



1 **Reconstruction of reservoir water level-storage relationship**
2 **based on capacity loss induced by sediment accumulation and**
3 **its impact on flood control operation**

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15 **Abstract.** Sediment accumulation in reservoirs can change the predefined water level-
16 storage (WLS) relationship by significantly reducing the storage capacity, further
17 threatening the flood control safety of reservoirs in long-term scheduling and operation.
18 However, reconstructing the WLS relationship has long been challenging, especially on
19 a large scale, due to the difficulties of traditional field bathymetric measurement. To fill
20 this knowledge gap, a method to estimate the reservoir WLS curve based on the
21 capacity loss induced by sediment accumulation is proposed in this study. To assess the
22 potential negative impact caused by inaccurate WLS curve, flood regulation
23 calculations for reservoirs are performed individually using six design flood
24 hydrographs with return intervals ranging from 200–10,000 years as reservoir inflow.
25 The flood regulation risk is quantified using the maximum flood regulation water level
26 (Z^*) and the ratio of periods exceeding the design flood level (γ). Based on hydrological
27 and sediment data and operational information over ten years, a cascade of nine
28 reservoirs in the Wujiang River in China is selected to conduct the established method.



29 The results show that sediment accumulation is more severe in reservoirs located in the
30 middle and upper reaches of the Wujiang River, leading to the most significant
31 reduction in capacity loss volume for Hongjiadu (180.3 million m³) and the largest loss
32 rate for Suofengying (25.02%) reservoirs. Using the current design WLS curve for
33 flood regulation calculations, Z^* is underestimated by 7.11 m and 1.84 m, and γ by 2%
34 and 3% for Suofengying and Dongfeng reservoirs, respectively, compared with the
35 reconstructed one. This underestimation increases with the length of the return interval.
36 This indicates that when storage capacity is considerably reduced, continued use of the
37 existing design WLS curve may significantly underestimate flood regulation risks, thus
38 posing potential safety hazards to the reservoir itself and downstream flood protection
39 objects.

40 **1 Introduction**

41 Reservoirs are artificial or heavily modified water bodies formed using dams, sluices,
42 and other engineering infrastructure for the purpose of regulating river discharge.
43 Reservoirs and dams play a critical role in modern water resources management and
44 utilization by generating electricity, mitigating flood risks, and supplying water
45 (Castelletti et al., 2012; Sen, 2021; Zhou et al., 2021). In the past century, more than
46 50,000 large reservoirs have been constructed worldwide, regulating over half of the
47 major river systems globally, with a total storage capacity of over 8,000 km³ (Hanasaki
48 et al., 2006). The volume of water stored in these reservoirs exceeds 20% of the world's
49 annual average runoff, equivalent to three times the annual average water storage in all
50 river channels globally, making them crucial elements in the hydrological and
51 biochemical cycles (Yassin et al., 2019). The number of reservoirs under construction
52 and planning continues to increase rapidly to meet the demands of population growth
53 and socioeconomic development, especially in developing countries (Zhong et al.,
54 2020). For instance, China has the largest number of reservoirs in the world, and
55 according to the First Bulletin of the National Water Resources Census, as of 2011,
56 China has a total of 98,002 reservoirs in operation or under construction, with a total



57 storage capacity exceeding 932.3 billion m³.

58 Reservoir water storage is a key variable in reservoir hydrology and serves as
59 fundamental information for reservoir scheduling and operational management (Gao,
60 2015; Liu et al., 2022). The primary method for obtaining reservoir water storage during
61 routine operations is by referring to the water level-storage (WLS) curve, which
62 quantifies the functional relationship between water level and storage based on gauge
63 water level observations. Therefore, the accuracy and reliability of the WLS curve are
64 crucial for determining the characteristic storage capacities of reservoirs, such as the
65 normal storage capacity and flood control storage capacity, which directly influence the
66 effectiveness of subsequent reservoir operations and management decisions. However,
67 the water storage capacity of a reservoir can change during long-term operation due to
68 multiple factors, both natural and anthropogenic, including river diversion, sand mining,
69 and especially sediment deposition. Sediment carried by upstream inflows can be
70 trapped by the dam and thus accumulate in the reservoir, continuously reducing its
71 effective storage capacity. If the extent of sediment accumulation and the storage
72 capacity are not investigated in a timely manner, the outdated design WLS curve will
73 continue to be used, potentially leading to a decline in the functionality and overall
74 benefits of the reservoir, or even causing safety incidents.

75 There are two main methods that have traditionally been used to reconstruct WLS
76 functional relationship in previous studies. The first method involves conducting
77 topographic surveys in the reservoir area to estimate the reservoir storage capacity. For
78 example, Sawunyama (2006) conducted field measurements of water depth and
79 coordinates in the reservoir to establish a power function between surface area and
80 storage capacity. Zhang et al. (2011) used an in situ bathymetric survey approach to
81 measure the water depth of a high-altitude lake and create isobathic maps to calculate
82 the storage capacity. However, the field measurement method is often limited by long
83 survey durations, complex topography conditions, and high costs, which collectively
84 make updating the WLS curve difficult. In recent years, the launch of high-resolution
85 optical and synthetic aperture radar (SAR) satellites has advanced satellite remote
86 sensing technology, positioning it as a cutting-edge tool in hydrology. These



87 technologies have gradually been applied to reservoirs and dams monitoring, although
88 this is still in its preliminary stages and accuracy needs to be improved (Gourgouletis
89 et al., 2022). By extracting reservoir areas from remote sensing images and combining
90 them with satellite radar altimetry, relationships among reservoir water levels, areas,
91 and storage volumes can be established to reconstruct Z-A-V (Elevation-Area-Volume)
92 curves (Gao et al., 2012; Guan et al., 2021; Li et al., 2020; Zhang et al., 2017).

93 The second method is based on measured hydrological data to estimate and revise
94 the WLS curve using the water balance principle. Specifically, the WLS curve can be
95 derived from the relationship between water level increments and storage capacity
96 increments detected from hydrological data measured during the dry season (Su Yepeng,
97 1999). Liu Dezong (1992) transformed the WLS curve calibration problem into an
98 outflow measurement problem through water balance analysis and verified the validity
99 of the reconstructed WLS curve for the Xueye Reservoir. On the other hand, the
100 accuracy of the WLS curve reconstructed using water balance relations is influenced to
101 some extent by the selected data to some extent, and there are challenges in determining
102 certain parameters in the water balance equation. Given the limitations of the above
103 approaches, although numerous previous studies have emphasized the urgent need to
104 recheck the reservoir WLS curve, most reservoirs have not yet conducted storage
105 capacity estimations.

106 Notably, sediment accumulation in reservoirs offers barriers to natural sediment
107 transport along river courses. Thus it is the key factor leading to the reduction of storage
108 capacity and results in serious problems in operation management (Sedláček et al.,
109 2022). As a result, the loss of reservoir storage capacity in China is the most serious in
110 the world, with an average capacity loss rate of over 11.27%, which is 2 to 4 times the
111 global average (Ran et al., 2013; Zhang et al., 2023). Estimating the storage capacity
112 loss induced by sediment accumulation and reconstructing the WLS curve provides a
113 new direction for the second category of methods (Huang et al., 2018). However, few
114 studies have investigated the validity of reconstructing the WLS curve based on
115 sediment accumulation, and there has been insufficient attention to the practical
116 effectiveness of the reconstructed curve. In particular, the differences in flood



117 regulation performance between the two curves, before and after reconstruction, have
118 not yet been elucidated.

119 To fill this knowledge gap, this study aims to estimate the WLS relationship of
120 reservoirs by proposing a storage capacity loss rate (LR) indicator based on sediment
121 accumulation and, furthermore, to identify the impact of the reservoir WSL relationship
122 on flood control operations through flood regulation risk indicators. A cascade of nine
123 reservoirs in the Wujiang River is used as a case study to conduct the reservoir WLS
124 curve estimation and impact analysis. Specifically, we seek to address the following
125 scientific questions: (a) What are the characteristics of sediment accumulation among
126 different reservoirs in the selected cascade? (b) Can the reservoir WLS curve be
127 effectively reconstructed using the proposed water storage capacity LR framework,
128 based on long-term water and sediment data? and (c) What is the impact of the outdated
129 design WLS curve on flood control operations?

130 The remainder of this paper is organized as follows: Section 2 describes the cascade
131 reservoirs located in the Wujiang River basin, along with observed water and sediment
132 data; Section 3 introduces the estimation of the LR indicator, reconstruction of the WLS
133 curve, and detection of flood prevention operation responses on the WLS curves before
134 and after reconstruction; Section 4 presents and discusses the results of our analysis;
135 finally, Section 5 provides the primary conclusions of this study.

136 **2 Study area and data**

137 **2.1 study area**

138 The Wujiang River, the largest tributary on the southern bank of the upper reaches of
139 the Yangtze River, is characterized by its considerable natural elevation drop and
140 abundant hydropower resources. The Wujiang River Basin covers a catchment area of
141 87,920 km² and extends over a length of 1,037 km with a natural fall of 2,124 m, and
142 has a subtropical wet monsoon climate. The basin's integral role in the "West-East
143 Electricity Transmission" project enhances its prominence, establishing it as the critical
144 one of China's thirteen major hydropower bases. The cascade reservoir system of the



145 Wujiang River used in this study comprises nine reservoirs with varying shapes, surface
146 areas, and regulation capacities. The Wujiang River exhibits relatively stable annual
147 runoff. The Hongjiadu (WJD) reservoir, in the upstream section, acts as the "leading
148 reservoir" of the cascade reservoir system, offering multi-year regulation capability.
149 The midstream Wujiangdu (WJD) reservoir provides annual regulation, while the
150 downstream Goupitan (GPT) reservoir also supports multi-year regulation. The spatial
151 distribution of reservoirs in the Wujiang River basin is illustrated in Fig. 1 After the
152 gradual completion of the cascade system in the basin, the Wujiang River Basin has
153 aggravated the interception of sediment. As a result, during long-term operation, the
154 storage capacity of the nine-reservoir cascade system has suffered varying degrees of
155 loss, which has had a potential negative impact on the operation and scheduling of the
156 reservoirs.

157 Before 1990, the mean sediment accumulation in the capacity of reservoirs along the
158 Wujiang River is about 9 million tons annually, predominantly influenced by large
159 reservoirs, while small and medium-sized reservoirs contribute a minor fraction of the
160 total capacity. From 1991 to 2005, the primary reservoirs that intercepted sediment on
161 the Wujiang River mainstream transitioned to the HJD and DF reservoirs, which were
162 impounded in 1994 and 2004 years, respectively. The average multi-year sediment
163 accumulation in the capacity of reservoirs on the Wujiang River was 16 million tons,
164 reflecting an increase compared with the period from 1956 to 1990, along with a rise in
165 the proportion of sediment accumulation in major reservoirs. Since 2006, although the
166 reservoirs located on the lower reaches of the Wujiang River have gradually completed
167 and began to operate, the HJD and DF Reservoirs in the upper reaches remain the
168 primary reservoirs for sand retention.

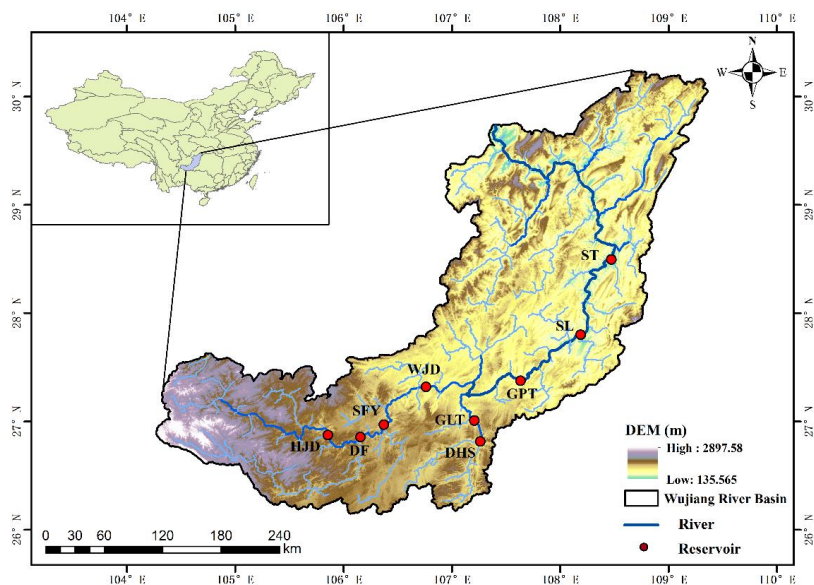


Figure 1. Location of the Wujiang River Basin and cascade reservoirs (HJD, DF, SFY, WJD, GPT, SL, ST, GLT, DHS denote the Hongjiadu and Dongfeng, Suofengying, Wujiangdu, Goupitan, Silin, Shatuo, Goupitan, Geliqiao and Dahuashui Reservoirs, respectively. Same as below.)

2.2 Data

This study collects fundamental hydrological and sediment data, such as sand content in the inflow water, inflow and outflow, and reservoir operation information including total storage capacity, design flood level, and calibration flood level for the nine-reservoir cascade system. Rigorous quality control on the water and sediment data was conducted by manually verifying and rectifying anomalous and erroneous data. The main parameters of each reservoir are presented in Table 1 It is worth noting that the duration of the selected hydrological and sediment data varies from 10 to 23 years during 2001 to 2023 among different reservoirs, due to different beginning time of construction and operation for different reservoirs.

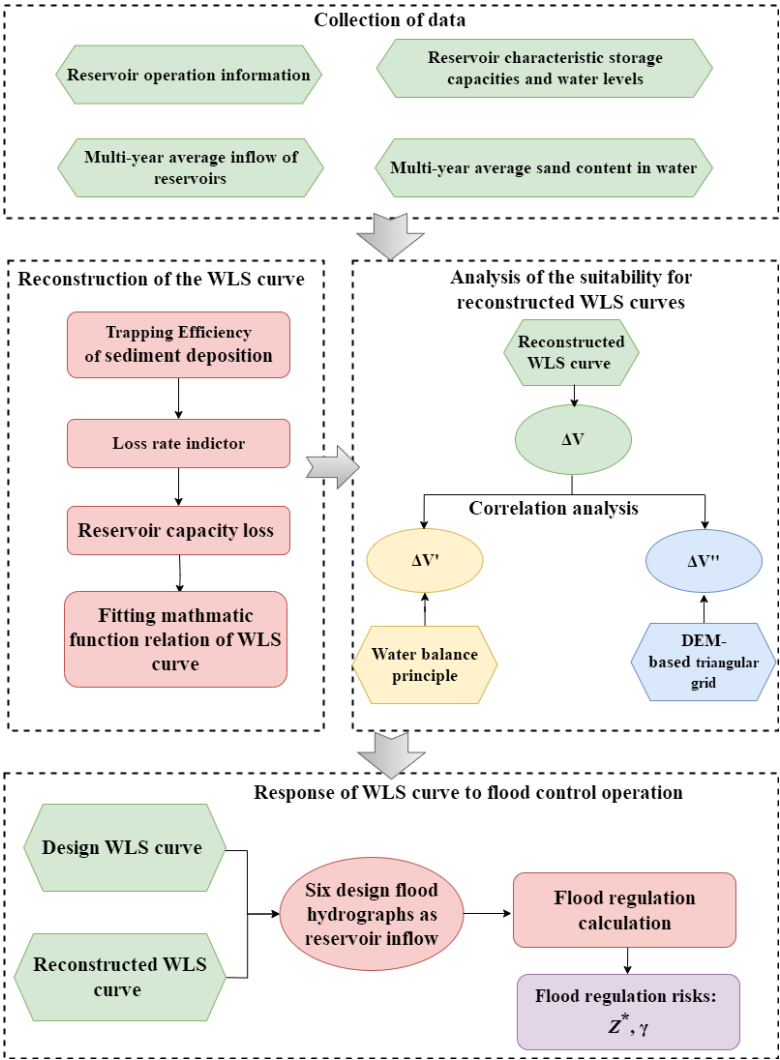


Table 1. Basic reservoir information of the Wujiang River

Reservoir	Total storage capacity (10 ⁸ m ³)	Dead storage capacity (10 ⁸ m ³)	Regulating capacity (10 ⁸ m ³)	Normal storage level (m)	Dead water level (m)	Design Flood Level (m)	Calibration Flood Level (m)
HJD	49.47	11.36	33.61	1140	1076.0	1141.34	1145.40
DF	10.25	3.74	4.91	970	936.0	975.69	977.53
SFY	2.01	1.01	0.67	837	822.0	837.97	842.37
WJD	23.0	7.8	13.60	760	720.0	760.30	762.80
GPT	64.54	26.62	29.02	630	590.0	632.89	638.36
SL	15.93	8.88	3.17	440	431.0	445.15	449.45
ST	9.21	4.83	2.87	365	353.5	366.73	369.65
DHS	2.77	1.15	1.355	868	845.0	868.43	871.35
GLQ	0.77	0.51	0.19	719	709.0	719.40	722.58

183 3 Methods

184 This study proposes a storage capacity LR indicator based on sediment accumulation
 185 to estimate the WLS relationship of reservoirs first. Second, flood regulation
 186 calculations are performed at reservoirs with relatively higher LR values, using six
 187 design flood hydrographs with different return intervals as typical inflow discharge, to
 188 identify the impact of reservoir WSL relationship on flood control operation. Finally,
 189 the flood regulation risks are assessed to quantify the response of the scheduling process
 190 to the reconstructed WLS relationship. The detailed methods and steps of this study are
 191 as follows (Fig. 2).



192

193 **Figure 2.** Schematic of the framework in this study.

194 **3.1 Deriving reservoir capacity loss volume and rate due to sediment accumulation**

195 In this study, the reservoir storage capacity LR due to sediment accumulation for each
196 reservoir in the cascade system is calculated based on the inflow series, sand content in
197 inflow water, and total reservoir capacity during the period covered by the documented
198 data. Subsequently, the corrected LR for each reservoir's storage capacity since its
199 construction is determined. For convenience, we assumes that the sediment
200 accumulation is spatio-temporally uniform. That is, the sediment is uniformly



distributed in the bottom and the deposition velocity is the same every year. Therefore, the LR represents the proportion of multi-year average reservoir storage capacity loss. The calculation equation of LR is as follows:

$$LR_i = \frac{n_i \times w_i \times Te_i}{\rho \times RC_i} \quad (1)$$

where n_i is the temporal interval of recorded data for the i th reservoir, in the unit of year; RC_i represents the reservoir capacity, measured in 10^8 m^3 ; w_i denotes the long-term average sediment contained in the inflow water of the i th reservoir, quantified in 10^8 kg/a ; ρ indicates the density of deposited sediment, expressed in kg/m^3 ; and Te_i reflects the sediment trapping efficiency, initially introduced by Brune (1953) and further extended and popularized by Mulu and Dwarakish et al. (2015) and Liu et al. (2022). The deposition rate of the sediment input into the reservoir represented by Te_i was simplified into the ratio of reservoir capacity to incoming flow, as follows:

$$Te_i = 1 - \frac{0.05\alpha}{\sqrt{\Lambda\tau}} \quad (2)$$

where α is the correction factor; $\Lambda\tau$ is the reservoir stagnation time, $\Lambda\tau = RC_i / Q_i$;

and Q_i is the multi-year average inflow water volume at the dam site of the i th reservoir, 10^8 m^3 .

3.2 Nonlinear fitting of the reservoir WLS relationship

The feature of reservoir capacity can be represented by a series of discrete water level and storage data. However, this can lead to inefficiencies in the algorithmic resolution of the scheduling model. In contrast, quantitative description can enhance the efficiency of various algorithms for solving the scheduling model. Therefore, it is essential to fit the discrete data points of water levels and storages into a functional relationship. In conjunction with the current literature on the fitting of reservoir WLS curves, elementary functions are amalgamated through rational operations to formulate three types of mathematic function (Eqs. 3- 5).

$$Z = f_1(V) = \alpha_1 V^3 + \alpha_2 V^2 + \alpha_3 V + \alpha_4 \quad (3)$$

$$Z = f_2(V) = \beta_1 V^{\beta_2} + \beta_3 \quad (4)$$

$$Z = f_3(V) = \gamma_1 e^{\gamma_2 V} + \gamma_3 e^{\gamma_4 V} \quad (5)$$

where V is the reservoir storage capacity, 10^8 m^3 ; Z is the concurrent water level, m;



230 and f_1, f_2 and f_3 represent polynomial, power, and exponential functions, respectively.

231 To assess the goodness-of-fit of the nonlinear models f_1, f_2 , and f_3 compared with the
232 discrete data points of reservoir water levels and storages, in this study, we employ three
233 typical statistical indices, including determination coefficient (R^2), sum squared error
234 (SSE), and root mean square error (RMSE) (Eqs. 6- 8).

$$235 \quad \text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N (Z_i - \hat{Z}_i)^2} \quad (6)$$

$$236 \quad R^2 = 1 - \frac{\sum_{i=1}^N (Z_i - \hat{Z}_i)^2}{\sum_{i=1}^N (Z_i - \bar{Z}_i)^2} \quad (7)$$

$$237 \quad \text{SSE} = \sum_{i=1}^N (Z_i - \hat{Z}_i)^2 \quad (8)$$

238 where Z_i is the observed water level corresponding to the assessed reservoir capacity V_i ,
239 m; $\hat{Z}_i$ is the estimated reservoir level, derived from back extrapolation of the reservoir
240 WLS curve, referred to as $\hat{Z}_i = f(V_i)$, m; $\bar{Z}_i$ is the average water level, m; and N is the
241 number of discrete data points sampled from reservoir WLS curve used to evaluate the
242 performance of the fitted relationship.

243 3.3 Reconstructing reservoir WLS curve based on the loss rate

244 The cumulative storage capacity loss over the period covered by the documented data
245 can be estimated first, based on the corrected storage capacity LR for each reservoir
246 determined in Section 3.1. Second, the total capacity loss is deducted from the original
247 capacity of discrete data points to derive the calibrated water level-storage discrete data
248 points. Third, the optimal line of f_i ($i = 1, 2, 3$) is fitted to model the calibrated discrete
249 data points of water levels and storages for the nine reservoirs, using the goodness-of-
250 fit evaluation metrics introduced in Section 3.2 and deriving the reconstructed WLS
251 curve, $Z = f'(V)$.

252 In this study, we employ two approaches, i.e., water balance equation and DEM, to
253 indirectly analyze the suitability of the reconstructed WLS curve. For the former, the
254 change of reservoir water storage detected from water balance budgets was compared
255 with that from storage capacity loss. The water storage volume change of the reservoir



over any time period is determined by the inflow water volume, outflow water volume, rainfall, evaporation, and seepage using the water balance equation represented in Eq. (9). The summer flood season in the Wujiang River basin is marked by rain storm which results in significant fluctuations in reservoir water storage. During this period, inflow and outflow dominate the variations in reservoir water storage, while the effects of rainfall, evaporation, and seepage on the closure of water balance are comparatively minimal. Consequently, we explore the measured inflow and outflow from April to August 2023 to estimate the change in reservoir water storage $\Delta V'$ according to water balance relation.

$$\Delta V' = V_{in} - V_{out} - V_{ET} - V_{seep} + V_{rain} \quad (9)$$

where $\Delta V'$ is the change in reservoir water storage, m^3 ; V_{in} is the volume of inflow water entering the reservoir, m^3 ; V_{out} is the volume of outflow water released from the reservoir, m^3 ; V_{ET} is the volume of water evaporated from the reservoir, m^3 ; V_{seep} is the volume of reservoir leakage water, m^3 ; and V_{rain} is the rainfall water falling into the reservoir surface.

As for the latter approach, we derive some discrete data of water levels and storages based on traditional method with DEM data to quantify the similarity with reconstructed WLS curve. This process primarily involves selecting the Copernicus DEM digital elevation model with a resolution of 30 m to create a digital triangular grid, using the ArcGIS platform to extract the surface area corresponding to each elevation at 1 m intervals, resulting in a series of scatter points representing the relationship between water levels and surface areas, then employing the prismatic table method (Eqs. 10-11) to calculate the reservoir storage capacity changes between adjacent water levels, finally, integrating the volume computed by ArcGIS at the initial elevation surface to derive the WLS curve, which is then compared with the reconstructed and design reservoir WLS curves.

$$V_i = \frac{1}{3} \Delta h (S_{i-1} + \sqrt{S_{i-1}S_i} + S_i) \quad (10)$$

$$V = \sum_{i=1}^L V_i + V_0 \quad (11)$$

where V_i is the difference in reservoir capacity between two neighboring water levels,



285 10^8 m^3 ; Δh is the water level difference between two neighboring water levels, m; S_i ,
286 S_{i-1} are the water surface areas corresponding to the two neighboring water levels, m^2 ;
287 i is the serial number; L is the cumulative number, and V_0 is the initial reservoir capacity,
288 10^8 m^3 .

289 **3.4 Quantifying the response of flood control operation to the WLS curve**

290 To demonstrate the necessity of rechecking current reservoir WLS curve, we select
291 reservoirs with higher LR values to implement the flood regulation calculation to assess
292 the resulting flood risks with reservoir WLS curve before and after the reconstruction,
293 respectively. Six design flood hydrographs with return intervals varying from 200 to
294 10000 years are individually taken as reservoir inflow discharge to quantify flood
295 operation risks. The flood operation risks are quantified based on the maximum
296 regulation water level (Z^*) and the ratio of the number of time periods in which the
297 characteristic water level is surpassed to the total number of time periods (γ). Flood
298 regulation calculations are conducted utilizing the water balance equation (Eq. 12). If
299 the values of Z^* and γ generated from reconstructed WLS curve exceed those generated
300 using the design WLS curve currently in use, it indicates that continued use of the
301 existing design WLS curve will lead to a potential underestimation of risk in flood
302 control and dispatching.

$$303 \quad V_2 - V_1 = \frac{(Q_1 + Q_2)}{2} \times \Delta t - \frac{(q_1 + q_2)}{2} \times \Delta t \quad (12)$$

304 where V_1 and V_2 denote the reservoir storage capacity at the beginning and end of the
305 time period, respectively, m^3 ; Q_1 and Q_2 are the inflow discharge at the beginning and
306 end of the time period, respectively, m^3/s ; q_1 and q_2 are the outflow discharge at the
307 beginning and end of the time period, respectively, m^3/s ; and Δt is the length of the time
308 period, h.

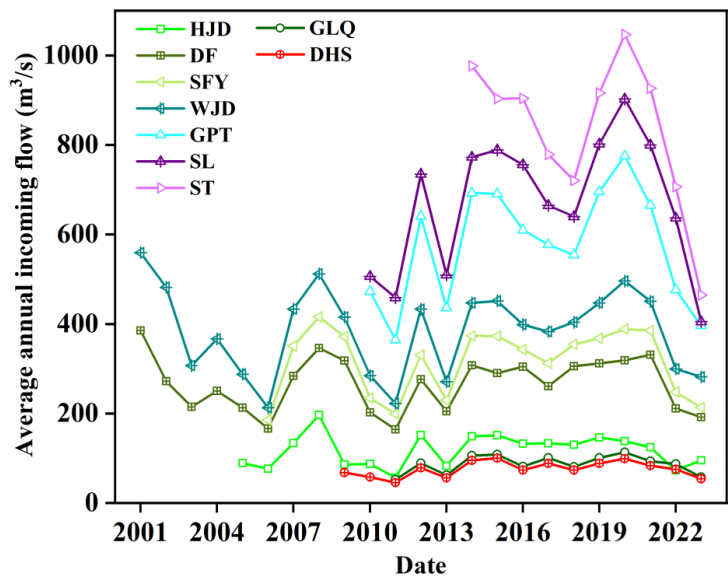
309 **4 Results**

310 **4.1 Analysis of total reservoir storage capacity loss rate and volume**

311 Figure. 3 illustrates the temporal dynamics of annual average inflow for each reservoir.



312 From Fig. 3, it can be clearly observed that the average annual inflow of reservoirs
313 located at the main stream increases progressively from upstream to downstream of the
314 Wujiang River. Hongjiadu Reservoir acts as the primary reservoir in the cascade system,
315 and shows low annual average inflow of between about 100 to 200 m³/s. Dongfeng,
316 Suofengying, and Wujiangdu Reservoirs exhibit median annual average inflows from
317 200 to 500 m³/s. In contrast, Goupitan, Silin, and Shatuo Reservoirs receive high annual
318 average inflow between 500 and 1000 m³/s. Dahuashui and Geliquiao Reservoirs are
319 located in the tributaries of the Wujiang River. Thus, their annual average inflow is
320 significantly lower than that of the main stream reservoirs, with a peak annual average
321 inflow of 113.53 m³/s recorded in 2020.



322
323 **Figure 3.** Dynamics of annual average inflow of the cascade reservoirs (The periods covered by
324 inflow data varies due to the reservoirs constructed in tributary and downstream is later than those
325 upstream.)

326 The intermediate results for deriving the LR of water storage capacity for each
327 reservoir in the cascade system are presented in Table 2 Subsequently, the total reservoir
328 capacity loss attributed to sediment deposition in each reservoir is derived from the
329 reservoir capacity LR, as illustrated in Fig. 4. In Fig. 4, the SFY Reservoir shows the
330 highest value of LR of 25.02%, followed by the DF and WJD Reservoirs with LR of

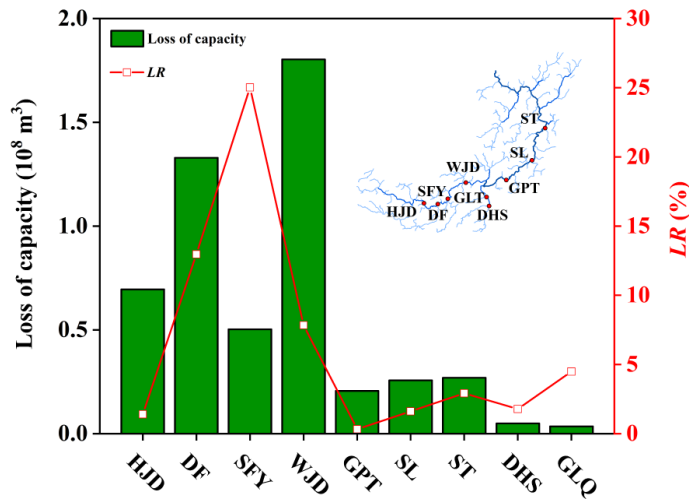


331 12.96% and 7.84%, respectively. The remaining six reservoirs demonstrate lower
332 capacity loss rates ranging from 0.32% to 4.49%. The WJD Reservoir exhibits the
333 highest volume of capacity loss of 180.3 million m³, followed by the DF, HJD, and SFY
334 Reservoirs with losses of 132.9 million m³, 169.5 million m³, and 50.3 million m³,
335 respectively. The other five reservoirs demonstrate lower capacity losses ranging from
336 0.035 million m³ to 26.9 million m³. It is indicated that the reservoirs with large capacity
337 losses (exceeding 5%) are situated in the middle and upper reaches of the Wujiang River,
338 in accordance with the principle that upstream reservoirs prioritize the capture of sand
339 in inflow water.

340 **Table 2.** Calculation table for the rate of loss of storage capacity

Reservoir	Time interval of data (year)	Sand content of inflow water (kg/m ³)	RC_i (10 ⁸ m ³)	Te_i (%)	w_i (10 ⁸ kg)
HJD	19	1.460	49.470	0.957	53.509
DF	23	1.130	10.250	0.856	94.434
SFY	18	0.609	2.012	0.648	60.428
WJD	23	0.982	23.000	0.885	118.881
GPT	14	0.127	64.540	0.916	22.471
SL	14	0.154	15.930	0.818	31.370
ST	10	0.204	9.210	0.733	51.374
DHS	15	0.228	2.765	0.852	5.390
GLQ	13	0.229	0.774	0.701	5.341

341



342

343 **Figure 4.** Rate and volume of the storage capacity loss in various reservoirs due to sedimentation
344 accumulation



4.2 Reconstructing the reservoir WLS curve

Three mathematic function types, i.e., f_1 , f_2 , and f_3 , were employed to fit the discrete raw water level-storage data points for each reservoir in the Wujiang cascade system, and the statistic indices were quantified to evaluate the goodness-of-fit of the regression coefficients. Figure 5 illustrates that the function type of f_2 , with the formula of $Z = f_2(V) = \beta_1 V^{\beta_2} + \beta_3$, demonstrates superior performance in modeling the relationship between reservoir water level and storage across the nine reservoirs. The goodness-of-fit indexes for type f_2 are consistently similar among different reservoirs, reflecting superior fitting performances of f_2 and indicating its applicability and reliability in depicting WLS curve. Conversely, function types of f_1 and f_3 exhibit satisfactory fitting performance in Dongfeng and Wujiangdu Reservoirs; however, they perform poorly in other reservoirs, revealing significant discrepancies among different reservoirs. This suggests that function types of f_1 and f_3 do not fulfill the reliability requirements for all reservoirs, indicating insufficient applicability. Consequently, $Z = f_2(V) = \beta_1 V^{\beta_2} + \beta_3$ is selected as the appropriate fitting function curve for the cascade reservoir system. The original water level-storage discrete point data for each reservoir within this cascade system were fitted to determine the regression coefficients. Subsequently, these parameters were combined with the adopted discrete point data generated by subtracting storage capacity losses, to obtain the new parameters for the reconstructed capacity curves of each reservoir. The regression coefficients in f_2 , which are optimized by the Least Squares method, are presented in Table 3.

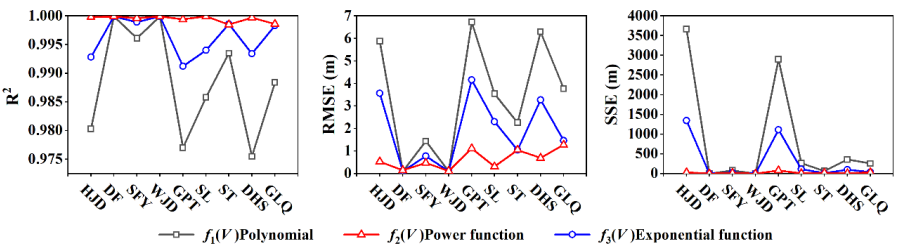


Figure. 5 Goodness-of-fit metrics for the three function types of f_1 , f_2 and f_3 to be determined.



Table 3. Power function parameters in the WLS curve before and after the reconstruction

Reservoir	β_1	β_2	β_3	β'_1	β'_2	β'_3
HJD	42.057	0.3597	975.20	30.723	0.4107	994.92
DF	71.840	0.3216	826.14	30.266	0.4925	889.29
SFY	69.479	0.3851	751.93	34.466	0.5727	798.90
WJD	67.158	0.2842	599.49	35.327	0.382	649.81
GPT	76.55	0.2643	408.33	58.417	0.3041	432.20
SL	26.977	0.4184	363.50	19.199	0.4939	374.77
ST	39.405	0.3491	284.12	28.707	0.4123	298.69
DHS	78.548	0.3285	761.95	69.373	0.3553	772.59
GLQ	109.79	0.3594	622.56	89.428	0.4318	643.96

*The parameter $\beta_i (i=1,2,3)$ represents the regression coefficients of the WLS functional relationship prior to the reconstruction, while the parameter $\beta'_i (i=1,2,3)$ demotes the coefficients of the reconstructed WLS function.

Figure 6 illustrates the reconstructed storage capacity curves against the design capacity curves currently used for three reservoirs with the most significant capacity LR. Sedimentation in the SFY and DF reservoirs is significant, with dead storage capacities decreasing considerably from 101.2 million m³ and 374.0 million m³ to 50.9 million m³ and 241.1 million m³, respectively. This reduction needs be considered in future reservoir scheduling, especially when scheduling for flood near the dead level, due to the capacity loss. In contrast, the WJD Reservoir also maintains a relatively large capacity, with its dead storage capacity decreased from 780.0 million m³ to 599.7 million m³. The storage error resulted from the biased WLS curve can be disregarded at high water levels, while careful attention is required at low water levels, especially near the dead level, as this error significantly affects normal operation.

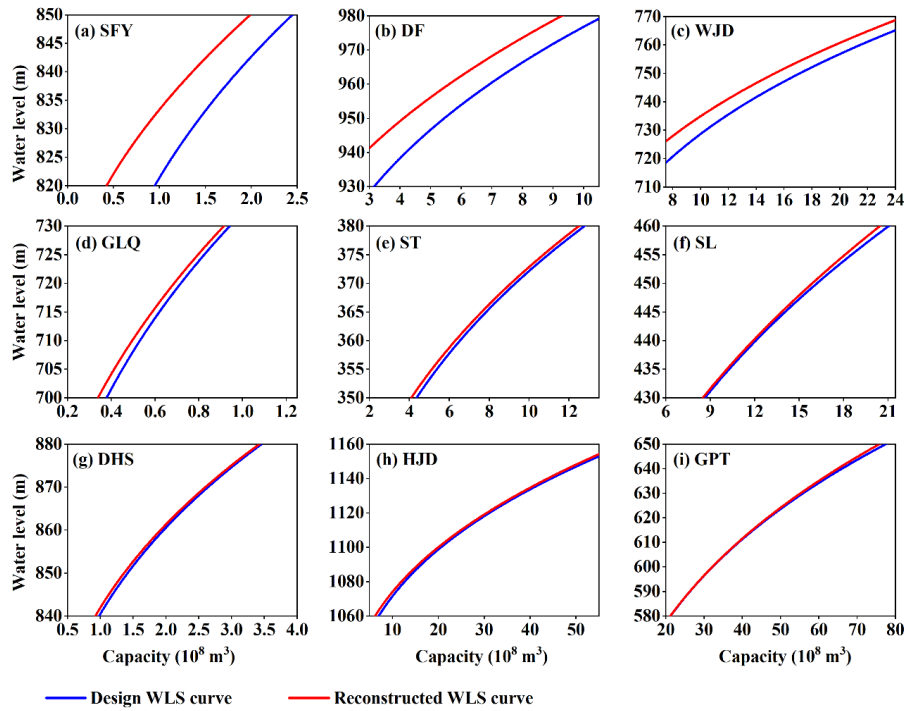


Figure 6. Reservoir capacity curves before and after reconstruction of nine reservoirs

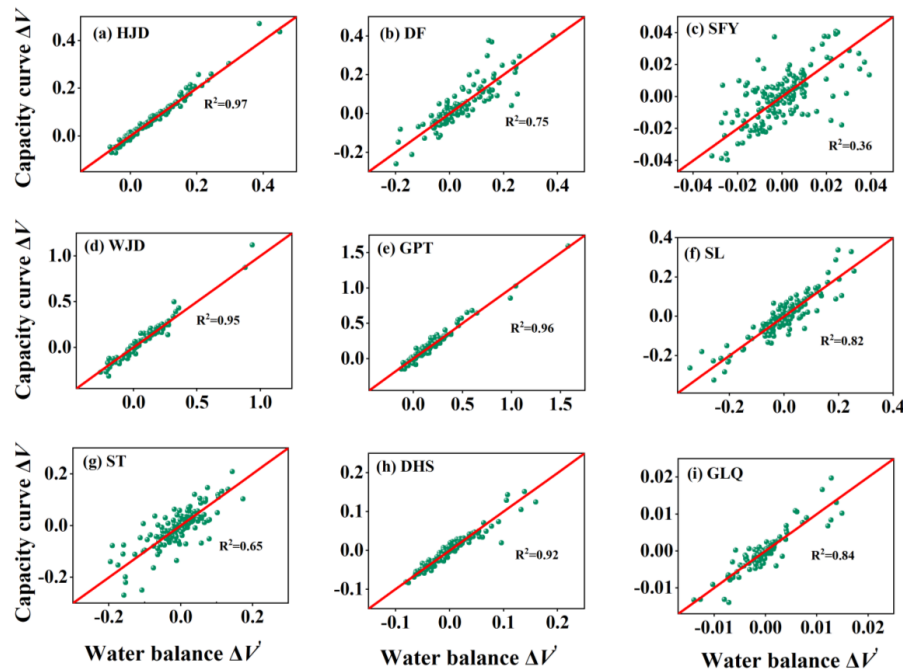
Except these three reservoirs analyzed above, the storage capacity LR of other reservoirs is all below 6%. The capacity curves before and after the reconstruction show median differences. Figure 6 illustrates that the dead capacity of the GLQ and ST reservoirs has decreased from 50.7 million m³ and 483.0 million m³ to 47.2 million m³ and 456.1 million m³, respectively. The error in the reservoir storage capacity curve is negligible during normal operations, but can become significant when the water level approaches the dead water level. In contrast, the SL, DHS, HJD, and GPT reservoirs exhibit minimal sedimentation and lower errors in their capacity curves, ensuring that normal dispatch operations remain unaffected.

4.3 Suitability analysis of the reconstructed reservoir WLS curve

Figure 7 shows the scatter plot of $\Delta V'$, which illustrates the volume change of reservoir water storage derived from the water balance method, against ΔV , which shows the volume change generated from the reconstructed capacity curve based on water level fluctuations. For most reservoirs, the scatters of $\Delta V'$ and ΔV are close to the diagonal



399 1:1 lines and show R^2 values within the range of 0.66-0.98, indicating the general
 400 suitability of the reconstructed capacity curve. The scatters of storage changes in the
 401 SFY Reservoir exhibit a disorganized distribution of data points, with a R^2 value of only
 402 0.37. This low fitting performance may be attributed to the inflow data of SFY
 403 Reservoir, which is primarily caused by abrupt changes in the measured water level at
 404 the dam and the irregular fluctuations and negative values of the inflow.



405
 406 **Figure 7.** Correlation between the storage changes generated from sediment accumulation and water
 407 balance budgets (10^8 m^3)

408 Taking the SFY and DF reservoirs, which show most considerable LR values as
 409 example, their DEM data were utilized to compute various scatter data points for water
 410 level-capacity. They were then compared with the reconstructed reservoir capacity
 411 curves presented in Section 3.2 (Fig. 8). Figure 8 illustrates that the reservoir capacity
 412 data points derived from DEM data align more closely with the reconstructed reservoir
 413 capacity curves, compared with the existing designs. However, the trends of these
 414 curves exhibit slight discrepancies from the reconstructed curves. This suggests that the
 415 methodology for assessing reservoir capacity curves proposed in this study more



accurately captures the temporal loss of total reservoir capacity. Furthermore, the calculation process is independent of measured data pertaining to reservoir area topography, rendering it both simple and efficient, although it demonstrates some limitations in spatial representativeness. Nonetheless, it lacks spatial representativeness and cannot quantify sediment siltation across the river sections.

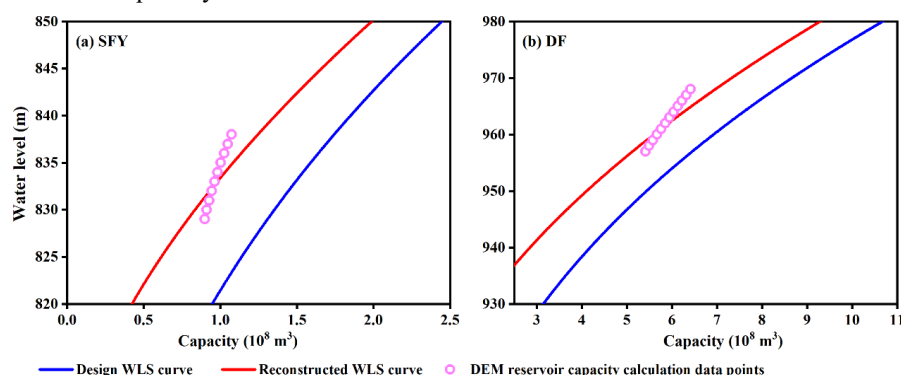


Figure 8. Comparison of reservoir capacity curves reconstructed with DEM and sediment accumulation for Suofengying (SFY) and Dongfeng (DF) reservoirs

4.4 Analysis of the response of flood regulation risk to WLS curve

The flood regulation calculation is focused on the SFY and DF reservoirs, which have the highest and second highest capacity LR. The calibrated flood levels currently used for the SFY and DF reservoirs are 842.37 m and 977.53 m, respectively. The design flood hydrograph was selected for six return intervals ranging from 200 years to 10,000 years with design frequencies of 0.01%, 0.02%, 0.05%, 0.1%, 0.2%, and 0.5% (Fig. 9). The selected design flood hydrograph is conducted with time intervals of 1 hour and durations of 170 hours. Figure 10 presents the operation risk for flood control characterized by Z^* and γ individually generated from the design and reconstructed reservoir WLS curves with radar maps. The Z^* values derived from the flood regulation calculation process of reconstructed reservoir WLS curve for both SFY and DF reservoirs exhibit a significant increase with the decreasing design flood frequencies. For the design flood hydrograph with six return intervals, the Z^* generated from reconstructed WLS curve is higher than that from the design WLS curve, and the discrepancy between these two Z^* increases from 0.20 m to 6.75 m and 0.86 m to 1.84



m for the SFY and DF reservoirs, respectively, as the return interval increases from 200 years to 1000 years. In addition, γ is greater than that quantified by the design WLS curve. For the design flood hydrograph with a return interval of 10,000 years, the γ of the SFY Reservoir increased from 22% with the design WLS curve to 23% with the reconstructed WLS curve. Similarly, the proportion of time periods exceeding the normal storage level of the DF Reservoir increased from 18% with design WLS curve to 21% with the reconstructed WLS curve.

The aforementioned results indicate that, according to the prevailing flood control and management principles, both the maximum reservoir water level and the ratio of flood regulation periods surpassing the characteristic water level derived from the existing design capacity WLS curve are lower than those generated from the reconstructed capacity WLS curve. Furthermore, the extent of underestimation escalates with the increasing magnitude of the design flood. If the storage capacity of reservoirs has been significantly reduced, continuing to use the original design capacity WLS curve will lead to an underestimation of the operation risk for flood control. This implies a potential risk of water levels surpassing the designated characteristic level during the actual operational management of the reservoirs, which putting the reservoir and dam infrastructure and downstream flood control at risk. This underscores the imperative for SFY and DF reservoirs to implement the methodology proposed in this study for the timely reconstruction and application of reconstructed capacity curves in future dispatching operations.

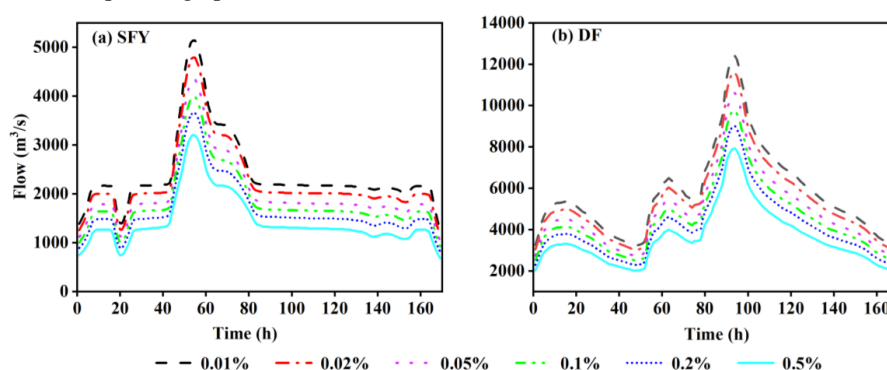
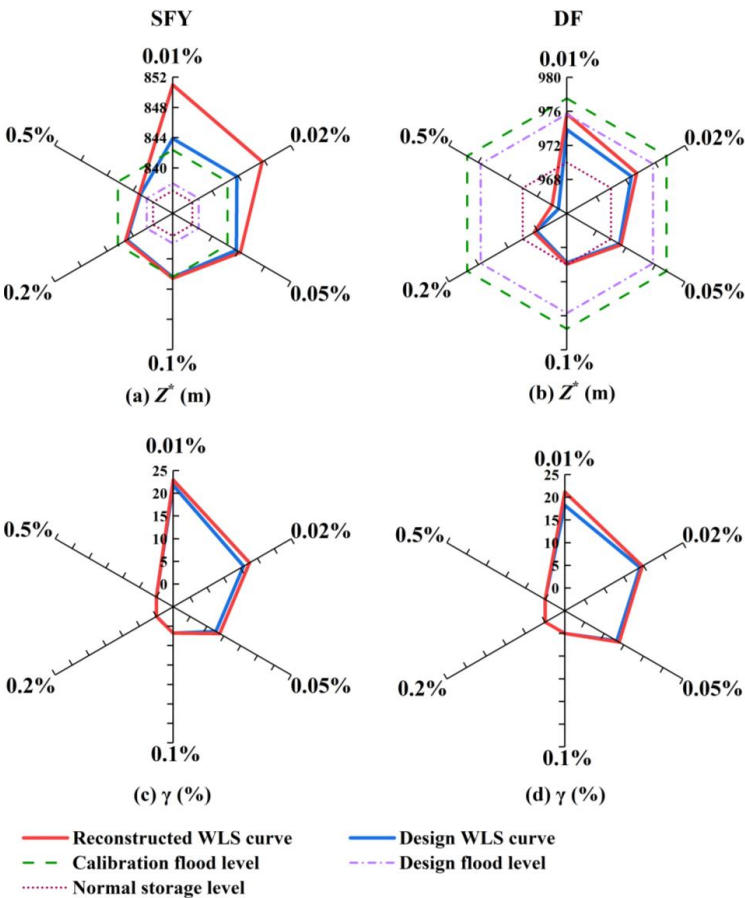


Figure 9. Design flood hydrographs for each frequency at Suofengying (SFY) and Dongfeng (DF) reservoirs



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Figure 10. Summary in risk indicators of the flood regulation calculations for Suofengying (SFY) and Dongfeng (DF) reservoirs

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5 Discussion

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5.1 Reasonableness and uncertainty in reconstructed reservoir WLS curve

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Although the WLS curve reconstructed by traditional field measurements with surveying and mapping technology is of high accuracy, the implementation of this method is often limited by the associated challenges in high cost, complex topographic conditions and long duration. Thus the in-situ WLS curve is lacking, and we cannot directly quantify the accuracy of the WLS curve reconstructed in this study. To analyze the reasonableness of the estimated WLS curve, we indirectly compare it with those



475 derived from water balance principle (Ahmad et al., 2022) and high resolution DEM
476 data (Vanthof and Kelly, 2019). The correlation analysis in Section 4.3 indicates that
477 the WLS curve generated from the water balance approach and the DEM approach is
478 much similar to the reconstructed one than the design one for each reservoir.

479 For estimation of the reservoir storage capacity, there are tradeoffs between accuracy
480 and both spatial scale of reservoirs and the suitable degree of explanatory variables
481 considered. In this study, the storage capacity derived from the WLS relationship and
482 used for a specific reservoir achieves a higher performance of the mathematic model
483 ($R^2 > 0.98$), due to the water levels used here directly being correlated with the storages.
484 In contrast, a previous study, which estimates storage capacity for multiple reservoirs
485 on a large scale with 16 influencing factors including reservoir morphological
486 parameters, underlying basin conditions, and climate types, performs significantly
487 worse (with the highest correlation coefficient < 0.97) (Yuan et al., 2024). On the other
488 hand, the XGBoost model driven by 16 explanatory factors is suitable for large scale
489 application, such as, the prediction of reservoir storage capacities on national scale in
490 that study.

491 In addition, the spatial pattern of storage capacity loss volumes and rates is
492 reasonable among different reservoirs in the cascade. Both larger capacity loss volumes
493 and rates occur for the three or four reservoirs situated at middle and upper reach of the
494 river. This is highly consistent with the conclusion of more serious sediment
495 accumulation in the upper reaches and the priority of the upper reservoir for trapping
496 sands (Brush, 1989). This fundamental pattern indirectly offers another evidence of the
497 reasonableness for the reconstructed WLS curves. In summary, our study contributes a
498 sediment accumulation-based reservoir capacity loss framework to reliably estimate
499 WSL relationships for multiple reservoir on a larger scale.

500 **5.2 Limitations of the proposed framework and further efforts**

501 Apart from sediment accumulation, other factors, such as river diversion and sand
502 mining, can result in the change of reservoir storage capacity. In this study, we consider
503 sediment accumulation as the most important one to influence the storage capacity,



504 while ignore other secondary factors. This situation is practical for the selected cascade
505 reservoir system in the Wujiang River. If the framework is to be applied to other
506 reservoirs, the applicability of this assumption should be carefully diagnosed first.
507 Furthermore, there are one potential limitation of the proposed framework, which needs
508 to be improved in further study. Therefore, the framework used to reconstruct WLS
509 relationship is available under relatively strict constraints. Specifically, we assume the
510 temporal velocity and spatial distribution of sediment accumulation are uniform using
511 the ratio of reservoir storage capacity to incoming flow (Te_i) defined in the mathematic
512 relationship of Eq. (2), to simplify the calculation of storage capacity loss rate. In fact,
513 dams and reservoirs are complex depositional systems for sediment, which vary with
514 reservoir bottom shapes, total volumes of stored water, river discharges, sediment loads
515 and sediment textures, and universal depositional models (Sedláček et al., 2022). Thus,
516 detailed sedimentation processes in reservoirs are more general and expected in the next
517 attempt. In the future, we will try to introduce physically-based hydrological models
518 coupled with reservoir models (Dong et al., 2022), deep learning algorithms (Cao et al.,
519 2020), and more public available explanatory factors including those extracted from
520 remote sensing missions (Bonnema and Hossain, 2019; Guan et al., 2021) with more
521 flexible non-linear change in sedimentation, to reduce the complexity of reconstructing
522 reservoir WLS relationship, especially on a large scale.

523 **6 Conclusions**

524 As intensified climate change and human activities exert a stronger influence on
525 hydrological process and water balance, improved representation of reservoir WLS
526 curves is valuable for developing more useful flood control adaptation measures. In this
527 study, we contribute a framework to reconstruct reservoir water level-storage (WLS)
528 curve by first constructing a reservoir capacity loss rate (LR) indicator caused by
529 sediment accumulation. Then, flood regulation calculations of reservoirs are performed
530 individually using six design flood hydrographs with six return intervals ranging from
531 200 to 10,000 years as reservoir inflow, to elucidate the response of reservoir flood



control operation to reconstructed WLS curve. Finally, the flood control risk is quantified, using the maximum flood control water level (Z^*) and the number of periods exceeding the design flood level (γ). A cascade system of nine reservoirs in the Wujiang River in China is selected to implement the established framework. The main conclusions are as follows:

(1) The results presented in this study demonstrate that the framework of reservoir storage loss volumes and rates induced by sediment accumulation can reconstruct suitable reservoir WLS relationship.

(2) The sediment accumulation in the Suofengying, Dongfeng, and Wujiangdu reservoirs, which are located in the upper reaches of the Wujiang mainstream, is more serious, resulting in significant capacity changes with the LR values over 25.02%, 12.96%, and 10%, respectively. The higher correlation between the water storage changes generated from reconstructed WLS curves in this study and those based on water balance and DEM data demonstrates the suitability of the estimated WLS curve associated with sediment accumulation.

(3) The use of the current design WLS curve for flood regulation calculations underestimates the maximal water level during flood regulation (Z^*) and the duration of regulation beyond the characteristic water level (γ). The underestimation increases with the return period of the design flood. For the Suofengying and Dongfeng reservoirs, the underestimation of Z^* increases from 0.20 m and 0.86 m for the 200-year return period to 6.75 m and 1.84 m for the 10,000-year return period. This indicates that when the storage capacity is significantly reduced, the continued use of the existing design WLS curve may significantly underestimate the flood regulation risks, thus posing potential safety hazards to reservoir itself and downstream flood protection objects.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available upon request (qiumeima@ncepu.edu.cn).



561 **Author contributions**

562 YZ, QM and ZD designed the study. QM, CX, ZD, and CYX developed the models,
563 with QM and CX implementing them. CX drafted the manuscript in close collaboration
564 with YZ, QM and CX contributed to the data curation. Throughout the study period, all
565 the authors engaged in discussions regarding the results, provided critical feedback, and
566 approved the final version of the paper.

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