



**Larger hydrological simulation uncertainties where runoff
generation capacity is high: insights from 63 catchments in
southeastern China**

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Abstract

Traditional parameter calibration strategies that focus on a single optimal parameter set may lead to large uncertainties and biases in simulating internal hydrological processes because of parameter equifinality. This study used the semi-distributed Tsinghua Hydrological Model based on Representative Elementary Watershed (THREW) to investigate the influence of parameter equifinality on uncertainties in surface–subsurface runoff partitioning. The model was implemented in 63 catchments in southeastern China with high-quality rainfall and streamflow data. Behavioral parameter sets were selected based on KGE thresholds to quantify uncertainty in estimates of the contribution of subsurface runoff (C_{sub}). Correlation analyses were conducted to investigate factors influencing these uncertainties. Results showed that: (1) the THREW model performed well across the 63 catchments, with an average optimal KGE (KGE_{opt}) of 0.846. C_{sub} varied widely among catchments, ranging from 1.0% to 74.1% (mean = 31.7%), and was below 50% in 84% of the catchments, indicating that surface runoff was the dominant runoff generation mechanism in the study area. (2) Substantial uncertainty in C_{sub} can arise from small differences in KGE, with notable variability among catchments. The uncertainty in C_{sub} was modest in most catchments, with mean Bias (difference between the



28 C_{sub} estimated using the optimal set and the average across all behavioral parameter sets) and
29 Range (max–min across behavioral sets) of 2.7% and 15.8%, respectively. However, the
30 uncertainty can be large in some catchments, where reliance on a single optimal parameter set
31 is likely inappropriate. (3) Runoff ratio was identified as an important catchment attribute
32 significantly correlated with C_{sub} and its uncertainty. In catchments with stronger runoff-
33 generation capacity, the model tended to be less sensitive and the simulation of internal runoff-
34 component partitioning tended to exhibit larger uncertainties. Such evidence can provide
35 empirical a priori guidance on the likely magnitude of uncertainties and help inform calibration-
36 strategy selection.

37

38 1. Introduction

39 Hydrological models are useful tools for understanding hydrological processes and
40 predicting variability in water resources. Parameter equifinality is a widely recognized issue in
41 hydrological modelling, meaning that different parameter sets may yield similar model
42 performance (Gupta et al., 2008). This can result in large uncertainties in the simulation of
43 internal hydrological processes despite producing similar total hydrographs (Delavau et al.,
44 2017; Nan & Tian, 2024). Understanding the characteristics and mechanisms of uncertainty
45 generation and propagation, systematically assessing uncertainty, and employing multiple
46 approaches to reduce uncertainty are important tasks in the field of hydrological modelling.

47 Parameter calibration is a necessary step in developing hydrological models. Streamflow
48 is the most commonly used data type for calibration, and other variables—such as soil moisture,
49 evapotranspiration, snow cover/depth, glacier mass balance, and isotopic tracers—are also
50 employed by some researchers to better constrain uncertainties (Chen et al., 2017; He et al.,
51 2019; Ala-aho et al., 2017; He & Pomeroy, 2023). Regardless of the datasets and objective
52 functions used (e.g., Nash–Sutcliffe efficiency, NSE; Kling–Gupta efficiency, KGE),
53 calibration strategies can be broadly classified into two types. One seeks a single optimal
54 parameter set that maximizes the chosen performance metric, which is often assumed to
55 represent realistic hydrological behavior and is subsequently used for process inference or



56 scenario analysis, for example to assess runoff response to climate change (Su et al., 2023). The
57 other approach employs an ensemble of parameter sets, typically obtained by applying a
58 performance threshold to Monte Carlo realizations or to parameter sets sampled during
59 calibration (Blasone et al., 2008; Nan et al., 2021).

60 Ensemble-based strategies not only support investigation of hydrological processes but
61 also allow for a systematic assessment of model sensitivity and uncertainty. In practice, the
62 choice of calibration strategy often depends on research objectives: ensemble methods are more
63 commonly applied in studies explicitly focused on uncertainties (He et al., 2019), while single-
64 optimal-parameter approaches remain the default in many applications (Beven & Binley, 2013;
65 Efstratiadis & Koutsoyiannis, 2010). From the perspective of model behavior, ensemble
66 approaches should be preferable in regions where parameter equifinality is pronounced,
67 whereas a single optimal parameter set may be adequate in catchments with limited equifinality.
68 However, existing studies rarely provide an a priori assessment of the likely degree of
69 equifinality for a given catchment, so researchers lack practical guidance for selecting the most
70 appropriate calibration strategy. This prevailing preference for single-best solution has
71 constrained advances in understanding model uncertainty to some extent.

72 The contribution of runoff components to streamflow is an important hydrological
73 characteristic that reflects runoff-generation mechanisms and is susceptible to parameter
74 equifinality (He et al., 2021). Previous studies have shown that, in some catchments, the
75 partitioning between surface and subsurface runoff can exhibit large uncertainty even when
76 streamflow simulations are classified as behavioral. Analyzing uncertainties in runoff
77 components and their controlling factors is essential for deepening our understanding of runoff-
78 generation processes and for improving the reliability of hydrological simulations and
79 predictions (Cui & Tian, 2025; Tudaji et al., 2025a). However, among studies addressing
80 uncertainties and sensitivities in hydrological models, the emphasis has primarily been on
81 parameter uncertainty, model overall performance and the simulation of total runoff (Di Marco
82 et al., 2021; Yang et al., 2019), whereas uncertainty in internal water partitioning has received
83 comparatively little attention. This lack of focus likely arises because internal water states and
84 fluxes are harder to observe than total runoff, making the validation of internal partitioning
85 more difficult and less common (Nan et al., 2025).



86 Motivated by the above background, this study utilized a semi-distributed hydrological
87 model to investigate the influence of parameter equifinality on internal water component
88 partitioning. In specify, the objectives of this study are: (1) to quantify the uncertainty in the
89 contribution of subsurface runoff (C_{sub}) resulting from small changes in model performance
90 metric (KGE), and (2) to identify factors that influence model uncertainty so as to provide
91 potential a priori empirical guidance for assessing uncertainty and selecting calibration
92 strategies.

93 **2. Materials and methodologies**

94 **2.1 Catchment and data set**

95 This study utilized the catchment set established by [Tudaji et al. \(2025b\)](#) to analyze the
96 hydrological simulation uncertainties. It included 63 small- to medium-scale catchments
97 located in southeastern China ([Figure 1](#)), most of which fall within the Yangtze River Basin.
98 The catchment attributes vary considerably ([Table 1](#)). The drainage areas of the catchments
99 range from 91.5 to 5,266 km², with an average of 1,528 km². These catchments exhibit
100 significant diversity in climate, topography, and rainfall–runoff relationships, with wide ranges
101 of mean annual rainfall (647–2,593 mm), topographic slope (1.8–26.2°), and runoff ratios
102 (0.31–0.96).

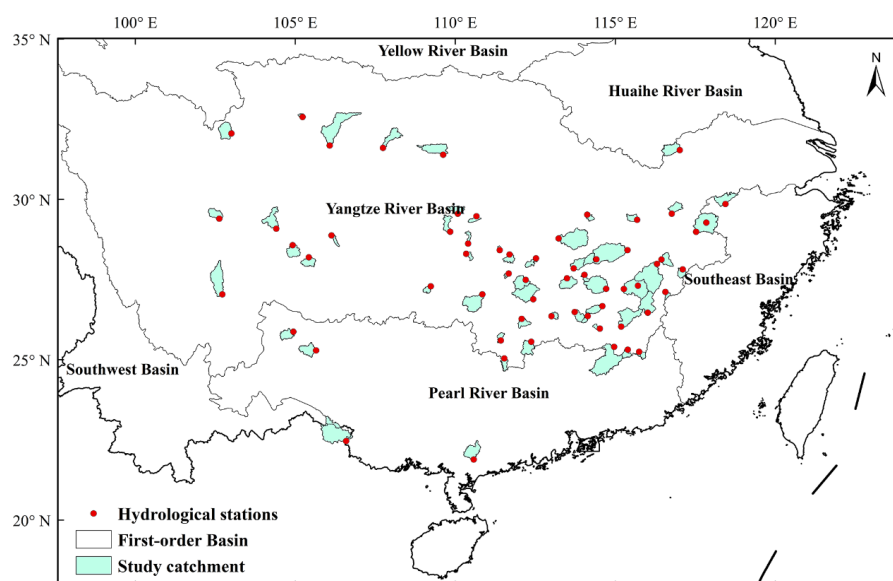


Figure 1. Geographic distribution of the study catchments (Adapted from Tudaji et al, 2025b).

Table 1. Statistical summaries of the catchment attributes

Attribute	Description	Min	Max	Average	Unit
DRA	Drainage area	92	5266	1528	km ²
MAR	Mean annual rainfall	647	2593	1531	mm
MAQ	Mean annual runoff	356	1571	868	mm
QR	Runoff ratio	0.31	0.96	0.58	-
TS	Topographic slope	1.83	26.18	11.77	°

Hourly discharge and rainfall data from 1 January 2014 to 31 December 2015 were collected from the National Rainfall and Hydrological Database, established by the Information Center of the Ministry of Water Resources (http://xxfb.mwr.cn/sq_dtcx.html, last access: 10 December 2023). Considering the variable quality of the raw data (mainly completeness and temporal resolution), 63 hydrological stations were selected based on high-quality standards. Specifically, the average temporal resolution—defined as the ratio of the time period to the number of measurements—exceeded 3,650 s. This threshold was slightly higher than 1 h, ensuring hourly resolution while allowing for individual missing data. In addition, to make full use of the water level data (which are generally more complete than discharge data) in the



116 database, the water level–discharge relationship was used to infer discharge values for periods
117 with only water level data. To ensure the accuracy of these calculations, selected stations met
118 the criteria that discharge data for more than 80% of the time steps also had water level data,
119 and the coefficient of determination (R^2) for the water level–discharge relationship exceeded
120 0.95.

121 Similar to the discharge data, 863 rainfall stations with hourly records were selected within
122 the spatial extent of the 63 catchments. The Thiessen polygon method (Han and Bray, 2006)
123 was employed to generate areal rainfall for each catchment. Each catchment was covered by 15
124 Thiessen polygons on average.

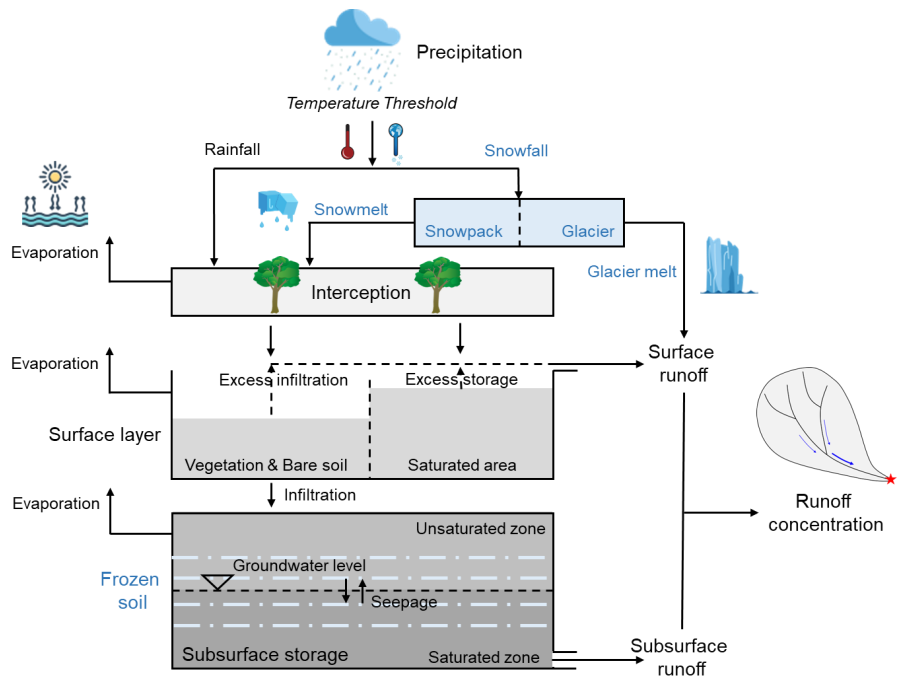
125 Other data used for model setup were collected from public datasets. The 90 m-resolution
126 Multi-Error-Removed Improved-Terrain Digital Elevation Model (MERIT DEM; Yamazaki et
127 al., 2017) was used for catchment extraction. Daily temperature and potential
128 evapotranspiration were sourced from ERA5-Land (Muñoz Sabater, 2019). Soil parameters
129 were estimated from the global high-resolution dataset of soil hydraulic and thermal parameters
130 (Dai et al., 2019). The 8-day leaf area index (LAI) and 16-day normalized difference vegetation
131 index (NDVI) products from MODIS (MOD15A2H, Myneni et al., 2021; MOD13A1, Didan,
132 2021) were used to represent vegetation conditions.

133 2.2 THREW Hydrological model

134 The Tsinghua Hydrological Model Based on Representative Elementary Watershed
135 (THREW), developed by Tian et al. (2006), was employed in this study. The THREW model is
136 based on a set of balance equations for mass, momentum, and energy, along with constitutive
137 equations controlling fluxes among simulation units. Each catchment is first divided into
138 several Representative Elementary Watersheds (REWs) based on DEM data, and several sub-
139 zones are defined within each REW, serving as the elementary simulation units of the THREW
140 model (Figure 2). Specifically, each REW is divided into surface and subsurface layers. Six
141 sub-zones are defined in the surface layer based on underlying types: vegetation zone (v-zone),
142 bare soil zone (b-zone), snow zone (n-zone), glacier zone (g-zone), sub-stream network zone
143 (t-zone), and main channel reach zone (r-zone). Two sub-zones are defined in the subsurface
144 layer according to soil saturation conditions: unsaturated zone (u-zone) and saturated zone (s-



145 zone). Considering the subtropical monsoon climate of the selected catchments—characterized
146 by high mean temperatures and the temporal coincidence of peak rainfall and temperature—the
147 influence of cryospheric processes on runoff is negligible; therefore, the snow and glacier
148 modules and the corresponding sub-zones were not activated in this study. The THREW model
149 has been described in our previous publications; for full model details see [Tian et al. \(2006\)](#).
150 This study primarily investigates uncertainties in runoff-component partitioning using the
151 THREW model.



152
153 **Figure 2.** Schematic illustration of the THREW model (Adapted from Tudaji et al., 2025b)

154 **2.3 Model calibration**

155 The parameters to be calibrated are listed in [Table 2](#). The Python Surrogate Optimization
156 Toolbox (pySOT; [Eriksson et al., 2019](#)) was employed for model calibration. The pySOT
157 algorithm utilizes radial basis functions (RBFs) as surrogate models to approximate model
158 simulations and reduce runtime per iteration. During each pySOT run, parameters were
159 generated using the symmetric Latin hypercube design (SLHD), and the optimization stopped
160 when the objective converged or the number of model runs reached a threshold (set to 3000 in



161 this study). The Kling–Gupta efficiency (KGE) was used as the optimization objective to reflect
 162 overall model performance in terms of correlation, variability, and bias (Eq. 1).

$$163 \quad KGE = 1 - \sqrt{(1 - r)^2 + (1 - \alpha)^2 + (1 - \beta)^2} \quad (1)$$

164 where, r represents the Pearson correlation coefficient between simulated and observed values,
 165 α is the ratio of the mean of simulated values to that of observed values, β is the ratio of the
 166 standard deviation of simulated values to that of observed values.

167 **Table 2.** Descriptions of calibrated parameters in the THREW model (Adapted from Tudaji et
 168 al., 2025b)

Symbol	Unit	Physical description	Range
WM	cm	Tension water storage capacity for saturation area calculation	0-10
B	-	Shape coefficient for saturation area calculation	0-1
KKA	-	Exponential coefficient for groundwater outflow calculation	0-6
KKD	-	Linear coefficient for groundwater outflow calculation	0-0.5
C1	-	Coefficient for runoff concentration calculation using Muskingum method	0-1
C2	-	Coefficient for runoff concentration calculation using Muskingum method	0-1

169 This study aimed to investigate model performance when the evaluation metric is
 170 relatively high. Consequently, for each catchment the pySOT algorithm was repeated 50 times,
 171 yielding 50 parameter sets. Parameter sets whose KGE exceeded a threshold were selected as
 172 behavioral parameters; the threshold was defined as 0.05 below the optimal KGE (KGE_{opt})
 173 obtained among the 50 sets.

174 2.4 Quantification of surface-subsurface runoff partitioning and its uncertainty

175 The surface–subsurface runoff partitioning in each catchment was analyzed based on
 176 THREW outputs of internal variables (Figure 2). Surface and subsurface runoff were defined
 177 as two runoff components based on runoff generation pathways as reviewed by He et al. (2021).
 178 Surface runoff includes rainfall occurring in areas where soils are saturated, where rainfall
 179 intensity exceeds infiltration capacity, or in impermeable areas such as river channels.
 180 Subsurface runoff is the outflow from the saturated zone. The contribution of subsurface runoff



181 to total runoff (C_{sub}) was calculated to represent the surface–subsurface runoff partitioning
182 characteristic (Eq. 2).

$$183 \quad C_{sub} = \frac{Q_{sub}}{Q_{sur} + Q_{sub}} \times 100\% \quad (2)$$

184 where, Q_{sur} and Q_{sub} are the amount of surface and subsurface runoff, respectively, which can
185 be obtained by the model outputs.

186 The uncertainty of C_{sub} was analyzed from two aspects. The first aspect is the
187 representativeness of C_{sub} estimated by the optimal parameter set, quantified by bias and relative
188 bias (RBias) between the C_{sub} estimated using the optimal set and the average C_{sub} across all
189 behavioral parameter sets (Eqs. 3 and 4). The second aspect is the variability of C_{sub} across the
190 behavioral parameter sets, quantified by the standard deviation (STD) and the range of C_{sub}
191 among those sets (Eqs. 5 and 6). To ensure adequate parameter set samples for uncertainty
192 analysis, only the catchments where the number of behavioral parameter sets exceed 10 were
193 selected for this analysis.

$$194 \quad Bias = |C_{sub}^{opt} - \overline{C_{sub}}| \quad (3)$$

$$195 \quad RBias = \frac{Bias}{\overline{C_{sub}}} \times 100\% \quad (4)$$

$$196 \quad STD = \sqrt{\frac{\sum_{i=1}^n (C_{sub,i} - \overline{C_{sub}})^2}{n}} \quad (5)$$

$$197 \quad Range = C_{sub}^{max} - C_{sub}^{min} \quad (6)$$

198 where, C_{sub}^{opt} is the C_{sub} estimated by the optimal parameter set, $\overline{C_{sub}}$ is the average C_{sub}
199 estimated by the behavioral parameter sets, n is the number of behavioral parameter sets, C_{sub}^{max}
200 and C_{sub}^{min} are the maximum and minimum of C_{sub} estimated by the behavioral parameter sets.

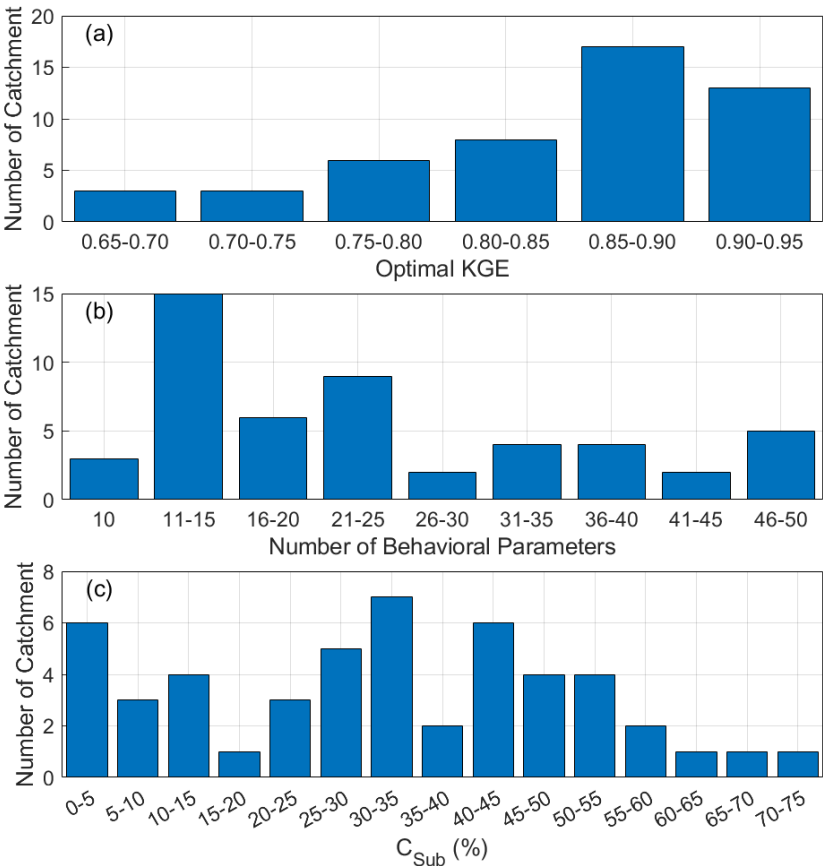
201 3. Results

202 3.1 Model performance

203 Among the 63 catchments, 50 had more than 10 behavioral parameter sets producing KGE
204 higher than $KGE_{opt} - 0.05$ (Figure 3a). The KGE_{opt} in these 50 catchments ranged from 0.663 to
205 0.947, with an average of 0.846, and 30 catchments achieved KGE_{opt} values above 0.85. The
206 comparisons of simulated and observed hourly streamflow in two typical catchments (with the



207 highest and lowest KGE_{opt}) are presented in Figure 4, showing strong consistency between
208 model outputs and observations. These metrics and results indicate generally good model
209 performance in the study area.



210
211 **Figure 3.** Summary of catchment counts with different (a) optimal KGE, (b) numbers of
212 behavioral parameter sets, and (c) contributions of subsurface runoff

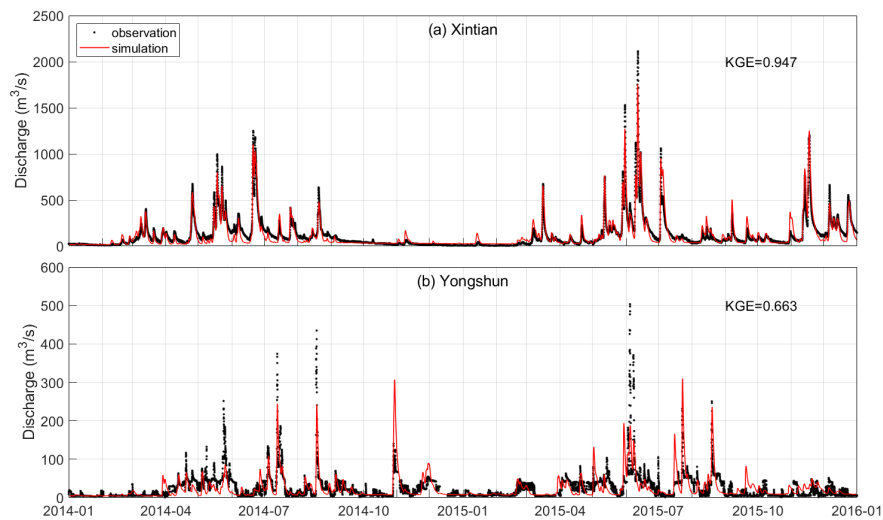


Figure 4. Comparison of simulated and observed hourly discharge in two typical catchments with the highest and lowest KGE: (a) Xintian, (b) Yongshun

The number of behavioral parameter sets varied significantly among these 50 catchments (Figure 3b). The average number was 24.28, and in 15 catchments this number fell in the range 11–15. In only one catchment were all 50 parameter sets obtained by the pySOT process identified as behavioral. Considering the random generation of initial parameter sets within each pySOT running, the number of behavioral parameter sets serve as a partial indicator of model sensitivity.

3.2 Surface-subsurface runoff partitioning and its uncertainties

For each catchment, the average C_{sub} estimated across all behavioral parameter sets was taken as the final estimation. As shown in Figure 3c, C_{sub} varied markedly among catchments, ranging from 1.0% to 74.1% with an average of 31.7%. In 42 of the 50 catchments, C_{sub} was below 50%, indicating that surface runoff was the dominant runoff generation mechanism. This dominance can be attributed to the generally wet climate in the study area, which leads to high soil water saturation and extensive saturated areas.

Figure 5 illustrates the uncertainty of C_{sub} in two typical kinds of catchments. In the Heishui catchment (Figure 5a), C_{sub} exhibited strong variability when KGE was within 0.05 of its optimal value. The bias between the C_{sub} when the optimal KGE achieved (C_{sub}^{opt}) and the



average C_{sub} produced by the behavioral parameter sets ($\overline{C_{sub}}$) was 13%, accounting for 23% of $\overline{C_{sub}}$. Moreover, the C_{sub} estimated by each individual behavioral parameter set ranged from 32% to 85%, and the difference between the maximum and minimum C_{sub} was as high as 53%, indicating that different behavioral parameter sets may imply different dominant runoff generation mechanisms. By contrast, in the Shuikou catchment (Figure 5b), although C_{sub} estimated by the original 50 parameter sets also spanned a wide range, the model performance was much more sensitive to C_{sub} than in the Heishui catchment, as evidenced by a sharp decline in KGE when C_{sub} deviated from C_{sub}^{opt} . As a result, only 13 parameter sets produced KGE higher than the behavioral threshold, yielding small values of Bias (0.6%) and Range (6%).

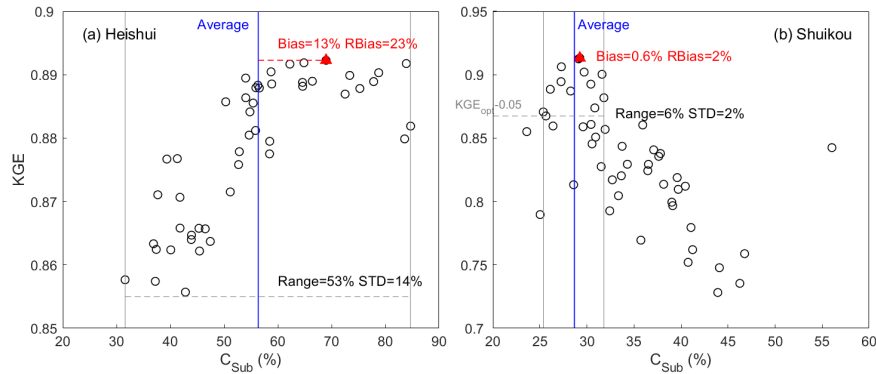
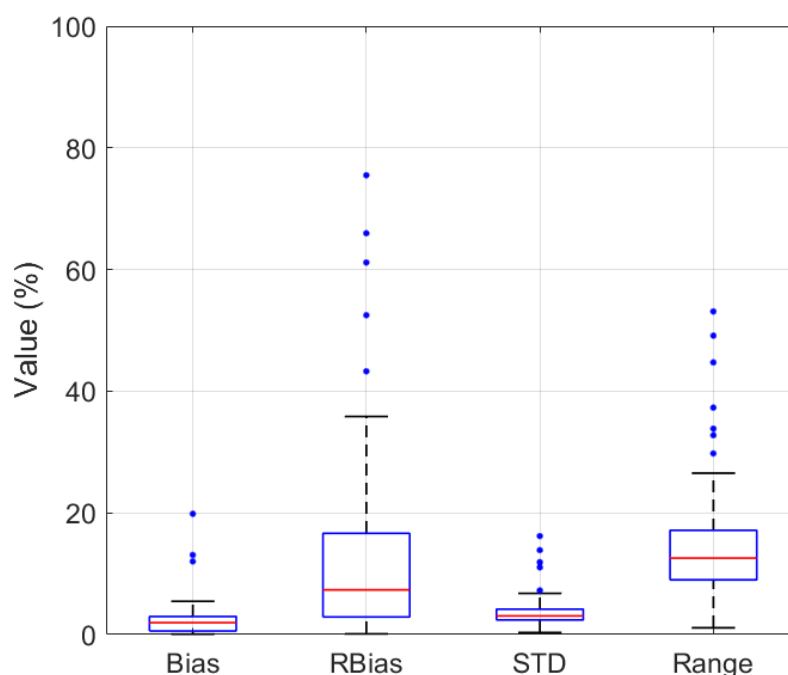


Figure 5. Relation between KGE and contribution of subsurface runoff in two typical catchments: (a) Heishui, (b) Shuikou. Optimal parameter set (red triangle), ensemble mean (blue line), and range (gray shading) are shown, and associated uncertainty metrics are illustrated.

Figure 6 shows the boxplot of C_{sub} uncertainty metrics derived by behavioral parameter sets in 50 catchments. Regarding the representativeness of the optimal C_{sub} , the Bias metric ranged from 0.1% to 19.8%, with an average of 2.7%. Bias was less than 3% in 40 of the 50 catchments, indicating that the C_{sub} obtained from the optimal parameter set was close to the mean across all behavioral parameter sets. However, Bias exceeded 10% in 3 catchments, indicating that relying solely on the optimal parameter set may still lead to misestimation of surface–subsurface runoff partitioning. The RBias metric exhibited a wider range, reaching a maximum of 75.5%, likely due to variations in average C_{sub} (i.e., the denominator in Eq. 2). As for the variability of the behavioral results, the STD and Range of C_{sub} varied from 0.3% to



255 16.2% and 1.1% to 54.1%, with average values of 4.0% and 15.8%, respectively. There was a
256 strong linear correlation between STD and Range (slope = 3.5, $R^2 = 0.914$). In around one third
257 of the catchments (16 of 50), the uncertainties of C_{sub} were relatively small (STD < 2.5% and
258 Range < 10%), but in four catchments STD and Range exceeded 10% and 35%, respectively.
259 Overall, although uncertainties in C_{sub} were modest in most catchments, they could be
260 extremely significant in some catchments.

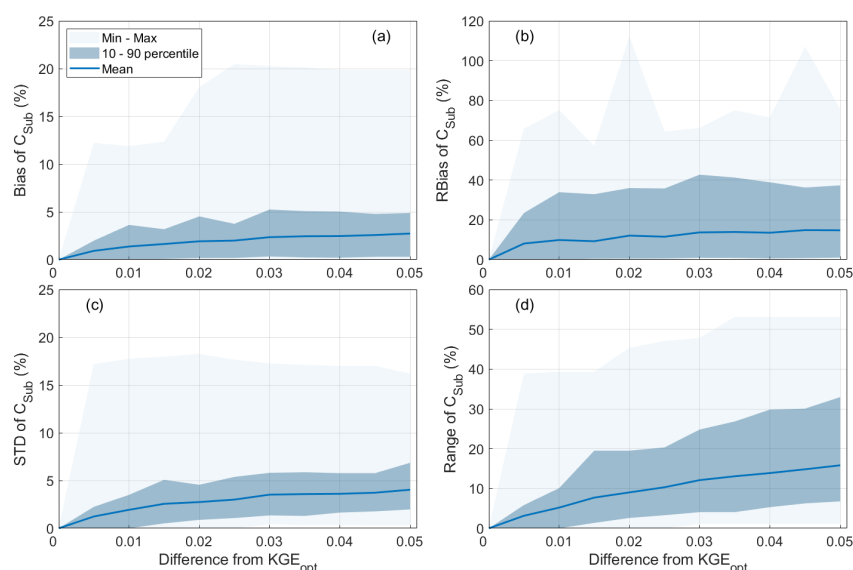


261
262 **Figure 6.** Boxplot of the uncertainty metrics of C_{sub} produced by behavioral parameter sets in
263 the selected 50 catchments

264 Changes in C_{sub} uncertainty with varying behavioral thresholds were further analyzed by
265 adjusting the difference between KGE_{opt} and the KGE threshold from 0.005 to 0.05 in 0.005
266 increments (Figure 7). As expected, most metrics increased as the KGE threshold decreased,
267 although some metrics showed non-monotonic extrema (e.g., the maximum RBias). Notably,
268 uncertainty metrics could still be large even when the KGE threshold was set very close to
269 KGE_{opt} . For instance, in the Yongshun catchment (Figure 4b), Bias and Range reached 12.2%



270 and 38.8%, respectively, when the KGE threshold was set only 0.005 below KGE_{opt} . However,
 271 the 90th percentiles of Bias and Range were below 5% and 10%, respectively, when the KGE
 272 threshold was set 0.01 below KGE_{opt} , indicating that C_{sub} estimation is robust in most
 273 catchments if the threshold is set sufficiently high.



274
 275 **Figure 7.** Changes in C_{sub} uncertainty metrics with changing behavioral KGE thresholds with
 276 an interval of 0.005

277 3.3 Influence factors of surface-subsurface runoff partitioning

278 To further understand the variability of surface-subsurface runoff partitioning and its
 279 uncertainties, we analyzed their correlations with the catchment attributes listed in Table 1.
 280 Considering the strong correlation between uncertainty metrics STD and Range, STD was not
 281 included in the correlation analysis for simplify. The correlation coefficients and the
 282 corresponding statistical significance are shown in Table 3. For the contribution of subsurface
 283 runoff, runoff ratio (QR) was the only attribute showing a statistically significant correlation
 284 ($p < 0.01$) with C_{sub} , indicating greater subsurface contribution in catchments with stronger
 285 runoff generation capacity. Notably, C_{sub} exhibited a positive correlation with topographic slope
 286 (TS), which is consistent with the global isotope-based study by Jasechko et al. (2016) that
 287 found the young-water fraction (associated with surface-runoff contribution) to be negatively



288 correlated with topographic gradient, although the correlation in our study was not statistically
 289 significant ($p = 0.26$).

290 **Table 3.** Correlation coefficient among C_{sub} , uncertainty metrics, and catchment attributes
 291 among 50 catchments. Bold values indicate $p < 0.05$, with * and ** denoting $0.01 < p < 0.05$ and
 292 $p < 0.01$, respectively.

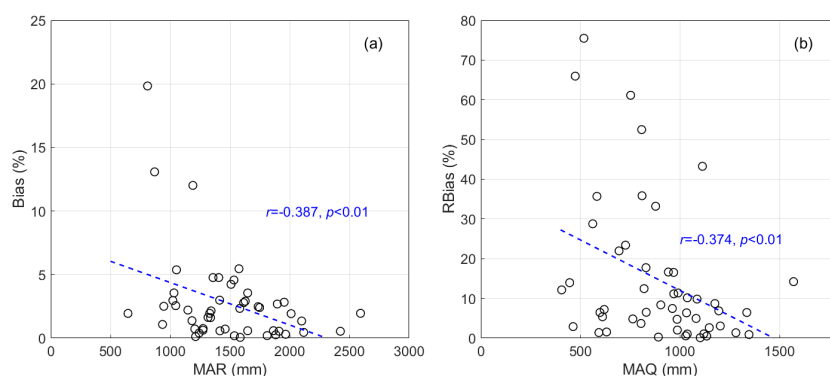
	C_{sub}	Bias	RBias	Range
DRA	0.055	0.167	0.025	0.031
MAR	-0.256	-0.387**	-0.289*	-0.244
MAQ	0.199	-0.128	-0.374**	0.019
QR	0.632**	0.434**	-0.126	0.380**
TS	0.162	0.064	-0.055	0.251
C_{sub}	\	0.074	-0.563**	0.217

293 The uncertainty metrics were correlated with both climate conditions and runoff-
 294 generation capacity. Bias and RBias were both significantly negatively correlated with mean
 295 annual rainfall (MAR) ($p < 0.01$ and $p < 0.05$, respectively). RBias was also significantly
 296 negatively correlated with mean annual runoff (MAQ) ($p < 0.01$). These results suggest that C_{sub}
 297 estimated from the optimal parameter set tended to be closer to the mean C_{sub} across all
 298 behavioral sets in wetter catchments (Figure 8). As expected, RBias was strongly negatively
 299 correlated with C_{sub} ($r = -0.563$), because C_{sub} appears in the denominator of the RBias
 300 calculation. QR was significantly positively correlated with Bias ($r = 0.434$, $p < 0.01$). The
 301 correlations between Range and the examined catchment attributes were similar to those for
 302 C_{sub} in both strength and statistical significance. QR was the only attribute significantly
 303 correlated with Range ($r = 0.380$, $p < 0.01$).

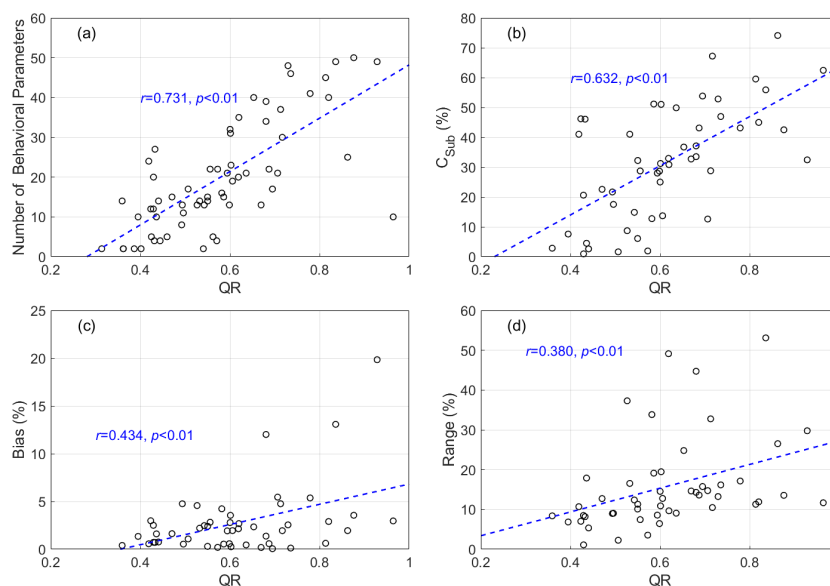
304 It is worth noting that QR was significantly correlated with both surface–subsurface runoff
 305 partitioning and its uncertainties (Figure 9b–d). We also examined the relationship between
 306 model sensitivity—represented by the number of behavioral parameter sets obtained from 50
 307 pySOT calibrations—and QR, and found a strong, significant correlation ($r = 0.731$, $p < 0.01$;
 308 Figure 9a). This suggests the model was less sensitive (i.e., produced a larger number of
 309 behavioral parameter sets) in catchments with higher QR. The positive correlation between C_{sub}



310 and QR likely reflects that a high QR implies a smaller fraction of rainfall lost to
311 evapotranspiration, favoring larger subsurface water storage and lateral subsurface flow.
312 Additionally, higher QR implies more runoff generation via multiple pathways, which may
313 increase variability and consequently the uncertainty in C_{sub} .



314
315 **Figure 8.** Scatter diagram of (a) Bias and MAR, and (b) RBias and MAQ. Blue dashed lines
316 represent the regression fit.



317
318 **Figure 9.** Scatter diagram of QR and (a) number of behavioral parameters, (b) C_{sub} , (c) Bias
319 and (d) Range. Blue dashed lines represent the regression fit.



320 4. Discussions

321 4.1 Implications on hydrological modelling in various conditions

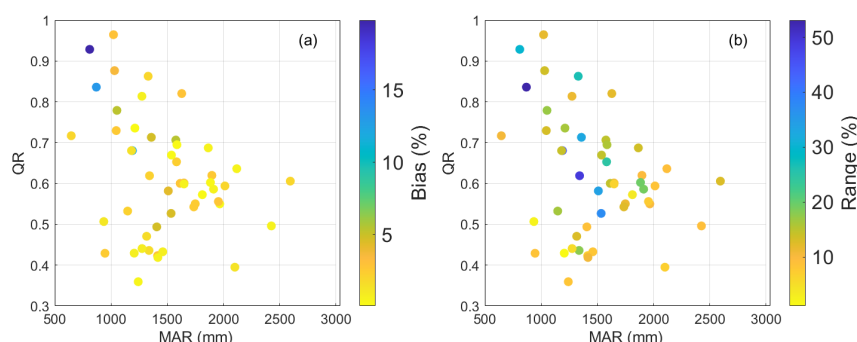
322 This study questions the reasonableness of commonly used hydrological model calibration
 323 strategies. Results show that in some catchments model performance is insensitive to internal
 324 process representation — a very small change in an evaluation metric (for example, a 0.005
 325 change in KGE) can correspond to very large differences in the estimated contribution of
 326 subsurface runoff. Similar phenomena were also reported for other runoff components, such as
 327 snowmelt and glacier melt runoff (He et al., 2019; Nan et al., 2025). In such cases, the optimal
 328 parameter set may not adequately represent the range of plausible hydrological behaviors, and
 329 analyses based on a single parameter set may therefore yield substantially biased estimates.
 330 Conversely, in a substantial proportion of catchments (approximately one-third in this study),
 331 uncertainties among behavioral parameter sets were relatively small, and the optimal parameter
 332 set can adequately represent the parameter sets that produced sufficiently high KGE.

333 The correlation analysis provides potential guidance for choosing appropriate calibration
 334 strategies under different catchment conditions. The runoff ratio (QR) emerged as a
 335 representative index for a priori assessment of potential modeling uncertainties: catchments
 336 with higher QR tended to exhibit greater uncertainties. In such cases, a systematic evaluation
 337 of model uncertainty, such as adopting Generalized Likelihood Uncertainty Estimation (GLUE)
 338 framework, is recommended. Uncertainties can be further reduced by assimilating multiple
 339 datasets (e.g., Tong et al., 2021). Conversely, in catchments with lower QR the model was more
 340 sensitive to parameterization, so a single parameter set that yields the optimal performance
 341 metric is more likely to credibly represent the underlying hydrological processes. In those cases,
 342 calibration that targets a single optimal parameter set may be acceptable.

343 Mean annual rainfall (MAR) was identified as a secondary representative index for a priori
 344 assessment of modeling uncertainties. MAR had a significant negative correlation with Bias
 345 (Figure 8a), and a negative (but not statistically significant) correlation with Range ($r = -0.244$,
 346 $p = 0.087$; Table 3). Meanwhile, the number of behavioral parameter sets was significantly
 347 negatively correlated with MAR ($r = -0.379$, $p < 0.01$), although its absolute correlation
 348 coefficient was smaller than that with QR ($r = 0.731$; Figure 9a).



349 These results indicate that modeling uncertainties tend to be lower in catchments with
350 lower runoff generation capacity and wetter climates. However, it is difficult to derive a reliable
351 equation to predict potential modeling uncertainty from catchment attributes, or to define a
352 MAR/QR threshold above or below which a single optimal parameter set can be judged
353 sufficiently credible. For example, among the five catchments with $MAR > 1500$ mm and
354 $QR < 0.55$, one still has a large Range of 37% (Figure 10b). Consequently, our results offer an
355 empirical criterion for anticipating model uncertainty, but complementary sensitivity and
356 robustness tests are always advisable (Song et al., 2015).



357

358 **Figure 10.** The interrelation among the QR, MAR, and (a) Bias and (b) Range

359 4.2 Limitations

360 This study used the contribution of subsurface runoff (C_{sub}) estimated by the THREW
361 model as a representative hydrological characteristic to analyze hydrological-model uncertainty
362 and its influencing factors. The main limitation of this study lies in the reliability of the
363 estimated C_{sub} and in the representativeness of the THREW model. Because of deficiencies in
364 observational data for multiple runoff components, it is difficult to directly validate the C_{sub}
365 estimates in this study, which consequently raises doubts about conclusions related to C_{sub} .
366 Nonetheless, some indirect evidence supports the C_{sub} estimates to some extent. On the one
367 hand, in our previous studies the C_{sub} estimates produced by the THREW model in two typical
368 catchments were independently validated by other methods, such as an end-member mixing
369 model and a groundwater model (Nan et al., 2021; Nan et al., 2023; Yao et al., 2021; Li et al.,
370 2020), demonstrating the THREW model's ability to simulate surface–subsurface runoff
371 partitioning. On the other hand, the positive correlation between C_{sub} and topographic slope and



372 the negative correlation between C_{sub} and mean annual rainfall are consistent with patterns
373 reported in previous studies (Jasechko et al., 2016; Nan et al., 2025), which provides additional
374 support to the reasonableness of our results.

375 Another limitation is the use of a single THREW model, which raises questions about the
376 generalizability of the conclusions. However, the structure and core equations of THREW
377 model are broadly similar to those of many commonly used semi-distributed hydrological
378 models, such as SWAT and HBV (Gassman et al., 2007; Lindström et al., 1997). Specifically,
379 the basic simulation units of THREW are subzones of the representative elementary watershed
380 (REW), defined by topography and land-surface type — analogous to the hydrological response
381 unit (HRU) concept in other models. Hydrological processes are computed within each unit,
382 including surface runoff, infiltration, subsurface flow, evapotranspiration, and changes in water
383 storage. We therefore expect qualitatively similar findings across semi-distributed models,
384 although specific quantitative outcomes may differ depending on parameterizations (Beck et
385 al., 2016), data conditions (Seibert & Beven, 2009), process representations (Knoben et al.,
386 2020), spatiotemporal resolution (Zhang et al., 2025), and calibration strategy (Sun et al., 2020).
387 Future work could include multi-model comparisons or ensemble simulations to assess how
388 model structural differences affect the robustness of the conclusions.

389 5. Conclusion

390 This study used the semi-distributed THREW model to investigate the influence of
391 parameter equifinality on runoff component partitioning. The model was implemented in 63
392 catchments in southeastern China with high-quality rainfall and streamflow records. Behavioral
393 parameter sets were selected using a KGE threshold ($KGE_{\text{opt}}=0.05$) to quantify uncertainty in
394 estimates of the contribution of subsurface runoff (C_{sub}). Correlation analyses were conducted
395 among C_{sub} , uncertainty metrics, and catchment attributes to identify influence factors. Our
396 main findings are as follows:

397 1. The THREW model showed generally good performance across the 63 catchments, with
398 KGE_{opt} ranging from 0.663 to 0.947 (mean = 0.846). C_{sub} varied widely among catchments,
399 from 1.0% to 74.1% (mean = 31.7%). C_{sub} was lower than 50% in 84% of the catchments,



400 reflecting dominant surface runoff in the study area.

401 2. Small differences in KGE can produce substantial uncertainty in C_{sub} , and the magnitude
402 of that uncertainty varied markedly among catchments. Bias (difference between the C_{sub}
403 estimated using the optimal set and the average across all behavioral parameter sets) ranged
404 from 0.1% to 19.8% (mean = 2.7%), and Range (difference between the maximum and
405 minimum C_{sub} among behavioral parameter sets) ranged from 1.1% to 54.1% (mean = 15.8%).
406 In catchments with larger uncertainty metrics, the calibration strategy focusing on a single
407 optimal parameter set is likely to result in misestimation of internal hydrological processes.

408 3. Runoff ratio (QR) was identified as the primary catchment attribute associated with both
409 surface-subsurface runoff partitioning and its uncertainty. QR was significantly correlated with
410 C_{sub} , Bias and Range ($p < 0.01$), and also had a strong correlation with model sensitivity
411 represented by the count of behavioral parameter sets ($r = 0.731$, $p < 0.01$). This finding indicates
412 that catchments with higher QR tend to have higher contributions of subsurface runoff and
413 larger uncertainties. Such evidence can provide an empirical priori assessment of the likely
414 magnitude of uncertainties and help inform calibration strategy selection.

415

416 **Author contributions**

417 YN conceived the idea, conducted the analysis and drafted the original manuscript. MT
418 contributed to the data collection and model establishment. FT provided comments on the
419 analysis. All the authors contributed to writing and revisions.

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425 During the preparation of this work the authors used ChatGPT in order to improve
426 language and readability of the original draft, with caution. After using these tools, the authors
427 reviewed and edited the content as needed and take full responsibility for the content of the



428 publication.

429 **Data and Code Availability**

430 Datasets used for model setup are available at: Yamazaki et al. (2019), Muñoz Sabater,
 431 (2019), Dai et al. (2019), Myneni et al. (2021) and Didan (2021). The basic information of the
 432 catchment set and the model code of a typical catchment are available at Zenodo:
 433 <https://zenodo.org/records/17089365>.

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