement error, and  $q = 2$  means the variability is twice the measurement error, which is typically assumed as the threshold of detectability (Jacob et al., 2016).

### 3.3 Detectability of $N_2O$ emissions at different spatial scales

A complimentary way of understanding  $N_2O$  detectability is to characterize the critical spatial scales of detectable  $N_2O$  emission sources. Here, we adopt the approach from Jacob et al. (2016) for  $CH_4$  detectability. Similar to Section 3.2, we aim to determine a critical spatial scale for emission,  $d^+(q, E)$ , beyond which the  $X_{N_2O}$  enhancement due to emissions at value  $E$  is  $q$  times the measurement error.

Assuming a uniform emission flux  $E$  and wind speed  $U$ , the enhancement of  $N_2O$  column amount due to emission at aggregated spatial scale  $d$  is

$$\Delta\Omega = \frac{Ed}{U}. \quad (19)$$



330 The  $N_2O$  enhancement increases with emission intensity and accumulating distance and decreases with wind speed. We assume  $U = 5 \text{ km h}^{-1}$  following Jacob et al. (2016). At the same length scale  $d$ , the measurement error of the observable column amount,  $\sigma_\Omega$ , can be derived from Eq. 14 by converting  $X_{N_2O}$  to a column amount:

$$\sigma_\Omega = \sigma_{X_{N_2O}} \frac{p_s(1 - \exp(-h_t/H))}{Mg} \frac{d_0}{d}, \quad (20)$$

335 where  $p_s$  is surface pressure assumed to be 1000 hPa,  $M$  is air molar weight, and  $g$  is gravity. The single-sounding measurement error  $\sigma_{X_{N_2O}}$  (at  $d_0$ , notation dropped for simplicity), sounding footprint size  $d_0$ , and observation altitude  $h_t$  are inherent properties of the instrument. Other parameters in Eq. 19 and 20 can be held constant except emission  $E$  and aggregation length scale  $d$ . Then, the detectability metric  $q$  can be calculated by dividing Eq. 19 and 20:

$$\begin{aligned} q(E, d) &= \frac{\Delta\Omega}{\sigma_\Omega} \\ &= \frac{Ed^2Mg}{U\sigma_{X_{N_2O}}d_0p_s(1 - \exp(-h_t/H))}. \end{aligned} \quad (21)$$

340 Equation 21 indicates that  $q$  increases linearly with emission,  $E$ , and quadratically with length scale,  $d$ , consistent with the intuition that more intensive and expansive emission sources are easier to detect. Alternatively, we can fix  $q$  to a certain value, e.g., 1 or 2, and solve for the critical length scale for emission level  $E$ :

$$d^+(q, E) = \sqrt{\frac{qU\sigma_{X_{N_2O}}d_0p_s(1 - \exp(-h_t/H))}{EMg}}. \quad (22)$$

## 4 Results

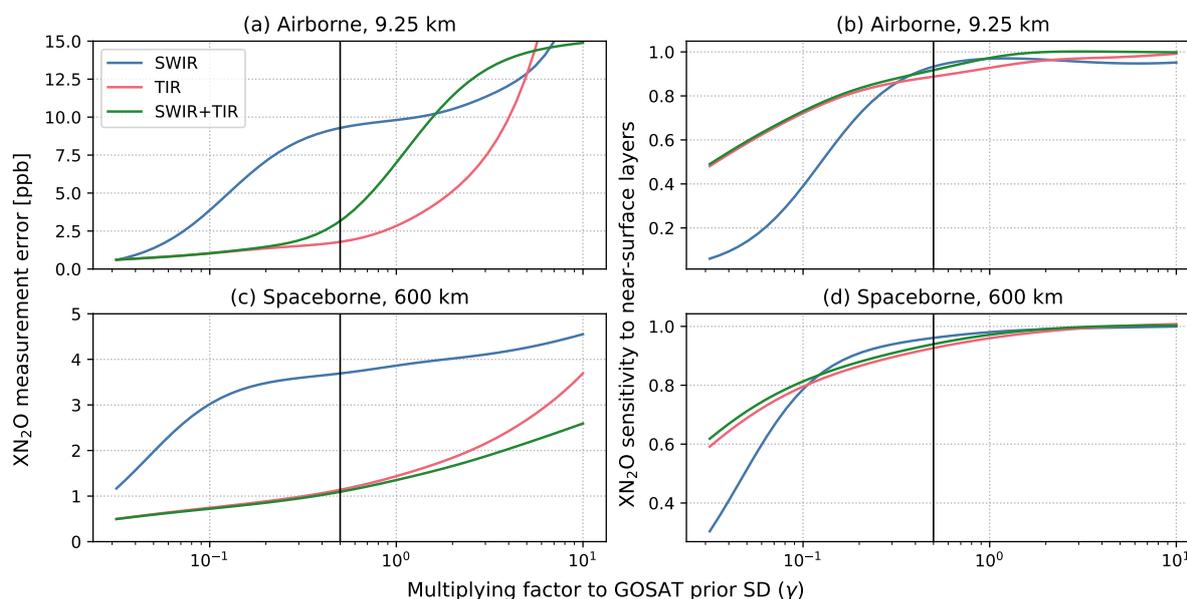
This section presents the outcomes of the linear sensitivity analysis and detectability methods introduced in the Section 3. Section 4.1 presents the dependence of  $X_{N_2O}$  measurement error and vertical sensitivity on spectral bands, observing platform properties, and a priori constraint strength. Section 4.2 uses semivariogram-based analysis to quantify the critical spatial scales at which natural  $X_{N_2O}$  variability becomes distinguishable from random measurement error. Section 4.3 relates emission strength,  $X_{N_2O}$  measurement error, and  $X_{N_2O}$  enhancement, providing a quantitative assessment of the critical spatial scales at which surface  $N_2O$  emissions can be resolved by the proposed instruments.

### 350 4.1 $X_{N_2O}$ measurement error and vertical sensitivity by airborne and spaceborne instruments

We evaluate the effectiveness of airborne and spaceborne instruments in retrieving  $X_{N_2O}$  by analyzing their measurement error and vertical sensitivity. Both metrics reflect the combined effect of observational constraint imposed by the instrument design and a priori constraint, as detailed in Section 3.1. Figure 7 illustrates the dependence of  $X_{N_2O}$  measurement error and near-surface sensitivity on the strength of a priori constraint for airborne and spaceborne instruments specified in Table 1 and compare results of three spectral settings; SWIR-only, TIR-only and joint SWIR–TIR setting. The a priori constraint is adjusted by scaling the GOSAT/MethaneSAT-based  $N_2O$  prior standard deviation profile (see Fig. 4a) by a factor  $\gamma$  in the range of 0.03 to



10. The said range of  $\gamma$  span regimes from strong domination by the prior regularization (small  $\gamma$ ) to those controlled primarily by the observations (large  $\gamma$ ). The results presented in Fig. 7 are the mean values from using the environmental conditions at 100 CrIS sounding locations shown in Fig. 1. Consistent across instruments and spectral settings,  $X_{N_2O}$  precision generally improves with tighter a priori constraint at small  $\gamma$  at the expense of degrading near-surface sensitivity.



**Figure 7.**  $X_{N_2O}$  measurement error (left panels) and near-surface sensitivity quantified by the PBL mean of column averaging kernel (right panels) as a function of the a priori constraint strength ( $\gamma$ ) applied to the  $N_2O$  prior standard deviation shown in Fig. 4a. Panels (a–b) correspond to the performance of the airborne instrument and panels (c–d) represent the performance of the spaceborne instrument. Each panel compares three spectral settings: SWIR-only (blue), TIR-only (pink), and combined SWIR–TIR (green) bands. Results are averaged over 100 CrIS soundings. The dual-band case achieves an optimal trade-off between near-surface sensitivity and  $X_{N_2O}$  measurement error at moderate strength of  $\gamma = 0.5$  by balancing the observational and a priori constraint for both remote sensing platforms.

For the airborne instrument (Fig. 7a-b), the  $X_{N_2O}$  measurement error shown in panel (a) reveals three distinct regimes. In the rightmost side with large  $\gamma$ , the retrieval is largely dependent on the amount of information provided by observations, with random detector noise dominating the error. In this regime, SWIR–TIR joint setting delivers the lowest measurement error as it combines information from two bands which increase the effective observational constraint. In contrast, the SWIR and TIR bands alone have fewer observations, leading to larger errors. In a transition regime where  $\gamma$  is roughly 2–5, dual-band case briefly exhibit higher measurement errors than those from the SWIR or TIR bands alone, because the retrieval is less stabilized by the a priori constraint as compared to the single-band cases. In other words, SWIR-only and TIR-only cases begin to “feel” the a priori constraint earlier due to weaker observational constraints. As  $\gamma$  continues decreasing, all three cases become increasingly controlled by the a priori constraint, so the errors converge and the dual-band case falls between the SWIR-only and TIR-only cases. Panel (b) highlights the trade-off value of  $\gamma$  between measurement error and near-surface sensitivity. A

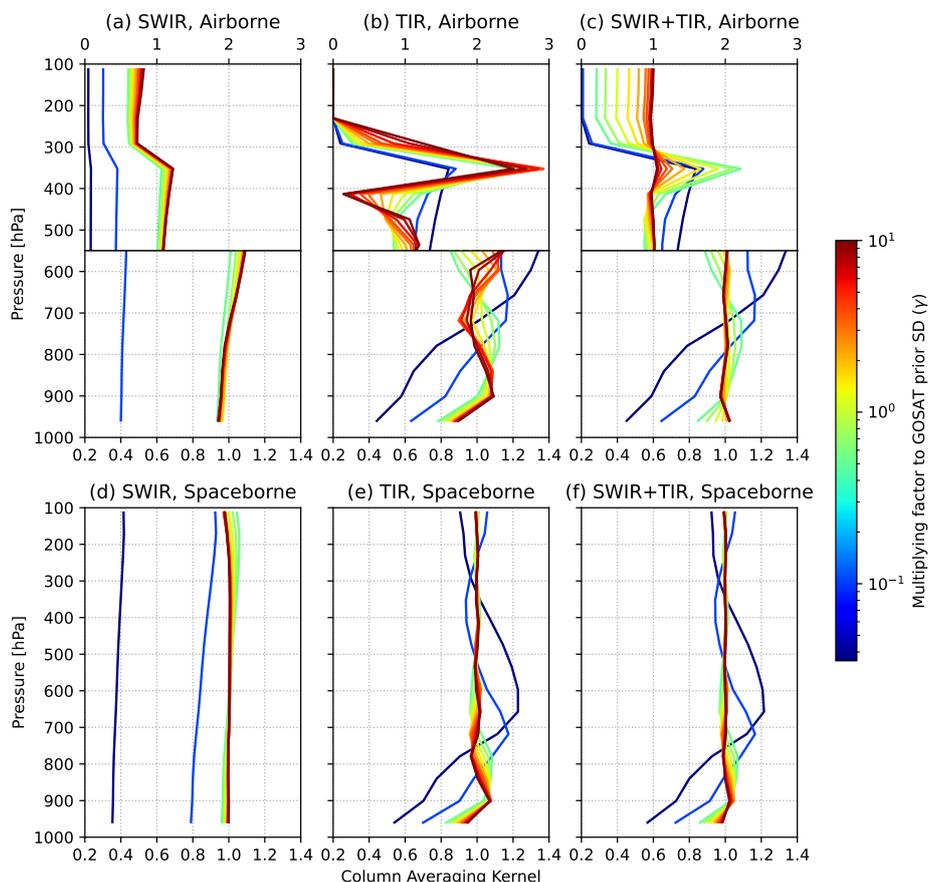


very strong prior (leftmost side, small  $\gamma$ ) suppresses the SWIR near-surface information which increases rapidly as the prior is relaxed and then reaches a plateau. A value of  $\gamma = 0.5$  (vertical black line) provides a balanced operating point because it sits on this plateau and SWIR near-surface sensitivity at this point is nearly saturated without entering the weak-prior regime where its value degrades quickly. This choice also keeps the dual-band case sensitive to observations in both bands, resulting  
375 in low measurement error while retaining sensitivity to the near-surface layers.

For the spaceborne instrument (Fig. 7c-d), the same qualitative order holds but the curves are less structured.  $X_{N_2O}$  measurement error (Fig. 7c) is overall lower than that from the airborne instrument largely due to the significantly wider TIR spectral range enabled by the spaceborne detector. The SWIR produces the largest measurement errors across all prior strengths. Both TIR-only and joint SWIR–TIR settings achieve comparable errors, but the integrated approach improves near-surface sensitivity relative to the TIR band alone (Fig. 7d). This added sensitivity is particularly beneficial given the inherently reduced surface  
380 sensitivity in satellite observations due to greater path lengths. We choose the same value of  $\gamma = 0.5$  for the spaceborne instrument because it provides a balanced operating point between observational and a priori constraint with retaining sensitivity to near-surface layers along with achieving low  $X_{N_2O}$  measurement error. At this selected operating point  $\gamma$ , single sounding  $X_{N_2O}$  measurement error for the joint SWIR–TIR retrieval spans the interval 2.8–3.8 ppb (mean: 3.2 ppb) for the airborne  
385 instrument at a footprint size of  $d_0 = 20$  m, whereas that for the spaceborne instrument ranges 0.6–1.8 ppb (mean: 1.1 ppb) at  $d_0$  of 0.7 km.

Figure 8 shows the vertical structure of the  $N_2O$  column averaging kernel for three spectral settings under different a priori strengths, illustrating how measurement information is spread throughout the observed atmospheric column. For the airborne instrument (Fig. 8a–c), the SWIR-only exhibits stronger sensitivity to the column with a discontinuity at the observation altitude  
390 of 9.25 km. This behavior follows the solar-backscattered nature of the viewing geometry where the incident sunlight samples the atmosphere only once above the aircraft, whereas the photons traverse the air mass twice (downward to the surface and then upward to the sensor) below the aircraft. In contrast, the TIR-only relies on thermal emissions and therefore show no sensitivity above the aircraft altitude, with its response confined to layers below 9.25 km. Within this region, TIR band shows an enhanced sensitivity in the layers just below the aircraft, which is plausibly related to the vertical weighting function in the  
395 retrieval. The joint SWIR–TIR setting alleviates this localized amplification and distributes the information more evenly by integrating complementary strengths of both bands.

For the spaceborne instrument (Fig. 8d–f), the overall vertical patterns are similar but smoother, because satellite geometry at orbital altitude avoids the discontinuity that appears in the case of airborne instrument. SWIR-only setting maintains strong column-wide sensitivity approaching near-unity kernel values for sufficiently relaxed a priori constraints. The TIR-only and  
400 the joint SWIR–TIR settings exhibit similar vertical response structures broadly, owing to the dominant contribution from the TIR band. Nevertheless, the inclusion of the SWIR band provides a visible improvement over the TIR-only case, particularly in enhancing sensitivity in the PBL, thereby highlighting the advantage of SWIR and TIR synergy for  $X_{N_2O}$  retrievals. For both instruments and all spectral settings, as the a priori constraint is relaxed (increasing  $\gamma$ ), the averaging kernels start incorporating information from the observational constraint and shift from prior-dominated to measurement-informed.



**Figure 8.** Column averaging kernels for  $N_2O$  retrievals using the SWIR-only (a, d), TIR-only (b, e), and joint SWIR–TIR (c, f) setting as a function of the a priori constraint strength ( $\gamma$ ) applied to  $N_2O$  prior standard deviation shown in Fig. 4a. Panels (a–c) show results for the airborne instrument at 9.25 km observational altitude, and (d–f) show results for the spaceborne instrument at 600 km.

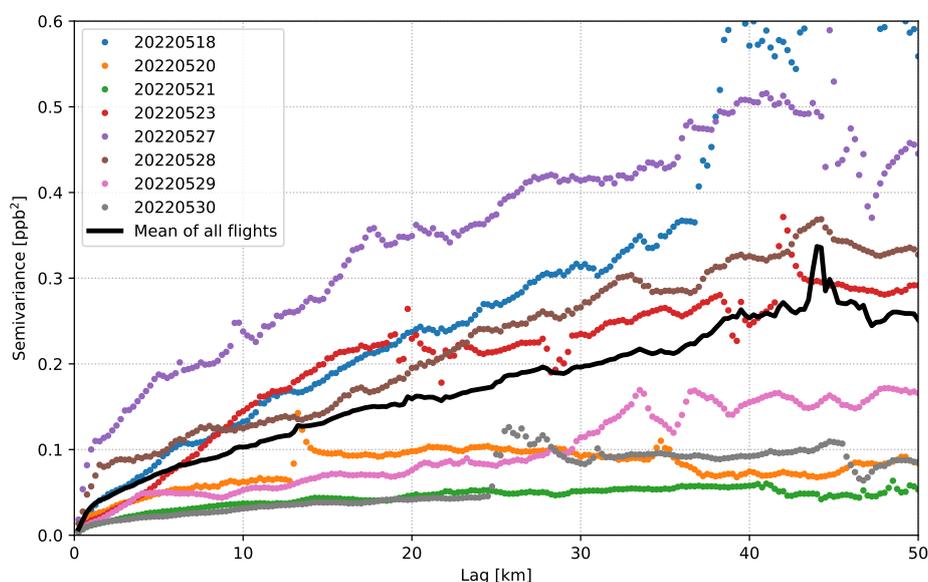
#### 405 4.2 Spatial scales of detectable $X_{N_2O}$ variability

We determine the critical spatial scales for the airborne and spaceborne instruments at which  $X_{N_2O}$  variability becomes distinguishable from measurement error. Here, the observed spatial structure of  $X_{N_2O}$  variability is inferred from in situ PBL  $N_2O$  observations, and the instrument-specific  $X_{N_2O}$  measurement errors are estimated from the linear sensitivity analysis (see Section 3.2).

410 Figure 9 presents the semivariograms of PBL  $N_2O$  mixing ratios derived from eight MAIZE flights (i.e.,  $\frac{1}{2} \langle (\Delta_d \mu_{N_2O})^2 \rangle$  in Eq. 17) along with their ensemble mean. Although the semivariance for all days generally increases with the separation distance, substantial variability is evident across individual flights. Several flights exhibit abrupt changes, which align with spatial intermittency in the PBL  $N_2O$  due to patchy sources and evolving boundary-layer conditions. The semivariogram sill, i.e., the

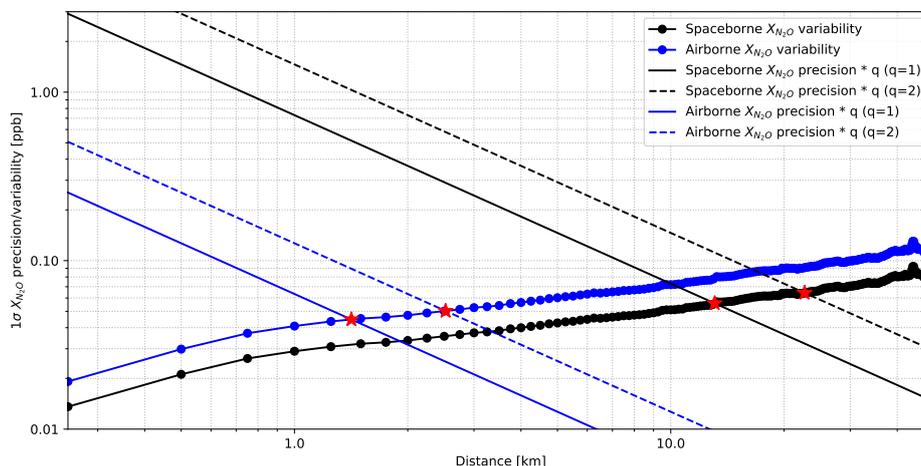


maximum variance, also shows significant variation across flights, reflecting substantial differences in the overall intensity of  
 415 heterogeneity. The extent of variability can also be attributed to meteorological conditions such as wind speed. Flights with  
 stronger winds (e.g. 20220520, 20220521, 20220529, 20220530) show reduced semivariance as enhanced horizontal mixing  
 diminishes spatial gradients, whereas flights with weaker winds (e.g. 20220518, 20220527) allow localized emission contrasts  
 to persist, leading to higher semivariance. The ensemble-mean semivariogram, shown as the black line in Fig. 9, exhibits a  
 smooth, steady rise and is utilized as a representative model of typical  $N_2O$  PBL variability for the subsequent detectability  
 420 analysis.



**Figure 9.** Semivariograms of PBL  $N_2O$  mixing ratios measured during the MAIZE campaign flights in 2022. Each colored line corresponds to a different flight date. The individual semivariograms reveal significant day-to-day variations likely due to heterogenetic nature of  $N_2O$  sources and localized meteorological conditions. The black line denotes the average semivariogram of all the flights, used as a representative model for quantifying critical spatial scales of detectable  $X_{N_2O}$  variability.

Built on the MAIZE semivariograms, the observed PBL  $N_2O$  variability translates to expected  $X_{N_2O}$  variability through  
 Eq. 17 and is then compared with  $X_{N_2O}$  measurement error for airborne and spaceborne instruments. Measurement error here  
 refers to the single-sounding uncertainty at the native footprint size  $d_0$ , whereas the uncertainty after averaging independent  
 soundings to the spatial aggregation scale  $d$  is referred to as  $X_{N_2O}$  precision. Figure 10 shows the trends of  $X_{N_2O}$  variability  
 425 and  $X_{N_2O}$  precision as functions of the spatial aggregation scale ( $d$ ). The two solid lines with circular markers in Fig. 10  
 represent the inferred  $X_{N_2O}$  variability for airborne (blue) and spaceborne (black) instruments, respectively. Although the  
 same semivariogram is used in calculating the  $X_{N_2O}$  variability for both instruments, the results differ, as this variability  
 depends on the observational altitude ( $h_t$ ) of the instrument (see Eq. 17) and thus the relative weight of PBL variability in the  
 observed atmospheric column. The higher  $h_t$  for the spaceborne instrument dilutes the boundary-layer heterogeneity more,



**Figure 10.**  $X_{N_2O}$  variability and  $X_{N_2O}$  precision for airborne (blue) and spaceborne (black) instruments. Solid lines with circular markers show  $X_{N_2O}$  variability derived from the MAIZE flights, solid and dashed straight lines represent aggregated  $X_{N_2O}$  precision multiplied by detectability thresholds of  $q = 1$  and  $q = 2$  respectively. The critical spatial scales  $d^*(q)$ , where the atmospheric variability become  $q$  times the precision, are indicated by red stars in the figure.

430 yielding smaller  $X_{N_2O}$  variability as compared to that for airborne instrument at a given horizontal distance. The blue solid line in Fig. 10 corresponds to the aggregated precision  $\sigma_{X_{N_2O}}(d)$  of airborne instrument, and black solid line corresponds to that of spaceborne instrument, computed from single-sounding  $X_{N_2O}$  measurement error ( $\sigma_{X_{N_2O}}(d_0) = 3.2$  ppb for the airborne instrument and  $\sigma_{X_{N_2O}}(d_0) = 1.1$  ppb for the spaceborne instrument) obtained in Section 4.1, using Eq. 14. Airborne and spaceborne precision lines do not overlap because  $\sigma_{X_{N_2O}}(d_0)$  for airborne is larger (3.2 ppb) as compared to that for

435 the spaceborne (1.1 ppb), and this quantity decreases quickly for the airborne instrument with the spatial averaging due to much smaller footprint size ( $d_0 = 20$  m for airborne and  $d_0 = 0.7$  km for spaceborne, see Table 1). As formulated in Eq. 14, the  $X_{N_2O}$  precision decreases log-linearly with  $d$  due to averaging of independent soundings, while the  $X_{N_2O}$  variability increases with  $d$  following the behavior shown in Fig. 9. The intersection points of these two quantities (marked with red stars in Fig. 10) define the critical spatial scale  $d^*(q)$ , at which atmospheric variability is  $q$  times the measurement error, as defined in

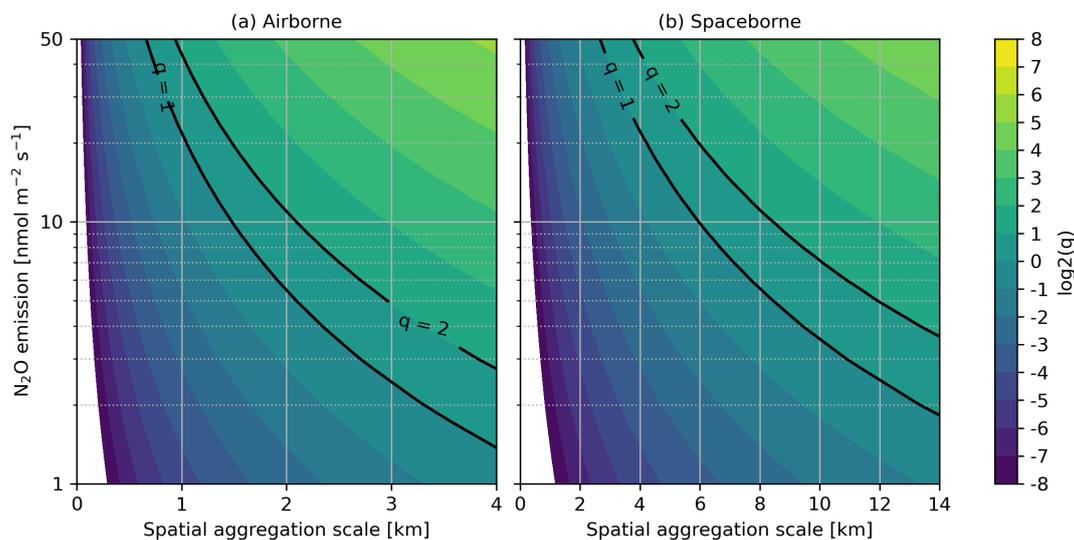
440 Eq. 18. The dashed lines represent a more conservative detectability requirement by plotting  $q \times \sigma_{X_{N_2O}}(d)$  with a commonly used criterion of  $q = 2$ . The corresponding intersection points locate the spatial scales where  $X_{N_2O}$  variability is twice the  $X_{N_2O}$  precision. For  $q = 2$ , the critical spatial scale ( $d^*(q = 2)$ ) is approximately 2.5 km for the airborne and 22 km for the spaceborne instrument. This reflects how  $X_{N_2O}$  variability can be resolved from measurement noise under typical conditions observed during MAIZE.



### 445 4.3 Spatial scales of detectable N<sub>2</sub>O emissions

In Section 4.2, the critical spatial scales for variability are inferred by comparing  $X_{N_2O}$  precision against  $X_{N_2O}$  variability that implicitly reflects the influence of surface emissions, but this variability does not provide a quantitative mapping between N<sub>2</sub>O emission strength and  $X_{N_2O}$  enhancements. Here, we make that connection explicit by modeling expected  $X_{N_2O}$  enhancement resulting from a uniform emission strength  $E$  and comparing it to the corresponding  $X_{N_2O}$  precision at matching spatial  
450 scales. We then quantify the emissions detectability using the  $q(E, d)$  metric, introduced in Section 3.3. Here  $q(E, d)$  is a continuous variable, defined as the ratio of emission-induced enhancement in  $X_{N_2O}$  to the aggregated measurement error at spatial aggregation scale  $d$  (Eq. 21). Figure 11 shows  $q(E, d)$  as a function of emission strength ( $E$ ) and spatial aggregation  
455 scales while weaker emissions require substantial spatial aggregation to achieve the same level of confidence  $q$ .

The black contour lines in Fig. 11 indicate the solutions of Eq. 21 for  $q = 1$  and  $q = 2$ ; these provide a convenient way to read off the level of spatial aggregation needed to achieve a chosen detectability for a given emission strength. Here,  $q = 1$  means that an emission-induced enhancement is equal to the aggregated precision and  $q = 2$  indicates  $X_{N_2O}$  enhancement becomes twice the aggregated precision at a given spatial aggregation scale  $d$ . Using a representative uniform emissions of  $5 \text{ nmol m}^{-2} \text{ s}^{-1}$ ,  
460 consistent with the mean value of all nodes from 21–24 May in Fig. 3b, Fig. 11 implies critical spatial scale  $d^+$  is  $\sim 2.1$  km for the airborne instrument at  $q = 1$  and  $\sim 2.9$  km at  $q = 2$ . For the spaceborne instrument, the corresponding values are substantially larger with  $d^+ \sim 8.4$  km at  $q = 1$  and  $\sim 12$  km at  $q = 2$ . For a higher uniform emissions of  $10 \text{ nmol m}^{-2} \text{ s}^{-1}$ , the  $d^+$  reduces to 1.5 km at  $q = 1$  and 2.1 km at  $q = 2$  for the airborne instrument, and the corresponding values decreases to 5.9 km ( $q = 1$ ) and 8.5 km ( $q = 2$ ) for the spaceborne instrument.  $d^+$  values are different for airborne and spaceborne instruments as it  
465 is dependent on instrument properties such as footprint size ( $d_0$ ), observational altitude ( $h_t$ ) and single-sounding measurement error ( $\sigma_{X_{N_2O}}(d_0)$ ). Overall, weaker emissions require larger-scale spatial aggregation to achieve a certain detectability level for both instruments.



**Figure 11.** Detectability metric  $q(E, d)$  as a function of emission strength ( $E$ ) and spatial aggregation scale ( $d$ ) for the (a) airborne and (b) spaceborne instruments. Solid black contours indicate  $q = 1$  and  $q = 2$ , where the  $X_{N_2O}$  enhancements due to emission  $E$  are equal to and twice the aggregated measurement error at  $d$ , respectively. Instrument-specific measurement errors at  $d_0$  are taken from linear sensitivity analysis. Stronger emissions can be resolved from noise at lower spatial scales while weaker emissions require more spatial aggregation.

#### 4.4 Critical spatial scales of $N_2O$ detection estimated using different approaches

This section provides a combined view of critical spatial scales reported as  $d^*$  and  $d^+$  in Section 4.2 and 4.3, respectively. Table 2 summarizes these scales for the airborne and spaceborne instruments at two detectability levels,  $q = 1$  and  $q = 2$ , illustrating how the required aggregation scale depends on detectability threshold and the approaches to estimate  $X_{N_2O}$  variability. In all cases, the airborne instrument consistently achieves smaller critical spatial scales as compared to spaceborne instrument. Although the airborne single-sounding error is larger, its much finer footprint size  $d_0$  of 20 m allows more rapid reduction of random error with aggregation length scale  $d$  and detectability is achieved quickly under favorable conditions. In contrast, the spaceborne instrument with footprint size  $d_0$  of 0.7 km, generally requires aggregation over several kilometers to reach the same detectability threshold, emphasizing that its strength lies in detecting broader regional patterns rather than localized enhancements.

For the variability-driven estimates, the choice of semivariogram primarily controls the inferred critical spatial scales. Using the mean semivariogram of all 8 flights conducted in May 2022 yields more conservative critical spatial scales than using the semivariogram of highest-variability flight (2022-05-27), which represents a more favorable scenario. When the  $X_{N_2O}$  variability is twice the  $X_{N_2O}$  precision,  $d^*$  reduces from 2.5 km to 1.7 km for the airborne instrument and from 22 km to 16 km for the spaceborne instrument when switching from the mean semivariogram to the high-variability semivariogram. For the emission-driven cases, the critical spatial scales  $d^+$  are reported for uniform emissions of  $E = 1, 5, 10$  and  $20 \text{ nmol m}^{-2} \text{ s}^{-1}$  in Table 2. As anticipated,  $d^+$  decreases systematically with increasing uniform emission strength. For instance, increasing  $E$



**Table 2.** Critical spatial scales at which  $X_{N_2O}$  signals become  $q$  times the aggregated measurement error for airborne and spaceborne instruments. Value are reported for  $q = 1$  and  $q = 2$ .

Source of variability	Airborne critical spatial scale [km]		Spaceborne critical spatial scale [km]	
	$q = 1$	$q = 2$	$q = 1$	$q = 2$
Semivariogram (2022-05 average)	1.4	2.5	13	22
Semivariogram (2022-05-27)	0.92	1.7	9.4	16
$E = 1 \text{ nmol m}^{-2} \text{ s}^{-1}$	4.7	6.6	19	26
$E = 5 \text{ nmol m}^{-2} \text{ s}^{-1}$	2.1	2.9	8.4	12
$E = 10 \text{ nmol m}^{-2} \text{ s}^{-1}$	1.5	2.1	5.9	8.5
$E = 20 \text{ nmol m}^{-2} \text{ s}^{-1}$	1.1	1.5	4.2	5.9

485 from 1 to 20  $\text{nmol m}^{-2} \text{ s}^{-1}$ , reduces the  $d^+(2, E)$  from 6.6 km to about 1.5 km for the airborne, and from 26 km to around 5.9 km for the spaceborne instrument. Together, the variability- and emission-driven results bracket the spatial scales over which  $X_{N_2O}$  signals are expected to become detectable under typical MAIZE-like boundary-layer variability and plausible agricultural emissions.

## 5 Discussion and Conclusions

490 This study develops a practical and physically grounded framework to evaluate the capability of remote sensing instruments to detect atmospheric  $N_2O$  variability and column enhancements. To achieve this purpose, we expand the capacity of the SPLAT-VLIDORT radiative transfer model to jointly simulate solar-reflected (SWIR) and thermal-emitted (TIR) spectra within a unified framework. This framework provides a quantitative basis for assessing the combined observation from the SWIR and TIR bands under a priori regularization, with a particular emphasis on the trade-off between random measurement error and sensitivity to near-surface variability. A central consideration here is the use of  $X_{N_2O}$  measurement error, which is derived by linear propagation of Gaussian instrument noise. Although this represents only one component of the total error budget, it provides a lower bound on the achievable single-sounding error and therefore a first-order constraint for any  $N_2O$ -focused mission. Also, in the error budget, measurement error is the only component that decreases predictably with spatial averaging of independent soundings, with the error scaling approximately as  $1/\sqrt{N}$ , where  $N$  is the number of independent soundings being aggregated. This relationship provides a direct link between single-sounding error and spatial aggregation scales required for resolving  $X_{N_2O}$  enhancements above the noise.

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The linear sensitivity analysis further shows that the a priori constraint plays a decisive role in balancing observational and a priori contributions to the vertical distribution of information. A key methodological direction for future refinement is to move beyond a scaled prior covariance toward an ensemble covariance that will allow the regularization to be informed by physically plausible variability rather than an assumed scaling. Within the current setup, the joint SWIR–TIR setting balances the observational and a priori information contributions at a moderate prior strength by scaling  $N_2O$  prior standard deviation

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by 0.5. At this prior strength, dual-band case yields single-sounding measurement error of 3.2 ppb for the airborne instrument with 20 m footprint size and 1.1 ppb for the spaceborne instrument with 0.7 km footprint size, while preserving sensitivity to the near-surface layers.

510 An additional factor that could influence the performance is the presence of atmospheric aerosols. Aerosol scattering in the SWIR band modifies the photon path length and if not handled properly can introduce biases in the retrieved  $X_{N_2O}$ . Although, SPLAT-VLIDORT framework can incorporate aerosol optical properties, the scope of this study is limited to clear-sky condition. Future work should incorporate the influence of aerosol properties on  $X_{N_2O}$  accuracy, and how the SWIR and TIR bands can synergized to account for aerosol influences.

515 The instrument precision alone does not fix the detectability; rather, it is determined by how the instrument precision interacts with real-world  $X_{N_2O}$  variability. We therefore estimate the critical spatial scales of detection using two data-informed approaches that address different aspects of this problem and rely on distinct simplifying assumptions. First, the semivariogram-based analysis provides an empirical constraint on how  $X_{N_2O}$  variability grows with separation distance under realistic agricultural conditions sampled during the MAIZE campaign. Its main assumption is that  $X_{N_2O}$  variability is dominated by PBL  
520 variability and the PBL  $N_2O$  mixing ratio is approximately uniform in the vertical direction (Eq. 16-17). Second, the emission-based detectability metric  $q(E, d)$  links emission strength and spatial aggregation scales to expected  $X_{N_2O}$  enhancements using an assumed wind speed of  $5 \text{ km h}^{-1}$ . The emission strengths considered are informed by the autochamber data shown in Fig. 3. These approaches are intended to provide first-order constraints rather than universal thresholds, and the inferred critical spatial scales should be interpreted as conditional on variability, emission strength, meteorology, and the chosen aggregation strategy.

525 Under MAIZE-like conditions, semivariogram-based analysis indicates that natural  $X_{N_2O}$  variability exceeds instrument precision at critical spatial scales of approximately 1–3 km for airborne and 10–23 km for spaceborne observations. Episodic agricultural emissions of  $5 \text{ nmol m}^{-2} \text{ s}^{-1}$  require aggregation of measurement error to spatial scales of roughly 2–3 km for airborne and  $\approx 8$ –12 km for spaceborne instrument to achieve required level of detection confidence. Together these results emphasize the complimentary roles of airborne and spaceborne observing platforms. Airborne instruments are best suited  
530 for resolving fine-scale heterogeneity associated with episodic emissions, whereas spaceborne observations can detect subtle column enhancements through spatial averaging while maintaining regional coverage. Overall, the combined SWIR–TIR band concept for  $N_2O$  remote sensing introduced in this study addresses the longstanding limitations of SWIR and TIR bands alone, laying a foundation for future  $N_2O$ -focused missions by offering practical guidance for instrument design.

*Code and data availability.* The code related to linear sensitivity analysis can be accessed at [https://github.com/Kang-Sun-CfA/Methane/11/](https://github.com/Kang-Sun-CfA/Methane/11/longwave.py)  
535 longwave.py

*Author contributions.* AR performed the analysis related to this study. KS developed the concept and linear sensitivity analysis framework. CCM contributed to the development of SPLAT. RS contributed to the development of VLIDORT. BB served as the primary contact for



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*Competing interests.* The authors declare that they have no competing interests.

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