



# Spatiotemporal optimization of NO<sub>x</sub> and VOC emissions using a hybrid inversion framework and its implication for ozone sensitivity diagnosis

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**Abstract.** Ozone (O<sub>3</sub>) over South Korea has risen in recent years, underscoring the need to accurately quantify emissions of nitrogen oxides (NO<sub>x</sub>) and volatile organic compounds (VOC). We develop a hybrid inverse modeling framework that couples the Finite Difference Mass Balance (FDMB) method with four-dimensional variational (4D-Var) assimilation using the Community Multiscale Air Quality (CMAQ) model to jointly constrain spatiotemporal NO<sub>x</sub> and VOC emissions. The inversion is constrained by Tropospheric Monitoring Instrument (TROPOMI) NO<sub>2</sub> and HCHO columns and by surface NO<sub>2</sub> and O<sub>3</sub> from the Air Quality Monitoring Station (AQMS) network. The analysis covers 1–14 May 2022, a period of climatologically high O<sub>3</sub>. Optimized NO<sub>x</sub> emissions exhibit strong diurnal adjustments relative to the prior (nighttime reductions up to 51 % and daytime increases up to 14 %). The joint inversion of NO<sub>x</sub> and VOC delivers the largest improvement in O<sub>3</sub> simulations, achieving the best agreement with observations (IOA > 0.8). Constrained emissions shift O<sub>3</sub> sensitivity from VOC-sensitive to NO<sub>x</sub>-sensitive across much of the domain, improving spatial consistency with TROPOMI-derived formaldehyde-to-NO<sub>2</sub> ratio (FNR) diagnostics. Adjoint-based hourly ΔO<sub>3</sub> responses reveal regime- and hour-dependent behavior: VOC controls are most effective under VOC-sensitive conditions, whereas NO<sub>x</sub> controls are more direct under NO<sub>x</sub>-sensitive conditions. Importantly, because O<sub>3</sub> titration is immediate while photochemical production requires finite reaction time, emissions released approximately 1–2 hours earlier have the greatest influence on current O<sub>3</sub>, motivating hour-specific, regime-specific controls.



35 Overall, the hybrid framework improves  $O_3$  simulations and sensitivity-regime diagnosis, enabling spatiotemporally resolved precursor emission reduction guidance for effective  $O_3$  mitigation.

## 1 Introduction

Surface ozone ( $O_3$ ) is a highly reactive secondary air pollutant primarily formed through complex photochemical reactions involving nitrogen oxides ( $NO_x \equiv NO + NO_2$ ) and volatile organic compounds (VOC). Elevated  $O_3$  concentrations have been associated with adverse respiratory health outcomes, including asthma and pneumonia, as well as broader impacts on air quality and ecosystem health (Gryparis et al., 2004; Turner et al., 2016; Raza et al., 2018). In recent years, a persistent increase in  $O_3$  levels has been observed across East Asia, leading to a growing demand for scientific investigation into its underlying causes. Previous studies have attributed this increase to multiple factors, including changes in atmospheric circulation patterns due to climate change, enhanced stratosphere–troposphere exchange, and shifts in the  $O_3$  sensitivity regime (Lee et al., 2021; Itahashi et al., 2022; Hou et al., 2023).

Among these factors, shifts in the  $O_3$  sensitivity regime play a key role in understanding the causes of rising recent  $O_3$  levels. The  $O_3$  sensitivity regime refers to the relative responsiveness of  $O_3$  formation to changes in its precursor emissions, primarily  $NO_x$  and VOC. In a VOC-sensitive regime,  $O_3$  production increases when VOC emissions rise, but shows little change or even decreases when  $NO_x$  emissions are reduced. Conversely, in a  $NO_x$ -sensitive regime,  $O_3$  formation responds strongly to reductions in  $NO_x$  emissions. Several recent studies have reported that many regions in East Asia are currently undergoing a transition from a VOC-sensitive regime toward a  $NO_x$ -sensitive or transitional regime, wherein reductions in  $NO_x$  emissions paradoxically result in increased  $O_3$  concentrations (Lee et al., 2021; Itahashi et al., 2022; Wang et al., 2025). Accordingly, the formulation of effective  $O_3$  mitigation strategies necessitates accurate characterization of region-specific sensitivity regimes, which in turn requires an accurate spatiotemporal estimation of  $NO_x$  and VOC emissions.

Emission estimates are typically derived using either bottom-up or top-down approaches. The bottom-up method relies on activity data and emission factors to statistically estimate emissions. While widely used, this approach is subject to high uncertainty due to variability in emission factors, spatial heterogeneity in activity data, and the extensive time and cost required to survey all emission sources (Zhao et al., 2011; Hristov et al., 2017; Solazzo et al., 2021). To overcome these limitations, top-down approaches based on inverse modeling have become increasingly prevalent. These methods assimilate satellite and ground-based observational data with chemical transport models to infer emissions that are consistent with observed atmospheric concentrations (Miller et al., 2014; Cheng et al., 2021). Various inverse modeling techniques have been proposed, including mass balance (Cooper et al., 2017; Li et al., 2019; Qu et al., 2019; Momeni et al., 2024), four-dimensional variational assimilation (4D-Var) (Hu et al., 2022; Voshtani et al., 2023; Nüß et al., 2025), and ensemble Kalman filter (EnKF) methods (Peng et al., 2017; Jia et al., 2022; Wu et al., 2023). The mass balance approaches are computationally efficient and suitable for rapid emission updates, but are known to be susceptible to smearing effects due to pollutant transport (Cooper et al., 2017). Among the mass balance-based methods, the Finite Difference Mass Balance (FDMB) method has been shown to improve



emission estimates by exploiting sensitivities between emissions and column concentrations (Cooper et al., 2017; Mun et al., 2023). In contrast, the 4D-Var approach uses adjoint sensitivity to trace the influence of emission sources backward in time, thereby reducing transport-induced smearing errors (Li et al., 2019). However, it is computationally intensive and requires the development of an adjoint model, which can be a substantial limitation. To leverage the strengths of both approaches, a hybrid inverse modeling framework combining the mass balance and the 4D-Var have been recently proposed (Chen et al., 2021; Choi et al., 2022; Moon et al., 2024).

Nevertheless, most inverse modeling studies have focused primarily on correcting the spatial distribution of emissions, with limited consideration of their temporal variability. This remains a critical limitation, particularly for  $O_3$ , which is both short-lived and chemically reactive. Diurnal variations in precursor emissions can strongly influence  $O_3$  formation due to nonlinear photochemical processes (Wang et al., 2018). Moreover, because  $O_3$  production is jointly controlled by  $NO_x$  and VOC, accurately reproducing  $O_3$  concentrations requires not only capturing the temporal evolution of emissions but also constraining the contributions of both precursor species. Therefore, accurate analysis of  $O_3$  distributions requires a comprehensive inverse modeling framework capable of simultaneously optimizing the spatiotemporal distribution of both  $NO_x$  and VOC emissions.

In this study, we develop a hybrid inverse modeling framework that combines the FDMB and 4D-Var methods with the Community Multiscale Air Quality (CMAQ) model to simultaneously constrain the spatiotemporal distributions of  $NO_x$  and VOC emissions over South Korea, to improve  $O_3$  simulations and sensitivity regime diagnostics, and to quantify hourly  $\Delta O_3$  responses to  $NO_x$  and VOC emissions using adjoint sensitivities. Here,  $\Delta O_3$  represents the change in  $O_3$  concentration attributable to a unit perturbation in precursor emissions, as diagnosed by the adjoint model. The inverse modeling system is constrained using satellite-based measurements from the TROPOspheric Monitoring Instrument (TROPOMI) and in situ observations from the Air Quality Monitoring Station (AQMS) network. We further analyze the changes in  $O_3$  concentrations and  $O_3$  sensitivity regimes before and after inverse modeling to propose a robust top-down emission adjustment approach that can inform the development of future  $O_3$  mitigation policies. The results are presented in four sections: (1) spatiotemporal changes in emissions (Section 3.1), (2) spatiotemporal changes in  $NO_2$ , HCHO, and  $O_3$  concentrations (Section 3.2), (3) improvement of  $O_3$  sensitivity regimes through hybrid inversion (Section 3.3), and (4) regime-dependent hourly  $\Delta O_3$  responses to  $NO_x$  and VOC emissions (Section 3.4).

## 2 Methods

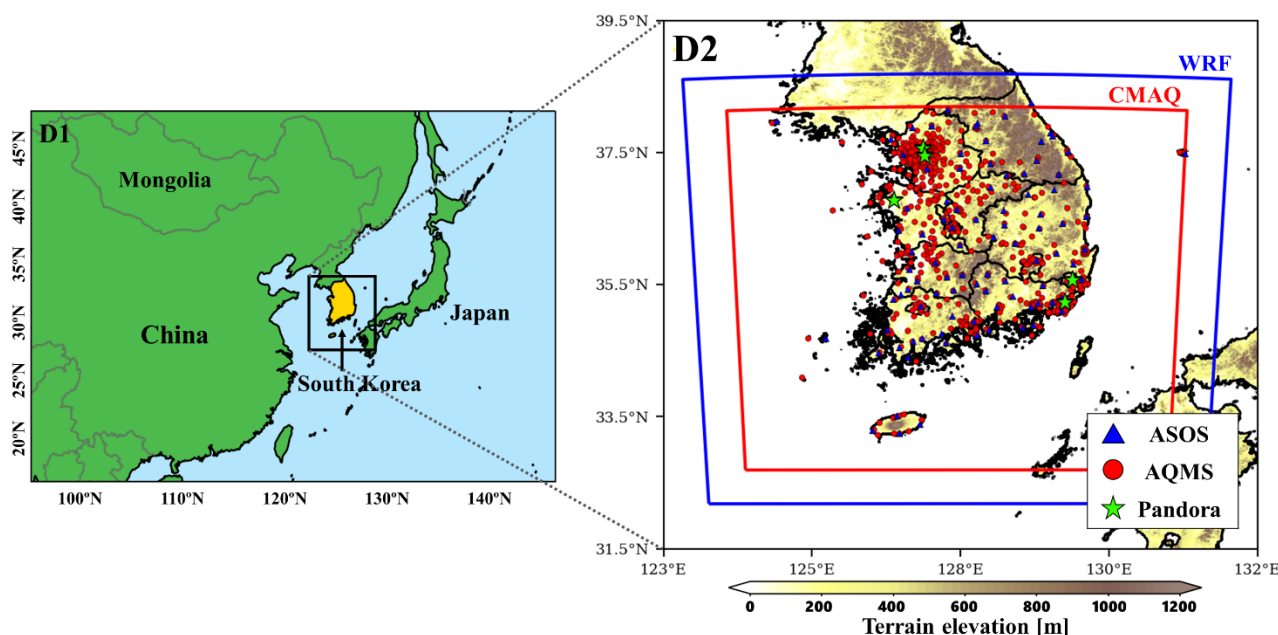
### 2.1 WRF/CMAQ modeling system

In this study, we employed version 5.0 of the Community Multiscale Air Quality (CMAQ) model, developed by the U.S. Environmental Protection Agency (EPA), which includes an adjoint model, to conduct 4D-Var inverse modeling (Zhao et al., 2020). Meteorological input fields required for the CMAQ simulation were generated using the Weather Research and Forecasting (WRF) model version 3.8.1 (Skamarock et al., 2008). The modeling domains consisted of two nested grids: a



coarse-resolution outer domain (D1) covering East Asia and a finer-resolution inner domain (D2) focusing on South Korea (Fig. 1).

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**Figure 1: WRF/CMAQ modeling domains and spatial distribution of observational sites (ASOS: blue triangles; AQMS: red circles; Pandora: green stars).**

105 This study targeted South Korea, and the inverse modeling was conducted exclusively over D2. The initial and boundary conditions for the WRF simulation were obtained from the ERA5 reanalysis dataset with a spatial resolution of  $0.25^\circ \times 0.25^\circ$ , provided by the European Centre for Medium-Range Weather Forecasts (ECMWF) (Hersbach et al., 2023a, b). To improve the accuracy of meteorological fields, grid nudging was applied during WRF simulations (Jeon et al., 2015).

We utilized the Emissions Database for Global Atmospheric Research-Hemispheric Transport of Air Pollution version 3 (EDGAR-HTAPv3) as the source of anthropogenic emissions. This inventory incorporates national emission estimates from South Korea's Clean Air Policy Support System (CAPSS) and provides monthly averaged emissions at a spatial resolution of  $0.1^\circ \times 0.1^\circ$  for nine key air pollutants: BC, CO,  $\text{NO}_x$ ,  $\text{SO}_2$ ,  $\text{NH}_3$ , OC, NMVOC (non-methane volatile organic compounds) or,  $\text{PM}_{10}$ , and  $\text{PM}_{2.5}$  (Crippa et al., 2023). To generate the hourly gridded emissions required for CMAQ modeling, the monthly data were temporally downscaled using sector-specific temporal allocation profiles (Crippa et al., 2020). In addition, biogenic volatile organic compound (BVOC) emissions, which serve as key precursors of  $\text{O}_3$ , were estimated using the Model of Emissions of Gases and Aerosols from Nature (MEGAN) version 2.1 (Guenther et al., 2012).

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The modeling period was set to May 1–14, 2022 (two weeks), selected for computational efficiency during the month that recorded the highest monthly average surface O<sub>3</sub> concentrations over South Korea in the past decade (Fig. S1). Detailed model configurations for both WRF and CMAQ are provided in Tables S1 and S2.

## 2.2 Observation data

### 2.2.1 Ground-based observations

For the evaluation of meteorological and air quality model performance and the implementation of inverse modeling over South Korea, we utilized ground-based observational data from Automated Surface Observing System (ASOS), Air Quality Monitoring Stations (AQMS), and Pandora spectrometers (Fig. 1). Hourly measurements of temperature, wind speed, and relative humidity from 95 ASOS sites were used to assess the accuracy of meteorological simulations. For air quality model evaluation and inverse modeling, we obtained hourly NO<sub>2</sub> and O<sub>3</sub> concentrations from 619 AQMS sites.

In addition, tropospheric HCHO Vertical Column Densities (VCDs) were obtained from Pandora spectrometers at five sites operated by the Pandonia Global Network (PGN) to evaluate the model's performance in simulating VOC. To ensure data reliability, only Pandora HCHO retrievals with Level 2 (L2) data quality flags classified as “high” (0, 10) or “medium” (1, 11) were used in this study (Bae et al., 2025; Fu et al., 2025). The Pandora observations were hourly averaged for comparison with model results.

### 2.2.2 TROPOMI NO<sub>2</sub> and HCHO observations

TROPOMI is the single payload aboard the European Space Agency (ESA)'s Sentinel-5 Precursor (S5P) satellite, launched on October 13, 2017 (Veefkind et al. 2012). Operating in a sun-synchronous polar orbit at an altitude of approximately 800 km, it provides daily global coverage with a high spatial resolution footprint of 5.5 km × 3.5 km at nadir and an equator crossing time near 13:30 local solar time.

Tropospheric VCDs of NO<sub>2</sub> and HCHO used in this study are obtained from the TROPOMI Level 2 operational products (De Smedt et al., 2021; van Geffen et al., 2022). Both products are retrieved using a three-step Differential Optical Absorption Spectroscopy (DOAS) technique: (1) fitting of the Slant Column Density (SCD), (2) separation of the tropospheric components from the total SCD, and (3) conversion from slant to vertical column using an air mass factor (AMF). The retrieval accuracy of VCD is highly sensitive to the a priori vertical profile used in the AMF calculation. In the operational products, these profiles are derived from global simulations of the TM5-MP chemistry model at a coarse resolution of 1° × 1°, which is much coarser than the native resolution of the TROPOMI SCDs. This spatial mismatch has been linked to underestimation of VCDs, particularly over regions with strong or localized emissions (Judd et al., 2020; Douros et al., 2023; Goldberg et al., 2024).

To mitigate this limitation, we recalculate the satellite VCDs using Eq. (1) (Souri et al., 2016), which adjusts the satellite-derived VCDs ( $VCD_{satellite}$ ) by accounting for differences between the a priori profiles used in the satellite retrieval and those from a regional chemical transport model.



$$VCD'_{satellite} = \frac{VCD_{satellite} \times AMF_{satellite}}{AMF_{model}} \quad (1)$$

150  $AMF_{satellite}$  is the AMF provided in the TROPOMI Level 2 product, and  $AMF_{model}$  is a model-derived AMF calculated using the vertical profile from the CMAQ model and the TROPOMI Averaging Kernel (AK) (Eq. (2)).

$$AMF_{model} = AMF_{apriori} \frac{\sum AK \times VCD_{model}}{\sum VCD_{model}} \quad (2)$$

To ensure data quality, we applied a quality assurance threshold of  $qa\_value > 0.75$  for  $NO_2$  (high quality), which is relaxed to  $> 0.5$  for  $HCHO$  (moderate quality) to retain sufficient sampling.

## 2.3 Inverse modeling

### 155 2.3.1 Finite Difference Mass Balance inversion using 3D-Var

The mass balance approach estimates emissions by assuming a linear relationship between observed column concentrations and surface emissions (Cooper et al., 2017). Among the mass balance-based methods, the Finite Difference Mass Balance (FDMB) method, proposed by Lamsal et al., (2011), introduces a scaling factor ( $\beta$ ) to account for nonlinear relationships between changes in column concentrations ( $\Delta\Omega$ ) and emissions ( $\Delta E$ ) (Eqs. (3) and (4)).

$$160 \quad E_{FDMB} = E_m \left( 1 + \frac{\Omega_o - \Omega_m}{\beta \Omega_m} \right) \quad (3)$$

$$\beta = \frac{\Delta\Omega_m / \Omega_m}{\Delta E_m / E_m} \quad (4)$$

Here,  $E_{FDMB}$  represents the FDMB emissions,  $E_m$  is the a priori model emissions,  $\Omega_o$  is the observed column density, and  $\Omega_m$  is the simulated column density. The sensitivity factor  $\beta$  is calculated from simulations using the prior emissions ( $E_m$ ) and emissions perturbed by 10 %.  $\beta$  value is constrained between 0.1 and 10 to prevent unrealistic corrections (Cooper et al., 2017; 165 Li et al., 2019; Mun et al., 2023).

In this study, we applied the FDMB inversion to jointly constrain  $NO_x$  and VOC emissions. We first optimized  $NO_x$  emissions by deriving an emission factor based on the sensitivity of  $NO_2$  columns to  $NO_x$  emissions (Eq. (5)). For VOC, total emissions were separated into anthropogenic VOC (AVOC) and BVOC, as the two categories have distinct VOC species compositions that lead to different  $HCHO$  responses (Millet et al., 2006; Choi et al., 2022; Oomen et al., 2024). We then 170 independently quantified the  $HCHO$  column sensitivities to AVOC and BVOC emissions (Eqs. (6) and (7)). Based on these sensitivities, we derived emission factors for both AVOC and BVOC components.

$$\beta_{NO_x} = \frac{\Delta\Omega_{NO_2} / \Omega_{NO_2}}{\Delta E_{NO_x} / E_{NO_x}} \quad (5)$$

$$\beta_{AVOC} = \frac{\Delta\Omega_{HCHO} / \Omega_{HCHO}}{\Delta E_{AVOC} / E_{AVOC}} \quad (6)$$

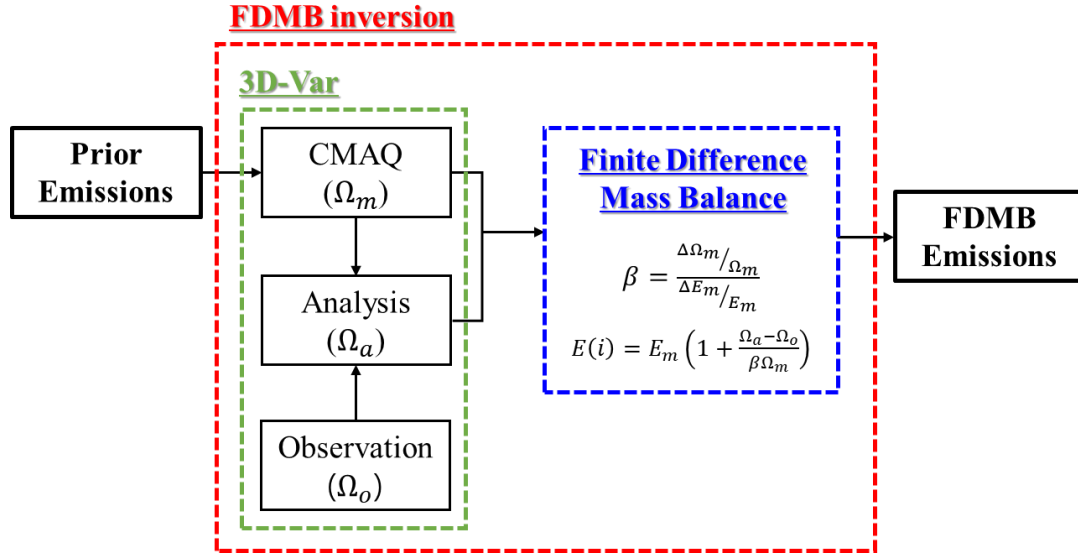
$$\beta_{BVOC} = \frac{\Delta\Omega_{HCHO} / \Omega_{HCHO}}{\Delta E_{BVOC} / E_{BVOC}} \quad (7)$$

175 However, traditional mass balance approaches may incorporate biases inherent in satellite observations into the inferred emission estimates. To address this limitation, East et al. (2022) applied the FDMB inversion using an analysis field generated



via three-dimensional variational (3D-Var) assimilation as the observational constraint. In this study, we generated a 3D-Var-based analysis field to minimize observational uncertainties and employed it as the constraint in the FDMB inversion process (Fig. 2).

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**Figure 2: Flowchart of the FDMB inversion framework with 3D-Var assimilation.** Red boxes denote the FDMB inversion process, green boxes represent the 3D-Var assimilation ( $\Omega_m$ : CMAQ VCD,  $\Omega_o$ : observed VCD,  $\Omega_a$ : analysis VCD), and blue boxes indicate the FDMB process that updates emissions using finite-difference sensitivities.

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Furthermore, to minimize errors associated with the smearing effect caused by atmospheric transport, the FDMB inversion was performed using a two-week-averaged column density over the study period. Consequently, this study focused on constraining the spatial distribution of emissions based on temporally averaged observations, without accounting for temporal variability in emissions.

### 190 2.3.2 4D-Var inversion

While the FDMB inverse modeling enables spatial correction of emissions effectively, it cannot account for their temporal variability. To overcome this limitation, we implemented a four-dimensional variational (4D-Var) inversion approach to constrain the spatial and temporal distribution of emissions. The cost function employed in this study is defined in Eq. (8).

$$J(\alpha) = \frac{1}{2} \gamma \sum_{i=0}^n (\alpha_i - 1)^T B_{e_i}^{-1} (\alpha_i - 1) + \frac{1}{2} \sum_{t=1}^{n+1} \sum_{i=t}^{n+1} (y_i^o - H_{i-1}(e_{i-1}))^T R_i^{-1} (y_i^o - H_{i-1}(e_{i-1})) \quad (8)$$

195 Here, the control variable is the emission ( $e$ ) over a defined time window ( $n$ ), and the emission scaling factor ( $\alpha = e/e^b$ ) represents the ratio between the updated and prior emissions.  $H$  denotes the observation operator,  $y$  is the observation vector, and  $B$  and  $R$  are the error covariance matrices for emissions and observations, respectively. Assuming spatial independence,



both  $B$  and  $R$  were configured as diagonal matrices. The emission uncertainties were set to 100 % of the prior emissions. For ground-based AQMS observations, the total observational error was estimated as the sum of measurement errors with representativeness errors (Elbern et al., 2007; Feng et al., 2018).

In this study, the assimilation time window was set to 24 hours to better represent diurnal variations in atmospheric processes. To prevent overfitting or underfitting in the inversion process, a regularization parameter  $\gamma$  was introduced (Henze et al., 2009; Chen et al., 2021; Yu et al., 2021), and its optimal value was determined using the L-curve test (Hansen, 1999). The optimized  $\gamma$  was then used to constrain the spatiotemporal distribution of emissions, ensuring physically realistic corrections.

### 2.3.3 Hybrid inverse modeling framework

In this study, we applied the hybrid inverse modeling framework proposed by Moon et al. (2024) to constrain the spatiotemporal distribution of  $\text{NO}_x$  and VOC, which are key precursors influencing  $\text{O}_3$  formation and destruction. The hybrid inverse modeling approach consists of a two-step process: an initial adjustment of the spatial distribution of emissions using the FDMB method, followed by a refinement of the spatiotemporal distribution through 4D-Var inverse modeling. While previous studies have primarily focused on single-species corrections such as CO or  $\text{NO}_2$ , we extended the approach to jointly optimize both  $\text{NO}_x$  and VOC emissions to better represent the nonlinear photochemical processes governing  $\text{O}_3$  formation. A schematic of the hybrid inverse modeling framework is shown in Fig. 3.

First, we performed FDMB inversions for  $\text{NO}_x$  and VOC emissions in two sequential steps. In the first step, TROPOMI  $\text{NO}_2$  VCDs were used to update the spatial distribution of  $\text{NO}_x$  emissions. In the second step, TROPOMI HCHO VCDs were utilized to correct VOC emissions. Given the different source characteristics of VOC, we estimated separate scaling factors for AVOC and BVOC.

Next, the FDMB  $\text{NO}_x$  and VOC emissions were used as the prior estimate for a 4D-Var inversion. In this step, we assimilated hourly  $\text{NO}_2$  and  $\text{O}_3$  measurements from the AQMS network, which are highly sensitive to changes in  $\text{NO}_x$  and VOC emissions. The control variables in the 4D-Var system included both  $\text{NO}_x$  and 15 VOC species (Table S3), enabling the joint optimization of key precursors that drive  $\text{O}_3$  formation and variability.

To evaluate the effectiveness of the hybrid inverse modeling approach, we designed three experiments: (1) Prior, which used the prior emissions; (2) Hybrid\_ $\text{NO}_x$ , which corrected only  $\text{NO}_x$  emissions; and (3) Hybrid\_ $\text{NO}_x$ +VOC, which jointly constrained  $\text{NO}_x$  and VOC emissions. By comparing the model outputs from both experiments with observations, we quantified the relative contributions of each precursor to changes in the spatiotemporal distribution of  $\text{O}_3$  and its sensitivity regime. Model performance was assessed using multiple statistical metrics (Table S4).



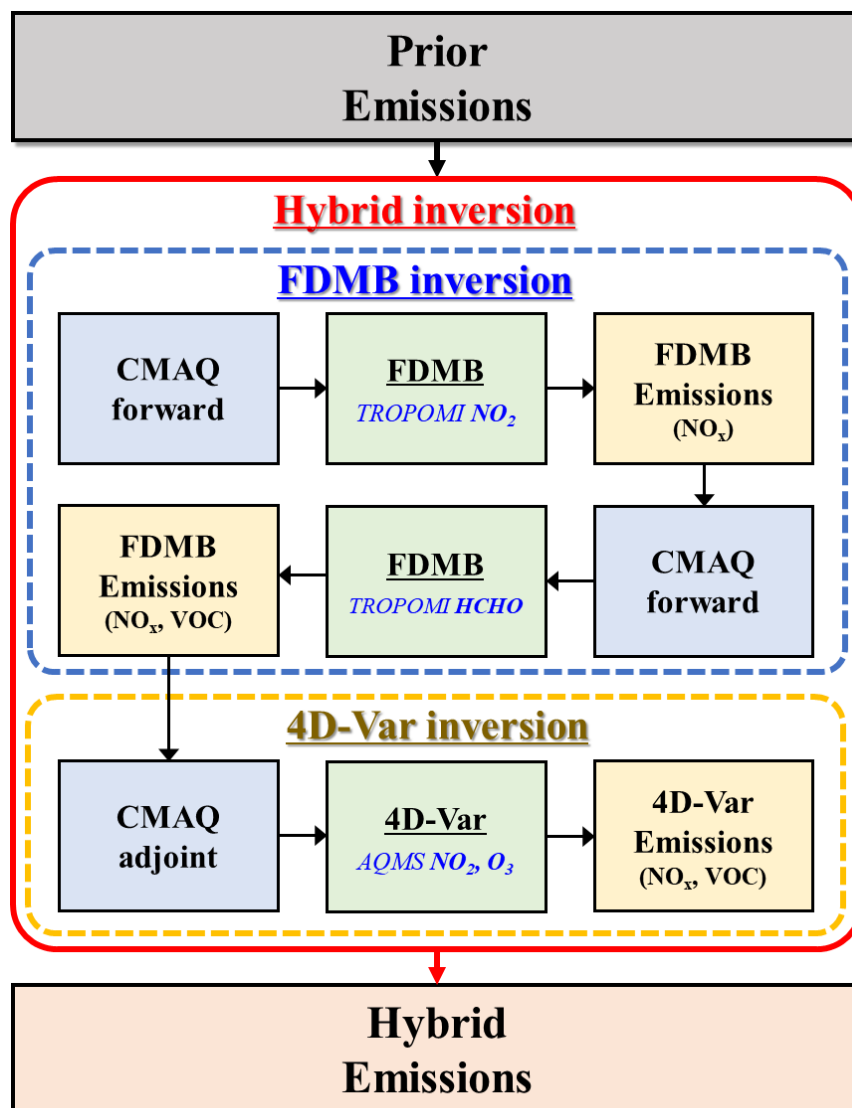


Figure 3: Schematic of the hybrid inverse modeling framework combining FDMB and 4D-Var inversions. In the first step, the FDMB inversion (blue box) corrects the spatial distribution of NO<sub>x</sub> and VOC emissions using TROPOMI NO<sub>2</sub> and HCHO VCDs. In the second step, the 4D-Var inversion (Yellow box) constrains the spatiotemporal distribution of NO<sub>x</sub> and VOC emissions by assimilating hourly ground-based NO<sub>2</sub> and O<sub>3</sub> observations.

## 2.4. O<sub>3</sub> sensitivity regime classification

The O<sub>3</sub> sensitivity regime can be classified based on the VOC/NO<sub>x</sub> ratio, for which several photochemical indicators—such as HCHO/NO<sub>2</sub>, H<sub>2</sub>O<sub>2</sub>/HNO<sub>3</sub>, and H<sub>2</sub>O<sub>2</sub>/NO<sub>y</sub>—have been widely applied (Sillman, 1995; Liu and Shi, 2021). Among these, the HCHO-to-NO<sub>2</sub> ratio (FNR) has been widely used because it is applicable to satellite observations and can effectively capture



regional-scale photochemical conditions (Duncan et al., 2010; Liu et al., 2021; Jang et al., 2023; Rahman et al., 2025). In this study, we assess the model's capability to diagnose O<sub>3</sub> sensitivity regimes by comparing FNR values derived from TROPOMI satellite measurements with those simulated by the model. Conventionally, we classified FNR values ≤ 2.0 as VOC-sensitive, ≥ 2.8 as NO<sub>x</sub>-sensitive, and between 2.0 and 2.8 as neutral, following the thresholds proposed by Jang et al. (2023) for South Korea.

## 2.5. Adjoint-based analysis of ΔO<sub>3</sub> responses to precursor emissions

We quantified the hourly influence of NO<sub>x</sub> and VOC emissions on O<sub>3</sub> as a function of the sensitivity regime using the CMAQ adjoint model driven by posterior emissions (Fig. 4). For each local hour  $h$ , the regime-specific cost function  $J_r(h)$  was defined as the two-week mean of the spatially averaged surface O<sub>3</sub> over grids classified as regime  $r$  at that hour.

$$J_r(h) = \frac{1}{|D|} \sum_{d \in D} \frac{1}{|G_r|} \sum_{g \in G_r} C_{O_3}(g, h, d), \quad h \in \{0, 1, \dots, 23\}, \quad r \in \{VOC\text{-sensitive}, NO_x\text{-sensitive}\} \quad (9)$$

Here,  $D$  is the set of analysis days (two weeks),  $G_r$  is the set of grids classified as regime  $r$ , and  $C_{O_3}(g, h, d)$  is the surface O<sub>3</sub> concentration at grid  $g$ .

A single adjoint integration provides, for a receptor hour  $t_2$ , the sensitivities of  $J_r(t_2)$  to emissions at all emission hours  $t_1$ :

$$S_i(t_1 \rightarrow t_2) = \frac{\partial J_r(t_2)}{\partial E_i(t_1)} \quad (10)$$

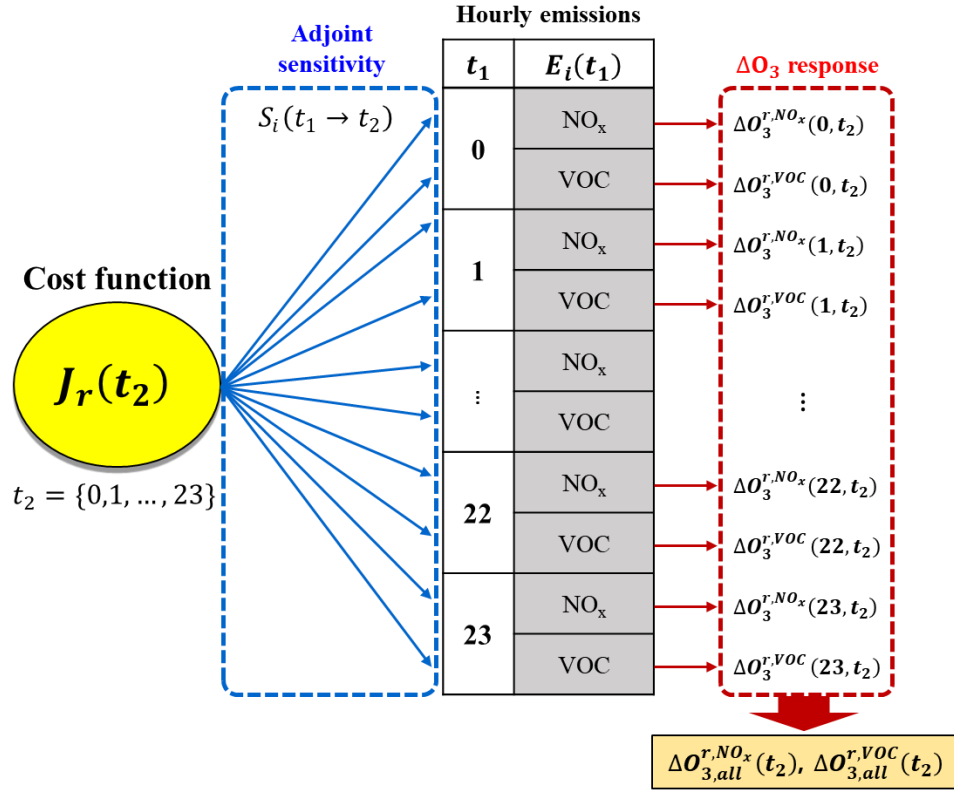
where  $i \in \{NO_x, VOC\}$  and  $E_i(t_1)$  is the hourly emission rate. Multiplying these sensitivities by the corresponding emissions yields the emission-time-specific O<sub>3</sub> response:

$$\Delta O_3^{r,i}(t_1, t_2) = S_i(t_1 \rightarrow t_2) \times E_i(t_1) \text{ [ppb]} \quad (11)$$

and summing over all emission hours yields the emission-time-integrated response at  $t_2$ :

$$\Delta O_{3,all}^{r,i}(t_2) = \sum_{t_1=0}^{23} S_i(t_1 \rightarrow t_2) \times E_i(t_1) \text{ [ppb]} \quad (12)$$

In our configuration,  $S_i$  has units of ppb per (moles s<sup>-1</sup>). Responses are evaluated over the grids classified as regime  $r$  at the receptor hour  $t_2$ , enabling regime-by-regime comparison of NO<sub>x</sub> and VOC influences. The adjoint simulations covered the full two-week analysis period. Because each receptor hour requires a distinct adjoint run, we performed 24 adjoint simulations per regime (VOC-sensitive and NO<sub>x</sub>-sensitive), for a total of 48 runs. Using the posterior emissions, we then computed and compared regime-, precursor-, and hour-resolved O<sub>3</sub> responses.



**Figure 4: Schematic of the adjoint-based O<sub>3</sub> response calculation.** A single adjoint run provides, for a receptor hour  $t_2$ , the sensitivities of the regime-mean surface O<sub>3</sub> cost function  $J_r(t_2)$  to precursor emissions at each emission hour  $t_1$ . Multiplying these sensitivities by the corresponding hourly emissions  $E_i(t_1)$  ( $i \in \{NO_x, VOC\}$ ) yields the emission-time-specific O<sub>3</sub> response  $\Delta O_3^{r,i}(t_1, t_2)$ . Summing over all emission hours  $t_1 = 0-23$  gives the emission-time-integrated response  $\Delta O_{3,all}^{r,i}(t_2)$ . Responses are evaluated over grids classified as regime  $r$  at hour  $t_2$ , enabling regime-by-regime comparison of NO<sub>x</sub> and VOC influences.

### 3 Results

#### 3.1 Spatiotemporal changes in NO<sub>x</sub> and VOC emissions

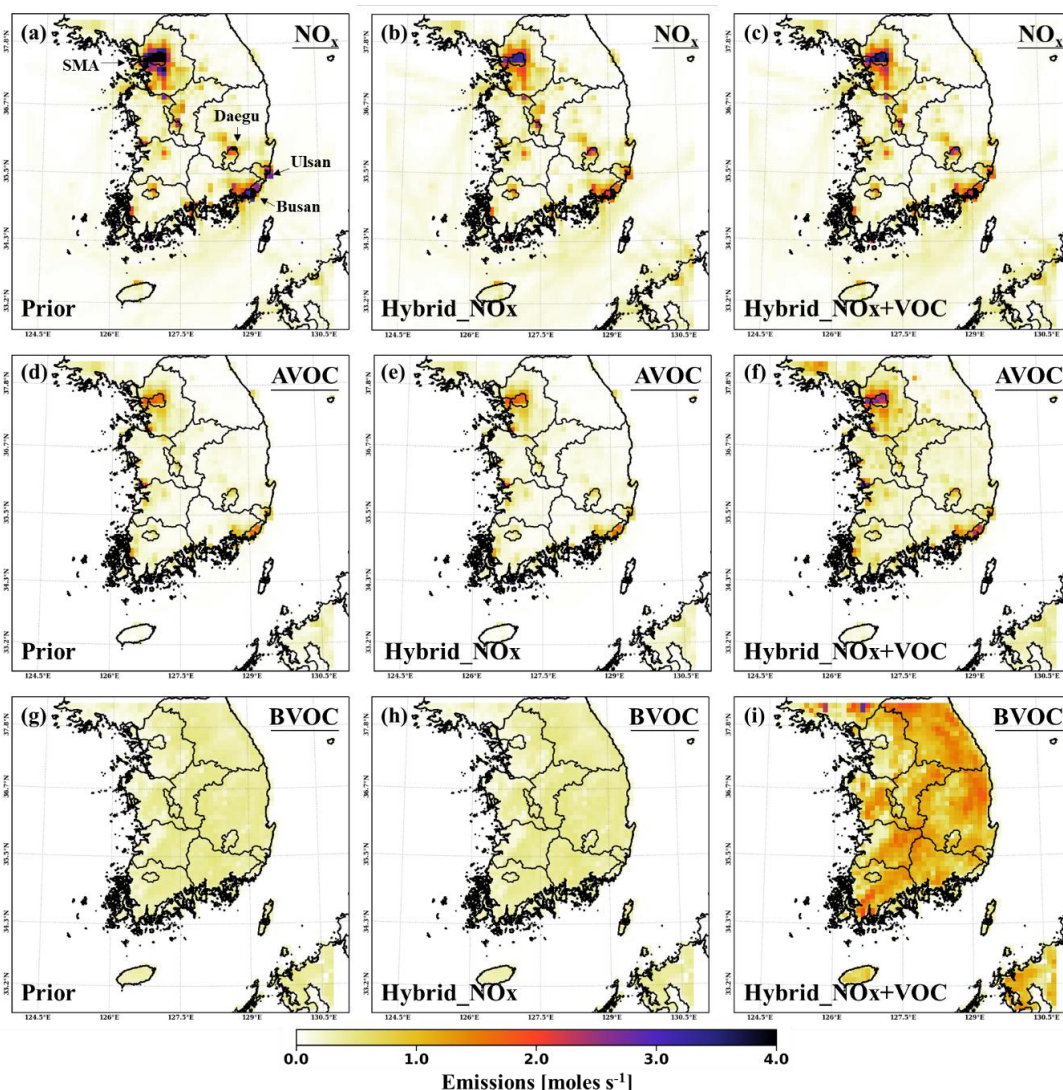
To investigate the spatiotemporal changes in emissions constrained by the hybrid inverse modeling, we compared the results from the Hybrid\_NOx experiment, which constrained only NO<sub>x</sub> emissions, and the Hybrid\_NOx+VOC experiment, which simultaneously constrained both NO<sub>x</sub> and VOC emissions, with those based on the Prior emissions. Prior to the hybrid inversion, an L-curve test was conducted to determine an appropriate  $\gamma$  for the 4D-Var inverse modeling and a value of  $\gamma = 10$  was selected (Fig. S2).

Figure 5 shows the spatial distributions of NO<sub>x</sub>, AVOC, and BVOC emissions averaged over the study period. In the Hybrid\_NOx experiment, NO<sub>x</sub> emissions were substantially reduced relative to the Prior experiment, particularly over major



urban regions such as the Seoul Metropolitan Area (SMA), Busan, Ulsan, and Daegu. On average,  $\text{NO}_x$  emissions across the entire modeling domain decreased by 18.23 %. The Hybrid\_ $\text{NO}_x$ +VOC experiment also showed a reduction in  $\text{NO}_x$  emissions, but to a lesser extent, with an average decrease of 15.50 %. In contrast, VOC emissions remained unchanged in the Hybrid\_ $\text{NO}_x$  experiment. However, in the Hybrid\_ $\text{NO}_x$ +VOC experiment, emissions of both AVOC and BVOC were substantially increased by approximately 70.54 % and 161.64 %, respectively, relative to the Prior. The increase in AVOC was largely concentrated over urban regions, similar to the  $\text{NO}_x$  distribution, while BVOC showed a more spatially homogeneous enhancement, especially over vegetated and mountainous areas across South Korea.

The different adjustment magnitudes for AVOC and BVOC emissions in the Hybrid\_ $\text{NO}_x$ +VOC experiment arise from the distinct VOC species compositions of the two source categories and the associated differences in their chemical reactivity. Because the HCHO-based optimization updates emissions according to precursor-specific sensitivities, AVOC and BVOC emissions can be adjusted by different amounts. A similar tendency was reported in Choi et al. (2022), where BVOC emissions showed larger adjustments than AVOC when constrained with HCHO column observations. These results indicate that the VOC adjustments in our inversion reflect the species-dependent sensitivities inherent in HCHO-based optimization.

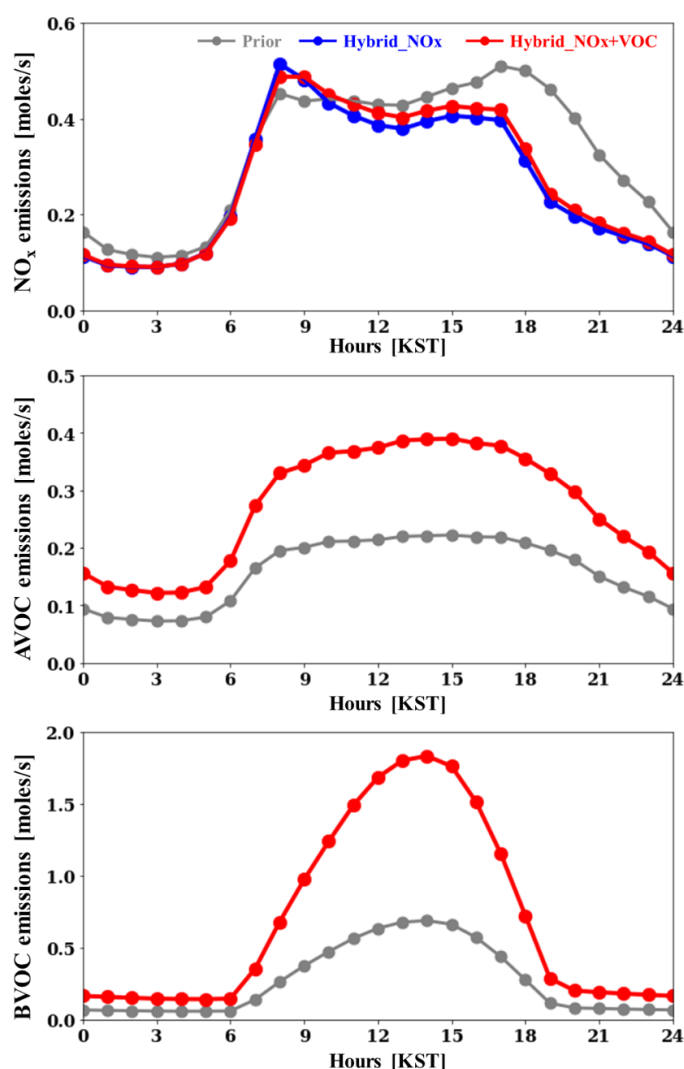


**Figure 5:** Spatial distributions of (a–c) NO<sub>x</sub>, (d–f) AVOC, and (g–i) BVOC emissions, averaged over the study period, for each experiment (Prior, Hybrid\_NO<sub>x</sub>, and Hybrid\_NO<sub>x</sub>+VOC).

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Figure 6 presents the diurnal variations in NO<sub>x</sub>, AVOC, and BVOC emissions for each experiment. The Prior NO<sub>x</sub> emissions show two peaks corresponding to morning and evening rush hours. In contrast, the Hybrid\_NO<sub>x</sub> and Hybrid\_NO<sub>x</sub>+VOC experiments exhibit a shift in temporal emission patterns, with increased emissions in the morning and substantial reductions in the evening and at night. This shift implies a redistribution of hourly emission characteristics driven by the inversion process. For VOC, the Hybrid\_NO<sub>x</sub>+VOC experiment resulted in a substantial increase in AVOC emissions during the daytime and a slight increase at night. BVOC emissions, which are primarily driven by photosynthetic and metabolic processes in vegetation, also showed a distinct increase during the daytime, reflecting a temporal pattern similar to that of the Prior emissions.

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305 **Figure 6: Diurnal variations of NO<sub>x</sub> (top), AVOC (middle), and BVOC (bottom) emissions for each experiment (Prior: gray, Hybrid\_NOx: blue, Hybrid\_NOx+VOC: red), averaged over South Korea during the study period.**

In summary, the Hybrid\_NOx+VOC experiment led to an overall reduction in NO<sub>x</sub> emissions and an increase in VOC emissions relative to the Prior inventory. Although NO<sub>x</sub> emissions decreased on average, they increased during the morning rush hour and decreased markedly during the evening and nighttime, indicating a shift in their temporal distribution. These results demonstrate that the proposed hybrid inverse modeling framework effectively adjusts both the spatial distribution and temporal allocation of emissions.



### 3.2 Spatiotemporal changes in NO<sub>2</sub>, HCHO, and O<sub>3</sub> concentrations

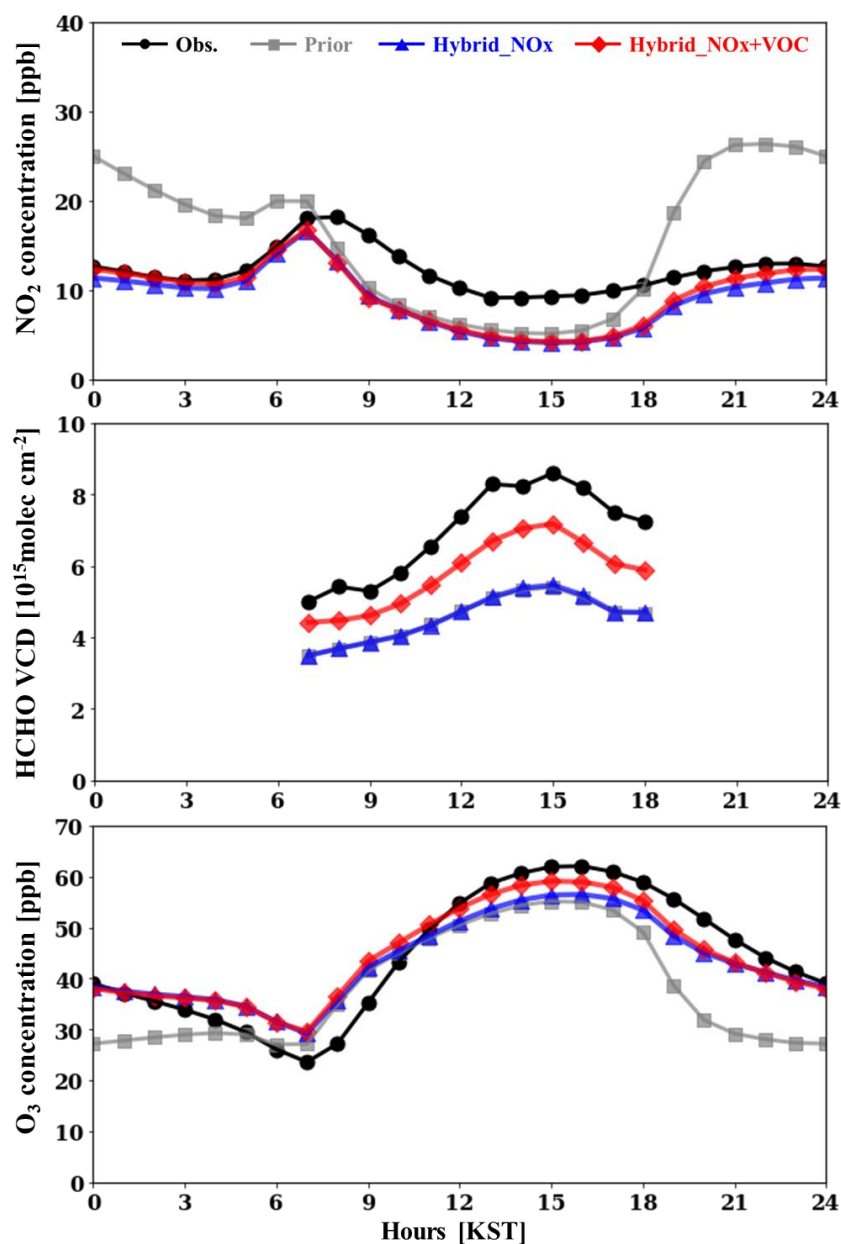
In this section, CMAQ simulations based on the Prior, Hybrid\_NOx, and Hybrid\_NOx+VOC experiments were performed to assess the effectiveness of the hybrid inverse modeling approach. Before evaluating the inverse modeling performance, the meteorological fields were first validated, with the results summarized in Table S5. The model showed good agreement with observations for temperature, wind speed, and relative humidity. Subsequently, the simulated NO<sub>2</sub>, O<sub>3</sub>, and HCHO concentrations for each experiment were evaluated against observational data, as summarized in Table 1.

**Table 1: Statistical evaluation of NO<sub>2</sub>, HCHO, and O<sub>3</sub> concentrations for each experiment (Prior, Hybrid\_NOx, and Hybrid\_NOx+VOC). Observations of NO<sub>2</sub> and O<sub>3</sub> were obtained from the AQMS network, while HCHO observations were based on Pandora measurements.**

Species	Experiment	Obs.	CMAQ	MBE	RMSE	IOA	r
NO <sub>2</sub> [ppb]	Prior		15.56	3.34	15.49	0.59	0.46
	Hybrid_NOx	12.22	9.00	-3.22	8.33	0.74	0.60
	Hybrid_NOx+VOC		9.41	-2.81	8.26	0.76	0.61
HCHO VCD [10 <sup>15</sup> molec cm <sup>-2</sup> ]	Prior		4.59	-2.47	4.40	0.54	0.52
	Hybrid_NOx	7.06	4.61	-2.45	4.36	0.55	0.53
	Hybrid_NOx+VOC		5.85	-1.22	3.94	0.67	0.52
O <sub>3</sub> [ppb]	Prior		38.20	-6.29	18.30	0.71	0.55
	Hybrid_NOx	44.48	43.74	-0.74	12.84	0.80	0.70
	Hybrid_NOx+VOC		44.72	0.24	12.34	0.83	0.73

For NO<sub>2</sub>, the Prior experiment exhibited a positive bias, with a mean bias error (MBE) of 3.34 ppb. This overestimation was notably reduced in the Hybrid\_NOx and Hybrid\_NOx+VOC experiments, with MBEs of -3.22 ppb and -2.81 ppb, respectively. The temporal pattern of bias also changed: while the Prior experiment overestimated NO<sub>2</sub> concentrations during nighttime, both hybrid simulations substantially reduced this overprediction, resulting in concentrations closer to observations (Fig. 7). These improvements, primarily attributable to decreased nighttime NO<sub>x</sub> emissions, led to enhanced agreement during nighttime. Consequently, the correlation coefficient (r) increased from 0.46 in the Prior experiment to above 0.6 in both hybrid experiments.





**Figure 7: Diurnal variations of NO<sub>2</sub> (top) and O<sub>3</sub> (bottom) concentrations for each experiment (Prior: gray, Hybrid\_NOx: blue, Hybrid\_NOx+VOC: red), averaged over South Korea during the study period.**

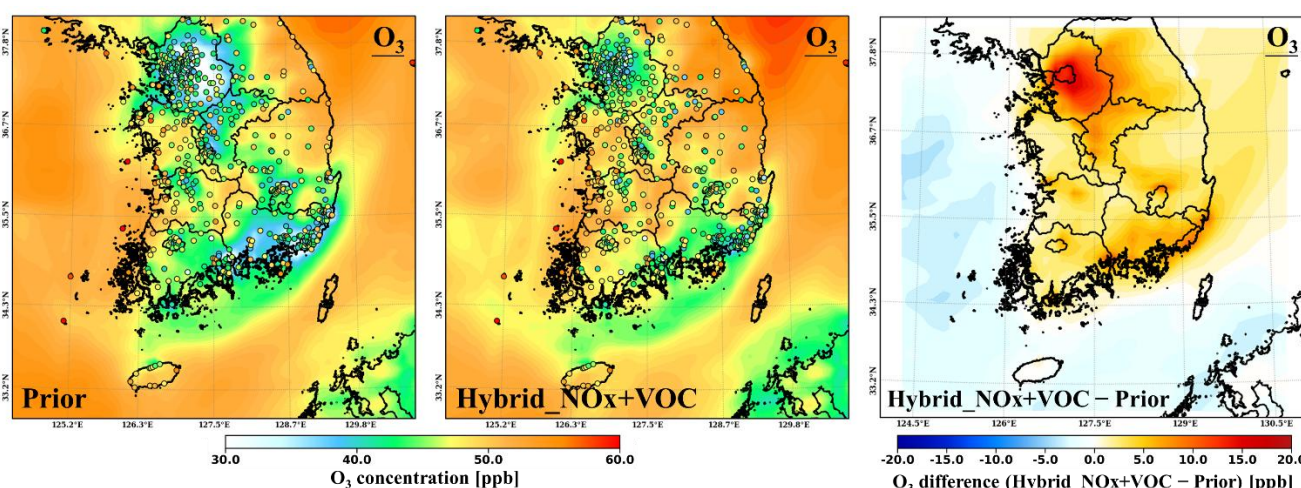
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For VOC, model results were compared with Pandora HCHO VCDs (Table 1). The Prior experiment showed a significant underestimation ( $\text{MBE} = -2.48 \times 10^{15} \text{ molec cm}^{-2}$ ). The Hybrid\_NOx experiment showed little improvement ( $\text{MBE} = -2.45 \times 10^{15} \text{ molec cm}^{-2}$ ), whereas the Hybrid\_NOx+VOC experiment more effectively reduced the bias ( $\text{MBE} = -1.22 \times 10^{15} \text{ molec cm}^{-2}$ )



and achieved the highest index of agreement (IOA = 0.67). During daytime, HCHO VCDs in both the Prior and Hybrid\_NOx experiments were underestimated relative to Pandora observations, whereas the Hybrid\_NOx+VOC experiment yielded higher HCHO VCDs that were closer to the Pandora measurements (Fig. 7). These results demonstrate that the underestimation of VOC emissions in the Prior experiment was effectively corrected in the Hybrid\_NOx+VOC experiment, leading to improved agreement with observations across South Korea.

Regarding O<sub>3</sub>, the Prior experiment underestimated surface concentrations, with an MBE of -6.28 ppb. The bias was substantially reduced in the Hybrid\_NOx (MBE = -0.74 ppb) and Hybrid\_NOx+VOC (MBE = 0.24 ppb) experiments. The IOA improved from 0.71 (Prior) to 0.80 (Hybrid\_NOx) and 0.83 (Hybrid\_NOx+VOC), indicating enhanced model performance in reproducing observed O<sub>3</sub> concentrations. In terms of diurnal variation, the Prior experiment generally underestimated O<sub>3</sub> with particularly large negative biases at night. In the Hybrid\_NOx experiment, nighttime O<sub>3</sub> concentrations increased markedly, although daytime changes were limited. By contrast, the Hybrid\_NOx+VOC experiment increased O<sub>3</sub> concentrations during both daytime and nighttime, yielding the closest agreement with observations. Spatially, the Prior experiment substantially underestimated O<sub>3</sub> concentrations in urban areas with high NO<sub>x</sub> emissions, whereas the Hybrid\_NOx+VOC experiment produced higher O<sub>3</sub> levels in these regions, resulting in improved agreement with the observations (Fig. 8).



**Figure 8: Spatial distributions of mean surface O<sub>3</sub> concentrations from the Prior (left) and Hybrid\_NOx+VOC (middle) experiments, and the differences (Hybrid\_NOx+VOC - Prior; right), averaged over the study period. Circles indicate O<sub>3</sub> observations from the AQMS network.**

Consequently, the titration of O<sub>3</sub> by NO during nighttime was reduced, leading to increased O<sub>3</sub> concentrations that were more consistent with observations. However, daytime O<sub>3</sub> levels remained similar to those in the Prior experiment. In contrast, the Hybrid\_NOx+VOC experiment significantly improved O<sub>3</sub> simulations during both daytime and nighttime. These findings

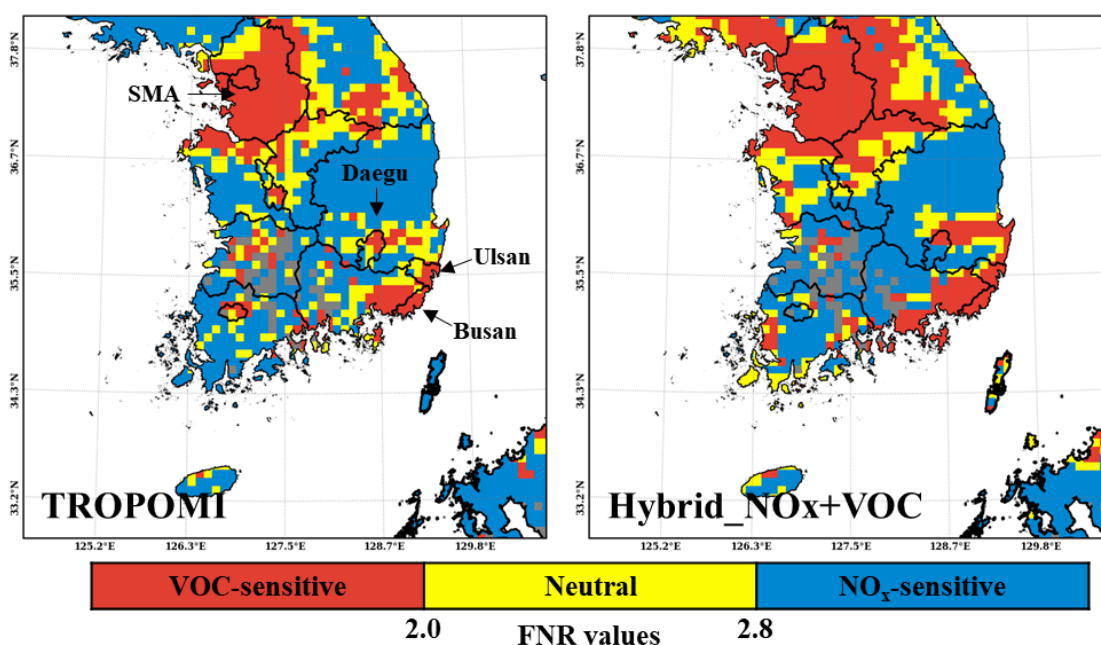
demonstrate that jointly constraining NO<sub>x</sub> and VOC emissions is more effective than constraining NO<sub>x</sub> alone in accurately reproducing O<sub>3</sub> concentrations over South Korea.

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### 3.3 Improvement of O<sub>3</sub> sensitivity regimes through hybrid inversion

In this section, we examine how the O<sub>3</sub> sensitivity regime changes before and after the application of the hybrid inverse modeling. The O<sub>3</sub> sensitivity is diagnosed using the FNR. Figure 9 compares the FNR distributions derived from TROPOMI with those simulated in the Hybrid\_NO<sub>x</sub>+VOC experiment. The TROPOMI-based FNR indicates VOC-sensitive regimes over major urban regions such as the SMA, Busan, Ulsan, and Daegu, whereas NO<sub>x</sub>-sensitive regimes dominate over mountainous and heavily vegetated areas where BVOC emissions are substantial.

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**Figure 9:** Spatial distributions of O<sub>3</sub> sensitivity regimes derived from TROPOMI-based FNR (left), and Hybrid\_NO<sub>x</sub>+VOC experiments (right), averaged over the study period. Red, yellow, and blue denote VOC-sensitive, neutral, and NO<sub>x</sub>-sensitive regimes, respectively, while gray areas indicate missing data.

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The Hybrid\_NO<sub>x</sub>+VOC experiment successfully reproduces the spatial pattern of the TROPOMI-based FNR, in sharp contrast to the Prior and Hybrid\_NO<sub>x</sub> experiments, which classify most of South Korea as VOC-sensitive (Fig. S3). The Prior emissions are based on the 2018 EDGAR HTAPv3 inventory, whose earlier base year may not fully reflect emission conditions in 2022, potentially biasing the Prior experiment toward VOC-sensitive regimes. Furthermore, adjusting NO<sub>x</sub> emissions alone

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in the Hybrid\_NOx experiment was insufficient to capture the observed O<sub>3</sub> sensitivity regime, indicating that simultaneous optimization of both NO<sub>x</sub> and VOC emissions is essential for accurately diagnosing O<sub>3</sub> chemical regimes.

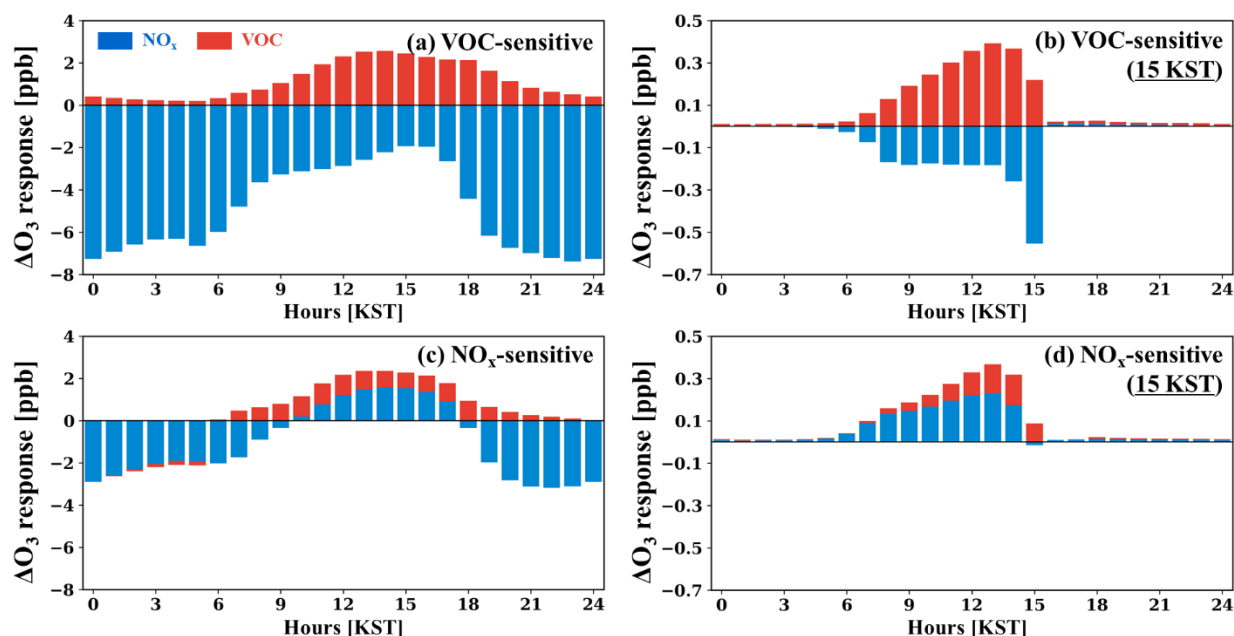
385 The improved agreement in the Hybrid\_NOx+VOC experiment highlights the importance of integrating recent satellite observations into emission updates, enabling the model to better reflect the current photochemical environment. These findings are consistent with recent studies reporting regional transitions in East Asia from VOC-sensitive toward NO<sub>x</sub>-sensitive or transitional regimes (Lee et al., 2021; Itahashi et al., 2022; Wang et al., 2025).

Given that the hybrid inversion yields O<sub>3</sub> sensitivity regimes that closely resemble those derived from TROPOMI, the optimized posterior state provides a robust foundation for further analysis. Accordingly, in Section 3.4, we assess the regime-  
390 dependent hourly  $\Delta O_3$  responses to NO<sub>x</sub> and VOC emissions using adjoint sensitivities derived from the posterior simulation.

### 3.4 Regime-dependent hourly $\Delta O_3$ responses to NO<sub>x</sub> and VOC emissions

We quantify hourly  $\Delta O_3$  responses using adjoint sensitivities to determine, within VOC-sensitive and NO<sub>x</sub>-sensitive regimes, which precursor (NO<sub>x</sub> or VOC) exerts a stronger influence on O<sub>3</sub> production or loss. Figure 10 shows regime-stratified hourly  $\Delta O_3$  responses to NO<sub>x</sub> and VOC emissions for 1–14 May 2022. Panels (a) and (c) show, for each local hour, the  $\Delta O_3$  at that  
395 hour resulting from emissions integrated over all emission times (Eq. (12)). This reflects not only the response to emissions released at the same hour but also the influence of the full diurnal emission profile of each precursor on hourly O<sub>3</sub>. Thus, the panels illustrate how the complete daily emission cycle of each precursor contributes to hourly O<sub>3</sub> within each regime.

In the VOC-sensitive regime (NO<sub>x</sub>-rich), the NO<sub>x</sub> response is negative at all hours, indicating net O<sub>3</sub> decreases consistent with rapid O<sub>3</sub> titration, whereas the VOC response is positive and strengthens during daytime, reflecting enhanced  
400 photochemical production. In the NO<sub>x</sub>-sensitive regime (VOC-rich), VOC provides a persistent positive daytime response, while the NO<sub>x</sub> response changes sign with time of day: negative at night (titration) and positive from late morning into the afternoon as radical chemistry intensifies.



405 **Figure 10:** Two-week mean  $\Delta O_3$  response (ppb) to  $NO_x$  (blue) and VOC (red) emissions, by local hour, for 1–14 May 2022. For each local hour, responses are summed over all grids classified in each regime at that hour; regimes are diagnosed with the FNR indicator from the Hybrid\_  $NO_x$ +VOC experiment. Panels (a) and (c) show, for VOC-sensitive and  $NO_x$ -sensitive regimes respectively, the  $\Delta O_3$  response at each local hour to emissions released over all hours (i.e., emission-time-integrated response). Panels (b) and (d) show the  $\Delta O_3$  response at 15 KST as a function of emission time (“emission-time response”).

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Panels (b) and (d) isolate the hour of maximum  $O_3$  (15 KST) and display the  $\Delta O_3$  response at 15 KST as a function of the emission time (Eq. (11)). In VOC-sensitive regimes,  $NO_x$  emitted at 15 KST yields the largest negative  $\Delta O_3$  response, consistent with the instantaneous  $O_3$  titration. By contrast, VOC emissions at 13 KST exert the strongest positive influence on 15 KST  $O_3$ , indicating an effective lag of about 2 hours associated with multistep photochemical production. In  $NO_x$ -sensitive regimes,  $NO_x$  generally promotes  $O_3$  formation; however,  $NO_x$  emitted at 15 KST still produces  $O_3$  losses through immediate titration. The largest positive effects on 15 KST  $O_3$  arise from  $NO_x$  at 13 KST and VOC at 14 KST, indicating a similar response time of approximately 1–2 hours.

Taken together, the results show that precursor impacts on  $O_3$  vary with both regime and hour. Under VOC-sensitive conditions, VOC reductions are more effective than  $NO_x$  reductions for lowering daytime  $O_3$ , whereas under  $NO_x$ -sensitive conditions,  $NO_x$  controls deliver the more direct decreases. Because titration is immediate but photochemical production requires chemical processing time, effective mitigation of high- $O_3$  periods requires hour-specific emission controls aligned with the prevailing  $O_3$  sensitivity regime.

A clear understanding of how precursor influences on  $O_3$  differ across sensitivity regimes and vary throughout the day is essential for designing realistic and region-specific  $O_3$  control strategies. In this context, the hybrid inversion framework presented in this study provides a practical basis for policy development, as it enables accurate identification of the dominant

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O<sub>3</sub> sensitivity regime and quantification of the major precursor contributions. By capturing both the chemical regime and the temporal characteristics of precursor impacts, the proposed methodology can provide valuable guidance for developing region-specific and effective emission reduction strategies.

This analysis is limited to a two-week period and may not capture the seasonal or longer-term variability of O<sub>3</sub> sensitivity regimes across South Korea. Nevertheless, the hybrid inverse modeling framework efficiently constrains precursor emissions on short time scales and enables assessments tailored to individual regions that explicitly account for the prevailing O<sub>3</sub> sensitivity regime, thereby supporting the implementation of emission reduction policies. Compared with conventional bottom-up inventories, the top-down approach reduces data and computational demands, enables rapid observation-driven estimates of O<sub>3</sub> precursor emissions, and provides timely guidance for O<sub>3</sub> management policies.

#### 4. Summary and Conclusions

This study aimed to enhance the accuracy of simulated O<sub>3</sub> concentrations and improve the diagnosis of O<sub>3</sub> sensitivity regimes over South Korea by applying a top-down hybrid inverse modeling approach to constrain the spatiotemporal distributions of NO<sub>x</sub> and VOC emissions, and to quantify hourly ΔO<sub>3</sub> responses to these precursors using adjoint sensitivities. The inverse modeling system used TROPOMI NO<sub>2</sub> and HCHO column densities along with surface NO<sub>2</sub> and O<sub>3</sub> measurements from the AQMS network. The modeling was conducted using CMAQ and its adjoint model. The hybrid inverse modeling approach combining the FDMB and 4D-Var methods was employed to constrain emissions. To assess the impact of major O<sub>3</sub> precursors on the spatiotemporal distribution and sensitivity regime of O<sub>3</sub>, three experiments were conducted: Prior, which used the EDGAR-HTAPv3 emission inventory; Hybrid\_NO<sub>x</sub>, in which only NO<sub>x</sub> emissions were optimized; and Hybrid\_NO<sub>x</sub>+VOC, in which both NO<sub>x</sub> and VOC emissions were jointly constrained.

In the Hybrid\_NO<sub>x</sub> experiment, where only NO<sub>x</sub> emissions were adjusted, emissions decreased by up to 51 % at night and increased by up to 14 % during the day relative to the Prior inventory, resulting in an overall average reduction of 18 %. These time-dependent adjustments enabled the correction of diurnal variability in the emission profile. Consequently, nighttime O<sub>3</sub> concentrations increased, reducing the mean bias error by 90 % relative to the Prior experiment and thereby improving agreement with observations. In contrast, during the daytime, constraining NO<sub>x</sub> emissions alone yielded only limited improvements in O<sub>3</sub> concentrations.

However, constraining NO<sub>x</sub> alone provided only limited improvement for daytime O<sub>3</sub>, indicating the need to additionally optimize VOC emissions. To address this limitation, the Hybrid\_NO<sub>x</sub>+VOC experiment was conducted, in which both NO<sub>x</sub> and VOC emissions were simultaneously constrained. Compared to the Prior emissions, NO<sub>x</sub> decreased by an average of 16 %, while anthropogenic AVOC and BVOC increased by 71 % and 162 %, respectively. The joint adjustment of NO<sub>x</sub> and VOC emissions yielded the greatest improvement in O<sub>3</sub> simulations during both daytime and nighttime, resulting in an IOA exceeding 0.8 when compared with AQMS O<sub>3</sub> observations. These results demonstrate that accurate O<sub>3</sub> simulation requires the simultaneous constraint of NO<sub>x</sub> and VOC emissions due to nonlinear chemical processes. Furthermore, given the



substantial differences in photochemical mechanisms between day and night, accurately representing not only the spatial distribution but also the diurnal variability of emissions is critical for improving O<sub>3</sub> model performance.

460 The hybrid inverse modeling also improved the simulation of O<sub>3</sub> sensitivity regimes. In the Hybrid\_NOx+VOC experiment, the spatial distribution of the simulated FNR closely matched the TROPOMI-derived regimes, reproducing VOC-sensitive conditions over major urban regions and NO<sub>x</sub>-sensitive conditions over mountainous and vegetated areas. This agreement highlights the ability of the hybrid inversion to incorporate observational constraints and accurately represent the relative contributions of NO<sub>x</sub> and VOC to O<sub>3</sub> formation. The improved regime classification further provides a reliable foundation for  
465 analyzing regime-dependent O<sub>3</sub> production and understanding how changes in precursor abundances drive transitions between VOC-sensitive and NO<sub>x</sub>-sensitive conditions.

Building on the improved regime representation obtained from the Hybrid\_NOx+VOC experiment, we further analyzed how each precursor influences O<sub>3</sub> in a regime- and time-dependent manner. Under VOC-sensitive conditions, VOC emissions sustain daytime O<sub>3</sub> production, whereas NO<sub>x</sub> emissions lead to net O<sub>3</sub> losses through rapid titration. In contrast, under NO<sub>x</sub>-  
470 sensitive conditions, NO<sub>x</sub> contributes positively to O<sub>3</sub> formation from late morning into the afternoon, while titration processes dominate during nighttime hours. These results clarify precursor-specific emission control priorities with explicit diurnal dependence: in VOC-sensitive regimes, reducing VOC emissions is most effective for mitigating daytime O<sub>3</sub>, whereas in NO<sub>x</sub>-sensitive regimes, NO<sub>x</sub> emission reductions provide more immediate and direct benefits. Because titration occurs almost instantaneously while photochemical production unfolds over finite chemical timescales, effective mitigation of high-O<sub>3</sub>  
475 periods requires hour-specific emission controls that are aligned with the prevailing O<sub>3</sub> sensitivity regime.

This analysis spans two weeks and therefore may not capture seasonal or long-term variability. In addition, because EDGAR\_HTAPv3 was spatiotemporally downscaled for CMAQ, inventory-related uncertainties could not be fully assessed. Despite these limitations, the findings suggest that extending the hybrid inverse modeling over longer periods and incorporating diverse observations would further improve the resolution and reliability of emission estimates. Overall, the  
480 proposed hybrid inverse modeling shows strong potential to enhance O<sub>3</sub> simulations and to support region-specific regime assessments and precursor emission control strategies.

**Code and data availability.** The WRF 3.8.1 model is distributed by NCAR (<https://www.mmm.ucar.edu/models/wrf>, last access: 21 November 2025; Skamarock et al., 2008). The CMAQ 5.0 adjoint model is available from Zenodo (<https://zenodo.org/records/3780216>, last access: 21 November 2025; Zhao et al., 2020). The MEGAN 2.1 model is available  
485 from the University of California, Irvine – Biogenic Aerosols and Interactions Research Group (BAI) (<https://bai.ess.uci.edu/megan/data-and-code/megan21>, last access: 21 November 2025; Guenther et al., 2012). ERA5 reanalysis data are distributed by the Climate Data Store of ECMWF (<https://cds.climate.copernicus.eu/datasets>, last access: 21 November 2025; Hersbach et al., 2023a, b). The EDGAR HTAPv3 emission inventory is provided by the European Commission Joint Research Centre ([https://edgar.jrc.ec.europa.eu/dataset\\_htap\\_v3](https://edgar.jrc.ec.europa.eu/dataset_htap_v3), last access: 21 November 2025; Crippa et





490 al., 2023). TROPOMI NO<sub>2</sub> and HCHO column data are available from the Copernicus Data Space (<https://dataspace.copernicus.eu>, last access: 21 November 2025). Pandora HCHO column data are accessible from the Pandonia Global Network (<https://www.pandonia-global-network.org>, last access: 21 November 2025). AQMS NO<sub>2</sub> and O<sub>3</sub> observations are available from AirKorea (<https://www.airkorea.or.kr/web>, last access: 21 November 2025).

**Author contributions.** JM designed and executed the model inversions, performed the data analysis, and prepared the manuscript. WJ, YC, HCK, and SYP provided scientific and technical guidance and contributed to the scientific analysis and interpretation of the results. WJ and SJ were responsible for funding acquisition. All authors contributed to the review and editing of the final paper.

**Competing interests.** The contact author has declared that none of the authors has any competing interests.

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## References

- 505 Bae, K., Song, C.K., Van Roozendaal, M., Richter, A., Wagner, T., Merlaud, A., Pinardi, G., Friedrich, M.M., Fayt, C., Dimitropoulou, E., Lange, K., and Bösch, T., Zilker, B., Latsch, M., Behrens, L.K., Ziegler, S., Ripperger-Lukosiunaite, S., Kuhn, L., Lauster, B., Reischmann, L., Uhlmannsiek, K., Cede, A., Tiefengraber, M., Gebetsberger, M., Park, R.J., Lee, H., Hong, H., Chang, L.S., Jeon, K. Validation of GEMS operational v2.0 total column NO<sub>2</sub> and HCHO during the GMAP/SIJAQ campaign. *Sci. Total Environ.* 974 (2), 179190, <https://doi.org/10.1016/j.scitotenv.2025.179190>, 2025.
- 510 Chen, Y., Shen, H., Kaiser, J., Hu, Y., Capps, S.L., Zhao, S., Hakami, A., Shih, J.-S., Pavur, G.K., Turner, M.D., Henze, D.K., Resler, J., Nenes, A., Napelenok, S.L., Bash, J.O., Fahey, K.M., Carmichael, G.R., Chai, T., Clarisse, L., Coheur, P.-F., van Damme, M., Russell, A.G.: High-resolution hybrid inversion of IASI ammonia columns to constrain US ammonia emissions using the CMAQ adjoint model, *Atmos. Chem. Phys.*, 21, 2067–2082, <https://doi.org/10.5194/acp-21-2067-2021>, 2021.
- 515 Cheng, X., Hao, Z., Zang, Z., Liu, Z., Xu, X., Wang, S., Liu, Y., Hu, Y., Ma, X.: A new inverse modeling approach for emission sources based on the DDM-3D and 3DVAR techniques: an application to air quality forecasts in the Beijing-Tianjin-Hebei region, *Atmos. Chem. Phys.*, 21 (18), 13747–13761, <https://doi.org/10.5194/acp-21-13747-2021>, 2021.



- Choi, J., Henze, D. K., Cao, H., Nowlan, C. R., González Abad, G., Kwon, H.-A., Lee, H.-M., Oak, Y. J., Park, R. J., Bates, K. H., Maasakkers, J. D., Wisthaler, A., and Weinheimer, A. J.: An inversion framework for optimizing nonmethane VOC emissions using remote sensing and airborne observations in northeast Asia during the KORUS-AQ field campaign, *J. Geophys. Res.-Atmos.*, 127, e2021JD035844, <https://doi.org/10.1029/2021JD035844>, 2022.
- Cooper, M.J., Martin, R.V., Henze, D.K., Jones, D.B.A.: Effects of a priori profile shape assumptions on comparisons between satellite NO<sub>2</sub> columns and model simulations, *Atmos. Chem. Phys.*, 20, 7231–7241, <https://doi.org/10.5194/acp-20-7231-2020>, 2020.
- Cooper, M., Martin, R.V., Padmanabhan, A., Henze, D.K.: Comparing mass balance and adjoint methods for inverse modeling of nitrogen dioxide columns for global nitrogen oxide emissions., *J. Geophys. Res.-Atmos.*, 122, 4718–4734, <https://doi.org/10.1002/2016JD025985>, 2017.
- Crippa, M., Guizzardi, D., Butler, T., Keating, T., Wu, R., Kaminski, J., Kuenen, J., Kurokawa, J., Chatani, S., Morikawa, T., Pouliot, G., Racine, J., Moran, M.D., Klimont, Z., Manseau, P.M., Mashayekhi, R., Henderson, B.H., Smith, S.J., Suchyta, H., Muntean, M., Solazzo, E., Banja, M., Schaaf, E., Pagani, F., Woo, J.-H., Kim, J., Monforti-Ferrario, F., Pisoni, E., Zhang, J., Niemi, D., Sassi, M., Ansari, T., Foley, K.: The HTAP\_v3 Emission Mosaic: Merging Regional and Global Monthly Emissions (2000–2018) to Support Air Quality Modelling and Policies, *Earth Syst. Sci. Data*, 15 (6), 2667–2694, <https://doi.org/10.5194/essd-15-2667-2023>, 2023.
- Crippa, M., Solazzo, E., Huang, G., Guizzardi, D., Koffi, E., Muntean, M., Schieberle, C., Friedrich, R., Janssens-Maenhout, G.: High resolution temporal profiles in the Emissions Database for Global Atmospheric Research, *Sci. Data*, 7 (1), 121, <http://dx.doi.org/10.1038/s41597-020-0462-2>, 2020.
- De Smedt, I., Pinardi, G., Vigouroux, C., Compennolle, S., Bais, A., Benavent, N., Boersma, F., Chan, K.L., Donner, S., Eichmann, K.U., Hedelt, P., Hendrick, F., Irie, H., Kumar, V., Lambert, J.C., Langerock, B., Lerot, C., Liu, C., Loyola, D., Peters, A., Richter, A., Rivera Cárdenas, C., Romahn, F., Ryan, R.G., Sinha, V., Theys, N., Vlietinck, J., Wagner, T., Wang, T., Yu, H., Van Roozendaal, M.: Comparative assessment of TROPOMI and OMI formaldehyde observations and validation against MAX-DOAS network column measurements, *Atmos. Chem. Phys.*, 21, 12561–12593, <https://doi.org/10.5194/ACP-21-12561-2021>, 2021.
- Douros, J., Eskes, H., van Geffen, J., Boersma, K. F., Compennolle, S., Pinardi, G., Blechschmidt, A.-M., Peuch, V.-H., Colette, A., Veefkind, P.: Comparing Sentinel-5P TROPOMI NO<sub>2</sub> column observations with the CAMS regional air quality ensemble, *Geosci. Model Dev.*, 16, 509–534, <https://doi.org/10.5194/gmd-16-509-2023>, 2023.
- Duncan, B.N., Yoshida, Y., Olson, J.R., Sillman, S., Martin, R.V., Lamsal, L., Hu, Y., Pickering, K.E., Retscher, C., Allen, D.J., Crawford, J.H.: Application of OMI observations to a space-based indicator of NO<sub>x</sub> and VOC controls on surface ozone formation, *Atmos. Environ.*, 44 (18), 2213–2223, <https://doi.org/10.1016/j.atmosenv.2010.03.010>, 2010.
- East, J.D., Henderson, B.H., Napelenok, S.L., Koplitz, S.N., Sarwar, G., Gilliam, R., Lenzen, A., Tong, D.Q., Pierce, R.B., Garcia-Menendez, F.: Inferring and evaluating satellite-based constraints on NO<sub>x</sub> emissions estimates in air quality simulations, *Atmos. Chem. Phys.*, 22, 15981–16001, <https://doi.org/10.5194/acp-22-15981-2022>, 2022.



- Elbern, H., Strunk, A., Schmidt, H., Talagrand, O.: Emission rate and chemical state estimation by 4-dimensional variational inversion, *Atmos. Chem. Phys.*, 7 (14), 3749–3769, <https://doi.org/10.5194/acp-7-3749-2007>, 2007.
- Feng, S., Jiang, F., Jiang, Z., Wang, H., Cai, Z., Zhang, L.: Impact of 3DVAR assimilation of surface PM<sub>2.5</sub> observations on PM<sub>2.5</sub> forecasts over China during wintertime, *Atmos. Environ.*, 187, 34–49, <https://doi.org/10.1016/j.atmosenv.2018.05.049>, 2018.
- Fu, W., Zhu, L., Kwon, H. A., Park, R. J., Lee, G. T., De Smedt, I., Liu, S., Li, X., Chen, Y., Pu, D., Li, J., Zuo, X., Zhang, P., Li, Y., Yan, Z., Zhang, X., Zhang, J., Wu, X., Shen, H., Ye, J., Wang, C., Fu, T.-M., Yang, X.: Evaluating GEMS HCHO retrievals with TROPOMI product, Pandora observations, and GEOS-Chem simulations, *Earth Space Sci.*, 12, <https://doi.org/10.1029/2024EA003894>, 2025.
- Goldberg, D.L., Tao, M., Kerr, G.H., Ma, S., Tong, D., Fiore, A.M., Dickens, A.F., Adelman, Z., Anenberg, S.C.: Evaluating the spatial patterns of U.S. urban NO<sub>x</sub> emissions using TROPOMI NO<sub>2</sub>, *Remote Sens. Environ.*, 300, 113917, <https://doi.org/10.1016/j.rse.2023.113917>, 2024.
- Gryparis, A., Forsberg, B., Katsouyanni, K., Analitis, A., Touloumi, G., Schwartz, J., Samoli, E., Medina, S., Anderson, H.R., Niciu, E.M., Wichmann, H.E., Kriz, B., Kosnik, M., Skorkovsky, J., Vonk, J.M., Dörtbudak, Z.: Acute effects of ozone on mortality from the “Air Pollution and Health: A European Approach” project, *Am. J. Respir. Crit. Care Med.*, 170, 1080–1087, <https://doi.org/10.1164/rccm.200403-333OC>, 2004.
- Guenther, A.B., Jiang, X., Heald, C.L., Sakulyanontvittaya, T., Duhl, T., Emmons, L.K., Wang, X.: The model of emissions of gases and aerosols from Nature version 2.1 (MEGAN2.1): an extended and updated framework for modeling biogenic emissions, *Geosci. Model Dev.*, 5, 1471–1492, <https://doi.org/10.5194/gmd-5-1471-2012>, 2012.
- Hansen, P. C.: The L-curve and its use in the numerical treatment of inverse problems, IMM Tech. Rep. 15/1999, Kongens Lyngby, Denmark, 1999.
- Henze, D. K., Seinfeld, J. H., Shindell, D. T.: Inverse modeling and mapping US air quality influences of inorganic PM<sub>2.5</sub> precursor emissions using the adjoint of GEOS-Chem, *Atmos. Chem. Phys.*, 9, 5877–5903, <https://doi.org/10.5194/acp-9-5877-2009>, 2009.
- Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., Nicolas, J., Peubey, C., Radu, R., Rozum, I., Schepers, D., Simmons, A., Soci, C., Dee, D., Thépaut, J.-N.: ERA5 hourly data on pressure levels from 1940 to present. Copernicus Climate Change Service (C3S) Climate Data Store (CDS), <https://doi.org/10.24381/cds.bd0915c6> (Accessed on 12-Sep-2025), 2023a.
- Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., Nicolas, J., Peubey, C., Radu, R., Rozum, I., Schepers, D., Simmons, A., Soci, C., Dee, D., and Thépaut, J.-N.: ERA5 hourly data on pressure levels from 1940 to present, Copernicus Climate Change Service (C3S) Climate Data Store (CDS), <https://doi.org/10.24381/cds.adbb2d47> (Accessed on 12-Sep-2025), 2023b.
- Hou, X., Wild, O., Zhu, B., Lee, J.: Future tropospheric ozone budget and distribution over east Asia under a net-zero scenario, *Atmos. Chem. Phys.*, 23, 15395–15411, <https://doi.org/10.5194/acp-23-15395-2023>, 2023.



- 585 Hristov, A.N., Harper, M., Meinen, R., Day, R., Lopes, J., Ott, T., Venkatesh, A., Randles, C.A.: Discrepancies and  
Uncertainties in Bottom-up Gridded Inventories of Livestock Methane Emissions for the Contiguous United States, *Environ.*  
*Sci. Technol.*, 51, 13668–13677, <https://doi.org/10.1021/acs.est.7b03332>, 2017.
- Hu, Y., Li, Y., Ma, X., Liang, Y., You, W., Pan, X., Zang, Z.: The optimization of SO<sub>2</sub> emissions by the 4DVAR and EnKF  
methods and its application in WRF-Chem, *Sci. Total Environ.*, 888, 163796,  
590 <https://doi.org/10.1016/j.scitotenv.2023.163796>, 2023.
- Hu, Y., Zang, Z., Ma, X., Li, Y., Liang, Y., You, W., Pan, X., Li, Z.: Four-dimensional variational assimilation for SO<sub>2</sub>  
emission and its application around the COVID-19 lockdown in the spring 2020 over China, *Atmos. Chem. Phys.*, 22,  
13183–13200, <https://doi.org/10.5194/acp-22-13183-2022>, 2022.
- Itahashi, S., Irie, H., Shimadera, H., Chatani, S.: Fifteen-year trends (2005–2019) in the satellite-derived ozone-sensitive  
595 regime in East Asia: a gradual shift from VOC-Sensitive to NO<sub>x</sub>-Sensitive, *Remote Sens.*, 14,  
<https://doi.org/10.3390/rs14184512>, 2022.
- Jang, J., Lee, Y. G., Yu, J. A., Sung, K. H., Kim, S. M.: Characteristic Analysis of Tropospheric Ozone Sensitivity from the  
Satellite-Based HCHO/NO<sub>2</sub> Ratio in South Korea, *Korean J. Remote Sens.*, 39 (5–1), 563–576,  
<https://doi.org/10.7780/kjrs.2023.39.5.1.8>, 2023.
- 600 Jeon, W., Choi, Y., Lee, H.W., Lee, S.H., Yoo, J.W., Park, J., Lee, H.J.: A quantitative analysis of grid nudging effect on each  
process of PM<sub>2.5</sub> production in the Korean Peninsula, *Atmos. Environ.*, 122, 763–774, <https://doi.org/10.1016/j.atmosenv.2015.10.050>, 2015.
- Jia, G., Huang, Z., Tang, X., Ou, J., Lu, M., Xu, Y., Zhong, Z., Sha, Q., Wu, H., Zheng, C., Deng, T., Chen, D., He, M., Zheng,  
J.: A meteorologically adjusted ensemble Kalman filter approach for inversing daily emissions: a case study in the Pearl  
605 River Delta, China, *J. Environ. Sci.*, 114, 233–248, <https://doi.org/10.1016/j.jes.2021.08.048>, 2022.
- Judd, L. M., Al-Saadi, J. A., Szykman, J. J., Valin, L. C., Janz, S. J., Kowalewski, M. G., Eskes, H. J., Veefkind, J. P., Cede,  
A., Mueller, M., Gebetsberger, M., Swap, R., Pierce, R. B., Nowlan, C. R., Abad, G. G., Nehrir, A., Williams, D.: Evaluating  
sentinel-5P TROPOMI tropospheric NO<sub>2</sub> column densities with airborne and Pandora spectrometers near New York City  
and Long Island sound, *Atmos. Meas. Tech.*, 13 (11), 6113–6140, <https://doi.org/10.5194/amt-13-6113-2020>, 2020.
- 610 Lamsal, L.N., Martin, R.v., Padmanabhan, A., van Donkelaar, A., Zhang, Q., Sioris, C.E., Chance, K., Kurosu, T.P.,  
Newchurch, M.J.: Application of satellite observations for timely updates to global anthropogenic NO<sub>x</sub> emission inventories,  
*Geophys. Res. Lett.*, 38, L05810, <https://doi.org/10.1029/2010GL046476>, 2011.
- Lee, H.J., Chang, L.S., Jaffe, D.A., Bak, J., Liu, X., Abad, G.G., Jo, H.-Y., Jo, Y.-J., Lee, J.-B., Kim, C.-H.: Ozone continues  
to increase in East Asia despite decreasing NO<sub>2</sub>: Causes and abatements, *Remote Sens.*, 13, 2177,  
615 <https://doi.org/10.3390/rs13112177>, 2021.
- Li, C., Martin, R.V., Shephard, M.W., Cady-Pereira, K., Cooper, M.J., Kaiser, J., Lee, C.J., Zhang, L., Henze, D.K.: Assessing  
the iterative finite difference mass balance and 4D-Var methods to derive ammonia emissions over North America using  
synthetic observations, *J. Geophys. Res.-Atmos.*, 124, 4222–4236, <https://doi.org/10.1029/2018JD030183>, 2019.



- Liu, J., Li, X., Tan, Z., Wang, W., Yang, Y., Zhu, Y., Yang, S., Song, M., Chen, S., Wang, H., Lu, K., Zeng, L., Zhang, Y.:  
620 Assessing the Ratios of Formaldehyde and Glyoxal to  $\text{NO}_2$  as Indicators of  $\text{O}_3$ - $\text{NO}_x$ -VOC Sensitivity, *Environ. Sci. Technol.*,  
55, 10935-10945, <https://doi.org/10.1021/acs.est.0c07506>, 2021.
- Liu, C., Shi, K.: A review on methodology in  $\text{O}_3$ - $\text{NO}_x$ -VOC sensitivity study, *Environ. Pollut.*, 291, 118249,  
<https://doi.org/10.1016/j.envpol.2021.118249>, 2021.
- Millet, D. B., Jacob, D. J., Turquety, S., Hudman, R. C., Wu, S., Fried, A., Walega, J., Heikes, B. G., Blake, D. R., Singh, H.  
625 B., Anderson, B. E., Clarke, A. D.: Formaldehyde distribution over North America: Implications for satellite retrievals of  
formaldehyde columns and isoprene emission, *J. Geophys. Res.-Atmos.*, 111, D24S02, doi:10.1029/2005JD006853, 2006.
- Miller, S.M., Michalak, A.M., Levi, P.J.: Atmospheric inverse modeling with known physical bounds: an example from trace  
gas emissions, *Geosci. Model Dev.*, 7, 303-315, <https://doi.org/10.5194/gmd-7-303-2014>, 2014.
- Momeni, M., Choi, Y., Yeganeh, A.K., Pouyaei, A., Jung, J., Park, J., Shephard, M.W., Damers, E., Cady-Pereira, K.E.:  
630 Constraining East Asia ammonia emissions through satellite observations and iterative Finite Difference Mass Balance  
(iFDMB) and investigating its impact on inorganic fine particulate matter, *Environ. Int.*, 184, 108473,  
<https://doi.org/10.1016/j.envint.2024.108473>, 2023.
- Moon, J., Choi, Y., Jeon, W., Kim, H.C., Pouyaei, A., Jung, J., Pan, S., Kim, S., Kim, C.-H., Bak, J., Yoo, J.-W., Park, J., Kim,  
D.: Hybrid IFDMB/4D-Var inverse modeling to constrain the spatiotemporal distribution of CO and  $\text{NO}_2$  emissions using  
635 the CMAQ adjoint model, *Atmos. Environ.*, 327, 120490, <https://doi.org/10.1016/j.atmosenv.2024.120490>, 2024.
- Mun, J., Choi, Y., Jeon, W., Lee, H.W., Kim, C.-H., Park, S.-Y., Bak, J., Jung, J., Oh, I., Park, J., Kim, D.: Assessing mass  
balance-based inverse modeling methods via a pseudo-observation test to constrain  $\text{NO}_x$  emissions over South Korea, *Atmos.*  
*Environ.*, 292, 119429, <https://doi.org/10.1016/j.atmosenv.2022.119429>, 2023.
- Oomen, G.-M., Müller, J.-F., Stavrou, T., De Smedt, I., Blumenstock, T., Kivi, R., Makarova, M., Palm, M., Röhling, A.,  
640 Té, Y., Vigouroux, C., Friedrich, M. M., Frieß, U., Hendrick, F., Merlaud, A., PETERS, A., Richter, A., Van Roozendaal, M.,  
Wagner, T.: Weekly derived top-down volatileorganic-compound fluxes over Europe from TROPOMI HCHO data from  
2018 to 2021, *Atmos. Chem. Phys.*, 24, 449–474, <https://doi.org/10.5194/acp-24-449-2024>, 2024.
- Peng, Z., Liu, Z., Chen, D., Ban, J.: Improving  $\text{PM}_{2.5}$  forecast over China by the joint adjustment of initial conditions and  
source emissions with an ensemble Kalman filter, *Atmos. Chem. Phys.*, 17, 4837–4855, [https://doi.org/10.5194/acp-17-](https://doi.org/10.5194/acp-17-4837-2017)  
645 4837-2017, 2017.
- Qu, Z., Henze, D.K., Theys, N., Wang, J., Wang, W.: Hybrid Mass balance/4D-var joint inversion of  $\text{NO}_x$  and  $\text{SO}_2$  emissions  
in East Asia, *J. Geophys. Res.-Atmos.*, 124, 8203–8224. <https://doi.org/10.1029/2018JD030240>, 2019.
- Rahman, M.M., Shults, R., Ali, M.F., Hasan, M.G., Shuo, W., Formaldehyde-to-Nitrogen dioxide ratio (FNR) analysis for  
ozone sensitivity: a case study over Bangladesh using OMI data, *Air. Qual. Atmos. Hlth.*, 18, 1879-1886,  
650 <https://doi.org/10.1007/s11869-025-01732-5>, 2025.



- Raza, A., Dahlquist, M., Lind, T., Ljungman, P.L.S.: Susceptibility to short-term ozone exposure and cardiovascular and respiratory mortality by previous hospitalizations, *Environ. Health*, 17, 37, <https://doi.org/10.1186/s12940-018-0384-z>, 2018.
- Sillman, S.: The use of NO<sub>y</sub>, H<sub>2</sub>O<sub>2</sub>, and HNO<sub>3</sub> as indicators for ozone-NO<sub>x</sub>- hydrocarbon sensitivity in urban locations, *J. Geophys. Res.*, 100 (D7), 14175-14188, <https://doi.org/10.1029/94JD02953>, 1995.
- Skamarock, W.C., Klemp, J.B., Dudhia, J., Gill, D.O., Barker, D.M., Duda, M.G., Huang, X.-Y., Wang, W., Powers, J.G.: A Description of the Advanced Research WRF Version 3, National Center for Atmospheric Research, Boulder, CO, USA, 2008.
- Solazzo, E., Crippa, M., Guizzardi, D., Muntean, M., Choulga, M., Janssens-Maenhout, G., Uncertainties in the Emissions Database for Global Atmospheric Research (EDGAR) emission inventory of greenhouse gases, *Atmos. Chem. Phys.*, 21, 5655-5683, <https://doi.org/10.5194/acp-21-5655-2021>, 2021.
- Souri, A.H., Choi, Y., Jeon, W., Li, X., Pan, S., Diao, L., Westenbarger, D.A.: Constraining NO<sub>x</sub> emissions using satellite NO<sub>2</sub> measurements during 2013 DISCOVER-AQ Texas campaign, *Atmos. Environ.*, 131, 371–381, <https://doi.org/10.1016/j.atmosenv.2016.02.020>, 2016.
- Turner, M.C., Jerrett, M., Pope, C.A., Krewski, D., Gapstur, S.M., Diver, W.R., Beckerman, B.S., Marshall, J.D., Su, J., Crouse, D.L., Burnett, R.T.: Long-term ozone exposure and mortality in a large prospective study, *Am. J. Respir. Crit. Care Med.*, 193, 1134–1142, <https://doi.org/10.1164/rccm.201508-1633OC>, 2016.
- van Geffen, J., Eskes, H., Compernelle, S., Pinardi, G., Verhoelst, T., Lambert, J.-C., Sneep, M., ter Linden, M., Ludewig, A., Boersma, K.F., Veefkind, J.P.: Sentinel5P TROPOMI NO<sub>2</sub> retrieval: impact of version v2.2 improvements and comparisons with OMI and ground-based data, *Atmos. Meas. Tech.*, 15, 2037–2060, <https://doi.org/10.5194/amt-15-2037-2022>, 2022.
- Veefkind, J., Aben, I., McMullan, K., Förster, H., De Vries, J., Otter, G., Claas, J., Eskes, H., De Haan, J., Kleipool, Q., van Weele, M., Hasekamp, O., Hoogeveen, R., Landgraf, J., Snel, R., Tol, P., Ingmann, P., Voors, R., Levelt, P.F.: TROPOMI on the ESA Sentinel-5 precursor: a GMES mission for global observations of the atmospheric composition for climate, air quality and ozone layer applications, *Remote Sens. Environ.*, 120, 70–83, <https://doi.org/10.1016/j.rse.2011.09.027>, 2012.
- Voshtani, S., Ménard, R., Walker, T.W., Hakami, A.: Use of Assimilation Analysis in 4D-Var Source Inversion: Observing System Simulation Experiments (OSSEs) with GOSAT Methane and Hemispheric CMAQ, *Atmosphere*, 14, 758, <https://doi.org/10.3390/atmos14040758>, 2023.
- Wang, Y., Wang, J., Xu, X., Henze, D.K., Qu, Z., Yang, K.: Inverse modeling of SO<sub>2</sub> and NO<sub>x</sub> emissions over China using multisensor satellite data - Part 1: Formulation and sensitivity analysis, *Atmos. Chem. Phys.*, 20, 6631–6650, <https://doi.org/10.5194/acp-20-6631-2020>, 2020.
- Wang, Y., Yu, C., Tao, J., Wang, Z., Si, Y., Cheng, L., Wang, H., Zhu, S., Chen, L.: Spatio-temporal characteristics of tropospheric ozone and its precursors in Guangxi, South China, *Atmosphere*, 9, 355, <https://doi.org/10.3390/atmos9090355>, 2018.



- 685 Wang, Z., Zhang, H., Shi, C., Ji, X., Zhu, Y., Xia, C., Sun, X., Zhang, M., Lin, X., Yan, S., Zhou, Y., Xing, C., Chen, Y., Liu, C.: Vertical and spatial differences in ozone formation sensitivities under different ozone pollution levels in eastern Chinese cities, *Npj Clim. Atmos. Sci.*, 8, 30, <https://doi.org/10.1038/s41612-024-00855-3>, 2025.
- Wu, H., Kong, L., Tang, X., Zhu, L., Zhu, J., Wang, Z.: Air quality forecasting with inversely updated emissions for China, *Environ. Sci. Technol. Lett.*, 10 (8), 655–661, <https://doi.org/10.1021/acs.estlett.3c00266>, 2023.
- 690 Yu, X., Millet, D.B., Henze, D.K.: How well can inverse analyses of high-resolution satellite data resolve heterogeneous methane fluxes? Observing system simulation experiments with the GEOS-Chem adjoint model (v35), *Geosci. Model Dev.*, 14, 7775–7793, <https://doi.org/10.5194/gmd-14-7775-2021>, 2021.
- Zhao, S., Russell, M. G., Hakami, A., Capps, S. L., Turner, M. D., Henze, D. K., Percell, P. B., Resler, J., Shen, H., Russell, A. G., Nenes, A., Pappin, A. J., Napelenok, S. L., Bash, J. O., Fahey, K. M., Carmichael, G. R., Stanier, C. O., Chai, T.: A
- 695 multiphase CMAQ version 5.0 adjoint, *Geosci. Model Dev.*, 13, 2925–2944, <https://doi.org/10.5194/gmd-13-2925-2020>, 2020, 2020.
- Zhao, Y., Nielsen, C.P., Lei, Y., McElroy, M.B., Hao, J.: Quantifying the uncertainties of a bottom-up emission inventory of anthropogenic atmospheric pollutants in China, *Atmos. Chem. Phys.*, 11, 2295–2308, <https://doi.org/10.5194/acp-11-2295-2011>, 2011.

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