



# A Fast and Physically Grounded Ocean Model for GCMs: The Dynamical Slab Ocean Model of the Generic-PCM (rev. 3423)

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**Abstract.** We present the new dynamical slab ocean model implemented in a 3-D General Circulation Model (GCM) called the Generic Planetary Climate Model (Generic-PCM; formerly the LMD-Generic GCM). Our two-layer slab ocean model features emergent ocean heat transport (OHT) arising from wind-driven Ekman transport, horizontal diffusion, convective adjustment, and a newly implemented Gent–McWilliams (GM) parameterisation for mesoscale eddies. Sea ice evolution is spectrally-dependent and varies with ice thickness. We first validate the model in an idealised aquaplanet setting under various OHT configurations. We show that enabling OHT transforms not only surface features – such as cooler tropical sea surface temperatures (SSTs) and reduced sea ice coverage – but also atmospheric structures, notably producing a double-banded precipitation pattern across the equator driven by Ekman-induced upwelling. Our modelled meridional OHT profiles are in agreement with fully coupled atmosphere-ocean GCMs, with Ekman transport dominating in the tropics and GM advection and diffusion peaking near the ice edge. When applied to modern Earth, the OHT-enabled configuration yields an annual global average surface temperature of 13°C, within 1°C of reanalysis estimates, and improves extrapolar SSTs and sea ice coverage relative to the OHT-disabled baseline. Seasonal SST and sea ice biases relative to observations are also significantly reduced to within 0.6°C and 3 million km<sup>2</sup>, respectively. We obtain a planetary bond albedo of around 0.32, in close agreement with observations. We additionally find that GM-induced mixing mimics vertical convection, while the inclusion of OHT reduces hemispheric asymmetries and improves the overall GCM numerical stability. Notably, these improvements are achieved at almost no additional computational cost compared to OHT-disabled simulations run over the same number of model years. This balance of computational efficiency and physical realism makes the model particularly well-suited for sensitivity studies and large parameter sweeps – crucial in exoplanet and paleoclimate applications where observational constraints are limited.



## 20 1 Introduction

Oceans are central to climate regulation on terrestrial planets due to their ability to store and redistribute heat. On Earth, ocean heat transport (OHT) plays a particularly crucial role: it carries excess thermal energy from the equator toward the poles, significantly reducing meridional temperature gradients. Observational estimates clearly reveal this latitudinal energy redistribution (e.g., Trenberth and Solomon, 1994), which is accomplished through a combination of shallow wind-driven gyres in the tropics and subtropics, and deeper overturning circulations linked to high-latitude convection (e.g., Trenberth and Caron, 2001; Marshall and Plumb, 2007). Together with the ocean's high thermal inertia and interactions with sea ice, these processes help dampen seasonal and regional temperature extremes — stabilising Earth's climate over long timescales and contributing fundamentally to its long-term habitability.

Ocean dynamics are also critical in other planetary contexts – including paleoclimates and exoplanets. Paleoclimate simulations have shown that OHT strongly influences transitions between climate states. For example, OHT can effectively delay or prevent global glaciation by limiting sea ice expansion in Snowball Earth scenarios (for e.g., Pierrehumbert et al., 2011; Yang et al., 2012a, b). Dynamic oceans have also been incorporated in studies of ancient climates on Earth (e.g., Olson et al., 2022; Ragon et al., 2024), as well as early Venus (e.g., Way et al., 2016; Way and Del Genio, 2020), where they play a key role in determining planetary climate regimes and potential habitability. Rose (2015) and Brunetti et al. (2019) demonstrated that the choice of oceanic representation can even determine the number and nature of climatic steady states.

Most known habitable zone (HZ; Kasting et al., 1993) exoplanets orbit low-mass stars and are expected to be in synchronous rotation (tidally locked), having a permanent dayside and nightside (Ribas et al., 2016; Turbet et al., 2016, 2018, 2020a) like Proxima-b (Anglada-Escudé et al., 2016) and TRAPPIST-1e (Gillon et al., 2017). Numerous General Circulation Model (GCM) studies have investigated their atmospheric dynamics (for e.g., Edson et al., 2011; Pierrehumbert, 2010; Leconte et al., 2013; Kopparapu et al., 2016; Turbet et al., 2016; Kopparapu et al., 2017; Boutle et al., 2017), but few have included dynamic oceans. Yet, the few studies that do incorporate OHT on synchronously rotating planets have demonstrated its profound impact on the climate – including broadening the area of surface liquid water (Hu and Yang, 2014) and modifying the large-scale circulation, surface temperatures and sea ice patterns (Del Genio et al., 2019). Cullum et al. (2016) highlighted the role of salinity in shaping ocean circulation and the climate at large. Checlair et al. (2019) showed that due to OHT, habitable tidally locked planets are unlikely to have snowball states. The implications of OHT of a few other studies (e.g., Yang et al., 2020; Olson et al., 2020; Batra and Olson, 2024) is further detailed in Sect. 5. All these effects are important not only for assessing planetary habitability but also for interpreting exoplanet observables: for instance, Yang et al. (2019) demonstrated that OHT can shift the thermal hotspot eastward in phase curves of temperate tidally locked planets.

These modelling insights are particularly timely, as we enter an era of high-precision exoplanet observations, probing the atmospheres — and soon, the surface conditions — of potentially habitable exoplanets. Small HZ rocky planets are now being discovered and are prime targets for atmospheric characterisation. Ongoing efforts include the James Webb Space Telescope



(JWST; Gardner et al., 2006), and near-future ground-based instruments such as RISTRETTO (Lovis et al., 2024) planned for the Very Large Telescope (VLT) and the ArmazoNES high Dispersion Echelle Spectrograph (ANDES; Palle et al., 2025) at the Extremely Large Telescope (ELT). These efforts will be complemented by future space-based observatories like the Habitable  
 55 Worlds Observatory (HWO; Gaudi et al., 2020) and the Large Interferometer For Exoplanets (LIFE; Quanz et al., 2022), which aim to detect and characterize the atmospheres of temperate terrestrial exoplanets. Understanding the climate dynamics of such planets — and assessing their potential habitability — is a major focus of both theoretical and observational research.

Most dynamic ocean studies to date have relied on fully coupled Atmosphere–Ocean General Circulation Models (AOGCMs). These represent the gold standard of physical realism, explicitly solving the Navier-Stokes equations in both the ocean and  
 60 atmosphere. However, this comes at the cost of computational expense and they require long integration times to reach equilibrium, making them impractical for large parameter space studies. As a compromise, most exoclimate studies opt for lower-level ocean representations described below.

The simplest way to model oceans is as a surface with a higher thermal inertia than land (for e.g., Spiegel et al., 2008; Dressing et al., 2010; Bolmont et al., 2016). A step up are slab ocean models without heat transport, where the ocean is  
 65 represented as a single wind-mixed layer with a homogenous temperature that is forced by local surface heat fluxes. This is arguably the most popular ocean modelling technique in exoplanet GCMs (for e.g., Kopparapu et al., 2016; Wolf et al., 2017; Turbet and Forget, 2021; Chaverot et al., 2023). A further refinement involves prescribing slab ocean models with meridional heat fluxes (q-fluxes) based on observations / AOGCM simulations (e.g., Wolf and Toon, 2015). This approach lacks flexibility as the OHT is imposed rather than emergent (see Sect. 5.3). Another step up are slab ocean models which simulate OHT  
 70 purely through a diffusive flux (for e.g., Donnadieu et al., 2006; Kilic et al., 2017). However, this approach misrepresents the structure of real ocean heat transport, notably failing to capture key features such as the equatorial cold tongue – the pronounced minimum in equatorial sea surface temperatures (DeConto and Pollard, 2003).

This paper presents a new "dynamical slab ocean model" that bridges the gap between higher-level slab oceans and fully coupled AOGCMs. In our model, OHT is an emergent process that effectively couples the atmosphere and ocean. It includes  
 75 wind-driven Ekman transport - the dominant driver of tropical meridional OHT in Earth observations (Levitus, 1987; Forget and Ferreira, 2019) – along with horizontal diffusion and convection, following Codron (2012) and Charnay et al. (2013). Our model also introduces mesoscale eddy mixing in slab oceans through the Gent-McWilliams parameterisation (Gent and McWilliams, 1990), enabling horizontal and vertical temperature mixing. Additionally, sea ice evolution depends on ice thickness and the incoming spectra.

The model is designed to support large ensemble studies — a critical need in exoplanet and paleoclimate science, where  
 80 observational constraints are sparse, motivating the exploration of a wide parameter space. Our goal is not to match the full complexity of AOGCMs, but to provide the modelling community a faster, physically grounded alternative - an improved compromise over traditional slab ocean models. This philosophy also aligns with the broader philosophy of intermediate-complexity GCMs like *ExoPlaSim* (Paradise et al., 2022), which enable large-scale explorations of planetary climates while  
 85 retaining core physical realism.



In this article, we first present the model in detail, highlighting the improvements made in sea ice evolution and OHT (Sects. 2.2 and 2.3 respectively). We then validate it against two benchmark cases: an aquaplanet (Sect. 3), and modern Earth (Sect. 4). Finally, we discuss the implications of our model, its strengths and limitations in Sect. 5.

## 2 Model description

90 The simulations presented here were conducted with rev. 3423 of the 3-D Generic Planetary Climate Model (Generic-PCM, formerly the LMD-Generic GCM, Forget et al. in prep.). Originally developed to study present-day Earth's climate (e.g., Hourdin et al., 2006; Charnay et al., 2013) and Mars (Forget et al., 1999), the model has since been generalised to simulate the (paleo-)climates of other solar system bodies (e.g., Charnay et al., 2013; Forget et al., 2013; Wordsworth et al., 2013; Turbet et al., 2021) as well as exoplanets (e.g., Wordsworth et al., 2011; Bolmont et al., 2016; Turbet et al., 2016, 2018; Kuzucan et al., 95 2025). Notably, it remains the only GCM capable of treating water vapour as a major atmospheric constituent, a crucial feature for investigating water-rich planetary environments (for e.g., Leconte et al., 2013). The associated flexibility is exemplified by studies that push the model to extreme scenarios; for instance, in its radiative transfer: simulating climates during (Chaverot et al., 2023) and post runaway greenhouse (Turbet et al., 2021), or, its numerical scheme: testing the effect of very large bolide impacts on the climate of early Mars (Turbet et al., 2020b).

100 The 3-D dynamical core of the model (Hourdin et al., 2006) solves the primitive equations of geophysical fluid dynamics in the atmosphere using a finite-difference method on an Arakawa C-grid. The GCM includes a comprehensive radiative transfer scheme accounting for absorption and scattering by atmospheric gases, clouds, and surface interactions, along with surface and subsurface processes such as condensation, evaporation, sublimation, and precipitation.

All simulations in this study use a horizontal resolution of  $64 \times 48$  grid points (longitude  $\times$  latitude;  $5.625^\circ \times 3.75^\circ$ ). The 105 atmosphere is discretised into 30 vertical layers extending from the surface up to 10 Pa, using hybrid  $\sigma$ -coordinates (where  $\sigma$  = pressure / surface pressure). Radiative transfer is based on the correlated-k method (Fu and Liou, 1992). We use tables from Leconte et al. (2013), computed using the HITRAN 2012 line lists (Rothman et al., 2013) across 38 thermal infrared and 36 visible spectral bands. Water vapour ( $\text{H}_2\text{O}$ ) is treated as a variable component capable of phase changes from the surface, ocean or atmosphere, with relative humidity computed self-consistently. Sub-grid scale processes, including turbulent mixing 110 and moist convection, follow parameterisations described in Leconte et al. (2013). Cloud condensation nuclei (CCN) radii are fixed at  $12 \mu\text{m}$  for liquid water and  $35 \mu\text{m}$  for ice, following Charnay et al. (2013). During the spin-up phase, our study keeps time-steps short to accurately capture rapid processes: the dynamical time-step (e.g., for winds) is 45 model seconds, the physical time-step (e.g., for evaporation) is 7.5 min, and the radiative time-step is 45 min. Post spin-up, all time-steps are doubled to improve computational efficiency.

115 Our dynamical slab ocean model builds on the works of Codron (2012) and Charnay et al. (2013). The model solves prognostic equations for ocean temperature and sea ice evolution on the same horizontal grid as the GCM's atmosphere and comprises two ocean layers. The upper layer represents the mixed surface layer interacting with the atmosphere, while the lower layer represents the deeper ocean, exchanging heat with the mixed layer but not directly with the atmosphere – this two-layer con-



figuration is key for facilitating heat transport. We compute the vertical heat flux using an upstream scheme while a centered  
 120 scheme is used in the meridional direction. Sea-ice fraction, thickness, and snow thickness are tracked at each ocean grid point. We set the coupling time-step between the ocean and atmosphere (“ocean time-step”) to match the physical time-step (either 7.5 or 15 model minutes, as discussed earlier).

In this study, we improve the two key processes historically handled by the dynamical slab ocean: (a) **Sea ice evolution**, by improving the spectral albedo representation, refining sea ice formation, melting and freezing, and introducing a finite heat  
 125 capacity for snow (Sect. 2.2); and (b) **Heat transport by ocean circulation**, by optimising horizontal diffusion and Ekman transport, and implementing a new Gent–McWilliams (advection) parameterisation that captures both, the effect of mesoscale eddies and convection (Sect. 2.3). Furthermore, the model is now fully parallelised, enabling fast computation.

## 2.1 General principle

At the heart of the dynamical slab ocean model lies the conservation of energy. The temporal evolution of the surface layer  
 130 temperature ( $\partial T_s / \partial t$ ) at a particular oceanic grid point is governed by the net heat fluxes, expressed as:

$$\rho C_p H \frac{\partial T_s}{\partial t} = F_{\text{surf}} + F_o + Q_{\text{flux}}, \quad (1)$$

where  $\rho$  is the density of seawater,  $C_p$  its specific heat capacity (refer to Table A1 for associated values) and  $H$  the depth of the mixed layer. The left-hand side of Eq. (1) represents the rate of change of heat content per unit area of the slab ocean. The right-hand side includes the net surface flux  $F_{\text{surf}}$  computed by the atmosphere model, an ocean heat flux term  $F_o$  (horizontal  
 135 and vertical transport) computed by our dynamical slab ocean model and an (optional) additional forcing ( $Q_{\text{flux}}$ ) that accounts for other processes. The net surface flux is given by  $F_{\text{surf}} = F_{\text{rad}} + F_{\text{sens}} + F_{\text{lat}}$ , where  $F_{\text{rad}}$  includes net shortwave and longwave radiation,  $F_{\text{sens}}$  represents enthalpy exchange due to temperature differences between the ocean surface and the air, and  $F_{\text{lat}}$  captures latent heat exchange during phase changes of water. The  $Q_{\text{flux}}$  term can be used in the absence of  $F_o$  to approximate the effects of ocean mixing and dynamics, but it can also represent other processes depending on the simulated planet (e.g.,  
 140 geothermal heating, important in exoplanet contexts). A positive (negative) sum of  $F_{\text{surf}} + F_o + Q_{\text{flux}}$  leads to a net gain (loss) of heat, increasing (decreasing) the ocean surface temperature.

## 2.2 Sea ice evolution

Sea ice develops when the ocean temperature falls below the freezing point of seawater ( $T_{\text{freeze}} = -1.8^\circ\text{C}$ )<sup>1</sup>. The vertical temperature profile within the sea ice linearly varies between a fixed bottom value  $T_{\text{freeze}}$  in contact with the ocean, and a  
 145 prognostic surface ice temperature  $T_i$ . The mean temperature of the ice is therefore equal to  $(T_i + T_{\text{freeze}})/2$ . A separate snow layer with its own temperature, thickness and finite heat capacity can accumulate on top of the ice.

The evolution of ice extent and thickness is governed by energy conservation during phase changes, ensuring that the ocean temperature remains at  $T_{\text{freeze}}$  as long as ice is present. Specifically, if the temperature of the surface ocean layer ( $T_s$ ) instan-

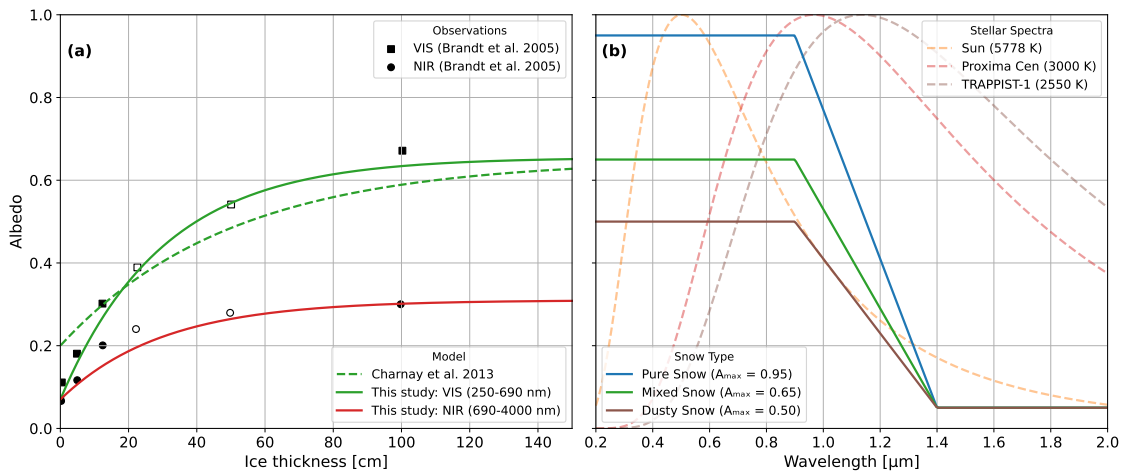
<sup>1</sup>This value reflects modern Earth’s average ocean salinity of 35 psu. The model’s  $T_{\text{freeze}}$  value can be changed as per the seawater salinity of the model planet.

taneously falls below its freezing point, its temperature is set back to  $T_{\text{freeze}}$  and the resulting energy difference creates ice.  
 150 Conversely, if the ocean temperature exceeds  $T_{\text{freeze}}$  when ice is present, the temperature is set back to  $T_{\text{freeze}}$ , and the excess energy is used to melt part of the ice. A similar mechanism governs melting from above. If snow has accumulated on top of the sea ice and the surface temperature (of snow-covered ice) exceeds  $T_{\text{melt}} = 0^\circ\text{C}$ , it is reset to  $T_{\text{melt}}$  and the energy difference is first used to melt the snow and then the ice. If the heat fluxes are strong enough such that energy is still remaining, it is used to warm the ocean, thus satisfying energy conservation. Sea ice may grow or melt primarily by adjusting either its area or  
 155 thickness, depending on whether the dominant energy flux is from the ocean below or the atmosphere above.

As described above, snow and ice are both subject to surface heat fluxes from the atmosphere ( $F_{a-i}$ ) and conductive fluxes from the ocean and within the ice itself ( $F_{i-o}$ ). Ocean heat transport or q-flux changes the ocean temperature, and so, only acts indirectly on the ice. Following Codron (2012), we rewrite Eq. (1) to specifically describe the evolution of the ice temperature  $T_i$ :

$$160 \quad \rho_i C_i H \frac{\partial T_i}{\partial t} = 2[F_{a-i} - F_{i-o}] \quad (2)$$

where  $\rho_i$  is the ice density,  $C_i$  is its specific heat capacity, and  $F_{i-o} = \frac{\lambda}{H}(T_i - T_0)$  is a vertical conductive flux, where  $\lambda$  is the thermal conductivity of ice (refer to Table A1 for associated values). The factor of 2 accounts for the linear (conductive) thermal profile within the ice. If a snow layer is present, we also account for the associated snow-ice conductive flux.



**Figure 1.** (a) Bare sea ice albedo as a function of ice thickness in the Visible (VIS; green) and Near-Infrared (NIR; red) bands in our study, with curves fit to Antarctic observations from Brandt et al. (2005, filled symbols: measurements; open: interpolated). The spectrally-independent albedo used in Charnay et al. (2013) is shown for reference (dashed green). (b) Broadband spectral distribution of snow and ice albedo for pure (blue), mixed (green), and dusty (brown) snow—with  $A_{\text{max}}$  values of 0.95, 0.65, and 0.50, respectively. Dashed lines indicate the normalised black body emission of the Sun (orange), Proxima Centauri (red), and TRAPPIST-1 (brown).

The parameterisation of sea ice and snow albedo also plays a critical role in shaping a model planet’s climate and consequently, its observability. Charnay et al. (2013) addressed this by treating the albedo of bare sea ice as a function of ice  
 165





thickness. In their framework, the surface albedo ( $A$ ) at an oceanic grid point could correspond to that of open ocean, overlying snow (if present), or bare sea ice, the latter varying with thickness according to:

$$A = A_{\text{ice}}^{\text{max}} - (A_{\text{ice}}^{\text{max}} - A_{\text{ice}}^{\text{min}})e^{-h_{\text{ice}}/h_{\text{ice}}^0} \quad (3)$$

In this study, we improve this scheme by incorporating a spectral dependence of albedo in addition to the existing thickness  
 170 dependence. Figure 1a shows how the model's prescribed sea ice albedo varies as a function of ice thickness in the Visible (VIS; 250-690 nm; green line) and Near-Infrared (NIR; 690-4000 nm; red line) spectral bands. The spectrally-independent albedo profile from Charnay et al. (2013) is also shown for reference (dashed green). This earlier scheme assigned an albedo of 0.2 to newly formed ice, whereas our formulation introduces a physically motivated transition, with the albedo increasing smoothly from its minimum possible value, i.e.,  $A_{\text{ice}}^{\text{min}} \equiv A_{\text{ocean}} = 0.07$ ,<sup>2</sup> up to a maximum value  $A_{\text{ice}}^{\text{max}}$ , following Eq. (3). We  
 175 calibrate  $A_{\text{ice}}^{\text{max}}$  by fitting this expression to long-term observations of Antarctic sea ice albedo, as documented by Brandt et al. (2005, filled symbols in Fig.1), and summarised by Pedersen et al. (2009). From this, we obtain  $A_{\text{ice}}^{\text{max}} \approx 0.65$  in the VIS and  $\approx 0.31$  in the NIR. The parameter  $h_{\text{ice}}$  denotes sea ice thickness (in m), while  $h_{\text{ice}}^0$  is a scaling parameter (set to 0.3 m) that governs the rate of transition between the minimum and maximum albedo values.

Figure 1b shows the Generic-PCM's broadband spectral distribution of snow and ice albedo for three idealised surface cases:  
 180 pure (blue line), mixed (green), and dusty (brown) snow. These are based on the works of Warren and Wiscombe (1980), Warren (1984) and Joshi and Haberle (2012) and are characterized by maximum albedos ( $A_{\text{max}}$ ) of 0.95, 0.65, and 0.50, respectively. Currently, our model does not account for an age-dependent snow albedo. Nevertheless, like Turbet et al. (2016), we adopt the mixed snow profile as it is a representative average of the albedo of snow-covered sea ice. The dashed lines indicate the normalised black body emission of the Sun (orange, 5778 K), Proxima Centauri (red, 3000 K), and TRAPPIST-1 (brown, 2550  
 185 K). For these stars, the bolometric albedo of mixed snow is approximately 0.55, 0.36 and 0.29 respectively<sup>3</sup>, highlighting the importance of including a spectral energy distribution in determining surface energy budgets.

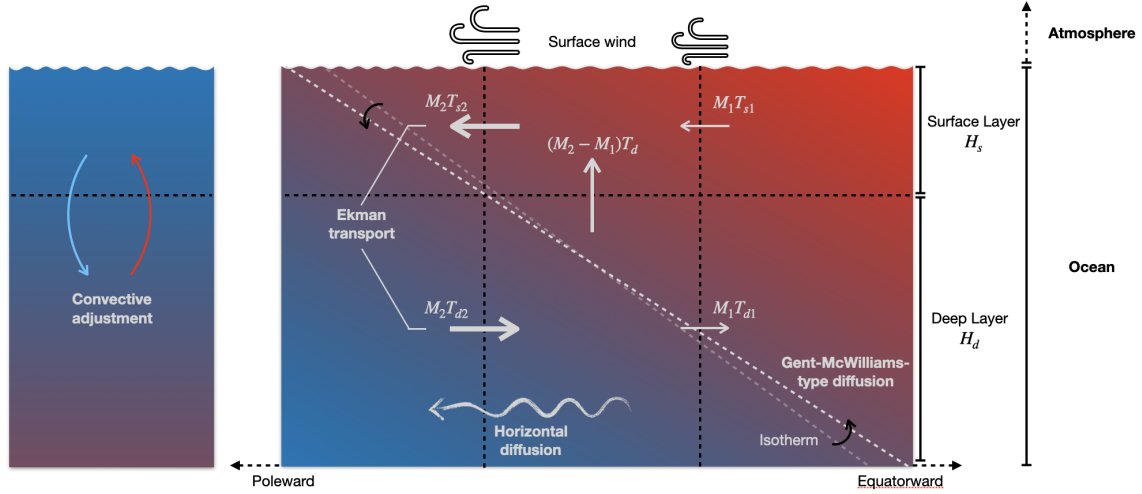
### 2.3 Heat transport by ocean circulation

The nomenclature "dynamical slab ocean model" is purposefully chosen to reflect our model's emphasis on ocean dynamics. Figure 2 provides a cross-sectional view of the ocean model in the horizontal (latitude) and vertical (depth) dimensions, and  
 190 illustrates the model's various OHT regimes. The upper section depicts the oceanic mixed (surface) layer, with a fixed thickness of  $H_s = 50$  m, where interactions with the atmosphere occur (see Sect. 5.5 for a discussion of the implications of using a fixed mixed-layer depth). The lower section corresponds to the deep ocean, with a thickness of  $H_d = 150$  m, which exchanges heat only with the surface layer.

In our model, heat transport by the ocean is represented by four components, detailed through Sects. 2.3.1–2.3.4:

<sup>2</sup>The albedo of open water primarily results from Fresnel reflection and is largely wavelength-independent, consistent with measurements (e.g., Payne, 1972; Katsaros et al., 1985; Pegau and Paulson, 2001).

<sup>3</sup>Assuming blackbody emission is a weak assumption for M-dwarfs, which exhibit significant absorption features.



**Figure 2.** Cross-sectional representation of the ocean along latitude and depth. The top section represents the oceanic mixed (surface) layer and the bottom represents the deep ocean layer. The different heat transport regimes are visible: the wind-driven Ekman transport and eddy advection based on the Gent-McWilliams (GM) scheme both yield horizontal mass fluxes across the grid interface ( $M_1, M_2$ ) opposed in the top and bottom layers. These are proportional to the surface wind stress (Ekman) or isotherm slope (GM). The vertical mass flux is deduced from mass conservation. The horizontal diffusive flux (wavy arrow) is downgradient in both layers. Convective adjustment, particularly relevant for high-latitudes, is also represented with a kink in the latitude dimension.

### 195 2.3.1 Wind-driven Ekman transport

We closely follow the 2-Layer Ekman model detailed in Codron (2012). A wind-driven horizontal mass flux  $M$  integrated over the ocean surface mixed layer is first computed as

$$\begin{cases} M_x = (\epsilon \tau_x + f \tau_y) / (\epsilon^2 + f^2) \\ M_y = (\epsilon \tau_y - f \tau_x) / (\epsilon^2 + f^2) \end{cases} \quad (4)$$

where  $M_x$  and  $M_y$  are the zonal and meridional oceanic mass fluxes and  $\tau_x$  and  $\tau_y$  are the corresponding wind stress components,  $f$  is the Coriolis parameter ( $f = 2\Omega \sin \phi$ , where  $\Omega$  is the rotation rate of the planet and  $\phi$  the latitude) and  $\epsilon$  is a frictional damping coefficient. In the limit when  $|f| \gg \epsilon$ , the wind-driven flux becomes equal to the Ekman transport  $\mathbf{M}_E = -\frac{1}{f} \mathbf{k} \times \boldsymbol{\tau}$ , where  $\mathbf{k}$  is the unit vector in the vertical direction. These mass fluxes are then used to advect the surface layer temperature, while equal and opposite mass fluxes are applied in the deep layer to conserve mass.

This process is illustrated on Fig. 2 along a single horizontal dimension, with frictional mass fluxes  $M_1$  and  $M_2$  at two neighbouring grid point boundaries in the surface layer and opposite fluxes at depth. If these horizontal mass fluxes are divergent – as on Fig. 2 – they give rise to compensating upwelling mass fluxes (or downwelling, when there is surface convergence), that advect the temperature vertically. The OHT term in the surface layer temperature evolution is then given by the divergence of





heat fluxes:

$$\rho H_s S \frac{\partial T_s}{\partial t} = M_1 T_{s1} - M_2 T_{s2} + (M_2 - M_1) T_d \quad (5)$$

210 Here,  $M_1$  is the vertically integrated mass flux computed from the wind stress for the latitude closer to the equator and  $M_2$  is that for the latitude closer to the pole (for the meridional component of the transport). Similarly,  $T_{s1,2}$  are the temperatures of the surface layer at the grid interfaces, computed using an upstream scheme.  $T_d$  is the temperature of the deep (upwelled) layer in the example shown, but is replaced by the surface temperature  $T_s$  in the case of downwelling.  $S$  is the horizontal area of the grid point. The temperature of the deep layer evolves in the same manner, but with opposite signs for the mass transports.

215 Our study also includes a modification of this scheme near the equator where  $f \rightarrow 0$ . According to Eq. (4), the mass transport becomes purely frictional and aligned with the wind in this limit. While this is indeed observed in the surface layers of Earth's oceans, the meridional mass transport component responsible for most of the energy transport across the equator on Earth is better captured by the Sverdrup balance, given by  $M_{Sv} = \frac{1}{\beta} \mathbf{k} \cdot (\nabla \times \boldsymbol{\tau})$ , where  $\beta = \left. \frac{\partial f}{\partial \phi} \right|_{\phi \rightarrow 0^\circ}$ . We therefore include a smooth transition from the frictional Ekman balance to a curl-driven Sverdrup balance near the equator. This transition is handled  
 220 using a weighting function of the form  $\exp(-f^2/\epsilon^2)$ , so that Sverdrup transport dominates when  $|f| \lesssim \epsilon$ , and is negligible at higher latitudes where  $|f| \gg \epsilon$ . For Earth, with  $\epsilon = 10^{-5} \text{ s}^{-1}$ , this corresponds to a transition centered around  $\pm 4^\circ$  latitude. This addition improves the modeled meridional transport in the tropics, especially on Earth-like rotating planets. However, this approach may have to be modified for slowly rotating planets:  $f$  and  $\beta$  become small, and the Sverdrup transport would become unrealistically large compared to the direct frictional transport.

### 225 2.3.2 Gent-McWilliams advection and diffusion

We model mesoscale ocean eddies using the Gent–McWilliams (GM) parameterisation (Gent and McWilliams, 1990), which represents the effect of eddies along isopycnals (surfaces of constant density). In the full theory, a residual eddy-induced transport velocity – with both horizontal and vertical components – is derived from the large-scale density field, with an overturning streamfunction proportional to the slope of the isopycnals (see Eq. 2 in Danabasoglu and McWilliams, 1995).  
 230 However, since our model does not include salinity, density reduces to a function of temperature alone, and so, the isopycnals are equivalent to the isotherms.

Like in the Ekman transport case, horizontal mass fluxes are computed at each grid interface, with opposite values in the surface and deep layers. This is equivalent to evaluating the GM streamfunction only at the interface between the two layers. The horizontal mass flux  $\mathbf{M}_{GM}$  in the surface layer is then given by  $\mathbf{M}_{GM} = \rho \kappa_{GM} \boldsymbol{\sigma}$ , where  $\kappa_{GM}$  is the GM thickness  
 235 diffusivity coefficient and  $\boldsymbol{\sigma}$  denotes the isotherm slope. These horizontal fluxes, along with vertical fluxes deduced from mass conservation, are then used to advect temperature. The amplitude of the eddy-induced mass transport is therefore proportional to the local isotherm slope, and acts to flatten tilted isotherms by transporting fluid along them – from deeper to shallower regions. This is illustrated in Fig. 2, where a representative isotherm is shown as a white dashed line.

We prescribe a GM diffusion coefficient of  $2000 \text{ m}^2 \text{ s}^{-1}$  and a maximum slope of 0.002 for numerical stability. These values  
 240 were tuned to fit the meridional ocean heat transport profile of an Earth-like aquaplanet using the MITgcm (Marshall et al.,



1997a, b; Adcroft et al., 2004), an AOGCM (see Sect. 3.1 for more details). The eddy-induced transport acts to reduce the slope of the isotherms, shown in Fig. 2 as the grey dashed line transforming into the white dashed line, resulting in high-latitude surface heating and low-latitude depth cooling. The vertically integrated eddy transport acts to redistribute heat from regions of higher to lower temperature, effectively behaving as a downgradient energy flux; but there is also a re-stratification of the ocean, increasing the temperature difference between the surface and deep ocean, in turn making the Ekman transport larger according to Eq. (5). In contrast, a purely diffusive flux would transport heat towards higher latitudes for both the surface and deep layers. Importantly, we also find that this restratification can simulate the effect of local convection (when the surface becomes colder than the deep ocean) quite well (see Sect. 5.1).

### 2.3.3 Horizontal diffusion

Mixing caused by turbulence and subgrid-scale eddies can also be accounted for by horizontal eddy diffusion (represented with a wavy arrow in Fig. 2), with a uniform diffusivity in both ocean layers. Codron (2012) prescribed a horizontal diffusion coefficient value of  $D = 25000 \text{ m}^2\text{s}^{-1}$  to best reproduce the meridional heat transport of aquaplanets simulated using fully coupled AOGCMs. However, now that we explicitly account for mesoscale eddies through the GM scheme, we prescribe a decreased diffusion coefficient value of  $8000 \text{ m}^2\text{s}^{-1}$  so as not to overestimate overall diffusive heating. Similar to the GM coefficient, we tuned this horizontal diffusion coefficient to fit the meridional OHT of an Earth-like aquaplanet, as modelled by the MITgcm (Marshall et al., 2007). It is also worth noting that this coefficient value may change as a function of the rotation rate of the planet. We briefly address this in Sect. 5.5, while a more detailed investigation is planned for future work.

### 2.3.4 Convective adjustment

The two-layer nature of the ocean model also facilitates a convective adjustment. Specifically, if the surface layer becomes colder than the deep layer (for e.g., in winter at mid-high latitudes), vertical convective adjustment ensures that the heat stored at depth is restored to the surface (see the high-latitude slab in the extreme left of Fig. 2). This effectively simulates (denser) colder water at the surface descending and ensures that the deep ocean temperature remains lower than the surface.

### 2.3.5 The Dynamical Slab Ocean Equation

We now consolidate these OHT processes into the governing equations for the evolution of the surface and deep layer temperatures (denoted by  $T_s$  and  $T_d$  respectively) at a given grid point. The evolution of the surface layer temperature is expressed as:

$$\frac{\partial T_s}{\partial t} = \frac{1}{\rho C H_s} (F_{a-o} + F_{i-o} + F_c) + D \nabla^2 T_s - \frac{1}{\rho H_s} \left[ \text{div}_H [(\mathbf{M}_{\text{Ek}} + \mathbf{M}_{\text{GM}}) T_s] - (\mathbf{W}_{\text{Ek}} + \mathbf{W}_{\text{GM}}) \hat{T} \right], \quad (6)$$

where,  $F_{a-o}$  and  $F_{i-o}$  represent the heat fluxes from the atmosphere and the sea ice to the ocean respectively, and  $F_c$  denotes the **convective heat flux** between the two slab layers.  $D$  is the **horizontal diffusion** coefficients. The horizontal divergence operator,  $\text{div}_H$ , calculates the net horizontal heat inflow or outflow at a grid point. **Ekman transport** and the **GM scheme** both change the horizontal and vertical mass fluxes. We decompose the horizontal mass flux,  $\mathbf{M}$ , into its Ekman and GM



contributions as  $\mathbf{M} = \mathbf{M}_{\text{Ek}} + \mathbf{M}_{\text{GM}}$ . The horizontal mass flux,  $\mathbf{M}$  (with units of  $\text{kg m}^{-1} \text{s}^{-1}$ ), along with the advected surface and deep temperatures  $T_s$  and  $T_d$ , are evaluated on the grid-point interfaces. The vertical mass flux,  $\mathbf{W}$ , can also be decomposed as  $\mathbf{W} = \mathbf{W}_{\text{Ek}} + \mathbf{W}_{\text{GM}} = \text{div}_H \mathbf{M}_{\text{Ek}} + \text{div}_H \mathbf{M}_{\text{GM}}$ . The vertically-advected temperature is denoted by  $\hat{T}$ . If  $\mathbf{W} > 0$ , water from  
 275 depth is upwelled and  $\hat{T} = T_d$  and if  $\mathbf{W} < 0$ , surface water is downwelled and  $\hat{T} = T_s$ .

The deep layer temperature,  $T_d$ , evolves in a similar way to the surface layer but without the direct influence of surface fluxes, i.e.,  $F_{a-o}$  and  $F_{i-o}$ . It changes due to convection, diffusion, vertical and horizontal advection. We use the same Ekman and GM transports as in the surface layer, but with a negative sign to reflect the opposing direction of the return flow. The evolution of  $T_d$  at a given grid point is then governed by:

$$280 \quad \frac{\partial T_d}{\partial t} = \frac{1}{\rho C H_d} F_c + D \nabla^2 T_d + \frac{1}{\rho H_d} \left[ \text{div}_H [(\mathbf{M}_{\text{Ek}} + \mathbf{M}_{\text{GM}}) T_d] - (\mathbf{W}_{\text{Ek}} + \mathbf{W}_{\text{GM}}) \hat{T} \right] \quad (7)$$

Our model does not include other pressure-driven ocean circulation features such as salinity-driven circulations or geostrophic currents such as horizontal gyres. Despite this, we find that our model reproduces the global meridional OHT quite closely compared to a full AOGCM, as we show in Sects. 3 and 4.

### 3 Model validation with a coupled aquaplanet

285 To clarify the OHT mechanisms, we first model an Earth-like atmosphere-ocean coupled aquaplanet — an idealised planet with 100% surface ocean coverage. The main physical parameters we use for the simulation are presented in Table 1. In our first set of aquaplanet simulations, we set both obliquity and eccentricity to 0 to eliminate orbital-parameter-induced temporal asymmetries. The atmosphere is composed of  $\text{N}_2$  with  $\text{CO}_2$  at close to modern Earth levels (0.375 mbar) and the initial average surface pressure is 1013 mbar.

290 We conduct a suite of simulations, under 7 different OHT regimes, detailed in Table 2 to assess their individual impacts on the planet's climate. Each simulation is initialised with an isothermal atmosphere and a uniform sea surface temperature (SST) of 290 K. Given the warm start, our model typically achieves a steady state within 20-40 years<sup>4</sup>. We also validate the performance of our dynamical slab ocean model compared to a full AOGCM, the MITgcm, specifically comparing our results with those described in Marshall et al. (2007) and Brunetti et al. (2019).

#### 295 3.1 Meridional climatic features

Figure 3a shows the decadal-averaged zonal mean SST profile, for the two extreme configurations: Case 1 (no OHT) and Case 7 (all OHT mechanisms enabled) experiments. The corresponding SST difference is shown in Fig. 3c, highlighting the impact of OHT. In Case 1 (Fig. 3a, blue line), the SST profile peaks sharply at the equator as there is no mechanism to redistribute heat from this location, with additional warming due to enhanced moisture and high cloud coverage. The inclusion of all OHT  
 300 processes (Case 7, red profile) brings two important distinctions. Firstly, the equatorial SST is cooler by  $\approx 8^\circ\text{C}$  (see Fig. 3c) compared to Case 1, with a flatter temperature profile and the presence of an equatorial cold tongue. This is driven by Ekman

<sup>4</sup>At the spatiotemporal resolution used in this study, one model year requires approximately 2.75 hours of computation on 24 cores.



Physical Parameter	Aquaplanet	Earth
Stellar spectrum	Sun	
Solar constant ( $\text{W/m}^2$ )	1366	
Rotation period (h)	24	
Orbital period (d)	365	
Radius (km)	6378.137	
Surface gravity ( $\text{m/s}^2$ )	9.81	
Surface roughness coefficient (m)	0.01	
H <sub>2</sub> O cloud droplet radius ( $\mu\text{m}$ )	12 (liquid) and 35 (ice) <sup>†</sup>	
Average surface pressure (bar)	1.013	
N <sub>2</sub> partial pressure (bar)	0.9996	
H <sub>2</sub> O partial pressure (bar)	Variable	
CO <sub>2</sub> partial pressure (mbar)	0.375 (370 ppm) <sup>†</sup>	
Obliquity (°)	0.0 or 23.44	23.44
Eccentricity	0.0	0.0167
Topography	flat	Earth's continents <sup>†</sup>
Surface albedo	0.07	Earth's albedo <sup>†</sup>
Thermal inertia ( $\text{J/m}^2/\text{s}^{1/2}/\text{K}$ )	18000	Earth's thermal inertia <sup>†</sup>

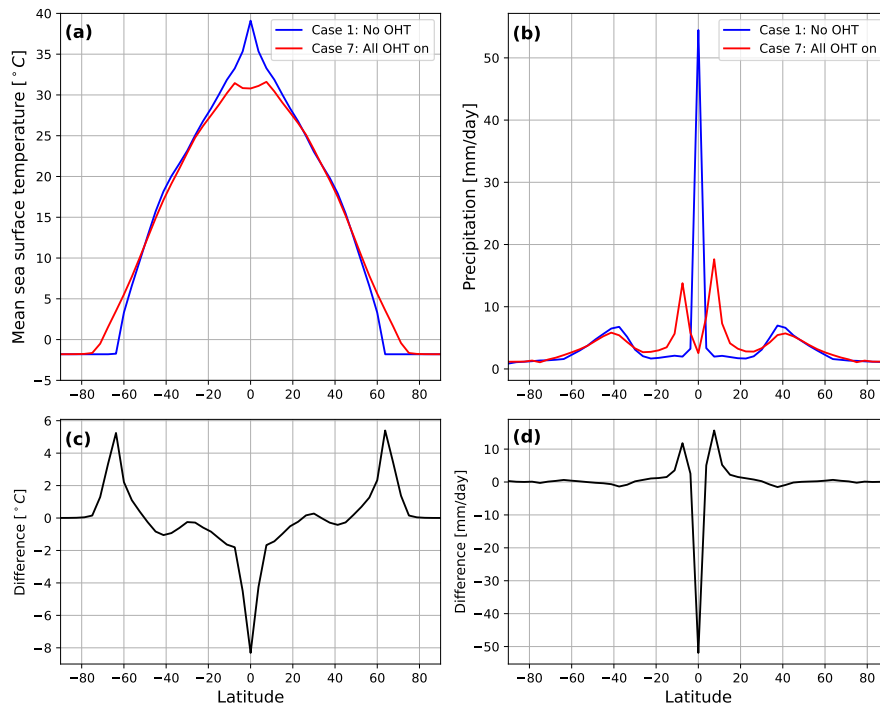
<sup>†</sup> Values adopted from Charnay et al. (2013).

**Table 1.** Summary of the main planetary parameters used in the GCM for the study.

Case	Horizontal diffusion	Gent-McWilliams	Ekman	Convective adjustment
1	–	–	–	–
2	+	–	–	–
3	–	–	+	–
4	+	–	+	–
5	–	+	+	–
6	+	+	+	–
7	+	+	+	+

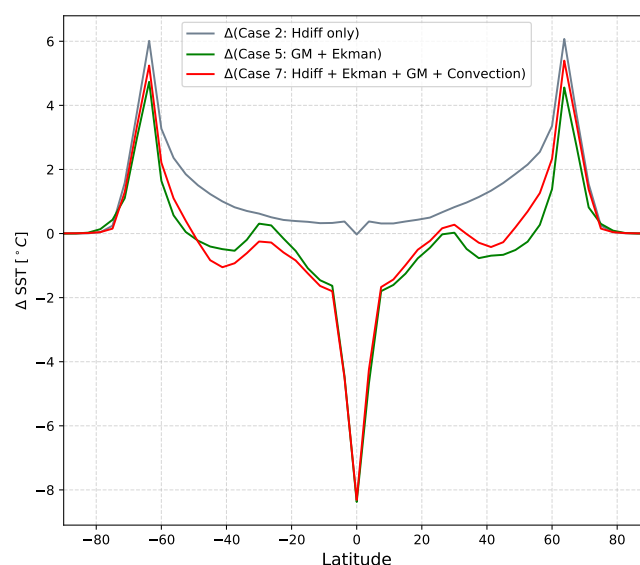
**Table 2.** Table showing the aquaplanet simulations tested using the dynamical slab ocean model. Case 1 represents a slab ocean with all oceanic heat transport (OHT) mechanisms turned off. Each successive case activates specific OHT processes, culminating in Case 7, which includes all OHT mechanisms: horizontal diffusion, Gent-McWilliams-type diffusion, Ekman transport and convective adjustment.

transport, which causes cold water upwelling due to the strong divergence of heat transport at the equator. Additionally, the polar regions are warmer (see Fig. 3c) due to diffusion (both, large scale Eddy diffusivity and the GM scheme), pushing the ice line poleward by 10-15° in latitude. The retreating ice line latitude further strengthens the warming of the planet through the ice-albedo-feedback. These features are also evident in the annually averaged SST maps of Case 1 and Case 7 shown in Fig. C1, as well as in the corresponding animations (see the Video supplement section). Figure 3c also clearly shows the regions of (Ekman-induced) equatorial cooling and (diffusion and GM-driven) polar warming.



**Figure 3.** (a) Zonal mean sea surface temperature (SST, 10-year average) of the aquaplanet for Case 1 (no oceanic heat transport, OHT) and Case 7 (all OHT on) simulations. (c) Difference in SST (ON – OFF), showing the effect of OHT on the same. (b) Zonal mean precipitation (rain + snow, 10-year average) for the same simulations. (d) Difference in precipitation (ON – OFF)

The corresponding zonal mean precipitation profiles (rain + snow) for Cases 1 and 7 are shown in Fig. 3b, and the precipitation difference (OHT on – OHT off) in Fig. 3d. The high equatorial temperature observed in Fig. 3a for Case 1 (OHT off) corresponds to strong water vapour convergence, resulting in the pronounced peak in equatorial precipitation (blue profile) seen in Fig. 3b. On the other hand, in Case 7, equatorial upwelling of cold water prevents precipitation at the equator. This leads to a double-banded precipitation pattern in the tropics on either side of the equator (Fig. 3b), effectively creating a double Intertropical Convergence Zone (ITCZ). The slight hemispheric asymmetry in Fig. 3b may be due to amplifications in internal feedbacks and numerical artefacts. This asymmetry is also visible in the related atmospheric profiles (see Fig. D1).



**Figure 4.** Zonal-mean sea surface temperature (SST) differences of the aquaplanet between selected simulations and Case 1 (no ocean heat transport, OHT), highlighting the impact of various transport mechanisms on the climate. The grey line shows the SST difference for Case 2 (horizontal diffusion only), the green for Case 5 (Gent–McWilliams and Ekman transport), and the red for Case 7 (all OHT enabled).

Figure 4 presents the decadal-mean difference in zonal-mean SST between selected cases from Table 2 and the baseline Case 1 (no OHT), illustrating how individual OHT mechanisms affect the planet’s climate. In Case 2 (horizontal diffusion only; grey line), SSTs progressively warm with latitude relative to Case 1, reaching +5–6°C at mid-to-high latitudes. This highlights the latitudinal smoothing effect of diffusion, with the magnitude of warming dependent on the chosen horizontal diffusion coefficient  $D$ , and on the mean temperature structure (see the Laplacian term in Eq. 6). In Case 5 (GM + Ekman; green line), the SST profile exhibits strong equatorial cooling (8°C) from Ekman-induced upwelling, coupled with moderate warming at subtropical (+2°C) and polar (+5°C) latitudes. Cases 6 (horizontal diffusion + Ekman + GM) and 7 (all OHT mechanisms active, i.e., Case 6 + convection) are nearly indistinguishable, suggesting that convective adjustment has only a minor effect (<1°C across all latitudes), well within model uncertainty. This minimal influence likely results from the GM scheme’s ability to capture vertical restratification effectively (see Sect. 5.1). Comparing Case 5 (green line) with Case 7 (red line) reveals that the addition of horizontal diffusion primarily enhances mid-latitude warming. Lastly, simulations with Ekman transport display minor hemispheric asymmetries. Since Ekman transport is wind-driven, these asymmetries may stem from the atmospheric model and warrant further investigation.

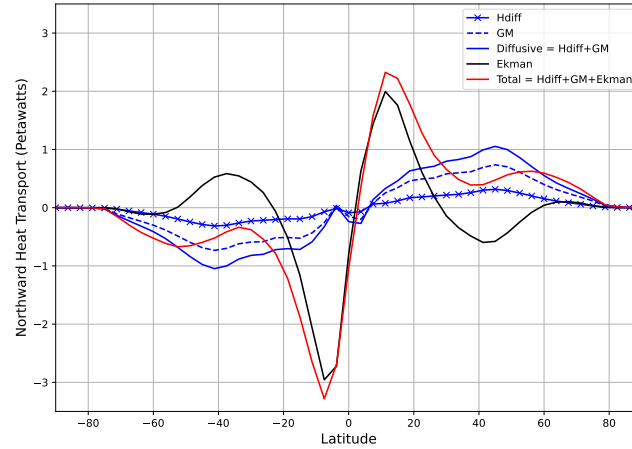
The contribution of each oceanic heating term can also be assessed by examining the meridional ocean heat transport. This diagnostic represents how energy is redistributed from regions of surplus (typically the equator) to those of deficit (poles), offering key insights into the mechanisms driving heat transport in a particular fluid (for e.g., the ocean and/or the atmosphere)



as detailed in Marshall et al. (2007). Our model outputs the heating rates (in  $\text{W/m}^2$ ) of each oceanic process contributing to the total oceanic heating (i.e., horizontal diffusion, Ekman and GM transport). The heating rate for each latitude can be converted to Northward oceanic heat transport by integrating the heating rate over the surface area of the planet and considering the cumulative transport northward. The northward heat transport  $Q$  at latitude  $\phi$  is then:

$$Q(\phi) = 2\pi R^2 \cos(\phi) \int_{-\pi/2}^{\phi} \bar{q}(\phi') d\phi', \quad (8)$$

where  $R$  is the planetary radius and  $\bar{q}(\phi')$  the zonal mean heating rate at latitude  $\phi'$ .



**Figure 5.** Contribution of each ocean heat transport (OHT) term towards the northward meridional OHT (in Petawatts, red line) for Case 7 (all OHT on) of the oblique aquaplanet simulation. Horizontal diffusion (crossed blue) and Gent-McWilliams (dashed blue) together make up the total diffusive transport (solid blue), while Ekman transport is in black.

We perform this analysis in the case of an oblique ( $23.44^\circ$ ) aquaplanet. Figure 5 shows the corresponding total meridional OHT (in Petawatts =  $10^{15}$  W) of Case 7 (all OHT active), decomposed into its contributing terms. The magnitude of Ekman transport is driven by the temperature difference between the surface and deep layers while its direction is dictated by the surface wind forcing. Ekman transport (black line) is strongest in the tropics, consistent with Earth-based observations (Levitus, 1987). This is due to the large temperature contrast between the warm surface water and cooler return flow below, as well as the influence of the Trade winds: via Ekman transport they drive surface waters poleward perpendicular to the wind, inducing equatorial upwelling. However, in the mid-latitudes, the dominant winds are the westerlies, which via Ekman transport drives surface waters equatorward, causing convergence (downwelling) in the subtropics, and a reversal in the meridional OHT. The hemispherical asymmetry in Ekman transport observed in Fig. 5 is likely due to an initial model bias (see Sect. 5.2 for more details).



We decompose the diffusive transport into its horizontal diffusion (crossed blue) and Gent-McWilliams (dashed blue) contributions. Like in Marshall et al. (2007), we find that horizontal diffusion plays a negligible role in the meridional heat transport, with a peak less than 0.3 PW at mid-latitudes. This is undoubtedly due to our lower horizontal diffusion coefficient value of  $8000 \text{ m}^2\text{s}^{-1}$  compared to Codron (2012). The GM transport, with its relatively high transfer coefficient of  $2000 \text{ m}^2\text{s}^{-1}$ , peaks around 0.7 PW and brings the global combined diffusive transport (solid blue line) to the same amplitude as that seen in Codron (2012). With all components accounted for, the overall transport (red line), which contributes to the large-scale ocean circulation, resembles those observed on Earth (Trenberth and Caron, 2001). Furthermore, the general amplitudes agree well with aquaplanet results using a full AOGCM (see Figs. 7 and 3 in Marshall et al., 2007; Brunetti et al., 2019, respectively).

## 355 4 Model validation with modern Earth

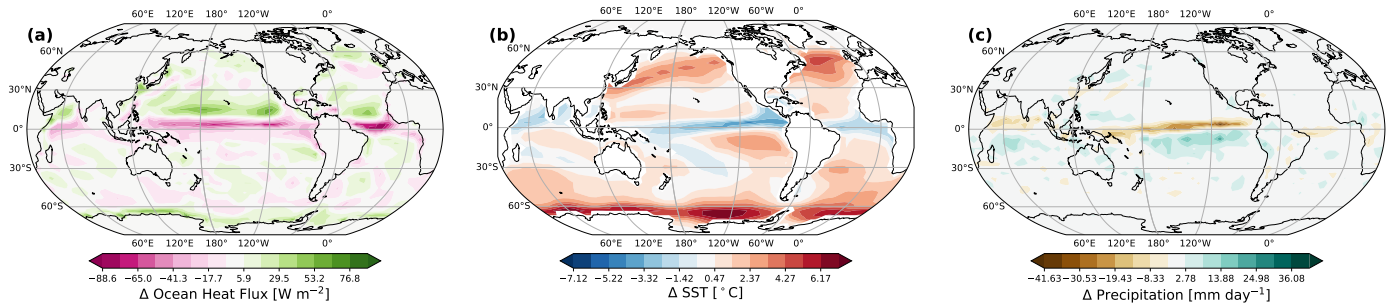
Now that we have better understood the role of the individual OHT regimes using an idealised planet, we apply it on the most widely-studied ocean planet – modern Earth. The parameters used for our modern Earth simulation are summarised in Table 1. The atmosphere is primarily composed of  $\text{N}_2$ , with  $\text{CO}_2$  at close to modern Earth levels ( $0.375 \text{ mbar} \approx 370 \text{ ppmv}$  – value set following Charnay et al. 2013) and variable  $\text{H}_2\text{O}$ . Oxygen and ozone are not included for the sake of simplicity in our radiative transfer calculations. Besides, as pointed out in Charnay et al. (2013), the absence of oxygen only causes small changes in Rayleigh scattering, while that of ozone implies the absence of a stratospheric thermal inversion.

We perform two baseline simulations, one with OHT entirely disabled (Case 1) and another with OHT fully enabled (Case 7). Additionally, we perform a variety of sensitivity tests (see Sect. 5.4). The simulations are initialised with an isothermal atmosphere and surface temperature distribution of 290 K. The simulation without OHT reaches equilibrium within 40 model years, while that with OHT takes around 70 model years to converge.

Simulating modern Earth also enables model validation through comparison with the extensive suite of observational and reanalysis datasets available for the present-day climate. Specifically, we evaluate our results against state-of-the-art reanalysis data from the National Centers for Environmental Prediction / National Center for Atmospheric Research (NCEP/NCAR; Kalnay et al. 1996) and the European Centre for Medium-Range Weather Forecasts (ECMWF) European Re-Analysis (ERA-15) dataset (Gibson et al., 1997). We also compare with observational data from the National Snow and Ice Data Center (NSIDC; Fetterer et al. 2017) and the National Oceanic and Atmospheric Administration (NOAA) Daily Optimum Interpolation Sea Surface Temperature (DOISST) version 2.1 dataset (Huang et al., 2021).

### 4.1 Impact of ocean heat transport on ocean-atmosphere fluxes

Figure 6a shows the decadal-averaged ocean heat flux from the OHT-on simulation, with net positive values indicating atmospheric heating by the ocean (ocean cooling, upward heat flux) and negative implying atmospheric cooling by the ocean (ocean warming). Alternatively, this plot can be seen as the vertically-integrated convergence of the OHT. We see that our model correctly produces surface ocean cooling (or OHT convergence) in subtropical and high-latitude oceans, and warming in the equatorial region. However, the particularly strong regions of cooling over the Gulf Stream and the Kuroshio currents that are



**Figure 6.** Example of the causal chain of the coupled ocean-atmosphere system: Impact of ocean heat transport (OHT) on decadal-averaged quantities of our modelled modern Earth. **(a)** Ocean-atmosphere heat flux from the OHT-on simulation. Note that the OHT-off case has zero ocean heat flux. **(b)** Corresponding SST difference (OHT-on – OHT-off). **(c)** Corresponding precipitation difference.

observed on Earth are not captured, since the return flow of the western boundary currents is not explicitly included in our model.

Figure 6b displays the decadal-averaged SST difference between the OHT-on and OHT-off simulations, effectively capturing the thermal response of the surface ocean. There is a clear spatial correspondence between the ocean heat flux (the forcing) and the SST (the response), particularly in the tropics, highlighting the role of OHT in shaping surface temperatures. The colour map is centred around  $\Delta T = 0^\circ\text{C}$  to emphasise regional warming and cooling. One of the most prominent features of Fig. 6b is that equatorial SSTs are 5–8°C cooler in the OHT-on simulation. As in the aquaplanet case (Fig. 3), this pronounced cold tongue—especially visible in the eastern Pacific—is primarily driven by Ekman-induced upwelling. A similar structure is also evident in observations (for e.g., Cromwell, 1953; Wyrtki, 1966). Meanwhile, mid-latitude SSTs are warmer when OHT is enabled, primarily due to horizontal diffusion, with some contribution from GM advection (also seen in Fig. 4). The Southern Ocean warms by 7–10°C in the OHT-on case, consistent with Codron (2012) and Charnay et al. (2013), again driven by GM advection and horizontal diffusion. Our OHT-on simulation also yields warmer and more realistic tropical SSTs than those in Charnay et al. (2013), with temperatures comparable to NCEP/NCAR reanalysis.

While OHT acts as the forcing and SSTs the response, the downstream consequence is seen in precipitation patterns. Figure 6c shows the corresponding decadal-averaged precipitation difference. As in the aquaplanet simulations, the OHT-off case features a precipitation peak at the equator. However, when OHT is enabled, we get a (weak) double-peaked precipitation structure around the equator due to suppressed evaporation given the Ekman-driven upwelling. Following Codron (2012), we note that lower values of the frictional damping coefficient  $\epsilon$  (see Sect. 2.3.1) lead to a more zonally extended equatorial cold tongue.

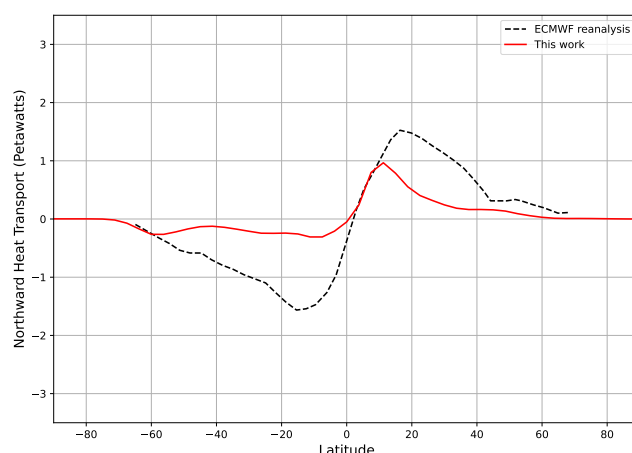
The annually-averaged position of the ITCZ on Earth lies near 5°N (Frierson et al., 2013; Marshall et al., 2014). This hemispheric preference arises due to a combination of factors, including the unequal distribution of landmasses and the oceanic



400 Meridional Overturning Circulation (MOC). The latter plays a particularly important role: Frierson et al. (2013) demonstrated that the ITCZ shifts northward in GCM simulations when OHT is included, even in the absence of continents. This suggests that the northward displacement of the tropical rain band is not merely a response to hemispheric radiative asymmetries, but is actively maintained by the MOC, which transports approximately 0.4 PW (Frierson et al., 2013; Marshall et al., 2014) of heat across the equator into the Northern Hemisphere, thereby shifting the ITCZ northward.

405 In our OHT-off simulation, the absence of OHT results in a near-equatorial ITCZ, slightly north-shifted ( $\approx 3.5^\circ\text{N}$ ), likely due to residual atmospheric processes (see Fig. 6c). In the OHT-on case, we find that the ITCZ is positioned around  $3.5^\circ\text{S}$ . This is due to: (a) the lack of density-driven MOC in our model, and (b), OHT causing sea ice loss in the Southern Hemisphere, resulting in excessive warming there. This Southern Hemisphere warming drives a northward atmospheric energy transport, which shifts the ITCZ southward to around  $3.5^\circ\text{S}$ , as shown in Fig. 6c. This behaviour is consistent with the compensation  
 410 mechanism discussed in Frierson et al. (2013), where the ITCZ migrates toward the hemisphere receiving more net heating.

## 4.2 Impact of ocean heat transport on meridional energy redistribution



**Figure 7.** Total northward meridional ocean heat transport (in Petawatts) for modern Earth, as simulated by our model (solid red line) and derived from ECMWF reanalysis data (black dashed line; Trenberth and Caron 2001).

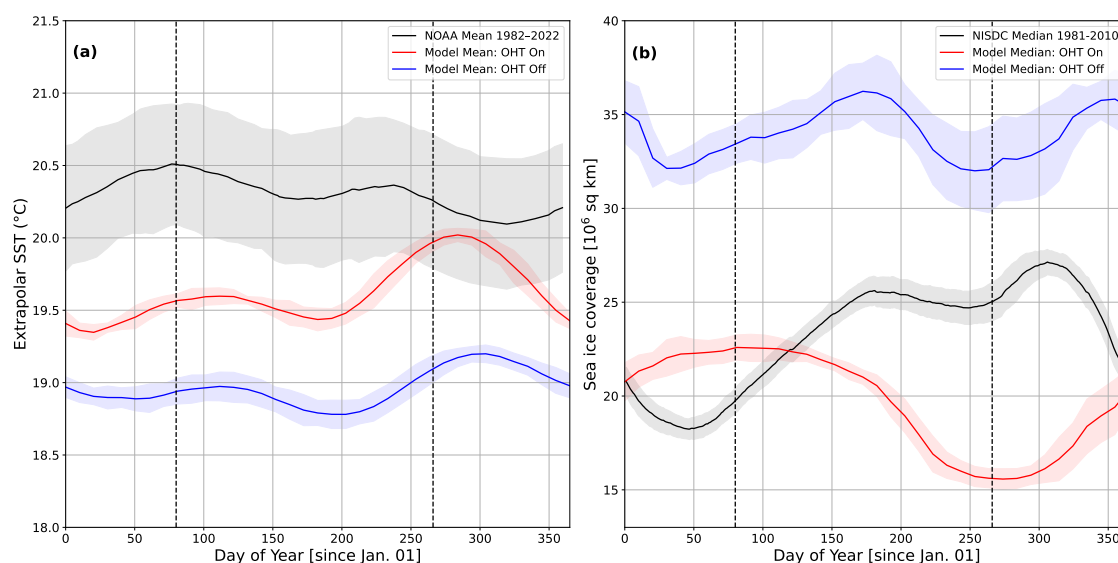
Figure 7 presents the meridional ocean heat transport (in petawatts) for modern Earth, comparing results from our model (solid red line) with estimates derived from ECMWF reanalysis (black dashed line; Trenberth and Caron 2001). While our model does not capture the full magnitude of Earth’s heat transport, it successfully reproduces the wind-driven component of the circulation well due to the combination of the Ekman and GM parameterisations. This is especially evident in the Northern Hemisphere tropics, where the Pacific Ocean dominates the total transport (see Fig. 5 in Trenberth and Caron 2001).  
 415

However, the peak northward OHT in our model ( $\approx 1$  PW) is lower than reanalysis estimates ( $\approx 1.5$  PW), and Southern Hemisphere OHT is similarly underestimated ( $-0.3$  PW vs.  $-1.5$  PW). These discrepancies stem primarily from the absence



of a full-depth MOC in our model. While we include Ekman transport, horizontal diffusion, and the GM parameterisation that together represent key aspects of the wind-driven and eddy-driven components of the MOC, we do not simulate density-driven processes such as deep water formation and diapycnal mixing. These components are critical for reproducing the full strength and structure of the observed MOC, particularly in the Atlantic and Southern Ocean, where density-driven transport dominates (see Fig. 5 in Trenberth and Caron 2001, and also Frierson et al. 2013 and Marshall et al. 2014).

### 4.3 Impact of ocean heat transport on seasonal climate and sea ice



**Figure 8.** (a) Seasonal evolution of extrapolar sea surface temperatures (SST; 60°S–60°N), and, (b) global sea ice coverage for NOAA/NISDC observations (black), for the model with ocean heat transport enabled (red), and disabled (blue). Shaded regions represent the  $2\sigma$  inter-annual variability (30–40 years). Vertical dashed lines indicate the timing of the March and September equinoxes.

The seasonal evolution of extrapolar SSTs (60°S–60°N, Fig. 8a) and global sea ice coverage (Fig. 8b) is strongly modulated by the presence or absence of OHT, which affects both the amplitude and phase of their annual cycles. Figure 8 compares these diagnostics across three cases: observations (black), the model with OHT enabled (red) and disabled (blue). Shaded regions represent the  $2\sigma$  interannual variability over a 30–40 year period<sup>5</sup>, and vertical dashed lines denote the March and September equinoxes.

Observed SSTs (from NOAA, Fig. 8a) exhibit a characteristic bimodal seasonal pattern, with peaks around the equinoxes, accompanied by corresponding advances and retreats in global sea ice coverage (NSIDC, Fig. 8b), reflecting seasonal polar heating and cooling. The physical origins of the observed SST peaks are rooted in hemispheric asymmetries. The first peak around the March equinox arises from the warming of the vast Southern Hemisphere oceans, whose influence outweighs that

<sup>5</sup>The observed SST variability is larger than in the model due to (a) the trend of rising atmospheric CO<sub>2</sub> levels between 1982–2022, and (b) multi-year climate variability, for instance, the El Niño–Southern Oscillation (ENSO).



of the colder, but smaller Northern Hemisphere ocean area during that time of the year. The second, smaller peak near the  
 435 September equinox is due to Northern Hemisphere warming, partially offset by cooler Southern Hemisphere SSTs. Our OHT-  
 on and -off simulations reproduce this bimodality to differing extents, but we produce a strong SST peak around the September  
 equinox. This is because our Southern Hemisphere oceans remain too warm due to underestimated Antarctic sea ice (see  
 Fig. E1). Additionally, we tend to lag observations by about a month likely due to a slightly elevated thermal inertia in our  
 model ocean and/or the assumption of a fixed mixed-layer depth. The latter overly damps SST variations in regions where the  
 440 real ocean mixed layer would be shallower – like in the tropics. We refer the reader to Sects. 5.4 and 5.5 for more details.

When OHT is disabled, the climate becomes 1.5–2°C cooler than observed (Fig. 8a), with a muted seasonal SST cycle. Sea  
 ice coverage is unrealistically high year-round – by approximately 10 million km<sup>2</sup> (Fig. 8b) – since the absence of poleward  
 heat transport allows ice to grow in both area and depth. This thick sea ice layer suppresses warming and inhibits ocean-  
 atmosphere coupling, damping SST variability further. Conversely, enabling OHT improves latitudinal heat redistribution,  
 445 leading to warmer extrapolar SSTs and limiting sea ice extent to values much closer to observations. Although the OHT-on  
 simulation does not fully capture the observed bimodality in sea ice, it more accurately captures the seasonal SST amplitude  
 and the annual averaged values of both SST and sea ice coverage. The annual mean biases are approximately 0.6°C for SST  
 and 3 million km<sup>2</sup> for sea ice coverage, respectively. The extent of sea ice also influences the planetary bond albedo, which  
 in our OHT-on and -off simulations, is approximately 0.32 and 0.33 respectively, closely matching the observed value of 0.30  
 450 derived from NCEP/NCAR reanalyses.

Figure 8b shows that the global median sea ice extent in the OHT-on simulation varies between 16–23 million km<sup>2</sup> – much  
 closer to the observed range (18–27 million km<sup>2</sup>) than the OHT-off case. However, both model versions overestimate Northern  
 Hemisphere sea ice (see Fig. E1), consistent with findings from Codron (2012). This likely stems from three factors: (a) the  
 absence of a deep overturning circulation transporting heat from the Southern Ocean to the North Atlantic, contributing to both,  
 455 excess sea ice in the North, and its lack in the South, (b) biases in sea ice albedo (see Sect. 5.4), and (c) the lack of sea ice drift,  
 which promotes excess ice build-up. In contrast, Antarctic sea ice (Fig. E1) is underestimated in both model configurations.  
 The same factors (a) and (b) apply here, as well as the missing Antarctic Circumpolar Current (ACC), which, in the real climate  
 system, helps thermally isolate the Antarctic continent and sustain sea ice cover.

We remind the reader that the primary objective of our model is not to exactly reproduce modern Earth’s climate, but to  
 460 capture its first-order features. This ensures greater confidence in the model’s behaviour when applied to different planetary  
 contexts, whether paleoclimate or exoplanets. Nevertheless, our modern Earth simulations yield surface temperatures that com-  
 pare well with both observational datasets and previous modelling studies (see Sect. 5.4). With OHT enabled, the simulation  
 produces a global annually averaged surface temperature of 13°C, in close agreement with the NCEP/NCAR reanalysis tem-  
 perature of 14.0°C for the 1981–2010 period. In contrast, the simulation without OHT yields a cooler average temperature of  
 465 12°C.

Beyond global average temperatures, the inclusion of OHT also improves other key diagnostics, such as extrapolar SSTs and  
 total sea ice extent, bringing them into closer alignment with observations. These quantities play a central role in the planet’s  
 energy balance—through their influence on albedo and outgoing longwave radiation—and are especially relevant for exoplanet



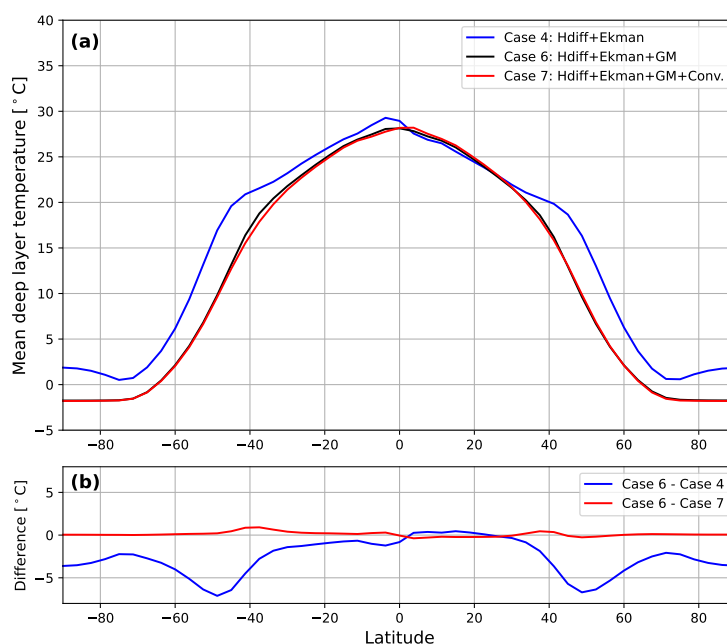
climate modelling. Given the limited constraints on exoplanet climates, such agreement with Earth benchmarks is a promising  
 470 validation of our model's physical realism.

## 5 Discussion

Given the successful validation of our model against aquaplanet and modern Earth benchmarks, this section explores the broader implications and insights of our dynamical slab ocean framework.

### 5.1 The dual role of Gent-McWilliams advection: Influence on Ekman transport and convection

475 One of the additions to the Generic-PCM's dynamical slab ocean model is the Gent-McWilliams (GM) parameterisation (Gent and McWilliams, 1990). The GM scheme enables isopycnal mixing, allowing for temperature diffusion across ocean layers and reducing excessive vertical temperature gradients. While this mixing tends to decrease stratification, it still modifies the temperature contrast between the surface and deeper layers that drives Ekman transport. As a result, the GM parameterisation introduces a two-way interaction between eddy-induced and wind-driven circulation, even within our idealised setup.



**Figure 9.** Gent-McWilliams (GM) restratification mimics the effect of convective adjustment: Zonally averaged deep ocean layer temperatures in the aquaplanet simulations. (a) Mean deep layer temperature (in °C) for cases including horizontal diffusion and Ekman transport (blue), with the addition of GM (black), and finally with convective adjustment (red). (b) Differences between selected simulations.

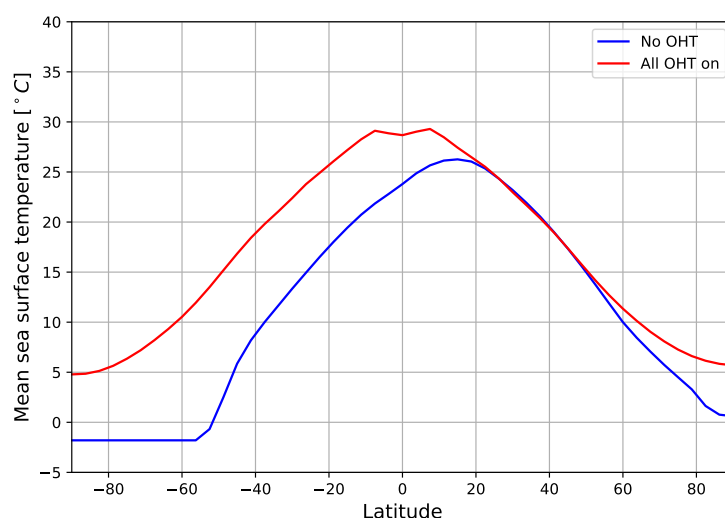
480 Interestingly, we find that the restratification produced by the GM scheme plays a role analogous to convective adjustment. Figure 9a shows the decadal-averaged zonal deep layer temperatures for three aquaplanet simulations. Case 6 (black line),



which includes horizontal diffusion, Ekman transport and GM, is nearly indistinguishable from Case 7 (red line), which also includes convective adjustment. This lack of difference indicates that convective processes contribute negligible additional transport in this configuration. In contrast, Case 4 (blue line), which excludes GM, exhibits significantly warmer deep layer  
 485 temperatures at mid-to-high latitudes. Figure 9b, which presents temperature differences between simulations, highlights this: the inclusion of GM cools the deep ocean by 3–7°C in high-latitude regions, whereas adding convection yields negligible change. These results suggest that under the tested conditions, GM alone captures the dominant effects typically associated with convective adjustment - namely, vertical mixing in regions of unstable stratification. Although our GM scheme was designed to parameterise mesoscale eddies along isopycnals, it also implicitly induces vertical mixing and thereby mimics  
 490 convection.

## 5.2 Hemispherical asymmetries and numerical instabilities

Previous aquaplanet simulations with obliquity using the Generic-PCM (e.g., Chaverot et al. 2023) revealed a persistent pronounced hemispheric asymmetry in surface temperature and cloud cover, even after year-long averaging. In Chaverot et al. (2023), simulations were initialised starting from the Vernal Equinox and without OHT. The resulting asymmetry was attributed to an initial hemispheric bias that triggered a net north–south atmospheric heat transport, allowing one Hadley cell to  
 495 dominate over the other. This induced a feedback that persisted throughout the simulation.



**Figure 10.** Ocean heat transport (OHT) suppresses hemispheric climate asymmetries caused by initialisation biases: zonally averaged sea surface temperatures for our oblique aquaplanet setup, with OHT disabled (blue) and enabled (red).

We propose an additional explanation involving the role of OHT. Our oblique aquaplanet simulations show that when OHT is disabled (blue line in Fig. 10), the hemispheric bias imprinted at model initialisation is not corrected by the system. In the absence of OHT, there is no mechanism—apart from atmospheric transport—to redistribute excess energy across hemispheres,



500 triggering a cascade of feedbacks. The initially warmer Northern Hemisphere delays sea ice growth, while the Southern Hemisphere cools rapidly due to atmospheric transport acting on short timescales. This cooling is amplified by the ice–albedo feedback, leading to early and extensive sea ice formation, which locks in a strong hemispheric asymmetry. Atmospheric heat redistribution alone is insufficient at evening out hemispherical differences – and can even amplify them – through feedbacks involving the cross-equatorial Hadley cell, which develops with ascending motion in the warmer hemisphere. The associated  
 505 cloud cover and moisture content further modulate the radiation budget, reinforcing the asymmetry.

When OHT is on (red line in Fig. 10), the ocean helps smooth out temperature gradients, mitigating the imprint of the initial bias. At model start, heat stored in the ocean is transported from lower to higher latitudes in both hemispheres through the mechanisms discussed in Sect. 2.3. This redistribution limits excessive sea ice formation in the South and prevents the North from staying anomalously warm. The ocean circulation forced by the cross-equatorial Hadley cell will also transport heat  
 510 across the equator towards the cold hemisphere, with opposite feedbacks from the ones associated with atmospheric transport. In general, strong persistent hemispheric asymmetries in aquaplanet setups are unphysical and typically reflect initial condition biases and/or numerical artefacts. The key takeaway is that *both*, oceanic and atmospheric heat transport, are essential for suppressing such asymmetries and maintaining a physically realistic climate state.

With further experiments, we found that enabling OHT also enhances numerical stability in the Generic-PCM. In the OHT-  
 515 off configuration, the model frequently encountered dynamical instabilities during long integrations. These usually manifest as spurious temperature dips near the surface or at the top of the atmosphere, often triggering radiative transfer scheme failures (temperatures dropping below the lower bounds of the lookup tables), causing the model to crash. These issues are largely absent when OHT is enabled. A likely explanation is that OHT efficiently smooths meridional temperature gradients – particularly at smaller scales due to the diffusive components – thereby reducing the likelihood of instabilities and excessive vertical  
 520 motions. These OHT-smoothened temperature fields may also improve numerical stability by reducing sharp vertical gradients that can otherwise trigger Courant–Friedrichs–Lewy (CFL) violations in the model’s dynamical core.

Altogether, our findings suggest that OHT acts not just as a physical driver of climate symmetry but also as a stabilising agent in coupled climate simulations. Furthermore, they highlight the importance of incorporating dynamic oceans in (exo-)climate models, particularly when strong climate feedbacks – such as the ice–albedo feedback in our case and the water  
 525 vapour feedback in Chaverot et al. (2023) – are present.

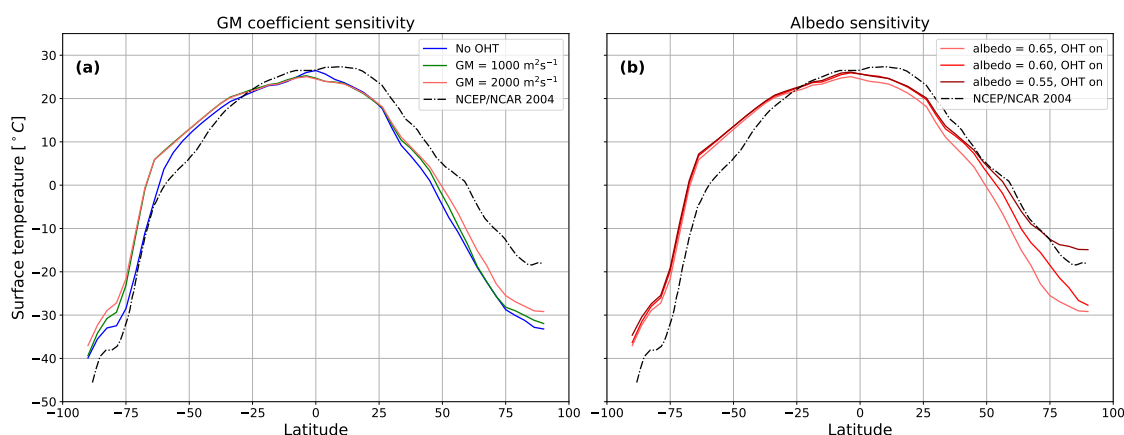
### 5.3 Comparison with a q-flux ocean

One approach in low-complexity ocean modelling is the q-flux method, where OHT is prescribed as a fixed meridional heat flux (q-flux) based on observational data or AOGCM simulations. While this avoids the computational cost of explicitly solving ocean dynamics, it requires an initial, expensive reference simulation to determine the appropriate OHT. In the context of  
 530 exoplanets, where observational constraints are limited and reference dynamical ocean simulations are typically unavailable (with some exceptions: for e.g., Del Genio et al., 2019; Yang et al., 2020; Batra and Olson, 2024), no q-flux can be prescribed. More critically, if an OHT is imposed rather than emergent, it cannot dynamically respond to changes in the atmosphere, ocean, or external forcing. As a result, key climate feedbacks—such as adjustments in meridional heat transport due to sea

ice growth, atmospheric circulation shifts, or changes in composition (e.g., chemistry, greenhouse gases)—are not captured self-consistently.

In contrast, our dynamical slab ocean model allows for an emergent OHT based on ocean-atmosphere interactions. This is particularly important in cases where strong feedbacks develop – such as the ice-albedo effect in our simulations or the water vapour feedback in Chaverot et al. (2023) – and more broadly because atmospheric and oceanic heat transports are strongly coupled via surface winds. Unlike q-flux oceans, our approach allows for the ocean to dynamically adjust to evolving atmospheric and external conditions, leading to a more physically consistent climate response.

#### 5.4 Model sensitivity to GM and albedo coefficients



**Figure 11.** Zonally averaged surface air temperature for modern Earth simulations under two different sensitivity experiments. **(a)** Gent-McWilliams (GM) coefficient sensitivity test comparing model simulations with two different GM values against NCEP/NCAR reanalysis (black dashed line). **(b)** Albedo sensitivity test comparing model simulations with three different sea ice/snow albedo values against reanalysis data.

Figure 11a explores model sensitivity to the GM and horizontal diffusion coefficients. In the OHT-off simulation (blue), surface temperatures at high northern latitudes ( $60^{\circ}$ – $90^{\circ}$ N) are up to  $15^{\circ}\text{C}$  colder than the NCEP/NCAR reanalysis (black dashed line). Introducing OHT by increasing the GM coefficient (green and red lines, for  $1000$  and  $2000\text{ m}^2\text{s}^{-1}$ , respectively) and/or varying the horizontal diffusion ( $8000$  to  $25000\text{ m}^2\text{s}^{-1}$ ) warms the Arctic modestly, raising temperatures by about  $3$ – $4^{\circ}\text{C}$ . However, this is insufficient to eliminate the persistent cold bias. Seasonal analysis reveals that while summer Arctic temperatures fall within expected bounds ( $-10^{\circ}\text{C}$  to  $0^{\circ}\text{C}$ ), average winter temperatures plunge to  $\approx -50^{\circ}\text{C}$  – approximately  $20^{\circ}\text{C}$  colder than observed. This suggests that a more dominant process is responsible, likely involving a combination of atmospheric transport inefficiencies, radiative imbalances, and/or model tuning choices such as surface albedo.

Figure 11b illustrates the model’s sensitivity to sea ice and snow albedo, which is reduced from  $0.65$  to  $0.60$  and  $0.55$  for the OHT-on simulation. Lowering the albedo does mitigate the Arctic cold bias, with a stronger warming effect than seen in the GM experiments. However, this comes at the cost of Southern Hemisphere sea ice almost completely disappearing, while



concurrently reducing annual global sea ice extents to unrealistic levels (10 million sq. km), introducing a new discrepancy. The systematic Southern Hemisphere warm bias also hints at a hemispheric imbalance, where the (orbital-parameter-induced) excess heat in the south is not being effectively redistributed to the Northern Hemisphere, despite the heat transport provided by the ocean. Additionally, the atmospheric model of the GCM may under-represent poleward moist static energy transport, particularly via latent heat. Together, these factors suggest a complex interplay between radiative, oceanic, and atmospheric processes that warrants deeper investigation. Nevertheless, we reiterate that these discrepancies remain within acceptable bounds, given that our model is not built with the intention of precisely reproducing modern Earth's climate but rather that of exoplanets, where observational constraints are far more uncertain.

## 5.5 Caveats and opportunities for future work

One of the driving applications for developing the dynamical slab ocean model is to simulate the climates of terrestrial exoplanets. Given that the model is flexible, relatively easy modifications can be made. For example, some exoplanets are expected to experience non-negligible geothermal heat fluxes – this additional energy source can be incorporated in the model as a constant or spatiotemporally varying ground-heating term (see Eq. 1). Moreover, many of the currently known terrestrial exoplanets are expected to be tidally locked in a 1:1 spin-orbit resonance, particularly those orbiting close to M-dwarf stars. In such cases, the planet's rotation period equals its orbital period – typically ranging from 5 to 15 Earth days for temperate planets. This can place these planets in dynamical regimes distinct from Earth-like rotators (for e.g., see Sergeev et al., 2022a, b). Most climate model parameters, including those governing subgrid-scale mixing, are traditionally calibrated for Earth-like rotation rates. For instance, the diffusion coefficients discussed in Sect. 2.3 were selected to match the meridional ocean heat transport of an Earth-like aquaplanet (Marshall et al., 2007). However, the reduced Coriolis parameter  $f$  on slowly rotating tidally locked planets will lead to a larger Rossby deformation radius (since  $L_D \sim \sqrt{g'H}/f$ , where  $g'$  and  $H$  are the reduced gravity and scale height respectively), which sets the typical scale of baroclinic eddies, from 10 to 100 km on Earth's ocean. This suggests that eddy-driven mixing processes may differ substantially on such climates (see Showman et al., 2010, for a detailed review). While a detailed prescription for this adjustment lies beyond the scope of this work, it will be the subject of future investigation.

A related limitation arises from our assumption of a globally uniform, fixed mixed-layer depth (MLD). In reality, the MLD varies with location and season due to wind forcing, ocean currents, and surface heating (e.g., McCreary Jr et al., 2001; Kara et al., 2003). Olson et al. (2020) also showed that mixed layer seasonality increases with planetary obliquity. The fixed MLD approach simplifies calculations of ocean heat transport, but can introduce biases. First, regions that should have a deeper MLD, such as high-latitude oceans during winter, may exhibit larger or faster surface temperature variations due to an artificially small heat capacity. Conversely, regions that should have a shallower MLD, such as tropical oceans, may experience overly dampened temperature variations. This limitation could impact the accuracy of (short-timescale) climate feedbacks, particularly the ice-albedo feedback, since a dynamically varying MLD would allow for more realistic oceanic heat uptake and redistribution. Choosing a representative MLD is particularly challenging for exoplanets, where no observational constraints exist – akin to the challenge of prescribing a  $q$ -flux. A promising direction for future work is to adopt an “Ekman mixed-layer ocean” scheme, which uses multiple slab layers and includes explicit vertical mixing. This approach, demonstrated by Hsu et al. (2022) – who



combined it with the Ekman transport parameterisation of Codron (2012) – may offer a more physically robust framework than using a fixed-depth single-layer ocean.

Our model includes salinity solely as a modifier of the freezing point of seawater. This is an important modification as a depressed freezing point inhibits sea ice formation – leading to reduced global sea ice cover with increasing salinity. Olson et al. (2022) demonstrated that higher salinities tend to warm planetary climates – offering a potential solution to the Faint Young Sun Paradox for Archean Earth – and attributed this warming primarily to changes in density-driven ocean dynamics rather than to freezing point depression. Building on this, Batra and Olson (2024) found that while salinity has a strong, nonlinear impact on G-star planets, leading to abrupt sea ice loss and surface warming, its effect on M-dwarf planets is more gradual, with minimal associated warming. Our model does not represent the dynamical effects of salinity – such as its role in setting ocean density or driving thermohaline circulation. As highlighted by Codron (2012), this can lead to an underestimation of convective exchanges in high-latitude regions and inadequate cooling of the deep ocean. The absence of salinity also prevents the model from capturing salt rejection during sea ice formation, a process that increases local water density and promotes vertical mixing. While including a prognostic salinity field would improve realism and enable the simulation of regional ocean features, it would also significantly increase model complexity. For exoplanet studies, where the priority lies in capturing first-order climate dynamics rather than detailed regional processes – this simplification remains justified. Nonetheless, future extensions of our model could explore ways to incorporate simplified density-driven processes without the overhead of full ocean dynamics.

The model does not simulate sea ice drift, a simplification made to reduce computation time. On modern Earth, this omission can lead to unrealistically high sea ice accumulation in the Arctic (as seen from our model data in Fig. E1), as ice is unable to be transported out of the region and instead thickens and expands in place (Codron, 2012). While this may be a secondary effect under present-day Earth conditions, sea ice dynamics has been shown to play a critical role in shaping planetary climate regimes. They are essential for simulating transitions between stable climate states on Earth and exoplanets. For example, dynamic sea ice facilitates equatorward transport, promoting Snowball Earth initiation and enhancing the instability of tropical sea ice margins (Lewis et al., 2007; Voigt and Abbot, 2012). These processes may be even more important on tidally locked planets, where strong day–night contrasts can interact with sea ice transport to produce qualitatively different climate outcomes (Yang et al., 2020). Future work is needed to assess whether incorporating sea ice drift is feasible within the framework of our model without incurring prohibitive computational costs.

## 6 Conclusions

We introduce a dynamical slab ocean model integrated into a 3-D GCM called the Generic-PCM. The fully parallelised model offers a compromise between the computational efficiency of slab ocean models and the physical realism of fully coupled AOGCMs. Sea ice and snow albedos are parameterised to be spectrally and thickness dependent (Fig. 1). Unlike imposed-q-flux approaches, our model features emergent ocean heat transport (OHT) including wind-driven Ekman transport, horizontal diffusion, convective adjustment (Codron, 2012; Charnay et al., 2013), and a newly implemented Gent–McWilliams (GM) pa-





parameterisation for mesoscale eddy mixing (summarised in Fig. 2). Importantly, the realism that comes with OHT-on simulations is at no additional computational cost compared to OHT-off simulations run over the same number of model years.

We first demonstrate the individual (and combined) impacts of our OHT mechanisms (Table 2) using a zero obliquity aquaplanet configuration. We find that enabling OHT reduces sea ice coverage and alters tropical SST structure — replacing the unrealistic equatorial SST peak (seen in OHT-off, Fig. 3a) with a relative temperature minimum due to Ekman-induced upwelling (OHT-on, Fig. 3a). This upwelling also suppresses equatorial precipitation, forming a double-banded ITCZ, consistent with theoretical expectations. Figure 5 shows our model aquaplanet’s meridional OHT profile, with Ekman transport dominating in the tropics as expected from observations (Levitus, 1987), and GM and horizontal diffusion peaking near the ice edge — in agreement with previous fully coupled AOGCM studies (Marshall et al., 2007; Brunetti et al., 2019).

We then simulate modern Earth, where our OHT-on configuration produces an annual global average surface temperature of 13°C, close to the NCEP/NCAR reanalysis (14°C), whereas our OHT-off simulation yields a temperature of 12°C. We find that enabling OHT not only drives more realistic SSTs and precipitation patterns (Fig. 6), but also improves seasonal extrapolar SSTs and sea ice extent (Fig. 8). Specifically, the OHT-on case yields extrapolar SSTs within  $\approx 0.6^\circ\text{C}$  and sea ice coverage within  $\approx 3$  million  $\text{km}^2$  of observations, whereas OHT-off shows much larger biases (upto  $2.0^\circ\text{C}$  lower SSTs and 10 million  $\text{km}^2$  higher annual sea ice coverage than observations). We also report a planetary bond albedo of 0.32, in close agreement with NCEP/NCAR reanalysis (0.30). Our annual means are quite close to observations and we consider this satisfactory by exoplanet modelling standards, given the large uncertainties associated.

Beyond these benchmarks, we find that the GM parameterisation contributes to both horizontal and vertical mixing, with the latter mimicking the effect of convective adjustment (Fig. 9). Additionally, OHT also reduces hemispheric asymmetries that may arise from initial condition biases (Fig. 10) and in general, improves model numerical stability. Given the flexibility of the dynamical slab ocean model, exoplanet-based applications are relatively easy to add. For instance, an additional heat source can be included to simulate geothermal heating, and/or the diffusion coefficients can be adjusted depending on planetary rotation rates. These extensions will be explored in future work.

We simulate well the wind-driven component of oceanic circulation on modern Earth. However, since we do not model the density-driven branch of the MOC, we cannot reproduce the full strength and structure of the observed MOC (Fig 7). Some discrepancies remain between our simulations and observations – including a southward-shifted ITCZ (Fig. 6), a colder Northern Hemisphere (Fig. 11), and minor deviations in sea ice extent and SSTs (Fig. 8) – which we analyse and discuss, along with potential strategies for improvement. We also assess the model’s sensitivity to the diffusion coefficients and sea ice albedo (Fig. 11), and outline future developments, including the addition of salinity, dynamic sea ice drift, and a varying mixed-layer depth.

The core aim of our model is to strike a balance between physical realism and computational efficiency, which makes it particularly well-suited for large parameter space exploration. By capturing crucial effects of OHT – without the associated computational cost of solving primitive equations – the model enables long-timescale simulations and broad sensitivity studies while retaining key processes that shape planetary climates. This work lays the foundation for the continued development of the



Generic-PCM, with the goal of enhancing its readiness to better interpret future observations of temperate terrestrial exoplanets  
655 from upcoming missions such as RISTRETTO@VLT, PCS@ELT, HWO, and LIFE.



## Appendix A: Ocean Physical Parameters

Parameter	Value
Freezing seawater temperature, $T_0$ [K]	271.35
Melting seawater temperature [K]	273.15
Mean ice density, $\rho_i$ [ $\text{kg m}^{-3}$ ]	917
Mean snow density [ $\text{kg m}^{-3}$ ]	300
Seawater density [ $\text{kg m}^{-3}$ ]	1026
Ice thermal conductivity, $\lambda$ [ $\text{W m}^{-1} \text{K}^{-1}$ ]	2.17
Snow thermal conductivity, [ $\text{W m}^{-1} \text{K}^{-1}$ ]	0.31
Specific heat capacity of ice (& snow), $C_i$ [ $\text{J kg}^{-1} \text{K}^{-1}$ ]	2067
Specific heat capacity of seawater, $C_p$ [ $\text{J kg}^{-1} \text{K}^{-1}$ ]	3994
Latent heat of fusion of ice (& snow), [ $\text{J kg}^{-1}$ ]	334000
Latent heat of sublimation of ice (& snow), [ $\text{J kg}^{-1}$ ]	2834000
Maximum albedo of ice (& snow)	0.65

**Table A1.** Oceanic physical parameters used in the model. Units are given in SI.



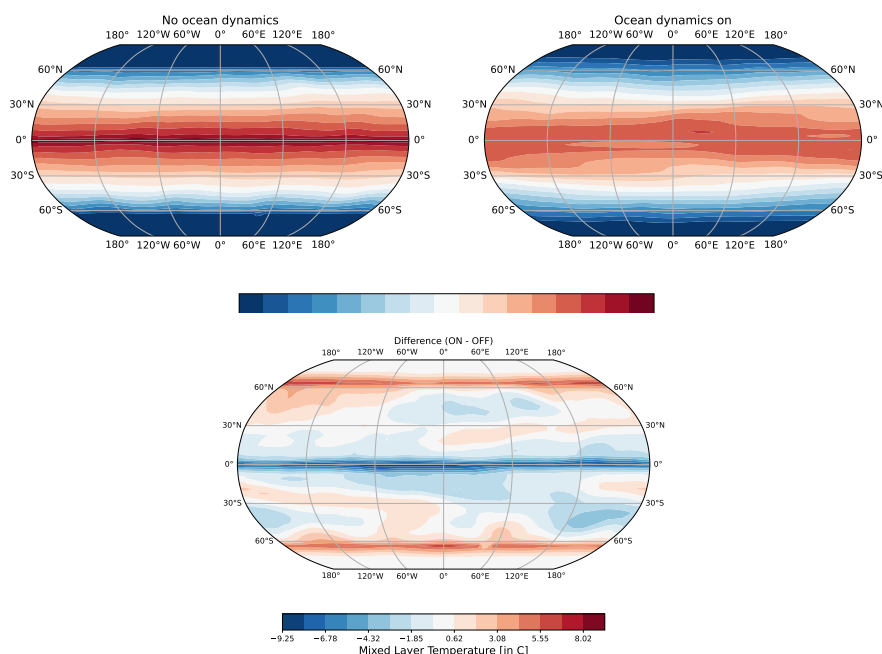
## Appendix B: Computation speed

At the spatiotemporal resolution used in this study (see Sect. 2), one model year requires approximately 2.75 hours of computation time on 24 cores – for both, the OHT-on and OHT-off cases. This suggests that Generic-PCM simulations requiring an ocean can enable OHT without incurring additional computational cost for the same number of model years. This efficiency arises from the way OHT is implemented in our dynamical slab ocean model: the diffusion-like processes (i.e., horizontal diffusion and the GM scheme) are relatively inexpensive to compute on coarse grids, and the added overhead per timestep is negligible compared to the cost of the atmospheric model and coupling processes.

However, at higher horizontal resolutions, OHT-on simulations may become more computationally demanding than OHT-off cases. This is due to the increased cost of additional Laplacian-based calculations, which scale with resolution and can introduce greater parallelisation overhead. But in this study, the ocean physics is called every physical timestep (once every 7.5 or 15 model minutes, see Sect. 2). This frequency could be reduced – for example, to a few calls per model day or even just once daily – with minimal impact on physical accuracy and a notable gain in computational efficiency. Nonetheless, even at high spatial resolutions, we expect our dynamical slab ocean model to remain significantly faster than a fully coupled AOGCM at equivalent resolution since it avoids solving the full set of fluid prognostic equations, which are typically the main computational bottleneck.



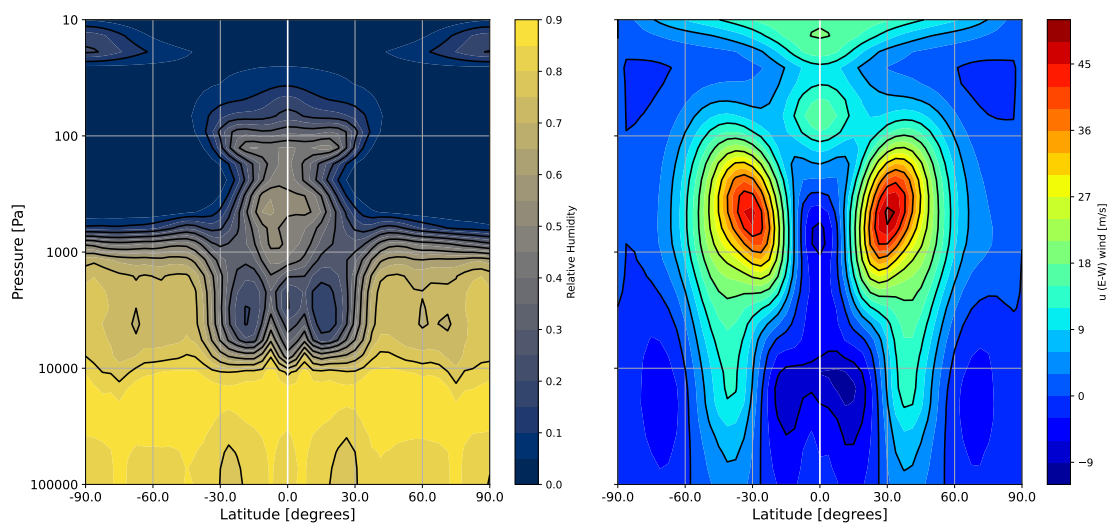
## Appendix C: Annually averaged maps



**Figure C1.** Annually averaged sea surface temperature (SST) maps for the zero-obliquity aquaplanet simulations. The top-left panel shows SST for Case 1 (no ocean heat transport, OHT), while the top-right panel shows SST for Case 7 (all OHT enabled). The bottom panel displays the difference between the two (Case 7 - Case 1), highlighting the impact of OHT. Notable features include equatorial upwelling of cold water and enhanced warming at higher latitudes.



## Appendix D: Atmospheric profiles

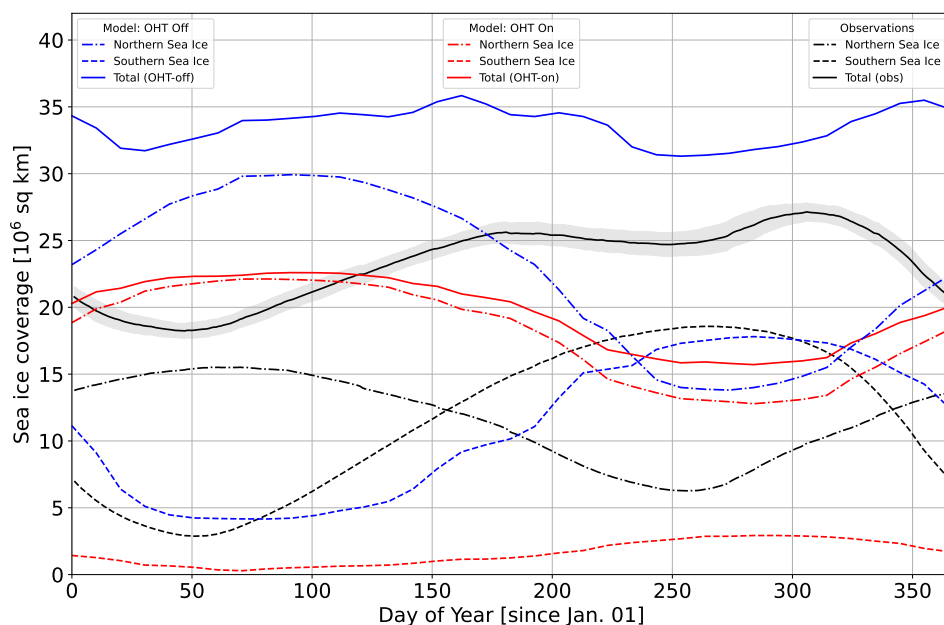


**Figure D1.** Annually averaged atmospheric profiles for the zero-obliquity aquaplanet simulations. The left plot shows the relative humidity of the atmosphere as a function of pressure levels and latitude for the Case 7 simulation (all ocean heat transport on). The plot on the right shows the same simulation's zonal winds, with the mid-latitude jet streams clearly visible.





## Appendix E: Seasonal evolution of modern Earth's sea ice coverage



**Figure E1.** Seasonal evolution of global sea ice coverage for NSIDC observations (black), the model with ocean heat transport enabled (red), and disabled (blue). For each case, the dashed lines represent Southern sea ice and the dash-dotted lines the Northern sea ice.



675 *Code and data availability.* All model simulations presented in this study were performed using revision 3423 of the Generic-PCM (Generic-PCM-Team, 2025, latest revision available at <http://svn.lmd.jussieu.fr/Planeto/trunk/LMDZ.GENERIC/>). A frozen version of the model code, together with the initial conditions and the GCM outputs from the final model year of the stable climate states for Cases 1 to 7 of the zero-obliquity aquaplanet, and for the OHT-on and -off modern Earth configurations, is archived on Zenodo (Bhatnagar et al., 2025, <https://doi.org/10.5281/zenodo.16417154>). This DOI represents all versions of the repository. Additional data supporting this article can be  
680 provided upon request to the corresponding author.

The primary routines related to the dynamical slab ocean model—`ocean_slab_mod.F90`, `slab_heat_transp_mod.F90`, `physiq_mod.F90` and `hydrol.F90`—are located within the physics directory of the Generic-PCM source code. Model documentation is provided on the Generic-PCM Wiki page (Generic-PCM-Team, 2025, [https://lmdz-forge.lmd.jussieu.fr/mediawiki/Planets/index.php/Overview\\_of\\_the\\_Generic\\_PCM](https://lmdz-forge.lmd.jussieu.fr/mediawiki/Planets/index.php/Overview_of_the_Generic_PCM)) and practical guidance on the dynamical slab ocean model is available on its dedicated page (Bhatnagar, 2025, [https://lmdz-forge.lmd.jussieu.fr/mediawiki/Planets/index.php/Slab\\_ocean\\_model](https://lmdz-forge.lmd.jussieu.fr/mediawiki/Planets/index.php/Slab_ocean_model)).  
685

All reanalysis and observational datasets used in this study are publicly available. NCEP/NCAR Reanalysis data (Kalnay et al., 1996) and NOAA DOISST V2.1 High Resolution Dataset (Huang et al., 2021) are provided by the NOAA Physical Sciences Laboratory, Boulder, Colorado, USA, and can be accessed at <https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html> and <https://psl.noaa.gov/data/gridded/data.noaa.oisst.v2.highres.html>, respectively. ECMWF ERA-15 reanalysis data (Gibson et al., 1997) are available through the Copernicus  
690 Climate Data Store at <https://cds.climate.copernicus.eu>. Observational sea ice extent data were obtained from the NSIDC Sea Ice Index, Version 3 (Fetterer et al., 2017, <https://doi.org/10.7265/N5K072F8>).

*Video supplement.* The video file available on Zenodo (Bhatnagar et al., 2025, <https://doi.org/10.5281/zenodo.16417154>) illustrates the temporal evolution of SST for the zero-obliquity aquaplanet simulations.

*Author contributions.* S.B., E.B., M.B., J.K., and M.T. developed the study's conceptualisation. S.B., F.C., E.M., and M.T. contributed to  
695 the model code. S.B., E.B., M.B., and J.K. developed the methodology and conducted the analysis. S.B. performed the simulations, related investigation and wrote the original draft. All authors contributed to the review and editing of the manuscript. E.B., M.B., and J.K. supervised the project and related administration. E.B. and J.K. acquired the project funding.

*Competing interests.* The authors declare that they have no conflict of interest.

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