



From Worst-Case Scenarios to Extreme Value Statistics: Local Counterfactuals in Flood Frequency Analysis

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Abstract.

Many aspects of flood risk management require flood frequency analysis (FFA) which is, however, often limited by short observational records - especially for flash floods in small basins. In order to address this issue, we propose to extend the underlying data by local counterfactual scenarios. To that end, heavy precipitation events (HPEs) from nearby, hydrologically similar catchments are used to simulate flood peaks which are then included in the FFA for the catchment of interest. In order to demonstrate the added value of this approach, we used 23 years of radar-based precipitation and a hydrological model, fitted the Generalized Extreme Value (GEV) distribution to three different datasets - observed peaks, counterfactual peaks, and their combination -, and evaluated the resulting three GEV fits by means of the quantile skill score (QSS). For a sample of more than 13,000 German headwater catchments, we could show that local counterfactuals improved quantile estimation, with the level of improvement increasing with return period. The improvement declines when the radius of the transposition domain is extended beyond 30 km. Overall, our results provide a tangible perspective to enhance traditional FFA, producing narrower confidence intervals and more robust estimates for design floods and risk assessments.

1 Introduction

Flood frequency analysis (FFA) addresses the probability of floods of a given magnitude and their expected recurrence. It provides the statistical basis for defining extreme events and is, since decades, fundamental for various aspects of flood risk management (Klemes, 1993; Merz and Blöschl, 2008), such as the design of hydraulic infrastructure, landscape planning, flood insurance and many more.

Typically, extremes are extracted from observations (of, e.g., discharge or precipitation accumulated over specific durations) via the block maxima or peak-over-threshold method, and a probability distribution is fitted (Gumbel, 1958), most commonly the Generalized Extreme Value (GEV) or Generalized Pareto (GP) distribution. This allows extrapolation of the tail beyond observed records (Cooley, 2012) and an estimation of occurrence probabilities (return periods) for unobserved events.



However, extreme floods occur rarely (by definition), resulting in limited sample sizes for FFA. Short observational records can increase the sampling error and thus the uncertainty of distribution fitting. Consequently, estimates of occurrence probability are often highly uncertain, which can lead to a severe misrepresentation of risk. This problem is amplified in the case of flash floods: these floods are characterized by a rapid onset and carry high sediment and debris loads, which makes them a highly destructive natural hazard (Barredo, 2007; Llasat et al., 2010; Petrucci et al., 2019; CRED/UCLouvain, 2023). The corresponding rainfall events are typically brief and intense and occur at small spatial scales. They only trigger a flash flood in case they coincide with basins that are able to convert rainfall into runoff, and rapidly propagate that runoff towards the outlet. These processes are governed by topography, geomorphology, soils, and land use. Furthermore, flash-flood-prone basins are generally small ($<1000 \text{ km}^2$). The local scarcity of extreme floods and the limited availability of corresponding streamflow records challenge conventional FFA for flash-flood risk management.

Several approaches, such as regionalization (e.g. Gaume et al., 2010; Guse et al., 2010; Nguyen et al., 2014; Halbert et al., 2016), probable maximum precipitation (PMP, Fuller, 1914; District and Morgan, 1916; Hansen, 1987; WMO, 2009), stochastic storm transposition (SST, Wright et al., 2014, 2017) or the use of stochastic weather generators (e.g. Falter et al., 2015; Apel et al., 2016) have been proposed to address data scarcity and the limitations of FFA. Their central idea is to augment the data basis, either by incorporating information from hydrologically similar sites or by forcing hydrological models with hypothetical heavy precipitation events (HPEs), which are generated by sampling and spatially transposing HPEs within a transposition domain (TD) that is considered to be "meteorologically homogeneous", or stochastically with weather generators.

Although the transposition of storms for flood hazard assessment - also referred to as spatial counterfactuals (Merz et al., 2024; Voit and Heistermann, 2024b; Vorogushyn et al., 2024; Thompson et al., 2025) - has received growing research attention in recent years, it is still rarely applied in practice. However, SST is designated to form the core of the U.S. Federal Emergency Management Agency's "Future of Flood Risk Data" initiative, aimed at remapping the nation's floodplains (Abbasian et al., 2025).

Due to the large variability in terminology with regard to the aforementioned concepts, we now clarify and define, for the sake of consistency, the following terms and acronyms for use throughout this paper:

- **HPE**: Heavy precipitation event. While sometimes termed "storms", we adopt the more precise designation HPE.
- **TD**: Transposition domain; a region that is assumed to be meteorologically homogeneous (with respect to the features of heavy rainfall). The basic idea is, that an HPE observed within the TD, could have also happened at any other location within the TD.
- **storm transposition**: Spatial transposition (relocation) of an observed HPE within a TD.
- **CoI**: Catchment of interest, the catchment that is the subject of an FFA.
- **NC**: Neighboring catchment. A catchments in proximity to the CoI, typically within a TD.
- **counterfactual**: A hypothetical realization of an event under alternative conditions, e.g., an HPE occurring at a different location.



- **factual peak.** Flood peak observed in the CoI or modelled with observed rainfall.
- **counterfactual peak:** Flood peak simulated by a hydrological model forced with a transposed (counterfactual) HPE.

The central issue with approaches such as regionalization, PMP, or SST is the plausibility of counterfactuals. Hazard assessments based on such methods are only meaningful if the counterfactuals are considered realistic. To this end, previous studies have proposed different methods to define a TD from which HPEs are sampled. Fontaine and Potter (1989) described it as a region where “significant storms are uniformly distributed in space,” while Zhou et al. (2019) suggested using cloud-to-ground lightning analyses. However, the outcome of these methods also depends on the length of the observed data. Instead of defining a TD based on a complex analysis, Voit and Heistermann (2024a) introduced the concept of local counterfactuals, where counterfactual floods were generated by selecting HPEs that caused high runoff peaks in basins from a close neighborhood and forcing a runoff model with these transposed HPEs. Even within this very small TD and based on only 23 years of data, local counterfactuals produced flood peaks comparable to a 200-year “extreme” flood.

But how can counterfactuals be incorporated into FFA? For numerous application contexts, return periods and design levels remain essential for stakeholders. SST provides one way to statistically assess the occurrence of hypothetical flood scenarios, but it requires both the definition of the TD and the selection of the most relevant rainfall duration for sampling events. The latter is not trivial, as the duration of extreme rainfall that generates the highest flood peak may vary between catchments and is often difficult to determine in advance. For this reason Voit and Heistermann (2024a) proposed a bottom-up approach by selecting the HPEs which caused high flood peaks nearby catchments, irrespective of rainfall duration.

In this study, we propose to extend the concept of local counterfactuals in order to formally integrate counterfactual flood peaks into flood frequency analysis (FFA). This is demonstrated in a case study on the basis of 23 years of radar-based precipitation records in Germany, in combination with a Germany-wide flash flood model as introduced by Voit and Heistermann (2024b): for each of 13,452 headwater catchments ($<750 \text{ km}^2$) in Germany, we fit three GEV distributions: (i) from the 23 annual flood peak maxima modelled in the basin of interest (our reference), (ii) from 230 counterfactual peaks derived by spatially transposing HPEs which caused 23 annual maximum peak discharge values in 10 hydrologically similar neighboring basins, and (iii) from the combined dataset. The quantile score (QS) (Bentzen and Friederichs, 2014) is then used to analyze whether counterfactual information improves the representation of extremes beyond the limited observational record. The QS can evaluate improvement for each quantile of interest. We repeat this procedure for four differently sized and shaped TDs and show how the design of the TD affects the results of the FFA. Finally, we discuss the return levels derived from the different GEV distributions and examine the corresponding confidence intervals.

2 Data

2.1 RADKLIM

We used the radar climatology product RADKLIM v2017.002 (2001–2023) to compute local counterfactuals and to drive continuous runoff modeling across Germany. RADKLIM is provided by Germany’s national meteorological service (Deutscher



Wetterdienst, DWD) and represents a reprocessed version (Lengfeld et al., 2019) of DWD's operational radar-based quantitative precipitation estimation product, RADOLAN (Winterrath et al., 2012). The dataset has a spatial resolution of $1 \times 1 \text{ km}^2$, an hourly temporal resolution, and is openly available via the DWD open data server (Winterrath et al., 2018).

2.2 DEM

For catchment delineation and runoff analysis, we used the EU-DEM (European Commission, 2016), which has a 25 m resolution and combines SRTM (Shuttle Radar Topography Mission) and ASTER GDEM (Advanced Spaceborne Thermal Emission and Reflection Radiometer Global Digital Elevation Model).

2.3 Land use and soil data

Information on land cover was obtained from CORINE CLC5-2018 (BKG, 2018), which classifies high-resolution satellite imagery into 37 land cover classes for Germany following the European Environmental Agency (EEA) nomenclature. The classification considers objects with a minimum size of 5 ha and is updated every three years. Soil data were derived from the BUEK 200 national soil survey (scale 1:200,000; BGR, 2018), compiled from federal state surveys by the Federal Institute for Geosciences and Natural Resources (BGR) in cooperation with the National Geological Services (Staatliche Geologische Dienste). For each mapping unit, BUEK 200 provides areal fractions of dominant soil types along with detailed profile information, including texture, bulk density, and other key properties.

3 Methods

Much of the data and methodology for this study are detailed in Voit and Heistermann (2024b). Here, we briefly describe the hydrological model, further explain the flood frequency analysis, and the selection of local counterfactuals.

3.1 Modelling surface runoff

The hydrological model (Voit, 2024) was specifically tailored to simulate flash flood events in small- to medium-sized basins. A detailed model description is provided in Voit and Heistermann (2024b). During flash floods, surface runoff dominates (Marchi et al., 2010; Grimaldi et al., 2010), while evaporation and groundwater dynamics are negligible. Accordingly, the model comprises two modules. First, effective rainfall is estimated using the SCS-CN method (U.S. Department of Agriculture-Soil Conservation Service, 1972), which is widely applied in flash flood modeling (Gaume et al., 2004; Borga et al., 2007; Emmanuel et al., 2017). Second, the geomorphological instantaneous unit hydrograph (GIUH), derived from the DEM, represents the concentration of quick runoff from effective rainfall. The model's lightweight design allows the computation of large numbers of counterfactual scenarios. As it does not account for channel hydraulics or engineered structures, the analysis is restricted to headwater catchments smaller than 750 km^2 . In our analysis, this corresponds to 13,452 sub-catchments with an mean area of 15.7 km^2 .

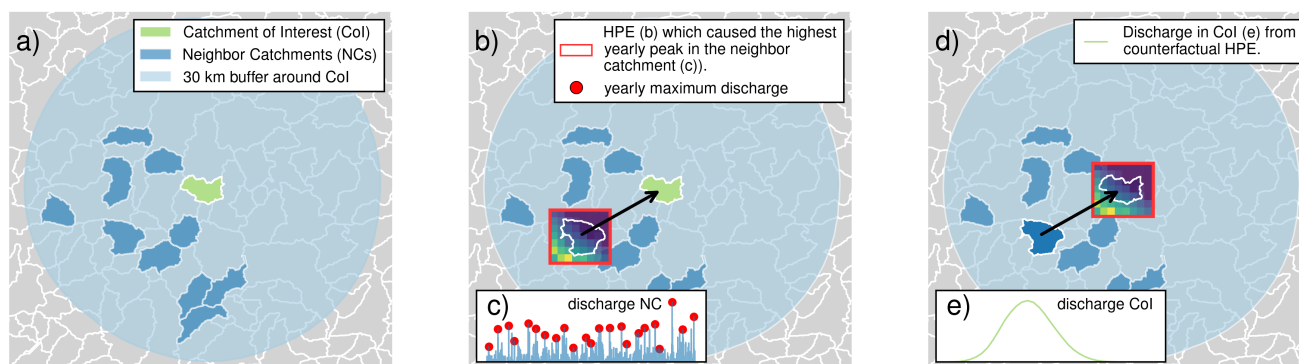


Figure 1. Development of local counterfactuals: a) Catchment of Interest (CoI, green) and its 10 neighbor catchments (NCs, dark blue) in a 30 km neighborhood (light blue). b) Selecting the HPE which caused the highest annual runoff peak (red dot, c) in the NC (red box). d) Transposing the HPE from the NC to the CoI and modelling the resulting runoff (e)). This procedure is repeated for each NC and steps c-e) are repeated for each year.

3.2 Design of local counterfactuals

Local counterfactuals are HPEs drawn from a neighborhood (TD) of a given catchment of interest (CoI) — the catchment to which the counterfactual scenarios are applied, and transposed to the CoI. In this study, all aforementioned 13,452 headwater catchments smaller than 750 km² are individually treated as a CoI, meaning that the following procedure is applied to each of these catchments (see also Fig. 1 for illustration):

1. For each CoI, we identified the ten most similar catchments located entirely within a 30 km buffer around the CoI. Similarity was quantified using a KDTree based on the following scaled catchment attributes: GIUH time to peak, GIUH standard deviation, GIUH unit peak discharge, mean slope, mean elevation, elevation standard deviation, area, and mean curve number (see section 3.1). We refer to these as *neighbor catchments* (NCs; see Fig. 1a).
2. For each of these NCs, we model the quick runoff from 2001 until 2023 (Fig. 1b). We then identify the annual maximum peak discharge for each of the 23 years (Fig. 1c).
3. From RADKLIM, we extract the data for the 23 HPEs which caused the annual maximum peaks in the NC (Fig. 1b) and transpose them from their original spatial position from the centroid of the NC to the centroid of the CoI, thereby creating spatial counterfactuals (Fig. 1d). We ensure that the CoI and all its upstream catchments will be completely covered by the HPE, by adding a 70 km buffer on each side of the RADKLIM subset (for better visualization we do not show the buffer in Fig. 1). To ensure a consistent soil moisture state we add a 14-day temporal buffer before the actual event. If the CoI has upstream basins, we additionally transpose the HPEs to the centroid of every upstream basin.
4. We model the surface runoff that these counterfactual HPEs would have caused in the CoI (Fig. 1e) and record the maximum counterfactual peak discharge values for each year. We repeat steps 3 and 4 for all NCs.



We hypothesize that the representativeness of counterfactuals for the meteorological processes governing the CoI generally decreases with the distance between the corresponding NC and the CoI. To test hypothesis, we compared four transposition domains (TDs): a 10 km buffer, a 30 km buffer, and two ring-shaped TDs with inner–outer radii of 30–60 km and 60–90 km around the CoI, respectively.

140 3.3 GEV distribution

Under certain conditions, block maxima are GEV-distributed (Fisher and Tippett, 1928; Gnedenko, 1943). These conditions are met for precipitation (Coles, 2001) and discharge. The cumulative distribution function (CDF) of the GEV is defined

$$G(x) = \begin{cases} \exp \left\{ - \left[1 + \xi \left(\frac{x-\mu}{\sigma} \right) \right]^{-1/\xi} \right\} & , \xi \neq 0 \\ \exp \left\{ - (\exp^{(x-\mu)/\sigma}) \right\} & , \xi = 0, \end{cases} \quad (1)$$

with location μ , scale σ and shape ξ .

145 From the GEV distribution, return levels can be obtained for return periods that are even longer than the length of record. However, this extrapolation is uncertain with limited sample size (Coles, 2001). Our suggestion is, hence, to increase the sample size with local counterfactuals. To fulfill the requirements of the Fisher-Tippet-Theorem, all block maxima have to be drawn from the same statistical distribution. We choose a very small area as TD and then select HPEs within this TD based on the streamflow response of neighboring catchments that are very similar regarding slope, elevation, land use and the unit
 150 hydrograph (see section 3.2). Based on this similarity of catchments and the small TD, we regard this first requirement as fulfilled. To fulfill the requirements of the Fisher-Tippet-Theorem, it is also paramount not to arbitrarily discard subsets of the data. More specifically, this mandates to include **all** annual maximum peak discharge values from an NC (instead of, e.g., just the highest one) to keep a consistent block size.

In FFA, special attention is given to the shape parameter ξ : a large shape parameter indicates a heavy tailed distribution
 155 where extreme events with high magnitude can occur. Especially when fitted to limited data points, the GEV distribution can produce implausible parameter estimates or "poor fits". For this reason we disregard catchments where one of the previous GEV distributions has a shape $0 \geq \xi < 0.5$. These thresholds are a compromise of values for ξ that are considered to be hydrologically plausible (Morrison and Smith, 2002; Merz et al., 2022). We used the Python package "scipy" (Virtanen et al., 2020) with a maximum likelihood estimator to fit the GEV distribution.

160 3.4 Quantile skill score

We utilize the quantile score (QS) (Bentzien and Friederichs, 2014) to quantify how well a GEV distribution represents the quantiles of the series of annual block maxima from the CoI. First, the tilted check-function $\rho_p(\cdot)$ is used to compute a penalty for estimated quantiles in comparison to the data points z_n .



$$\rho_p(u) = \begin{cases} pu & , u > 0 \\ (p-1)u & , u \leq 0 \end{cases} \quad (2)$$

$$165 \quad (3)$$

With $u = z_n - q$. For high non-exceedance probabilities p (which corresponds to a return period $T = \frac{1}{1-p}$), it leads to a strong penalty for data points that are still higher than the modeled quantile ($z_n > q$).

The quantile score is then computed for each non-exceedance probability p :

$$QS(y, q; p) = \sum_i^n \rho_p(y_i - q) \quad (4)$$

170 with p -quantile q (a return level corresponding to T), tilted check-function $\rho_p(\cdot)$ and block maximum y_i obtained from the n factual peaks in the CoI.

We estimate the parameters of three GEV distributions that are fitted on different subsets of data and refer to them as follows:

- **GEV_{CoI}**: fitted only to the factual peaks from the CoI.
- **GEV_{NCs}**: fitted only to the counterfactual peaks from the NCs.
- 175 – **GEV_{all}**: fitted to both factual peaks from the CoI and the counterfactual peaks from the NCs.

Essentially, **GEV_{NCs}** and **GEV_{all}** are the GEV variants that we introduce as competitors against the conventional **GEV_{CoI}** which is exclusively based on information obtained in the CoI. In order to verify the added value of the new GEV variants, **GEV_{CoI}** serves as a reference. For this purpose, we use the quantile skill score (QSS) which compares the QS of **GEV_{NCs}** and **GEV_{all}** (denoted **QS_{NCs}** and **QS_{all}**, respectively) to the QS of our reference **GEV_{CoI}** (**QS_{CoI}**) as follows:

$$180 \quad QSS_i = 1 - \frac{QS_i}{QS_{CoI}} \text{ with } i \in \{NCs, all\} \quad (5)$$

The QSS can take values between minus infinity and 1. Positive values indicate that the competing GEV (**GEV_{NCs}** or **GEV_{all}**) is superior to the reference.

As the quantile score (Eq. 4) is always computed for a specific return period T (or non-exceedance probability p), the QSS itself is obtained for specific values of T , too (20, 50, 100 and 200 years in this study), similar to Fauer and Rust (2023, Fig. 4).

185 The reference **QS_{CoI}** itself is obtained by means of a leave-one-out cross-validation: to that end, one year i is excluded from the CoI's series of factual annual maxima and the **GEV_{CoI}** is estimated from the remaining training years. From the fitted **GEV_{CoI,i}**, a return level (p -quantile) is calculated and a quantile score **QS_{CoI,i}** is determined from this return level and the annual maximum value for year i . This is repeated for all years in the CoI series. **QS_{CoI}** is then obtained as the average of all **QS_{CoI,i}**.

4 Results and Discussion

190 4.1 Verifying the added value of counterfactual peaks on GEV estimation

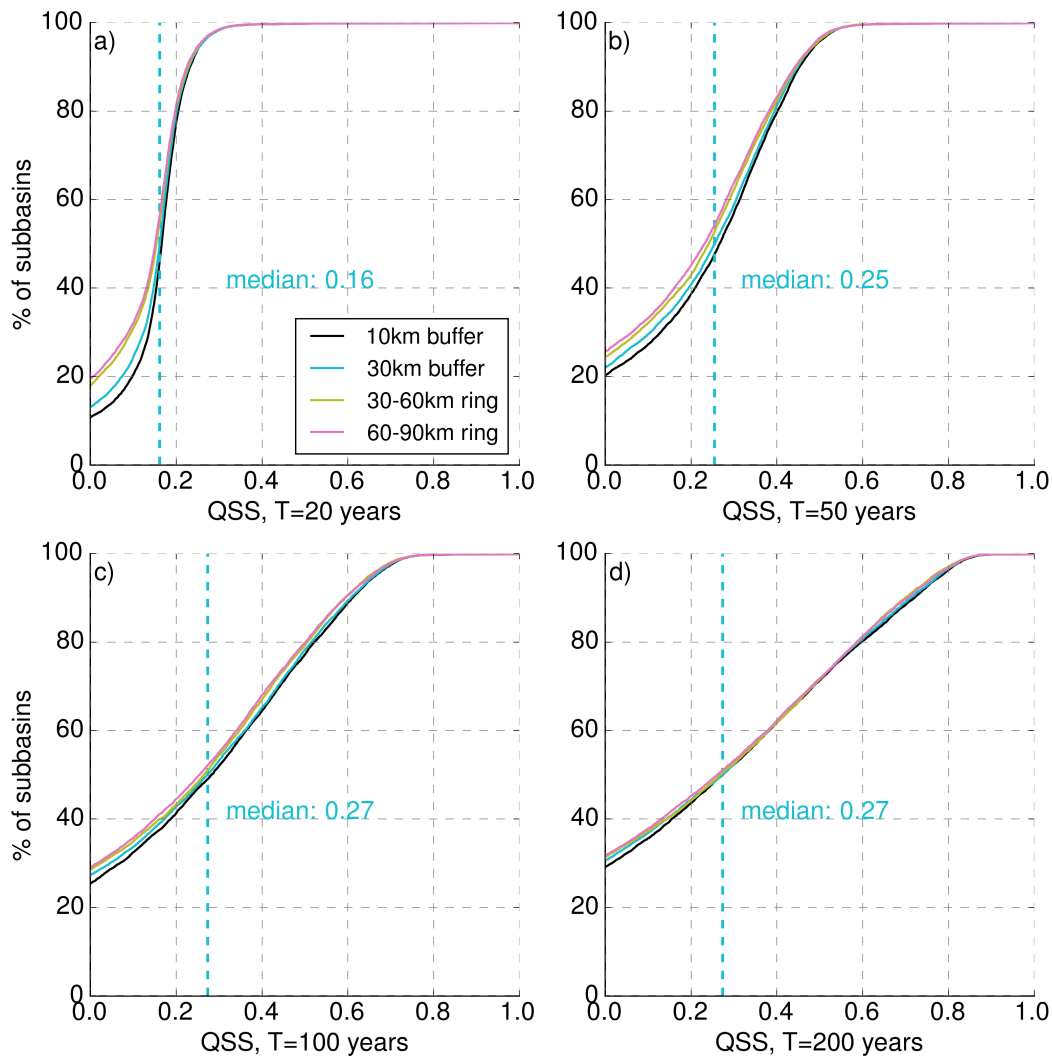


Figure 2. Cumulative distributions showing the quantile skill scores for GEV_{NCs} in reference to GEV_{CoI}, for all subbasins and for four different transposition domains (10-km buffer: yellow, 30-km buffer: blue, 30-60-km ring: green, 60-90-km ring: orange). Subplots a)-d) show different quantiles that relate to the a) 20-year, b) 50-year, c) 100-year and d) 200-year flood. A quantile score > 0 indicates the superiority of the GEV_{NCs}. The median QSS of the 30-km buffer is indicated with the vertical blue dashed line



For each small-scale basin in Germany, we created local counterfactuals (section 3.2) and used these counterfactual flood peaks to fit a GEV distribution for the CoI. To validate how well local counterfactuals are able to represent the quantiles in the data (the factual flood peaks in the CoI), we performed an out-of-sample-test by comparing the GEV_{NCs} with the GEV_{CoI} .

The inspection of the GEV parameters for each catchment reveals a large number of implausible shape parameters, especially for GEV_{CoI} , which is fitted to only 23 year-maxima. Because the number of data points increases by adding counterfactual peaks, the fits for GEV_{NCs} improve: about 29 % of the basins cannot be included in the analysis because the implausible fit of GEV_{CoI} whereas 5 % of the catchments have to be excluded because of an implausible fit of GEV_{NCs} (see section 3.3). In total this leads to an exclusion of ≈ 33 % of the basins.

Figure 2 shows the results for all TDs and for four different return periods (20, 50, 100 and 200 years). Since negative values of the QSS are harder to interpret, we show only $QSS \geq 0$. We will discuss the differences between the different TDs in the following section. For now, we focus on the TD with a radius of 30 km. The main result is that the GEV_{NCs} - which has never seen any information from the CoI - clearly outperforms the GEV_{CoI} : across all return periods and transposition domains, the majority of catchments have positive QSS values. E.g., for the TD with a 30 km buffer, the percentage of catchments with positive QSS_{NCs} values (see intercept on the y-axis) is 87% for $T=20$ a, 78% for $T=50$ a, 73% for $T=100$ a, and 69% for $T=200$ a. Evidently, GEV_{NCs} performs worse for the corresponding remainder to 100%.

We would like to take a closer look at the differences between the return periods. Increasing return periods lead to a decreasing fraction of catchments with positive QSS_{NCs} values - obviously not desirable -, but also to a desirable increase of catchments with very high QSS values (for $T=20$ a, 0.2% of the catchments have a $QSS > 0.5$, while this fraction grows to 28% for $T=200$ a). Altogether, the median QSS continuously grows from a value of 0.16 for $T=20$ a to a value of 0.27 for $T=200$ a, suggesting that the value added by using GEV_{NCs} increases with the return period. This is plausible, since return levels for low return periods can be estimated more robustly from short time series (for $T=20$ a, the estimation of a return level from an annual series of 23 years does not even imply extrapolation).

These results serve as a proof of concept: for the majority of cases, we are able to better represent the quantiles in the data of the CoI by using a GEV distribution fitted exclusively to the counterfactual peaks (GEV_{NCs}). The improvement is more pronounced for higher quantiles (or return periods). In practice the GEV would be fitted to both factual *and* counterfactual peaks together (GEV_{all}), which only marginally increases the robustness of the return level estimates. The QSS for GEV_{all} is shown in Figure S1 in the supplement.

4.2 Effect of different transposition domains

We calculated the QSS_{NCs} for four different TDs. This way, we want to investigate whether HPEs transposed from larger distances are less "typical" for the CoI and will therefore result in less representative GEV fits with lower values of QSS_{NCs} . This effect can be observed in Figure 2. For each return period, the intercepts of the QSS distributions on the y-axis are higher for the ring-shaped TDs (30–60 and 60–90 km) than the intercepts of the TDs with a 10- or 30 km buffer. This effect is less pronounced with increasing quantiles. The differences between the 10- and 30 km-buffers are very small. These results support the hypothesis that HPEs transposed over short distances are more representative for the HPEs occurring directly over the



225 CoI. Nevertheless, the sampling process of the NCs can also have an impact on the results. Within the TD we sample ten
 catchments which are most similar to the CoI (section 3.2). If the TD is very small, there are less basins to sample from so
 that the representativeness of the sampled HPEs for the CoI might suffer. Likewise it could also be possible that basins are less
 similar to each other with increasing distance. Due to the complex topography around every catchment, we think that there
 can be hardly a generalized solution for the "perfect" transposition domain. However, our results show, that there is, for most
 230 small-scale basins in Germany, no large difference whether the TD is a 10-, or 30 km buffer. Providing large computational
 resources this could be systematically investigated further by increasing the size of the TD step by step and evaluating the QSS.

4.3 Return levels

We would now like to demonstrate how the use of local counterfactuals affects return levels, in comparison to the conventional
 use of factual discharge peaks in the CoI. While GEV_{NCs} was used for verification in section 4.1, we will now use GEV_{all} there
 235 is not reason to entirely discard the data from the CoI data for GEV fitting. For the 200-year return period, Figure 3 shows the
 ratio between the return level obtained from GEV_{all} and from GEV_{CoI} (as a histogram over all analysed catchments). For all
 TDs, the median ratio is very close to one, so using local counterfactuals results in lower return levels for half of the basins
 and to higher return level for the other half. In our view, this is an important insight: in contrast to our intuitive expectation,
 the use of local counterfactuals for GEV fitting does not systematically increase the resulting return levels, but simply reduces
 240 the estimation error over all CoIs (based on the higher QSS and the narrower confidence intervals, see below). However, this
 improvement of the GEV estimation is still based on the inclusion of higher discharge maxima via counterfactuals. This is
 illustrated by the gray histograms in Fig. 3 which show, for each catchment, the ratio between the highest value in the annual
 maximum series of counterfactual *and* factual peaks and the highest value in the annual maximum series of just the factual
 peaks. The gray histograms clearly show that counterfactuals increase the maximum of the complete series of annual maxima,
 245 leading to more robust GEV fits. The medians for all TDs are between 1.43 and 1.6. It is important to note that the four
 TDs cover very different spatial extents: the 30-60-km-ring has an area of 14,137 km², while the 10 km buffer has a size of
 ~466 km² (for a circular basin with an area of 15 km²). The larger the TD we sample HPEs from, the more options we have to
 find catchments which are very similar to the CoI. Thus, it is also more likely that we are sampling HPEs that matter regarding
 the formation of an extreme flood peak in the CoI. This absolute maximum peak could serve as reference for the probable
 250 maximum flood (PMF) and is automatically included in the results of the analysis. Yet, remember that sampling from such
 more distant and larger neighborhoods does not improve the GEV estimation, as was shown in section 4.2.

The difference between the two medians shown in Figure 3 may appear counterintuitive. However, two factors account for
 this observation. First, although the counterfactual dataset exhibits some higher peaks, these peaks occur jointly with the entire
 set of annual maxima from this NC (23 values). In many cases these high peaks have little impact on the GEV fit due to the
 255 amount of data points that are just "average" peaks. Figure 4 shows an example of this case. The sampling error with small
 sample sizes as the 23 annual maxima for the GEV_{CoI} can lead to very heavy tailed GEV fits, high return level estimates and
 very wide confidence intervals. Even though the data pool for GEV_{all} (253 values) contains more extreme peaks (max. CoI:

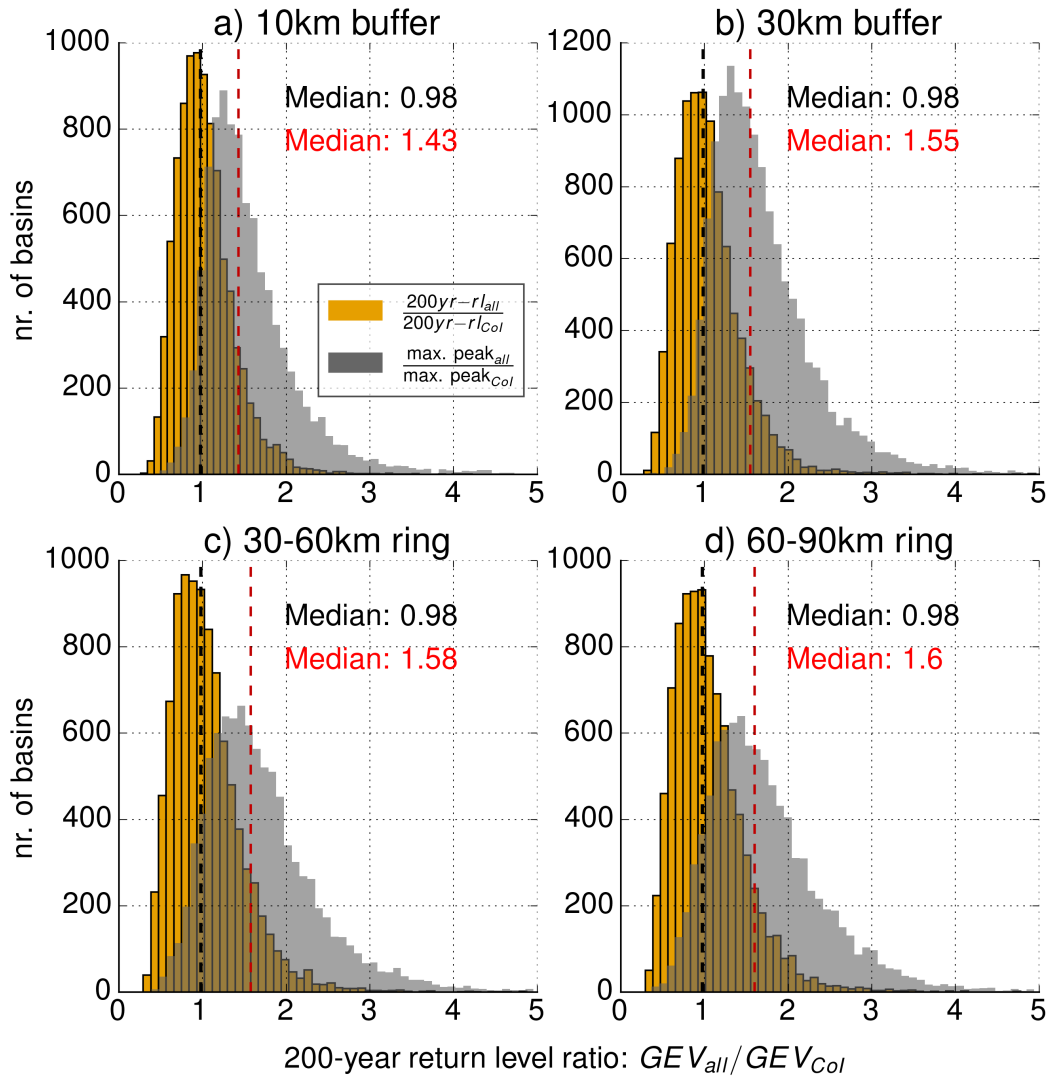


Figure 3. Histogram of the ratio between the 200-year return level from GEV_{all} and from GEV_{CoI} for four TDs. Gray histograms indicate the ratio of the highest peaks in the respective datasets used for fitting (see main text for further explanation). The median ratio of the return levels ratio is marked in black, and the median ratio of maximum peak discharge values in red.

43.2 $m^3 s^{-1}$, max. all: 87.3 $m^3 s^{-1}$), the fit is still mainly influenced by the larger amount of moderate peaks and results in lower return level estimates.

260 Secondly, local counterfactuals also induce spatial smoothing (which is desired): each catchment is a CoI once, but serves as neighbor for many other CoIs. As a result, nearby and hydrologically similar catchments often share almost identical sets of peaks. When a counterfactual peak increases the return level estimate for one CoI, the peaks from that CoI will also enter the

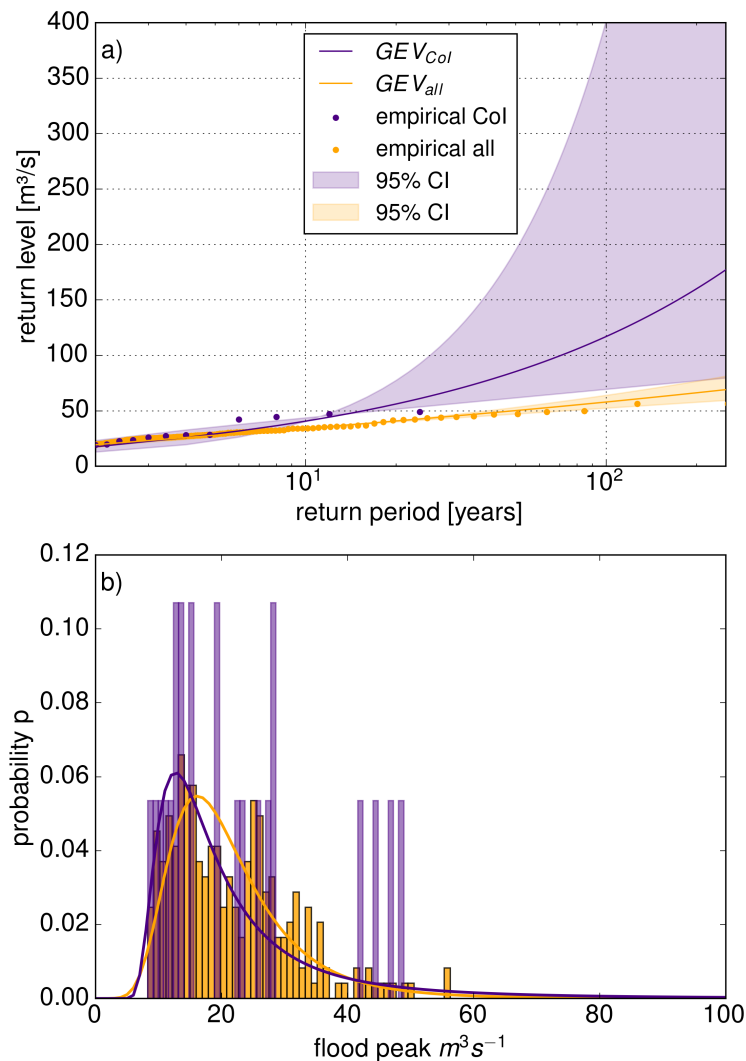


Figure 4. Comparison of two GEV_{Col} and GEV_{all} for one exemplary basin. a) Return levels estimated by GEV_{all} (orange) are lower than by GEV_{Col} (purple). The shaded areas mark the 95 % confidence interval estimated with boot strapping ($n=500$). The empirical return periods were estimated with the Weibull plotting position and are indicated with the semi-transparent dots. b) Density histogram of the annual maxima and fitted GEV distribution.

NC data pool once their roles are reversed. In this case, the inclusion of the peak can reduce the return level estimate for the neighboring catchment.

265 The estimation of return levels beyond the observational period comes with large uncertainties in the case of GEV_{Col} in the example in Fig. 4: the 200-year return level is between 34 and $325 \text{ m}^3\text{s}^{-1}$ (95 % confidence interval). This range is much smaller for GEV_{all} , where the 200-year return level is between 87 and $130 \text{ m}^3\text{s}^{-1}$. Across all catchments, the 95 % confidence



intervals shrink substantially. Within the 30 km buffer, the median reduction in interval span is 78.75 % for the 20-year return level, 86.25 % for the 50-year level, 89.75 % for the 100-year level, and 92.25 % for the 200-year level.

270 5 Limitations

The main limitation in this study is the short observational period. The radar-based precipitation dataset RADKLIM covers 23 years. For the computation of the QSS, the 23 annual maximum flood peaks, which were modelled, using RADKLIM as forcing, served as the verification for GEV_{CoI} and GEV_{NCs} . Even though it would be desirable to have more data for this comparison, there is simply no stream or rain gauge data available for the majority of small-scale basins in Germany. Stream
 275 gauge observations are rarely longer than 30 years, so our experiments were designed upon the practical availability of data. Our results underline that using the GEV based on little observations has to be done with great care. We had to dispose 31 % of GEV fits, mainly because of the small sample size for the GEV_{CoI} .

The HPEs transposed to create local counterfactuals are selected based on the discharge peaks they generate in the NC. This approach avoids the need to predefine the characteristics of a relevant HPE prior to selection. However, discharge-relevant
 280 HPEs may be overlooked—for instance, in cases where an extreme HPE precipitates across a watershed. To at least partially address this limitation, we additionally transposed HPEs to every subbasin within larger CoIs, thereby capturing a greater degree of spatial variability.

Finally, our hydrological model surely introduces uncertainty. We assume that catchment-specific biases of the simulated flood peaks to a certain degree cancel out when comparing return periods and return levels. More importantly, our hydrological
 285 model was chosen to systematically conduct our study for all of Germany and for a large amount of catchments. The presented *concept* of using local counterfactuals for GEV estimation is independent of the hydrological model. For practical applications, e.g. in agencies in charge of risk management or design of hydraulic infrastructure, we would recommend to repeat the analysis with a hydrological model that is calibrated and validated to the local conditions.

6 Conclusions

290 In this study, we introduced a framework to increase the robustness of the GEV fits for flood frequency analysis by utilizing local counterfactuals. While being inspired by the concept of stochastic storm transposition, we follow a different approach in selecting candidate HPEs (based on the discharge response they caused in hydrologically similar neighbor catchments within a specific search radius around the the CoI), and in transposing these candidate events within the transposition domain (not stochastically, but systematically right over the CoI).

295 In a case study for Germany, we provided a proof-of-concept by applying this framework to a set of $\approx 13,452$ catchments smaller than 750 km^2 . For that purpose, we combined 23 years of radar-based precipitation records with a Germany-wide flash flood model. By using the quantile skill score, we verified that the use of local counterfactuals improves the fit of GEV



parameters for the vast majority of catchments. As expected, the value added by this approach increases with the return period of interest.

300 The main advantage of this approach the increased precision of the GEV return level estimates with much narrower confidence intervals. This is especially relevant for floods with return periods beyond the observational period. According to the Floods Directive of the European Union (2007/60/EC, (European Commission, Directorate-General for Environment, 2013)), this is particularly relevant for floods of "medium probability" ($T=100$ a) and floods of low probability (which in Germany is defined as a flood with $T=200$ a). We could show that, across return periods, the use of local counterfactuals improves GEV
305 fitting, but does not lead to a systematic change of return levels across the entirety of investigated catchments. Furthermore, our approach also automatically yields the worst-case flood.

The selection of the TD affects the quality GEV estimation when local counterfactuals are employed. We showed that the QSS decreased when HPEs were sampled from a distance of more than 30 km away from the CoI. Still, the optimal definition of the TD will remain arbitrary and represents a subject for further research, as it represents an inherent trade-
310 off: while an increasing distance allows us to sample from a larger variety of events and particularly from a larger choice of hydrologically similar catchments, an increasing distance will typically sample HPEs that are less representative for the meteorological processes that govern the CoI. At of now, the 30 km radius remains a rather pragmatic choice and a compromise between these two requirements.

The practical application of our framework appears suitable for all contexts in which observational records are short in
315 comparison to the return period required for a specific purpose, such as land use planning, design, or insurance. For such applications, we strongly recommend to use a hydrological model that is calibrated and validated for the local or regional conditions.

Code and data availability.

We published notebooks and code which demonstrate our hydrological model for a small, exemplary region (Altenahr
320 basin): the derivation of GIUHs from a digital elevation model, the extraction of rainfall data from and effective rainfall for the subbasins from RADKLIM data and the modelling of quick runoff. The code is published at: <https://doi.org/10.5281/zenodo.10473424>.

All data used in this study is accessible at the open data repository of the DWD: the RADKLIM_RW_2017.002 dataset is available at https://opendata.dwd.de/climate_environment/CDC/grids_germany/hourly/radolan/reproc/2017_002, (Winterrath
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330 *Author contributions.* PV, FF, and MH conceptualized this study. PV carried out the analysis, produced the figures and wrote the manuscript,
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