

Response to Reviewers: Dry and moist convective upper bounds for near-surface temperatures

Summary for the reviewers and the editor:

We thank both reviewers for their positive and encouraging comments. Reviewer 2 expressed some concerns about the way we framed the implications of the manuscript: our work points out a shortcoming of the approach of Zhang & Boos (2023) in the limit of very dry surface air, and suggests focusing on PBL properties in order to obtain a universal bound on surface temperatures in such cases. Yet, this approach has been extensively taken in previous heatwave studies, especially in the land-atmosphere interactions community. We have made extensive changes to the first part of our discussion in order to clarify this point, better acknowledge existing literature on PBL growth during heatwaves, and provide potential avenues forward. These changes are reviewed below in our point-by-point answer to Reviewer 2.

During the course of the review, we received offline comments from Yi Zhang and William R. Boos (who authored the study which inspired this work, and with whom we had shared the study before the original submission). These comments targeted the way we were framing our discussion of their theory. Specifically, the original submission presented their theory as relying on two hypotheses that were contradictory. They presented us with a formulation of the theory which deviates from our interpretation, and does not result from a logical contradiction. This alternative formulation is still inconsistent with the data presented in section 4 (where we analyze profiles that exceed the dry adiabatic bound), so the main conclusions drawn from section 4 and the discussion are unaffected. We have added a paragraph at the end of Section 3.3 to discuss this interpretation of ZB23's theory, and changed a couple of instances where the theory was labeled "contradictory" or "inconsistent". We apologize for the unprompted changes that this exchange resulted in.

Below are our responses to the reviewer comments and our description of the corresponding changes to the manuscript. The reviewer comments are indicated in black and our responses are in blue font.

Reviewer 1

"Dry and moist convective upper bounds for near-surface temperatures" by Nicolas and Hotz explores the constraints imposed by atmospheric convection on how hot near-surface air can get. This study follows recent influential papers on these "upper bounds", notably by Zhang & Boos (2023). The authors follow a similar approach to Zhang & Boos and assume that the temperature at the upper bound is realised when the atmospheric column becomes statically unstable. A typical bulk measure of stability is used, namely the difference between near-surface moist static energy (MSE) and saturation MSE at the 500 hPa level (a more accurate formulation in terms of potential temperature is also presented).

The study highlights an important inconsistency in the Zhang & Boos formulation that results in a non-trivial effect on the upper bound. Specifically, the authors highlight that two assumptions

embedded in the Zhang & Boos framework – of zero near-surface specific humidity and a lifted condensation level below 500 hPa – are inconsistent with each other. An alternative upper bound on near-surface temperature (limited by dry convection), which reconciles these inconsistencies, is derived and is shown to better capture daily maximum temperatures over NH extratropical land in ERA5. The authors also introduce an additional upper bound which is determined by moist convection and is only relevant when near-surface specific humidity is large enough so that an adiabatically-lifted parcel reaches saturation below 500 hPa. Taken together, these new upper bounds derived by Nicolas and Hotz represent a significant advance in our understanding of how convection limits heat extremes. The authors then explore why a non-negligible fraction of days can exceed the theoretical upper bound and highlight the importance of deep boundary layers and super-adiabatic lapse rates very close to the surface. This latter effect is under-explored for heatwaves and the manuscript neatly sets up the problem of understanding the physics of these super-adiabatic layers as a key next question in this line of research.

This is an excellent paper: exciting new results on an important topic; interesting ideas for next steps which I believe will be influential in shaping the field over coming years; and very well written and presented, with physical mechanisms explained clearly. I recommend publication 'as is'.

We thank the reviewer for the very kind words of appreciation. The study has undergone some changes during the review process, but the main elements you quote (except perhaps the “inconsistency” wording for ZB23’s derivation) are all still present.

Reviewer 2

Summary:

The authors revisit a moist convective upper bound for near-surface air temperatures proposed by Zhang and Boos (2023, ZB23), identifying an important inconsistency in their argument: their upper bound takes surface specific humidity to be zero, but that implies the lifting condensation level must exceed 500 hPa, contradicting another assumption. In attempting to correct this inconsistency, the authors show that, logically, the upper bound should be instead set by dry convection but, in fact, the resulting dry convective upper bound is regularly exceeded in dry and/or high altitude regions. They attribute this to the presence of a superadiabatic layer at the surface, which is ignored by ZB23 and in the derivation of their updated dry convective bound. They further note that the gradient of this layer is proportional to the surface sensible heat flux, which ties this argument back to the surface energy budget. They conclude by noting that the structure of dry convective boundary layers and resulting bounds on heatwaves depends strongly on land surface properties.

Major comments:

This is an interesting and well-written study. The authors clearly explain the inconsistency in ZB23 and make a compelling argument that I find persuasive. I support publication with minor revisions. That said, the paper could be improved in various ways.

I like the study but it is, to some extent, a victim of its own success. It has clearly shown a major problem with ZB23's upper bound. To recap, ZB23's upper bound was surprising because it provided an upper bound for heatwaves purely from free-tropospheric observations. That was somewhat surprising since it is well-known that land surface properties – in particular, dry soils – are very important in attaining the highest temperatures during heatwaves. Their upper bound strongly implied a “top down” control on heatwaves that dominated land surface controls, which was both elegant and practically useful, since the land surface is much messier and poorly understood than the free troposphere, in general. In contrast, the authors conclude here that (line 327) “in such conditions [arid and/or high altitude], T500 may not reliably be considered an external control on surface temperature – understanding the dynamics of PBL growth over dry surfaces may be a more fruitful approach to bounding heatwave intensities in such cases.” This is a more traditional “bottom up” view, in which the details of the land surface are extremely important; but that is also less interesting, since there is a large literature that already makes that point and takes that approach. The authors should more comprehensively review that literature, particularly the many studies that couple a surface energy budget to a bulk mixed layer model to study heat extremes (e.g., Miralles et al. 2014, van Heerwaarden and Teuling 2014, Stap et al. 2014). The authors should also discuss and cite Garratt (1992), which looks at upper bounds on land surface temperatures from the perspective of the surface energy budget, although with a focus on land surface temperature rather than near-surface air temperature, and without coupling the surface energy budget to the PBL.

My question for the authors is: what is learned from this study, beyond the problems identified with ZB23 (which are certainly novel, but apply narrowly to that one prior study) and beyond what is already known in the literature (especially since we already know that land surface properties dictate the magnitude of the superadiabatic layer and are a major control on heatwaves)? What results hold the most lasting value? I encourage the authors to reflect on these questions in revising the manuscript so that the study receives the attention it deserves.

We thank the reviewer for their thoughtful and helpful comments. These comments made us realize that we had overlooked part of the literature on the interaction between the land surface and the convective boundary layer, and that our discussion and conclusions needed better framing. We have extensively modified the first part of the discussion and changed part of the conclusions, taking into account all of the points raised, and believe that the resulting text better describes the new elements and the limits of our study, as well as potential next steps.

The central point of the study remains the problem identified with ZB23 in the limit of dry surfaces. This result is, of course, only relevant to one prior study, but we believe that it is important to clarify the mechanics of these upper bounds based on convective stability

assumptions, as they have gained traction in recent years. In particular, one of the contributions of the paper is to clearly state under which conditions different kinds of upper bounds can be applied, as well as to clarify the processes that can lead these bounds to be exceeded (section 5.2 and conclusions).

However, as correctly identified by the reviewer, we do not provide an alternative upper bound valid for dry cases: the dry upper bound relies on T_{500} , which itself becomes slaved to T_s for very deep boundary layers, and we do not give a bound on the strength of the superadiabatic layer. The original discussion perhaps did not emphasize this enough, and we have modified it to better reflect potential ways forward.

Specifically, we have described the two views of heatwaves based on “bottom-up” and “top-down” controls, and clarified that one of the conclusions of our study is a breakdown of the “top-down” view for very dry heat extremes. We have also clarified the fact that our study does not provide an upper bound for dry heat extremes (because of superadiabaticity and surface control on T_{500}), but we discuss two complementary avenues for deriving such a bound: the search for a maximal reachable PBL depth, and the search for a bound on superadiabatic layer strength.

For the first avenue, we now extensively review the “bottom-up” literature on land-PBL coupling and PBL growth over dry surfaces, including the studies the reviewer suggested. However, we point out that the vast majority of these studies look at the processes that grow the PBL, and not those that can arrest its growth. Does the PBL keep growing *ad infinitum* in dry heatwave conditions, or does it always lead to cloud formation after a long enough time? Can it reach a radiative–dry-convective equilibrium? Such questions are all valuable research directions.

For the second avenue, we believe that little focus has been placed on superadiabatic layer strength in the context of heatwaves. Many studies using a bulk model of the convective boundary layer do not include a superadiabatic layer, and studies using single-column or more complex models do not put much emphasis on it. We have kept our discussion of the controls on superadiabatic layer strength but slightly modified it to recognize that the main control, i.e. the surface sensible heat flux, is itself relatively well understood thanks to a vast body of land-atmosphere studies.

We hope that this new framing of our discussion (also reflected in the last paragraph of our conclusions) better conveys the main takeaways and limitations of our paper, and thank the reviewer again for raising these points.

Specific comments:

Abstract: “We show that these occur exclusively in regions where daytime superadiabatic layers develop near the surface and the boundary layer top reaches deep into the mid-troposphere.” I suggest adding “..., as is common over dry land surfaces” or similar, so that readers are not left

with the impression that daytime superadiabatic layers are mysterious or a novel finding of the study. It is well understood that they should arise near dry land surfaces.

Done.

Abstract: “Our work underscores the need for a finer understanding of the structure of dry convective boundary layers to constrain the intensity of future heatwaves.” It would be good to more explicitly note the need for better understanding of land surface properties relevant to heatwaves – this is in stark contrast to ZB23 and their top down perspective. And, land surface properties are the major source of uncertainty in understanding dry convective boundary layers, anyway.

We have modified the sentence to read “*Our work suggests that deriving physical limits on boundary layer depth and superadiabatic layer strength, two quantities largely influenced by land surface properties, may better help constrain the intensity of future dry heatwaves.*”. This way, it is more precise and includes the mention of land surface properties required by the reviewer.

Line 157: “Under the assumption that T_s is limited by the onset of convective instability, ...” Given the authors’ findings, how warranted is this assumption now? ZB23 argued that the onset of moist convective instability triggered rainfall, which acted to reduce surface temperatures. In contrast, dry convective instability needn’t trigger rainfall over land. I know that the authors are aware of this, and to some extent are simply working through the implications starting from the arguments of ZB23, but it would be good to more clearly make those caveats as the argument progresses.

There are two different implications behind this comment: the first one is that temperature profiles with significant convective instability do exist, and the second is that the presence of convective instability does not necessarily negatively feedback on surface temperature.

Concerning the first point, we have added a sentence at the beginning of section 5.1 (l. 244–248) explaining that this assumption breaks down in many cases: “*There are two issues with [the dry upper bound] [...] Second, the assumption of convective neutrality does not always hold, leading it to be exceeded by up to 8 K in ERA5 and 5K in the observations we considered.*”

Our analysis does not directly touch on the second point, as we do not look at the temporal evolution of temperature profiles during dry heatwaves. We have nevertheless acknowledged the fact that the processes limiting temperature increase in dry cases remain unknown, in the second-to-last paragraph of section 4 (l.219–222), and in the second-to-last paragraph of section 5.1.1 (l.274–278).

Figure 1: please make the grey and black lines thicker so as to more easily discern them from other lines on the Skew-T diagram.

Done.

Line 183: “The profile of Fig. 2b suggests that two conditions are required to exceed the dry adiabatic limit: a deep boundary layer and a strong superadiabatic surface layer.” It would be good to recognize here that decades of prior literature indicates that these two conditions tend to coincide: a strong superadiabatic surface layer typically implies a strong surface sensible

heat flux, which, in turn, implies a high boundary layer, all else equal. This would be predicted by any bulk mixed layer model of the ABL coupled with a dry land surface, and there are many studies that look at this already. The two conditions are not exactly equivalent, of course, particularly if the free tropospheric stability is large, but there is a lot of work already looking at this.

Agreed, and we have added a sentence to that effect in l.202-203. We would argue, though, that boundary layer depth depends on an integral of the sensible heat fluxes over several days, while the superadiabatic layer strength essentially depends on its instantaneous value, hence the conditions are far from equivalent (the correlation coefficient is 0.6 on our ERA5 data).

Line 187: “This suggests that there is a quasi-equivalence between a PBL reaching higher than 500 hPa and dry bound exceedance.” Yes, exactly, which brings me back to my earlier question: since rainfall is not necessarily triggered when the PBL grows higher than 500 hPa, how much relevance does this have to constraining maximum temperatures over land?

As highlighted in our response to your earlier comment (that relative to line 157 of the original manuscript), the revised manuscript now acknowledges this shortcoming of the dry bound, and potential ways forward to constrain near-surface temperatures over land (l.219–222 and 274–278).

References

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