

Responses to Reviewer's Comments for Manuscript egusphere-2025-620

In Situ Monitoring of Seasonally Frozen Ground Using Soil Freezing Characteristic Curve in Permittivity-Temperature Space

TC

Authors' Response to Reviewer 2

Reviewer #2's comment

I must confess I've had difficulties understanding the goal of the work presented in the manuscript. After having read what is presented as "advancement [that] addresses a critical gap in cold regions science", I still do not know what new things I have learned, and what is the purported breakthrough. As the remote sensing community appears to be one of the target users of this innovation, what exactly should they do differently now, and how?

Response:

We appreciate the reviewer's observation and agree that the original version did not clearly convey the study's goal and contribution. We have substantially revised and restructured the manuscript to clarify our objectives and avoid overstating the novelty. Our goal is now explicitly stated: we applied the Soil Freezing Characteristic Curve (SFCC) directly in *permittivity-temperature space* to enable continuous, in-situ monitoring of seasonally frozen ground using dielectric sensors, without the need for calibration to estimate liquid or ice water content. This approach allows direct use of field measurements in terms of dielectric permittivity, which is already the primary observable in most soil moisture probes. While SFCC models are well established, their long-term, in-situ application across diverse Canadian ecozones remains scarce. Our study therefore contributes a multi-year, multi-network dataset (87 sites across 8 monitoring networks) that provides hourly probabilities of soil freezing and associated continuous soil-state classifications.

The revised manuscript clarifies that our contribution does not introduce new physical concepts of soil freezing, but rather applies the well-established SFCC to field observations to monitor soil states *in situ*. The resulting dataset provides high-temporal-resolution ground-truth data that can directly support the remote sensing community in evaluating and training freeze-thaw retrieval algorithms. Current validation practices typically rely on air temperature (often from land surface models) or soil temperature measurements

alone (see the next comment for further details), which overlook the transitional, partially frozen states that persist across all our networks—particularly within the eastern boreal forests of Canada.

Specific revisions made:

- The title was changed to accurately reflect the study’s focus without overstating its novelty.

Modified text in manuscript (Title):

~~Improving In Situ Monitoring of~~ Seasonally Frozen Ground ~~Monitoring~~ Using Soil Freezing Characteristic Curve in Permittivity-Temperature Space

- The *Abstract*, *Introduction*, *Results*, and *Conclusion* sections were rewritten and reorganized to more clearly articulate our objectives, workflow, and findings, and to better support the revised narrative. For brevity, we include the revised *Abstract* below as an example, while the corresponding sections (*Introduction*, and *Results*) have been fully revised in the manuscript and can be consulted there for detailed changes.

Modified text in manuscript (Abstract):

Frozen ground, a key indicator of climate change, profoundly influences ecological, hydrological, and carbon flux processes in cold regions. ~~However, traditional monitoring methods, which rely on a binary 0°C soil temperature threshold, fail to capture the complexities of soil freezing, such as freezing point depression and transitional states where water and ice coexist. This study introduces a framework that fits a theoretical Soil Freezing Characteristic Curve (SFCC) in permittivity-temperature space to site- and cycle-specific~~ The Soil Freezing Characteristic Curve (SFCC), which defines the relationship between liquid water content and subzero temperatures, provides a framework for understanding soil freezing processes. However, accurately measuring liquid water content in frozen soils under field conditions remains challenging. We therefore recast an empirical SFCC model into permittivity-temperature space and fitted it to in situ measurements ~~. This approach enables the quantification of the degree of soil freezing and the classification of soil states as frozen, unfrozen, or in transition (partially frozen). We analyzed 135 freezing cycles from~~ from eight monitoring networks (87 sites, each equipped with permittivity-based soil moisture probes. These sites are part of eight monitoring networks spanning diverse Canadian landscapes, including eastern boreal forests (Montmorency Forest, La Romaine, James Bay, Chapleau), western boreal forests (Candle Lake), prairies (Kenaston sites) spanning Canadian boreal forests, prairies, and tundra ecozones, encompassing 96 freezing cycles measured with three sensor types (HydraProbe, TEROS12, and CS616). Using Bayesian hierarchical partial pooling, we derived stabilized estimates of key SFCC parameters: the freezing onset temperature (T_f) and the shape factor (b), which controls transition sharpness. Network-level T_f ranged from 0.15 to 0.44°C, while b varied from 0.92 to 3.47 °C⁻¹, reflecting distinct freezing regimes across ecozones. During the six-month freezing season (1 September–1 March), the James Bay (BJ), Montmorency Forest (FM), Chapleau (CP), and ~~tundra regions (Trail Valley Creek~~

and George River). On average, eastern boreal forest sites exhibited prolonged unfrozen and transitional states due to high soil moisture retention and insulation from snow and vegetation cover (23 frozen days, 46 transitional days). La Romaine (LR) networks, located in eastern boreal forests with thick organic layers and high moisture, remained predominantly unfrozen (70 days) or in transitional states (110 days) throughout winter despite persistent snow cover (> 90%) and subzero air temperatures. In contrast, western boreal forest sites experienced more extensive freezing under drier conditions (73 frozen days, 76 transitional days). Prairie sites displayed equal durations of frozen and transitional states (71 days each), while tundra sites had the longest frozen periods (145 frozen days, 52 transitional days). Notably, transitional periods lasted as long as—or even longer than—frozen ones, underscoring the limitations of binary classifications. Furthermore, the traditional 0°C threshold misclassified transitional soil states, overestimating frozen days by over 87% in prairie and western boreal regions, and unfrozen days by 86% in the eastern boreal forest. In tundra, the bias was more balanced, with 64% and 36% of transitional days misclassified as unfrozen and frozen, respectively. This SFCC-based framework enhances seasonally frozen ground monitoring, offering deeper insights into soil freeze-thaw dynamics. These advancements have implications for improving climate change assessments, refining carbon flux models, the Trail Valley Creek (TV) and training and validating remote sensing products. Additionally, the resulting database of soil states from this study provides a valuable resource for advancing frozen ground research, particularly in remote sensing and ecosystem modeling efforts. George River (GR) networks, located in tundra, exhibited prolonged frozen conditions (115 days) under extreme cold, though GR's higher moisture delayed freezing relative to TV under similar air temperature conditions. The Candle Lake (BT) network, located in western boreal forest, and the Kenaston (KN) network, located in prairies, showed intermediate responses, with BT experiencing 90 frozen and 30 transitional days, and KN averaging 70 frozen and 60 transitional days despite comparable air temperatures to the eastern boreal networks. These contrasting patterns reflect the combined effects of insulation layer such as snowpack, vegetation canopy, litter, and organic layers, together with moisture rather than air temperature alone, demonstrating how ground surface properties modulate soil thermal regimes. This framework provides a reproducible field-based approach to quantify seasonal surface soil freezing processes and a dataset for model and remote sensing evaluation.

- The *Conclusions* section was simplified to directly state how this study supports remote-sensing applications rather than presenting it as a conceptual breakthrough.

Modified text in manuscript (Conclusions):

This study applied an SFCC in permittivity-temperature space to enable robust monitoring of frozen ground states using standard dielectric sensors, transitional, and unfrozen days. Such a perspective provides a dynamic and accurate representation of soil without the calibration challenges inherent in estimating liquid water content. The key insight from our multi-network analysis is that variations in freezing behavior are dominated by local ground surface properties rather than regional air temperature patterns. Importantly, the transitional (partially frozen) state accounts for the majority of the freezing season in eastern boreal networks and persists for at least one month even in western boreal and tundra networks—dynamics that binary frozen/unfrozen classifications fail to capture. These findings reinforce that air temperature alone cannot predict frozen ground extent, demonstrating that remote sensing products and land surface models must account for spatial variations in ground surface properties to accurately represent freeze-thaw behavior, acknowledging the frequent transitions and short-term fluctuations that occur in natural settings. This finer-scale approach more closely aligns with the actual processes

~~taking place in the soil, allowing for improved monitoring and understanding of seasonally frozen ground conditions.~~

~~This study introduces a new framework for seasonally frozen ground monitoring that moves beyond the traditional binary classification approach, offering a more nuanced understanding of soil freeze-thaw dynamics at regional scales. The practical value of this approach lies in its compatibility with widely deployed sensor networks and its systematic, straightforward methodology for constructing SFCCs from in situ measurements. Numerous soil monitoring networks across cold regions (e.g., RISMA, SNOTEL, AmeriFlux) already measure both soil temperature and dielectric permittivity. These existing infrastructures could readily adopt the methodology presented in this study to monitor seasonally frozen ground. This is particularly important given the rapid warming of high-latitude regions and the need for ground-truth evaluation of satellite-based freeze-thaw products, which currently rely primarily on air or soil temperature observations for training and evaluation (Rautiainen et al., 2025; Donahue et al., 2023; Roy et al., 2020; Kou et al., 2017; Gao et al., 2016). By integrating in situ soil temperature and permittivity measurements through an SFCC model, we can now quantify the degree of soil freezing and identify crucial transitional states—a capability particularly valuable for understanding shoulder season processes and carbon flux dynamics. This advancement addresses a critical gap in cold regions science, where accurate characterization of soil states directly impacts our understanding of hydrological processes, ecosystem responses, and carbon cycling. The framework’s ability to detect and quantify transitional states, which we found can persist as long as fully frozen periods, has significant implications for improving climate models, particularly their representation of shoulder season biogeochemical processes. Additionally, this methodology provides a robust foundation for validating and improving remote sensing products, potentially enabling more accurate regional and global assessments of frozen ground conditions. Looking forward, this approach opens new avenues for integrating ground-based observations with satellite data, ultimately advancing our ability to monitor and predict cold region responses to climate change.~~

We believe these changes now make the purpose, scope, and value of the study transparent to both the cold-regions and remote-sensing communities.

Reviewer #2's comment

As far as I understood, one of the reported ‘novelties’ is that the soil moisture doesn’t switch from fully unfrozen to fully frozen at 0 °C. This is elementary knowledge in physics and in permafrost science. Additionally, I am presented with evidence that dielectric permittivity, which relates to unfrozen soil moisture fraction, changes gradually over a range of temperatures. Once again, what is the novelty of this?

Response:

We agree with the reviewer that the gradual nature of soil freezing and the existence of partially frozen states are well-established in cold-region science and permafrost research. These concepts are not the novelty of our study. Our intent in the original manuscript was to highlight a gap between established cold-region science and current remote-sensing evaluation practices. Many remote-sensing freeze-thaw studies—from early work (Kim et al., 2011; Zhang and Armstrong, 2001) to recent applications (Taghipourjavi et al., 2024; Gao et al., 2020; Kou et al., 2017; Roy et al., 2020; Derksen et al., 2017)—rely on 0°C soil or air temperature thresholds for training and evaluation, without accounting for partially frozen states. Only recently have researchers begun integrating soil moisture, temperature through SFCCs into freeze-thaw model evaluation (Rautiainen et al., 2025). Our study demonstrates that transitional (partially frozen) states are comparably significant to fully frozen and unfrozen states across our networks; indeed, our eastern boreal networks never reached complete freezing during our observation period. However, we acknowledge that emphasizing these well-known physical principles in the Introduction distracted from our actual contribution.

To address this, we made the following revisions:

- **Deleted** the paragraph in the *Introduction* that overstated the gradual-freezing concept. Based on the revised narrative of our study, this paragraph no longer aligns with our objectives, and removing it helps focus readers on our actual contribution.

Modified text in manuscript:

~~Traditionally, the state of the soil has been defined through a single measurement of soil temperature within the top few centimeters of the ground (Andersland and Ladanyi, 2003). Soil is labeled as frozen if the soil (or air temperature) is below 0°C and unfrozen if above. This approach is widely used in numerous studies, particularly in remote sensing, to monitor seasonally frozen ground conditions (Kim et al., 2011; Taghipourjavi et al., 2024; Zhang and Armstrong, 2001; Gao et al., 2020; Kou et al., 2017). However, the soil freezing and thawing process is not binary, and using a single threshold of 0°C—the freezing point of pure water—is not sufficiently accurate (Pardo Lara et al., 2020; Mavrovic et al., 2020). In natural environments, soil typically begins to freeze at temperatures below 0°C (Dobiński, 2020), a phenomenon known as soil freezing point depression, which occurs due to adsorption, capillary action, adhesive and cohesive forces, and osmotic effects (Tian et al., 2014; Bouyoucos and McCool, 1915). Moreover, freezing occurs over a range of temperatures due to the presence of various types of water in the soil—hygroscopic (unfreezable) water, capillary water, water in soil pores, and gravitational water—all of which behave differently during freezing. This diversity creates a transitional zone where water and ice coexist, challenging the traditional binary classification (Tian et al., 2014; Zhang et al., 2019; Bouyoucos and McCool, 1915).~~

~~Considering soil freezing point depression, rather than 0°C threshold, would enhance the accuracy of detecting the soil's state, thereby minimizing false positives and negatives in assessments. Additionally, detecting the transitional period is crucial for accurately determining “zero curtain” periods. The zero curtain, observed during shoulder seasons, is a phase when soil temperatures hover around the soil's freezing point regardless of air temperatures. This period is critical as the soil's near-freezing temperature sustains microbial activity (Schimel and Mikan, 2005), significantly impacting carbon dioxide fluxes (Arndt et al., 2023). Studies show that carbon emissions during the zero curtain in the fall can match or exceed those of the rest of winter (Arndt et al., 2023; Mavrović et al., 2023). Furthermore, an observed increase in the duration of the zero curtain period extending into the fall and winter seasons leads to higher carbon emissions during the non-growing season, underscoring the importance of accurately identifying these periods (Arndt et al., 2023).~~

- **Removed** all language throughout the manuscript that could be interpreted as claiming discovery of partial freezing behavior.
- **Reframed** our contribution as providing a practical and systematic framework for constructing SFCCs from in situ dielectric measurements across diverse environmental settings, rather than introducing a new physical concept.
- **Expanded** the discussion of environmental factors (e.g., organic matter and snow cover) regulating freezing behavior, which are directly relevant to our study's focus on field-based monitoring.

These changes ensure that the revised manuscript correctly reflects that the novelty lies in the operational implementation of SFCC-based monitoring at multiple Canadian sites, not in the fundamental physics of soil freezing.

Reviewer #2's comment

The authors repeatedly make the claim that there exists so called “traditional binary approaches” to describing soil frozen state, and “traditional monitoring methods, which rely on a binary 0 °C soil temperature threshold”. I may not fully understand which approaches are referred to as “traditional”. In my knowledge, now for decades in permafrost science and monitoring, we have not been limiting the description of ground state to frozen or unfrozen and in fact, great efforts have been directed to quantitatively and accurately describe soil partially frozen state. I think this

misunderstanding could be because the authors confound two distinct definitions used in permafrost context. [...]

Response:

We appreciate the reviewer’s clarification. By “traditional binary methods,” we intended to refer specifically to *remote-sensing evaluation practices* that classify soil as frozen or unfrozen based solely on temperature thresholds—typically 0 °C from land-surface model or in-situ soil temperature data. As correctly noted, in permafrost and seasonally frozen-ground studies, it has long been standard to distinguish between unfrozen, partially frozen, and fully frozen states using soil-specific freezing and thawing curves.

We have therefore revised the manuscript to remove all references to “traditional binary approaches” and to eliminate any suggestion that this three-state framework is new. As discussed in Comment 2, our intent was to emphasize that, unlike purely thermal classifications, the SFCC approach quantifies the *water-phase composition* of the soil and provides a continuous measure of freezing that can be directly derived from dielectric measurements.

To prevent confusion between the water/ice phase and thermal (cryotic/non-cryotic) definitions of frozen ground, the revised version ensures that our work focuses on the frozen state of the topsoil—where the state of water is the key variable—rather than on the thermal classification commonly used in permafrost mapping. The paragraph in the original *Introduction* that introduced the term “traditional binary” and compared these definitions has been entirely removed (the same paragraph that was discussed in Comment 2), as it was unnecessary and diverted attention from the main objective of our study.

Changes made:

- Deleted the paragraph in the *Introduction* that introduced the “traditional binary” terminology (see previous comment for modified text).
- Removed all remaining instances of the phrase “traditional binary approaches” throughout the manuscript.

- Clarified that the study concerns the monitoring of seasonally frozen ground through SFCCs, not the cryotic/non-cryotic thermal state relevant to permafrost classification.

Reviewer #2's comment

The authors seem to be unaware of evidence contradicting their assumptions about equal freezing and thawing curve patterns in in-situ measurements (Line 153–154). Field studies by Overduin et al. (2006) and Tomaškovičová & Ingeman-Nielsen (2024) showed very strong hysteresis effects in in-situ measurements of unfrozen soil moisture using dielectric permittivity sensors. It is possible that these effects may not be in fact related to real unfrozen water content difference between freezing vs. thawing branches of soil moisture curve at the same temperature (Wu, 2017), but nevertheless, the apparent hysteresis does affect in-situ soil moisture measurements based on electric principles.

Response:

We appreciate this important remark and acknowledge the significance of hysteresis between freezing and thawing curves. We are well aware of this phenomenon, as two of our co-authors have discussed it extensively in prior publications (Pardo Lara et al., 2020; Mavrovic et al., 2020).

In the initial submission, we assumed equivalence between the SFCC (Soil Freezing Characteristic Curve) and STCC (Soil Thawing Characteristic Curve) for the practical purpose of constructing a continuous annual time series of soil freezing probabilities. This assumption was informed by Pardo Lara et al. (2020), who reported weak hysteresis in the uppermost 5 cm of soil, in contrast to fine-grained, saturated permafrost samples where stronger hysteresis has been observed (e.g., Overduin et al., 2006; Tomaškovičová and Ingeman-Nielsen, 2024).

However, we agree that applying the SFCC to thawing periods introduces uncertainty—particularly after snowmelt—when additional water inputs violate the constant

total-water-content assumption required for curve construction. We have therefore revised the manuscript to limit the analysis exclusively to freezing cycles.

To address this comment, we implemented two major revisions:

- **Focused exclusively on freezing cycles:** We now explicitly state in the *Methodology* and *Discussion* sections that only the freezing periods are analyzed. We also clarify that reliable STCCs could not be constructed *in situ* due to hydrological inputs during thawing, especially from snowmelt, which invalidate the closed-system assumption of the SFCC model.

Modified text in manuscript (Methodology – data preprocessing):

.... Specifically, any fluctuations within $\pm 2\sigma_T$ of 0°C , where σ_T represents the instrument-specific temperature uncertainty, were ignored (see Appendix ?? for details on sensor uncertainty). If, during a freezing cycle, the soil temperature never dropped below the $-\sigma_T$ threshold and ε_{eff} remained relatively unchanged, we classified these sites as never frozen. Although curve fitting was not feasible for these ~~sites~~ cycles due to insufficient data in Zones 2 and 3, they were retained for ~~further analysis to investigate the freezing process across our monitoring networks. In this analysis, we~~ subsequent analysis of freeze monitoring across our networks. We assumed that the total water content in the system remained equal to the initial water content and did not change during the freezing or thawing processes (He and Dyck, 2013). We monitored ε_{eff} throughout both freezing and thawing cycles to validate this assumption. We interpreted significant, sudden surges in ε_{eff} as indicators of additional water entering the system, violating this assumption. Consequently, we excluded such cycles from further analysis. While this assumption generally held during freezing cycles, it was often invalid during thawing cycles, primarily due to snowmelt introducing substantial amounts of water into the soil. As a result, the SFCC could be reliably constructed for freezing cycles, but constructing the STCC from in situ measurements during thawing cycles was ~~often~~ not feasible. ~~Since this study aimed to use site- and cycle-specific SFCC/STCC to determine the degree of soil freezing and classify soil states, we applied the SFCC from each freezing cycle to the subsequent thawing cycle at the same site. Although differences between SFCC and STCC—primarily driven by hysteresis effects—are pronounced in laboratory settings, previous studies (Pardo Lara et al., 2020; Mavrović et al., 2020) found no visually discernible differences in situ. We assumed that the SFCC could reliably represent the STCC until a significant change in total soil water content, marked by a sudden surge in ε_{eff} , which approximately corresponds to the snowmelt event. To assess the reliability of applying the SFCC for thawing cycles, we evaluated its performance over the full thawing cycle and up to the snowmelt date. Therefore, in this study we focused exclusively on freezing cycles, excluding thawing cycles from further analysis.~~

Modified text in manuscript (Discussion – exclusion of thawing period):

The thawing cycles, however, were not analyzed in this study because constructing the STCC from in situ measurements is not reliably feasible. During thawing, snowmelt and rainfall introduce additional water into the soil, violating the constant total water content assumption required for curve development

- **Added explicit literature review of hysteresis (Introduction):** A new section was added to the *Introduction* acknowledging the occurrence of hysteresis

and referencing the key studies mentioned by the reviewer (Overduin et al., 2006; Tomaškovičová & Ingeman-Nielsen, 2024).

Modified text in manuscript (Introduction – hysteresis):

[...] especially under field conditions. The hysteresis between SFCC and STCC has been widely documented, particularly under laboratory conditions (Mavrovic et al., 2020; Pardo Lara et al., 2020; Wu et al., 2017) In situ studies, such as Tomaškovičová and Ingeman-Nielsen (2024), reported approximately 10% higher unfrozen water content during freezing than during thawing at equivalent temperatures under saturated, fine-grained permafrost conditions, reflecting latent heat effects, cryosuction, and slow pore-water redistribution. Similarly, Overduin et al. (2006) documented asymmetric freezing-thawing transitions in saturated silty clays caused by latent heat and moisture migration. By contrast, near-surface, non-permafrost measurements (Pardo Lara et al., 2020) found hysteresis to be theoretically expected but generally weak or indistinguishable.

Together, these revisions ensure that the revised manuscript explicitly addresses hysteresis effects, properly defines the scope of our analysis, and justifies the exclusion of thawing periods to maintain methodological consistency.

Reviewer #2's comment

Conclusion is made that the presented work will improve monitoring of permafrost, but it is unclear to me if this is for field or remote-sensing monitoring. The authors mention only field measurements, and they don't seem to make the link to the remote-sensing applications. For improving field measurements, again, the claim seems stretched, especially when insisting on the "binary classification" of soil moisture state.

Response:

We initially had some difficulty understanding this comment, as our study specifically addresses seasonally frozen ground, and the term permafrost is not mentioned anywhere in the manuscript. That said, we agree with the reviewer that certain statements in the original version may have been overstated. The study is primarily focused on *in-situ monitoring of seasonally frozen ground* across different Canadian ecozones using the SFCC framework. The revised version now ensures that our main focus remains on

field-based observations and analysis rather than on improving soil freezing monitoring in general.

We have also revised the *Conclusions* section to clearly state how the dataset generated from this study can support remote-sensing validation practices. Specifically, the dataset provides ground-truth information that includes transitional (partially frozen) states, which are often underrepresented in current evaluation datasets that rely mainly on air/soil temperature measurements. This clarification better links our in-situ work to its practical application in remote-sensing contexts.

Changes made:

- Removed overstated claims about “improving monitoring.” The title was updated to emphasize the study’s focus on in-situ monitoring.
- Clarified throughout that this work is a field-based study and not intended to improve soil freezing monitoring directly.
- Revised the *Conclusions* section to explicitly mention the dataset’s relevance for remote-sensing evaluation, highlighting its inclusion of transitional soil states.

Modified text in manuscript (Conclusions excerpt):

This is particularly important given the rapid warming of high-latitude regions and the need for ground-truth evaluation of satellite-based freeze-thaw products, which currently rely primarily on air or soil temperature observations for training and evaluation (Rautiainen et al., 2025; Donahue et al., 2023; Roy et al., 2020; Kou et al., 2017; Gao et al., 2020).

Reviewer #2’s comment

Another conclusion claims to be able to quantify the degree of soil freezing. However, I do not see evidence of quantitative analysis in the work which appears limited to the qualitative description of soil as unfrozen, transitional and frozen.

Response:

We appreciate this observation and acknowledge that our initial manuscript did not sufficiently highlight the quantitative nature of our approach. In the revised version,

we clarify that the *freezing probability* represents a continuous, quantitative measure of the degree of soil freezing. This probability is derived by propagating uncertainty from the hierarchical posterior distributions of T_f and b through the normalized SFCC formulation.

To make this explicit, the following revisions were implemented:

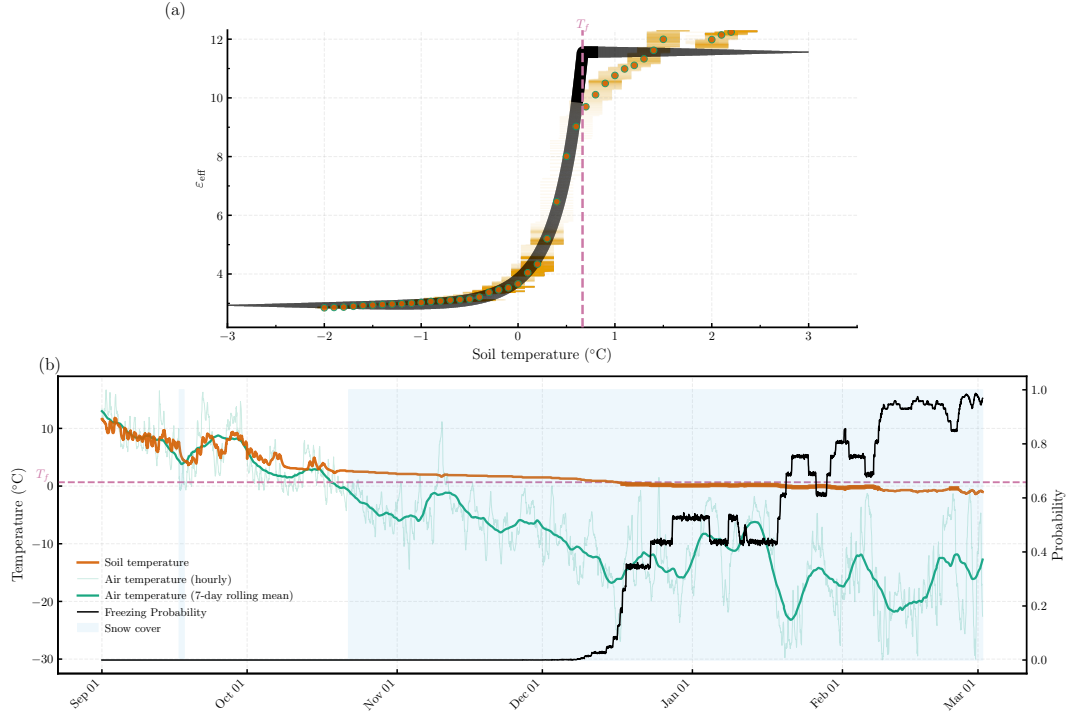
- **Revised Methodology Section (Probability of Frozen Ground)** to more clearly and concisely describe how P_{frozen} is computed and interpreted as a quantitative measure of soil freezing.

Modified text in manuscript - methodology:

The probability of frozen ground (hereafter referred to as the freezing probability), which can also be interpreted as the degree of soil freezing at the network level, was computed by propagating uncertainty from the hierarchical posterior distributions of T_f and b . For each network, paired posterior samples $\{(T_f^{(s)}, b^{(s)})\}_{s=1}^S$ were drawn from the *PyMC* hierarchical models, where $b^{(s)} = \exp(b_j^{(s)})$ restores the parameter to its original scale. Soil temperature observations were perturbed according to sensor uncertainty, $T_{\text{sim}}^{(s)} \sim \mathcal{N}(T_{\text{obs}}, \sigma_T^2)$, where σ_T was assigned based on the sensor type. For each posterior draw, the freezing probability was evaluated using the normalized SFCC, and the results were averaged across all Monte Carlo samples to obtain the mean freezing probability at each timestamp.

- **Updated Figures 6–9** to display time series of freezing probability alongside soil and air temperature, visually emphasizing its continuous and quantitative nature.

Modified figure in manuscript (Results):



- **Clarified the Results section** to explain that the framework enables quantitative comparison of soil freezing behavior across networks and ecozones.

These clarifications ensure that readers can recognize P_{frozen} as a quantitative metric of soil freezing rather than a qualitative classification.

Reviewer #2's comment

Additionally, there appear to be a number of misconceptions, or perhaps poorly presented concepts, reiterated throughout the manuscript. For example, the concept of zero curtain (isothermal process of phase change between water and ice) appears to be confounded with the transitional zone, which encompasses a wider temperature (and liquid water content) range, based on Figures 6–10.

Response:

We agree with the reviewer's observation. In the revised manuscript, we ensured that the concepts of the *zero curtain* and the *transitional zone* are clearly distinguished. The

zero curtain refers to the period when soil temperature remains near 0 °C due to latent heat effects during the phase change between water and ice. In contrast, the transitional zone (Zone 2 of the SFCC) represents the broader temperature range over which ice and liquid water coexist, encompassing a wider range of liquid water contents.

To eliminate any ambiguity, the manuscript now focuses exclusively on the transitional state as defined within the SFCC framework. All mentions of the zero-curtain effect have been clarified or removed where they could be confused with the transitional zone.

Changes made:

- Removed or clarified all instances where the zero-curtain and transitional-zone concepts were conflated.
- Focused the discussion on the transitional state as defined by the SFCC framework.
- Ensured consistent and precise terminology throughout the manuscript.

Reviewer #2's comment

“Notwithstanding these remarks, I do think that the dataset seems extremely interesting, and worthy of publication, if adequately exploited.”

Response:

We sincerely thank the reviewer for recognizing the value of the dataset. In the revised manuscript, we have taken several steps to better exploit and present its potential.

Revisions implemented:

- **Applied Bayesian hierarchical partial pooling** to derive more stable parameter estimates across sites and networks within ecozones.
- **Revised the Conclusions section** to clearly emphasize the dataset's potential applications in model development and remote-sensing validation.
- **Committed to publishing the dataset publicly** following manuscript acceptance to facilitate its reuse by the broader cold-regions and remote-sensing communities.

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