



1 **A hybrid model based on Boruta feature selection and** 2 **neural network for forecasting hydrological drought**

3 Min Li¹, Yuhang Yao¹, Ming Ou¹, Changman Yin¹

4 ¹College of Hydraulic Science and Engineering, Yangzhou University, Yangzhou, China, 225000

5 *Correspondence to:* Min Li (limintju@126.com)

6 **Abstract:** Accurate hydrological drought prediction is vital for water management. This study proposes
7 a hybrid model combining Boruta feature selection, convolutional neural network (CNN), and
8 bidirectional long short-term memory (BiLSTM) methods, to predict hydrological drought in the Huaihe
9 River Basin of China. The Boruta algorithm selected key predictors from 31 potential drought-
10 influencing factors. By comparing the established model Boruta-CNN-BiLSTM with other models,
11 including Boruta-CNN-LSTM, Boruta-CNN-XGBoost, Boruta-BiLSTM, Boruta-LSTM, and Boruta-
12 XGBoost, the results show Boruta significantly enhances all models. The Boruta-CNN-BiLSTM model
13 has achieved the highest accuracy across 28 basin grid regions, exhibiting the largest performance gains.
14 Furthermore, the prediction performance of the model is mainly influenced by factors such as
15 precipitation, volumetric soil water (0-7cm), volumetric soil water (7-28cm) and surface net solar
16 radiation. The model's prediction performance is most affected by precipitation, followed by volumetric
17 soil water (0-7cm), volumetric soil water (7-28cm), and surface net solar radiation has the least impact.
18 It provides enhanced support for basin-scale drought risk assessment and water resources management.

19 **Keywords:** Drought forecasting; hybrid machine learning; Boruta; SRI; Huaihe River Basin

20 **1 Introduction**

21 Drought is one of the most widespread natural disasters globally, causing significant economic
22 losses (Apurv et al., 2017; Dikshit and Pradhan, 2021; Zhou et al., 2021; Li et al., 2024). In recent years,
23 the frequency of drought events has increased due to global warming in the climate, posing severe threats
24 to food production and water resource management (Zhang et al., 2019; Zhang et al., 2022; Wang et al.,
25 2022). Therefore, the development of accurate drought prediction models is crucial for enhancing
26 drought resilience, effectively managing water resources, and reducing drought-related losses.



27 However, the complex nature of droughts and their variability across different regions make
28 monitoring and predicting droughts inherently challenging. To address these challenges, researchers have
29 developed various drought indices, such as the Palmer Drought Severity Index (PDSI) (Palmer, 1965),
30 the Standardized Precipitation Index (SPI) (McKee et al., 1993), and the Standardized Runoff Index (SRI)
31 (Shukla and Wood, 2008). Each drought index has its unique advantages and limitations. The SRI index
32 has been widely adopted in many studies to characterize hydrological droughts (Li et al., 2019; Kubiak-
33 Wójcicka and Juskiewicz, 2020; Kadapala et al., 2024; Liu et al., 2024a). Because it provides a reliable
34 measure of drought severity based on runoff data and is easy to calculate, versatile, and capable of
35 assessing droughts over multiple time scales (Achite et al., 2023). Hence, this study employs the SRI to
36 characterize hydrological droughts.

37 In recent years, machine learning has been very popular in the field of drought prediction (Sun and
38 Scanlon, 2019; Ardabili et al., 2020; Zounemat-Kermani et al., 2021; Gyaneshwar et al., 2023).
39 Numerous studies have shown that models such as Support Vector Machines (SVM), Random Forests
40 (RF), Convolutional Neural Networks (CNN), and Long Short-Term Memory Networks (LSTM)
41 perform strongly in predicting drought events, particularly when dealing with complex, nonlinear data
42 (Chen et al., 2024; Elbeltagi et al., 2023; Khan et al., 2020; Kheyri et al., 2023; Kuswanto and Naufal,
43 2019; Liu et al., 2024b; Zhu et al., 2021). However, single models often fail to perform well in many
44 complex hydrological situations. To overcome these limitations, existing hybrid models attempt to
45 combine the strengths of multiple models. For instance, Wu et al. (2022) demonstrated that integrating
46 atmospheric circulation models with a dynamic LSTM hybrid model can significantly improve seasonal
47 drought prediction accuracy in China. Similarly, Xu et al. (2022) employed an ARIMA-LSTM hybrid
48 model to enhance drought prediction capabilities based on the Standardized Precipitation
49 Evapotranspiration Index (SPEI). Yalcin et al. (2023) utilized a model combining CNN and LSTM,
50 which exhibited significant advantages in the time series prediction of drought indices, particularly in
51 processing complex time series data, thereby improving spatiotemporal consistency and prediction
52 accuracy. While these hybrid models have achieved significant advancements by leveraging the strengths
53 of multiple models, they still face major challenges in feature selection. Poor feature selection can lead
54 to unstable model performance and increased computational costs, limiting the overall effectiveness of
55 these approaches (Karbasi et al., 2024). Therefore, it is necessary to explore optimized feature selection



56 methods to enhance the stability and accuracy of these models when applied to complex drought
57 prediction scenarios.

58 Given the importance of feature selection, optimizing this aspect is crucial for improving the
59 performance of machine-learning models in drought prediction (Li et al., 2017; Prodhan et al., 2022;
60 Nandgude et al., 2023). Previous studies have demonstrated that advanced feature selection techniques
61 can significantly enhance model performance. For example, Karbasi et al. (2024) utilized the Boruta
62 feature selection algorithm for feature selection and combined it with a Bidirectional Long Short-Term
63 Memory Network (BiLSTM), which significantly improved the performance of the model in pan
64 evaporation forecasting, especially under complex climatic conditions, achieving higher predictive
65 accuracy. Sayyad et al. (2022) showed that a hybrid feature selection method combining Random Forest
66 and Principal Component Analysis (PCA) can effectively reduce feature redundancy, thereby enhancing
67 model accuracy and robustness in tool wear prediction. Ahmed et al. (2021) combined a feature
68 extraction algorithm based on the Boruta-Random Forest approach with an LSTM model to predict river
69 water levels, which effectively improved the predictive performance of the model. As a powerful feature
70 selection method, the Boruta-random forest hybridizer algorithm is particularly noteworthy. It can
71 identify the features that are most relevant to the target variable and eliminate unnecessary features
72 (Kursa et al., 2010; Christ et al., 2017; Prasad et al., 2019; Subbiah et al., 2023). These selected features
73 are then used as inputs to various nonlinear models. By integrating feature selection with advanced
74 machine learning techniques, the overall predictive performance can be significantly enhanced.

75 Most existing models still have significant limitations in feature selection, failing to fully consider
76 multidimensional data characteristics in complex hydrological environments, resulting in unstable
77 performance when dealing with highly nonlinear data. Furthermore, although hybrid models have
78 attempted to combine the advantages of multiple algorithms, they still lack in optimizing the matching
79 between input features and model structures, leading to limitations in prediction accuracy. Based on these
80 shortcomings, the primary objective of this study is to develop a novel hybrid machine learning model,
81 the Boruta-CNN-BiLSTM model, to improve the accuracy of hydrological drought prediction. First, the
82 study aims to accurately select features most relevant to hydrological droughts using the Boruta-random
83 forest hybridizer algorithm, thereby reducing feature redundancy and mitigating the overfitting risk.
84 Second, these selected features will be combined with the CNN-BiLSTM model to fully leverage the

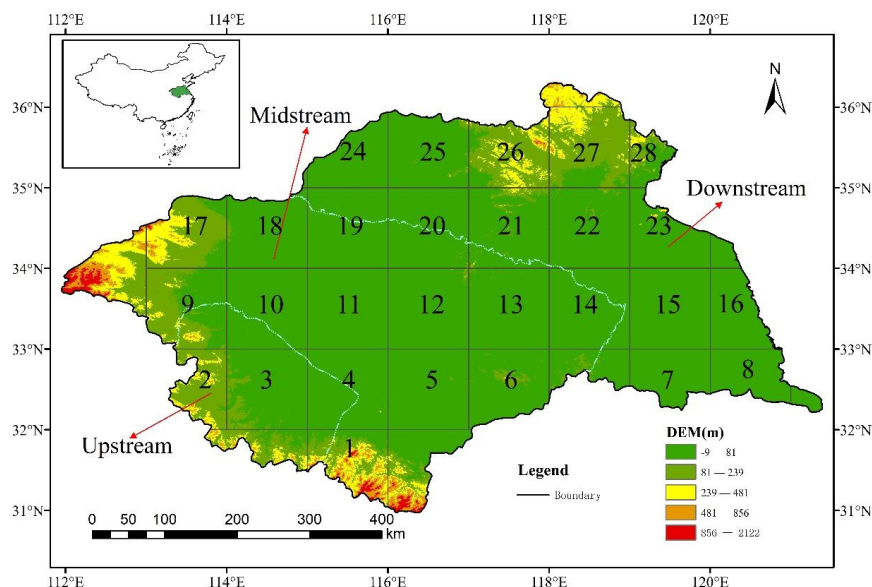


85 spatial feature extraction capabilities of CNN and the temporal data processing capabilities of BiLSTM,
86 enhancing the predictive performance of the model in complex hydrological dynamics. Finally, the study
87 also aims to validate the performance of the Boruta-CNN-BiLSTM model in drought prediction from
88 2011 to 2020 using actual data from 28 regions in the Huaihe River Basin and compare it with other
89 models to determine its applicability and superiority under different spatial conditions, providing
90 important references and insights for future drought prediction research.

91 **2 Study area and data**

92 **2.1 Study area**

93 In this paper, as shown in Fig 1, the Huaihe River Basin is selected as the research area, and the grid
94 is divided at a resolution of $1^{\circ}\text{lat}\times 1^{\circ}\text{lon}$, with a total of 28 grid areas. The Huaihe River Basin is located
95 in eastern China, between $111^{\circ}55'-121^{\circ}20'$ E and $30^{\circ}55'-36^{\circ}20'$ N, covering an area of approximately
96 270,000 square kilometers. The basin is located in the north-south climate transition zone of China. The
97 north of the Huaihe River is a warm temperate zone, and the south of the Huaihe River is a northern
98 subtropical zone. The climate is mild, and the annual average temperature is 11-16 °C. The temperature
99 change in the basin increases from north to south and from coast to inland. The amount of evaporation is
100 small in the south and large in the north. The annual average water surface evaporation is 900-1500 mm.
101 The average annual precipitation in the Huaihe River Basin is about 920 mm, and its distribution is
102 roughly decreasing from south to north. Mountainous areas are greater than plains, and coastal areas are
103 greater than inland. Due to recurrent droughts in winter and spring, coupled with high temperatures and
104 intense rainfall during summer and autumn, the Huaihe River Basin is highly susceptible to extreme
105 climatic events (Yang et al., 2016). The frequent droughts in the basin cause significant losses to the local
106 area every year. On average, 2.698 million hectares of crops are affected every year, accounting for 21 %
107 of the total area of cultivated land in the basin.



108 **Figure 1: Huaihe River Basin and 28 grid region location.**

109 **2.2 Data**

110 The monthly datasets for rainfall, 2m dewpoint temperature, evapotranspiration, runoff, surface net
111 solar radiation, surface pressure, soil temperature at different depths (0-7cm, 7-28cm, 28-100cm), and
112 Volumetric soil water at different depths (0-7cm, 7-28cm, 28-100cm) for the Huaihe River Basin,
113 covering the period from 1960 to 2020, were obtained from the ERA5-Land reanalysis dataset
114 (<https://cds-beta.climate.copernicus.eu/>). Grid analysis was conducted at a resolution of 1°lat×1°lon,
115 covering a total of 28 grid points. Using the interpolation method in array, the data of Huaihe River Basin
116 are interpolated into 28 grid regions.

117 In this paper, the potential climate prediction factors for the Huaihe River basin, such as Nino3.4,
118 Atlantic Multidecadal Oscillation (AMO), Pacific Decadal Oscillation (PDO), Arctic Oscillation (AO),
119 and Trans-Niño Index (TNI) data, were obtained from the National Oceanic and Atmospheric
120 Administration (NOAA) website (<http://www.esrl.noaa.gov/psd/data/climateindices/>)(1960-2020).



121 **3 Methods**

122 **3.1 Drought index**

123 The standardized runoff index (SRI), as an effective and accurate index to describe hydrological
124 drought characteristics, was first proposed by Shukla and Wood (2008). SRI is a standardized
125 hydrological drought index based on runoff data, which can be used to compare and analyze hydrological
126 drought at different times and spaces. In this study, the SRI-1 index, calculated at a monthly scale, is
127 used as the target variable for predicting hydrological drought conditions. Moreover, SRI is simple in
128 calculation and flexible in use and has been widely used in hydrological drought identification. The
129 calculation method of SRI is as follows:

130
$$f(x) = \frac{x^{\alpha-1} e^{-\frac{x}{\beta}}}{\beta^{\alpha} \Gamma(\alpha)} \quad (1)$$

131
$$F(x) = \int_0^x f(x) dx \quad (2)$$

132 Assuming that the precipitation series x at a certain time scale follows a stationary gamma
133 distribution, where α and β are the scale and shape parameters ($\alpha > 0, \beta > 0$). The cumulative
134 probability $F(x)$ of each item is normalized to obtain the corresponding SRI.

135 **3.2 Boruta-feature selection algorithm**

136 Feature selection is a critical step in enhancing the performance of machine learning models, aimed
137 at improving predictive accuracy by selecting the most relevant input features. The Boruta algorithm, an
138 extension of the random forest method, derives its name from the Slavic mythological deity of the forest
139 (Breiman, 2001). Boruta evaluates the importance of each input predictor by comparing it to a set of
140 “shadow features” (randomly generated irrelevant features) using Z-scores, which represent the ratio of
141 mean loss to standard deviation (Kursa et al., 2010). This study utilizes the Boruta algorithm to select
142 significant drought-influencing factors from 31 potential predictors, including climate indices, soil
143 temperature, and precipitation. The algorithm employs a recursive feature elimination strategy, ranking
144 features based on their Z-scores and selecting those with significant contributions. Feature importance is
145 determined by examining the residuals from the Boruta process. In this study, the feature selection



146 process was implemented using the Boruta package in R, ensuring efficiency and stability in identifying
147 the most significant features for model construction.

148 3.3 Machine learning models

149 3.3.1 XGBOOST

150 The Extreme Gradient Boosting (XGBoost) is an ensemble learning algorithm in the Boosting
151 category. It utilizes decision trees as its fundamental elements and implements the gradient boosting
152 algorithm to minimize loss when adding new models (Chen and Guestrin, 2016). XGBoost is designed
153 to improve both the training speed and the predictive performance of gradient-boosted decision trees.

154 Assuming we have K base models denoted as $f_t(x) \in F$, $t = 1, 2, \dots, K$, where F is the model space
155 containing all the base models, the XGBoost model can be represented using the following function:

$$156 \hat{y} = F(x) = \sum_{t=1}^k f_t(x) \quad (3)$$

157 Where the parameters of the XGBoost model consist of the structure of each tree and the scores in
158 the leaf nodes, that is the learning of each function $f_t(x)$.

159 As each base model is generated in a certain sequential order, the creation of the subsequent tree
160 takes into account the predictions made by the preceding tree. Therefore, the objective function of the t
161 base model can be expressed as follows:

$$162 y^{(t)} = \sum_{i=1}^n l(y_i, \hat{y}_i^{(t-1)} + f_t(x_i)) + \Omega(f_t) \quad (4)$$

163 Here, $l(y_i, \hat{y}_i^{(t-1)})$ represents the loss function related to $y_i, \hat{y}_i^{(t-1)}$, $y_i^{(t-1)}$ denotes the predictions
164 of the first $t-1$ decision trees for the sample i (i.e., the sum of predictions made by the first $t-1$
165 trees), y_i represents the actual value of the sample i , $f_t(x_i)$ represents the prediction of the t
166 decision tree for sample i , and $\Omega(f_t)$ represents the model complexity of the t tree. Therefore,
167 the predictions of the first k trees for the sample i are equal to the predictions of the first $k-1$
168 trees plus the prediction of the k tree.

169 3.3.2 LSTM

170 The long short-term memory network (LSTM) model is a variant of recurrent neural network (RNN),
171 which is specifically used to process time series data (Hochreiter and Schmidhuber, 1997). In recording



172 long-term sequence data, RNN will lead to gradient disappearance or gradient explosion due to the
 173 continuous accumulation of information, which makes it difficult for the network to learn long-term
 174 dependence (Jaseena and Kovoor, 2021). The LSTM model is designed for this problem. Mainly through
 175 the gating mechanism to adjust the information to solve. The LSTM model consists of four interacting
 176 layers: input gate, forgetting gate, unit state gate, and output gate, as shown in Figure 2. The input gate
 177 determines which new information will be stored in the storage unit. The forgetting door determines
 178 which information is forgotten by the memory unit. The cell state is responsible for transmitting and
 179 storing long-term memory information so that long-term dependencies can be better captured when
 180 processing long-sequence data. The output gate is the neural layer used to calculate the output value at
 181 the current moment. The mathematical description of the LSTM model is as follows:

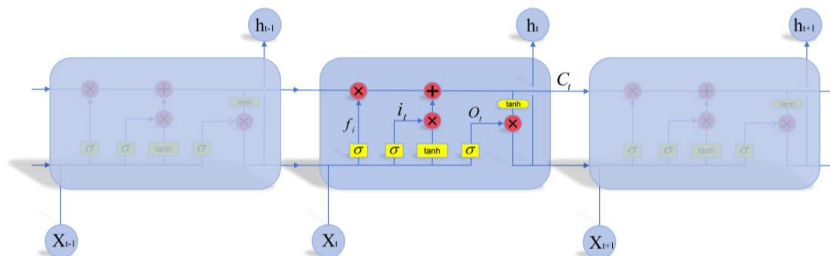
$$182 \quad i_t = \sigma(W_i \cdot [h_{t-1}, x_t]) \quad (5)$$

$$183 \quad f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f) \quad (6)$$

$$184 \quad C_t = f_t \cdot C_{t-1} + i_t \cdot \tanh(W_c \cdot [h_{t-1}, x_t] + b_f) \quad (7)$$

$$185 \quad O_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \quad (8)$$

186 Where i , f , C , and O donate the input gate, forget gate, cell state, and output gate, respectively. σ
 187 and \tanh donate sigmoid and hyperbolic tangent activation functions, respectively. x_t , t , W , and b
 188 donate input vector, time, a weight matrix, and the bias vectors, respectively.



189 **Figure 2: Structure of the LSTM model.**

190 **3.3.3 BiLSTM**

191 In a traditional unidirectional LSTM model, the input is processed in only one direction, utilizing
 192 information derived from past states. In contrast, a Bidirectional Long Short-Term Memory Network
 193 (BiLSTM) consists of two layers of LSTM: one processes the input sequence in the forward direction,



194 while the other analyzes it in the backward direction (Schuster and Paliwal., 1997). The forward layer
 195 captures information from previous time steps, whereas the backward layer (also known as the reverse
 196 LSTM) captures information from future time steps in the input sequence. Figure 3 shows the BiLSTM
 197 model structure.

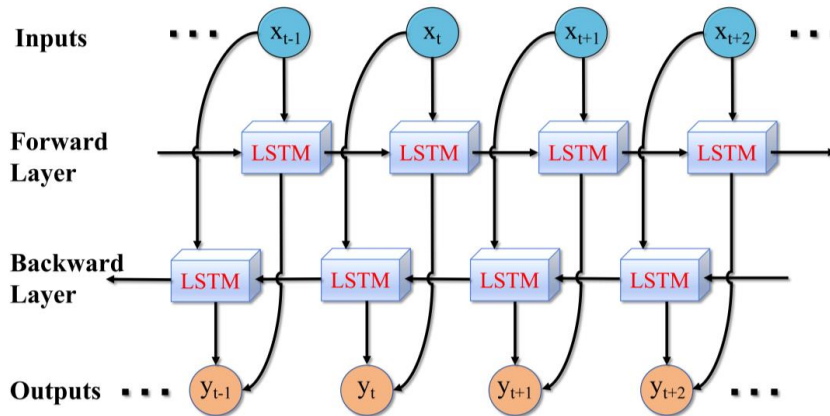
198 After passing through both layers, the outputs from the forward and backward passes are combined
 199 for further processing. In a BiLSTM network, the hidden state at each time step (h_t) comprises three
 200 components: the forward hidden vector (h_t^{forward}), the backward hidden vector (h_t^{backward}), and the
 201 current input (x_t). The hidden state for each time step can be represented as follows (Joseph et al., 2022):

$$202 \quad h_t^{\text{forward}} = \text{LSTM}(x_t, h_{t-1}^{\text{forward}}) \quad (9)$$

$$203 \quad h_t^{\text{backward}} = \text{LSTM}(x_t, h_{t-1}^{\text{backward}}) \quad (10)$$

$$204 \quad y_t = \alpha_t h_t^{\text{forward}} + \beta_t h_t^{\text{backward}} + C_t \quad (11)$$

205 Here, LSTM () refers to the standard mechanism of the LSTM network. The terms α_t and β_t
 206 denote the forward and backward output weights of the hidden layer, respectively, while C_t is the bias
 207 optimization parameter at time t .



208 **Figure 3: Structure of the BiLSTM model.**

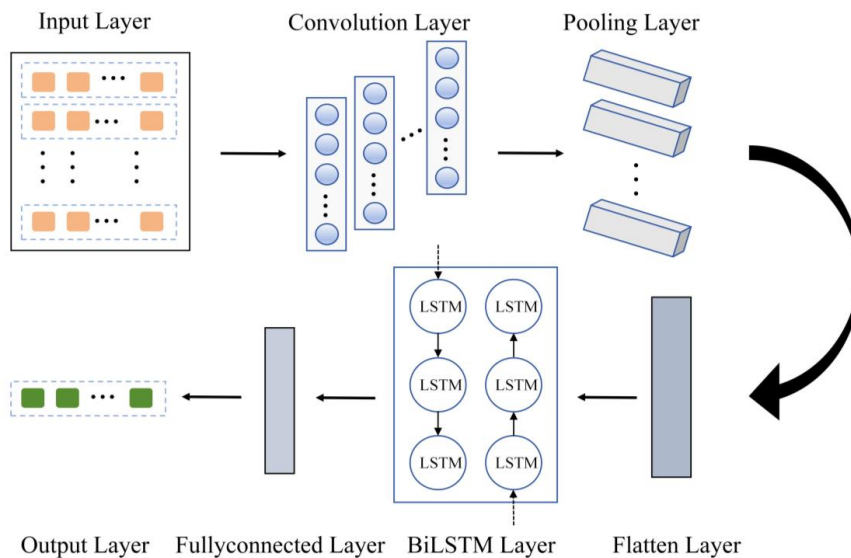
209 3.3.4 CNN-BILSTM

210 Convolutional Neural Networks (CNNs) are a class of feedforward neural networks characterized
 211 by convolutional computation and deep structures. The core idea of CNN is to construct multiple
 212 convolutional filters that can extract features from data. Using a hierarchical convolutional structure,



213 CNNs can capture hidden topological features within input data (Choi and Kil, 2021). As the network
214 depth increases, the extracted features become more abstract. These abstract features are then integrated
215 through fully connected layers and processed by activation functions such as softmax or sigmoid for
216 classification or regression tasks (Li et al., 2024).

217 CNNs and BiLSTM models are two crucial deep-learning techniques. CNN is more suitable for
218 spatial expansion, which can effectively extract local features and combine them into high-level feature
219 representations. BiLSTM is more suitable for time expansion has strong long-term memory ability and
220 is ideal for processing time scales (Lin et al., 2023). By fully combining the strengths of both approaches,
221 time series data processing can be significantly improved. Figure 4 shows the CNN-BiLSTM hybrid
222 model structure.



223 **Figure 4: Structure of the CNN-BiLSTM Hybrid Model.**

224 3.4 Hyperparameter tuning

225 Hyperparameter optimization can improve the performance and efficiency of machine learning
226 model prediction. The Bayesian optimization algorithm using the Bayesian theorem can make full use of
227 the evaluation information of the previous function. It can select the next most promising sampling point
228 according to the posterior distribution of the objective function. The Bayesian optimization algorithm
229 can achieve the global optimal solution of the function with fewer iterations, so it is more suitable for the



230 hyperparameter search optimization problem of the deep learning model (Wu et al., 2023). The short
231 pseudo-code is shown in Table 1.

232 **Table 1: Algorithm: Bayesian Optimization for Hyperparameter Tuning.**

Input: Objective function $f(\cdot)$, hyperparameter domain X , initial sample size n_0 , total budget N

Randomly sample n_0 points $\{x_i\}$ and evaluate $\{y_i = f(x_i)\}$

$D \leftarrow \{(x_i, y_i)\}$

While $|D| < N$:

Train Gaussian Process (GP) on D to obtain mean $\mu_n(x)$ and variance $\sigma_n(x)$

Construct acquisition function $a(x)$

Select next sampling point $x_{\text{next}} = \operatorname{argmax}_x a(x)$

Evaluate $y_{\text{next}} = f(x_{\text{next}})$. Train model and compute validation metric.

Update dataset $D \leftarrow D \cup \{(x_{\text{next}}, y_{\text{next}})\}$

end while

Output: optimal hyperparameters corresponding to the best validation metric in D .

233 3.5 Performance Indicators

234 This study used five indicators to evaluate the predictive performance of the proposed machine
235 learning model: coefficient of determination (R^2), root mean square error (RMSE), mean absolute error
236 (MAE), mean square error (MSE) and normalized root mean square error (NRMSE). R^2 measures the
237 proportion of variance in the observed data interpreted by the model. The closer the value is to 1, the
238 higher the prediction accuracy is. RMSE calculates the square root of the average square difference
239 between the predicted value and the observed value, reflecting the overall size of the prediction error.
240 MAE represents the average absolute difference between the predicted value and the observed value,
241 and describes the accuracy of the model on a more interpretable scale. MSE is the mean of the square
242 difference between the predicted value and the observed value, which emphasizes the larger error.
243 NRMSE is obtained by dividing RMSE by the range of observed values, thus providing a standardized
244 prediction error metric that can be directly compared between different data sets and regions.

245 These five indicators provide a comprehensive evaluation of model performance from multiple
246 perspectives. These indicators are expressed as follows:



$$R^2 = 1 - \frac{\sum_i (\bar{y}_i - y_i)^2}{\sum_i (\bar{y}_i - y_i)^2} \quad (12)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad (13)$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (14)$$

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (15)$$

$$NRMSE = \frac{\sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}}{\max(y_i) - \min(\bar{y}_i)} \quad (16)$$

Where y_i represents the actual observed values, \bar{y}_i is the mean of the actual observed values, \hat{y}_i denotes the predicted values from the model, and n refers to the length of the time series. When the RMSE, MAE, NRMSE, and MSE approach zero, it indicates that the prediction error of the model is minimal. Additionally, when R^2 approaches 1, it suggests that the model demonstrates strong predictive accuracy.

3.6 Convergent Cross Mapping (CCM)

Convergent cross mapping (CCM) is adopted to assess nonlinear causal linkage between a potential driver X and a response Y based on delay-embedding reconstruction (Sugihara et al., 2012). Let $X = \{x(1), x(2), \dots, x(L)\}$ and $Y = \{y(1), y(2), \dots, y(L)\}$ be two monthly time series with $L = 120$. CCM relies on the premise that, if X influences Y , information about Y can be recovered from the manifold reconstructed from X , and such recovery skill should increase and stabilize as the library size grows. Given the assumed one-way influence, X is treated as the cause and the predicted SRI-1 series is treated as the effect Y . The simple procedural steps for the calculation of CCM are presented as follows:

(1) Reconstruct the shadow manifold. A delay-embedded vector is formed from X to represent the system state:

$$x(t) = \{X(t), X(t - \tau), \dots, X(t - (E - 1)\tau)\}, t = 1 + (E - 1)\tau, \dots, L \quad (17)$$

where E is the embedding dimension and τ is the lag step. The $\tau = 2$ and the $E = 3$ is adopted in this study.

(2) Search nearest neighbors and assign weights. For each point $x(t)$ on M_x , its $E + 1$ nearest neighbors $x(t_i)$ are identified based on Euclidean distances $d[x(t), x(t_i)]$. The weights are computed as:

$$w_i = \frac{m_i}{\sum_{j=1}^{E+1} m_j}, (i = 1, 2, \dots, E + 1) \quad (18)$$



274
$$m_i = \exp^{-\frac{d[x(t),x(t_i)]}{d[x(t),x(t_1)]}} \tag{19}$$

275 where t_1 is the index of the closest neighbor.

276 (3) Estimate Y via cross mapping. Using the weighted neighbors, the cross-mapped estimate of
 277 Y is obtained by:

278
$$\hat{y}(t)|M_x = \sum_{i=1}^{E+1} w_i y(t_i) \tag{20}$$

279 (4) Evaluate cross-map skill and test convergence. The CCM skill is measured by the correlation
 280 ρ between $\hat{y}(t)|M_x$ and the original Y . Causality is supported only when ρ shows a convergent
 281 pattern with increasing library size. In this study, the coefficient of variation $C_v < 0.1$ is used as a
 282 necessary criterion to indicate convergence (Zhou et al., 2023). Given the assumed one-way influence,
 283 the drivers are treated as the cause (X) and the predicted SRI-1 series is treated as the effect (Y); the
 284 converged ρ is interpreted as the causal strength.

285 **4 Results**

286 To validate the performance of the proposed machine learning hybrid model, the proposed model
 287 predicts hydrological drought conditions in 28 grid regions of the Huaihe River Basin using monthly
 288 scale data of different drought-influencing factors from 1960 to 2020. The calibration period of the model
 289 is from 1960 to 2010, and the verification period is from 2011 to 2020. To construct six different machine
 290 learning models for each grid region, the Boruta feature selection algorithm was applied to select relevant
 291 drought-influencing factors from a total of 31 drought-influencing factors. The selected features were
 292 then inputted into six machine learning models, with the output value being a 1-month time scale
 293 SRI(SRI-1). Due to space constraints, this study takes four representative grid regions as the analysis
 294 object, which are the 1st, 7th, 17th, and 21st regions.

295 **Table 2: Drought influencing factors input by the Boruta feature selection algorithm (T is the lead time,**
 296 **SPI-1, SPI-3, SPI-6, and SPI-9 are SPI values at different monthly scales).**

Drought influencing factors	
1	SPI-1
2	SPI-3
3	SPI-6
4	SPI-9
5	T=1 SPI-1
6	T=1 SPI-3
7	T=1 SPI-6



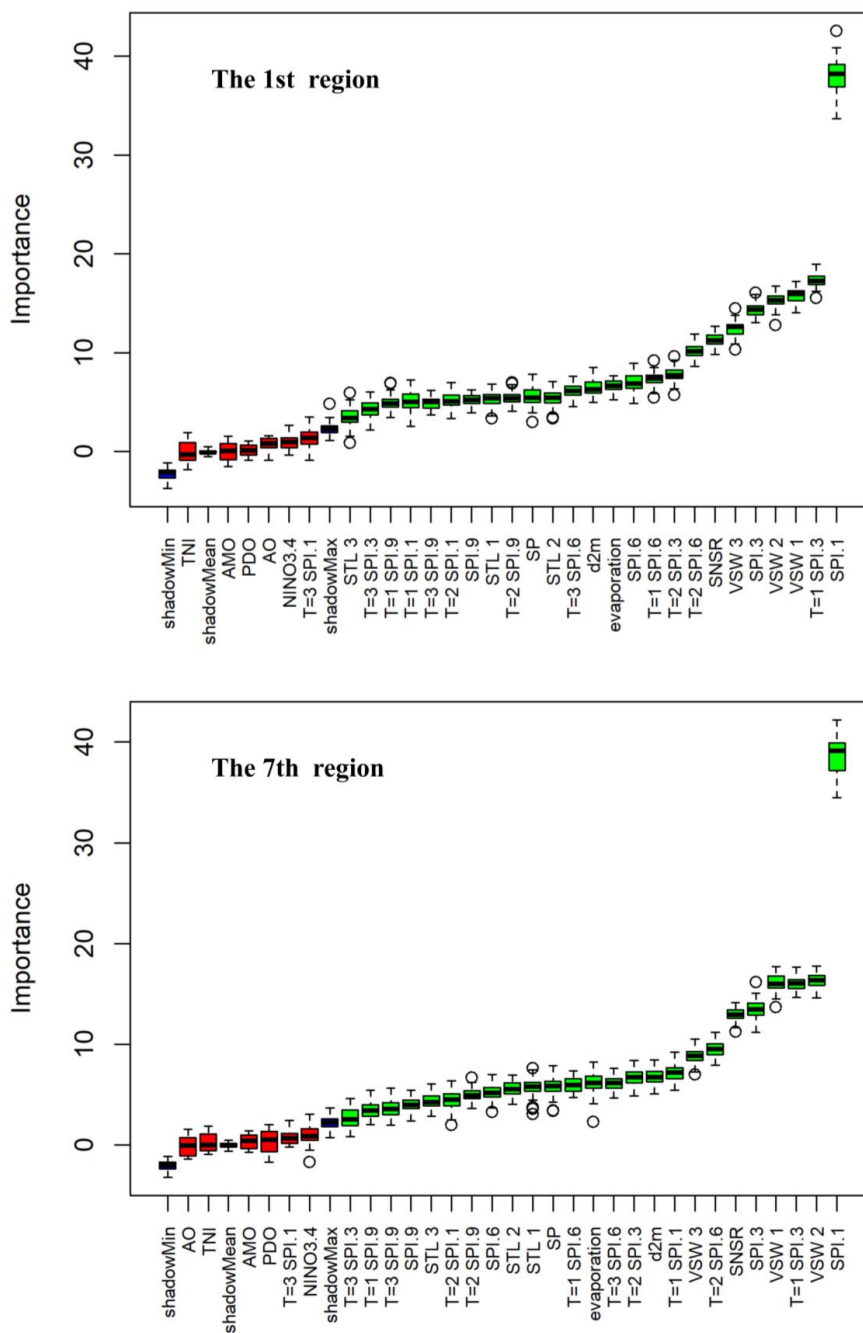
8	T=1 SPI-9
9	T=2 SPI-1
10	T=2 SPI-3
11	T=2 SPI-6
12	T=2 SPI-9
13	T=3 SPI-1
14	T=3 SPI-3
15	T=3 SPI-6
16	T=3 SPI-9
17	d2m temperature
18	surface pressure
19	evapotranspiration
20	surface net solar radiation (SNSR)
21	soil temperature (0-7cm) (STL1)
22	soil temperature (7-28cm) (STL2)
23	soil temperature (28-100cm) (STL3)
24	volumetric soil water (0-7cm) (VSW1)
25	volumetric soil water (7-28cm) (VSW2)
26	volumetric soil water (28-100cm) (VSW3)
27	Nino3.4
28	AMO
29	PDO
30	AO
31	TNI

297 **4.1 Feature selection**

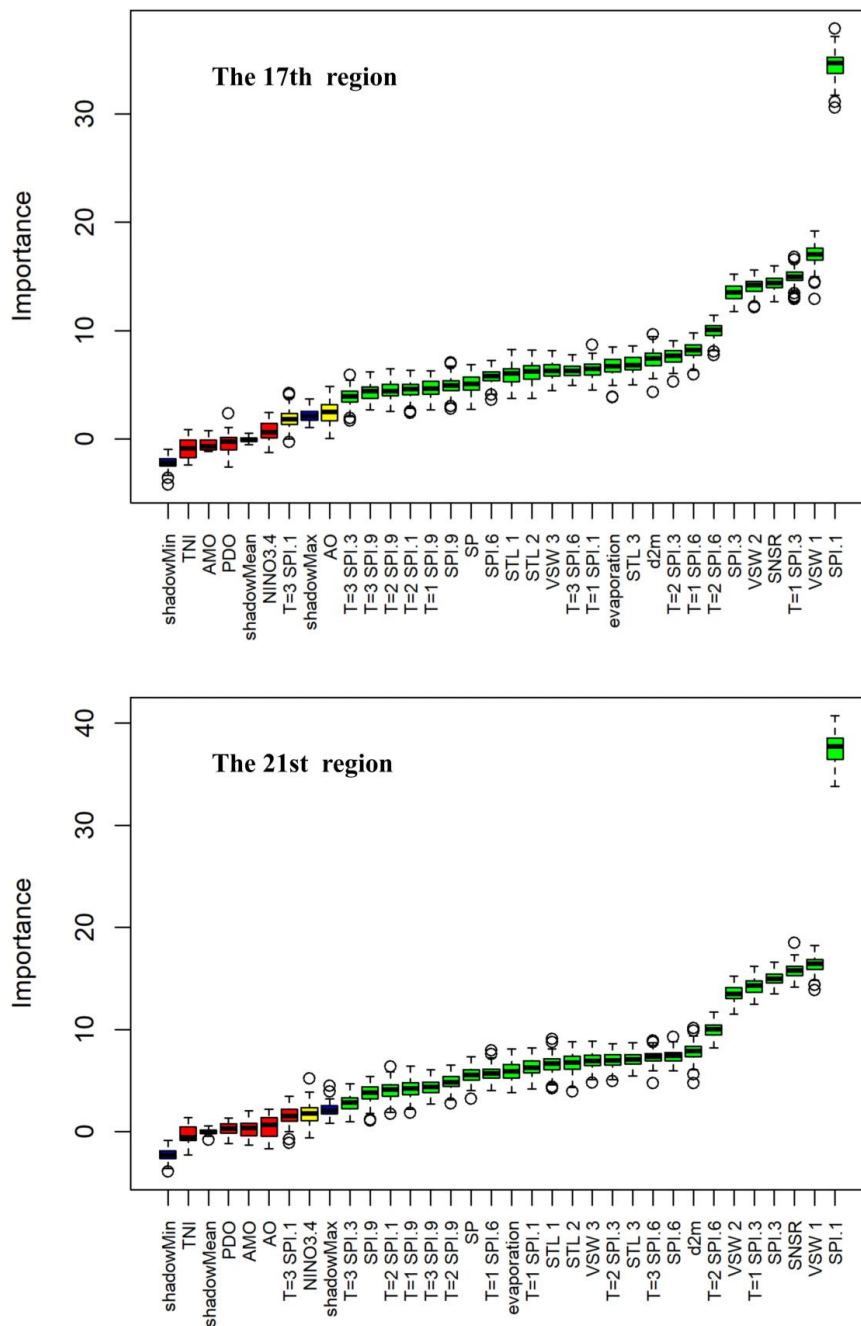
298 To enhance the prediction performance of the model, 35 drought-influencing factors are selected
 299 using the Boruta feature selection algorithm. Figure 5 and Figure 6 show Boruta feature selection results
 300 in four grid regions. Green represents the features that have a significant contribution to the model
 301 prediction results, and these features are considered important. Red represents unimportant features,
 302 indicating that these features have no significant contribution to model prediction. Blue represents
 303 shadow features, which are randomly disrupted features for comparison with actual features to determine
 304 whether actual features are more important than random features. Yellow represents the undetermined
 305 feature, that is, the importance of the feature is uncertain. In this paper, the Boruta feature algorithm
 306 selects the significant contribution features of green representatives. Boruta feature selection plays a key
 307 role in improving model accuracy by reducing feature redundancy. The selected features, such as SPI-1,
 308 evapotranspiration, and soil temperature, have important contributions to the predictive ability of the
 309 model. Among them, SPI-1 was found to be the most influential feature in all regions, and its importance



310 score exceeded 30, which was much higher than other features, highlighting its importance in
311 hydrological drought prediction. This shows that the addition of relevant climate indices significantly
312 improves the prediction ability of the model in different spatial backgrounds.



313 **Figure 5: The Boruta feature selection results of the 1st and 7th grid regions (SPI.n are SPI values at**
 314 **different monthly scales, n=1,3,6,9).**



315 **Figure 6: The Boruta feature selection results in the 17th and 21st grid regions (SPI.n are SPI values at**
 316 **different monthly scales, n=1,3,6,9).**

317



318 **4.2 Model parameters optimization**

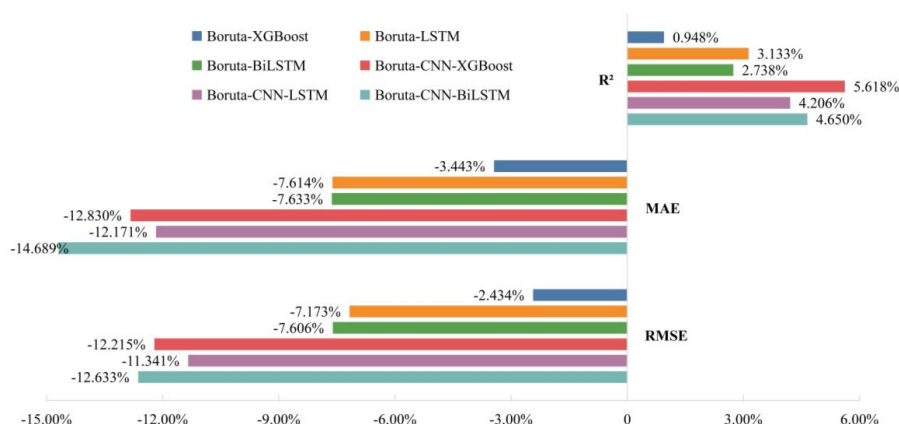
319 In this study, Bayesian optimization is used to fine-tune the hyperparameters of each model to ensure
 320 optimal performance. Table 3 shows the optimized parameters of the six models in the 7th grid region.
 321 For example, in the Boruta-CNN-BiLSTM model, a learning rate of 0.0023 is selected, and 38 Bi LSTM
 322 hidden units and 31 convolutional filters are configured to achieve an optimal balance between model
 323 complexity and generalization ability. This highlights the importance of model parameterization in
 324 effectively capturing cross-regional hydrological dynamics.

325 **Table 3: Parameters of six models in the 7th grid region after Bayesian optimization.**

Model	Parameters
Boruta-CNN-BiLSTM	learningRate:0.0023; BiLSTM numUnits:38; convFilterSize:22; convNumFilters:31; poolSize:2; MaxEpochs:116; dropoutRate:0.34
Boruta-CNN-LSTM	learningRate:0.0038; LSTM numUnits:27; convFilterSize:25; convNumFilters:7; poolSize:4; MaxEpochs:182; dropoutRate:0.22
Boruta-CNN-XGBoost	convFilterSize:3; convNumFilters:13; poolSize:2; num_Trees: 244; eta: 0.177; max_depth:6
Boruta-BiLSTM	numUnits:3; learningRate:0.0216; dropoutRate:0.26; MaxEpochs:216
Boruta-LSTM	numUnits1:10; numUnits2:50; numUnits3:50; learningRate:0.0732; dropoutRate:0.16; MaxEpochs:188
Boruta-XGBoost	eta:0.0746; max_depth:2; num_trees:895

326 **4.3 Model evaluation**

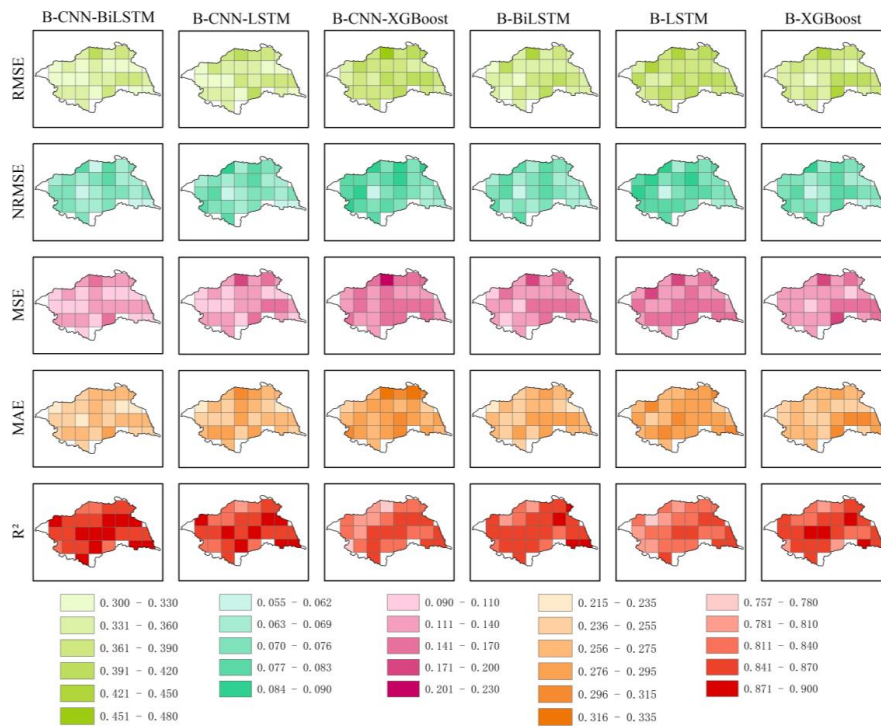
327 Figure 7 shows the average improvement of the prediction performance of each model after using
 328 the Boruta algorithm to filter features. It can be seen from the figure that the prediction performance of
 329 all models has improved, among which the Boruta-CNN-BiLSTM model has the most significant
 330 improvement: RMSE decreased by 12.633%, MAE decreased by 14.689%, and R2 increased by 4.650%.
 331 For other models, for example, the RMSE and MAE of the Boruta-CNN-XGBoost model are reduced by
 332 12.215% and 12.830%, respectively, while the Boruta-XGBoost model has the smallest performance
 333 improvement, and the RMSE is only reduced by 2.434%. This shows that the combination of the Boruta
 334 feature selection method can effectively reduce the feature redundancy of the model and improve the
 335 stability and prediction accuracy of the model under complex hydrological conditions.



336 **Figure 7: The improvement of prediction performance of various models after the application of the Boruta**
 337 **algorithm (The data presented represent the average performance improvement of each model in 28 grid**
 338 **regions).**

339 Table 4 shows the average values of five evaluation indexes (RMSE, NRMSE, MSE, MAE, R²) of
 340 the six models in 28 grid regions. The Boruta-CNN-BiLSTM achieved the lowest average error and the
 341 highest R², confirming its leading performance. Boruta-CNN-LSTM is sub-optimal, while Boruta-
 342 BiLSTM ranks third. Tree-based models and single LSTM perform worse and have higher errors. As
 343 shown in Figure 8, Boruta-CNN-BiLSTM dominates in almost all regions, although Boruta-CNN-LSTM
 344 obtains slightly higher R² in one region, while Boruta-BiLSTM is slightly better in some other regions,
 345 which is consistent with Table 4.

346 In addition, the Boruta-CNN-BiLSTM and Boruta-CNN-LSTM models are superior to the models
 347 without CNN, while the Boruta-CNN-XGBoost model shows the highest error, reflecting its limitations
 348 in capturing complex nonlinear dynamics. These comparisons confirm that combining CNN with
 349 appropriate deep learning and feature selection produces the most robust model.



350

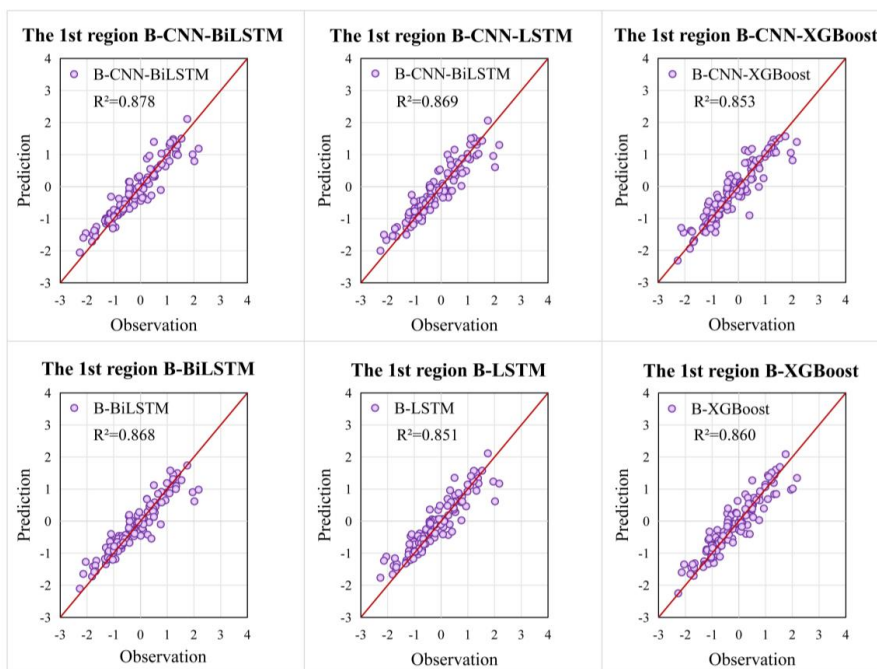
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Figure 8: The spatial distribution of five evaluation metrics for the six models across the 28 grid regions.

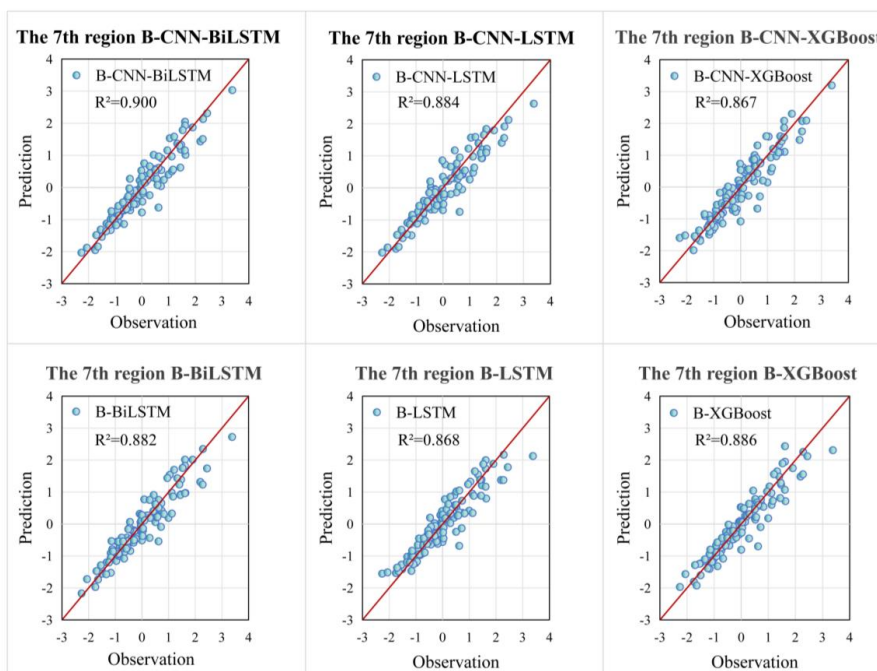
352

Table 4: The average value of five evaluation indexes of six models in 28 grid regions.

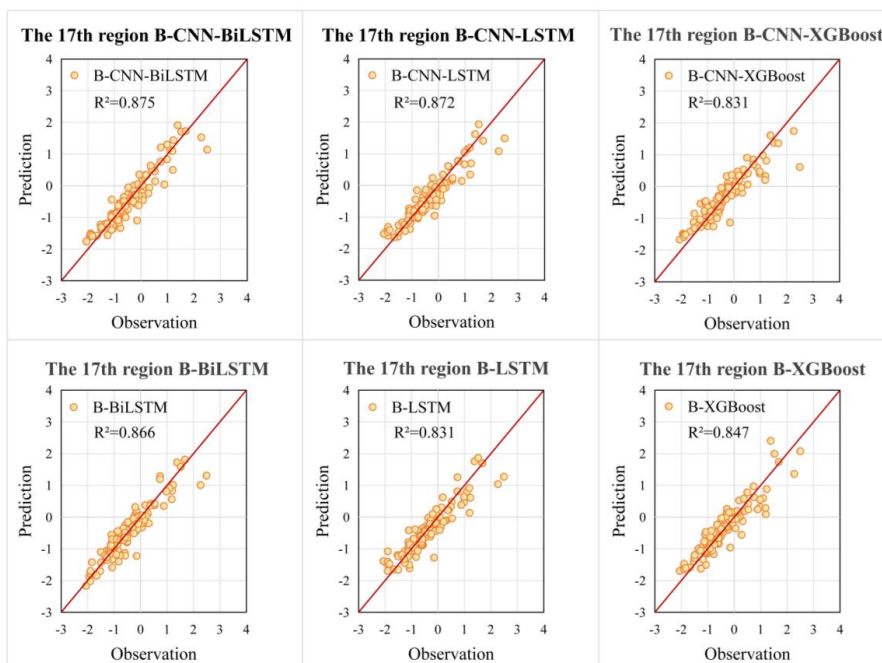
Model	RMSE	NRMSE	MSE	MAE	R ²
Boruta-CNN-BiLSTM	0.341	0.069	0.117	0.252	86.31%
Boruta-CNN-LSTM	0.352	0.071	0.125	0.262	85.35%
Boruta-CNN-XGBoost	0.38	0.077	0.145	0.284	82.93%
Boruta-BiLSTM	0.357	0.072	0.128	0.263	84.89%
Boruta-LSTM	0.383	0.077	0.147	0.279	82.66%
Boruta-XGBoost	0.364	0.073	0.134	0.277	84.38%



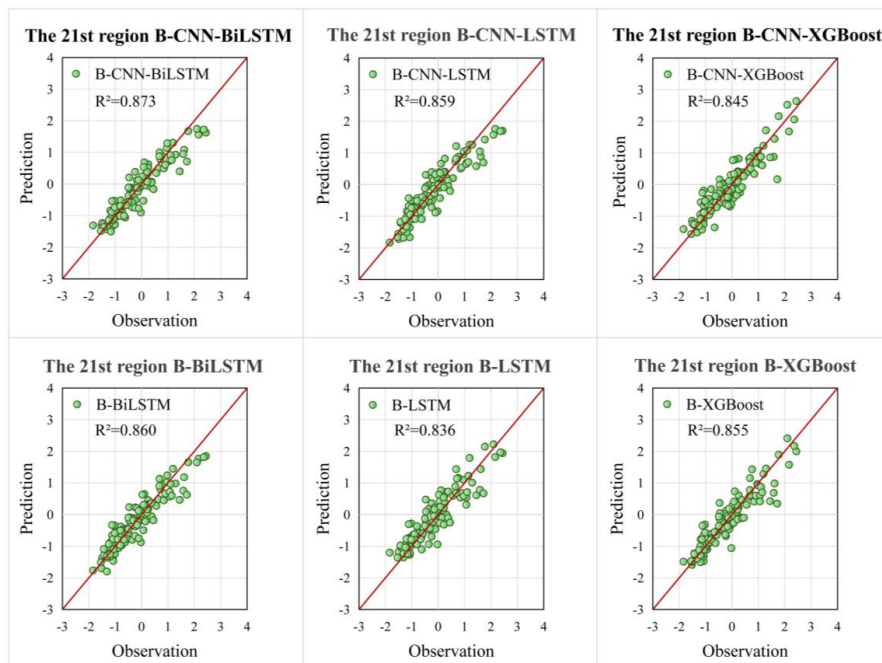
353 **Figure 9: Scatter plot of the 1st grid region model prediction.**



354 **Figure 10: Scatter plot of the 7th grid region model prediction.**



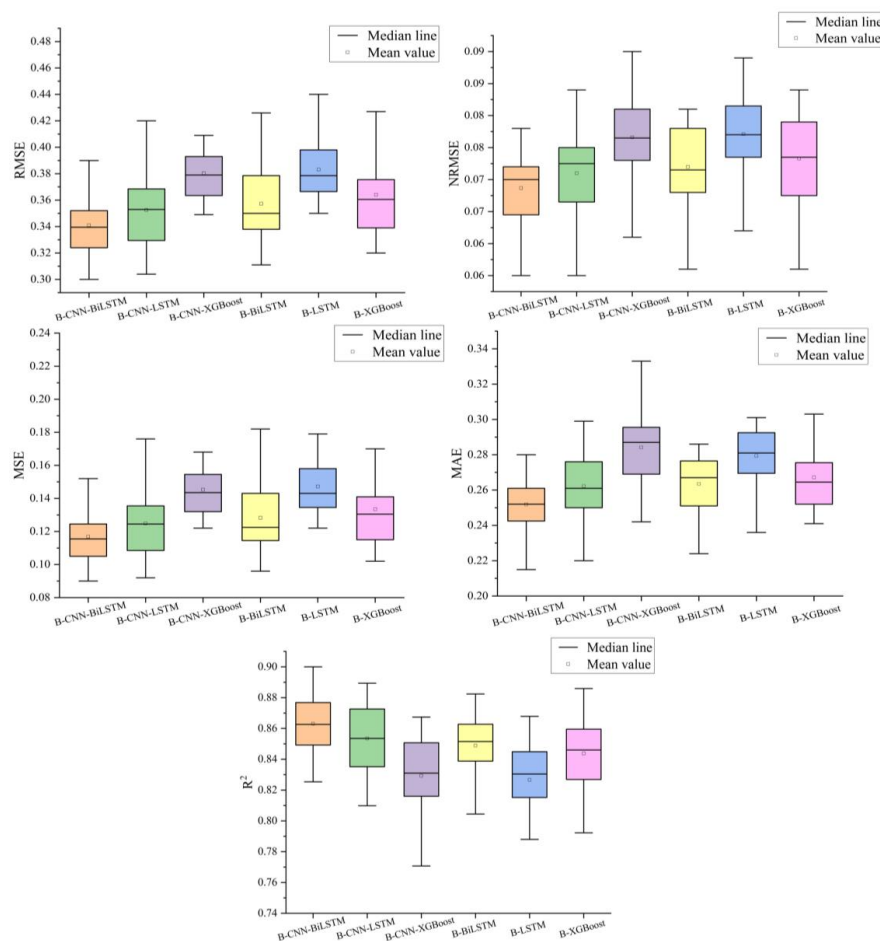
355 **Figure 11: Scatter plot of the 17th grid region model prediction.**



356 **Figure 12: Scatter plot of the 21st grid region model prediction.**



357 To further assess and compare the accuracy of hydrological drought predictions for each model, the
 358 predicted and measured values of each model were linearly fitted. Taking four regions as examples, the
 359 scatter plots of the predicted and measured values of the model in each region are shown in Figures 9-
 360 12. It can be seen that in the four regions, the predicted values of the Boruta-CNN-BiLSTM model are
 361 closely gathered around the diagonal, indicating that the predicted values are in good agreement with the
 362 actual values. In addition, the predictions of the Boruta-CNN-LSTM model in the 1st, 7th, and 17th grid
 363 regions and the Boruta-BiLSTM model in the 21st region are also close to the diagonal. In contrast, the
 364 Boruta-LSTM model in the 1st, 17th, and 21st grid regions and the Boruta-CNN-XGBoost model in the
 365 7th grid region show more data points scattered around the diagonal, indicating weaker performance than
 366 the Boruta-CNN-BiLSTM.

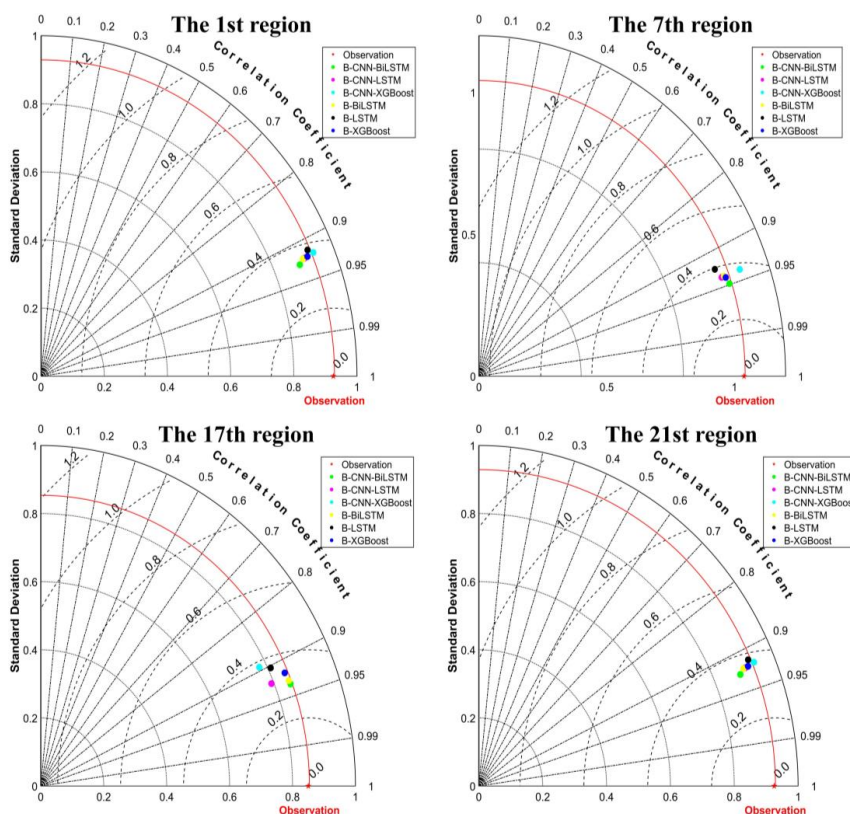


367
 368 **Figure 13: Box plots of six models about five indicators.**



369 In order to provide a comprehensive comparison of model performance, Figure 13 shows a box plot
370 of five evaluation indicators (RMSE, MAE, MSE, NRMSE, R^2) of six models in all regions. It can be
371 seen that the Boruta-CNN-BiLSTM model has always achieved the lowest error value and the highest
372 R^2 value, highlighting its superiority over other models. Specifically, most of the RMSE values remain
373 below 0.35, and the MAE values are generally below 0.26, while MSE and NRMSE remain at the lowest
374 levels in the whole model. This shows that the Boruta-CNN-BiLSTM model not only minimize absolute
375 deviation and square deviation, but also maintains a stable normalized error, thus ensuring robustness
376 and comparability between different regions. In contrast, the Boruta-CNN-XGBoost model showed the
377 highest error level among all indicators, reflecting weak predictive performance. For BiLSTM and LSTM
378 models, prediction accuracy is significantly improved after adding CNN, which confirms the role of CNN
379 in improving spatial feature extraction and model robustness.

380 Figure 14 further illustrates the predictive accuracy of the six models using Taylor diagrams in four
381 representative grid regions (1st, 7th, 17th, and 21st). The Boruta-CNN-BiLSTM model produces
382 predictions most closely aligned with the observed data, showing the highest correlation coefficients and
383 the smallest deviations in all four regions. In the 1st, 17th and 21st grids, the Boruta-BiLSTM model
384 ranks second in accuracy, while in the 7th grid, the Boruta-CNN-LSTM model is the second best model.
385 These results once again highlight the comprehensive advantages of the Boruta-CNN-Bi LSTM model,
386 which combines effective feature selection with strong spatio-temporal expression ability, thus achieving
387 superior performance across multiple evaluation indicators and regional conditions.



388

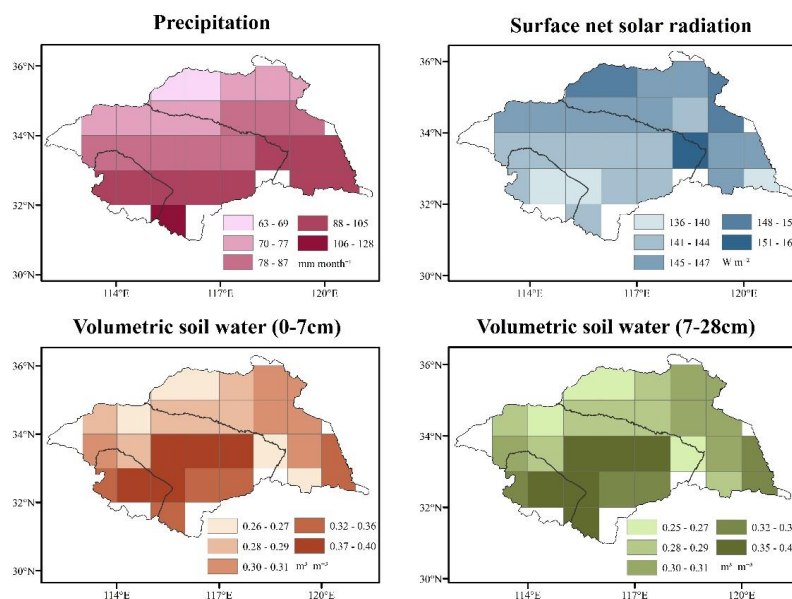
389 **Figure 14: The Taylor diagrams of the six models in the 1st, 7th, 17th, and 21st grid regions.**

390 **5 Discussion**

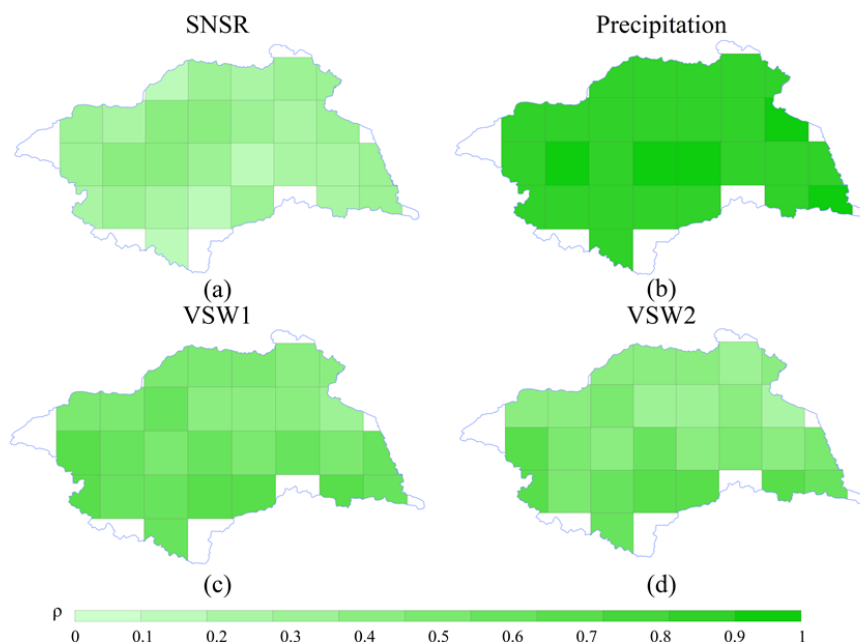
391 In order to analyze the reasons for the spatial differences in the prediction accuracy of the Boruta-
 392 CNN-BiLSTM model, the most influential factors obtained by the Boruta method were selected, namely
 393 precipitation, volumetric soil water (0-7cm), volumetric soil water (7-28cm) and surface net solar
 394 radiation. The CCM method was used to quantify the impacts of each influencing factor on the model
 395 evaluation index R^2 . The results are shown in Figures 16 and 17. According to Figures 15, 16 and 17,
 396 precipitation is the most significant influencing factor affecting the prediction accuracy of the model
 397 across the entire watershed. The mean value of the p -value is close to 0.9, and the range is mainly between
 398 0.8 and 1.0. The data are relatively concentrated, which indicates that the model's prediction accuracy is
 399 sensitive to precipitation and is distributed relatively uniformly in space. However, the precipitation is
 400 unevenly distributed across the basin, with more in the south and less in the north. VSW1 and VSW2 are



401 factors that have a greater impact on model prediction accuracy after precipitation. The mean ρ -value
402 ranging from 0.4 to 0.5, and the range is mainly between 0.2 and 0.7. The wide range of data distribution
403 indicates that the sensitivity of the model's prediction accuracy to precipitation varies significantly in
404 space. The specific manifestation is that the sensitivity in the upper and middle reaches is greater than
405 that in the downstream areas. The distribution of VSW1 and VSW2 across the basin is also uneven, its
406 distribution is consistent with the partial sensitivity. The factor that has the least impact on the model's
407 prediction accuracy is SNSR, with a mean close to 0.2 and a distribution range between 0 and 0.4. This
408 study analyzed the SRI based on a 1-month time scale, constructed several different prediction models,
409 and conducted evaluations. This study analyzed the SRI based on a one-month time scale, constructed
410 several prediction models, and evaluated the effectiveness of the prediction models from multiple aspects.
411 The results show that the Boruta-CNN-BiLSTM model has the most effective prediction effect. However,
412 the SRI on different time scales may have a significant impact on the performance of the prediction model.
413 In addition to that, drought is also affected by human activities, basin geographical features, etc. For
414 future research, the uncertainty of the model's prediction performance due to different time scales and
415 various influence factors can be considered.



416
417 **Figure 15: Spatial distribution maps of monthly mean values of precipitation, volumetric soil water (0-7cm),**
418 **volumetric soil water (7-28cm) and surface net solar radiation in the basin from 1960 to 2010.**



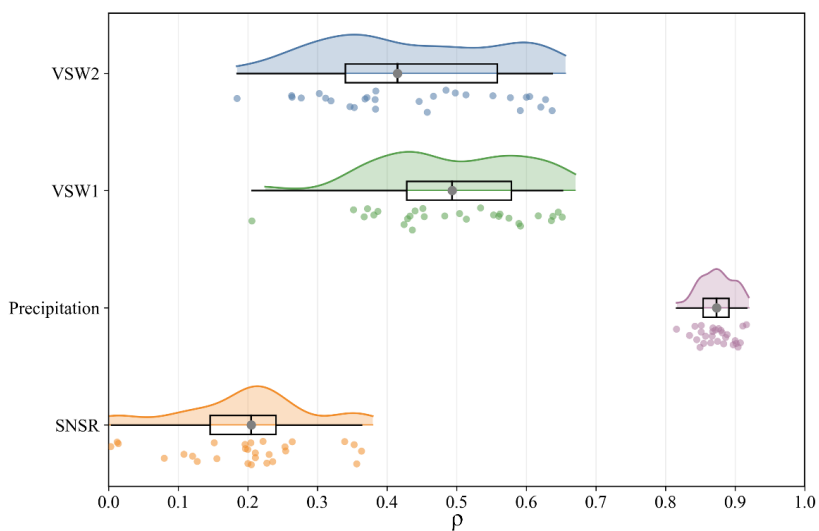
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Figure 16: Spatial distribution of the influence intensity (ρ) of precipitation, volumetric soil water (0-7cm) (VSW1), volumetric soil water (7-28cm) (VSW2) and surface net solar radiation (SNSR) on the prediction accuracy of the Boruta-CNN-BiLSTM model.



423

424

425

Figure 17: Raincloud plots of the influence intensity (ρ) of different factors on the prediction accuracy of the Boruta-CNN-BiLSTM model.



426 **6 Conclusion**

427 This paper proposes an innovative hydrological drought prediction model called Boruta-CNN-
428 BiLSTM, which is a hybrid model of the Boruta feature selection algorithm, a bidirectional long- and
429 short-term memory network (BiLSTM), and a convolutional neural network (CNN). It is used to predict
430 hydrological drought in the Huaihe River Basin in China. In addition, five models, Boruta-CNN-LSTM,
431 Boruta-CNN-XGBoost, Boruta-BiLSTM, Boruta-LSTM, and Boruta-XGBoost were established for
432 comparison. The main conclusions are as follows:

433 (1) The addition of Boruta significantly improved all benchmark models. Among the six models,
434 Boruta-CNN-BiLSTM showed the largest gain, with an average RMSE decrease of 0.42, a mean MAE
435 decrease of 0.32, an average NRMSE decrease of 0.008, a mean MSE decrease of 0.03, and a median R^2
436 increase of 3.65%. It highlights the importance of optimizing feature selection for robust prediction.

437 (2) Boruta-CNN-BiLSTM achieved the highest overall accuracy across all regions. The next best is
438 Boruta-CNN-LSTM. Boruta-LSTM model performs the poorest. Boruta-BiLSTM, Boruta-CNN-
439 XGboost and Boruta-XGboost perform in the middle. These results highlight the robustness of this hybrid
440 approach to capturing the spatial and temporal dynamics associated with hydrological droughts.
441 Compared with other models, the model effectively characterizes complex hydrological patterns and
442 significantly improves drought prediction accuracy in the Huaihe River Basin.

443 (3) The prediction effect of the Boruta-CNN-BiLSTM model is mainly influenced by factors such
444 as precipitation, volumetric soil water (0-7cm), volumetric soil water (7-28cm) and surface net solar
445 radiation. Among them, precipitation has an absolute dominant influence throughout the entire watershed,
446 and the influence varies a little in the spatial distribution of the watershed. Volumetric soil water (0-7cm)
447 and volumetric soil water (7-28cm) follow, and their influences on the model's prediction effect have
448 certain spatial differences. The influence in the middle and upper reaches is more significant than in
449 downstream areas. SNSR has the least influence on the model's prediction effect among the four
450 influencing factors.

451 **Statements & Declarations**

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457 **Competing Interests**

458 The authors declare no conflict of interest.

459 **Author Contributions**

460 All authors contributed this paper: Conceptualization, M L, YH Y; Data curation, YH Y, M L, M O,
461 CM Y; Visualization, YH Y, M L; Validation, M L, YH Y; Methodology, M L, YH Y, M O; Formal
462 Analysis, M L, YH Y; Funding acquisition, M L, YH Y; Writing – original draft, YH Y; Writing – review
463 & editing, M L.

464 **Data availability**

465 We are grateful to the National Oceanic and Atmospheric Administration
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467 European Centre for Medium-Range Weather Forecasts (<https://cds.climate.copernicus.eu/>) for
468 providing monthly mean precipitation, volumetric soil water, evapotranspiration, 2m dewpoint
469 temperature, surface net solar radiation, surface pressure and runoff datasets. The data and materials of
470 this study are available.

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