

A hybrid framework for the spin-up and initialization of distributed coupled ecohydrological-biogeochemical models - SUPPLEMENTARY INFORMATION

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Table S1. Examples of spin-up methods and applications used in ecohydrological and biogeochemical models across different spatial scales. The table summarizes the model name, spatial scale, and methodological approach. The category indicates whether the spin-up scheme was newly introduced or applied and eventually compared to other methods.

| Source | Model | Scale | Description | Category |
|------------------------------|------------------------------------------------------------|-----------------------------|-------------------------------------------------------------------------------------------------------------------------------------|------------|
| Zhan et al. (2003) | Simplified Simple Biosphere Model (SSiB) | Regional scale & Plot scale | Developed semi-analytical solution to stabilize and accelerate spin-up. | Introduced |
| Thornton & Rosenbloom (2005) | Biome-BGC Model | Plot scale | Introduced multiple spin-up acceleration methods: accelerated decomposition, N addition, General multivariate minimization methods. | Introduced |
| Basso et al. (2011) | DSSAT-CENTURY Model | Plot scale | Developed SOC pool initialization using site-specific land-use history. | Introduced |
| Hashimoto et al. (2011) | CENTURY v4 Model | Plot scale | Proposed slow-relaxation scaling of C/N pools during spin-up. | Introduced |
| Xia et al. (2012) | Community Atmosphere Biosphere Land Exchange Model (CABLE) | Global scale & Plot scale | Developed semi-analytical solution to accelerate coupled C-N model spin-up. | Introduced |
| Koven et al. (2013) | Community Land Model version 4 (CLM4) | Global scale | Introduced vertically resolved C-N model with pool-specific modified accelerated decomposition spin-up. | Introduced |
| Ng et al. (2014) | Community Land Model with Carbon-Nitrogen (CLM-CN) | Plot scale | Combined data assimilation with spin-up adjustments. | Introduced |
| Qu et al. (2018) | Terrestrial Ecosystem Model (TEM) | Plot scale | Developed analytical solution-based fast spin-up algorithm. | Introduced |
| Bruun & Jensen (2002) | Daisy Model | Plot scale | Compared equilibrium initialization vs. historical simulation. | Tested |
| Foereid et al. (2012) | DAYCENT Model | Plot scale | Tested steady-state and trend-fitting SOC initialization. | Tested |
| Nemo et al. (2017) | Rothamsted Carbon Model (RothC) | Plot scale | Evaluated C input adjustment and SOC fractionation methods. | Tested |
| Dimassi et al. (2018) | CENTURY v4.5 Model | Plot scale | Tested SOC initialization scenarios combining crop history and relaxation. | Tested |
| Lavin-Gullon et al. (2023) | Regional Climate Model (RCM) | Regional scale | Assessed spin-up time and variability in overlapping time slices. | Tested |

Table S2. Comparison between soil organic carbon and nitrogen (SOC, SON) from the steady state condition with the biogeochemistry-only module (i.e., no coupled vegetation-soil biogeochemistry dynamics) and the reference steady state from the most comprehensive plot-scale spin-up (i.e., considering coupled vegetation-soil biogeochemistry dynamics) in the ten cells (see Fig. 2h in the main text). Information on vegetation cover and soil texture in these cells is also provided.

| ID | Vege | Sand [%] Clay [%] Organic [%] | SOC [kg C/m ²] | | | SON [kg N/m ²] | | |
|----|-------|-------------------------------------|----------------------------|--------|-------------------------|----------------------------|--------|-------------------------|
| | | | Steady | Coevo. | Relative difference (%) | Steady | Coevo. | Relative difference (%) |
| 1 | Tree | 40.9 27.5 6.8 | 12.51 | 13.51 | -7.40 | 0.93 | 1.04 | -10.58 |
| 2 | Tree | 42.0 24.9 9.0 | 10.46 | 12.31 | -15.03 | 0.80 | 0.96 | -16.67 |
| 3 | Tree | 42.5 24.3 8.6 | 10.36 | 11.94 | -13.23 | 0.81 | 0.94 | -13.83 |
| 4 | Tree | 42.5 25.9 7.2 | 11.90 | 13.74 | -13.39 | 0.89 | 1.06 | -16.04 |
| 5 | Tree | 39.5 25.9 8.3 | 11.53 | 12.90 | -10.62 | 0.87 | 1.00 | -13.00 |
| 6 | Grass | 41.7 26.5 6.7 | 6.70 | 8.42 | -20.43 | 0.84 | 0.90 | -6.67 |
| 7 | Grass | 41.3 26.9 7.1 | 6.41 | 8.00 | -19.88 | 0.82 | 0.86 | -4.65 |
| 8 | Grass | 40.4 27.9 8.5 | 6.32 | 7.76 | -18.56 | 0.81 | 0.84 | -3.57 |
| 9 | Grass | 40.1 26.7 7.2 | 6.91 | 8.29 | -16.65 | 0.87 | 0.89 | -2.25 |
| 10 | Grass | 41.6 26.5 6.3 | 6.73 | 8.36 | -19.50 | 0.85 | 0.90 | -5.56 |

Table S3. Jensen–Shannon divergence ($\times 10^{-4}$) between the probability density functions (PDFs) of soil organic carbon (SOC) and soil organic nitrogen (SON) from different percentages of tracked cells and those from the benchmark simulation across multiple simulation scenarios. Values in parentheses under the Random Soil scenario represent results obtained when clay content was included as an additional predictor in the random forest model.

| Scenarios/Track cells [%] | 10 | 20 | 40 | 60 | 80 | |
|---------------------------|-----|-------------|-----------|-----------|------|------|
| <i>Original</i> | SOC | 6.04 | 2.84 | 1.05 | 0.59 | 0.27 |
| | SON | 0.99 | 0.57 | 0.28 | 0.15 | 0.08 |
| <i>Random Veg</i> | SOC | 3.40 | 2.66 | 1.13 | 0.61 | 0.34 |
| | SON | 0.82 | 0.62 | 0.29 | 0.18 | 0.12 |
| <i>Homog. Veg</i> | SOC | 2.49 | 1.10 | 0.79 | 0.31 | 0.11 |
| | SON | 0.98 | 0.56 | 0.33 | 0.18 | 0.05 |
| <i>Random Soil</i> | SOC | 6659 (6.80) | 24 (4.05) | 21 (2.12) | | |
| | SON | 6725 (3.39) | 16 (2.26) | 2 (1.81) | | |
| <i>Homog. Soil</i> | SOC | 4.37 | 1.36 | 0.53 | | |
| | SON | 0.50 | 0.24 | 0.12 | | |
| 0.5 h_{max} | SOC | 5.62 | 2.16 | 0.88 | | |
| | SON | 0.98 | 0.57 | 0.25 | | |
| 0.2 h_{max} | SOC | 4.08 | 2.68 | 0.68 | | |
| | SON | 0.70 | 0.37 | 0.18 | | |

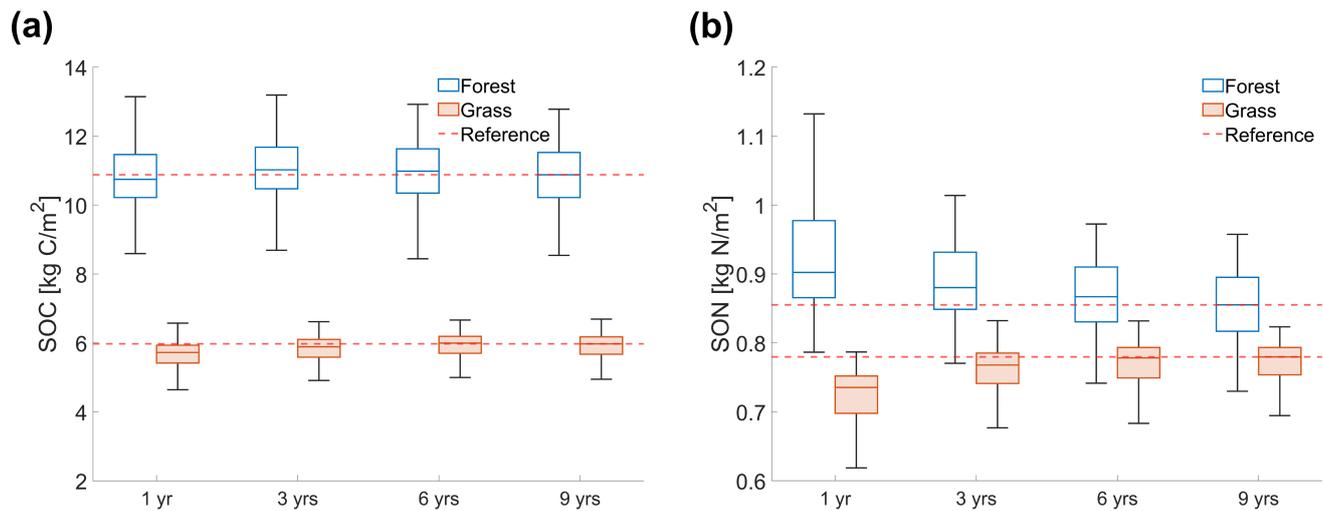


Figure S1. Comparison of steady state of (a) soil organic carbon (SOC) and (b) soil organic nitrogen (SON) using only the biogeochemistry module, with forcing and flux tracking periods of 1 year, 3 years, 6 years, and 9 years (reference). The forcing and flux tracking period is repeated to complete the 1000-year spin-up of the biogeochemistry module.

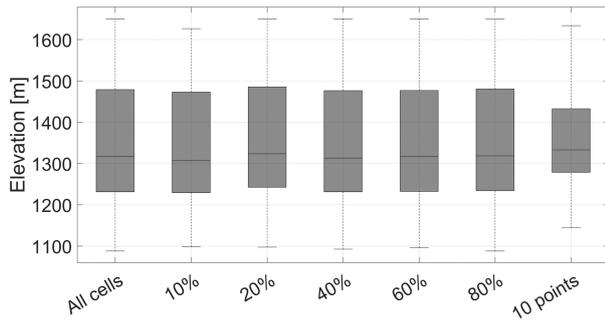
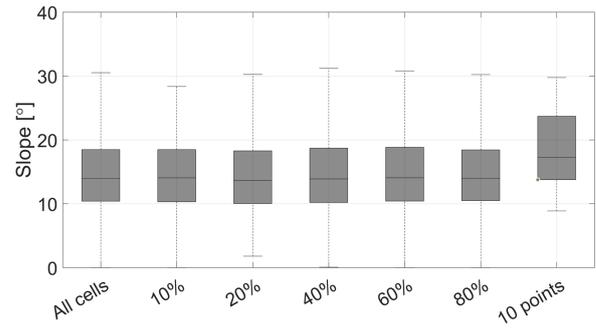
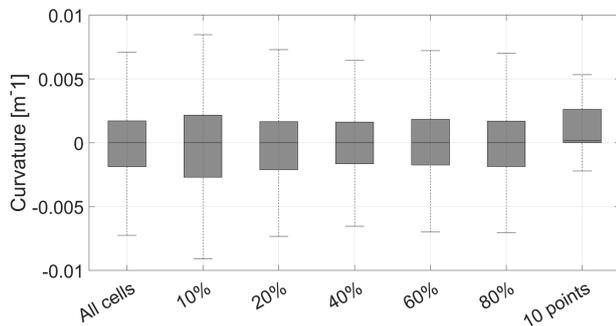
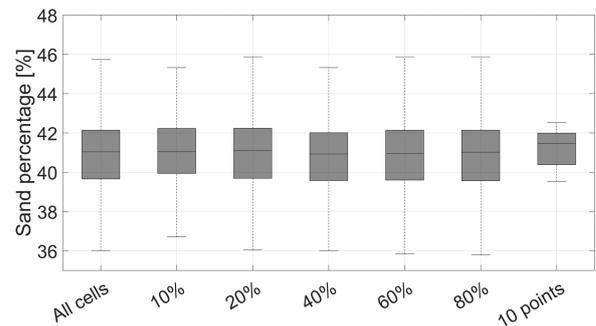
(a)**(b)****(c)****(d)**

Figure S2. Distribution of topographic and soil attributes for all grid cells and selected subsets used for random forest model training. Panels show the distributions of (a) elevation, (b) slope, (c) curvature, and (d) sand percentage for all cells in the domain (“All cells”), different percentages of tracked training cells (10%–80%), and the 10 selected reference points for additional plot-scale simulation. The distributions indicate that the selected subsets preserve the key topographic and soil characteristics of the full domain.

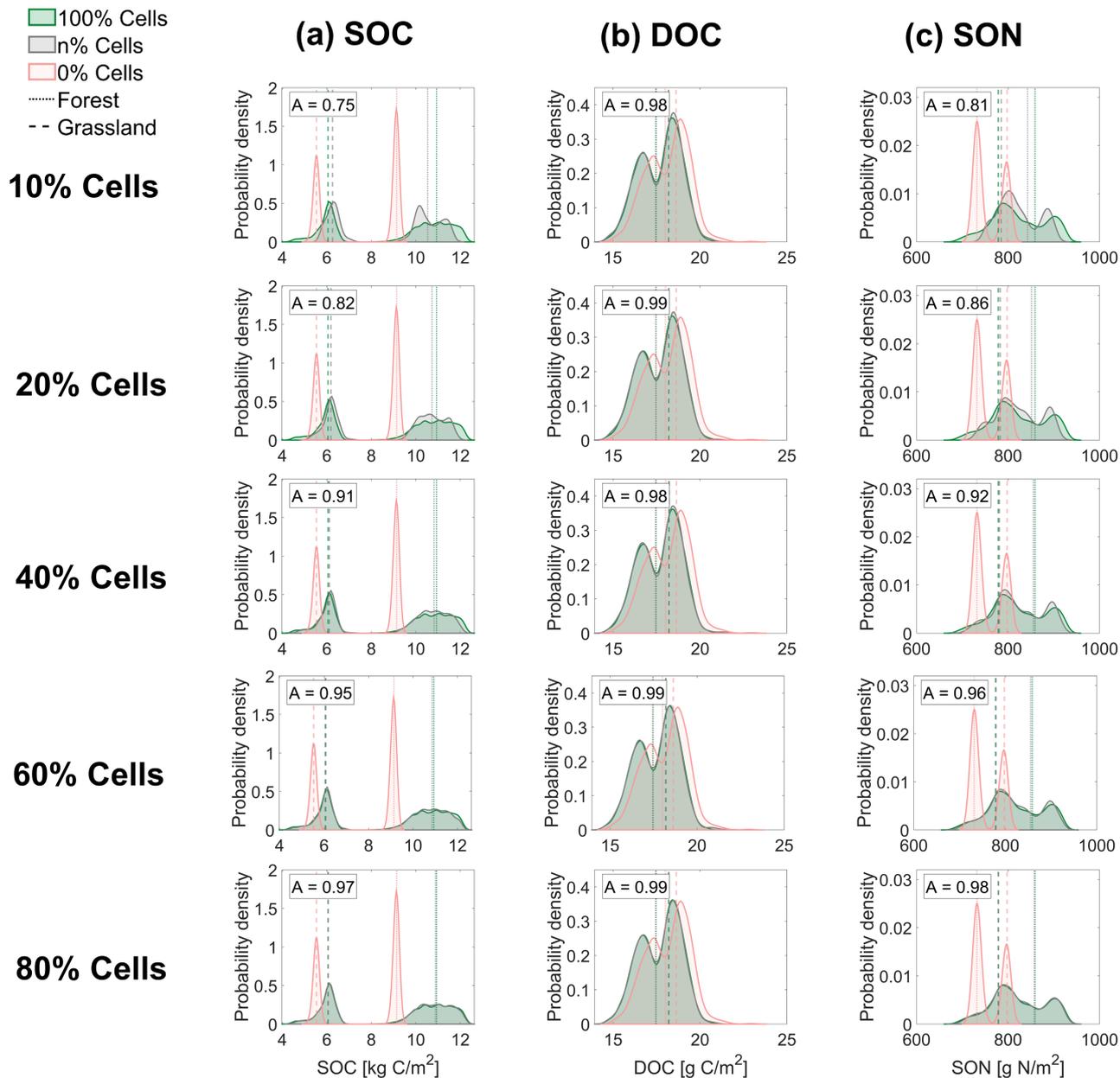


Figure S3. Probability density functions (PDFs) of (a) soil organic carbon (SOC), (b) dissolved organic carbon (DOC), and (c) soil organic nitrogen (SON) under different initialization settings using Random Forest (RF) with $n = 10\%$, 20% , 40% , 60% , and 80% . Each subplot compares the resulting distribution with those from the benchmark simulation using 100% of tracked cells (100% Cells) and from the simulation without cell tracking or RF (0% Cells). Shaded areas represent the overlapping region with the benchmark distribution. The overlap area between PDFs (A value) in each panel quantifies the similarity between the PDF and the benchmark. Dashed and dotted lines represent median values for grassland and forest areas, respectively.

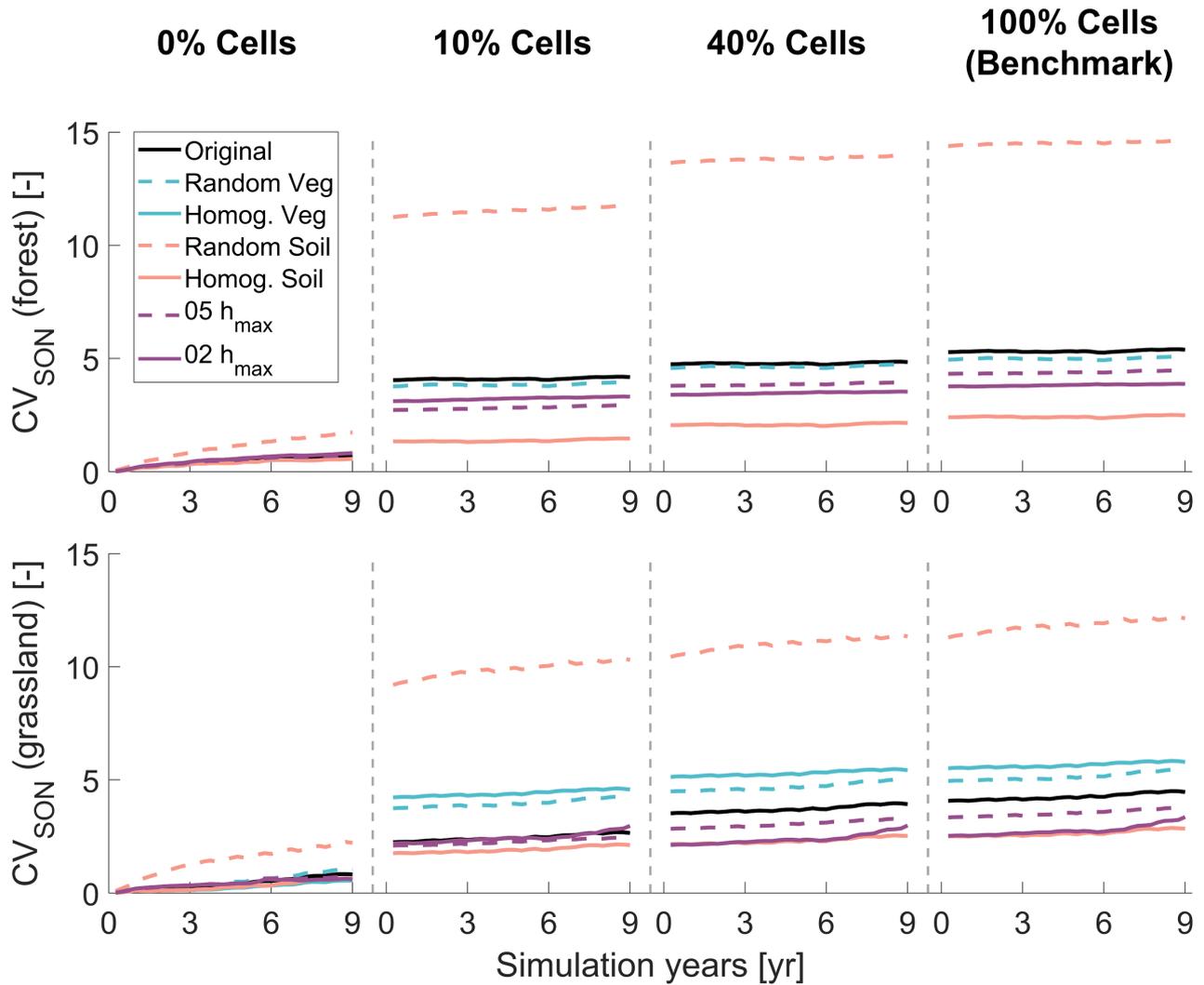


Figure S4. Temporal evolution of the coefficient of variation (CV) of soil organic nitrogen (SON) over a 9-year simulation period in forest (top) and grassland (bottom) under different initialization settings and simulation scenarios. Each column represents one initialization setting: no cells tracking and no random forest (0% Cells), $n = 10\%$ cells tracking and random forest (10% Cells), $n = 40\%$ cells tracking and random forest (40% Cells), and $n = 100\%$ cells tracking (100% Cells). Line colors and styles indicate results from different simulation scenarios, as shown in the legend.

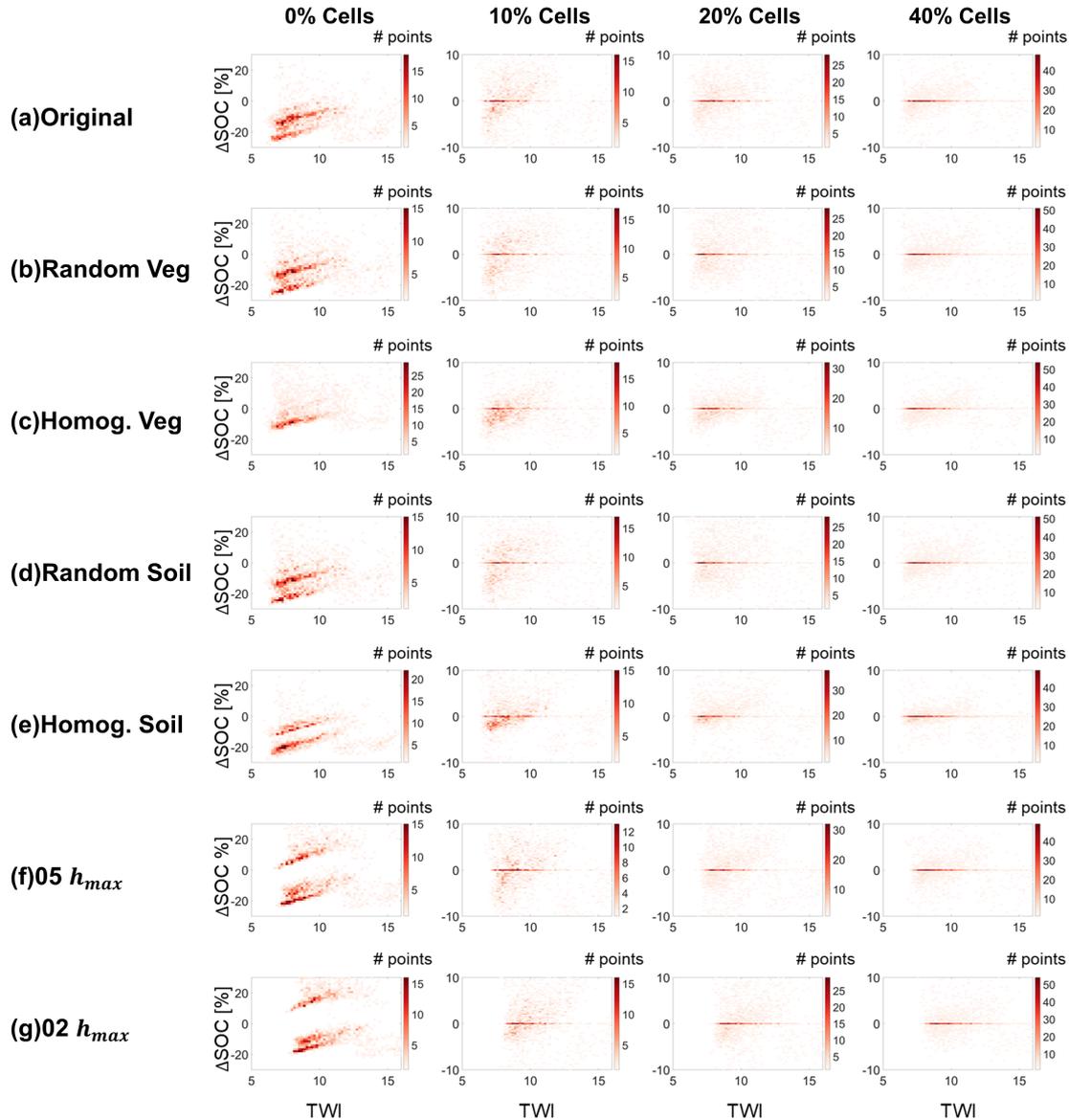


Figure S5. Density plots showing the relationship between relative SOC bias ($\Delta SOC = (SOC_{simulation} - SOC_{benchmark}) / SOC_{benchmark}$), where $SOC_{simulation}$ represents results from different initialization settings, and the topographic wetness index (TWI) across all simulation scenarios. Results are shown for (a) Original, (b) Random Veg, (c) Homog. Veg, (d) Random Soil, (e) Homog. Soil, (f) $0.5 h_{max}$, and (g) $0.2 h_{max}$ simulation scenarios. Columns represent different initialization settings: no cell tracking or RF ($n = 0\%$, 0% Cells), and RF-based initialization using $n = 10\%$, 20% , and 40% of tracked cells. The red color scale indicates the number of grid cells per bin.

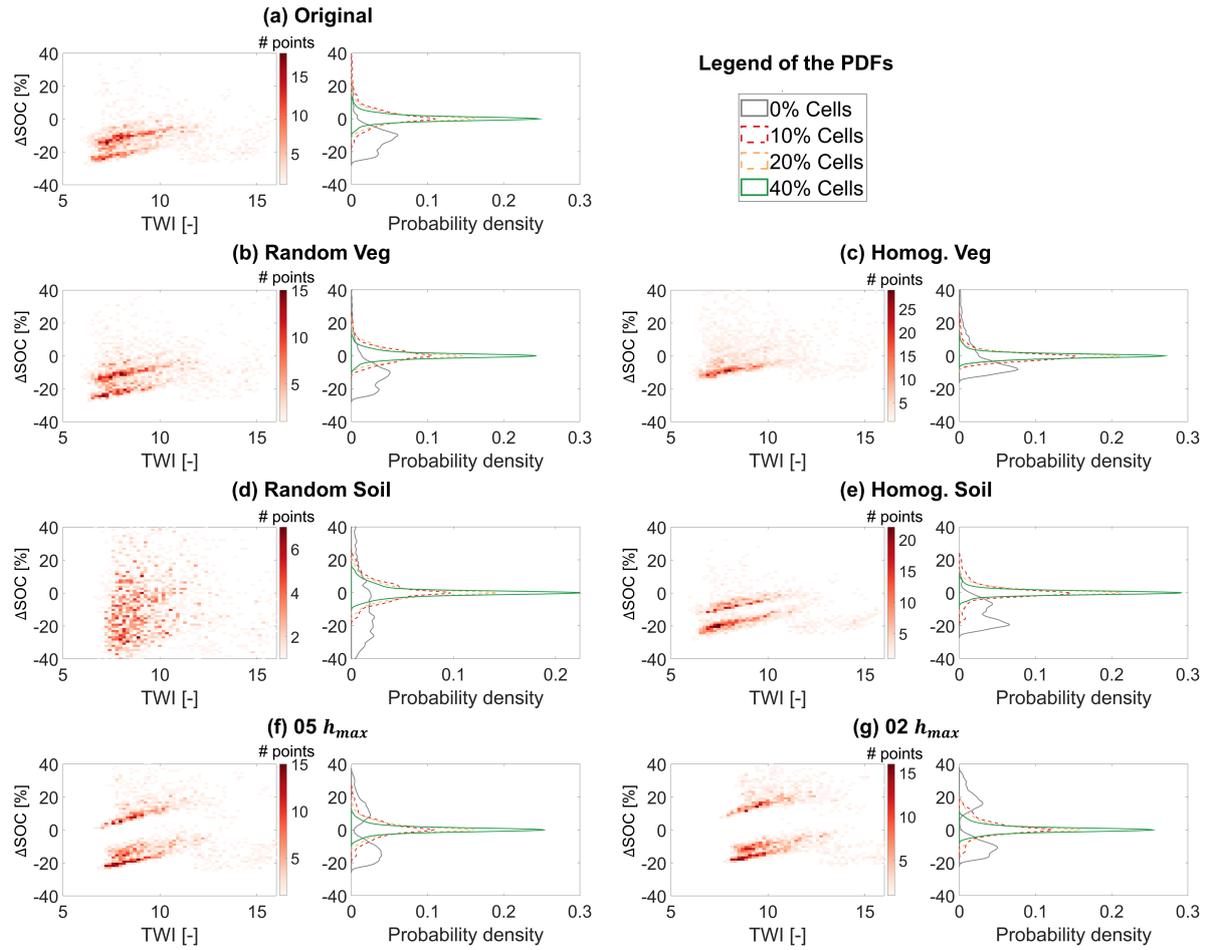


Figure S6. Density maps showing the relationship between SOC bias from the simulations without cell tracking and random forest ($n = 0\%$, 0% Cells) and topography wetness index (TWI) across different simulation scenarios (left panels of each subfigure; $\Delta SOC = SOC_{simulation} - SOC_{benchmark}$). Probability density functions (PDFs) of ΔSOC from $n = 0\%$ simulation (in gray), and with RF-based initialization using $n = 10\%$ (red), 20% (yellow), and 40% (green) of tracked cells (right panels). Results are shown for (a) Original, (b) Random Veg, (c) Homog. Veg, (d) Randon Soil, (e) Homog. Soil, (f) $0.5 h_{max}$, and (g) $0.2 h_{max}$ simulation scenarios.

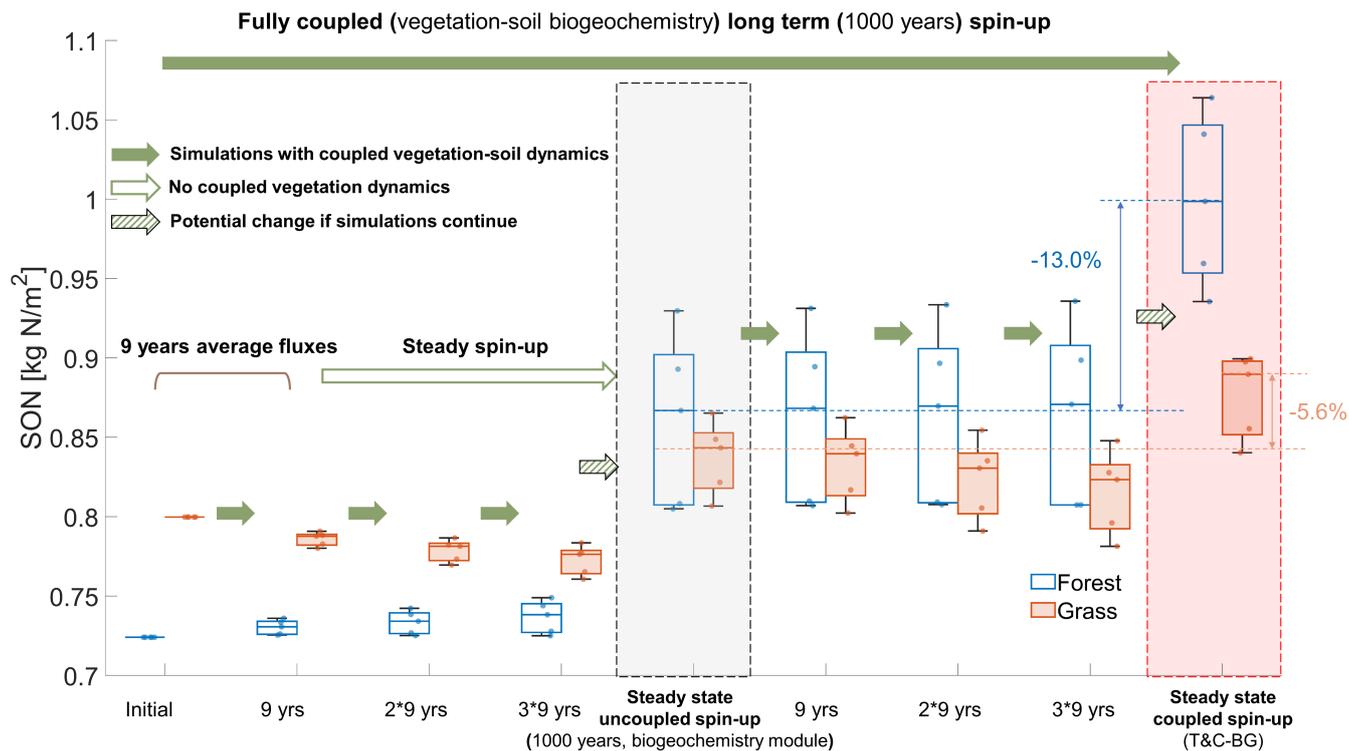


Figure S7. Evolution of soil organic nitrogen (SON) during different initialization schemes and simulation durations at 10 selected sites (Fig. 2h in the main text). Blue/orange boxplots represent forest/grassland sites. Arrows indicate simulation transitions between stages. The initial values (far left) are followed by 3*9-year simulations using the fully coupled T&C-BG model (solid green arrows). The average vegetation fluxes are extracted from the first 9 years to obtain a steady state condition with the biogeochemistry-only module (outlined green arrow, middle gray box). This is followed by three additional 9-year simulations. A comprehensive long-term spin-up using the fully coupled T&C-BG model (i.e., considering coupled vegetation and soil biogeochemical dynamics) is shown in the right red box. Striped arrows indicate the potential direction of SON change if coupled simulations continue beyond the current duration.

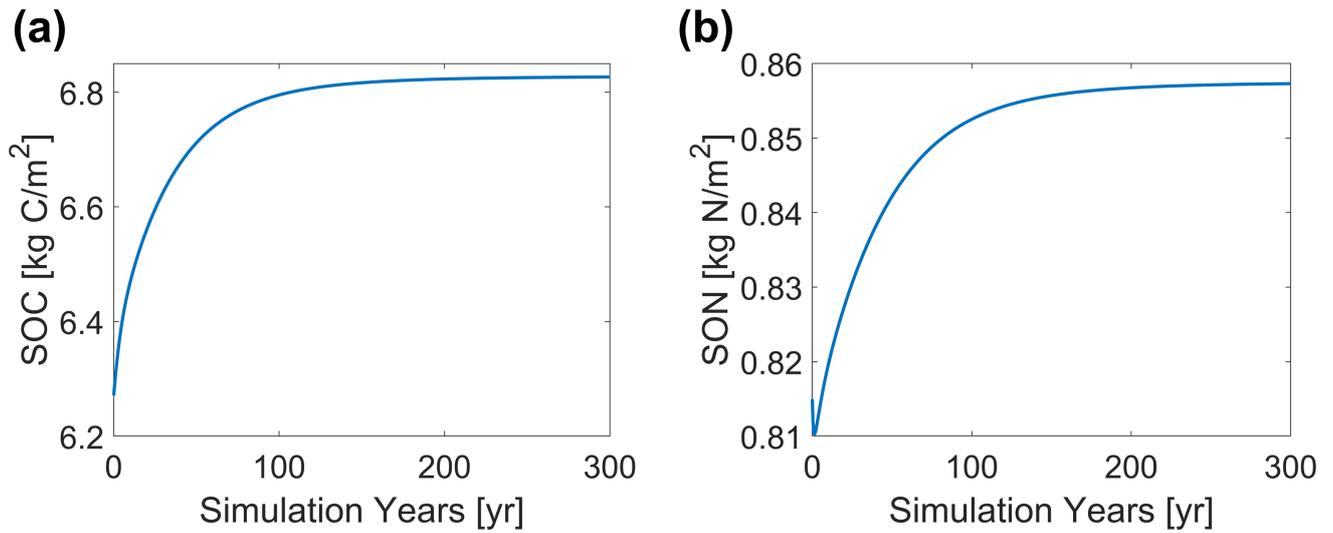


Figure S8. Example of temporal evolution of (a) soil organic carbon (SOC) and (b) soil organic nitrogen (SON) in a one-dimensional spin-up without coupled vegetation-soil biogeochemistry dynamics, based on repeated meteorological forcing at a representative grassland site in Erlenbach. SOC increases gradually over time, while SON initially declines before rising toward a steady state. The figure illustrates the slow convergence of soil carbon and nitrogen pools even under simplified conditions.

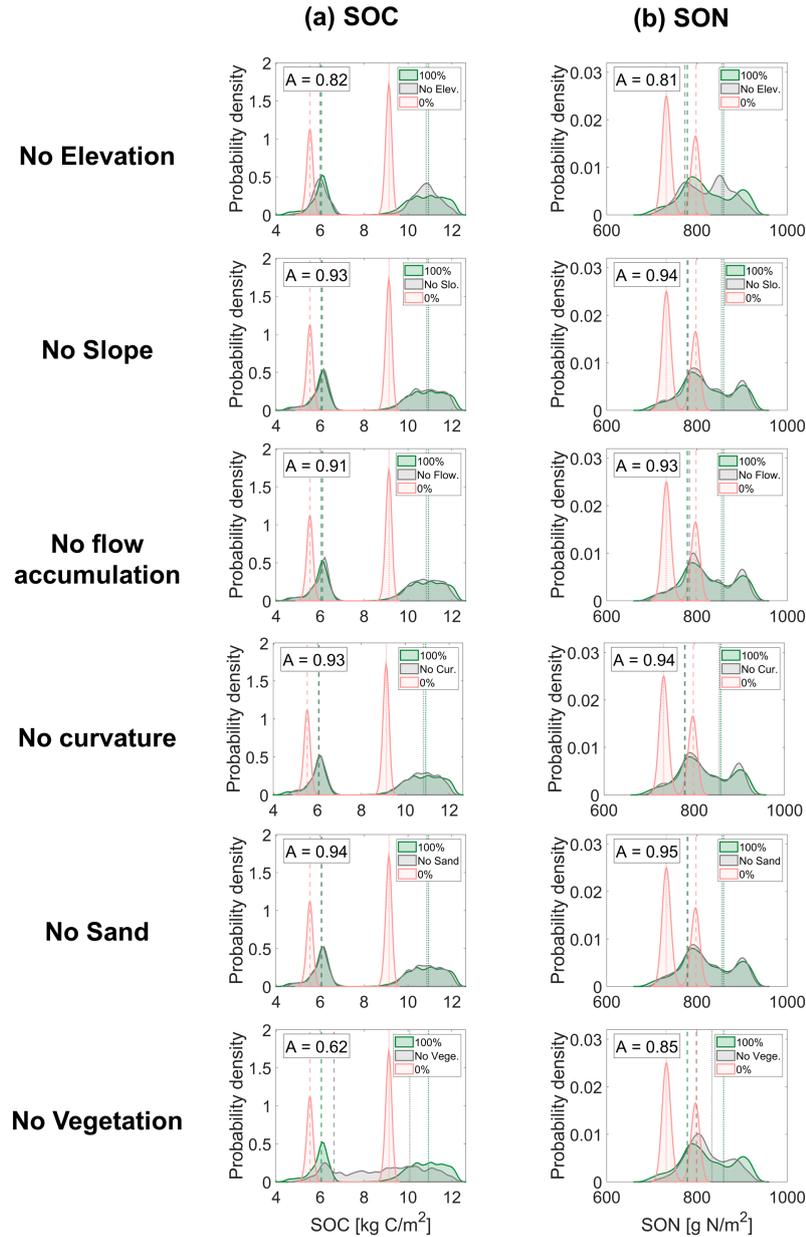


Figure S9. Sensitivity analysis of predictor importance in the Random Forest (RF) model for initializing spatial distributions of (a) soil organic carbon (SOC) and (b) soil organic nitrogen (SON) in the Erlenbach catchment. The analysis is conducted under the original simulation scenario using $n = 40\%$ of tracked cells for RF initialization. Each row shows the probability density functions (PDFs) of model outputs after removing one predictor from the RF training: elevation, slope, flow accumulation area, curvature, sand percentage, and vegetation type. Results are compared with the benchmark simulation using $n = 100\%$ tracked cells and the simulation without RF (No RF). Overlap area between PDFs (A value) quantifies the similarity between the RF-based distributions and the benchmark. Dashed and dotted lines represent median values for grassland and forest areas, respectively.

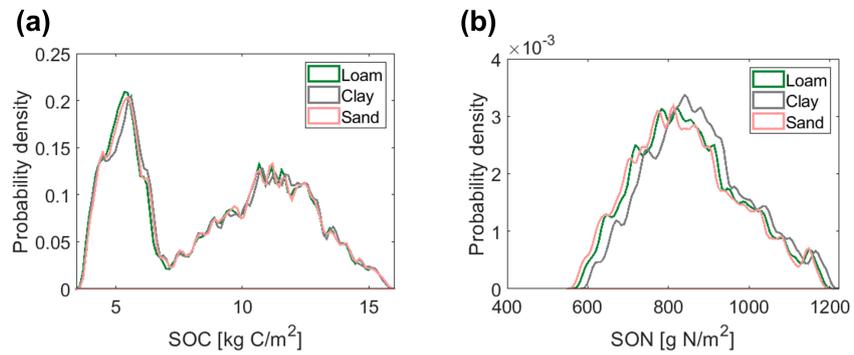


Figure S10. Probability density function of the spatial distribution of soil organic carbon (SOC) and soil organic nitrogen (SON) using three soil texture settings as initial conditions in step (a) in the initialization procedure. The spatial distribution results are the output of step (d) in Fig. 2 in the main text.

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