



Improved Estimation of Extreme Sea Levels via Non-asymptotic Statistical Methods for Coastal Hazard Assessment

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Abstract. Understanding the likelihood of extreme sea level events intensified by climate change is vital for effective coastal management. This study focuses on the Mediterranean and part of the European Atlantic coastline. Because sea level records are often short, non-asymptotic extreme value modeling is more accurate, as it does not depend on large-sample limiting
10 assumptions. However, selecting independent events (IEs) is critical and depends on the chosen threshold sea level (TSL) and time window width (TWW) used. Existing literature often lacks a definitive methodology for IE selection. This study aimed to fill this gap by proposing two methodologies for selecting IEs (overlapping and sorting approaches) and a methodology to find the optimal combination of TWW and TSL. The identified IEs were employed to model extreme sea level events utilizing the Peak Over Threshold-Generalized Pareto Distribution (POT-GPD) and the metastatistical extreme
15 value distribution (MEVD) approaches. A cross-validation approach, along with statistical metrics, was used to rigorously assess performance. Findings indicate that MEVD outperforms POT-GPD and is effective in estimating extreme events with longer return periods (RPs). Overall, MEVD with the overlapping method proved more effective at predicting long RP events, although MEVD with the sorting approach had comparatively lower uncertainty.

1 Introduction

20 Sea level is a critical coastal-hazard parameter that responds to a complex combination of interacting processes occurring in the atmosphere, in the ocean, and on the land surface (Ribeiro et al., 2014). In particular, extreme sea levels pose significant risks at vulnerable locations, such as low-lying coastal regions, leading to extensive damage to ecosystems as well as human communities and infrastructure (Tebaldi et al., 2021). Extreme sea levels are predominantly driven by the combination of tides and storm surges (meteorologically-induced increase in sea level), with wave setup further elevating water levels near
25 shore (Kirezci et al., 2020). Recent studies reported that coastal flooding potentially impacts approximately 700 million people in low-elevation coastal zones, where around \$ 13 trillion of global wealth is generated (Kirezci et al., 2023). With the ascending global temperatures, an acceleration in global mean sea-level rise is expected (Sithara et al., 2024), which, alone, has the potential to increase the frequency of coastal flooding, even in the absence of changes in waves and storm surges (Tebaldi et al., 2021, Favaretto et al., 2025). Additionally, changes in storminess may significantly influence the



30 frequency and magnitude of sea level extremes (Woodworth et al., 2011; Caruso and Marani, 2022). The compound effect of
these changes has indeed increased the risk of coastal flooding worldwide over the past few decades, a pattern projected to
continue as a result of climate change (Seneviratne et al., 2021). In this context, reliable estimates of extreme sea levels are
critical for informed decision-making and coastal protection (Ribeiro et al., 2014).

The widely adopted approach to estimate extreme events is the classical Extreme Value Theory (EVT). The classical EVT
35 originated in the early twentieth century and describes the probability distribution of maxima and minima of event
magnitudes within a time interval (block) of fixed duration (often taken to be one year). The classical EVT leads to a single,
summarized analytical form known as the Generalized Extreme Value (GEV) distribution (Von Mises, 1936), which
encompasses three possible limiting distributions (Fisher and Tippett, 1928; Gnedenko, 1943). This method either uses a
limited number of block maxima (BM) (Coles, 2001; Smith, 2001; Hamdi et al., 2014) or a few exceedances of large values
40 above a high threshold, termed peak over threshold (POT) (Pickands, 1975; Martins and Stedinger, 2001), to fit the GEV
distribution. The BM-GEV and POT-GEV approaches thus both refer to an asymptotic GEV block-maximum distribution,
but use different data to obtain distributional parameter estimates, i.e., just the yearly maxima or all exceedances over a high
threshold, thus producing different numerical results. This traditional EVT is the basis for a large body of literature and
applications in a wide range of disciplines, including storm surges (Hamdi et al., 2014; Vousdoukas et al., 2016), droughts
45 (Sousa et al., 2011; Potisomporn et al., 2024), hurricanes (Coles and Casson, 1998), and many more. A significant challenge
when using the traditional EVT-GEV methodology in investigating extreme sea levels is the scarcity of observations, both in
terms of quantity and quality (Bernier et al., 2024; Fouad et al., 2025). Under these circumstances, the BM-GEV approach is
critically inappropriate because it discards most of the already scarce available information and only makes use of block
(typically yearly) maxima, resulting in an inefficient use of the data (Coles and Tawn, 2005; Haigh et al., 2010). The POT-
50 GEV framework exploits information more effectively than the BM-GEV approach (Coles, 2001). However, estimation
uncertainty is highly reliant on the threshold selection. A threshold that is too high will retain only a few peak values above
the threshold, resulting in considerable error variance. On the other hand, a low threshold may select values that deviate
significantly from a GPD distribution and may contradict the independence hypothesis of the framework (Coles, 2001). The
use of a feasible intermediate threshold, e.g., in daily rainfall studies, typically leads to retaining a few events/year, thus not
55 dramatically increasing the amount of information used in the estimation.

Additionally, it may be noted that the classical EVT (BM-GEV and POT-GEV) assumes the asymptotic GEV form, without
the possibility to test for convergence. Hence, the asymptotic theory may be fitting the “wrong” distribution to the data at
hand if the actual distribution is far from its limiting form. To address these limitations of the traditional EVT, Marani and
Ignaccolo (2015) introduced the Metastatistical Extreme Value Distribution (MEVD), which does not assume an a-priori
60 asymptotic distribution, and, instead, derives the distribution of extremes directly from the finite sample of the observed
events.

Non-asymptotic methods, while presenting several advantages, require the definition of ordinary events, i.e., events in the
observational record that may be considered to be realizations of independent random variables. This is required by the basic



assumptions of both asymptotic and non-asymptotic methodologies and entails the screening of observational time series so
65 as to isolate only the values in the record that are not generated by the same physical event (e.g., the same storm).
Independent event separation has been studied for variables such as precipitation, river discharge, significant wave height,
and winds (An and Pandey, 2005; Gao et al., 2020; Agilan et al., 2021; Pan et al., 2022). In those cases, a clear identification
of periods in which no event is active is quite straightforward. The identification of independent storm surges within sea-
level records is more complex, as the total sea level value includes both tidal and surge contributions. In practice,
70 independence is ensured by defining events based on a threshold value and a minimum time separation. However, a
definitive methodology to select the appropriate threshold and time window remains elusive.
Here we study the performance of non-asymptotic (MEVD) approaches, relative to asymptotic GEV results, while
expanding the MEVD application by integrating two novel independent event (IE) selection methodologies. The analysis
rigorously uses a cross-validation method so as to be able to quantify the predictive estimation uncertainty associated with
75 different non-asymptotic/asymptotic methods and different independent event separation methodologies.
The paper is organized as follows: Sect. 2 describes the study area and data used. Sect. 3 outlines the methodology employed
in this application, and the results are elucidated in Sect. 4. In Sect. 5, conclusions are drawn.

2 Study Area and Data

This study focused on coastal regions in the Mediterranean Sea and in the Atlantic Ocean in Southern Europe (Fig. 1).
80 Hourly sea level observations from 29 tidal gauges along the coastline of the Mediterranean Sea and 10 tidal gauges along
the coastline of Atlantic Ocean in Southern Europe were utilized for the analysis (Table 1).

The Mediterranean basin undergoes substantial anthropogenic pressure, with an approximate population of 160 million on its
coastlines (UNEP/MAP, 2020; Toomey et al., 2025). Mediterranean coastlines are one of the most popular tourist
destinations in the world. The irreplaceable cultural heritage sites attract one-third of international tourism flows. It also
85 exhibits some of the world's busiest shipping routes (MedECC, 2020; Ali et al., 2022). Extensive infrastructures have been
built in close proximity to the Mediterranean coasts due to the minimal tidal variation. The Mediterranean Sea is a global hot
spot for climate change, with an above-average projected increase in temperatures (Toomey et al., 2025). Moreover, sea
level changes are highly variable in space and time in the Mediterranean Sea. Satellite altimetry observations indicated a
mean increase of 2.6 ± 0.2 mm/year in absolute (geocentric) sea level across the Mediterranean Sea over 1993–2015 (Ibáñez
90 and Caiola, 2021). The Mediterranean basin experiences the highest rates of cyclogenesis globally. Hence, coastlines are
highly exposed to extreme sea level events driven by climate change (Toomey et al., 2022), exacerbating coastal hazards
such as flooding, shoreline retreat, and saltwater intrusion, posing a significant threat to heavily populated cities and vital
infrastructure systems. Given the high population density and economic significance of the Mediterranean coasts, it is
essential to understand the likelihood of extreme sea level events.



95 The Atlantic coastline in Southern Europe is home to hundreds of thousands of people, with several high-value economic activities and extensive infrastructures that must be adapted to intensifying natural coastal hazards (Antunes et al., 2019).

There is considerable variability in observed extremes, with values in the Atlantic exceeding 250 cm above datum, while those in the Mediterranean are on average around 50–60 cm, with high values of the order of 150–160 cm in numerous locations (e.g., Venice). Moving from the Bay of Biscay to Portugal and the southern coasts of Spain, the maximum
100 observed values decrease by almost a meter. This spatial distribution is primarily driven by the tides (Tsimplis and Shaw, 2010). Moreover, the Atlantic coast is highly vulnerable to marine flood hazard (Breilh et al., 2014).

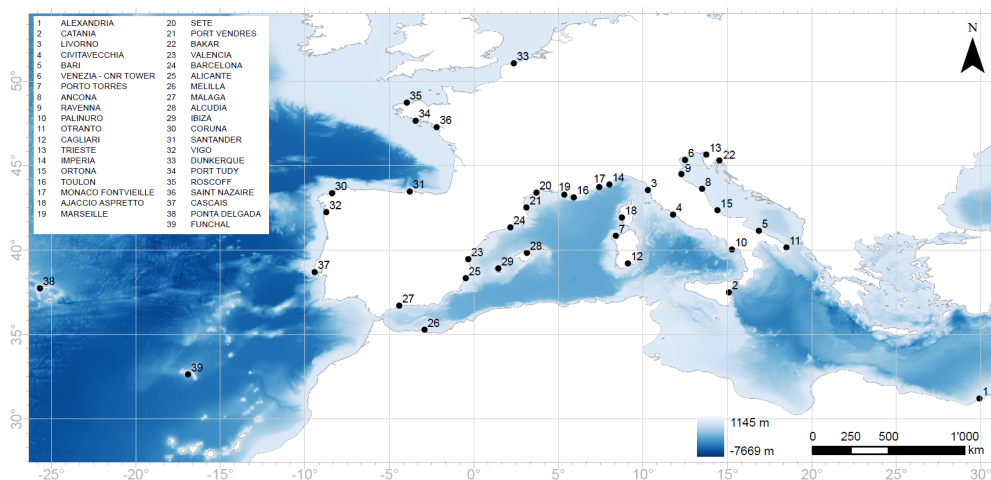


Figure 1: Tidal gauge locations (the bathymetry source: GEBCO 2025 Grid)

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Table 1: Details of tidal gauge stations

Station number	Station Name	Data availability	Country	Source
1	Alexandria	1958 – 1976	EGY	Global Extreme Sea Level Analysis (GESLA)
2	Catania	1999 – 2024	ITA	Istituto Superiore per la Protezione e la Ricerca Ambientale (ISPRA)
3	Livorno	1999 – 2024	ITA	ISPRA
4	Civitavecchia	1999 – 2024	ITA	ISPRA
5	Bari	1999 – 2024	ITA	ISPRA
6	Venezia - CNR Tower	1983 – 2023	ITA	Consiglio Nazionale delle Ricerche (CNR)
7	Porto Torres	2000 – 2024	ITA	ISPRA
8	Ancona	1999 – 2024	ITA	ISPRA
9	Ravenna	1999 – 2024	ITA	ISPRA
10	Palinuro	1999 – 2024	ITA	ISPRA
11	Otranto	2001 – 2024	ITA	ISPRA
12	Cagliari	1999 – 2024	ITA	ISPRA
13	Trieste	1905 – 2022	ITA	ISPRA
14	Imperia	1999 – 2024	ITA	ISPRA
15	Ortona	1999 – 2024	ITA	ISPRA
16	Toulon	1993 – 2024	FRA	Réseaux de Référence des Observations Marégraphiques (REFMAR)
17	Monaco Fontvieille	1999 – 2024	FRA	REFMAR
18	Ajaccio Aspretto	2002 – 2024	FRA	REFMAR
19	Marseille	1999 – 2024	FRA	REFMAR
20	Sete	2008 – 2024	FRA	REFMAR
21	Port Vendres	2008 – 2024	FRA	REFMAR
22	Bakar	1950 – 2021	HRV	Međugorac, I., Pasarić, M., & Orlić, M. (2021). Historical sea-level measurements at Bakar (east Adriatic).
23	Valencia	1993 – 2024	ESP	Puertos del Estado
24	Barcelona	1993 – 2024	ESP	Puertos del Estado
25	Alicante	1957 – 2018	ESP	Puertos del Estado
26	Melilla	2008 – 2024	ESP	Puertos del Estado
27	Malaga	1993 – 2024	ESP	Puertos del Estado
28	Alcudia	2010 -2024	ESP	Puertos del Estado
29	Ibiza	2003 – 2024	ESP	Puertos del Estado
30	Coruna	1992 – 2025	ESP	Puertos del Estado
31	Santander	1992 – 2025	ESP	Puertos del Estado
32	Vigo	1993 – 2025	ESP	Puertos del Estado
33	Dunkerque	1997 – 2025	FRA	REFMAR
34	Port Tudy	1977 – 2025	FRA	REFMAR
35	Roscoff	1979 – 2025	FRA	REFMAR
36	Saint Nazaire	1984 – 2025	FRA	REFMAR
37	Cascais	1971 – 2005	PRT	University of Hawaii Sea Level Center (UHSLC)
38	Ponta Delgada	1996 – 2018	PRT	UHSLC
39	Funchal	1986 – 2013	PRT	UHSLC



115 3 Methodology

3.1 Trend removal

Sea level includes contributions from a deterministic astronomical tidal component, a stochastic meteorological surge, and a long-term trend in mean sea level. The latter introduces a non-stationary component that must be removed prior to performing an extreme value analysis. In this study, the total sea level arising from the combined effects of astronomical and meteorological contributions was considered for all analyses, assuming the storm climate to be stationary over the period of record. From a statistical point of view, tides and surges could be analyzed separately. However, adding them back to obtain the total sea level requires assumptions regarding their independence, and the final result is affected by the accuracy with which the separation of these components could be obtained. Hence, attempts to separate the two signals are not without consequences for the subsequent analyses. In this study, we chose not to separate tidal and surge components, implicitly including tide–surge interactions and treating their sum as a single random variable. According to this approach, the observed total sea level $l(t)$ at any instant of time t can be represented as (Caruso and Marani, 2022):

$$l(t) = MSL(t) + a(t) + m(t) \quad (1)$$

where $MSL(t)$ is the mean sea-level measured with respect to an arbitrary datum, $a(t)$ is the astronomical tide and $m(t)$ is the storm surge, both measured with respect to the mean sea-level at time t .

$MSL(t)$ changes because of long-term fluctuations in global sea levels, due to water volume changes, and to possible changes in datum elevation, e.g., if this is chosen to coincide with the soil surface, as a result of possible land uplift or subsidence. The tidal contribution, $a(t)$, caused by astronomical factors and by coastal morphology, contains periodic components with periods from 6 hours to 18.61 years, the lunar nodal cycle (Valle-Levinson et al., 2023). The contribution of storm surge $m(t)$ is associated with the spatial distribution of atmospheric pressure and with wind direction and speed (Conte and Lionello, 2014; Bajo et al., 2023).

The sum of the tidal and surge components, subsequent to the subtraction of the mean sea-level constitutes the detrended sea level, $s(t)$:

$$s(t) = l(t) - MSL(t) \quad (2)$$

Because sea level records at numerous tidal gauge stations were short, the detrended sea level here is obtained by simply removing a linear trend computed from the entire observed time series. After removing this long-term trend in the sea level observations, it is possible to study storm surge event magnitude as a random variable, even in the presence of the deterministic tidal element, as its phase with the storm contribution is itself random. The detrended sea level data were further processed to eliminate (i) years with less than 6 months of sea level observations, and (ii) measurement errors, i.e., the observations during periods that are not coherent with the regime of the remaining time series.



145 **3.2 Extreme value theory**

3.2.1 Asymptotic Extreme Value Theory

The standard extreme value theory (EVT) studies the distribution of maxima from data. Let us consider T independent and identically distributed (IID) random variables, X_1, X_2, \dots, X_T , with a common distribution, the "ordinary value" distribution $F(x)$ (here, an upper-case letter refers to the random variable, and a lower-case letter indicates the value of the random variable). We next divide the sample into non-overlapping blocks of equal size n and, for each block, we study $Y = \max(X_1, \dots, X_n)$, the block maximum. The cumulative distribution function of block maxima can be expressed as, $P(Y \leq x) = F(x)^n$.

Under certain circumstances, there exist scaling constants $a_n > 0$ and b_n such that the normalized maximum converges to a nondegenerate distribution $H(y)$ (Smith, 2001). In other words, after rescaling, the maximum of a large sample can have a stable limiting distribution. The convergence occurs only when very large values become rarer at a specific rate as the sample size increases.

As the block size becomes infinitely large, the distribution of block maxima converges to one of three types of extreme value distributions according to the three-type theorem (Fisher and Tippett, 1928; Gnedenko, 1943): Gumbel, Fréchet, or inverse Weibull distributions. These distributions can all be represented within a single framework using the generalized extreme value (GEV) distribution, as parameterized by Jenkinson (1955), and described in detail by Coles (2001).

$$H(y; \mu, \sigma, \xi) = \exp \left\{ - \left[1 + \xi \left(\frac{y - \mu}{\sigma} \right) \right]^{\frac{-1}{\xi}} \right\} \quad (3)$$

where, $\{y: 1 + \xi(y - \mu)/\sigma > 0\}$, $\mu \in (-\infty, \infty)$ is the location parameter, $\sigma > 0$ is a scale parameter, and $\xi \in (-\infty, \infty)$ is the shape parameter. The case $\xi > 0$ represents a tail described by power-law (fat-tailed). The case $\xi = 0$ corresponds to an exponentially decreasing tail (light-tailed), while $\xi < 0$ is the case of a finite upper endpoint (short-tailed) (Batt et al., 2017; Smirlis et al., 2025). In practice, the GEV distribution is commonly fitted using the block maxima approach (BM-GEV). The BM-GEV approach is fitted to the yearly maxima extracted from the data series (Smith, 1989). An alternative to BM is the peaks over threshold (POT-GEV), focuses on exceedances over high thresholds instead of maxima over predetermined time periods (Smith, 1989; Caruso and Marani, 2022).

Suppose the exceedances, or differences between the observations over the threshold (u) and the threshold itself, are independent with a common distribution function F . For a sufficiently large threshold (upper endpoint), the distribution F of the exceedances $((Z - u)|Z > u)$ converges to the Generalized Pareto Distribution (GPD) given by (Davison and Smith, 1990)

$$G(y; \sigma, \xi) = 1 - \left(1 + \xi \frac{y}{\sigma} \right)^{\frac{-1}{\xi}} \quad (4)$$

where $\sigma > 0$ and ξ is arbitrary; the range of y is $0 < y < \infty$ if $\xi \leq 0$, $0 < y < \frac{\sigma}{\xi}$ if $\xi > 0$. For sufficiently high u , there is some σ_u (depends on u) and some ξ for which the GPD is an excellent approximation to the exceedances distribution



function F_u . Pickands (1975) already demonstrated this connection, and in that case, ξ in Eq. (4) is the same as that of the corresponding GEV distribution. Similar to GEV, there are three different cases based on the sign of ξ (Smith, 2001):

- (i) If $\xi > 0$, Eq. (4) is valid for $0 < z < \infty$ and the tail distribution function satisfies $1 - G(y; \sigma, \xi) \sim cy^{-1/\xi}$ with $c > 0$, which is a traditional Pareto Tail.
- 180 (ii) If $\xi < 0$, the G has an upper endpoint at $w_G = \sigma/|\xi|$, which corresponds to the inverse Weibull type of GEV.
- (iii) If $\xi = 0$, then $G(y; \sigma, 0) = 1 - \exp\left(-\frac{y}{\sigma}\right)$, which is the exponential distribution with mean σ leading to a Gumbel distribution in the GEV framework.

For a fixed u , if the number of exceedances is assumed to be a random variable, it can be modeled by leveraging the Poisson property of the exceedances, resulting in a model called the Poisson-GPD model. If the number (N) of exceedances above u in any one year has a Poisson distribution with mean λ , such that $N \geq 1$, the exceedances Y_1, Y_2, \dots, Y_N are IID from the GPD (Eq. (4)). The probability that the annual maxima of the process less than a specified value z is:

$$Pr\{\max_{1 \leq i \leq N} Y_i \leq z\} = \exp\left\{-\lambda \left(1 + \xi \frac{z-u}{\sigma}\right)^{-1/\xi}\right\} \quad (5)$$

Eq. (5) is the same as Eq. (3), if $\sigma = \psi + \xi(u - \mu)$, and $\lambda = \left(1 + \xi \frac{u-\mu}{\psi}\right)^{-1/\xi}$.

Here we used this approach, which is often termed POT-GPD, and, hereinafter, this terminology is used in this paper.

190 3.2.2 Non-asymptotic Extreme Value Theory

The MEVD approach developed by Marani and Ignaccolo (2015) relaxes the specific hypotheses under which the BM-GEV and POT-GEV approaches are derived and considers the parameters defining the cumulative distribution function of ordinary events as well as the number of ordinary events in a block as stochastic (Marani and Ignaccolo, 2015). Thus, the cumulative distribution of block maxima for the MEVD is defined as:

$$195 \quad Q(x) = \sum_{n=1}^{\infty} \int_{\Omega_{\theta}} F(x; \theta)^n q(n, \theta) d\theta \quad (6)$$

where $q(n, \theta)$ is the joint probability distribution of event occurrences within a specified block and of the parameter vector, which is discrete in N and continuous in θ ; and Ω_{θ} is the population encompassing all possible values of parameters.

For practical applications, the theoretical MEVD can be approximated by replacing the ensemble average in Eq. (6) with the sample average calculated over all the blocks in the time series. Furthermore, in this study, the MEVD was approximated by using the same parameters for the blocks while allowing n to vary in each block. Hence, the MEVD formulation adopted here can be expressed as

$$200 \quad Q(x) \cong \frac{1}{M} \sum_{j=1}^M F(x; \theta)^{n_j} \quad (7)$$



where M is the number of blocks in the historical record and n_j is the number of events observed in the j^{th} block. $F(x; \theta)$ is the cumulative distribution of ordinary event magnitudes, which is independent of a division in blocks: the entire calibration dataset here was used to estimate the parameters. As discussed by (Zorretto et al., 2016), in case one considers (i) x as the exceedance over a high threshold, (ii) $F(x; \theta_j)$ as GPD with fixed deterministic parameters, and (iii) n follows a Poisson distribution, then the GEV distribution can be derived as a particular case of the MEVD distribution.

Unlike the traditional asymptotic EVT, the MEVD approach is non-asymptotic and can leverage most of the available data to estimate the distribution parameters. The use of a large proportion of observations afforded by the MEVD reduces the estimation uncertainty, particularly in the estimation of high quantiles, in comparison to the classical asymptotic EVT approaches (Caruso and Marani, 2022, Boumis et al., 2024). However, the MEVD formulation additionally requires prior understanding of the probability distribution that describes the underlying ordinary events.

The non-asymptotic MEVD adopted here uses a GPD for describing the ordinary event distribution, $F(x; \theta)$, following results from existing cross-validation analyses (Caruso and Marani, 2022). The ordinary-event GPD distribution parameters were estimated using the Probability Weighted Moments (PWMs) method (Greenwood et al., 1979). The PWMs approach is widely applied due to its reduced estimation bias and sensitivity to outliers in the data (Hosking, 1990).

3.3 Return Period

The primary purpose of the extreme value analysis is to determine the average recurrence interval or Return Period (RP) of specific event magnitudes. For a stationary process, the RP of a specific magnitude event is the average time between two consecutive exceedances of that magnitude. If the annual maximum magnitude s is surpassed, on average, once every RP years, the exceedance probability $E(s) = 1 - Q(s)$, in any given year is $E(s) = P[S \geq s] = 1/RP(s)$. Consequently, the RP associated with a sea level value s is the reciprocal of the probability of exceedance and can be represented as a function of the cumulative distribution $Q(s)$ of yearly maxima. For the case of MEVD, RP can be expressed as: $RP(s) = 1/E(s) = 1/1 - Q(s)$

For a specific value of MSL , there exists a one-to-one association between the aggregate of astronomical and storm surge contributions and the consequent total sea level ($l = s + MSL$). Hence, it follows that $Q_s(s) = P[S > s] = P[S > l - MSL] = P[L - MSL > l - MSL] = P[L > l] = Q_l(s)$. This implies that, once the cumulative distribution is known, the RP for the total sea level ($RP(l)$) is:

$$RP(l) = \frac{1}{1 - Q_l(s)} = \frac{1}{1 - Q_s(s)} = \frac{1}{1 - Q(l - MSL)} \quad (8)$$

3.4 Selection of independent sea level events

Independence of exceedances and the ordinary events is a basic requirement for the POT-GPD and MEVD approaches, respectively. The conventional approach used to ensure independence is a declustering process. In the case of POT-GPD, the procedure often involves choosing a sufficiently high threshold, and, if there are clusters of exceedances, it is treated as a



single event with the maximum in the cluster as the representative. Threshold selection entails a trade-off between bias and
235 variance; lower thresholds may introduce bias, while higher thresholds increase variance due to fewer instances of
exceedance (Smith, 2001; Caruso and Marani, 2022). The original formulation of the MEVD, developed with application to
daily rainfall, defined ordinary events based on a low threshold to isolate events generated by the same physical processes.
Independence is in that context either an acceptable hypothesis for the original process (e.g., in the case of daily rainfall) or
ensured using declustering approaches (Marra et al., 2018; Miniussi and Marani, 2020; Caruso and Marani, 2022).

240 In the present study, declustering was performed to identify independent events (IEs), which is based on site-specific
characteristics, viz., threshold sea level (TSL) and time window width (TWW). The TSL choice depends on the magnitude
of the local tidal range as well as storm contributions. The threshold is also selected to be sufficiently high to filter out water
level peaks that are entirely influenced by tidal fluctuations, in the absence of any storm contribution (Caruso and Marani,
2022). Traditionally, the optimal choice of TSL is identified via goodness-of-fit measures (Davison and Smith, 1990) or
245 mean excess plots (Smith, 2001), whereas a methodology for determining the optimal TWW remains elusive. Some studies
concerning storm surge adopted a TWW between 24 and 72 hours (Haigh et al., 2010; Bernardara et al., 2014; Cid et al.,
2016).

The present study explored two new declustering approaches for selecting IEs based on appropriate TSL and TWW. First, all
the down-crossings, i.e., intersections between the TSL and the detrended sea level line when the latter is characterized by a
250 negative derivative. Two subsequent down-crossing points define a temporal interval over which the hourly sea levels are
above a specific threshold. The maximum sea level observed within this interval is defined as an event (blue points in Fig. 2a
and 2b). The range of TSL values experimented with was set between the 90th percentile and 1.25 times the 99th percentile
(to account for very high TSLs), further subdivided into equally spaced intervals, with a minimum width of 0.02 m.

Independence was then ensured by specifying an appropriate time window width (TWW) between successive events,
255 yielding independent events (red points in Fig. 2a and 2b). The TWW values were adopted so that they spanned from 2 to 10
days across all tide gauges. A TWW of 6 days signifies 3 days prior to and 3 days after the event. The tidal regimes in the
Mediterranean Sea and Atlantic Ocean are predominantly diurnal and semidiurnal, respectively, and some regions within
these bodies of water exhibit a mixed tidal pattern. Consequently, the minimum TWW chosen was 2 days (across all
stations), which is greater than the tidal cycle. An upper limit of 10 days was chosen, considering the range of the longest
260 wind storm events (Besio et al., 2017; Amarouche et al., 2022; Borzi et al., 2024).

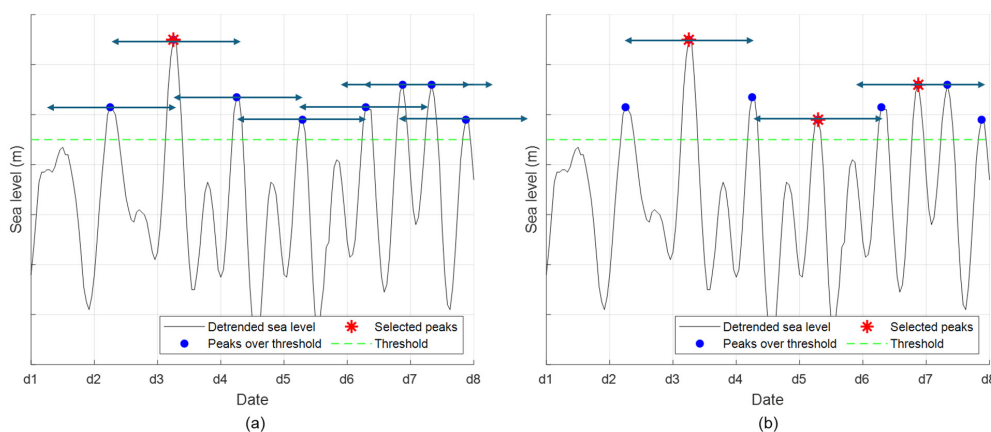
After extracting the events based on the TSLs, two different methodologies were applied employing the TWWs to ensure
independence: overlapping time window and sorting methods, as described below. Employing both methods, IEs were
extracted for each TSL-TWW combination across all gauge stations. Here, the number of independent events selected for a
specific combination of TSL and TWW is the same for both POT-GPD and MEVD: unlike in other studies and applications
265 of non-asymptotic methods, differences on the results of the different extreme value methods do not depend on a difference
in the amount of data that is utilized in the asymptotic vs the non-asymptotic approach. The differences only depend on the
different formulations and assumptions underlying the two approaches.



The optimal TSL and TWW for each station for each extreme value model were identified via a cross-validation procedure, as explained in Sec. 3.5.1.

270 3.4.1 Overlapping time window method

The TWW is centered over each of the events, and wherever there is an overlap between the TWW of adjacent events, these events are merged into one (as seen in Fig. 2a). Among the merged events, the highest one (and the corresponding time) is extracted as representative (red asterisk in Fig. 2a). This process is carried out using an image processing algorithm named morphological dilation, utilizing a linear structuring element with a width proportional to the defined TWW.



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Figure 2: Selection of independent sea level events using (a) overlapping time window approach and (b) sorting approach. The green dashed lines represent the TSL, whereas the ↔ symbols depict the TWW.

3.4.2 Sorting method

The events extracted based on TSL are sorted in descending order of magnitude. Starting from the highest available event, all other events within the specified TWW from that event are excluded from the sorted list (Fig. 2b). For example, with a TWW of 6 days, once the first event in the sorted list is selected, events occurring three days prior to and three days following this event are eliminated. One then moves on to the next available event, the procedure was repeated, ultimately resulting in a set of IEs.

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3.5 Optimal TSL and TWW selection and model performance evaluation through cross-validation

Accuracy assessment is critical to select and test a methodology. A common approach is to use goodness-of-fit metrics to compare the performance of various candidate distributions in describing observed samples (e.g., Chowdhury et al., 1991; Serinaldi and Kilsby, 2014; Krit et al., 2021). However, these goodness-of-fit metrics are not capable of indicating the



accuracy with which the return period of an unseen extreme event can be estimated. In contrast, cross-validation approaches can provide out-of-sample estimates of uncertainty that more accurately characterize predictive uncertainty (Miniussi and Marani, 2020).

Here, we used a cross-validation procedure to (i) select the optimal TSL and TWW and (ii) evaluate the performance of the MEVD and POT-GPD approaches, particularly for high-quantile estimation. The cross-validation procedure involves a comparison of the probability of occurrence of the events predicted using the statistical models with the frequencies derived from observed data that are not used for model parameter estimation. This cross-validation was performed by dividing the available data into two subsets: calibration (sample used to estimate model parameters) and test data (used for comparison of model predictions with observations). As the key focus of this work is to confirm the reliability of the proposed framework for yielding accurate results with short sea level records, we used a very short calibration sample size. Here, the calibration sample size was fixed at 4 years since it is the smallest RP that was able to compute for all the stations used in this study. The procedure can be summarized as follows:

- i. The observational years in the record were randomly reshuffled while retaining all independent sea-level events within their original year of occurrence. This approach allows for the preservation of both the ordinary value frequency distribution for each year and the distribution of the number of events per year, while removing potential correlations within the time series.
- ii. The observational sample was divided into two independent sub-samples by randomly selecting S years from the original record of length M , designated as the “calibration sample,” which was utilized for parameter estimation. The remaining data, comprising $V = M - S$ years, is referred to as the “test sample,” and was employed for testing.
- iii. The empirical cumulative frequencies were computed using the Weibull plotting position formula $F_k = k/(V + 1)$, where $k = 1, \dots, M$ is the rank of the value x_k in an ascending order in a list of the annual maxima from the test sample. The return period (RP) associated with each yearly maximum is given by $RP_k = 1/(1 - F_k)$.
- iv. The MEVD and GPD quantiles were estimated using the parameters obtained from the calibration sample.
- v. The cross-validation scheme was repeated 1000 times to obtain a complete statistical description of the error metric.

3.5.1 Selection of optimal TSL and TWW

A specific Root Mean Square Error (RMSE*) was computed using all quantile estimates in the test sample with $RP \leq$ size of the calibration sample (here, 4 years) during cross-validation. The optimal TSL-TWW combination to define the IEs was identified as the configuration that yielded the lowest RMSE*. The evaluation of RMSE* using shorter RP events was made because the study's primary goal is to assess the utility of the proposed methodology in data-scarce situations. In other words, whether reliable outputs can be achieved when the observational record is very short. This procedure allows us to determine whether the optimal TSL-TWW combination, chosen based on RMSE* computed from quantiles with short RPs, can effectively be applied to estimate high quantiles. Here, for all the stations, the optimal combination of TSL and TWW



was identified for POT-GPD and MEVD approaches integrated with two IE selection methodologies, yielding four distinct cases. These optimal TSLs and TWWs were used for the final modeling of extreme sea level events.

3.5.2 Model performance evaluation

The performance of the POT-GPD and MEVD methods was compared by evaluating RMSE and Nash Sutcliffe Efficiency (NSE) (Nash and Sutcliffe, 1970) across all quantiles in the test sample during the cross-validation process. Additionally, a Quantile Ratio (QR) was computed on the highest quantiles in the test sample to understand the estimation uncertainty with regard to predicting longer RP events (Eq. (9)).

$$QR = \frac{q_{predicted}}{q_{observed}} \quad (9)$$

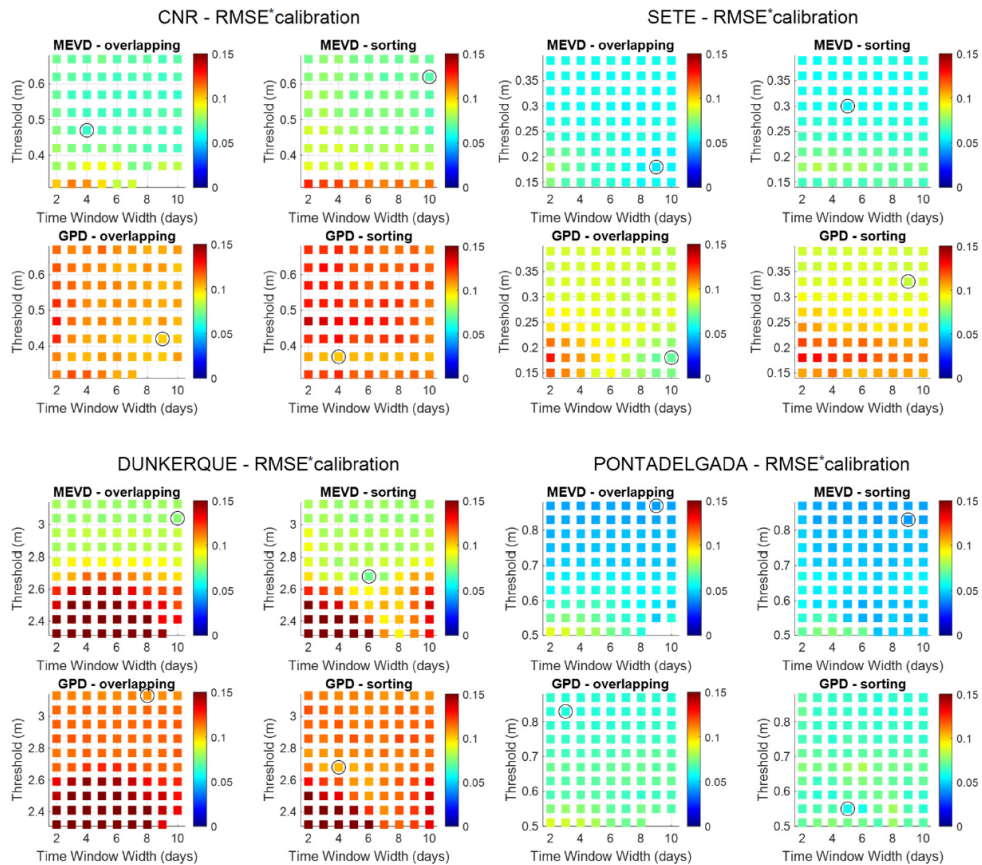
4 Results and Discussion

The independent sea level events identified for different combinations of thresholds and time window width employing the overlapping and sorting approach, which were subsequently used as input to the POT-GPD and MEVD approaches. The analysis encompasses four primary methodological approaches: (i) MEVD utilizing the overlapping time window method for the selection of independent events (MEVD-overlapping), (ii) MEVD employing the sorting method for independent event selection (MEVD-sorting), (iii) POT-GPD with the overlapping time window method (POT-GPD-overlapping), and (iv) POT-GPD utilizing the sorting method for independent event selection (POT-GPD-sorting). The results of the cross-validation procedure used to select the best TSL-TWW combination and to evaluate model performance are described below.

Among the 39 stations, results of four stations are presented here to describe the application in detail. The four selected stations are Venice-CNR, Sete, Dunkerque, and Ponta Delgada. Figure 3 depicts the best TSL-TWW combinations selected for these stations. Notably, certain combinations were excluded from evaluation for the Venice-CNR, Dunkerque, and Ponta Delgada stations due to the scarcity of annual maxima when employing the overlapping time window approach, as it was impossible to compute the maximum observed RP. As seen in the figures, for the Sete and Dunkerque stations, it is evident that the TSL and TWW selected for both the MEVD-overlapping and the POT-GPD-overlapping methodologies are quite close. Likewise, the optimal TSL and TWW values determined for the MEVD-sorting and POT-GPD-sorting approaches are similar. In contrast, the chosen TSL and TWW values for the other two stations (Venice-CNR and Ponta Delgada) differ across methodologies. These findings indicate that suitable TSLs and TWWs exhibit variability across different stations and methodologies, underscoring the necessity for careful consideration of local conditions when determining optimal parameters for extreme value analysis. This study found that in some cases MEVD approaches selected a higher TSL than those of POT-GPD approaches. Furthermore, it was interesting to note in the study carried out by (Caruso and Marani, 2022) that the TSL values used for the MEVD approach were not markedly smaller than those used for the POT-GPD method. In



fact, the difference between the thresholds was ~6-10 cm. Therefore, choosing a lower TSL and TWW may not invariably define the ordinary events appropriately.

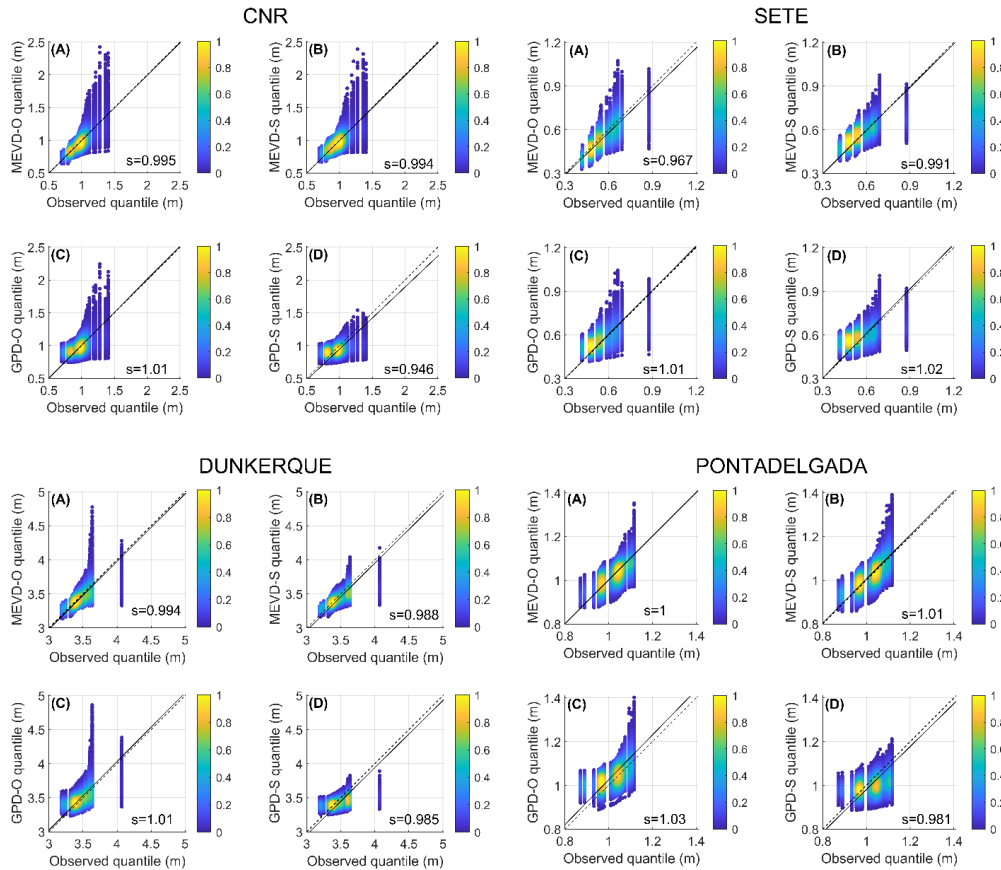


355 **Figure 3: Heat maps indicating the best TSL-TWW combination based on the RMSE* computed on all quantiles in the test sample with return periods less than or equal to 4 years during cross-validation.**

The performance of the models with regard to extreme sea level was assessed graphically and using statistical metrics. Figure 4 shows the Q-Q plots of the extreme sea level events based on the optimal TSL-TWW across methods for the Venice-CNR, Sete, Dunkerque, and Ponta Delgada stations, as an example. Quantiles predicted by the MEVD approach match well with observed ones, as evidenced by a good alignment along the 1:1 line in the QQ plots. This alignment seems 360 to be tighter for MEVD predictions than for observed POT-GPD-predicted quantiles, both for high and low values of



extreme surges (Fig. 4, panels C and D). Similar results were observed for other stations. For 33 out of 39 stations, the slope of the best-fit line of the predicted quantiles is closer to 1 with MEVD methods than with POT approaches.



365 **Figure 4: Q-Q plots of all sea level quantiles computed for the best combination of TSL and TWWs selected for each method. The plot shows the slope (s) of the best-fit line (solid black line) of the quantiles and the 1:1 line (dashed black line).**

Further analysis was conducted to enhance the understanding of the variability in TSLs and TWWs. Figure 5 illustrates the violin plots displaying the variation of the Quantile Ratio (QR) evaluated for the highest quantile in a cross-validation experiment, across different methods for various TSLs while maintaining a fixed TWW of 4, 9, 6, and 3 days for the stations Venice-CNR, Sete, Dunkerque, and Ponta Delgada, respectively. QR values vary significantly as a function of the thresholds, underscoring the critical role of threshold selection in extreme value analysis. QR values for the highest quantile show a large variation as a function of TWW (Fig. 6). At some sites, e.g., Dunkerque, there is significant variation in QR



across the methods. Overall, the results show that the choice of TWW is important. However, the model's predictions are less influenced by TWW compared to TSL.

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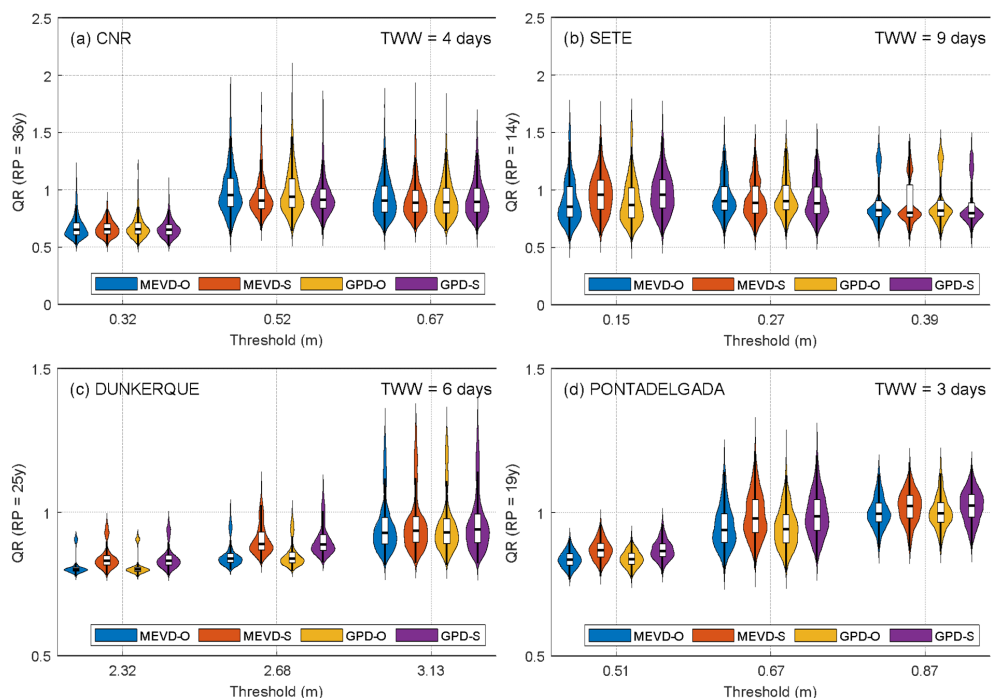
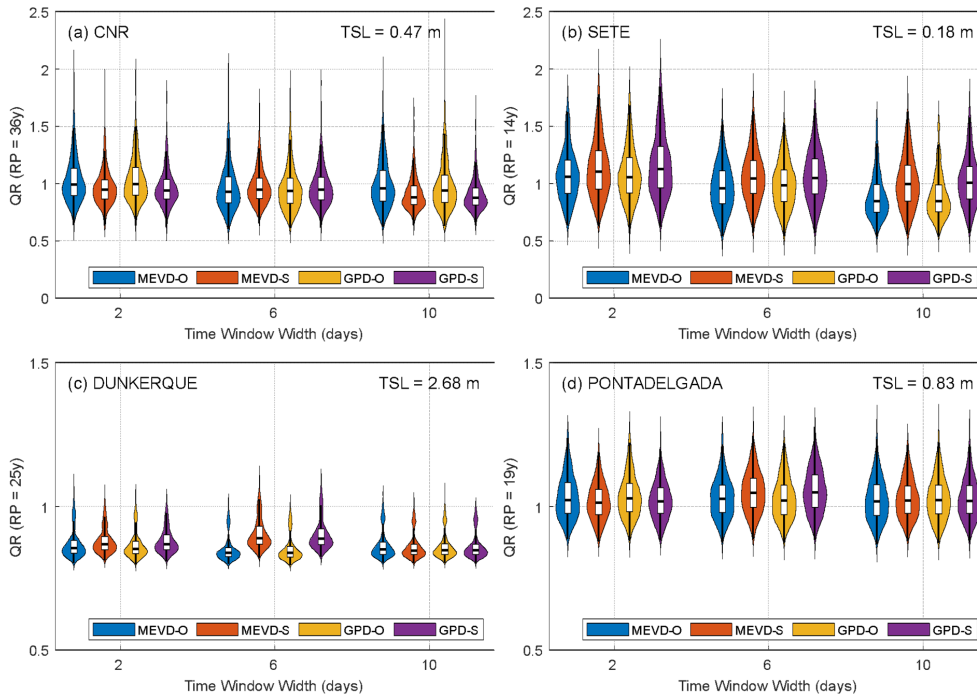


Figure 5: Violin plots showing variation of QR computed on the highest quantiles during the cross-validation for a fixed TWW for the stations (a) Venice-CNR and (b) Sete (c) Dunkerque (d) Ponta Delgada.



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Figure 6: Violin plots showing variation of QR computed on the highest quantiles during the cross-validation for a fixed TSL for the stations (a) Venice-CNR and (b) Sete (c) Dunkerque (d) Ponta Delgada.

The performance of the four methods was also evaluated based on the QR computed on the highest quantiles as well as RMSE and NSE computed on all quantiles for all the stations. All the metrics were evaluated using the results obtained for the optimal TSL-TWW combination across stations. As seen in Figs. 7 and 8, the MEVD approaches outperform POT-GPD approaches across all stations in terms of RMSE and NSE. No negative values of NSE, which correspond to highly erroneous predictions, were found for MEVD. Analogously, there is a good agreement between the observations and MEVD predictions for the highest quantile (extreme sea level events associated with long RPs) across the stations, as shown in Fig. 9 (left). Figure 9 (right) illustrates the best method identified for each station, in terms of QR computed from high quantiles, against the longest RP evaluated at each station. From this figure, it is apparent that the MEVD approach can estimate longer return period events compared to the POT-GPD approach. From the heat maps (Fig. 3), it was already seen that MEVD methods used higher TSL compared to POT-GPD methods in certain instances. Therefore, it is clear that MEVD worked well also with a smaller number of events compared to POT-GPD methods. This could be attributed to the formulation of MEVD, which explicitly incorporates the number of events (n_j) as represented in Eq. (7).

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395 The analysis was further extended to explore the role of the number of events/year utilized in fitting the MEVD and POT-GPD methods. Figure 10 compares the number of events per year used by MEVD and that used by the POT-GPD, along with performance information. MEVD outperforms POT-GPD at 25 out of 39 stations for the overlapping method and 33 out of 39 with the sorting method. Interestingly, as shown in Fig. 10 (left), the MEVD-overlapping approach consistently employed a number of events between ~5-12 per year, regardless of the location. The MEVD-sorting approach used a smaller number of events (~5-20) per year compared to POT-GPD-sorting for all the stations except for 8 stations along the Atlantic coastline. For those 8 stations, the number of events used by MEVD-sorting aligns with POT-GPD-sorting. This observation suggests that the number of events required for the MEVD-sorting approach is more site-specific. This can be attributed to local hydrodynamic processes or geometry, specifically the tidal dominance in the Atlantic Ocean, as well as the fact that the location of some of these stations near harbors results in moderate events. The sorting approach identifies more events than the overlapping approach, because the latter merges more events into one. Consequently, the MEVD-sorting approach uses a larger number of events per year than the MEVD-overlapping method to capture the process accurately. Focusing on TSL-TWW combinations that produce ~5-12 events per year is advisable for analysis using the MEVD-overlapping approach. However, the optimal combination should be determined based on RMSE*.

The estimation error (difference between predicted and observed values) associated with the MEVD-overlapping and MEVD-sorting approaches regarding high quantile estimation was evaluated across stations, as illustrated in Fig. 11. In the boxplot, the interquartile range is a measure of uncertainty. It is apparent from the figure that for both methods, the median of the estimation error is around zero. However, the prediction uncertainty is comparatively less for the MEVD-sorting approach.

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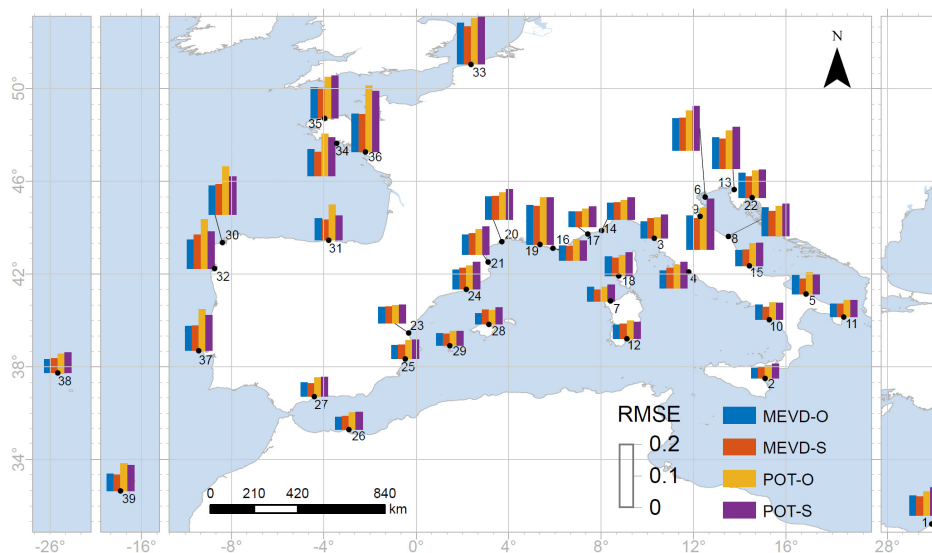
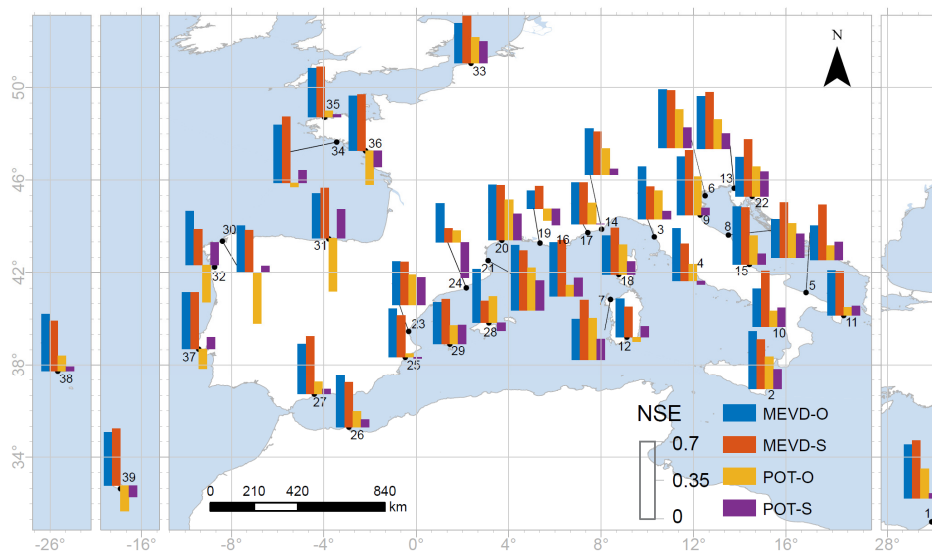
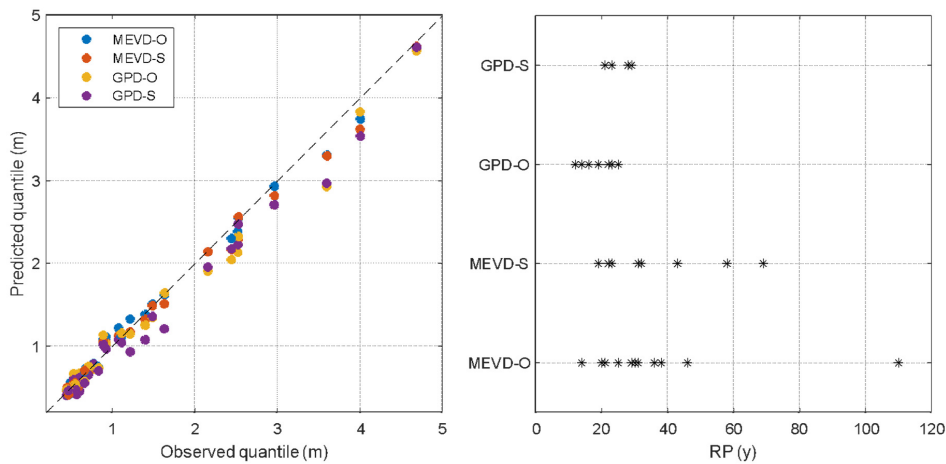


Figure 7: RMSE computed on all quantiles estimated for the best combination of TSL and TWW during cross-validation across all methods and stations.



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Figure 8: NSE computed on all quantiles estimated for the best combination of TSL and TWW during cross-validation across all methods and stations.



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Figure 9: Observed vs. predicted highest quantiles across stations (left) and outperformed method (i.e. the one which yielded the best QR among the four) vs. maximum RP computed for each station (right).

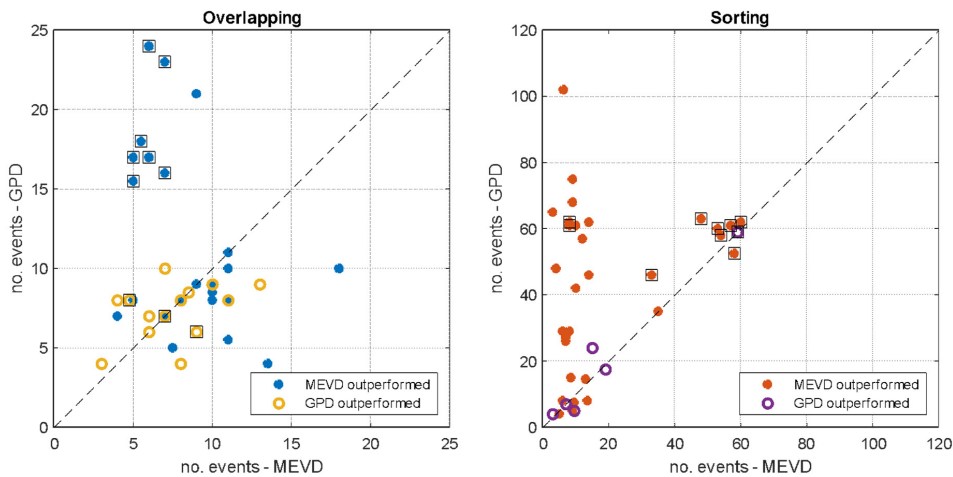
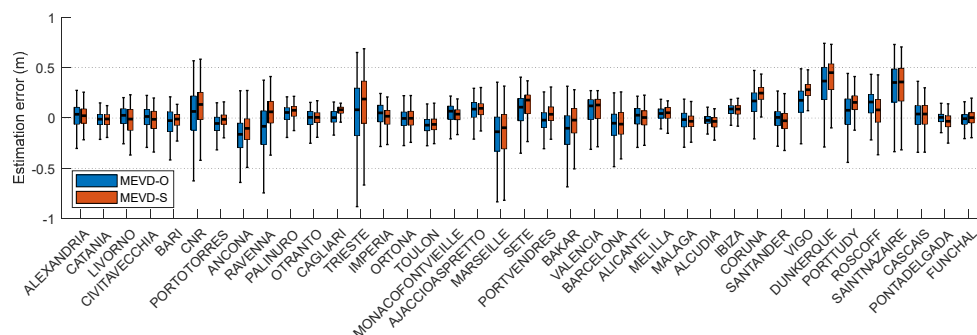


Figure 10: Number of events per year used by POT-GPD approach vs. those used by MEVD approach. The points enclosed in a square are the ones corresponding to the stations along the Atlantic coast.



430 **Figure 11: Boxplot of estimation error associated with the highest quantiles predicted using the MEVD-sorting method vs. those predicted using the MEVD-overlapping method.**

5 Conclusions

The comparative assessment MEVD and POT-GPD models, when integrated with novel independent event selection methodologies and applied to sea level observations across 39 stations along the Mediterranean and southern European Atlantic coastlines, provided insights into the predictive performance of the models. Our investigations quantitatively confirm the advantages of the MEVD over the conventional POT-GPD stemming from the conceptual differences between the methods. The quantitative evaluation of the predictive uncertainty of the statistical models with respect to high-quantile estimation was made possible by the systematic use of a cross-validation process. Selection of the optimal TSL and TWW based on RMSE* values evaluated across all quantiles with $RP \leq$ calibration sample size (4 years), using the cross-validation procedure, revealed that selecting the appropriate TSL and TWW is very important for defining independent ordinary events in the case of MEVD. However, the model's predictions are more sensitive to TSL choice in comparison to TWW. The optimal TSL-TWW combination selected based on the analyses performed using a very short record of observations could reliably model the high quantiles, as evidenced by the cross-validation results. A lower TSL and a minimum TWW will not invariably yield independent ordinary events within a block. With a fixed calibration sample size of 4 years, the comparative evaluation of four model configurations (a) MEVD-overlapping, (b) MEVD-sorting, (c) POT-GPD-overlapping, and (d) POT-GPD-sorting (IEs defined based on the optimal TSL-TWW combination) evaluated based on the statistical metrics (QR, RMSE, and NSE), indicates that MEVD approaches outperform POT-GPD approaches in terms of prediction accuracy in the context of data scarcity. We found that the MEVD approaches yield reliable estimates of high quantiles for almost all the tidal gauge stations examined, even with a small calibration sample size (4 years). Results indicated that MEVD approaches are more effective at estimating long RP events compared to POT-GPD approaches. Both POT-GPD approaches reliably estimated only extreme sea level events with RP less than 40 years, whereas the MEVD approaches predicted events with RP greater than 65 years. Specifically, the MEVD-overlapping method estimated events with RP greater than 100 years.



A notable finding of the study is that the MEVD-overlapping approach consistently utilized a number of events per year between ~5-12, regardless of the location. The MEVD and POT-GPD approaches integrated with the sorting method for IE selection utilized a smaller number of events per year, except for a few stations along the Atlantic coastline. This disparity could be linked to local hydrodynamic processes (tidal dominance) or specific geometric factors (e.g. in the presence of harbors). Furthermore, among the MEVD approaches, prediction uncertainty was comparatively less for the MEVD-sorting approach. Overall, it can be concluded that while the optimal IE selection methodology is slightly site-specific, the MEVD formulation facilitates estimation of longer RP events even in data-scarce contexts. The findings of this study help quantify the risk associated with rare extremes and design robust defense infrastructures. For practical applications for the Mediterranean coastline, the MEVD-overlapping approach is suggested with a TWW of 6-10 days and a TSL of 0.35 m in the Alboran Sea, 0.2-0.25 m in the Western basin, including the Tyrrhenian Sea, and 0.2-0.3 m in the Southern Adriatic Sea, up to 0.7 m in the Northern Adriatic Sea.

Data availability

All datasets used in the present study are publicly available. The sea level observations for the Italian stations were sourced from Istituto Superiore per la Protezione e la Ricerca Ambientale (ISPRA) (<https://www.mareografico.it/>). Data for the French stations were obtained from Réseaux de Référence des Observations Marégraphiques (REFMAR) (<https://refmar.shom.fr/donnees-refmar-sur-data.shom.fr/telechargement-des-donnees>), while Spanish stations' data from Puertos del Estado (<https://portus.puertos.es/#/?locale=en>). Egyptian and Portuguese stations' data were acquired from the University of Hawaii Sea Level Center (UHSLC) (<https://gesla787883612.wordpress.com/downloads/>). Sea level observations of the Croatian station were retrieved from an open data repository SEANOE (DOI: 10.17882/85171).

Author contributions

SS: Conceptualization, Methodology, Formal analysis, Software, Validation, Investigation, Data curation, Visualization, Writing (original draft preparation), Writing (review and editing); CF: Conceptualization, Methodology, Data curation, Validation, Visualization, Supervision, Writing (review and editing); PR: Conceptualization, Methodology, Validation, Supervision, Writing (review and editing); MM: Conceptualization, Methodology, Validation, Supervision, Funding acquisition, Project administration, Writing (review and editing)

Competing interests

The authors have no competing interests to declare that are relevant to the content of this article.



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485 C93C22005160002).

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