



1 Vertical Mode and Cyclonic Eddy Encounters Govern Internal 2 Tide Propagation and Intermodal Cascades: High-resolution 3 Eddy Permitting Simulations

4 Fabius Kouogang^{1,2}, Ariane Koch-Larrouy¹, Xavier Carton³, Moacyr Araujo²

5 ¹CECI, Université de Toulouse, CERFACS/CNRS/IRD, Toulouse, France

6 ²Departamento de Oceanografia, Universidade Federal de Pernambuco, DOCEAN/UFPE, Recife, Brazil

7 ³Physical and Spatial Oceanography Laboratory, European Institute for Marine Studies, University of
 8 WesternBrittany, Plouzane, France

9 Correspondence to: Fabius Kouogang (fabius.cedric@yahoo.fr)

10 **Abstract.** The interaction between internal tides (ITs) and mesoscale features plays a key role in ocean energy
 11 dissipation. Understanding how IT energy is transformed in energetic western boundary regions remains a central
 12 challenge, particularly in regions of vigorous mesoscale activity.
 13 To this aim, we apply vertical mode decompositions to the flow from high-resolution (3 km) NEMO-AMAZON36
 14 simulations during September-December 2015. This study shows that the IT vertical mode and the precise point
 15 of IT-eddy encounter determine whether the IT energy propagates freely, deviates, or is trapped, and how
 16 topography and coherent eddies synergistically scatter energy between baroclinic modes off the Amazon shelf.
 17 Three representative interaction cases, each captured in a separate 25 hour snapshot, were examined: undisturbed
 18 propagation until crossing the Ceará Rise seamount, interaction with a cyclonic eddy (CE) core, and interaction
 19 with a CE eastern periphery. The principal findings establish two points.
 20 First, an IT response (propagation, deviation or scattering) is dually controlled by its vertical mode and the
 21 mesoscale encounter properties. In the absence of a strong eddy, the Mode-1 IT propagates as a coherent beam
 22 with a long propagation range (O (1100 km)). In the presence of a strong CE, however, the IT beams are disrupted,
 23 preventing sustained long-range transmission. Within the eddy core, the Mode-1 IT is coherently refracted
 24 northward ($\sim 35^\circ$ relative to its northeastward incident direction) while maintaining high energy fluxes exceeding
 25 200 W m^{-1} . At the CE periphery, Mode-1 is diffracted into two distinct branches, with one propagating northward
 26 ($\sim 39^\circ$) and the other eastward ($\sim 35^\circ$). In contrast, the IT higher modes are highly susceptible to blocking and
 27 trapping: Mode-2 energy, despite initial amplitudes comparable to Mode-1, is completely arrested at the CE-
 28 seamount interface, while Mode-3 remains weak (below 200 W m^{-1}) and less propagative.
 29 Second, intermodal energy transfer is governed by a hierarchical synergy between the seamount and CE's
 30 background flow. The seamount drives a forward energy cascade (O ($10^{-8} \text{ W m kg}^{-1}$)) from the Mode-1 IT to
 31 higher modes. In contrast, the CE's strong horizontal shear triggers a competing inverse energy cascade (O (10^{-8}
 32 W m kg^{-1})) from the background flow to the IT modes. This interaction is critical for the extreme damping of
 33 Mode-2 and explains the observed redistribution of energy fluxes.
 34 These results provide mechanistic insight into the fate of IT energy in complex oceanic environments and advance
 35 understanding of multi-scale ocean dynamics.



36 1 Introduction

37 Internal tides (ITs)—internal waves at tidal frequencies—are generated when barotropic tides interact with
 38 topography, forcing vertical displacements of the stratified water column (Garrett and Kunze, 2007; Kelly and
 39 Nash, 2010; Buijsman et al., 2012; Zhao, 2014; Chen et al., 2022). They enhance turbulent mixing and influence
 40 deep-water circulation (Wunsch and Ferrari, 2004; Kunze, 2017).

41 High-mode ITs, characterized by short wavelengths and large vertical shear, typically dissipate near their
 42 generation sites (Vic et al., 2019; Koch-Larrouy et al., 2015; Kouogang et al., 2025). In contrast, low-mode ITs
 43 propagate thousands of kilometers, redistributing tidal energy and acting on open-ocean mixing (Zhao, 2017;
 44 Alford et al., 2019; Wang et al., 2021; Kouogang et al., 2025). During their propagation, ITs can interfere with
 45 other tidal beams (e.g., tidal beams from other sources), interact with oceanic flows (e.g., subtidal currents,
 46 mesoscale eddies) and topography (e.g., seamounts, ridges), generating nonlinear internal solitary waves (ISWs)
 47 (Pereira et al., 2007; Zhang et al., 2014; Kelly and Lermusiaux, 2016; Wang et al., 2021; Xu et al., 2021; Wang
 48 et al., 2024; Li et al., 2024). Low-mode ITs can be scattered into higher modes by bathymetric roughness (Johnston
 49 and Merryfield, 2003; Mathur et al., 2014). These multiscale interactions cause IT incoherence and
 50 nonstationarity, challenging satellite detection (Zaron and Egbert, 2014; Savage et al., 2020).

51 Mesoscale eddies (MEs)—comprising both anticyclonic (AEs) and cyclonic (CEs) types—often possess
 52 horizontal scales comparable to those of low-mode ITs. This scale similarity allows MEs to alter oceanic
 53 stratification and currents, thereby influencing IT generation, propagation, and inter-modal energy redistribution
 54 through processes such as scattering, refraction, trapping, and damping (Dunphy and Lamb, 2014; Clément et al.,
 55 2016; Dunphy et al., 2017; Guo et al., 2023; Wang and Legg, 2023). MEs can enhance or weaken the topography
 56 scattering of ITs, causing spatial divergence (Li et al., 2024). Low-mode ITs can also be refracted or trapped by
 57 background currents like the looping and leaping Gulf Stream (Duda et al., 2018; Kelly and Lermusiaux, 2016;
 58 Kelly et al., 2016), Kuroshio (Cao et al., 2022; Xu et al., 2021; Chen et al., 2022) and Brazil Current (Pereira et
 59 al., 2007), changing their direction of propagation (Huang et al., 2018). Scattering by topography and background
 60 circulation to higher modes can redistribute energy toward more dissipative pathways (Lahaye et al., 2020; Fan
 61 et al., 2024).

62 Although the IT responses to background circulation (stratification, currents, and eddies) are well-documented on
 63 seasonal and interannual timescales (Pereira et al., 2007; Nash et al., 2012; Tchilibou et al., 2020, 2022), their
 64 variability at shorter, daily timescales remains less explored. Our study addresses this gap by investigating the
 65 rapid variability of IT responses to MEs off the Amazon shelf.

66 The region off the Amazon shelf is a dynamic region with a strong western boundary current (North Brazil
 67 Current, NBC), receiving large amounts of freshwater from the Amazon and Para Rivers. The area is also marked
 68 by high mesoscale activity (MEs), and the presence of seamounts, ITs, and ISWs (Fig. 1). The NBC flows
 69 northwestward, exhibiting a seasonal double retroflexion eastward, a first one into the North Equatorial Counter-
 70 Current (NECC) at about 5–8° N near 50° W, and a second one into the Equatorial Undercurrent (EUC) in winter-
 71 spring (Didden and Schott, 1993). Shear instabilities within these currents and their interaction with the Amazon
 72 slope generate the CEs and AEs (NBC rings) in this region (Fratantoni and Glickson, 2002; Barnier et al., 2001;
 73 Silva et al., 2009). From August to December (ASOND), mean currents and eddy kinetic energy (EKE) are
 74 stronger, and the pycnocline is deeper and weaker than during the March-to-July (MAMJJ) season (Aguedjou et
 75 al., 2019; Barbot et al., 2021; Tchilibou et al., 2022). Generated at multiple sites (A to E, Fig. 1) along the Amazon



76 shelf break (Tchilibou et al., 2022; Assene et al., 2024; Magalhaes et al. 2016), ITs from the most energetic sites
 77 (A and D, Fig. 1) can either propagate over long distances or interact with other processes to potentially
 78 disintegrate into ISWs, which have been observed via in situ measurements (Brandt et al., 2002), SAR imagery
 79 (Magalhães et al., 2016), MODIS (De Macedo et al., 2023), and SWOT data (Goret et al., 2025). This makes the
 80 region an ideal laboratory for studying the tidal variability of IT responses during the propagation of tidal flux.
 81 Using numerical modeling, Tchilibou et al. (2022) reported that the M2 coherent baroclinic tidal flux propagates
 82 more northward during MAMJJ in the region off the Amazon shelf. During ASOND, however, it becomes
 83 incoherent—branching and deviating near 6°N—due to strong interactions with MEs and background currents off
 84 the Amazon shelf. This variability in flux behavior (e.g., free propagation, refraction, branching) during ASOND
 85 may result from the interaction of the coherent flux with MEs, sheared currents (e.g., NECC), changes in
 86 stratification, topography (e.g., Ceará Rise seamount, Mid-Atlantic ridge; Fig. 1), other internal wave sources, or
 87 coupled processes.
 88 Motivated by the complex mesoscale interplay off the Amazon shelf, we investigate the fate of IT within this
 89 dynamic environment at daily timescales from the realistic model outputs. Specifically, we examine whether ITs
 90 propagate freely, are deviated, or become trapped by mesoscale features. We further determine whether these
 91 outcomes depend on the vertical modes of ITs or the properties of the MEs, distinguishing, for instance, between
 92 interactions at a CE core versus its periphery. Finally, we explore the synergistic roles of topography (e.g., Ceará
 93 Rise seamount) and CEs in governing modal energy transfers.

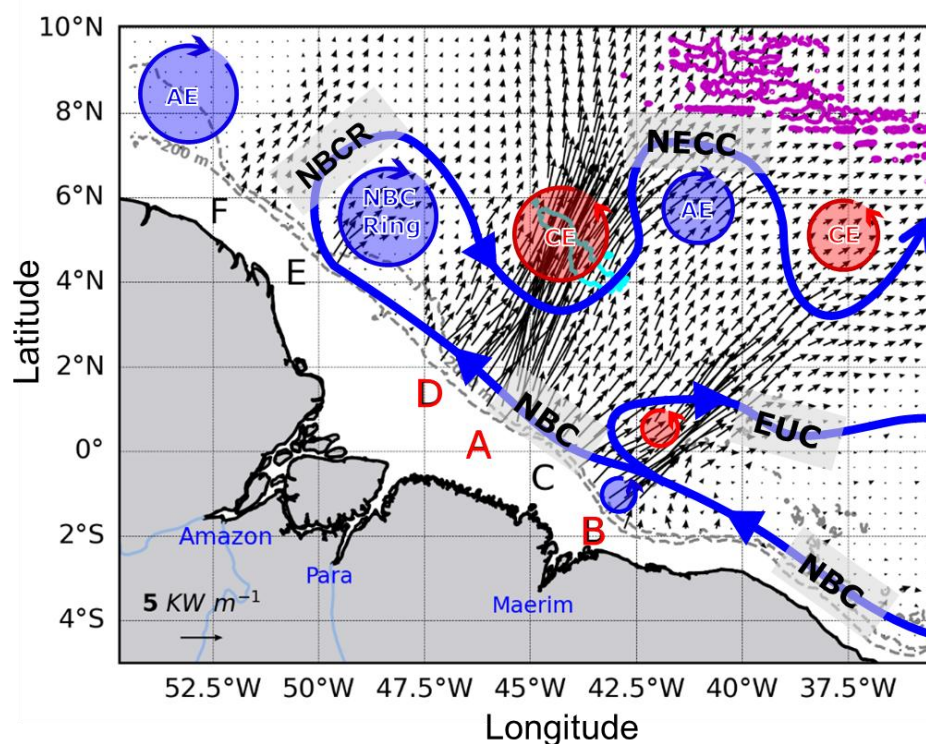




Figure 1. Internal tide generation and propagation, and regional circulation off the Amazon shelf. Key IT generation sites (A–F) are marked along the shelf break slope, with the three primary sites (A, B, D) highlighted in red. The associated M_2 baroclinic energy flux, represented by black arrows, is the 25-hour mean depth-integrated flux from the September–December (SOND) 2015 period. The schematic background circulation includes the North Brazil Current (NBC), its retroflection (NBCR), North Equatorial Countercurrent (NECC), and Equatorial Undercurrent (EUC) (solid blue lines). Mesoscale eddies are indicated by cyclonic (CEs, red circles) and anticyclonic eddies (AEs, blue circles), the latter including the NBC Ring. Topography is detailed with the 200 m and 2000 m isobaths (grey lines) and specific features outlined by their 3500 m isobath (Ceará Rise seamount: cyan contour; Mid-Atlantic ridge: magenta contour).

2 Methodology

2.1 High-resolution Numerical Modeling

We use output from the Nucleus for European Modeling of the Ocean (NEMO) model, specifically the AMAZON36 configuration (Madec et al., 2019). This high-resolution ($1/36^\circ$, ~ 3 km) model is designed for the western tropical Atlantic (54.7° W– 35.3° W, 5.5° S– 10° N) and features 75 vertical layers, with 23 levels in the upper 100 m to resolve near-surface processes. This configuration capably resolves low-mode ITs and accurately represents the topography critical to their generation and propagation from the Amazon shelf break (Tchilibou et al., 2022; Assene et al., 2024).

The model employs a third-order upstream biased scheme for momentum advection and a second-order flux-corrected transport scheme for tracers (Zalesak, 1979). Subgrid-scale parameterizations include Laplacian isopycnal tracer diffusion ($20 \text{ m}^2 \text{ s}^{-1}$) and a k - ϵ turbulent closure scheme for vertical mixing. Lateral boundaries are free-slip and bottom friction is quadratic (drag coefficient: 2.5×10^{-3}). Temporal integration uses a leapfrog scheme with an Asselin filter and a baroclinic time step of 150 s, while a time-splitting technique handles the free surface.

The model bathymetry was extracted from GEBCO (General Bathymetric Chart of the Ocean) 2020 data, surface conditions from the ERA5 reanalysis (Hersbach et al., 2020), and river runoff from the ISBA (Interaction Sol-Biosphère-Atmosphère) model: <https://www.umr-cnrm.fr/spip.php?article146&lang=en>, last access: 20 September 2024). Open boundary conditions are provided by the FES2014 tidal atlas (15 constituents: M_2 , S_2 , N_2 , K_2 , $2N_2$, MU_2 , NU_2 , L_2 , T_2 , K_1 , O_1 , Q_1 , P_1 , S_1 , and M_4 ; Lyard et al., 2021) and hydrographic/velocity data from the MERCATOR-GLORYS12v1 reanalysis (Lellouche et al., 2018).

The simulation runned for 11 years until December 2015 and provides three-dimensional, hourly AMAZON36 output. This dataset has previously been used to study IT interactions with background circulation and stratification (Barbot et al., 2021; Tchilibou et al., 2022; Assene et al., 2024; Kouogang et al., 2025).

For this study, we focus on the period from September to December (SOND) 2015, when stronger mean currents and EKE contribute to more incoherent ITs (Tchilibou et al., 2022). To analyze the rapid variability of IT responses to MEs like CEs, we examine 25-hour segments within this season.

2.2 Internal Tides and Mesoscale Activity

Our analysis for each 25-hour window of AMAZON36 outputs during the SOND period involves several steps: extracting the M_2 IT constituent, separating the barotropic and baroclinic components, projecting the baroclinic



components onto vertical modes, extracting MEs and characterizing their properties, and examining the mean background current pattern and topographic features.

136

2.2.1 Undecomposed IT Energy equations

First, to examine the variability of IT responses to MEs, we explore all 25-hour snapshots of IT energy flux from the AMAZON36 output during the SOND period. Following the method of Kelly et al. (2010), barotropic and baroclinic tidal constituents were separated. This separation is performed directly by the NEMO model to ensure accuracy, providing the total energy for all resolved propagation modes at a given tidal frequency (Tchilibou et al., 2022). Our analysis focuses solely on the M2 harmonic, the dominant tidal constituent in this region (Fassoni-Andrade et al., 2023).

The energy budget for IT can be expressed from the following equations (Wang et al., 2016; Buijsman et al., 2012; Kerry et al., 2013; Tchilibou et al., 2022; Siyanbola et al. 2024):

146

$$\nabla_h \cdot \mathbf{F} + D + R = C \quad (1)$$

148

In contrast to energy budgets decomposed into vertical modes, we refer to these as the undecomposed IT energy equations. Here, $\nabla_h \cdot \mathbf{F}$ is the divergence of the depth-integrated energy flux, $\mathbf{F} = (F_x, F_y)$ the energy flux vector, C , represents the depth-integrated barotropic-to-baroclinic energy conversion, and D is the depth-integrated energy dissipation term. The term R includes the energy tendency term, implicit horizontal dissipation, wave-mean flow and wave-wave interaction terms, and other offline computation errors. $\nabla_h = (\partial/\partial x, \partial/\partial y)$ is the horizontal gradient operator.

In the following, a particular attention is given to depth-integrated and time-averaged energy flux term \mathbf{F} , which was defined as (Tchilibou et al., 2022; Assene et al. 2024):

157

$$[\mathbf{F}_{bc}, \mathbf{F}_{bt}] = \left[\int_{-H}^{\eta} \mathbf{u}_{bc} p_{bc} dz, \mathbf{u}_{bt} p_{bt} \right], \quad (2)$$

159

where $\mathbf{u} = (u, v)$ is the horizontal baroclinic tidal velocity vector, and p_{bt} the barotropic tidal pressure. Here, the subscripts bt and bc denote barotropic and baroclinic components, respectively. η is the sea surface height.

162

2.2.2 Projection of IT Motions Onto Vertical Modes

Second, to investigate whether the IT responses to MEs is mode-dependent and to examine potential inter-modal energy transfer, we project the M₂ tidal constituent onto a set of vertical modes for selected 25-hour snapshots that capture ME-induced IT responses. This selective approach substantially reduces the computational cost associated with processing high-resolution 3D data for all 25-hour windows during the SOND period.

168

Vertical Mode Decomposition

For each selected snapshot, we first extract the M2 harmonic via harmonic analysis. We then decompose the tidal currents and pressure using a locally computed set of vertical modes. This method provides a more accurate separation of barotropic and baroclinic tides than simpler approaches (Kelly, 2016; Lahaye et al., 2020; Lahaye et al., 2024; Siyanbola et al. 2024). The vertical modes are obtained by solving the standard Sturm-Liouville



174 eigenvalue problem at each horizontal grid point, assuming a flat bottom, a free surface, horizontally
 175 homogeneous stratification (based on the time-mean buoyancy frequency, $\overline{N^2}$), and no background flow (Gerkema
 176 and Zimmerman, 2008; Bella et al., 2024):

177

$$178 \quad \partial_z \left(\frac{\partial_z \Phi_n}{N^2} \right) + \frac{\Phi_n}{c_n^2} = 0, \quad (3)$$

179

180 with the boundary conditions:

$$181 \quad \partial_z \Phi_n = 0 \text{ at } z = -H, \text{ and } g \partial_z \Phi_n + \overline{N^2} \Phi_n = 0 \text{ at } z = \bar{\eta}, \quad (4)$$

182

183 where ∂_z denotes the partial derivative in z-direction, Φ_n is the horizontal velocity/pressure eigenfunction for
 184 mode n, c_n is the modal phase speed, H is the seafloor depth, and g is gravity. The associated vertical
 185 velocity/buoyancy eigenfunction, φ_n , is given by:

186

$$187 \quad \partial_z \varphi_n = \Phi_n, \text{ and } \partial_z \Phi_n = -\frac{\overline{N^2}}{c_n^2} \varphi_n. \quad (5)$$

188

189 The vertical modes satisfy the orthogonality condition (Kelly, 2016; Lahaye et al., 2024; Bella et al., 2024):

190

$$191 \quad \int_{-H}^{\bar{\eta}} \Phi_m \Phi_n \, dz = H \delta_{mn} \quad (6)$$

192

193 where δ_{mn} is the Kronecker delta and $\bar{\eta}$ is the time-averaged sea surface height.

194 We solved Equation 3 for the first 10 modes ($n = 0, 1, \dots, 9$) at each grid point, where $n = 0$ represents the barotropic
 195 mode. In this study, the analysis of energy flux focuses primarily on the first three baroclinic modes, which are
 196 the most dynamically significant at the model's resolution (~ 3 km).

197 The horizontal velocity \mathbf{u} and pressure p fields are projected onto these modes to obtain the depth-independent
 198 modal amplitudes:

199

$$200 \quad [u_n(\mathbf{x}, t), p_n(\mathbf{x}, t)] = \frac{1}{H} \int_{-H}^{\bar{\eta}} [\mathbf{u}(\mathbf{x}, z, t), p(\mathbf{x}, z, t)] \Phi_n(\mathbf{x}, z) \, dz, \quad (7)$$

201

202 with $\mathbf{x} = (x, y)$ denoting the horizontal direction.

203 The full 3D structure of \mathbf{u}_n fields for each mode can be reconstructed as (Li et al., 2024):

204

$$205 \quad \mathbf{u}_n(\mathbf{x}, z, t) = \mathbf{u}_n(\mathbf{x}, t) \Phi_n(\mathbf{x}, z) \quad (8)$$

206

207 Modal Energy Budget

208 To analyze the inter-modal energy transfer/scattering and redistribution, we examine the terms of the modal
 209 energy budget of a given mode interacting with physical features such as topography and mesoscale flow (Fan et
 210 al., 2024; Bella et al., 2024; Kelly, 2016; Kelly and Lermusiaux, 2016):



$$\nabla_h \cdot \mathbf{F}_m + D_m + \Psi_m = \sum_n (C_{mn} + A_{mn} + H_{mn} + V_{mn} + B_{mn}). \quad (9)$$

Here:

- C_{mn} is the nonlinear scattering (from mode $m > 0$ into mode n) of energy by topography and stratification.
- A_{mn} represents the advection of the ITs by the background flow and MEs.
- H_{mn} and V_{mn} represent the effect of the horizontal and vertical shear of the background flow, respectively.
- $\mathbf{F}_m = H p_m \mathbf{u}_m$ is the depth-integrated and time-averaged baroclinic energy flux for mode n .
- B_{mn} consist of the three-way interaction term and the horizontal gradient of the buoyancy field.
- Ψ_m consists of the energy tendency terms.
- D_m is the dissipation term of modal energy budget, which also includes interactions with unresolved modes, other physical dissipation processes leading to local dissipation (Alford & Zhao, 2007), and other offline computation errors.

A previous seasonal-scale study by Bella et al. (2024) found the nonlinear coupling terms C_{mn} , A_{mn} , H_{mn} , and V_{mn} to be dominant across the North Atlantic basin. For our investigation on a daily timescale, a preliminary analysis identified C_{mn} and H_{mn} as the dominant terms in our study region. We therefore focus on estimating these dominant couplings terms as defined by Bella et al. (2024):

$$C_{mn} = \langle H p_m \mathbf{u}_n \cdot \mathbf{T}_{nm} - H p_n \mathbf{T}_{mn} \cdot \mathbf{u}_m \rangle, \quad (10)$$

228

$$H_{mn} = \langle -H (U_{mn}^v \mathbf{u}_n) \cdot \mathbf{u}_m \rangle, \quad (11)$$

$$\text{with } T^{mn} = \frac{1}{H} \int_{-H}^{\bar{\eta}} \Phi_m \nabla_h (\Phi_n) dz, \quad (U_{mn}^v)_{ij} = \frac{1}{H} \int_{-H}^{\bar{\eta}} \Phi_m \Phi_n \frac{\partial \bar{u}_{h,i}}{\partial x_j} dz.$$

231

Here, the angle bracket $\langle \cdot \rangle$ denotes the average over a M2 tidal period, $\bar{\mathbf{u}}_h = (\bar{\mathbf{U}}, \bar{\mathbf{V}})$ is the time-averaged total horizontal velocity vector. $\frac{\partial \bar{u}_{h,i}}{\partial x_j}$ is the tensor.

The modal horizontal kinetic energy (HKE_n) of M2 IT is estimated as (Kelly et al., 2012; Fan et al., 2024):

235

$$HKE_n = \frac{\rho_0 H}{2} \langle u_n^2 + v_n^2 \rangle, \quad (12)$$

where ρ_0 is the reference density.

238

Symmetric–Antisymmetric Separation of Nonlinear Coupling Terms

The energy transfer matrices—including topographic scattering (C_{mn}) and (H_{mn})—are decomposed into symmetric and antisymmetric components, following the established methodology (Savage et al., 2020; Bella et al., 2024). For any general transfer matrix (X_{mn}), the standard mathematical definitions are: the antisymmetric component, $X_{mn}^A = \frac{1}{2} (X_{mn} - X_{nm})$, and the symmetric component, $X_{mn}^S = \frac{1}{2} (X_{mn} + X_{nm})$.

The antisymmetric component, X_{mn}^A , represents the internal reallocation of energy—specifically, the scattering or transfer of energy among the various IT vertical modes. Critically, this process conserves the total energy of the IT field, as it analytically redistributes energy across the system modes and spatial scales without introducing



a net gain or loss. For instance, the term C_{mn} is inherently antisymmetric and thus provides a canonical reference for conservative internal energy transfer. Conversely, the symmetric component, X_{mn}^S , describes the net energy exchange between the IT and the low-frequency background flow. When integrated in a basin, this component acts as a source or sink for the IT system, quantifying the total energy gained from or lost to the slowly varying circulation (Bella et al., 2024). The direction of energy transfer is interpreted from the sign of the matrix elements. Considering a specific mode m :

- For the full matrix X_{mn} , a negative value indicates a net forward transfer of energy from mode m to mode n , while a positive value indicates a net backward transfer from mode n to mode m .
- For the antisymmetric component X_{mn}^A , a negative value signifies a forward transfer from mode m to mode n of the IT field, and a positive value signifies a backward transfer.
- For the symmetric component X_{mn}^S , a negative value indicates a forward transfer from mode- m IT to the mode- n background flow, whereas a positive value indicates energy is transferred from the mode- n background flow to mode- m IT.

2.2.3 Eddy detection and structure

Third, to investigate whether the IT responses to MEs depend on eddy properties and location, we detected and characterized eddies from 25-hour mean snapshots of AMAZON36 output during the SOND period. The mesoscale activity in this region during the 2015 ASOND period was previously assessed by Tchilibou et al. (2022). Their analysis, which compared the model's surface EKE with satellite data, showed reasonable agreement in both the spatial pattern and amplitude of the mean EKE, especially in regions dominated by the NECC. Eddies were identified in our model outputs using the Okubo-Weiss parameter (W), chosen for its ability to detect coherent vortices on specific isopycnal surfaces or depths (Okubo, 1970; Weiss, 1991; 1991; Kurian et al., 2011; Xu et al. 2019). The W parameter is defined as:

$$W = S_n^2 + S_s^2 + \zeta^2, \quad (13)$$

where the normal strain (S_n) and shear strain (S_s), and the relative vorticity (ζ) are:

$$S_n = \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y}, \quad S_s = \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y}, \quad \zeta = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}. \quad (14)$$

Regions where rotation dominates strain ($W < 0$) indicate potential eddy cores.

The detection of eddies on selected isopycnal surfaces (between 23 and 27 kg m^{-3} isopycnals) following the procedure of Kurian et al. (2011) and Xu et al. (2019). First, the W fields were smoothed using a 50 km \times 50 km half-power filter to suppress small-scale noise. For each 25-hour mean snapshot, we then applied a constant threshold of $W_0 = -3 \times 10^{-11} \text{ s}^{-2}$ to isolate vorticity-dominated regions ($W < W_0$). Closed contours corresponding to $W = W_0$ were identified, and each contour was subjected to a series of quality control criteria to be classified as an eddy: a shape error (deviation from a fitted circle) of less than 50%, a mean azimuthal velocity greater than 5 cm s^{-1} , and a radius larger than 50 km.



For each identified eddy, its thickness was defined as the vertical extent of its W_0 contours, and its center location was defined as the centroid of the closed W_0 contour. Detected eddies were classified as cyclonic or anticyclonic based on the sign (positive for CEs and negative for AEs) of their potential vorticity anomaly (PVA; Fig. 2a).

To analyze the eddy dynamical structure, we used the framework of rescaled potential vorticity (PV_r). This method filters out high-frequency wave noise to isolate the balanced mesoscale signal. The PV_r is derived from the classical Ertel (1942) potential vorticity, rescaled by a reference stratification at rest, $\rho^*(z)$, following the approach of Morel et al. (2023, 2019) and subsequent studies (e.g., Delpech et al., 2020; Aguedjou et al., 2021; Ernst et al., 2023).

Its expression is:

$$PV_r = -(\nabla \cdot \mathbf{U} + f) \cdot \nabla Z(\rho) = \nabla \cdot [(\nabla \cdot \mathbf{U} + f) \nabla Z(\rho)], \quad (15)$$

where \mathbf{Z} is a rescaling function defined by $\mathbf{Z}(\rho^*) = z$. ρ^* is defined by the adiabatically rearranged state of minimum potential energy, following the concept of Lorenz (1955) as formalized by Nakamura (1995) and Winters and D'Asaro (1996). ρ is the potential density and f , the local Coriolis parameter. An eddy dynamical core is then identified by its anomaly from the background planetary vorticity, $PVA = PV_r - f$, within a layer bounded by two isopycnals.

To distinguish subsurface eddies from surface-intensified ones, we classified them based on the isopycnal level of their core of PVA. Following the method of Kouogang et al. (2025), we used the base of the pycnocline (defined by $\sim 26.5 \text{ kg m}^{-3}$ isopycnal) as the boundary of the lower pycnocline depth. Eddies with their PVA core on isopycnals less dense than 26 kg m^{-3} were classified as surface-intensified eddies (Fig. 2b), while those with their core on denser isopycnals ($> 26.5 \text{ kg m}^{-3}$) were classified as subsurface-intensified eddies as formalized by Aguedjou et al. (2021) in the tropical Atlantic Ocean. This classification scheme was applied to all eddies detected during the SOND period. This study focuses specifically on these surface-intensified eddies.

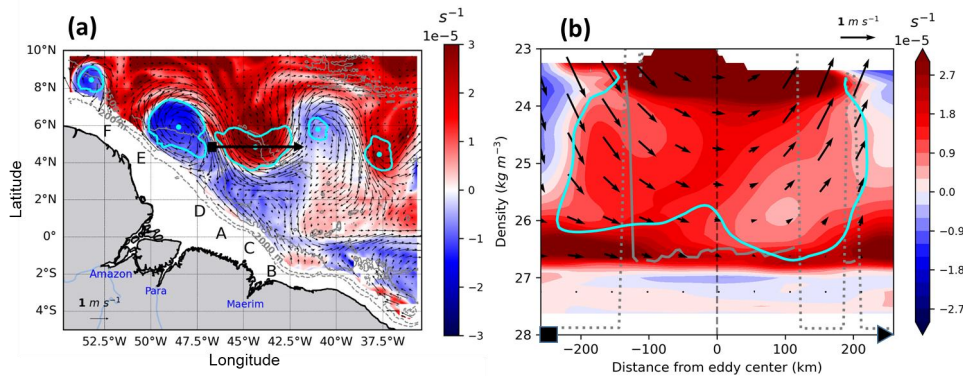


Figure 2. Detection and vertical structure of a representative ME (17 September 2015). (a) PVA (color shading) averaged within the $23\text{--}25.5 \text{ kg m}^{-3}$ isopycnal layer ($\sim 50\text{--}160 \text{ m}$ depth). Panel (a) shows detected eddy edges (cyan contours) and mean background currents (black arrows) along the 24 kg m^{-3} isopycnal. (b) Vertical cross-section of PVA along the transect in (a) (black arrow), passing through the core of a CE. The transect endpoints



are marked by a square (start) and triangle (end). The vertical dashed black line indicates the eddy centroid, black arrows show the CE-associated currents, and grey lines mark the upper (dotted) and lower (solid) thermocline limits. PVA and mean background currents fields were smoothed using a $50 \text{ km} \times 50 \text{ km}$ half-power filter to suppress small-scale noise.

3 Results

In order to examine the variability of IT responses to MEs, particularly to CEs, we first present three representative cases of interactions between the (non-modal) baroclinic energy flux of the M_2 IT and the detected eddy fields, identified from all 25-hour mean snapshots during SOND 2015. We then analyze the IT's vertical mode responses, focusing on the encounter location of the fluxes — originating from the most energetic generation sites A and D — with a CE along their path, and examine the potential modal energy transfer and redistribution.

3.1 Variability of IT responses to MEs: three distinct cases

Following the method described in Sects. 2.2.1 and 2.2.3 (Eqs. (1)-(2) and (13)-(15)), we identified three distinct cases from the SOND 2015 period for analysis, each occurring near a spring tide maximum to ensure comparably high and consistent tidal energy levels (Fig. 3). This setup minimizes the influence of tidal variability, allowing us to isolate the eddy-induced effects.

Figure 4 illustrates in the three relevant cases, the M_2 baroclinic energy flux, and MEs detected and their polarity given by the sign of PVA.

The selected cases are:

- No-Eddy case (NE, 24 November 2015): Energy flux from the primary generation sites (A and D) propagated freely, crossing the Ceará Rise seamount ($\sim 500 \text{ km}$ from sites A and D; between 4°N – 6°N , 45°W – 42.5°W) and reaching the Mid-Atlantic ridge ($\sim 1100 \text{ km}$ from sites A and D). A similar pattern was observed from site B (Fig. 4a).
- Cyclone Eddy Center case (CEC, 17 September 2015): Energy flux from sites A and D was refracted into a single beam at the core of a CE positioned (4.9°N , 44.4°W) above the seamount. Note that the seamount has an amplitude (h_{max}) of $\sim 1000 \text{ m}$ and width (w_{max}) of $\sim 100 \text{ km}$. Separately, flux from the less energetic site E was also refracted into a single beam, emanating from the center of a nearby AE (centered at 5.9°N , 48.5°W) (Fig. 4b).
- Cyclone Eddy Edge case (CEE, 29 September 2015): Energy flux from sites A and D was diffracted into multiple beams at the eastern periphery of a CE located (5.3°N , 45.0°W) on the northern flank of the seamount (Fig. 4c).

To determine whether these response patterns depend on the IT's vertical structure or eddy properties and location, we focus on the IT response to CEs and project the energy flux into vertical modes (Sect. 2.2.2). This approach enables us to examine the specific response of each vertical mode to the CE and potential modal energy redistribution and transfer resulting from these interactions.

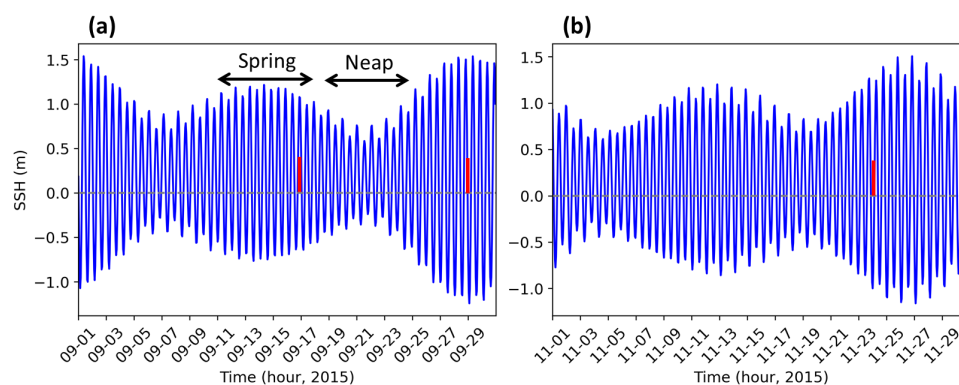


Figure 3. Sea surface height (SSH) from AMAZON36 simulations (station location: 1.29° N, 46.34° W) in (a) September and (b) November 2015. Red bars denote the three case study dates, and black arrows mark the spring-neap tidal cycle.

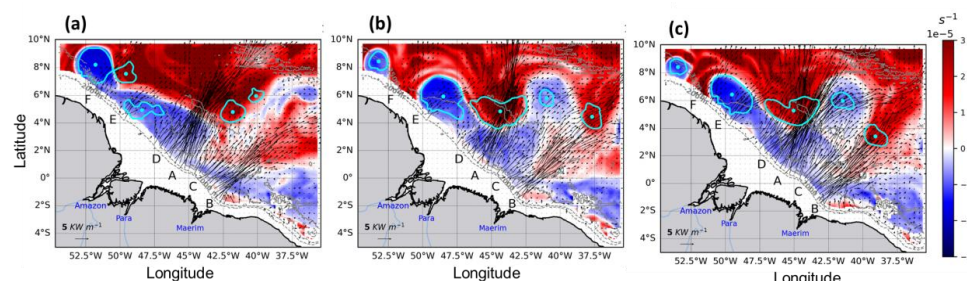


Figure 4. Depth-integrated M2 total baroclinic energy flux (black arrows) and isopycnally-averaged PVA (color shading), for the (a) NE, (b) CEC, and (c) CEE cases. All fields are 25-hour mean snapshots. The PVA is averaged within the 23–25.5 kg m⁻³ density layer (approximately 50–160 m). Detected eddies along the 24 kg m⁻³ isopycnal are overlaid, with edges (cyan contours) and centroids (cyan dots). The respective dates are 24 November 2015 (a), 17 September 2015 (b), and 29 September 2015 (c).

3.2 IT Responses to CEs

Following the method described in Sect. 2.2.2 (Eqs. (3)-(12)), we separately analyze the first three vertical modes of the M2 IT in the three cases.

3.2.1 NE Case: IT without Eddy

We first analyse the tidal energy diagnostics for the NE case to establish an eddy-free propagation baseline. Figures 5a-c maps the energy flux propagation and HKE for the first three modes, revealing distinct patterns for each.

Mode-1 energy propagation is highly dominant. The flux, generated constructively from sites A and D, forms a notably coherent beam that propagates northeastward (~37° azimuth) for over 1100 km with minimal deviation



(Fig. 5a). This long-distance propagation maintains a relatively constant HKE of 150–200 J m⁻², with a wavelength (λ_1) estimated between 90–125 km. In contrast, the Mode-2 flux propagates a significantly shorter distance (500–600 km, λ_2 : 60–85 km) and terminates abruptly at the seamount (Fig. 5b). Mode-3 forms no coherent beams but appears as scattered patches extending only 50–100 km (λ_3 : 35–50 km; Fig. 5c). Along their respective beams, Mode-1 and Mode-2 exhibit stronger energy flux amplitudes (>200 W m⁻¹) compared to Mode-3 (<200 W m⁻¹). The spatial distribution of these modal energy fluxes is consistent with the vertical structure of the corresponding baroclinic velocity profiles (Appendix A, Figs. A1–A2). A sharp Mode-2 damping is clearly visible over the seamount, while Mode-3 energy appears trapped over the seamount and ridge where the Mode-1 flux diminishes, suggesting that topographic features drive scattering to higher vertical modes.

To quantitatively assess the mechanisms responsible for this energy loss, we compute intermodal energy transfer terms (Eqs. (9)–(11)) and map only the dominant terms in Figures 5d–o. These dominant terms, of order of magnitude comparable ($O(10^{-8}$ W m kg⁻¹)), are topographic scattering term (C_{mn} , Eq. (10)), and the horizontal shear term (H_{mn} , Eq. (11)) of background flow. They then are separated into its antisymmetric and symmetric part for the analysis. All other background flow-induced energy transfer terms, such as advection and vertical shear, are negligible in comparison ($O(10^{-10}$ W m kg⁻¹); figures not shown).

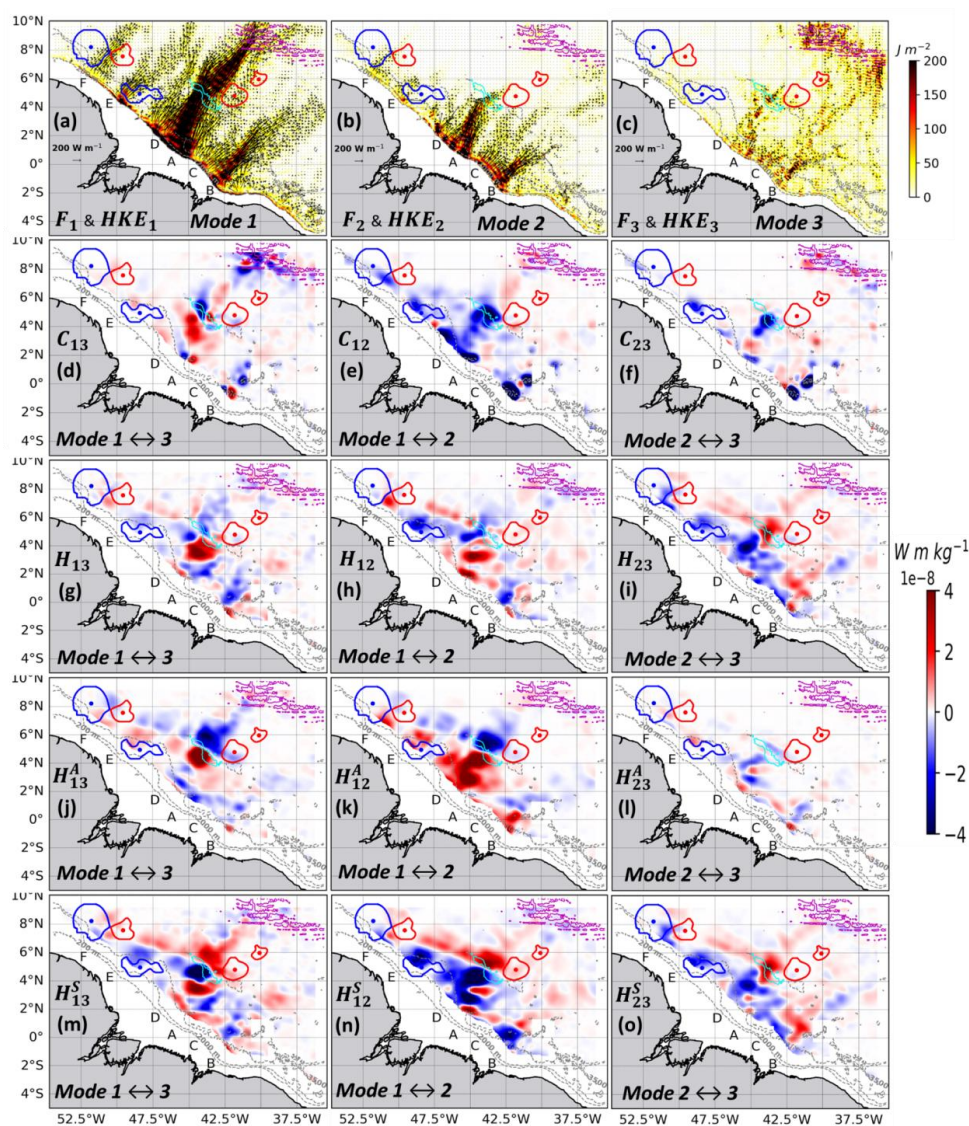
The analysis reveals a primary pathway of intermodal energy transfer driven by topographic scattering term (C_{mn}), which is antisymmetric by construction. Along the IT path from generation sites A and D, a dominant forward energy cascade occurs near major bathymetric features—the shelf break and seamount—with a magnitude of $|C_{mn}| \sim 4 \times 10^{-8}$ W m kg⁻¹. Specifically, energy is sequentially transferred from Mode-1 to Mode-2 IT (Fig. 5e, blue patches), and then from Mode-2 to Mode-3 IT (Figs. 5f, blue patches). In contrast, energy transfer is significantly weaker in the region downstream of the seamount (Fig. 5f, near-zero values). This area exhibits strong horizontal gradients in stratification (Appendix A, Fig. A2), suggesting that in the term C_{mn} , background stratification is not a primary mechanism for inter-modal energy transfer in this region.

Furthermore, direct energy transfer occurs between Mode-1 and Mode-3 IT over the ridge (Figs. 5d, blue patches), where Mode-1 loses energy towards Mode-3 IT. Between the seamount and shelf break, this relationship reverses, with Mode-1 IT gaining energy from Mode-3 (Fig. 5d, red patches). This direct backward energy transfer may result from other processes, notably the shear of background flow, whose influence is detailed below.

Decomposing the horizontal shear term H_{mn} (Figs. 5g–i) into its antisymmetric (Figs. 5j–l) and symmetric (Figs. 5m–o) components shows that its net influence ($|H_{mn}| \sim 4 \times 10^{-8}$ W m⁻¹ kg⁻¹) is primarily due to the antisymmetric part. This latter facilitates energy transfer between IT modes. Indeed, energy is transferred from Mode-2 to Mode-1 IT (Figs. 5k, red patches) and from Mode-3 to Mode-1 IT (Figs. 5j, red patches) between the continental slope and the seamount. However, between Modes 2 and 3, the symmetric part of H_{mn} dominates the net effect, indicating an energy exchange with the background flow rather than between IT modes. Specifically, Mode-2 IT loses energy to the Mode-3 background flow between the continental slope and seamount (Figs. 5o, blue patches), and gains it back between the seamount and ridge (Figs. 5o, red patches).



417 In essence, in the NE case, coherent energy flux from sites A and D propagates until encountering major
 418 topographic features (seamounts and ridges). While Mode-1 IT energy propagates over long distances with
 419 amplitudes exceeding 200 W m^{-1} , the higher modes behave differently. Mode-2 IT energy, despite having a
 420 comparable amplitude to Mode-1, is effectively damped. In contrast, the weaker Mode-3 IT energy ($< 200 \text{ W m}^{-1}$)
 421 becomes trapped by the topography. The interaction with topographic features, potentially enhanced by the
 422 background flow, triggers significant intermodal energy transfer on the order of $10^{-8} \text{ W m}^{-1} \text{ kg}^{-1}$. This transfer is
 423 governed by two primary mechanisms: (1) topographic scattering drives a dominant forward energy cascade
 424 through the IT modes (Mode-1 \rightarrow Mode-2 \rightarrow Mode-3), and (2) the horizontal shear of the background flow
 425 facilitates a direct energy scattering from Mode-2 IT to the Mode-3 background flow.



426



Figure 5. Tidal energy diagnostics for the NE case on 24 November 2015, averaged over a M2 tidal period. Panels (a–c) show the depth-integrated M2 baroclinic energy fluxes (\mathbf{F}_m ; black arrows) and horizontal kinetic energy (HKE_m; color shading) for (a) mode-1 (\mathbf{F}_1 , HKE₁), (b) mode-2 (\mathbf{F}_2 , HKE₂), and (c) mode-3 (\mathbf{F}_3 , HKE₃). Panels (d–f) present the effects of topographic scattering and stratification (C_{mn} ; color shading) for (d) C_{13} , (e) C_{12} , and (f) C_{23} . Panels (g–i) show the net component of horizontal shear induced by the mean background flow (H_{mn} ; color shading) for (g) H_{13} , (h) H_{12} , and (i) H_{23} . Panels (j–l) show the antisymmetric component of this horizontal shear (H_{mn} ; color shading) for (j) H^A_{13} , (k) H^A_{12} , and (l) H^A_{23} . Panels (m–o) show the symmetric component of horizontal shear (H_{mn} ; color shading) for (m) H^S_{13} , (n) H^S_{12} , and (o) H^S_{23} . All panels include the detected eddy edges (closed contours) and eddy centroids (dots) for anticyclones (blue) and cyclones (red). Topography is shown using the 200 m and 2000 m isobaths (grey contours), with specific features highlighted by the 3500 m isobath (seamount: cyan contour; Mid-Atlantic Ridge: magenta contour). The C_{mn} and H_{mn} fields were smoothed with a Gaussian filter ($\sigma = 7$ grid points) to aid interpretation.

3.2.2 CEC Case: IT Encountering a CE Core

We next examine IT responses when the energy flux from sites A and D encounter the core of a surface-intensified CE (CEC case, Fig. 2b). The CE, centered at 4.9° N, 44.4° W above the localized mid-seamount, has a radius of 157 km, maximum velocity 1.35 m s⁻¹, and a core bounded by 23–25.5 kg m⁻³ isopycnals extending ~150 m within the pycnocline.

Prior to interaction, the incident mode-1 IT energy fluxes converge and interfere. Upon encountering the CE core, this energy is refracted into a single beam (Fig. 6a), which emanates from the eddy center and propagates northward at approximately 35° from their northeastward incident direction. Both incident and refracted beams maintain comparable HKE of 150–200 J m⁻² (Fig. 6a), though the refraction process locally confines the energy, leading to a reduction in HKE (25–50 J m⁻²) in the northwestern lee of the eddy. Concurrently, the Mode-2 IT energy flux is blocked at the southern edge of the CE and seamount (Fig. 6b), while Mode-3 appears as scattered patches in the regions where Mode-2 is trapped (Fig. 6c), indicating active intermodal energy scattering. As in the NE case, Mode-1 and Mode-2 IT exhibit higher energy flux amplitudes (>200 W m⁻¹) along their beams than Mode-3 (<200 W m⁻¹) (Figs. 6a–c). The vertical structure of the along-transect baroclinic velocity further supports these results (Appendix A, Figs. A1, A3).

An analysis parallel to that conducted for the NE case identified the topographic scattering term (C_{mn}) and the horizontal shear term (H_{mn}) of the background flow as the dominant mechanisms responsible for the active energy scattering observed.

The analysis of the term C_{mn} in the CEC case reveals a distinct coupling pattern modulated by the CE core in conjunction with the seamount along the IT path from sites A and D. A dominant forward energy transfer ($|C_{mn}| \sim 4 \times 10^{-8}$ W m kg⁻¹) from Mode-1 to Mode-2 occurs near the shelf break (Fig. 6e, blue patches), consistent with the NE case (Fig. 5e). A significant shift occurs near the southern edge and core of the CE, where a dominant backward energy transfer is observed (with the exception of Mode-1 to Mode-3 IT). Here, energy is sequentially



467 gained by Mode-1 from Mode-2 (Fig. 6e, red patches near the southern edge and core of the CE) and by Mode-2
 468 from Mode-3 (inverse cascade, Fig. 6f, red patches), while energy is simultaneously lost from Mode-1 to Mode-
 469 3 (direct forward transfer, Fig. 6d, blue patches).

470

471 Analysis of the background flow horizontal shear term (H_{mn}) shows that its magnitude ($|H_{mn}| \sim 4 \times 10^{-8} \text{ W m}^{-1}$
 472 kg^{-1}) is comparable to the topography scattering term as in NE case. In the CEC case, the net effect of H_{mn} (Figs.
 473 6g-i) is primarily governed by its symmetric part (Figs. 6m-o), which facilitates energy exchange from the
 474 background flow to the IT modes. Specifically, between the shelf break and the southern edge of the CE, Mode-
 475 2 IT loses energy to the Mode-3 background flow (Fig. 6o, blue patches). Then, near the CE core and seamount,
 476 the background flow loses energy to the IT modes, with Mode-2 background flow energizing Mode-1 IT (Fig. 6n,
 477 red patches) and Mode-3 background flow energizing Mode-2 IT (Fig. 6o, red patches). However, between Mode-
 478 1 and Mode-3, the antisymmetric and symmetric parts of H_{mn} work in opposition (Figs. 6g,j,m), resulting in a
 479 near-zero net energy transfer. These overall patterns indicate a deflection of Mode-1 and Mode-2 IT, and provide
 480 strong evidence for a dominant energy pathway from the background flow to the IT modes driven by horizontal
 481 shear. This latter is coupled with direct forward energy transfer between IT modes driven by topographic scattering
 482 previously observed.

483

484 In summary, in the CEC case, the interaction with the CE core dictates distinct fates for IT modes. Mode-1 IT
 485 from sites A and D is not freely propagating but is primarily refracted into a single northward beam. In contrast,
 486 Mode-2 IT is blocked, and Mode-3 IT is scattered at the eddy edge and seamount. Energy flux amplitudes for
 487 Modes 1 and 2 exceed 200 W m^{-1} along their beams, whereas Mode-3 remains below this threshold. This
 488 interaction facilitates a significant energy transfer ($O(\sim 10^{-8} \text{ W m kg}^{-1})$) governed by a complex interplay of two
 489 mechanisms: 1) a dominant backward energy cascade, where horizontal shear transfers energy from the Mode-3
 490 background flow to Mode-2 IT, and from the Mode-2 background flow to Mode-1 IT; and 2) a forward scattering,
 491 where topography directly transfers energy from Mode-1 to Mode-3 IT.

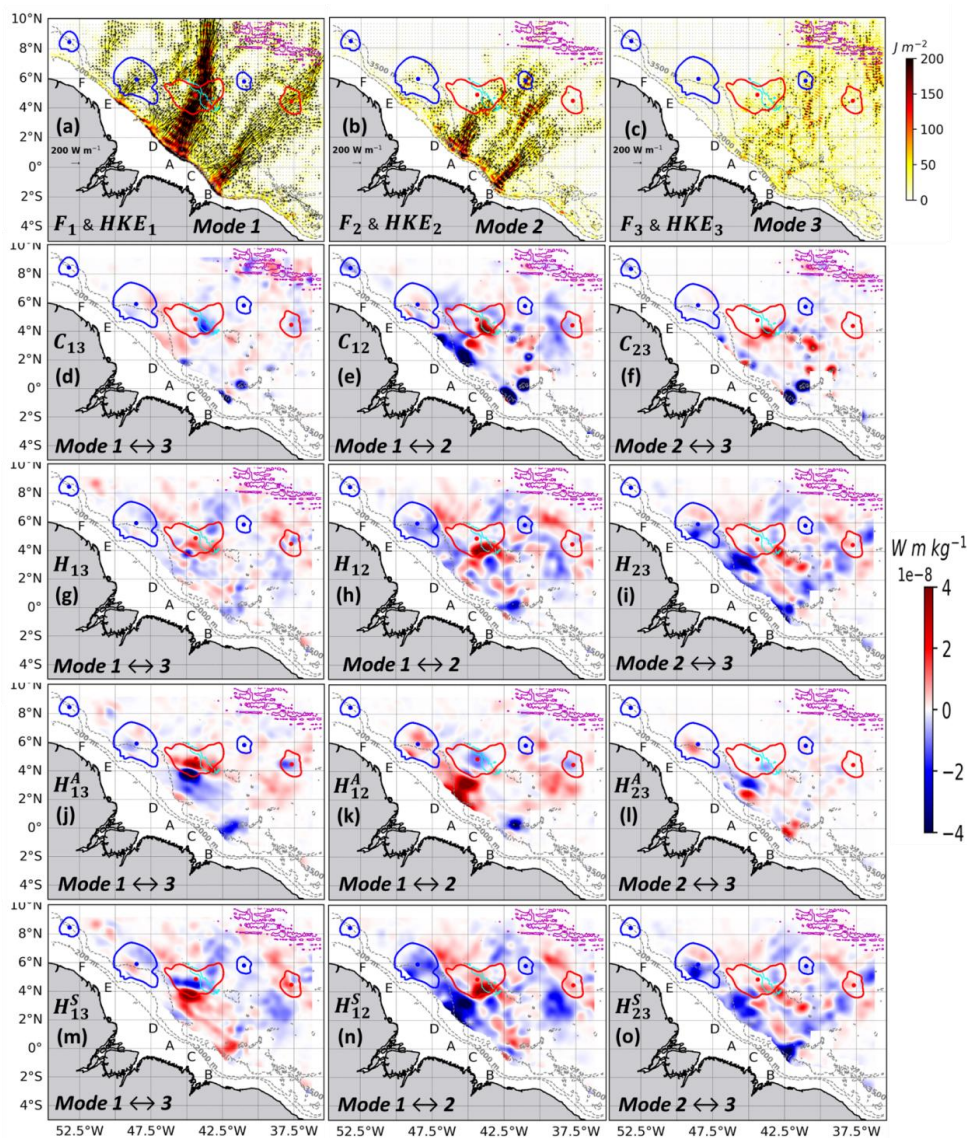


Figure 6. Tidal energy diagnostics for the CEC case (17 September 2015), following the format of Fig. 5.

3.2.3 CEE Case: IT Encountering a CE Edge

Finally, we assess IT interactions with the periphery of a surface-intensified CE centered at 5.3° N, 45.0° W (radius 143 km, maximum velocity 1.23 m s⁻¹, core bounded by 23–25.5 kg m⁻³ isopycnals extending ~100 m above the pycnocline).

This interaction yields a different kinematic response. The incident Mode-1 energy fluxes from sites A and D converge and, at the eddy edge, clearly diffract into two distinct beams (Fig. 7a): one propagating northward



503 (~39°) and the other eastward (~35°) relative to their northeastward incident direction. The northward-refracted
 504 beam maintains high HKE (150–200 J m⁻²), while HKE is sharply reduced (25–50 J m⁻²) in the northeast lee of
 505 the CE (Fig. 7a). Separately, the eastward-refracted beam, less energetic (HKE <100 J m⁻²) than the northward
 506 beam, passes near the eastern periphery of a small AE. Mode-2 flux is sheared at the CE periphery with limited
 507 directional change (Fig. 7b), and Mode-3 becomes trapped along the northeastern CE edge and near the ridge (Fig.
 508 7c). Consistent with previous cases, Mode-1 and Mode-2 exhibit higher energy flux amplitudes (>200 W m⁻¹)
 509 than Mode-3 (<200 W m⁻¹), and the energy flux patterns is supported by the vertical structures of the baroclinic
 510 velocity (Appendix A, Figs. A1, A4).

511
 512 As in prior cases, the analysis identified topographic scattering (C_{mn}) and horizontal shear (H_{mn}) of the background
 513 flow as the two dominant mechanisms driving intermodal scattering in the CEE case.

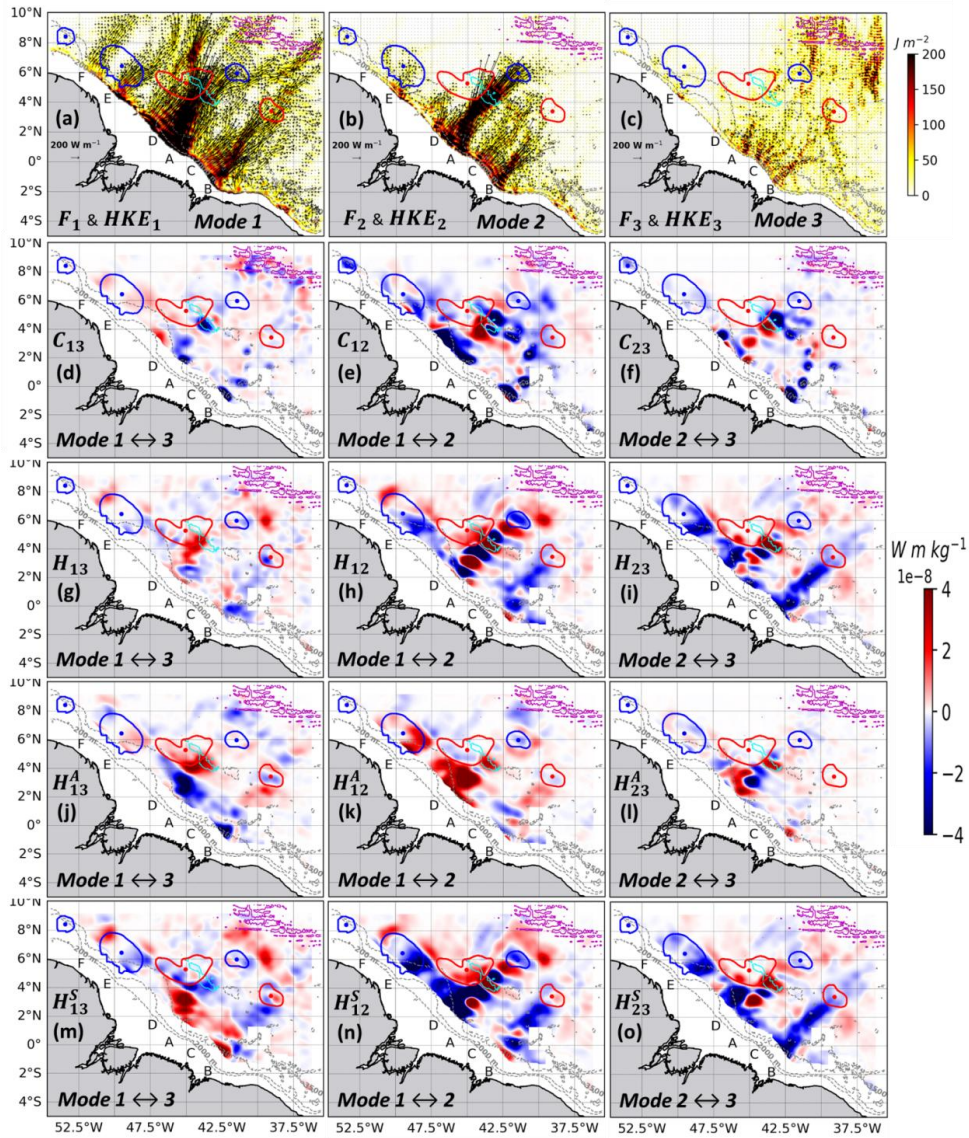
514
 515 The analysis of the term C_{mn} reveals a pattern modulated by the CE edge and seamount along the IT path from
 516 sites A and D. A dominant forward energy transfer ($|C_{mn}| \sim 4 \times 10^{-8} \text{ W m kg}^{-1}$) from Mode-1 to Mode-2 (Figs. 7e,
 517 blue patches) and from Mode-1 to Mode-3 IT (Figs. 7d, blue patches) occurs near the shelf break. Near the eastern
 518 edge of the CE and the southern flank of the seamount, a backward energy transfer occurs between IT modes
 519 (except between Mode-1 and Mode-3). Specifically, energy is gained by Mode-1 from Mode-2 IT (Figs. 7e, red
 520 patches) and by Mode-2 from Mode-3 IT (Figs. 7f, red patches), while energy is directly lost from Mode-1 to
 521 Mode-3 (Fig. 7d, blue patches). However, immediately after the seamount on the eastern CE edge, energy cascades
 522 forward from Mode-1 to Mode-2 (Fig. 7e, blue patches) and from Mode-2 to Mode-3 (Fig. 7f, blue patches).
 523 These overall patterns indicate that the CE edge inhibits the forward energy cascade observed in the NE case and
 524 instead initiates a dual mechanism: a potential flow shear-induced energy transfer from the background flow to
 525 IT modes, and a topographically-driven direct forward energy scattering between IT modes.

526
 527 As in previous cases, the horizontal shear term (H_{mn}) in the CEE case is of comparable magnitude ($|H_{mn}| \sim 4 \times$
 528 $10^{-8} \text{ W m}^{-1} \text{ kg}^{-1}$) to the topographic scattering term. The net effect of H_{mn} (Figs. 7g-i) is primarily dominated by
 529 its symmetric part (Figs. 7m-o), facilitating energy exchange from the background flow to the IT modes along the
 530 IT path from sites A and D. Between the continental slope and the southern CE edge, energy is lost and gained
 531 between the Mode-1 background flow and Mode-2 IT (Figs. 7n, blue and red patches), and Mode-2 background
 532 flow and Mode-3 IT (Figs. 7o, blue and red patches). Near the eastern CE edge and the southern seamount flank,
 533 energy is gained by the Mode-1 background flow from the Mode-2 IT (Figs. 7n, red patches), and by the Mode-2
 534 background flow from the Mode-3 IT (Figs. 7o, red patches). However, between Modes 1 and 3, the antisymmetric
 535 part of H_{mn} dominates (Figs. 7g,j), indicating an energy transfer between IT modes, where Mode-1 IT gains
 536 energy from Mode-3 IT (Figs. 7j, red patches near the CE edge and seamount). As in the CEC case, these patterns
 537 provide strong evidence for a dominant energy pathway from the background flow to the IT modes driven by
 538 horizontal shear, coupled with a topographically-driven direct forward energy transfer between IT modes.

539
 540 In summary, in the CEE case, upon interacting with the CE periphery, each IT mode meets a distinct fate. Mode-
 541 1 IT from sites A and D splits into two energetic beams, propagating northward and eastward with energy fluxes
 542 exceeding 200 W m⁻¹. In contrast, Mode-2 IT is sheared apart, while Mode-3 IT is scattered by the eddy edge and



543 seafloor topography, its energy flux remaining below 200 W m^{-1} . During this encounter, a significant energy
 544 transfer ($\sim 10^{-8} \text{ W m kg}^{-1}$) occurs through a similar interplay as in the CEC case: 1) a dominant inverse energy
 545 cascade from the background flow to the IT modes (Mode-3 \rightarrow Mode-2 \rightarrow Mode-1) driven by horizontal shear,
 546 which can act to suppress the topographically-driven downscale energy, and 2) a direct forward energy transfer
 547 from Mode-1 to Mode-3 IT driven by topographic scattering.



548
 549 **Figure 7.** Tidal energy diagnostics for the CEE case (29 September 2015), following the format of Fig. 5.



550 4 Discussion

551 This study investigated the fate of M_2 IT energy on the Amazon shelf during the turbulent period of SOND 2015.
 552 We addressed three questions: (1) Does the IT propagate freely, deviate, or become trapped by mesoscale features?
 553 (2) Do these outcomes depend on the IT's vertical mode or the properties and location of the MEs (CE core vs.
 554 periphery)? (3) What are the synergistic roles of topography and CEs in governing modal energy transfers? By
 555 projecting energy flux into vertical modes and performing intermodal energy transfer terms, we dissected these
 556 interactions more deeply.

557

558 4.1 The Variable Fate of Internal Tides: Free Propagation, Deviation, and Trapping

559

560 Our results show that the fate of IT energy is not uniform but is dictated by interactions with mesoscale features,
 561 affecting the intensity and distribution of energy flux. The NE case established a baseline of efficient, long-range
 562 propagation, where the Mode-1 energy flux maintained amplitudes exceeding 200 W m^{-1} along a coherent beam
 563 for over 1100 km. This free propagation aligns with previous studies (e.g., Xu et al., 2016; Fan et al., 2024) and
 564 confirms Mode-1's characteristic as a freely propagating IT (Zhao et al., 2010). Its path is governed by Snell's
 565 law (Small, 2001; Zhao, 2014), with minimal Coriolis constraint (f) near the equator ($f/\omega_{M2} \ll 1$, with ω_{M2} the M_2
 566 tidal frequency), shifting steering mechanisms to wave–current and wave–stratification interactions. The stability
 567 of the Mode-1 IT beam in background flow is consistent with ray-tracing results, such as those at the Hawaiian
 568 Ridge, where typical currents had only slight effects (Rainville and Pinkel, 2006). While high-resolution and
 569 idealized simulations suggested reduced Coriolis constraints at low latitudes (Wang et al., 2021; Le Dizes et al.,
 570 2025), our realistic simulations advance these findings by forcing nonlinear interactions in a highly complex field.

571

572 In the NE case, strong background flow, particularly the NECC, moved quasi-perpendicular to incident Mode-1
 573 IT beams, and horizontal stratification varied. The subcritical seamount ($h_{\text{max}}/H \sim 0.2$) acted only as a minor
 574 directional obstacle ($\lambda_1/w_{\text{max}} \sim 0.9\text{--}1.25$) for propagating Mode-1 IT, though it could affect higher-order modes
 575 intensified near the bottom.

576

577 The presence of a CE consistently disrupted free propagation, leading to deviation or trapping with distinct energy
 578 modulations. The incident Mode-1 IT was deviated into convergent energy beams, creating a zone of reduced
 579 energy flux in the lee of the eddy, consistent with processes modeled by Wang and Legg (2023) and Dunphy and
 580 Lamb (2014). This reduction in coherent energy flux is strongly supported by in situ observations south of the
 581 Azores, which reported a reduction in low-mode IT energy flux during interactions with a surface-intensified eddy
 582 (Löb et al., 2020). Across all cases, Mode-3 energy never formed a coherent beam and consistently exhibited the
 583 weakest fluxes ($<200 \text{ W m}^{-1}$). The most relevant blockage occurred for Mode-2 (with flux amplitude comparable
 584 to Mode-1) in the CEC case, where an otherwise energetic mode was completely impeded at the eddy–seamount
 585 interface. This vulnerability aligns with global observations that Mode-2 M_2 IT generally has smaller sea surface
 586 height amplitudes and shorter propagation distances ($O[100 \text{ km}]$) than Mode-1 (Zhao, 2018). MEs thus act as
 587 potent filters that selectively dissipate or trap the energy of specific vertical modes.

588

589 4.2 The Dual Control of IT Response: Vertical Mode and Eddy Encounters



590

591 A key finding of this study is that the IT responses to an ME is dually controlled by its vertical mode and the
 592 specific properties and location of the eddy encounter. Mode-1 IT is robust and long-ranging but susceptible to
 593 beam steering, while Mode-2 is far more vulnerable to damping and blocking. Mode-3 IT is consistently weak
 594 and scattered, behaving as a trapped mode that seldom forms coherent beams. Only Mode-1 IT underwent large-
 595 scale deviation by MEs or background flow fields, with energy loss occurring via forward energy transfer at
 596 localized, energetic interaction sites (seamount, eddy boundaries). This is consistent with studies showing that
 597 remote IT energy is scattered to higher modes at continental margins (Siyanbola et al., 2024; Fan et al., 2024) and
 598 with findings that an ME focuses Mode-1 energy flux in specific areas while inducing vertical mode scattering
 599 (Dunphy and Lamb, 2014). Our observation of Mode-1 deviation is analogous to the redirection of ISWs by ME
 600 fields (Liao et al., 2012; Goret et al., 2025).

601

602 IT beam deviation is sensitive to eddy properties. The direction of deviation depends strongly on eddy polarity,
 603 as shown by previous studies (e.g., Huang et al., 2018; Guo et al., 2023; Dunphy et al., 2017; Wang and Legg,
 604 2023; Li et al., 2024) and as observed—though not focused in our study—in the energy flux path emanating from
 605 the less energetic generation site E (see Section 3.1, Fig. 4b: deviation of the energy flux due to an AE core
 606 centered at 5.9°N and 48.5°W). While earlier work noted that AE cores speed up Mode-1 propagation and induce
 607 clockwise (southward) refraction, whereas CE cores slow it down and induce counterclockwise (northward)
 608 refraction, our findings link specific interaction geometries to distinct intermodal energy pathways in a realistic
 609 framework.

610

611 The distinction between the CEC (core) and CEE (periphery) cases reveals that the same CE can impose
 612 fundamentally different fates on a passing Mode-1 IT. Interaction with the eddy core refracted the incident beam
 613 coherently by $\sim 35^\circ$ into a single northward path. In contrast, an encounter at the eddy periphery diffracted the
 614 energy into two distinct beams propagating northward ($\sim 39^\circ$) and eastward ($\sim 35^\circ$). This demonstrates that “eddy
 615 lensing” is nuanced and sensitive to the radial structure and shear fields of the eddy. Recent SWOT satellite
 616 observations corroborate this finding, documenting analogous refraction at a CE core and diffraction at a western
 617 AE edge within the study region (Goret et al., 2025). Our results provide a mechanistic explanation for incoherent
 618 IT signals and variable trapping noted in high-resolution models of the ASOND period in this region (Tchilibou
 619 et al., 2022).

620

621 While Mode-1 IT is susceptible to beam steering, higher modes (Mode-2 and Mode-3) are more sensitive to
 622 topography and are quickly damped, trapped, and become primary recipients of energy via downscale cascades
 623 linked to topographic scattering (Lahaye et al., 2020; Fan et al., 2024; Bella et al., 2024). Our results advance
 624 these findings by showing that higher modes are also more sensitive to the presence of a CE in conjunction with
 625 a localized seamount. Therefore, the energy scattering from lower to higher IT modes and the trapping of those
 626 modes by CE’s flow are two linked processes facilitating the IT dissipation (Wang and Legg, 2023).

627

628 This study was limited to surface-intensified eddies. Future work should investigate whether similar IT
 629 interactions occur with other ME types, such as deep intrathermocline eddies or complex multi-eddy systems. A



key question is whether eddies with thin vertical structures—and thus higher vertical modes—are capable of trapping ITs, which warrants specific examination.

4.3 Synergistic Roles of Topography, Background Flow, and CEs in Modal Energy Transfers

Our results reveal a complex hierarchy of interactions that governs modal energy transfers, where even without strong MEs, the combined effects of topography and background flow establish a baseline for energy pathways.

The NE case shows the seamount acts as a critical site for modal scattering, driving a dominant forward energy cascade from Mode-1 to Mode-2 to Mode-3 IT ($\sim 4 \times 10^{-8} \text{ W m kg}^{-1}$). This magnitude of transfer is characteristic of interactions over abrupt topography, consistent with quantifications of energy cascades on continental slopes (Kelly and Nash, 2012). This topographically driven transfer is significantly modulated by background flow (NECC/NBC) through horizontal shear mechanisms of comparable strength, aligning with studies in the North Atlantic concluding that low-frequency flow strongly impacts the IT energy cycle, often transferring energy toward smaller scales (Bella et al., 2024). Background flow actively participates in energy exchange, facilitating transfer from Mode-3 background flow to Mode-2 IT over the seamount. Thus, seamount–topography interaction with background flow creates a dynamic environment for energy redistribution even before considering ME effects.

Introducing a CE—particularly one co-located with the seamount, as in the CEC case—fundamentally reorganizes the energy transfer landscape. The CE’s strong horizontal shear dominates background flow effects and reverses the canonical energy pathway, initiating a dominant inverse energy cascade from background flow to IT modes. This shift from the topographically driven forward cascade observed in the NE case is mediated by horizontal shear, supported by analyses using coupled-mode shallow-water models that emphasize advection terms involving mean flow and buoyancy shear (Kelly et al., 2016). The synergy between the CE and seamount creates competing pathways: topographically driven forward scattering operates concurrently with eddy-driven inverse cascades, leading to complex energy redistribution that explains observed modal blocking and trapping. This aligns with studies detailing how CEs and AEs differently affect topographic scattering (Li et al., 2024) and underscores that cross-scale energy exchange is a key driver in the tropical western Atlantic (Wang et al., 2025).

The consistent co-location of CEs and the seamount with background flow (e.g., NECC) suggests background flow variability further enhances IT refraction and diffraction—a mechanism supported by studies in other western boundary currents (Duda et al., 2018; Cao et al., 2022; Xu et al., 2021; Kelly and Lermusiaux, 2016; Chen et al., 2022; Pereira et al., 2007; Kelly et al., 2016), though fully isolating the NECC’s individual contribution will require future idealized modeling.

5 Conclusion

This study illustrates the complex pathways of M_2 IT energy in the region off the Amazon shelf during the period of SOND 2015. By applying vertical mode decomposition to high-resolution NEMO-AMAZON36 simulations, we examined three representative interaction cases (Fig. 8): undisturbed propagation until crossing a topography,



669 interaction with a CE core, and interaction with a CE eastern periphery. For each case, we systematically computed
 670 the intermodal energy transfer terms to identify the governing mechanisms.

671

672 The two primary conclusions are as follows:

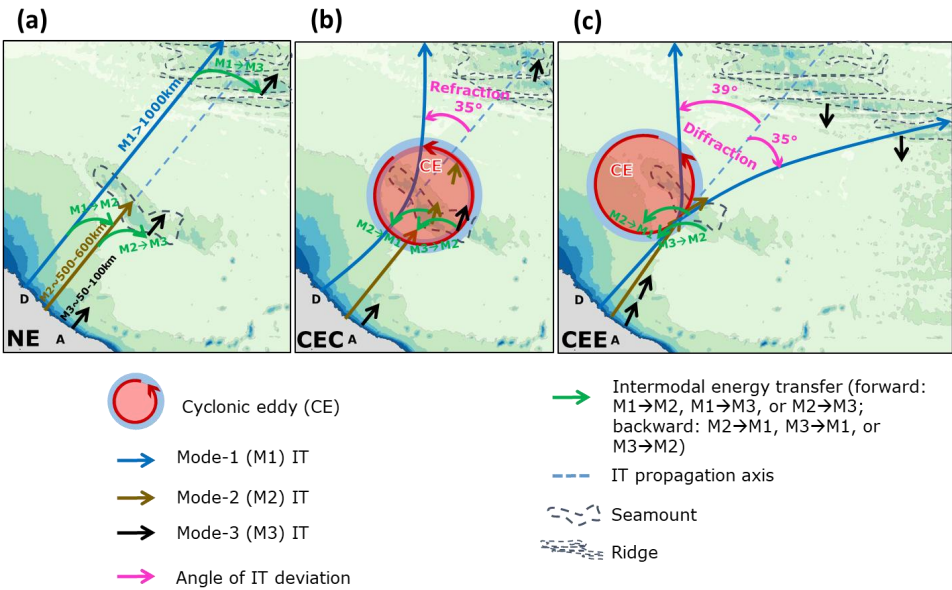
673 First, the specific response of an IT—whether it propagates freely or deviates—is dually controlled by its vertical
 674 modal structure and the properties of the mesoscale eddy it encounters. In the absence of a strong eddy (NE case),
 675 Mode-1 IT propagated freely as a coherent, long-range beam. Interactions with a CE, however, consistently
 676 disrupted this pattern, leading to refraction, diffraction, or trapping. An encounter with a CE core coherently
 677 refracted the Mode-1 beam northward by approximately 35° , maintaining high energy fluxes ($>200 \text{ W m}^{-1}$). In
 678 contrast, interaction at the eddy periphery diffracted the energy, splitting it into two distinct beams propagating
 679 northward ($\sim 39^\circ$) and eastward ($\sim 35^\circ$). Higher modes were particularly susceptible to trapping; Mode-2 energy
 680 flux—despite an amplitude comparable to Mode-1—was completely blocked and trapped at the eddy-seamount
 681 interface, while Mode-3 energy remained weak ($<200 \text{ W m}^{-1}$), scattered, and confined near the generation site
 682 without ever forming a coherent beam.

683

684 Second, the redistribution of energy via intermodal transfers is governed by a hierarchy of synergistic interactions
 685 between the seamount and the background flow of the eddy. In the NE case, the seamount drives a dominant
 686 forward energy cascade from Mode-1 to higher modes ($O(10^{-8} \text{ W m kg}^{-1})$), a process modulated by the
 687 background flow's horizontal shear. The presence of a CE colocated with the seamount fundamentally reorganizes
 688 this dynamic. The CE's strong horizontal shear initiates a dominant inverse energy cascade from the background
 689 flow to the IT modes, directly competing with the ongoing topographic forward cascade. This specific synergy is
 690 crucial for explaining the extreme blocking of Mode-2 and the complex redistribution of energy fluxes observed.

691

692 Nonetheless, the region is shaped by a complex, co-located interplay of forces—including the NECC, MEs (CEs
 693 and AEs), and the topographic features—making it challenging to fully isolate their individual effects on ITs in
 694 realistic simulations. To disentangle and quantify the specific contributions of each mechanism with greater
 695 precision, future work should employ idealized modeling frameworks. Such an approach is essential for isolating
 696 the deterministic impacts of mesoscale flow and advancing toward a predictive understanding of IT energy
 697 pathways in complex oceanic environments.



698
699 **Figure 8.** Schematics summarizing the fate of propagating M2 IT from generation sites A and D on the Amazon
700 shelf-break. The panels correspond to the three analyzed cases: (a) NE, (b) CEC, and (c) CEE. The diagram
701 highlights the key dynamic IT responses—inter-modal scattering, refraction, and diffraction—resulting from
702 interaction with mesoscale structures, emphasizing the pronounced effects of CEs. The specific IT response is
703 dually controlled by its vertical mode and the CE encounter properties. Furthermore, intermodal energy scattering
704 is governed by a hierarchical synergy between the seamount and the CE’s background flow.

705
706 **Data availability**

707 The NEMOV3.6 model outputs are available upon request by contacting the corresponding author.

708
709 **Authors contributions**

710 Funding acquisition: AKL, XC and MA. Conceptualization and methodology: FK, AKL and XC. Data processing:
711 FK. Formal analysis: FK with interactions from all co-authors. Preparation and writing of the manuscript: FK with
712 contributions from all co-authors.

713
714 **Competing interests**

715 The contact author has declared that none of the authors has any competing interests.

716
717 **Acknowledgments**

718 This work is a contribution to the project “MIAMAZ-ETI” (Multi-Sensors study of the fine scale processes and
719 their impacts on ocean color, off the Amazon shelf : Eddy-Tides Interactions). The authors thank Guillaume
720 Morvan for providing NEMO model data.

721
722 **Financial support**



723 This work is part of the PhD thesis of Fabius Kouogang, conducted under the joint supervision of Ariane Koch-
 724 Larrouy, Xavier Carton, and Moacyr Araujo. The research received support from “Coordenação de
 725 Aperfeiçoamento de Pessoal de Nível Superior” (CAPES); the Institute of Research for Development (IRD,
 726 France) via an ARTS grant; the ISblue project, Interdisciplinary graduate school for the blue planet (ANR-17-
 727 EURE-0015) and co-funded by a grant from the French government under the program “Investissements d’Avenir”
 728 embedded in France 2030; and the “Centre National d’Études Spatiales” (CNES) through the APR MIAMAZ-
 729 ETI project (Principal Investigators: Ariane Koch-Larrouy, Camila Artana, Isabelle Dadou). Moacyr Araujo was
 730 funded by the Brazilian National Council for Scientific and Technological Development (CNPq), and Xavier
 731 Carton received support from the University of Western Brittany.

732

733 References

734 Aguedjou, H. M. A., Dadou, I., Chaigneau, A., Morel, Y., and Alory, G.: Eddies in the tropical Atlantic Ocean
 735 and their seasonal variability, *Geophys. Res. Lett.*, 46, 12156–12164, <https://doi.org/10.1029/2019GL083925>,
 736 2019.

737

738 Aguedjou, H. M. A., Chaigneau, A., Dadou, I., Morel, Y., Pegliasco, C., Da-Allada, C. Y., and Baloitcha, E.:
 739 What can we learn from observed temperature and salinity isopycnal anomalies at eddy generation sites?
 740 Application in the tropical Atlantic Ocean, *J. Geophys. Res.: Oceans*, 126, e2021JC017630,
 741 <https://doi.org/10.1029/2021JC017630>, 2021.

742

743 Alford, M. H., Simmons, H. L., Marques, O. B., and Girtton, J. B.: Internal tide attenuation in the North Pacific,
 744 *Geophys. Res. Lett.*, 46, 8205–8213, <https://doi.org/10.1029/2019GL082648>, 2019.

745

746 Alford, M. H., and Zhao, Z.: Global patterns of low-mode internal-wave propagation. Part I: Energy and energy
 747 flux, *J. Phys. Oceanogr.*, 37, 1829–1848, <https://doi.org/10.1175/jpo3085.1>, 2007.

748

749 Assene, F., Koch-Larrouy, A., Dadou, I., Tchilibou, M., Morvan, G., Chanut, J., Costa Da Silva, A., Vantrepotte,
 750 V., Allain, D., and Tran, T.-K.: Internal tides off the Amazon shelf – Part 1: The importance of the structuring of
 751 ocean temperature during two contrasted seasons, *Ocean Sci.*, 20, 43–67, <https://doi.org/10.5194/os-20-43-2024>,
 752 2024.

753

754 Barbot, S., Lyard, F., Tchilibou, M., and Carrere, L.: Background stratification impacts on internal tide generation
 755 and abyssal propagation in the western equatorial Atlantic and the Bay of Biscay, *Ocean Sci.*, 17, 1563–1583,
 756 <https://doi.org/10.5194/os-17-1563-2021>, 2021.

757

758 Barnier, B., Reynaud, T., Beckmann, A., Böning, C., Molines, J.-M., Barnard, S., and Jia, Y.: On the seasonal
 759 variability and eddies in the North Brazil Current: Insights from model intercomparison experiments, *Prog.*
 760 *Oceanogr.*, 48, 195–230, [https://doi.org/10.1016/S0079-6611\(01\)00005-2](https://doi.org/10.1016/S0079-6611(01)00005-2), 2001.

761



- 762 Bella, A., Lahaye, N., and Tissot, G.: Internal tide energy transfers induced by mesoscale circulation and
 763 topography across the North Atlantic, *J. Geophys. Res.: Oceans*, 129, e2024JC020914,
 764 <https://doi.org/10.1029/2024JC020914>, 2024.
- 765
- 766 Brandt, P., Rubino, A., and Fischer, J.: Large-amplitude internal solitary waves in the North Equatorial
 767 Countercurrent, *J. Phys. Oceanogr.*, 32, 1567–1573, [https://doi.org/10.1175/1520-0485\(2002\)032<1567:LAISWI>2.0.CO;2](https://doi.org/10.1175/1520-0485(2002)032<1567:LAISWI>2.0.CO;2), 2002.
- 768
- 769
- 770 Buijsman, M. C., Legg, S., and Klymak, J.: Double-ridge internal tide interference and its effect on dissipation in
 771 Luzon Strait, *J. Phys. Oceanogr.*, 42, 1337–1356, <https://doi.org/10.1175/jpo-d-11-0210.1>, 2012.
- 772
- 773 Cao, A., Guo, Z., Wang, S., Guo, X., and Song, J.: Incoherence of the M2 and K1 internal tides radiated from the
 774 Luzon Strait under the influence of looping and leaping Kuroshio, *Prog. Oceanogr.*, 206, 102850,
 775 <https://doi.org/10.1016/j.pcean.2022.102850>, 2022.
- 776
- 777 Chen, J., Zhu, X.-H., Wang, M., Zheng, H., Zhao, R., Nakamura, H., and Yamashiro, T.: Incoherent signatures of
 778 internal tides in the Tokara Strait modulated by the Kuroshio, *Prog. Oceanogr.*, 206, 102863,
 779 <https://doi.org/10.1016/j.pcean.2022.102863>, 2022.
- 780
- 781 Clément, L., Frajka-Williams, E., Sheen, K. L., Brearley, J. A., and Garabato, A. N.: Generation of internal waves
 782 by eddies impinging on the western boundary of the North Atlantic, *J. Phys. Oceanogr.*, 46, 1067–1079,
 783 <https://doi.org/10.1175/JPO-D-14-0241.1>, 2016.
- 784
- 785 De Macedo, C. R., Koch-Larrouy, A., Da Silva, J. C. B., Magalhães, J. M., Lentini, C. A. D., Tran, T. K., Rosa,
 786 M. C. B., and Vantrepotte, V.: Spatial and temporal variability of mode-1 and mode-2 internal solitary waves from
 787 MODIS/TERRA sunglint off the Amazon shelf, *Ocean Sci.*, 19, 1357–1374, <https://doi.org/10.5194/os-19-1357-2023>, 2023.
- 788
- 789
- 790 Delpech, A., Cravatte, S., Marin, F., Morel, Y., Gronchi, E., and Kestenare, E.: Observed tracer fields structuration
 791 by middepth zonal jets in the tropical Pacific, *J. Phys. Oceanogr.*, 50, 281–304, <https://doi.org/10.1175/JPO-D-19-0091.1>, 2020.
- 792
- 793
- 794 Didden, N., and Schott, F.: Eddies in the North Brazil Current retroflection region observed by Geosat altimetry,
 795 *J. Geophys. Res.*, 98, 20121, <https://doi.org/10.1029/93JC01184>, 1993.
- 796
- 797 Duda, T. F., Lin, Y.-T., Buijsman, M., and Newhall, A. E.: Internal tidal modal ray refraction and energy ducting
 798 in baroclinic Gulf Stream currents, *J. Phys. Oceanogr.*, 48, 1965–1983, <https://doi.org/10.1175/JPO-D-17-0230.1>,
 799 2018.
- 800



- 801 Dunphy, M., and Lamb, K. G.: Focusing and vertical mode scattering of the first mode internal tide by mesoscale
802 eddy interaction, *J. Geophys. Res.: Oceans*, 119, 523–536, <https://doi.org/10.1002/2013JC009363>, 2014.
- 803
- 804 Dunphy, M., Ponte, A. L., Klein, P., and Le Gentil, S.: Low-mode internal tide propagation in a turbulent eddy
805 field, *J. Phys. Oceanogr.*, 47, 649–665, <https://doi.org/10.1175/JPO-D-16-0099.1>, 2017.
- 806
- 807 Ernst, P. A., Subrahmanyam, B., Morel, Y., Trott, C. B., and Chaigneau, A.: Subsurface eddy detection optimized
808 with potential vorticity from models in the Arabian Sea, *J. Atmos. Ocean. Technol.*, 40, 677–700,
809 <https://doi.org/10.1175/JTECH-D-22-0050.1>, 2023.
- 810
- 811 Ertel, H.: On hydrodynamic eddy theorems, *Phys. Z.*, 43, 526–529, 1942.
- 812
- 813 Fan, L., Sun, H., Yang, Q., and Li, J.: Numerical investigation of interaction between anticyclonic eddy and
814 semidiurnal internal tide in the northeastern South China Sea, *Ocean Sci.*, 20, 241–264, <https://doi.org/10.5194/os-20-241-2024>, 2024.
- 815
- 816
- 817 Fassoni-Andrade, A. C., Durand, F., Azevedo, A., Bertin, X., Santos, L. G., Khan, J. U., Testut, L., and Moreira,
818 D. M.: Seasonal to interannual variability of the tide in the Amazon estuary, *Cont. Shelf Res.*, 255, 104945,
819 <https://doi.org/10.1016/j.csr.2023.104945>, 2023.
- 820
- 821 Fratantoni, D. M., and Glickson, D. A.: North Brazil Current Ring generation and evolution observed with
822 SeaWiFS, *J. Phys. Oceanogr.*, 32, 1058–1074, [https://doi.org/10.1175/1520-0485\(2002\)032<1058:NBCRGA>2.0.CO;2](https://doi.org/10.1175/1520-0485(2002)032<1058:NBCRGA>2.0.CO;2), 2002.
- 823
- 824
- 825 Garrett, C., and Kunze, E.: Internal tide generation in the deep ocean, *Annu. Rev. Fluid Mech.*, 39, 57–87,
826 <https://doi.org/10.1146/ANNUREV.FLUID.39.050905.110227>, 2007.
- 827
- 828 GEBCO Compilation Group: GEBCO_2020 grid, British Oceanographic Data Centre, National Oceanography
829 Centre, NERC, UK [data set], <https://doi.org/10.5285/a29c5465-b138-234d-e053-6c86abc040b9>, 2020.
- 830
- 831 Gerkema, T., and Zimmerman, J. T. F.: An introduction to internal waves, Lecture Notes, Royal Netherlands
832 Institute for Sea Research, 2008.
- 833
- 834 Goret, C., Koch-Larrouy, A., Kouogang, F., de Macedo, C. R., M’Hamdi, A., Magalhães, J., da Silva, J. C. B.,
835 Tchilibou, M., Artana, C., Dadou, I., Delepouille, A., Barbot, S., Ballarotta, M., Carrère, L., and Costa da Silva,
836 A.: Internal solitary waves refraction and diffraction from interaction with eddies off the Amazon shelf from
837 SWOT, *EGUsphere* [preprint], <https://doi.org/10.5194/egusphere-2025-3933>, 2025.
- 838
- 839 Guo, Z., Wang, S., Cao, A., Xie, J., Song, J., and Guo, X.: Refraction of the M2 internal tides by mesoscale eddies
840 in the South China Sea, *Deep-Sea Res. Pt. I*, 192, 103946, <https://doi.org/10.1016/j.dsr.2022.103946>, 2023.



- 841
- 842 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu,
 843 R., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot,
 844 J., Bonavita, M., De Chiara, G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R.,
 845 Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R. J., Hólm, E., Janisková, M., Keeley, S., Laloyaux,
 846 P., Lopez, P., Lupu, C., Radnoti, G., de Rosnay, P., Rozum, I., Vamborg, F., Villaume, S., and Thépaut, J.-N.:
 847 The ERA5 global reanalysis, *Q. J. Roy. Meteor. Soc.*, 146, 1999–2049, <https://doi.org/10.1002/qj.3803>, 2020.
- 848
- 849 Huang, X., Wang, Z., Zhang, Z., Yang, Y., Zhou, C., Yang, Q., Zhao, W., and Tian, J.: Role of mesoscale eddies
 850 in modulating the semidiurnal internal tide: Observation results in the northern South China Sea, *J. Phys.*
 851 *Oceanogr.*, 48, 1749–1768, <https://doi.org/10.1175/JPO-D-17-0238.1>, 2018.
- 852
- 853 Johnston, T. M. S., and Merrifield, M. A.: Internal tide scattering at the Line Islands Ridge, *J. Geophys. Res.*, 108,
 854 3365, <https://doi.org/10.1029/2003JC001844>, 2003.
- 855
- 856 Kelly, S. M.: The vertical mode decomposition of surface and internal tides in the presence of a free surface and
 857 arbitrary topography, *J. Phys. Oceanogr.*, 46, 3845–3859, <https://doi.org/10.1175/JPO-D-16-0164.1>, 2016.
- 858
- 859 Kelly, S. M., and Lermusiaux, P. F. J.: The cascade of tidal energy from low to high modes on a continental slope,
 860 *J. Phys. Oceanogr.*, 42, 1276–1292, <https://doi.org/10.1175/JPO-D-11-0231.1>, 2012.
- 861
- 862 Kelly, S. M., and Lermusiaux, P. F. J.: Internal-tide interactions with the Gulf Stream and Middle Atlantic Bight
 863 shelfbreak front, *J. Geophys. Res.: Oceans*, 121, 6271–6294, <https://doi.org/10.1002/2016JC011986>, 2016.
- 864
- 865 Kelly, S. M., Lermusiaux, P. F. J., and Duda, T. F.: A coupled-mode shallow-water model for tidal analysis:
 866 Internal tide reflection and refraction by the Gulf Stream, *J. Phys. Oceanogr.*, 46, 3747–3767,
 867 <https://doi.org/10.1175/JPO-D-16-0125.1>, 2016.
- 868
- 869 Kelly, S. M., Nash, J. D., Martini, K. I., Alford, M. H., and Kunze, E.: The cascade of tidal energy from low to
 870 high modes on a continental slope, *J. Phys. Oceanogr.*, 42, 1217–1232, <https://doi.org/10.1175/jpo-d-11-0231.1>,
 871 2012.
- 872
- 873 Kelly, S. M., Nash, J. D., and Kunze, E.: Internal-tide energy over topography, *J. Geophys. Res.-Oceans*, 115,
 874 C06014, <https://doi.org/10.1029/2009JC005618>, 2010.
- 875
- 876 Kelly, S. M., and Nash, J. D.: Internal-tide generation and destruction by shoaling internal tides, *Geophys. Res.*
 877 *Lett.*, 37, L23611, <https://doi.org/10.1029/2010GL045598>, 2010.
- 878
- 879 Kerry, C. G., Powell, B. S., and Carter, G. S.: Effects of remote generation sites on model estimates of M2 internal
 880 tides in the Philippine Sea, *J. Phys. Oceanogr.*, 43, 187–204, <https://doi.org/10.1175/jpo-d-12-081.1>, 2013.



- 881
- 882 Koch-Larrouy, A., Atmadipoera, A., van Beek, P., Madec, G., Aucan, J., Lyard, F., Grelet, J., and Souhaut, M.:
 883 Estimates of tidal mixing in the Indonesian archipelago from multidisciplinary INDOMIX in-situ data, Deep-Sea
 884 Res. Pt. I, 106, 136–153, <https://doi.org/10.1016/j.dsr.2015.09.007>, 2015.
- 885
- 886 Kouogang, F., Koch-Larrouy, A., Magalhaes, J., Costa Da Silva, A., Kerhervé, D., Bertrand, A., Cervelli, E.,
 887 Ternon, J.-F., Rousselot, P., Lee, J., Rollnic, M., and Araujo, M.: Turbulent dissipation from AMAZOMIX off
 888 the Amazon shelf along internal tide paths, Ocean Sci., 21, 1589–1608, <https://doi.org/10.5194/os-21-1589-2025>,
 889 2025.
- 890
- 891 Kunze, E.: Internal-wave-driven mixing: Global geography and budgets, J. Phys. Oceanogr., 47, 1325–1345,
 892 <https://doi.org/10.1175/JPO-D-16-0141.1>, 2017.
- 893
- 894 Kurian, J., Colas, F., Capet, X., McWilliams, J. C., and Chelton, D. B.: Eddy properties in the California Current
 895 System, J. Geophys. Res.-Oceans, 116, <https://doi.org/10.1029/2010jc006895>, 2011.
- 896
- 897 Lahaye, N., Gula, J., and Roulet, G.: Internal tide cycle and topographic scattering over the north mid-Atlantic
 898 ridge, J. Geophys. Res.: Oceans, 125, e2020JC016376, <https://doi.org/10.1029/2020JC016376>, 2020.
- 899
- 900 Lahaye, N., Ponte, A., Le Sommer, J., and Albert, A.: Internal tide surface signature and incoherence in the North
 901 Atlantic, Geophys. Res. Lett., 51, e2024GL108508, <https://doi.org/10.1029/2024GL108508>, 2024.
- 902
- 903 Le Dizes, C., Grisouard, N., Thual, O., and Mercier, M. J.: Three-dimensional modelling of internal tide
 904 generation over isolated seamounts in a rotating ocean, J. Fluid Mech., 1022, A5,
 905 <https://doi.org/10.1017/jfm.2025.10647>, 2025.
- 906
- 907 Lellouche, J.-M., Greiner, E., Le Galloudec, O., Garric, G., Regnier, C., Drevillon, M., Benkiran, M., Testut, C.-
 908 E., BourdalleBadie, R., Gasparin, F., Hernandez, O., Levier, B., Drillet, Y., Remy, E., and Le Traon, P.-Y.: Recent
 909 updates to the Copernicus Marine Service global ocean monitoring and forecasting realtime 1=12° high-resolution
 910 system, Ocean Sci., 14, 1093–1126, <https://doi.org/10.5194/os-14-1093-2018>, 2018.
- 911
- 912 Li, B., Xu, M., Chen, W., Yuan, Y., Liu, Y., and Li, S.: Evolution of internal tide scattering hidden below
 913 mesoscale eddies, Prog. Oceanogr., 226, 103305, <https://doi.org/10.1016/j.pocean.2024.103305>, 2024.
- 914
- 915 Liao, G., Yang, C., Xu, X., Shi, X., Yuan, Y., and Huang, W.: Effects of mesoscale eddies on the internal solitary
 916 wave propagation, Acta Oceanol. Sin., 31, 26–40, <https://doi.org/10.1007/s13131-012-0205-5>, 2012.
- 917
- 918 Lorenz, E. N.: Available potential energy and the maintenance of the general circulation, Tellus, 7, 157–167,
 919 <https://doi.org/10.1111/j.2153-3490.1955.tb01148.x>, 1955.
- 920



- 921 Löb, J., Köhler, J., Mertens, C., Walter, M., Li, Z., and von Storch, J.-S.: Observations of the low-mode internal
 922 tide and its interaction with mesoscale flow south of the Azores, *J. Geophys. Res.: Oceans*, 125, e2019JC015879,
 923 <https://doi.org/10.1029/2019JC015879>, 2020.
- 924
- 925 Lyard, F. H., Allain, D. J., Cancet, M., Carrère, L., and Picot, N.: FES2014 global ocean tide atlas: Design and
 926 performance, *Ocean Sci.*, 17, 615–649, <https://doi.org/10.5194/os-17-615-2021>, 2021.
- 927
- 928 Madec, G., Bourdallé-Badie, R., Chanut, J., Clementi, E., Coward, A., Ethé, C., Iovino, D., Lea, D., Lévy, C.,
 929 Lovato, T., Martin, N., Masson, S., Mocavero, S., Rousset, C., Storkey, D., Vancoppenolle, M., Müeller, S.,
 930 Nurser, G., Bell, M., and Samson, G.: NEMO ocean engine, Zenodo, <https://doi.org/10.5281/zenodo.3878122>,
 931 2019.
- 932
- 933 Magalhaes, J. M., Da Silva, J. C. B., Buijsman, M. C., and Garcia, C. A. E.: Effect of the North Equatorial Counter
 934 Current on the generation and propagation of internal solitary waves off the Amazon shelf (SAR observations),
 935 *Ocean Sci.*, 12, 243–255, <https://doi.org/10.5194/os-12-243-2016>, 2016.
- 936
- 937 Mathur, M., Carter, G. S., and Peacock, T.: Topographic scattering of the low-mode internal tide in the deep
 938 ocean, *J. Geophys. Res.-Oceans*, 119, 2165–2182, <https://doi.org/10.1002/2013JC009152>, 2014.
- 939
- 940 Morel, Y., Gula, J., and Ponte, A.: Potential vorticity diagnostics based on balances between volume integral and
 941 boundary conditions, *Ocean Model.*, 138, 23–35, <https://doi.org/10.1016/j.ocemod.2019.04.004>, 2019.
- 942
- 943 Morel, Y., Morvan, G., Benshila, R., Renault, L., Gula, J., and Auclair, F.: An “objective” definition of potential
 944 vorticity: Generalized evolution equation and application to the study of coastal upwelling instability, *Ocean*
 945 *Model.*, 186, 102287, <https://doi.org/10.1016/j.ocemod.2023.102287>, 2023.
- 946
- 947 Nakamura, N.: Modified Lagrangian-mean diagnostics of the stratospheric polar vortices. Part I. Formulation and
 948 analysis of GFDL SKYHI GCM, *J. Atmos. Sci.*, 52, 2096–2108, [https://doi.org/10.1175/1520-0469\(1995\)052<2096:MLMDOT>2.0.CO;2](https://doi.org/10.1175/1520-0469(1995)052<2096:MLMDOT>2.0.CO;2), 1995.
- 949
- 950
- 951 Nash, J. D., Kelly, S. M., Shroyer, E. L., Moum, J. N., and Duda, T. F.: The unpredictable nature of internal tides
 952 on continental shelves, *J. Phys. Oceanogr.*, 42, 1981–2000, <https://doi.org/10.1175/JPO-D-12-028.1>, 2012.
- 953
- 954 Okubo, A.: Horizontal dispersion of floatable particles in vicinity of velocity singularities such as convergence,
 955 *Deep-Sea Res.*, 17, 445, [https://doi.org/10.1016/0011-7471\(70\)90059-8](https://doi.org/10.1016/0011-7471(70)90059-8), 1970.
- 956
- 957 Pereira, A. F., Castro, B. M., Calado, L., and da Silveira, I. C. A.: Numerical simulation of M2 internal tides in
 958 the South Brazil Bight and their interaction with the Brazil Current, *J. Geophys. Res.*, 112, C04009,
 959 <https://doi.org/10.1029/2006JC003673>, 2007.
- 960



- 961 Rainville, L., and Pinkel, R.: Propagation of low-mode internal waves through the ocean, *J. Phys. Oceanogr.*, 36,
 962 1220–1236, <https://doi.org/10.1175/JPO2924.1>, 2006.
- 963
- 964 Savage, A. C., Waterhouse, A. F., and Kelly, S. M.: Internal tide nonstationarity and wave–mesoscale interactions
 965 in the Tasman Sea, *J. Phys. Oceanogr.*, 50, 2931–2951, <https://doi.org/10.1175/JPO-D-20-0081.1>, 2020.
- 966
- 967 Silva, A. C., Bourles, B., and Araujo, M.: Circulation of the thermocline salinity maximum waters off the Northern
 968 Brazil as inferred from in situ measurements and numerical results, *Ann. Geophys.*, 27, 1861–1873,
 969 <https://doi.org/10.5194/angeo-27-1861-2009>, 2009.
- 970
- 971 Siyanbola, O. Q., Buijsman, M. C., Delpech, A., Barkan, R., Pan, Y., and Arbic, B. K.: Interactions of remotely
 972 generated internal tides with the U.S. West Coast continental margin, *J. Geophys. Res.: Oceans*, 129,
 973 e2023JC020859, <https://doi.org/10.1029/2023JC020859>, 2024.
- 974
- 975 Small, J.: A nonlinear model of the shoaling and refraction of interfacial solitary waves in the ocean. Part II:
 976 Oblique refraction across a continental slope and propagation over a seamount, *J. Phys. Oceanogr.*, 31, 3184–
 977 3199, [https://doi.org/10.1175/1520-0485\(2001\)031<3184:ANMOTS>2.0.CO;2](https://doi.org/10.1175/1520-0485(2001)031<3184:ANMOTS>2.0.CO;2), 2001.
- 978
- 979 Tchilibou, M., Gourdeau, L., Lyard, F., Morrow, R., Koch Larrouy, A., Allain, D., and Djath, B.: Internal tides in
 980 the Solomon Sea in contrasted ENSO conditions, *Ocean Sci.*, 16, 615–635, [https://doi.org/10.5194/os-16-615-](https://doi.org/10.5194/os-16-615-2020)
 981 2020, 2020.
- 982
- 983 Tchilibou, M., Koch-Larrouy, A., Barbot, S., Lyard, F., Morel, Y., Jouanno, J., and Morrow, R.: Internal tides off
 984 the Amazon shelf during two contrasted seasons: Interactions with background circulation and SSH imprints,
 985 *Ocean Sci.*, 18, 1591–1618, <https://doi.org/10.5194/os-18-1591-2022>, 2022.
- 986
- 987 Vic, C., Naveira Garabato, A. C., Green, J. M., Waterhouse, A. F., Zhao, Z., Melet, A., de Lavergne, C., Buijsman,
 988 M. C., and Stephenson, G. R.: Deep-ocean mixing driven by small-scale internal tides, *Nat. Commun.*, 10, 2099,
 989 <https://doi.org/10.1038/s41467-019-10149-5>, 2019.
- 990
- 991 Wang, W., Li, J., and Huang, X.: Semidiurnal internal tide interference in the northern South China Sea, *J. Marine*
 992 *Sci. Eng.*, 12, 811, <https://doi.org/10.3390/jmse12050811>, 2024.
- 993
- 994 Wang, X., Peng, S., Liu, Z., Huang, R. X., Qian, Y.-K., and Li, Y.: Tidal mixing in the South China Sea: An
 995 estimate based on the internal tide energetics, *J. Phys. Oceanogr.*, 46, 107–124, [https://doi.org/10.1175/JPO-D-](https://doi.org/10.1175/JPO-D-15-0082.1)
 996 15-0082.1, 2016.
- 997
- 998 Wang, Y., Curchitser, E., Legg, S., and Kang, D.: Internal tide interactions with submesoscale and mesoscale
 999 eddies in the tropical western Atlantic, *J. Phys. Oceanogr.*, 55, 1245–1262, [https://doi.org/10.1175/JPO-D-24-](https://doi.org/10.1175/JPO-D-24-0063.1)
 1000 0063.1, 2025.



- 1001
- 1002 Wang, Y., and Legg, S.: Enhanced dissipation of internal tides in a mesoscale baroclinic eddy, *J. Phys. Oceanogr.*,
- 1003 53, 2533–2550, <https://doi.org/10.1175/JPO-D-22-0205.1>, 2023.
- 1004
- 1005 Wang, Y., Xu, Z., Hibiya, T., Yin, B., and Wang, F.: Radiation path of diurnal internal tides in the northwestern
- 1006 Pacific controlled by refraction and interference, *J. Geophys. Res.: Oceans*, 126, e2020JC016972,
- 1007 <https://doi.org/10.1029/2020JC016972>, 2021.
- 1008
- 1009 Weiss, J.: The dynamics of enstrophy transfer in 2-dimensional hydrodynamics, *Physica D*, 48, 273–294,
- 1010 [https://doi.org/10.1016/0167-2789\(91\)90088-Q](https://doi.org/10.1016/0167-2789(91)90088-Q), 1991.
- 1011
- 1012 Winters, K. B., and D’Asaro, E. A.: Diascalar flux and the rate of fluid mixing, *J. Fluid Mech.*, 317, 179–193,
- 1013 <https://doi.org/10.1017/S002211209600007X>, 1996.
- 1014
- 1015 Wunsch, C., and Ferrari, R.: Vertical mixing, energy, and the general circulation of the oceans, *Annu. Rev. Fluid*
- 1016 *Mech.*, 36, 281–314, <https://doi.org/10.1146/annurev.fluid.36.050802.122121>, 2004.
- 1017
- 1018 Xu, A., Yu, F., and Nan, F.: Study of subsurface eddy properties in northwestern Pacific Ocean based on an eddy-
- 1019 resolving OGCM, *Ocean Dynam.*, 69, 463–474, <https://doi.org/10.1007/s10236-019-01255-5>, 2019.
- 1020
- 1021 Xu, Z., Liu, K., Yin, B., Zhao, Z., Wang, Y., and Li, Q.: Longrange propagation and associated variability of
- 1022 internal tides in the South China Sea, *J. Geophys. Res.-Oceans*, 121, 8268–8286,
- 1023 <https://doi.org/10.1002/2016JC012105>, 2016.
- 1024
- 1025 Xu, Z., Wang, Y., Liu, Z., McWilliams, J. C., and Gan, J.: Insight into the dynamics of the radiating internal tide
- 1026 associated with the Kuroshio current, *J. Geophys. Res.: Oceans*, 126, e2020JC017018,
- 1027 <https://doi.org/10.1029/2020JC017018>, 2021.
- 1028
- 1029 Zhao, Z.: The global mode-2 M2 internal tide, *J. Geophys. Res.: Oceans*, 123, 7725–7746,
- 1030 <https://doi.org/10.1029/2018JC014380>, 2018.
- 1031
- 1032 Zhao, Z.: Internal tide radiation from the Luzon Strait, *J. Geophys. Res.: Oceans*, 119, 5434–5448,
- 1033 <https://doi.org/10.1002/2014JC010150>, 2014.
- 1034
- 1035 Zhao, Z., Alford, M. H., MacKinnon, J. A., and Pinkel, R.: Long-range propagation of the semidiurnal internal
- 1036 tide from the Hawaiian Ridge, *J. Phys. Oceanogr.*, 40, 713–736, <https://doi.org/10.1175/2009JPO4207.1>, 2010.
- 1037
- 1038 Zhao, Z.: The global mode-1 S2 internal tide, *J. Geophys. Res.-Oceans*, 122, 8794–8812,
- 1039 <https://doi.org/10.1002/2017JC013112>, 2017.
- 1040



1041 Zalesak, S. T.: Fully multidimensional flux-corrected transport algorithms for fluids, J. Comput. Phys., 31, 335–
 1042 362, [https://doi.org/10.1016/0021-9991\(79\)90051-2](https://doi.org/10.1016/0021-9991(79)90051-2), 1979.

1043

1044 Zaron, E. D., and Egbert, G. D.: Time-variable refraction of internal tides at the Hawaiian Ridge, J. Phys.
 1045 Oceanogr., 44, 538–557, <https://doi.org/10.1175/JPO-D-12-0238.1>, 2014.

1046

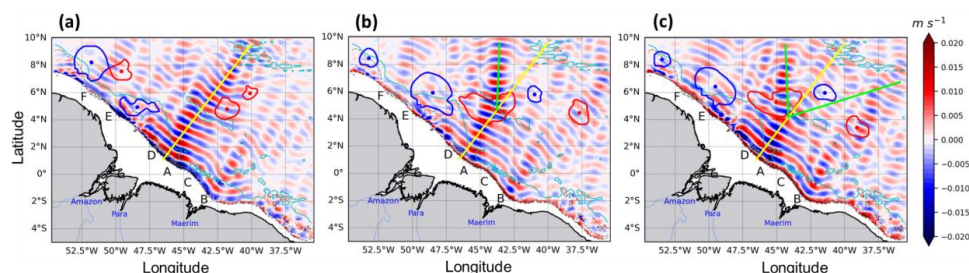
1047 Appendix

1048

1049 Appendix A: M₂ Tidal Beam Dynamics

1050

1051 To better determine whether the response of ITs to MEs, specifically CEs, is governed more by the IT's vertical
 1052 structure or by the CE's properties and location, we analyzed the M₂ baroclinic velocity field. Following the
 1053 methodology in Sect. 2.2.2, we projected the velocity field into vertical modes and defined transects along
 1054 different IT beams for the NE, CEC, and CEE cases (Fig. A1): the northeastward incident beam (yellow) from
 1055 sites A and D, northward refracted beams from CE core (green), and diffracted beams (northward and eastward)
 1056 from CE periphery (green). We then decomposed the modal velocities into along- and cross-transect components.
 1057 The transect along the incident tidal beam was identical in all three cases to enable a direct comparison. Our
 1058 analysis focused on the more energetic along-transect component, as shown in Figs. A2-A4. The vertical structure
 1059 of this velocity component was found to be coherent with the modal M₂ energy flux patterns in all analyzed cases.



1060

1061 **Figure A1.** Horizontal propagation of mode-1 M₂ IT beams. Snapshots (at $t = 6$ h) of meridional baroclinic
 1062 velocity for the (a) NE, (b) CEC, and (c) CEE cases. The corresponding dates are 24 November 2015, 17
 1063 September 2015, and 29 September 2015, respectively. All panels include defined transects along different IT
 1064 beams: the northeastward incident beam (yellow) from sites A and D, northward refracted beams from CE core
 1065 (green), and diffracted beams (northward and eastward) from CE periphery (green). Detected eddy edges (closed
 1066 contours) and centroids (dots) for AE (blue) and CE (red) are also shown.

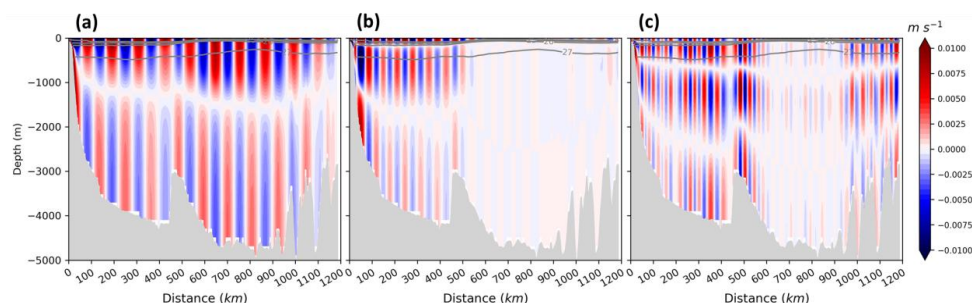


Figure A2. Vertical structure of the first three M2 IT modes in the NE case. Snapshots ($t = 6$ h on 24 November 2015) of the along-transect baroclinic velocity component for modes 1 (a), 2 (b), and 3 (c) along the northeastward incident beam. All panels include selected potential density isopycnals ($23\text{--}27 \text{ kg m}^{-3}$, grey contours), and the seafloor topography (grey shading).

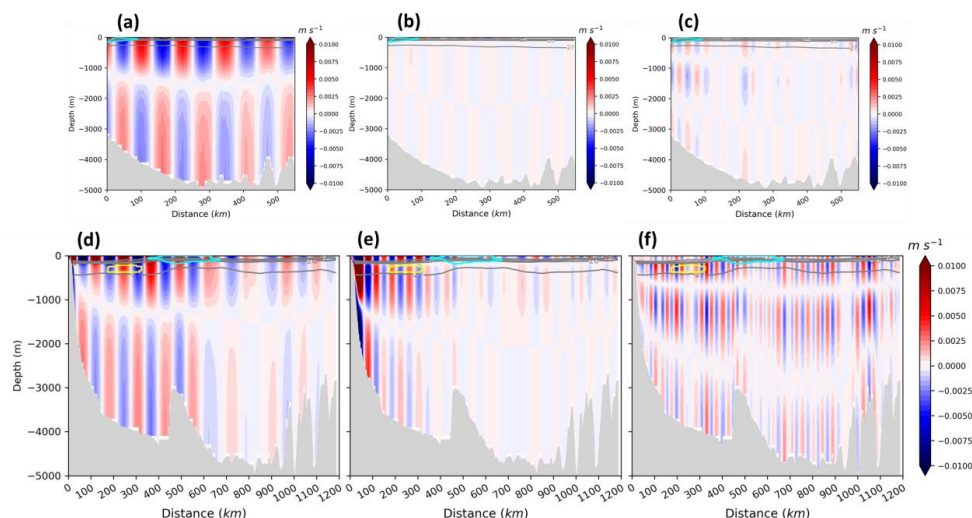


Figure A3. Vertical structure of the first three M2 IT modes in the CEC case. Snapshots ($t = 6$ h on 17 September 2015) of the along-transect baroclinic velocity component for modes 1 (a, d), 2 (b, e), and 3 (c, f) along different beams: the northward diffracted beam (a-c) and the northeastward incident beam (d-f). All panels include detected eddy edges for AE (yellow) and CE (cyan), selected potential density isopycnals ($23\text{--}27 \text{ kg m}^{-3}$, grey contours), and the seafloor topography (grey shading).

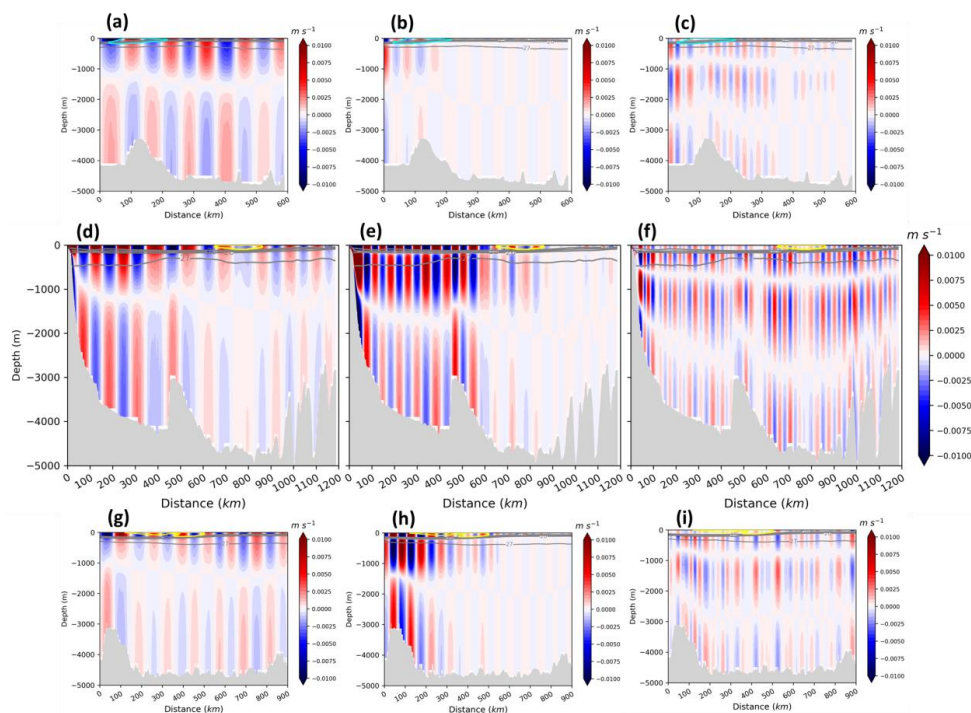


Figure A4. Vertical structure of the first three M2 IT modes in the CEE case. Snapshots ($t = 6$ h on 29 September 2015) of the along-transect baroclinic velocity component for modes 1 (a, d, g), 2 (b, e, h), and 3 (c, f, i) along different beams: the northward diffracted beam (a-c), the northeastward incident beam (d-f), and the eastward diffracted beam (g-i). All panels include detected eddy edges for AE (yellow) and CE (cyan) eddies, selected potential density isopycnals ($23\text{--}27\text{ kg m}^{-3}$, grey contours), and the seafloor topography (grey shading).