



1 Evaluation of Turbulent Flux Parameterizations over a 2 Continental Glacier on the Tibetan Plateau

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12 **Abstract.** A lack of observations of turbulent fluxes over continental glaciers limits our
13 understanding of the mechanisms that control glacier variations and associated water resource
14 changes across the Tibetan Plateau (TP). Here, we present the first comprehensive analysis of turbulent
15 flux characteristics and a systematic evaluation of turbulent flux methods for a continental glacier on the
16 TP, using eddy covariance observations from the Dundee Glacier (May–October, 2023). The Dundee
17 Glacier persistently lost energy through latent heat flux (mean LE: -10.34 W m^{-2}) and gained energy via
18 sensible heat flux (mean H: 6.93 W m^{-2}), with pronounced seasonal and diurnal variability. On the basis
19 of these measured data, we tested five turbulent flux methods for the Dundee Glacier, including those
20 derived from katabatic flow models, simplified Monin–Obukhov similarity theory without stability
21 corrections, Monin–Obukhov similarity theory with stability corrections using two different bulk
22 Richardson numbers, and the Monin–Obukhov similarity theory with universal stability functions.
23 Among all schemes, the Monin–Obukhov similarity theory with universal stability functions achieved
24 the highest accuracy for both H and LE at different timescales. We further evaluated the performance of
25 these parameterizations in energy and mass balance modeling. Our results show that the recalibrated
26 turbulent flux parameterizations are an effective approach for improving the accuracy of modelled glacier
27 energy and mass balance, and that the Monin–Obukhov similarity theory with universal stability
28 functions yielded the best simulation performance for modelled glacier mass balance. We also found that
29 the Dundee Glacier experienced a sharp increase in H and reversal in LE during a humid heatwave event,
30 shifting from a negative total turbulent flux under the mean climate condition to positive values during



31 the extreme event. However, none of the turbulent flux methods fully captured the high values that
32 occurred during the extreme weather and climate event, indicating that there is currently an
33 underestimation of the contribution of turbulent fluxes to glacier melt energy. These findings advance
34 our knowledge of turbulent fluxes for continental glaciers on the TP and provide important guidance for
35 the improvement of glacier models.



36 **1 Introduction**

37 Turbulent fluxes, including latent heat flux (LE) and sensible heat flux (H), are critical components
38 of the surface energy balance (SEB) of glaciers and markedly influence glacier mass-loss processes.
39 Research on the Tibetan Plateau (TP) shows that turbulent fluxes contribute approximately 14%–35% of
40 the glacial energy budget (Li et al., 2011; Mandal et al., 2022; Zhang et al., 2013; Zhu et al., 2017),
41 serving as the primary energy source sustaining sublimation-driven mass loss, particularly during the
42 cold season (October–May) (Azam et al., 2014a; Potocki et al., 2022). In addition, turbulent fluxes are
43 one of the primary energy sources driving extreme glacier loss events (Thibert et al., 2018). Such events
44 enhance the provision of water resources to downstream regions (Gao et al., 2019; Yao et al., 2022),
45 altering hydrological processes therein (Radić and Hock, 2011; Zhu et al., 2024a); they may also be
46 linked to glacier-related disasters, such as glacier avalanches (Zhao et al., 2022). Under ongoing global
47 warming, the frequencies and intensities of extreme weather and climate events are projected to increase,
48 likely contributing to severe future glacier mass loss owing to enhanced turbulent fluxes (Brun et al.,
49 2018; Duan et al., 2012; Hugonnet et al., 2021; Yao et al., 2012). Therefore, a comprehensive
50 understanding of the magnitude and variability of turbulent fluxes is essential to accurately quantify
51 glacier SEB and project future glacier mass-balance changes.

52 Currently, glacier turbulent flux data are obtained through two main approaches: direct
53 measurement using the eddy covariance (EC) method and estimation using numerical models. Turbulent
54 flux observations over glaciers on the TP remain scarce, primarily owing to the difficulty of obtaining
55 sustained measurements on glacier surfaces (Box and Steffen, 2001; Cullen et al., 2007; Kuipers
56 Munneke et al., 2009). Notably, Yang et al. (2011) carried out observations over a 3-month period on
57 the Parlung No. 4 Glacier, a maritime glacier on the southeastern TP characterized by high air
58 temperatures and precipitation. They reported that during summer, the observed average H reached 28
59 W m^{-2} , whereas LE remained relatively low at -1 W m^{-2} . However, to date, there have been no reported
60 observations of turbulent fluxes over continental glaciers on the TP characterized by low temperatures
61 and precipitation, one of the most widely distributed glacier types on the TP. This data gap has resulted
62 in an inadequate understanding of the energy balance processes of TP glaciers, which, in turn, is
63 important to understand the climatic mechanisms controlling glacier variations across the TP.



Owing to the scarcity of observational data, numerical modeling has become the primary method by which glacier turbulent fluxes are estimated on the TP (Mölg et al., 2012; Yang et al., 2011; Zhu et al., 2018). Current turbulent flux modeling approaches predominantly rely on Monin–Obukhov similarity theory (MOST) (Monin and Obukhov, 1954), which provides accurate simulations of turbulent fluxes but is computationally intensive. In addition to sophisticated turbulent flux models that strictly implement MOST (Hock and Holmgren, 2005; Yang et al., 2002), various simplified turbulent flux parameterizations have been developed to derive LE and H. To improve computational efficiency, Oerlemans (2000) developed a highly simplified derivative model based on MOST, eliminating typically required iterative calculations. Essery and Etchevers (2004) and Suter et al. (2004) introduced stability functions to simulate turbulent fluxes. Oerlemans and Grisogono (2002) developed a turbulent flux model adapted to local glacier climatic conditions, which considers the influence of glacier wind on turbulent fluxes. However, the modeled turbulent fluxes for a given glacier tend to differ substantially across different turbulent flux parameterizations (Radić et al., 2017). Taking the Zhadang Glacier as an example, Zhang et al. (2016) found that the turbulent heat fluxes were 13.4 and 5.7 W m⁻² for the winter and summer seasons, respectively, during the period 2011–2014; meanwhile, Li et al. (2014) reported that the turbulent heat fluxes were –1 and –11 W m⁻² for the winter and summer seasons, respectively, during the period 2006–2011. The important reasons of such difference are the lack of observational data which can be used to calibrate the turbulent flux parameterizations. evaluations of the accuracy of those different turbulent flux parameterizations remain limited on the TP. Guo et al. (2011) evaluated three turbulent flux parameterizations for the Parlung No.4 Glacier (maritime glacier) and found that the scheme proposed by Yang et al. (2002) produced lower errors in turbulent flux estimates during both individual melt phases and the entire ablation season. Compared with the other two schemes evaluated (Andreas, 1987; Smeets and van den Broeke, 2008), the mean absolute deviation (MAD) was reduced by approximately 12–29%. Yet, no comprehensive analysis exists for continental glaciers and no evaluation of the impact of the various parameterizations on glacier mass balance simulation on the TP. And we still do not know if these parameterizations can accurately capture the influence of extreme weather and climate events on turbulent fluxes. These uncertainties hinder accurate simulations of glacier energy and mass balances and impede a comprehensive understanding of accumulation and ablation processes and the physical relationship between glaciers and climate (Zhu et al., 2023).



93 Here we provide the first systematically analyze of meteorological and glacier mass balance
94 observations and direct eddy-covariance-based turbulent flux measurements at the Dunde Glacier in the
95 Qilian Mountains, the northeastern TP, to evaluate the applicability of multiple widely used turbulent
96 flux methods over continental glaciers on the TP. We systematically analyze observed and modeled
97 turbulent fluxes across multiple temporal scales, including seasonal, daily mean, diurnal, and notably
98 under extreme weather conditions, to test the model robustness. Finally, we assess the influence of the
99 various turbulent flux parameterizations on the simulated glacier mass balance by implementing the
100 parameterizations in the energy and mass balance model. The findings allow us to improve the accuracy
101 of glacier surface energy and mass balance modeling and to advance our understanding of ablation
102 processes on continental glaciers on the TP.

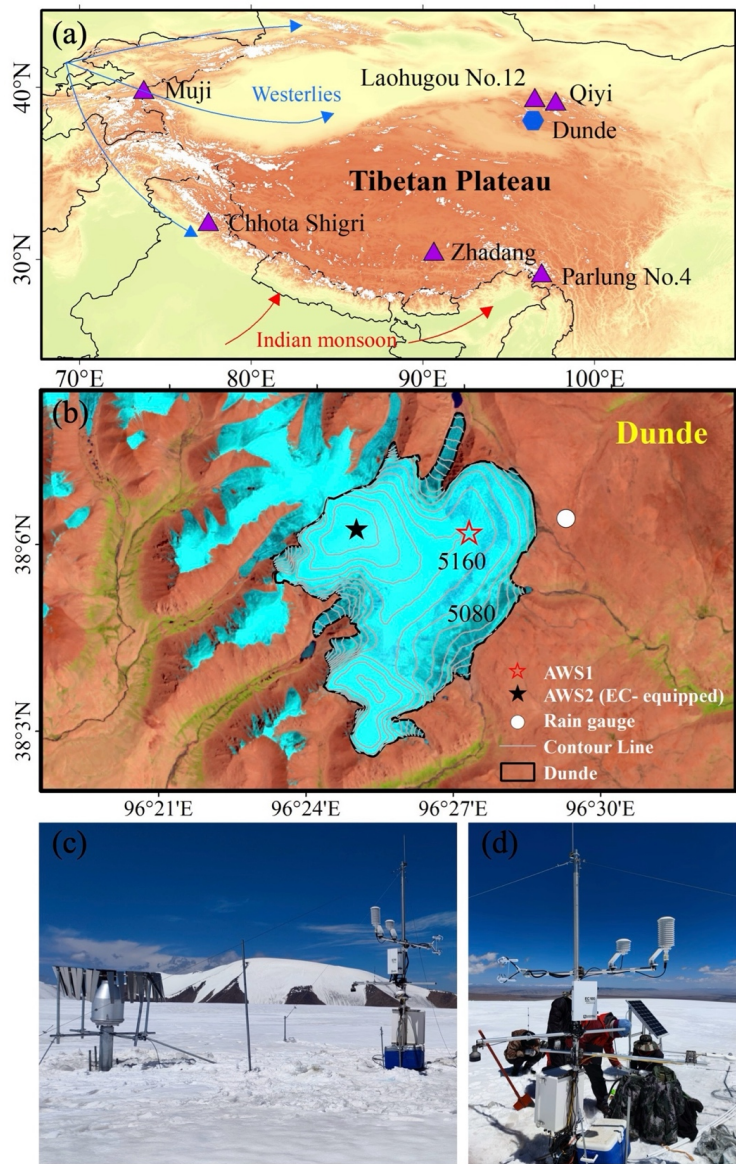
103 **2 Study Area and Data**

104 The Dunde Glacier is located in the western part of the Qilian Mountains, on the northeastern TP.
105 It is a typical continental glacier, with an elevation ranging from 4400 to 5500 m (Guo et al., 2015). The
106 ice cap covers an area of approximately 60 km², with an average annual elevation change rate of $+0.04$
107 ± 0.15 m yr⁻¹ (Hugonnet et al., 2021; Shean et al., 2020). The region experiences pronounced annual and
108 diurnal temperature variations, with a mean annual temperature of approximately -5 °C and annual
109 precipitation ranging from 300 to 400 mm. Meltwater from the glacier primarily feeds into the Tataleng
110 and Haerteng rivers, which provide an important water source to their respective drainage basins.

111 Turbulent fluxes were measured using the eddy covariance (EC) instrument (Campbell-IRGASON),
112 operating from 14 May until 12 October, 2023; this is a widely adopted technique in micrometeorological
113 research that enables real-time, high-precision, and continuous monitoring of atmospheric turbulence.
114 All turbulence raw data were collected at 10 Hz, including the three components of wind velocity, virtual
115 temperature, and water vapor concentration. The observation site was situated on the surface of the
116 Dunde Glacier (38°06'23" N, 96°24'54" E) at an elevation of 5317 m a.s.l., as shown in Fig. 1. In addition,
117 air temperature (T_a), air pressure, relative humidity, wind speed and direction, incoming and outgoing
118 shortwave radiation, incoming and outgoing longwave radiation, and glacier surface height were also
119 measured at this site, using Campbell-ClimaVUE50 automatic weather station (AWS). Precipitation was
120 measured using a Geonor T-200B rain gauge at 4970 m a.s.l., and missing values in the precipitation



121 record were supplemented using ERA5 reanalysis data. Details of the sensors used to measure each
122 variable are provided in Table 1.
123



124
125 **Figure 1:** (a) Locations of the Dundu Glacier (blue hexagon) and selected reference glaciers (purple triangles)
126 on the Tibetan Plateau. (b) Topographic map of the Dundu Glacier (40 m contour intervals) and locations of
127 AWS1 and AWS2 (red and black stars, respectively). (c–d) Photographs of AWS2, equipped with an eddy
128 covariance (EC) system (Photo credit: Meilin Zhu).



129

130 **Table 2: Characteristics of the sensors installed in the eddy covariance system to measure turbulent fluxes**
 131 **and meteorological variables in this study.**

Variable	Symbol (unit)	Sensor	Accuracy	Range	Height
Air temperature	T_a (°C)	Vaisala HMP155A	$\pm (0.055 + 0.0057 \cdot T_a)$ °C	−80 to 60 °C	2.17 m
Relative humidity	RH (%)	Vaisala HMP155A	$\pm 1\%$	0%–100%	2.17 m
Wind speed	u (m s ^{−1})	LICOR LI-7500DS	$\pm 1.5\%$	0–100 m s ^{−1}	2.05 m
Wind direction	WD (°)	LICOR LI-7500DS	$\pm 2^\circ$	360 °	2.05 m
Air pressure	P (pa)	Vaisala PTB210	± 0.5 hPa	50–1100 hPa	2.05 m
Incoming and outgoing longwave radiation	LWI, LWO (W m ^{−2})	Campbell CNR4	$\pm 1\%$	−250 to 250 W m ^{−2}	1.6 m
Incoming and outgoing shortwave radiation	SWI, SWO (W m ^{−2})	Campbell CNR4	$\pm 1\%$	0–2000 W m ^{−2}	1.6 m
Precipitation	(mm)	Geonor T-200B	$\pm 0.1\%$ FS	0–600 mm	1.7 m

132 3 Methods

133 The naming of the turbulent flux calculation methods in this study follows the convention of Radić
 134 et al. (2017). However, differences exist in the implementation of the C_{M-O} method (3.5). Specifically,
 135 although both our C_{M-O} method and that of Radić et al. (2017) are based on the bulk aerodynamic method
 136 combined with Monin–Obukhov similarity theory and iterative closure of the H , the source of roughness
 137 lengths is treated differently. Radić et al. (2017) prescribed fixed roughness lengths obtained as the
 138 logarithmic means of 30-min OPEC inversions under near-neutral conditions, whereas in this study, the
 139 roughness lengths are computed dynamically following Andreas (1987), as functions of the friction
 140 velocity and the Reynolds number. This modification allows the scalar roughness lengths (z_{0t} and z_{0e})
 141 to respond to changes in atmospheric stability and flow regime, thereby providing a more physically
 142 responsive formulation.

143 3.1. C_{kat} method



144 The C_{kat} method incorporates the influence of glacier winds (katabatic flows) on surface energy
145 fluxes using the bulk aerodynamic method, which relates turbulent fluxes to the structure of the ambient
146 atmosphere (Oerlemans and Grisogono, 2002). In a stably stratified atmosphere, it identifies H and
147 vertical advection as the primary contributors to the surface energy budget; LE and H are expressed as:

$$148 \quad LE = 0.622\rho L_{s/f}C_{kat}(e_a - e_s), \quad (1)$$

$$149 \quad H = 0.622C_pC_{kat}(T_a - T_s), \quad (2)$$

150 where, ρ and C_p are the density ($\text{kg}\cdot\text{m}^{-3}$) and heat capacity of air, respectively; $L_{s/f}$ is the latent heat
151 of sublimation/fusion, selected based on surface temperature; e_a and e_s are the atmospheric vapor
152 pressure and saturated vapor pressure at the glacier surface (Pa), respectively; T_a and T_s denote the air
153 temperature and glacier surface temperature, respectively; and C_{kat} is the katabatic bulk exchange
154 coefficient, calculated using the following equation:

$$155 \quad C_{kat} = -C_{tub}C_{tub2}^2C\left(\frac{g}{T_0\gamma P_r}\right)^{1/2}, \quad (3)$$

156 Here, C_{tub} and C_{tub2} are dimensionless empirical constants; $T_0 = 273.15$ K; γ is the potential
157 temperature gradient; P_r is the Prandtl number (~ 0.71); and g is gravitational acceleration (~ 9.8
158 $\text{m}\cdot\text{s}^{-2}$).

159 3.2. C_{log} method

160 This method represents a highly simplified derivative of MOST (Oerlemans, 2000). It does not
161 dynamically adjust atmospheric stability, and instead retains only a linear relationship for surface fluxes;
162 LE and H are expressed as:

$$163 \quad LE = 0.622\rho L_{s/f}C_h u(e_a - e_s)/P, \quad (4)$$

$$164 \quad H = \rho C_p C_h u(T_a - T_s), \quad (5)$$

165 where, u is wind speed ($\text{m}\cdot\text{s}^{-1}$), P is atmospheric pressure (Pa), and C_h is the turbulent exchange
166 coefficient.

167 3.3. C_{Rib1} method



The C_{Rib1} method replaces the Monin–Obukhov length (L) with the bulk Richardson number (Ri_b) to diagnose atmospheric stability (Suter et al., 2004). It replaces the stability functions (ψ) in MOST with a composite function ($f_h(Ri_b)$), derived from stability functions for momentum (ϕ_m), heat (ϕ_h), and water vapor (ϕ_q) (Dyer, 1974; Holtslag and Bruin, 1988). This approach avoids complex iterative calculations while preserving the core MOST principle of stability modulated turbulent exchange.

$$LE = \rho L_{s/f} k^2 z_u z_q \left(\frac{\Delta \bar{u} \Delta \bar{q}}{z^2} \right) (\phi_m \phi_h)^{-1}, \quad (6)$$

$$H = \rho C_p k^2 z_u z_t \left(\frac{\Delta \bar{u} \Delta \bar{T}}{z^2} \right) (\phi_m \phi_q)^{-1}, \quad (7)$$

$$\begin{cases} (\phi_m \phi_{h,q})^{-1} = (1 - 5Ri_b)^2 & (Rib > 0) \\ (\phi_m \phi_{h,q})^{-1} = (1 - 16Ri_b)^{0.75} & (Rib \leq 0) \end{cases}, \quad (8)$$

$$Ri_b = \frac{g \frac{\Delta T}{\Delta z}}{\bar{T} \left(\frac{\Delta \bar{u}}{\Delta z} \right)^2}, \quad (9)$$

where, k (~ 0.4) is the von Kármán constant; $\bar{u}$, $\bar{q}$, and $\bar{T}$ represent the mean wind speed, specific humidity, and air temperature, respectively; z is the measurement height, where $z_{u,t,q}$ are the log mean heights defined as:

$$z_{u,t,q} = \frac{z - z_{0u,t,q}}{\ln \left(\frac{z}{z_{0u,t,q}} \right)}, \quad (10)$$

and $z_{0u,t,q}$ denotes the surface roughness lengths for momentum, humidity, and temperature, which are typically assumed equal.

3.4. C_{Rib2} method

Similar to C_{Rib1} , the C_{Rib2} method is a non-iterative method for calculating turbulent fluxes (Essery and Etchevers, 2004). It replaces L and ψ with Ri_b and $f_h(Ri_b)$, respectively, thereby reducing computational complexity while preserving the physical consistency of MOST. Turbulent fluxes in the C_{Rib2} method are calculated as:

$$LE = \rho L_{s/f} C_H u [q_{sat}(T_s, P_s) - q], \quad (11)$$

$$H = \rho C_p C_H u [T_s - T_a], \quad (12)$$

where, $q_{sat}(T_s, P_s)$ denotes the saturation specific humidity at surface temperature T_s and pressure P_s , and C_H is a surface exchange coefficient. Following Louis (1979), the exchange coefficient for surface



192 sensible and latent heat flux is calculated as $C_H = C_{Hn} f_h$, where

$$193 \quad C_{Hn} = 0.16 \left[\ln \left(\frac{z_1}{z_0} \right) \right]^{-2}, \quad (13)$$

194 is the neutral exchange coefficient for roughness length z_0 and

$$195 \quad f_h = \begin{cases} (1 + 10Ri_b)^{-1} & Ri_b \geq 0 \\ 1 - 10Ri_b(1 + 10Ri_b C_{Hn} \sqrt{-Ri_b/f_z})^{-1} & Ri_b < 0 \end{cases}, \quad (14)$$

196 with

$$197 \quad f_z = \frac{1}{4} \left(\frac{z_0}{z_1} \right)^{1/2}, \quad (15)$$

198 Although atmospheric stability is also characterized by Ri_b , the calculation approach in C_{Rib2} method

199 differs from that in C_{Rib1} method as follows:

$$200 \quad Ri_b = \frac{gz_1}{u^2} \left\{ \frac{T_a - T_s}{T_a} + \frac{q - q_{sat}(T_s, P_s)}{q + \epsilon/(1 - \epsilon)} \right\}, \quad (16)$$

201 where, z_1 is the observation height and ϵ is the ratio of the molecular weights of water and dry air.

202 3.5. C_{M-O} method

203 This method, which adds stability corrections using universal stability functions, employs a
204 complete MOST framework that explicitly calculates the friction velocity (u^*), ψ , and L (Hock and
205 Holmgren, 2005). It separately applies roughness lengths for temperature (z_{0t}), humidity (z_{0e}), and
206 momentum (z_{0w}). Iterative calculations ensure closure of the turbulent fluxes, utilizing nonlinear stability
207 functions from Beljaars and Holtslag (1991) under stable conditions, and Businger–Dyer expressions for
208 unstable conditions, iteratively solving for u^* and L (Beljaars and Holtslag, 1991; Paulson, 1970).

$$209 \quad LE = L_{s/f} \frac{0.622\rho}{P_0} \frac{k^2}{\left[\ln \left(\frac{z}{z_{0w}} \right) - \psi_M \left(\frac{z}{L} \right) \right] \left[\ln \left(\frac{z}{z_{0e}} \right) - \psi_E \left(\frac{z}{L} \right) \right]} u(e_a - e_s), \quad (17)$$

$$210 \quad H = \rho C_p \frac{k^2}{\left[\ln \left(\frac{z}{z_{0w}} \right) - \psi_M \left(\frac{z}{L} \right) \right] \left[\ln \left(\frac{z}{z_{0t}} \right) - \psi_H \left(\frac{z}{L} \right) \right]} u(T_a - T_s), \quad (18)$$

211 3.6. Evaluation of model performance

212 We used three statistical measures to quantify model accuracy: root mean square error (RMSE),
213 MAD, and mean bias error (MBE). The RMSE quantifies the differences between observed (Q_o) and
214 modeled (Q_m) fluxes:



215
$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Q_{mi} - Q_{oi})^2}, \quad (19)$$

216 The MAD reflects the average magnitude of deviations:

217
$$MAD = \frac{1}{n} \sum_{i=1}^n |Q_{oi} - Q_{mi}|, \quad (20)$$

218 The MBE represents systematic biases in model predictions:

219
$$MBE = \frac{1}{n} \sum_{i=1}^n (Q_{oi} - Q_{mi}), \quad (21)$$

220 **4 Results**

221 **4.1 Meteorological conditions on the Dundee Glacier**

222 Meteorological data observed at 5317 m a.s.l., including air temperature (T_a), glacier surface
223 temperature (T_s), relative humidity (RH), wind speed (u) and direction (WD), and atmospheric pressure
224 (Pres), were collected from 14 May to 12 October, 2023 (Fig. 2). During the study period, daily mean T_a
225 at the Dundee Glacier ranged from -14.1 to 3.3 °C, averaging -4.0 °C (Fig. 2a). Instances of a daily mean
226 T_a above 0 °C occurred primarily in July and August, which are the warmest months, with a mean value
227 of -1 °C. October was the coldest month, with an average daily mean T_a of -9.5 °C. Air temperature
228 exhibited pronounced seasonal variability, with higher summer averages (-2.1 °C) compared with spring
229 (-7.8 °C) and autumn (-6.5 °C). The mean daily T_s was -5.4 °C, ranging from -17.2 °C (7 October) to
230 0 °C (10 and 11 July, and 14 and 16 August; Fig. 2c). Seasonal variations in T_s closely mirrored those of
231 T_a , peaking in summer (average of -3.4 °C) and dropping substantially in spring (average of -9.0 °C)
232 and autumn (average of -8.3 °C). The difference between T_a and T_s also exhibited seasonal variability,
233 reaching a maximum in autumn (1.8 °C), with lower values in spring (1.2 °C) and summer (1.3 °C). In
234 addition, both T_a and T_s displayed clear diurnal cycles, characterized by single-trough and single-peak
235 patterns; T_s peaked at -1.0 °C around 14:00, while T_a reached a maximum of -2.0 °C at 16:00, about
236 two hours later. In contrast, both T_s and T_a exhibited minimum values at 06:00, with T_s dropping to
237 -9.4 °C and T_a to -5.6 °C. The earlier T_s peak is interpreted to reflect the rapid radiative response of the
238 glacier surface to incoming solar radiation; T_a responds more slowly owing to the thermal inertia of air
239 and gradual development of convective mixing. At night, however, both the glacier surface and air cool
240 synchronously under stable stratification and weak turbulence, resulting in the coincident early morning
241 T_s and T_a minima. Generally, T_a was higher than T_s for most of a given day, indicative of a persistent



242 near-surface temperature inversion layer over the glacier surface (Fig. 2b and d).

243 Mean daily relative humidity at the Dundee Glacier was 56.3%, with notable seasonal variability
244 (Fig. 2e). The highest seasonal average occurred in spring (62.6%), whereas autumn was the driest season
245 (50.7%), particular September, which recorded the lowest monthly average (47.5%). On a diurnal scale,
246 relative humidity exhibited an inverse pattern compared with that of T_a , characterized by a distinct
247 midday trough and nighttime peak (Fig. 2f). Daily minimum humidity typically occurred around noon,
248 coinciding with peak solar radiation and higher T_a . Thereafter, relative humidity gradually increased,
249 reaching a maximum of 58.8% at approximately 21:30; this likely resulted from the combined effects of
250 rapid radiative cooling of the glacier surface, low T_a , and weak wind conditions.

251 Daily mean wind speeds ranged from 1.7 to 10.5 m s⁻¹, averaging 4.1 m s⁻¹, with marked seasonal
252 variability (Fig. 2g). The strongest winds occurred during spring (average of 5.51 m s⁻¹), while summer
253 recorded the weakest winds (average of 3.6 m s⁻¹), particularly August, which recorded the lowest
254 monthly mean (3.1 m s⁻¹). Autumn wind speeds were intermediate, averaging 4.6 m s⁻¹. On a diurnal
255 scale, wind speed exhibited substantial variation, with an average diurnal range of 1.5 m s⁻¹. Morning
256 winds were generally weak, increasing notably after 10:30, peaking around 15:30, and subsequently
257 decreasing to a daily minimum around 23:30 (Fig. 2h). Nighttime wind speeds remained relatively stable,
258 associated with stable atmospheric stratification. Prevailing wind directions were westerly and
259 northwesterly (Fig. 2i and j), highlighting the dominant influence of the mid-latitude westerlies on
260 regional meteorological conditions.

261 Daily mean atmospheric pressure at the Dundee Glacier during our study period ranged from 527.9
262 to 538.4 hPa, with an average of 534.4 hPa (Fig. 2k). The highest seasonal mean atmospheric pressure
263 occurred in summer (535.2 hPa) and the lowest in spring (530.6 hPa). On a diurnal scale, atmospheric
264 pressure exhibited a distinct double-peak, double-trough daily pattern, with minimum pressure occurring
265 at 06:00, maximum at 23:30, a secondary minimum between 17:30 and 18:00, and a secondary maximum
266 at 12:00 (Fig. 2l). Variations in atmospheric pressure markedly influence glacier surface energy exchange
267 by altering specific humidity gradients and air density, thus indirectly controlling turbulent fluxes on the
268 glacier surface.

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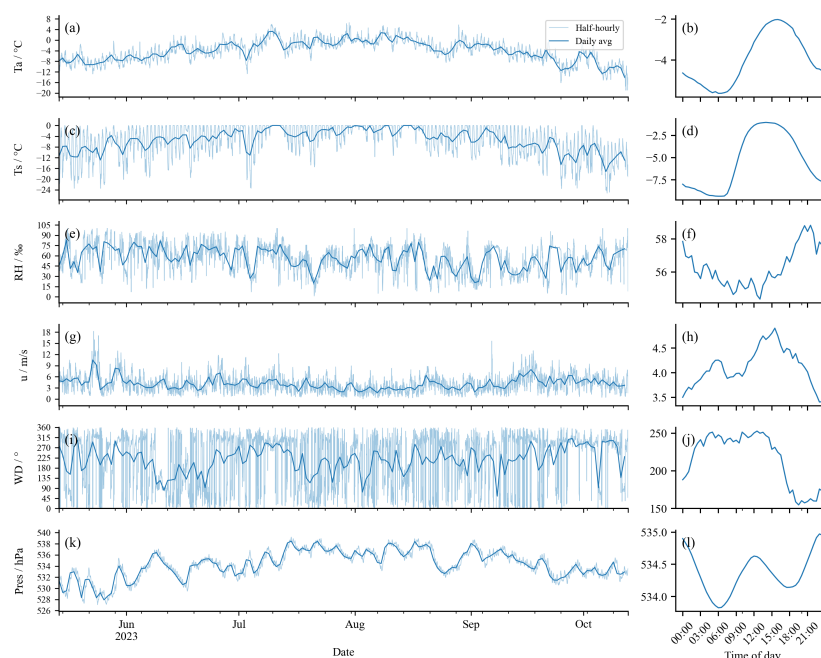


Figure 2. Half-hourly and daily average values (left panels) together with mean diurnal cycles (right panels) of six meteorological variables at the Dundee Glacier for the period May–October, 2023: (a, b) air temperature (T_a); (c, d) surface temperature (T_s); (e, f) relative humidity (RH); (g, h) wind speed (u); (i, j) wind direction (WD); and (k, l) atmospheric pressure (Pres).

4.2 Observed turbulent fluxes on the Dundee Glacier

Herein, turbulent fluxes are defined as positive when directed from the atmosphere to the glacier, and negative in the opposite direction. Figure 3 shows that the observed daily mean LE ranged from -35.9 W m^{-2} (21 August, 2023) to 10.4 W m^{-2} (11 July, 2023), with an average of -9.6 W m^{-2} over the study period, indicating persistent sublimation/evaporation from the glacier surface. There was notable seasonal variability, with the absolute mean seasonal LE being highest in spring (-15.1 W m^{-2}), lowest in autumn (-8.1 W m^{-2}), and moderate in summer (-10.4 W m^{-2}), reflecting varying intensities of moisture exchange between the glacier and the atmosphere (Fugger et al., 2022).

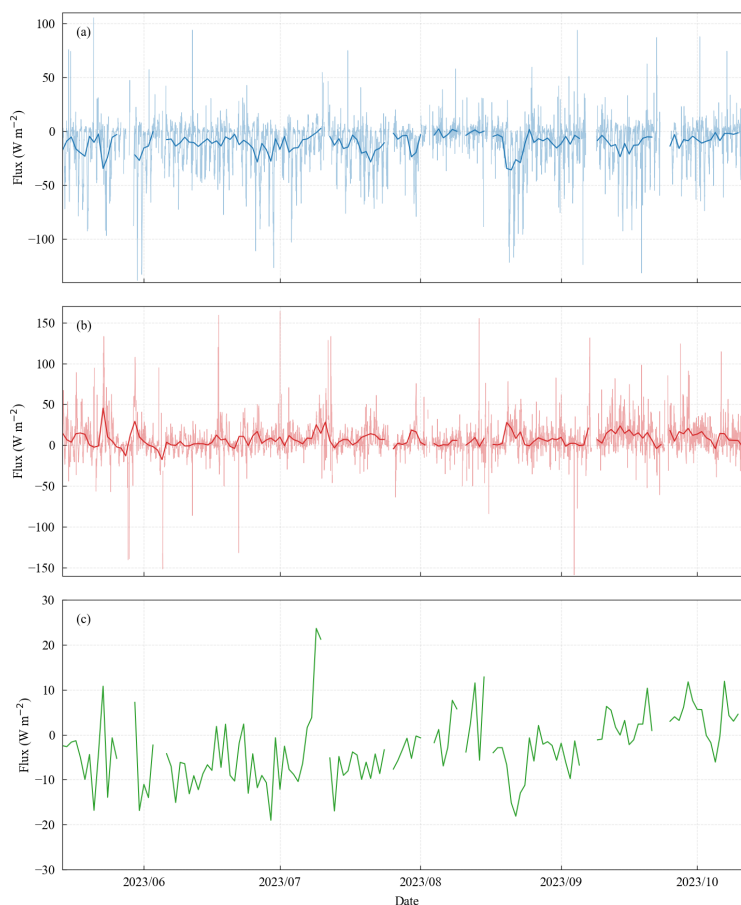
In contrast, observed H was generally positive, averaging 6.9 W m^{-2} , indicating continuous heat transfer from the atmosphere to the glacier. There were pronounced seasonal variations, with high mean H values in spring (9.3 W m^{-2}) and autumn (9.2 W m^{-2}), and a monthly peak in September (10.1 W m^{-2}).



287 The lowest values were recorded in summer, which averaged 5.4 W m^{-2} , with June having the lowest
288 monthly average (3.1 W m^{-2}).

289 Overall, the absolute magnitude of LE generally exceeded that of H. This resulted in a
290 predominantly negative total turbulent flux (LE + H), averaging -2.9 W m^{-2} , indicating net heat loss
291 from the glacier through turbulent exchange. From May to mid-September, the total turbulent flux was
292 negative (glacier losing energy), while from mid-September to mid-October, it became positive (glacier
293 receiving energy). June exhibited the strongest turbulent flux (-8.0 W m^{-2}), whereas September recorded
294 the weakest (1.5 W m^{-2}). These findings underscore the overall state of heat loss from the glacier through
295 turbulent fluxes during the study period.

296



297



Figure 3: Half-hourly (thin lines) and daily average (thick lines) variations in (a) latent heat flux, (b) sensible heat flux, and (c) total turbulent flux over the Dundee Glacier during the study period. The green line in (c) represents the daily average of total turbulent flux.

4.3 Evaluation of different turbulent flux parameterizations

In this section, we present the results of our evaluation of the simulation ability of five turbulent flux methods (C_{kat} , C_{log} , C_{Rib1} , C_{Rib2} , and C_{M-o}) across different timescales.

4.3.1 Overall model performance during the entire study period

We compared the temporal evolution of modeled LE and H at the Dundee Glacier against in-situ observations (Fig. 4). Over the observation period, all models captured the general trend of turbulent fluxes reasonably well. However, during May, when turbulent fluxes fluctuated to the greatest degree, all model simulations substantially underestimated the observed variability. Model-simulated H also deviated considerably from observations in early to mid-September, characterized by systematic underestimation. Additionally, during abrupt changes in observed LE in late June and mid-August, the C_{kat} and C_{log} methods failed to reproduce the observed flux transitions, markedly underestimating LE during these periods.

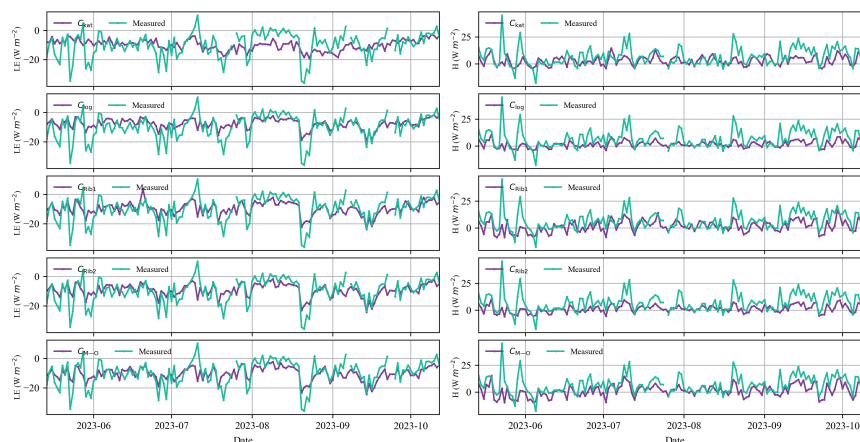


Figure 4: Time series of daily mean latent heat (LE) and sensible heat (H) fluxes modeled by the five different schemes (C_{kat} , C_{log} , C_{Rib1} , C_{Rib2} , and C_{M-o}) compared with eddy covariance-derived values (measured).



Statistical comparisons between modeled and observed fluxes were conducted for the entire study period to quantitatively assess method performance (Table 2). For LE, C_{kat} and $C_{\text{M-O}}$ method slightly underestimated the flux, while the other three methods (C_{log} , C_{Rib1} and C_{Rib2}) tended to give overestimations. The C_{kat} method exhibited the highest RMSE and MAD values, indicating poorer LE simulation accuracy compared with the other methods. Meanwhile, C_{log} presented the largest systematic bias (MBE = 1.96). Hence, the C_{Rib1} , C_{Rib2} , and $C_{\text{M-O}}$ methods performed best in terms of LE, with the C_{Rib1} and C_{Rib2} methods slightly underestimating the flux, and the $C_{\text{M-O}}$ method slightly overestimating it. For H, all methods showed some underestimation, with the C_{kat} and $C_{\text{M-O}}$ methods exhibiting lower RMSE values (8.60 and 8.63 W m^{-2} , respectively), indicating the best accuracy among the tested methods.

Table 2: Comparative statistics of modeled latent heat (LE) and sensible heat (H) fluxes over the entire study period (based on adjusted parameterizations) against eddy covariance observations. RMSE = root mean square error; MAD = mean absolute deviation; MBE = mean bias error.

Method	LE (W m^{-2})			H (W m^{-2})		
	RMSE	MAD	MBE	RMSE	MAD	MBE
C_{kat}	7.96	6.12	-0.31	8.60	6.02	-3.83
C_{log}	6.82	4.82	1.96	8.82	6.08	-5.17
C_{Rib1}	6.62	4.78	0.03	8.80	6.43	-5.16
C_{Rib2}	6.35	4.48	0.30	8.85	6.22	-5.58
$C_{\text{M-O}}$	6.36	4.64	-0.66	8.63	6.18	-5.46

4.3.2 Seasonal variability in method performance

To further explore method behavior under different atmospheric conditions, we conducted seasonal evaluations of the five turbulent flux methods, providing critical insights into their applicability across varying meteorological regimes (Table 3). All five methods exhibited similar patterns of seasonal error. For LE, the largest simulation errors occurred in spring, typically manifested as underestimations, while the smallest errors were found in autumn, with a tendency for slight overestimations. For H, the largest errors occurred in spring and the smallest in summer, with underestimations in both cases. These findings suggest that the simulation accuracy of all methods decreases under conditions of intense turbulent exchange, such as high temperature, humidity, and wind speed, whereas performance is more stable



342 during other seasons.

343 In a seasonal context, for LE, all parameterizations consistently exhibited the lowest simulation
344 accuracy in spring (Table 3). The C_{M-O} scheme achieved the best spring performance, with an RMSE of
345 8.48 W m^{-2} and MAD of 6.59 W m^{-2} , these values being markedly lower than those of the other schemes.
346 In summer, the C_{Rib2} and C_{M-O} methods exhibited the lowest RMSE values, outperforming the other
347 schemes. In autumn, the C_{log} method yielded the best LE simulation performance (RMSE: 3.86 W m^{-2} ,
348 MAD: 2.68 W m^{-2}), while the C_{kat} method exhibited the lowest accuracy. The remaining schemes
349 displayed intermediate and comparable performances. In addition, the C_{kat} and C_{log} methods exhibited
350 the greatest seasonal variability in accuracy, with RMSE differences between spring and autumn reaching
351 6.84 and 6.70 W m^{-2} , respectively, indicating poor seasonal consistency and limited robustness under
352 non-extreme conditions. In contrast, the C_{M-O} method demonstrated remarkable seasonal stability, with
353 only a 3.26 W m^{-2} difference in RMSE between spring and autumn, highlighting its adaptability and
354 robustness across seasons.

355 For H, all methods exhibited reduced accuracy in spring, although the C_{kat} method performed
356 relatively well with a RMSE of 13.78 W m^{-2} , MAD of 8.65 W m^{-2} , and MBE of -6.3 W m^{-2} . Other
357 methods showed similar spring statistics. Summer was the best-performing season for H across all
358 parameterizations, with the C_{M-O} method achieving the lowest summer errors. In autumn, both C_{kat} and
359 C_{M-O} yielded relatively low RMSE values (8.71 and 8.73 W m^{-2} , respectively), while the C_{Rib2} method
360 exhibited the highest RMSE at 9.19 W m^{-2} ; the remaining schemes produced intermediate and
361 comparable results. Overall, the C_{M-O} method achieved the best performance for H during both summer
362 and autumn.

363

364 **Table 3: Seasonal performance of latent heat (LE) and sensible heat (H) flux methods, evaluated against eddy**
365 **covariance observations. RMSE = root mean square error; MAD = mean absolute deviation; MBE = mean**
366 **bias error.**

Method	Season	LE (W m^{-2})			H (W m^{-2})		
		RMSE	MAD	MBE	RMSE	MAD	MBE
C_{kat}	Spring	12.78	9.66	7.02	13.78	8.65	-6.30
	Summer	7.47	5.99	-1.13	7.07	5.17	-2.61
	Autumn	5.94	4.81	-1.76	8.71	6.73	-5.41



$C_{\log}$	Spring	10.56	8.10	6.39	14.19	9.18	-7.77
	Summer	6.86	5.07	2.21	7.13	5.01	-3.98
	Autumn	3.86	2.68	-0.65	9.12	7.08	-6.64
C_{Rib1}	Spring	9.41	7.06	4.20	14.79	10.71	-9.67
	Summer	6.49	4.71	0.41	7.01	5.42	-3.79
	Autumn	5.19	3.87	-2.79	8.83	6.79	-6.19
C_{Rib2}	Spring	9.37	7.05	4.61	14.48	9.85	-8.88
	Summer	6.22	4.49	0.66	7.04	5.06	-4.32
	Autumn	4.70	3.29	-2.55	9.19	7.16	-6.90
$C_{\text{M-O}}$	Spring	8.48	6.59	2.92	14.81	10.71	-9.88
	Summer	6.32	4.55	-0.14	6.70	5.01	-4.26
	Autumn	5.22	3.94	-3.51	8.73	6.78	-6.16

367

368 4.3.3 Evaluation of diurnal variations

369 An evaluation of diurnal variations in modeled turbulent fluxes offers important diagnostic
370 information on the simulation ability of a given parameterization. At the diurnal scale, the simulated
371 turbulent fluxes aligned well with in-situ observations, with both LE and H exhibiting a distinct single-
372 trough daily pattern (Fig. 5). For LE, the simulated values obtained from all methods exhibited higher
373 accuracy during nighttime and early morning hours, with smaller deviations from observed values (Fig.
374 5a). In contrast, during periods of intense flux variability—typically around noon—method performance
375 declined, and simulation errors became larger. For H, the methods generally performed better than for
376 LE during noon, but all exhibited limited capability in capturing the early-morning fluctuations (Fig. 5b).
377 Among the five schemes, the $C_{\text{M-O}}$ method exhibited the best overall performance (Fig. 5); it accurately
378 captured turbulent fluxes during the relatively stable 18:00–08:00 period, and despite some degree of
379 error, it most effectively reproduced the pronounced fluctuations in LE and H during the period of
380 intensified flux activity (13:00–15:00).

381

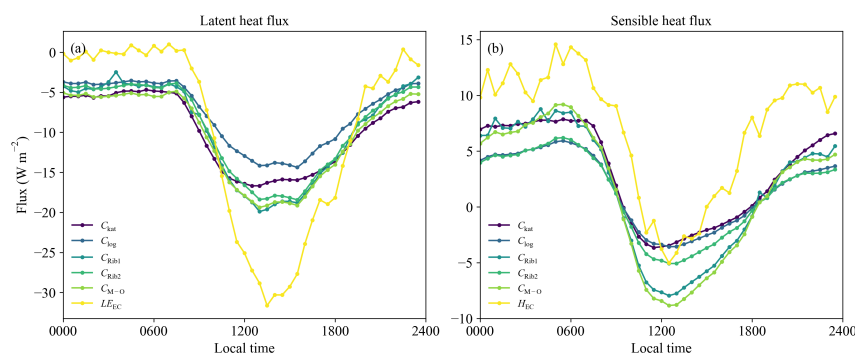


Figure 5: Mean diurnal cycles of modeled latent heat and sensible heat fluxes obtained from the five different schemes (C_{kat} , C_{log} , C_{Rib1} , C_{Rib2} , and C_{M-O}) compared with eddy covariance-derived values (LE_{EC} and H_{EC}).

In summary, among the five evaluated methods, the C_{M-O} method delivered the most accurate and stable performance for LE throughout the study period, and it also ranked among the top performers for H. Both the C_{kat} and C_{M-O} methods performed well for H, without any substantial seasonal deficiencies. Moreover, the C_{M-O} method also demonstrated the best agreement with observations in reproducing the diurnal variations in LE and H across different seasons. Therefore, the C_{M-O} method emerges as a particularly suitable option for simulating turbulent fluxes on the Dundee Glacier, offering both high accuracy and temporal robustness on daily and seasonal scales.

5 Discussion

5.1 Differences in performance among turbulent flux methods

Variations in the performance of different turbulent flux parameterizations primarily arise from their respective approaches to computing turbulent exchange coefficients and applying atmospheric stability corrections. These methodological differences directly affect method accuracy under varying temperature gradients, humidity gradients, and wind speed conditions, leading to discrepancies in the simulated LE and H.

The C_{kat} method explicitly considers katabatic flows, introducing the katabatic bulk exchange coefficient (C_{kat}) to partially overcome the limitations of MOST during strong katabatic wind conditions (Oerlemans and Grisogono, 2002). This approach emphasizes intensified katabatic turbulence during nocturnal cooling or cold-air intrusions, enhancing turbulent exchange (Horst and Doran, 1988). However, the C_{kat} method lacks explicit stability corrections and dynamic roughness length adjustment,



405 leading to a slow response under rapidly changing surface conditions (Denby, 2000). Hence, its
406 application is more suited to small and medium-sized glaciers rather than large-scale domains such as
407 the Greenland Ice Sheet.

408 The $C_{\log}$ method employs a constant exchange coefficient (C_H) driven by near-surface wind speed
409 and the difference in air temperature (or humidity) and surface temperature (or humidity), providing a
410 simplified, computationally efficient structure suitable for large-scale climate models (Oerlemans, 2000).
411 Being a wind-speed-driven scheme, it performs well under less stable stratification conditions. However,
412 the method also exhibits certain limitations. Owing to the absence of atmospheric stability parameters in
413 its structure, it cannot identify or respond to surface inversions forming at night or in the early morning.
414 Herein, the LE RMSE in spring reached 10.56 W m^{-2} , ranking among the largest errors of all evaluated
415 methods (Table 3); this method also exhibited substantial diurnal simulation errors.

416 The C_{Rib1} and C_{Rib2} methods are based on a single-step turbulence parameterization method centered
417 on the Richardson number for stability correction. Their structures are concise, do not rely on multi-level
418 observational data, and avoid complex iterative procedures, making them among the most robust
419 parameterization schemes for simulating turbulent fluxes. However, these approaches also have
420 limitations. They do not dynamically iterate L , which limits their responsiveness to complex and rapidly
421 changing atmospheric conditions when compared with fully dynamic MOST-based methods (Högström,
422 1988). In addition, the adjustment of z_0 not only affects the simulation of turbulent fluxes but also
423 influences surface albedo, complicating independent parameter calibration and hindering reliable flux
424 validation.

425 The $C_{\text{M-O}}$ method, which exhibited the best performance among all evaluated methods in this study,
426 adopts a complete implementation of the MOST framework, explicitly calculating u^* , stability correction
427 functions, and L . The scheme separately applies distinct roughness lengths for momentum (z_{0w}),
428 temperature (z_{0t}), and humidity (z_{0e}), enhancing physical consistency in flux estimation. The utilization
429 of a robust iterative algorithm ensures energy balance closure. From our overall statistical evaluation, the
430 $C_{\text{M-O}}$ method achieved one of the best performances among the five evaluated methods, with an RMSE
431 of only 6.36 W m^{-2} for LE and 8.63 W m^{-2} for H (Table 2). More importantly, the $C_{\text{M-O}}$ method exhibited
432 minimal seasonal variability in flux estimation accuracy. The RMSE values for LE in spring, summer,
433 and autumn were 8.48 , 6.32 , and 5.22 W m^{-2} , respectively, giving an inter-seasonal RMSE difference of
434 approximately 3.3 W m^{-2} , much smaller than the differences observed in other methods (e.g., a difference



435 exceeding 5 W m^{-2} for the C_{Rib1} method). Additionally, the $C_{\text{M-O}}$ method demonstrated higher sensitivity
436 and precision in simulating diurnal variations in turbulent fluxes, showing the closest alignment with
437 observed diurnal cycles of LE and H, particularly during periods of intense midday convection.
438 Nonetheless, the $C_{\text{M-O}}$ method also possesses structural limitations. Specifically, the roughness lengths
439 (z_{0t} , z_{0e} , and z_{0w}) lack direct observational support, necessitating iterative parameter calibration,
440 thereby reducing method interpretability and generalizability.

441 **5.2 Performance improvement of the SEB model by optimizing turbulent flux methods**

442 To assess the importance of turbulent flux methods in simulating glacier mass balance, we included
443 three representative turbulent flux methods (the C_{log} , C_{Rib2} , and $C_{\text{M-O}}$ methods) in a coupled energy
444 balance–snow and firn model (EBFM; Van Pelt et al., 2012, 2019) applied at the point scale. The
445 turbulent fluxes, T_s , ice surface height, and cumulative mass balance (CMB) were simulated using both
446 original and recalibrated parameters, and compared against observational data (Fig. 6). Quantitative
447 evaluation indices, including the correlation coefficient (R), RMSE, and MAD and estimates of CMB,
448 were used to demonstrate improvements resulting from model optimization (Table 4).

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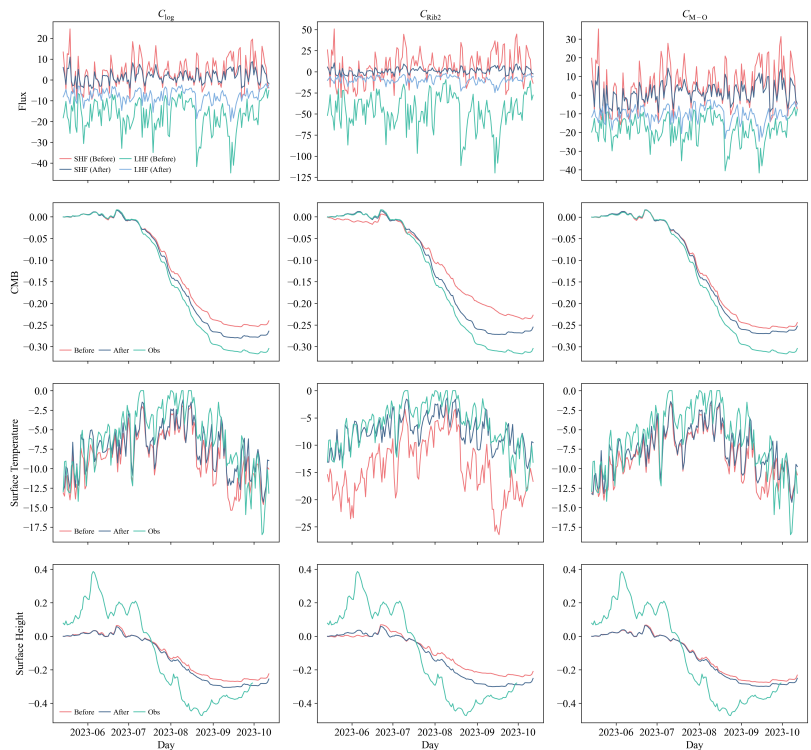


Figure 6: Time series of turbulent fluxes, cumulative mass balance (CMB), surface temperature, and surface height over the Dundee Glacier during the study period, based on original methods (before), recalibrated methods (after), and observations (obs).

Table 4: Comparative statistics between observations and surface energy balance model simulations of surface temperature (T_s), surface height, and cumulative mass balance at the Dundee Glacier, using both original (before) and recalibrated (after) parameters.

Method	Before			After		
	T_s	Surface height	Mass balance	T_s	Surface height	Mass balance
C_{log}	$R = 0.84$ $RMSE = 3.26$	$R = 0.93$ $RMSE = 0.16$ $MAD = 0.14$	-238.41	$R = 0.85$ $RMSE = 2.45$	$R = 0.93$ $RMSE = 0.15$ $MAD = 0.14$	-262.14
C_{Rib2}	$R = 0.78$ $RMSE = 8.79$	$R = 0.91$ $RMSE = 0.18$ $MAD = 0.16$	-225.77	$R = 0.85$ $RMSE = 2.53$	$R = 0.93$ $RMSE = 0.15$ $MAD = 0.13$	-252.87
C_{M-O}	$R = 0.86$ $RMSE = 3.16$	$R = 0.94$ $RMSE = 0.16$ $MAD = 0.14$	-242.41	$R = 0.86$ $RMSE = 2.53$	$R = 0.94$ $RMSE = 0.14$ $MAD = 0.13$	-256.80



458

459 We first ran the SEB models under uncalibrated conditions with three turbulent flux methods (the
460 C_{log} , C_{Rib2} , and C_{M-O} methods). These gave RMSE values for T_s of 3.26, 8.79, and 2.53 °C, respectively.
461 The R values between modeled and measured T_s exceeded 0.78 for all three schemes. The RMSE values
462 for surface height change ranged from 0.16 to 0.18 m, while the CMB estimates were −238.41, −225.77,
463 and −242.41 mm, respectively, all deviating markedly from the observed value of −304.19 mm.
464 Following parameter calibration, all three schemes exhibited marked improvements in model
465 performance. The C_{Rib2} method showed the greatest improvement, giving a CMB value of −252.87 mm,
466 equating to an error reduction of 34.55% relative to the uncalibrated result. In parallel, the RMSE values
467 for T_s and surface height decreased by 71.2% and 16.6%, respectively. The C_{M-O} method-based model
468 yielded the highest overall accuracy after optimization, with R values of 0.86 for T_s and 0.94 for surface
469 height. Although a residual bias remained in the CMB simulation, it was substantially mitigated
470 compared with the original configuration. Overall, these findings highlight that turbulent flux parameter
471 optimization is an effective approach to improve glacier SEB model accuracy.

472 **5.3 Evaluation of turbulent flux methods under extreme weather conditions**

473 Our analysis above demonstrates that the optimization of turbulent flux parameterizations markedly
474 enhances the accuracy of glacier surface energy and mass balance simulations under the mean climate
475 state (e.g., multi-year averages of T_a and precipitation). However, the ability of SEB models to simulate
476 turbulent fluxes under extreme weather and climate events remains uncertain and warrants further
477 investigation. Between 8 and 11 July, 2023, the Dundee Glacier experienced a typical humid heatwave
478 (Fig. 7). During this event, the daily average air temperature reached 2.4 °C, this being substantially
479 higher than the July average outside of the heatwave event (−1.5 °C). Nighttime air temperatures from 9
480 to 11 July consistently exceeded 0 °C, exhibiting reduced diurnal fluctuations, and then sharply dropped
481 below freezing on 12 July immediately after the heatwave event. Relative humidity during the humid
482 heatwave reached an average of 94.3%, this being markedly higher than during the July non-heatwave
483 period (89.1%). The concurrent anomalies in air temperature and humidity during this humid heatwave
484 would inevitably lead to anomalous turbulent fluxes.

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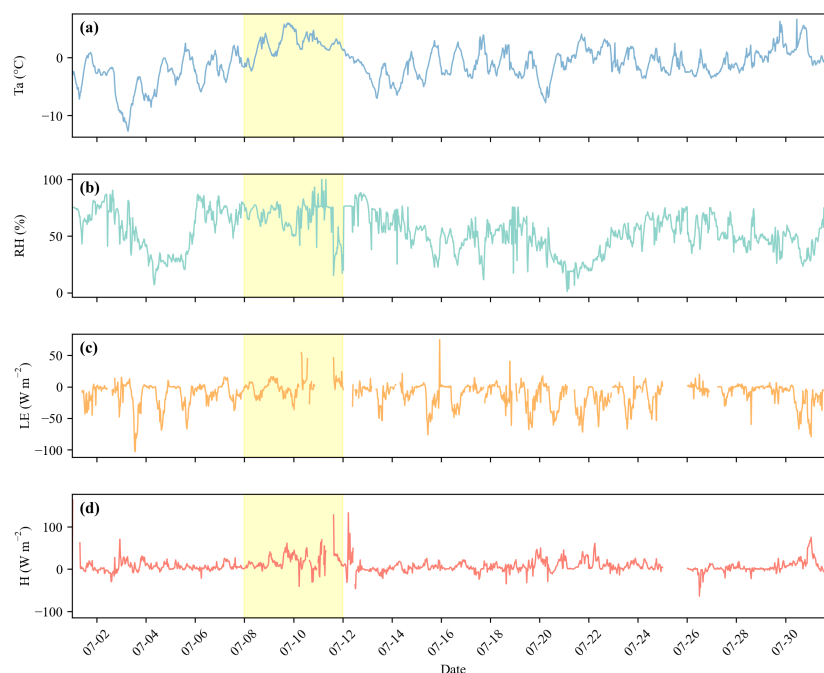


Figure 7: Half-hourly values of (a) air temperature (T_a), (b) relative humidity (RH), (c) latent heat flux (LE), and (d) sensible heat flux (H) over the Dundee Glacier during July, 2023. The yellow-shaded area highlights the period of the humid heatwave event (8–11 July, 2023).

To clarify turbulent flux behaviors under such anomalous climatic conditions, we compared turbulent fluxes during the humid heatwave (8–11 July, 2023) with those during the non-heatwave period (the remainder of July, 2023) based on observational data. The H markedly increased during the humid heatwave, reaching a daily average of 18.3 W m^{-2} , this being nearly three times higher than the non-heatwave average (6.13 W m^{-2}). The peak H of 128.2 W m^{-2} occurred at 15:00 on 11 July, 2023. Moreover, the diurnal variation in H during the heatwave event ranged from 0.85 to 61.2 W m^{-2} , substantially exceeding the range observed during the non-heatwave period (-5.0 to 16.3 W m^{-2}). This extraordinary increase in H during the humid heatwave indicates that substantial heat was transferred from the atmosphere to the glacier during this event. Concurrently, LE exhibited a remarkable reversal during the humid heatwave. During the non-heatwave period, LE remained negative, with an average value of -12.5 W m^{-2} . Such negative LE values are a common characteristic of continental glaciers on the TP. However, during the humid heatwave, LE values became positive, averaging 0.11 W m^{-2} . This shift was further



503 reflected in diurnal LE variations, with a range of -19.2 to 24.3 W m^{-2} during the humid heatwave, which
504 was markedly different from the range of -36.5 to 1.2 W m^{-2} observed during the rest of July. This
505 unusual reversal implies pronounced atmosphere-to-surface moisture condensation, resulting in
506 increased heat input onto the glacier surface (Zhang et al., 2017). Such positive LE values are commonly
507 observed over maritime glaciers (Yang et al., 2011).

508 The glacier surface transitioned into a state of net turbulent energy gain, with the mean total
509 turbulent flux ($LE + H$) reaching 18.53 W m^{-2} during the humid heatwave. In contrast, the non-heatwave
510 period in July was characterized by net turbulent energy loss, averaging -6.25 W m^{-2} . This contrast
511 underscores a distinct shift from turbulent heat loss to heat gain under humid heatwave conditions.
512 Concurrently, surface albedo decreased and melt energy increased, triggering intense ablation. Thus,
513 although short-lived, such anomalous turbulent flux variations during the humid heatwave markedly
514 altered the glacier's energy-balance processes by modifying albedo and melt energy, with potential
515 implications for longer-term melt dynamics (Zhu et al., 2024b).

516 We further evaluated the ability of the five methods to simulate turbulent fluxes under extreme
517 weather and climate events. Among the five turbulent flux methods tested, all captured the pronounced
518 increase in H during the humid heatwave (Fig. 4), with the C_{M-O} method showing the best performance.
519 Although the C_{M-O} method calculated mean (10.2 W m^{-2}) was lower than the observed value
520 (18.3 W m^{-2}), it outperformed the other schemes. The C_{log} method exhibited the poorest performance,
521 simulating a mean H of only 5.3 W m^{-2} . Meanwhile, the mean H values during the humid heatwave
522 simulated by the C_{kat} , C_{Rib1} , and C_{Rib2} methods were 5.7 , 8.9 , and 5.5 W m^{-2} , respectively. In contrast, all
523 methods failed to reproduce the observed reversal of LE during the humid heatwave (Fig. 4). The mean
524 LE values simulated by the C_{kat} , C_{log} , C_{Rib1} , C_{Rib2} , and C_{M-O} methods were -5.8 , -6.2 , -6.7 , -6.9 , and
525 -7.7 W m^{-2} , respectively, all substantially deviating from the observed value of 0.11 W m^{-2} . The reasons
526 behind this discrepancy warrant further investigation. Overall, the methods, particularly the C_{M-O} method,
527 demonstrated a strong response to the anomalous increase in H during the humid heatwave. However,
528 none of the methods captured the observed reversal of LE . All calculated values were markedly lower
529 than the measured values, suggesting that current turbulent flux parameterizations may underestimate
530 the magnitudes of H and LE under extreme meteorological conditions, and hence underestimate their
531 contributions to glacier melting.

532 Under ongoing global warming, the climate system is recording notable warming and moistening



533 trends on the TP (Wang et al., 2010). This means that the TP will likely experience an increased frequency
534 and intensity of humid heatwave events (Zhang et al., 2025). Such conditions will cause continental
535 glaciers, such as the Dundee Glacier, to increasingly exhibit turbulent flux characteristics that resemble
536 those of maritime glaciers, including reversed LE directions and markedly increased H. Thus, continued
537 warming may drive future glacier-type transitions.

538 **6. Conclusions**

539 In this study, we conducted a comprehensive analysis of turbulent fluxes on the continental Dundee
540 Glacier (Qilian Mountains, TP), using continuous meteorological observations and EC flux
541 measurements collected from May to October, 2023. Throughout the observation period, the Dundee
542 Glacier exhibited energy loss through LE (mean = -10.34 W m^{-2}) while simultaneously gaining energy
543 via H from the atmosphere (mean = 6.93 W m^{-2}). Clear seasonal variations in turbulent fluxes were
544 observed: the absolute magnitude of LE was largest in spring (mean -15.1 W m^{-2}) and smallest in autumn
545 (mean -8.1 W m^{-2}), whereas H was higher during spring and autumn (means 9.3 and 9.2 W m^{-2} ,
546 respectively) and lower in summer (mean 5.4 W m^{-2}). The magnitude of LE exceeded that of H, resulting
547 in continuous net heat loss from the glacier surface via turbulent exchange.

548 In addition, we systematically assessed the performance of commonly used turbulent flux methods.
549 Among the five schemes evaluated, the method based on Monin–Obukhov similarity theory with
550 universal stability functions demonstrated the best overall performance in simulating turbulent fluxes,
551 both in terms of simulation accuracy (RMSE of 6.36 W m^{-2} for LE and 8.63 W m^{-2} for H) and in capturing
552 diurnal variability. Furthermore, after parameter optimization, the SEB model incorporating this method
553 achieved the highest accuracy, with R values of 0.86 and 0.94 for T_s and ice surface height, respectively.
554 These results suggest that the method based on Monin–Obukhov similarity theory with universal stability
555 functions may be the most suitable for estimating turbulent fluxes over continental glaciers on the TP.

556 Lastly, we investigated the impacts of extreme weather and climate events (e.g., humid heatwaves)
557 on turbulent flux characteristics. The analyzed humid heatwave event markedly altered the typical
558 turbulent flux patterns, resulting in a dramatic increase in H and reversal of the LE direction; this caused
559 the average turbulent flux to reach 18.53 W m^{-2} during the humid heatwave period, temporarily
560 transitioning the glacier surface from a heat-loss to a pronounced heat-gain state. However, all methods



561 exhibited increased errors under high-temperature, high-humidity, and intensely turbulent conditions
562 (e.g., during spring or heatwave periods), demonstrating substantial limitations in method robustness
563 under extreme or rapidly changing climate conditions. During the analyzed humid heatwave, all methods,
564 and particularly the C_{M-O} method, a complete implementation of the Monin–Obukhov similarity theory
565 framework, successfully captured the sharp increase in H , although the simulated values were
566 consistently lower than the observed values. Meanwhile, none of the methods reproduced the reversal of
567 LE direction, indicating that the contribution of turbulent fluxes to glacier melt energy under extreme
568 meteorological conditions is likely underestimated.

569 In summary, our findings emphasize the critical importance of turbulent flux parameterizations for
570 accurate glacier SEB modeling and specifically highlight the superior performance and applicability of
571 the method based on Monin–Obukhov similarity theory with universal stability functions in mid-latitude
572 continental glacier environments. Future research should intensify efforts to elucidate the physical
573 mechanisms behind anomalous turbulent flux behavior during extreme weather and climate events (e.g.,
574 humid heatwaves), and thus enhance modeling accuracy under exceptional meteorological conditions.

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578 **Code/Data Availability** ERA5 is available for download at <https://cds.climate.copernicus.eu/cdsapp#!/search?type=dataset>. The EBFM model is available via <https://github.com/wardvp/EBFM-glacier>. Data supporting the findings of this study are available from the corresponding author upon reasonable request.

582 **Author contribution** XYZ: data curation, formal analysis, visualization, writing (original draft
583 preparation). ZML: conceptualization, methodology, supervision, writing (review and editing), field
584 observations, funding acquisition. GJ: conceptualization, supervision, writing (review and editing), field
585 observations, project administration. LDJ: data curation, field observations, writing (review and editing).
586 HL: data curation, resources. ZF: data curation. ZHB: field observations, data curation. ZFY: project
587 administration.

588 **Competing interests** The authors declare that they have no conflict of interest.

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