



Integrating Multi-Step-Flux-Method for full range soil hydraulic characterisation: From saturation to oven-dryness

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Abstract. Soil hydraulic properties (SHP), defined by the water retention curve (WRC) and the hydraulic conductivity curve (HCC), are crucial to describe water storage and flow in soils. Several methods have been developed and combined to measure these two fundamental curves across the full range from saturation to oven dryness. However, for the HCC, there is still a data gap between approximately -1 to -100 hPa, which is expected to be affected by soil structure. We present an experimental workflow in which the multi-step-flux (MSF) method is integrated into the well-established combination of methods for measuring SHP, namely the falling head method, the simplified evaporation method, and the dew point method, specially designed to be applied to the same sample. The MSF is an adaptive, direct measurement of the HCC based on applying series of steady-state water flows to a soil sample characterised by unit hydraulic gradient. Once equilibrium is achieved, the sample is characterised at each step by a constant pressure head, constant water content and constant unsaturated hydraulic conductivity which is equal to the applied flux. We tested the method for three different soil columns: a repacked sand with a very well-defined air-entry pressure and two undisturbed structured silt loams. For the sand, the MSF results coincide with the saturated hydraulic conductivity value, measured with the falling head method. For the undisturbed loam samples, the structural effect on the HCC is clearly visible. Integrating the MSF into the common lab-workflow to characterise SHP will help future studies to investigate soil structure effect on SHP.

20 **1 Introduction**

The water retention curve (WRC) and the hydraulic conductivity curve (HCC) characterise the soil hydraulic properties (SHP). The WRC provides information on how much water is bound at specific energy levels within soils. The HCC describes how easily water flows through soil. A complete characterisation, from full saturation to oven-dry conditions, is essential for modelling water movement in soils and many related processes such as plant water uptake, nutrient transport, or pollutant leaching (Vereecken et al., 2016; Diamantopoulos et al., 2024).

Several methods have been developed to measure both curves accurately and reliably; however, none of them can measure both curves simultaneously from saturation to very dry conditions. Thus, a combination of methods is usually used in soil physical laboratories. A time-effective combination of methods consists of the simplified evaporation method (Wind, 1968; Peters and Durner, 2008), the dewpoint method (Schelle et al., 2013) and the falling head method for the saturated hydraulic



30 conductivity (Hohenbrink et al., 2023). For the WRC the simplified evaporation method can provide data points at pF -1-3,
depending on how well the tensiometers are degassed. If the air-entry of the ceramic tip is used, an additional point at pF 3.8
(assuming that the air entry pressure of the tensiometer is around pF 3.8) can be obtained (Schindler et al., 2010). The dewpoint
method provides WRC data between pF 4.5 and 6.5 (METER Group GmbH, 2025). For the HCC, the falling head method
provides only one data point, the saturated hydraulic conductivity and the simplified evaporation method provides HCC points
35 between pF 1.8 and 3 and one additional point at around pF 3.8 if the air-entry of the tensiometer is used (Schindler et al.,
2010).

Therefore, in the HCC there are substantial data gaps in both the near-saturation (pF -1 to around 1.8) and dry (pF > 3.8) ranges.
The latter has most recently been addressed by using humidity sensors, which extend the HCC curve to pF 5.5 for sand and pF
6 for loam (Bosse et al., 2025). The wet range data gap of the HCC has been bridged by Sarkar et al. (2019b) by adding an
40 extra step to the falling head and simplified evaporation method. In this extra experiment, they applied a constant flux through
the soil sample, by fixing the same negative pressure head at the top and at the bottom of the column. Under these conditions,
gravity is driving water flow, and the flux density can be estimated by measuring the water outflow at the lower end of the
column. By keeping equal and fixed the pressure heads at the top and at the bottom and by only changing the height of the soil
column, different points of the HCC were estimated (Sarkar et al., 2019a, 2019b). A limitation of this method is that the porous
45 plate on top of the soil has a smaller surface area than the soil, in order to allow air to invade the soil (for a drainage process).
According to Sarkar et al. (2019a) this introduces an error of the flux rate to be less than 10%. A more robust method for
directly measuring the near saturation unsaturated hydraulic conductivity, can be achieved by integrating the MSF method. In
the MSF, water flow is maintained constant on top of the soil sample by drip irrigation, the pressure head is measured within
the upper part of the soil sample, and the pressure head beneath the sample is regulated to ensure zero pressure head gradient
50 in the sample or simple gravity only flow conditions (Weller et al., 2011). The advantage of the MSF is that the sample can
freely ventilate without compromising the measurement.

Including the MSF as a standard measurement not only closes the data gap from saturation to field capacity, but it also provides
the possibility to study structure driven macro-pore flow in detail (Jarvis et al., 2016). The near saturation data point of the
HCC is known to be affected by soil structure which again can be examined by using the MSF (Bonetti et al., 2021).

55 A crucial point when comparing WRC and HCC from different methods is that the phenomenon of dynamic non-equilibrium
must always be considered. In simple terms, dynamic non-equilibrium refers to the dependence of the measured WRC and
HCC on the flow conditions (Hassanizadeh et al., 2002; Diamantopoulos and Durner, 2012; Vogel et al., 2023). Topp et
al.(1967) were the first to show that, during a drainage process, more water is retained by the soil matrix (at a specific pressure
60 head) under transient conditions compared with steady-state and equilibrium conditions. The faster the water flow, the greater
the difference between transient and equilibrium WRC and HCC curves. Dynamic non-equilibrium effects are observed in
both MSF measurements (Weller and Vogel, 2012) and simplified evaporation measurements (Diamantopoulos and Durner,
2012).



65 In this study, we present an experimental protocol that combines the falling head method, the MSF, the simplified evaporation
method and the dew point method to characterise the WRC and the HCC including the pF range of -1 to 1.8. This measurement
protocol is optimal for studies which examine soil structure effects on SHP. We applied the protocol to a repacked sand with
a well-defined air-entry pressure to test the consistency of the different methods. In addition, two undisturbed samples of the
same texture, collected under different soil tillage systems, allowed us to assess the protocol's ability to capture structural
70 effects. To further evaluate the workflow and the importance of the MSF data, WRC and HCC models were fitted to
experimental data with and without including the MSF data. For this, the single porosity van Genuchten-PDI model (Peters,
2013; Iden and Durner, 2014) was fitted to all the experimental data. For improving, the fitting for one of the silt loams samples,
we had to introduce a bimodal version of the van Genuchten-PDI model that is more flexible in the wet range of the HCC.

2 Materials and Methods

75 2.1 Method workflow

Two undisturbed soil cores (volume of 250 cm³ and a surface area of 50 cm²) of the same texture (a silt loam (USDA, 1999))
were taken from a conventional ploughed topsoil with a bulk density of 1.5 g cm⁻³(Loam 1) and from a subsoil under a disk
harrow tillage system with a bulk density of 1.6 g cm⁻³ (Loam 2) by gently hammering a steel cylinder into the soil. In addition,
four steel cylinders were repacked to a bulk density of 1.59 g cm⁻³(standard error 0.01 g cm⁻³) with a sand with uniform grain
80 size distribution (Sand, Quarzsand, grain size distribution; >200 μ 0.24%, >64 μ 99.01%, <64 μ 0.75%). All steel cylinders used
in this study, had a hole (diameter 0.5 cm) at a depth of 2 cm from the top of the cylinder for the installation of a tensiometer
for the MSF experiment. For all other experiments, the hole was sealed with vehicle body sealant (Teroson RB IX) and tape.

The workflow begins with a five-day stepwise saturation of the sample with degassed tap water. Four different methods were
used in series for the sample to measure the WRC and HCC (Fig. 1): the falling head method (using the KSAT device, Meter
85 Group USA), the multi-step flux method (using a custom made MSF device), the simplified evaporation method (using the
HYPROP device, Meter Group USA), and the dew point method (using the WP4C device, Meter Group USA). After the MSF,
a two-day stepwise re-saturation was conducted to ensure the sample was fully saturated and to reduce the risk of air entrapment
for the HYPROP measurement. The experiment ends with the samples being dried in an oven at 105 °C for 24 hours. We
repeated KSAT and HYPROP measurements for three sand columns to ensure reproducibility of the repacking and SHP, and
90 for the MSF we used one sand column, which was not used for other experiments. Both undisturbed loam columns completed
the full workflow.

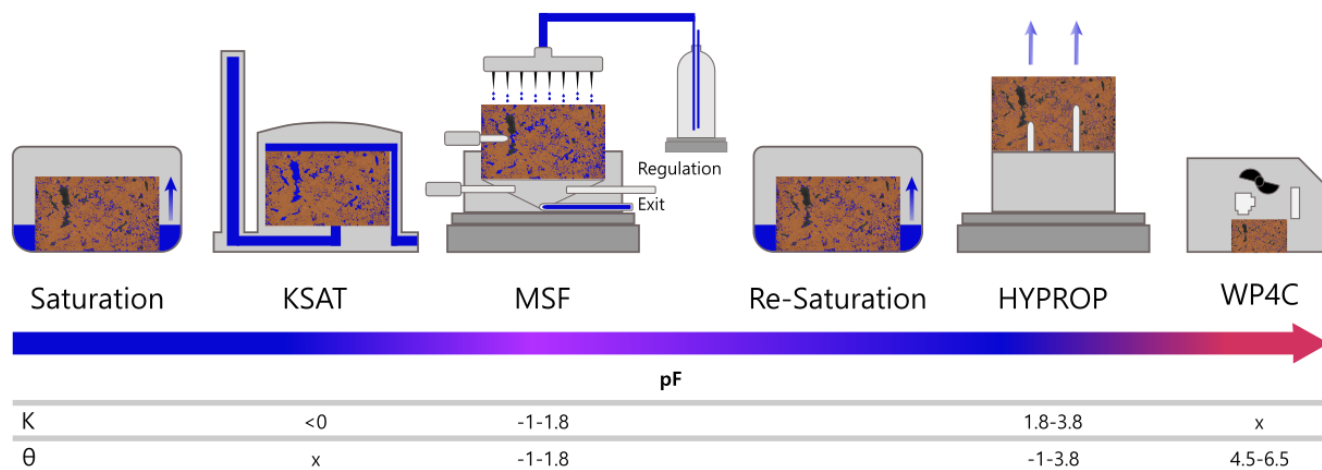


Figure 1: A schematic overview of the workflow.

2.1.1 Falling head, KSAT

- 95 The saturated hydraulic conductivity (K_{sat}) was measured using the falling head method as implemented in the KSAT device. The flux density at saturation for laminar flow is described by on Darcy's law Eq. (1):

$$q = -K_{sat} \nabla H \quad (1)$$

Where q is the flux density [cm day^{-1}], H is the hydraulic head [cm], defined as: $H = h + z$, where z is the spatial coordinate [cm] and h is the pressure head [cm], and K_{sat} [cm day^{-1}] is the saturated hydraulic conductivity. The falling head method works by mounting a fully saturated soil sample on the KSAT device, which consists of a water reservoir with a defined volume.

- 100 Once the experiment starts, the water moves from the container and through the sample. A pressure sensor continuously measures the pressure drop between the free surface of water in the container and the upper end of the sample (outflow point). An exponential decay function is automatically fitted to the measured data and the K_{sat} value is estimated as a function of the fitted exponent. For more information about the method, we refer to Operation Manual (METER Group GmbH).

2.1.2 Multistep flux, MSF

- 105 The MSF quantifies the hydraulic conductivity near saturation (pF -1 to 1.8). Water flow during an MSF experiment is described by Darcy-Buckingham's equation:

$$q = -K(h) \nabla H \quad (2)$$

where h is the pressure head [cm], and $K(h)$ is the unsaturated hydraulic conductivity [cm day^{-1}] at h . For the MSF method, a constant q is applied on top of the soil column, and the h is measured with a tensiometer at 2 cm. At the bottom of the column,



the same pressure head, h , is applied, forcing the system to reach unit hydraulic head (gravity flow), where the whole column
110 is characterised by a unique water flux q , pressure head h and water content. Under these conditions, equation (2) becomes:

$$q = -K(h) \quad (3)$$

And the applied flux is equal to the unsaturated hydraulic conductivity at pressure head, h .

The MSF device consist of a Mariotte bottle, a system of tubs, a peristaltic pump, an irrigation head, two balances, a tensiometer
115 installed inside the sample, a sample chamber, a pressure sensor installed in the chamber, two pressure-regulation valves, a
vacuum pump, and custom-made regulation and logging software (LabVIEW). Prior to the start of the experiment, a three-
point calibration curve of the tensiometer was established using a hanging water column. The calibration curve was then used
to correct the tension measurements at the data processing stage. The pressure sensor, connected to the chamber below the
sample, was checked against a high-precision reference sensor. After the calibration phase, each soil sample is mounted on a
pressure plate (ROBU VitraPOR Filterplatte biplane \varnothing 90mm, por. ASTM Fine) fixed in the chamber, with a tensiometer
120 installed in the sample (2 cm). Water flow is supplied by a Mariotte bottle and distributed through a peristaltic pump and an
irrigation head over the sample. Both the sample and the Mariotte bottle were placed on an electronic balance to calculate
water flux and changes in the samples water content. Given the accuracy of the balances, we estimate that the error of the
water content of the sample is 0.3%. The chamber under the sample is connected to the water outflow, a pressure sensor and a
regulation system (Fig. 1). The regulation system is automatically adjusting the pressure head at the bottom of the sample to
125 the one measured by the tensiometer inside the soil sample. This is done by two regulating valves and by opening to either
under pressure or atmospheric air. The maximum difference between measured and adjusted potential was controlled by a
software input parameter, the delta value, which introduces an uncertainty of the final pressure head. At low pressure head (0
to -5 cm), the delta values were set between 1.5-2, for pressure head values between -5 and -10 cm, between 2-3, and for <-10
cm, between 2-4.

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Different water fluxes were applied on the soil sample in a stepwise manner, starting with a high flow rate and then gradually
reducing the flow rate for each new step (drainage process). Each step run for at least one hour to ensure that the system reaches
steady state water flow conditions and equilibrium conditions were assessed for each sample by checking when the matric
potential and sample mass remained relatively stable. Once the experiment was finished, the actual flow rates were calculated
135 from the changes in the Mariotte bottle's weight during the last 10 minutes of the step. For the tension, we use the median of
the tension over the last 10 minutes of each step.

To further evaluate the agreement between the simplified evaporation method and the MSF, the water content for each flux
can also be calculated by:



$$\theta_i = \frac{(\theta_{i-1} * V_{total} + \frac{d_i}{\rho_w})}{V_{total}} \quad (4)$$

140 where θ_i is the volumetric water content at flow rate step i [$\text{cm}^3 \text{cm}^{-3}$], V_{total} is the total volume of the sample (250 cm^3), ρ_w is the water density assumed equal to 1 g cm^{-3} for all calculations and d_i is the weight difference from step i and step $i-1$ [g]. Critical to this calculation is the assumption that the initial water content θ_0 [$\text{cm}^3 \text{cm}^{-3}$] is given by:

$$\theta_0 = \theta_{sat} = n \quad (5)$$

where n [$\text{cm}^3 \text{cm}^{-3}$] is the estimated porosity from:

$$n = 1 - \frac{\rho_b}{\rho_s} \quad (6)$$

Where ρ_b is the bulk soil density and ρ_s is the density of the particle (2.65 g cm^{-3}).

145 **2.1.3 Simplified evaporation method, HYPROP**

After re-saturation, the WRC (pF -1–3.8) and HCC (pF around 1.8–3.8) were estimated using the HYPROP device. Two tensiometers were installed at 1.25 cm and 3.75 cm inside the sample and the whole setup was placed on an electronic balance connected to a computer. The sample let evaporate until air entered both tensiometers.

150 The data points on the WRC were calculated by averaging the pressure head values measured by two tensiometers and the weight loss measured by the electronic balance. Data points on the HCC were estimated by applying darcy law to the weight and tensiometer data (Peters and Durner, 2008).

2.1.4 Dew point, WP4C

Subsamples of around 3 grams were taken from the top, middle and bottom of each soil column at the end of the HYPROP experiment to cover a broad range of pressure heads between pF 4.5 and 6.5. First, the weight of the moist sample was quantified. Second, pressure head of the dry sample was measured using WP4C device. Third, the subsamples and HYPROP samples were oven dried at $105 \text{ }^\circ\text{C}$ for at least 24 hours to calculate the gravimetric water content, the total soil dry weight and bulk density. The gravimetric water content of the subsamples is finally converted to volumetric water content by using the bulk density.

2.2 SHP models and fitting strategy

160 **2.2.1 SHP models**

To evaluate our data, two SHP models were fitted. The first model is the van Genuchten-PDI model (VG-PDI) (Peters, 2013; Iden and Durner, 2014) which is given by:

$$\theta(h) = (\theta_s - \theta_r)S^{cap} + \theta_r S^{ad} \quad (7)$$



where $\theta(h)$ is the volumetric water content [$\text{cm}^3 \text{cm}^{-3}$] at pressure head h [cm], θ_s is the saturated water content [$\text{cm}^3 \text{cm}^{-3}$], θ_r is the maximum water content for the water adsorption part [$\text{cm}^3 \text{cm}^{-3}$], S^{cap} is the saturation function for the capillary part, and S^{ad} is the saturation function for the adsorptive part (Peters, 2013; Iden and Durner, 2014).

The HCC for the VG-PDI model is:

$$K(h) = K_{sat} [(1 - \omega) K_{rel}^{cap}(S^{cap}) + \omega K_{rel}^{film}(S^{cap})] \quad (8)$$

where K_{sat} is the saturated hydraulic conductivity [cm day^{-1}], K_{rel}^{cap} is the relative conductivity for the capillary part and K_{rel}^{film} is the relative conductivity for the adsorptive (film) part, and ω is a weighting factor. For more information about the model, the reader is referred to Peters (2013) and Iden and Durner (2014).

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Since the VG-PDI model couldn't fully describe the Loam 2 data, we made a slight modification by adding a macropore conductivity component in the HCC. In that case:

$$K(h)_{total} = K(h)_{mac} + K(h)_{matrix} \quad (9)$$

Where $K(h)_{total}$ is the full model, $K(h)_{mac}$ describes the macropore region as one single S-sharp:

$$K(h)_{mac} = K_{sat_{mac}} * (1 + (\alpha_{mac} * |h|)^{n_{mac}})^{m_{mac}} \quad (10)$$

where $K_{sat_{mac}}$ is the hydraulic conductivity at saturation for the macropore region, which is defined by equation (13), and α_{mac} , n_{mac} , and m_{mac} ($m_{mac} = 1 - 1/n_{mac}$) are fitting parameters that reflect the shape and steepness of the S-shape. $K(h)_{matrix}$ in equation (9) describes the matrix component of the model that fits the MSF and HYPROP data. $K(h)_{matrix}$ is described by van Genuchten-PDI following equation (8).

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$$K(h)_{matrix} = K_{sat_{matrix}} * \left((1 - \omega) K_{rel}^{cap}(S^{cap}) + \omega K_{rel}^{film}(S^{cap}) \right) \quad (11)$$

where $K_{sat_{matrix}}$ is the hydraulic conductivity at saturation for the matrix region, determined by fitting.

We note that the K_{sat} value measured with the falling head method is assumed to be equal to:

$$K_{sat}^{falling\ head} = K_{sat_{mac}} + K_{sat_{matrix}} \quad (12)$$

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2.2.2 Fitting strategy

Data for each soil and method were compiled using the LABROS SoilView analysis software (5.4.0.0), which further enabled the fitting of the WRC and HCC described in the previous paragraph. For all the fittings presented in the results section, the following weights were given to the different data groups: i) for HYPROP and WP4C data, a weight of 1 was used and for ii) KSAT and MSF data, a weight of 10 was used. The different weighting scheme was implemented to account for the higher number of HYPROP and WP4C data points relative to the MSF (and KSAT) data. For all three soils we conducted two fittings. In the first fitting (VG-PDI without MSF data) the K_{sat} was fixed to the measured value, and the MSF data were omitted from

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the objective function. In the second fitting (VG-PDI with MSF data) the K_{sat} was fixed to the measured value, and the MSF data were included in the objective function.

190 Only for the Loam 2 soil sample, we additionally fitted the model described by equations (9)-(12). First, we fitted the VG-PDI model to the HYPROP, MSF, and WP4C data (excluding K_{sat}). In that way, the “matrix” SHP were estimated and described by the VG-PDI model, where the hydraulic conductivity $K_{sat_{matrix}}$ where fitted. Afterwards, we calculate the $K_{sat_{mac}}$ by:

$$K_{sat_{mac}} = K_{sat}^{falling\ head} - K_{sat_{matrix}} \quad (13)$$

And applied equation (10) for the HCC, by assuming $n_{mac}=10$ [-], $\alpha_{mac}=4$ [cm^{-1}] (big pores).

3 Results and Discussion

195 3.1 Result of the repacked sand: proof of the workflow

For the repacked sand, the combination of methods provided a full data set of the WRC from approximately pF 0 to pF 6.5 and for the HCC from pF -1 (assumed to correspond to the pF for K_{sat}) to pF 2.5 (Fig. 2, left panel). The sand had a well-defined air-entry value at around pF 2 after which a steep drop of water content from 40 to 5 vol.% occurred. The calculated water retention data from the MSF were 42 vol.% at pF 0.54, 39.7 vol.% at pF 0.57, 38.6 vol.% at pF 0.59, and 28.9 vol.% at
200 pF 1.72, which were very close to the water retention estimated with HYPROP (41.1-38.6 vol.%). Differences can be explained by (i) the higher uncertainty due to tubing and the accuracy of the balance and (ii) the flow rate dependence of the SHP (Diamantopoulos and Durner, 2012; Diamantopoulos et al., 2015). In the simplified evaporation method, the samples are evaporating continuously, which is a slow but dynamic process. In the MSF, we waited for some time for the system to reach equilibrium in water flow, water content and pressure head. According to Diamantopoulos and Durner (2012), in equilibrium,
205 less water is retained by the soil at a specific pF value compared to the dynamic experiment, which can explain why the MSF data show a lower water content than the simplified evaporation data. The water contents derived by WP4C were between 1.95-0.03 vol.% and showed good agreement with the HYPROP data.

The log-transformed saturated hydraulic conductivity, $\log_{10}(K_{sat})$, for the sand was 2.83 $\log_{10}(cm\ day^{-1})$ (standard error 1.72) (Fig. 2, left lower panel). The log-transformed conductivity, $\log_{10}(K(h))$, measured with the MSF ranged from 2.91-2.80
210 $\log_{10}(cm\ day^{-1})$ for the pF range of 0.5 to 1.9. The HYPROP $\log_{10}(K(h))$ data for the sand were in the range -1.08-(-4.11) $\log_{10}(cm\ day^{-1})$ at pF 2-2.5.

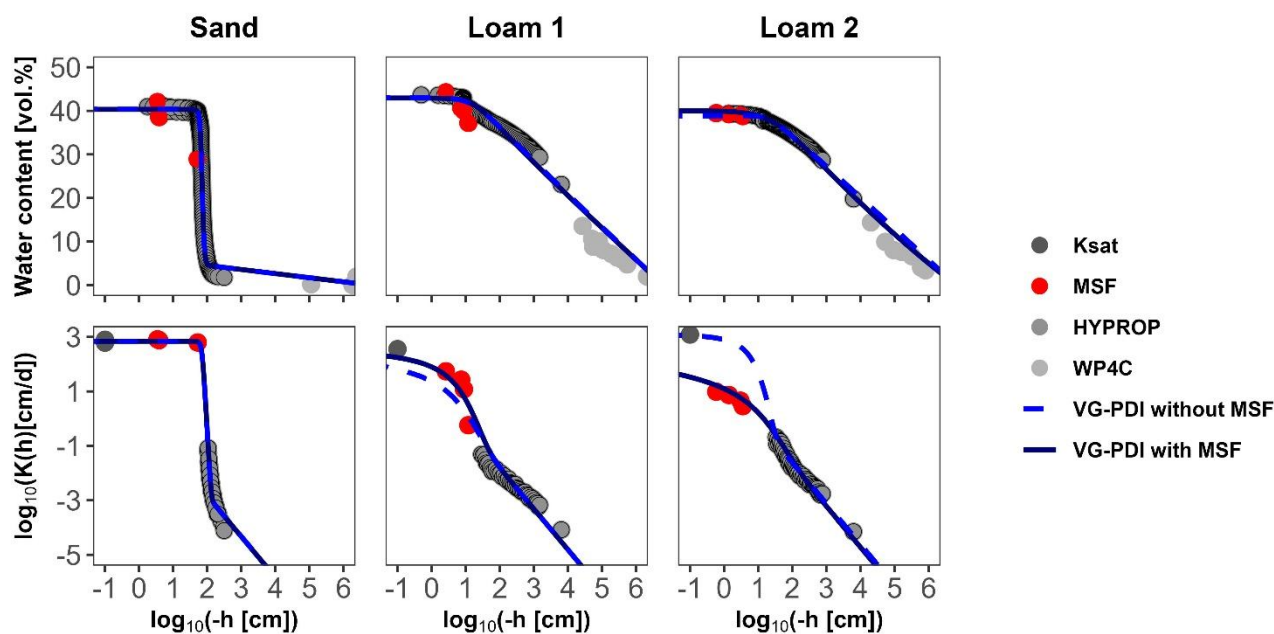
Overall, the agreement of hydraulic conductivity data and the water retention data measured with the KSAT, the MSF, and the HYPROP device (Fig. 2 lower panel) was excellent, indicating good consistency between methods and confirming the reliability of the measurements across the investigated pressure head range. This is particularly important because this
215 combination of methods has the potential to characterize near-saturation unsaturated hydraulic conductivity, which is currently not captured by state-of-the-art methods (Hohenbrink et al., 2023) and pedotransfer functions (Weber et al., 2024).



3.2 Result of the undisturbed loams; the workflows ability to measure structural effects in SHP

It has been suggested that soil structure affects the SHP near saturation (Bonetti et al., 2021). The WRC for the two loams had similar shapes, except that Loam 1 begins at a higher water content and had a small step drop in the wet range (around pF 1), whereas Loam 2 decreases more steadily (Fig. 2 upper middle and right panel). The HYPROP WRC data range for Loam 1 was 44-23 vol.%, and for Loam 2 it was 39-20 vol.%. The MSF water retention data for Loam 1 ranged from 44-37 vol.% water content, corresponding to a pF range of 0.4-1.1. Thereby the MSF captured the small step decrease at around pF 1 which was also observed in the HYPROP data, thereby increasing confidence in the reliability of the MSF. For Loam 2, the ranges were 39.5-38.8 vol.% water content and pF range of -0.2-0.6. For both loams, the MSF data displayed lower water content at the same pF values compared to the HYPROP data, as also observed for the sand. We again attributed this to differences in the dynamic and equilibrium states of the two methods. The WP4C data for Loam 1 ranged from 14-2 vol.% water content, corresponding to a pF range of 4.4-6.4, and for Loam 2, from 14.4-3.4 vol.% water content, with a pF range of 4.3-6. For both loams, the WP4C data continued from the HYPROP measurements, demonstrating good agreement between the two methods. For the Loam 1, there was a smooth transition from the $\log_{10}(K_{\text{sat}})$ measurement ($2.55 \log_{10}(\text{cm day}^{-1})$) to the $\log_{10}K(\text{h})$ MSF data ($1.74-(-0.24) \log_{10}(\text{cm day}^{-1})$) and then to the $\log_{10}K(\text{h})$ HYPROP measurements ($-3.1-(-4.08) \log_{10}(\text{cm day}^{-1})$) (Fig. 2 lower middle). For Loam 2, there was a 2 order of magnitude drop from the $\log_{10}(K_{\text{sat}})$ measurement ($3.09 \log_{10}(\text{cm day}^{-1})$) compared with the $\log_{10}K(\text{h})$ MSF data points ($0.99-0.46 \log_{10}(\text{cm day}^{-1})$). The $\log_{10}K(\text{h})$ HYPROP measurements ($-0.68-(-4.15) \log_{10}(\text{cm day}^{-1})$) smoothly continued the $\log_{10}K(\text{h})$ MSF data (Fig. 2 right panel).

Both loams had no clear air-entry. The most notable difference between the two loams was observed for the MSF data: Loam 1 conducted more water than Loam 2 at the same pF in the range near saturation (Fig. 2), indicating differences in the structural pore sizes. Loam 1 originated from a topsoil plot where the main structure-forming processes were ploughing (Schlüter et al., 2018; Munkholm et al., 2013), freeze-thaw cycles (Leuther and Schlüter, 2021), and biological activity (Meurer et al., 2020). Loam 2, in contrast, was a subsoil with no tillage, and presumably, no freeze-thaw events; its main structural-forming processes were likely earthworm and plant root activity (Zhang et al., 2018), as well as compression from the overlying layer. Therefore, we suspect that Loam 1 contains more medium-sized pores, created by tillage, compared to Loam 2. Combining knowledge of the soil's origin with the HCC data, we can conclude that the two loams have distinctly different soil structures.



245 **Figure 2: Water retention data and WRC on the top panel for the three soils. Bottom panel data of hydraulic conductivity data and HHC. For the saturated hydraulic conductivity matrix potential is not measured but set to be $-1 \log_{10}(-h[\text{cm}])$ The sand has three replicas for the KSAT and HYPROP devices.**

3.3 The model

SHP models are frequently used in soil physics and soil hydrology studies to simulate soil water dynamics with the Richards equation (Richards, 1931), with dual-permeability models (Holbak et al., 2021), to develop pedotransfer functions (Weber et al., 2024), and to calculate the equivalent pore-size distribution (Leij et al., 2002), among other applications.

250 For all samples, the WRC models provided good fits to the data. For the sand HCC, VG-PDI fits with and without MSF data agreed very well, even when the MSF data were not included in the objective function (RMSEs 0.17 and 0.18 respectively) (Fig. 2, left). Therefore, for an unstructured, repacked soil with a very well-defined air entry pressure, the combination of KSAT, HYPROP, and WP4C, measurements cover most of the SHP range and inclusion of MSF data does not necessarily improve the fit.

255 For Loam 1, both VG-PDI HCC fittings (with and without MSF data) captured the data reasonably well (RMSEs 0.38 and 0.36 respectively). However, the VG-PDI without MSF data showed a slightly poorer fit (Fig. 2, middle panel) to the MSF data, underestimating the HCC at the wet range (around pF 1), while the fits were nearly identical for the rest of the pF range. A clear difference was observed for the HCC of Loam 2 between the VG-PDI without MSF and VG-PDI with MSF data (RMSEs 0.54 and 0.23 respectively) (Fig. 2, right). The VG-PDI without the MSF data overestimated the near saturation



260 unsaturated hydraulic conductivity compared with the measured MSF data. The VG-PDI with MSF data cannot describe both
the K_{sat} at pF -1 and the MSF data. Even though the K_{sat} was fixed to the measured value, the VG-PDI model predicted an
unrealistic drop of the conductivity near saturation, something that cannot be justified physically (Ippisch et al., 2006). To
adequately describe these data, a different type of model is required to represent the behaviour mathematically. As described
in Section 2.2, this issue was addressed by adopting a model that combines an extra van Genuchten (1980) S-shaped function,
265 to describe the drop in the conductivity in the wet range (Fig. 3). Only with this approach could the full HCC range be
satisfactorily described. These results indicate that soil structure strongly affects the HCC, a feature not evident in the WRC
data. This simple extension of the van Genuchten-PDI model is not meant to be the solution for modelling these kinds of data,
but it highlights the need for a new modelling approach to represent this hydraulic behaviour because a small volume of water
contained in large pores drives the sharp decline in the hydraulic conductivity curve. Recognizing these structural effects on
270 near-saturation conductivity, and the consequent need to modify existing models, would not have been possible without
incorporating MSF measurements into the SHP workflow.

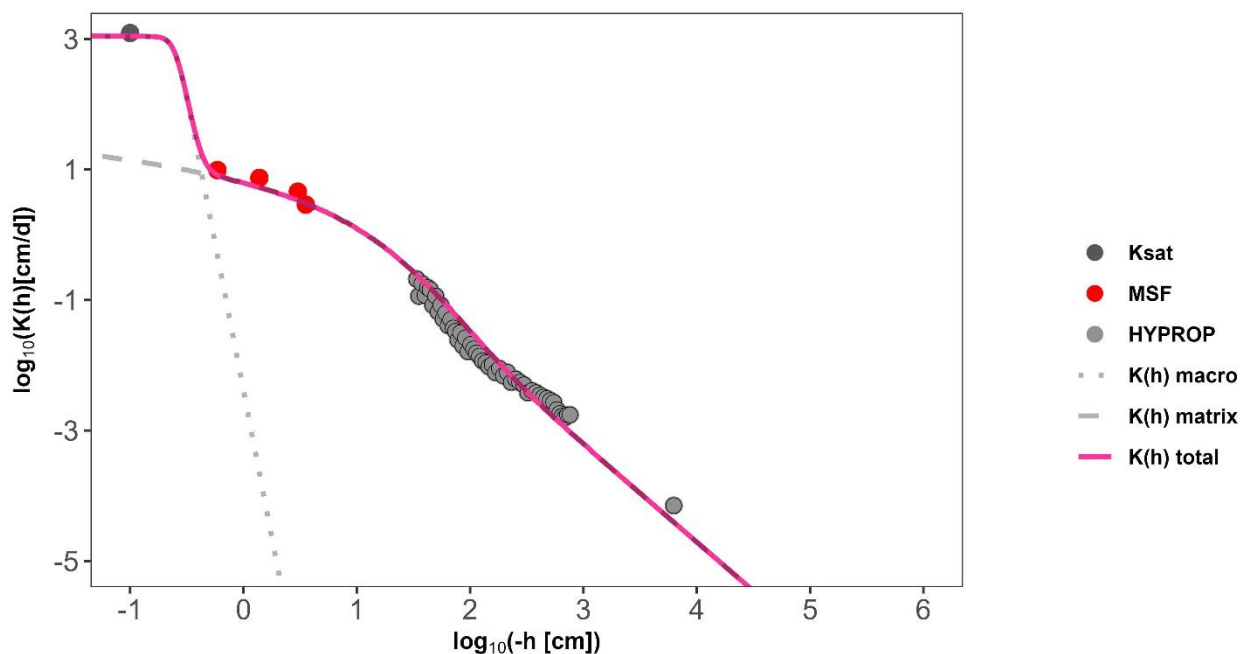


Figure 3: The modified model, $K(h)_{total}$, for HCC that can capture both the K_{sat} and the MSF for Loam 2, and the two compartments of the $K(h)_{total}$ model the $K(h)_{macro}$ and $K(h)_{matrix}$.

275 4 Conclusions

In this study, we present a workflow for measuring SHP from saturation down to pF 6.5 for the WRC and to approximately pF 3.8 for the HCC, including the critically important range between pF -1 and 1.8, which is highly dependent on soil structure. We demonstrate that the MSF is a reliable method that can be integrated with existing techniques. Our findings shows that the



280 absence of near-saturation HCC data, as measured by the MSF, can cause overestimation of hydraulic conductivity close to saturation during modelling. Furthermore, for structurally complex soils, new models may be required to adequately describe SHP mathematically. Lastly, the new protocol can be used to characterise structural pore domains like in dual-permeability model, but additional studies are needed in that direction.

Code/Data availability

285 Code and data not available.

Author contribution

Mathilde B. S. Nielsen: conceptualization, data curation, formal analysis, visualization, writing original draft and editing. Frederic Leuther: conceptualization, supervision, writing - review and editing. Efstathios Diamantopoulos: conceptualization, supervision, writing - review and editing.

290 Competing interests

The authors have no competing interests.

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