

A spatiotemporal analysis of errors in InSAR SWE measurements caused by non-snow phase changes

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Abstract. Spatially distributed measurements of snow water equivalent (SWE) in mountainous terrain are not currently feasible from existing satellite platforms. The NISAR satellite has the potential to provide high resolution (80 m) SWE measurements on a 12-day orbit cycle over many of Earth's snowy regions, which would represent a new era of spaceborne snow monitoring. The most promising approach for NISAR SWE measurements uses interferometric synthetic aperture radar (InSAR) techniques to derive the 12-day change in SWE (Δ SWE) from the change in phase between two SAR acquisitions. However, many non-snow factors can also change in this 12-day period which subsequently modulate the SAR phase. These non-snow factors can vary differently in both space and time, and in turn introduce spatially and temporally variable errors into InSAR-derived Δ SWE measurements. Here we explore the effects of six non-snow factors that can affect InSAR phase: electron content of the ionosphere, atmospheric water vapor, atmospheric pressure, soil permittivity, vegetation permittivity, and surface deformation. We show how these factors affect phase-based SWE measurements at 13 SNOTEL stations across the western US, as well as regionally across North America. We consider errors resulting from ~~a~~ individual 12-day ~~baselines~~ periods, as well as the cumulative effects of ~~these~~ ~~the~~ errors when a timeseries of Δ SWE measurements ~~are~~ ~~is~~ integrated to derive peak seasonal SWE.

~~The ionospheric effect results~~ Ionosphere effects result in the largest cumulative error at all ~~stations~~ SNOTEL stations in our analysis, with changes in the total electron content resulting in phase changes equivalent to 0.271–0.414 m of SWE, or more than 500% larger than the median April 1 SWE at some shallow snow stations. When ~~ionospheric~~ ionosphere effects are removed, the remaining cumulative error ranges from –0.074–0.022 m of SWE, equivalent to 0–89% of April 1 SWE, ~~with results~~. Relative error results are affected primarily by differences in peak SWE rather than differences in absolute error values. ~~Individual error components can show offsetting effects, where positive and negative biases partially cancel out to result in a lower total cumulative error.~~ For a randomly selected 12-day baseline period, exceedance probability analysis shows that there is a 50% chance the ionospheric component introduces an error larger than 0.211 m into the overall Δ SWE measurement, while the remaining five components have a 50% exceedance probability of 0.031 m. We also find that individual error components can show offsetting effects, where positive and negative biases partially cancel out to lower the total cumulative error. Accurate Δ SWE measurements using NISAR data will not be possible unless ionospheric effects can be appropriately addressed. Removal of other error sources requires careful consideration of the SWE monitoring application: for tracking ~~total~~ seasonal

SWE accumulation in areas with deeper snowpacks, correcting some errors but not others may actually decrease accuracy by removing offsetting cumulative effects. For individual 12-day ~~baselines, removing as many errors as possible will generally lead to improved accuracy~~ periods, wet and dry tropospheric effects (due to changes in water vapor and pressure) should be removed for accurate interpretation of spatial patterns of snow accumulation at basin to range scales, and site-specific factors should be considered to assess the relative influence of vegetation, soils, and surface deformation.

1 Introduction

~~Current measurement capabilities do not provide accurate, spatially distributed measurements of snow~~ Snow water equivalent (SWE) ~~in mountainous terrain at the spatial or temporal resolutions required for many scientific and water management applications (Tsang et al., 2022).~~ SWE measurements derived from interferometric synthetic aperture radar (InSAR) sensors have shown promising accuracy in dry snowpacks. Specifically, at low radar frequencies ($\leq \sim 5$ GHz), the dry snowpack is nearly transparent, but causes a signal delay as incident microwave radiation travels to the snow-ground interface and back to the receiver. ~~The Changes in the radar time-of-flight through snow has been used for decades to measure SWE using ground-based systems (from two acquisitions separated in time change the phase of the wave measured at the receiver. These changes in phase can be used to measure changes in SWE (Δ SWE) over the same period by applying differential InSAR techniques (see Marshall and Koh (2008) for review). Differential interferometric SAR (InSAR) techniques can be applied to measure SWE changes from changes in the radar time-of-flight and resulting InSAR phase change from two acquisitions separated in time (Leinss et al., 2015). Such measurements have been demonstrated from tower-based (Leinss et al., 2015; Ruiz et al., 2022), airborne (Palomaki and Sproles, 2023; Tarricone et al., 2023; Belinska et al., 2024; Bonnell et al., 2024b, a; Hoppinen et al., 2024; Tarricone et al., 2024), and satellite (Gunteriusen et al., 2001; Rott et al., 2003; Deeb et al., 2011; Oveisgharan et al., 2024; Ruiz et al., 2024) InSAR platforms. These Individual Δ SWE measurements can then be integrated through time to track seasonal SWE accumulation. Previous investigations with tower-mounted radars have reported seasonal errors below 9 mm (8%) SWE (Leinss et al., 2015). A multifrequency tower-mounted radar experiment (Ruiz et al., 2022) demonstrated that lower radar frequencies and shorter temporal baselines (elapsed time between radar acquisitions) result in lower SWE errors, down to 4 mm (3%) SWE at L-band (~ 1.3 GHz) with a 6-hour baseline. SWE measurements derived from airborne L-band data show similarly low errors in a variety of snow climates across the western United States (Tarricone et al., 2023; Bonnell et al., 2024b; Hoppinen et al., 2024; Tarricone et al., 2024) and Austrian Alps (Belinska et al., 2024), though challenges still remain where snow is generally difficult to measure, including in dense forests (Bonnell et al., 2024a) and shallow, heterogeneous snowpacks (Palomaki and Sproles, 2023). Additionally, these techniques are applicable primarily during the accumulation season when snow is dry. The presence of significant liquid water in the snowpack strongly attenuates incident radiation and changes the radar velocity, making SWE estimates difficult.~~

For many years, Earth observing satellites did not satisfy spatiotemporal InSAR-derived SWE measurements have also been demonstrated using C-band (~ 5 GHz) and L-band satellite data, including from ERS 1/2 (Gunteriusen et al., 2001; Rott et al., 2003; Deeb et al., 2011), Sentinel-1 (Oveisgharan et al., 2024), and ALOS-2 (Ruiz et al., 2024). Results from these studies showed that satellite measurements could capture spatial patterns of SWE accumulation, and in some cases showed high correlation to in situ validation data (Oveisgharan et al., 2024).

60 . However, none of the satellite platforms used in these studies satisfy spatiotemporal (100 m, 3–5 days) plus accuracy ($\pm 10\%$ for SWE values up to 2.5 m) monitoring requirements for SWE in mountainous regions set in the 2017–2027 National Academies Decadal Survey (100 m, 3–5 days; National Academies of Sciences, Engineering, and Medicine, 2018) (National Academies of Sciences, Engineering, and Medicine, 2018).
The recently-launched NISAR satellite platform ~~will provide~~ provides L-band (1.257 GHz) InSAR data at 80 m spatial resolution (Brancato et al., 2024) with ~~a~~ overlapping ascending and descending passes in its global 12-day orbit cycle, resulting in data acquisition every 3–6 days over many snowy regions. However, NISAR (or any InSAR satellite) phase can be modulated by many non-snow factors which introduce random errors or bias into phase-based SWE measurements. ~~We detailed the physical basis and governing equations for~~ Here we consider six non-snow ~~error sources in a recent publication (Hoppinen et al., submitted)~~ factors: ionospheric advance, wet and dry tropospheric delay, changes in soil and vegetation permittivity, and land surface deformation. ~~However, our previous theoretical discussion did not assess the expected real-world magnitude of these errors on InSAR SWE measurements. This is an important step to determine if NISAR-derived measurements can meet the accuracy requirements noted in the 2017–2027 Decadal Survey. While the Decadal Survey does not list a SWE accuracy requirement specific to mountain regions, we will use the $\pm 10\%$ accuracy target for global SWE to frame this analysis.~~

75 ~~In this paper we use observational and modeled data to quantify how these six non-snow factors influence InSAR phase and introduce error into phase-based SWE measurements. We note that this is a non-exhaustive list of potential error sources. We base our analysis on a 12-day temporal baseline to provide a discussion relevant for NISAR. As detailed in our previous paper (Hoppinen et al., submitted), five of the six error sources are independent of radar frequency. For the remaining frequency-dependent ionospheric component we assess errors based on the central 1.257 GHz frequency of the L-band sensor on NISAR.~~

~~For this analysis we~~ For example, we do not assess errors that arise due to platform-specific factors ~~. For example, temporal decorrelation like temporal decorrelation, which~~ increases uncertainty in the calculated InSAR phase (Zebker and Villasenor, 1992) ~~, thereby increasing error in and subsequently~~ any phase-based measurement. Temporal decorrelation at a given location is affected by local incidence angle, which is determined by the specific imaging geometry of the sensor as well as the radar frequency. Although decorrelation will be an important factor to consider for NISAR SWE measurements, modeling these effects which are also influenced by changing snow conditions is beyond the scope of this work. Instead, we focus on ~~major~~ platform-agnostic non-snow factors to quantify the relative magnitude of the errors and illustrate site- and season-specific considerations for improving the accuracy of NISAR SWE measurements. This is an important step to determine if NISAR-derived measurements can meet the 2017–2027 Decadal Survey $\pm 10\%$ accuracy target.

2 Error sources and calculations

~~The change in SWE (ΔSWE) at~~ In this paper we quantify how six non-snow factors influence InSAR phase and introduce error into phase-based SWE measurements and compare the results to measured SWE at SNOTEL stations around the western United States (WUS). We base our analysis on the 12-day change in the ~~surface can be approximated from the change in~~ InSAR phase ($\Delta\phi$) as (Leinss et al., 2015) non-snow factors to provide a discussion relevant for NISAR and its 12-day orbit cycle. For each non-snow factor, we use observed or modeled data to simulate the phase modulation over a 12-day baseline.

then convert that change in phase to the associated (erroneous) change in SWE. In Section 2 we provide the governing equations for the error factors and describe our analysis methods. We present results in a cumulative seasonal context in Section 3 and in a single 12-day baseline context in Section 4. We discuss our findings in Section 5 and provide suggestions for minimizing NISAR-derived SWE errors in Section 6.

2 Derivation of non-snow errors

2.1 Phase-to-SWE equation

The change in InSAR phase $\Delta\phi_s$ caused by a change in snow over the same temporal baseline can be calculated as (Gunteriusen et al., 2001)

$$\Delta\text{SWE}\phi_s = -2\kappa\Delta\phi_{z_s} \cdot \frac{\lambda}{2\pi\alpha} \left(\frac{1.59 + \cos\theta_i^{5/2} - \sqrt{\varepsilon - \sin^2\theta_i}}{\varepsilon} \right)^{-1} \quad (1)$$

where λ is the wavelength, α is an empirical correction factor, and $\kappa = 2\pi/\lambda$ is the wavenumber, Δz_s is the change in snow depth in m, θ_i is the incidence angle. Although the phase delay through the snowpack can be calculated directly if the permittivity of the snow is known, this is difficult to measure directly and often in radians, and ε is the bulk snowpack permittivity. The factor of 2 at the beginning of the equation accounts for the two-way travel time between the transmitter and the target. The bulk snowpack permittivity of dry snow can be approximated by snow density, another variable that is difficult to estimate across space using remote sensing techniques. Hence, Equation ?? is an approximation that is particularly convenient for satellite-based InSAR but spatially distributed measurements of either permittivity or density are rarely available and both are difficult to model accurately. Using an empirical approximation to remove the density-dependent term (Leinss et al., 2015) and multiplying snow depth and snow density to obtain SWE, (1) can be rearranged to solve for directly for ΔSWE as

$$\Delta\text{SWE} = \Delta\phi_s \cdot \frac{\lambda}{2\pi\alpha} \left(1.59 + \theta_i^{5/2} \right)^{-1} \quad (2)$$

More details of this derivation can be found in Leinss et al. (2015) and Palomaki and Sproles (2023). Despite additional error introduced by the empirical approximation (Leinss et al., 2015), (2) is better suited than (1) for use with satellite-derived SWE measurements because it removes the dependence on snow density does not require snow density as an input. We use (2) to derive the non-snow error equations in the next section. For our analysis in this paper, we fix $\alpha = 1$ (for which retrieval error is below 7% for $\theta_i = 40^\circ$ (0.698 rad; approximately the average incidence angle for NISAR scenes) and $\lambda = 0.2385$ m (NISAR L-band wavelength) in (2). This density-independent approximation introduces additional error of up to 7% for a wide range of densities and incidence angles (Leinss et al., 2015, their Figure 9).

2.2 Non-snow error equations

Surface and atmospheric conditions other than SWE that change over a 12 day temporal baseline period can modulate the measured InSAR phase and introduce errors into the SWE retrieval. Here we consider six non-snow factors (Table 1): ionospheric

effects (changes in total electron content), wet tropospheric effects (changes in atmospheric water vapor), dry tropospheric effects (changes in atmospheric pressure), soil permittivity (primarily changes in soil moisture), vegetation permittivity (primarily changes in air temperature), and surface deformation (Table 1). As an example, the dielectric permittivity of soil is a function of both soil composition and soil moisture. Although we assume the soil composition is static over a 12-day period, changes in soil moisture will change the soil permittivity and affect measured phase changes in surface elevation. For this analysis we quantify errors in InSAR-derived SWE by calculating $\Delta\phi$ associated with a given non-snow factor, then use Equation ?? (2) to calculate the error in ΔSWE resulting from the non-snow related $\Delta\phi$. The relevant $\Delta\phi$ equations for each factor are given in Appendix A and full derivations of these equations are provided in Hoppinen et al. (submitted). For all calculations we fix $\alpha = 1$ (for which retrieval error is below 7% for $\theta < 50^\circ$), $\theta_i = 40^\circ$, and $\lambda = 0.2385\text{ m}$. For clarity in several of the following derivations, we make the substitution $2\kappa = 4\pi/\lambda$. Throughout the analysis, negative errors mean that the measured SWE change ΔSWE is underestimated compared to the true change, and positive errors indicate overestimated SWE change.

Table 1. Data sources and characteristics for each modeled non-snow error component factors.

Non-snow factor	Wavelength independent?	Relevant variables	Data source	Data characteristics
Ionosphere	No	Total electron content	IGS IONEX	2-hourly 0.5 degree raster
Wet troposphere	Yes	Atmospheric water vapor	MERRA-2	Hourly 50 km raster
Dry troposphere	Yes	Surface pressure	MERRA-2	Hourly 50 km raster
Soil permittivity	Yes	Soil moisture	SNOTEL	Hourly point data
		Soil composition*	SoilGrids	Static 250 m raster
Vegetation permittivity	Yes	Air temperature	SNOTEL	Hourly point data
		Canopy height*	LANDFIRE 2023	Static 30 m raster
Surface deformation	Yes	Surface elevation	GNSS stations	Daily point data

* assumed constant over 12 days

2.2.1 Ionospheric error

Changes in the vertically integrated total electron content ΔTEC in the ionosphere affect the InSAR phase. The varying electron density of the ionosphere is affected by solar UV radiation, Earth's magnetic field, and atmospheric gas concentrations; interactions between these factors cause electron density concentrations to vary over multiple spatial (sub-kilometer to tens of kilometers) and temporal (diurnal, seasonal, and interannual) scales (Lean et al., 2016). The resulting impacts on InSAR phase are frequency-dependent and can introduce larger errors at lower frequencies, like NISAR's L-band measurements (Meyer and Agram, 2017). The phase change $\Delta\phi_{\text{ion}}$ due to ΔTEC in units of TECU (10^{16} electrons per m^2) is

$$\Delta\phi_{\text{ion}} = -\frac{4\pi K\lambda}{c^2} \Delta\text{TEC} \quad (3)$$

140 where K is a constant ($40.28 \text{ m}^3\text{s}^{-2}$) and c is the speed of light (Rosen et al., 2010). Inserting $\Delta\phi_{\text{ion}}$ from (3) into (2) we obtain

$$\Delta\text{SWE}_{\text{ion}}(\Delta\text{TEC}) = -\frac{2K\lambda^2}{c^2\alpha(1.59 + \theta_i^{5/2})}\Delta\text{TEC} \quad (4)$$

At a fixed $\theta_i = 40^\circ$, this corresponds to 0.258 m of SWE error per unit increase of TEC for NISAR-derived measurements. The negative indicates this non-snow factor causes a phase advance while most other factors cause phase delays. We use (4) to calculate ionospheric error in our analysis using TEC data from IGS IONEX (Schaer et al., 1998).

2.2.2 Tropospheric errors

Temporal variation in water vapor, temperature, and air pressure in the troposphere affect the InSAR phase. These tropospheric effects are typically separated into two components (Jolivet et al., 2014). The first is the wet delay $\Delta\phi_{\text{wet}}$, a function of changes in water vapor pressure e and air temperature T given by

$$\Delta\phi_{\text{wet}} = \frac{4\pi}{\lambda} \frac{10^{-6}}{\cos(\theta_i)} \int_{z_{\text{surf}}}^{z_{\text{ref}}} \left(k_2 - \frac{R_d}{R_v} k_1 \right) \frac{\Delta e}{\Delta T} + k_3 \frac{\Delta e}{\Delta T^2} dz \quad (5)$$

where k_1 , k_2 , and k_3 are constants (0.776 K Pa^{-1} , 0.716 K Pa^{-1} , and $3.75\text{e}3 \text{ K}^2 \text{ Pa}^{-1}$, respectively), R_v is the specific gas constant for water vapor ($461.52 \text{ J kg}^{-1} \text{ K}^{-1}$), z_{surf} is the surface height and z_{ref} is a high altitude reference height representing the top of the atmospheric column. By integrating the column water vapor into the meters of precipitable water (PW) and using an average atmospheric temperature, we can approximate the phase change $\Delta\phi_{\text{PW}}$ due to ΔPW as

$$\Delta\phi_{\text{wet}} = \frac{4\pi}{\lambda} \frac{6.5}{\cos(\theta_i)} \Delta\text{PW} \quad (6)$$

The relative error in this estimate is approximately equal to the error in the average atmospheric temperature estimate, which in reality can vary by up to 20% (Bevis et al., 1994). Inserting $\Delta\phi_{\text{wet}}$ from (6) into (2) we obtain

$$\Delta\text{SWE}_{\text{wet}}(\Delta\text{PW}) = \frac{2}{\alpha(1.59 + \theta_i^{5/2})} \frac{6.5}{\cos\theta_i} \Delta\text{PW} \quad (7)$$

The wet delay is the main contributor to tropospheric phase delay (Jolivet et al., 2014). At a fixed $\theta_i = 40^\circ$, this corresponds to 8.516 m of SWE error per meter of ΔPW . We use (7) to calculate the wet tropospheric error in our analysis using precipitable water data from MERRA-2 (Global Modeling And Assimilation Office and Pawson, 2015).

The second and typically smaller tropospheric error component is the hydrostatic delay (also referred to as the dry or stratified delay) due to changes in air pressure P (Jolivet et al., 2014). The dry delay $\Delta\phi_{\text{dry}}$ is given by

$$\Delta\phi_{\text{dry}} = \frac{4\pi}{\lambda} \frac{10^{-6}}{\cos(\theta_i)} \frac{k_1 R_d}{g_m} \Delta P(z) \quad (8)$$

165 where R_d is the specific gas constant for dry air ($287.05 \text{ J kg}^{-1} \text{ K}^{-1}$), g_m is the local gravitational acceleration (assumed static at 9.81 m s^{-2}), and $\Delta P(z)$ is the change in relative air pressure in Pa. Inserting $\Delta\phi_{\text{dry}}$ from (8) into (2) we obtain

$$\Delta\text{SWE}_{\text{dry}}(\Delta P(z)) = \frac{2}{\alpha(1.59 + \theta_i^{5/2})} \cdot \frac{10^{-6}}{\cos(\theta_i)} \frac{k_1 R_d}{g_m} \Delta P(z) \quad (9)$$

At a fixed $\theta_i = 40^\circ$, this corresponds to 0.0297 m of SWE error per kPa change in air pressure. We use (9) to calculate the wet tropospheric error in our analysis using surface pressure data from MERRA-2 (Global Modeling And Assimilation Office and Pawson, 2011).

170 . It is important to note that both dry and wet tropospheric effects vary with elevation, since radar waves must travel through more of the atmosphere to reach lower altitudes. This elevation dependence can produce patterns tropospheric effects that resemble those associated with snow accumulation or ablation.

2.2.3 Soil permittivity errors

At L-band frequencies some radar energy will typically penetrate into the soil medium at the snow-ground interface. The soil permittivity, which influences the speed of radar waves in soil, is controlled primarily by soil composition and moisture content. 175 Assuming the soil is isotropic, uniform, and linear, De Zan et al. (2014) showed that the phase change $\Delta\phi_{\text{soil}}$ due to changes in soil permittivity can be calculated using

$$\Delta\phi_{\text{soil}} = \frac{1}{2jk'_{z1} - 2jk'_{z2}^*} \quad (10)$$

where k'_{z1} and k'_{z2} are the vertical soil wavenumbers at the first and second radar acquisitions, respectively, and the * operator 180 denotes the complex conjugate. The vertical soil wavenumber k'_z can be expressed as

$$k'_z = \sqrt{\omega^2 \epsilon' \mu - k_x^2} \quad (11)$$

where $\omega = \kappa c$ is the angular frequency of the radar wave, ϵ' is the real component of the soil dielectric permittivity, μ is the soil magnetic permeability, and $k_x = \kappa \sin \theta_i$ is the horizontal wavenumber of free air. For most soils, magnetic permeability is approximately equal to 1 at low radar frequencies (Patzitz et al., 1995; Youn et al., 2010). The real part of the dielectric 185 permittivity is a function of frequency, water content, and soil type (e.g., clay, silt, and sand fractions). Using polynomial approximations for the real component of soil dielectric permittivity (Hallikainen et al., 1985), we estimate SWE error using (10) and (11) for a variety of soil types based on changes in soil moisture (Figure 1). The largest soil-related SWE errors occur when moisture changes in relatively dry soils, with errors leveling off with moisture changes in wetter soils. Soils of various compositions show similar trends, with increasing clay content associated with smaller dielectric changes and associated SWE 190 errors. For our analysis we use soil composition data from SoilGrids (Poggio et al., 2021) and soil moisture data from SNOTEL sites.

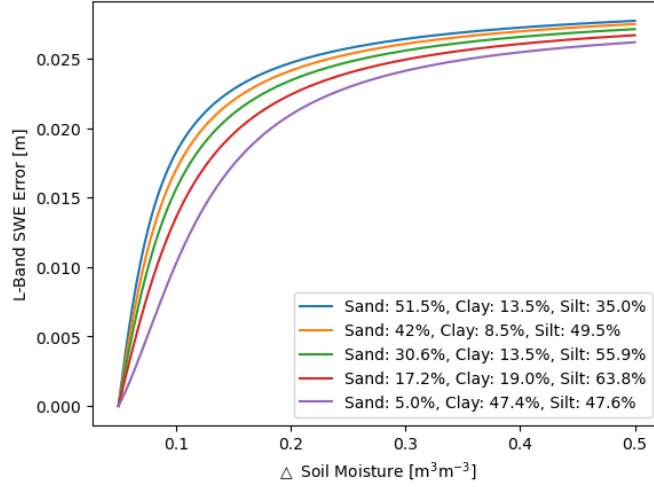


Figure 1. Example L-band SWE error curves for five soil types based on soil moisture content to avoid erratic polynomial effects, soil moisture content starts at $0.05 \text{ m}^3 \text{ m}^{-3}$.

2.2.4 Vegetation permittivity errors

Subfreezing air temperatures can cause liquid water within vegetation to freeze. The transition from liquid water to ice within wood affects the dielectric permittivity of trees (Schwank et al., 2021). To calculate the phase change $\Delta\phi_{\text{veg}}$ due to changes in vegetation permittivity we use the mixing model between wood, water, air, and ice given by Schwank et al. (2021):

$$\Delta\phi_{\text{veg}} = \frac{4\pi}{\lambda} H \left(\sqrt{\epsilon_{c,2} - \sin^2(\theta_i)} - \sqrt{\epsilon_{c,1} - \sin^2(\theta_i)} \right) \quad (12)$$

where H is the canopy height and the canopy permittivity ϵ_c at time 1 and 2 is defined by

$$\epsilon_c = \epsilon_{\text{air}} + \frac{(\epsilon_{\text{wood}} - \epsilon_{\text{air}})(\epsilon_{\text{wood}} + 5\epsilon_{\text{air}})v_{\text{SCC}}}{3(\epsilon_{\text{wood}} + \epsilon_{\text{air}}) - 2(\epsilon_{\text{wood}} - \epsilon_{\text{air}})v_{\text{SCC}}} \quad (13)$$

where v_{SCC} is the volume fraction of space occupied by small canopy constituents (branches, stems, trunks), ϵ_{air} is the permittivity of free air, and ϵ_{wood} is the permittivity of wood. Wood permittivity is calculated from the porosity and density of the wood combined with wood cell, water, and ice permittivities and ratios as

$$\epsilon_{\text{wood}} = v_{\text{H}_2\text{O}}\epsilon_{\text{H}_2\text{O}} + (1 - \text{por})\epsilon_{\text{wood-cell}} + (\text{por} - v_{\text{H}_2\text{O}})\epsilon_{\text{air}} \quad (14)$$

We assume that the only temporally variable parameter in winter is permittivity of the water within the wood, which is controlled by the the water-to-ice ratio within the wood cell (v_{water}):

$$\epsilon_{\text{H}_2\text{O}} = v_{\text{water}}\epsilon_{\text{water}} + (1 - v_{\text{water}})\epsilon_{\text{ice}} \quad (15)$$

While direct measurements of ice-water ratio within wood are challenging, we use the approximation using air temperature T given in Schwank et al. (2021):

$$v_{\text{water}}(T) = \begin{cases} 1, & \text{if } T > 0^\circ\text{C} \\ \exp\left(\frac{T}{T_{\text{melt}}}\right), & \text{if } T \leq 0^\circ\text{C} \end{cases} \quad (16)$$

210 We use (12) through (16) to calculate the vegetation permittivity error in our analysis using air temperature data from SNOTEL and canopy height data from LANDFIRE (Dewitz, 2026). For all constant parameters in (12) through (16) we use values in Table 1 of Schwank et al. (2021).

2.2.5 Surface deformation

Changes in surface elevation change the line-of-sight distance between the ground and the sensor. Surface elevation can shift due to many factors, including earthquakes, subsidence, solid earth and ocean tides, and permafrost thaw. The phase change
215 $\Delta\phi_R$ due to surface elevation change ΔR is given by

$$\Delta\phi_R = \frac{4\pi}{\lambda} \Delta R \quad (17)$$

Inserting $\Delta\phi_R$ from (17) into (2) we obtain

$$\Delta\text{SWE}_{\text{def}}(\Delta R) = \frac{2}{\alpha(1.59 + \theta_i^{5/2})} \Delta R \quad (18)$$

220 At a fixed $\theta_i = 40^\circ$, this corresponds to 1.001 m of SWE error per meter of surface deformation. We use (18) to calculate the surface deformation error in our analysis using surface elevation data from GNSS stations.

2.3 Error analysis methods

We consider two potential applications of InSAR-based SWE measurements. The first is estimating April 1 SWE by integrating a regular 12-day timeseries of ΔSWE measurements (i.e., from nearest-neighbor interferograms) over the accumulation season. In this application the non-snow errors from any one interferogram are less important than the cumulative error at the time of
225 peak SWE. Because the total error from non-snow factors can be either positive or negative for any single InSAR pair, integrated SWE measurements can-could have smaller cumulative error if positive and negative errors cancel out over time. The second application is quantifying changes in the spatial distribution of snow across a landscape within a single 12-day period. Here-In this case we are interested in a comparison of the non-snow errors relative to a single ΔSWE value, not the total accumulated SWE.

230 ~~We selected~~ To illustrate how non-snow errors vary across snow climates, we applied our analysis at locations across the WUS representing 13 SNOTEL stations across the conterminous western US to represent 13 major mountain ecoregions denoted by Trujillo and Molotch (2014). ~~Stations within each region were chosen~~ We chose a 10-year period between water

235 years 2016–2025 (October 1, 2015 through September 30, 2025), which includes high (2023), average (2022), and low (2016) snow seasons, to examine the temporal variability of the errors. All other datasets we use to calculate the non-snow errors (Table 1) are also available for water years 2016–2025. Within each ecoregion, stations were selected based on data availability from water years 2016–2025. The (98% complete data records for SWE, air temperature, and 2 inch soil moisture for each of the 10 seasons). When more than one station in an ecoregion met the data availability criteria, we selected so that the final 13 stations also span a range of snow classes (Sturm and Liston, 2021), vegetation types and heights, and other environmental characteristics (Table 2).

240 At each station we apply all error calculations over a rolling 12-day period using a 12-day moving window with a step size of one day to simulate all possible NISAR acquisitions. An example for soil permittivity error for water year 2021 at the Paradise station is shown in Figure 2. First, we use the daily soil moisture data (Figure 2a) to calculate a daily timeseries of soil permittivity error (Figure 2b) by applying Equation 10 on a 12-day baseline with a step size of 1-day moving window. In this example we used data from September 2020 in order to get a valid error value on October 1. Cumulative error calculations are

245 then applied to the daily timeseries over all possible 12-day baselines, again with a moving window of one day (e.g., October 1, 13, 25,...; October 2, 14, 26,...) (Figure 2c). We combine all possible 12-day cycles into a single daily timeseries, then compute a rolling 12-day mean of the cumulative error to remove cyclic artifacts (Figure 2d). In our analysis and figures below we use the rolling 12-day cumulative error (orange line in Figure 2d) in the context of seasonal SWE errors (Section 3), and the daily error timeseries (Figure 2b) in the context of individual 12-day snapshot-baseline errors (Section 4).

250 As noted in Table 1, the data sources we use to calculate the non-snow errors have different characteristics (e.g., point data vs. rasters of various resolutions). When raster datasets are used as input to error calculations, we use the value of the pixel that contains the SNOTEL station used for comparison. For surface deformation calculations, we make the assumption that the 12-day surface deformation at a given SNOTEL site is equivalent to that of the nearest GNSS station, even though the SNOTEL and GNSS points are not co-located. We do not attempt to spatially interpolate or otherwise adjust the GNSS data to

255 account for the separation distance.

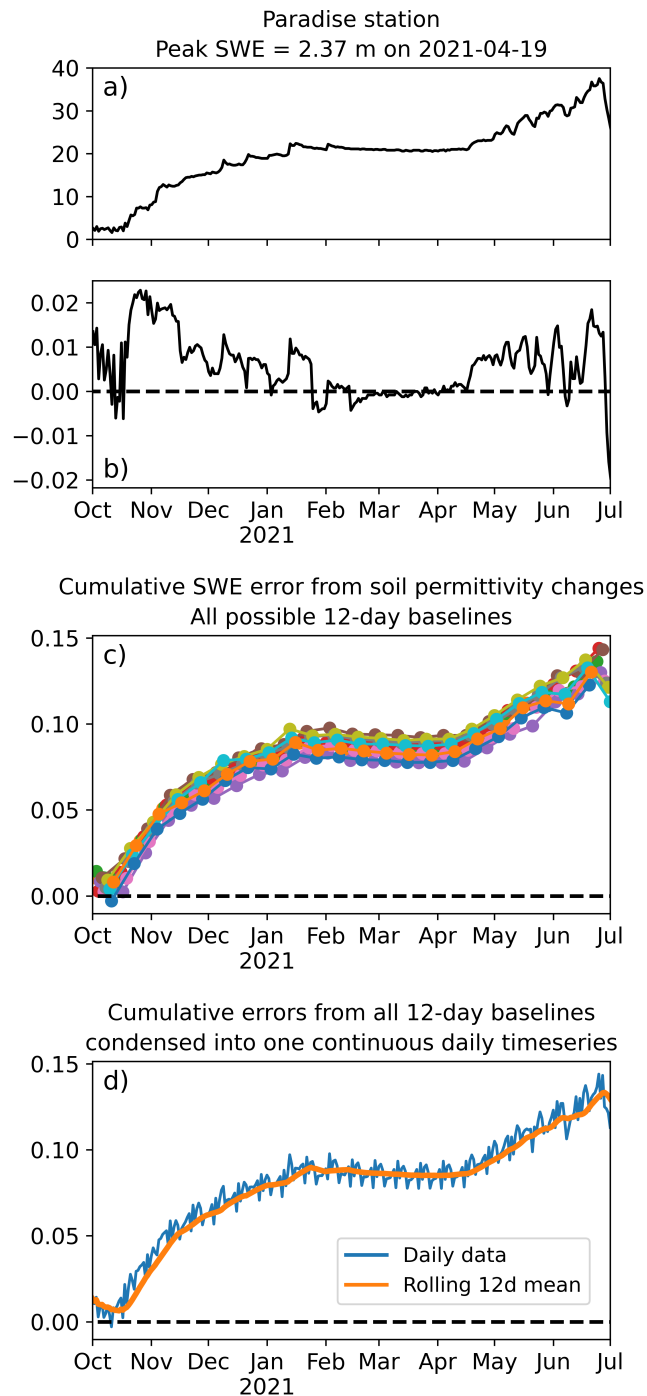


Figure 2. Workflow example using soil moisture changes at the Paradise SNOTEL. Changes in soil moisture (a) result in changes in soil permittivity, a non-snow error component for InSAR SWE measurements. First, we calculate the resulting SWE error for each 12-day pair in the timeseries (b). We then apply cumulative error calculations to the daily timeseries over all possible 12-day baselines (c). Finally, all possible 12-day cumulative error baselines are combined and we apply a rolling 12-day mean (d).

Table 2. Site Characteristics

No.	Station Name	Ecoregion ¹	Coordinates	State	Elev (m)	Snow Class ²	Median 2016-25 Peak SWE [m]	Soil Composition [Sand/Clay/Silt %] ³	Canopy Height [m]
1	Paradise	North Cascades	46.78, -121.75	WA	1570	Maritime	2.04	74.8/1.9/23.3	19
2	Sunset	Columbia Mtns/ Northern Rockies	47.56, -115.82	ID	1701	Montane Forest	0.51	30.4/11.0/58.6	20
3	Clackamas Lake	Cascades	45.10, -121.75	OR	1036	Ephemeral	0.36	52.4/16.4/31.2	24
4	Tipton	Blue Mountains	44.66, -118.43	OR	1570	Montane Forest	0.37	38.6/9.5/51.9	20
5	Galena Summit	Idaho Batholith	43.88, -114.71	ID	2676	Boreal Forest	0.57	49.7/12.6/37.7	11
6	Snake River Station	Middle Rockies	44.13, -110.67	WY	2103	Montane Forest	0.49	41.9/20.6/37.5	14
7	Annie Springs	Eastern Cascades	42.87, -122.17	OR	1835	Maritime	1.12	70.5/2.4/27.1	27
8	Palisades Tahoe	Sierra Nevada	39.19, -120.27	CA	2441	Maritime	1.01	67.6/7.2/25.2	0.5
9	Disaster Peak	Northern Basin and Range	41.97, -118.19	NV	1908	Prairie	0.19	42.1/21.8/36.1	1
10	Corral Canyon	Central	40.28, -115.54	NV	2573	Prairie	0.55	43.0/19.0/38.0	16
11	Trial Lake	Basin and Range Wasatch and Uinta Mountains	40.68, -110.95	UT	3039	Boreal Forest	0.65	34.6/27.2/38.2	10
12	Jackwhacker Gulch	Southern Rockies	39.57, -105.80	CO	3362	Boreal Forest	0.31	48.5/17.6/33.9	16
13	Quemazon	AZ/NM Mountains	35.92, -106.39	NM	2893	Montane Forest	0.19	40.1/14.3/45.6	11

¹ after Trujillo and Molotch (2014)

² after Sturm and Liston (2021)

³ from SoilGrids dataset

⁴ from LANDFIRE [2023-2024](#) dataset

3 Cumulative Tracking seasonal SWE: cumulative error analysis

Examples of measured SWE and simulated non-snow InSAR errors are shown for three SNOTEL stations (Figure 3). Different water years were selected at the different stations only to illustrate how results change in snowpacks of varying depths. Panels in the left column top row show measured SWE at a given SNOTEL station with the cumulative non-snow errors added to the measured SWE curves. We include separate curves with (grey) and without (orange) the ionosphere error because it can be an order of magnitude larger than the other errors. These are idealized scenarios where the SWE changes recorded by the SNOTEL station can be retrieved exactly once the six non-snow errors are removed. The additional error of up to 7% introduced by using the density-independent approximation (Equation ??2) is not reflected. Panels in the right column bottom row show cumulative individual error components over time. We removed the ionosphere error from these panels to better show the detail of the other error components (dry and wet troposphere, vegetation and soil permittivity, and surface deformation).

Individual error components (Figure 3, right column bottom row) have partially offsetting effects at the three stations. For example, at all stations the cumulative soil permittivity error introduces a consistent positive bias by the middle of the accumulation season while the wet troposphere error introduces a negative bias during the same period. The dry troposphere error is the closest to unbiased random noise, with the cumulative error fluctuating around 0 cm during the accumulation season at all stations. These three examples all show negative total cumulative errors (thick black lines) for non-ionospheric components over most of the accumulation season.

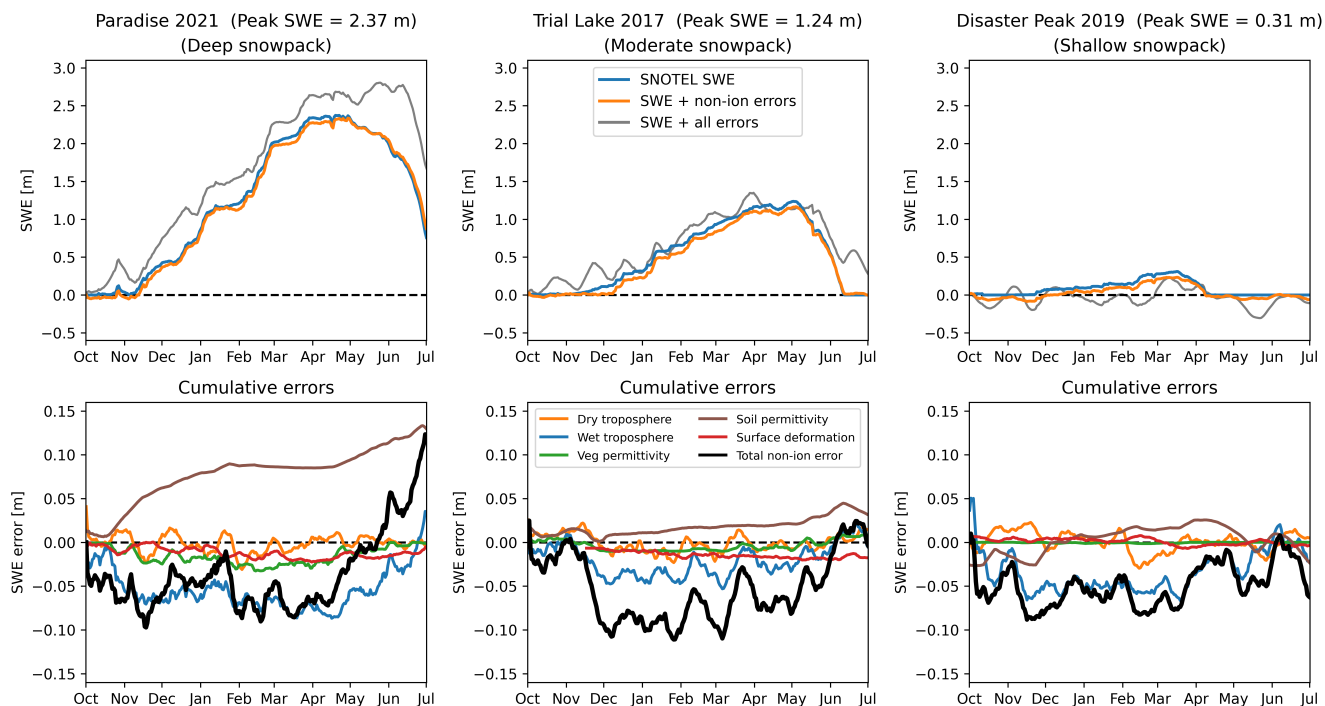


Figure 3. Left column Top row: SNOTEL SWE curves (blue), theoretical simulated InSAR-derived SWE curves including non-ionospheric error sources (orange), and theoretical simulated InSAR-derived SWE curves including all error sources (gray). Right column Bottom row: Cumulative error for individual error components and total non-ionospheric error. In both columns rows, the legends shown in the second row column apply to all panels in the column row.

Figure 3 shows only one season at three stations. We repeat this analysis for multiple years (2016–2025) at multiple stations to investigate the interannual variability of total non-ionospheric cumulative errors. A summary of the total error integrated between October 1 and April 1 gives more evidence of a trend toward negative total cumulative errors on April 1 (Figure 4). If this error is not removed from the InSAR phase, the overall effect at these stations is that InSAR-derived SWE measurements will tend to underestimate April 1 SWE. However, the interannual variability of the total cumulative error (i.e., the width of the boxplot) changes between stations and most stations also show positive errors (overestimated SWE) in at least one year. ~~Wide interannual variability is likely driven by the complex interactions between the error factors and their physical drivers at seasonal scales.~~ This indicates that it may be difficult to predict the general behavior of the total error at any site based on errors measured in previous seasons. For example, at Sunset the largest positive error (0.096 m) occurred in 2016 and the largest negative error (−0.191 m) occurred in 2025, but peak SWE measurements in the two years were very similar (0.452 m in 2016 and 0.444 m in 2025). Wide interannual variability at a site is likely driven by the complex interactions between the error factors and their physical drivers at seasonal scales. For example, a series of several early season snow accumulation/melt events would likely result in fluctuating tropospheric effects (i.e., changes in air pressure and precipitable water associated

285 with frontal passage) but the secondary soil permittivity effects from melting snow are partially controlled by antecedent soil moisture conditions, which we do not assess in our analysis.

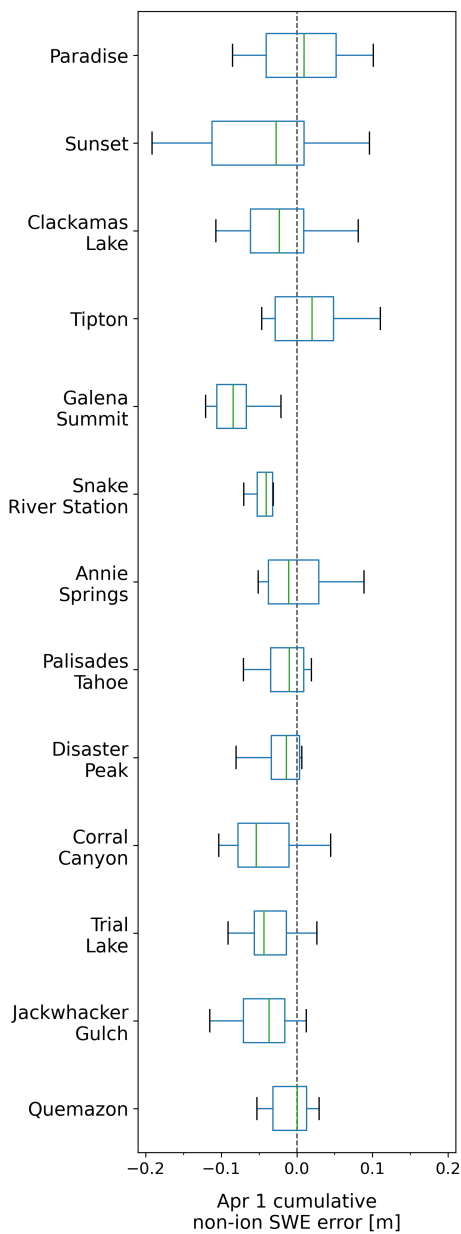


Figure 4. Boxplots summarizing total cumulative non-ionospheric errors on April 1 for 10 seasons (2016–2025) at 13 SNOTEL stations (Table 2).

Results in Figure 4 also show median cumulative errors on April 1 at all sites are between ± 0.1 m of SWE. Whether this represents a significant error at any given station depends on the average April 1 SWE. The inset bar charts in Figure 5 show how the average cumulative errors compare to the average April 1 SWE at each station. Cumulative errors are calculated each year between October 1 and April 1 for water years 2016–2025, averaged over ~~time~~the 10 water years, and divided by the average April 1 SWE. The different colored bars represent different error types, with the total non-ionospheric error shown in black. All inset axes are clipped to $\pm 10\%$ of average April 1 SWE on the y-axis. Cumulative error components that extend beyond this range are indicated with an arrowhead at the end of the bar. Again we have removed the ionosphere error from this figure to better visualize the other error components. All cumulative errors, including the ionosphere component, are also listed in Table 3 as absolute values and percentages of April 1 SWE at each station.

The average 2016–2025 total cumulative error ranges across stations between 0.271–0.414 m, and at all stations is larger than 10% of April 1 SWE (Table 3). The stations with the deepest average April 1 snowpack (Paradise, Palisades Tahoe, and Annie Springs) have the smallest relative total errors (17%, 29%, and 35%, respectively). Two stations with shallow snow (Disaster Peak and Quemazon) have total errors larger than 500% of average April 1 SWE, which is less than 0.1 m at both stations. At these low-elevation locations, April 1 may not be an appropriate date to use as a proxy for peak SWE. For example, at Disaster Peak in water year 2019 much of the accumulated SWE had already melted by April 1 (Figure 3). Shifting the cumulative error calculation to an earlier date would slightly improve these results at Disaster Peak and Quemazon, but we expect that these shallow snowpack stations would still have the largest errors because we report our results relative to average SWE. We do not note any obvious trends in performance solely based on snow class.

The cumulative ionosphere error is the largest error component. At all stations it introduces a large positive bias that represents the vast majority of the total cumulative error. Again we note that the ionosphere error is the only non-snow factor considered here that is a function of the radar frequency, with larger errors at lower frequencies (Rosen et al., 2010). The results in Table 3 show the importance of correcting for ionospheric effects when using L-band data to derive InSAR SWE measurements. While the NISAR platform has a dedicated subband offset from the main instrument frequency to allow for measurement of the dispersive ionospheric effects, other L-band platforms (e.g. ~~ALOS PALSAR-2~~ALOS-2) may require advanced data processing techniques like a split-spectrum approach (Wegmüller et al., 2018) to remove ionospheric effects. Additionally, it is possible for NISAR to operate in a quasi-quad-pol configuration utilizing subband data that prevents ionospheric corrections. NISAR data collected in this configuration will require advanced processing techniques before the phase information can be used for SWE retrievals.

At most stations, removing the ionosphere error brings the remaining cumulative error to within $\pm 10\%$ of April 1 SWE, meeting accuracy targets established in the 2017–2027 Decadal Survey. Soil permittivity errors tend to introduce positive biases into the cumulative error. As illustrated at Paradise during water year 2021 (Figure 3), this error can increase quickly at the beginning of the water year ~~season~~—as early season snow accumulation and melt events influence the soil moisture. The cumulative soil permittivity error remains relatively constant in the middle of the accumulation season with colder temperatures and deeper snowpacks. The remaining components (wet and dry troposphere, vegetation permittivity, and surface deformation)

tend to introduce smaller negative biases as they are influenced by meteorological factors (atmospheric water vapor, surface pressure, and air temperature) that fluctuate at daily to weekly timescales.

325 Total non-ionospheric error is still outside $\pm 10\%$ at Disaster Peak, Jackwhacker Gulch, and Quemazon (stations 9, 12, and 13, respectively). As discussed previously, these results at Disaster Peak and Quemazon are influenced by very small values for average April 1 SWE. A comparison of results at Jackwhacker Gulch, Tipton (station 4), and Clackamas Lake (station 3) makes for a more interesting discussion. All stations have relatively shallow snowpacks on April 1 (0.308, 0.326, and 0.285 m, respectively) but Jackwhacker Gulch does not meet the Decadal Survey accuracy target with -24% total non-ionospheric error while the Tipton and Clackamas Lake results do (7% and 4%, respectively). The wet troposphere, dry troposphere, and vegetation permittivity errors at the three sites all negatively bias the cumulative error, but the magnitude of the bias for all three components is larger at Jackwhacker Gulch than both Tipton and Clackamas Lake. The difference in magnitudes may be due to differences in station elevations: temporal fluctuations in atmospheric water vapor, surface pressure, and air temperature have different patterns at Jackwhacker Gulch (3362 m in a continental snow climate) compared to Tipton and Clackamas Lake (1570 m and 1036 m, respectively, in maritime snow climates). Additionally, at Tipton and Clackamas Lake, positive biases from soil permittivity errors partially offset the other negative biases. Soil permittivity error is much smaller (and negative) at Jackwhacker Gulch, likely a result of its high-elevation setting with consistently cold temperatures throughout the accumulation season, and does not offset the effects from other error components. This example illustrates two important points: 1) the feasibility of InSAR SWE measurements at a given site cannot be determined solely by average snowpack depth but is also controlled by snow climate and other environmental factors, and 2) for non-ionospheric error sources, correcting some errors but not others may actually decrease accuracy by removing effects of offsetting positive and negative biases.

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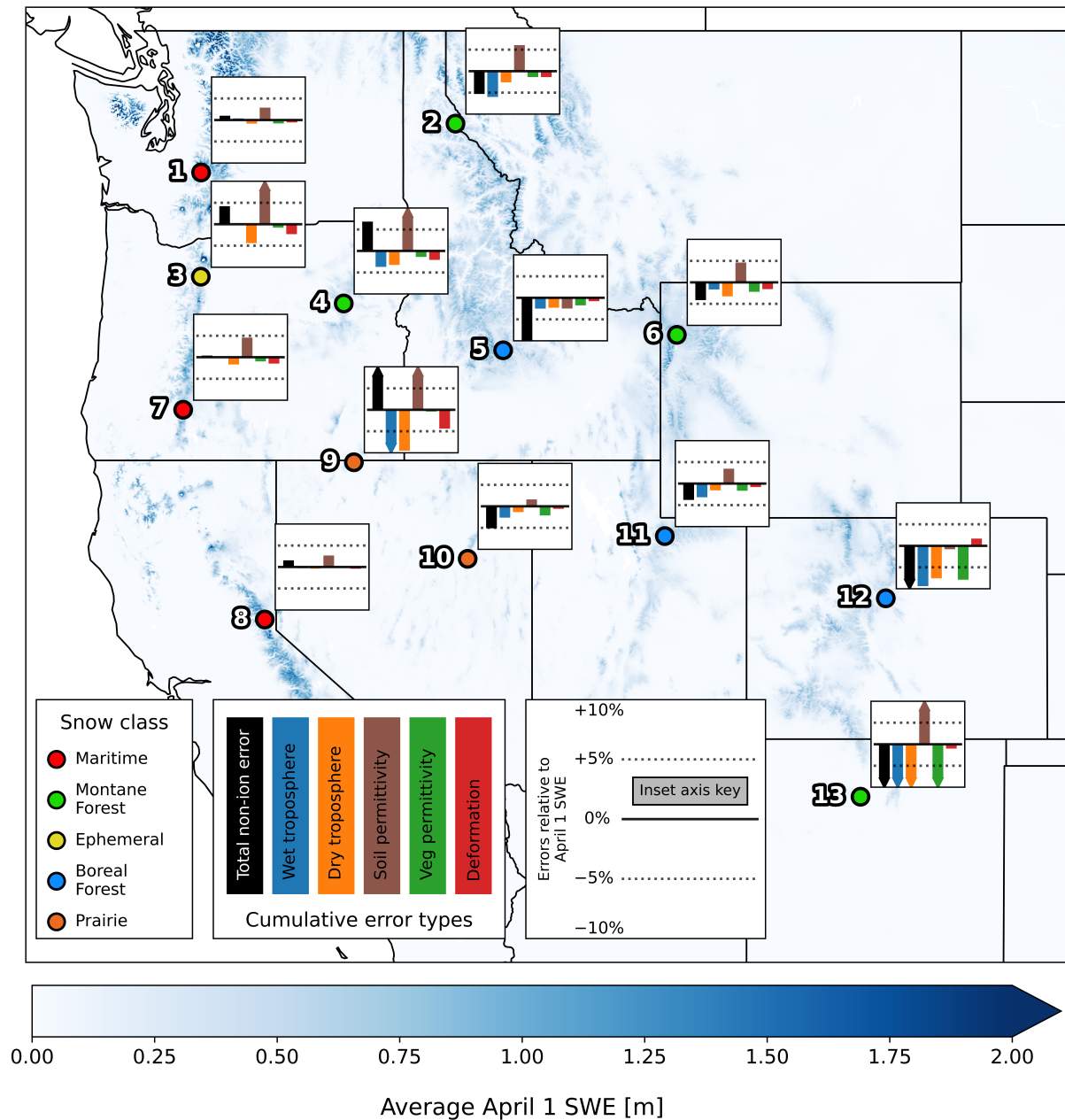


Figure 5. Average cumulative non-snow errors relative to average April 1 SWE at 13 SNOTEL stations, with consistent y-axis scales shown in the bottom inset. Averages are calculated over a 10-year period from water years 2016–2025. In the inset bar charts, the black bars represent the total non-ionospheric error with other colors showing individual error components. The vertical extent of all inset charts are clipped to $\pm 10\%$ of April 1 SWE for the given station with horizontal dashed lines indicating $\pm 5\%$. Error components that extend beyond this range are indicated with an arrowhead at the end of the bar. Station points are colored by snow class (Sturm and Liston, 2021) and the background shows average April 1 SWE calculated using an 800 m reanalysis product (Broxton et al., 2019).

Table 3. Average cumulative errors calculated from October 1 to April 1 over water years 2016–2025. Errors are given as absolute values in meters as well as percentages relative to average April 1 SWE at each station.

No.	Station Name	April 1 SWE [m]	Total Error	Ionosphere	Total Non-Ion Error	Wet Troposphere	Dry Troposphere	Soil Permittivity	Vegetation Permittivity	Surface Deformation
1	Paradise	1.807	0.302 (17%)	0.285 (16%)	0.018 (1%)	0.007 (0%)	-0.015 (-1%)	0.052 (3%)	-0.015 (-1%)	-0.011 (-1%)
2	Sunset	0.479	0.271 (57%)	0.296 (62%)	-0.026 (-5%)	-0.029 (-6%)	-0.012 (-3%)	0.029 (6%)	-0.007 (-1%)	-0.007 (-1%)
3	Clackamas Lake	0.285	0.351 (123%)	0.339 (119%)	0.012 (4%)	0.000 (0%)	-0.013 (-4%)	0.033 (12%)	-0.002 (-1%)	-0.007 (-2%)
4	Tipton	0.326	0.358 (110%)	0.336 (103%)	0.022 (7%)	-0.012 (-4%)	-0.011 (-3%)	0.056 (17%)	-0.005 (-2%)	-0.007 (-2%)
5	Galena Summit	0.532	0.272 (51%)	0.325 (61%)	-0.053 (-10%)	-0.013 (-3%)	-0.012 (-2%)	-0.013 (-3%)	-0.009 (-2%)	-0.004 (-1%)
6	Snake River Station	0.436	0.308 (71%)	0.326 (75%)	-0.018 (-4%)	-0.007 (-2%)	-0.014 (-3%)	0.020 (5%)	-0.010 (-2%)	-0.007 (-2%)
7	Annie Springs	1.035	0.296 (29%)	0.293 (28%)	0.004 (0%)	0.000 (0%)	-0.017 (-2%)	0.047 (5%)	-0.010 (-1%)	-0.015 (-1%)
8	Palisades Tahoe	1.103	0.385 (35%)	0.368 (33%)	0.017 (2%)	-0.003 (0%)	-0.004 (0%)	0.029 (3%)	-0.000 (0%)	-0.005 (0%)
9	Disaster Peak	0.074	0.371 (504%)	0.352 (478%)	0.018 (25%)	-0.010 (-14%)	-0.007 (-10%)	0.039 (53%)	-0.000 (0%)	-0.003 (-4%)
10	Corral Canyon	0.522	0.342 (66%)	0.368 (71%)	-0.027 (-5%)	-0.014 (-3%)	-0.007 (-1%)	0.008 (2%)	-0.011 (-2%)	-0.003 (-1%)
11	Trial Lake	0.670	0.355 (53%)	0.380 (57%)	-0.026 (-4%)	-0.021 (-3%)	-0.011 (-2%)	0.023 (3%)	-0.011 (-2%)	-0.005 (-1%)
12	Jackwhacker Gulch	0.308	0.414 (134%)	0.488 (158%)	-0.074 (-24%)	-0.029 (-9%)	-0.023 (-8%)	-0.002 (-1%)	-0.024 (-8%)	0.005 (2%)
13	Quemazon	0.060	0.347 (581%)	0.400 (670%)	-0.053 (-89%)	-0.055 (-92%)	-0.013 (-21%)	0.025 (41%)	-0.010 (-16%)	-0.001 (-1%)

Although some non-snow errors diminish when integrated over the accumulation season, errors within a given-single 12-day nearest-neighbor interferogram are important considerations for other applications. For example, if a single interferogram is used to examine the spatial variability of snow accumulation from a single event (relevant for avalanche forecasting, for example), non-snow errors can potentially lead to incorrect conclusions about spatial patterns of snow across a landscape. In this context we are interested in absolute values of the non-snow errors as well as their magnitude relative to a single Δ SWE value, not the total accumulated SWE on a particular date. Figure 6 shows the seasonal variability of the six non-snow error components using data from 10 water years (2016–2025) for the same three SNOTEL stations as in Figure 3. The thick blue line indicates the median error for a given day during the 10-year period, with shading between the interquartile range (25th–75th percentiles). For the ionosphere error (bottom row) we show the 12-day error calculated for at both 06:00 local time (representative of NISAR sampling during ascending orbits) and 18:00 local time (NISAR descending orbits).

As indicated by the varying y-axis limits between the rows, the range of absolute error values is smallest for surface deformation (top row) and increases down the rows. Note that all panels in a given row have the same y-axis limits. Surface deformation errors do not show apparent seasonality at any of the three stations. The range of soil permittivity error (second row) is approximately double that of surface deformation error. At Paradise and (left column) and Trial Lake (middle column), soil permittivity errors are largest and most variable between October–December and May–July, with relatively small and consistent errors during the January–April. This reflects early season soil moisture changes from small accumulation and melt events with air temperatures near freezing, and late-season soil moisture changes due to snow melt. We note that errors (from any non-snow factor) in June and July are unlikely to affect InSAR SWE measurements at most locations because liquid water in the snowpack will have already rendered the technique impractical. Soil permittivity errors at Disaster Peak (right column) are more variable throughout the entire winter, which reflects the shallow snowpack and occasional mid-season melt events at this site. At all stations the soil permittivity error is positive for a majority of the season, which leads to the consistently positive cumulative errors shown in Figure 3.

Vegetation permittivity errors (Figure 6, third row) are influenced by canopy height and air temperature. The relatively large and variable vegetation permittivity errors throughout the season at Paradise are a result of tall vegetation (Table 2) and air temperatures that fluctuate both above and below freezing. In contrast, vegetation permittivity errors at Trial Lake show some early-variability in the early season but are consistently small between January and April as air temperatures become consistently cold. Vegetation permittivity errors at Disaster Peak are virtually zero because the surrounding shrub vegetation is only 0.5 m tall according to in the LANDFIRE canopy height dataset.

Error ranges for the dry and wet troposphere components (Figure 6, fourth and fifth rows) are larger at all stations than those for surface deformation, soil permittivity, and vegetation permittivity components. At all stations the dry troposphere error fluctuates both above and below 0 and does not show pronounced seasonality. These patterns result in the small and fluctuating cumulative dry troposphere error shown in Figure 3. The wet troposphere error does show some seasonal variation with generally negative values between October–March and generally positive values between April–July. These results indicate

that wet troposphere effects are likely to negatively bias InSAR SWE measurements calculated from single nearest-neighbor
375 interferograms during the majority of the accumulation season.

The ~~ionospheric~~ ionosphere error (Figure 6, bottom row) is the largest error component by two orders of magnitude. Accurate Δ SWE measurements using NISAR L-band data will not be possible unless ionospheric effects can be appropriately addressed. At all stations there is less ionospheric variability (and therefore less error variability) when the 12-day difference is calculated with morning observations instead of evening observations. ~~Therefore~~ For example, at Trial Lake, the seasonal average AM
380 ionosphere error (mean of the middle AM orbit line) is 0.010 m with an average interquartile range (IQR) of 0.377 m. The seasonal average PM ionosphere error is 0.013 m with an average IQR of 1.031 m. The largest average difference between AM and PM errors is 0.312 m on November 27, a critical early-season period when total SWE and Δ SWE are typically small. Ionosphere errors of 0.312 m potentially represent more than 100% of the snowpack at many WUS locations in late November. The largest difference between AM and PM IQR is 1.206 m on April 12, another critical monitoring period around the timing
385 of peak SWE in the WUS. AM and PM results are similar at Paradise and Disaster Peak. For these reasons, we recommend using ascending NISAR overpasses to generate NISAR interferograms for Δ SWE measurements, which will acquire data at approximately 06:00 local time. However, depending on the area of interest, it may be the case that target locations are imaged only during descending overpasses (e.g., if a slope is within an area of radar shadow for the ascending overpass). Carefully accounting for ionosphere errors in these contexts will be critical for accurate interpretation of NISAR SWE measurements.

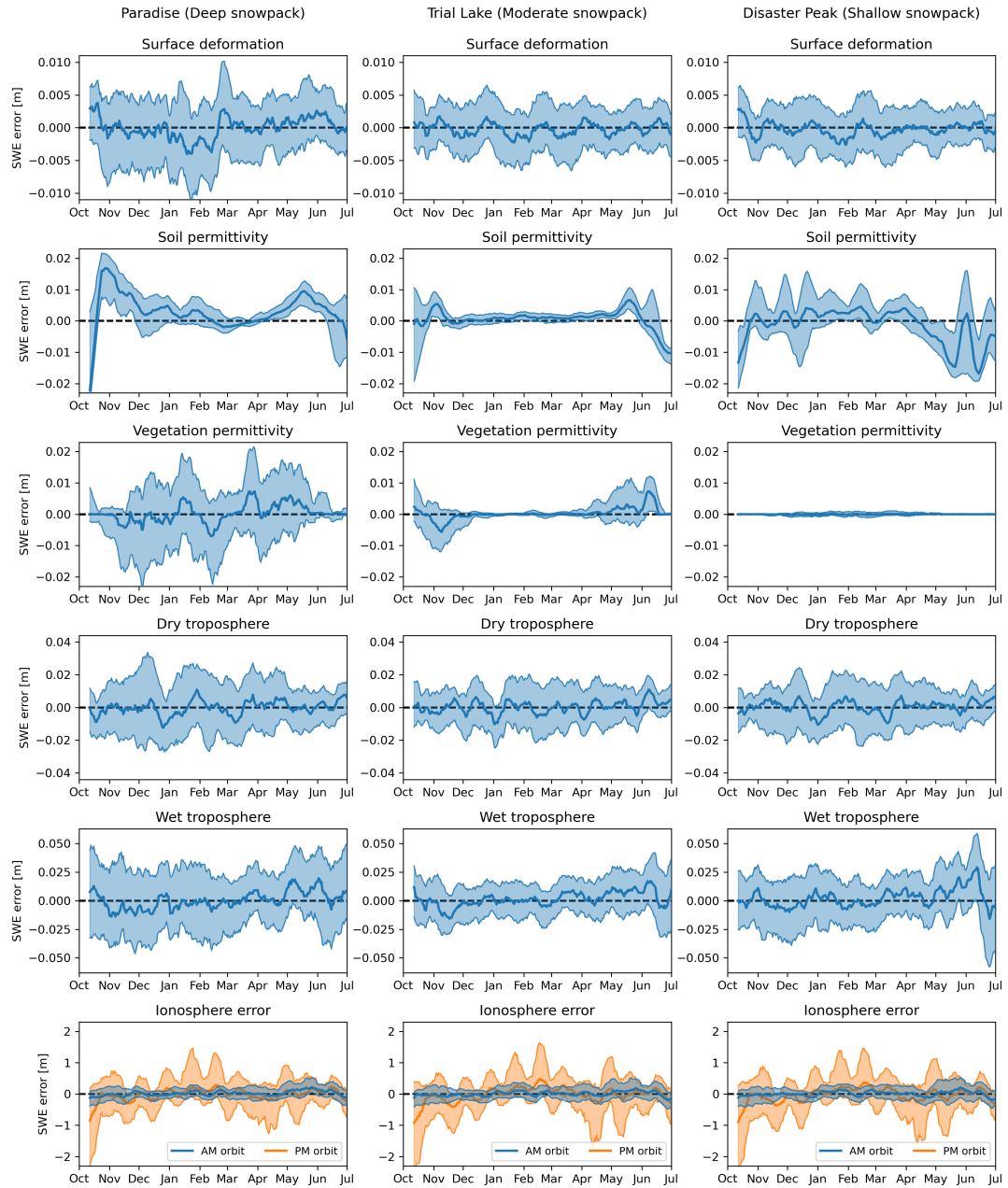


Figure 6. Non-snow error components at Paradise (left column), Trial Lake (middle column) and Disaster Peak (right column). In all subpanels the thick line shows the median value over water years 2016–2025 with shading between the interquartile range. Note the different y-limits for different rows.

390 We summarize the non-snow errors over all 13 stations using error exceedance curves (Figure 7), which show the probability of exceeding an error of a given magnitude if a single measurement is drawn at random from the distribution of all errors. All exceedance curves in the left panel of Figure 7 were calculated using a combined timeseries of daily errors calculated between October 1 and April 1 for all water years at all stations (23,397-482 total measurements). For the western US stations we selected for this analysis, there is a 50% chance that the total non-snow error present in any 12-day NISAR measurement is greater than 0.21-0.212 m (thick red line). If the ionosphere error is removed, the remaining non-ionospheric error (thick black line) will be greater than 0.031 m with 50% probability. ~~Similar calculations~~ The 50% exceedance error values for all curves are given in Table 4. Similar calculations for different probability thresholds can be done using exceedance curves for individual error components shown in the figure. the exceedance curves in the Figure 7.

400 We used a similar analysis to investigate whether non-snow errors behave differently on days with vs. without a snow event. We split the October 1 through April 1 dataset into days where $\Delta SWE = 0$ (1784 total measurements) and days where $\Delta SWE \neq 0$ (21,698 total measurements), representing both accumulation and ablation events. When $\Delta SWE = 0$, the 50% exceedance thresholds were 0.210 m for total non-snow error and 0.031 m for non-ionospheric error. When $\Delta SWE \neq 0$, the 50% exceedance thresholds were 0.230 m for total non-snow error and 0.030 m for non-ionospheric error. The error curves for the two cases (not shown) were quite similar to those in the left panel of Figure 7. This result indicates that non-snow factors affect the phase relatively consistently, regardless if a snow event occurs or not.

405 It is also important to consider the magnitudes of these errors relative to the real ΔSWE values measured at the stations during the same periods. ~~We filtered our initial error distributions~~ To investigate snow events of varying magnitudes, we filtered our error dataset to select only 12-day periods at each station where at least SWE accumulation measurements where the 12-day SWE accumulation at a given station was above a certain threshold (i.e., 0.01 m to include both small and large accumulations, or 0.2 m to isolate large accumulations only), then divided the total non-ionospheric errors from those periods by the accumulated SWE (Figure 7, right panel). These ~~We removed the ionosphere error from this figure to improve clarity.~~ The results indicate that for small SWE accumulations down to 0.01 m, there is a 50% chance that the total non-ionospheric error present in a randomly selected NISAR measurement is greater than 67% of the SWE accumulated during the same period. When we restrict the data to only consider large 12-day SWE accumulations (0.2 m or larger), the 50% exceedance probability drops to 15% of accumulated SWE. 12-day SWE accumulation events larger than 0.2 m were relatively rare in our dataset and occurred in less than 3% of all 12-day periods.

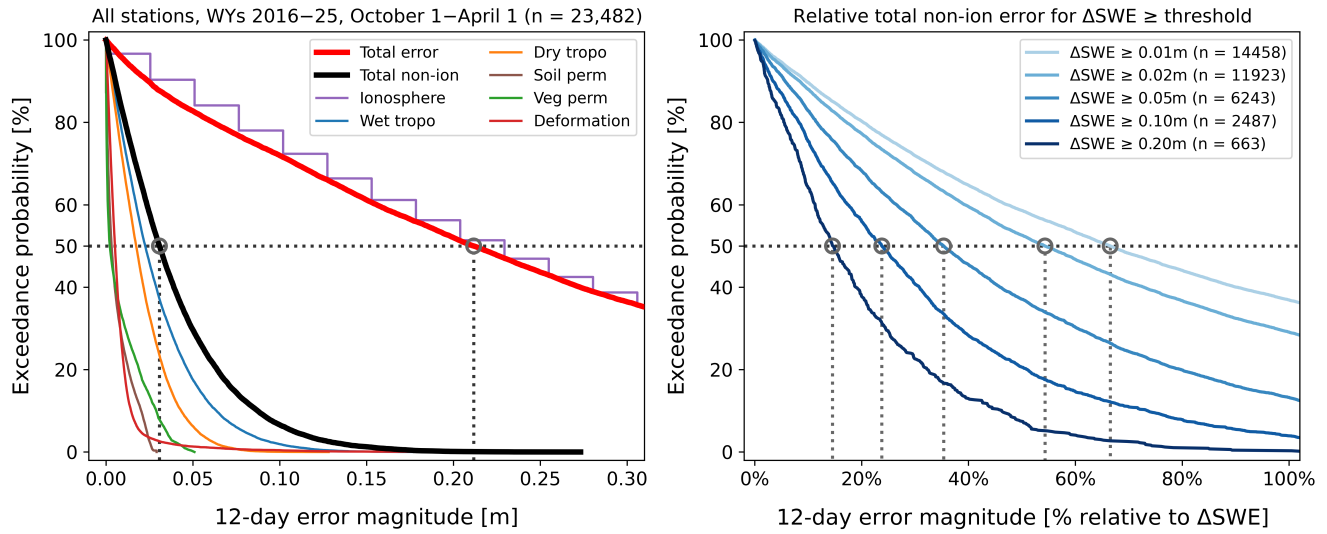


Figure 7. Exceedance probabilities for different non-snow errors. In both panels, the exceedance distributions are calculated using data from all stations (Table 2) for water years 2016–2025. Distributions in the left panel are calculated using 12-day errors from every day between October 1 and April 1 and presented as absolute values in units of meters. Note that the stepwise appearance of the ionospheric error (purple curve) is due to the relatively coarse precision of the IGS IONEX data (see Table 1). Distributions in the right panel are calculated from subsets of 12-day periods between October 1 and April 1 when ΔSWE was larger than the indicated threshold value (0.01, 0.02, 0.05, 0.1, and 0.2 m).

Table 4. 50% exceedance errors [m] for error curves shown in Figure 7, left panel.

<u>Error type</u>	<u>50% exceedance error [m]</u>
<u>Total Error</u>	<u>0.211</u>
<u>Ionosphere</u>	<u>0.229</u>
<u>Total Non-Ion Error</u>	<u>0.031</u>
<u>Wet troposphere</u>	<u>0.023</u>
<u>Dry troposphere</u>	<u>0.017</u>
<u>Surface deformation</u>	<u>0.005</u>
<u>Soil permittivity</u>	<u>0.003</u>
<u>Vegetation permittivity</u>	<u>0.002</u>

4.1 Error variation over North American transects

With gridded datasets it is possible to assess how non-snow error components vary across larger regions, even if in situ stations are not available. Based on data availability we explore only the wet troposphere, dry troposphere, and morning/evening
420 ionosphere errors between 2016–2025 across several transects in North America (Figure 8). Over the North America S–N transect, the dry troposphere error becomes larger than the wet troposphere error north of approximately 63° latitude. Although the tropospheric errors in this region are only equivalent to several centimeters of SWE, the tundra snowpacks in northern Canada may only accumulate some tens of centimeters of SWE in a given season, and average Δ SWE is similarly small. Hence it remains important to account for both wet and dry troposphere effects when retrieving Δ SWE at high latitudes. We also note
425 that the spatial correlation length of atmospheric pressure is on the order of hundreds of kilometers for atmospheric pressure, but is on the order of tens of kilometers for atmospheric water vapor. Therefore we expect that over a NISAR interferogram spanning hundreds of kilometers, the dry troposphere error may be relatively constant and vary primarily with topography but the wet troposphere error could vary horizontally over the scene. Correcting this wet troposphere effect will be critical, and potentially challenging, for accurate interpretation of spatially distributed Δ SWE measurements from NISAR.

430 Similar to results from the SNOTEL stations, the average ionosphere error in the spatial transects is much larger than either the wet or dry troposphere errors. Decreases in errors in the middle of the North America S–N and Canadian Border transects are visible, indicating smaller 12-day ionospheric changes over the middle of the continent. However, even in these regions the ionospheric signal would dwarf expected values of Δ SWE in the same 12 day period. Regardless of location, there is less ionospheric variability (and therefore less error) when the 12-day difference is calculated with morning observations instead
435 of evening observations (see ~~also~~ Figure 6). Therefore, for areas that fall within both ascending and descending overpasses, we again recommend using the ascending (morning) overpasses to generate NISAR interferograms for Δ SWE measurements. Morning overpasses also increase the probability of imaging dry snow during the transition from accumulation to melt season, which improves InSAR coherence and could potentially extend the measurement season by several weeks. For areas that fall only within descending overpasses, or if descending and ascending overpasses are used together to improve the temporal
440 resolution of Δ SWE measurements, carefully addressing the ionosphere error will be crucial for accurate SWE measurement.

We are not aware of a daily, gridded soil moisture product that provides valid data during winter months. Based on the results of the SNOTEL analysis (Figure 5, Table 3), soil permittivity errors have the greatest impact on shallow, low-elevation snowpacks with midwinter melt events or other factors leading to ephemeral snow. Although ephemeral and marginal snow-
445 packs can play important ecological and climatological roles (Petersky and Harpold, 2018; López-Moreno et al., 2024), these snowpacks are less critical observation targets for current water resources applications in the western US. Measurements at high latitudes with intermittent frozen soils may see increased errors at the beginning of the accumulation season as soils go through freeze/thaw cycles, as this changes the penetration depth of the radar signals. We also note that changes in soil moisture are difficult to measure and interpret when soil temperatures are near freezing, which could further complicate soil effects on InSAR SWE measurements in permafrost regions.

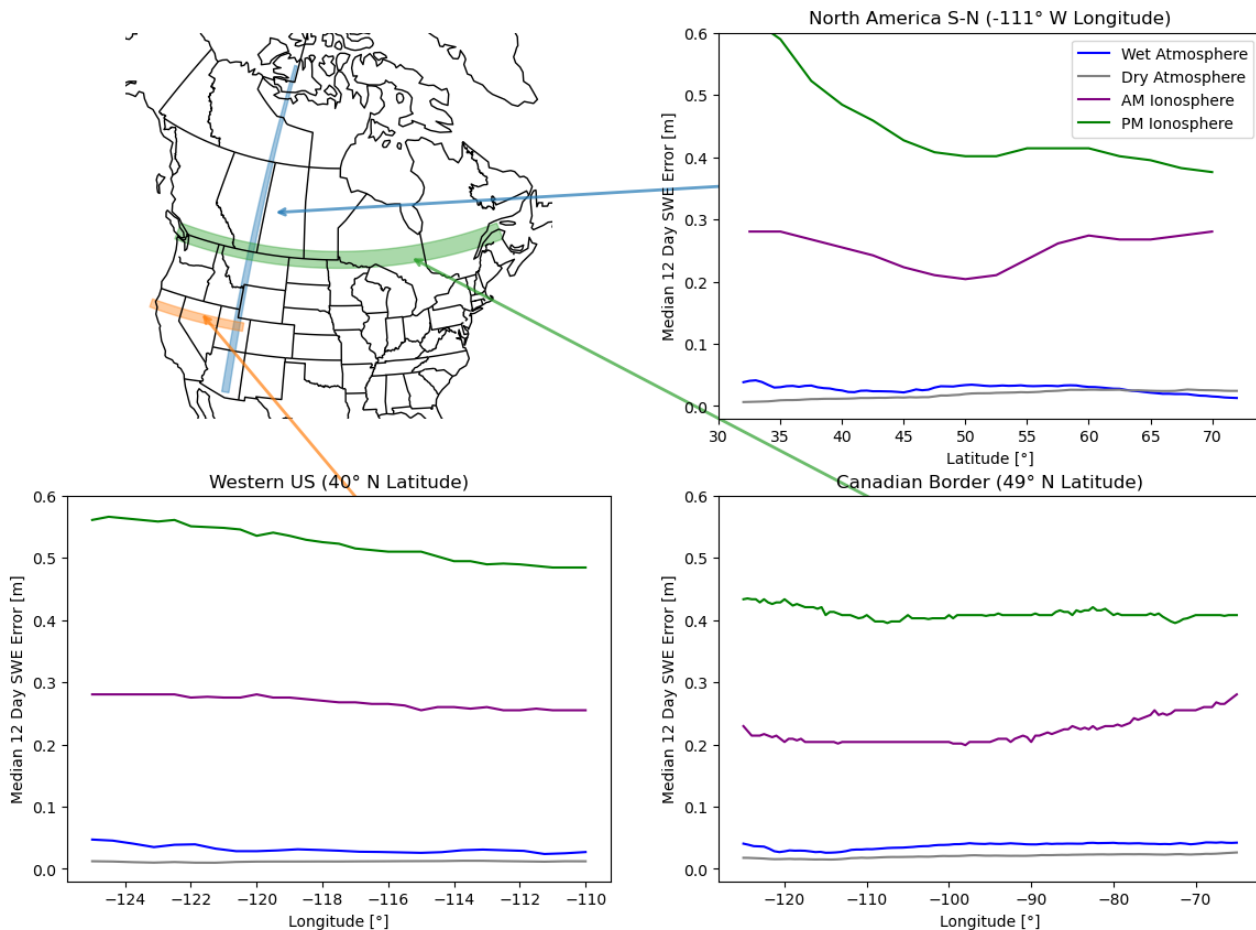


Figure 8. Spatial variation in wet atmospheric, dry atmospheric, and ionospheric errors across different transects in North America.

450 5 Discussion

We analyzed the impact on SWE retrievals of five frequency-independent error sources and one frequency dependent (ionospheric) error source. For SWE measurements with L-band NISAR data, our analysis shows that the ionosphere, wet troposphere, and dry troposphere components have the largest error values for InSAR SWE retrievals across the western US (Figure 7, Table 4). Fortunately, corrections for these three errors are planned for NISAR standard interferogram products (Brancato et al., 2024), which will ultimately improve the accuracy of Δ SWE retrievals from a single interferogram. However, it is important to consider the offsetting effects of different error components when the total SWE is calculated by integrating a timeseries of Δ SWE measurements. At many stations, the cumulative wet and dry troposphere errors introduced negative bias into April 1 SWE measurements while soil moisture errors introduced a positive bias on average over the 10 year period investigated (Figure 5). Removing only the troposphere errors may actually decrease the overall accuracy of the April 1 SWE measurements

460 at those locations. For some locations with moderate to deep snowpacks, it may be better to leave all non-ionospheric errors present in Δ SWE calculations, assuming a sufficiently long integration time.

Another consideration for troposphere corrections in NISAR standard interferograms is the length scales at which the corrections are calculated and applied. Atmospheric pressure may have a correlation length approaching 100 kilometers, approximately the size of a satellite tile. However, the correlation length of atmospheric water vapor is smaller than that of pressure. 465 ~~At:~~ at horizontal spatial scales less than 6 km, atmospheric water vapor is well-approximated by Gaussian random fields (Calbet et al., 2022). Hence, temporal changes in atmospheric water vapor may add unbiased spatially variable random errors to InSAR SWE measurements over a basin of interest, while temporal changes in atmospheric pressure may add overall bias to measurements over the same region. But this assumes that the atmospheric models used to calculate the corrective layers can accurately represent atmospheric spatial variability in complex terrain. If the models are too coarse to simulate relevant atmo- 470 spheric processes over mountainous regions, significant troposphere effects may still be present in phase measurements even after an attempted correction. This may complicate the interpretation of Δ SWE measurements from a single interferogram, especially in complex terrain where snow depth can have a correlation length in the tens of meters (Blöschl, 1999). Future work to examine atmospheric errors in NISAR SWE measurements could involve reprocessing Level 1 data with higher resolution weather models (e.g., HRRR over the western US) and exploring time-series inversion approaches.

475 Efforts to estimate SWE from NISAR in other regions should carefully consider all error components based on site-specific characteristics. In some environments it is possible that some non-snow error factors are correlated. For example, measurements at high latitudes may be particularly influenced by surface deformation caused by freezing and thawing soils, which may also increase soil permittivity errors early in the accumulation season. Additionally, we note that sensor-specific factors may affect InSAR SWE measurements to a greater degree than the error components discussed here. We did not consider temporal 480 coherence of InSAR phase, which is a function of incidence angle as well as changes in surface characteristics (Zebker and Villasenor, 1992; Rosen et al., 2000). In particular, although vegetation permittivity errors were small at most stations (Figures 5 and 7), InSAR SWE measurements are not possible over sufficiently dense forest cover due to high temporal decorrelation; previous work has shown SWE retrievals possible for forest cover fractions less than 0.5 (Bonnell et al., 2024a). These and other sensor-specific factors (e.g., radar shadow) must be considered alongside the non-snow error components discussed here.

485 ~~Finally, we~~ We note several limitations of our analysis. First, this work focused on the simplest time series approach using cumulative nearest-neighbor interferograms. We do not attempt to explore the improvements from more complex time-series approaches like small-baseline subset analysis (Li et al., 2022) or phase-linking (Eppler and Rabus, 2022) to separate systematic signals of interest from temporally random fluctuations in atmospheric phase. If applied carefully, more advanced InSAR methods have the potential to significantly reduce non-snow errors compared to a nearest-neighbor approach. Next, there is 490 considerable range in the spatial resolution and fidelity of the datasets we used to calculate non-snow errors. For example, soil moisture measurements came from point-based, high fidelity instruments while the data relevant for ionosphere and troposphere errors came from coarse reanalysis products that contain larger errors and biases. ~~Our aim was primarily to illustrate the relative magnitudes and importance of these error sources for InSAR SWE retrievals.~~ Future work with other data sources such as radiosondes for troposphere changes and multi-frequency SAR systems for the ionosphere would be valuable.

495 Finally, this work could be expanded both spatially and temporally. ~~A~~ We analyzed errors at only 13 SNOTEL stations across
the WUS. Although this selection was partially dictated by data availability (see Section 2.3), it is possible that our results
would change if we had selected different sites. For example, two of our three shallow snowpack stations (Disaster Peak and
Quemazon) are in post-burn areas and may have snow accumulation and melt dynamics that are not fully representative of their
broader geographic regions (Smoot and Gleason, 2021). However, our intent is not to draw broad conclusions about the method
500 based on the 13 sites selected; rather, we aim to illustrate that the non-snow factors we considered here can have different
magnitudes and effects in different snowpacks. Especially given that wildfire area has been increasing in snow-dominated
regions across the WUS since the 1980s (Kampf et al., 2022) and WUS snowpacks are projected to continue their general
decline (Siirila-Woodburn et al., 2021), it is likely that the WUS will become more reliant on shallow and post-burn snowpacks
for water resources in the coming years and decades. We encourage future work in snow remote sensing to continue examining
505 shallow and marginal snowpacks (López-Moreno et al., 2024). More broadly, a future global scale analysis would be useful
in capturing the variability of each component in a larger diversity of ecoregions, including regions with more frequent large
accumulation events. We did not evaluate the error associated with very large SWE changes that would cause phase wrapping
($\Delta\text{SWE} \geq 0.2385$ ~~≥ 0.2385~~ > 0.2385 m), as this would require evaluation of the impact of various phase unwrapping algorithms beyond
the scope of this study. We note that 12-day $\Delta\text{SWE} \geq 0.2385$ m was only recorded 418 times in our dataset, approximately
510 1.8% of observations. Expanding the analysis with a longer temporal record would better capture ionospheric cycles which
occur on the order of years to decades.

6 Conclusions

We ~~quantified~~ simulated errors in six non-snow components (ionosphere, wet troposphere, dry troposphere, soil permittivity,
vegetation permittivity, and surface deformation) for SWE measurements derived from L-band (1.257 GHz) InSAR measure-
515 ments at a 12-day measurement frequency, ~~simulating the expected~~ based on the NISAR data acquisition strategy over the
western US. We compared the non-snow errors to SWE measured at 13 SNOTEL stations spanning a range of snow and envi-
ronmental characteristics (Table 2). Temporal variation of total electron content in the ionosphere causes the largest non-snow
error by an order of magnitude, with 50% of measured 12-day errors exceeding 0.229 m or 463% of measured ΔSWE (when
 $\Delta\text{SWE} \geq 0.01$ ~~≥ 0.01~~ > 0.01 m) over the same periods (Table 4, Figure 7). When ionosphere errors are removed, the 50% exceedance
520 probability of remaining non-snow error is reduced to 0.031 m or 67% of ΔSWE . The wet and dry troposphere errors, due to
temporal variation in atmospheric water vapor and pressure, respectively, are the largest non-ionospheric components, followed
by surface deformation, vegetation permittivity, soil permittivity, ~~and surface deformation~~.

When a timeseries of 12-day ΔSWE measurements is integrated to obtain ~~total accumulated SWE~~ seasonal SWE accumulation,
the cumulative effects of non-snow errors partially offset each other (Figure 5). At most stations, cumulative soil permittivity
525 errors introduce a positive bias into April 1 SWE measurements, while cumulative troposphere errors introduce a negative bias.
The net result is that at 10 of 13 SNOTEL stations, the total cumulative error for all non-ionospheric components is within
10% of measured April 1 SWE (Table 3), meeting accuracy targets for remotely sensed SWE measurements established in

the 2017–2027 National Academies Decadal Survey. The three stations where errors exceeded 10% of April 1 SWE represent shallow snowpacks (average April 1 SWE between 0.060–0.308 m) and in two cases, post-burn areas. However, the cumulative
530 ionosphere error at all stations ranged between 16–670% of April 1 SWE, well outside the target accuracy threshold.

The importance and challenge of accounting for all of these error sources, including evaluating the uncertainty in the corrections, demonstrates the requirement-necessity for independent calibration and validation ~~observations~~ from in situ stations and field efforts. InSAR SWE estimates will not produce spatially and temporally complete information, since NISAR has a 12-day orbit cycle and the technique will not work in all locations at all times (i.e., in dense forests or wet snowpacks). A data
535 assimilation approach that uses InSAR SWE estimates and in situ observations to correct a physically-based snowpack model will likely provide the most robust SWE estimates.

For future work that makes use of NISAR-derived SWE measurements, we make the following suggestions:

- Careful removal of ionospheric effects from phase data is critical for accurate SWE measurements from NISAR, both for 12-day Δ SWE and season-long accumulation. If possible, use interferograms generated from ascending (morning)
540 NISAR acquisitions to reduce ionospheric error and improve chances of imaging dry snow.
- Wet and dry troposphere errors must be removed for accurate Δ SWE measurements from a single NISAR interferogram. This is especially relevant for interpreting spatial patterns of snow accumulation at basin to range scales. Removing errors from surface deformation, vegetation permittivity, and soil permittivity will also improve accuracy but are less critical.
- Removing non-ionospheric error components from cumulative measurements requires careful consideration. Integrated
545 errors between October 1 and April 1 had offsetting effects for different components (e.g., soil permittivity and wet troposphere); removing a single component without its offsetting effect may actually decrease the accuracy of accumulated SWE measurements. Future work should examine how these offsetting effects change over varying integration periods, and the inter-annual as well as the interannual variation of these relationships.
- Site-specific factors should be considered to identify more or less influential error sources. For example, surface deformation may be more important to correct for SWE measurements over permafrost than over the non-frozen soils we
550 considered here.
- Although we could not consider sensor-specific factors like temporal coherence, radar shadow, or phase unwrapping in this analysis, they may introduce more error into NISAR SWE measurements than some of the components we discussed here.
- Removing non-snow errors may be more feasible using more complex InSAR data processing algorithms, including
555 small-baseline subset analysis or phase-linking.

Code and data availability. All raw data used for this analysis are publicly available at the repositories described in the text. Code and processed data to recreate all figures in this analysis are available at https://github.com/rpalomaki/SWE_error_analysis .

7 Error Terms Equations

560 We provide the following equations for each non-snow error term and direct the reader to Hoppinen et al. (submitted) for a more in-depth discussion and analysis of these equations. In all equations λ is the central free-air wavelength for the SAR sensors and θ_i is the local incidence angle.

6.1 Surface Deformation

Phase change due to surface elevation changes is given by

$$565 \quad \underline{\Delta\phi_{\text{defo}} = \frac{4\pi}{\lambda} \Delta R}$$

where ΔR is the change in the line-of-sight distance between the ground and the sensor.

6.1 Ionospheric Advance

Phase change due to changes in electron density in the ionosphere is given by

$$\underline{\Delta\phi_{\text{iono}} = -\frac{4\pi K \lambda}{c^2} \Delta\text{TEC}}$$

570 where K is a constant ($40.28 \text{ m}^3\text{s}^{-2}$), c is the speed of light, and TEC is the vertically integrated total electron content (ΔTEC) given in total electron count units (TECU or $1\text{e}16$ electrons per m^2) (Rosen et al., 2010).

6.1 Tropospheric Delay

The dry tropospheric phase change is given by

$$\underline{\Delta\phi_{\text{dry-atmo}} = \frac{4\pi}{\lambda} \frac{10^{-6}}{\cos(\theta_i)} \frac{k_1 R_d}{g_m} \Delta P(z)}$$

575 where k_1 is a constant ($0.776 \text{ K}\cdot\text{Pa}^{-1}$), R_d is the specific gas constant for dry air ($287.05 \text{ J}\cdot\text{kg}^{-1}\cdot\text{K}^{-1}$), and g_m is the local gravitational acceleration (assumed static at $9.81 \text{ m}\cdot\text{s}^{-2}$). $\Delta P(z)$ is the change in surface pressure in Pa between two SAR acquisitions (Jolivet et al., 2014).

The wet tropospheric phase change is given by

$$\underline{\Delta\phi_{\text{wet-atmo}} \approx \frac{4\pi}{\lambda} \frac{6.5}{\cos(\theta_i)} \Delta\text{PW}}$$

580 where PW is the vertically integrated height of water vapor within an atmospheric column in meters of precipitable water vapor (?).

6.1 Soil Moisture

Phase change due to changes in soil permittivity changes is given by-

$$\Delta\phi_{\text{soil}} = \frac{1}{2jk'_{z1} - 2jk'_{z2}}$$

585 where the vertical wavenumber k'_z characterizes the wave speed and can be expressed in terms of the angular frequency of the radar wave (ω), the real part of the soil dielectric permittivity (ϵ'), the soil magnetic permeability (μ), and the horizontal free-air wavenumber (k_x) (De Zan et al., 2014) as-

$$k'_z = \sqrt{\omega^2 \epsilon' \mu - k_x^2}$$

590 We assume magnetic permeability is approximately one at low radar frequencies Youn et al. (2010) and calculate the real part of the dielectric permittivity based on the polynomial approximations for moisture and soil composition given in Hallikainen et al. (1985) :-

6.1 Vegetation Permittivity

We use the mixing model between wood, water, air, and ice given in Schwank et al. (2021). The primary equation for phase changes due to canopy permittivity is-

$$595 \Delta\phi_{\text{vege}} = \frac{4\pi}{\lambda} H \left(\sqrt{\epsilon_{c,2} - \sin^2(\theta_i)} - \sqrt{\epsilon_{c,1} - \sin^2(\theta_i)} \right)$$

where H is the canopy height, and the canopy permittivity ϵ_c at time 1 and 2 is defined by:-

$$\epsilon_c = \epsilon_{\text{air}} + \frac{(\epsilon_{\text{wood}} - \epsilon_{\text{air}})(\epsilon_{\text{wood}} + 5\epsilon_{\text{air}})v_{\text{SCC}}}{3(\epsilon_{\text{wood}} + \epsilon_{\text{air}}) - 2(\epsilon_{\text{wood}} - \epsilon_{\text{air}})v_{\text{SCC}}}$$

600 where v_{SCC} is the volume fraction of space occupied by small canopy constituents (branches, stems, trunks) and ϵ_{air} is the permittivity of free air, and ϵ_{wood} is the permittivity of wood. This permittivity is calculated from the porosity and density of the wood combined with wood cell, water, and ice permittivities and ratios as-

$$\epsilon_{\text{wood}} = v_{\text{H2O}}\epsilon_{\text{H2O}} + (1 - \text{por})\epsilon_{\text{wood-cell}} + (\text{por} - v_{\text{H2O}})\epsilon_{\text{air}}$$

We assume that the only temporally variable parameter in winter is permittivity of the water within the wood, which is controlled by the the water-to-ice ratio within the wood cell (v_{water}):-

$$\epsilon_{\text{H2O}} = v_{\text{water}}\epsilon_{\text{water}} + (1 - v_{\text{water}})\epsilon_{\text{ice}}$$

605 While direct measurements of ice-water ratio within wood are challenging we use the approximation using air temperature (T_C) given in Schwank et al. (2021):-

$$v_{\text{water}}(T_C) = \begin{cases} 1, & \text{if } T_C > 0^\circ\text{C} \\ \exp\left(\frac{T_C}{T_{\text{melt}}}\right), & \text{if } T_C \leq 0^\circ\text{C} \end{cases}$$

For all non-varying parameters in Equations 12–16 we use those given in Table 1 of Schwank et al. (2021).

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610 the initial draft of the manuscript and ZH and HPM provided feedback for subsequent drafts.

Competing interests. The authors declare that they have no conflict of interest.

Disclaimer. TEXT

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615 References

- Belinska, K., Fischer, G., and Hajnsek, I.: Combining Differential SAR Interferometry and Copolar Phase Differences for Snow Water Equivalent Estimation, *IEEE Geoscience and Remote Sensing Letters*, 21, 1–5, <https://doi.org/10.1109/LGRS.2024.3461229>, 2024.
- Bevis, M., Businger, S., Chiswell, S., Herring, T. A., Anthes, R. A., Rocken, C., and Ware, R. H.: GPS Meteorology: Mapping Zenith Wet Delays onto Precipitable Water, *Journal of Applied Meteorology and Climatology*, 33, 379–386, 1994.
- 620 Blöschl, G.: Scaling Issues in Snow Hydrology, *Hydrological Processes*, 13, 27, 1999.
- Bonnell, R., Elder, K., McGrath, D., Marshall, H. P., Starr, B., Adebisi, N., Palomaki, R. T., and Hoppinen, Z.: L-band InSAR Snow Water Equivalent Retrieval Uncertainty Increases with Forest Cover Fraction, *Geophysical Research Letters*, 51, e2024GL111708, <https://doi.org/10.1029/2024GL111708>, 2024a.
- Bonnell, R., McGrath, D., Tarricone, J., Marshall, H.-P., Bump, E., Duncan, C., Kampf, S., Lou, Y., Olsen-Mikitowicz, A., Sears, M.,
625 Williams, K., Zeller, L., and Zheng, Y.: Evaluating L-band InSAR Snow Water Equivalent Retrievals with Repeat Ground-Penetrating Radar and Terrestrial Lidar Surveys in Northern Colorado, *The Cryosphere*, 18, 3765–3785, <https://doi.org/10.5194/tc-18-3765-2024>, 2024b.
- Brancato, V., Jung, J., Huang, X., and Fattahi, H.: NASA SDS Product Specification: Level-2 Geocoded Unwrapped Interferogram, Tech. Rep. JPL D-102272 (Rev E), NASA Jet Propulsion Laboratory, Pasadena, California, 2024.
- 630 Broxton, P., Zeng, X., and Dawson, N.: Daily 4 Km Gridded SWE and Snow Depth from Assimilated In-Situ and Modeled Data over the Conterminous US, Version 1, <https://doi.org/10.5067/0GGPB220EX6A>, 2019.
- Calbet, X., Carbajal Henken, C., DeSouza-Machado, S., Sun, B., and Reale, T.: Horizontal Small-Scale Variability of Water Vapor in the Atmosphere: Implications for Intercomparison of Data from Different Measuring Systems, *Atmospheric Measurement Techniques*, 15, 7105–7118, <https://doi.org/10.5194/amt-15-7105-2022>, 2022.
- 635 De Zan, F., Parizzi, A., Prats-Iraola, P., and López-Dekker, P.: A SAR Interferometric Model for Soil Moisture, *IEEE Transactions on Geoscience and Remote Sensing*, 52, 418–425, <https://doi.org/10.1109/TGRS.2013.2241069>, 2014.
- Deeb, E. J., Forster, R. R., and Kane, D. L.: Monitoring Snowpack Evolution Using Interferometric Synthetic Aperture Radar on the North Slope of Alaska, USA, *International Journal of Remote Sensing*, 32, 3985–4003, <https://doi.org/10.1080/01431161003801351>, 2011.
- Dewitz, J.: LANDFIRE 2024 Update, <https://doi.org/10.5066/P1XVKXRL>, 2026.
- 640 Eppler, J. and Rabus, B. T.: Adapting InSAR Phase Linking for Seasonally Snow-Covered Terrain, *IEEE Transactions on Geoscience and Remote Sensing*, 60, 1–13, <https://doi.org/10.1109/TGRS.2022.3186522>, 2022.
- Global Modeling And Assimilation Office and Pawson, S.: MERRA-2 inst1_2d_int_Nx: 2d, 1-Hourly, Instantaneous, Single-Level, Assimilation, Vertically Integrated Diagnostics V5.12.4, <https://doi.org/10.5067/G0U6NGQ3BLE0>, 2015.
- Gneriussen, T., Hogda, K., Johnsen, H., and Lauknes, I.: InSAR for Estimation of Changes in Snow Water Equivalent of Dry Snow, *IEEE
645 Transactions on Geoscience and Remote Sensing*, 39, 2101–2108, <https://doi.org/10.1109/36.957273>, 2001.
- Hallikainen, M. T., Ulaby, F. T., Dobson, M. C., El-rayes, M. A., and Wu, L.-k.: Microwave Dielectric Behavior of Wet Soil- Part 1: Empirical Models and Experimental Observations, *IEEE Transactions on Geoscience and Remote Sensing*, GE-23, 25–34, <https://doi.org/10.1109/TGRS.1985.289497>, 1985.
- Hoppinen, Z., Oveisgharan, S., Marshall, H.-P., Mower, R., Elder, K., and Vuyovich, C.: Snow Water Equivalent Retrieval over Idaho – Part
650 2: Using L-band UAVSAR Repeat-Pass Interferometry, *The Cryosphere*, 18, 575–592, <https://doi.org/10.5194/tc-18-575-2024>, 2024.

- Hoppinen, Z., Palomaki, R. T., Marshall, H.-P., and Bishop, A. E.: Separating Snow from Signal: Quantifying Non-Snow Errors in InSAR SWE Retrievals, TechRxiv [preprint], submitted.
- Jolivet, R., Agram, P. S., Lin, N. Y., Simons, M., Doin, M.-P., Peltzer, G., and Li, Z.: Improving InSAR Geodesy Using Global Atmospheric Models, *Journal of Geophysical Research: Solid Earth*, 119, 2324–2341, <https://doi.org/10.1002/2013JB010588>, 2014.
- 655 Kampf, S. K., McGrath, D., Sears, M. G., Fassnacht, S. R., Kiewiet, L., and Hammond, J. C.: Increasing Wildfire Impacts on Snowpack in the Western U.S., *Proceedings of the National Academy of Sciences*, 119, e2200333 119, <https://doi.org/10.1073/pnas.2200333119>, 2022.
- Lean, J. L., Meier, R. R., Picone, J. M., Sassi, F., Emmert, J. T., and Richards, P. G.: Ionospheric Total Electron Content: Spatial Patterns of Variability, *Journal of Geophysical Research: Space Physics*, 121, 10,367–10,402, <https://doi.org/10.1002/2016JA023210>, 2016.
- Leinss, S., Wiesmann, A., Lemmetyinen, J., and Hajnsek, I.: Snow Water Equivalent of Dry Snow Measured by Differential Interferometry, *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing*, 8, 3773–3790, <https://doi.org/10.1109/JSTARS.2015.2432031>, 2015.
- 660 Li, S., Xu, W., and Li, Z.: Review of the SBAS InSAR Time-series Algorithms, Applications, and Challenges, *Geodesy and Geodynamics*, 13, 114–126, <https://doi.org/10.1016/j.geog.2021.09.007>, 2022.
- López-Moreno, J., Callow, N., McGowan, H., Webb, R., Schwartz, A., Bilish, S., Revuelto, J., Gascoin, S., Deschamps-Berger, C., and 665 Alonso-González, E.: Marginal Snowpacks: The Basis for a Global Definition and Existing Research Needs, *Earth-Science Reviews*, 252, 104 751, <https://doi.org/10.1016/j.earscirev.2024.104751>, 2024.
- Marshall, H.-P. and Koh, G.: FMCW Radars for Snow Research, *Cold Regions Science and Technology*, 52, 118–131, <https://doi.org/10.1016/j.coldregions.2007.04.008>, 2008.
- Meyer, F. J. and Agram, P. S.: Modeling Ionospheric Phase Noise for NISAR Mission Data, in: 2017 IEEE International Geoscience and 670 Remote Sensing Symposium (IGARSS), pp. 3806–3809, ISSN 2153-7003, <https://doi.org/10.1109/IGARSS.2017.8127829>, 2017.
- National Academies of Sciences, Engineering, and Medicine: Thriving on Our Changing Planet: A Decadal Strategy for Earth Observation from Space., The National Academies Press, Washington, D.C., ISBN 978-0-309-46757-5, 2018.
- Oveisgharan, S., Zinke, R., Hoppinen, Z., and Marshall, H. P.: Snow Water Equivalent Retrieval over Idaho – Part 1: Using Sentinel-1 Repeat-Pass Interferometry, *The Cryosphere*, 18, 559–574, <https://doi.org/10.5194/tc-18-559-2024>, 2024.
- 675 Palomaki, R. T. and Sproles, E. A.: Assessment of L-band InSAR Snow Estimation Techniques over a Shallow, Heterogeneous Prairie Snowpack, *Remote Sensing of Environment*, 296, 113 744, <https://doi.org/10.1016/j.rse.2023.113744>, 2023.
- Patitz, W. E., Brock, B. C., and Powell, E. G.: Measurement of Dielectric and Magnetic Properties of Soil, Tech. rep., Sandia National Laboratories, Albuquerque, New Mexico 87185 and Livermore, California 94550, 1995.
- Petersky, R. and Harpold, A.: Now You See It, Now You Don't: A Case Study of Ephemeral Snowpacks and Soil Moisture Response in the 680 Great Basin, USA, *Hydrology and Earth System Sciences*, 22, 4891–4906, <https://doi.org/10.5194/hess-22-4891-2018>, 2018.
- Poggio, L., de Sousa, L. M., Batjes, N. H., Heuvelink, G. B. M., Kempen, B., Ribeiro, E., and Rossiter, D.: SoilGrids 2.0: Producing Soil Information for the Globe with Quantified Spatial Uncertainty, *SOIL*, 7, 217–240, <https://doi.org/10.5194/soil-7-217-2021>, 2021.
- Rosen, P., Hensley, S., Joughin, I., Li, F., Madsen, S., Rodriguez, E., and Goldstein, R.: Synthetic Aperture Radar Interferometry, *Proceedings of the IEEE*, 88, 333–382, <https://doi.org/10.1109/5.838084>, 2000.
- 685 Rosen, P. A., Hensley, S., and Chen, C.: Measurement and Mitigation of the Ionosphere in L-band Interferometric SAR Data, in: 2010 IEEE Radar Conference, pp. 1459–1463, ISSN 2375-5318, <https://doi.org/10.1109/RADAR.2010.5494385>, 2010.
- Rott, H., Nagler, T., and Scheiber, R.: Snow Mass Retrieval by Means of SAR Interferometry, in: *Proceedings of the FRINGE 2003 Workshop*, p. 7, Frascati, Italy, 2003.

- Ruiz, J. J., Lemmetyinen, J., Kontu, A., Tarvainen, R., Vehmas, R., Pulliainen, J., and Praks, J.: Investigation of Environmental Effects on Coherence Loss in SAR Interferometry for Snow Water Equivalent Retrieval, *IEEE Transactions on Geoscience and Remote Sensing*, 60, 1–15, <https://doi.org/10.1109/TGRS.2022.3223760>, 2022.
- Ruiz, J. J., Merkouriadi, I., Lemmetyinen, J., Cohen, J., Kontu, A., Nagler, T., Pulliainen, J., and Praks, J.: Comparing InSAR Snow Water Equivalent Retrieval Using ALOS2 With In Situ Observations and SnowModel Over the Boreal Forest Area, *IEEE Transactions on Geoscience and Remote Sensing*, 62, 1–14, <https://doi.org/10.1109/TGRS.2024.3439855>, 2024.
- Schaer, S., Gurtner, W., and Feltens, J.: IONEX: The Ionosphere Map Exchange Format Version 1, in: Proc. of the IGS AC. Workshop. Darmstadt, Germany. February 9, vol. 11, pp. 233–247, 1998.
- Schwank, M., Kontu, A., Mialon, A., Naderpour, R., Houtz, D., Lemmetyinen, J., Rautiainen, K., Li, Q., Richaume, P., Kerr, Y., and Mätzler, C.: Temperature Effects on L-band Vegetation Optical Depth of a Boreal Forest, *Remote Sensing of Environment*, 263, 112542, <https://doi.org/10.1016/j.rse.2021.112542>, 2021.
- Siirila-Woodburn, E. R., Rhoades, A. M., Hatchett, B. J., Huning, L. S., Szinai, J., Tague, C., Nico, P. S., Feldman, D. R., Jones, A. D., Collins, W. D., and Kaatz, L.: A Low-to-No Snow Future and Its Impacts on Water Resources in the Western United States, *Nature Reviews Earth & Environment*, 2, 800–819, <https://doi.org/10.1038/s43017-021-00219-y>, 2021.
- Smoot, E. E. and Gleason, K. E.: Forest Fires Reduce Snow-Water Storage and Advance the Timing of Snowmelt across the Western U.S., *Water*, 13, 3533, <https://doi.org/10.3390/w13243533>, 2021.
- Sturm, M. and Liston, G. E.: Revisiting the Global Seasonal Snow Classification: An Updated Dataset for Earth System Applications, *Journal of Hydrometeorology*, 22, 2917–2938, <https://doi.org/10.1175/JHM-D-21-0070.1>, 2021.
- Tarricone, J., Webb, R. W., Marshall, H.-P., Nolin, A. W., and Meyer, F. J.: Estimating Snow Accumulation and Ablation with L-band Interferometric Synthetic Aperture Radar (InSAR), *The Cryosphere*, 17, 1997–2019, <https://doi.org/10.5194/tc-17-1997-2023>, 2023.
- Tarricone, J., Palomaki, R., Rittger, K., Nolin, A., Marshall, H.-P., and Vuyovich, C.: Investigating the Impact of Optical Snow Cover Data on L-Band InSAR Snow Water Equivalent Retrievals, *Journal of Remote Sensing*, 5, 0682, <https://doi.org/10.34133/remotesensing.0682>, 2025.
- Trujillo, E. and Molotch, N. P.: Snowpack Regimes of the Western United States, *Water Resources Research*, 50, 5611–5623, <https://doi.org/10.1002/2013WR014753>, 2014.
- Tsang, L., Durand, M., Derksen, C., Barros, A. P., Kang, D.-H., Lievens, H., Marshall, H.-P., Zhu, J., Johnson, J., King, J., Lemmetyinen, J., Sandells, M., Rutter, N., Siqueira, P., Nolin, A., Osmanoglu, B., Vuyovich, C., Kim, E., Taylor, D., Merkouriadi, I., Brucker, L., Navari, M., Dumont, M., Kelly, R., Kim, R. S., Liao, T.-H., Borah, F., and Xu, X.: Review Article: Global Monitoring of Snow Water Equivalent Using High-Frequency Radar Remote Sensing, *The Cryosphere*, 16, 3531–3573, <https://doi.org/10.5194/tc-16-3531-2022>, 2022.
- Wegmüller, U., Werner, C., Frey, O., Magnard, C., and Strozzi, T.: Reformulating the Split-Spectrum Method to Facilitate the Estimation and Compensation of the Ionospheric Phase in SAR Interferograms, *Procedia Computer Science*, 138, 318–325, <https://doi.org/10.1016/j.procs.2018.10.045>, 2018.
- Youn, H.-s., Lee, L. Y., and Iskander, M.: In-Situ Broadband Soil Measurements: Dielectric and Magnetic Properties, in: 2010 IEEE International Geoscience and Remote Sensing Symposium, pp. 4483–4486, ISSN 2153-7003, <https://doi.org/10.1109/IGARSS.2010.5649039>, 2010.
- Zebker, H. and Villasenor, J.: Decorrelation in Interferometric Radar Echoes, *IEEE Transactions on Geoscience and Remote Sensing*, 30, 950–959, <https://doi.org/10.1109/36.175330>, 1992.