

Optimizing Airborne Emission Rate Retrievals with Sub-Hectometre Resolution Numerical Modelling

Sepehr Fathi^{1,2}, Mark Gordon³, Jingliang Hao³

¹ Air Quality Research Division, Environment and Climate Change Canada, 4905 Dufferin Street, Toronto, ON M3H 5T4, Canada

² Formerly at Physics and Astronomy Department, York University, 4700 Keele Street, Toronto, ON M3J 1P3, Canada

³ Department of Earth and Space Science and Engineering, York University, 4700 Keele Street, Toronto, ON M3J 1P3, Canada

Correspondence to: Mark Gordon (mgordon@yorku.ca)

Abstract. A comprehensive model-based study is designed to provide optimal flight paths for airborne top-down emission rate retrieval methodologies. The meteorology and plume dispersion were modelled using the Weather Research and Forecasting (WRF) modelling platform with the Advanced Research WRF (ARW) dynamical core at 50-m resolution. Multiple flight path designs and parameters were investigated to determine emission rate retrieval accuracy for emissions of a trace gas as a function of downwind distance and transect spacing, which are ultimately related to flight time and cost. Three unique source types (multiple smokestack plumes, small area sources, and a large area source) were investigated for 4 summer afternoon flight cases over 2 days. The results demonstrate that emissions estimate uncertainty is primarily due to storage and release, with uncertainties as high as 30% at optimal downwind distances (which vary by source type). Interpolation of the sparse measurements can be a significant source of error close to the source, but the uncertainty is $\leq 17\%$ for $D \geq 6$ km. The average advective flux estimates are within 12% of the known emissions for downwind distance of $D \geq 4$ km. Variability between flights decreases with D . For stack sources the variability near $D = 10$ km is approximately half that at $D = 4$ km. For small area sources, there is less reduction with D , and for the large area source, variability reaches a minimum at $D = 8$ km. For stack sources, transect spacing is optimized at 100 m, while for area sources, a spacing of 50 m reduces uncertainty. Error due to extrapolation below the lowest flight path is less than 20% for stack sources and less than 30% for area sources for non-dimensionalized downwind distance of $D' \geq 3$. Results demonstrate the need for surface sampling coincident with the flights to reduce extrapolation error, and the use of modeling with reanalysis data to account for storage and release effects.

1 Introduction

During airborne field studies for top-down retrieval of source emission rates, the environmental fields (meteorology and pollutant concentrations) are sampled around and/or downwind of emission sources. Typically, the aircraft flies in a repeating pattern that either encloses the source area (e.g., Peischl et al., 2010; Kalthoff, 2002; Gordon et al., 2015; Kim et

al., 2025), or that captures the extent of a downwind plume (e.g. Cambaliza et al., 2014). The time and spatial resolutions of such measurements are determined by the sampling frequency and range of the measuring instruments, the speed of the sampling platform, the sampling path and geographical locations (Gordon et al., 2015; Conley et al., 2017). The sparse spatial measurements that are made over time are processed and analyzed according to various assumptions regarding how representative they are of the mean and real-time environmental conditions (e.g., wind field, emissions: Alfieri et al., 2010). The post-processed data are then used for estimating emission rates from sources of pollution (Ryoo et al., 2019; Karion et al., 2015; Gordon et al., 2015).

Regardless of the measurement approach, the spatial heterogeneity and temporal variability of meteorology and concentration fields can result in large uncertainties in top-down estimates. Previous studies have attributed large uncertainties (20% to 40%) to the gap of information (spatial and temporal) in the sampled data (e.g., Angevine et al., 2020). For instance, airborne measurements are commonly made at elevations above 150 m agl for safety considerations. Gordon et al. (2015) identified the unsampled region below the lowest flight level as a large source of uncertainty in mass-balance analysis (e.g., up to 26% for CH₄ plumes). The gap of information in the sampled data, due to limitations on spatio-temporal resolution and range of the sampling method, can be partially filled by combining data from different measurement platforms. For instance, airborne samplings (aircraft, UAV) can be complimented by ground-based measurements (Brus et al., 2021b; Bell et al., 2021; Islam et al., 2021). Fixed location in-situ measurement techniques of meteorology and tracer concentrations include tower measurements at heights of up to 350 m agl (Heintzenberg et al., 2011; Andreae et al., 2015), and radiosonde (tethered/balloon) measurements include heights up to 2 km agl (Nygård et al., 2017; Nambiar et al., 2020). Ground-based remote-sensing can also be conducted from mobile surface land vehicles (de Boer et al., 2021; Davis et al., 2019), generating column measurements at higher spatial (horizontal) resolution. Remote-sensing datasets can be analyzed in conjunction with airborne measurements for both validation (Davis et al., 2020) and as complementary information (Krings et al., 2018; Brus et al., 2021a) in air quality studies. In a study based on the same model output used in this study, Fathi (2022) suggests augmenting airborne in-situ measurements with aircraft-based remote sensing (lidar) towards improving aircraft mass-balance retrievals.

Dispersion models have also been used to infer emissions from aircraft measurements, as alternative to the more common mass-balance approach. For example, Karion et al. (2019) used an inverse approach comparing different dispersion models (HYSPLIT, STILT, LPDM, FLEXPART) that optimizes emission rates to best fit observation. However, there was significant range in the predicted emission rate depending on the model used. Simpler, Gaussian footprint models can also be used to similar effect (Kim et al., 2025). These techniques offer the advantage of being able to estimate emission rates from multiple sources when the plumes overlap (e.g. Kostinek et al., 2021; Raznjevic et al, 2022). **Estimating separate emission rates for each source** is more difficult to do with the mass-balance method and requires individual plumes to be well defined and separate (e.g. Baray et al., 2018).

To better understand the mass-balance method and to quantify uncertainties, models can also be used to optimize the mass-balance measurement technique. Virtual aircraft can fly through model output fields, where emissions are known and the

65 relative contributions of advection, turbulence, and flux below the lowest flight path can be determined. This also allows
different flight configurations to be compared and optimized to increase emission measurement accuracy as a function of
flight time (cost). Panitz et al. (2002) were the first (to our knowledge) to use model output to evaluate the aircraft mass-
balance method. They used the KAMM/DRAIS model system to evaluate box flight measurements described in Kalthoff et
al. (2002). They determined advective fluxes were 85% of NO emissions and 95% of CO emissions, suggesting that total
70 emissions estimated based on downwind advective flux measurements, could be underestimated by up to 15% (for NO) or
5% (for CO) by neglecting other terms in the mass-balance equation. Both Tadic et al. (2017) and Conley et al. (2017)
appear to be the first to fly a spiral (or cylinder) flight pattern, which was proposed in Gordon et al. (2015) and also used in
Han et al. (2024). Conley et al. (2017) ran LES simulations to optimize the spiral radius and the number of passes. It is
demonstrated that a minimum non-dimensional radius can be determined, as

$$75 \quad R' = \frac{Rw_*}{Uz_i}, \quad (1)$$

where R is the actual radius, w_* convective velocity, U mean wind speed, and z_i boundary-layer height. A value of $R' > 0.45$
resulted in nearly constant concentration below the lowest flight path (150 m), which reduces the uncertainty due to
extrapolation of these unknown values. Using order-of-magnitude estimates of $w_* = 1$ m/s, $z_i = 1000$ m, and $U = 10$ m/s,
gives $R = 4.5$ km (as an example). Conley et al. (2017) also test the number of laps around the source required to reach
80 convergence over multiple tests and find that 15 or more laps (at a normalized radius of $R' = 0.25$) are required to repeatedly
produce the most accurate results (which is an accuracy of near 85% in this case). However, a real-life controlled release
experiment suggests that as many as 25 laps are required to reach comparable accuracy.

This study aims to optimize flights to determine emission rates from large emitting stacks in industrial complexes such as the
Canadian oil sands (Liggio et al., 2019; Li et al., 2017). These kinds of operations typically include stack emissions, dust and
85 vehicle exhaust from roadways that connect different operations, surface sources of pollution that span over a large area such
as surface mine excavation sites, and larger area sources such as tailings ponds (Baray et al., 2018; Davis et al., 2020).

Various emission scenarios (e.g., point, area sources) and tracer dispersion and transport under different meteorological
conditions were simulated using a high-resolution WRF model described in Fathi et al., 2023. The output data from this
high-resolution (with LES parameterization) WRF model is assessed here as a proxy for real-world environmental fields
90 (virtual sampling). The range of spatial and temporal variability in fields sampled by a mobile platform for top-down
retrievals can impact the accuracy of the estimates. For example, spatio-temporal variability in sampled fields is dependent
on the downwind distance and hence investigating the optimized sampling distance using model data (following Conley et
al., 2017) is desirable and can provide valuable advice in terms of observational flight planning and data processing. By
studying the output fields from several different WRF simulation scenarios, we investigate the impact of different sampling
95 strategies on the accuracy of top-down estimates and provide operational recommendations for general and specific cases.

2 Methods

2.1 Case Studies and Location

This analysis uses WRF output data described in Fathi et al. (2023). The WRF model output data span a geographical location over the northwest portion of Athabasca oil sands region, Alberta, Canada. Although three different cases were simulated in Fathi et al. (2023), we focus here on Case 1 on Aug 20 (all dates in 2013) and Case 3 on Sep 2. Case 2 on Aug 26 was a stagnant, low-wind speed case with high vertical wind shear. For this case, the vertical motion of the plume in the presence of strong wind shear resulted in plume recirculation causing significant storage within the control volume during the flight time. Hence, Case 2 was not considered suitable for the mass-balance technique (see also Fathi et al., 2021 for more discussion of this effect). The dates of Case 1 and 3 coincide with aircraft emission retrieval flights over the CNRL facility in the northwest area of the oil sands region, during the 2013 JOSM (Joint Canada-Alberta Implementation Plan on Oil Sands Monitoring) field campaign (JOSM, 2013) and they are the two flights described in detail in Gordon et al. (2015). Both cases (summer, afternoon flight times) demonstrate thermally and dynamically unstable conditions in both the measurements (Gordon et al., 2015) and model output (Fathi et al., 2023).

2.2 Model Description

Model details are discussed in Fathi et al. (2023) and are summarized here. The Weather Research and Forecasting model (WRF, version 3.9) was used with the ARW dynamical core. In this analysis, we use the velocity components (u , v , w), meteorological parameters (temperature, pressure, and **water vapour mixing ratio**), and 11 tracer scalars, corresponding to different point, line, and area emission sources (described below). ARW solves for advection of momentum, scalars, and geopotential in flux form (the governing equations).

Five nested grid domains are used in both the horizontal and vertical, with increasing horizontal resolution from 31.25 km to 50 m, and vertical resolution of 11.62 m (for the lowest 40 grid levels in the finest domain), and a time step of 0.16 s (in the finest domain). **This resolution is often referred to as “super-resolution” (Wu et al., 2021; Onishi et al., 2019; and Watson et al., 2020).** The coarsest domain was driven with North American Regional Reanalysis (NARR) GRIB (GRIdded Binary) data (at 3 h intervals, **31.25 km resolution**) from NOAA (National Oceanic and Atmospheric Administration) archives. Our WRF-ARW model configuration conserves mass within 1–5% and successfully resolves turbulent eddies at aircraft-observed scales by leveraging the full suite of large-eddy simulation (LES) options. For details of the super-resolution modelling setup, see Fathi et al. (2023).

We use 7 modeled emission locations in this analysis, which are described in Fathi et al. (2023). The locations are shown in Figure 1. These are comprised of 4 elevated (stack) sources, two small area surface sources (surface mines), and a large area source (tailings pond). The stacks (CNRL1-4) **have respective heights of 114, 54, 30, and 54 m.** The large area source (POND) is approximately 50 km², and the small area sources (MINE1 and MINE2) are 550 m × 550 m and 350 m × 550 m, respectively. Each source **in the model** emits a known amount, E_S , which can be compared to the emissions determined from

the TERRA mass-balance method, E_{Total} , discussed in Section 2.3. Emissions from each source are independent in the model and are treated separately. Each of the 4 stacks emits at the same rate and the area sources all emit at the same rate per unit area. Here we group the different emission source types together: stacks (the sum of CNRL1, 2, 3, and 4), small area sources (the sum of MINE1 and MINE2), and the large area source (POND), and we investigate each of the three groups separately. Emissions are all treated as trace gas. These results could be extrapolated to particulate emissions (which would be expected from an area source such as an open pit mine); however, dust processes such as gravitational settling and deposition are not considered here.

Meteorological and tracer values were output from the finest domain every 1-second over the area shown in Figure 1 (also extending south of what is shown in the figure to 57.15 °N). Model runs start at 09:00 local time (15:00 UTC). The Aug 20 run stops at 18:47 UTC and the Sep 2 run stops at 18:09 UTC. As discussed in Fathi et al. (2023), meteorological fields converge in under 1 hour of simulation. All analysis discussed herein starts after 16:20 UTC (80 minutes after startup) to allow sufficient model spin-up time for the meteorological fields to converge over the modelling domain and ensure that all the plumes have reached the edge of the model domain.

2.3 Mass-Balance Calculation

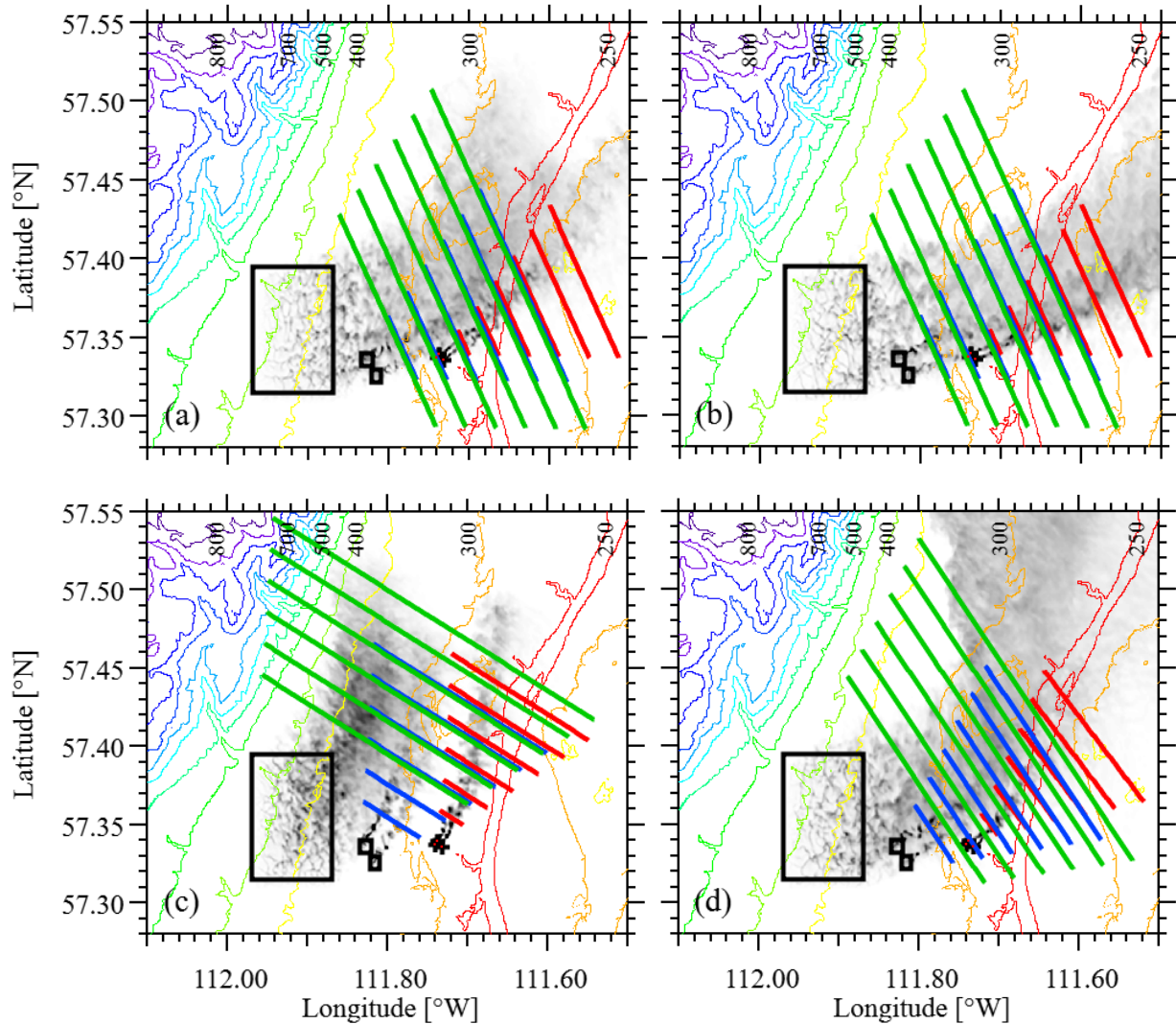
Airborne top-down emission rate retrievals are usually accomplished by flying at a distance downwind of the emission source and at several altitude levels. Although flights that are far enough downwind of a source (or over a large homogenous surface source) can assume a well mixed boundary layer and fly at a single altitude (e.g. Turnbull et al., 2009; Karion et al., 2013; Hiller et al., 2014), we restrict our analysis here to relatively short flights (~10's of kms) where the plume is not uniformly mixed and flights at multiple heights are required to characterize the plume (Fig. 1).

Following the TERRA algorithm outlined in Gordon et al. (2015) the emission rate within a control volume can be calculated as

$$E_{Total} = E_H + E_{HT} + E_V + E_{VT} + E_{VD} - E_M - E_X + S, \quad (2)$$

where E_{Total} is the total emissions rate integrated over all activities within the facility, E_H is the horizontal advective flux through the box walls, E_{HT} is the horizontal turbulent flux through the box walls, E_V is the advective flux through the box top, E_{VT} is the turbulent flux through the box top, E_{VD} is the deposition to the surface, E_M is the increase in mass within the volume due to a change in air density, and E_X is the increase in mass due to chemical changes of the compound within the box volume. As demonstrated in Fathi et al. (2021), a storage term (S) must be included to account for emissions trapped within the control volume or released from the control volume after a previous build-up. Fathi et al. (2021) demonstrate that storage/release is related to non-steady state wind conditions, changes in stability, vertical wind shear, and upwind emissions (for enclosed flight patterns). A significant part of the storage term can be due to eddies and circulation at scales comparable to the control volume or flight time. As horizontal winds decrease (or increase), the total concentration within the volume will increase giving $S > 0$ (or decrease giving $S < 0$). Very generally, the horizontal turbulence term (E_{HT}) estimates flux due to boundary-layer turbulence, while the storage term (S) estimates flux due to mesoscale turbulence. However, as

discussed in Fathi et al. (2021), storage can also include the effects of any non-steady-state conditions. For example, changes in atmospheric stability can modify the plume's buoyancy, moving the plume to different heights and resulting in changes in the horizontal advection speed of the plume.



165

170

Figure 1: Topography (meters above sea-level) of the finest model domain showing source locations for the stacks (plus symbols), two small area sources, and the large area source (black rectangles). Emissions from all stacks are followed using a single tracer in the model. Emissions from two small area sources are grouped similarly. Plumes (integrated total concentrations with arbitrary scales) are shown as instantaneous snapshots at Aug 20 16:20 (a) and 17:20 (b), and Sep 2 16:20 (c) and 17:10 (d). Flight paths are shown for each of the three source locations at downwind distances of $D = 2, 4, 6, 8, 10,$ and 12 km for the stack sources (red lines), the small area sources (blue lines), and the large area source (green lines). The model domain extends to 57.15°N , but only north of 57.30°N is shown here.

175 As past studies have shown (Kalthoff et al., 2002; Gordon et al., 2015), the most significant term in Equation 2 is the horizontal advective flux. This is calculated by first creating a 2-dimensional screen from the flight measurements (using some form of interpolation), with horizontal dimension s , and vertical dimension z , transformed from the 4-dimensional (x, y, z, t) measurements. The advective flux is then calculated as

$$E_H = \iint C U_{\perp} ds dz, \quad (3)$$

180 where s is the distance along the flight path, z is the height from the ground, C is the species concentration at each screen location (s, z) , and U_{\perp} is the wind speed perpendicular to the screen at each screen location (s, z) , calculated as $U_{\perp} = \vec{U} \cdot \hat{n}$, where \hat{n} is the unit vector (horizontal) normal to the flight path, s (positive outward). Both C and U_{\perp} are typically measured simultaneously (or close to it) during the flight, which accounts for variation in the wind pattern across the area of the screen. The simplest and lowest cost approach (i.e. least flight time) is to ignore the control volume and fly in a single screen
185 downwind of the plume (e.g. Mays et al., 2009; Cambaliza et al., 2014). A background concentration must be calculated either from an upwind pass or from the plume edges. The terms $E_V, E_{VT},$ and E_M in Equation 2 can be assumed negligible (provided there is no indication of mass on the higher levels of the flight, and no deep convection is observed). The terms $E_{HT}, E_{VD},$ and E_X can be estimated if the plume source location is known. When multiple downwind screens are used, this method can be used to estimate deposition (E_{VD}) in the area between the screens (e.g. Liggo et al., 2019; Hayden et al.,
190 2021).

To assess the upwind fluxes and to better estimate all the terms in Equation 2, the plane can fly in a repeating closed circuit at different heights to trace a 3-dimensional prism or a cylinder. In actual flights at this location (Gordon et al., 2015; Liggi
et al., 2019; He et al., 2024), rectangular “box” shapes (or a 5-sided near-rectangle with a cut corner) were flown with sides aligned with compass directions (and facility roads and layouts). In this study, we focus only on screen flights and then
195 extrapolate these results to estimate the uncertainties in enclosed flight patterns. To calculate the emission rate for an enclosed cylinder or box flight, the perpendicular wind speed (U_{\perp}) in Equation 2 must take into account the changing flight path direction.

The data (wind and concentration) along the flight path (x, y, z, t) within the model are sampled from the model values at the nearest grid location. No interpolation is done within the grid-cell or time-step. The sampling locations are then mapped to
200 screen locations (s, z) , and interpolation of the 2D screens is done with the kriging method, which is standard for multiple-path screen flights (e.g. Cambaliza et al., 2014, Gordon et al., 2015, Ryoo et al., 2019, Kim et al., 2025). The kriging algorithm used here (Wavemetrics) fits a spherical function to the variogram to determine the appropriate range value. We also compare results using an exponential variogram model and a Voronoi nearest-neighbour interpolation. In all cases, the screens are interpolated to a resolution of $40 \text{ m} \times 20 \text{ m}$ (s and z respectively).

205 Although various extrapolation methods are available to fill the values between the lowest flight path and the ground (Gordon et al., 2015), for simplicity we assume a constant value between the ground and lower flight path equal to the

concentration at the height of the lowest flight path. As discussed above, Conley et al. (2017) determine the optimized flight radius (R' in Eq. 1) for a cylindrical pattern as the minimum downwind distance at which the concentration is uniformly mixed (constant) below the lower flight path. Here, we use known model output to optimize the flight distance based on
210 downwind distance of the screen and we investigate the accuracy of this extrapolation method, and whether other extrapolation methods (e.g. linear to zero at the surface, half-Gaussian) would improve emission estimation.

The second largest term in Equation 2 is typically the storage term, although it is never (to the authors' knowledge) accounted for in mass-balance estimation. Conley et al. (2017) include the flux divergence (analogous to storage/release) in their derivation but demonstrate that it is at least an order of magnitude less than the gradient term (as estimated by the
215 advective flux) under ideal conditions. Reproducing actually flown box-flight patterns (as part of the JOSM campaign) on the same days simulated in this study (Aug 20 and Sep 2), and sampling SO_2 (primarily from stack sources), Fathi et al. (2021) found that **the ratio of the storage term to the known emission rate (S/E_S)** was -3% for the Aug 20 flights and -29% for the Sep 2 flights (negative storage is termed release and represents net loss from the control volume enclosed by the box flight after a previous build-up). Using the same model setup discussed in this paper, Fathi et al. (2023) determined the
220 storage term for a box flight enclosing all the sources with an east wall 5 km downwind of the stack locations. The **ratio of the storage term to the known emission rate (S/E_S)** for the emissions released from the 4 existing stacks (CNRL1-4), the surface mines (MINE), and the tailings pond (POND), ranged from -10.9% to -2.9% for Aug 20 and -27.5% to 15.4% for Sep 2. Hence, storage can be significant even when winds appear to be steady state, and optimization of flight parameters must consider how to reduce this uncertainty.

225 **2.4 Flight Design**

2.4.1 Flight Parameters

Screen and circuit emission retrieval flights can be flown with a variety of aircraft sizes, including UAVs (Han et al., 2024; Yong et al., 2024), small aircraft such as Cessna (Krings et al. 2018; Fiehn et al., 2020; Conley et al., 2017), or larger aircraft, such as Convair (Gordon et al., 2015; Liggio et al., 2019; Kim et al., 2025). UAV speeds range from 2 to 18 m/s, small
230 aircraft typically fly between 40 and 75 m/s, while larger aircraft flight near 100 m/s and up to 150 m/s. Sampling rates can vary from 0.5 to **as high as 10 Hz (e.g. France et al., 2021)**, depending on the instrument used, resulting in a wide variety of horizontal sampling scales. In this study, we use a sample distance of 100 m (100 m/s at 1 Hz) to fly through the model space, following the scale of actual studies done at this location (e.g. Gordon et al., 2015; Liggio et al., 2019). These results can potentially be scaled to smaller aircraft sizes (or UAVs).

235 The lowest flight path is taken as 150 m agl (above ground level), following standard restrictions (e.g. Gordon et al., 2015; Conley et al., 2017). We assume an upward flight path, starting at 150 m agl and moving upward to a new height after each circuit or screen transect. During an actual field campaign, the concentrations can be monitored in real time, and sampling can be stopped after the last transect samples only background concentration (to avoid wasted flight time). To mimic this in

model space, the aircraft flies through the model up to a height of 800 m (well above all tracer emissions), but upper
240 transects above the first background-level transect are removed from the analysis and not counted towards the total flight
time.

Multiple screens are flown at distances $D = 2, 4, 6, 8, 10,$ and 12 km downwind of the smokestack location or edge of the
line or area source. To account for plume spread, the screen length is determined as $L = L_0 + 2D \sin \varphi$, where L_0 is the
width of the line or area source perpendicular to the wind ($L_0 = 0$ for smokestack sources), and φ accounts for the spread of
245 the plume with downwind distance. Based on visual inspection of the plume spread in the model, we choose $\varphi = 30^\circ$ to
ensure the entire plume is captured under varying wind conditions. For smokestacks, this simplifies to $L = D$. Figure 1
shows the resulting screen lengths. In actual flights, the screen length would likely be determined in real time by observing
concentrations while flying through the plume.

For these screens, an initial value of the vertical transect spacing (i.e. the height between each subsequent pass along the
250 screen length) is set to $\Delta Z = 100$ m, to match the horizontal spacing. Once the screen distance is optimized, the transect
vertical spacing is optimized for that distance by analyzing flights with T values of 50, 100, 150, and 200 m. At the end of
each transect, 1 minute is added to turn the aircraft around and elevate to the next transect level (based on flight paths from
Gordon et al., 2015 and Liggio et al., 2016) but no measurements are taken during these maneuvers.

For each value of D or T , a set of 10 flights are flown to provide a statistical evaluation of the variability and uncertainty in
255 the emissions estimates. For each set of 10 flights, each subsequent flight starts 1 minute later than the start of the previous
flight. This offset is added to investigate the uncertainty in the estimated emission rate due to turbulent fluctuations with time
scale on the order of 1 to 10 mins.

Each flight begins at the most NW location at a height of 150 m agl. There are two sets of flights on each of the two days for
each of the three sources. The first set starts at 16:20 UTC. The second set starts at 17:20 UTC on Aug 20 and 17:10 UTC on
260 Sept 2. As explained above, for each set of 10 flights, each subsequent flight within the set starts 1 minute later than the
previous flight (e.g. start times = 16:20, 16:21... 16:29). To simulate turbulent fluctuations in the flight, at each 1-s timestep
of the flight, the horizontal aircraft speed is randomly offset by a Gaussian random number with a standard deviation of 3
m/s and the vertical position is offset by a Gaussian random number with a standard deviation of 1 m. These random offsets,
although potentially exaggerated compared to the variability of real flight speed or position, were found to produce visually
265 similar flight paths compared to paths shown in Gordon et al. (2015). Given that this is a very subjective comparison, we
investigate the effect of reduced offsets in Section 3.1.2 below. Although the analysis demonstrates that the effect of the
randomized offset is small (<7% change in the average horizontal advective flux), the temporal and spatial offsets ensures
that each of the 10 flights (for each D and ΔZ value) is distinct but generally sampling the same meteorological and emission
conditions.

270 2.4.2 Uncertainty Estimation

Through the statistical analysis of multiple flights, we can also assess how effective repeated flights (or multiple sampling with 2 or 3 UAVs or aircraft) are in reducing the measurement uncertainty in the emission rate estimate. Since subsequent flights may not be statistically independent, we determine the autocorrelation function of the times series of the horizontal advective flux (E_H) for each set of 10 flights. This is used to calculate the effective number of flights, n_{eff} , following Zieba
275 (2010), which is < 10 if subsequent flights are not statistically independent. This gives the effective degrees of freedom for the calculation of the mean ($n_{eff} - 1$), which can be used to calculate the expanded uncertainty of the mean, following JCGM, 2008. If we can assume that the variability within a flight set (σ) is representative of the real variability a flight would encounter under similar conditions, then we can use that value to estimate the uncertainty in a single flight estimate of E_H in the real world. Using the value of $n_{eff} = 7$ as an example, we are 95% certain that a single estimate is within 2.45σ of
280 the actual mean E_H value (Table G2 in JCGM for 6 degrees of freedom and a 95% confidence interval). If, for example, two real flights can be flown (far enough apart in time to assume they are independent measurements), then this uncertainty in the estimate of E_H is reduced by $\sqrt{2}$ to 1.41σ . It is noted that the uncertainty calculated here effectively combines our uncertainty in the variability in the flights due to a limited number of samples (approximately 26%, since an infinite number of flights would reduce 2.45σ to 1.95σ) with the actual variability between flights, which could be due to storage
285 fluctuations, interpolation/extrapolation errors, or sparse sampling.

2.4.3 Instantaneous Screens

For comparison, we also output the full model screen at one instant in time. In this case, the concentration at all grid cells along the screen (between the surface and 800 m agl) is output. This calculates all the tracer mass passing through the screen at a given time, removing the effect of spatially sampling a temporally changing environment. By sampling at the grid square
290 spacing from the surface (i.e. no lowest flight path height restriction), this removes the uncertainty associated with both kriging interpolation and extrapolation below the lowest flight path. These screens are **sampled (at the grid square spacing)** at downwind distances of $D = 2, 6, \text{ and } 10$ km. To investigate the variability of the E_H value estimated by this method (primarily associated with the storage term, S), 10 flights are flown at each distance, starting at 16:20 UTC with each subsequent screen 1 minute later. We refer to these **calculated emission rates** as “instantaneous”.
295 The instantaneous screens are also used to test and compare the image interpolation methods. In these cases, we use the flight path positions described above (s, z) and sample the concentrations at those positions from the instantaneous screens. Each series of points sampled from an instantaneous screen is then used to create an interpolated screen, which can be directly compared to the instantaneous screen at the same resolution. This allows us to isolate the error caused by image interpolation alone. We can also calculate the error associated with the extrapolation of a constant concentration below the
300 lowest flight path.

2.5 Meteorological Conditions

Figure 2 show the temperature (T) and winds (U, V) from the model at a height of 150 m above ground level for the two dates at three locations: the stacks, the centre of the small area sources, and the centre of the large area source. The flight durations are also shown for comparison (straight lines on the T -axis) for the two sets of flights on each date. The instantaneous flights (the shortest lines) span 9 minutes (e.g. 16:20, 16:21... 16:29). The longest screens downwind of the stack sources (at $D = 12$ km) span approximately 27 minutes, including 18 minutes of flight time plus 9 minutes since each of the 10 flights is offset by 1 minute each. Similarly, the longest small area and large area flight sets span 32 and 49 minutes, respectively. Screen flights closer to the source are always shorter in duration since the screen lengths are shorter, the plume tends to be lower to the ground and less transects are required to capture the entire plume.

The friction velocity (u_*) and the bulk Richardson number (Ri) demonstrate the turbulence and the stability conditions, respectively. The largest bulk Richardson number (shown in Fig. 2 as a negative value on a log scale) is $Ri = -0.49$, which demonstrates that the conditions are always turbulent and likely unstable during these model runs. Temperature rises consistently during both afternoons, by approximately 3°C on Aug 20 and 4°C on Sept 2. Although these two afternoons were chosen for their steady-state conditions, the winds can vary considerably over time and between different locations, demonstrating potential for storage and release during the flights.

2.6 Enclosed Flights

Although the single-screen flight is the most efficient way to sample emissions since it captures the greatest downwind area without expending flight time flying upwind of the emission source, there are sometimes situations where an enclosed flight path (such as a cylinder or box flight) is necessary. For a small downwind distance, it could be more economical to continue in a circle (or spiral) pattern around the source, eliminating the need for the tight turning circle at the end of each screen transect. Or the aircraft could be equipped to measure multiple pollutants (potentially from multiple sources), and a single, large, enclosed flight path can capture a volume containing all the emission sources better than a single screen much further downwind. Or there may be upwind sources of the pollutant (or a strong background value) that must be subtracted from the horizontal advective flux.

For the stack (i.e. point) sources, calculating the screen length based on an assumed $\pm 30^\circ$ lateral plume spread results in a screen length that is approximately 1/6 of a total circle circumference. The difference in distance from the source between a circle arc (radius R) and a straight line over a $\pm 30^\circ$ range is less than 7% of R . Hence the only significant differences between a spiral or cylinder flight and the downwind screens investigated here would be the extra time required to complete the remaining 5/6 of the circle for each transect (assuming no upwind sources or background concentration). For the stack emissions, we can investigate the difference in emissions estimates by using the same screen configuration, but we add a time offset after each transect to account for the time required to complete the flight path around the source.

We compare the difference between the screen flights and a circular enclosed flight pattern for a downwind distance of $D = 10$ km for the stack sources only. For the stack sources, the screen length at $D = 10$ km is $L = 10$ km. Thus, each screen transect (at a speed of 100 m/s) takes 100 seconds. For the circular enclosed flight comparison, we recalculate the flight, adding a 500 second offset to each transect to account for the time required to complete the loop. The flight time required (for all 10 circular enclosed flights) is 91 minutes in total (16:20 to 17:51 UTC), effectively spanning most of the model output duration and overlapping with both the 16:20 and 17:20 or 17:10 flight sets (Figure 2).

2.7 Ground-vehicle Sampling

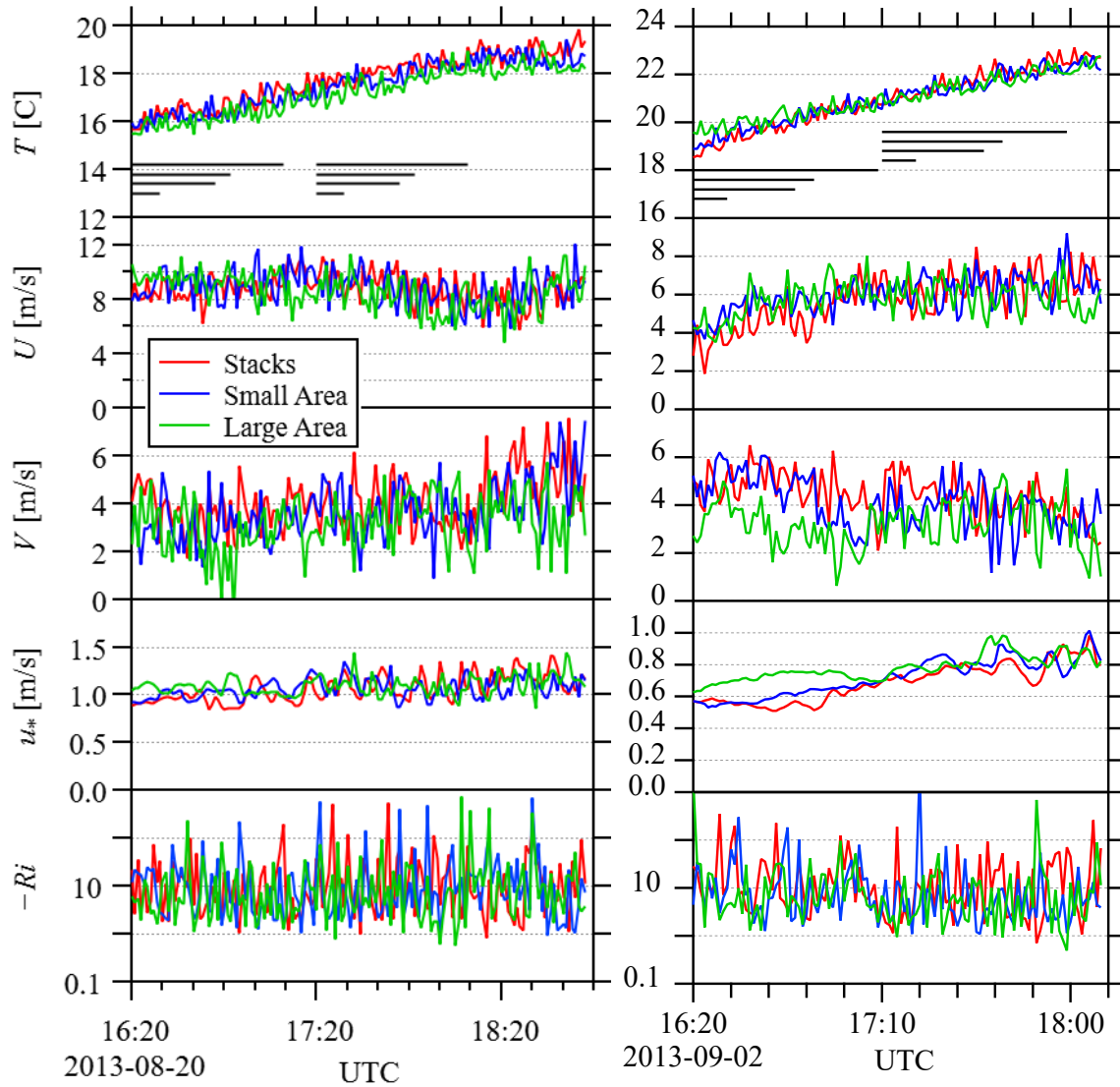
We also investigate the potential improvement to the emissions estimate through ground-based mobile vehicle concentration sampling. For the case of the Aug 20 (starting at 16:20) flight set downwind of the stack sources, we simultaneously sample concentrations at the lowest model level beneath the flight path. Although vehicle path locations are typically limited to roadways, we investigate here the highly idealized case where a car or truck can drive directly beneath the flight path of the aircraft for the duration of the flight. We assume a constant vehicle speed of 60 km/hr (16.7 m/s) and drive a single transect south-eastward from the most NW location. These values are then used in the interpolation of the screen (at $z = 1$ m) without the need to assume a profile below a height of 150 m. Results are discussed in Section 3.1.5.

2.8 Storage Variability

As discussed in Section 2.3, Fathi et al. (2021) estimated the ratio of the storage term to the known emission rate (S/E_S) based on actual flight paths and Fathi et al. (2023) estimated S/E_S for a modeled flight path for different source emissions. Since the storage term is highly variable and the effect of large-scale turbulent fluctuations can change during the time it takes to fly a screen, we investigate the variability of the storage term for various flight lengths associated with the different flight configurations. The total integrated concentration within each control volume is calculated as a time series for the model run duration on each date. For each flight configuration (3 sources, 6 downwind distances), the control volume is defined as an area enclosed by the screen on the north-east side, extending south to a latitude 2 km south of the source and west to a longitude 2 km west of source, where the 2 km buffer accounts for any upwind diffusion from the source. The time-averaged storage is then determined as the average rate of change in integrated concentration within the volume over that period, which is positive for build up of emissions within the volume or negative for release of material from the volume. The period length investigated corresponds to the average flight time for a given source at a given distance. For example, the average flight lengths for the screen 6 km downwind of the small area sources (on Aug 20, 16:20) is 700 s (i.e. approximately 7 transects of 9 km (1.5-min each) plus turning time). The average storage (over 700 s) is then calculated (within the volume enclosing the small area source up to the screen at 6 km) for each 700 s period in the entire 147 min time series (16:20 to 18:47), and the standard deviation of these values (σ_S) is determined. While this cannot give us the exact value of the storage term for each flight investigated (since the plume is sampled at different points in time and space while

the storage term is changing), this does provide a quantification of the relative uncertainty due to changing storage for different flight configurations on different dates. The resulting storage variability is discussed in Section 3.3.

365



370

Figure 2: Meteorological variables during the model runs at 3 locations: (red) stacks, (blue) centre of small area sources, (green) centre of large area source. Temperature (T) and winds (U, V) are at a height of 150 m. Friction velocity (u_*) and negative bulk Richardson number ($-Ri$) are shown. The bulk Richardson number is based on a 10-m to 150-m height difference. The straight lines on the T axis show flight durations. From shortest to longest lines, they are: 10 instantaneous flights (spanning 9 minutes), stack flights, small area flights, and large area flights.

2.9 Scaling

375 Although Conley et al. (2017) normalize R (to give R' in Equation 1), in this study we present D as dimensional (km) lengths. To compare both approaches, we non-dimensionalize the downwind distance following Equation 1 (with D' and D instead of R' and R) and investigate whether this improves the results in Section 3.4. As with Conley et al. (2017), we approximate the convective flux as $w_* = \sigma_U/0.6$, where σ_U is the standard deviation of the horizontal wind speed. The boundary-layer heights (z_i) are output from the model at the source locations. An average value of z_i is determined for each flight set and the effect of boundary-layer growth is discussed below. Using these values with the average wind speeds for each flight duration, D' is calculated for each set of 10 flights and we investigate whether this collapses the results for all cases.

3 Results and Discussion

3.1 Stack Sources

3.1.1 Optimizing Screen Flights for D

385 Figure 3 shows the calculated horizontal advection fluxes (E_H , Eq. 2) for screens at given downwind distances (D) for the 4 cases: Aug 20 at 16:20 and 17:20, and Sept 2 at 16:20 and 17:10. The fluxes are calculated for the emissions from the 4 stacks (CNRL1-4) and are normalized by these known emissions (E_S). Each calculated advection flux (E_H/E_S) is the average of 10 flights. The standard deviation of E_H/E_S from the 10 flights is shown as both error bars on the average values and absolute values (to clearly demonstrate how σ changes with D). For clarity, in the discussion below all values of E_H/E_S are given as a ratio (e.g. 1.0), while all values of the standard deviation are given as percentages (e.g. 10%).

390 At a downwind distance of 2 km the instantaneous screen captures nearly all the stack emissions, with E_H/E_S values ranging from 0.90 and 0.98. This ratio generally increases with downwind distance, except for the Sep 2 17:10 flights. Deviation from a ratio of $E_H/E_S = 1$ may be due to uncertainty in the **estimated** mean (which ranges from 0.24 to 0.35 for these results at a 95% CI), or one (or more) of the 7 other terms on the right side of Equation 2 may be non-negligible. As demonstrated in Fathi et al. (2023) there is negative mass creation in the model near the plume emission point (where concentration gradients are large) **as an artifact of diffusion and mass conservation schemes common for numerical chemical transport models near sharp gradients in concentration**. This is generally consistent with the slight underestimation near the source and the increase in E_H/E_S with downwind distance (for 3 of the 4 cases).

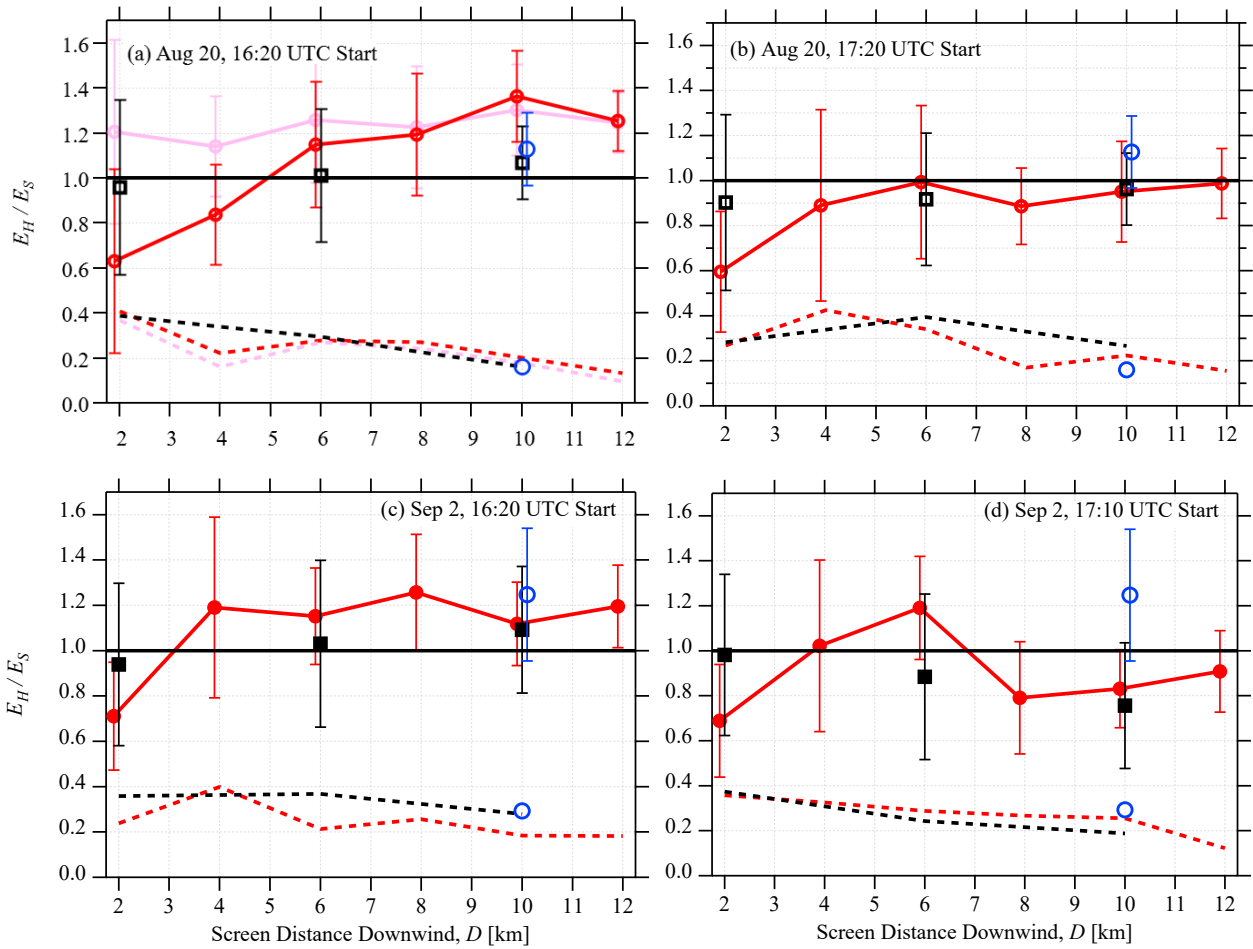


Figure 3. The variation in the ratio of horizontal advection flux (E_H) to the known emission rate (E_S) with downwind screen distance (D) for **the stack sources** for 4 flight cases: Aug 20, starting 16:20 (a) and 17:20 (b), and Sep 2, starting 16:20 (c) and 17:10 (d). The black squares are the E_H/E_S values from the instantaneous flight sets. The red circles are the flights through the model (assuming a constant value between the lowest flight path at 150-m and the surface). Error bars show one standard deviation (σ) calculated from 10 flights (offset horizontally for clarity). The dashed lines show σ as absolute values to highlight the change in σ with D . The blue circles are the same variables (E_H/E_S and σ) for 2 enclosed cylindrical flight patterns (on Aug 20 and Sep 2) starting at 16:20 and ending at 17:51. The pink lines in (a) demonstrate a case with additional measurements from a ground-based vehicle, discussed in Section 3.1.5.

At a downwind distance of 2 km, there is substantial variation between the instantaneous flights (σ ranges from 28% to 41%). Further from the source, σ generally decreases with D , with values ranging from 19% to 28% at a downwind distance of 10 km. From Equation 2, there may be some variation in horizontal turbulent flux (E_{HT}) for different flights. Fathi et al. (2023) estimated E_{HT} as $< 0.4\%$ and $< 1.8\%$ of E_S for Aug 20 and Sep 2 respectively. Since the screen captures the full

415 vertical extent of the plume, E_V and E_{VT} (flux through the box top) should be zero. There is no deposition or chemistry in the model, so E_{VD} and E_X are zero. E_M (the change in mass within the volume due to density change) is zero, since the screen is an instantaneous snapshot. Hence, this substantial variation between flights is likely due to storage, with changes in wind speed and direction temporarily changing the advection flux through the screen (i.e. accumulation or subsequent release of pollutant between the stack and the screen). The storage terms estimated for 8 flights in Fathi et al. (2021), excluding a
420 rejected flight, varied from -27% to 20% , which is comparable in scale to the variation seen between instantaneous cases here. Storage uncertainty is investigated further in Section 3.3.

For the non-instantaneous flights, which include uncertainty due to kriging interpolation and the extrapolation below the lowest flight path height in addition to the uncertainty of storage, the emission rate near the source (at $D = 2$ km) is underestimated by the horizontal advective flux in all cases (ranging from 0.60 to 0.71). Further from the source, at $D = 6$
425 km, the emissions are either nearly correct (0.99) or overestimated (up to 1.19). Beyond $D \geq 8$ km, the estimations vary considerably for different cases (ranging from 0.79 and 1.37). Much of this underestimation and overestimation is likely due to the extrapolation to the surface below the lowest flight path. Figures 4a-d show the profiles of the instantaneous flights, averaged for all 10 flights across the entire flight length. At $D = 2$ km, the plume concentration below 150 m increases with concentration towards the surface, which results in an underestimation of the emission rate (i.e. a lower E_H/E_S value is
430 estimated by the assumed below 150-m concentration relative to what would be determined with the actual below 150-m concentrations). At $D = 6$ km, there is some decrease in concentration towards the surface in 3 of the 4 cases, which results in an overestimation of E_S for that flight. At $D = 10$ km, the concentration is nearly constant with height for the Sep 2 flights, although there is still substantial variability for the Aug 20 flights.

The standard deviation of E_H/E_S generally decreases with downwind distance, from as high as 41% at $D = 2$ km to 12% at
435 $D = 12$ km. The standard deviations of the instantaneous, known flights for the same downwind distances is similar in magnitude to the variability in the flown sampled flights, suggesting that no substantial variability is added due to either the extrapolation below the lowest flight path, the kriging interpolation of the sparse sampling, or the sampling over an extended period of time (as opposed to an instantaneous snapshot). The decrease in variability with downwind distance suggests that uncertainty in individual flight estimations can be reduced with greater downwind distance, likely due to increased mixing
440 and dispersion with downwind distance and the resulting smoothing of the plume across a larger area. In a real-world scenario, there may be additional error due to noise in the concentration measurements, particularly for concentrations with a high background level. In these cases, moving further downwind (where the concentration enhancements above background due to the plume are much smaller), may result in a relative increase in error.

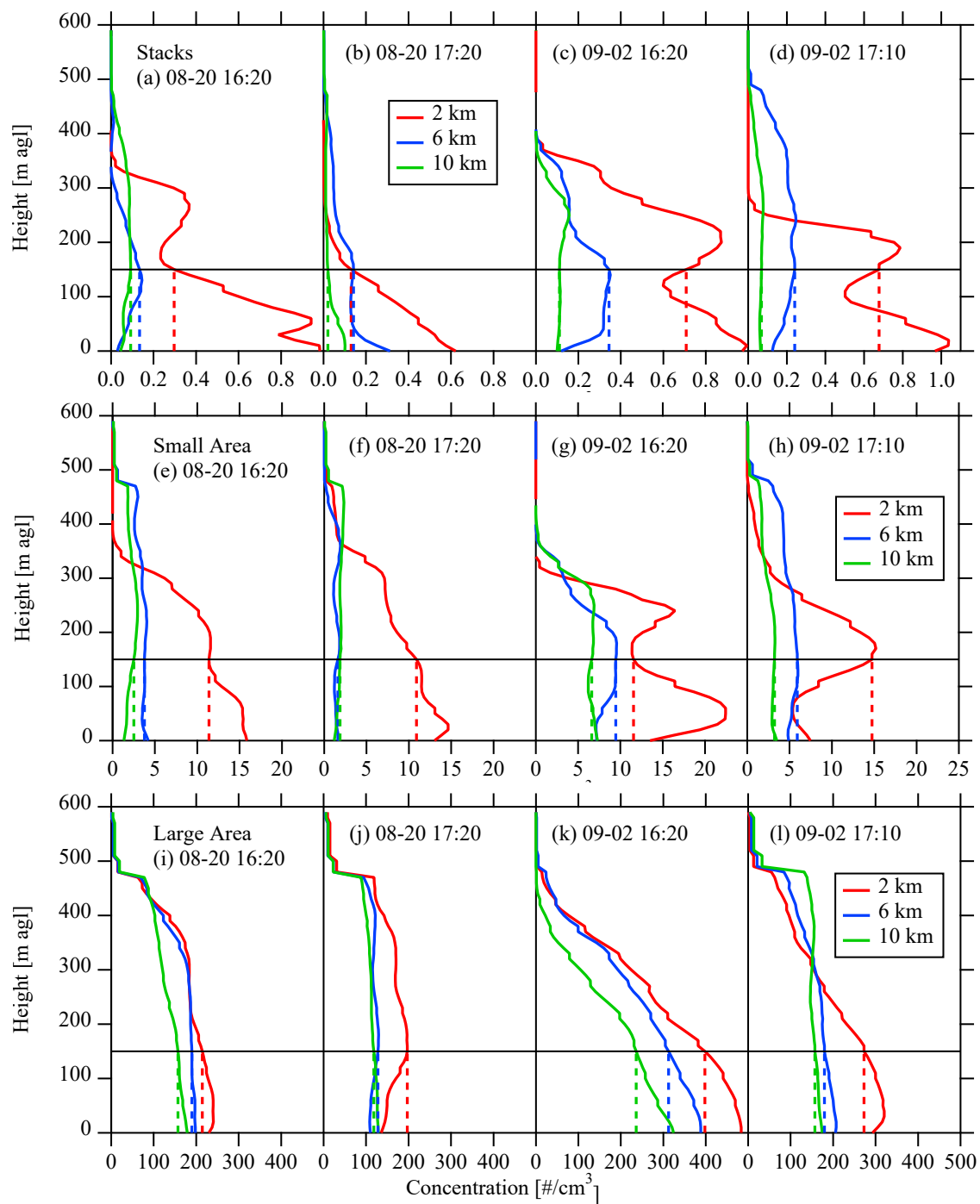


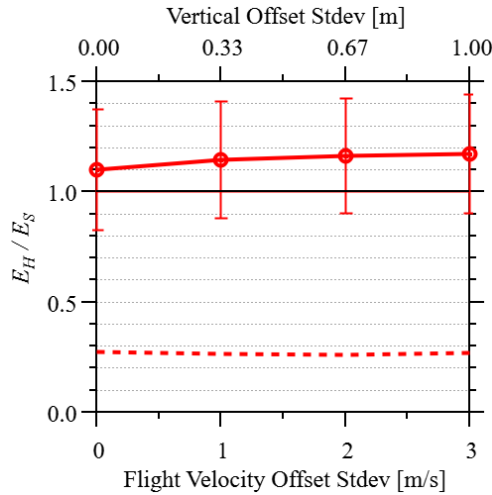
Figure 4. The concentration profiles from the instantaneous screens for the 4 flight cases and 3 source types at various downwind distances. These profiles are ensemble averages of 10 flight profiles averaged across the flight length (L) at each height. The dashed lines compare constant concentration below the lowest flight path (at $z_l = 150$ m).

The non-instantaneous emission estimates may also be higher than the instantaneous emission estimates due to oversampling of a vertically moving plume. If the plume is moving in the same direction as the sampling (upwards in these cases), then the aircraft can sample the same plume multiple times. Conversely an opposite moving plume (downward for upward sampling) will result in under-estimation relative to the instantaneous estimates. **This is investigated in Section 3.1.4 below.** This effect should be reduced with downwind distance as the plume becomes more vertically mixed and spread across a larger height range.

The results demonstrate that it is difficult to determine an optimal flight distance, since there are multiple criteria that include optimization of E_H/E_S , reduction of σ , or correct extrapolation below the lowest flight path, and it will depend on the goals of the investigation. Generally, flying too close to the source ($D = 2$ km) results in an underestimation of the emission rate. For $D \geq 4$ km, the variation between flights decreases with distance, reaching approximately half its value at 10 km (relative to the value at $D = 4$ km). Flying at a downwind distance of $D = 10$ km, generally results in a constant concentration below the lowest flight path, but the results are still inconsistent at this distance. At a distance of $D = 10$ km, the emission rate at $D = 10$ km varies from 0.83 to 1.37, and the uncertainty in the estimate from a single flight (based on the variability between flights) is as high as 60% (2.36σ , corresponding to the value of $n_{eff} = 8$ for these cases, JCGM, 2008).

3.1.2 Sensitivity to Random Offsets

As discussed in Section 2.4, at each 1-s timestep of the flight, the horizontal aircraft speed is randomly offset by a Gaussian random number with a standard deviation of 3 m/s, and the vertical position is offset by a Gaussian random number with a standard deviation of 1 m. To assess the sensitivity of the results to the scale of the offsets, we rerun the analysis for the set of flights on Aug 20 flight (at 16:20) at $D = 6$ km with both horizontal speed and vertical position offsets (3 m/s and 1 m respectively) simultaneously modified by a factor of 0 (i.e. no offset), 1/3, and 2/3. The resulting changes in estimated E_H/E_S and the variability (σ) are shown in Figure 5 (in addition to the 3 m/s and 1 m offsets used throughout the study). Using an evenly spaced, elevation-following grid with no offsets give a value of $E_H/E_S = 1.10$ with $\sigma = 28\%$. Adding a small amount of random offset (a factor of 1/3) to the grid increases E_H/E_S to 1.15. The offsets higher than that (factors of 2/3 and 1) both give $E_H/E_S = 1.17$. The difference in variability between flights within the flight set is $< 1\%$. Hence, although there is a slight difference between no random offsets (even grid spacing) and the inclusion of random offsets (E_H/E_S of 1.10 versus 1.15), the results are not sensitive to the size of the offset over the range of values investigated here.



480 **Figure 5. The variation in the ratio of horizontal advection flux (E_H) to the known emission rate (E_S) with change in the random offsets along the flight path for the Aug 20 flight set starting at 16:20. Error bars show one standard deviation (σ) calculated from 10 flights and the dashed lines show σ as absolute values.**

3.1.3 Optimizing Screen Interpolation

485 As shown in Figure 3, the estimation of E_S is generally higher in the non-instantaneous flight sets, relative to the instantaneous flight sets, for $D \geq 6$ km, but lower in the non-instantaneous flight sets for $D = 2$ km. This may be due to the kriging interpolation causing an overestimation of the screen concentrations. To test the interpolation, we sampled the instantaneous screens using the non-instantaneous flight path positions, allowing us to compare the interpolated screens with the high-resolution model output screens. We applied the same extrapolation of a constant concentration for heights below
 490 150 m. The average concentration is then calculated from the interpolated screens, $\langle C_K \rangle$, which can be compared with the average concentration for the model output screens, $\langle C_M \rangle$. The ratio of $\langle C_K \rangle$ to $\langle C_M \rangle$ is shown in Figure 6, separated into the averages above 150 m and below 150 m (where the concentration is assumed constant). For simplicity, we only compare 2 cases: Aug 20 and Sep 2 with 16:20 flight start times.

The differences between the different interpolation methods are small relative to the errors in the interpolation at different
 495 downwind distance, D . For $z > 150$ m, kriging with the spherical variogram model gives a slightly better average ($\langle C_K \rangle / \langle C_M \rangle = 1.07$ for all downwind distances on Aug 20 and $\langle C_K \rangle / \langle C_M \rangle = 1.01$ for Sep 2, versus 1.08 and 1.01 respectively for an exponential variogram model, and 1.10 and 1.03 respectively for the Voronoi nearest neighbour). For the spherical model, the results are also not sensitive to the goodness of fit of the variogram model. For examples, for the Aug 20 values for $z > 150$ m, halving or doubling the range value of the variogram model changes the average value of
 500 $\langle C_K \rangle / \langle C_M \rangle$ by less than 2%. Hence, the choice of interpolation method and the details associated with those choices seems to be less consequential than the changes in the sparseness of the sampling at different downwind distances.

The interpolation for $z > 150$ m generally overestimates the actual concentration and shows high variability between flights when close to the source ($D = 2$ km). Further downwind ($D \geq 6$ km), the interpolation is significantly improved and the variability between flights is reduced, with values of $\langle C_K \rangle / \langle C_M \rangle = 1.00$ and $\sigma = 6\%$ for the Aug 20 16:20 flights, and $\langle C_K \rangle / \langle C_M \rangle = 1.01$ and $\sigma = 3\%$ for the Sep 2 16:20 flights (both at $D = 10$ km with the spherical kriging).

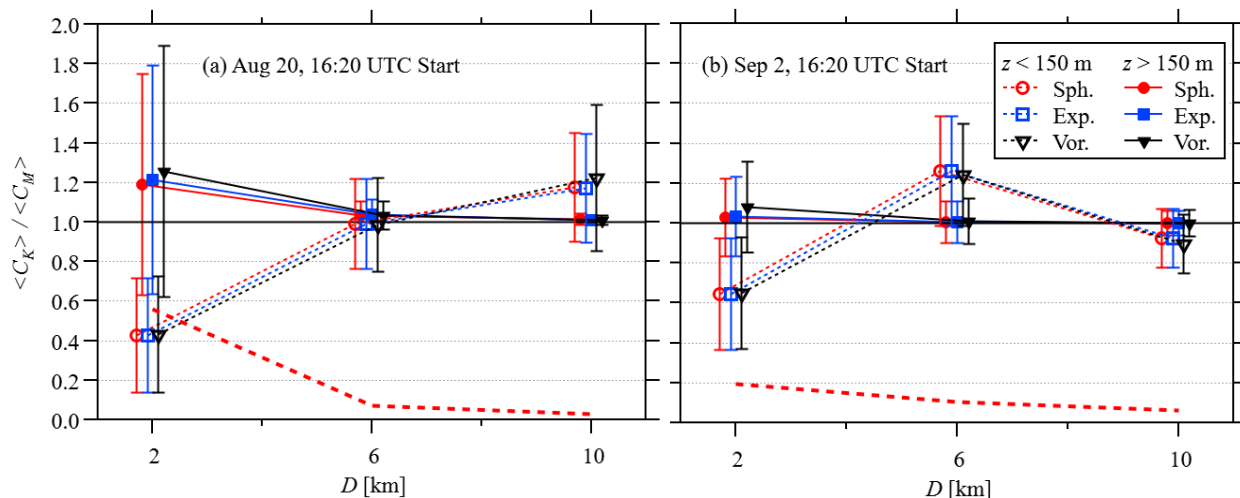


Figure 6. A comparison of average concentration from the instantaneous screens (at downwind distance, D) $\langle C_M \rangle$, to the average concentration from an interpolation of those flights with sparse sampling $\langle C_K \rangle$ downwind of stack sources (given as ratio $\langle C_K \rangle / \langle C_M \rangle$). The averages are separated into below and above 150 m (open symbols with dotted lines, and closed symbols with solid lines, respectively), where the below 150 m concentrations are assumed constant (see Fig 4). Three interpolation methods are compared: kriging with a spherical variogram model (red circles), kriging with an exponential variogram model (blue squares), and Voronoi nearest-neighbour (black triangles). The markers are offset slightly for clarity. The standard deviations of the 10 flights (σ) are shown as error bars, as well as red dashed lines for the spherical kriging (> 150 m) only. Results are shown for the Aug 20 (a) and Sep 2 (b) 16:20 flight sets, corresponding to Fig. 3a and c, respectively.

The total interpolation errors appear correlated with the difference between the instantaneous and non-instantaneous flight set emissions estimates shown in Figures 3a and c. For example, in Figure 3a, for the Aug 20 16:20 flight set at $D = 2$ km, $E_H/E_S = 0.63$ for interpolated, non-instantaneous flight set, compared to $E_H/E_S = 0.96$ for the instantaneous flight set. Figure 6 for the same flight set (at $D = 2$ km) shows an underestimation with $\langle C_K \rangle / \langle C_M \rangle = 0.43$ for $z < 150$ m and $\langle C_K \rangle / \langle C_M \rangle = 1.19$ for $z > 150$ m, suggesting a net underestimation (although the relationship between concentration and advection flux is also influenced by wind speed and the plume maybe not be evenly distributed between below and above 150 m). Similarly, for most other distances shown in Figure 6, an underestimation (or overestimation) in $\langle C_K \rangle / \langle C_M \rangle$ is generally associated with a similar scale underestimation (or overestimation) in E_H/E_S for the non-instantaneous flight sets relative to the instantaneous flight sets (which are not interpolated). This implies that the sparseness of sampling is a

significant source of error for interpolation close to the stack sources ($D = 2$ km), while further downwind ($D \geq 6$ km), there can be significant errors due to the extrapolation of a constant concentration below 150 m (as discussed in Section 3.1.1 and shown in Figure 4).

3.1.4 Optimizing Screen Flights for ΔZ

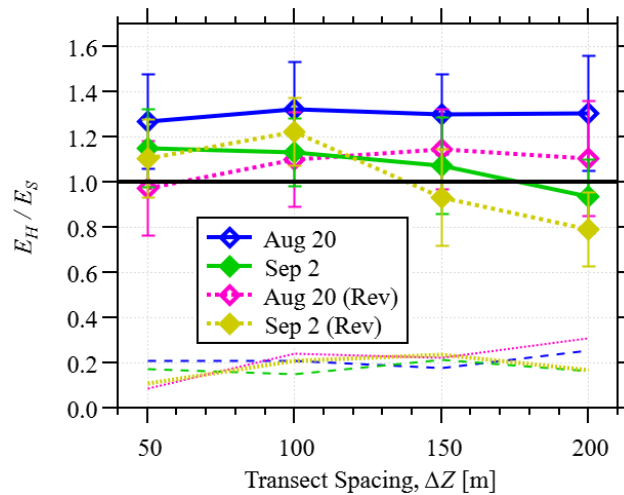
530 To further optimize the emission estimation as a function of flight time, we test the sensitivity of E_H/E_S to the vertical spacing of the transects at a downwind distance of $D = 10$ km. We compare 2 cases: Aug 20 and Sep 2 with 16:20 flight start times. As shown above (Section 3.1.3), the errors associated with interpolation (above 150 m) at a distance of $D = 10$ km are small and it may be possible to increase spacing between flight paths without significantly increasing the error. Figure 7 demonstrates the variation in E_H/E_S with transect spacing. For the Aug 20 flights, emissions are overestimated by a

535 factor between 1.27 and 1.32 with no dependence on ΔZ . For the Sep 2 flights, the emissions estimate ratio decreases with transect spacing from 1.15 at $\Delta Z = 50$ m to 0.94 at $\Delta Z = 200$ m. The variability shows no strong pattern with ΔZ and is lowest at a 150-m spacing (18%) for the Aug 20 flights, and at a 100-m spacing (15%) for the Sep 2 flights. For the Aug 20 flights, there is little dependence on ΔZ for either E_H/E_S and σ , suggesting that spacing could optimally be increased to 150 m or 200 m to reduce flight time; however for the Sep 2 flights, the ratio E_H/E_S changes significantly with increased

540 spacing, suggesting that spacing of $\Delta Z > 100$ m will modify the emissions estimation and result in underprediction. The transition from overestimation at small spacing to underestimation at larger spacing could be due to vertical movement of the plume opposite to the sampling direction, resulting in transects missing the plume centre at larger spacing. To investigate this, we repeat the flight sets using the same flight paths with the directions reversed (i.e. top-to-bottom). In these cases, the flight begins at 16:20 (for the first flight in the sets) at the highest point and each flight samples at identical

545 locations in the opposite direction, finishing at the lowest point at a height of 150 m. The reversed direction results in significant improvement in the estimation of E_H/E_S for the Aug 20 flight sets (especially at smaller transect spacing), but increased error for the Sep 2 flight sets. In both cases, the variability between flights in each set is reduced for a transect spacing of $\Delta Z = 50$ m, but is slightly higher than the variability of the bottom-to-top flight sets with $\Delta Z \geq 100$ m. As mentioned in Section 2.4, real flights are often flown in an upward direction so that the vertical extent of the plume can be

550 determined while flying. While it is difficult to know the vertical extent of the plume beforehand (which would be required for a flight in the downward direction), these results demonstrate the potential advantage of flying once in the upward direction, followed by a subsequent flight back in the downward direction.



555 **Figure 7.** The variation in horizontal advection flux (E_H) to the known emission rate (E_S) with transect spacing (ΔZ) for both the Aug 20 (blue, open symbols) and Sep 2 (green, closed symbols) **stack source** cases with 16:20 flight set start times. Error bars and dashed lines show one standard deviation (calculated from the set of 10 flights). The flight sets are repeated along the same flight paths with a reversed direction (i.e. starting at the top and ending at a height of 150 m) for Aug 20 (magenta, open symbols, dotted lines) and Sep 2 (yellow, closed symbols, dotted lines).

560 3.1.5 Adding Ground-based Vehicle Measurements

Figure 4 demonstrates that there can be considerable error associated with the assumed concentration profile below the lowest flight path of 150 m. As discussed in Section 2.4, in some situations, it may be possible to measure concentrations at ground level with a mobile measurement platform on a car or truck. With these surface-level measurements, the assumption of a constant profile below the height of 150 m is no longer necessary, and the screen can be interpolated using these additional measurement values. Resulting emissions estimates for the Aug 20, 16:20 flight set augmented by ground-based vehicle measurements are shown in Figure 3a. The horizontal advective flux with ground-based measurements consistently overestimates the emission rate for all downwind distances, with values of E_H / E_S ranging from 1.14 to 1.30 for $2 \leq D \leq 12$ km. This demonstrates that the underestimation of the horizontal advective flux close to the stacks ($D < 6$ km) with an assumed constant concentration below 150 m is predominantly due to a large amount of the plume being below the lowest flight path, as was shown in Figures 4 and 6. Further, the variability between flights is consistently reduced by between 1% and 6%. The results demonstrate significant value is obtaining surface-level measurements where possible, so that extrapolation below the lowest flight path is not required.

3.1.6 Comparing Enclosed Circular Flights

575 The results from the screen flights show that different conditions at different times of day can lead to error in the emissions estimation, most likely due to storage and release. As discussed above, sometimes enclosed flight designs are necessary. The enclosed flight designs extend the flight time due to the time required to complete the circuit. For our investigated cases here, 2 circular enclosed flights span the flight times of the two screen flight times on each day. On Aug 20, the 16:20 screen flight at $D = 10$ km (Fig. 3a) overestimates the emissions (1.37), while the 17:20 screen flight (Fig. 3b) underestimates the emissions (0.95). The circular enclosed flight (Figs. 3a and b) is in the middle of these values (1.13), as might be expected since the sampling is spread out over a longer time. However, this is not the case for the Sep 2 flights. On Sept 2, the 16:20 screen flight at $D = 10$ km (Fig. 3c) similarly overestimates the emissions (1.12), while the 17:10 screen flight (Fig. 3d) underestimates the emissions (0.83), but the circular enclosed flight (Figs. 3c and d) overestimates the emissions (1.26) more than the 16:20 screen flight. For both days, the variability (16% and 29%) is not substantially different from the variability of the screen flights. Hence, based on this analysis, we cannot conclude that the longer sampling time of the enclosed circular flights modifies the sampling efficiency in any predictable way.

3.2 Area Sources

3.2.1 Optimizing Screen Flights for D

590 The analysis described above was repeated for the small area (mines) and large area (tailings pond) sources. These sources emit uniformly from the surface within the areas shown in Figure 1. The resulting horizontal advective fluxes (normalized by the known emission rates) are shown for the small area sources in Figs. 8a-d and for the large area source in Figs. 9a-d. The instantaneous results are inconsistent for the different sources and flights, suggesting that storage may affect the advective fluxes significantly. For the small area sources (Figs. 8a-d), the instantaneous flight horizontal advective fluxes underestimate (or slightly overestimate) the emission rate close ($D = 2$ km) to the source, ranging from 0.74 to 1.01. Beyond this distance, E_H/E_S ranges from 0.87 to 1.15. The non-instantaneous flights closely estimate the emissions in most cases, except for the Sep 2 16:20 case, where the emissions are overestimated. For the large area sources on Aug 20 (Figs. 9a-b), the emissions estimates are generally consistent, ranging from 0.91 to 1.18 (for both instantaneous and non-instantaneous flights). The Sep 2 flights (Figs. 9c-d) show a strong dependence on D , with both instantaneous and non-instantaneous flights showing similar values. Opposite patterns are seen for the Sep 2 16:20 flights (Fig. 9c), emissions are overestimated near the source for $D < 10$ km and underestimated for $D \geq 10$ km. For the Sep 2 17:10 flights (Fig. 9d), emissions are nearly 1.0 near the source for $D \leq 4$ km, underestimated for $6 \leq D \leq 10$ km and overestimated at $D = 12$ km. This implies that high variability in winds in these cases is leading to storage and release, resulting in build-up and subsequent release of pollutants at different distances downwind of the source. The relatively good agreement between instantaneous and non-instantaneous estimates implies that vertical motion of the plume does not result in over- or under-sampling.

605

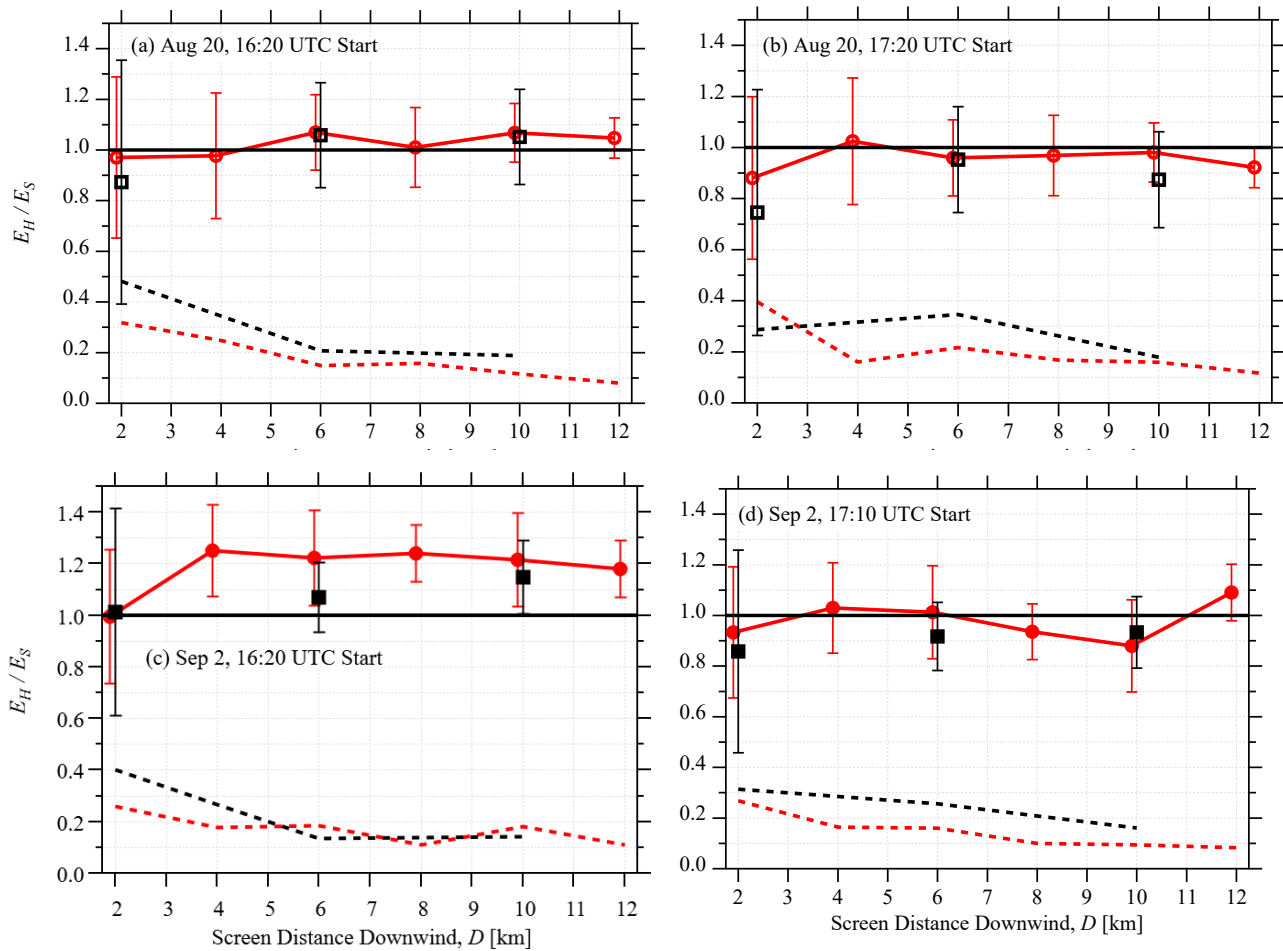


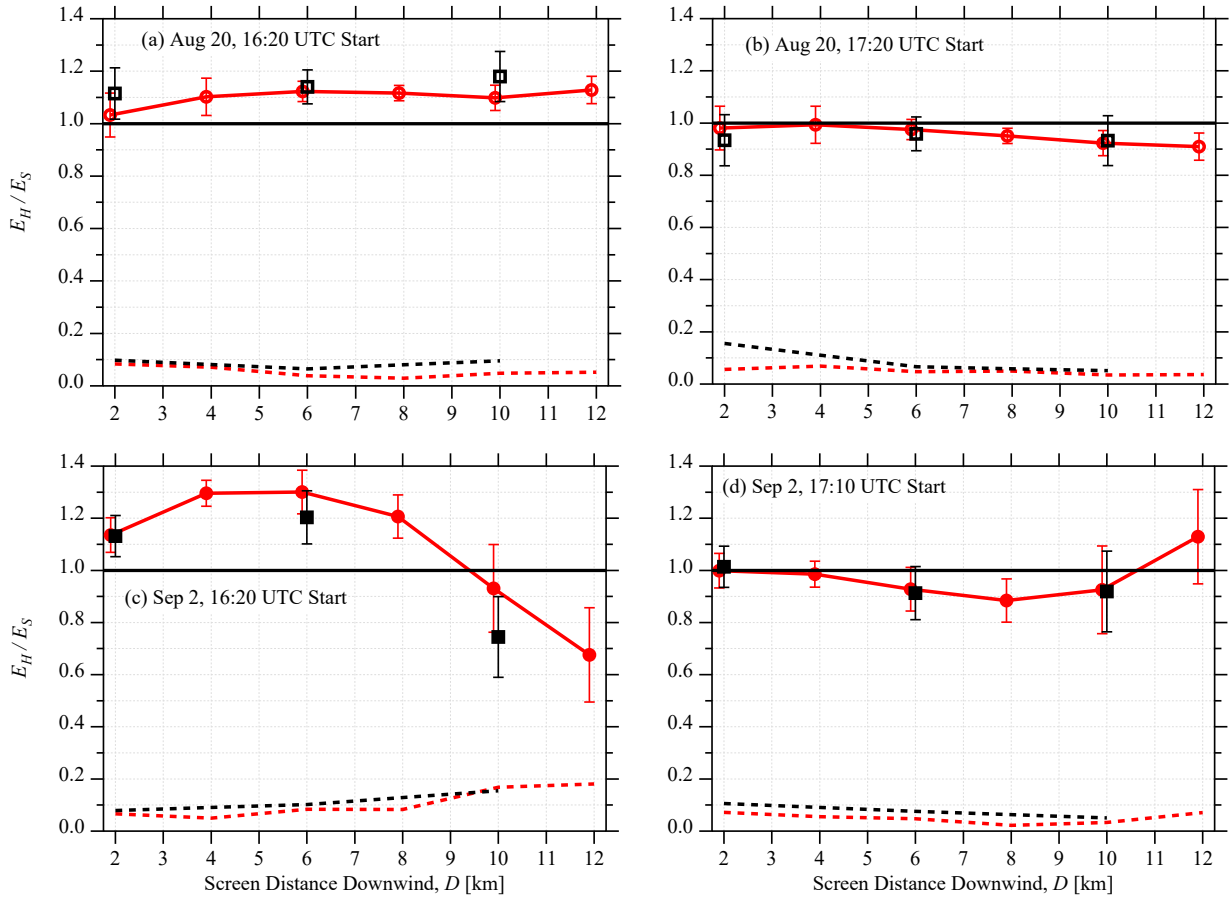
Figure 8. As Figure 3 for the flights downwind of the small area sources. Error bars and dashed lines show one standard deviation (calculated from 10 flights).

610

For the small area sources (Figs.8a-d), the variability between the flights is consistently reduced with distance from the source, ranging from 26% to 48% at $D = 2$ km to between 8% and 12% at $D = 12$ km. The variability of the large area source measurements is much lower and does not consistently decrease with D , with values ranging from 2% to 13%. The lower variation for the large area source is expected since the wide plume from such a large area would be much less susceptible to wafting and the smaller-scale variation due to local wind effects. This indicates that a single flight sampling a large area source shows substantially less uncertainty relative to a single flight sampling small area sources. For example, at $D = 6$ km, the uncertainty in the estimate from a single flight (based on the variability between flights) is 20% for the large area source, compared to 51% for the small area sources (2.36σ , corresponding to the value of $n_{eff} = 8$ for these cases, JCGM, 2008). Additionally, since D is defined as distance from the edge of the area source (as is necessary to sample the entire source area), emissions from the upwind side of the area source will have had more time to mix relative to the

620

emissions from the downwind side of the area source. Hence, it would be expected that larger area sources have smaller uncertainties for similar D values relative to small area sources.



625

Figure 9. As Figure 3 for the flights downwind of the large area sources. Error bars and dashed lines show one standard deviation (calculated from 10 flights).

Concentration profiles are shown in Figure 4(e-l) from the instantaneous area source **sampling**, where they are compared to the extrapolation of a constant concentration below the lowest flight path. For the small area sources (Figs. 4e-h), the concentration is nearly constant below 150 m at $D = 6$ km for Aug 20, but it is overestimated by the constant extrapolation at $D = 6$ km for Sep 2. At $D = 10$ km, the concentration is nearly constant for all except the Aug 20 16:20 case, where it is overestimated by the extrapolation. For the large area source, the profiles for the Aug 20 flights (Figs. 4i-j) approach constant below the lowest flight path at $D = 6$ km; however, at 10 km downwind the concentration increases toward the ground for the 16:20 flights. For the Sep 2 flights at 16:20 (for the large area source), the profiles (Fig. 4k) do not deviate from an exponential increase towards the surface at all distances, while for the 17:10 flights, they approach nearly constant at

635

$D = 10$ km (with a slight underestimation by the extrapolation). It would be expected that an underestimation due to extrapolation (most prominent for the Sep 2 17:10 flights) would result in an underestimation of the emission rate for the non-instantaneous flights (relative to the instantaneous flights); however, this is not seen in Figure 9c, where the instantaneous advection flux is lower than the non-instantaneous advection flux (which includes the extrapolation).

As with the flights sampling the stack sources, it is difficult to determine an optimized downwind distance for these flights. For the small area sources, the minimum distance with consistent emission estimation, minimum variability, and close to constant concentration below 150 m is $D = 6$ km; however, the non-constant concentrations below 150 m during the Sep 2 flights (at $D = 6$ km) suggests that the optimized value of D may be further downwind in some circumstances. For the large area sources, there is little variation in the concentration profile shape with downwind distance and the variance between flights is relatively small and independent of downwind distance. For this source **and these atmospheric conditions**, we can suggest an optimum downwind distance of $D = 4$ km. However, it is noted that, for both sources, the horizontal advection flux (E_H) differs significantly from the known emission rate (E_S), with factors between 0.96 and 1.22 for the small area sources (at $D = 6$ km) and between 0.99 and 1.30 for the large area sources (at $D = 4$ km). The overestimation **could be associated with** negative storage (release).

3.2.2 Optimizing Screen Flights for ΔZ

Using these optimal downwind distances (6 km and 4 km), we investigate the change in estimated emissions with transect spacing, ΔZ using only the 16:20 flights. For the small area source (at $D = 6$ km), there is no change in E_H/E_S (≈ 1.06) with ΔZ for the Aug 20 flights (Fig. 10a); however, the variance between flights increases from 11% at $\Delta Z = 50$ m to 19% at $\Delta Z = 200$ m. For the Sep 2 flights, E_H/E_S decreases with increasing ΔZ , from 1.29 to 1.02, and the variance is lower at $\Delta Z = 50$ m (10%) and highest at $\Delta Z = 100$ m (20%). These results suggest that the uncertainty due to variation between flights can be minimized with a 50 m spacing; however, the emission rate estimation for the Sep 2 flights at this spacing is high ($E_H/E_S = 1.29$). Increasing the spacing to 200 m will reduce the flight time by a factor of 4 but nearly doubles the uncertainty due to variation between flights.

The variation of E_H/E_S and σ with ΔZ for the large area source (Fig. 10b) is similar to the variation seen for the small area source. For the Aug 20 flights, E_H/E_S increases with ΔZ , from 1.08 at $\Delta Z = 50$ m to 1.15 at $\Delta Z = 150$ m and the variance increases from 6% at $\Delta Z = 50$ m to 10% at $\Delta Z = 200$ m. For the Sep 2 flights, E_H/E_S decreases with increasing ΔZ , from 1.31 to 1.26, and the variance ranges from a minimum of 4% at $\Delta Z = 50$ m to $\sim 7\%$ for other values. Similar to the small area source, the spacing is optimized (based on variation between flights) at 50 m or 100 m but increasing the spacing to 200 m increases the uncertainty from 6 to 10% (Aug 20) or 4% to 6% (Sep 2), which could be acceptable depending on the required accuracy and the cost of flight time.

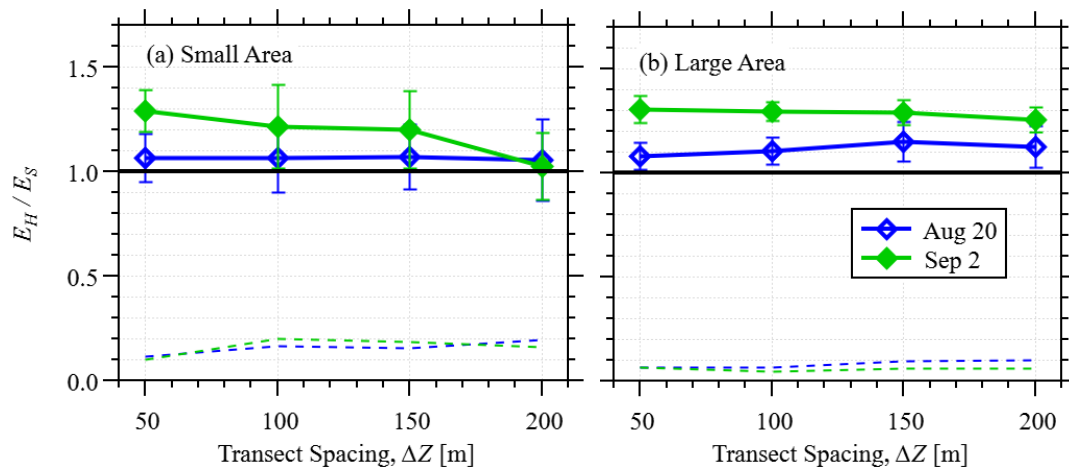
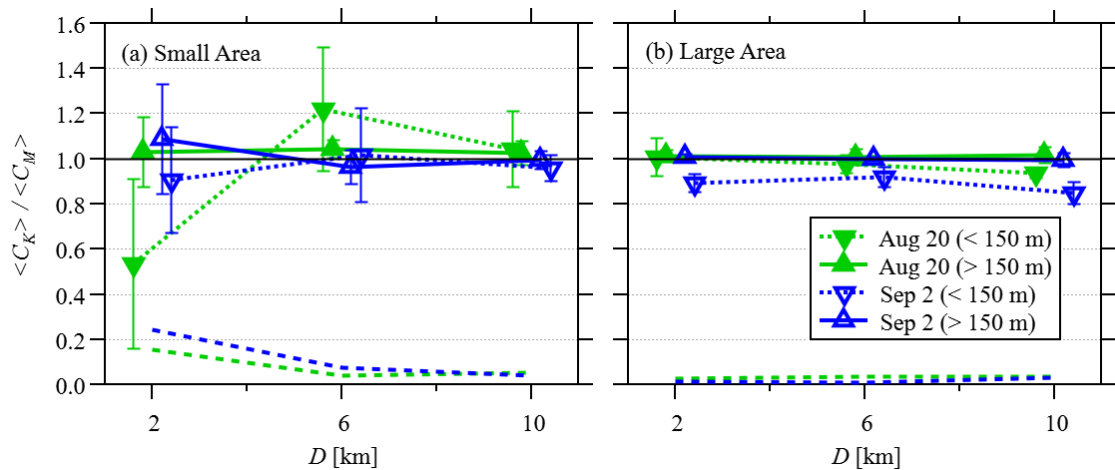


Figure 10. As Figure 7 for the flights downwind of the small (a) and large (b) area sources **for the flights starting at 16:20 only.** Aug 20 shown as blue, open symbols, and Sep 2 shown as green, closed symbols.

670 3.2.3 Optimizing Screen Interpolation

We repeat the investigation of the interpolation described in Section 2.4.3 and 3.1.3 for the small and large area sources. Here we only investigate the kriging interpolation with the spherical variogram model, having demonstrated small differences between the different interpolation methods in Section 3.1.3. Results for the small area source are similar to the results for the stack sources shown in Figure 11. Close to the source ($D = 2$ km), there is overestimation in the interpolated concentration for $z > 150$ m, and significant underestimation of the extrapolated concentration for $z < 150$ m. Further from the source ($D \geq 6$ km), the average ratio (for each flight set) of interpolated to actual concentration ($\langle C_K \rangle / \langle C_M \rangle$) for $z > 150$ m varies from 0.96 to 1.04, while the extrapolated concentration below 150 m shows significant errors (with $\langle C_K \rangle / \langle C_M \rangle$ as high as 1.22). In all cases, the variability between flights decreases with downwind distance, ranging from 4 to 7% for the $z > 150$ m interpolation for $D \geq 6$ km. For the large area sources, there is much less error in the interpolation above 150 m, relative to the error in the interpolation from the stack or small area sources. Average values of $\langle C_K \rangle / \langle C_M \rangle$ range from 0.99 to 1.02, and the variability between flights is less than 4% for all downwind distances. There is significant underestimation of the extrapolated concentration below 150 m, especially for the Sep 2 flight sets, which was previously demonstrated in Section 3.2.1 (e.g. Fig. 4k).



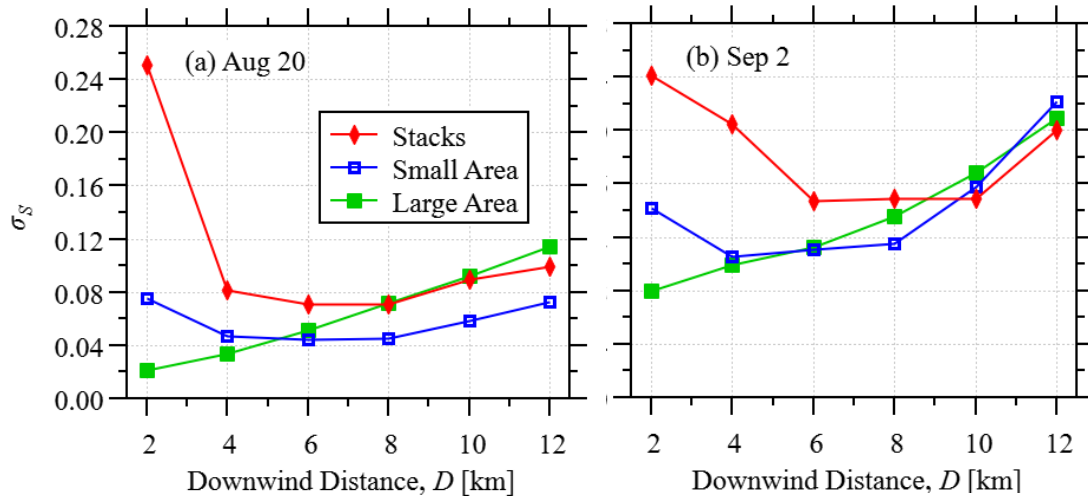
685 **Figure 11. A comparison of average concentration from the instantaneous screens (at downwind distance, D) $\langle C_M \rangle$, to the average**
concentration from an interpolation of those flights with sparse sampling $\langle C_K \rangle$ downwind of stack sources. The averages are
separated into below (downward triangles with dotted line) and above (upward triangles with solid lines) 150 m, where the below
150 m concentrations are assumed constant (see Fig 4). The markers are offset slightly for clarity. Results are shown for (a) the
small area sources and (b) large area source, for the Aug 20 (green solid triangles) and Sep 2 (blue open triangles) 16:20 flight sets.
690 **The standard deviations of the 10 flights (σ) are shown as error bars, as well as dashed lines (for > 150 m only).**

3.3 Storage

We calculate the variability in the storage term (σ_S) for the volume defined by each flight configuration (3 sources, 6
downwind distances), for the two flight dates, as discussed in Section 2.8. The two dates investigated use the flight
695 configurations for the flight sets starting on Aug 20 at 16:20 (Fig. 1a) and the flight sets starting on Sep 2 at 16:20 (Fig. 1c).
The resulting variabilities in S/E_S as a function of D (using the average flight length for that flight set) are shown in Figure
12. Generally, for the stack and small area sources, the variability in the storage term is minimum between $D = 6$ and 8 km,
while the variability in the storage term for the large area source increases with D . For the stack and small area sources, the
higher σ_S at small D is likely because these flights take less time (typically 1 to 2 min) which leads to a higher variability
700 between flights since each flight is a snapshot of a changing large-scale flow field. This effect is more pronounced for the
stack sources, relative to the small area sources, and the effect is not seen for the large area sources, since there would likely
be more variability in a thinner wafting plume from stacks or small area sources compared to the spread-out plume
associated with a large area source. The higher σ_S at large D may be due to the larger volume enclosing the source and
plumes, which encloses large-scale eddies and circulation, offsetting the reduced variability due to the longer flight
705 durations.

The autocorrelation of the storage rate (S) time series (which is 147 min and 109 min long for the Aug 20 and Sep 2 dates
respectively) gives a timescale of less than 3 min for all cases. Hence, we are 95% confident that storage term for any one

710 flight will be within $\pm 2.03\sigma_S$ (35 degrees of freedom, JCGM, 2008). For the configurations investigated here, an optimal downwind distance of $D = 6$ or 8 km gives σ_S between 4.4 and 7% for Aug 20 and between 11 and 15% for Sep 2, suggesting an uncertainty as high as 14% and 30% respectively. This is in good agreement with the values of S/E_S reported in Fathi et al. (2021) (-3% for the Aug 20 flights and -29% for the Sep 2 flights) and those reported in Fathi et al. (2023) (up to 10.9% for Aug 20 and -27.5% for Sep 2). For large area sources, the uncertainty associated with storage can be reduced to 4% and 14% (for Aug 20 and Sep 2) by flying the screen closer to the source at $D = 2$ km.



715 **Figure 12.** The variability (σ_S) in the storage term normalize by emission rate (S/E_S) as a function of the averaging period (τ) over the model run, from (a) Aug 20 16:20 to 18:47 and (b) Sep 2 16:20 to 18:09. The volumes are defined for the 3 source types (red line stacks, blue lines small area, green lines large area) and the 6 downwind distances ($D = 2$ to 12 km), which the furthest distances have the highest variability. For emphasis, the closest (2 km) and furthest (12 km) distances for each source type are highlighted.

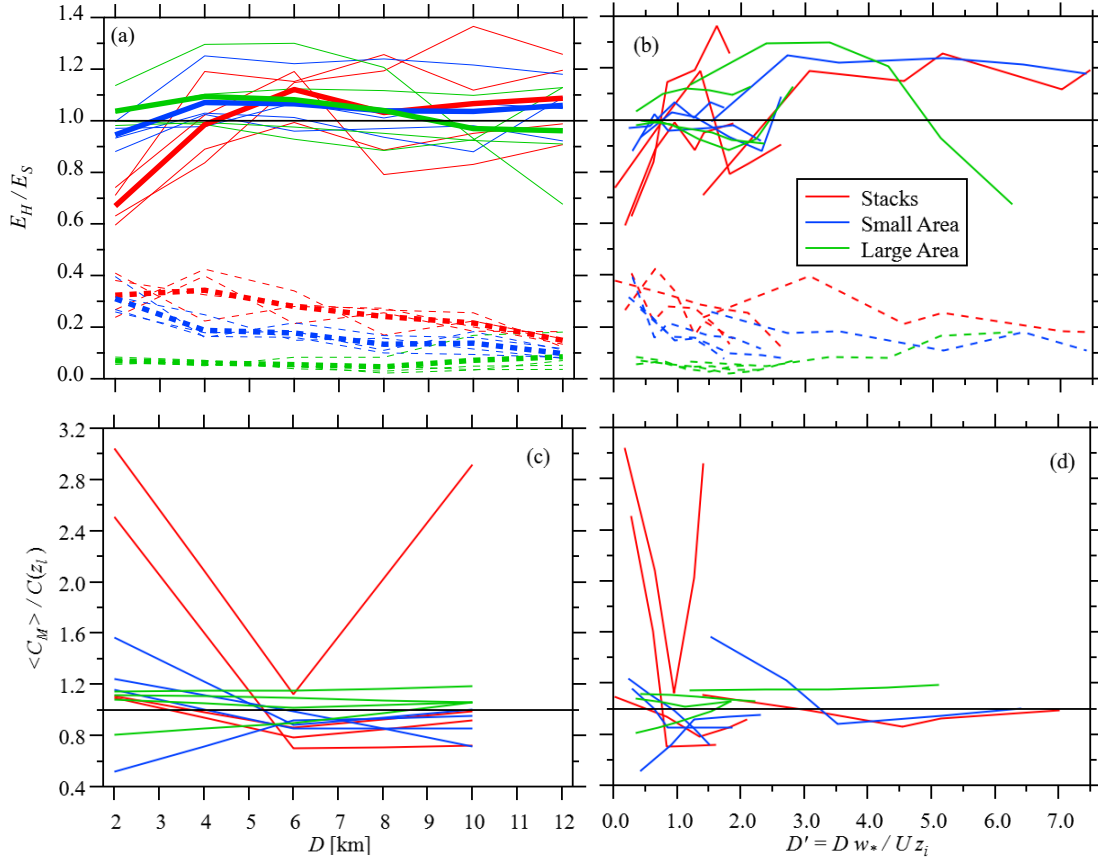
720

3.4 Scaling

725 Figures 13a and 13b compare the emission flux estimates and variation for all the sources for both dimensionalized downwind distance, D (Fig. 13a), and non-dimensionalized downwind distance, D' (Fig. 13b). As shown in Equation 1, D' is normalized by the boundary-layer height (z_i). Here we use an average z_i value for each flight set but note that this value can vary significantly during the flights. For all Aug 16:20 flight set, the model value of z_i is constant (824 m). It then grows linearly during the 17:20 flight sets, from 867 m to 1315 m (for the 40-min duration of longest flights at $D = 12$ km). During the Sep 2 flight sets, z_i increases from 528 m at 16:20 to 1078 m at 17:00 and then decreases from 1078 m at 17:10 to 952 m at 17:50. Hence, this normalization should be interpreted with some degree of caution. Although the variation is relatively small in most cases (more than 50% of the flight sets show less than 5% change in z_i during the flight durations), in some cases the increase in z_i can be up to 100%.

730

Using these estimations of D' , the results are not collapsed due to non-dimensionalization as substantial variation is seen in the results using either D or D' . There is significant variability in the average values of E_H/E_S for all sources over a wide range of D' values, and the results do not asymptote to a value of $E_H/E_S = 1.0$. For the **large** area sources, the standard deviation, σ (the variability between the 10 flights) is lowest for $D' \leq 6$, while for the **stack and large area** source flights, σ tends to decrease with D' , but there is no apparent minimum or asymptotic D' value.



740 **Figure 13.** A summary of the results shown in Figures 3, 4, 8, and 9, compared to both downwind distance D (a, c), and non-dimensionalized downwind distance, D' (b, d). Panels (a) and (b) show the ratio of estimated advection flux, E_H , to the known emission rate, E_S , and the standard deviation of the ratio, σ . In Panel (a), the thicker line is the average of all 4 flight times. Panels (c) and (d) show the ratio of average concentration, $\langle C_M \rangle$, below the lowest flight level ($z_l = 150$ m) to the constant concentration, $C(z_l)$, extrapolation (see Fig. 4).

745 We also investigate the effect of non-dimensionalization on the accuracy of the constant concentration extrapolation below the lowest flight path. The average concentration below the lowest flight path $\langle C_M \rangle$ is calculated from the instantaneous flights (see Fig. 4) and this is normalized by the extrapolated concentration at the lowest flight path level, $C(z_l)$, where $z_l =$

150 m. When the results are non-dimensionalized, $\langle C_M \rangle / C(z_l)$ varies from 0.85 to 1.19 for $D' \geq 3$, suggesting that the extrapolation should be within approximately 20% beyond that distance. However, this analysis ignores the significant overestimation of $\langle C_M \rangle$ for the Aug 20 17:20 stack flights at $D = 10$ km (see Fig. 4b), and it is unclear what would happen at further downwind distances for that flight.

4 Conclusions

The results of this study demonstrate that emissions estimates can be substantially varied under different conditions. This reinforces the importance of storage and release discussed in Fathi et al. (2021) and Fathi et al. (2023). A vertically moving (rising or falling) plume may also lead to under- or over-estimation of the emissions for the non-instantaneous flight, although this would not explain under- or over-estimation in the instantaneous flights. Further uncertainty is introduced by the sparse interpolation, especially close to the source, with uncertainties as high as 132% for stack sources or 57% for small area sources (both at $D = 2$ km). Further from the source ($D \geq 6$ km) the uncertainty associated with interpolation is much smaller ($\leq 17\%$).

When all the different flight times are averaged, the storage/release conditions tend to cancel and the average E_H values are within 12% of E_S for a downwind distance of 4 km or more. Hence, based on the average estimate of E_H/E_S alone for the cases studied here, a screen at a downwind distance of 4 km or more provides the same level of accuracy for the three types of sources investigated here (i.e. elevated stacks, small surface area sources, or a large surface area source).

However, variability between individual flights is a very large source of uncertainty. This variability is likely due to changes in storage/release over the flight times, since similar variability is seen in instantaneous results. At a downwind distance of 4 km, for elevated stack sources, this variability between flights can be as much as $\sigma = 42\%$, which suggests an uncertainty of 99% (at a 95% CI) in that particular case. At the same distance, variability for the surface area sources is much less ($\sigma = 25\%$ for small area sources, and 7% for the large area source). The variability between flights tends to decrease with increasing downwind distance. For the stack and small area sources, σ reaches half the $D = 4$ km value between $D = 10$ and 12 km. However, flight time also increases with downwind distance. For the case of the stack sources, the screen at 12 km takes 3 times as long to complete as the screen at 4 km (since $L = D$ for the smokestack screens). Hence, 3 flights can be flown at $D = 4$ km in the same time it takes to fly one flight at $D = 12$ km. Taking the average of these 3 flights (assuming the results are independent), would reduce the uncertainty by a factor of 0.58 ($1/\sqrt{3}$). Hence, comparable accuracy can be achieved by taking multiple flights closer to the source relative to a single flight further downwind. In these cases (for the conditions investigated here), results show that estimates can be improved and variability reduced by completing multiple screens in opposite directions (e.g. up then down). For large area sources, the variation is small and reaches a minimum (average $\sigma = 5\%$) at $D = 8$ km. For this source type, increasing the downwind distance of the screen does not reduce uncertainty due to variability between flights. Generally, in real-life conditions, any reduced uncertainty due to flying further downwind from source must be balanced against increased relative uncertainty due to instrument measurement noise,

780 especially for pollutants with high background concentrations (due to the weaker concentration signal as the plume disperses).

For elevated stack sources, the results show that, for these cases, reducing the transect spacing below 100 m does not offer any benefits in emission estimation, but increasing the space beyond 150 m can increase uncertainty and modify the E_H estimates. For the area sources we investigate here, the variability between flights is minimized with a transect spacing of

785 $\Delta Z = 50$ m. For the small area sources we investigate here, increasing the spacing to 200 m (reducing flight time by a factor of 0.25) doubles the uncertainty, while for the large area source we investigate here, increasing the spacing to 200 m increases the uncertainty by a factor of ~ 1.5 . As with the optimization of downwind flight distance, multiple flights with a larger transect spacing may result in similar uncertainties compared to a single flight at smaller transect spacing.

Analysis of the storage term for the various flight configurations investigated here suggest that the uncertainty associated

790 with the storage term is minimized at downwind distances between $D = 6$ and 8 km for stack and small area sources. For the flights on Aug 20 this uncertainty is as high as 14%, while for flights on Sep 2 it is as high as 30%, demonstrating a strong dependence on meteorological conditions, likely due to non-stationary wind and stability conditions. For the large area source, the uncertainty is minimal close to the source ($D = 2$ km), and is estimated here as 4% and 14% for the flights on Aug 20 and Sep 2, respectively.

795 These results further demonstrate that one of the most substantial sources of error in the emissions estimate is due to the extrapolation of the results between the surface and the lowest flight path level (as outlined by Gordon et al., 2015 and Conley et al. 2017 for example). Extrapolation error is most significant close to the source, as would be expected, but it can be surprisingly persistent further downwind, in one flight case (for the stack sources), overestimating the concentration below 150 m by a factor of 3 at $D = 10$ km. For the area sources, the extrapolation error is less than 30% for distances of 4

800 km or greater. Non-dimensionalization of the results suggests that the extrapolation error is within 20% for non-dimensional distance of $D' \geq 3$, with the caveat that more results at this distance are required to confirm this result. Although gravitational settling of particles or deposition (of gas or particles) to the surface could modify the concentration profiles, especially near the surface, these results generally emphasize the need to constrain aircraft measurements with coincident surface or near-surface measurements whenever possible. Tests with a mobile vehicle sampling at ground level suggest that

805 variability between flights can be reduced by as much as 6% and underestimation of the emissions close to the source (where the plume is typically lower) is eliminated in the case investigated here. Substantial improvements in emission estimation accuracy could potentially be achieved with UAV or remote sensing (e.g. lidar) sampling beneath the aircraft.

The results demonstrate that it is difficult to provide a single optimized distance and transect spacing given the variability of conditions and the effects of storage and release. However, the results suggest that emission rate retrieval could potentially

810 be improved by accompanying any flight campaign with a strong modelling effort, at least to help with the estimation of storage uncertainty and the understanding of plume dynamics and behaviour.

Author Contribution

SF set up and ran all the WRF modelling. SF and MG designed the experiments using the WRF model output, performed the analysis, and wrote the manuscript. SF and JH provided code for WRF output analysis.

815 Competing Interests

The authors declare that they have no conflict of interest.

Financial Support

Funding to MG and SF provided by the NSERC Discovery Grant (RGPIN-2015-04292). Computational resources provided by Digital Research Alliance of Canada (RRG #3535).

820 Code/Data availability

Code and data are available on request from the authors.

References

- Alfieri, S., Amato, U., Carfora, M., Esposito, M., and Magliulo, V.: Quantifying trace gas emissions from composite landscapes: A mass-budget approach with aircraft measurements, *Atmospheric Environment*, 44, 1866–1876, <https://doi.org/https://doi.org/10.1016/j.atmosenv.2010.02.026>, 2010.
- 825 Andreae, M. O., Acevedo, O. C., Araùjo, A., Artaxo, P., Barbosa, C. G. G., Barbosa, H. M. J., Brito, J., Carbone, S., Chi, X., Cintra, B. B. L., da Silva, N. F., Dias, N. L., Dias-Júnior, C. Q., Ditas, F., Ditz, R., Godoi, A. F. L., Godoi, R. H. M., Heimann, M., Hoffmann, T., Kesselmeier, J., Könemann, T., Krüger, M. L., Lavric, J. V., Manzi, A. O., Lopes, A. P., Martins, D. L., Mikhailov, E. F., Moran-Zuloaga, D., Nelson, B. W., Nölscher, A. C., Santos Nogueira, D., Piedade, M. T.
- 830 F., Pöhlker, C., Pöschl, U., Quesada, C. A., Rizzo, L. V., Ro, C.-U., Ruckteschler, N., Sá, L. D. A., de Oliveira Sá, M., Sales, C. B., dos Santos, R. M. N., Saturno, J., Schöngart, J., Sörgel, M., de Souza, C. M., de Souza, R. A. F., Su, H., Targhetta, N., Tóta, J., Trebs, I., Trumbore, S., van Eijck, A., Walter, D., Wang, Z., Weber, B., Williams, J., Winderlich, J., Wittmann, F., Wolff, S., and Yáñez Serrano, A. M.: The Amazon Tall Tower Observatory (ATTO): overview of pilot measurements on ecosystem ecology, meteorology, trace gases, and aerosols, *Atmospheric Chemistry and Physics*, 15, 10 723–10 776,
- 835 <https://doi.org/10.5194/acp-15-10723-2015>, 2015.

- Angevine, W. M., Peischl, J., Crawford, A., Loughner, C. P., Pollack, I. B., and Thompson, C. R.: Errors in top-down estimates of emissions using a known source, *Atmospheric Chemistry and Physics*, 20, 11 855–11 868, <https://doi.org/10.5194/acp-20-11855-2020>, 2020.
- Baray, S., Darlington, A., Gordon, M., Hayden, K. L., Leithead, A., Li, S.-M., Liu, P. S. K., Mittermeier, R. L., Moussa, S.,
840 G., O'Brien, J., Staebler, R., Wolde, M., Worthy, D., and McLaren, R.: Quantification of methane sources in the Athabasca Oil Sands Region of Alberta by aircraft mass balance, *Atmospheric Chemistry and Physics*, 18, 7361–7378, <https://doi.org/10.5194/acp-18-7361-2018>, 2018.
- Bell, T. M., Klein, P. M., Lundquist, J. K., and Waugh, S.: Remote-sensing and radiosonde datasets collected in the San Luis Valley during the LAPSE-RATE campaign, *Earth System Science Data*, 13, 1041–1051, <https://doi.org/10.5194/essd-13-1041-2021>,
845 1041-2021, 2021.
- Brus, D., Gustafsson, J., Kemppinen, O., de Boer, G., and Hirsikko, A.: Atmospheric aerosol, gases, and meteorological parameters measured during the LAPSE-RATE campaign by the Finnish Meteorological Institute and Kansas State University, *Earth System Science Data*, 13, 2909–2922, <https://doi.org/10.5194/essd-13-2909-2021>, 2021a.
- Brus, D., Gustafsson, J., Vakkari, V., Kemppinen, O., de Boer, G., and Hirsikko, A.: Measurement report: Properties of
850 aerosol and gases in the vertical profile during the LAPSE-RATE campaign, *Atmospheric Chemistry and Physics*, 21, 517–533, <https://doi.org/10.5194/acp-21-517-2021>, 2021b.
- Cambaliza, M. O. L., Shepson, P. B., Caulton, D. R., Stirm, B., Samarov, D., Gurney, K. R., Turnbull, J., Davis, K. J., Possolo, A., Karion, A., Sweeney, C., Moser, B., Hendricks, A., Lauvaux, T., Mays, K., Whetstone, J., Huang, J., Razlivanov, I., Miles, N. L., and Richardson, S. J.: Assessment of uncertainties of an aircraft-based mass balance approach
855 for quantifying urban greenhouse gas emissions, *Atmos. Chem. Phys.*, 14, 9029–9050, doi:10.5194/acp-14-9029-2014, 2014.
- Conley, S., Faloon, I., Mehrotra, S., Suard, M., Lenschow, D. H., Sweeney, C., Herndon, S., Schwietzke, S., Pétron, G., Pifer, J., Kort, E. A., and Schnell, R.: Application of Gauss's theorem to quantify localized surface emissions from airborne measurements of wind and trace gases, *Atmospheric Measurement Techniques*, 10, 3345–3358, <https://doi.org/10.5194/amt-10-3345-2017>, 2017.
- 860 Davis, Z. Y. W., Baray, S., McLinden, C. A., Khanbabakhani, A., Fujs, W., Csukat, C., Debosz, J., and McLaren, R.: Estimation of NO_x and SO₂ emissions from Sarnia, Ontario, using a mobile MAX-DOAS (Multi-AXis Differential Optical Absorption Spectroscopy) and a NO_x analyzer, *Atmospheric Chemistry and Physics*, 19, 13 871–13 889, <https://doi.org/10.5194/acp-19-13871-2019>, 2019.
- Davis, Z. Y. W., Frieß, U., Strawbridge, K. B., Aggarwal, M., Baray, S., Schnitzler, E. G., Lobo, A., Fioletov, V. E.,
865 Abboud, I., McLinden, C. A., Whiteway, J., Willis, M. D., Lee, A. K. Y., Brook, J., Olfert, J., O'Brien, J., Staebler, R., Osthoff, H. D., Mihele, C., and McLaren, R.: Validation of MAX-DOAS retrievals of aerosol extinction, SO₂, and NO₂ through comparison with lidar, sun photometer, active DOAS, and aircraft measurements in the Athabasca oil sands region, *Atmospheric Measurement Techniques*, 13, 1129–1155, <https://doi.org/10.5194/amt-13-1129-2020>, 2020.

- de Boer, G., Waugh, S., Erwin, A., Borenstein, S., Dixon, C., Shanti, W., Houston, A., and Argrow, B.: Measurements from mobile surface vehicles during the Lower Atmospheric Profiling Studies at Elevation – a Remotely-piloted Aircraft Team Experiment (LAPSE-RATE), *Earth System Science Data*, 13, 155–169, <https://doi.org/10.5194/essd-13-155-2021>, 2021.
- Fathi, S.: Optimizing Top-down Airborne Emission Retrievals through High and Super-Resolution Numerical Modelling, Dissertation, <http://hdl.handle.net/10315/40663> (last access: 4 July 2025), 2022.
- Fathi, S., Gordon, M., and Chen, Y.: Passive-tracer modelling at super-resolution with Weather Research and Forecasting – Advanced Research WRF (WRF-ARW) to assess mass-balance schemes, *Geosci. Model Dev.*, 16, 5069–5091, <https://doi.org/10.5194/gmd-16-5069-2023>, 2023.
- Fathi, S., Gordon, M., Makar, P. A., Akingunola, A., Darlington, A., Liggio, J., Hayden, K., and Li, S.-M.: Evaluating the impact of storage- and-release on aircraft-based mass-balance methodology using a regional air-quality model, *Atmospheric Chemistry and Physics*, 21, 15 461–15 491, <https://doi.org/10.5194/acp-21-15461-2021>, 2021.
- Fiehn, A., Kostinek, J., Eckl, M., Klausner, T., Gałkowski, M., Chen, J., Gerbig, C., Röckmann, T., Maazallahi, H., Schmidt, M., Korbeń, P., Nečki, J., Jagoda, P., Wildmann, N., Mallaun, C., Bun, R., Nickl, A.-L., Jöckel, P., Fix, A., and Roiger, A.: Estimating CH₄, CO₂ and CO emissions from coal mining and industrial activities in the Upper Silesian Coal Basin using an aircraft-based mass balance approach, *Atmos. Chem. Phys.*, 20, 12675–12695, <https://doi.org/10.5194/acp-20-12675-2020>, 2020.
- Gordon, M., Li, S.-M., Staebler, R., Darlington, A., Hayden, K., O’Brien, J., and Wolde, M.: Determining air pollutant emission rates based on mass balance using airborne measurement data over the Alberta oil sands operations, *Atmospheric Measurement Techniques*, 8, 3745–3765, <https://doi.org/10.5194/amt-8-3745-2015>, 2015.
- He, M.; Ditto, J. C.; Gardner, L.; Machesky, J.; Hass-Mitchell, T. N.; Chen, C.; Khare, P.; Sahin, B.; Fortner, J. D.; Plata, D. L.; Drollette, B. D.; Hayden, K. L.; Wentzell, J. J. B.; Mittermeier, R. L.; Leithead, A.; Lee, P.; Darlington, A.; Wren, S. N.; Zhang, J.; Wolde, M.; Moussa, S. G.; Li, S.-M.; Liggio, J.; Gentner, D. R.: Total organic carbon measurements reveal major gaps in petrochemical emissions reporting. *Science*, 383,426-432(2024), <http://doi:10.1126/science.adj6233>, 2024.
- Han, T., Xie, C., Liu, Y., Yang, Y., Zhang, Y., Huang, Y., Gao, X., Zhang, X., Bao, F., and Li, S.-M.: Development of a continuous UAV-mounted air sampler and application to the quantification of CO₂ and CH₄ emissions from a major coking plant, *Atmos. Meas. Tech.*, 17, 677–691, <https://doi.org/10.5194/amt-17-677-2024>, 2024.
- Hayden, K., Li, S.-M., Makar, P., Liggio, J., Moussa, S. G., Akingunola, A., McLaren, R., Staebler, R. M., Darlington, A., O’Brien, J., Zhang, J., Wolde, M., and Zhang, L.: New methodology shows short atmospheric lifetimes of oxidized sulfur and nitrogen due to dry deposition, *Atmos. Chem. Phys.*, 21, 8377–8392, <https://doi.org/10.5194/acp-21-8377-2021>, 2021.
- Heintzenberg, J., Birmili, W., Otto, R., Andreae, M. O., Mayer, J.-C., Chi, X., and Panov, A.: Aerosol particle number size distributions and particulate light absorption at the ZOTTO tall tower (Siberia), 2006–2009, *Atmospheric Chemistry and Physics*, 11, 8703–8719, <https://doi.org/10.5194/acp-11-8703-2011>, 2011.

- Hiller, R., Neining, B., Brunner, D., Gerbig, C., Bretscher, D., Künzle, T., Buchmann, N., Eugster, W.: Aircraft-based CH₄ flux estimates for validation of emissions from an agriculturally dominated area in Switzerland, *JGR Atmos.*, 119(8), <https://doi.org/10.1002/2013JD020918>, 2014.
- Islam, A., Shankar, A., Houston, A., and Detweiler, C.: University of Nebraska unmanned aerial system (UAS) profiling during the LAPSE- RATE field campaign, *Earth System Science Data*, 13, 2457–2470, <https://doi.org/10.5194/essd-13-2457-2021>, 2021.
- JCGM: Evaluation of measurement data — Guide to the expression of uncertainty in measurement, 1st Edn., JCGM 100 : 2008, JCGM (EC, IFCC, ILAC, ISO, IUPAC, IUPAP, OIML and BIPM), https://www.bipm.org/documents/20126/2071204/JCGM_100_2008_E.pdf (last access: 23 October 2025), 2008.
- JOSM: Joint Oil Sands Monitoring Plan, Integrated Monitoring Plan for the Oil Sands, Air Quality Component, p. 72, <http://publications.gc.ca/site/eng/394253/publication.html>, 2013.
- Karion, A., Sweeney, C., Pétron, G., Frost, G., Hardesty, R. M., Kofler, J., Miller, B. R., Newberger, T., Wolter, S., Banta, R., Brewer, A., Dlugokencky, E., Lang, P., Montzka, S. A., Schnell, R., Tans, P., Trainer, M., Zamora, R., and Conley, S.: Methane emissions estimate from airborne measurements over a western United States natural gas field, *Geophys. Res. Lett.*, 40, 4393–4397, doi:10.1002/grl.50811, 2013.
- Karion, A., Lauvaux, T., Lopez Coto, I., Sweeney, C., Mueller, K., Gourdj, S., Angevine, W., Barkley, Z., Deng, A., Andrews, A., Stein, A., and Whetstone, J.: Intercomparison of atmospheric trace gas dispersion models: Barnett Shale case study, *Atmospheric Chemistry and Physics*, 19, 2561–2576, <https://doi.org/10.5194/acp-19-2561-2019>, 2019.
- Kalthoff, N., Corsmeier, U., Schmidt, K., Kottmeier, C., Fiedler, F., Habram, M., and Slemr, F.: Emissions of the city of Augsburg determined using the mass balance method, *Atmos. Environ.*, 36, 19–31, [https://doi.org/10.1016/S1352-2310\(02\)00215-7](https://doi.org/10.1016/S1352-2310(02)00215-7), 2002.
- Kim J., Lee, G., Jun, J., Seo, B.-K., Choi, Y., Quantification of SO₂ and CO₂ emission rates from coal-fired power plants in the Korean peninsula via airborne measurements, *Sci. Tot. Env.*, 978, 179430, <https://doi.org/10.1016/j.scitotenv.2025.179430>, 2025.
- Kostinek, J., Roiger, A., Eckl, M., Fiehn, A., Luther, A., Wildmann, N., Klausner, T., Fix, A., Knote, C., Stohl, A., and Butz, A.: Estimating Upper Silesian coal mine methane emissions from airborne in situ observations and dispersion modeling, *Atmos. Chem. Phys.*, 21, 8791–8807, <https://doi.org/10.5194/acp-21-8791-2021>, 2021.
- Krings, T., Neining, B., Gerilowski, K., Krautwurst, S., Buchwitz, M., Burrows, J. P., Lindemann, C., Ruhtz, T., Schüttemeyer, D., and Bovensmann, H.: Airborne remote sensing and in situ measurements of atmospheric CO₂ to quantify point source emissions, *Atmos. Meas. Tech.*, 11, 721–739, <https://doi.org/10.5194/amt-11-721-2018>, 2018.
- J.L. France, P. Bateson, P. Dominutti, G. Allen, S. Andrews, S. Bauguitte, M. Coleman, T. Lachlan-Cope, R.E. Fisher, L. Huang, A.E. Jones, J. Lee, D. Lowry, J. Pitt, R. Purvis, J. Pyle, J. Shaw, N. Warwick, A. Weiss, S. Wilde, J. Witherstone, S. Young: Facility level measurement of offshore oil and gas installations from a medium-sized airborne platform: method

- development for quantification and source identification of methane emissions, *Atmos. Meas. Tech.*, 14, pp. 71-88, 10.5194/amt-14-71-2021, 2021
- 935 Li, S.-M., Leithead, A., Moussa, S. G., Liggio, J., Moran, M. D., Wang, D., Hayden, K., Darlington, A., Gordon, M., Staebler, R., Makar, P. A., Stroud, C. A., McLaren, R., Liu, P. S. K., O'Brien, J., Mittermeier, R. L., Zhang, J., Marson, G., Cober, S. G., Wolde, M., and Wentzell, J. J. B.: Differences between measured and reported volatile organic compound emissions from oil sands facilities in Alberta, Canada, *Proceedings of the National Academy of Sciences*, 114, E3756–
- 940 E3765, <https://doi.org/10.1073/pnas.1617862114>, 2017.
- Liggio, J., Li, SM., Hayden, K., Y.M. Taha, C. Stroud, A. Darlington, B.D. Drolette, M. Gordon, P. Lee, P. Liu, A. Leithead, S.G. Moussa, D. Wang, J. O'Brien, R.L. Mittermeier, J.R. Brook, G. Lu, R.M. Staebler, Y. Han, T.W. Torarek, H.D. Osthoff, P.A. Makar, J. Zhang, D.L. Plata, D. Genter: Oil sands operations as a large source of secondary organic aerosols. *Nature* 534, 91–94. <https://doi.org/10.1038/nature17646>, 2016.
- 945 Liggio, J., Li, S.-M., Staebler, R. M., Hayden, K., Darlington, A., Mittermeier, R. L., O'Brien, J., McLaren, R., Wolde, M., Worthy, D., and Vogel, F.: Measured Canadian oil sands CO₂ emissions are higher than estimates made using internationally recommended methods, *Nature Communications*, 10, 1863, <https://doi.org/10.1038/s41467-019-09714-9>, 2019.
- Mays, K.L., Shepson, P.B., Stirm, B.H., Karion, A., Sweeney, C., Gurney, K.R.: Aircraft-Based Measurements of the
- 950 Carbon Footprint of Indianapolis, *Environ. Sci. Technol.*, 43, 20, 7816–7823, <https://doi.org/10.1021/es901326b>, 2009.
- Nambiar, M. K., Byerlay, R. A. E., Nazem, A., Nahian, M. R., Moradi, M., and Aliabadi, A. A.: A Tethered Air Blimp (TAB) for observing the microclimate over a complex terrain, *Geoscientific Instrumentation, Methods and Data Systems*, 9, 193–211, <https://doi.org/10.5194/gi-9-193-2020>, 2020.
- Nygård, T., Tisler, P., Vihma, T., Pirazzini, R., Palo, T., and Kouznetsov, R.: Properties and temporal variability of summertime temperature inversions over Dronning Maud Land, Antarctica, *Quarterly Journal of the Royal Meteorological Society*, 143, 582–595, <https://doi.org/https://doi.org/10.1002/qj.2951>, 2017.
- Onishi, R., Sugiyama, D., and Matsuda, K.: Super-Resolution Simulation for Real-Time Prediction of Urban Micrometeorology, *SOLA*, 15, 178–182, <https://doi.org/10.2151/sola.2019-032>, 2019.
- Panitz, H.-J., Nester, K., and Fiedler, F.: Mass budget simulation of NO_x and CO for the evaluation of calculated emissions
- 960 for the city of Augsburg (Germany), *Atmos. Environ.*, 36, 33–51, 2002.
- Peischl, J., Ryerson, T. B., Holloway, J. S., Parrish, D. D., Trainer, M., Frost, G. J., Aikin, K. C., Brown, S. S., Dubé, W. P., Stark, H., and Fehsenfeld, F. C.: A top-down analysis of emissions from selected Texas power plants during TexAQS 2000 and 2006, *Journal of Geophysical Research: Atmospheres*, 115, <https://doi.org/https://doi.org/10.1029/2009JD013527>, 2010.
- Ražnjević, A., van Heerwaarden, C., van Stratum, B., Hensen, A., Velzeboer, I., van den Bulk, P., and Krol, M.: Technical note: Interpretation of field observations of point-source methane plume using observation-driven large-eddy simulations, *Atmos. Chem. Phys.*, 22, 6489–6505, <https://doi.org/10.5194/acp-22-6489-2022>, 2022.

- Ryoo, J.-M., Iraci, L. T., Tanaka, T., Marrero, J. E., Yates, E. L., Fung, I., Michalak, A. M., Tadić, J., Gore, W., Bui, T. P., Dean-Day, J. M., and Chang, C. S.: Quantification of CO₂ and CH₄ emissions over Sacramento, California, based on divergence theorem using aircraft measurements, *Atmospheric Measurement Techniques*, 12, 2949–2966, <https://doi.org/10.5194/amt-12-2949-2019>, 2019.
- Tadić, J. A.M. Michalak, L. Iraci, V. Ilić, O. Sébastien, C. Biraud, D.R. Feldman, T. Bui, M.S. Johnson, M. Loewenstein, S. Jeong, M.L. Fischer, E.L. Yates, J.-M. Ryoo. Elliptic Cylinder Airborne Sampling and Geostatistical Mass Balance Approach for Quantifying Local Greenhouse Gas Emissions, *Environ. Sci. Technol.* 51, 17, 10012–10021, <https://doi.org/10.1021/acs.est.7b03100>, 2017.
- 975 Turnbull, J. C., Karion, A., Fischer, M. L., Faloona, I., Guilderson, T., Lehman, S. J., Miller, B. R., Miller, J. B., Montzka, S., Sherwood, T., Saripalli, S., Sweeney, C., and Tans, P. P.: Assessment of fossil fuel carbon dioxide and other anthropogenic trace gas emissions from airborne measurements over Sacramento, California in spring 2009, *Atmos. Chem. Phys.*, 11, 705–721, doi:10.5194/acp-11-705-2011, 2011.
- Watson, C. D., Wang, C., Lynar, T., and Weldemariam, K.: Investigating two super-resolution methods for downscaling precipitation: ESRGAN and CAR, arXiv [preprint], <https://doi.org/10.48550/ARXIV.2012.01233>, 2020.
- 980 Wu, Y., Teufel, B., Sushama, L., Belair, S., and Sun, L.: Deep Learning-Based Super-Resolution Climate Simulator-Emulator Framework for Urban Heat Studies, *Geophys. Res. Lett.*, 48, e2021GL094737, <https://doi.org/10.1029/2021GL094737>, e 2021.
- Yong, H., Allen, G., Mcquilkin, J., Ricketts, H., Shaw, J.T.: Lessons learned from a UAV survey and methane emissions calculation at a UK landfill, *Waste Manag.*, 180 (47-54), <https://doi.org/10.1016/j.wasman.2024.03.025>, 2024.
- 985 Zięba, A.: Effective Number of Observations and Unbiased Estimators of Variance for Autocorrelated Data – an Overview, *Metrol.Meas. Syst.*, <https://doi.org/10.2478/v10178-010-0001-0>, 2010.