



# 1 Synergistic Fusion of Aerosol Optical Depth over India from Multi-Sensor 2 Satellite Retrievals with Ground-based Measurements

3 Shiba Shankar Gouda<sup>1,2</sup>, Mukunda M. Gogoi<sup>1</sup>, S Suresh Babu<sup>1</sup>

4 <sup>1</sup>Space Physics Laboratory, Vikram Sarabhai Space Centre, ISRO, Thiruvananthapuram,  
5 695022, India

6 <sup>2</sup>Research Centre, Department of Physics, University of Kerala, Thiruvananthapuram,  
7 695034, India

8 Correspondence: Dr. Mukunda M Gogoi ([dr\\_mukunda@vssc.gov.in](mailto:dr_mukunda@vssc.gov.in))

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## 10 Abstract

11 Synergistic fusion of aerosol parameters from multi-sensor measurements (satellite and  
12 ground-based) is crucial for integrating diverse data sources and generating spatially  
13 consistent representations of aerosol distribution for accurate climate impact assessment. In  
14 this study, a two-stage Universal Kriging (UK) framework is employed. In the first stage, UK  
15 is used for spatial interpolation to fill missing values in individual satellite datasets (MODIS  
16 and MISR). In the second stage, Kriging is formulated as a fusion model by incorporating  
17 spatial covariance structures derived from variogram models of the satellite data, thereby  
18 producing fused AOD estimates from both satellite and ground-based (ARFINET)  
19 observations. Following this, seasonal fused AOD maps are generated for winter, pre-  
20 monsoon, and post-monsoon periods. Leave-one-out cross-validation (LOOCV) shows that  
21 the 95% confidence interval ( $\pm 2\sigma$ ) of the fused AOD values accommodate more than 80% of  
22 the ground-based observations, effectively capturing regional variations. This also highlights  
23 the influence of number of ground measurement points in the generation of fused map. To  
24 address this, a Residual Kriging with Machine Learning (RK-ML) approach is explored. The  
25 RK-ML framework captures stable spatial patterns and yields LOOCV scores comparable to  
26 those of the UK method, even under sparse ground-based coverage. These findings  
27 demonstrate the suitability of both UK and RK-ML approaches (with adequate ground-based  
28 observations) for producing reliable and near-instantaneous fused AOD fields over the Indian  
29 region.

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31 Keywords: Aerosol Optical Depth, Universal Kriging, RK-ML, ARFINET, MODIS, MISR

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## 43 1. Introduction

44 Atmospheric aerosols play a significant role in introducing uncertainties into climate change  
 45 projections. Although various factors such as microphysical parameters and chemical  
 46 composition are important, aerosol optical depth (AOD), quantified by the total amount of  
 47 columnar aerosol loading in the atmosphere, is the most critical parameter for understanding  
 48 their climate forcing effects. With advances in technology and retrieval-algorithms, the  
 49 number of satellites and ground-based observations of AOD is increasing. Although satellites  
 50 are known to capture spatial heterogeneity of AOD, there could be bias or uncertainty (Huang  
 51 et al., 2021) compared to ground-based measurements. Even if different satellites observe the  
 52 same aerosol load over the same region nearly at the same time, the retrieved AOD differs  
 53 due to the differences in algorithms, calibration, and resolution of the sensors (Kinne, 2009;  
 54 Schutgens et al., 2020). The geographical complexity also challenges satellites to accurately  
 55 retrieve AOD over highly heterogeneous land surfaces. On the other hand, data from ground-  
 56 based sensors, though sparsely distributed, are more reliable than satellite measurements due  
 57 to improved accuracy of measurement and retrieval procedure (Holben et al., 1998; Moorthy  
 58 et al., 2007). Thus, the discrepancy between various satellite measurements and between  
 59 satellite- and ground-based measurements of AOD is a serious concern in accurately  
 60 characterizing aerosol loading over different parts of the globe (Wong et al., 2013; Sogacheva  
 61 et al., 2020). Some studies have reported that if the correlations between the AOD from  
 62 multiple sensors are sufficiently strong (Liu et al., 2004; Jiang et al., 2007; Prasad and Singh,  
 63 2007), then the ground-based and space-based observations can be used together for optimal  
 64 characterization of aerosol features over a broader region. In this context, there is a growing  
 65 demand for fused products to address limitations and achieve an optimal outcome, thereby  
 66 strengthening reliability of aerosol database (Kahn et al., 2023).

67 Efforts have been undertaken to fuse satellite products from various sensors using multiple  
 68 techniques, such as Single Scanning spread Function (Gupta et al., 2008), Maximum  
 69 Likelihood Estimation (Leptoukh et al., 2007; Nirala, 2008), adaptive weighted estimate  
 70 algorithm (Guo et al., 2013), semi-empirical optical algorithm (Xu et al., 2012), Spatial  
 71 Statistical Data Fusion (Nguyen et al., 2012; Jinnagara Puttaswamy et al., 2014); Ensemble  
 72 Kalman Filter (Li et al., 2020), Bayesian Maximum Entropy (Tang et al., 2016), Neural  
 73 Network Model (Qifang et al., 2005) etc. Among the various data fusion techniques, Kriging  
 74 has gained significant attention for its applicability under Geostatistical framework which  
 75 accounts spatial autocorrelation (Stein & Corsten, 1991; Zhao et al., 2017). The Kriging  
 76 outcomes are also found to be comparable with those from Deep Neural Networks (DNN)  
 77 (Chen et al., 2020; Kadow et al., 2020). Hence, the Kriging methodology has been  
 78 extensively applied and validated across diverse domains within atmospheric research. It has  
 79 also been utilized for spatial mapping of nutrients over oceans (Zhou et al., 2014) and as well  
 80 as in mining, hydrology, electro-magnetic field mapping, and remote sensing image  
 81 processing (Rossi et al., 1994).

82 In this study, we have adapted the Kriging technique to produce optimal fused AOD products  
 83 over India. Previous research over the Indian region has estimated fused AOD from ground  
 84 and satellite based observations using Cressman method, which employs inverse distance  
 85 weighting (IDW), a widely used Geostatistical approach (Pathak et al., 2019). In contrast,



Kriging has long been recognized as a robust and effective Geostatistical technique for spatial estimation (Zimmerman et al., 1999; Shi et al., 2007; Prafull Singh & Verma, 2019) and has been further extended to multi-sensor fusion methods (Lilla and Castrignanò, 2019). While Kriging approaches have been previously applied to fuse AOD over northern India, the amount of ground data included in their studies was limited (Singh and Venkatachalam, 2014; Singh et al., 2016). In this study, AOD measurements carried out from more than 40 ground-based observatories of the Aerosol Radiative Forcing over India Network (ARFINET) are primarily used to supplement the satellite-based observations from Moderate Resolution Imaging Spectrometer (MODIS) and the Multi-angle Imaging Spectro-Radiometer (MISR). Additionally, ground-based AOD data from the Aerosol Robotic Network (AERONET) are utilized to enhance the robustness of the database. In addition to the above, a hybrid approach of Machine Learning and Residual Kriging (RK-ML) has been adapted to counter nonlinear optimal estimation and more reliable fused estimation even in presence of less number of ground based observation.

## 2. Data and Methodology

### 2.1 Ground-based AOD

The ground-based AOD is primarily obtained from ARFINET observations. ARFINET is the largest network of aerosol observatories over south Asia, having continuous measurements across the region since 1985. The spectral AOD measurements in the ARFINET observatories are carried out using a Multi-wavelength solar Radiometer (MWR) and the handheld Microtops Sun photometer. Both these instruments have been extensively inter-compared, and their consistencies have been established (Kompalli et al., 2010). The MWR is built on the principle of filter wheel radiometry. The measurements of direct solar flux using MWR are made at ten narrow wavelength bands centered at 380, 400, 450, 500, 600, 650, 750, 850, 935, and 1025 nm. The AOD is estimated following the Langley Technique (Shaw, 1973; Moorthy et al., 2007; Moorthy et al., 2007) after subtracting the contribution due to molecular scattering and absorption due to O<sub>3</sub> and water vapour from total optical depth. For this, the MWR raw data (voltage readings corresponding to the time of acquisition) for the entire day are split into forenoon and afternoon. If the data span during each half of the day is more than 3 hours, the Langley plot is made separately for both forenoon and afternoon following cloud screening criteria. In order to estimate instantaneous AOD corresponding to each MWR measurement, the time-weighted Langley intercept for the entire day is calculated from the forenoon and afternoon data as

$$LI_{\text{daily}} = (LI_{\text{FN}} * T_{\text{FN}} + LI_{\text{AN}} * T_{\text{AN}}) / (T_{\text{FN}} + T_{\text{AN}})$$

Where,  $T_{\text{FN}}$  and  $T_{\text{AN}}$  are the durations of MWR measurements during the forenoon and afternoon. Based on this, the instantaneous AOD (after correcting the contributions due to Rayleigh scattering, Ozone, and water vapor) is estimated as:

$$AOD_{\text{ins}} = \{(LI_{\text{daily}} - \ln V) / m\} - (\tau_{\text{R}} + \tau_{\text{O}_3} + \tau_{\text{WV}})$$

The typical error in the retrieved AOD is ~ 0.02-0.03 at different wavelengths. The variance of the Langley intercept typically causes an uncertainty of ~ 5%. The instrument details, AOD retrieval method, and error budget have been discussed elsewhere (Gogoi et al., 2009; Kompalli et al., 2010; Moorthy et al., 2007).



128 Apart from MWR, AOD is obtained from handheld Microtops sun-photometer (Solar Light  
 129 Company, USA) at five wavelengths (440, 500, 675, 870, and 936 nm). Microtops can  
 130 achieve AOD estimates with accuracy comparable to CIMEL Sun photometers used in the  
 131 AERONET network, with uncertainties ranging from 0.01 to 0.02, as reported by Ichoku et  
 132 al. (2002). In addition to ARFINET measurements, simultaneous AOD products (version 3,  
 133 level 2.0) available within the study region from AErosol RObotic NETwork (AERONET)  
 134 measurements are used. The CIMEL sun-photometers in AERONET measure AOD at 340,  
 135 380, 440, 500, 675, 870, and 1020 nm in a time interval of 5 to 15 min for cloud-free  
 136 conditions with an uncertainty  $\sim 0.01 - 0.02$  (Eck et al., 1999; Holben et al., 1998; Giles et al.,  
 137 2019). To use the ARFINET and AERONET AOD in the fusion experiment, the AOD values  
 138 are interpolated to 550 nm (corresponding to MODIS and MISR AOD) using the  
 139 methodology of Liu et al. (Liu et al., 2004):

$$140 \quad \ln\left(\tau_{\lambda_1}/\tau_{\lambda_2}\right) = -\alpha \ln\left(\lambda_1/\lambda_2\right) \quad (1)$$

141 Where,  $\tau_{\lambda_1}$  and  $\tau_{\lambda_2}$  are AODs at wavelengths  $\lambda_1$  and  $\lambda_2$ , respectively and  $\alpha$  is Angstrom  
 142 Exponent.  $\alpha$  is determined by applying a linear least squares fit to the logarithmic values of  
 143 AOD measured at various wavelengths.

## 144 2.2 Satellite retrieved AOD

145 The satellite-based AOD for this study is obtained from MODIS and MISR. MODIS data  
 146 (Collection 6.1 Level-2 AOD at 550 nm; ‘AOD\_550\_Dark\_Target\_Deep\_Blue\_Combined’;  
 147 spatial resolution of 10 km; over land) is obtained from NASA’s Level-1 and Atmosphere  
 148 Archive and Distribution System Distributed Active Archive Center (LAADS DAAC).  
 149 Sensitivity studies across diverse land surfaces employing various algorithms have validated  
 150 that integrating the Dark Target and Deep Blue methods yields enhanced accuracies, but  
 151 errors persistently emerge over South Asia (Gao et al., 2021; Tian et al., 2018; Wei et al.,  
 152 2019). Furthermore, the performance of the product has been evaluated across different  
 153 seasons (Sharma et al., 2021). Overall, the AOD measurement with an expected error of  
 154  $0.05 \pm 0.15 \times AOD$  over the land and  $0.03 \pm 0.05 \times AOD$  over the ocean is validated in  
 155 most studies throughout the years of algorithm up gradations (Levy et al., 2005; Sayer et al.,  
 156 2013; Wei et al., 2019).

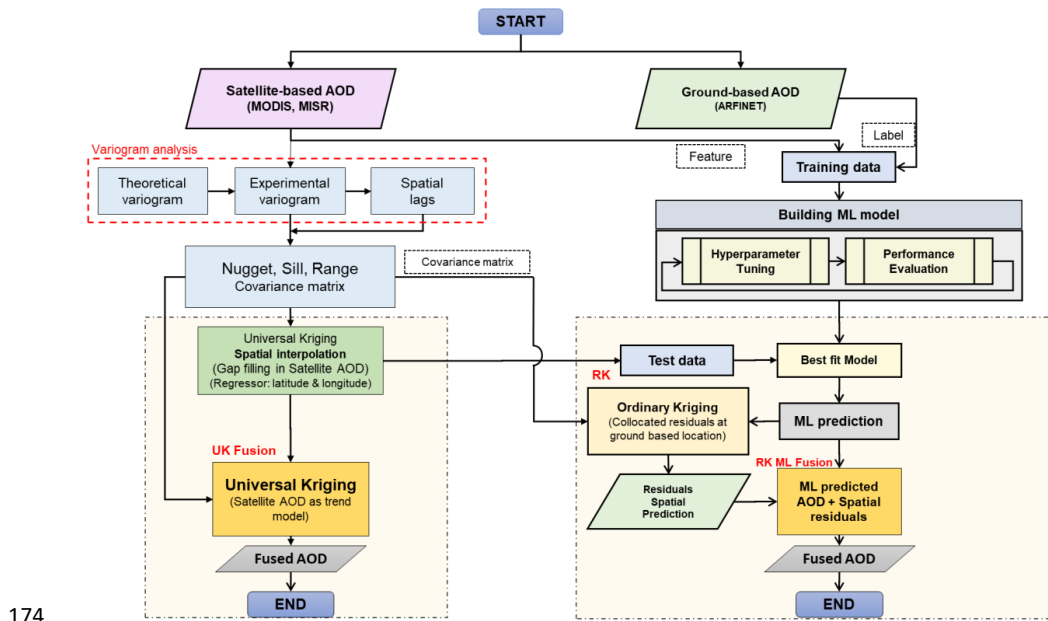
157 The MISR AOD (version V23) is obtained from Atmospheric Science Data Centre (ASDC).  
 158 MISR V23 products provide aerosol information with a spatial resolution of  $4.4 \text{ km} \times 4.4 \text{ km}$   
 159 (Garay et al., 2017; Sayer et al., 2020; Witek et al., 2018, 2021). Theoretical sensitivity  
 160 studies and performances for MISR (Kahn et al., 2001; Tao et al., 2020) have projected  
 161 standard deviations of the measurement error associated with optical depth to be  $\pm (0.05 +$   
 162  $20\% AOD_{\text{AERONET}})$ , showing a consistently narrower range over ocean compared to bright  
 163 land surfaces.

## 164 2.3 Fusion methodology

165 The Geostatistical data fusion method used in this study combines spatial data from multiple  
 166 sources (satellite and ground-based, as detailed in section 2.1 and 2.2) with varying  
 167 resolutions, accuracies, and types of measurements. The aim is to enhance the overall



168 understanding and prediction of spatial variables (e.g., AOD) to produce a more accurate and  
 169 comprehensive representation of columnar AOD. For this, we have adapted universal Kriging  
 170 methodology, where data interpolation relies on unknown functions (e.g., satellite derived  
 171 AOD) represented as trend models with spatial autocorrelation through variogram analysis.  
 172 The overview of the fusion method is presented in **Fig. 1**, followed by a detailed description  
 173 of each step in the following sections.



175 **Figure 1.** Flowchart of fusion methodology: Universal Kriging (UK) and Residual Kriging  
 176 Machine Learning (RK-ML). The machine learning best model is designed based on the long  
 177 term MODIS and MISR data which were collocated with ground-based observations.

### 178 2.3.1 Correlation analysis

179 As a first step of the fusion processes, the correlation analysis between the satellite and  
 180 ground-based AOD is made to understand the association/ biases between the two data sets at  
 181 different spatiotemporal scales. This is useful to understand the requirement of multi-sensor  
 182 data fusion. Satellites offer broad spatial coverage, while ground-based measurements  
 183 provide representative data at specific point locations with high temporal coverage. To  
 184 improve the efficacy of AOD measurements from both satellite and ground-based sources, a  
 185 statistical approach has been employed, incorporating key concepts introduced in the analysis  
 186 reported elsewhere (Basart et al., 2009; Chu et al., 2002; Filonchyk et al., 2019; Ichoku et al.,  
 187 2002). The spatial grid over the study domain (south Asia) is considered as  $0.5^\circ$  and the  
 188 temporal window of 30 min which accommodates 14 to 15 measurements from MWR (data  
 189 frequency 2 min) and 1 to 2 measurements from CIMEL (data frequency 15 min)  
 190 observations. For this, we averaged all satellite-based AOD over a  $0.5^\circ$  grid box and  
 191 compared it against ground-based AOD averaged over  $\pm 15$  min around terra-satellite  
 192 overpass time. This AOD values are averaged over a certain month to represent the monthly



193 mean AOD. From this, the difference between satellite and ground AOD is assessed for  
194 different periods of the year over the study region. The results that emerged from the  
195 correlation analysis of monthly mean AODs are included in section 3.2.

### 196 **2.3.2 Variogram Analysis**

197 Variogram analysis is used to quantify and model the spatial autocorrelation (i.e., spatial  
198 dependence) of a dataset. It evaluates how the spatial variability between data points changes  
199 as a function of lag distance—the distance separating two sample points in space. To capture  
200 the spatial dependency of the data, geographical parameters such as latitude, longitude, and  
201 elevation are often incorporated as covariates in the trend function, thereby incorporating the  
202 spatial context of the sampling locations. This approach has been widely applied in studies  
203 involving meteorological parameters (Chua and Bras, 1982; Holdaway, 1996; Nalder and  
204 Wein, 1998). In the present context, spatial representation of AOD is fairly represented as a  
205 trend function comprising of latitude, longitude, and elevation, which serve as proxies for  
206 underlying spatial variations of geographical and atmospheric influences that significantly  
207 affect aerosol distribution. However, it is important to note that most geostatistical methods,  
208 such as Kriging, assume the underlying field to follow second order or, intrinsic stationarity  
209 (mean is constant, and the covariance or, variance of increments depends only on spatial lag).  
210 However, real-world environmental/ geophysical data often contain large-scale spatial trends,  
211 having elevation or latitude/longitude dependencies, and systematic gradients due to physical  
212 or geographical factors. These trends violate the stationarity assumption which can lead to  
213 unbounded variogram. In such a situation, detrending separates the large-scale trend from the  
214 random spatial variations. In order to validate this assumption, we have obtained (**Fig-S1**) the  
215 frequency distribution of satellite AOD and their residuals after detrending. A nearly  
216 symmetric histogram of detrended residuals indicates that the trend component has been  
217 effectively removed, which is a prerequisite for second-order stationarity (Tang et al., 2016).

218 The semivariance, which measures the degree of spatial variability between pairs of sample  
219 points as a function of their separation distance, known as the lag-distance ( $h$ ), is calculated  
220 as:

$$221 \quad \gamma(h_x) = 1/2n(h) (\sum [z(x_i) - z(x_i + h)]^2) \quad (2)$$

222 Where  $z(x_i)$  and  $z(x_i+h)$  are the values of the variables of interest at locations  $x_i$  and  $x_i + h$  ( $=$   
223  $x_j$ ), respectively;  $n(h)$  is the number of pairs of points separated by the lag-distance  $h$ , which  
224 is given as:

$$225 \quad h_x = r \cos^{-1}(\sin \varphi_i \sin \varphi_j - \cos \varphi_i \cos \varphi_j \cos(\theta_i - \theta_j)) \quad (3)$$

226 Where  $\varphi_{i,j}$  represent longitudes of locations  $x_i$  and  $x_j$ , and  $\theta_{i,j}$  represent latitudes of locations  
227  $x_i$  and  $x_j$ ;  $r$  is the mean radius of the earth. Following this, the empirical variogram is  
228 calculated from the actual observational data, showing the relationship between semivariance  
229 and lag distance for each set of observations. The experimental variogram is obtained after  
230 binning semivariance at certain lags of the empirical variogram. The experimental variogram  
231 is then fitted with a theoretical model to describe the spatial continuity of the variable. The  
232 theoretical models considered in the present study include Exponential, Spherical, and  
233 Matheron models; the mathematical expressions are given as:



$$234 \quad \gamma_{theo}(h_x) = \begin{cases} 0 & h_x = 0 ; \\ \sigma_n^2 + \sigma_b^2 (1 - \exp(-h_x/l)) & h_x > 0 \end{cases} \quad \text{(Exponential)} \quad (4)$$

$$235 \quad \gamma_{theo}(h_x) = \begin{cases} 0 & h_x = 0 ; \\ \sigma_n^2 + \sigma_b^2 \left( \frac{3h_x}{2l} - \frac{1h_x^3}{2l^3} \right) & 0 < h_x \leq l ; \\ \sigma_n^2 + \sigma_b^2 & h_x > l \end{cases} \quad \text{(Spherical)} \quad (5)$$

$$236 \quad \gamma_{theo}(h_x) = \begin{cases} 0 & h_x = 0 ; \\ \sigma_n^2 + \sigma_b^2 \left( 1 - \exp\left(-\frac{h_x^2}{l^2}\right) \right) & h_x > 0; \end{cases} \quad \text{(Matheron)} \quad (6)$$

237 In the above equations,  $\sigma^2 = \sigma_n^2 + \sigma_b^2$ , represents the total variance observed in AOD data at  
 238 larger lag distances (spatially uncorrelated AOD data).  $\sigma_n^2$  is nugget (y-intercept of the  
 239 variogram), which represents the semivariance at a very small lag distance, approaching zero.  
 240 Nugget (spatial variation at distances smaller than the smallest sampling interval) is indicative  
 241 of the presence of measurement error or noise in the data. A large nugget relative to the sill  
 242 (i.e., the semivariance value where the variogram levels off, representing maximum  
 243 variability or correlation between data points at a given spatial distance) suggests significant  
 244 measurement error or unresolved variability. This can indicate potential issues with data  
 245 quality. On the other hand, a small nugget implies that the data is relatively free of noise and  
 246 that most of the spatial variability is due to the structured spatial process.  $\sigma_b^2$  is variance in  
 247 spatially correlated data, and this parameter gradually increases with increasing lag distances  
 248 until it reaches sill.  $l$  is the range parameter, the distance at which the semivariance reaches  
 249 the sill; up to this distance, data are spatially correlated with each other. The higher the range,  
 250 the more similar the values are at greater distances from each other. The spatial covariance  
 251 function can be derived from the variogram model as:

$$252 \quad C_{ij} = \sigma^2 - \gamma_{theo} \quad (7)$$

### 253 2.3.3 Universal Kriging (UK)

254 Universal Kriging, also referred to as Kriging with a trend model, extends Ordinary Kriging  
 255 by incorporating a deterministic trend component alongside the stochastic spatial component.  
 256 This approach is useful when there is an underlying trend in the data that varies across the  
 257 study area. The universal Kriging method uses both the spatial autocorrelation structure and  
 258 the deterministic trend to make predictions. The universal Kriging model can be expressed as:

$$259 \quad Z = M_z \beta + \epsilon \quad \text{Or, } \epsilon = Z - M_z \beta \quad (8)$$

260 Where,  $Z = [Z(x_1), Z(x_2), \dots, Z(x_n)]^T$  represent the values of the variables of interest at  
 261 locations  $x_1, x_2, \dots, x_n$ , respectively.  $M_z$  is the deterministic trend component of the model  
 262 ( $n \times p$ ) where  $p$  is representing the number of regressors; and  $\beta$  is the unknown drift  
 263 coefficient ( $p \times 1$ ) to be estimated;  $\epsilon$  is the stochastic component or stochastic residuals  
 264 ( $n \times 1$ ), i.e., mean zero random fields.





265 In the present study, the trend component  $M_z$  for fusion is defined as

$$266 \quad M_z = \begin{pmatrix} 1 & MODIS_{AOD_1} & MISR_{AOD_1} \\ 1 & MODIS_{AOD_2} & MISR_{AOD_2} \\ \vdots & \vdots & \vdots \\ 1 & MODIS_{AOD_n} & MISR_{AOD_n} \end{pmatrix} \quad (9)$$

267 This is similar to a multiple regression model, which is described through a combination of a  
268 constant term and two sensor measurements that act as regressors to predict AOD at  
269 estimation locations. The first component of this trend model represents the overall offset  
270 (i.e., the mean of the portion of the AOD distribution that is not captured by MISR and  
271 MODIS). This constant term thereby represents any systematic offset between the combined  
272 (MISR and MODIS) satellite-retrieved AOD and the ground-measured AOD.

273 Following equation (8), the expected value at prediction locations ( $x_s$ ) can be expressed as  
274 the best linear unbiased prediction (BLUP):

$$275 \quad \hat{Z}(x_s) = m_s^T \hat{\beta} + C_{zs}^T C_{zz}^{-1} (Z - M_z \hat{\beta}) \quad (10)$$

276 Here,  $C_{zs}(n \times s)$  is the spatial covariance matrix of the residuals between the sample location  
277 (i.e., measurement locations) and prediction locations (i.e., estimation locations) and  $C_{zz}(n \times$   
278  $n)$  is the spatial covariance matrix of the residuals between the sample locations (i.e.,  
279 measurement locations) as obtained from equation (7). The unknown coefficient  $\hat{\beta}$  can be  
280 expressed as the generalized least squares (GLS) estimator from the covariance matrix,

$$281 \quad \hat{\beta} = (M_z^T C_{zz}^{-1} M_z)^{-1} M_z^T C_{zz}^{-1} Z \quad (11)$$

282 Alternatively, minimizing the mean square error (MSE) of all predictions among the  
283 predictors of the form  $\lambda^T Z$  subjected to unbiasedness constraint, i.e.,  $E(\lambda^T Z) = E(Z(x_s))$  for  
284 all  $\beta$ , which is identical to  $\lambda^T M_z \hat{\beta} = m_s^T \hat{\beta}$  and under conditions for minimizing variance  
285 ( $\lambda^T Z - Z$ ), Lagrange multipliers ( $\mu(p \times s)$ ) are used to solve the linear constraint equations  
286 as given below,

$$287 \quad \begin{bmatrix} C_{zz} & M_z \\ M_z^T & 0 \end{bmatrix} \begin{bmatrix} \lambda \\ \mu \end{bmatrix} = \begin{bmatrix} C_{zs} \\ m_s \end{bmatrix} \quad (12)$$

288 Here,  $M_z (n \times p)$  and  $M_z^T (p \times n)$  are trend models of AOD given by equation (9);  $m_s$   
289 ( $p \times s$ ) is trend model at  $s$  estimation locations;  $\lambda(n \times s)$  are the Kriging weights,  $\mu$  is the  
290 Lagrange multiplier.

291 The system of equations is solved for Lagrange multiplier  $\mu$  and weights  $\lambda$  to estimate AOD  
292 at estimation locations. This can be expressed as:

$$293 \quad \begin{bmatrix} \lambda \\ \mu \end{bmatrix} = \begin{bmatrix} C_{zz} & M_z \\ M_z^T & 0 \end{bmatrix}^{-1} \begin{bmatrix} C_{zs} \\ m_s \end{bmatrix} \quad (13)$$

$$294 \quad \lambda = \{C_{zz}^{-1} - C_{zz}^{-1} M_z (M_z^T C_{zz}^{-1} M_z)^{-1} M_z^T C_{zz}^{-1}\} C_{zs} + C_{zz}^{-1} M_z (M_z^T C_{zz}^{-1} M_z)^{-1} m_s \quad (14)$$

$$295 \quad \lambda^T Z = C_{zs}^T C_{zz}^{-1} (Z - M_z \beta) + m_s^T \beta \quad (15)$$

296 The prediction variance associated with predicted values, can be represented as

$$\text{Var}(Z(x_s) - \hat{Z}(x_s)) =$$





$$\sigma_{Z(x_s)}^2 - C_{zs}^T C_{zz}^{-1} C_{zs} + (m_s^T - (M_z^T C_{zz}^{-1} C_{zs})^T) (M_z^T C_{zz}^{-1} M_z)^{-1} (m_s^T - (M_z^T C_{zz}^{-1} C_{zs})^T) \quad (16)$$

The above weighting approach decides the values at prediction locations. Our foremost approach involved creating a full satellite-based map of AOD over the study region using geographical parameters as the trend model where UK method acts as spatial interpolation method to get full AOD spatial map over the study domain. Subsequently, in the final spatial fused predictions, the ground-based AODs were treated as the response variables, where the satellite data, along with the elevation model (used as additional information), were used as regressors.

### 2.3.4 Residual Kriging Machine Learning (RK-ML)

While satellite and ground-based AOD measurements generally exhibit a linear correlation, regional and environmental factors introduce biases, noises and nonlinear dependencies. Although nonlinear extensions within the UK framework are possible, they require sophisticated techniques to achieve optimal performance, making the hybrid approach a compelling alternative. UK depends on spatial covariance structures with regression methods to enhance spatial predictions. The trend component in UK is conventionally modeled using low-order polynomials (e.g., first or second degree). However, real-world relationships between influencing factors and response variables are often highly non-linear, making such assumptions inadequate. While UK with linear trends is widely used, studies exploring non-linear trend modeling within the UK framework are still relatively rare. For instance, Snepvangers et al. (2003) incorporated a logarithmic trend to improve prediction of soil water content using net precipitation as an auxiliary variable. Freier and Lieres (2015) proposed a Taylor-based linearization technique combined with iterative parameter estimation to capture non-linear trend functions in UK. Freier et al. (2017) further extended this approach to interpolate low-density, irregular bio catalytic data. These techniques are effective when the functional form of the non-linearity is known a priori. However, in most practical scenarios, such explicit formulations are unavailable due to complex, unknown interactions between design factors and responses. In this context, machine learning (ML) models—especially kernel-based methods like SVR—offer an alternative for capturing non-linear and implicit relationships from data without the need for predefined functional forms. In this study, we introduced a Residual Kriging with Machine Learning (RK-ML) framework that integrates Support Vector Regression (SVR) for trend estimation. The preference for using SVR over decision-based algorithms in RK-ML stems from its suitability for problems with a small number of features and limited datasets. SVR is also well known for the robustness of regularized methods in both regression and classification (Sifaou et al., 2021). Random Forest (RF), as a bagging method, and XGBoost can also be applied within RK-ML; however, a sensitivity study comparing SVR, XGBoost, and RF on 20% of the MODIS test data showed that SVR achieved comparable or better performance metrics (R, RMSE; Supplementary Fig. S2). Overall, unlike UK, RK-ML does not require strict scaling for stationarity or normality, making it particularly suitable for generating fused AOD.

In this study, the RK-ML is implemented through a hybrid approach to make reliable estimates of fused AOD with improve predictive accuracy with fewer numbers of ground-based observations. For this, the best-performing SVR model is first identified based on a



time window of five years of data (simultaneous MODIS, MISR and ground measurements) for a specific month (season) targeting consistent aerosol conditions. Subsequently, this model leverages spatially interpolated features from MODIS and MISR data (gap filled AOD by UK) to generate SVR-predicted maps to obtain a full generalized AOD map for that month. The discrepancies between SVR-predicted values and observed ground measurements are treated as residuals, which are then spatially modeled using Ordinary Kriging. The resulting residual predictions are combined with SVR outputs to produce Residual Kriging Machine Learning (RK-ML)-fused products. This approach provides a robust alternative to traditional UK-based data fusion techniques by capturing complex relationships between predictors and target variables. The detailed RK-ML methodology is given below.

SVR transforms features into a higher-dimensional space, making them linearly separable and helps improving the prediction of target variables like ground based AOD. The use of SVR in Kriging has been reported in previous studies to improve model predictions (Wang et al., 2008; Baisad et al., 2023). The SVR model is represented by:

$$Z_{svr} = w^T \varphi + b \quad (17)$$

where  $\varphi$  is the kernel transformed input features,  $w$  is the nonzero vector normal to hyperplane (the plane or decision boundary that best fits the  $n$  dimension input vectors while maintaining a margin of tolerance ( $\varepsilon$ -insensitive zone) around it) and  $b \in \mathbb{R}$ . This expression assumes that  $Z_{svr}$  exist when it approximates all  $w^T \varphi$  with  $\varepsilon$  precision for linearly separable data. Along with it, the concept of soft margin loss function is considered which introduces slack variable  $\xi(+ve)$  and  $\xi^*(-ve)$  to allow some points lying inside the hyperplane.

Hence the optimization problem is subject to minimization of

$$\frac{1}{2} \|w\|^2 + C \sum_{i=1}^l (\xi + \xi^*) \quad \text{Such that} \begin{cases} Z - w^T \varphi - b \leq \varepsilon + \xi \\ w^T \varphi + b - Z \geq \varepsilon + \xi^* \\ \xi_i \xi_i^* \geq 0 \end{cases} \quad (18)$$

The regularization constant  $C$  trades off between the model complexity and empirical error up to which deviations larger than  $\varepsilon$  can be tolerated.  $\xi$ ,  $\xi^*$  are regression errors. The detailed explanation of SVR model is available in the literature (Smola & Schölkopf, 2004; Brereton & Lloyd, 2010). In the present study, best model of SVR is decided from the minimum RMSE between predicted AOD and real AOD after tuning its hyperparameters.

The residuals, which are the difference between collocated AOD of SVR predictions from ground based AOD, are estimated from the difference between  $\hat{Z}_{svr}(x_s)$  and  $Z$ , i.e.,  $\hat{Z}_{svr}(x_s) - Z$ . These residuals under ordinary Kriging are modeled as  $\delta(s) = \mu + \varepsilon(s)$  where  $\mu$  refers to the mean values of residuals over study domain, which resembles similar mathematics of universal Kriging, except  $M_z$  &  $m_s = 1$  (eq. (8) to eq. (15)). Following this, the estimated residuals at unknown locations are determined as

$$\delta(x_s) = \lambda^T \delta(x_z)$$

The weighting parameter  $\lambda$  is obtained from the covariance matrices as follows

$$\begin{bmatrix} \lambda \\ \mu \end{bmatrix} = \begin{bmatrix} C_{zz} & 1 \\ 1 & 0 \end{bmatrix}^{-1} \begin{bmatrix} C_{zs} \\ 1 \end{bmatrix} \quad (19)$$



376 The ordinary Kriging estimation contains the spatial relation while the SVR prediction  
 377 contains the optimal estimations from features (Satellite) and labels (Ground AOD). The final  
 378 fused map can then be estimated as

$$379 \quad Z = \delta(x_s) + Z_{svr}(x_s) \quad (20)$$

380 To minimize overfitting, the SVR hyperparameters were optimized using a grid-search with  
 381 the neg-mean squared error metric under a leave-one-out cross-validation (LOOCV) scheme  
 382 on the training data. This approach maximized the use of available data while providing an  
 383 unbiased estimate of model performance. Based on this procedure, a linear kernel was  
 384 identified as the optimal choice for the RK-ML models, which were subsequently evaluated  
 385 on independent test sets (20% for MODIS, N=318; 10% for MISR, N=71). For MODIS AOD  
 386 features, the best model configuration was  $C = 1$ ,  $\gamma = \text{'scale'}$ ,  $\text{kernel} = \text{'linear'}$ ; for  
 387 MISR AOD features, the optimal configuration was  $C = 100$ ,  $\gamma = \text{'scale'}$ ,  $\text{kernel} =$   
 388  $\text{'linear'}$ . The use of a linear kernel suggests a predominantly linear relationship between  
 389 satellite observations and ground-based AOD. Inclusion of the regularization parameters  $C$   
 390 and  $\gamma$  controls overfitting and penalizes noisy inputs, enabling the ML framework to  
 391 generate more reliable estimates. These estimates were further corrected using spatial  
 392 residuals from RK, allowing RK-ML to outperform UK under conditions of limited or biased  
 393 AOD observations.

394 The final models were evaluated using  $R^2$ , correlation coefficient ( $R$ ), MAE, and RMSE on  
 395 both training and test sets (**Table ST1**). Results indicate that training and test performances  
 396 were comparable (with training  $R^2$  values either lower or close to test  $R^2$ ), correlation  
 397 coefficients were consistently high, and errors (RMSE, MAE) were low. These outcomes  
 398 confirm that the SVR models did not suffer from overfitting and generalized well to unseen  
 399 data, despite the limited sample size.

400 There are other data fusion approaches such as Deepkriging (Chen et al., 2024), Bayesian  
 401 data fusion (Pilz and Spöck, 2008; Tang et al., 1955; Xue et al., 2017), ensemble Kriging  
 402 (Yang, 2018) etc. The Bayesian fusion has been applied across different satellites (Tang et al.,  
 403 2016), while neural network (NN) and Gaussian weighted regression (GWR) has been  
 404 implemented for large number of collocated ground and satellite observations (Li et al.,  
 405 2017). However, implementing these approaches for real-time fusion is challenging, as they  
 406 require large datasets and substantial computational resources, particularly for procedures  
 407 such as Monte Carlo Markov Chain (MCMC) simulations. Bayesian approaches additionally  
 408 require the specification of prior distributions and a sufficient number of collocated  
 409 observations to estimate error structures reliably. From these discussions, it appears that RK-  
 410 ML is particularly well-suited for multi-sensor fusion in regions where ground datasets are  
 411 sparse and limited.

### 412 **3. Results and discussions**

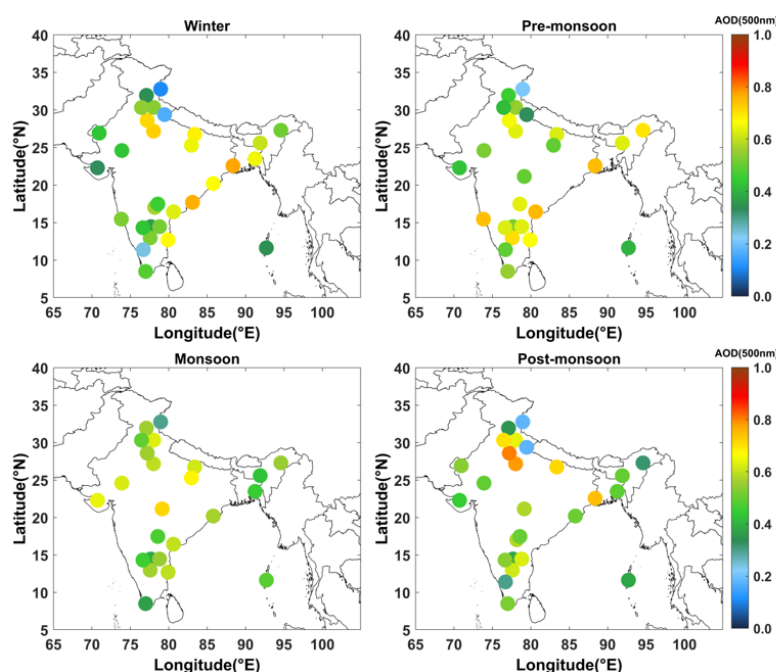
#### 413 **3.1 Regional pattern of AOD from ground-based and satellite observations**

414 The analysis of spatial pattern of AOD is crucial for understanding the consistency of  
 415 measurements across different sensors. The large-scale spatial variations in the data help



416 identify overall spatial trends over latitude-longitude and elevation wise. Emphasizing spatial  
 417 trends is also critical for assessing the mathematical assumptions underlying Kriging and  
 418 variogram analysis, which rely on the condition of second-order stationarity within the  
 419 sampled data.

420 The typical AOD patterns over different regions over India from ground-based  
 421 measurements, derived from 10 years of measurements from the ARFINET database using  
 422 MWR and Microtops instruments, is illustrated in **Fig. 2**.



423

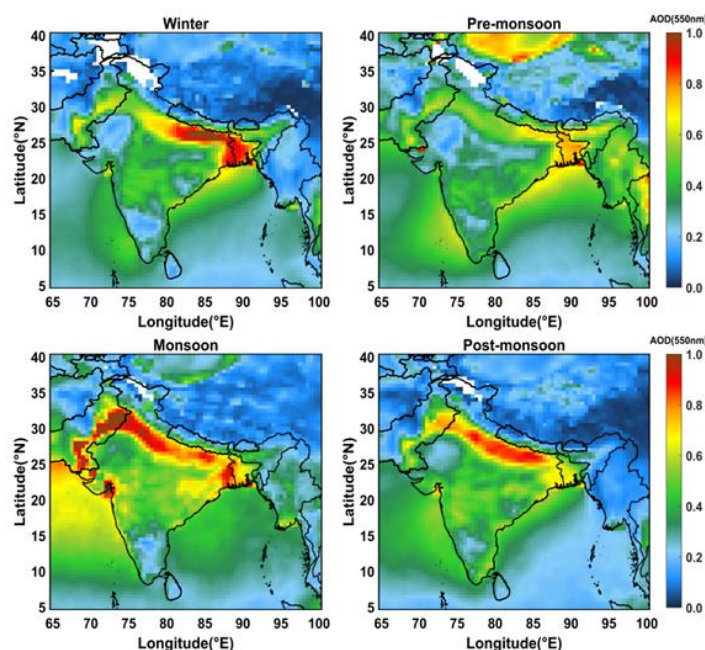
424 **Figure 2.** Long term (2011-2020) ground-based AOD at 500 nm from MWR and Microtops  
 425 measurements in the ARFINET over the Indian region. The seasons are winter: December,  
 426 January, February (DJF); Pre-monsoon: March, April, May (MAM); Monsoon: June, July,  
 427 August, September (JJAS); Post-monsoon: October, November (ON). The different regions  
 428 considered for representing Indo-Gangetic plane (IGP), North-west (NW), North-east (NE),  
 429 Peninsular India (PI), and Central India (CI) is provided (**Fig. S3**).

430 Various factors such as the dominance of natural and anthropogenic sources, local and  
 431 synoptic meteorology cause observed spatio-temporal variations in AOD at a particular  
 432 location. Over most of the locations in the Indo-Gangetic Plains (IGP), AOD shows  
 433 consistent high values ( $> 0.6$ ) throughout different seasons. This is similar to the observations  
 434 reported by Lodhi et al., (2013); Singh et al., (2020); Tiwari et al., (2018). Next to the IGP,  
 435 the north-eastern (NE) India experiences higher AOD with peak during the pre-monsoon  
 436 season. Similar pattern is reported elsewhere (Gogoi et al., 2009). In Peninsular India (PI),  
 437 AOD is highest during the pre-monsoon period, followed by a significant reduction during



the summer monsoon. This is similar to the earlier studies by Kalluri et al., (2016); Kumar et al., (2009); Sinha et al., (2013); Vachaspati et al., (2018).

The spatial patterns of a decadal average MODIS AOD (2011–2020; **Fig. 3**) also shows persistent high AOD values in the IGP and its outflow across all seasons. In PI, the presence of elevated mountain ranges such as the Western and Eastern Ghats, coupled with its proximity to the Indian Ocean, results in regional-scale AOD variability. During the pre-monsoon and monsoon periods, oceanic and coastal regions exhibit higher AOD levels compared to the winter and post-monsoon periods.



**Figure 3.** Long term (2011–2020) satellite based AOD (at 550 nm) from MODIS over south-Asian region.

Overall, the spatial patterns of AOD from ground and satellite observations reveal the following:

- During the pre-monsoon period, northern India experiences increased AOD.
- During the winter season, cold temperatures, a low boundary layer height, and humid air create hazy conditions with high AOD (Nair et al., 2020). Along with it, winds over the IGP are mostly north-westerly, with an anti-cyclonic pattern over central India, driving aerosols to peninsular region.
- The post-monsoon AOD also remains high, similar to winter levels, particularly in the IGP due to biomass burning (Kumar et al., 2012; Lodhi et al., 2013; Subba et al., 2021).
- The spatial patterns of AOD across different seasons are well captured by both satellite and ground-based observations. However, notable differences exist between





461 ground-based and MODIS AOD. While MODIS tends to overestimate AOD over the  
 462 IGP, it generally underestimates AOD over the PI, NE, and NW regions.

### 463 3.2 Inter-comparison of satellite- and ground-based AOD

464 The associations or biases between satellite and ground-based AOD at different year periods  
 465 are examined for the years 2012, 2016, and 2021 (Supplementary **Figs. S4-S6**). The quartile-  
 466 based plots highlight significant spatio-temporal variability in AOD, with both sensors  
 467 displaying higher AOD over terrestrial regions, particularly in the IGP, its outflows, and  
 468 South (Peninsular) and Central India. The third and fourth quartiles are more representative  
 469 for AOD over land regions than in surrounding areas like oceans and elevated terrain. Data  
 470 with respect to longitude and latitude show that higher AOD values are mostly confined to  
 471 20°-30°N latitude and 80°-95°E longitude. However, MODIS consistently recorded  
 472 significantly higher AOD values than MISR, with notable dissimilarities in quartile patterns  
 473 over northern India during May (**Figs. S7-S9**).

474 The spatial variability of AOD within each 0.5° spatial grid of satellite AOD values (from  
 475 both MODIS and MISR) around each nearest ground station is accounted for sub-grid scale  
 476 heterogeneity. Due to the dynamic nature of atmospheric conditions, a temporal window of  
 477  $\pm 15$  minutes was considered for ground-based AOD measurements, and the averaged values  
 478 were collocated with satellite data within a 0.5° spatial domain around each station.  
 479 Sensitivity tests with varying temporal ( $\pm 15$ ,  $\pm 30$ ,  $\pm 60$  minutes) and spatial windows (0.2°,  
 480 0.5°, 1°, and 2°) indicated that spatio-temporal variability was marginal for the  $\pm 15$ -minute  
 481 and 0.5° configuration ( $\Delta\text{MAE} \approx 0.002\text{--}0.004$ ;  $\Delta R \approx 0.002\text{--}0.01$ ; **Table ST2, Fig. S10**). Both  
 482 MODIS and MISR showed strong correlations ( $R > 0.93$ ) with ground-based AOD for 0.2°–  
 483 0.5° resolutions, while correlations decreased at 1° (notably for MISR) and further at 2°.  
 484 Correspondingly, RMSE and MAE values were lower at finer resolutions (0.2°, 0.5°) than at  
 485 coarser ones (1°, 2°). These results demonstrate that the spatial domain has a stronger  
 486 influence on collocation accuracy than the temporal window, and that the use of monthly-  
 487 averaged datasets further enhances the correlation between satellite and ground observations  
 488 by smoothing short-term variability (**Fig. S11**). The number of ground stations included in the  
 489 correlation studies is given in **Table 1**. During the winter months of January, MODIS and  
 490 MISR AOD show correlations of approximately 0.8 with ground observations. The  
 491 association between satellite and ground-based AOD in May is weaker than in January and  
 492 November. During November, both sensors showed better correlation (approximately  $> 0.8$ ).  
 493 The prominent locations contributing to mean errors and weak correlations with ground  
 494 observations are situated in the NW and IGP regions.

495 The above observations provide evidence of the differences in satellite-based AOD between  
 496 MODIS and MISR and ground-based measurements (as revealed in **Figs. S7-S9**). Earlier  
 497 studies on comparative analyses over the same geographic regions have indicated that the  
 498 frequency of observations, cloud masking, and geographical factors impact both MODIS and  
 499 MISR observations, stemming from algorithm assumptions related to cloud masking and  
 500 SSA. The current assessment highlights that MISR outperforms in mountainous and complex  
 501 regions, which is attributed to its advantages in multi-angle measurements. In these regions,  
 502 MISR measurements align well within the expected range, displaying robust correlation  
 503 values with respect to ground observations (Farahat, 2019).



**Table 1:** Number of ground stations data used in different months of the year 2012, 2016, and 2021.

2012	2016	2021	2012	2016	2021	2012	2016	2021
Jan	Jan	Jan	May	May	May	Nov	Nov	Nov
21	26	16	22	25	13	27	26	16

### 3.3 Fusion of satellite- and ground-based AOD

#### 3.3.1 Variogram analysis

For the fusion of satellite- and ground-based AOD, the experimental variogram (using eq.2) is first obtained from the gridded satellite data after detrending its geographical covariates, i.e., longitude, latitude, and elevation. As mentioned in section 2.3.2, a well-fitted variogram is essential for determining appropriate parameters in geographical processes. These variogram parameters like sill, range, and nugget are not unique but depend on the theoretical models used. The choice of fitting is determined through a least square approach, selecting the best fit based on the least sum of squared errors (SSE). However, the availability of a large number of satellite data sets has made this task easier. The variogram depicted in supplementary **Figs. S12, S13, and S14** demonstrate a flattening of variance after a certain lag (interval between distances), affirming the effectiveness of our implemented detrending method. AOD values within the range highlight spatial correlation, wherein the correlated AOD values are influential in determining missing AOD values. The variogram parameters obtained from the fitted theoretical model are given in **Tables 2 and 3**.

**Table 2:** Parameters obtained from variogram in different seasons (January, May, and November) of different years (2012, 2016, and 2021) from MODIS.

Year	Month	MODEL	Nugget	sill	Range (in km)
2012	Jan	Matheron	0	0.033954	848.5
2016	Jan	Exponential	0.000015	0.057399	453.3
2021	Jan	Exponential	0	0.052327	854.0
2012	May	Matheron	0	0.026499	555.6
2016	May	Matheron	0	0.029704	489.1
2021	May	Matheron	0	0.034273	378.3
2012	Nov	Matheron	0	0.030027	548.3
2016	Nov	Spherical	0	0.029582	1080.7
2021	Nov	Exponential	0	0.040153	696.2

The variogram parameters corresponding to different sensors exhibit noticeable variation across months and years, reflecting differences in their retrieval characteristics and ability to represent AOD. For instance, both MODIS and MISR show shorter spatial correlation lengths in May compared to January and November. Such reduced ranges are typically associated with long-range dust or smoke transport processes, which dominate during this period in the study region. Conversely, longer ranges indicate that the sensor retrievals capture more





spatially homogeneous values, suggesting an improved ability to represent regional heterogeneity. In this study, we prioritize MODIS variograms because of their higher sill and range values, which demonstrate stronger spatial dependency (Isaaks, 1991; Vieira et al., 2009). Nevertheless, sensitivity tests indicate that using variograms derived from either MODIS or MISR produces only negligible differences ( $\sim 0.01$ ) in the fused AOD estimates. (Fig. S15). At this stage, it is also to be noted that geographically weighted or local variogram approaches can better represent spatial heterogeneity, particularly over complex terrains such as the Himalayas and Western Ghats. However, in the present study, this approach was not feasible due to the limited availability of ground-based AOD observations, especially across high-altitude regions. The sparse coverage restricts the stability and generalizability of local variogram fitting, particularly at regional boundaries where different models would be required. For this reason, we adopted a single variogram model, following the approach used for large regions (e.g., eastern and western USA; Chatterjee et al. (2010)), which provides a more consistent framework for regional-scale fusion).

**Table 3:** Parameters obtained from variogram in different seasons (January, May, and November) of different years (2012, 2016, and 2021) from MISR.

Year	Month	MODEL	Nugget	sill	Range (in km)
2012	Jan	Exponential	0.000062	0.011589	645.6
2016	Jan	Spherical	0.000177	0.017749	1060.6
2021	Jan	Matheron	0	0.027958	927.9
2012	May	Matheron	0	0.016100	371.1
2016	May	Exponential	0.001741	0.018171	463.0
2021	May	Matheron	0.000833	0.017896	533.5
2012	Nov	Exponential	0.000022	0.014509	638.7
2016	Nov	Matheron	0	0.018378	583.0
2021	Nov	Matheron	0.0000925	0.019104	516.4

### 3.3.2 Spatial interpolation of AOD

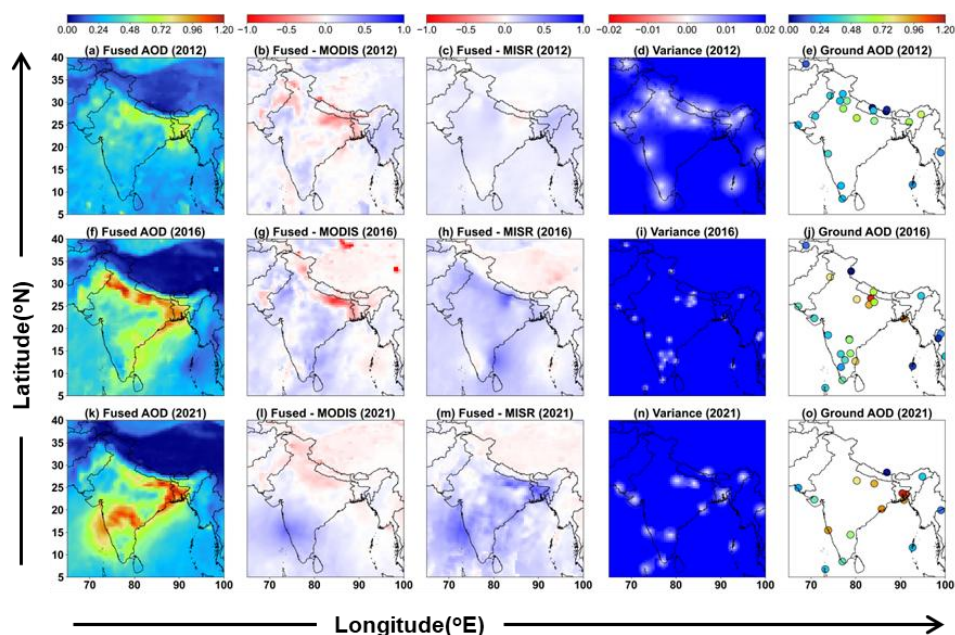
Monthly mean AOD gives the advantage of almost full picture over south-Asian region. However, it is observed that both MODIS and MISR AOD show gaps in some of the regions, either due to consistent cloud coverage or due to complex orography coupled with highly reflective land masses (e.g., snow-covered regions of the Himalayas). Universal Kriging is applied to fill these missing areas (which are found to be  $\sim 2$ -11%) to obtain a complete spatial picture of AOD over the south-Asian region. In universal Kriging of satellite data, geographic parameters (latitude, longitude, elevation) are taken as regressors. Since Kriging gives a probability map, the associated variance is higher in the gap regions than in the regions where values exist. Thus, the interpolated values and variances are not unique, as they depend on the variogram and trend models used in the interpolation. On the other hand, the variogram can have uncertainties that stem from factors such as lag spacing, the quantity of data points, and model fitting, as highlighted by researchers (Derakhshan and Leuangthong, 1982; Koushavand and Deutsch, 2008).



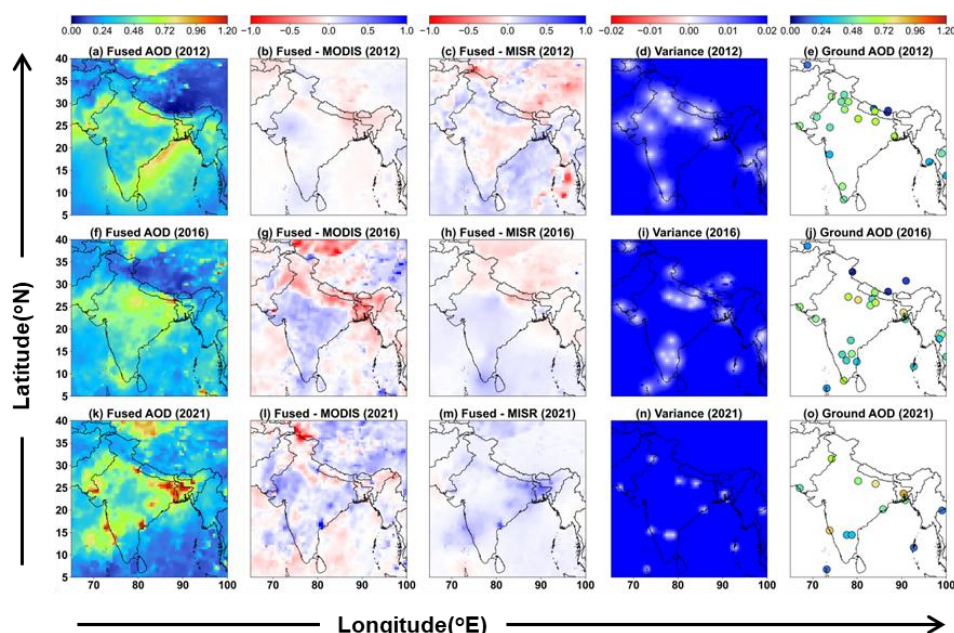
561 The  $0.5^\circ$  gridded monthly mean AOD from MODIS and MISR and their spatial distribution  
 562 after Spatial Prediction are shown in supplementary **Figs. S16-S21**. The variances of  
 563 predictions are also shown in the figure. It is observed that compared to oceans and high-  
 564 elevated surfaces like the Himalayan Mountain ranges, the spatial predictions are highly  
 565 accurate over mainland regions of India, where natural and anthropogenic activities are more  
 566 dominant. On the other hand, the limitations of the model over remote oceanic and high-  
 567 altitude regions are expected due to significant variations in meteorological or environmental  
 568 factors, which may have been overlooked. The gap regions where spatial prediction has been  
 569 applied exhibit higher variance compared to the variance observed in the previously available  
 570 data. Overall, using large numbers of data to interpolate a small fraction of missing values  
 571 makes it possible to create a reliable picture with less associated variance.

### 572 3.3.3 Fused AOD

573 The fusion method retains the overall spatial signatures of AOD from each satellite sensor.  
 574 The optimal AOD values are determined by the weights obtained from spatial relationships,  
 575 along with the trend of the satellite-based AOD at the estimation locations. **Figs. 4-6** show the  
 576 fused maps of AOD at different seasons of the years 2012, 2016, and 2021. The regional  
 577 average values of fused AOD, along with AOD from individual sensors, are given in  
 578 **Supplementary Tables - ST4, ST5, and ST6**.

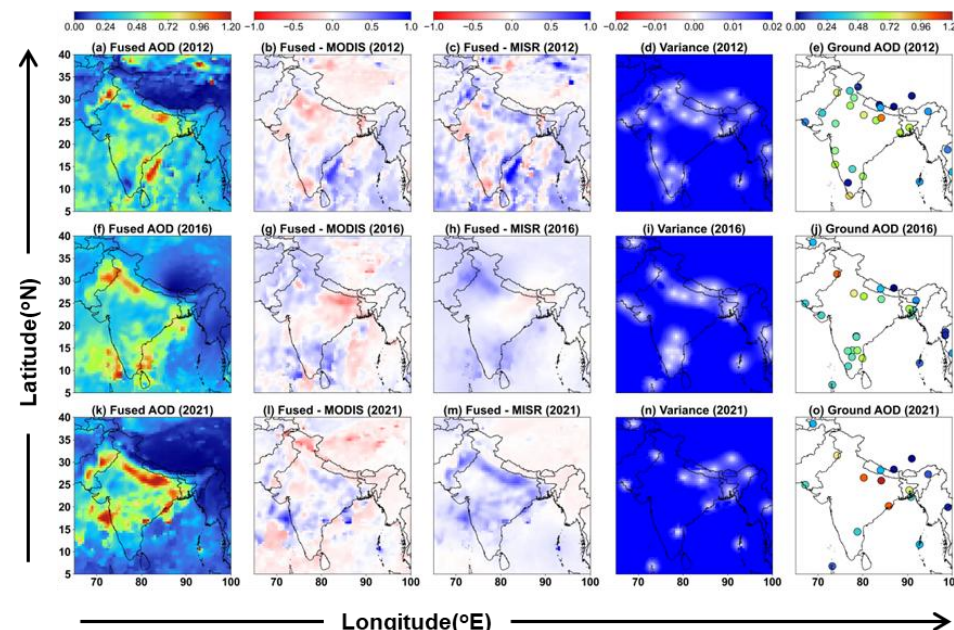


579 **Figure 4.** Fused AOD (at 550 nm) maps [(a),(f),(k)] in January for the years 2012, 2016,  
 580 2021; [(b),(g),(i)] and [(c),(h),(m)] - the deviations of fused AOD from corresponding  
 581 sensors, i.e., MODIS and MISR; [(d),(i),(n)] - variance; and [(e),(j),(o)] - ground-based AOD  
 582 used to generate fused maps. Blue indicates overestimations, and red means an  
 583 underestimation of fused AOD from satellite retrieved AOD. The white dots in variance plots  
 584 show the ground station locations.



586  
 587

**Figure 5.** Similar analysis as in Figure 4, but for the month of May in 2012, 2016, and 2021.



588  
 589  
 590

**Figure 6.** Similar analysis as in Figure 4, but for the month of November in 2012, 2016, and 2021.

591 Throughout the observation period, the fusion maps highlight the significant impact of  
 592 ground-based AOD on the fusion method. Notably, the scarcity of ground-based AOD  
 593 measurements directly influences the stability and reliability of spatial models, as it  
 594 challenges the fulfilment of key geostatistical assumptions such as stationarity, normality, and



appropriate data transformation. In this study, UK is carefully applied to generate fused AOD from transformed ground data through Box-cox method using optimal  $\lambda_{bc}$  values. This transformed data is back transformed after Kriging method, which helps to mitigate adverse effects (e.g. negative values or undefined values) of data scarcity. This underscores that the operational applicability of UK with small datasets is dependent upon careful pre-processing of the target variable and its covariates an effort intensive and data specific process.

In the analysis conducted on a seasonal basis, it is evident that the correlation between MODIS/MISR AOD with ground AOD for May is notably weaker and shows large biases (Table. 4, 5) compared to other months. During fusion experiment, this discrepancy is particularly influenced by ground AOD at specific locations during certain months, as detailed in the analysis below. Overall, the fused AOD demonstrates little enhancements in the correlation between MODIS and MISR data than the ground-based measurements.

**Table 4.** Error and bias analysis of MODIS AOD with ground and fused AOD at ground station locations.

Year	Month	Correlation	RMSE	MAE	Slope	Bias	Correlation	RMSE	MAE	Slope	Bias
		MODIS & Ground					MODIS & Fused				
2012	Jan	<b>0.781</b>	<b>0.144</b>	<b>0.106</b>	<b>0.858</b>	<b>0.074</b>	<b>0.789</b>	<b>0.142</b>	<b>0.105</b>	<b>0.896</b>	<b>0.067</b>
	May	0.770	0.128	<b>0.102</b>	0.704	0.147	0.788	0.122	0.096	0.732	0.137
	Nov	0.846	0.155	0.120	0.872	0.049	0.871	0.140	0.108	0.924	0.030
2016	Jan	0.792	0.250	0.164	1.096	-0.037	0.822	0.237	0.154	1.175	-0.083
	May	0.542	0.269	0.207	0.776	0.184	0.583	0.259	0.208	0.910	0.127
	Nov	0.773	0.157	0.121	0.759	0.064	0.787	0.153	0.115	0.774	0.055
2021	Jan	<b>0.861</b>	<b>0.199</b>	<b>0.138</b>	<b>0.911</b>	<b>0.010</b>	<b>0.879</b>	<b>0.185</b>	<b>0.127</b>	<b>0.958</b>	<b>-0.011</b>
	May	0.752	0.236	0.152	1.030	0.038	0.778	0.230	0.147	1.120	0.004
	Nov	<b>0.944</b>	<b>0.143</b>	<b>0.120</b>	<b>0.761</b>	<b>0.082</b>	<b>0.947</b>	<b>0.139</b>	<b>0.115</b>	<b>0.766</b>	<b>0.082</b>

**Table 5.** Error and bias analysis of MISR AOD with ground and fused AOD at ground station locations.

Year	Month	Correlation	RMSE	MAE	slope	bias	Correlation	RMSE	MAE	slope	bias
		MISR & Ground					MISR & Fused				
2012	Jan	<b>0.884</b>	<b>0.115</b>	<b>0.090</b>	<b>0.676</b>	<b>0.049</b>	<b>0.897</b>	<b>0.106</b>	<b>0.082</b>	<b>0.704</b>	<b>0.042</b>
	May	0.643	0.159	<b>0.132</b>	0.437	0.189	0.656	0.154	0.129	0.452	0.184
	Nov	0.760	0.223	0.175	0.466	0.098	0.780	0.212	0.168	0.492	0.089
2016	Jan	0.783	0.270	0.206	0.421	0.010	0.818	0.263	0.203	0.454	0.081
	May	0.662	0.167	0.129	0.606	0.153	0.736	0.140	0.117	0.736	0.098
	Nov	0.814	0.186	0.143	0.515	0.079	0.834	0.185	0.144	0.528	0.072
2021	Jan	<b>0.824</b>	<b>0.346</b>	<b>0.267</b>	<b>0.372</b>	<b>0.131</b>	<b>0.838</b>	<b>0.332</b>	<b>0.258</b>	<b>0.390</b>	<b>0.123</b>
	May	0.772	0.205	0.160	0.458	0.147	0.805	0.185	0.147	0.502	0.130
	Nov	<b>0.944</b>	<b>0.251</b>	<b>0.186</b>	<b>0.492</b>	<b>0.092</b>	<b>0.948</b>	<b>0.248</b>	<b>0.182</b>	<b>0.495</b>	<b>0.091</b>

A correlation study between MISR and ground observations in January 2012 shows lower error and a better correlation coefficient compared to MODIS and ground observations, resulting in the fused map closely resembling the MISR map. In 2016, MODIS overestimated AOD in the IGP region ( $\sim 0.99 \pm 0.31$ ), while the fused AOD corrected it to  $\sim 0.87 \pm 0.16$ ,

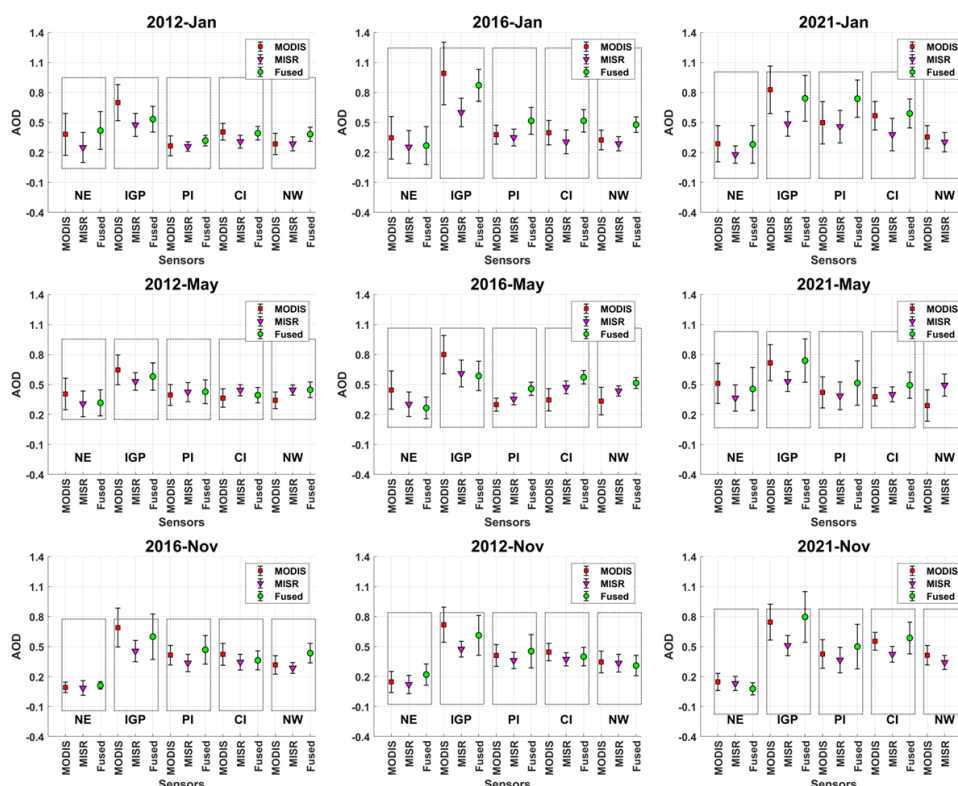




1616 closely matching with ground-based AOD ( $\sim 0.86$ ). Ground stations in the IGP, including  
 1617 Gandhi College (WUP), Kanpur (KNP), Gorakhpur (GKP), and Varanasi (VNS), were  
 1618 underestimated by MISR, while MODIS exhibited a mix of overestimations and  
 1619 underestimations. Excluding WUP and GKP stations, MODIS demonstrated lower errors  
 1620 (RMSE  $\sim 0.149$  and MAE  $\sim 0.117$ ) and a better correlation coefficient ( $\sim 0.85$ ) with ground  
 1621 observations, leading the fused map to reflect MODIS patterns predominantly. Similarly, in  
 1622 2021, MODIS and MISR observed widespread AOD over peninsular India but  
 1623 underestimated ground-based AOD at GOA ( $\sim 0.95$ ), reporting  $\sim 0.36$  and  $\sim 0.30$ . The fused  
 1624 AOD captured the high values and showed continuous flow toward the Arabian coast.

1625 Across several stations of Northwestern India and IGP, including Karachi (KRC), GKP,  
 1626 WUP, Dhaka (DHK), Agra (AGR), VNS, and Bhola (BHL), MODIS overestimated ground  
 1627 observations in May-2016. This overestimation resulted in poor correlation and higher errors  
 1628 with ground-AOD compared to that between MISR and ground-AOD. However, during May  
 1629 in 2012 and 2021, MODIS demonstrated better performance than MISR, showing a strong  
 1630 association with ground observations, e.g., except at BHL in 2021, with improved correlation  
 1631 and errors ( $R \sim 0.90$ , RMSE  $\sim 0.122$ , MAE  $\sim 0.102$ ). Consequently, deviation maps revealed  
 1632 white patches, indicating the influence of each sensor, which was also reflected in the fused  
 1633 maps. In Nov-2016, over the NW and IGP, a significant discrepancy was observed between  
 1634 fused AOD data and satellite measurements, as noted by ground stations. For example, LHR  
 1635 (Lahore) reported an AOD of approximately 1.02, while AGR recorded around 0.78.  
 1636 Additionally, a flow pattern on the east coast of peninsular India, detected by the MISR, was  
 1637 also preserved in the fused map. This map showed an enhanced AOD value attributed to  
 1638 observations from ground stations Chennai (CHN) and Kadapa (KDP), which had been  
 1639 underestimated by both MODIS and MISR. Similarly, in November 2021, the flow over the  
 1640 IGP was modified in the fused map based on ground observations, such as those from WUP  
 1641 with an AOD of 1.28 and KNP with an AOD of 1.03.

1642 Since, different time periods have different number of ground stations; the regional analysis  
 1643 can only assess the improvement in the fused AOD estimates over MODIS and MISR. **Fig. 7**  
 1644 illustrates that the regional mean fused AOD values closely follow the variations observed in  
 1645 individual satellite sensor data, although the magnitude differs significantly. This highlights  
 1646 that ground-based AOD, though traditionally advantageous for its temporal coverage,  
 1647 contributes to improved spatial representation. Over the IGP, where ground-based  
 1648 observations are more abundant than in any other region of India, the regional mean fused  
 1649 AOD generally lies between MODIS and MISR values. This reflects the tendency of MODIS  
 1650 to overestimate and MISR to underestimate AOD in this region, with the fusion process  
 1651 balancing these biases. In contrast, over Peninsular India, which has the second-highest  
 1652 number of ground stations after the IGP, the fused AOD is higher than both MODIS and  
 1653 MISR, suggesting that satellite observations underestimate AOD in this region. Similarly, in  
 1654 central India, the fused AOD exceeds both sensors. Over northwest India during May, when  
 1655 dust loading is high, the fused AOD is close to MISR, consistent with previous studies  
 1656 showing that MISR performs better than MODIS in dust-dominated regions due to its multi-  
 1657 angle capability. However, over the NE, CI, and NW regions, the fused AOD remains higher  
 1658 than satellite estimates. Fused AOD estimates over the Himalayas and oceanic regions are not  
 1659 analyzed further due to the lack of sufficiently distributed ground-based observations.



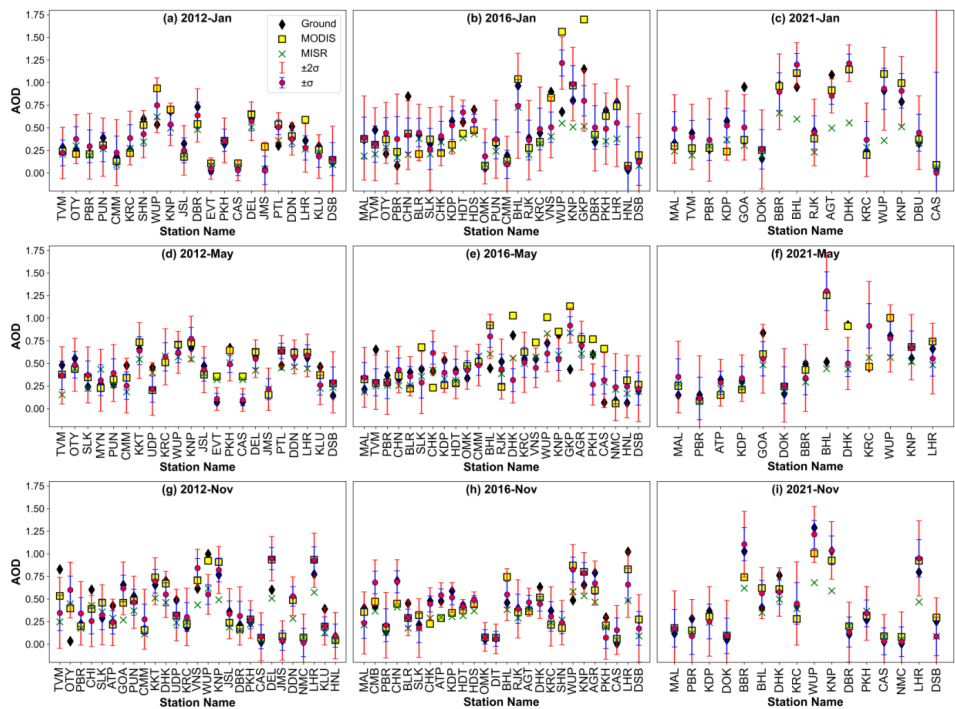
**Figure 7.** The regional analysis plots showing the difference between the AOD obtained from MODIS and MISR, and AOD estimated using the fusion method. On the y-axis, AOD values are shown as mean  $\pm$  standard deviation.

### 3.3.4 Performance analysis and cross-validation

The performance analysis carried out using the correlation analysis parameters such as Root mean square error (RMSE) and mean absolute error (MAE), revealed a decrease in RMSE and MAE in fused data and an increase in correlation with MODIS and MISR (Figs S22-S24; Table 4, 5). Along with this, bias is also improved each time. However, the improvement is inconsistent due to factors such as the variogram model used, errors between observation values of ground observation, and MODIS, MISR. Thus, the final characteristics of fused products are influenced by their individual instruments. The accuracy of fusion can be concluded from the cross-validation analysis. This is characterized by LOOCV method. Figure 8 shows the predicted AOD values at each ground location during each leave-one-out process. The prediction model performances analyzed in terms of mean prediction error (MPE) and root mean square prediction error (RMSPE) are given in Table 6. The predicted AOD values (as magenta points) at each of the ground locations with standard error bars  $\pm \sigma$  (blue line),  $\pm 2\sigma$  (grey line) are also shown in Figure-8, along with AOD from the ground (black diamond), MODIS (yellow triangle), MISR (red cross) observations. The figure shows that more than 80% of ground AOD are within  $\pm 2\sigma$  (95% Confidence interval) of predicted AOD for seven out of nine months. The highest accuracy was achieved in 2021 November



681 and 2012 May (100%), and the lowest in 2016 May (76%), indicating the importance of the  
682 association between different sensors during the fusion process. The enhanced accuracy of the  
683 model for fused estimations required good correlation and reduced errors, as indicated in  
684 **Table 4, 5 & 6.**



685  
686 **Figure 8.** Predicted AOD values (as magenta points) with error bars  $\pm\sigma$  (blue line),  $\pm2\sigma$  (red  
687 line), and ground observed AOD (black diamond), MODIS observation (yellow square),  
688 MISR (green cross) at different stations. For station names refer **Table ST7 and ST8.**

689 **Table 6.** Accuracy assessment of the predicted AOD through leave-one-out cross-validation.

Year	Month	Correlation	RMSPE	MPE	Ground AOD within $\pm\sigma$ (in %)	Ground AOD within $\pm2\sigma$ (in %)
2012	Jan	<b>0.852</b>	<b>0.108</b>	<b>0.091</b>	<b>76.19</b>	<b>95.24</b>
	May	<b>0.809</b>	<b>0.118</b>	<b>0.093</b>	<b>77.27</b>	<b>100</b>
	Nov	0.676	0.215	0.152	59.26	77.78
2016	Jan	0.708	0.213	0.160	65.38	84.62
	May	0.367	0.219	0.170	56	76
	Nov	0.793	0.146	0.109	65.38	88.46
2021	Jan	<b>0.893</b>	<b>0.162</b>	<b>0.121</b>	<b>81.25</b>	<b>81.25</b>
	May	0.451	0.302	0.212	61.54	84.62
	Nov	<b>0.964</b>	<b>0.108</b>	<b>0.086</b>	<b>87.50</b>	<b>100</b>

690

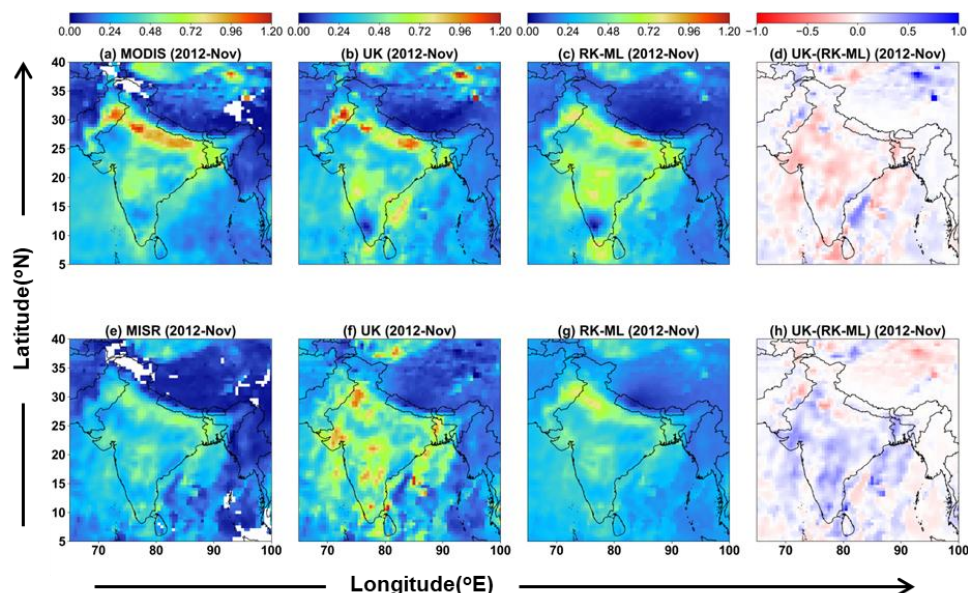
### 691 3.3.5 Machine Learning enhanced Geostatistical data fusion

692 To understand the influence of number of ground measurement points in the generation of  
693 fused map, sensitivity studies has been carried out by varying the number of ground based





694 measurement points. The number of ground points from maximum of 27 ground locations has  
 695 been subsequently reduced to 22, 13, 8, and 6 respectively. The corresponding variations in  
 696 the fused outputs are provided (Supplementary **Fig. S25-S26**) and a special case is included in  
 697 **Fig-9**. The figure clearly explains the changes in prevailing spatial pattern of aerosols  
 698 according to changes in number of data points, indicating that RK-ML method is a good  
 699 alternative to UK, when the available ground measurements are limited. This study also  
 700 indicates an inherent limitation in UK method, alike to multiple linear regression models,  
 701 which are highly susceptible to noise in predictor variables. In contrast, RK-ML demonstrates  
 702 greater robustness by first modeling the deterministic component using a machine learning  
 703 regressor (in this case, SVR), followed by kriging of the residuals to capture the stochastic  
 704 component. This two-step approach effectively leverages machine learning for optimized  
 705 estimation under noisy conditions, while kriging incorporates spatial variability of residuals  
 706 obtained from observations, resulting in more reliable spatial predictions.



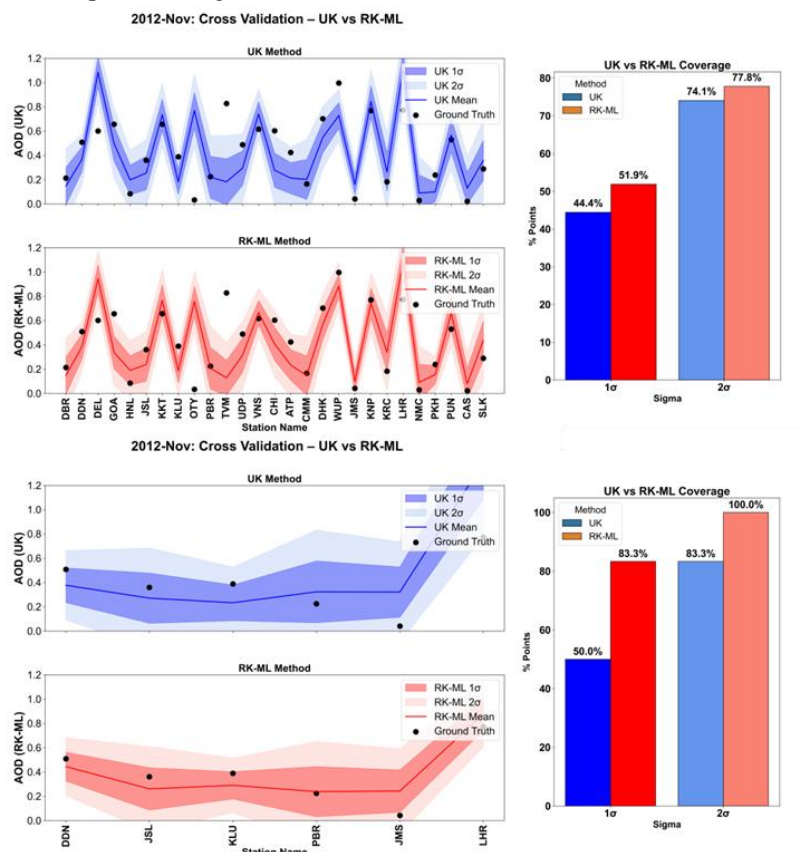
707 **Figure 9.** MODIS (a), MISR (e), and fused AOD using Universal Kriging (UK, (b), (f)), and  
 708 Residual Kriging with Machine Learning (RK-ML, (c), (g)); Difference between UK and RK-  
 709 ML predictions ((d), (h)). Blue color indicates where UK predictions exceed those of RK-  
 710 ML, and vice versa. The top panels of fused AOD shows estimations using 27 ground-data  
 711 points, while the bottom panel shows fused AOD derived from 6 ground-data points.  
 712

713 Notably, when data points are fewer, UK has overestimated AOD values in mainland regions  
 714 relative to RKML predictions. This discrepancy may arise due to the complexity of the  
 715 underlying surface, where Ordinary Kriging (OK) has been shown to outperform UK, as  
 716 discussed on basis of different surface types (Zimmerman et al., 1999). Since RK is an  
 717 extension of OK, it inherits these advantages, contributing to the improved performance of  
 718 the RK-ML method. The sensitivity study further highlights that variations in the number of  
 719 ground station data points and associated errors have a lesser impact on fused AOD from RK-  
 720 ML approach in terms of retaining spatial patterns compared to the UK-approach. This



721 demonstrates the RK-ML fusion ability to better manage observational uncertainties and data  
 722 sparsity.

723 The UK and RK-ML approach yields comparable results when the observations are higher in  
 724 number. On the other hand, RK-ML outperforms UK when the number of ground observation  
 725 is significantly decreased (**Fig. 10**). Hence, the accuracy of this estimation is significantly  
 726 influenced by the availability of small datasets, which indicates that the large number of  
 727 ground stations are crucial for best representation of fused AOD products from Universal  
 728 Kriging, while RK-ML is a good choice in case of limited number of ground observations.  
 729 Hence, the applicability of RK-ML can be made for generating fused AOD on daily basis per  
 730 each satellite overpasses over ground based stations.



731 **Figure 10.** Line plots of LOOCV results from UK method (blue line) and RK-ML method  
 732 (red line), covering the ground AOD (black dots) for Case-1 (27 points) and case -2 (6 points)  
 733 within  $1\sigma$  (dark shade) and  $2\sigma$  (light shade). For station names, refer to supplementary **Tables**  
 734 **– ST7 and ST8.**

736 The applicability of UK and RK-ML depends on their ability to capture realistic spatial  
 737 patterns from spatially representative data points (e.g., ground-based AOD) in order to  
 738 produce accurate fused AOD distributions. These estimations inherently carry uncertainties,  
 739 which increase with distance from ground observation sites. Consequently, the resulting maps



show elevated uncertainties in areas with sparse ground coverage. To evaluate model performance under varying ground-station availability, we employed LOOCV. Results indicate that RK-ML is generally more effective than UK when fewer ground observations are available, as it can capture nonlinear relationships and penalize erroneous AOD values. However, the Kriging step still requires a sufficient number of data points to propagate spatial residuals. Similarly, UK applied with a limited number of stations (e.g., 27 in the present study) estimates weights from collocated AOD points and satellite regressors (MODIS and MISR). Thus, accurate uncertainty representation and improved fused AOD maps require a more uniformly distributed network of ground stations. As illustrated in **Fig. S25**, increasing station density enhances the similarity between fusion maps from both methods, as seen in the larger white patches of the deviation plots (**Fig. S25a–d**).

### 3.3.6 Limitations of this Study and Future Scope

The present study encounters a few limitations due to:

1. A limited number of ground-based observations across geographically complex regions, further affected by data gaps due to cloudy conditions, instrumental and operational issues. Hence, fusion using UK requires careful data transformations to avoid spurious values (e.g., negatives) that may arise from unconstrained regression in UK.
2. Our collocation approach assumes spatially uniform aerosol variation within the selected spatio-temporal window and grid resolution. At instantaneous collocation scales, the variability depends on grid size, with approximate values of 0.05 for 0.1°–0.25° resolution, 0.1 for 0.5°, and 0.15 for 1°. This variability is substantially reduced when averaged to monthly means. Sensitivity tests indicate that variability increase noticeably beyond 1°, while resolutions between 0.2° and 0.5° yield comparable metrics. The typical spatial representativeness errors are in the range of ~0.01–0.09.  
  
In our fusion methodology, representativeness errors are not explicitly corrected at individual locations but are considered at the domain level. These errors are generally estimated from the nugget effect of collocated points. However, due to limited availability of such data, this estimation was not applied here, which likely increased the nugget effect and produced smoothed averages rather than fully resolving local variability. We therefore acknowledge that spatial representativeness error is a limitation of our current approach.
3. Uncertainties arising from the use of uniform gridding criteria have been indicated through nugget errors. The application of single variogram/trend model across diverse geographic regions and seasons may cause bias, but using geographical weighted or local variograms were impractical to create a best realization of fused AOD over a large domain while it may help when we have sufficient ground points well distributed in different regions. Though various sensor variograms can affect inaccuracies of ~0.01.



779 4. The availability of low number of ground stations and LOOCV as metric to quantify  
 780 the model's performance can have limitations in regions with highly heterogeneous nearby  
 781 observations, which lowers LOOCV scores.

782 Despite these challenges, the fusion methodology employed in this study underscores the  
 783 importance of creating a fused AOD data product from space-borne and ground-based  
 784 observations for large-scale applications. While our analysis does not claim to fully capture  
 785 the real-world scenario, it provides optimally fused results based on the available ground  
 786 observational points serving as the primary influence. When a sufficient number of  
 787 simultaneous ground-based and satellite observations are available, the fusion technique can  
 788 better capture fine-resolution continuous processes while representing simplified trend  
 789 expressions across geographically distinct regions. With advancements in computational  
 790 power and the increasing robustness of machine learning models applied to long-term  
 791 observations across various sensors, real-time product generation using multiple sensors  
 792 presents a potential extension of this work.

#### 793 4. Conclusion

794 The utilization of a universal Kriging approach, combining satellite-based measurements with  
 795 ground-based observations, has demonstrated enhanced AOD estimation with reduced  
 796 uncertainties compared to relying on a single instrument. Despite inherent differences among  
 797 instruments, the implemented approach capitalizes on their complementary features,  
 798 statistically combining the three datasets to provide robust estimates. The significant  
 799 outcomes of this study are as follows:

- 800 • MODIS and MISR observations exhibit good but variable associations with ground-  
 801 based AOD measurements influenced by seasonal and geographic differences.
- 802 • Variogram analysis reveals different autocorrelation length implying capability of  
 803 each sensor to get the spatial variability or auto correlation structure in different  
 804 periods. In some of the months, MODIS shows higher spatial range as compared to  
 805 MISR, while the opposite is seen during the rest of the months. On the other hand, sill  
 806 is always higher in case of MODIS.
- 807 • Spatial interpolation of AOD through variogram analysis provides very good  
 808 predictions at the missing grids of the satellite observations, emphasizing the  
 809 effectiveness of the universal Kriging method.
- 810 • The fused AOD maps reveal distinct results, highlighting the significant impact of  
 811 ground-based AOD on the fusion process. Especially in pre-monsoon period, the  
 812 correlation coefficient and slope between MISR and fused AOD (comparable to  
 813 ground-based AOD at the point locations) improved by ~11% and ~21% respectively,  
 814 with reduction in RMSE by ~16% as compared to before fusion.
- 815 • Cross-validation experiments further underline the effectiveness of the models in this  
 816 study, e.g., strong correlations (0.964) and low RMSPE (0.108) and MPE (0.086)  
 817 errors during November 2021. Even the model is able to predict 87.50 % of ground  
 818 truths within  $\pm\sigma$  and even 100% within  $\pm 2\sigma$ . Moreover the measurements which were



failed in predictions are due to highly local heterogeneity influenced by nearby ground measurements only.

- Incorporating a greater number of ground-based measurements enhances the fused results, yielding a cross-validation accuracy ranging from approximately 78% to 88% (based on 27 ground location points in November 2012 and 26 points in November 2016). However, the alternative RK-ML method can also be effective when long-term observation stations are available, even if their numbers are limited. The establishment of additional ground-based stations is recommended to strengthen the representation of air quality, especially in regions with high heterogeneity. This methodology can be implemented to get the fusion maps of finer spatiotemporal resolution.

#### Author Contributions Statement:

**SSG** - Data Curation, Software, Formal analysis, Visualization, Investigation, Writing - Original Draft and Editing; **MMG** - Methodology, Visualization, Validation, Software, Writing, Review and Editing, Supervision; **SSB** - Conceptualization, Supervision, Review and Editing, Project administration.

**Acknowledgments:** This study was carried out as part of the ARFI project of ISRO-GBP. We express our sincere thanks to the ARFINET investigators for the continued support and long-term contributions over the years in operating the network. We authors are also thankful to the AERONET team for providing AOD data (data available at <http://aeronet.gsfc.nasa.gov>). Additionally, we acknowledge NASA's Level-1 and Atmosphere Archive and Distribution System Distributed Active Archive Center (LAADS DAAC) and the Atmospheric Science Data Center (ASDC) for making the MODIS and MISR datasets available.

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