



# Constraining urban CO<sub>2</sub> emissions in Seoul using combined ground and satellite observations with Bayesian inverse modelling

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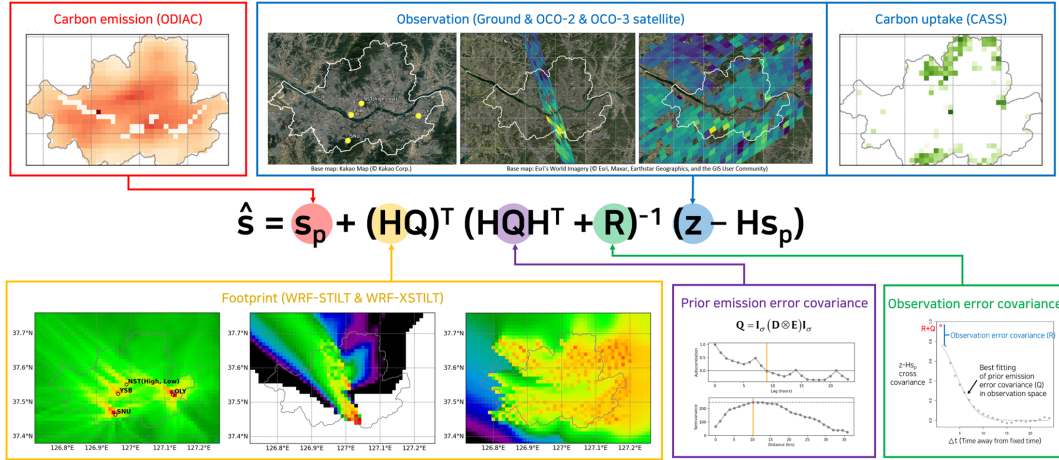
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**Abstract.** Accurate carbon emission estimates are essential for guiding climate action toward net zero emissions by 2050. The Bayesian inverse method, combined with atmospheric CO<sub>2</sub> measurements and the transport model, can serve as an independent verification approach to improve accuracy. In this study, we developed a Bayesian inverse modelling framework using ground- and space-based measurements and applied it to Seoul to test the framework and constrain its CO<sub>2</sub> emissions. By leveraging the high temporal resolution of ground-based in situ observations and the broad spatial coverage of satellite data, we improved the accuracy of emission estimates. Our results indicate a 4.43% increase in posterior emissions compared to prior estimates, suggesting that the prior emissions were slightly underestimated. The spatiotemporal variability of posterior emissions increased significantly, enabling us to track CO<sub>2</sub> fluctuations and assess the impact of carbon reduction policies over time and space. Additionally, the mean absolute error was reduced, improving the agreement between simulated and observed CO<sub>2</sub> enhancements. We thoroughly investigated the performance of the inverse model through a sensitivity analysis that considered different observational network configurations. The most substantial reductions in uncertainties (19.2%) were observed when all available observations were used. The extensive coverage of satellite observations enabled further corrections in areas not covered by ground observations. Overall, this study highlights the importance of combining multiple observational sources to better constrain urban CO<sub>2</sub> emissions. The framework also shows strong potential for application in other cities and can support the development of effective climate mitigation policies.



## Graphical abstracts



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## 1 Introduction

Global carbon emissions from fossil fuel combustion and land-use change are redistributed among the atmosphere, ocean, and land (Friedlingstein et al., 2022). In the global carbon cycle, these five major components closely interact to maintain balance. However, anthropogenic emissions of greenhouse gases (GHGs), particularly carbon dioxide ( $\text{CO}_2$ ), have dominated since the industrial era, resulting in rising atmospheric  $\text{CO}_2$  levels and driving climate change (Friedlingstein et al., 2022). Human-caused climate change amplifies global surface temperatures and impacts weather extremes such as heatwaves, tropical cyclones, droughts, and heavy precipitation (IPCC, 2023). To mitigate the adverse effects of climate change worldwide, international climate agreements like the United Nations Framework Convention on Climate Change, the Kyoto Protocol, and the Paris Agreement have been implemented (IPCC, 2023). The IPCC 1.5°C Special Report declared that achieving global net-zero  $\text{CO}_2$  emissions by 2050 is imperative to limit the increase in global temperature to 1.5 °C above pre-industrial levels (IPCC, 2018). More than 130 countries have signalled an intention to reduce  $\text{CO}_2$  emissions to near net-zero by around mid-century (Robinson and Shine, 2018).

By 2050, 68% of the world's population is projected to reside in urban areas (UN-DESA, 2018). At least 70% of global anthropogenic  $\text{CO}_2$  emissions originate from cities (IEA, 2015). Given the concentration of population and  $\text{CO}_2$  emissions in cities, they bear significant responsibility for emission reduction and are expected to play a major role in meeting their net-zero goals. The C40 Climate Leadership Group, comprising around 100 cities worldwide, has pledged to reduce GHG



emissions and developed a science-based approach (40 Cities, 2022). To support urban emission reduction strategies, the quality assurance of CO<sub>2</sub> emission estimates is required (Gurney et al., 2021; IPCC, 2019). Accurate emission estimates can provide detailed guidance to establish a baseline for prioritizing climate action and assessing policy progress over time (Mueller et al., 2021).

Various efforts are underway to estimate CO<sub>2</sub> emissions through a bottom-up approach. This approach calculates anthropogenic CO<sub>2</sub> emissions based on socio-economic databases (e.g., energy consumption, housing statistics, and road networks) and emission factors. Because of limited access to activity data and unknown emission factors within urban areas, detailed CO<sub>2</sub> emission estimates with high spatial and temporal resolution have been developed only for certain cities, such as Indianapolis (Gurney et al., 2012), Los Angeles (Feng et al., 2016; Gurney et al., 2019b), Salt Lake City (Patarasuk et al., 2016), and New York (Gately et al., 2015). Other types of emission data products, including CDIAC (Carbon Dioxide Information and Analysis Center), EDGAR (Emissions Database for Global Atmospheric Research), and ODIAC (Open-Data Inventory for Anthropogenic Carbon Dioxide), have been devised to downscale global/national total emission estimates using proxies such as nighttime lights and population. Large discrepancies between bottom-up and downscaled CO<sub>2</sub> emission estimates at the urban scale have been reported, primarily stemming from the large point sources and road traffic (Gurney et al., 2019a). Such uncertainties limit the establishment of a CO<sub>2</sub> emissions baseline and assessing mitigation outcomes at the city levels.

A complementary and independent approach to verify these CO<sub>2</sub> emission estimates is deemed necessary (IPCC, 2019). In the top-down approach, emission estimates can be constrained via real-time CO<sub>2</sub> measurements and atmospheric transport models.

Consequently, combining bottom-up and top-down estimates has been explored using a Bayesian inversion approach for accurate CO<sub>2</sub> emission estimation. Bayesian inversion approach has been used in recent studies to optimize existing bottom-up estimates over Salt Lake City (Kunik et al., 2019; Mallia et al., 2020), Paris (Lian et al., 2022; Nalini et al., 2022), Los Angeles (Ye et al., 2020), and Tokyo (Ohyama et al., 2023; Pisso et al., 2019). They obtained optimal CO<sub>2</sub> emissions with the uncertainty reduction of 39.32% (Kunik et al., 2019), 27.7% (Mallia et al., 2020), 8–10% (Lian et al., 2022), 2–10% (Nalini et al., 2022), ~50% (Ohyama et al., 2023), and 20.09% (Pisso et al., 2019) compared to prior emissions.

Previous studies that performed inverse modelling for urban areas have primarily relied on a single type of observation to constrain emissions, most commonly ground-based in situ CO<sub>2</sub> measurements (Breón et al., 2015; Göckede et al., 2010; Lauvaux et al., 2016; Lian et al., 2023, 2022; Mallia et al., 2020; McKain et al., 2012; Nalini et al., 2022; Sargent et al., 2018; Staufer et al., 2016). Some studies have instead used ground-based Fourier Transform Infrared (FTIR) column-averaged CO<sub>2</sub> (XCO<sub>2</sub>) observations (Hedelius et al., 2018; Ohyama et al., 2023), airborne observations (Lopez-Coto et al., 2020; Pitt et al., 2022), or satellite observations (Hamilton et al., 2024; Kaminski et al., 2022; Roten et al., 2023; Wu et al., 2018; Ye et al., 2020). However, studies that combine multiple observation types to leverage their complementary strengths remain rare. Although Pisso et al. (2019) integrated in situ airborne and ground-based observations to assess Lagrangian inverse modelling, and Che et al. (2024) combined ground-based FTIR and satellite data to estimate CO<sub>2</sub> emissions, these studies focused on either near-surface CO<sub>2</sub> concentrations or vertical CO<sub>2</sub> profiles, rather than incorporating both perspectives. In this study, we



integrate ground-based in situ CO<sub>2</sub> observations, which provide detailed information on surface emissions and uptake with high temporal resolution, and satellite observations, which offer broad spatial coverage and capture the total atmospheric CO<sub>2</sub> column. By combining these two complementary datasets, we simultaneously account for surface CO<sub>2</sub> fluxes and their impact on the vertical distribution of atmospheric CO<sub>2</sub>. To our knowledge, this is the first inverse modelling study to fully utilize surface and column-integrated CO<sub>2</sub> measurements, providing a more comprehensive constraint on urban CO<sub>2</sub> emissions. Seoul is a megacity with a population of approximately 10 million, which accounts for 18% of South Korea's total population in 2022 (KOSIS, 2023). The population and infrastructure in Seoul are densely concentrated, making it more susceptible to severe damage from climate change than other regions. It also has one of the highest carbon emissions among the 13,000 cities worldwide (Moran et al., 2018). Seoul has participated in the C40 Climate Leadership Group since 2006, and in 2020, it announced the '2050 GHGs Reduction Promotion Plan' to achieve a net-zero emissions goal (Seoul Metropolitan Government, 2021). Within Seoul, a comprehensive CO<sub>2</sub> monitoring network has been established, encompassing numerous stationary monitoring sites and mobile platforms to understand the urban carbon cycle (Park et al., 2020; Sim et al., 2020). Given its dense population, concentrated emissions, and extensive measurement networks, Seoul can be an optimal testbed city for studies to verify CO<sub>2</sub> emission estimates and assess the effectiveness of the CO<sub>2</sub> monitoring network. In this study, we used a Bayesian inverse model and ground- and space-based measurements to improve the accuracy of CO<sub>2</sub> emission estimates over Seoul. We developed a high-resolution Bayesian inverse modelling framework with a spatial resolution of 0.01° and a temporal resolution of 1 h, incorporating anthropogenic CO<sub>2</sub> emissions, biogenic CO<sub>2</sub> fluxes, atmospheric CO<sub>2</sub> measurements, a Lagrangian transport model, and error covariances of both prior emissions and observations. We then estimated the optimal spatiotemporal distribution of CO<sub>2</sub> emissions over Seoul for December 2021, verifying existing emission data. Additionally, we evaluated the effectiveness of the inversion by comparing observed and simulated CO<sub>2</sub> enhancements using prior and posterior emissions. Finally, we conducted sensitivity tests on different observational datasets to assess their impact on emission estimates.

## 2 Data and methods

### 2.1 Bayesian inverse method

In this study, data assimilation is employed to estimate optimal (posterior) CO<sub>2</sub> emissions close to the true emissions. Data assimilation in CO<sub>2</sub> estimation optimally combines information from atmospheric CO<sub>2</sub> observations with a transport model and prior CO<sub>2</sub> emissions to produce accurate posterior estimates of CO<sub>2</sub> emissions. Posterior CO<sub>2</sub> emissions are derived through the minimization of the cost function (Enting, 2002; Tarantola, 1987) defined as follows:

$$L_s = \frac{1}{2}(\mathbf{z} - \mathbf{H}\mathbf{s})^T \mathbf{R}^{-1}(\mathbf{z} - \mathbf{H}\mathbf{s}) + \frac{1}{2}(\mathbf{s} - \mathbf{s}_p)^T \mathbf{Q}^{-1}(\mathbf{s} - \mathbf{s}_p) \quad (1)$$

Where  $\mathbf{z}$  is a vector of observed CO<sub>2</sub> enhancements,  $\mathbf{H}$  is the Jacobian matrix of footprint values from the atmospheric transport model,  $\mathbf{s}$  is a vector of the unknown true CO<sub>2</sub> emissions,  $\mathbf{R}$  is the covariance of observational errors,  $\mathbf{s}_p$  is a state vector of





prior CO<sub>2</sub> emissions, and  $\mathbf{Q}$  is the covariance of prior emission errors. The solution obtained by minimizing the cost function defined in Eq. (1) yields the optimized posterior CO<sub>2</sub> emission estimates ( $\hat{s}$ ), expressed as:

$$\hat{s} = s_p + (\mathbf{H}\mathbf{Q})^T(\mathbf{H}\mathbf{Q}\mathbf{H}^T + \mathbf{R})^{-1}(\mathbf{z} - \mathbf{H}s_p) \quad (2)$$

110 The posterior uncertainty covariance ( $\mathbf{V}_{\hat{s}}$ ) can be expressed as:

$$\mathbf{V}_{\hat{s}} = \mathbf{Q} - (\mathbf{H}\mathbf{Q})^T(\mathbf{H}\mathbf{Q}\mathbf{H}^T + \mathbf{R})^{-1}(\mathbf{H}\mathbf{Q}) \quad (3)$$

Using the posterior uncertainty covariance obtained from Eq. (3), the reduction in uncertainty resulting from the constraints on emissions can be calculated as:

$$\text{Error reduction} = \frac{\sqrt{Q_{bt}} - \sqrt{V_{\hat{s},bt}}}{\sqrt{Q_{bt}}} \times 100\% \quad (4)$$

115 Here,  $\mathbf{Q}_{bt}$  represents the domain- and time-averaged covariance of prior emission errors and  $\mathbf{V}_{\hat{s},bt}$  represents the domain- and time-averaged covariance of posterior emission errors.

In this study, we assessed the validity of posterior emissions resulting from the inverse model by calculating the reduced chi-squared value ( $\chi_r^2$ ) following Tarantola (1987). It is computed using the equation:

$$\chi_r^2 = \frac{1}{v} [(\mathbf{z} - \mathbf{H}\hat{s})^T \mathbf{R}^{-1}(\mathbf{z} - \mathbf{H}\hat{s}) + (\hat{s} - s_p)^T \mathbf{Q}^{-1}(\hat{s} - s_p)] \quad (5)$$

120 Where the squared data residual ( $\mathbf{z} - \mathbf{H}\hat{s}$ ) and emissions residual ( $\hat{s} - s_p$ ) from the inversion are normalized by their respective variance matrices,  $\mathbf{R}$  and  $\mathbf{Q}$ . The residuals are expected to follow a chi-squared distribution with  $v$  degrees of freedom, which in this study corresponds to the number of observations. The closer the reduced chi-squared value is to 1, the more accurately the prescribed errors of observations and prior emissions are set, leading to a more reliable estimation of posterior emissions.

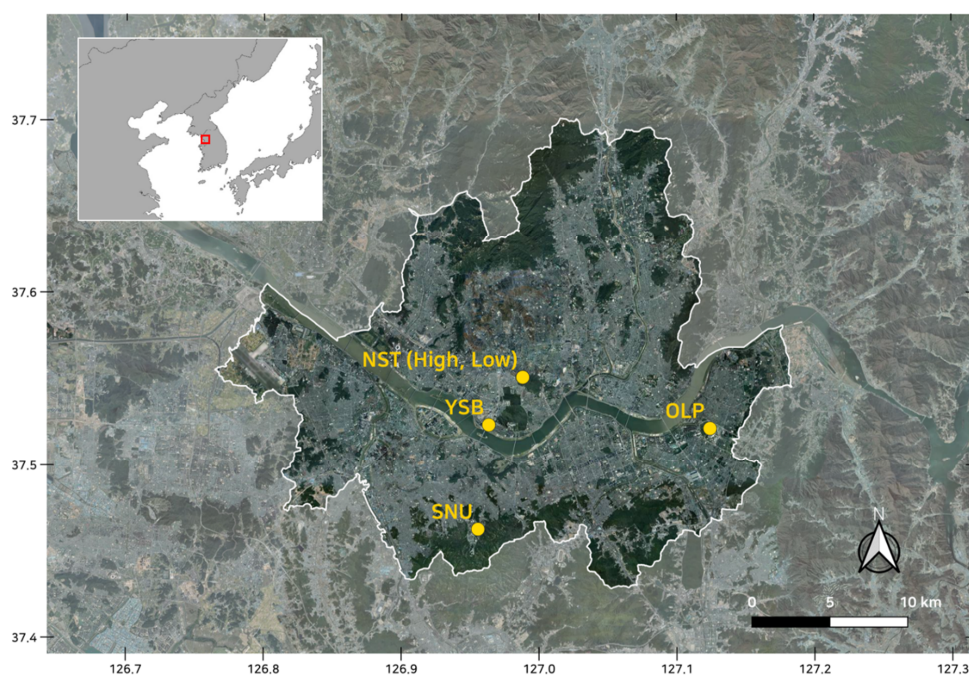
## 125 2.2 Observations

A set of measurements from ground-based and satellite observations, all collected during December 2021, was selected to obtain atmospheric CO<sub>2</sub> concentrations in Seoul. Although ground-based observations offer the advantage of real-time measurements of atmospheric CO<sub>2</sub> concentrations over an extended period, satellite observations provide broader spatial coverage.

130 For the ground measurements, we used observed CO<sub>2</sub> concentrations from five different sites in Seoul (Park et al., 2020): Namsan Seoul Tower-High (NST<sub>H</sub>), Namsan Seoul Tower-Low (NST<sub>L</sub>), Olympic Park (OLP), Seoul National University (SNU), and Yongsan Building (YSB), as shown in Fig. 1. The instrument inlet heights of NST<sub>H</sub>, NST<sub>L</sub>, OLP, SNU, and YSB, combined with the site altitude, are 420, 265, 27, 173, and 113 m, respectively. The observation instruments installed at NST<sub>L</sub> and OLP are PICARRO's G2301, whereas those installed at NST<sub>H</sub>, SNU, and YSB are LICOR's LI-850. We utilized only  
135 daytime data (10:00–16:00 KST) for the inverse modelling to minimize the impact of model biases in the planetary boundary layer height. The CO<sub>2</sub> concentrations measured at each ground observation site exhibit different patterns of variation because of differences in altitudes and surrounding environments (Fig. 2a). The average daytime CO<sub>2</sub> concentrations at NST<sub>H</sub>, NST<sub>L</sub>,

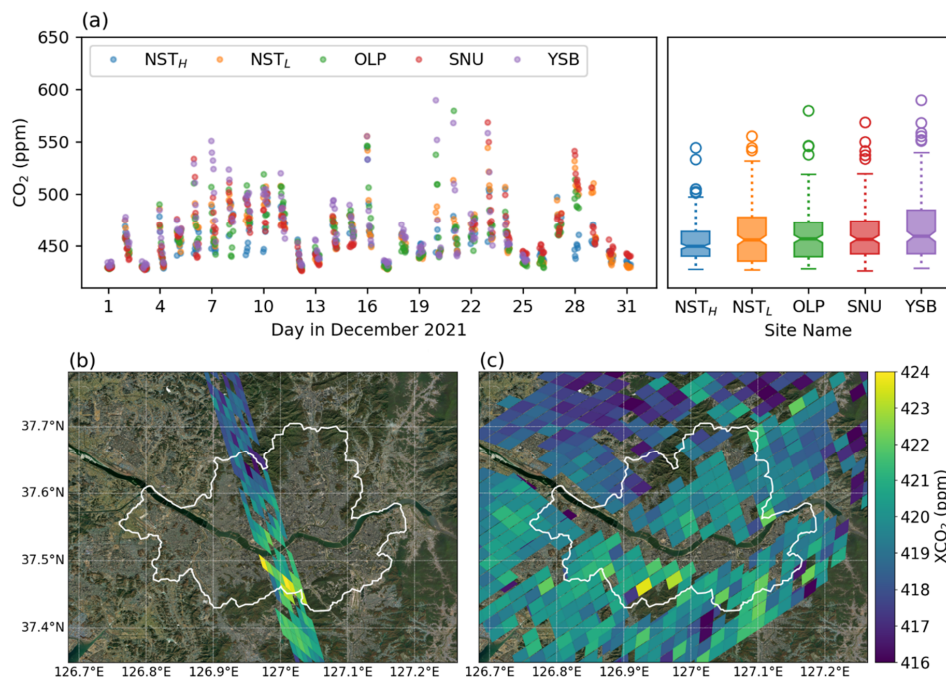


OLP, SNU, and YSB were  $453.7 \pm 19.6$ ,  $460.1 \pm 27.1$ ,  $460.2 \pm 26.7$ ,  $461.5 \pm 26.6$ , and  $466.9 \pm 31.4$  ppm, respectively. The lowest average concentration at NST<sub>H</sub> is attributed to its location at the top of the tall tower, whereas the highest average concentration at YSB is because of its location in a commercial area with high vehicle traffic.



**Figure 1:** Map of Seoul with the locations of CO<sub>2</sub> ground observation sites: Namsan Tower-high (NST<sub>H</sub>), Namsan Tower-low (NST<sub>L</sub>), Olympic Park (OLP), Seoul National University (SNU), and Yongsan Building (YSB). Observation sites are denoted with yellow points. The background map is sourced from Kakao Map (© Kakao Corp.).

We used data from the Orbiting Carbon Observatory-2 (OCO-2) and the Orbiting Carbon Observatory-3 (OCO-3) for satellite measurements. OCO-2 and OCO-3, launched on July 2, 2014, and May 4, 2019, respectively, observe the dry-air column-averaged volume mixing ratio of CO<sub>2</sub> (XCO<sub>2</sub>). On December 4 and 5, 2021, the OCO-2 and OCO-3 satellites passed over Seoul at 13:00 and 11:00 KST, respectively, yielding 60 and 167 soundings (Figs. 2b and 2c). Only good-quality data were considered when processing the XCO<sub>2</sub> data for observational input in inverse modelling. In both datasets, the XCO<sub>2</sub> values were higher in the southern part of Seoul compared to the northern part.



**Figure 2: Observation data used in the Bayesian inverse modelling framework over Seoul during December 2021. (a) Time series of daytime-only (10:00–16:00 KST) CO<sub>2</sub> concentrations measured at five ground sites and box plot of the daytime CO<sub>2</sub> concentrations from ground sites. Spatial distributions of XCO<sub>2</sub> measured by (b) OCO-2 on December 4, 2021, at 13:00 KST and (c) OCO-3 on December 5, 2021, at 11:00 KST. The background maps in (b) and (c) are based on Esri's World Imagery (© Esri, Maxar, Earthstar Geographics, and the GIS User Community).**

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The vector of observed CO<sub>2</sub> enhancements, denoted as  $\mathbf{z}$  in Eq. (1), represents the  $\Delta\text{CO}_2$  affected by nearby emission sources. Because we aim to optimize Seoul's CO<sub>2</sub> emissions using atmospheric observations, we must calculate  $\Delta\text{CO}_2$  influenced only by anthropogenic emissions within Seoul, excluding the effects of background and biogenic fluxes. To obtain the  $\Delta\text{CO}_2$ , the background and vegetation-affected concentrations must be subtracted from the observed CO<sub>2</sub> concentrations. We defined the background value for ground observations using the 24-h moving 5<sup>th</sup> percentile values from each site (Chandra et al., 2016; Gamage et al., 2020). For satellite observations, the background value was calculated from the daily median of measured XCO<sub>2</sub> over non-urban areas within a  $\sim 500,000 \text{ km}^2$  background box centered among Seoul (Labzovskii et al., 2019; Park et al., 2021). The calculation method for the vegetation-affected concentration is described in Sect. 2.4.



## 170 2.3 Atmospheric Transport

The Weather Research and Forecasting model with the (X-)Stochastic Time-Inverted Lagrangian Transport (WRF-(X)STILT) was used to derive the Jacobian matrix of footprint values ( $\mathbf{H}$ ) at a fine spatial resolution (e.g.,  $0.01^\circ$ ). We employed the STILT model (Fasoli et al., 2018; Lin et al., 2003) for ground-based observations and X-STILT (Wu et al., 2018) for satellite observations, both driven by meteorological fields from WRF model version 3.9.1 (Skamarock and Klemp, 2008). WRF-  
175 (X)STILT is an effective tool for simulating realistic atmospheric transport using a Lagrangian particle dispersion model within the planetary boundary layer (Nehrkorn et al., 2010). Previous studies have widely used WRF-(X)STILT as an atmospheric transport model for applying GHG inverse modelling in urban areas (Kunik et al., 2019; McKain et al., 2012; Ohyama et al., 2023; Sargent et al., 2018; Wu et al., 2018; Zhao et al., 2009).

The model releases backward 3D virtual air particle trajectories with stochastically turbulent dispersion from the observation  
180 location (receptor) to potential source regions that influence the receptor. It then counts the dispersed air particles (footprints) in each grid. Footprints quantify the sensitivity of the observation to upstream source regions. They can be regarded as the average contribution of the surface flux at the receptor, as they represent how densely and how long the air particles lingered backward in time within each discretized volume of the upwind source regions. In Bayesian inverse modelling, the footprint acts as an operator, connecting individual  $\text{CO}_2$  observations (unit: ppm) and gridded fluxes (unit:  $\mu\text{mol}/(\text{m}^2 \text{ s})$ ). Using footprints  
185 representing concentration per unit flux allows direct comparison between  $\text{CO}_2$  emissions and atmospheric  $\text{CO}_2$  enhancements. For WRF-STILT, one thousand air particles were released from each observation site and tracked backward in time for 24 h (Fig. 3a). In the case of WRF-XSTILT, one thousand air particles were released from each column level for OCO-2 and OCO-3 soundings and tracked backward for 24 h (Figs. 3b and 3c). The column receptors consisted of 37 levels at 100 vertical spacing up to 3000 m above ground level (a.g.l.) and 500 vertical spacing up to 6000 m a.g.l. thereafter. Details on the WRF  
190 configuration and footprint calculation for STILT and X-STILT are provided in Texts S1 and S2 of the supplementary material, respectively.

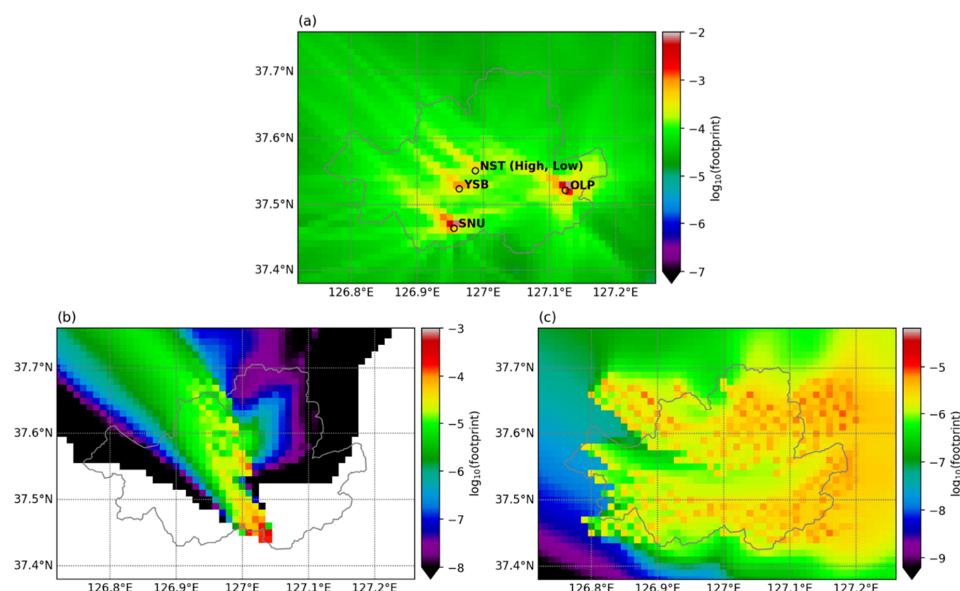


Figure 3: Footprint averages on a  $\log_{10}$  scale to upwind source regions of (a) ground observations, (b) OCO-2 satellite data, and (c) OCO-3 satellite data across the Seoul domain. The footprints are calculated using only daytime observation (10:00–16:00 KST) for December 2021. The footprint units are  $\text{ppm}/(\mu\text{mol}/(\text{m}^2\cdot\text{s}))$ . Note that the footprint ranges differ in panels (a), (b), and (c) for visualization purposes.

## 2.4 CO<sub>2</sub> emissions & biogenic fluxes

### 2.4.1 Anthropogenic CO<sub>2</sub> emissions

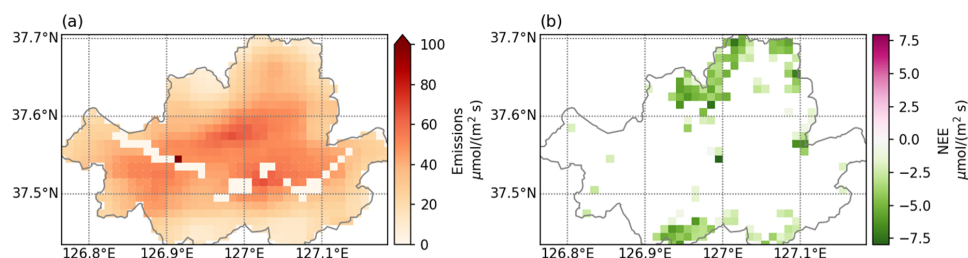
We used anthropogenic CO<sub>2</sub> emissions data from ODIAC version 2022 as prior emissions (Oda et al., 2018; Oda and Maksyutov, 2011). ODIAC provides global fossil fuel CO<sub>2</sub> emission estimates at a high spatial resolution of  $1 \times 1 \text{ km}^2$ , using power plant profiles and space-based nighttime light data (Oda et al., 2018). ODIAC is based on the CDIAC national emissions estimates, which categorize emissions by fuel type—liquid, gas, solid fuel, cement, gas flare, and international bunker. The ODIAC dataset has been widely used in various research areas, such as urban emission evaluation, monitoring network design experiments, and the inverse estimation of CO<sub>2</sub> emissions (Che et al., 2024; Crowell et al., 2019; Fasoli et al., 2018; Hedelius et al., 2018; Kunik et al., 2019; Lauvaux et al., 2016; Lian et al., 2023, 2022; Mallia et al., 2020; Ohyama et al., 2023; Sim et al., 2023; Wu et al., 2018; Ye et al., 2020).

ODIAC is based on downscaling bottom-up CO<sub>2</sub> emission estimates using spatial proxies. Global geolocation information and power plant magnitudes are sourced from the Carbon Monitoring and Action database. However, this database occasionally



misplaces point sources, necessitating manual correction (Kunik et al., 2019; Ohyama et al., 2023). For instance, the Korea Central Power Corporation in Seoul, located in the western part of the city, is inaccurately positioned in the ODIAC data. To correct this spatial discrepancy, we customized the ODIAC data, as shown in Fig. S3 of the supplementary material. We manually relocated the misaligned point source to match the power plant location. Additionally, for the grid cell with significantly high CO<sub>2</sub> emissions mistakenly identified as a point source, we replaced the emission value with the average of the surrounding eight grid cells.

Because the temporal resolution of ODIAC is monthly, it is necessary to refine the data to achieve hourly CO<sub>2</sub> emission estimates. We applied weekly and diurnal temporal scaling factors (Nassar et al., 2013) specific to Seoul to adjust the monthly ODIAC emission data, as shown in Fig. S4 in the supplementary material. The weekly scaling factors for Seoul remain consistent on weekdays, with values exceeding 1, but decrease over the weekends (Fig. S4a). The diurnal scaling factors exhibit typical daily emission patterns, increasing in the morning, peaking in the afternoon, and decreasing in the evening (Fig. S4b). Figure S4c shows the hourly CO<sub>2</sub> emissions time series after applying these temporal scaling factors. After spatial and temporal pre-processing, the daytime (1–7 UTC) emissions for December 2021 serve as the state vector for prior CO<sub>2</sub> emissions, denoted as ' $s_p$ ' (Fig. 4a).



**Figure 4: Averaged CO<sub>2</sub> fluxes of (a) prior emissions and (b) net biogenic ecosystem exchange over Seoul for daytime (10:00–16:00 KST) in December 2021.**

#### 2.4.2 Biogenic CO<sub>2</sub> fluxes

In the urban carbon cycle, atmospheric CO<sub>2</sub> is mainly influenced by emissions from fossil fuel combustion and vegetation carbon uptake. Given that Seoul has forests covering 25.3% of its total area (Korea Forest Service, 2021), the impact of biogenic CO<sub>2</sub> fluxes cannot be ignored. To account for the influence of biogenic CO<sub>2</sub> on the observed concentration, we incorporated biogenic CO<sub>2</sub> fluxes estimated by a data-based model known as CASS (Carbon Simulator from Space). CASS generates terrestrial carbon flux data from vegetation using information such as air temperature, relative humidity, photosynthetically active radiation, enhanced vegetation index, and land surface water index. CASS employs the random forest





method to determine optimal coefficients for each region and applies them to the estimation of carbon uptake. We utilized hourly net ecosystem exchange (NEE) data, which were resampled from a 250-meter resolution to 0.01°, as the biogenic CO<sub>2</sub> flux data within Seoul (Fig. 4b). CO<sub>2</sub> uptake can be observed in grids where Seoul's mountains and parks are located during the daytime. We obtained the vegetation-affected concentration by multiplying the footprints from the atmospheric transport model by the gridded biogenic CO<sub>2</sub> flux data using Eq. (S2) or (S4).

## 2.5 Prior error covariance

The prior error covariance matrix ( $\mathbf{Q}$ ) is derived from both the variance in prior emissions uncertainty ( $\sigma$ ) and the temporal and spatial covariances ( $\mathbf{D}$  and  $\mathbf{E}$ ). We construct the prior error covariance matrix as follows:

$$\mathbf{Q} = \mathbf{I}_\sigma (\mathbf{D} \otimes \mathbf{E}) \mathbf{I}_\sigma \quad (6)$$

Where  $\mathbf{I}_\sigma$  is a diagonal matrix whose elements represent the uncertainty of prior emissions. Instead of directly constructing the full  $\mathbf{Q}$  matrix, the temporal and spatial error covariance matrices are combined using a Kronecker product ( $\otimes$ ) to reduce computational costs, particularly when dealing with large emission state vectors (Yadav and Michalak, 2013).

In previous studies on urban inverse modelling, three methods for estimating prior emissions uncertainty were mainly identified. Most studies assumed a relative uncertainty for prior estimates, such as 30% uncertainty for each emission source in Central California (Zhao et al., 2009), 15% for large point sources and 85% for the rest in Tokyo (Ohyama et al., 2023), 20% for Los Angeles and 40% for Riyadh and Cairo (Ye et al., 2020), 20% (Lian et al., 2022), and 60% (Nalini et al., 2022) for Paris. Kunik et al. (2019) and Mallia et al. (2020) defined the uncertainty of prior emissions as the difference between the prior and true emission estimates (e.g., Hestia). Another approach to estimating prior emissions uncertainty is inter-comparison with different inventories (Sargent et al., 2018; Wu et al., 2018). In this study, we assumed a relative uncertainty of 15% for large point sources and 100% for the rest of Seoul, similar to the approach used for Tokyo in Ohyama et al. (2023). For grids with prior emissions of 0  $\mu\text{mol m}^{-2} \text{s}^{-1}$ , such as rivers, a minimum uncertainty value of 1  $\mu\text{mol m}^{-2} \text{s}^{-1}$  was assigned, following the method of Kunik et al. (2019).

The temporal and spatial covariance matrices are defined using exponential decay equations:

$$\mathbf{D} = \exp\left(-\frac{\mathbf{X}_t}{l_t}\right) \quad (7)$$

$$\mathbf{E} = \exp\left(-\frac{\mathbf{X}_s}{l_s}\right) \quad (8)$$

The temporal covariance is computed based on lag-times ( $\mathbf{X}_t$ ) between time steps, divided by temporal correlation range parameters ( $l_t$ ), where  $l_t$  represents the time at which errors in the prior emissions are considered uncorrelated. The spatial covariance is calculated using separation distances ( $\mathbf{X}_s$ ) between grid cells, divided by spatial correlation range parameters ( $l_s$ ), where  $l_s$  indicates the distance at which errors in the prior emissions are considered uncorrelated. Previous studies have shown that suitable spatiotemporal correlation parameters vary by city. For example, in Salt Lake City, the temporal and spatial correlations were determined to be 2 d and 6 km, respectively (Kunik et al., 2019), whereas in Tokyo, the parameters were 0



d and 10 km (Ohyama et al., 2023). We performed a lagged autocorrelation function and variogram analysis to determine the  
270 optimal temporal and spatial correlation lengths for Seoul, respectively (Fig. S5). Based on the results, the optimal temporal  
and spatial correlation range parameters for the inversion over Seoul were 9 h and 10 km, respectively.

## 2.6 Observational error covariance

We estimated the observational error covariance ( $\mathbf{R}$ ) using the departure-based diagnostics, commonly known as the  
275 Hollingsworth/Lönnberg method (Hollingsworth and Lönnberg, 1986; Lönnberg and Hollingsworth, 1986; Rutherford, 1972).  
The departure (or innovation) is defined as  $\mathbf{z} - \mathbf{H}\mathbf{s}_p$ , representing the difference between the observed  $\Delta\text{CO}_2$  and the values  
simulated by WRF-(X)STILT with prior emissions, following Eqs. (S2) and (S4). Because the standard deviation of departures  
reflects the combined effects of observation and prior emissions errors, we separate their contributions based on certain  
assumptions. The Hollingsworth/Lönnberg method assumes that prior emissions errors exhibit spatial correlation, whereas  
280 observation errors are spatially uncorrelated (Bormann et al., 2009). Additionally, prior emissions and observation errors are  
considered independent. Here, observation error includes uncertainties arising from the instrument, transport model,  
representation, background inflow (boundary conditions), and biogenic fluxes.

To estimate observation errors, we first compute the covariance of departure pairs as a function of separation distance. A  
function is then fitted to the covariance values at various distances, excluding the value at zero separation, and extrapolated to  
285 estimate the covariance at zero distance. At zero separation, the total variance is decomposed into a spatially correlated  
component (representing prior emissions error) and an uncorrelated component (representing observation error). Based on  
these assumptions, the value of the fit gives the prior emissions error in observation space at zero separation, and the  
observation error is determined by subtracting this value from the total covariance at zero distance.

In this study, we applied the Hollingsworth/Lönnberg method to estimate the observational error covariance for both ground-  
290 based and satellite observations. We first divided the observation vector into subsets:  $\text{NST}_H$ ,  $\text{NST}_L$ , OLP, SNU, YSB, OCO-2,  
and OCO-3, assuming that error statistics within each subset are homogeneous. Because this method was originally developed  
for satellite data, which has wide spatial coverage but infrequent revisit cycles, we applied it directly for satellite observations.  
We assumed satellite observation errors are spatially uncorrelated and fitted a function (Limited-memory Broyden-Fletcher-  
Goldfarb-Shanno with Box constraints in R language) to the covariance as a function of separation distance. For ground-based  
295 observations, which provide data over a long period, we assumed that observation errors are temporally uncorrelated. Instead  
of using spatial distance, we fitted a function to the covariance as a function of time steps. The inferred observation error for  
each dataset was obtained by subtracting the value of the fit at zero separation (distance or time step) from the total covariance.  
The fitting results for each observation type are shown in Fig. S6. The inferred observation error was multiplied by the square  
of the standard deviation of departures, and the square of the mean departure was added to correct for bias. Finally, the  
300 estimated observation error for each observation was placed on the diagonal of the  $\mathbf{R}$  matrix.



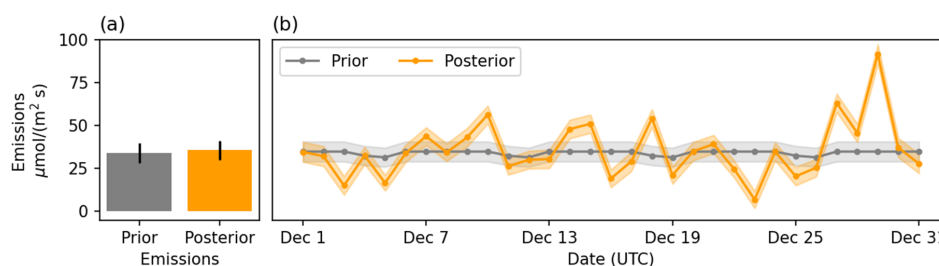


### 3 Results and discussion

In Sect. 3.1, we compare CO<sub>2</sub> emissions from prior and posterior estimates to investigate the spatiotemporal differences following the inversion run. In Sect. 3.2, we assess CO<sub>2</sub> enhancement between observations and simulations using prior and posterior emissions to evaluate the effectiveness of the inversion. Further exploration of sensitivity tests for observations using all data, only ground-based, only OCO-2, and only OCO-3 data, along with uncertainty reduction to estimate constraint effects, is presented in Sect. 3.3. A comprehensive discussion accompanies each set of results.

#### 3.1 Comparison between prior and posterior emissions

We obtained posterior CO<sub>2</sub> emissions over Seoul for December 2021 using Bayesian inverse modelling, incorporating ground-based and satellite observations. Figure 5a compares the average CO<sub>2</sub> emissions between the prior and posterior estimates. The mean daytime prior and posterior emissions were 34.12 and 35.63  $\mu\text{mol m}^{-2} \text{s}^{-1}$ , respectively. The average correction from prior to posterior emissions was approximately +4.43%, suggesting a slight increase in posterior emissions, and the prior emissions were slightly underestimated. However, the difference between the domain- and time-averaged prior and posterior emissions was not statistically significant. Similar findings have been reported in previous studies conducted in Tokyo (Ohyama et al., 2023). The reduced chi-squared value for the posterior emissions was 1.38. Although this is slightly higher than the ideal value of 1.0, it still indicates a reasonable representation of prior emissions error and observation error covariance assumptions. Further reducing this value closer to 1 would require assuming larger error metrics.



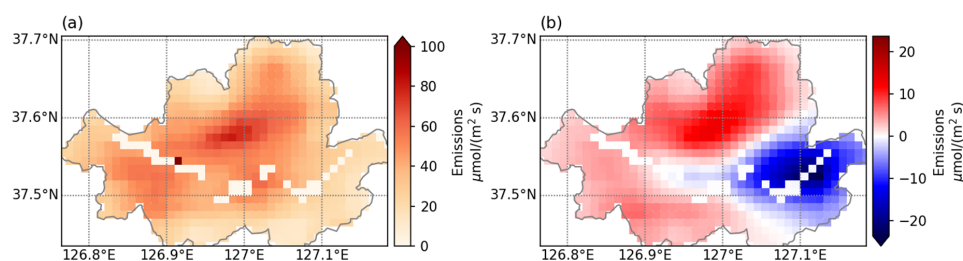
**Figure 5: (a) Comparison of time- and domain-averaged emissions between prior and posterior estimates for December 2021 in Seoul, and (b) time series of domain-averaged daily (daytime average) prior and posterior CO<sub>2</sub> emissions, including emission uncertainties.**

The daily time series of temporally resolved prior and posterior emissions averaged over the Seoul domain is shown in Fig. 5b. For prior emissions, the monthly ODIAC data was pre-processed using temporal scaling factors, resulting in higher emissions on weekdays and lower emissions on weekends. In contrast, posterior emissions exhibit greater temporal variability,



reflecting a more realistic pattern. Until December 22, posterior emissions fluctuated relative to prior emissions, but they showed a significant decrease on December 23, followed by a notable increase from December 27 to 29.

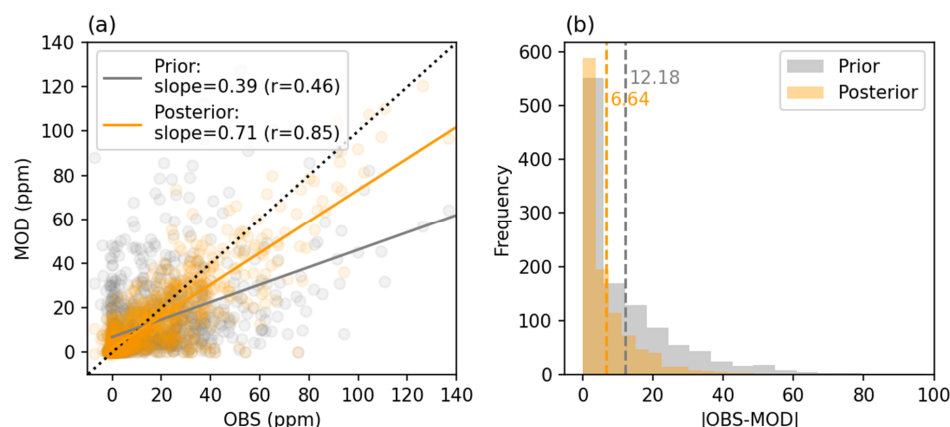
- 330 Figure 6 shows the spatial distribution of posterior CO<sub>2</sub> emissions and emission corrections from the inversion using all observation data over Seoul. Compared to the spatial patterns of prior CO<sub>2</sub> emissions in Fig. 4a, the posterior emissions in Fig. 6a exhibit a similar distribution, with higher emissions concentrated in central Seoul and lower emissions near the city's boundaries. However, the posterior correction map, obtained by subtracting prior emissions from posterior emissions, reveals spatial variations in emission adjustments ranging from  $-23.59$  to  $13.61 \mu\text{mol m}^{-2} \text{s}^{-1}$  (Fig. 6b). Most areas in Seoul experienced
- 335 either increased or decreased emissions through Bayesian inverse modelling. Notably, emissions in the eastern part of Seoul were strongly corrected in the negative direction, whereas most other regions underwent positive corrections. This suggests that prior emissions were overestimated in the eastern part of Seoul and underestimated in the other areas.



- 340 **Figure 6: Averaged CO<sub>2</sub> fluxes over Seoul for daytime over December 2021. (a) Posterior emissions and (b) emission corrections (posterior minus prior) after the inversion run that used five ground sites, OCO-2, and OCO-3 data.**

### 3.2 Comparison of CO<sub>2</sub> enhancement between observation and simulation

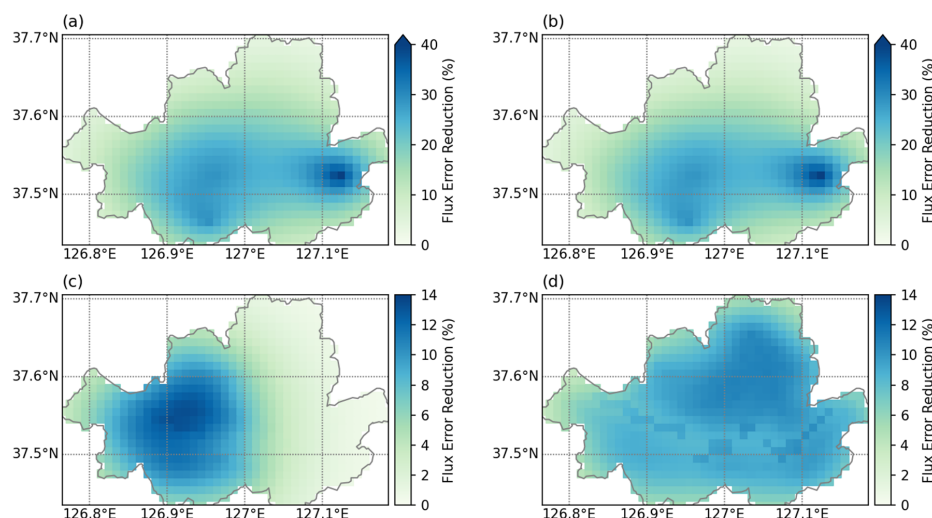
- A comparison between observed CO<sub>2</sub> enhancements (OBS) and simulated CO<sub>2</sub> enhancements (MOD) was conducted to
- 345 evaluate the performance of the inversion framework and assess how well atmospheric CO<sub>2</sub> data constrained emissions over Seoul. Figure 7 shows the changes in the relationship between OBS and MOD from prior to posterior emissions. MOD, based on prior emissions, was significantly lower than OBS, with a slope of 0.39 in Fig. 7a. However, after the inversion, the discrepancies were reduced, and MOD became closer to OBS, with the slope increasing to 0.71. Additionally, the correlation coefficient between OBS and MOD improved from 0.46 to 0.85, indicating a better agreement after the inversion. The mean
- 350 absolute error between OBS and MOD also decreased significantly, from 12.18 to 6.64 ppm, when using posterior emissions data, shown in Fig. 7b. These results indicate that the inversion framework effectively constrained CO<sub>2</sub> emissions over Seoul by incorporating information from observational data.



355 **Figure 7: Comparison of observed CO<sub>2</sub> enhancements (OBS) and simulated CO<sub>2</sub> enhancements (MOD) using prior (gray) and posterior (orange) emissions during daytime over December 2021. (a) Scatter plots of OBS vs. MOD, with the slope and correlation coefficient (r). (b) Frequency distributions of absolute differences between OBS and MOD (|OBS-MOD|). The dashed lines in (b) indicate the mean absolute error between OBS and MOD.**

### 360 3.3 Sensitivity test for observations used

We evaluated the performance of the inverse model through a sensitivity analysis considering different observational network configurations (Fig. 8). The cases included 1) using all observation data, 2) using only five ground sites, 3) using only OCO-2 data, and 4) using only OCO-3 data. The most substantial reductions in uncertainty were observed when all available observations were used, with an average reduction exceeding 19.2% (Fig. 8a). In this case, the spatial distribution of uncertainty reduction was similar to that obtained using only ground sites (Fig. 8b), as ground-based observations had a greater influence on the constraint than satellite data because of their continuous temporal coverage throughout the entire month. When using five ground sites, the uncertainty reduction in posterior emissions was 18.7%. The largest reductions occurred where ground observation sites were concentrated, particularly around OLP (eastern region), SNU (southern region), and surrounding NST<sub>H</sub>, NST<sub>L</sub>, and YSB. The reduction in uncertainty extended beyond the observation sites, covering the broader footprint influence range in Fig. 3a. Notably, a decrease was observed northwest of the observation sites, the upwind region. However, the impact on uncertainty reduction was minimal in western and northern Seoul, where no ground-based observation sites were present.



**Figure 8: Daytime percent uncertainty reduction in posterior emissions over Seoul for the inverse analysis using different observation datasets: (a) all observation data from December 2021, (b) only five ground sites from December 2021, (b) only OCO-2 data from December 3–5, 2021, and (c) only OCO-3 data from December 3–5, 2021, when the satellite passed over Seoul. Note that the percent reduction ranges in panels (a), (b), (c), and (d) vary for visualization purposes.**

Because OCO-2 and OCO-3 passed over Seoul on December 4 and 5, 2021, respectively, the uncertainty reduction results for satellite data are focused on December 3–5, highlighting the effect of satellite observations. The OCO-2 data significantly reduced the uncertainty of posterior emissions over western Seoul, with an average reduction of 6% (Fig. 8c). This can be attributed to the satellite's north-to-south overpass, covering the western footprint, an upwind region in Fig. 3b. OCO-2 contributed to uncertainty reduction in the western parts of Seoul, areas not covered by ground-based observations. Most of Seoul experienced uncertainty reduction due to OCO-3, which had 167 soundings across the city (Figure 8d). The domain-averaged uncertainty reduction from December 3–5 was 8.4%. OCO-3 contributed to uncertainty reduction in the northern region of Seoul, which was not covered by ground-based or OCO-2 observations. The extensive coverage of satellite observations enabled further corrections in areas lacking ground observations, demonstrating the added value of satellite constraints in reducing uncertainty.



#### 390 4 Summary and conclusions

This study developed a Bayesian inverse modelling framework (version 1) to optimize CO<sub>2</sub> emissions using both ground- and space-based observations and applied it to Seoul. By incorporating high-resolution (0.01° spatial, 1 h temporal) anthropogenic and biogenic CO<sub>2</sub> fluxes, atmospheric CO<sub>2</sub> measurements, a Lagrangian transport model, and uncertainty quantification, we improved the accuracy of emission estimates. Ground-based (NST<sub>H</sub>, NST<sub>L</sub>, OLP, SNU, YSB) and satellite (OCO-2, OCO-3) observations from December 2021 were used to constrain emissions, with WRF-(X)STILT footprints linking emissions to observed CO<sub>2</sub> enhancements.

Although the averaged CO<sub>2</sub> emissions difference between prior and posterior estimates was relatively small (4.43% increase), the inversion revealed significant spatiotemporal variations. Posterior emissions exhibited greater variability, highlighting underestimation in most areas and overestimation in eastern Seoul. This information enables us to track when and where CO<sub>2</sub> emissions fluctuate and assess the impact of carbon reduction policies over time and space. Comparing observed and simulated CO<sub>2</sub> enhancements confirmed the effectiveness of the inversion, reducing the mean absolute error by nearly half. Sensitivity tests showed that ground- and space-based data achieved the greatest uncertainty reduction (19.2%), with OCO-2 and OCO-3 providing critical constraints in areas lacking ground-based observations. These results emphasize the complementary role of satellite data, particularly OCO-3's snapshot capability, in enhancing urban CO<sub>2</sub> monitoring.

Despite these improvements, some limitations remain, which future work will address. First, the inversion results depend on the accuracy of the transport model, introducing uncertainties in simulating atmospheric transport. Future improvements to WRF-(X)STILT will incorporate terrain elevation data that more closely represent real-world topography and implement observation nudging to enhance transport accuracy. Second, the analysis was limited to a 1-month, which may not fully capture seasonal emission variations. Extending the analysis to a full year will enable comparisons with Korea's national greenhouse gas inventory. Third, although the reduced chi-square value has been evaluated, additional validation using independent datasets such as radiocarbon ( $\Delta^{14}\text{C}$ ) and flux tower measurements will be conducted. Finally, expanding the observational network will allow this approach to be applied to other cities and eventually to all of Korea, enabling a more comprehensive assessment of spatiotemporal CO<sub>2</sub> distribution, identifying regional emission hotspots, and improving the accuracy of national-scale carbon budget estimates to support mitigation policies.

By integrating high-resolution inverse modelling with multiple observational sources, this study provides a robust framework for quantifying urban CO<sub>2</sub> emissions. The findings refine emission estimates by reducing uncertainties and support data-driven policymaking for effective carbon mitigation strategies. Importantly, the proposed framework is designed to be transferable and applicable to other cities, contributing to broader efforts in long-term climate change mitigation.



#### 420 **Data Availability**

The prior emissions data from ODIAC were obtained from the Center for Global Environmental Research (<https://db.cger.nies.go.jp/dataset/ODIAC>). Biogenic CO<sub>2</sub> fluxes data from the CASS were downloaded from the Korea Carbon Project website (<https://korea-carbon-project.org/map>). The WRF model is freely distributed to the scientific community by the National Center for Atmospheric Research (NCAR) and can be accessed at [https://www2.mmm.ucar.edu/wrf/users/download/get\\_source.html](https://www2.mmm.ucar.edu/wrf/users/download/get_source.html). The STILT and X-STILT models available for installation at <https://uataq.github.io/stilt/#/> and <https://github.com/uataq/X-STILT>, respectively. OCO-2 and OCO-3 satellite data are publicly available from <https://ocov2.jpl.nasa.gov/science/oco-2-data-center/> and <https://ocov3.jpl.nasa.gov/science/oco-3-data-center/>, respectively.

#### **Competing interests**

430 The authors declare that they have no conflict of interest.

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