

1 Streamflow elasticity as a function of aridity

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9 Abstract

10 Relating variations in annual streamflow to a climate anomaly, commonly referred to
11 as *streamflow elasticity to climate*, is central for a rapid assessment of the impact of
12 climate change on water resources. This elasticity is classically estimated via a multiple
13 linear regression between anomalies in streamflow and climate variables. However,
14 this approach does not explicitly account for the fact that elasticity depends on aridity
15 as suggested by “Budyko-type” water balance formulas. Using a large dataset of 4,122
16 catchments from four continents, we first verify empirically the link between elasticity
17 and aridity. Then, we propose a method to constrain elasticity coefficients with
18 derivatives from a “Budyko-type” water balance formula, that allows introducing an
19 explicit dependency between elasticity and aridity. We show that adding this
20 dependency produces a regionalized elasticity formula with physically-realistic
21 elasticity coefficients.

22
23 **Keywords:** elasticity, sensitivity, aridity index, humidity index, Schreiber formula,
24 Oldekop formula, Turc-Mezentsev formula, Bagrov formula, Tixeront-Fu formula,
25 Budyko hypothesis, hierarchical linear model

26 Notations

27 This study uses three hydrological fluxes: precipitation (P_n), streamflow (Q_n), and
28 potential evaporation (E_{0n}). All fluxes are computed at the catchment scale as annual
29 sums, expressed in millimeters per year. The subscript n refers to a specific
30 hydrological year. For the Northern Hemisphere, the hydrological year spans from 1st

31 October of year $n - 1$ to 30th September of year n . For the Southern Hemisphere, it
32 spans from 1st April of year n to 31st March of year $n + 1$. Thus, Q_n , represents the
33 streamflow for the hydrological year n . Long-term mean values are denoted by an
34 overbar (e.g., \bar{Q}). Annual anomalies, denoted by Δ , are computed as the difference
35 between the annual value and the long-term mean. For example, the streamflow
36 anomaly is calculated as $\Delta Q_n = Q_n - \bar{Q}$. This is also applied to precipitation ($\Delta P_n = P_n -$
37 \bar{P}) and potential evaporation ($\Delta E_{0n} = E_{0n} - \bar{E}_0$).

38 Additionally, we also define a combined flux, Λ_n (see [Eq. 2Eq-2](#)), which reflects the
39 synchronicity of precipitation and potential evaporation. This is also expressed in
40 millimeters per year, and its anomalies are computed as $\Delta \Lambda_n = \Lambda_n - \bar{\Lambda}$.

41 The *aridity index*, φ , corresponds to the ratio \bar{E}_0/\bar{P} , while the inverse ratio \bar{P}/\bar{E}_0
42 corresponds to the *humidity index*.

43 1 Introduction

44 1.1 About streamflow elasticity

45 The climate elasticity of streamflow (Schaake and Liu, 1989; Dooge et al., 1999;
46 Sankarasubramanian et al., 2001) describes the sensitivity of streamflow to changes
47 in a climate variable. Elasticity is classically derived from the following regression:

$$\Delta Q_n = e_{Q/P} \Delta P_n + e_{Q/E_0} \Delta E_{0n} \quad \text{Eq. 1}$$

48 where: $e_{Q/P}$ denotes the precipitation elasticity of streamflow, e_{Q/E_0} denotes the
49 potential evaporation elasticity of streamflow; both coefficients are dimensionless. Note
50 that elasticity is defined here in absolute terms, i.e. as the sensitivity between quantities
51 of the same dimension (ΔQ , ΔP and ΔE_0 are all in mm/y) following Andréassian et al.
52 (2016).

53 Andréassian et al. (2025) recently proposed to enrich the traditional computation given
54 in [Eq. 1Eq-1](#), to account for the seasonal time shift between precipitation and potential
55 evaporation, because of its decisive impact on catchment water yield (see e.g. Pardé,
56 1933; Coutagne and de Martonne, 1934; Thornthwaite, 1948; Milly, 1994; Yokoo et al.,
57 2008; Roderick and Farquhar, 2011; de Lavenne & Andréassian, 2018; Feng et al.,
58 2019). We compute the synchronous amount of precipitation and potential evaporation
59 Λ , using monthly data as in [Eq. 2Eq-2](#):

$$\Lambda_n = \frac{\sum_{m=1}^{12} \min(P_{m,n}, E_{0,m,n})}{\sqrt{P_n * E_{0n}}} * \bar{P} \quad \text{Eq. 2}$$

60 Where index m stands for the month. The dimension of Λ_n is mm/y and it represents
 61 the annual precipitation volume most easily accessible to evaporation. For two years
 62 with the same annual amounts of precipitation and potential evaporation, Λ will be
 63 higher when they are synchronous, and lower when they are out of phase (for more
 64 details, please refer to Andréassian et al., 2025). With this new term, the regression in
 65 [Eq. 1](#) becomes:

$$\Delta Q_n = e_{Q/P} \Delta P_n + e_{Q/E_0} \Delta E_{0n} + e_{Q/\Lambda} \Delta \Lambda_n \quad \text{Eq. 3}$$

66 1.2 Using aridity to estimate streamflow elasticity

67 The link between streamflow elasticity and catchment aridity is a well-established
 68 concept in hydrology, an idea that can be traced back to Oldekop (1911) and his
 69 followers, including Budyko (1948), Bagrov (1953) and Mezentsev (1955). Many
 70 'modern' hydrologists such as Dooge (1992) and Dooge et al. (1999) discussed the
 71 form that aridity-dependent streamflow formulas could take. This dependency was
 72 emphasized by Koster and Suarez (1999), who write that "*the partitioning of a
 73 precipitation anomaly into evaporation and runoff anomalies is a simple function of the
 74 dryness index*", as well as by Sankarasubramanian et al. (2001) who argue that
 75 empirical elasticity estimates would only follow the direction shown by the Budyko-type
 76 formulas for the very humid regions of the US, while Arora (2002) concludes that "*the
 77 use of aridity index provides a straight-forward method to obtain a first order estimate
 78 of the effect of climate change on annual runoff*". Chiew (2006) shows the dependency
 79 of streamflow elasticity on aridity, Renner et al. (2012) stress that the elasticity of
 80 streamflow "*is largely dependent on [...] the aridity of the climate*" and Roderick and
 81 Farquhar (2011) underline that "*the response of runoff to changes in the main driving
 82 variables is not constant but depends on the overall climatic dryness*".

83 More recently, the concept has been applied at a global scale, with Berghuijs et al.
 84 (2017) who use the elasticity pattern provided by the Tixeront-Fu formula to propose a
 85 world map of aridity-dependent streamflow elasticities, Zhang et al. (2022) discuss the
 86 impact of aridity on the sensitivity of the elasticity coefficient to the aggregation time
 87 step, and Anderson et al. (2024) extends the computation of elasticity to different flow

88 quantiles, and show that aridity impacts the shape of the curve relating the different
89 elasticity quantiles.

90 However, Addor et al. (2018), using random forests to explain (among others) the
91 precipitation elasticity of streamflow, concluded that signatures of “hydrological
92 dynamics are poorly predicted by aridity alone, or even by a combination of several
93 climatic indices”.

94 **1.3 Local vs class estimation of elasticity**

95 To estimate the climate elasticity of streamflow at regional or national scales, making
96 the dependency of streamflow elasticity on aridity explicit can constrain the estimation
97 of elasticity coefficients and increase their physical realism.

98 For a given catchment with a sufficiently long series of annual observations, streamflow
99 elasticity can be computed *locally* by linear regression (Andréassian et al., 2016).
100 However, for ungauged catchments, local estimation of elasticity coefficients is no
101 longer possible. Instead, a *class*-elasticity can be estimated by combining all available
102 records in a region. The estimation by class has both advantages and drawbacks.
103 While this approach improves the statistical significance of elasticity coefficients, which
104 can have high uncertainty when estimated locally (especially for potential evaporation),
105 it also requires combining data from catchments with different aridity indices. This
106 presents a challenge, precisely because we know that aridity and elasticity are linked.
107 Methods to estimate local- and class-elasticity are detailed in section 2.

108 **1.4 Formulas relating streamflow elasticity to aridity**

109 We mentioned above the seminal work of the hydrologists who, following Oldekop
110 (1911), developed various mathematical formulas to represent catchment water
111 balance. These studies established simple water balance formulas from which a
112 “theoretical” elasticity of streamflow can be derived as their partial derivatives. In [Table](#)
113 [1Table-4](#), we present four long-term water balance formulas that can be used to
114 provide these theoretical elasticity estimates. The Schreiber and Oldekop formulas are
115 parameter-free, while the Turc-Mezentsev and Tixeront-Fu formulas each have one
116 parameter (ω^1 and m , respectively). These last two formulas are equivalent when

¹ We use ω instead of the more commonly used “ n ” on purpose, to avoid confusion with the subscript n used for years.

117 setting $m = \omega + 0.72$ (Yang et al., 2008; Andréassian and Sari, 2018), which explains
118 why their curves overlap in some of the later figures.
119 ~~Table 1~~ [Table 4](#) also presents the partial derivatives for each formula, allowing to
120 compute the precipitation and the potential evaporation elasticities of streamflow.
121 Unsurprisingly, these formulas are all functions of the aridity index.
122

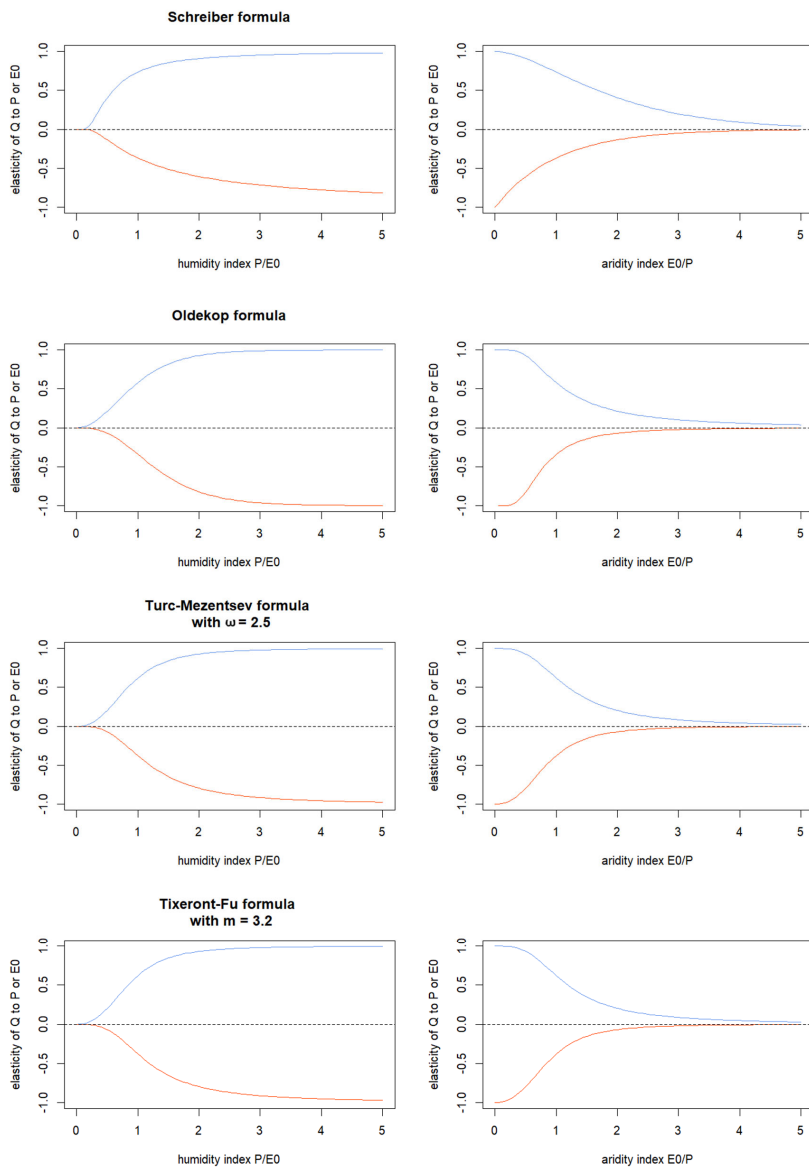
123 Table 1. Common long-term water balance formulas and the associated
 124 elasticities (\bar{Q} – long-term average streamflow [mm/y], \bar{P} – long-term average
 125 precipitation [mm/y], \bar{E}_0 – long-term average reference evaporation [mm/y], $\varphi =$
 126 $\frac{\bar{E}_0}{\bar{P}}$ is the aridity index)

Name	Formula	Precipitation elasticity $\frac{\partial \bar{Q}}{\partial \bar{P}}$	Potential evaporation elasticity $\frac{\partial \bar{Q}}{\partial \bar{E}_0}$
Schreiber (Oldekop, 1911)	$\bar{Q} = \bar{P} \cdot \exp\left(-\frac{\bar{E}_0}{\bar{P}}\right)$ Eq. 4	$e_{Q/P} = (1 + \varphi)e^{-\varphi}$ Eq. 5	$e_{Q/E_0} = -e^{-\varphi}$ Eq. 6
Oldekop (Oldekop, 1911)	$\bar{Q} = \bar{P} - \bar{E}_0 \cdot \tanh\left(\frac{\bar{P}}{\bar{E}_0}\right)$ Eq. 7	$e_{Q/P} = \tanh^2\left(\frac{1}{\varphi}\right)$ Eq. 8	$e_{Q/E_0} = -\tanh\left(\frac{1}{\varphi}\right) + \frac{1}{\varphi} \left[1 - \tanh^2\left(\frac{1}{\varphi}\right)\right]$ Eq. 9
Turc-Mezenisev (Turc, 1954; Mezenisev, 1955)	$\bar{Q} = \bar{P} - [\bar{P}^{-\omega} + \bar{E}_0^{-\omega}]^{\frac{1}{\omega}}$ with $\omega > 0$ Eq. 10	$e_{Q/P} = 1 - (\varphi^{-\omega})^{-\frac{1}{\omega}-1}$ Eq. 11	$e_{Q/E_0} = -(\varphi^{\omega})^{-\frac{1}{\omega}-1}$ Eq. 12
Tixeront-Fu (Tixeront, 1964; Fu, 1981)	$\bar{Q} = [\bar{P}^m + \bar{E}_0^{-m}]^{\frac{1}{m}} - \bar{E}_0$ with $m > 1$ Eq. 13	$e_{Q/P} = (1 + \varphi^m)^{\frac{1}{m}-1}$ Eq. 14	$e_{Q/E_0} = -1 + (\varphi^{-m})^{\frac{1}{m}-1}$ Eq. 15

127

128 [Figure 1](#) illustrates the similarities and differences among the formulas by
129 showing their respective elasticity-aridity relationships. The embedded dependency on
130 aridity is clearly visible, and we notice that the four formulas have distinct but similar
131 shapes (with the difference between the Turc-Mezentsev and the Tixeront-Fu being
132 negligible). Furthermore, the precipitation elasticity is bounded between 0 and 1, which
133 means that one millimeter of additional precipitation will always result in less than one
134 millimeter of additional streamflow. Similarly, the potential evaporation elasticity is
135 bounded between 0 and -1, which means that one millimeter of additional potential
136 evaporation will always result in a decrease of streamflow of less than one millimeter.
137 These bounds represent a *physically-realistic* catchment response, in the sense that
138 the yield (of the additional mm of precipitation or the additional mm of potential
139 evaporation) must be comprised (in absolute value) between 0 and 100%.

140



141
 142 **Figure 1: Theoretical relationships between streamflow elasticities and the humidity index (left**
 143 **panel) and the aridity index (right panel). Blue lines represent the precipitation elasticity of**
 144 **streamflow, and orange lines represent the potential evaporation elasticity of streamflow.**

145 1.5 Purpose of this paper

146 This paper aims to verify empirically the fact that streamflow elasticity depends on
147 aridity, and to show how the theoretical pattern provided by the “Budyko-type” water
148 balance formulas can help constrain the estimation of elasticity coefficients, yielding
149 physically-coherent regionalized streamflow elasticities. We use for this purpose a
150 large dataset of catchments covering a wide variety of climates.

151 2 Catchments and Method

152 2.1 Test catchments

153 To ensure that our analysis was based the widest possible range of climates, we used
154 a set of 4,122 catchments, representing 162,005 station-years of data (average length
155 of catchment time series is 39 years). It includes catchments from Australia (Fowler et
156 al., 2024), Brazil (Almagro et al., 2021), Denmark (Liu et al., 2024), France (Delaigue
157 et al., 2024), Germany (Loritz et al., 2024), Sweden (de Lavenne et al., 2022),
158 Switzerland (Höge et al., 2023), the United Kingdom (Coxon et al., 2020) and the USA
159 (Addor et al., 2017). Because this dataset is exactly the same as the one used by
160 Andréassian et al. (2025), we refer the reader to this paper for the details of the
161 selection of the catchments from the original datasets. Let us just mention that we
162 excluded a few catchments with a long memory, for which the linear elasticity model
163 presented in [Eq. 16](#) would not have been justified. Indeed, if a catchment has a
164 hydrogeology that provides it long memory, the elasticity cannot be expressed as a
165 function of the current year climate, but instead should be estimated by accounting for
166 as many previous years as necessary. The absence of interannual memory
167 guarantees the lack of autocorrelation in annual streamflow, which is an important
168 statistical assumption for OLS.

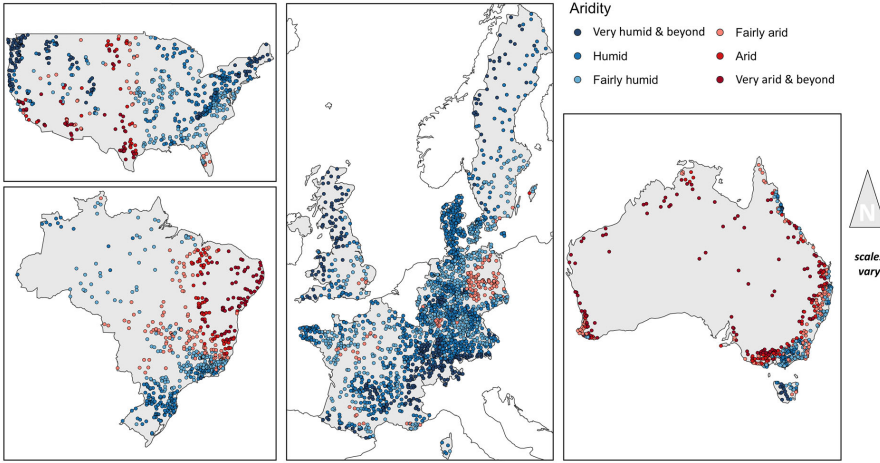
169 In our dataset, the aridity indices range from 0.1 to 6.3, with a first quartile of 0.6 and
170 a third quartile of 1.0. The mean and the median of the aridity index are both 0.8. To
171 assess the generality of the results, we will discuss them at the global scale and also
172 by aridity classes (as defined in [Table 2](#)).

173

174 Table 2. Aridity classes used in this study (we only kept the classes counting more than 100
 175 catchments)

Aridity class	Average aridity of the class	Number of catchments	Name
[0.25,0.50[0.39	484	Very humid
[0.50,0.75[0.64	1461	Humid
[0.75,1.00[0.85	1238	Fairly humid
[1.00,1.25[1.09	434	Fairly arid
[1.25,1.50[1.37	186	Arid
[1.50,1.75[1.61	109	Very arid

176



177

178 Figure 2. location of the catchments studied and repartition by aridity classes

179

180 2.2 Computation of local elasticities

181 Our reference method will consist in the local (i.e., catchment-specific) computation of
 182 streamflow elasticities using [Eq. 16](#) ~~Eq. 16~~:

$$\Delta Q_n = e_{Q/P}^{loc} \Delta P_n + e_{Q/E_0}^{loc} \Delta E_{0n} + e_{Q/\Lambda}^{loc} \Delta \Lambda_n \quad \text{Eq. 16}$$

183 Because the elasticity coefficients are obtained through linear regression, they are
 184 associated with statistical uncertainty, which we assess using the p-value. A
 185 significance threshold must be chosen, above which a coefficient is not considered
 186 statistically different from zero. For this paper, we use a conventional threshold of 0.05.
 187 With this local approach, a unique triplet of elasticities is computed for each of the
 188 4,122 catchments, and the goodness of fit for each regression is, by definition,
 189 maximized (hence our choice of the local calibration as reference).

190 Note that the correlation between the independent variables of the regression
191 presented in [Eq. 16](#) is rather limited: the correlations computed at the catchment
192 scale are comprised for 90% of the cases in the range [-0.6,0.2] for $(\Delta P_n, \Delta E_{0n})$, in the
193 range [-0.7,0.5] for $(\Delta P_n, \Delta \Lambda_n)$, and in the range [-0.5,0.4] for $\Delta E_{0n}, \Delta \Lambda_n)$,

194 2.3 Computation of unique elasticities by aridity class and for the entire dataset

195 We can also estimate a single triplet of elasticities for each different aridity class (as
196 defined in [Table 2](#)) and we then use [Eq. 17](#) for all the catchments of the
197 given aridity class.

$$\Delta Q_n = e_{Q/P}^{cl} \Delta P_n + e_{Q/E_0}^{cl} \Delta E_{0n} + e_{Q/\Lambda}^{cl} \Delta \Lambda_n \quad \text{Eq. 17}$$

198 Estimating a single triplet of elasticities for each class allows investigating the
199 dependency of elasticity to aridity. To calibrate the three parameters, we use a simple
200 grid search algorithm, exploring the following intervals: [-0.1,1.1] for $e_{Q/P}^{cl}$, and [-1.1,0.1]
201 for e_{Q/E_0}^{cl} and $e_{Q/\Lambda}^{cl}$, first with a coarse step of 0.1 and then a finer step of 0.01 around
202 the optimum. The objective function to be maximized is the bounded Nash-Sutcliffe
203 Efficiency of Mathevet et al. (2006), which is first calculated for each catchment
204 separately, and then averaged over the catchments belonging to the class and used
205 as the objective to maximize (see Section 2.5).

206 For reference, we also compute a single triplet of elasticities at the global scale by
207 pooling all 4,122 catchments together. By construction, this world-wide triplet yields
208 the lowest mean efficiency.

209 2.4 Computation of regionalized elasticities

210 In the regionalized approach, we use the entire dataset to calibrate a single underlying
211 model, similarly to the calculation of elasticities at the global scale. However, this
212 method ultimately produces catchment-specific results. Each catchment has a distinct
213 triplet of elasticities because the elasticities for precipitation ($e_{Q/P}^{reg}$) and potential
214 evaporation (e_{Q/E_0}^{reg}) are modeled as functions of each catchment's aridity index (φ),
215 given by [Eq. 18](#). The regionalization formulas are adjusted by a shape parameter
216 noted α :

217

$$\Delta Q_n = e_{Q/P}^{reg} \Delta P_n + e_{Q/E_0}^{reg} \Delta E_{0n} + e_{Q/\Lambda}^{reg} \Delta \Lambda_n \quad \text{Eq. 18}$$

$$e_{Q/P}^{reg} = f_P(\alpha_P, \varphi)$$

$$e_{Q/E_0}^{reg} = f_{E_0}(\alpha_{E_0}, \varphi)$$

$$e_{Q/\Lambda}^{reg} = \text{constant (does not depend on } \varphi)$$

218
 219 There were several alternatives available for choosing the shape of functions f_P , and
 220 f_{E_0} , as well as for adjusting the shape parameters. For f_P and f_{E_0} we used the
 221 derivatives of the Oldekop formula (see [Eq. 8Eq-8](#) and [Eq. 9Eq-9](#)). The variation range
 222 for these functions was constrained based on the results of the class calibration
 223 (Section 2.3). The synchronicity elasticity ($e_{Q/\Lambda}^{reg}$) was kept constant because no clear
 224 empirical relationship was observed when examining either the local or the class-
 225 calibrated elasticities.

226 [Figure 3](#) illustrate the dependency of streamflow elasticities to aridity, which is apparent
 227 both with the locally- and the class-estimated values. To keep the number of adjusted
 228 parameters low, we adjusted only three parameters (α_P , α_{E_0} and $e_{Q/\Lambda}^{reg}$) for [Eq. 18Eq-](#)
 229 [48](#), the variation bounds were set up empirically once for all based on the results of the
 230 class calibration.

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231 2.5 Model evaluation criterion

232 To evaluate the performance of the different elasticity models in simulating streamflow
 233 anomalies, we use the classical Nash and Sutcliffe (1970) efficiency criterion (NSE).
 234 The NSE is usually computed for each of the 4,122 catchments separately using [Eq.](#)
 235 [19Eq-19](#):

$$NSE = 1 - \frac{\sum_n (\Delta Q_n^{obs} - \Delta Q_n^{cal})^2}{\sum_n (\Delta Q_n^{obs} - \Delta Q_n^{obs})^2} \quad \text{Eq. 19}$$

236 Because the NSE varies in the interval $]-\infty, 1]$, it is not recommended to compute an
 237 average over large sets (indeed, a few very low criteria values will impact the average
 238 criterion value). For this reason, we follow Mathevet et al. (2006) and use the bounded
 239 form (called "C2M" in the original paper) as in [Eq. 20Eq-20](#):

$$\text{Bounded NSE (C2M)} = \frac{NSE}{2 - NSE} \quad \text{Eq. 20}$$

240

241 **3 Results**

242 **3.1 Empirical verification of the dependency between locally-estimated**
243 **streamflow elasticities and aridity**

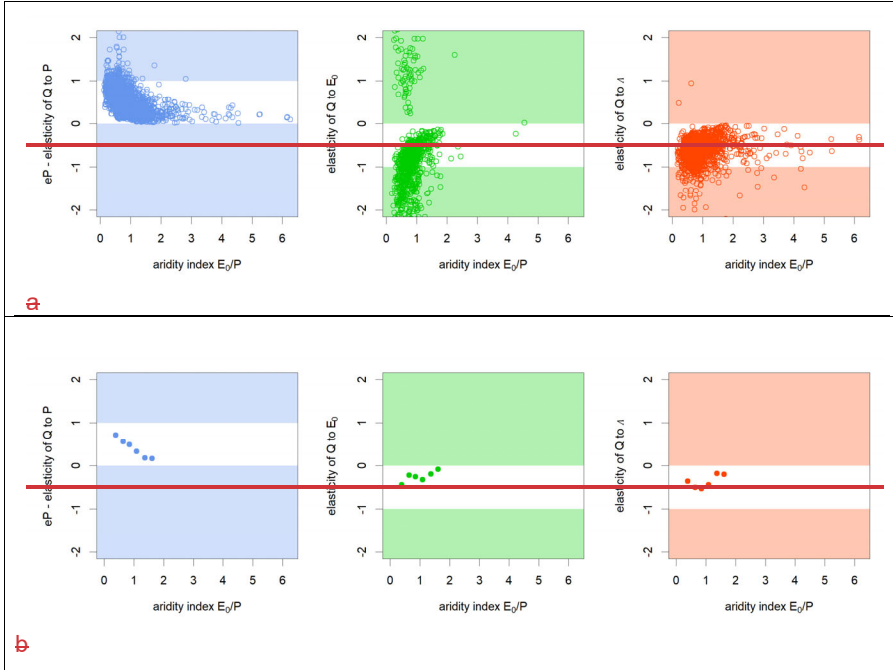
244 ~~We first computed the local streamflow elasticities for each catchment by linear~~
245 ~~regression (Eq. 16). Choosing an (arbitrary) significance level equal to 0.05, our~~
246 ~~dataset yielded 97% of the catchments with a significant $e_{Q/P}$ parameter, but only 23%~~
247 ~~of the catchments with a significant e_{Q/E_0} parameter, and 64% of the catchments with~~
248 ~~a significant $e_{Q/\Lambda}$ parameter.~~

249 ~~We first computed the local streamflow elasticities for each catchment by linear~~
250 ~~regression (Eq. 16), and retained only the coefficients that were statistically significant~~
251 ~~at the 0.05 level. In our dataset, 97% of the catchments had a significant $e_{Q/P}$~~
252 ~~parameter, only 23% of the catchments had a significant e_{Q/E_0} parameter, and 64% of~~
253 ~~the catchments had a significant $e_{Q/\Lambda}$ parameter.~~

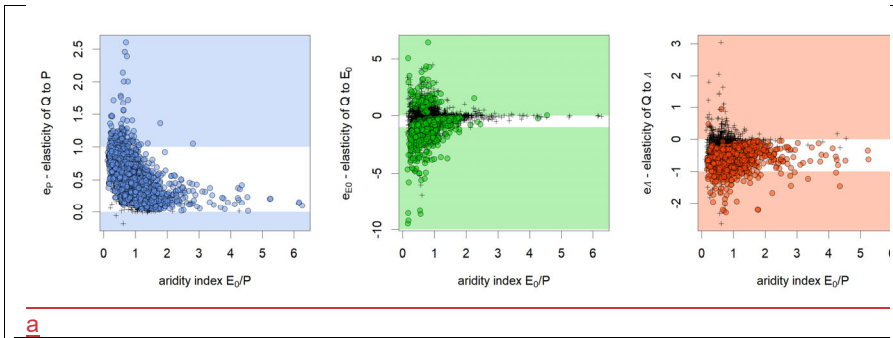
254 ~~Figure 3~~ presents the link between aridity and the locally-estimated elasticity
255 coefficients. The results confirm the expected dependency between precipitation
256 elasticity and aridity, which was previously shown for the theoretical formulas in ~~Figure~~
257 ~~1~~Figure 4. For the potential evaporation elasticity, a satisfying trend is visible but many
258 physically unrealistic elasticities show that additional constraints are required for this
259 term. Finally, the Λ -elasticity of streamflow (i.e. the streamflow elasticity towards the
260 synchronous amounts of precipitation and streamflow), shows no clear dependency
261 on the aridity index (but we did not expect any relationship).

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264 **Figure 3. Relationship between the aridity index and locally-estimated climatic elasticities of**
 265 **streamflow, for precipitation elasticity (left), potential evaporation elasticity (middle),**
 266 **synchronicity elasticity (right). The white domain indicates the physically-plausible range (i.e.**
 267 **[0,1] for precipitation elasticity and [-1,0] for potential evaporation and synchronicity**
 268 **elasticities. a – (upper panel) locally calibrated elasticity coefficients, all plots include only catchments with**
 269 **statistically significant elasticity coefficients ($p < 0.05$), resulting in different sample sizes for**
 270 **each panel ($N = 4017$ for $e_{Q/P}$, $N = 957$ for e_{Q/E_0} and $N = 2630$ for $e_{Q/A}$); b – (lower panel) class**
 271 **calibrated elasticity coefficients (from Table 3)**



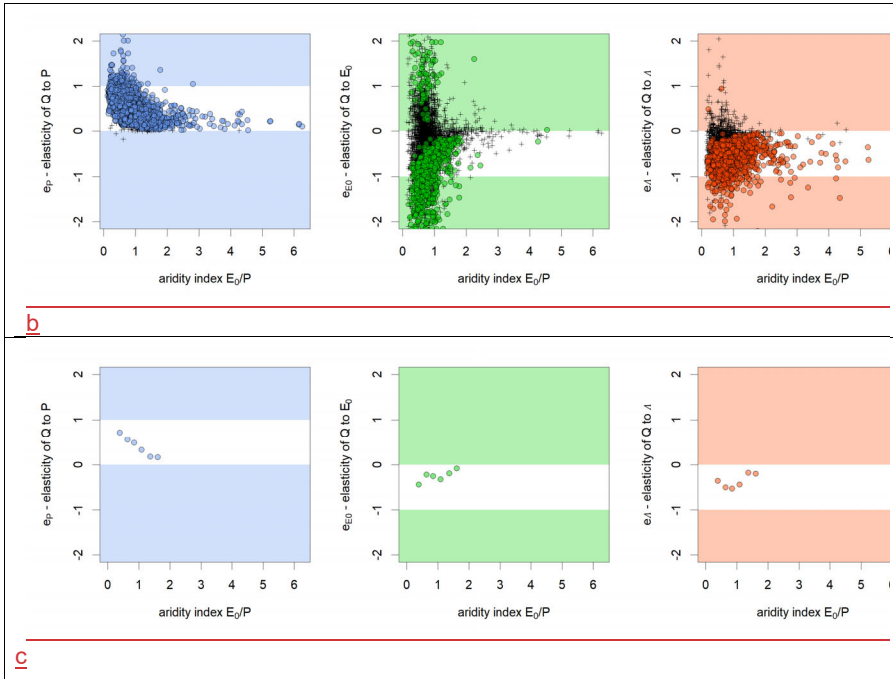


Figure 3. Relationship between the aridity index and locally-estimated climatic elasticities of streamflow, for precipitation elasticity (left), potential evaporation elasticity (middle), synchronicity elasticity (right). The white domain indicates the physically-plausible range (i.e. [0,1] for precipitation elasticity and [-1,0] for potential evaporation and synchronicity elasticities. a – (upper panel) locally calibrated elasticity coefficients, showing all catchments (elasticities coefficients non-significant at the 0.05 level are figured as crosses), b – (middle panel) same as a with a zoom on the [-2,2] range; c – (lower panel) class calibrated elasticity coefficients (from Table 3)

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281 3.2 Results by aridity class

282 We also calibrated the three elasticity coefficients to obtain a single triplet of values for
 283 each of the aridity classes as defined in sections 2.4 and 3.2. The resulting class-
 284 calibrated values are presented in Table 3. As reference, the performance of the local
 285 (catchment-specific) estimation is also provided (by construction, it represents the
 286 upper limit of performance).

287

288 **Table 3. Class-calibrated elasticity values for catchments grouped by the aridity index φ**

Aridity class	Number of catchments	Elasticity values			Performance expressed in mean bounded NSE for	
		$e_{Q/P}^{cl}$	e_{Q/E_0}^{cl}	$e_{Q/A}^{cl}$	Class approach (same elasticities for all catchments in the same class)	Reference approach (local i.e., catchment-specific estimation)
Very Humid $\varphi \in [0.25, 0.5[$	484	0.72	-0.44	-0.36	0.59	0.68
Humid $\varphi \in [0.5, 0.75[$	1461	0.56	-0.22	-0.50	0.46	0.57
Fairly Humid $\varphi \in [0.75, 1[$	1238	0.49	-0.25	-0.53	0.42	0.52
Fairly Arid $\varphi \in [1, 1.25[$	434	0.33	-0.32	-0.44	0.32	0.49
Arid $\varphi \in [1.25, 1.5[$	186	0.18	-0.19	-0.18	0.27	0.56
Very Arid $\varphi \in [1.5, 1.75[$	109	0.17	-0.08	-0.20	0.29	0.55
World	4,122	0.46	-0.19	-0.56	0.38	0.56

289
 290 The numeric values in Table 3 confirm the tendency identified in [Figure 3](#): the
 291 precipitation elasticity of streamflow shows a clear decreasing trend with increasing
 292 aridity, while the potential evaporation elasticity shows a symmetric increasing trend.
 293 The empirical range of variation observed in the class-calibrated results is narrower
 294 than the theoretical range from the water balance formulas: for $e_{Q/P}$, the observed
 295 range is [0.17, 0.72] compared to the theoretical [0, 1], and for e_{Q/E_0} , the range is [-0.44,
 296 -0.08] compared to the theoretical [-1, 0]. Finally, there is no clear trend identifiable for
 297 $e_{Q/A}$. A clear advantage of the class-based calibration approach is that all resulting
 298 elasticities values fall, without exception, within the physically-realistic ranges.

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299 **3.3 Constraining the elasticity estimation with an aridity-dependent**
 300 **formulation: test for the entire dataset**

301 The observed link between the aridity index and the local elasticity estimates
 302 suggested us to test the solution presented in section 2.4, using a “regionalized”
 303 estimation of the elasticities of streamflow. This approach makes use of the identified
 304 pattern to enforce physical coherence across the entire dataset. To parameterize this
 305 relationship, we adapted the partial derivative of the parameter-free Oldekop formula

306 (Table 1-4). We constrained the output of the Oldekop formulas to the empirical
 307 range observed in the class-based calibration (Table 3), offsetting the range for e_p to
 308 [0.15, 0.75], and for e_{E_0} to [-0.45, -0.10]. Thus, the regionalized elasticities are
 309 calculated as:

$$e_{Q/P}^{reg} = 0.15 + |0.75 - 0.15| * f_{p-Oldekop}(\alpha_p, \varphi) \quad \text{Eq. 21}$$

where $f_{p-Oldekop}$ is given by Eq. 8

$$e_{Q/E_0}^{reg} = -0.10 + |-0.45 + 0.10| * f_{E_0-Oldekop}(\alpha_{E_0}, \varphi) \quad \text{Eq. 22}$$

where $f_{E_0-Oldekop}$ is given by Eq. 9

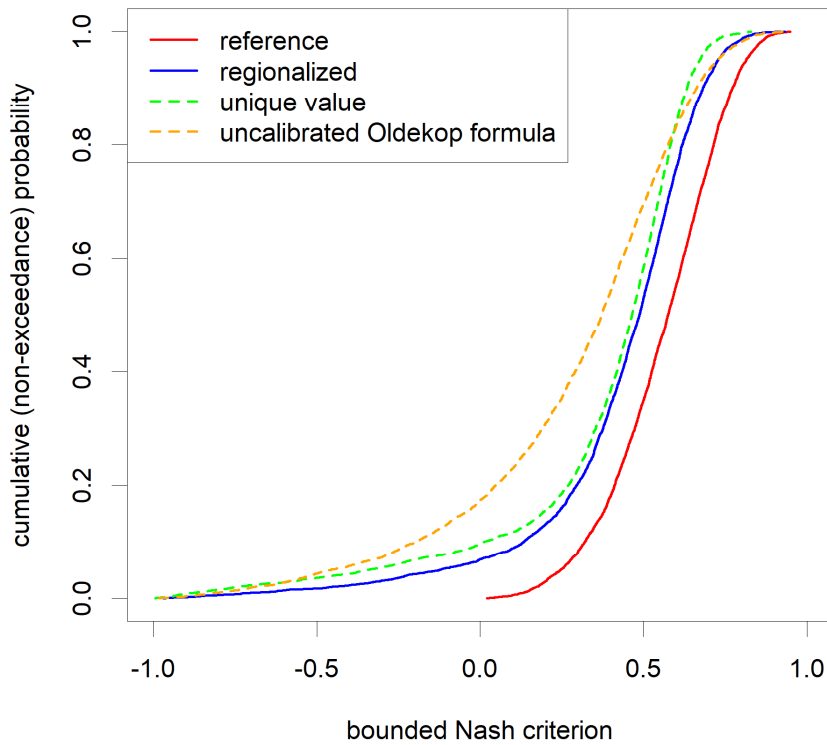
311 Note that the restricted ranges remain within the physically-realistic limits.

312
 313 We can now compare the performance of three modeling approaches: the “upper
 314 reference” where elasticities are calibrated locally at the catchment scale, the
 315 regionalized approach, and a “lower reference” with elasticities calibrated at global
 316 scale. While the upper reference requires the estimation of 12,366 parameters (3
 317 elasticities for 4,122 catchments), the latter two require only 3 parameters each. The
 318 corresponding results are presented below in Table 4 and Figure 4.

319 **Table 4. Results of the application of the regionalized approach to all the catchments of our**
 320 **dataset (4,122): the performance is compared to a upper reference (with locally calibrated**
 321 **elasticity values) and a lower reference (with a unique value calibrated for all the catchments in**
 322 **the world)**

Performance expressed in mean bounded NSE for		
Upper reference approach: <i>local, i.e. catchment-based estimation</i>	Regionalized approach: <i>elasticities function of each catchment's aridity index</i>	Lower reference approach: <i>same elasticities for all catchments</i>
0.56	0.43	0.38

324
 325 There is a clear advantage for taking into account the aridity in the regionalized
 326 formula. This approach covers 28% of the performance gap between the lower and
 327 upper references, while using only three parameters. In addition, all elasticity
 328 parameters remain within the physically-realistic range. The proposed parametrization
 329 is therefore successful from both explanatory and predictive point of views, which is a
 330 clear advantage (Andréassian, 2023).



331
 332 **Figure 4.** Distribution of the performances of the options compared in our paper, with the
 333 addition of the uncalibrated theoretical formulation derived from the Oldekop formula. The
 334 (unreachable) upper reference at the extreme right is followed by our regionalized solution,
 335 which has a better performance than an elasticity formula with a unique value (that would be
 336 independent from aridity) or than the elasticities derived from the (uncalibrated) Oldekop
 337 formula.

338

339 **4 Discussion**

340 In this paper, our aim was two-fold: (i) to empirically verify that at the catchment scale,
 341 streamflow elasticity and climate aridity are linked, and (ii) to propose an aridity-
 342 dependent parameterization allowing for the quantification of elasticity.

343 **4.1 The need for an empirical verification**

344 Because of the present popularity of Budyko's framework and its associated theoretical
345 formulas (~~Table 1~~Table 1), an empirical verification of the elasticity-aridity link might
346 appear superfluous. However, applying these theoretical formulas, such as the
347 Oldekop derivative, relies on a "space-for-time-trade" assumption. This consideration
348 assumes that a model validated across different spatial locations will also be valid for
349 those locations for different time periods (see Peel and Blöschl, 2011, and Singh et al.,
350 2011).

351 Berghuijs and Woods (2016) have warned that this trade requires validation, and
352 Berghuijs et al. (2020) stress that although the Budyko-type curves have been used to
353 predict the evolution of catchments in response to climatic changes, they originate from
354 "*observations of spatial differences in long-term water balances, and not from*
355 *observations or theory of how individual catchments respond to aridity changes*". Thus,
356 we argue that the elasticity-aridity link cannot be taken for granted and requires
357 empirical verification, especially given the mixed results reported by Oudin and
358 Lalonde (2023), who tested the classical space-time trading when parametrizing a land
359 use dependent hydrological model, which failed to efficiently predict the direction and
360 magnitude of hydrological changes after land use conversions.

361 **4.2 An aridity-dependent parameterization that uses the shape of the Oldekop**
362 **formula**

363 Regarding our parameterization, our results confirm the general shape of the elasticity-
364 aridity relationship given by the Oldekop formula, but they use a narrower range of
365 variation than the theoretical one. Our work is therefore only partially coherent with the
366 theoretical Budyko-type formulas, which appear to provide a wider range of elasticity
367 values than our empirical data support. This should not be a surprise to hydrologists
368 who know in particular how precipitation intensities impact the hydrological response
369 of arid catchments. What is remarkable, however, is that the intuition of Schreiber
370 (1904) and Oldekop (1911), embedded in formulas of elegant simplicity, remain so
371 useful in the 21st century. We agree on this point with Zhang and Brutsaert (2021) who
372 suggested that the "Budyko hypothesis" could justifiably have been named after
373 Schreiber and Oldekop, who, with so little data and only slide rules, were able to
374 imagine tools still in use today.

375 Concerning the difference between the elasticities derived from the theoretical Budyko-
 376 type formulas and the empirical class-calibrated values, we can suggest two
 377 explanations: first, a Budyko-type formula will always remain a conjecture (an elegant,
 378 mathematically relevant one but nevertheless, still a conjecture); second, Gnann et al.
 379 (2026) have shown that realistic observational noise will introduce systematic
 380 departures from the theoretical optimum.

381 5 Conclusion

382 5.1 Summary

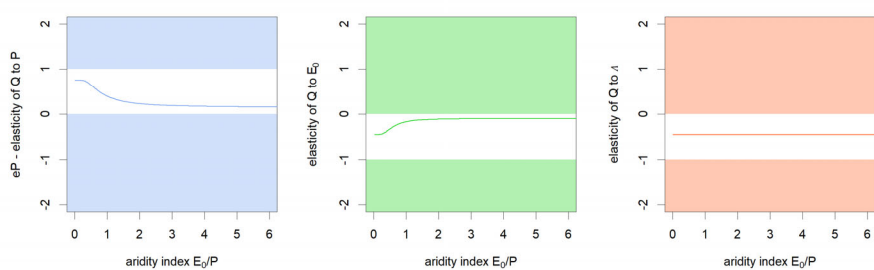
383 In this paper, we investigated the dependency between streamflow elasticity and aridity
 384 using a large dataset of 4,122 catchments across Europe, Australia, North America
 385 and South America. Our analysis confirmed the well-established dependency between
 386 elasticity and aridity and showed that the shape of this dependency can be effectively
 387 reproduced by existing theoretical formulas. We further demonstrated that these
 388 theoretical formulas can be used to guide the regionalization process, producing a
 389 regionalized aridity-dependent estimate of streamflow elasticity for each catchment,
 390 based on a parsimonious parameterization. The proposed solution, based on the
 391 Oldekop formula, is summarized in [Table 5](#) below and illustrated in Figure 5.

392
 393 **Table 5: Summary of the proposed aridity-accounting regionalized formulas for computing the**
 394 **precipitation and potential evaporation elasticities of streamflow. ΔQ , ΔP , ΔE_0 and $\Delta \Lambda$ are the**
 395 **annual streamflow, precipitation, potential evaporation and synchronicity anomalies,**
 396 **respectively [$mm\ year^{-1}$]. The nondimensional aridity index ($\varphi = \overline{E_0/P}$) is computed as a long-**
 397 **term average. $f_P(\varphi)$ and $f_{E_0}(\varphi)$ are borrowed from the Oldekop formula (see [Table 1](#))**

$\Delta Q = e_{Q/P}\Delta P + e_{Q/E_0}\Delta E_0 + e_{Q/\Lambda}\Delta \Lambda$
$e_{Q/P} = 0.15 + 0.6 * f_P(\varphi)$
$f_P(\varphi) = \tanh^2\left(\frac{1}{1.32 * \varphi}\right)$
$e_{Q/E_0} = -0.10 + 0.35 * f_{E_0}(\varphi)$
$f_{E_0}(\varphi) = -\tanh\left(\frac{1}{1.43 * \varphi}\right) + \frac{1}{1.43 * \varphi} \left[1 - \tanh^2\left(\frac{1}{1.43 * \varphi}\right)\right]$
$e_{Q/\Lambda} = -0.47$

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398



399
 400 **Figure 5. Regionalized relationships (from the equations in Table 5Table-5) for the climatic**
 401 **elasticities of streamflow as a function of the aridity index: precipitation elasticity (left), potential**
 402 **evaporation elasticity (middle), synchronicity elasticity (right). The white domain indicates the**
 403 **physically-plausible range, i.e. [0,1] for precipitation elasticity and [-1,0] for potential evaporation**
 404 **and synchronicity elasticities.**
 405

406 **5.2 Limitations and perspectives**

407 Because our work was empirical, and even if it is based on a very large set of real-
 408 world data, it will remain provisory, until improved by others. It is important to note three
 409 limitations in our study. First, the relationships in Table 5Table-5 were developed on
 410 catchments with limited interannual memory (in the sense of de Lavenne et al., 2022):
 411 this excludes those catchments for which Eq. 3 would not be warranted to estimate
 412 streamflow elasticity, since additional independent variables expressing the climatic
 413 anomalies of the previous years would have been required. This could have been done
 414 following the work of de Lavenne et al. (2022), or of Pelletier and Andréassian, (2020),
 415 but we preferred to keep the elasticities' estimation as simple as possible. Second,
 416 aridity was computed using the Oudin et al. (2005) formula for potential evaporation,
 417 and the use of other formulas might require a recalibration of the model parameters.
 418 Third, although we do believe that aridity is the first-order driver of elasticity at the
 419 global scale, it is not the only one, and our regional model is clearly only a first step in
 420 the search for physical explanations.

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429 **8 Author contributions**

430 VA: conceptualization and writing, GMG: computations, figures, discussion, writing
431 (review and editing), AL: computations, discussion JL: discussion, writing (review and
432 editing)

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