



# Processing Multiple GNSS RO Data Using FSI and ROPP: Results from the ROMEX

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## Abstract

Global Navigation Satellite System (GNSS) Radio Occultation (RO) is a vital technique in atmospheric remote sensing, providing all-weather, high-resolution vertical observations that support numerical weather prediction (NWP) and atmospheric research. To enhance understanding of GNSS RO processing uncertainties and inter-algorithm consistency, NOAA/STAR developed an independent RO inversion algorithm based on the Full Spectrum Inversion (FSI) technique to derive bending angle and refractivity profiles from excess phase data. As part of the international Radio Occultation Modeling Experiment (ROMEX), endorsed by the International Radio Occultation Working Group (IROWG), STAR's FSI results were systematically compared with outputs from the community standard Radio Occultation Processing Package (ROPP) and EUMETSAT datasets. Leveraging multi-GNSS RO observations from both commercial and government-funded missions, the study evaluates consistency across processing approaches using the European Centre for Medium-Range Weather Forecasts (ECMWF) Reanalysis v5 (ERA5) as the reference and structural differences against the three-dataset mean for the ROMEX period. Results reveal high overall agreement, while identifying variations linked to the signal-to-noise ratio (SNR) and mission characteristics, providing critical insights for interpreting ROMEX forecast impact studies and improving GNSS RO data assimilation systems.

## 1. Introduction

Global Navigation Satellite System (GNSS) Radio Occultation (RO) has become a cornerstone of atmospheric remote sensing, offering high vertical resolution, global coverage, long-term stability, and minimal bias (Kursinski et al., 1997; Anthes et al., 2008; Ho et al., 2020). By measuring the bending of GNSS signals as they pass through the atmosphere, RO enables retrievals of refractivity, temperature, pressure, and humidity profiles. As a limb-sounding technique, it is largely unaffected by clouds and precipitation, providing an all-weather observing capability essential for weather forecasting and climate monitoring (Cucurull et al., 2007; Healy, 2008; Steiner et al., 2020).

Over the past two decades, the expansion of GNSS constellations (e.g., GPS, GLONASS, Galileo, BeiDou) and the increasing availability of RO missions, including government-funded programs (e.g., COSMIC-1/2, Metop-A/B/C, Sentinel-6) and commercial ventures (e.g., Spire, GeoOptics, PlanetiQ), have significantly increased the volume of RO observations (Anthes, 2011; Schreiner et al., 2020; Ho et al., 2023). Today, global RO data counts exceed 35,000-40,000 profiles per day, with substantial contributions from commercial providers through initiatives such as NOAA's Commercial Data Purchase (CDP) program. While this growth enhances the value of RO for numerical weather prediction (NWP) and climate applications, it also introduces challenges due to differences in instrument design, tracking strategies, sampling patterns, and processing methodologies.



51 RO retrievals involve several steps: i) deriving clock-synchronized excess phase and signal-to-  
 52 noise ratio (SNR) data, ii) inverting excess phase to bending angle (BA) profiles, and iii)  
 53 retrieving refractivity from BA via Abel or statistical methods (Gorbunov, 2002a). In the lower  
 54 troposphere, strong gradients and multipath propagation complicate retrievals, motivating  
 55 advanced inversion techniques such as Full Spectrum Inversion (FSI) (Jensen et al., 2003;  
 56 Adhikari et al., 2016, 2021), Canonical Transform Type 2 (CT2) (Gorbunov et al., 2005), and  
 57 Phase Matching (PM) (Jensen et al., 2004; Sokolovskiy et al., 2011). Among these, FSI has  
 58 demonstrated particular strength in resolving fine-scale atmospheric structures.

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 60 The international RO community is currently undertaking a coordinated effort to evaluate the  
 61 impact of large volumes of RO data on NWP. This initiative, known as the Radio Occultation  
 62 Modeling Experiment (ROMEX), is endorsed by the International Radio Occultation Working  
 63 Group (IROWG) (<https://irowg.org/ro-modeling-experiment-romex/>) and provides a  
 64 collaborative platform for data providers and processing centers to assess RO retrievals under  
 65 a standardized framework (Anthes et al., 2024). GNSS RO observations from a broad range of  
 66 government-funded and commercial missions were submitted to EUMETSAT for centralized  
 67 processing, and the resulting products were distributed via the Radio Occultation Meteorology  
 68 Satellite Application Facility (ROM SAF). ROMEX provides a standardized framework for  
 69 assessing inter-mission and inter-algorithm differences. Central questions include whether  
 70 assimilating larger RO volumes improves forecasts, and how variations in data quality and  
 71 inversion methods affect the outcome.

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 73 In support of ROMEX, the NOAA Center for Satellite Applications and Research (STAR)  
 74 contributed independent datasets processed using the FSI algorithm, which was integrated into  
 75 version 10.0 of the Radio Occultation Processing Package (ROPP) (ROPP, 2020). This  
 76 customized system, referred to as STAR ROPP with the capability to select the CT2 and FSI  
 77 methods, ensures compliance with ROPP standards while incorporating STAR-developed  
 78 retrieval methods. Distinguishing STAR ROPP from the official ROM SAF processing is  
 79 critical, as it enables an independent assessment of algorithmic effects on RO data quality.

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 81 This study evaluates the STAR FSI-based processing system (RFSI) within the ROMEX  
 82 framework. Retrievals from RFSI are compared against those from the STAR ROPP with the  
 83 CT2 method and the EUMETSAT-processed ROMEX dataset (with COSMIC-2 data provided  
 84 by UCAR). The analysis focuses on November 2022 and utilizes the European Centre for  
 85 Medium-Range Weather Forecasts (ECMWF) Reanalysis v5 (ERA5) (Hersbach et al., 2023)  
 86 as a reference to evaluate algorithmic performance across various missions. The STAR RFSI  
 87 dataset for ROMEX is one of the three RO datasets, along with those from EUMETSAT and  
 88 UCAR, that were released to ROMEX participants through ROM-SAF (Shao and Folsche,  
 89 2024).

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 91 Intercomparisons included statistical evaluations (mean biases, standard deviations) and inter-  
 92 algorithm consistency. This design helps isolate processing-related uncertainties (e.g.,  
 93 structural uncertainty; Ho et al., 2012) and ensures that differences in NWP impact can be  
 94 attributed to data quality and processing methodology rather than uncontrolled input or  
 95 evaluation effects.

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 97 The paper is organized as follows: Session 2 describes the GNSS RO observations and datasets  
 98 used in this study. Session 3 presents the FSI algorithm in detail. Session 4 provides inter-  
 99 algorithm and inter-mission comparison results using ROMEX RO data. Conclusions are  
 100 summarized in session 5.



## 2. GNSS RO Observations and Data Used in this Study

### 2.1 GNSS RO Observations

Modern satellite missions, including COSMIC-2, Spire, and PlanetiQ, have significantly increased the volume of GNSS radio occultation data. These missions track signals from multiple constellations, including GPS, GLONASS, Galileo, and BeiDou, thereby improving global spatial and temporal coverage for atmospheric profiling.

LEO satellite receivers track GNSS signals using two primary methods: Closed Loop (CL) and Open Loop (OL). CL tracking ensures stable signal acquisition in the upper atmosphere but may fail under rapidly varying conditions in the lower troposphere. OL tracking, by contrast, is specifically designed to capture multipath-affected signals in the lower atmosphere. A combination of CL and OL tracking enables robust performance across the full vertical extent of the atmosphere.

The raw data, consisting of signal phase and amplitude measurements, are processed to calculate bending angle and refractivity profiles. A critical step in this process is correcting ionospheric effects. This is achieved by using dual-frequency signals (e.g., L1 and L2), which allow separation of the frequency-dependent ionospheric interference from the non-dispersive signal of the neutral atmosphere. This isolation is essential for accurate atmospheric retrievals.

### 2.2 RO Data Used in this Study

This study utilizes Level 1b atmospheric excess phase data (in conPhs/atmPhs format) from the ROMEX campaign. The dataset includes contributions from commercial providers, such as PlanetiQ, Spire, and GeoOptics, as well as government-funded missions, including Metop-B/C and COSMIC-2. A summary of mission-specific data coverage for the period 1 September to 30 November 2022 is provided in Table 1. These excess phase datasets, delivered in NetCDF format and available exclusively to ROMEX participants, serve as the primary input for deriving neutral atmospheric bending angle and refractivity profiles. On average, the dataset comprises approximately 37,700 profiles per day.

The high scientific value and cost-effectiveness of GNSS RO technology have driven increased private-sector participation in recent years. U.S. companies Spire Global, PlanetiQ, and GeoOptics, along with Yunyao Aerospace in China, have deployed RO receivers on commercial satellites to supply high-quality data to the scientific community. Among them, Spire Global Inc. contributes approximately 17,000 profiles per day to ROMEX, followed by Yunyao Aerospace with about 6,200, PlanetiQ with about 3,300, and GeoOptics with roughly 300.

Several government-funded RO satellite missions were routinely processed by the UCAR COSMIC Data Analysis and Archive Center (CDAAC) and made available to both the research and operational communities during the ROMEX period. These missions include COSMIC-2 (~6,000 profiles/day), KOMPSAT-5 (~300), PAZ (~200), and both TerraSAR-X and TanDEM-X (~100 each). RO data from Metop-B/C and Sentinel-6 were provided by EUMETSAT, delivering approximately 1,200 and 800 profiles per day, respectively. RO profiles from FY-3C/D/E and Tianmu were supplied by the National Satellite Meteorological Center (NSMC) of the Chinese Meteorological Administration (CMA) and the National Space Science Center (NSSC) of the Chinese Academy of Sciences (CAS), respectively, with average daily counts of approximately 2,100 and 100.



For this study, we processed RO data from all ROMEX missions except Sentinel-6 and GeoOptics, as well as from the Chinese government or Chinese companies (e.g., FY-3, Yunyao, and Tianmu). For each processed mission, we generated bending angle and refractivity profiles using both the STAR RFSI and STAR ROPP (CT2) algorithms. These datasets were submitted to EUMETSAT and distributed to ROMEX participants through the ROM SAF. By processing multiple missions with independent algorithms, we ensured consistent inputs across platforms. We enabled a direct assessment of algorithm-dependent uncertainties, thereby clarifying how data processing influences the interpretation of ROMEX NWP impact experiments.

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Table 1: RO Missions are included in ROMEX

| RO mission         | RO profiles/day | Excess phase provider | STAR ROPP/RFSI | EUMETSAT       |
|--------------------|-----------------|-----------------------|----------------|----------------|
| Metop B, C (GRAS)  | 1200            | EUMETSAT              | √              | √              |
| COSMIC-2           | 6000            | UCAR                  | √              | √ <sup>#</sup> |
| SPIRE              | 17000           | Spire                 | √              | √ <sup>*</sup> |
| PlanetiQ           | 3300            | PlanetiQ              | √              | √ <sup>*</sup> |
| GeoOptics          | 300             | GeoOptics             | x              | √              |
| KOMPSAT-5          | 300             | UCAR                  | √              | √              |
| PAZ                | 200             | UCAR                  | √              | √              |
| TerraSAR-X         | 100             | UCAR                  | √              | √              |
| TanDEM-X           | 100             | UCAR                  | √              | √              |
| Sentinel-6         | 800             | EUMETSAT              | x              | √              |
| FY3-C, D, E (GNOS) | 2100            | CMA/NSMC              | x              | √              |
| Yunyao             | 6200            | Yunyao                | x              | √              |
| Tianmu             | 100             | CAS/NSSC              | x              | √              |
| ROMEX total        | 37700           |                       |                |                |

√<sup>#</sup> UCAR provided both bending angle and refractivity in the EUMETSAT ROMEX dataset.  
 √<sup>\*</sup> No refractivity available in the EUMETSAT dataset for PlanetiQ and Spire, only bending angle

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### 3. Full Spectrum Inversion Algorithm

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The STAR RFSI algorithm provides a robust framework for generating bending-angle and refractivity profiles from GNS RO measurements, particularly in the presence of lower-tropospheric multipath. As described by Chen et al. (2024), the STAR RFSI algorithm has been integrated into ROPP version 10.0 (ROPP, 2020). RFSI processes dual-frequency excess phase and SNR data along with satellite position and timing information. It supports a wide range of satellite missions and tracking configurations.

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The STAR RFSI end-to-end process involves four main steps (see Fig. 1):

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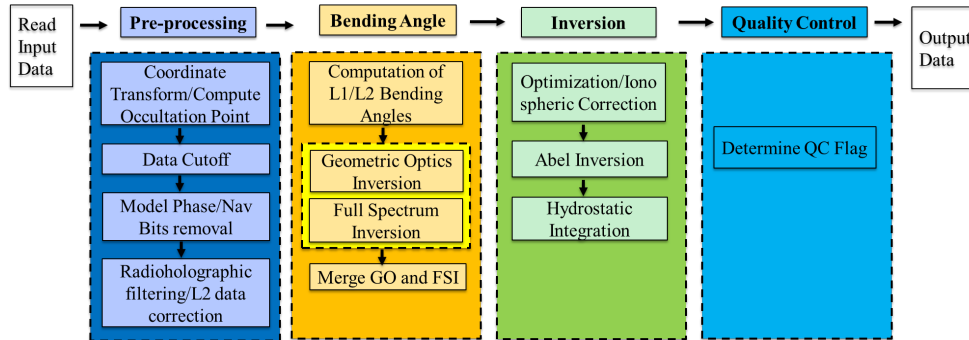
(1) data input and pre-processing: RO data, including satellite geometry, excess phase, and SNR measurements, are ingested and prepared for further processing. Satellite coordinates, if provided at lower frequencies, are interpolated to align with the sampling time using clock bias-corrected transmitter and receiver times (see Section 3.1).

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- (2) bending angle calculation: excess phase data are converted to bending angles, with ionospheric corrections applied using dual-frequency measurements (see Section 3.2).
- (3) inversion to refractivity and dry temperature: bending angles are inverted using Abel integration to derive refractivity profiles, which can subsequently be used to compute dry atmospheric temperature (see Section 3.3).
- (4) quality control (QC): a comprehensive quality assessment is conducted by applying quality flags based on threshold criteria for bending angle differences, determined through comparisons with ERA5 simulations. This process ensures that only high-quality profiles are retained as valid (see Section 3.4). Additionally, we have developed an internal quality control system designed explicitly for near-real-time processing. This internal check was not included in the ROMEX data when it was generated.

Figure 1 illustrates the complete RO data processing workflow implemented in the STAR FSI system, highlighting the transition from raw signal acquisition to the generation of quality-controlled atmospheric profiles (bending angle and refractivity).



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Fig. 1: Flow chart depicting the steps used in the FSI RO data processing of the geometry and phase data.

### 3.1 Data Input and Pre-processing

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The STAR RFSI system ingests Level 1b dual-frequency excess phase and SNR data, along with satellite position and time information, to generate high-resolution atmospheric profiles. The geometry files typically contain satellite position vectors at a lower sampling rate (e.g., 1 Hz), whereas the excess phase and SNR are sampled at higher rates (e.g., 50-100 Hz). To align these data, satellite coordinates are interpolated to the excess-phase sampling times using clock-bias-corrected receiver and transmitter times. Satellite geometry and excess phase/SNR time series are interpolated into a common sampling rate. Given start time ( $t_s$ ), sampling time ( $t$ ), and clock bias-corrected receiver time ( $t_{orb}$ ) and transmitter time ( $t_{txm}$ ). The interpolated receiver coordinates ( $r_{leo}$ ), transmitter time ( $t_{txmHR}$ ), and GNSS coordinates ( $r_{gns}$ ) can be calculated using simple quadratic interpolation as:

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$$r_{leo} = \text{interpolate}(r_{leoLR}, t_{orb}, t + t_s, \text{quadratic}) \quad (1)$$

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$$t_{txmHR} = \text{interpolate}(t_{txm}, t_{orb}, t + t_s) \quad (2)$$

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$$r_{gns} = \text{interpolate}(r_{gnsLR}, t_{txm}, t_{txmHR}, /quadratic) \quad (3)$$

where  $r_{leoLR}$  and  $r_{gnsLR}$  are the original coordinates.

The time series of satellite positions is initially provided in the Earth-Centered Inertial (ECI) J2000 frame. These positions are converted to Earth-Centered Earth-Fixed (ECEF) coordinates according to the IERS 2010 conventions, which include corrections for polar motion and Earth rotation (Adhikari et al., 2021; Petit and Luzum, 2010; Luzum and Petit, 2010). This transformation enables geolocation of the occultation tangent point at each time step.

To satisfy the assumption of local spherical symmetry during inversion, occultation geometry is reprojected to the local center of curvature. The intersection of the line-of-sight with the WGS84 ellipsoid defines the tangent point location. The latitude, longitude, and local radius of curvature are computed at this reference tangent point and used to shift both GNSS and LEO positions into a local spherical coordinate system. This step ensures accurate mapping of impact parameters and tangent altitudes for each ray path.

RO signals acquired using OL tracking may contain low-SNR regions near the surface due to signal fading or tracking loss. To prevent the propagation of noise-contaminated signals through the inversion chain, a systematic signal truncation method is employed using SNR-based thresholds. The truncation procedure includes the following steps: (1) initial cut-off impact height: the initial threshold of impact height is set based on the LEO satellite's altitude, as it influences the signal's penetration depth and the quality of retrieved atmospheric profiles; (2) dynamic background SNR calculation: the background SNR is estimated for each time series using the lowest 10 seconds of the smoothed data. A 3-second moving average is applied to the time series to smooth out high-frequency fluctuations; (3) initial SNR threshold determination: starting from the lowest point in the time series, the first point where the SNR exceeds three times the calculated background SNR in step (2) is identified as a preliminary threshold. (4) final cut-off point selection: moving backward from the uppermost point identified in step (3), the cut-off point is determined as the first point where the SNR drops below 1.5 times the background SNR, and the associated impact height is higher than the threshold established in step (1).

This filtering removes anomalous low-level SNR spikes, which can occur due to OL tracking artifacts, particularly in tropical and high-humidity conditions. Improper truncation can degrade the quality of bending angle measurements: truncating too high removes real signals, introducing a negative bias, while truncating too low retains noise, leading to oscillations in the retrieved profiles. The chosen thresholds aim to maximize vertical coverage without sacrificing data quality.

### 3.2 Computation of Bending Angles using Full Spectrum Inversion

Bending angle retrieval is performed in two steps: (1) computation of the model phase and correction of navigation bit jumps, and (2) inversion of observed signals using FSI to retrieve bending angles as a function of impact parameter.

#### 3.2.1 Calculation of model phase



271 The model phase is derived from a reference refractivity profile computed using the MSIS90  
 272 climatology, assuming 90% relative humidity below 15 km. Refractivity ( $N$ ) is calculated as

$$274 \quad N = 77.6 \frac{P}{T} + 3.73 \times 10^5 \frac{e}{T^2} \quad (4)$$

275  
 276 where  $P$  is pressure,  $T$  is temperature, and  $e$  is water vapor. The model impact parameter ( $a$ ) at  
 277 altitude  $z$  is calculated as

$$278 \quad a = n(R + z) = nr, \quad (5)$$

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 281 where,  $n = 1 + N \times 10^{-6}$ ,  $R$  is the local radius of curvature of the Earth, and  $r = R + z$ .  
 282

283 The bending angle ( $\alpha$ ) profile is derived from  $n$  and  $a$  using Abel integration

$$284 \quad \alpha(p) = 2p \int_{r_1}^{\infty} \frac{a}{\sqrt{n^2 r^2 - a^2}} \frac{dn(n)}{dr} dr, \quad (6)$$

286  
 287 The impact parameter and bending angle profiles, along with occultation time ( $t$ ), satellite  
 288 positions, and velocities, are then used to derive the Doppler shift associated with the  
 289 atmospheric refractivity  $n(z)$ . The model phase, computed from occultation time and the  
 290 Doppler shift, provides a reference for identifying navigation bit jumps.

291  
 292 In most RO data, navigation bits embedded in the excess phase and coordinate time series can  
 293 introduce discontinuities of  $\pm\pi$ . These phase jumps are identified by comparing the measured  
 294 excess phase with the model phase, especially at high sampling rates ( $\geq 50$  Hz). Once detected,  
 295 the navigation bit pattern is applied to correct discontinuities in the measured phase, ensuring  
 296 continuity and accuracy in the processed phase time series.

### 297 298 **3.2.2 Full Spectrum Inversion**

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 300 To retrieve bending angles from RO signals, it is essential to reduce high-frequency noise in  
 301 the excess phase. This is typically achieved using low-pass or radio-holographic filters  
 302 (Gorbunov et al., 2005). In the current RFSI inversion system, a 0.5-second low-pass Fourier  
 303 filter is applied to the excess Doppler signal (the time derivative of excess phase). The filtered  
 304 Doppler is then reintegrated to recover a smoothed excess phase. The 0.5-second window  
 305 approximately matches the vertical resolution of RO observations, corresponding to the first  
 306 Fresnel zone (Kursinski et al., 1997). To better resolve fine-scale refractivity structures in the  
 307 lower atmosphere, a shorter, height-dependent smoothing window is used below 10 km: 0.05  
 308 seconds for 100 Hz data and 0.1 seconds for 50 Hz, enabling noise reduction while preserving  
 309 small-scale features.

310  
 311 Bending angles are computed using geometric optics (GO) above 25 km and the full spectrum  
 312 inversion method below this altitude. In FSI, the received signal is expressed as a sum of  
 313 narrowband sub-signals in the open-angle domain  $\theta$ :

$$314 \quad u(\theta) = \sum_p A_p(\theta) e^{i\varphi_p(\theta)} \quad (7)$$

316  
 317 where,  $A_p$  and  $\varphi_p$  are the amplitude and phase of the  $p$ th sub-signal, respectively. The Fourier  
 318 transform of Eq. (7) is:



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$$320 \quad F(\hat{\omega}) = \sum_p \int_{\theta_1}^{\theta_2} A_p(\theta') e^{i(\varphi_p - \hat{\omega}') d\theta'} \quad (8)$$

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322 where  $\theta_1$  and  $\theta_2$  represent the open angles at the start and end of the occultation, respectively.

323

324 Applying the method of stationary phase (MSP) (Born and Wolf, 1999; Jensen et al., 2003),  
 325 the transform simplifies to:

326

$$327 \quad F(\hat{\omega}) \approx B e^{i(\varphi_q - \hat{\omega}_q \theta_s)} \quad (9)$$

328

329 where  $B$  is an approximately constant amplitude, and the pseudo frequency  $\hat{\omega}_q$  satisfies

330

$$331 \quad \hat{\omega}_q = \left. \frac{d\varphi_q}{d\theta} \right|_{\theta=\theta_s} \quad (10)$$

332

333 The stationary points  $\theta_s$  is then given by:

334

$$335 \quad \theta_s = -\frac{d\psi}{d\hat{\omega}}, \text{ where } \psi = \varphi_q - \hat{\omega}_q \theta_s \quad (11)$$

336

337 The derivative of the phase ( $\varphi_q$ ) with respect to  $\theta$ , accounting for the signal path from the  
 338 GNSS to LEO satellite, is:

339

$$340 \quad \frac{d\varphi_q}{d\theta} = \hat{\omega}_q = ka + k \frac{dR_L}{d\theta} \sqrt{1 - \left(\frac{a}{R_L}\right)^2} + k \frac{dR_G}{d\theta} \sqrt{1 - \left(\frac{a}{R_G}\right)^2}, \quad (12)$$

341

342 where  $k$  is the wavenumber of the carrier signal,  $R_L$  and  $R_G$  are the distances from the GNSS  
 343 and LEO satellites to the local center of curvature, respectively, and  $a$  is the impact parameter.

344

345 Assuming circular orbits, the derivatives of  $R_L$  and  $R_G$  vanish, reducing Eq. (12) to:

346

$$347 \quad \frac{d\varphi_q}{d\theta} = ka \quad (13)$$

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349 Differentiating with respect to  $\hat{\omega}$  gives:

350

$$351 \quad da = \frac{1}{k} d\hat{\omega}, \quad (14)$$

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353 The spectral resolution of the Fourier transform phase,  $d\hat{\omega}$ , is given by (Adhikari et al. 2016):

354

$$355 \quad d\hat{\omega} = \frac{2\pi}{\Delta\theta}, \text{ where } \Delta\theta = \theta_2 - \theta_1 \quad (15)$$

356

357 Finally, with the impact parameter  $a$  and the open angle  $\theta$ , the bending angle is computed as:

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$$359 \quad \alpha(a) = \theta + \arcsin\left(\frac{a}{R_L}\right) + \arcsin\left(\frac{a}{R_G}\right) - \pi. \quad (16)$$

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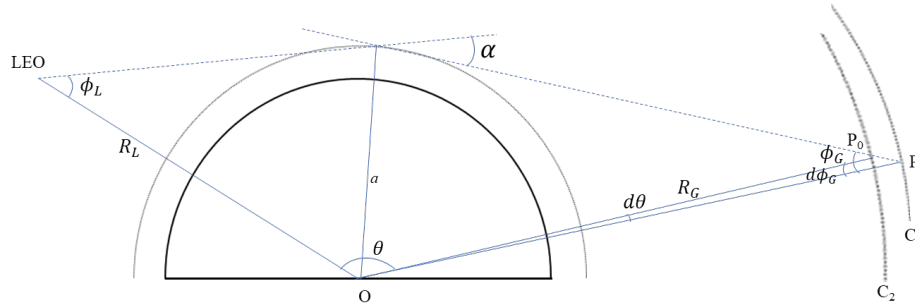
### 361 3.2.3 Correction for non-spherical trajectory

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363 The assumption underlying Eq. (16) is invalid in realistic occultation scenarios due to the  
 364 Earth's oblateness and the non-coplanar nature of GNSS and LEO satellite orbits. To account  
 365 for these effects, a correction must be applied to the observed phase to project the signal path  
 366 onto circular, coplanar trajectories. As illustrated in Fig. 2, the actual GNSS satellite orbit  
 367 is represented by arc  $C_1$ , with each point along the trajectory projected onto a circular orbit,  $C_2$ .  
 368 Notably, the impact parameter ( $a$ ) remains unchanged during this projection. In this process,  
 369 the GNSS position is shifted from  $P_1$  on arc  $C_1$  to  $P_0$  on arc  $C_2$ . This projection alters the open  
 370 angle ( $\theta$ ), the signal ray ( $\phi_G$ ), and the phase of the signal. Although Fig. 2 focuses on the GNSS  
 371 orbit, the same projection method is also applied to the LEO receiver orbit. Given the known  
 372 positions of the GNSS and LEO satellites, the resulting changes in phase and open angles can  
 373 be determined geometrically.

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375

376 Fig. 2: Projection of a non-circular orbit relative to the local center of curvature to a circular  
 377 orbit.

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379 After calculating bending angles for the L1 and L2 frequencies separately, the profiles are  
 380 truncated using the FSI amplitude. This step is necessary because the FSI method produces  
 381 bending angle and impact parameter pairs over an infinite range of impact parameters.  
 382 Determining the lowest impact parameter and its corresponding bending angle is critical. In the  
 383 current STAR FSI inversion approach, the pair with the lowest impact parameter and bending  
 384 angle is identified based on the amplitude of the Fourier transform. The amplitude is first  
 385 normalized using the signal's mean amplitude within the 10-50 km range. The lowest point is  
 386 defined as the location where the amplitude drops below 0.35 of the normalized amplitude.

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### 388 3.2.4 Bending Angle Uncertainty Calculation

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390 The uncertainty in the bending angle is estimated using a sliding spectrogram with a 500 m  
 391 window. First, a smoothed bending angle profile is generated to identify the central component.  
 392 Then, the bending angle from the unsmoothed signal is calculated at 1 m impact height  
 393 resolution. With each spectral window, deviations from the central component are used to  
 394 construct a local power spectrum of the shifted bending angle, computed using a finite bending  
 395 angle increment ( $\delta\alpha = 0.0005$  rad). The spectral width ( $\Delta s$ ) is determined as the mean of the  
 396 absolute value of the shifted bending angle ( $\alpha$ ) weighted by the spectral power ( $\rho$ ) of each  
 397 component, as follows:

398

$$399 \Delta s = \sqrt{\frac{\sum_{i=1}^n \rho_i \alpha^2 \delta\alpha}{\sum_{i=1}^n \rho_i \delta\alpha}} \quad (17)$$

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Figure 3(a) presents a representative bending angle profile at 1 m resolution as a function of the impact height (black dots), along with its central component (red line). Figure 3(b) and 3(c) show the corresponding normalized power spectrum (black line) and accumulated power spectrum (red line) at impact heights of 3 km and 7 km, respectively. As illustrated, the spectral range at 3 km is broader than at 7 km, indicating greater atmospheric variability at lower altitudes. The bending angle uncertainty is quantified as half the spectral width, calculated using Eq. (17).

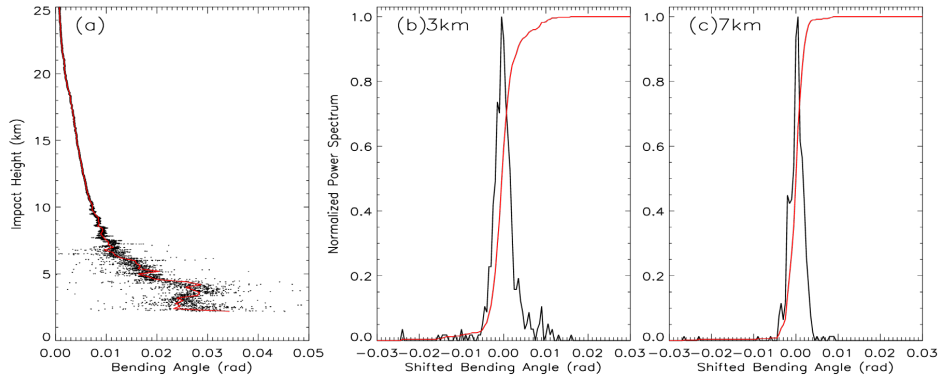


Fig. 3: (a) Spectrogram of the RO signal, power spectrum at (b) 3 km, and (c) 7.5 km impact heights.

### 3.3 Bending angle Inversion

#### 3.3.1 Ionospheric Correction and Optimization

To remove first-order ionospheric effects, a linear combination of L1 and L2 bending angles ( $\alpha_1(a)$  and  $\alpha_2(a)$ ) is computed:

$$\alpha_{LC}(a) = \frac{\alpha_1(a)f_1^2 - \alpha_2(a)f_2^2}{f_1^2 - f_2^2} \quad (18)$$

where  $f_1$  and  $f_2$  are the RO frequencies.

This is followed by statistical optimization (Gorbunov, 2002c):

$$\alpha(a) = \alpha_{BG(a)} + \frac{\sigma^S}{\sigma^S + \sigma^N} (\alpha_{LC}(a) - \alpha_{BG}(a)) \quad (19)$$

where,  $\sigma^S$  and  $\sigma^N$  are the covariances of the neutral atmospheric signal and residual noise, respectively, and  $\alpha_{BG}(a)$  is the background bending angle from a climatological model.

Covariance matrices are estimated from the deviation ( $\Delta\alpha$ ) of L1 and L2 bending angles from the background model ( $\alpha_{L1,L2} - \alpha_m$ ). For ionospheric signal and noise, deviations in the impact heights (impact parameter minus local center of curvature) of 50-70 km are used; for neutral atmospheric signal, the 12-35 km range is used. In the lower troposphere, near the surface, where the L2 signals weaken, a constant correction is applied based on the lowest valid L2 altitude.



### 3.3.2 Abel Inversion

Refractivity is retrieved from ionosphere-corrected bending angles using the Abel transform (Fjeldbo et al., 1971). The bending angle profile is extended up to 150 km using climatological data to stabilize the upper boundary condition. Tangent point locations are recovered by interpolating the occultation time and satellite positions. Since time information is lost during the Fourier transform of the RO signal, the occultation time is reconstructed from the bending angle-impact parameter profile and used to infer the latitude and longitude of each tangent point.

### 3.4 Quality control

Due to the lack of effective internal quality control in the ROPP v10 package, we rely on external quality control procedures to identify bad profiles. The fractional difference between the observed (O) and simulated (B) bending angles, calculated from ERA5 forecast fields, is used to assess the quality of the RO data at each altitude level:

$$BA_{diff} = \frac{O-B}{B} \quad (20)$$

Figure 4 shows the monthly mean standard deviation of the fractional bending angle differences for 2020, from 8 to 43 km altitude. The annual mean standard deviation ( $\sigma_{year}$ ) is used as a benchmark. A profile is flagged as ‘bad’ if the bending angle difference exceeds  $7\sigma_{year}$  at any altitude level between 10 and 40 km, where RO data quality is highest and model-observation agreement is strongest. A sensitivity study confirmed that using a  $7\sigma$  year threshold provides an optimal balance between data retention and data quality.

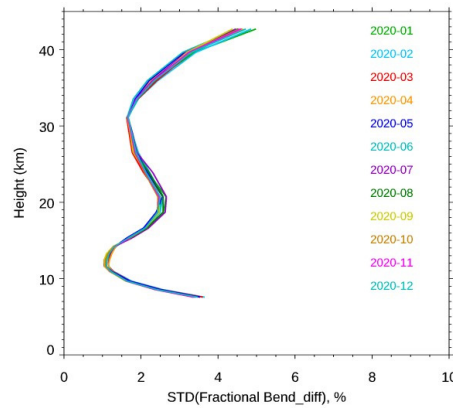


Fig. 4. Monthly standard deviation of the fractional bending angle differences in 2020.

In addition, profiles are also flagged as ‘bad’ under any of the following conditions: (1) Model simulation data is unavailable; (2) The fractional BA difference exceeds  $7\sigma_{year}$ ; (3) The top height of the profile is below 20 km; (4) The bottom height is above 20 km; and (5) A negative bending angle is detected below 50 km.

It is important to note that this quality control procedure applies only to bending angles within a specific height range (10–40 km). In rare cases, even when the bending angle passes QC,



anomalies in refractivity or dry temperature may still occur due to limitations in the Abel inversion. Future updates to the QC procedures will address such issues. This process ensures that only high-quality profiles are retained as valid. An internal quality control system tailored for near-real-time processing is under development; however, it was not incorporated into the ROMEX data when that dataset was produced.

## 4. Comparison Results

### 4.1 Bending angle comparison with STAR RFSI, STAR ROPP, and EUMETSAT

Figure 5 shows the height-dependent fractional bending angle differences between RO observations and ERA5 background fields (O-B) for multiple satellite missions processed using the RFSI algorithm during November 2022. The selected missions include COSMIC-2, Spire, PlanetiQ, Metop-B, Metop-C, Kompsat5, PAZ, TerraSAR-X, and TanDEM-X. The comparison serves as a proxy for evaluating the quality and inter-mission consistency of RFSI-processed RO data relative to a widely used global reanalysis.

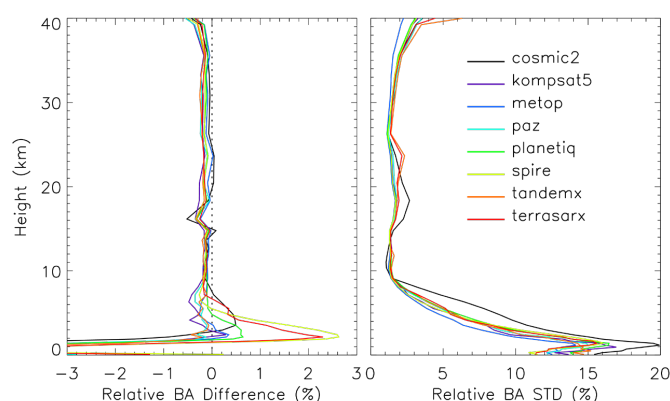


Fig. 5. Comparison of height-dependent fractional bending angle between RO observations and ERA5 simulations (O-B) among different RO missions. BA mean biases (left) and standard deviations (right) in terms of fractional BA difference (%) for RFSI over November 2022.

In the middle and upper troposphere through the lower stratosphere (8-35 km), all missions exhibit excellent agreement with ERA5. Mean O-B differences are generally within  $\pm 0.2\%$ , and standard deviations remain below 3%, indicating high internal consistency among the RO datasets and strong alignment with ERA5 in this well-observed atmospheric region.

In the lower troposphere (below 8 km), larger biases and variability are evident, especially near the surface. Spire and TerraSAR-X show mean biases up to 1-2% at 2 km, with standard deviations exceeding 10%. COMSIC-2 exhibits the highest variability in this region, with standard deviations approaching 20% at approximately 1 km. These discrepancies are likely attributed to increased atmospheric variability in the boundary layer, limitations in signal tracking during multipath propagation, and the sensitivity of bending angle retrievals to SNR cut-off thresholds. In contrast, PlanetiQ, Metop-B, and Metop-C demonstrate smaller near-surface biases (typically  $<0.5\%$ ) and reduced variability, suggesting robust signal tracking and/or more effective pre-processing of low-altitude data.



Above 35 km, mean biases increase to approximately 0.6%, and standard deviations increase with height and can exceed 5% at 40 km. These deviations are primarily due to limitations in ionospheric correction at higher altitudes, where residual ionospheric effects are more challenging to remove completely.

Among the evaluated missions, PlanetiQ consistently shows low mean biases and standard deviations across nearly the entire vertical range, indicating strong data stability and processing robustness. Metop-B and Metop-C also exhibit excellent performance, likely due to mature sensor platforms and the use of well-established pre-processing procedures in the ROPP system. Spire data, while reliable in the mid- to upper troposphere, shows elevated near-surface variability, likely due to its higher sensitivity to excess phase pre-processing (e.g., cycle-slip removal and parameter tuning).

COSMIC-2 displays distinct behavior relative to other missions, with positive biases of 8-35 km and increased variability near the tropopause. These features are likely influenced by its low-inclination orbit and limited latitudinal coverage ( $\pm 45^\circ$ ), which concentrates observations in tropical and subtropical regions with higher atmospheric variability. Similar features and their impact on data assimilation performance have been discussed in previous studies (Ho et al., 2023; Miller et al., 2025).

Figure 6 shows O-B bending angle differences for the same missions and period, but with data processed using the ROPP-CT2 method. The vertical structure of mean biases and variability is broadly similar to that in the RFSI results, reflecting consistent retrieval behavior between the two approaches. In the 8-35 km range, both methods yield small biases (within  $\pm 0.2\%$ ) and standard deviations below 3%, confirming the reliability of both retrievals in the core atmospheric region. One exception is KOMPSAT-5, which shows a slight negative bias ( $\sim -0.2\%$ ) between 17 and 23 km.

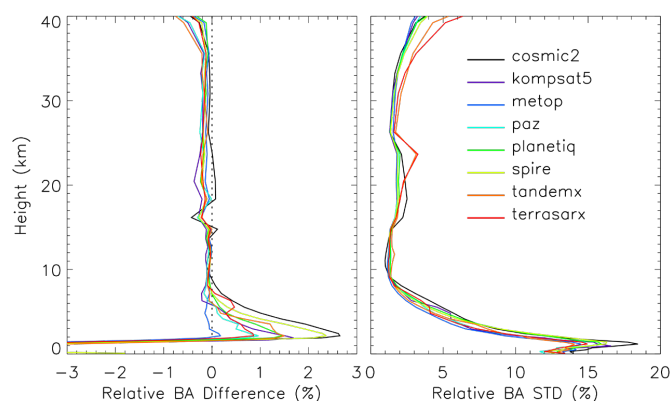


Fig. 6. Same as Fig. 5, but for RO data generated from the ROPP package using the CT2 method.

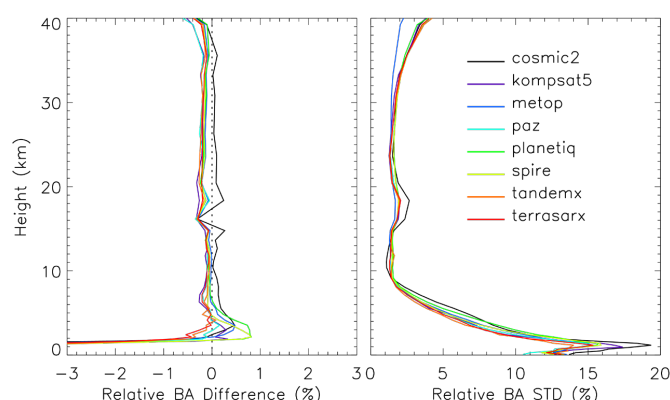
Standard deviations increase above 35 km and below 8 km in both datasets, highlighting common challenges in the upper and lower atmospheric regions, including multipath effects, signal noise, and uncertainty in ionospheric corrections. However, the CT2 retrievals generally exhibit larger near-surface biases than those of RFSI. For all missions except Metop-B and Metop-C, the CT2-processed profiles exhibit biases of 1-2% near the surface, likely due to the more conservative use of signals and stronger smoothing.



547

548 Figure 7 displays ERA5 O-B differences for RO profiles processed by EUMETSAT, covering  
 549 the same missions and period. Like the other two datasets, EUMETSAT results show high  
 550 consistency in the 8-35 km range, with mean biases within  $\pm 0.2\%$  and standard deviations  
 551 below 3%. COSMIC-2 again stands out, showing a positive bias of  $\sim 0.2\%$ , while most other  
 552 missions exhibit slightly negative biases, suggesting a systematic offset in COSMIC-2 data  
 553 relative to the ensemble.

554



555

556 Fig. 7. Same as Fig. 5, but for RO data provided from EUMETSAT.

557

558 In the lower troposphere, EUMETSAT retrievals exhibit the smallest mean biases ( $<1\%$  at 2  
 559 km) among the three datasets, suggesting more effective mitigation of noise and multipath  
 560 effects near the surface. By comparison, RFSI-processed profiles for Spire and TerraSAR-X  
 561 show near-surface biases of up to  $\sim 2\%$ , while CT2 retrievals yield 1-2% biases for most  
 562 missions. COSMIC-2 exhibits high variability below 8 km across all three datasets, although  
 563 the CT2 method appears to reduce it slightly.

564

565 Above 35 km, the bending angle uncertainty increases in all datasets. However, EUMETSAT  
 566 results exhibit more uniform performance across missions, with mean biases generally below  
 567 0.5% and smaller inter-mission variability. Metop-B and Metop-C show the lowest standard  
 568 deviations across all datasets in this altitude range, indicating highly stable performance at high  
 569 altitudes.

570

571 Together, these intercomparisons highlight key trade-offs among the different retrieval  
 572 approaches. The RFSI method leverages the full frequency content of the RO signal, offering  
 573 enhanced sensitivity to fine-scale atmospheric features. However, it is also more sensitive to  
 574 noise, particularly near the surface. In contrast, the CT2 method employs a canonical  
 575 transformation that simplifies retrieval but is more conservative in its use of signal data,  
 576 resulting in smoother profiles and slightly larger near-surface biases. EUMETSAT's  
 577 processing strikes a balance between these extremes, achieving consistent results across the  
 578 full vertical range while effectively suppressing noise in the lower troposphere and upper  
 579 stratosphere.

580

#### 581 4.2 Refractivity comparison with STAR RFSI, STAR ROPP, and EUMETSAT

582

583 Figure 8 presents the fractional refractivity differences between RO observations processed  
 584 using the RFSI algorithm and ERA5 background fields for November 2022. The vertical



structures of refractivity O-B statistics largely mirror those of the bending angle differences shown in Fig. 5, reflecting the propagation of bending angle quality into the refractivity retrieval. In the well-constrained 8-30 km region, all missions show excellent agreement with ERA5. Mean biases remain within  $\pm 0.15\%$ , and standard deviations are typically below 1%, indicating that refractivity retrievals in this core region retain the stability and consistency of the underlying bending angle data.

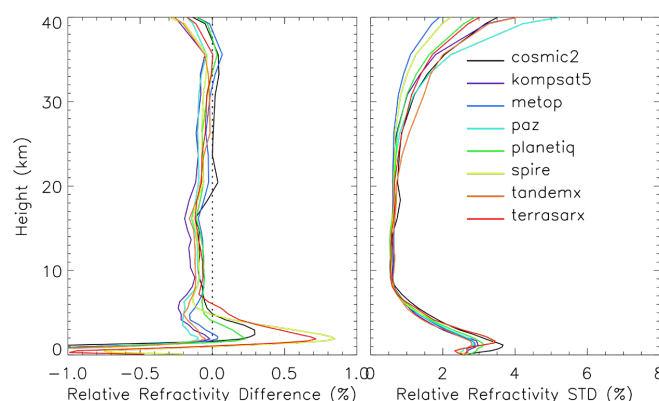


Fig. 8. Comparison of height-dependent fractional refractivity between RO observations and ERA5 simulations (O-B) among different RO missions. Refractivity mean biases (left) and standard deviations (right) in terms of fractional difference (%) for RFSI over November 2022.

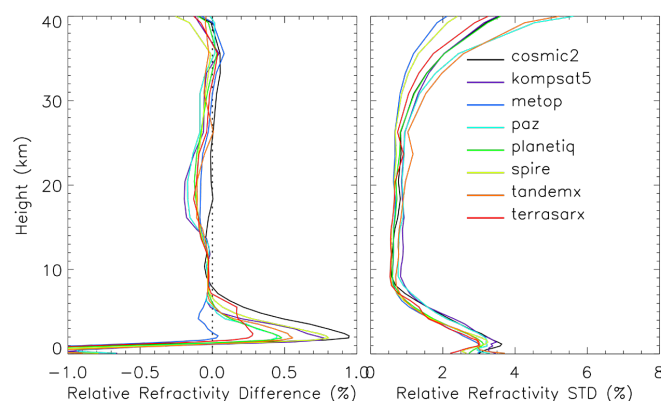
In the lower troposphere (below  $\sim 8$  km), refractivity differences exhibit a significantly larger inter-mission spread, consistent with Fig. 5, although both biases and standard deviations are generally reduced. Spire and TerraSAR-X exhibit the most pronounced positive biases, reaching  $\sim 0.7$ - $0.8\%$  near 2 km, along with elevated standard deviations exceeding 3%. COSMIC-2 again exhibits high variability below 5 km, with standard deviations peaking at over 3.5% near 1 km. However, its mean refractivity bias remains relatively small compared to those from Spire or TerraSAR-X, suggesting increased random error rather than systematic offset.

In the upper atmosphere (above  $\sim 35$  km), where refractivity is less sensitive to the RO signal due to the exponential decrease in atmospheric density, the mean biases for all missions begin to increase negatively, reaching values of  $\sim -0.2\%$  to  $-0.4\%$  near 40 km. Standard deviations also rise, ranging from  $\sim 2\%$  to 5%, consistent with the increased variability observed in the bending angle differences shown in Fig. 5. These errors are primarily attributed to residual ionospheric correction uncertainties and the influence of high-altitude extrapolation assumptions in the RFSI algorithm. The use of climatological models in the upper atmosphere also introduces additional variability, as refractivity becomes more sensitive to model inaccuracies in this region.

Figure 9 shows the refractivity O-B differences derived from RO data processed with the ROPP CT2 method. Between 8 and 15 km, CT2 results exhibit improved inter-mission consistency in mean bias compared to RFSI, although the standard deviations are generally larger. In the lower troposphere (below  $\sim 8$  km), CT2 retrievals produce larger positive biases, typically around 0.5-1% near 2 km (except for Metop-B, Metop-C, and TerraSAR-X), with the largest bias observed for COSMIC-2 ( $\sim 1\%$ ). These biases are notably larger than those from RFSI,

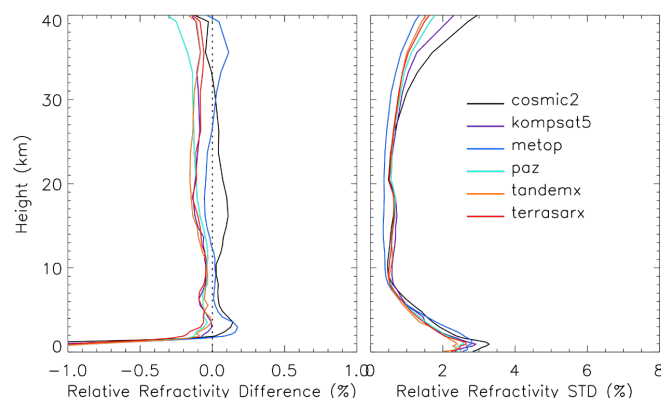


623 which remain below 0.3% for most missions, except for Spire and TerraSAR-X. Between 15-  
 624 25 km, the CT2 results show a greater inter-mission spread in both mean bias and standard  
 625 deviation compared to RFSI. Above 25 km, CT2 and RFSI show broadly similar behavior,  
 626 with rising uncertainty consistent with bending angle trends.  
 627



628  
 629 Fig. 9. Same as Fig. 8, but for RO refractivity processed using the ROPP package with the CT2  
 630 method.  
 631

632 Figure 10 presents the refractivity O-B differences from the EUMETSAT dataset. Note that  
 633 refractivity profiles are not available for PlanetiQ and Spire in this dataset. Similar to bending  
 634 angle results, COSMIC-2 exhibits a distinct positive bias in the 4-30 km region, along with a  
 635 notably larger inter-missions spread in the 8-40 km range compared to CT2 (Fig. 9) and RFSI  
 636 (Fig. 8) results. In contrast, in the lower troposphere (below ~8 km), the EUMETSAT retrievals  
 637 show the smallest near-surface mean biases, generally within  $\pm 0.2\%$  above 2.5 km, and the  
 638 lowest standard deviation across all available missions. These results suggest that the  
 639 refractivity data from EUMETSAT are particularly effective at mitigating noise and multipath  
 640 effects near the surface.  
 641



642  
 643 Fig. 10. Same as Fig. 8, but for RO data provided from EUMETSAT. Note that refractivity  
 644 data is not available in the EUMETSAT dataset for PlanetiQ and Spire.  
 645

646 Taken together, the comparisons between Figs. 5 and 8, Figs. 6 and 9, and Figs. 7 and 10 reveal  
 647 that many mission-specific features observed in bending angle retrievals persist in the



refractivity domain. This reinforces the importance of bending angle quality, particularly near the surface and in the upper atmosphere, for achieving accurate refractivity retrievals. The heightened sensitivity of refractivity to small-scale errors at the profile boundaries also underscores the need for robust quality control, optimized signal tracking, and careful algorithm design in future RO missions and processing systems.

### 4.3 Structural Uncertainty among Different Processing Methods

Figures 11-15 illustrate the structural bending angle uncertainty associated with the ROPP (CT2), RFSI, and EUMETSAT processing algorithms for five representative GNSS RO missions: COSMIC-2, Spire, PlanetiQ, Metop-B, and Metop-C. For each mission, the figure shows the height-dependent relative mean differences and standard deviations of bending angles with respect to the three-dataset mean, along with the number of common profiles processed for each algorithm.

Several important structural differences emerge from these comparisons:

For COSMIC-2 (Fig. 11), the three processing methods demonstrate strong consistency in the middle and upper troposphere and stratosphere (above ~10 km), where both the relative differences and standard deviations of bending angles remain below approximately 0.1% and 1%, respectively, indicating minimal structural uncertainty. Below 10 km, method-dependent differences become more pronounced. The largest deviations are observed near the surface, with relative differences of approximately 1.5% for ROPP, -1.0% for EUMETSAT, and -0.5% for RFSI. Additionally, the ROPP algorithm exhibits higher bending angle standard deviations in the lowest 10 km, indicating greater sensitivity to retrieval ambiguities under conditions of multipath propagation. In contrast, above 25 km, ROPP shows slightly lower standard deviations than RFSI and EUMETSAT. Despite these lower-tropospheric differences, the overall structural agreement among the three COSMIC-2 processing methods is robust. Although the number of available profiles (right panel) decreases significantly near the surface, sufficient observations are present throughout the vertical domain to enable meaningful statistical comparisons.

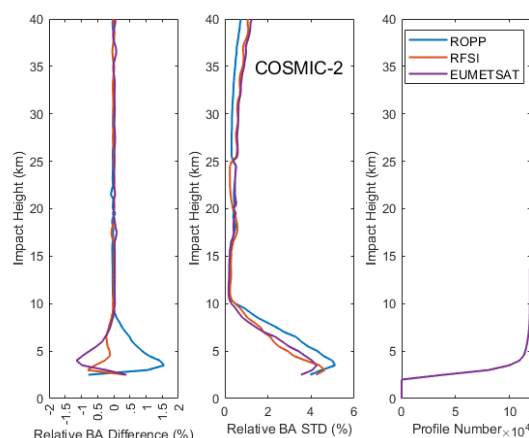
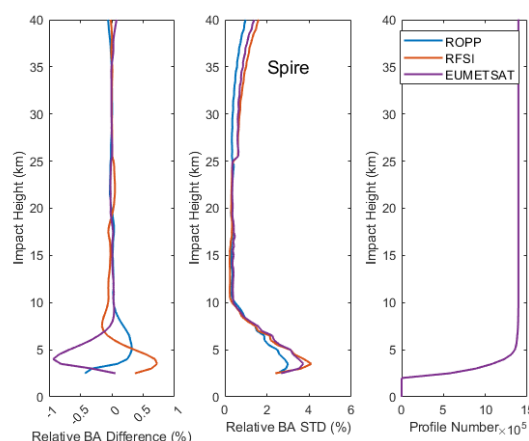


Fig. 11. Structural bending angle uncertainty among different processing methods for COSMIC-2. Note that the bending angle profiles from the EUMETSAT dataset are processed by the UCAR CDAAC using the phase-matching method.



683 For Spire (Fig. 12), a similar pattern of agreement is observed. Above approximately 10 km,  
 684 the relative bending angle differences across the three methods are generally within  $\pm 0.1\%$ ,  
 685 and the standard deviations remain below 1% up to approximately 35 km, indicating good  
 686 consistency in the upper atmosphere. However, RFSI exhibits a distinct pattern in the 8-25 km  
 687 range, with a relative positive difference in the 19-25 km region and a negative difference in  
 688 the 8-19 km region, compared to the nearly identical ROPP and EUMETSAT solutions. As  
 689 with COSMIC-2, larger discrepancies emerge below 10 km. Notably, the ROPP and RFSI  
 690 solutions show small positive differences near the surface (up to  $\sim 0.7\%$  and  $\sim 0.3\%$ ,  
 691 respectively), whereas the EUMETSAT solution exhibits a negative deviation of up to  $-1.0\%$ .  
 692 The bending angle standard deviations in the lower troposphere are higher for RFSI and  
 693 EUMETSAT, reaching  $\sim 4\%$ , while ROPP shows slightly lower variability (below 3%) near  
 694 the surface. Above 25 km, ROPP again yields lower standard deviations compared to the other  
 695 two methods, consistent with the COSMIC-2 results.



696  
 697 Fig. 12. Same as Fig. 11, but for Spire.  
 698

699 For PlanetiQ (Fig. 13), a higher level of consistency is observed among the three processing  
 700 methods across the vertical profile compared to those from COSMIC-2 and Spire. Above  
 701  $\sim 10$  km, the solutions are nearly identical, except for a slight positive deviation in the 19-25 km  
 702 region from the RFSI solution. Relative bending angle differences remain within  $\pm 0.05\%$ , and  
 703 standard deviations are below 1% up to  $\sim 38$  km, indicating excellent agreement in the middle  
 704 and upper atmosphere. Below 10 km, small but systematic differences become evident. The  
 705 ROPP solution shows a modest positive bias, peaking at approximately  $+0.4\%$  near a 3 km  
 706 impact height, while the RFSI solution exhibits a slight negative bias of similar magnitude.  
 707 The EUMETSAT data remain close to zero throughout this region. As with COSMIC-2, the  
 708 standard deviations increase toward the surface, with ROPP exhibiting greater variability  
 709 below 10 km than RFSI and EUMETSAT. However, for PlanetiQ, the overall variability is  
 710 lower, reaching a standard deviation of  $\sim 3\%$  near the surface. This improved consistency  
 711 suggests enhanced robustness in PlanetiQ's onboard processing, a more stable tracking  
 712 geometry and antenna design, and larger SNR, which may reduce sensitivity to retrieval  
 713 algorithm differences.

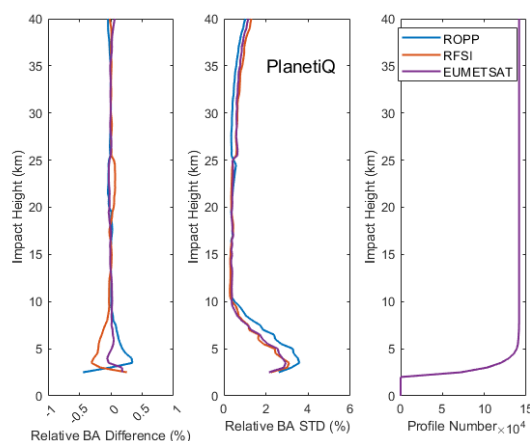
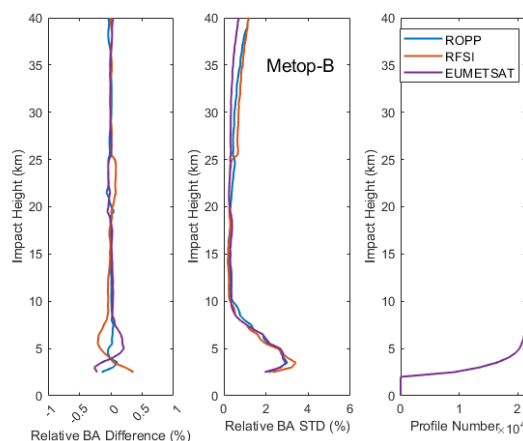


Fig. 13. Same as Fig. 11, but for PlanetiQ.

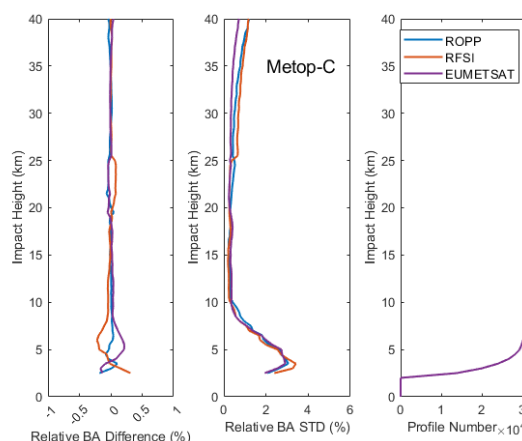
Metop-B (Fig. 14) and Metop-C (Fig. 15), both long-operational polar-orbiting satellites with mature and well-characterized instrumentation, exhibit nearly identical inter-method structural uncertainties. For brevity, the discussion here focuses on Metop-B. While broad similarities exist across the three processing methods, structural differences are more pronounced for Metop-B than for the highly consistent PlanetiQ results. Below an impact height of  $\sim 8$  km, the standard deviation profiles from all three algorithms converge closely, indicating similar variability near the surface. Relative bending angle differences show a maximum positive deviation of approximately  $+0.2\%$  for the EUMETSAT solution and a negative deviation of about  $-0.2\%$  for RFSI near 5 km.

In contrast, the ROPP solution remains close to zero. A slight negative bias is also observed in the RFSI solution below  $\sim 13$  km ( $\sim -0.1\%$ ). In the upper stratosphere, above 25 km, a clear separation in variability emerges: RFSI exhibits the largest standard deviations, followed by ROPP, with EUMETSAT showing the lowest variability. This divergence suggests that the upper-atmospheric retrievals are more sensitive to processing methodology in the case of Metop-B.





734 Fig. 14. Same as Fig. 11, but for Metop-B.  
 735



736  
 737 Fig. 15. Same as Fig. 11, but for Metop-C.  
 738

739 Except for COSMIC-2, RFSI shows a small positive bias ( $<0.1\%$ ) at 20–25 km for Spire,  
 740 PlanetiQ, and Metop-B/C relative to STAR ROPP and EUMETSAT. Possible causes include  
 741 spectral windowing and filtering choices, as RFSI applies a sliding polynomial filter below 25  
 742 km and an optimal estimation filter above, which can introduce systematic offsets. Degraded  
 743 L2 signals and reduced GNSS SNR above  $\sim 20$  km further amplify noise, and because FSI is  
 744 more noise-sensitive than geometric optics or canonical transform methods, incomplete noise  
 745 suppression may yield small positive biases. The exact causes are under active investigation to  
 746 further mitigate this effect.

747 These results highlight that structural uncertainty is both algorithm- and mission-dependent,  
 748 influenced by signal quality, onboard processing, antenna design, and orbit characteristics. The  
 749 findings highlight the crucial role of processing methodology in ensuring consistency and  
 750 accuracy in retrieving RO bending angle data, particularly when data from diverse missions  
 751 are used in operational weather forecasting systems. Future efforts in GNSS RO should focus  
 752 on developing harmonized processing standards and conducting inter-comparison studies to  
 753 quantify and mitigate structural uncertainty in bending angle datasets.

## 754 5. Discussions and Summary

755  
 756 This study presents the first comprehensive cross-mission intercomparison of the STAR-  
 757 developed Full Spectrum Inversion algorithm with the community-standard ROPP CT2 and  
 758 EUMETSAT dataset within the framework of ROMEX. Using bending angle and refractivity  
 759 profiles from key GNSS RO missions (e.g., COSMIC-2, Spire, PlanetiQ, Metop-B/C) during  
 760 the ROMEX period (September–November 2022), we assessed inter-algorithm consistency  
 761 against ERA5 reanalysis and structural uncertainty against the three-dataset mean.  
 762

763 A significant finding is the excellent agreement among all three processing methods in the  
 764 middle and upper troposphere and lower stratosphere (8–35 km). In this region, the mean  
 765 bending angle differences remained within  $\pm 0.2\%$  and the standard deviations were below 3%,  
 766 demonstrating the maturity and robust internal coherence of RO observations across diverse  
 767



missions. Similarly, refractivity retrievals in this core region exhibited high stability, with mean biases within  $\pm 0.15\%$  and standard deviations typically below 1%.

Anthes et al. (2025) reported that the UCAR-processed COSMIC-2 bending angles included in ROMEX exhibit a positive bias of approximately  $+0.1$ – $0.15\%$  relative to ERA5 in the lower stratosphere, larger than the biases seen for Spire and other ROMEX datasets. Similar lower-stratospheric positive biases for UCAR COSMIC-2 have also been documented by Ho et al. (2024, 2025). Figure 16 provides a zoomed-in comparison of the height-dependent fractional O–B bending-angle differences for the COSMIC-2, Spire, and PlanetiQ missions, between the EUMETSAT/UCAR processing and the STAR RFSI processing. In Fig. 16a, the COSMIC-2 data are from UCAR, while the Spire and PlanetiQ datasets are processed by EUMETSAT; in Fig. 16b, all three missions are processed consistently by STAR RFSI.

While the UCAR-provided COSMIC-2 ROMEX datasets show a small positive O–B bias compared to EUMETSAT-processed Spire and PlanetiQ data in the lower stratosphere (Fig. 16a), the STAR RFSI-processed COSMIC-2 bending angles exhibit improved consistency with the Spire and PlanetiQ results (Fig. 16b). The underlying cause of the subtle differences in lower-stratospheric O–B bending-angle among the processing centers (STAR, EUMETSAT, UCAR) will be further examined in future work.

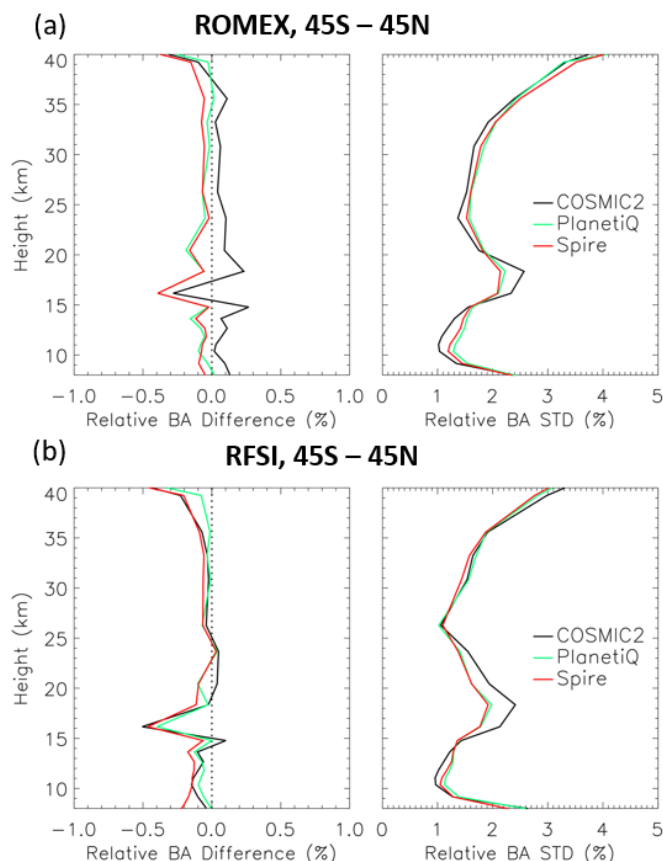


Fig. 16. Zoomed-in height-dependent fractional bending-angle differences (O–B) between RO observations and ERA5 simulations are shown for COSMIC-2, Spire, and PlanetiQ. Panels (a)



791 and (b) display the mean bending-angle biases (left) and standard deviations (right) for RO  
 792 data processed by EUMETSAT and by STAR RFSI, respectively.

793  
 794 Conversely, larger discrepancies and heightened variability emerged in the lower troposphere  
 795 (below ~8 km) and upper atmosphere (above ~35 km). These regions are challenged by  
 796 multipath effects, increased tracking noise, and varying SNR. The FSI method, designed to  
 797 resolve fine-scale atmospheric structures by leveraging full-spectrum signal information,  
 798 demonstrated improved sensitivity in the lower atmosphere, particularly for missions such as  
 799 PlanetiQ and Metop-B/C. However, it also showed increased variability and greater  
 800 dependence on SNR cut-off and quality control thresholds, as seen with Spire and TerraSAR-  
 801 X near the surface. In contrast, the CT2 method, while generally yielding smoother profiles  
 802 with reduced noise, sometimes showed larger near-surface biases (e.g., CT2 for COSMIC-2  
 803 and Spire), suggesting a more conservative approach that might underestimate bending in  
 804 complex conditions. EUMETSAT's dataset, in particular, achieved the smallest near-surface  
 805 bending angle and refractivity biases across missions, indicating effective mitigation of noise  
 806 and multipath.

807  
 808 A crucial finding of this study is that structural uncertainty depends on both the processing  
 809 algorithm and the satellite mission. A greater inter-method spread was observed across all  
 810 missions below 8 km, likely due to their distinct approaches to handling multipath, noise, and  
 811 signal truncation. This structural uncertainty complicates the consistent use of multi-mission  
 812 RO data. For instance, COSMIC-2 data processed by ROPP CT2 showed higher near-surface  
 813 variability than those processed by RFSI and EUMETSAT. In contrast, missions like Metop-  
 814 B/C exhibited stronger consistency across all three methods, while PlanetiQ demonstrated the  
 815 highest inter-method consistency throughout the profile. These mission-specific patterns,  
 816 clearly illustrated in Figs. 11-15, underscore the critical need to characterize and account for  
 817 algorithmic effects when assimilating multi-mission RO data into operational weather  
 818 forecasting systems.

819  
 820 The ROMEX results unequivocally highlight the importance of quantifying algorithm-related  
 821 structural uncertainty for data assimilation applications. To ensure a consistent and optimal  
 822 representation of RO data in numerical weather prediction systems, it may be necessary to  
 823 harmonize retrieval strategies across different processing centers or to apply mission- and  
 824 algorithm-specific bias corrections.

825  
 826 The successful integration of STAR's FSI algorithm into ROPP version 10.0 represents a  
 827 significant advancement, providing users with a robust and flexible alternative to existing  
 828 algorithms. This enhancement facilitates consistent RO data processing across both  
 829 government-funded and commercial missions, offering customizable settings to meet specific  
 830 scientific and operational requirements.

831  
 832 In summary, this study demonstrates the critical influence of algorithm choice, particularly in  
 833 the lower troposphere; confirms strong consistency among processors in the mid-to-upper  
 834 atmosphere; identifies distinct mission-dependent structural uncertainties; and recommends  
 835 applying bias correction or ensemble strategies to improve data assimilation. The findings  
 836 strongly support continued efforts to harmonize across agencies through collaborative  
 837 initiatives, such as ROMEX. As the volume and diversity of GNSS RO data continue to  
 838 expand, these insights underscore the paramount need for robust algorithm development,  
 839 thorough uncertainty quantification, and coordinated processing strategies to fully leverage RO  
 840 observations and advance weather forecasting and climate monitoring capabilities.



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