



1 **Three-Dimensional Geological Modeling based on Dual-Task**
2 **Stratigraphy-Aware Attention Networks (Geo-SAN v1.0)**

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11 **Abstract:** The current three-dimensional (3D) geological implicit modelling methods
12 are mainly based on interpolation methods, such as Kriging and radial basis functions
13 (RBFs), which struggle to capture the nonlinear characteristics of complex geological
14 structures and are limited in their capacity to integrate multi-source modeling data. To
15 overcome these limitations, we proposed a 3D geological modelling framework, Geo-
16 SAN, which consists of a dual-task stratigraphy-aware attention network. The
17 framework starts with graph neural networks (GNNs) with a multi-scale neighborhood
18 aggregation mechanism which is aimed to identify critical sampled points adjacent to
19 fault planes and aggregate the lithological features. Subsequently, a stratigraphy-aware
20 attention mechanism is introduced to explicitly incorporate similarities in stratigraphic
21 sequence into the framework. A unidirectional stratigraphic scalar field penalty to
22 lithological classification is developed and incorporated into loss functions, thereby
23 denoising lithological classification. Finally, a dual-task prediction head is designed to
24 simultaneously complete lithological classification and scalar field interpolation.
25 Ablation experiment further validates the contributions of the three core components,
26 that is, graph neighborhood aggregation, stratigraphy-aware attention, and dual-task
27 learning. A case study at the Lingnian-Ningping region of Guangxi Zhuang
28 Autonomous Region (GZAR), China, demonstrates that the proposed Geo-SAN
29 framework, with an accuracy of 92.1% in lithological classification and a coefficient of
30 determination (R^2) of 0.96 in predicting the scalar field, outperforms the Hermite RBFs
31 (HRBFs). In summary, the proposed framework is an important innovation of
32 intelligent modelling of intricate geological formations, which is promising in the
33 application of concealed mineral exploration.



34 **Keywords:** three-dimensional geological modelling; graph neighborhood aggregation;
35 stratigraphic sequence; dual-task learning; stratigraphy-aware attention network.

36 **1 Introduction**

37 Three-dimensional (3D) geological modelling is the process of creating
38 mathematical representation of geological structures with the help of suitable computer
39 data structures. The result models are the reflections of the geometrical forms,
40 topological relationships, and spatial distributions of physical and chemical properties
41 of geological bodies. This technique is widely used in earth sciences in visualization,
42 statistical analysis, and numerical simulation (Alcalde et al., 2017; Wang et al., 2019;
43 Du et al., 2026).

44 3D geological geometric modelling can be divided into explicit and implicit
45 techniques. Explicit modelling generally involves a huge amount of human-computer
46 interaction to connect boundary lines and define the 3D surface model of geological
47 bodies (Sprague and De Kemp, 2005; Caumon et al., 2009; Khan et al., 2021; Shah et
48 al., 2024). Implicit modelling treats geological interfaces as iso-surfaces of a scalar field,
49 thereby preserving topological consistency of geological interfaces. The resulting
50 model automatically satisfies geological contact relationships and facilitates consistent
51 handling of faults and stratigraphic interfaces (Hillier et al., 2013; Guo et al., 2020;
52 Zhang et al., 2023a). Implicit methods, under spatial relationship constraints, can
53 control geological structural topological consistency, orientations of geological
54 structures, and influences of interpolation distances (Khan et al., 2023). They can also
55 integrate geophysical inversion data (such as gravity, magnetic, and seismic) to enhance
56 the ability to interpret deep geological structures (Wellmann et al., 2017; Jessell et al.,
57 2022; Giraud et al., 2024). However, implicit modeling methods suffer limitations such
58 as overfitting in sparse data representation, neglecting lithology classification
59 information, and ignoring geological prior knowledge. An important requirement exists
60 to devise efficient data aggregation methods and reflect correlations between lithology
61 and stratigraphy.

62 The rapid advancement of deep learning technologies has opened new avenues for
63 3D geological modelling (Reichstein et al., 2019; Bergen et al., 2019). These methods,
64 collectively termed neural network geomodelling (NNG) (Li et al., 2024; Lyu et al.,
65 2024), encompass graph neural networks (GNNs) (Hillier et al., 2021; Chu et al., 2025;
66 Hu et al., 2024), convolutional neural networks (CNNs) (Bi et al., 2022; Zhang et al.,



67 2024; He et al., 2025; Ren et al., 2025), and multilayer perceptron (MLP) (Hillier et al.,
68 2023; Guo et al., 2024; Chu et al., 2024). Compared to traditional implicit modelling,
69 neural network modelling approaches offer superior speed and efficiency when
70 handling complex geological structures, enabling their automated modelling, while
71 they require high-quality training data for model training. Since geological sampling
72 data exhibits pronounced spatial irregularity and sparsity (Wang et al., 2012; De La
73 Varga et al., 2019; Wang et al., 2022), Gori et al. (2005) introduced the concept of GNNs,
74 which apply neural network operations on graph-structured data. By propagating
75 information through node connectivity patterns, GNNs accommodate irregular
76 neighborhood structures and are therefore capable of capturing complex geological
77 relationships and structural patterns (Zhang et al., 2023b; Peng et al., 2024; Wang et al.,
78 2024; Yin et al., 2026). Spatial discontinuities arising from geological structures, such
79 as faults, intrusions, and unconformities, further challenge modelling efforts, as
80 traditional similarity-based attention mechanisms struggle to capture contact
81 relationships among geological bodies. Consequently, the direct application of generic
82 attention mechanisms leads to substantial inaccuracies, underscoring the need for
83 deeper integration of stratigraphic sequence and lithological similarity of NNG models.

84 To address the complexity of geological setting, we propose a 3D geological
85 modelling framework utilizing a dual-task stratigraphy-aware attention network (Geo-
86 SAN), including GNN-based neighborhood aggregation, stratigraphy-aware attention
87 mechanism, and a dual-task prediction head that allows integrating lithological
88 classification and scalar field estimation. To start with, the 3D geological space is
89 modeled as a graph by means of the tetrahedral subdivision, where nodes are sampling
90 points and edges are spatial adjacency. Multi-scale features are extracted and
91 propagated using graph attention networks (GAT) and graph sample and aggregate
92 network (GraphSAGE). Secondly, a new stratigraphy-aware attention mechanism is
93 proposed. This mechanism considers similarities of stratigraphic sequence between the
94 query node and the observation point. Finally, a head of the dual-task prediction is used
95 to collaboratively produce discrete lithological classifications and continuous scalar
96 field estimates.

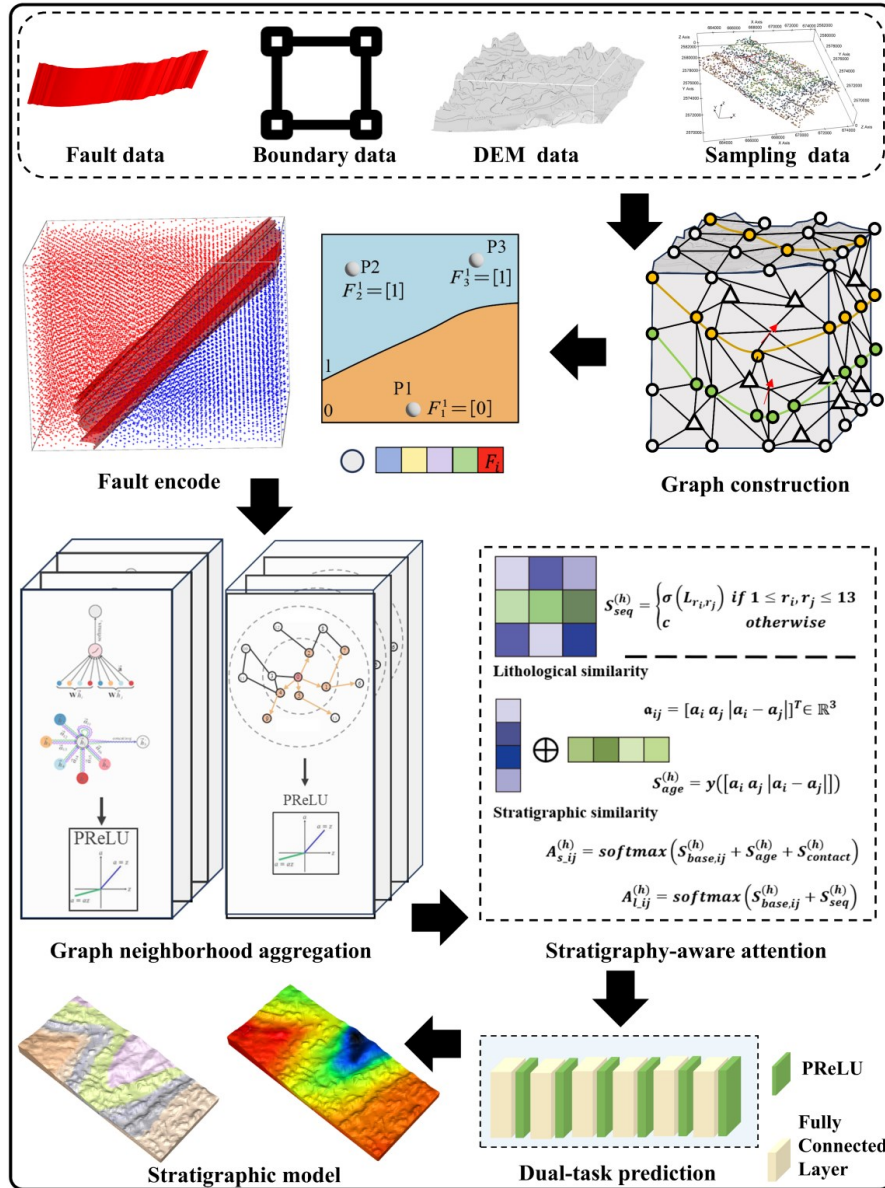
97 **2 Methods**

98 **2.1 Geo-SAN Architecture**

99 The workflow of the proposed 3D geological modelling method (Geo-SAN),



100 based on a dual-task stratigraphy-aware attention network, is illustrated in Figure 1.
101 The workflow comprises five key stages, graph construction, graph neighborhood
102 aggregation, stratigraphy-aware attention, lithology classification and implicit
103 interpolation, and 3D geological model reconstruction. The method begins with
104 extracting features from sampled data using the graph neighborhood aggregation and
105 stratigraphy-aware attention mechanisms. Subsequently, a dual-task prediction head is
106 employed to estimate both continuous scalar field values and discrete lithological
107 categories. Finally, the predicted result is integrated to construct a coherent 3D
108 geological model.



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Fig. 1. Workflow of Geo-SAN.

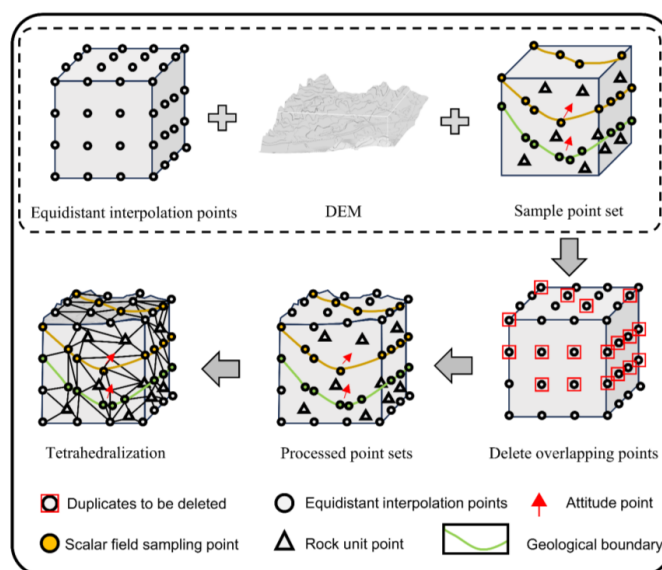
111 2.1.1 Graph Neighborhood Aggregation

112 To address the complexity of geological setting and the large volume of geological
 113 data inherent in 3D geological modelling, we employ spatial-domain GAT and
 114 GraphSAGE to aggregate node features, thereby harnessing the strong nonlinear
 115 integration capabilities of GNNs.



116 **(1) Graph Construction**

117 The tetrahedral meshing of the sampled points is performed to create graph
 118 structured data. All the sampling points and the other densifying points are both
 119 included into the graph data. As shown in Figure 2, the base and the lateral boundaries
 120 are determined by the modeling extent whereas the top boundary is determined by the
 121 digital elevation model (DEM). Each sampling point is a vertex of a tetrahedron, and
 122 the topological connection of the sampling point is maintained during tetrahedron
 123 subdivision. Densifying points are created based on the given modelling resolution;
 124 overlapping points are eliminated. The resulting mesh has a multi-resolution structure,
 125 with tetrahedra around sampled points having smaller volumes and higher densities.
 126 Graph nodes are represented as tetrahedral vertices, and graph edges are represented as
 127 tetrahedral edges. Finally, the faults are encoded as a feature of nodes in relation to fault
 128 planes, which is combined with other node features as model inputs.



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Fig. 2. Graph construction.

132 **(2) GNN Neighborhood Aggregation**

133 The multi-scale graph neighborhood aggregation mechanism is formulated into
 134 the proposed framework. GAT with its learnable attention mechanism gives a specific
 135 weight to the neighboring nodes (Veličković et al., 2017), which is especially useful in
 136 a geological modeling task where local heterogeneity and sensitivity to the boundaries
 137 are considered to be a significant issue. When processing nodes near faults, GAT learns



138 to down-weight connections to neighbors on the opposite side of the fault, effectively
139 preventing spurious propagation of stratigraphic samples across the discontinuity. At
140 stratigraphic boundaries, GAT preferentially attends to aggregate nodes within the same
141 unit, allowing for sharper delineation of geological discontinuities. For node i and its
142 neighbor node j , the attention coefficient α_{ij} is calculated, which reflects the
143 importance of node j in propagating features to node i , as follows:

$$144 \quad \alpha_{ij} = \frac{\exp(\text{LeakyReLU}(\mathbf{a}^T [\mathbf{W}\mathbf{h}_i \parallel \mathbf{W}\mathbf{h}_j]))}{\sum_{k \in \mathcal{N}(i)} \exp(\text{LeakyReLU}(\mathbf{a}^T [\mathbf{W}\mathbf{h}_i \parallel \mathbf{W}\mathbf{h}_k]))} \quad (1)$$

145 where \mathbf{a} is the learned attention parameter vector, \parallel represents the concatenation of
146 feature vectors, \mathbf{W} is the weight matrix, and \mathbf{h}_i and \mathbf{h}_j are the feature representations of
147 nodes i and j , respectively.

148 GraphSAGE statistically incorporates neighboring node features into the central
149 node through a mechanism primarily designed to capture regional geological
150 characteristics and spatial continuity patterns (Hamilton et al., 2017). For scalar value
151 prediction tasks, this approach demonstrates robust capability in capturing spatial
152 gradient patterns, given that scalar properties within a continuous domain generally
153 exhibit gradational transitions rather than abrupt discontinuities. In lithological
154 classification tasks, GraphSAGE exploits the geological principle that spatially
155 proximate nodes tend to share similar features, thereby incorporating the lithological
156 distribution within the statistical neighborhood to inform classification decisions at
157 each target node. GraphSAGE aggregates the features of neighboring nodes layer by
158 layer through a multi-layer neural network, with the embedding update formula for each
159 layer's nodes, as follows:

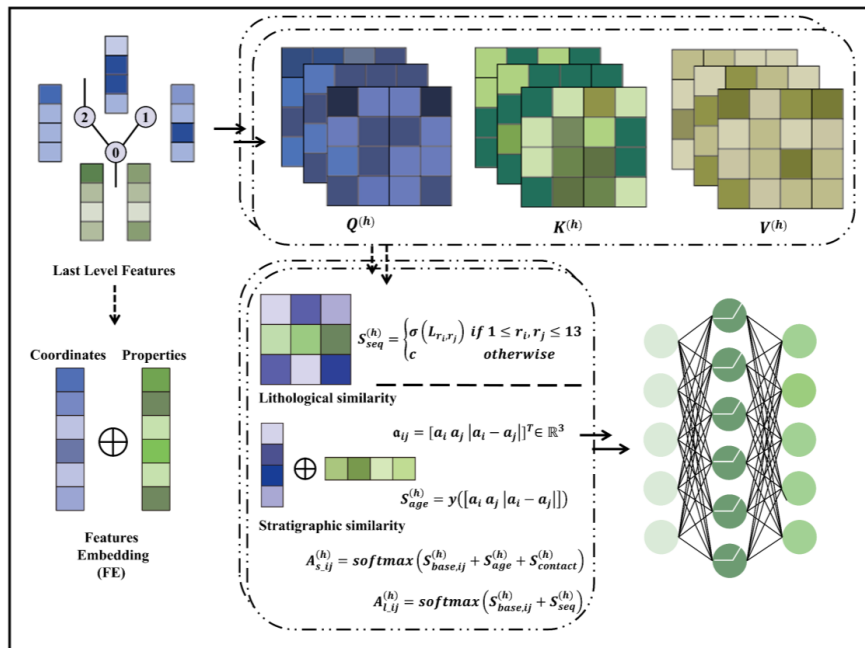
$$160 \quad \mathbf{h}_v^k = \sigma(\mathbf{W}^k \cdot \text{AGGREGATE}_k(\{\mathbf{h}_1^{k-1}, \forall u \in \mathcal{N}(v)\}) \oplus \mathbf{h}_v^{k-1}) \quad (k = 1, \dots, K) \quad (2)$$

161 where \mathbf{h}_v^k is the embedding vector of node v at the k layer, $\mathcal{N}(v)$ is the neighborhood
162 of node v , and AGGREGATE_k is the aggregation function of the k layer. Common
163 choices for aggregation functions include pooling aggregation and long short-term
164 memory (LSTM) aggregation. Given the similarity of geological features within the
165 same region in geological modeling, the average pooling aggregation function is used
166 in this study to embed the features. \mathbf{W}^k represents the learnable weight matrix, and
167 \oplus denotes the vector concatenation operation.



168 **2.1.2 Stratigraphy-Aware Attention Network**

169 Geological data are distinguished by a high degree of spatial heterogeneity,
 170 thereby similar characteristics in different geological environments may have entirely
 171 distinct meanings. Such domain-specific subtleties are not reflected in conventional
 172 attention mechanisms, which only compute weights using feature similarity. To address
 173 this weakness, we present a stratigraphy-aware attention (SAN) process that involves
 174 the prior constraints of stratigraphic sequences. Through the incorporation of
 175 lithological similarity and stratigraphic sequence, the mechanism gains a meaningful
 176 combination of stratigraphy knowledge for the proposed framework (Figure 3).



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Fig. 3. Stratigraphy-aware attention network.

180 First, the SAN receives the following inputs: features aggregated from the graph
 181 neighborhood, query vectors Q derived from graph nodes, observation point features
 182 K from the graph, and feature V used for aggregation. The input features undergo an
 183 initial linear transformation that projects them into the attention space. Secondly, the
 184 projected features are partitioned into H attention heads, each processing $d_k = d/H$
 185 dimensional features. For nodes i and j , the base score of the h head is:

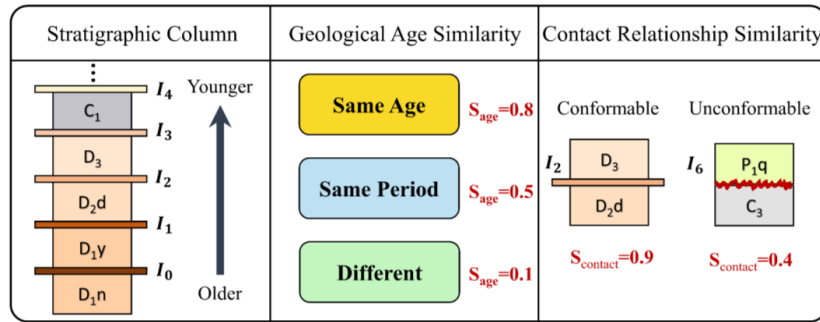


186
$$S_{base,ij}^{(h)} = \frac{1}{\sqrt{d_k}} \sum_{l=1}^{d_k} Q_{i,h,l} \cdot K_{j,h,l} \quad (3)$$

187 We first define the mapping function from lithology to geological age as $a_i =$
 188 $Age(r^i)$, as shown in Figure 4. For node (i, j) , the output $S_{age}^{(h)}$ denotes the value for
 189 stratigraphic age similarity between node (i, j) at the h head, as follows:

190
$$S_{age}^{(h)}(i, j) = y([a_i \ a_j \ |a_i - a_j|]) \quad (4)$$

191 where $y(\cdot)$ is the age mapping function.



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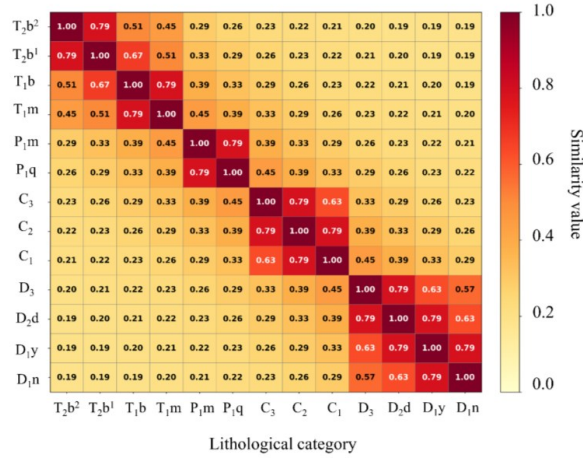
Fig. 4. Stratigraphic similarity

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195 Then, we define a learnable lithological similarity matrix $L \in \mathbb{R}^{K \times K}$, where K is
 196 the number of lithological categories. Adjacent strata show stronger lithological
 197 similarity, with stratigraphic quantitative difference correlating inversely to lithological
 198 resemblance. For nodes i and j , lithological similarity S_{seq} is:

199
$$S_{seq}^{(h)}(i, j) = \begin{cases} \sigma(L_{r_i, r_j}) & \text{if } 1 \leq r_i, r_j \leq K \\ c & \text{otherwise} \end{cases} \quad (5)$$

200 where $\sigma(x) = \exp(-d(i, j)/3)$, and $d(i, j) = |i - j|$ denotes that the quantitative
 201 difference between the ordinal numbers of two lithological categories within the
 202 stratigraphic sequence. A lithological similarity matrix from the experiment is shown
 203 in Figure 5.



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Fig. 5. Lithological similarity matrix.

When predicting scalar values, for the h attention head, the enhancing attention for node pair (i, j) is as follows:

$$A_{s,ij}^{(h)} = \text{softmax}(S_{base,ij}^{(h)} + S_{age}^{(h)} + S_{contact}^{(h)}) \quad (6)$$

where $S_{contact}^{(h)}$ is the similarity of adjustable contact relationship.

When lithological classification, for the h attention head, the enhancing attention for node pair (i, j) is as follows:

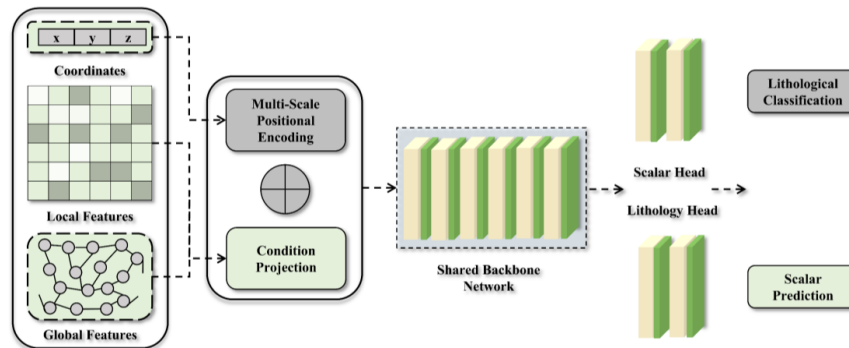
$$A_{l,ij}^{(h)} = \text{softmax}(S_{base,ij}^{(h)} + S_{seq}^{(h)}) \quad (7)$$

The SAN mechanism begins by computing standard base attention scores through linear projection of node features and their division into multiple attention heads. Its key innovation is the concurrent incorporation of stratigraphic sequence domain knowledge as prior constraints. Specifically, a learnable lithological similarity matrix quantifies the association strength between different lithological categories, while a stratigraphic sequence captures the geological age orders and contact relationship between node pairs. By injecting stratigraphy priors into the attention mechanism, the model allocates weights in a manner that reflects both feature similarity and domain-specific stratigraphic sequences, thereby enabling weighted aggregation and stratigraphic sequence information propagation.



224 **2.1.3 Dual-Task Prediction Module**

225 Following the extraction of spatial perceptual features by the SAN, a dual-task
 226 learning head is employed to simultaneously perform lithological classification and
 227 scalar field prediction, as illustrated in Figure 6.



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229 Fig. 6. Dual-task of lithological classification and scalar field prediction.

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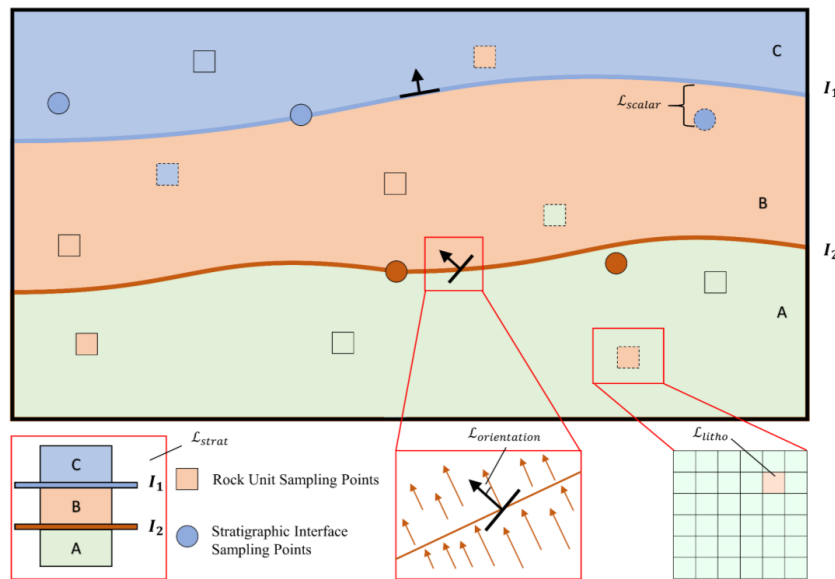
231 The dual-task module may consist of two prediction branches which use the same
 232 inputs, namely node features with GAT, GraphSAGE, and the SAN mechanism, then
 233 the two branches perform distinct tasks by using multilayer perceptron (MLP) decoders.
 234 The scalar-field prediction branch produces values of a continuous scalar field $[N,1]$,
 235 where N is number of nodes; the lithological classification branch produces a
 236 probability distribution vector $[N,K]$, where $K=13$ in this study.

237 **2.2 Loss Functions**

238 Three-dimensional geological modeling is a quintessential multi-constrained
 239 optimization issue. This study developed the scalar field loss function (\mathcal{L}_{scalar}), attitude
 240 loss function ($\mathcal{L}_{orientation}$), lithology category loss function (\mathcal{L}_{litho}) and stratigraphic
 241 constraint loss function (\mathcal{L}_{strat}). Figure 7 demonstrates \mathcal{L}_{scalar} measures the
 242 discrepancy between the observed scalar value S_v at a sampling point and the predicted
 243 scalar value S_v^{scalar} produced by Geo-SAN. The lithological loss \mathcal{L}_{litho} quantifies
 244 the disparities between the actual lithological labels and the predicted categories of the
 245 model. $\mathcal{L}_{orientation}$ evaluates the discrepancy between the measured direction at
 246 orientation sampling points and the direction derived obtained from the predicted scalar
 247 field at the corresponding nodes. \mathcal{L}_{strat} converts lithological similarity metrics of
 248 stratigraphic sequence into differentiable restrictions, directing neural networks to



249 acquire predictions aligned with stratigraphy principles. The a priori probability
 250 distribution of each lithological categories can be computed and determined according
 251 to predicted scalar values. Lithological predictions of the model are then regularized to
 252 the prior model with the help of the Kullback-Leibler (KL) divergence penalty, which
 253 serves as a soft probabilistic constraint. Meanwhile, a compatibility loss term imposes
 254 strict penalties on scalar field predictions falling outside the stratigraphically admissible
 255 intervals for corresponding lithological categories. Thus, the cross-task constraint may
 256 enforce consistency with stratigraphic sequences to yield geologically meaningful
 257 predictions.



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Fig. 7. Loss functions.

260 **2.2.1 Scalar Field Loss Function**

261 Geo-SAN predicts the scalar field f_v , which is constrained by stratigraphic
 262 interfaces and orientation points like dip angle and strike. We can define 3D space as a
 263 scalar function $f(v)$, where represents the scalar field values at each point v in 3D space.
 264 A series of H stratigraphic interfaces can be articulated as:

265
$$f_1 > \dots > f_H \tag{8}$$

266 where f_1 to f_H represent the scalar values of the oldest to newest stratigraphic
 267 interfaces, respectively.

268 For a certain stratigraphic interface I with a scalar field value f_I , the subset of



269 graph nodes sampled from it can be denoted as:

$$270 \quad I = \{v \in V | f_v = f_i\} \quad (9)$$

271 The loss functions \mathcal{L}_{scalar} can be used to find the difference between the scalar
272 field at the stratigraphic interface sampling point and the predicted scalar field by Geo-
273 SAN, as follows:

$$274 \quad \mathcal{L}_{scalar} = \frac{1}{N} \sum_{i=1}^N (\hat{f}_i - f_i)^2 \quad (10)$$

275 2.2.2 Attitude Loss Function

276 Nodes with attitudes can be extracted from geological maps, which represent the
277 local morphology of the strata at these nodes. A unit vector \mathbf{n} in the normal direction of
278 the stratigraphic interfaces can be transformed from the attitudes:

$$279 \quad \mathbf{n} = \begin{bmatrix} \sin \theta \cdot \sin \delta \\ \cos \theta \cdot \sin \delta \\ \cos \delta \end{bmatrix} \quad (11)$$

280 where θ and δ are the strike and dip angles of the stratum, respectively.

281 To measure predicted gradient and the actual direction of angular error, the
282 gradient of the predicted scalar field is gained at these graph nodes. This study employs
283 the first-order Taylor series approximation of the scalar field in the node's first-order
284 neighborhood to estimate the scalar field gradient, as follows:

$$285 \quad \mathbf{P}_v^T \mathbf{P}_v \nabla f_v = \mathbf{P}_v^T \begin{bmatrix} f_u - f_v \\ \vdots \end{bmatrix} \quad (12)$$

286 where the angle between the gradient at node v and the known vector $\nabla f_v =$
287 $(\partial f_v / \partial x, \partial f_v / \partial y, \partial f_v / \partial z)$ can be used to measure the angular error, and u is the
288 neighbor of node v .

$$289 \quad \mathbf{P}_v = \begin{bmatrix} x_u^* - x_v^* & y_u^* - y_v^* & z_u^* - z_v^* \\ \vdots & \vdots & \vdots \end{bmatrix}, \forall u \in N_v \quad (13)$$

290 where x^* , y^* , and z^* are the normalized spatial coordinates of the given node.

291 The estimated angle between the gradient ∇f_v at node v and the known vector
292 α_v in the observed attitude node-set o is utilized to formulate the loss function, as
293 follows:

$$294 \quad \mathcal{L}_{orientation} = \sum_{v \in o} \cos(\nabla f_v, \alpha_v) = \sum_{v \in o} \frac{\alpha_v \cdot \nabla f_v}{\|\alpha_v\| \|\nabla f_v\|} \quad (14)$$

295 2.2.3 Lithology Category Loss Function

296 In the lithology node-set R , comprising $N_{classes}$ lithology categories, each



297 lithology node is associated with a one-hot encoded vector \mathbf{l}_v , denoting its respective
298 lithology category. The loss function employed for lithology nodes is the cross-entropy
299 loss function, as follows:

$$300 \quad \mathcal{L}_{litho} = -\sum_{v \in R} (\mathbf{l}_v \cdot \log(\hat{\mathbf{l}}_v)) \quad (15)$$

301 where $\hat{\mathbf{l}}_v$ is the predicted probability distribution for node v , and the predicted
302 lithology category is determined based on the highest probability from the softmax
303 distribution of $\hat{\mathbf{l}}_v$.

304 2.2.4 Cross-Task Loss Function

305 The KL divergence loss function (soft constraint) is utilized to measure the
306 discrepancy between lithological classification and scalar field prediction, thus
307 encouraging models to adhere to stratigraphic sequence patterns, as follows:

$$308 \quad \mathcal{L}_{KL} = \text{KL}(\hat{\mathbf{l}} \parallel \hat{\mathbf{f}}) = \sum_{i=1}^N \sum_{j=1}^K \hat{l}_i^j \log \frac{\hat{l}_i^j}{\hat{f}_i^j} \quad (16)$$

309 where \hat{l}_i^j denote that model's predicted probability distribution over j -th lithological
310 category at i -th node, and \hat{f}_i^j denote that the probability distribution derived from
311 stratigraphic scalar field.

312 The compatibility loss function evaluates whether expected scalar field conform
313 to the acceptable range for lithological category, imposing penalties on forecasts that
314 contravene geological principles, as follows:

$$315 \quad \mathcal{L}_{compat} = \frac{1}{N} \sum_{i=1}^N \left(1 - \exp\left(-\frac{\Delta f(i)}{F}\right) \right) \quad (17)$$

316 where F denotes exceeding the upper or lower threshold. The deviation $\Delta f(i)$
317 measures how far the predicted scalar value is outside the valid range:

$$318 \quad \Delta f(i) = \max(0, \hat{f}_i - tl_i) + \max(0, bl_i - \hat{f}_i) \quad (18)$$

319 where tl_i and bl_i are the top and bottom interface scalar values according to the observed
320 lithological category at node i . When $bl_i \leq \hat{f}_i \leq tl_i$, then $\Delta f(i) = 0$ (perfect
321 compatibility). The cross-task loss function is expressed as:

$$322 \quad \mathcal{L}_{strat} = \mathcal{L}_{KL} + \mathcal{L}_{compat} \quad (19)$$

323 The overall loss function is as follows:

$$324 \quad \mathcal{L} = \alpha \mathcal{L}_{scalar} + \beta \mathcal{L}_{orientation} + \gamma \mathcal{L}_{litho} + \delta \mathcal{L}_{strat} \quad (20)$$

325 where α, β, γ , and δ are adjustable parameters.



326 2.3 Experimental Environment

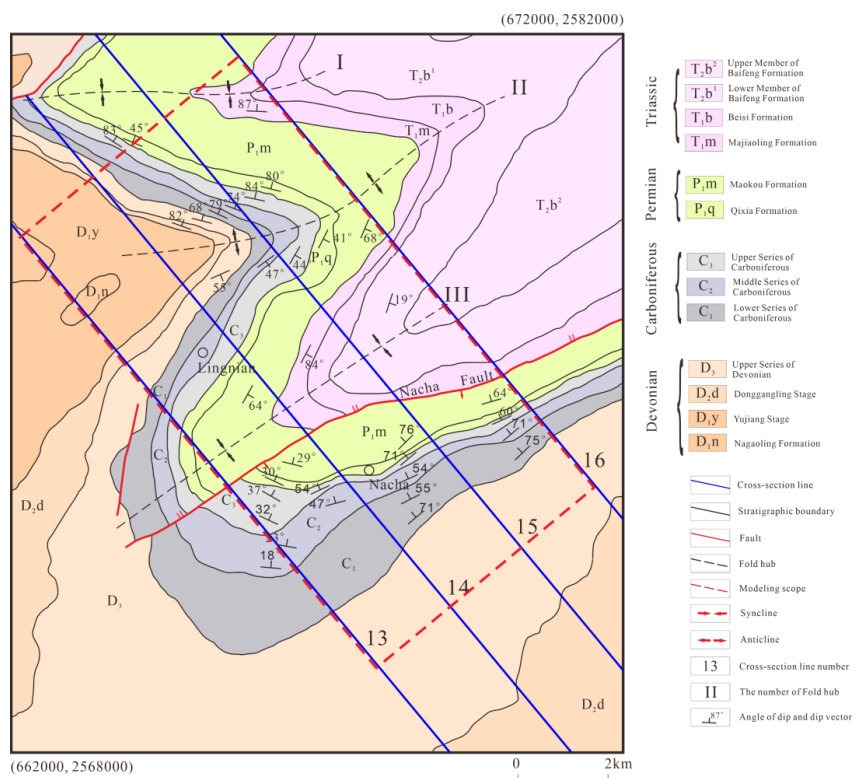
327 The experiments in this study are based on the PyTorch Geometric graph machine
328 learning library (Fey and Lenssen, 2019), as shown in Table 1.

329 Table 1. Experimental environmental.

Configuration	Value
CPU	Intel(R) Xeon(R) Gold 5120 CPU @ 2.20GHz
GPU	NVIDIA GeForce RTX 3090(24G)
Memory (RAM)	128G
Operating system	Ubuntu 24.04.1
Deep learning framework	PyTorch Geometric 2.2.0
CUDA version	12.1

330 3 Study Area and Dataset

331 The study area is situated in the Lingnian-Ningping area in Guangxi Zhuang
332 Autonomous Region (GZAR), China (Figure 8). The area predominantly exhibits strata
333 from the Late Paleozoic onwards, therein, strata from the Late Permian (P_3) and Late
334 Triassic to Pleistocene (T_3-N_2) are absent. The Middle Permian (P_2) and Early Triassic
335 (T_1) strata exhibit parallel unconformity, whereas the Middle Triassic (T_2) and
336 Quaternary (Q) strata display angular unconformity. In the central region of the study
337 area, a left-lateral strike-slip reverse fault, the Nacha Fault, intersects the Maokou
338 Formation and Carboniferous strata, dipping southeast at approximately 70° and
339 extending roughly 12 kilometers outside the study area. Within the area, there exist two
340 synclines (I and III) and one anticline (II). Syncline III, located at the center of the study
341 area, has high symmetry, featuring a northeast-trending axial trace, and is truncated
342 along its southern limb by the Nacha Fault. Anticline II is situated in the northwestern
343 section of the study area, demonstrating a notable symmetry and a northeast-oriented
344 axis. Sampling points for stratigraphic interfaces, lithologies, and attitudes were
345 extracted from a planar and four cross-section geological maps (Figure 9) to constitute
346 the modeling dataset. There are 1410 stratigraphic interface sampling points, 18,619
347 lithology sampling points, and 34 attitude points.

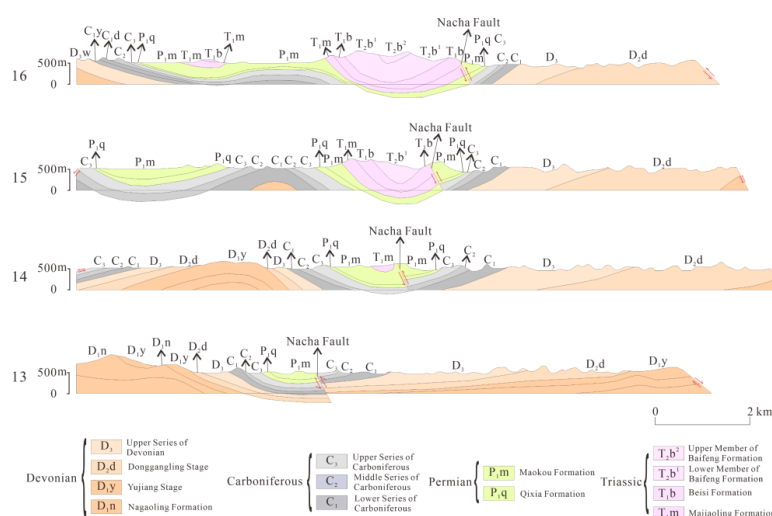


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Fig. 8. Geological map of the study area, modified after Zhang et al. (2023a).



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Fig. 9. Geological cross-section maps of the study area, modified after Zhang et al. (2023a).



353 **4 Results**

354 **4.1 Model Performance**

355 During model training, various configurations significantly affect performances
 356 levels. To evaluate impacts of graph neighborhood aggregation, SAN, and the dual-task
 357 learning head modules on overall modeling accuracy, four models were developed, as
 358 detailed in Table 2. Model M1 utilizes solely the GAT-based embedding module, while
 359 model M2 uses entirely on GraphSAGE for feature embedding. Model M3 employs an
 360 alternating technique utilizing both GAT and GraphSAGE embedding while excluding
 361 the SAN and the dual-task learning head. Model M4 incorporates three essential
 362 modules for comprehensive comparison.

363 Table 2. Ablation experiments.

Model	Graph neighborhood aggregation	SAN	Dual-task	Description
M1	GAT	✓	✓	Dual-GAT-SAN
M2	GraphSAGE	✓	✓	Dual-GraphSAGE-SAN
M3	GAT/GraphSAGE	×	×	GAT-GraphSAGE
M4	GAT/GraphSAGE	✓	✓	GAT-GraphSAGE-SAN

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365 The ratio of training dataset to testing dataset is set as 8:2, with all models trained
 366 according to hyperparameters specified in Table 3.

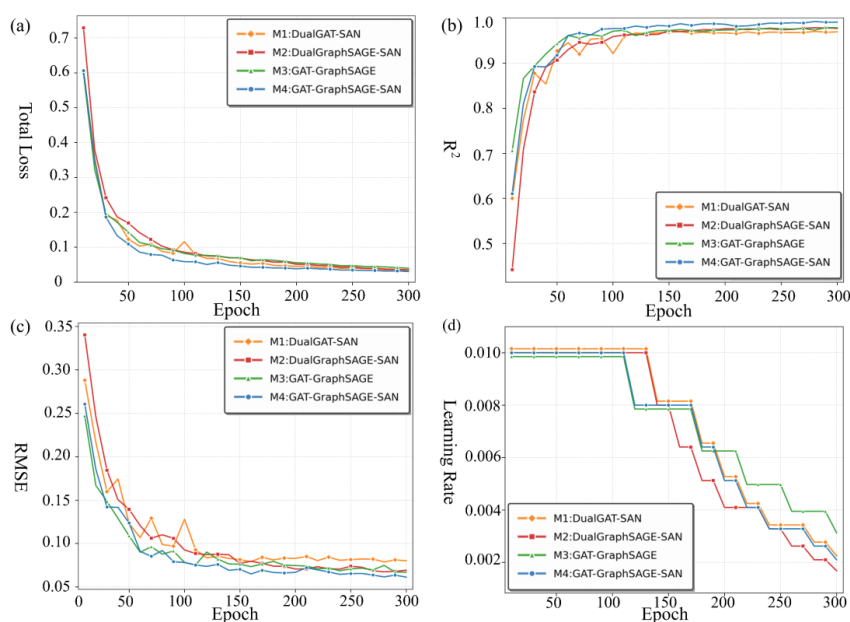
367 Table 3. Model hyperparameters.

Model Hyperparameters	Graph neighborhood aggregation	Lithology classification /scalar field interpolation
Number of embedding layers	6	8
Learning rate	0.01	0.01
Learning rate scheduler	ReduceLROnPlateau	ReduceLROnPlateau
Learning rate decay	0.8	0.8
Activation function	PreLU	PreLU
Embedding dimension	64	128
Number of attention heads	2	/
Epochs	/	300

368 To evaluate performances of various models during training, we plot evolution
 369 curves for each model over the two tasks: scalar field prediction and lithology
 370 classification. Figure 10 illustrates that all four models achieve convergence after



371 roughly 300 epochs. In the scalar field prediction task, models utilizing the integrated
372 GAT+GraphSAGE embedding exhibit much more quick reductions in loss and root
373 mean square error (RMSE), together with swifter enhancements in the coefficient of
374 determination R^2 (M4 and M3 surpass M1 and M2). This suggests that the
375 GAT+GraphSAGE architecture provides enhanced feature extraction for node-level
376 scalar field interpolation, effectively identifying latent geological patterns during the
377 training process.



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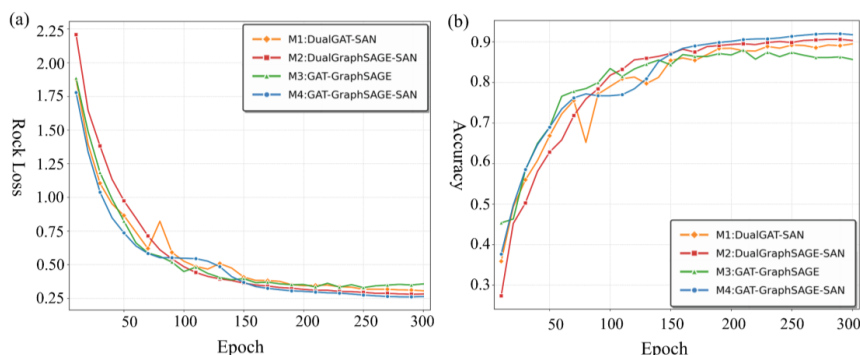
379 Fig. 10. Model evaluation metrics for scalar field interpolation training processes: (a) total loss, (b) R^2 ,
380 (c) RMSE, and (d) learning rate.

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382 The lithological classification training curves in Figure 11 show that the SAN-
383 augmented embedding model has a faster decrease in losses and a faster increase in
384 accuracy than the GAT–GraphSAGE model ($M3 < M4$). This behavior can be explained
385 by the geological principle that lithologies that are close to each other tend to be similar.
386 The SAN effectively directs feature aggregation during training by incorporating
387 lithological similarity and stratigraphic sequence constraints. In contrast, the GAT–
388 GraphSAGE model (M3), which relies solely on graph neighborhood aggregation,
389 lacks the ability to organically integrate stratigraphic sequence prior knowledge during
390 data-driven learning. As a result, its lithological classification performance is noticeably



391 worse at the beginning of training process.



392

393 Fig. 11. Model evaluation metrics in lithological classification training processes: (a) loss, and (b)

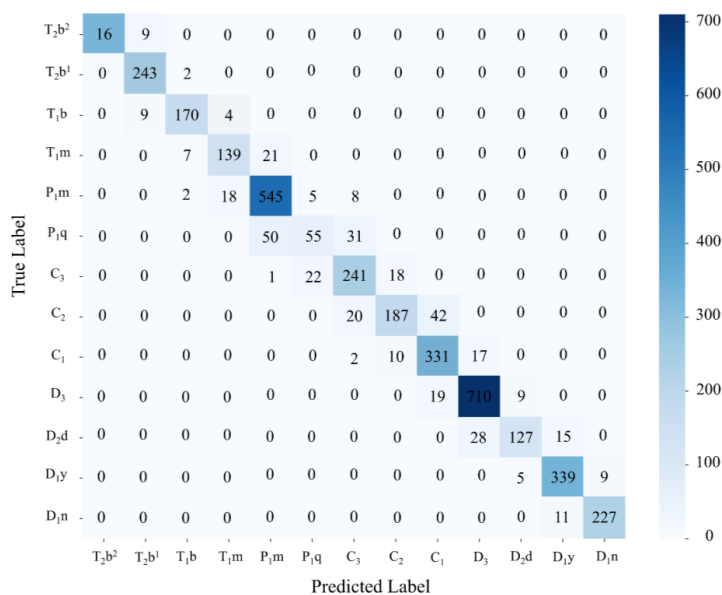
394

accuracy.

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396 The confusion matrix (Figure 12) shows that the proposed model performs well in
 397 all thirteen lithological categories. The model's highest classification accuracy is for D_3
 398 and P_{1m} lithologies. T_{2b^1} , C_3 , C_1 , D_{1y} , and D_{1n} have over 85% correctly identified
 399 samples, demonstrating strong generalization and stable prediction. Although T_{1m} and
 400 P_{1m} , and D_{2d} and D_{1y} are slightly confused, the overall misclassification remains low,
 401 learning meaningful feature representations for each lithological category. Results show
 402 three major benefits: (1) Thirteen lithological categories are accurately recognized; (2)
 403 Most predictions are correctly along the diagonal with few off-diagonal errors; And (3)
 404 residual confusion is between lithologies with similar stratigraphic attributes or
 405 transitional relationships. The proposed Geo-SAN model performs well in automated
 406 lithology classification under complex geological conditions and provides an intelligent
 407 foundation for 3D geological modelling.

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Fig. 12. Geo-SAN lithological classification confusion matrix.

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According to category-wise performance metrics (Figure 13), the model demonstrates well in lithological classification. Most lithological categories have F1-scores above 0.80, with T₂b¹, P₁m, D₃, D₁y, and D₁n having values above 0.90, indicating high classification reliability. Most lithology categories, except P₁q (0.671), have precision between 0.79 and 0.99, indicating good false positive control. Most categories maintain recall values between 0.74 and 0.99, indicating high true positive detection rates. The model’s robustness under extreme sample imbalance (25 samples of T₂b² to 738 samples of D₃) is noteworthy. This shows the Geo-SAN architecture’s powerful feature-learning capability and the training strategy’s efficacy. Although the recall of P₁q is relatively low (0.404), likely due to its feature similarity with adjacent lithologies, the model still achieves F1-scores above 0.82 for most sparse categories, demonstrating strong small-sample generalization. The model exhibits three major strengths: (1) balanced precision and recall, with most lithological categories achieving values above 0.90 for both metrics; (2) high resilience to sampling imbalance, maintaining stable performance even under severely skewed sample distributions; (3) strong lithological classification applicability, with F1-scores ranging from 0.50 to 0.95.

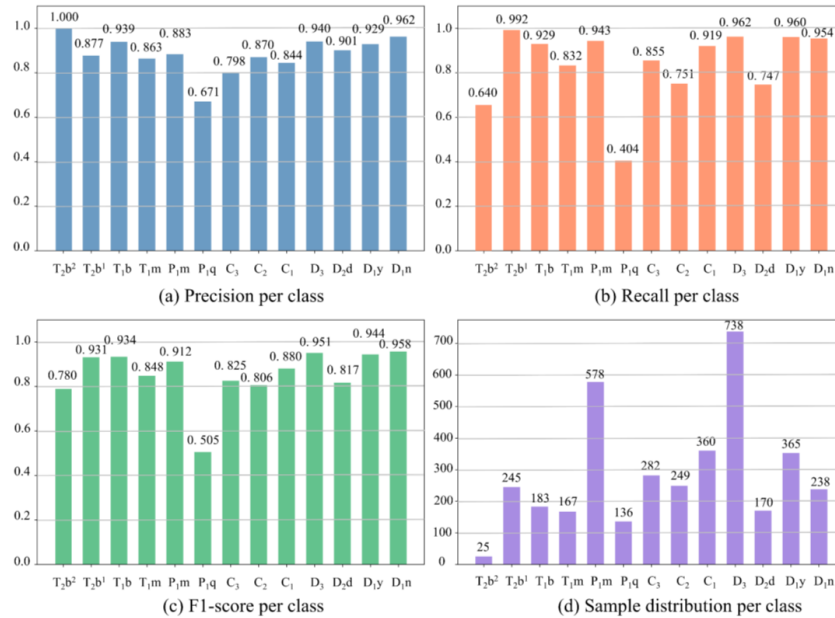


Fig.13. Geo-SAN model lithological classification evaluation metrics.

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Further analysis of the model evaluation metrics (Table 4) shows that Model M4 achieves the lowest loss values across its all components after training. This indicates that the integrated strategy, combining GAT+GraphSAGE embedding, SAN, and a dual-task learning head, provides substantially improved predictive performance. For scalar field prediction (evaluated by R^2 and RMSE), the models rank as follows: $M4 > M2 > M1 > M3$. Models incorporating both GAT and GraphSAGE for scalar field prediction yield higher overall R^2 values and lower RMSEs. For lithology classification (evaluated by accuracy), the performance ranking is: $M4 (92\%) > M2 (90\%) > M1 (90\%) > M3 (84\%)$. This demonstrates that GraphSAGE’s local feature aggregation, together with the SAN and the dual-task learning structure, significantly enhances lithological classification accuracy.

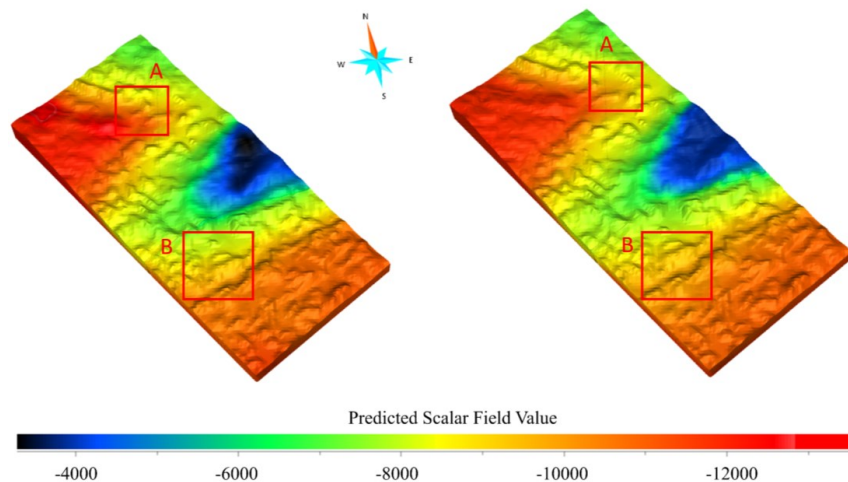
Table 4. Model performance evaluation metrics (300 epochs).

Model	\mathcal{L}_{scalar}	$\mathcal{L}_{orientation}$	\mathcal{L}_{litho}	R^2	RMSE	Accuracy	Time
M1	0.0066	0.4735	0.3056	0.95	0.079	0.88	162.15s
M2	0.0049	0.5073	0.2817	0.96	0.070	0.90	127.58s
M3	0.0056	0.5175	0.3956	0.96	0.074	0.84	61.49s
M4	0.0053	0.4541	0.2719	0.97	0.070	0.92	162.51s



443 4.2 Scalar Field

444 Comparative analysis of scalar fields by Geo-SAN and gradient-adaptive Hermite
445 radial basis function (AdaHRBF) (Zhang et al., 2023a), as shown in Figure 14, shows
446 that both modeling approaches exhibit a broad consistency of large-scale trends and
447 accurately describes the smooth changes of the scalar fields. The AdaHRBF method
448 creates several inharmonious changes in values of scalar fields in structurally
449 complicated areas that are attributed to uneven distribution of sampling points in the
450 spaces and presence of noise which may lead to instability and local distortion. On the
451 other hand, the scalar field generated by Geo-SAN has more gradual and geological
452 smooth transitions in the same areas. The Geo-SAN method improves robustness and
453 local adaptivity by combining SAN and graph-based neighborhood aggregation,
454 creating more robust scalar field representations in complex geological settings.



455

456 Fig. 14. Three-dimensional scalar fields modeled by (a) AdaHRBF and (b) Geo-SAN.

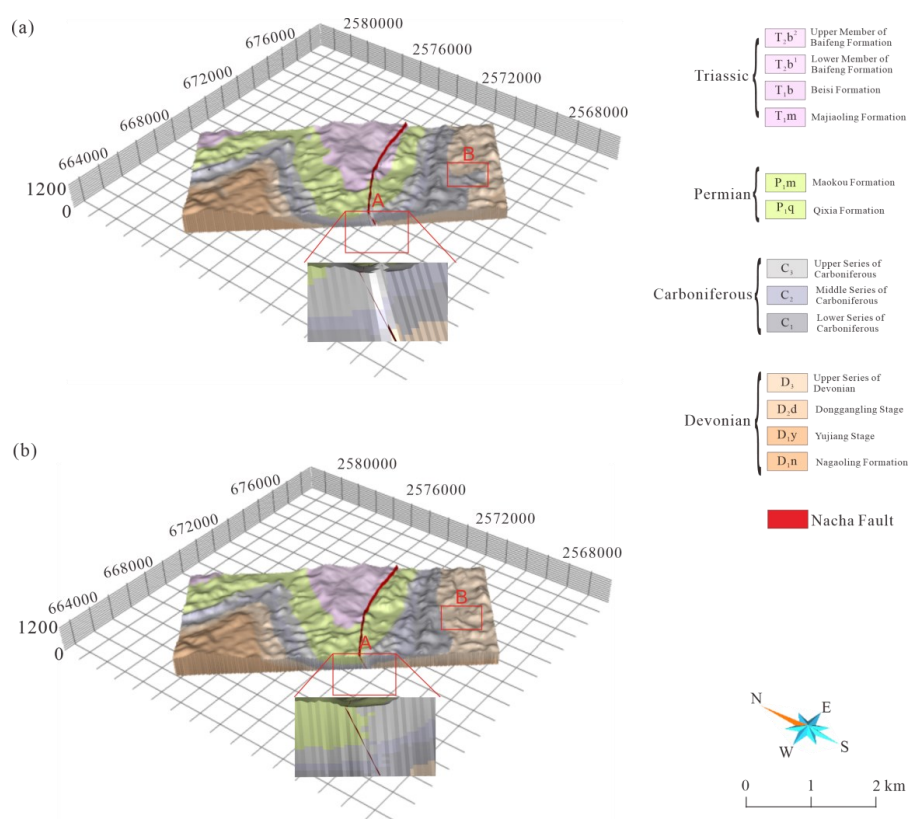
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458 4.3 Lithology Classification

459 The proposed Geo-SAN method establishes an inherent coupling between scalar
460 field and lithological categories, thereby enabling direct prediction of lithological
461 classes. In contrast, the AdaHRBF method derives lithological categories indirectly
462 through inequalities of scalar field. Constrained by the DEM surface, two stratigraphic
463 models were reconstructed (Figure 15). Both approaches yield stratigraphic models that
464 reasonably reproduce the major geological structures in the study area, including
465 Synclines I and III and Anticline II. The stratigraphic model generated by the AdaHRBF



466 method, however, has local unnatural stratigraphic forms (marked in red), and high
 467 levels of inconsistency in stratigraphic ordering and thickness distribution on both sides
 468 of fault-involved areas. In contrast, the Geo-SAN -based model has good stratigraphic
 469 continuity within these structurally complex areas and displays no apparent
 470 stratigraphic sequence or thickness anomaly.

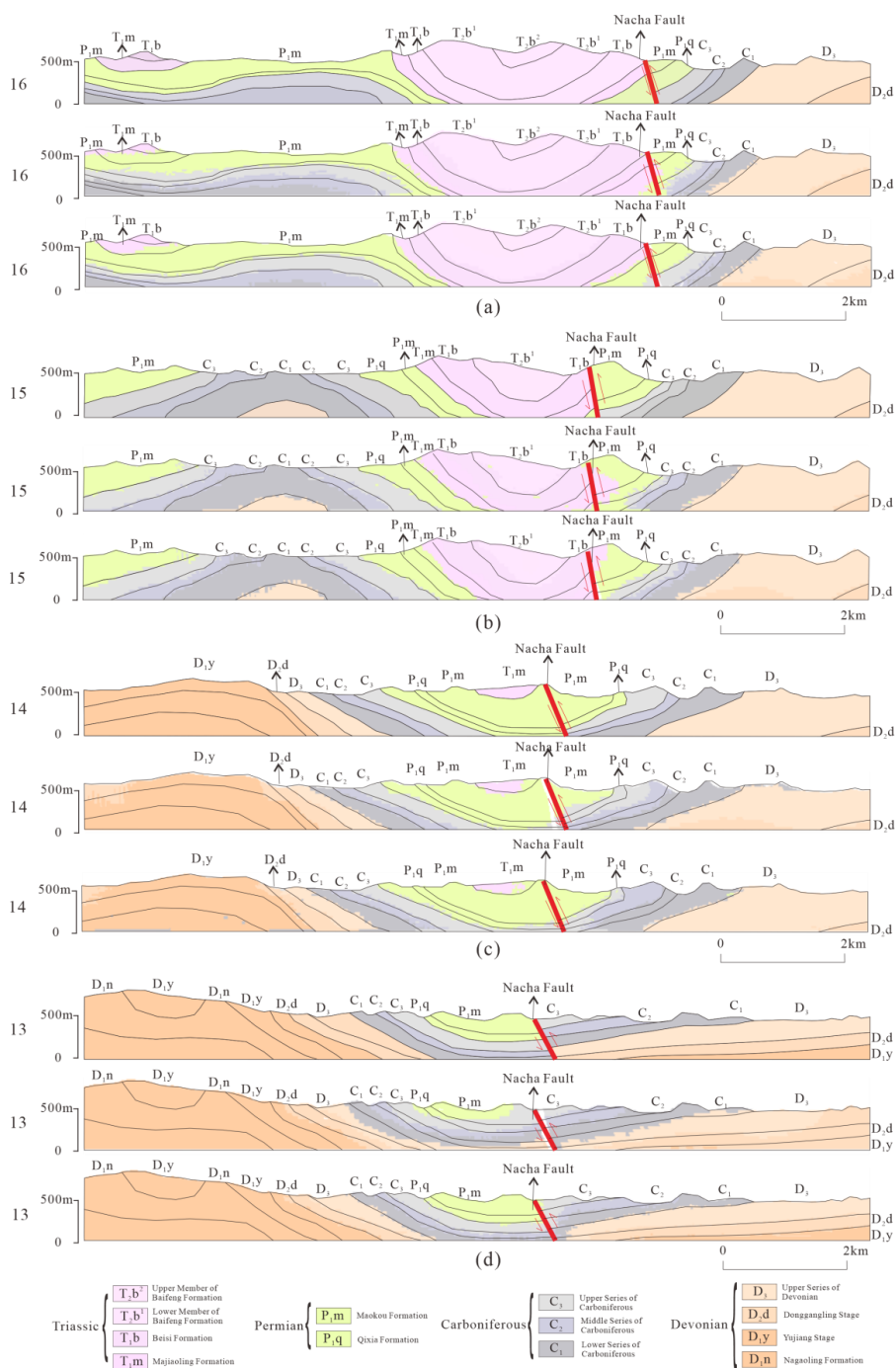


471

472 Fig. 15. Three-dimensional stratigraphic models by (a) AdaHRBF and (b) Geo-SAN.

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474 Four geological cross-sections are extracted out of the 3D stratigraphic models by
 475 AdaHRBF and Geo-SAN, as shown in Figure 16. Cross-sections gained in the
 476 AdaHRBF model indicate unnatural stratigraphic forms that show pronounced
 477 inequalities in stratigraphic sequence and changes in thickness on both sides of fault-
 478 involved areas. Conversely, the Geo-SAN approach exhibits remarkable stratigraphic
 479 consistency in these regions, with no discernible sequence flaws.



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Fig. 16. Compare the cross-section Nos. of (a) 16, (b) 15, (c) 14, and (d) 13 generated by actual, AdahRBF and Geo-SAN models.



483 **5 Discussions**

484 This study presents a 3D geological modelling framework, Geo-SAN, which is
485 founded upon a dual-task stratigraphy-aware attention network. Unlike conventional
486 implicit modelling methods, which rely on interpolation algorithms and the solution of
487 large-scale linear equations, the suggested method utilizes the message-passing
488 capabilities of GNNs to obtain the multi-scale aggregation of geological data, which is
489 highly effective in overcoming the spatial modelling issues of sparse and irregular
490 sampling points. The scheme is capable of dynamically modifying its feature
491 aggregation strategy based on the lithological similarity and stratigraphic relationship
492 so that a smooth incorporation of data-driven learning and knowledge-driven
493 stratigraphic sequence constraints can be incorporated.

494 Hillier et al. (2021) used GNNs operating on tetrahedral meshes to perform
495 coupled implicit scalar field modeling and lithological classification. Gao and
496 Wellmann (2025) introduces a fault encoding scheme, in which discontinuous fault data
497 is added as extra binary feature (0/1) to observation and query point positions that allow
498 the neural network to learn to jump the scalar field at faults and to remain continuous
499 elsewhere. The novelty of this paper is based on two main points compared to current
500 deep learning methods: (1) introducing a stratigraphy-aware attention mechanism that
501 incorporates lithological similarity and stratigraphic sequence instead of using pure
502 data-driven fitting to solve the problem, and (2) developing a dual-task framework to
503 establish a cross-task constraints for the link between the scalar field and lithology.

504 Ablation experiments show that removing the SAN module leads to a 8% decline
505 in classification accuracy, underscoring the essential role of stratigraphical sequence
506 prior knowledge in constraining feature aggregation and improving model robustness.
507 This SAN module applied successfully to 3D geological modelling does not only
508 increase the reliability of the modelling but also offers reference methodology on how
509 to resolve a wide variety of geoscience inverse problems, such as structural
510 reconstruction, geophysical parameter inversion, and subsurface petrophysical property
511 estimation.

512 Despite these advances, there are still several limitations. First, the framework is
513 still conditional upon training data density and exhibits observable performance
514 regression in case of extremely sparse sampling. Second, the existing framework is
515 highly developed to stratified geological bodies and its applicability to more complex



516 geological structures, including igneous intrusions, salt domes, and very heterogeneous
517 mixed rocks, has not been confirmed. Third, model interpretability is still limited, and
518 it would be required to conduct more theoretical research on the geological
519 interpretation and internal learning processes of attention weights. Therefore, future
520 improvements are suggested on: (1) active learning to optimize sampling strategy and
521 minimize reliance on the spatial distribution of dataset, (2) adding structural constraint
522 pattern or modeling strategies that use topological relationships to better express
523 irregular boundaries, complicated contact relationships, and spatial topology, and (3)
524 utilizing statistical analysis of attention weight distributions and feature sensitivity
525 analysis to investigate focus of the models under diverse geological settings and their
526 correlation with genuine geological control elements.

527 **6 Conclusions**

528 This study addresses the computational inefficiency, limited capacity for
529 constraint integration, and inadequate treatment of spatial discontinuities commonly
530 encountered by traditional geological implicit modelling methods when dealing with
531 complex geological structures. We introduce a 3D geological modelling framework,
532 Geo-SAN, which consists of a dual-task stratigraphy-aware attention network, and
533 allows the joint optimization of lithological classification and scalar field interpolation.
534 The proposed method obtains a lithological classification accuracy of 92.1% and an R^2
535 of 0.96 to predict scalar field.

536 The principal contributions of the study include the following: (1) A multi-scale
537 graph neighborhood aggregation mechanism is developed by alternately integrating
538 GAT and GraphSAGE message-passing layers, which effectively extracts
539 representative features from sparse and irregular sampling data; (2) The stratigraphy-
540 aware attention mechanism is proposed, which uses knowledge of stratigraphic
541 sequence and lithological similarity directly as a part of the feature aggregation
542 mechanism; (3) A dual-task learning architecture is constructed that will complete the
543 task of lithological classification and scalar field prediction simultaneously.

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552 Central South University for providing MapGIS® software (Wuhan Zondy Cyber-Tech
553 Co. Ltd., Wuhan, China).

554 **Code and Data availability**

555 The Geo-SAN v1.0 is available from the GitHub (<https://github.com/Geo3D-AI->
556 [CSU/Geo-SAN](https://github.com/Geo3D-AI-CSU/Geo-SAN)) under the Creative Commons Attribution 4.0 License. The exact
557 version of the model used to produce the results used in this study is archived
558 on Zenodo under DOI: 10.5281/zenodo.19903694 (Fang and Zhang, 2026), as are input
559 data and scripts to run the model and produce the plots for all the simulations presented
560 in this study.

561 **CRedit author statement**

562 **ZF:** Methodology, Software, and Writing—original draft preparation. **TZ:**
563 Software and Writing—original draft preparation. **WC:** Data curation. **YS:**
564 Investigation and Funding acquisition. **SYAS:** Conceptualization and Writing—review
565 and editing. **OABKK:** Validation and Data curation. **BZ:** Conceptualization, Validation,
566 Writing—review and editing, and Funding acquisition.

567 **Conflict of interest**

568 The authors declared that there is no conflict of interest.

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