



1 Quantifying Temperature-sliding Inconsistency in Thermomechanical Coupling: A  
2 Comparative Analysis of Geothermal Heat Flux Datasets at Totten Glacier

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16 **Abstract.** Rapid sliding of ice sheets requires warm basal temperatures and lubricating  
17 basal meltwater, whereas slow velocities typically correlate with a frozen bed. However,  
18 ice sheet models often infer basal sliding by inverting surface velocity observations  
19 with the vertical structure of temperature and hence rheology held constant. If the  
20 inversion is allowed to freely vary sliding over the model domain, then inconsistencies  
21 between the basal thermal state and ice motion can arise lowering simulation realism.  
22 In this study, we propose a new method that quantifies inconsistencies when inferring  
23 warm and cold-bedded regions of ice sheets. This method can be used to evaluate the  
24 quality of ice sheet simulation results without requiring any englacial or subglacial  
25 measurements. We apply the method to evaluate simulation results for Totten Glacier  
26 using an isotropic 3D full-Stokes ice sheet model with eight geothermal heat flux (GHF)  
27 datasets and compare our evaluation results with inferences on basal thermal state from  
28 radar specularity. The rankings of GHF datasets based on inconsistency are closely  
29 aligned with those using the independent specularity content data. Examples of the  
30 method utility are 1. an inconsistency characterizing overcooling with all GHFs near  
31 the western boundary of Totten Glacier between 70°S-72°S, where there is a bedrock  
32 canyon and fast surface ice velocities, which suggests that GHF is low in all published  
33 datasets; 2. an overheating inconsistency in the eastern Totten Glacier with all GHFs  
34 that leads to overestimation of ice temperature due, in this case, to an unrealistically  
35 warm surface temperature. Our approach opens a new avenue for assessing the self-  
36 consistency and reliability of ice sheet model results and GHF datasets, which may be  
37 widely applicable.



## 38 **1. Introduction**

39 Ice sheet models are an important tool for projections of ice sheet mass balance  
40 and their contribution to sea level rise. Ice sheet models are usually initialized by “spin-  
41 up” or data assimilation such that they reproduce the present-day geometry or surface  
42 velocity of an ice sheet (Seroussi et al., 2019). Often ice sheet model simulations derive  
43 ice dynamics using ice temperatures taken from other studies (e.g., Gillet-Chaulet et al.,  
44 2012; Van Liefferinge and Pattyn, 2013; Cornford et al., 2015; Pittard et al., 2016;  
45 Siahaan et al., 2022). In thermo-mechanically coupled ice sheet simulations, the ice  
46 sheet model is usually spun up with idealized temperature-depth profiles and then run  
47 in a thermo-mechanically coupled mode constrained by geothermal heat flux (GHF)  
48 and surface ice temperature fields (Seroussi et al., 2019). While advances in satellite  
49 and field observation technologies have led to a preliminary consensus on ice sheet  
50 geometry and surface ice temperature, significant uncertainties persist in basal  
51 boundary conditions, including GHF and basal friction, since reliable observational  
52 data are scarce. These basal properties introduce significant uncertainty in the simulated  
53 ice sheet dynamics, and thus ice sheet mass balance.

54 The GHF, the heat flow from the Earth's crust to the base of ice sheet, is a critical  
55 variable in the basal boundary condition for simulating the ice temperature profile, and  
56 hence ice rheology and flow dynamics (Fisher et al., 2015; Smith - Johnsen et al., 2020;  
57 Reading et al., 2022). Several GHF datasets exist, derived in various ways from  
58 geophysical observations and models, and they exhibit significant variability in both  
59 spatial distribution and magnitude (e.g., An et al., 2015; Dziadek et al., 2017; Martos et  
60 al., 2017; Shen et al., 2020; Stål et al., 2021). These GHF datasets have been widely  
61 used in thermodynamic simulations of Antarctica (e.g., McCormack et al., 2022;  
62 Shackleton et al., 2023; Park et al., 2024; Van Liefferinge et al., 2018). However,  
63 assessing the GHF field accuracy is problematic because in situ measurements such as  
64 boreholes are sparse. Few studies have assessed the quality and reliability of GHF  
65 datasets over specific regions. Kang et al. (2022) employed a combination of forward  
66 model and inversion using a 3D full-Stokes ice flow model to simulate the basal thermal  
67 state in the Lambert–Amery Glacier region and evaluate different GHFs using the  
68 locations of subglacial lakes, but the constraints used were asymmetric between cold  
69 and warm beds, and assigned inflated reliability to the warmer GHF maps. Indirect  
70 estimates of basal conditions have used airborne radar specular content (Schroeder  
71 et al., 2013, 2015; Young et al., 2016) as proxies for basal wetness/dryness and thermal  
72 regime (Dow et al., 2020). Huang et al. (2024) used an inverse modeling approach  
73 similar to that of Kang et al. (2022) for Totten Glacier and combined this with measured  
74 radar specular content to derive a two-sided constraint on the basal thermal state in  
75 addition to subglacial lakes locations. However, specular content is not yet available  
76 for many regions of Antarctica.



77           The basal friction field is another poorly known boundary condition in ice sheet  
78 modeling, and a key source of uncertainty in the long-term projection of ice sheets and  
79 glaciers. Although basal slip is crucial to the 3D ice flow, it is difficult to observe.  
80 Several basal sliding parameterizations have been proposed and widely used  
81 (Weertman, 1957; Kamb, 1970; Nye, 1970; Budd et al., 1979; Fowler, 1981; Schoof,  
82 2005; Gagliardini et al., 2007; Gladstone et al., 2014; Tsai et al., 2015; Brondex et al.,  
83 2017, 2019). The linear Weertman basal sliding parameterization is the most widely  
84 used due to its simple form. Given prescribed or modelled ice temperatures and hence  
85 ice viscosity, numerous studies have inferred the spatial distribution of basal friction  
86 coefficient over grounded ice to best match observed present-day surface ice velocities  
87 or ice sheet geometry using snapshot or time-dependent data assimilation and inverse  
88 methods (MacAyeal, 1993; Morlighem et al., 2010; Rignot et al., 2011; Gillet-Chaulet  
89 et al., 2012; Larour et al., 2012; Pollard and DeConto, 2012; Morlighem et al., 2013;  
90 Perego et al., 2014; Pattyn, 2017; Albrecht et al., 2020; Lipscomb et al., 2021; Choi et  
91 al., 2023). However, such inversions typically allow the friction coefficient to vary  
92 freely to match the surface velocity observations. This can potentially lead to conflicts  
93 with the temperature field used during the inversion, which we refer to as  
94 “inconsistencies” in this study. For instance, relatively fast surface ice velocity may  
95 demand basal sliding in areas where the basal temperatures are below the local pressure  
96 melting point. These inconsistencies may be due to unrealistic ice temperatures or a  
97 lack of complete physics in the ice sheet model. However, many studies overlook this  
98 aspect, and use the inversion results to initialize ice sheet dynamics simulations and  
99 estimate glacier mass balance and its contribution to sea level rise (Seroussi et al., 2019;  
100 Peyaud et al., 2020; Schannwell et al., 2020; Payne et al., 2021).

101           To the best of our knowledge, there has been no study of such inconsistencies  
102 between simulated ice temperature and observed surface ice velocity. Here we develop  
103 a novel and generally applicable method to estimate this inconsistency without relying  
104 on basal observation data. We utilize the inconsistency of the modelled ice temperature  
105 and observed velocity fields to evaluate the quality of ice flow model results. Notably,  
106 this approach can also serve as a supplementary method for assessing geothermal heat  
107 flux datasets, relying solely on surface ice velocity observations rather than additional  
108 englacial or subglacial data.

109           We apply our method to Totten Glacier, a primary outlet of the Aurora subglacial  
110 basin in East Antarctica (Greenbaum et al., 2015; Pritchard et al., 2009). The Totten  
111 Glacier subregion experienced the largest mass loss among drainage basins in East  
112 Antarctica during the period 1979-2017 and 2003-2020 (Kim et al., 2024; Rignot et al.,  
113 2019) (Fig. 1a). We examine inconsistencies between simulated ice temperature and ice  
114 velocity fields using a 3D full-Stokes model using the various GHFs included in Huang  
115 et al. (2024) and use this analysis to rank the reliability of different GHF fields. This



116 GHF ranking closely resembles that reported by Huang et al. (2024), which used the  
117 agreement between the modelled basal thermal regime and specularity content, which  
118 we take as a validation of the method. Since the new method does not require any  
119 englacial or subglacial data, it can be applied to many glaciers, particularly those  
120 lacking observations. Our approach can provide a swift assessment of the plausibility  
121 of basal temperature and velocity simulated by ice sheet models. Additionally, it can be  
122 effectively utilized to map the spatial distribution of GHF over- or under-estimation.

123

## 124 2. Method

125 The inconsistencies defined in this study are essentially between the modelled  
126 basal thermal state and observed surface ice flow motion. More specifically, the  
127 inconsistencies are between modelled frozen bed and modelled basal sliding (which is  
128 tuned to match the observed fast surface velocity during the inversion), and between  
129 modelled warm bed and observed slow surface velocity. The inconsistencies originate  
130 from multiple causes, including uncertainties in GHF, surface ice temperature, ice sheet  
131 geometry, bed topography, surface velocity, ice density and incomplete ice flow  
132 mechanics.

133 There is no direct correlation between basal temperature and surface velocity;  
134 rather, they are linked through the basal thermal state - the basal temperature being at  
135 or below the pressure melting point. The ice bottom in the study domain can be  
136 partitioned into warm and cold beds depending on whether the simulated basal ice  
137 temperature reaches the local pressure melting point. To effectively penalize models  
138 exhibiting both localized overheating (bed too warm) and overcooling (bed too cold),  
139 we establish overheating metrics within the warm-bedded region and overcooling  
140 metrics within the cold-bedded region to quantitatively assess the inconsistency  
141 between the simulated temperature and velocity fields. Thus, we provide two-sided  
142 constraints on the temperature field that penalize both too high and too low ice  
143 temperature.

144 Overcooling occurs where basal temperature is underestimated. Crucially, in  
145 regions with relatively fast observed surface velocity, the inverse method nevertheless  
146 yields a nonzero basal velocity — a physically inconsistent result given the cold basal  
147 temperature. When basal ice temperature is below the pressure melting point, the basal  
148 modelled velocity is expected to approach zero. This inconsistency is larger for faster  
149 simulated basal ice speed and for colder simulated basal temperatures. We therefore use  
150 a formula that accounts for both variables to quantify overcooling:

$$151 \quad AOC = (T_{melt} - T_{bm}) \times U_{bm}, \quad (1)$$

152 where  $AOC$  stands for absolute overcooling,  $T_{melt}$  is the basal pressure melting point,  
153  $T_{bm}$  represents the simulated basal ice temperature and  $U_{bm}$  means the simulated basal  
154 ice speed.



155 For the overheating metric, since the first term of the right-hand side of Eq. (1)  
156 becomes zero at a warm bed, we cannot use a similar formula as Eq. (1). It is not  
157 straightforward to quantify the inconsistencies between modelled warm bed and  
158 expected slow basal speed given slow observed surface speed. We note the fact that  
159 modelled basal sliding speed must remain non-negative. If the ice is warm and soft  
160 enough to permit deformation such that the modelled surface speed is much faster than  
161 the observed, then a friction inversion will be ineffective to correct this misfit,  
162 producing a bias towards positive misfits (i.e., model velocities are too fast) in the  
163 inversion results. Therefore, we use the positive difference between the simulated  
164 surface ice speed and the observed speed to calculate the inconsistency caused by the  
165 overheating effect:

$$166 \quad AOH = \max(0, U_{sm} - U_{obs}), \quad (2)$$

167 where  $AOH$  refers to absolute overheating,  $U_{sm}$  represents the modelled surface ice  
168 speed and  $U_{obs}$  is the observed surface ice speed. We only calculated  $AOH$  for the warm-  
169 bedded areas, i.e.  $T_{bm} = T_{melt}$ , because observed surface ice speed errors are  
170 proportionally much less in warm-bedded areas (corresponding to fast flow regions)  
171 than in cold-bedded area (correspond to slow flow regions).

172 To mitigate the impact of substantial differences in observed surface ice speed  
173 across various areas, we also define "relative overheating" ( $ROH$ ) and "relative  
174 overcooling" ( $ROC$ ), dividing  $AOH$  and  $AOC$  by the observed surface ice speed  
175 respectively:

$$176 \quad ROH = \frac{\max(0, U_{sm} - U_{obs})}{U_{obs}}, \quad (3)$$

$$177 \quad ROC = (T_{melt} - T_{bm}) \times \frac{U_{bm}}{U_{obs}}. \quad (4)$$

178 The summation of the above four metric values is computed across grid points  
179 where each metric is explicitly defined. Specifically,  $AOH$  and  $ROH$  metrics are  
180 computed over the warm bed region, and  $AOC$  and  $ROC$  metrics are computed over the  
181 cold bed region for each simulation result. This summation approach was chosen to  
182 preserve the total magnitude of inconsistencies, as the warm bed and cold bed regions  
183 are different due to distinct GHF boundary conditions. Furthermore, since all  
184 experiments utilize identical mesh, the cumulative values remain directly comparable  
185 for cross-experiment analysis. We only consider grounded ice and exclude points  
186 located at the domain boundary due to relatively poor model performance there.

187 To evaluate the inconsistencies for the whole domain, we linearly normalized the  
188 overheating inconsistency and overcooling inconsistency to range from 0 to 1 and then  
189 sum them as:

$$190 \quad ACI = L_N(AOC) + L_N(AOH), \quad (5)$$

$$191 \quad RCI = L_N(ROC) + L_N(ROH), \quad (6)$$



192 where  $ACI$  means absolute combined inconsistency,  $RCI$  represents relative combined  
 193 inconsistency, and  $L_N$  represents linear normalization. Taking  $AOC$  as an example, its  
 194 linear normalization is:

$$195 \quad L_N(AOC) = \frac{AOC - AOC_{min}}{AOC_{max} - AOC_{min}}. \quad (7)$$

196 where  $AOC_{min}$  and  $AOC_{max}$  denote the minimal and maximal  $AOC$  values across all the  
 197 simulation results when multiple simulation outcomes are available. Therefore, we  
 198 obtain 6 metrics consisting of three absolute inconsistencies ( $AOH$ ,  $AOC$ ,  $ACI$ ) and  
 199 three relative inconsistencies ( $ROH$ ,  $ROC$ ,  $RCI$ ).

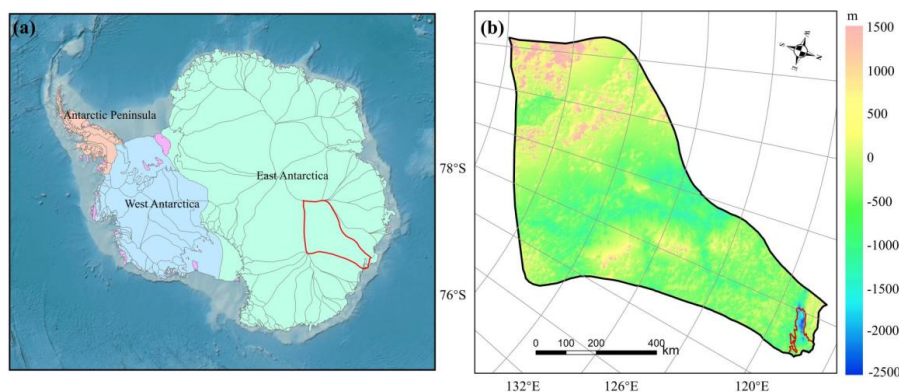
200 These 6 indicators can comprehensively analyze the temperature-sliding  
 201 inconsistency in the inversion results of ice sheet model. For each metric, simulation  
 202 results are assigned ranks ranging from 1 to  $N$  (where  $N$  represents the total number of  
 203 simulation results), with 1 indicating the smallest inconsistency and  $N$  the largest. The  
 204 final score for each simulation result is subsequently calculated as the arithmetic mean  
 205 of its six metric-derived scores, ensuring a comprehensive evaluation framework. as a  
 206 reasonable simulation result should perform well across warm bed, cold bed, and the  
 207 whole region.

208

### 209 3. Application to Totten Glacier with Different GHFs

#### 210 3.1 Study domain and Data

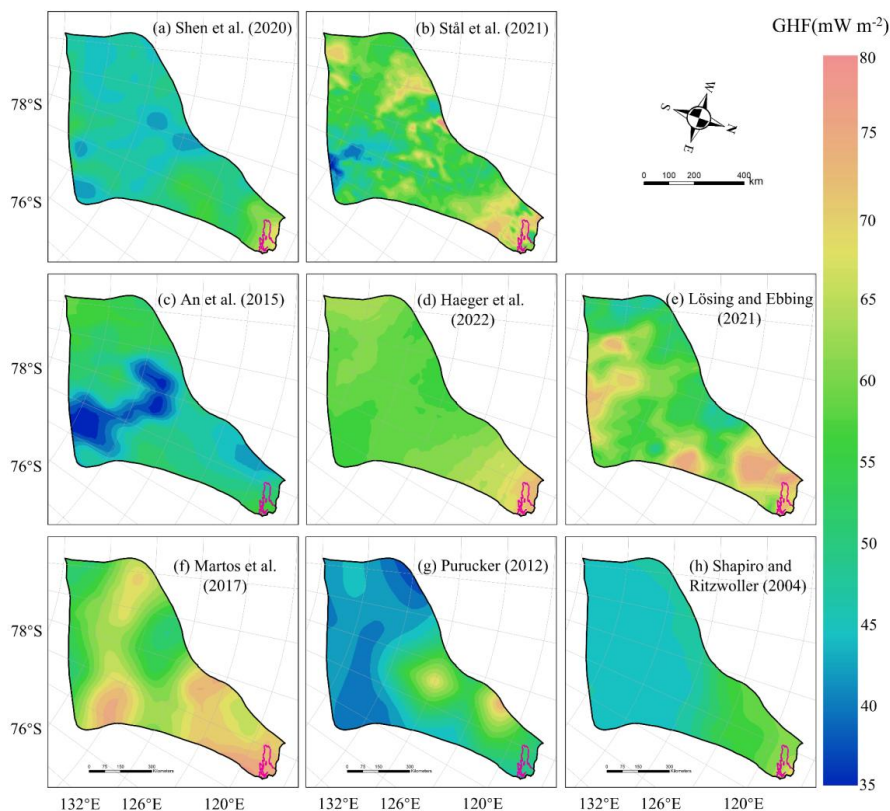
211 We apply our method to evaluate simulated ice temperature and ice velocity in  
 212 Totten Glacier by following Huang et al. (2024) and using eight GHF datasets. Huang  
 213 et al. (2024) used the present-day surface ice temperature (Le Brocq et al., 2010) and  
 214 ice sheet topography data from BedMachine Antarctica, version 2 (Morlighem et al.,  
 215 2020). The eight GHF datasets were derived by various methodologies, resulting in  
 216 significant differences in both spatial distribution and magnitude (Fig. 2). GHF fields  
 217 from Stål et al. (2021), Haeger et al. (2022), Lösing and Ebbing (2021) and Martos et  
 218 al. (2017) generally exhibit higher magnitudes than the other GHFs.



219



220 **Figure 1.** (a) Geographic location of Totten Glacier (red outline) in Antarctica; (b) bed  
 221 elevation of Totten Glacier, the red curve represents the grounding line.  
 222



223  
 224 **Figure 2.** The spatial distribution of the 8 GHF datasets for Totten Glacier (a–h) used  
 225 as input data in Huang et al. (2024). The purple line depicts the grounding line.  
 226

227 The spatial distribution of modelled basal temperature using the 8 GHFs displays  
 228 both similarities and heterogeneity. In the northern part of Totten Glacier, there is a  
 229 consistent warm-bedded pattern across all eight simulation results (Fig. S1), which  
 230 originates from the grounding line and extends upstream to approximately 71°S. This  
 231 warm-bedded area is not contiguous with the lateral boundaries of Totten Glacier but is  
 232 instead bordered by cold bed. All 8 GHF datasets produce low basal ice temperatures  
 233 in the inland southwest, with Purucker et al. (2012), Shapiro and Ritzwoller (2004),  
 234 Shen et al. (2020) and Lösing and Ebbing (2021) being colder. The basal ice velocities



235 modelled from the 8 different GHF datasets produce similar spatial distributions (Fig.  
236 S2), which can be expected as they were derived using the same inverse method and  
237 constrained by the identical observed surface ice velocity. The modelled basal ice  
238 velocity is fast near the grounding line and its upstream area. There are also high  
239 velocities between 70°S and 72°S close to the western boundary of Totten Glacier,  
240 which are associated with subglacial canyon features in the basal topography (Fig. 1b)  
241 and observed fast surface ice velocity there.

242

### 243 **3.2 Spatial Distribution of Inconsistencies**

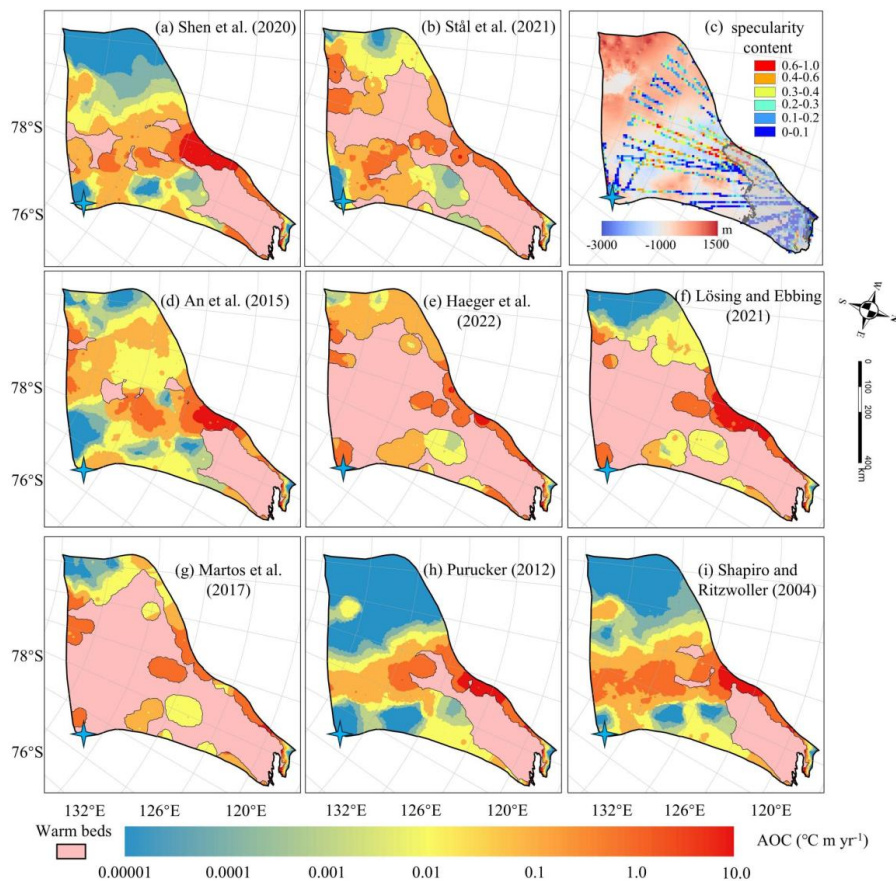
244 We calculate the absolute inconsistencies, *AOH*, in the warm bed, and *AOC* in the  
245 cold bed. The spatial distribution of *AOC* reveals that most GHF datasets exhibit  
246 significant local overcooling inconsistencies at the subglacial canyon between 70°S and  
247 72°S (Fig. 3). There is fast basal sliding in the inverse model results (Fig. S2), however,  
248 the modelled basal ice temperatures inferred from most of the GHF datasets are below  
249 the pressure melting point (Fig. S1). High specular content in radar data (Fig. 3c)  
250 suggests the presence of basal water in the subglacial canyons here (Dow et al., 2020;  
251 Huang et al., 2024), which also suggests that the basal ice temperature should be at the  
252 pressure melting point and confirms the inconsistency between the modelled  
253 temperature and velocity fields.

254 The area near the grounding line is characterized by fast ice flow and warm bed  
255 (Fig. 3), yet some of the margin is cold-bedded with modelled basal temperature below  
256 the pressure melting point, resulting in high *AOC*. Overall, modelled results with most  
257 GHF datasets show small overcooling inconsistencies. The modelled results using GHF  
258 from Purucker et al. (2012), Shapiro and Ritzwoller (2004), Shen et al. (2020), Lösing  
259 and Ebbing (2021) exhibit no overcooling inconsistency in southwestern Totten Glacier  
260 (Fig. 3).

261 The spatial distribution of relative overcooling inconsistencies, *ROC* (Fig. 4),  
262 differs from that of absolute inconsistencies, *AOC*, and is due to the spatial variability  
263 in surface ice speed. The largest value of *ROC* across most GHF occurs at Dome C,  
264 where the observed surface ice speed is close to zero.

265

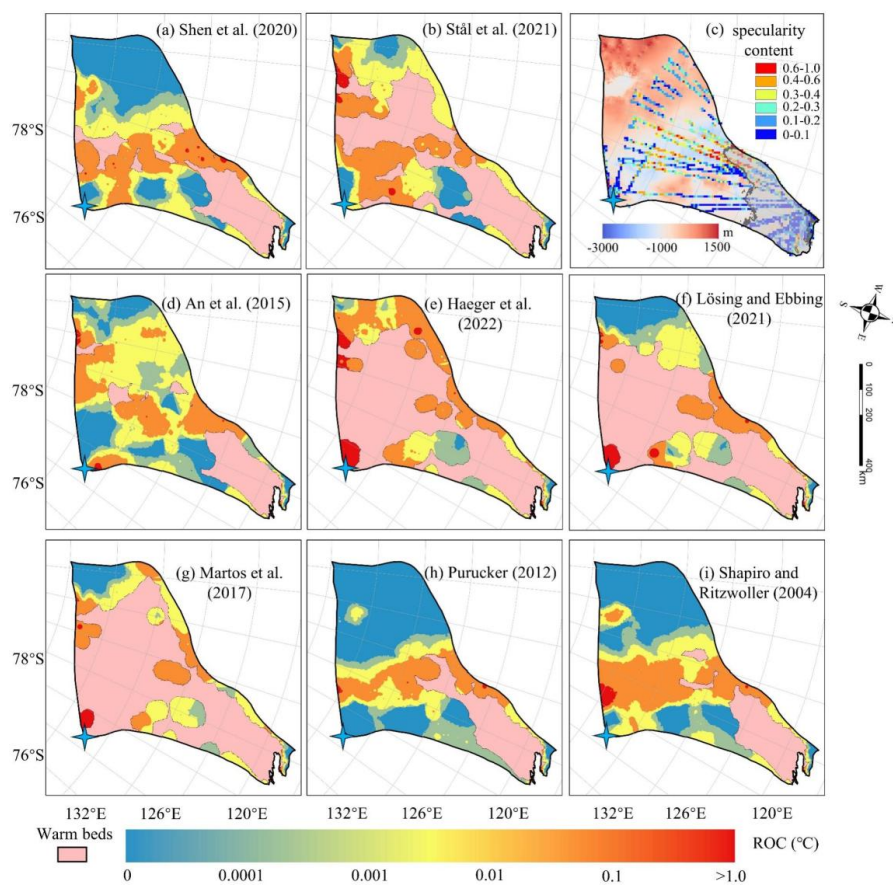




266

267 **Figure 3.** Spatial distribution of *AOC* inconsistency in modelled cold-bedded regions  
 268 **(a-b, d-i)** associated with the GHFs **(a-h)** in Fig. 2. The colormap is on logarithmic  
 269 scale. The pink region represents modelled warm bed. **(c)** Specularity content sourced  
 270 from radar data collected by ICECAP (Dow et al., 2020) with the bed elevation in the  
 271 background. Gray area in **(c)** corresponds to surface speed exceeding 30 m yr<sup>-1</sup>. The  
 272 blue star represents Dome C.

273

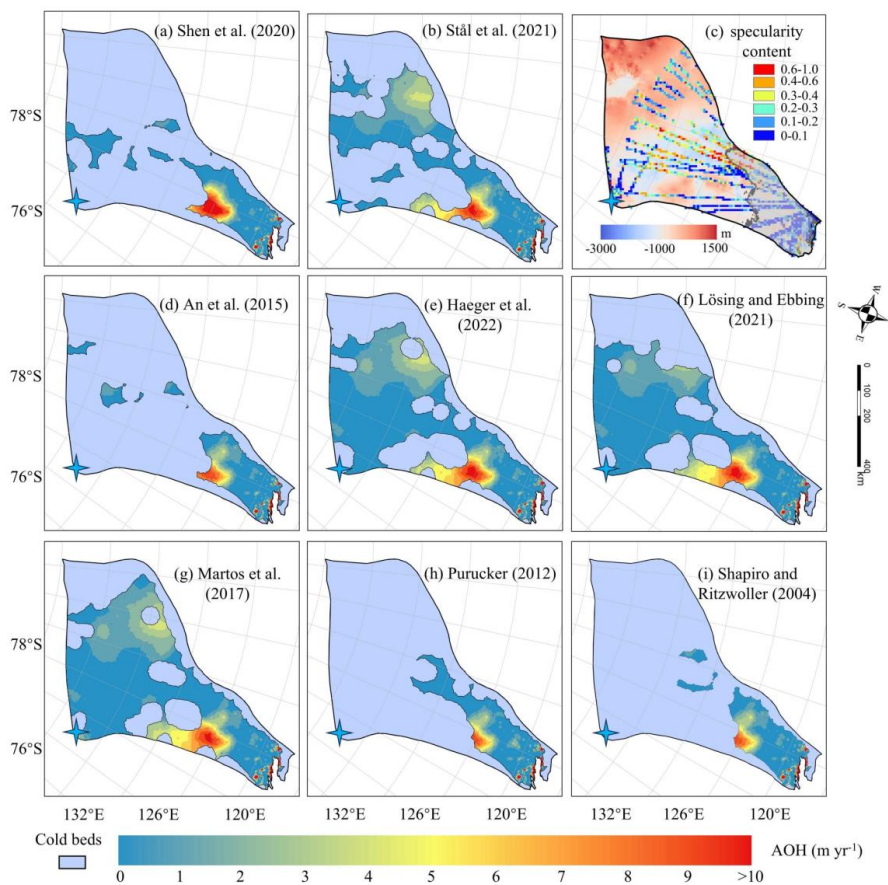


274  
 275 **Figure 4.** The spatial distribution of relative overcooling (*ROC*) inconsistency in cool  
 276 beds with (a), (b) and (d) to (i) corresponding to the GHFs (a – h) in Figure 2. The pink  
 277 area represents the warm beds. Dome C is marked by a blue star. (c) Locations of  
 278 specularity content derived from radar data collected by ICECAP (Dow et al., 2020)  
 279 and with the bed elevation in the background. The gray curve is the contour of the  
 280 surface speed of 30 m yr<sup>-1</sup>. Note the colormap is non-linear.

281  
 282 The GHF datasets of Stål et al. (2021), Haeger et al. (2022), Lösing and Ebbing  
 283 (2021) and Martos et al. (2017) which have higher than average GHF values provide  
 284 larger areas of warm bed than the other 4 GHFs. The simulations with all 8 GHFs yield  
 285 similar spatial distributions of *AOH* (Fig. 5) on the common area of warm bed, and  
 286 similar locations of high *AOH* values. A common high *AOH* area is located between  
 287 69°S and 72°S in the eastern part of Totten Glacier, due to simulated surface ice

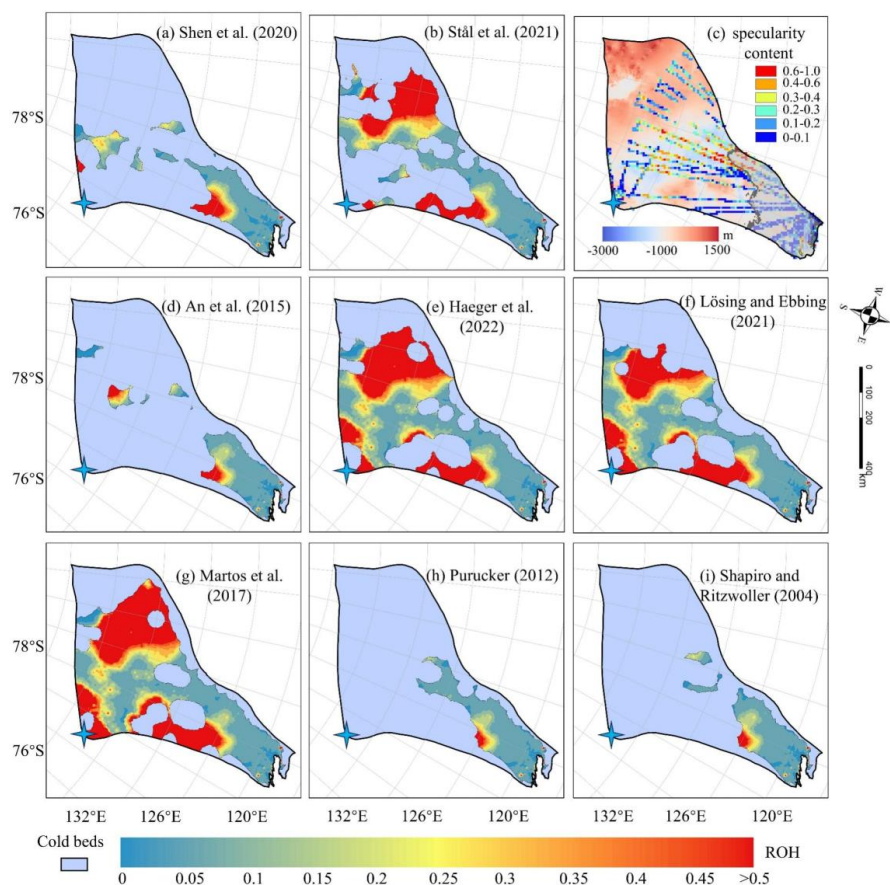


288 velocities greatly exceeding the observed surface ice velocities. Low specularity  
 289 content from radar data (Fig. 5c) suggests there is no basal water in the area (Dow et  
 290 al., 2020; Huang et al., 2024). Therefore, it is likely that the basal ice temperature is  
 291 overestimated there. The simulations with all the 8 GHFs also yield similar spatial  
 292 distribution of *ROH* (Fig. 6), but its largest values are mostly in the slow flowing region  
 293 as one may expect from its formulation (Eq. (3)).



294

295 **Figure 5.** Spatial distribution of *AOH* in warm-bedded regions with (a-b, d-i)  
 296 corresponding to the GHFs (a-h) in Fig. 2. The blue region indicates cold-bedded areas.  
 297 (c) Locations of specularity content, same as Fig. 3c. The blue star represents Dome C.  
 298



299  
 300 **Figure 6.** The spatial distribution of relative overheating (*ROH*) inconsistency in warm  
 301 beds with (a), (b) and (d) to (i) corresponding to the GHFs (a - h) in Figure 2. The light  
 302 purple mask represents the cold beds. (c) Locations of specularity content (coloured  
 303 points), same as Fig. 5.

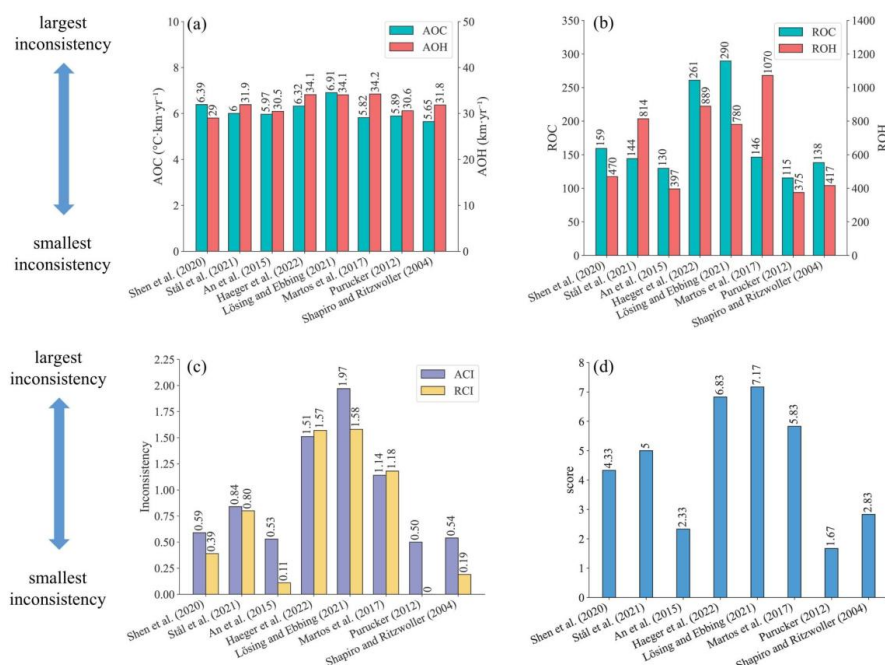
304  
 305 **3.3 Evaluation of Model Inconsistency with Eight GHFs**

306 All inconsistency indices for the simulation results using the eight GHF datasets  
 307 are illustrated in Fig. 7. The overheating inconsistency associated with Purucker et al.  
 308 (2012) and Shapiro and Ritzwoller (2004) GHFs is predominantly localized in fast-  
 309 flowing regions. Consequently, after normalization by the surface observed ice speed,  
 310 their relative rankings improve (Fig. 7). The GHFs from Purucker et al. (2012), An et  
 311 al. (2015), Shapiro and Ritzwoller (2004), and Shen et al. (2020) demonstrate balanced  
 312 performance with respect to both overheating and overcooling inconsistency metrics,



313 thereby securing the top four positions in both *ACI* and *RCI*. Their *ACI* values exhibit  
314 similarity, ranging from 0.50 to 0.59 (Fig. 7c). In contrast, simulation result utilizing  
315 Martos et al. (2017) GHF exhibits low *AOC* but high *AOH*. Simulation results utilizing  
316 Stål et al. (2021) GHF show low *ROC* but relatively high *ROH*. Notably, simulation  
317 results employing GHFs from Martos et al. (2017), Haeger et al. (2022), and Lösing  
318 and Ebbing (2021) demonstrate comparably high *AOH* values. These four GHF  
319 datasets—Martos et al. (2017), Stål et al. (2021), Haeger et al. (2022), and Lösing and  
320 Ebbing (2021)—are ranked in the bottom four positions for both *ACI* and *RCI* metrics.  
321 Furthermore, the ranking order of the eight GHFs remains consistent between *ACI* and  
322 *RCI*.

323 We combine the above six metrics using the ranking of each metric from 1 to 8,  
324 with 1 denoting the smallest inconsistency and 8 the largest. The final averaged ranking  
325 (Fig. 7d) using the arithmetic mean of the individual metric scores, is the same as that  
326 of *ACI* and *RCI*. Purucker et al. (2012), An et al. (2015) and Shapiro and Ritzwoller  
327 (2004) GHFs occupy the top three positions. Following closely, Shen et al. (2020) and  
328 Stål et al. (2021) GHFs secure the 4th and 5th positions, respectively. Martos et al.  
329 (2017), Haeger et al. (2022) and Lösing and Ebbing (2021) GHFs are ranked as the  
330 bottom three among the eight GHFs in Totten Glacier. The thermal state produced by  
331 the optimal GHF result shows that warm beds predominantly cluster around the  
332 grounding line and its upstream regions. Conversely, the inland areas of Totten largely  
333 exhibit cold temperatures, with relatively sparse warm-bedded areas.



334  
 335 **Figure 7.** Six inconsistency indicators and the final ranking of 8 GHF datasets. **(a)** the  
 336 cumulative values of *AOC* across grid points over cold bed region and *AOH* across grid  
 337 points over warm bed region; **(b)** the cumulative values of *ROC* across grid points over  
 338 cold bed region and *ROH* across grid points over warm bed region; **(c)** the absolute and  
 339 relative combined inconsistencies, *ACI* and *RCI*; **(d)** the average of ranking scores from  
 340 1 to 8 using the six inconsistency indicators. The value of inconsistencies and scores  
 341 are labeled at the top of the bars.

342

#### 343 4. Discussion

##### 344 4.1 Causes of Inconsistencies and Sources of Uncertainty

345 Our method evaluates the quality of an ice sheet temperature field by quantifying  
 346 the inconsistency between that temperature field and the velocity field that is obtained  
 347 if that temperature field is used to compute the rheology in a mechanical inversion.  
 348 Because mechanical inversions use surface velocity observations as a constraint, we  
 349 have developed an indirect method for using surface velocity observations to check the  
 350 quality of an englacial temperature simulation. However, the mere fact that  
 351 inconsistencies exist does not by itself tell us what caused those inconsistencies.

352 Broadly speaking, the measured inconsistencies can come from two sources:  
 353 temperature or velocity. Uncertainties in any of the input datasets used to compute those



354 two fields can produce inconsistencies, as can simplifications in the model physics.  
355 Here, we have tested the influence of one particular boundary condition, GHF, since  
356 that field is particularly hard to constrain. Because all other inputs are kept constant,  
357 the differences in the inconsistencies that we calculated between different simulations  
358 can be attributed to the GHF fields. However, we also found that all of the models we  
359 tested had non-zero inconsistency (Fig. 3; Fig. 5). The absolute inconsistencies, *AOH*  
360 and *AOC*, had particularly small between-model variability in comparison to their mean  
361 value. This could be because none of the input GHF fields correctly captured the true  
362 GHF, but it could also indicate problems with other model inputs. For instance, the  
363 surface temperature used in Huang et al. (2024) represents the present-day climate, but  
364 the thermal structure of the ice sheet may reflect colder temperatures during the last  
365 glacial cycle. We discuss an additional experiment we performed to test the influence  
366 of uncertainty in surface temperature on our inconsistency metrics in Section 4.3 below.  
367 By contrast, surface accumulation rate should have been lower during glacial periods,  
368 which would have a warming influence on ice sheet temperatures. Uncertainties in bed  
369 topography should influence both our thermal and our mechanical models, with deeper  
370 ice being more likely to be warm, and with errors in ice thickness producing  
371 compensating errors in basal sliding in our mechanical inversion. In the study of Huang  
372 et al. (2024), BedMachine v2 was used for ice thickness and subglacial topography.  
373 However, Bedmap3 (Pritchard et al., 2025) has better-resolved mountains and smoother  
374 trough margins.

375 The simulation results we use from Huang et al. (2024) came from a 3D isotropic  
376 full-Stokes ice flow model. While full-Stokes is generally considered the gold standard  
377 of ice sheet mechanical modeling, the use of an isotropic rheology may not be valid in  
378 some parts of the ice sheet, such as near ice divides or at the margin of an ice stream  
379 where the history of past ice deformation creates anisotropic crystal fabric that affects  
380 the present-day mechanical properties (Martín et al., 2009; Zhao et al., 2018b; Zwinger  
381 et al., 2014). Isotropic flow laws often require the use of an “enhancement factor” for  
382 vertical shear in the lower part of the ice column, an ad hoc correction that would have  
383 a particularly large influence on our computed overcooling metrics. Thus the isotropic  
384 flow law potentially introduces errors in modelled strain rates and, hence, bias in basal  
385 sliding velocities obtained by inversion methods (Budd and Jacka, 1989; Gerber et al.,  
386 2023; Rathmann and Lilien, 2022). Simulated surface ice velocities can be influenced  
387 by other factors in addition to ice fabric; shear margins are also impacted by  
388 accumulated rupture, such as damage along a shear margin (e.g., Benn et al., 2022;  
389 Lhermitte et al., 2020; Schoof, 2004; Sun et al., 2017). Ice deposited during the last  
390 glaciation has different chemistry (especially concentrations of chloride and possibly  
391 sulphate ions) which leads to smaller crystals that develop a strong, near-vertical,  
392 single-maximum fabric (Paterson, 1991). However, ice fabric data is sparse, known



393 from direct observations at ice cores (Azuma and Higashi, 1985) or inferred from  
394 specialized radar measurements (Fujita and Mae, 1994; Jordan et al., 2022), and its  
395 impact beyond the scope of this study as we refrain from incorporating additional  
396 observational data relying only on widely-available surface ice velocities.

397 Our inconsistency metrics are designed to provide bidirectional constraints,  
398 wherein the model is penalized for both overheating and overcooling. By adopting this  
399 bidirectional constraint framework, we aim to mitigate the risk of unidirectional  
400 constraints leading to excessively cold or warm outcomes being deemed optimal.  
401 However, our inconsistency metrics only provide a bidirectional constraint when  
402 viewed in a spatially integrated sense. Locally, we only have unidirectional constraints.  
403 This is because our overheating metrics are only computed where the bed is at the  
404 melting point, and our overcooling metrics are only computed where the bed is below  
405 the melting point. This makes methodological sense, as we know for sure that sliding  
406 must only occur where the bed is warm. However, in reality it is entirely possible that  
407 some of the areas where the modelled bed reaches the pressure melting point are still  
408 too cold (the modelled melt rate is lower than the real melt rate), and conversely, it is  
409 also possible that some of the areas where the modelled bed is below the pressure  
410 melting point are still too warm (the real temperature is colder still). Our method cannot  
411 identify these areas. Thus, our inconsistency metrics may underestimate variability in  
412 the ice sheet thermal state: we have no way to penalize cold regions that are not cold  
413 enough or warm regions that are not warm enough. We leave the development of these  
414 constraints to future work.

415

#### 416 **4.2 Sensitivity of Inconsistencies to GHF Datasets**

417 Comparing the GHF dataset rankings between this study and Huang et al. (2024),  
418 we find that the top 4 and the bottom 4 are the same in the two studies, albeit with slight  
419 variations in ranking. The lower ranking of Shen et al. (2020) in this study may be  
420 attributed to several factors. Firstly, Huang et al. (2024) excludes areas with ice speed  
421 exceeding  $30 \text{ m a}^{-1}$  (Fig. 3c) because specular content is an ambiguous indicator of  
422 wet beds there. Secondly, the GHF from Shen et al. (2020) yields higher basal  
423 temperature and also faster basal ice velocities in most of the cold bed of Totten Glacier,  
424 hence exhibits greater overcooling inconsistency, compared with Purucker et al. (2012),  
425 leading to a decrease in its rankings (Fig. S3). Lastly, Huang et al. (2024) primarily  
426 relied on specular content, while our study evaluated datasets based on  
427 inconsistencies in the simulation results. Despite these methodological differences, both  
428 studies identified four relatively well-performing GHF datasets for Totten Glacier,  
429 which exhibit similar distributions of warm and cold beds when compared to the other  
430 four datasets (Fig. 3 and Fig. 5). This similarity underscores that the warm bed is  
431 concentrated near and upstream of the grounding line. Datasets from Stål et al. (2021),





432 Martos et al. (2017), Haeger et al. (2022), and Lösing and Ebbing (2021) exhibit a  
433 tendency to overestimate GHF in central Totten Glacier.

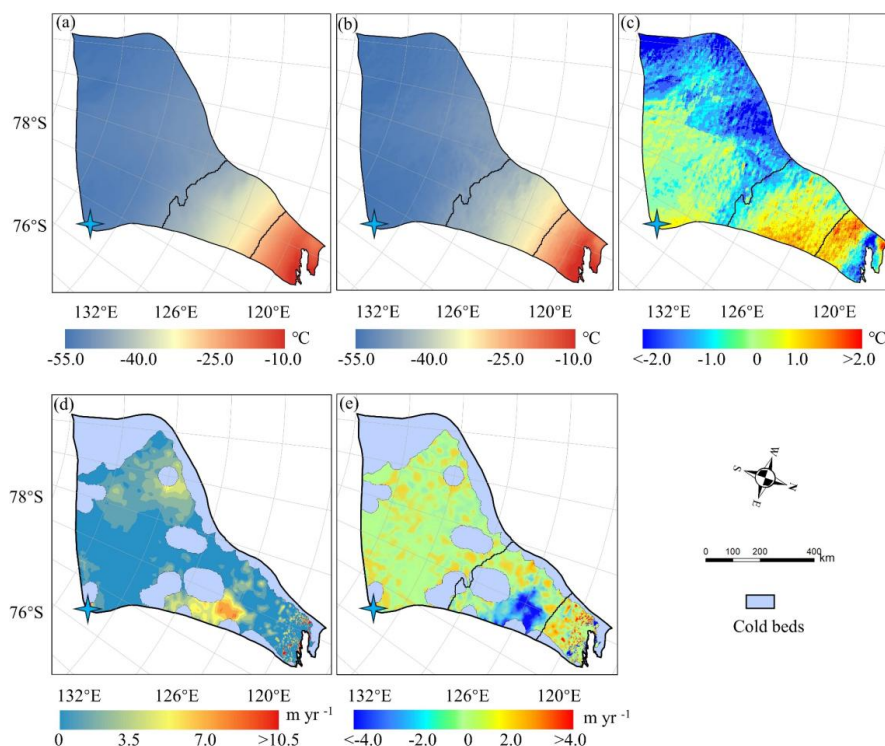
434 Simulations employing GHF datasets from Stål et al. (2021), Martos et al. (2017),  
435 Haeger et al. (2022), and Lösing and Ebbing (2021) yield more extensive warm-bedded  
436 regions and are expected to exhibit greater overheating inconsistency. Nevertheless,  
437 these models also exhibit relatively high overcooling inconsistency despite the limited  
438 extent of cold-bedded regions. We quantified the discrepancies between these four GHF  
439 datasets and the Purucker et al. (2012) GHF in terms of modelled basal velocity, basal  
440 temperature relative to the pressure melting point, and *AOC* (Fig. S4). The Purucker et  
441 al. (2012) GHF yields lower basal ice temperatures and slower basal velocities across  
442 most cold-bedded regions, consequently resulting in lower *AOC* values compared to  
443 the other four GHF datasets.

444

#### 445 **4.3 Implications for Ice Sheet Dynamics**

446 There is a common area between 69°S and 72°S in the eastern part of Totten  
447 Glacier with the largest *AOH* (Fig. 5) for all the GHFs varying from 48 to 70 mW m<sup>-2</sup>,  
448 which suggests that the *AOH* inconsistency is from other ice sheet properties rather than  
449 GHF. Zhang et al. (2022) reconstructed Antarctic near-surface air temperature based on  
450 MODIS land surface temperature measurements and in situ air temperature records  
451 from meteorological stations from 2001 to 2018. We compared the reconstruction of  
452 near-surface air temperature in the year 2001 (Zhang et al., 2022) and the ALBMAP v1  
453 dataset used in Huang et al. (2024). The surface air temperature in the area with large  
454 *AOH* from ALBMAP v1 is 0.6-3.1 °C higher than that from the reconstructed near-  
455 surface air temperature in 2001 (Fig. 8). The MODIS-based near-surface air  
456 temperature product shows warming in Totten Glacier from 2001 to 2018. Even so, the  
457 surface air temperature in the area with large *AOH* from ALBMAP v1 is still higher  
458 than that in 2018 but over a smaller area. Therefore, we infer that the large *AOH* may  
459 be attributed to the present-day ice surface temperature derived from ALBMAP v1 in  
460 this area being unrealistically warm. The englacial temperature will be lower than  
461 present-day ice sheet surface temperature used in the model but warmer than the  
462 average surface temperature during the last glacial-interglacial cycle. We lowered the  
463 surface ice temperature in this area by 1 °C, reran the simulation, and found that *AOH*  
464 with all the GHFs was halved (Fig. 8e).

465



466

467 **Figure 8.** Surface ice temperature from ALBMAP v1 (a) and MODIS-based near-  
 468 near-surface air temperature (b) in the year 2001, and their difference (c). (d) The AOH using  
 469 modified surface ice temperature by reducing the temperature between the two thick  
 470 black curves (contour lines of  $-44\text{ }^{\circ}\text{C}$  and  $-26\text{ }^{\circ}\text{C}$ ) in (a) by  $1\text{ }^{\circ}\text{C}$  and GHF of Martos  
 471 et al. (2017). (e) The difference between the AOH using cooler surface ice temperature  
 472 and the original AOH. The blue star represents Dome C.  
 473

474 Given that data assimilation and inverse methods are widely employed to infer  
 475 basal friction coefficients in ice sheet simulations, it is essential to acknowledge the  
 476 impact of the inconsistencies identified in our study on ice sheet dynamics. A cold bed  
 477 is supposed to provide substantial resistance and limit basal sliding; however, if the  
 478 basal temperature is overestimated, it may decrease viscosity and enhance basal sliding.  
 479 This overheating inconsistency would lead to an overestimation of ice flow speeds,  
 480 discharge, and the dynamic ice loss (Artemieva, 2022; Burton-Johnson et al., 2020).  
 481 Similarly, under representation of warm bedding would slow ice discharge estimates,  
 482 and hence potential ice sheet response to climate warming. The basal thermal regime



483 critically influences the stability of grounding lines and the behavior of ice streams. In  
484 a warming climate, increases in geothermal or frictional heating can trigger basal  
485 thawing in these areas, lowering basal friction and potentially initiating rapid grounding  
486 line retreat—a key component of marine ice sheet instability (MISI) (Reese et al., 2023;  
487 Ross et al., 2012). Without incorporating a self-consistent thermal model into the  
488 inversion, projections may misrepresent the onset and extent of these dynamic  
489 instabilities. Our findings underscore that a fully coupled inversion framework would  
490 use not only surface velocity data but also incorporate direct or proxy observations of  
491 basal temperature and subglacial hydrology. Such an approach would better constrain  
492 the basal friction coefficient in a physically consistent manner, reducing the risk of  
493 producing nonphysical states. This integration is especially critical for projections of  
494 ice sheet evolution under climate change, as the dynamic response is sensitive to even  
495 small changes in basal conditions.

496

## 497 **5. Conclusion**

498 We propose a novel and rapid method to quantify the inconsistencies between  
499 modelled basal ice temperature and observed surface ice speed and assess the quality  
500 of ice sheet model simulation results without using subglacial observation data.  
501 Previously, it has been assumed that checking the quality of an ice sheet temperature  
502 model required in situ observations, whether from ice cores or geophysical techniques  
503 like ice penetrating radar. By using the ice temperature field to compute the rheology  
504 structure needed for a mechanical inversion and then quantifying the inconsistency  
505 between the inverted velocity field and the original ice temperature field, we are able  
506 to use remotely sensed surface velocity observations as a check on the quality of  
507 modelled englacial temperatures. Given the challenges in acquiring subglacial data, our  
508 method can provide a streamlined and effective approach to evaluation.

509 We apply this method to the simulation results of Totten Glacier using a 3D full-  
510 Stokes model with 8 different GHF datasets. Assuming the inconsistencies are mainly  
511 due to unrealistic GHF datasets, we use the inconsistencies to assess the reliability of  
512 those GHF datasets. We compare our GHF ranking with that by Huang et al. (2024)  
513 which used specularly content to derive a two-sided constraint on the basal thermal  
514 state. We find that the top 4 and the bottom 4 GHFs are the same in the two studies,  
515 albeit with slight variations in ranking. Furthermore, we find that the simulations with  
516 all GHF datasets underestimate the basal ice temperature in a canyon on the western  
517 boundary of Totten Glacier, and we infer that the common high overheating  
518 inconsistencies with all the GHF datasets in the eastern Totten Glacier between 69°S  
519 and 72°S may be attributed to the unrealistically warm surface ice temperature used  
520 there in the model. While we demonstrate that this approach works on simulation results  
521 for Totten Glacier, testing of the method on other glaciers would be useful to assess if



522 the approach is worthwhile for revealing ambiguous conflicts in observations and  
523 simulations.

524

525

526

527 *Data availability.* MEaSURES BedMachine Antarctica, version 2, is available at  
528 <https://doi.org/10.5067/E1QL9HFQ7A8M> (Morlighem, 2020). MEaSURES InSAR-  
529 Based Antarctic Ice Velocity Map, version 2, is available at  
530 <https://doi.org/10.5067/D7GK8F5J8M8R> (Rignot et al., 2017). MEaSURES Antarctic  
531 Boundaries for IPY 2007–2009 from Satellite Radar, version 2, is available at  
532 <https://doi.org/10.5067/AXE4121732AD> (Mouginot et al., 2017). ALBMAP v1 and the  
533 GHF dataset of Shapiro and Ritzwoller (2004) are available at  
534 <https://doi.org/10.1594/PANGAEA.734145> (Le Brocq et al., 2010b). The GHF dataset  
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536 <http://www.seismolab.org/model/antarctica/lithosphere/AN1-HF.tar.gz> (last access: 11  
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538 <https://sites.google.com/view/weisen/research-products?authuser=0> (last access: 11  
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540 <https://doi.org/10.1594/PANGAEA.882503>. The GHF dataset of Purucker (2012) is  
541 available at  
542 [https://core2.gsfc.nasa.gov/research/purucker/heatflux\\_mf7\\_foxmaule05.txt](https://core2.gsfc.nasa.gov/research/purucker/heatflux_mf7_foxmaule05.txt) (last  
543 access: 11 April 2023).

544

545 *Author contributions.* LZ and JCM conceived the study. LZ, MW, and JCM designed  
546 the methodology. JW and LZ analyzed the data and conducted visualization. JW  
547 and LZ wrote the original draft, and all the authors revised the paper.

548

549 *Competing interests.* The contact author has declared that none of the authors has any  
550 competing interests.

551

552 *Acknowledgements.* This work was supported by National Key Research and  
553 Development Program of China (grant no. 2021YFB3900105) and Academy of  
554 Finland (grant no. 355572).

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