

# biogeodyn-MITgcmIS (v1): a biogeodynamical tool for exploring climate steady states with a new global-scale ice sheet model

Laure Moinat<sup>1,2,3</sup>, Florian Franziskakis<sup>2</sup>, Christian V  rard<sup>3,4</sup>, Daniel N. Goldberg<sup>5</sup>, and Maura Brunetti<sup>1,2,3</sup>

<sup>1</sup>Group of Applied Physics, University of Geneva, Rue de l'  cole de M  decine 20, 1205 Geneva, Switzerland

<sup>2</sup>Institute for Environmental Sciences, University of Geneva, Bd. Carl-Vogt 66, 1205 Geneva, Switzerland

<sup>3</sup>Centre pour la Vie dans l'Univers (CVU), University of Geneva, Geneva, Switzerland

<sup>4</sup>Section of Earth and Environmental Sciences, University of Geneva, Rue des Mara  chers 13, 1205 Geneva, Switzerland

<sup>5</sup>School of GeoSciences, University of Edinburgh, Edinburgh, UK

**Correspondence:** Laure Moinat (laure.moinat@unige.ch)

**Abstract.** Modelling the climate system is challenging when slow-response components, such as the deep ocean, vegetation and ice sheets, must be evolved alongside fast-response ones. This is crucial for investigating, for example, **the dynamical structure of the Earth climate, including steady states, their basin boundaries and their response to external forcing and internal variability.** ~~climate tipping elements and their interactions on the global spatial scale over multimillennia timescales.~~

5 While Earth system models, such as those used in the Coupled Model Intercomparison Project (CMIP), are too computational expensive for simulations spanning thousands of years, simplified parameterizations and coarse resolutions in Earth Models of Intermediate Complexity (EMICs) can significantly affect the nonlinear interactions among climate components. Here, we describe a new tool, *biogeodyn-MITgcmIS*, which **is in between these two types of models.** ~~has a complexity level intermediate between EMICs and CMIP-class models.~~ The core of *biogeodyn-MITgcmIS* is a coupled MITgcm setup that includes atmosphere, ocean, thermodynamic sea ice, and land modules. To this, we ~~have added offline~~ **asynchronous** couplings  
10 with a vegetation model (BIOME4), a hydrological model (*pysheds*), and a new global-scale ice sheet model (*MITgcmIS*). The latter is implemented on the same cubed-sphere grid as MITgcm, using the shallow-ice approximation, as well as MITgcm outputs and a modified Positive Degree Day method to estimate the ice-sheet surface mass balance. Here, we describe in detail the new ice sheet model and the coupling procedure. We evaluate *biogeodyn-MITgcmIS* using **a pre-industrial simulation**  
15 **initialized from bedrock topography and leading to the ice-sheet formation, together with a forced simulation covering** ~~for the pre-industrial period and the 1979-2009 period.~~ These two experiments allow us to assess the model's performance against CMIP-class models, as well as a combination of reanalyses and observations. **To evaluate the ability of our model setup to represent completely different climate conditions and continental configurations, we discuss also a Permian-Triassic simulation.** *biogeodyn-MITgcmIS* successfully reproduces the large-scale climate and its major components, with results comparable to  
20 those of two CMIP models with dynamical vegetation **in the pre-industrial scenario.** We discuss its potential applications and future developments.

# 1 Introduction

As the atmospheric CO<sub>2</sub> concentration has raised since the pre-industrial era under leading to the present-day climate crisis, there is an increasing risk of crossing critical thresholds where some parts of the climate system suddenly change, potentially in an irreversible manner. In this context, it is important to understand the dynamical structure of the Earth climate by identifying the different climate steady states (attractors) under external forcing (e.g. CO<sub>2</sub>), their limits of existence (basins of attraction), and the associated boundaries, which may correspond to global tipping points (that is, forcing values beyond which the climate system shifts towards a new steady state). Reaching stationarity is an important property for characterizing climatic attractors (Hawkins et al., 2011; Drótos et al., 2017; Lucarini and Bódai, 2017; Brunetti et al., 2019; Brunetti and Ragon, 2023; Moinat et al., 2024). However, to reach equilibrium among all climate components, including those with a slow response, such as the deep ocean, terrestrial vegetation or ice sheets, simulations must be run on millennia time scales. This type of analysis requires dedicated modelling techniques. Many elements of the Earth climate (denoted as ‘tipping elements’) can indeed experience abrupt changes in their dynamics (Lenton et al., 2008; Lenton et al., 2022). Some examples were reported from proxy data related to past climate regime shifts, such as the Atlantic Meridional Overturning Circulation (AMOC) or ice sheets during the glacial cycles (Boers et al., 2018; Boers et al., 2021). Tipping behavior in the climate system is very difficult to study because changes occur over a large range of temporal scales (from decades in the Amazon forest to centuries in AMOC or multimillennia for the complete melting of ice sheets), at local or global spatial scales (Wunderling et al., 2024). Causal relationships giving rise to tipping cannot be easily inferred from sparse proxy data, and numerical simulations are often not able to span all the timescales because of too high computational costs.

There are several numerical techniques that have been proposed for studying tipping dynamics points, from regional to global circulation models, at different levels of complexity in process representation, depending on the selected temporal and spatial scales (Wunderling et al., 2024). We are interested in a modeling setup that allows for the description of climates where the ice sheets are not confined to high latitudes, but can spread to large regions like during glaciation periods, waterbelt or snowball states. Thus, we need a modeling setup that can span daily to millennial timescales at the global spatial scale, thus including at least atmosphere, surface and deep ocean, sea ice, land vegetation and ice sheet dynamics. While these components are sometimes included in CMIP-like models (Eyring et al., 2016), these models require high computational costs to run for thousands of years and thus simulations cannot reach stationarity in slow deep-ocean and ice sheet dynamics (Balaji et al., 2017). In contrast, Earth Models of Intermediate Complexity (EMICs) can reach a stationary state rapidly are fast-reaching a stationary state (Claussen et al., 2002; Willeit et al., 2022), but their coarse spatial resolutions and simplified parameterizations can have non negligible impacts on the nonlinear interaction among climatic components.

Reaching stationarity is an important property for characterizing climatic attractors, i.e. control runs describing the asymptotic state of all climatic variables under a given forcing and unveiling the nonlinear backbone structure of the climate dynamics (Hawkins et al., 2011). Once the attractors are found, transient simulations can also be run using different kinds of perturbation (random noise or deterministic scenarios) to investigate shifts from one stationary state to another (Lucarini and Bódai, 2020; Lucarini and Bódai, 2022; Lucarini et al., 2023). In particular, these transient simulations under decreasing and increasing forcing can reveal not only tipping dynamics over

millennial time scales, but also domino effects and process reversibility at local or global spatial scales. However, it is crucial that all climatic components evolve in a consistent way under the same forcing, including those with slow response, such as the deep ocean, ice sheets and terrestrial vegetation, which have been identified as potential tipping elements (Wunderling et al., 2024).

Nowadays, there are few CMIP6 models with interactive ice sheets (Ackermann et al., 2020; Muntjewerf et al., 2020; Madsen et al., 2022; Smith et al., 2021) and/or dynamical vegetation (Drüke et al., 2021). However, as said above, high computational costs of this type of models makes them only adapted for **However, high computational costs make these models appropriate for** studying climate evolution on centennial timescales. A technique for speeding up complex models and thus enabling them to explore feedbacks on longer timescales is ~~offline~~ (or asynchronous) coupling (Claussen, 1994; Herrington and Poulsen, 2011; Pohl et al., 2016). ~~This is particularly useful for including tipping elements with a slow response.~~ In practise, the climate is first estimated with fixed ice sheets and vegetation, and eventually the latter are updated to match the equilibrium conditions of the former (Foley et al., 1998). The procedure can be repeated until convergence. In this way, fast and slow components evolve consistently until a stationary state is reached. ~~Similar steps can be used in transient simulations between one climatic steady state and another by increasing the coupling frequency.~~

Here, we propose a simulation tool, called *biogeodyn-MITgcmIS*, that combines surface processes, biology adaptation, and climate dynamics on multimillennial timescales, **with a state-of-the-art ocean and simplified atmospheric parameterizations, hence having a higher vertical resolution in the ocean and a higher spatial resolution than traditional EMICs (Holden et al., 2016; Willeit et al., 2022)** ~~with a complexity that is in between EMICs and CMIP-like models.~~ Such coupled setup, **which includes asynchronous coupling with a vegetation model and a newly developed global-scale ice sheet model,** allows one to take into account in a consistent manner the evolution of major processes of the Earth over a multimillennial time scale: vegetation, atmosphere, ocean, cryosphere, hydrosphere and their interactions, under different boundary conditions given by continental and oceanic configurations. **Therefore, this setup is also suitable for investigating deep-time climates, which are characterized by huge uncertainties in the initial conditions, especially for ice sheets and vegetation.** We will provide a complete description of ~~all~~ **a short description of the dynamical core (MITgcm), the vegetation model (BIOME4) and the hydrology model (*pysheds*), as they have been already explicitly detailed elsewhere, while we will extensively describe the ice sheet model the components and** ~~in particular the newly developed ice sheet model (*MITgcmIS*).~~ To assess the capability of *biogeodyn-MITgcmIS* to represent the present climate, we will validate its results against those obtained using some CMIP6 class models and reanalysis products. **In addition, to display its ability to simulate ice sheets developing for different continental configurations and climate conditions, a simulation for the Permian-Triassic paleogeography based on Ragon et al. (2024) is presented and discussed.**

## 2 Biogeodynamical tool

Here, we describe each component of our biogeodynamical tool, including the boundary conditions and the coupling strategy.

## 2.1 GCM - Coupled MITgcm Setup

The dynamical core of our tool is given by the MIT general circulation model (MITgcm) (Marshall et al., 1997a, b; Adcroft et al., 2004), which solves the Navier-Stokes equations for the atmosphere and the ocean over the same cubed-sphere (CS) grid (Marshall et al., 2004). In particular, we consider MITgcm (version c68s) in a coupled setup including atmosphere, ocean, thermodynamic sea ice and land (denoted as Coupled MITgcm Setup). In our simulations, we use the so-called CS32 configuration, where each face of the cube has  $32 \times 32$  grid cells, corresponding to an average horizontal resolution of  $2.8^\circ$ . This or similar setups have been already used for studying idealised configurations such as the coupled aquaplanet (Ferreira et al., 2011; Rose, 2015; Ferreira et al., 2018; Brunetti et al., 2019; Ragon et al., 2022; Zhu and Rose, 2023; Brunetti and Ragon, 2023; Moinat et al., 2024), deep-time climates (Brunetti et al., 2015; Ragon et al., 2024, 2025) and the present-day climate (Brunetti and V erard, 2018).

Physical parameterizations for the atmosphere are based on the 5-layer SPEEDY model (Simplified Parameterizations, primitive-Equation Dynamics) (Molteni, 2003). SPEEDY is in the intermediate-complexity class a model of intermediate complexity for the atmosphere, and includes simplified representations of convection, large-scale condensation, vertical diffusion, surface fluxes of momentum and energy. The radiative scheme uses two spectral bands for the shortwave radiation and four for the longwave radiation. Cloud cover and thickness are defined diagnostically from the values of relative and absolute humidity. Cloud albedo depends on latitude, as done in Ragon et al. (2022), for reducing the net solar radiation at high latitudes and therefore having a better agreement with observational data (Kucharski et al., 2013). Five pressure levels are represented, going from 1000 hPa to 0 Pa, where the bottom level represents the planetary boundary layer, the top one the stratosphere, and the remaining three the free troposphere. SPEEDY has been evaluated against NCEP-NCAR and ERA5 reanalysis (Molteni, 2003) and, despite its simplified parameterizations, has been assessed to provide a realistic description of the atmosphere, with the advantage of requiring less computer resources than state-of-the-art Atmospheric GCMs. A simple 2-layer land model (Hansen et al., 1983) is coupled to SPEEDY.

The physics packages activated for the oceanic component are the KPP scheme (Large and Yeager, 2004) to account for vertical mixing in the water column, and the Gent and McWilliams scheme (Gent and McWilliams, 1990) to describe to capture mixing by mesoscale eddies. The Winton model (Winton, 2000) is used to include sea ice thermodynamics (THSICE), while sea ice dynamics is neglected. In our setup, there are 25 vertical nonuniform levels in the ocean, with thickness ranging between 20 m near the surface and 1300 m at the bottom.

The Coupled MITgcm Setup needs to have the following input files: bare-surface albedos, vegetation fraction, bathymetry, topography, runoff routing map, salinity and sea temperature for all the ocean levels (the latter two files are provided at the initial step, and then updated by the dynamical core). Orbital parameters can be set by specifying the obliquity, precession and eccentricity. In addition, the duration of the day and the radiative influx from the sun can be modified. It runs about 200 years per day using 25 cores, which is equivalent to 300 CPU hours for 100 simulated years. 200 years per CPU day using 25 cores.

## 2.2 Boundary conditions - land-ocean configurations

Our tool can be applied for describing the present-day **climate** as well as deep-time climates **using different paleogeographies**.  
120 While the continental configuration for the present day is well known and based on observations, we need to use paleogeography reconstructions for deep-time climates. Several options are available (Scotese, 2021; Merdith et al., 2021; V  rard, 2019). Even if in previous works the MITgcm setup was coupled to the PANALEISIS reconstructions (Brunetti et al., 2015; Brunetti and V  rard, 2018; Ragon et al., 2024, 2025), it is important to note that our tool can be started from any boundary conditions (i. e., alternative paleogeographical reconstructions, idealised land-ocean configurations or aquaplanet) and ocean depths,  
125 which is useful for exoplanet or conceptual studies.

In both cases of present-day and deep-time climates, the procedure for adapting the high resolution geographical maps to the MITgcm grid will be **is** the same. Either using the present-day ETOPO global relief model (ETOPO, 2022) or a paleogeographic reconstruction from PANALEISIS, the input geography is given in the latitude/longitude coordinates system with arc-sec horizontal resolution. Since the simulations are performed with the cubed-sphere CS32 grid, a smoothing procedure is  
130 needed to upscale to the 2.8   resolution. Then, we need to remove isolated oceanic points or lakes independent of their size, since the MITgcm becomes numerically unstable when there are enclosed areas of water. Moreover, very shallow waters are also prone to instability, especially when sea ice develops; therefore, we set all oceanic points shallower than -20 m to this depth.

## 2.3 Vegetation - BIOME4

135 BIOME4 is a vegetation model that predicts the global steady state of the vegetation distribution corresponding to long-term averages of monthly mean surface air temperature (SAT), sunshine and precipitation (Kaplan, 2001). Additional inputs are soil depth and texture, which are used to determine water holding capacity and percolation rates (Kaplan et al., 2003). Moreover, the atmospheric CO<sub>2</sub> content needs to be specified. All these quantities are obtained from steady-state simulations performed using MITgcm in the coupled configuration described in Sec. 2.1. **The albedo and the vegetation map obtained as outputs of**  
140 **BIOME4 are then reused in the next iteration of the coupling system. Water holding capacity and percolation rates are kept constant in our simulations and set to the present-day average value.**

BIOME4 follows the principle that ecosystems can be divided into a set of biomes characterised by the performance of plant functional types (PFTs), **i.e. key parameters used to classify plant species having a similar response to the environment** (Haxeltine and Prentice, 1996; Kaplan, 2001). The model selects among a set of 12 PFTs the subset that can be present in a grid  
145 cell on the basis of physiological and climatic constraints, like minimal temperature and water supply. Using a coupled carbon and water flux model, BIOME4 calculates the net primary productivity (NPP) of each **PFT PFT** and the corresponding seasonal maximum leaf area index (LAI) that maximises NPP. At this point, competition among **PFTs PFTs** is simulated by selecting the **PFT PFT** with the optimal NPP as the dominant plant type. Opposing effects due to light competition and wildfires are included through semi-empirical rules. The final output is the vegetation distribution in terms of the dominant and secondary PFTs, total  
150 LAI and NPP, which can be classified into biome types, for a total of 27 biomes (28 including land ice). **Land-ice points are**

determined by the ice sheet extent computed by *MITgcmIS* (see next section). Therefore, the grid points that are identified as land ice overwrite the biome number given by BIOME4.

155 Main differences between BIOME4 and earlier versions (developed by Prentice et al. (1996); Haxeltine and Prentice (1996)) are the inclusion of new PFTs to represent vegetation types in the polar regions, and the calculation of photosynthetic pathways (for C<sub>3</sub> and C<sub>4</sub> plants) that depend on the PFT. BIOME4 and its earlier versions have been used to investigate climate-biosphere interactions in the past (de Noblet-Ducoudré et al., 2000; M. Haywood et al., 2002; Kaplan et al., 2003; Salzmann et al., 2008; Sellwood and Valdes, 2008; Ragon et al., 2024, 2025). BIOME4 has also been used to assess the impact of current climate changes on the distribution of vegetation types (Allen et al., 2024).

## 2.4 Ice sheet - *MITgcmIS*

160 We have developed a Python code, called *MITgcmIS*, that describes the evolution of ice sheets at the global scale on the same cubed-sphere grid used by MITgcm. A global-scale ice sheet model is required when the climate state allows for the presence of ice sheets at low latitudes, for example during glaciation periods, waterbelt states or snowball states (Kirschvink, 1992; Hoffman and Schrag, 2002). Since we are interested in simulating the main processes occurring at spatial resolutions of around horizontal resolutions of the order of 2° or coarser, we can neglect basal melting and other fine-scale processes, as calving and ice streams, since they cannot be resolved at such coarse resolutions. Note that there is already an MITgcm module, called STREAMICE, which implements in Fortran these small-scale processes at the km-scale (Goldberg and Heimbach, 2013), however this package is not used in our coupled setup.

170 In *MITgcmIS*, we use the shallow-ice approximation (Cuffey and Paterson, 2010) to model the ice-sheet movement and an improved the Positive Degree Day (PDD) method (Braithwaite, 1977) to compute the S<sub>surface</sub> M<sub>mass</sub> B<sub>balance</sub> (SMB), as we also want to apply our coupled framework to paleoclimates. In particular, we choose an improved the PDD approach as described in Tsai and Ruan (2018) instead of the Surface Energy Balance (SEB) method, since the latter requires quantities at the km-scale to estimate the energy budget, such as layer structure, surface roughness, and stability of the surface terrain to obtain latent and sensible heat fluxes (Hock and Holmgren, 2005). Thus, the SEB method is generally used in regional climate models, which are able to reach the required accuracy in the representation of the climatic fields (especially clouds), in general provided by reanalyses (Wake and Marshall, 2015). This is an important limiting factor to consider that makes it difficult to apply SEB to paleoclimate simulations.

180 Although the PDD approach succeeds in representing the SMB surface mass balance in coarse simulations, it can underestimate the melting in past periods of high insolation (Plach et al., 2018). Moreover, since this method does not account for energy exchanges between the ice sheet and the other components of the climate system, it cannot ensure a closed energy budget. Despite its limitations, we believe that the PDD method is the best choice when the representation of the atmosphere and snow processes are is at the global scale on a coarse grid and simplified as in the SPEEDY and land modules (Sec. 2.1).

## 2.4.1 Basic description

We start from the equation that describes the depth-integrated mass conservation for incompressible ice (Schoof and Hewitt, 2013):

$$185 \quad \frac{dH}{dt} = -\nabla \cdot \mathbf{q} + \dot{A} - \dot{B} \quad (1)$$

where  $H = z_S - z_B$  is the height of the ice sheet between the bed  $z_B$  and the surface  $z_S$  vertical coordinates,  $\mathbf{q} = \int_{z_B}^{z_S} \mathbf{U} dz$  is the horizontal flux obtained by vertical integration over the ice thickness of the horizontal part  $\mathbf{U}$  of the velocity vector,  $\dot{A}$  is the **SMBsurface mass balance** rate and  $\dot{B}$  is the basal melting rate. In our case, we neglect the basal melting rate, hence  $\dot{B} = 0$ . Eq. (1) is simply an expression of mass continuity; but the specific form of  $\mathbf{q}$  derives from the full Stokes equations in the  
 190 so-called shallow-ice approximation, based on the low aspect ratio ( $\sim 10^{-2}$ - $10^{-3}$ ) between vertical and horizontal length in ice sheets. This relationship describes how ice flux responds to ice-sheet geometry, as described below.

Ice rheology can be simplified by neglecting the ice bed movement, by considering that the only important type of deformation is vertical shearing, and by assuming a power-law shear thinning viscous rheology, with strain rates  $\dot{\epsilon}$  proportional to the driving stress  $\tau_d$ , as  $\dot{\epsilon} = a\tau_d^n$ , where  $a$  is the Glen's law coefficient, which is assumed constant, and  $n$  is typically set to 3. This  
 195 leads to the following relation (Cuffey and Paterson, 2010):

$$q = \frac{2a}{n+2} \tau_d^n H^2 = -D \nabla z_S \quad (2)$$

where  $\tau_d = -\rho_i g H \nabla z_S$ ,  $\alpha = -\nabla z_S$  is the surface slope,  $g$  the gravitational acceleration,  $\rho_i = 920 \text{ kg m}^{-3}$  the ice density, and

$$D = \frac{2a}{n+2} (\rho_i g)^n |\nabla z_S|^{n-1} H^{n+2} \quad (3)$$

200 By combining the two relations, one obtains

$$\frac{dH}{dt} = \nabla \cdot (D \nabla H) + \nabla \cdot (D \nabla z_B) + \dot{A} \quad (4)$$

Eq. (4) is numerically integrated in Python on the cubed-sphere grid, once the **SMBsurface mass balance rate term**  $\dot{A}$  is determined, as detailed in the next sections.

As noted above, we do not consider spatially varying Glen's law parameter  $a$  or basal sliding. Both processes are sometimes  
 205 included in modelling of paleo ice sheets, by employing thermomechanical components to model ice temperature (which influences Glen's law, Cuffey and Paterson (2010)), and to determine where basal sliding occurs due to thawed-bed conditions (e.g., Moreno-Parada et al., 2023). However, the coarse resolution of our numerical grid does not allow representing of the fast streaming that results from basal melting. Since our purpose is to investigate climatic steady states in which ice sheets are in balance with the ocean, atmosphere, and biosphere, through their impacts of global albedo, large-scale orography and  
 210 freshwater fluxes, we choose not to represent these higher-order **km-scale** processes. Moreover, the inclusion of such processes would introduce additional uncertain quantities and formulations – such as the temperature dependence of  $a$ , the pattern and

magnitude of geothermal heat flux, and the response of basal stress to basal water formation and drainage. Instead, using a single parameter,  $a$ , to describe ice-sheet dynamics allows it to be constrained straightforwardly using ice volume, as shown in the results section Sec. 3.1.1.

## 215 2.4.2 Surface mass balance –ablation

To compute the **SMBsurface mass balance** we use a method based on the Positive Degree Day (PDD), which has in addition a percolation layer for correctly assessing the melting (Tsai and Ruan, 2018).

The idea of the improved **this** PDD method is to account for the presence of a percolation layer of thickness  $H_p$  that creates a delay in melting at the ice surface, as the ice is not expected to melt as soon as the SAT reaches  $0^\circ\text{C}$  (Tsai and Ruan, 2018). The  
 220 heat is assumed to be diffused downwards in the percolation layer, which reaches a uniform temperature  $T_p$  on a relatively fast timescale. In our setup, we assume that the percolation depth  $H_p$  is constant even if in reality it can slightly change, depending on the type of ice. Below the percolation depth, the temperature quickly relaxes to an equilibrium value that does not depend on diffusion (Tsai and Ruan, 2018).

We assume that, between the ice surface ( $z = 0$ ) and the height where the temperature measurement is performed ( $z = h$ ),  
 225 there is a constant temperature gradient. Thus, the heat flux can be written as:

$$q(t) = -k \frac{\partial T}{\partial z} = -k \frac{T_a(t) - T_p(t)}{h} \quad (5)$$

where  $k$  is the effective thermal conductivity of air,  $T_a$  is the temperature at  $z = h$ , and  $T_p$  is the percolation layer temperature. From this assumption, and using conservation of energy between the percolation layer and the air, one can compute the **ODE ordinary differential equations** for the percolation layer temperature and for the ablation rate  $a_r$  (Tsai and Ruan, 2018):

$$230 \quad \frac{dT_p}{dt} = \frac{k}{h\rho_i c_P H_p} (T_a - T_p) \quad \text{if } T_p < 0 \text{ or } T_a < 0 \quad (6)$$

$$a_r(t) = -\frac{dz_s}{dt} = \frac{k}{h\rho_i L} (T_a - T_p) \quad \text{if } T_p = 0 \text{ or } T_a > 0 \quad (7)$$

where  $z_s$  is the ice surface elevation. Constants  $k$ ,  $h$ ,  $\rho_i$ ,  $c_P$ ,  $H_p$  and  $L$  are all assumed to be known. We have used  $\rho_i = 920 \text{ kg m}^{-3}$ ,  $c_P = 2100 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$  and  $L = 334 \text{ kJ kg}^{-1}$  the same values as in Tsai and Ruan (2018), which result from a present-day calibration, namely, and we set  $k/h = 4024 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$ ,  $H_p = 10 \text{ m}$ ; and  $h = 2 \text{ m}$  in our setup. The required input  
 235 is the air surface temperature  $T_a$  at  $h = 2 \text{ m}$ , which is an MITgcm output. Tsai and Ruan (2018) showed good agreement with observations, along with a significant improvement in capturing early-season melting compared to the classical PDD method. During each model iteration, we compute the **SMBsurface mass balance** by including a lapse rate correction that accounts for changes in surface elevation (see Sec. 2.4.3).

To determine the remaining contribution to the **SMBsurface mass balance**, we evaluate the accumulation of snow. This quan-  
 240 tity is obtained by using outputs from the MITgcm. To be consistent with the energy budget in the MITgcm, the accumulation is estimated from the snow precipitation per grid cell. Since the MITgcm land module does not include accurate snow physics and, in particular, a process that densifies snow over time to obtain glacial ice, this densification is assumed to happen instanta-

neously. Therefore, as snow precipitation is expressed in units of  $[\text{kg m}^{-2} \text{s}^{-1}]$ , we divide this quantity directly by the glacial ice density,  $\rho_i = 920 \text{ kg m}^{-3}$  to obtain the accumulation rate in  $[\text{m s}^{-1}]$ .

245 In summary, two MITgcm outputs are needed: the surface air temperature (for the ablation) and the snow precipitation (for the accumulation). These two quantities are extracted from a simulation that has reached a steady state. We take daily outputs over an interval of 30 years, and then we take the average of these quantities for each day and each grid cell. Finally, the **SMB surface mass balance rate  $\dot{A}$**  is obtained by subtracting the ablation from the accumulation rates, and inserted at the right-hand side of Eq. (4), which is then solved in terms of the ice thickness  $H$ .

### 250 2.4.3 Isostatic, lapse-rate, freshwater and sea-level corrections

Taking into account the isostatic ~~correction~~ **adjustment** due to the ice sheet mass can be computed in several ways. Here, we adopt the Local Lithosphere Relaxing Asthenosphere (LLRA) method, where a time delay is included (Greve and Blatter, 2009). The idea behind this method is that there is a **vertical displacement  $w_{ss}$  (measured in meters)** of the lithosphere ~~in the  $z$  direction by  $w_{ss}$ , which~~ **that** is due to the ice load. A steady state is reached when the buoyancy force equilibrates the ice load (Greve and Blatter, 2009):

$$\rho_a g w_{ss} = \rho_i g \Delta H_{\text{ice}} \quad (8)$$

where  $\rho_i = 920 \text{ kg m}^{-3}$  is the ice density,  $\rho_a = 3300 \text{ kg m}^{-3}$  is the density of the asthenosphere and  $\Delta H_{\text{ice}}$  is the ice thickness calculated by the ice sheet model. Thus

$$w_{ss} = \frac{\rho_i}{\rho_a} \Delta H_{\text{ice}} \quad (9)$$

260 However, the response of the asthenosphere is not immediate due to its viscous properties, and has a time delay that can be parameterised as:

$$\frac{dw}{dt} = -\frac{1}{\tau_a} (w - w_{ss}) \quad (10)$$

where  $\tau_a$  is typically set to 3000 years (Greve and Blatter, 2009). At the end of each iteration  $\Delta t$  of *MITgcmIS*, the ice sheet elevation is computed as:

$$265 \quad H_{\text{total}} = H_{\text{topo}} + \Delta H_{\text{ice}} - \frac{dw}{dt} \Delta t \quad (11)$$

where  $H_{\text{topo}}$  is given by the topography file.

As the surface elevation is varied when an ice sheet develops by  $\Delta z$ , not only the topography changes but also the SAT. Thus, a correction needs to be included by estimating the lapse rate  $dT/dz$ , as follows:

$$T_{\text{new}} = T_{\text{old}} - \frac{dT}{dz} \Delta z \quad (12)$$

270 **where  $T_{\text{new}}$  is the temperature after the lapse rate correction.** ~~where  $T$~~  The lapse rate is computed at each ice-sheet grid point using the MITgcm output of the ~~first~~ **previous run. A temperature value is extracted from each pressure level in the atmosphere,**

and then, based on the corresponding altitude, the slope of the linear regression (zonally averaged) is used to estimate the lapse rate.

275 Finally, since some new ice sheets formed or disappeared, the amount of water that has been exchanged with the ocean is estimated. For each iteration the freshwater flux to or from the ocean is computed and included at restart at the ocean boundary of the ice sheet. To guarantee the conservation of salt, a compensation is performed at the global scale, as it is done in AMOC North Atlantic hosing experiments (Jackson et al., 2023). The variation of water volume in the ocean is converted in sea level change, with updated coastlines defining new topography (including ice sheet height), mask and bathymetry files.

## 2.5 Runoff - *pysheds*

280 In our study, we need to consider different continental configurations corresponding to the Earth’s evolution, under a range of ice sheet loading. Hence, for each new configuration, we need to recalculate the runoff map. The MITgcm needs as an input a file with three arrays, specifying for each land point  $L_i$  the corresponding precipitation storage area  $A_i$  and the ocean point  $O_i$  where it is drained (outlet point).

285 For present-day as well as for past (palæo-) topographies, we discriminate between land and ocean points by defining a contour line at 0 m in elevation. If any area with negative values are fully enclosed within area with positive values, they are considered as ‘lakes’ unless elevation reaches values below  $-2000$  m. In such cases, we re-assign the elevation in order to remove the depression and reroute the flow direction. For this purpose, as well as for cleaning local pits, depressions and flat terrains are corrected using the `fill_pits`, `fill_depressions`, and `resolve_flats` functions from *pysheds* (Bartos, 2020). This ensures a continuous Digital Elevation Model (DEM) with no single pixel or stagnant areas where water would not flow. Finally, we  
290 clip the DEM to all elevations above 0 m and retrieve the closest outlet point.

Every point in the MITgcm grid is hence defined as ‘continental’ or ‘oceanic’ depending on whether or not it is located inside the land (positive elevation) or not. Using the corrected topography, we generate a flow direction by applying an eight-direction (D8) flow routing algorithm from *pysheds*. This method assumes that water from each cell in the DEM will flow to one of its eight neighboring cells, the one that results in the steepest descent. The D8 algorithm is computationally efficient and widely  
295 used for hydrological modelling.

The slope from a cell  $c$  to each of its eight neighbors  $i$  is calculated as:

$$s_i = \frac{Z_c - Z_i}{d_i} \quad (13)$$

where  $Z_c$  is the elevation at the center cell,  $Z_i$  is the elevation of the  $i^{\text{th}}$  neighbor, and  $d_i$  is the distance to that neighbor. For cardinal directions (N, E, S, W),  $d_i = 1$ , and for diagonal directions (NE, SE, SW, NW),  $d_i = \sqrt{2}$ .

300 Then, the flow direction is determined by selecting the neighbor with the maximum positive slope:

$$\text{flow\_dir} = \arg \max_i (s_i), \quad \text{where } s_i > 0 \quad (14)$$

The resulting direction is encoded using a directional mapping:

$$[N, NE, E, SE, S, SW, W, NW] = [64, 128, 1, 2, 4, 8, 16, 32]$$

Each cell is assigned one of these values in the resulting flow direction map, indicating the direction water would flow from that cell based on the steepest slope. We then trace the flow path for every continental point using the flow direction until we reach the ocean, and define the nearest oceanic point as its outlet. Each initial continental point ultimately is being assigned one oceanic outlet, while initial oceanic points are their own outlet. Note that this approach mimicking the drainage system is a great improvement regarding the water cycle relative to many climate models where the outlet of a drop of water is merely assigned to the closest ocean point **different from grid schemes used in CMIP6 models (Hou et al., 2023)**.

Moreover, since the MITgcm has no proper online ice sheet model, excess water that would accumulate to form ice sheets is instead evacuated via runoff. More precisely, in the MITgcm code, snow precipitation  $P_{\text{snow}}$  exceeding the tolerated limit (usually set to 10 m) is automatically redirected into the ocean via the runoff. This creates an artificial excess of runoff in our asynchronous coupling, where  $P_{\text{snow}}$  is now used in the **SMB surface mass balance** accumulation term, and hence a correction is necessary **in the first steps of the coupling procedure**. Thus, we introduce the following correction in the precipitation storage area  $A_i$  at each land point:

$$A'_i = A_i \left( 1 - \frac{P_{\text{snow}}^i}{P_{\text{tot}}^i + P_{\text{snow}}^i} \right) \quad (15)$$

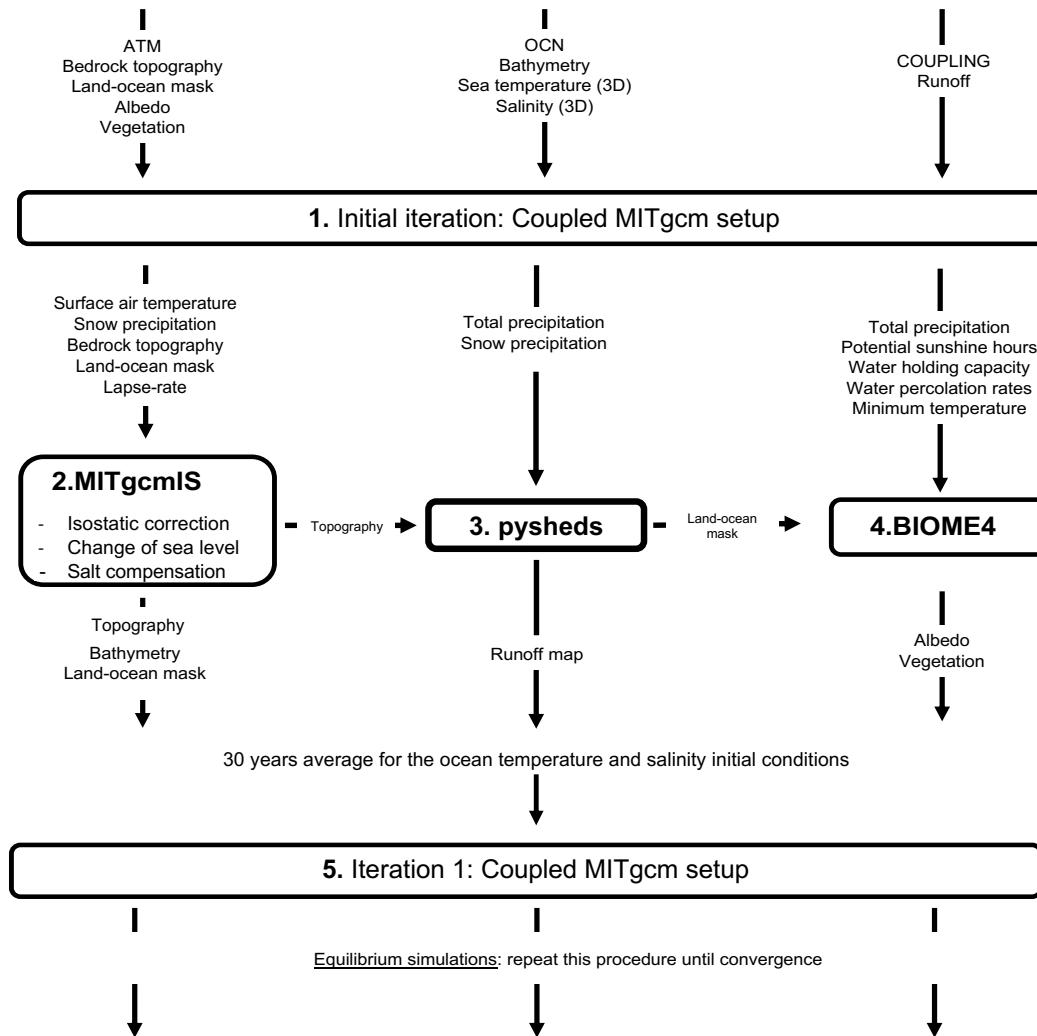
where  $P_{\text{tot}}^i$  is the total rain precipitation at the land point  $i$  and  $P_{\text{snow}}^i \leq P_{\text{tot}}^i$ . This correction has an effect only on land points where the ice sheet is developing.

## 2.6 Coupling framework

Offline coupling between the Coupled MITgcm atmosphere-ocean-sea ice-land Setup and BIOME4 has been already successfully applied in Ragon et al. (2024, 2025). Here, we will document the comprehensive framework that includes BIOME4, the new ice sheet module *MITgcmIS* and the runoff map calculation for different boundary conditions (present-day, paleo or idealised configurations), as schematically illustrated in Fig. 1.

A first simulation is run until the Coupled MITgcm Setup has reached a steady state, defined by having a surface energy balance  $F_s < 0.2 \text{ W/m}^2$  (usually several thousands of simulated years are required). Afterwards, **two simulations additional 30 yr are run** with different output frequencies are run, one with monthly frequency (for **the variables required by BIOME4**) and the other with daily frequency (for **the variables required by MITgcmIS**).

At this point, the offline coupling workflow can start. Before running the ice sheet model, the following corrections are required. For representing an advancing ice flow over shallow ocean, we mimic this process as follows: if the sea ice thickness is equal to the ocean depth, the ocean point becomes a land point and hence the ice sheet can develop on it (up to  $-20 \text{ m}$  of depth). Then, the corrected topography file is given as an input to the ice-sheet model, together with daily MITgcm outputs per grid cell for SAT and snow precipitation, which are used for calculating ablation and accumulation rates, respectively. *MITgcmIS* is run for an equivalent of 40-100 thousand years, **during which the isostatic adjustment is calculated and the lapse rate from the previous convergence step is used**, until the ice sheet reaches a steady state (MacAyeal, 1997). **The isostatic, lapse rate and S**sea level corrections **and salt compensation** (Sec. 2.4.3) are included at this stage, giving rise to new topography (including ice sheet height), mask and bathymetry files. Afterwards, *pysheds* is applied using **these files in input the mask and**



**Figure 1.** Schematic representation of the ~~offline~~ asynchronous coupling framework.

335 the topography, closing lakes and small passages if necessary, and giving in output a new runoff map and giving a new runoff map as output.

Finally, the vegetation model is run based on the new files. The outputs needed from MITgcm and the ice-sheet model (namely, precipitation, SAT (corrected by the lapse rate) and sunshine) are converted on a latitude/longitude grid and then given to the BIOME4 model. The equilibrium biome distribution is converted in new files for vegetation fraction and surface  
 340 albedo using the values reported in Haywood et al. (2010). Due to the coordinate change, some land and ocean points can be inverted on the CS grid. Hence, a vegetation fraction equal to 0 and an albedo value equal to the default water value of 0.07 are assigned to new ocean points on the CS grid, while the value of the closest land point is assigned to new land points.

Before running a second iteration, the pickup files that are used to restart a MITgcm simulation need to be updated to the new values of SAT (including the lapse-rate correction) salinity and sea temperature at all ocean levels are averaged over the last 30 yr to generate new input files for the Coupled MITgcm Setup. Then, the new pickup files these files, along with the new vegetation fraction, albedo, topography, bathymetry, runoff and mask files, are given back to the MITgcm to run the whole coupling process at least twice, so that the GCM has time to adjust to the new input files. Convergence is considered achieved when less than 10% of the land points experience a change in biome distribution and total ice sheet volume. Moreover, the Coupled MITgcm simulation needs to have a surface energy imbalance  $F_s < 0.2 \text{ W m}^{-2}$ , corresponding to extremely low drifts in both the global ocean temperature and the surface air temperature. The whole procedure forms the coupled *biogeodyn-MITgcmIS* model, which thus describes in a consistent way the climatic steady state the evolution of all the climatic variables, including those components with a slow response, like deep-ocean dynamics, vegetation and ice sheets.

### 3 Results

#### 3.1 Validation procedure

##### 3.1.1 *biogeodyn-MITgcmIS* initial conditions

To start the first run of our simulations, it is necessary to provide initial conditions that are representative of the present-day climate. The three-dimensional distributions of sea potential temperature and salinity are derived from the Levitus World Ocean Atlas (Levitus, 1982). Orbital forcing is prescribed at present-day values, with a solar constant of  $1368.13654 \text{ W m}^{-2}$  and obliquity of  $23.45^\circ$ . Topography (including ice sheets and glaciers), bathymetry and the corresponding files are taken from the ETOPO2 dataset (ETOPO2, 2006) with a resolution of 2 arcminutes. Annual mean values of bare-surface albedos (in the absence of snow or sea ice) and fraction of land-surface covered by vegetation are the same as those used in Molteni (2003) and derived from the ERA dataset. A smoothing procedure is applied to convert these maps to the resolution of the MITgcm CS32 grid.

In order to assess the ability of *MITgcmIS* to correctly generate the ice sheets, we need to provide an input map of land elevation in the absence of ice. Such This map was generated using the BedMachine dataset that is part of the MEASUREs program of NASA (Morlighem, 2022; Morlighem et al., 2022), with the addition of an isostatic correction as in Paxman et al. (2022) for Antarctica and Greenland. The BedMachine dataset provides a density-corrected satellite-based DEM of the ice sheet surface, as well as a data-constrained estimate of bedrock elevation and a mask for identifying the different parts of the ice sheets. There are two separate products for Antarctica (Morlighem, 2022) and Greenland (Morlighem et al., 2022), respectively. The surface elevation of the ice sheets are used to assess the performance of *MITgcmIS*, while bedrock elevations with isostatic adjustment are used as initial boundary conditions, as shown in Fig. 2. For both, we apply the same smoothing procedure as for ETOPO2, taking into account the different resolutions. The resulting isostatic map is shown in Fig. 2 on the CS32 grid. Note that, regarding paleoclimate simulations, PANALEISIS or other reconstructions directly provide bedrock elevations.

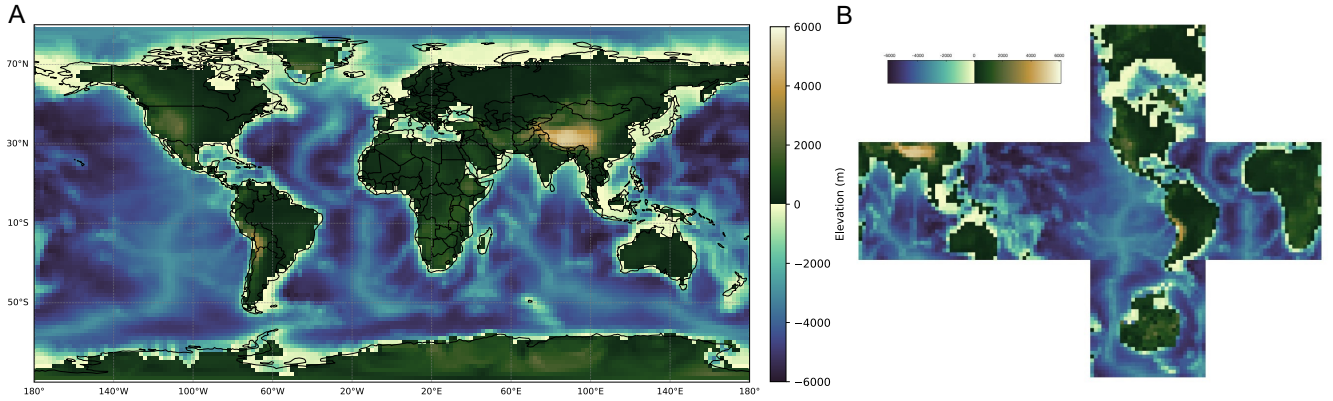
375 Finally, it is important to also describe the tuning procedure. In order to obtain pre-industrial conditions at 280 ppm, once all the albedo values for vegetation cover, snow and ice have been fixed, we tune the relative humidity threshold for the formation of low clouds (a parameter denoted as  $RHCL2$  in SPEEDY) so that the average global SAT becomes approximately equal to the observed value of  $13.7^{\circ}\text{C}$  (NOAA National Centers for Environmental Information, 2024). The adjusted value,  $\cancel{RHCL2}=0.808RHCL2=0.7727$ , is applied to all simulations. Moreover, ~~the pre-industrial run was used to determine~~  
380 the coefficient  $a$  in Glen's law, which in our simulations is assumed to be constant (see eq. (2)) and governs the ice sheet formation, ~~is determined as follows. This value has been set to  $a=1.2\cdot 10^{-15}\text{ Pa}^{-3}\text{ s}^{-1}$  and its justification based on the SMB surface mass balance of Antarctica can be found in Sec. 3.2.4.~~

Evaluating the surface mass balance produced for Antarctica in our setup is necessary to calibrate the Glen's law parameter using the total ice sheet volume. The reason is that the volume is strongly sensitive to both the net surface mass balance and the  
385 Glen's law coefficient; without a good estimate of the surface mass balance, the correct volume can be achieved for the wrong reasons. The surface mass balance of Antarctica is estimated by the Coupled MITgcm Setup started from the present-day ice sheets (ETOPO2), and turns out to be approximately  $1500\text{ Gt yr}^{-1}$ . This value can be compared with the ensemble mean obtained from a comparison of Regional Climate Models (RCMs) in Mottram et al. (2021). In that study, the ensemble mean over the grounded ice sheet is estimated at  $2073\pm 306\text{ Gt/yr}^{-1}$ . Although the value obtained in our simulation is slightly lower  
390 than this ensemble mean, as well as lower than the values obtained by all individual models in that comparison, it is important to consider that the spatial smoothing applied to obtain  $2.8^{\circ}$  resolution in our simulations implies a different representation of the Antarctic continent compared to models with higher resolutions (25-50 km). Additionally, there are known limitations in the representation of snow processes in the land module, as discussed in Sec. 2.4. Therefore, even if our value is slightly lower than those obtained from RCMs, it remains within the same order of magnitude. Using this value for the surface mass  
395 balance, we apply our ice sheet model *MITgcmIS* (which always starts from the bedrock and isostatic adjusted topography) with a range of  $a$  values. This yields different Antarctic volumes (Table A1), while maintaining a similar surface elevation profile. We selected  $a=0.6\cdot 10^{-15}\text{ Pa}^{-3}\text{ s}^{-1}$  as a compromise, as it produces a volume within 10% of the observed value and surface elevations consistent with observations.

### 3.1.2 Comparison with data and CMIP models

400 To assess the performance of our climate framework, we run two simulations. The first one, denoted as run1, is the pre-industrial simulation at 280 ppm. This simulation will be assessed against two CMIP6 models, as there is a lack of observational data for this period. The second simulation (run2), which corresponds to the 1979-2009 period which has with an average  $\text{CO}_2$  concentration of 360 ppm (Lan et al., 2025), is started from the run1 steady state by applying a constant increase of  $\text{CO}_2$  of 1 ppm/yr for 80 yr and keeping the ice sheet fixed. This run will be is evaluated against the reanalysis and observational data.

405 More specifically, for assessing the pre-industrial run at 280 ppm, we use the output data from the IPSL-CM6A-LR model (Boucher et al., 2018) and the NorESM2-LM model (Seland et al., 2020) using the *piControl* dataset (Eyring et al., 2016). We chose these two CMIP models because they include dynamical vegetation. For the second run at 360 ppm, we compare our data with the following datasets: ERA5 (Hersbach et al., 2023) for the atmosphere, OSRA5 (Copernicus Climate Change



**Figure 2.** Initial conditions given to MITgcm on the cubed-sphere CS32 grid with (A) the mask file and (B) the **b**Bedrock topography (with isostatic adjustment) and bathymetry used as initial boundary conditions in run1 on the latitude-longitude grid (A) and on the cubed-sphere grid (B).

**Table 1.** Models description: module names with corresponding number of vertical levels or type of coupling.

	<i>biogeodyn-MITgcmIS</i>	Levels/type	IPSL-CM6A-LR	Level/type	NorESM2-LM	Level/type
Resolution	2.8 °	NA	1.6°	NA	2°	NA
Land	LAND	2	ORCHIDEE	11	CLM5	15
Atmosphere	SPEEDY	5	LMDZ6A-LR	79	CESM2.1-CAM6	7
Ocean	MITgcm	25	NEMO-OPA	75	BLOM	75
Ice sheet	<i>MITgcmIS</i>	offlineasynchronous	NA	NA	NA	NA
Vegetation	BIOME4	offlineasynchronous	ORCHIDEE	online	CLM5	online
Sea ice	THSICE	online	NEMO-LIM3	online	CICE	online

Service, 2021) for ocean diagnostics, MODIS for the vegetation, BedMachine for the surface elevation of Greenland and  
 410 Antarctica (Morlighem et al., 2022; Morlighem, 2022), RAPID observations for the **Atlantic Meridional Overturning Circulation** (AMOC) profile (Moat et al., 2025), and the Sea Ice index for the sea ice extent (Fetterer et al., 2002).

Two **Five** iterations of the procedure illustrated in Fig. 1 were necessary to reach convergence **in run1**. Convergence is considered achieved when less than 10% of the land points experience a change in biome distribution and total ice sheet volume. Moreover, the Coupled MITgcm simulation needs to have a surface energy imbalance  $F_s < 0.2 \text{ W m}^{-2}$ , corresponding  
 415 to extremely low drifts in both the global ocean temperature and the SAT. The last 30 years of the second run **fifth iteration** are used for diagnostics. To be consistent in comparisons, all diagnostics are converted to the same longitude-latitude coordinate system with a spatial resolution of  $2^\circ \times 2^\circ$ .

The outputs were treated using Matlab version 2023b and the figures were made using python. The MITgcm took approximately one **1500 simulated years per** week to reach equilibrium using 25 processors **for each iteration**. BIOME4 and *pysheds*

**Table 2.** Global annual mean values averaged over the last 30 years, and associated standard deviations derived from interannual variability. The acronyms in the table are: surface air temperature (SAT), top-of-the-atmosphere budget ( $R_t$ ), ocean surface budget ( $F_s$ ), northern hemisphere (NH), southern hemisphere (SH), evaporation minus precipitation (E - P), sea surface temperature (SST) and sea surface salinity (SSS).

	Pre-industrial conditions			1979 - 2009 conditions	
	IPSL-CM6A-LR	NorESM2-LM	<i>biogeodyn-MITgcmIS</i>	ERA5/OSRA5	<i>biogeodyn-MITgcmIS</i>
	1850–1880	1850–1880	run1: 280 ppm	1979–2009	run2: transient 360 ppm
SAT (°C)	12.8±0.1	14.4±0.1	13.78±0.08	14.2±0.2	15.9±0.3
$R_t$ (W m <sup>-2</sup> )	0.8±0.6	0.0±0.3	-0.5±0.1	0.4±0.6	0.9±0.2
$F_s$ (W m <sup>-2</sup> )	1.3±0.2	0.6±0.5	0.0±0.2	7±2	2.48±0.37
NH sea ice extent (10 <sup>6</sup> km <sup>2</sup> )	12.7±0.6	11.0±0.1	9.2±0.1	9.385±0.001	7.5±0.3
SH sea ice extent (10 <sup>6</sup> km <sup>2</sup> )	13.4±0.6	6.9±0.5	22.6±0.5	8.732±0.001	15.8±0.7
$E - P$ (10 <sup>-8</sup> kg m <sup>-2</sup> s <sup>-1</sup> )	-7±2	-3±2	0±2	0.08±0.01	0±2
SST (°C)	16.29±0.06	17.84±0.08	17.31±0.03	17.6±0.1	18.3±0.2
SSS (psu)	34.37±0.05	32.189±0.008	36.242±0.005	34.36±0.03	36.235±0.009

420 run in less than 5 minutes on a desktop computer. *MITgcmIS* needs 5 hours around 1 hour of CPU time due to the daily stepping of the ODEs in eqs. (6)-(7) for all land points.

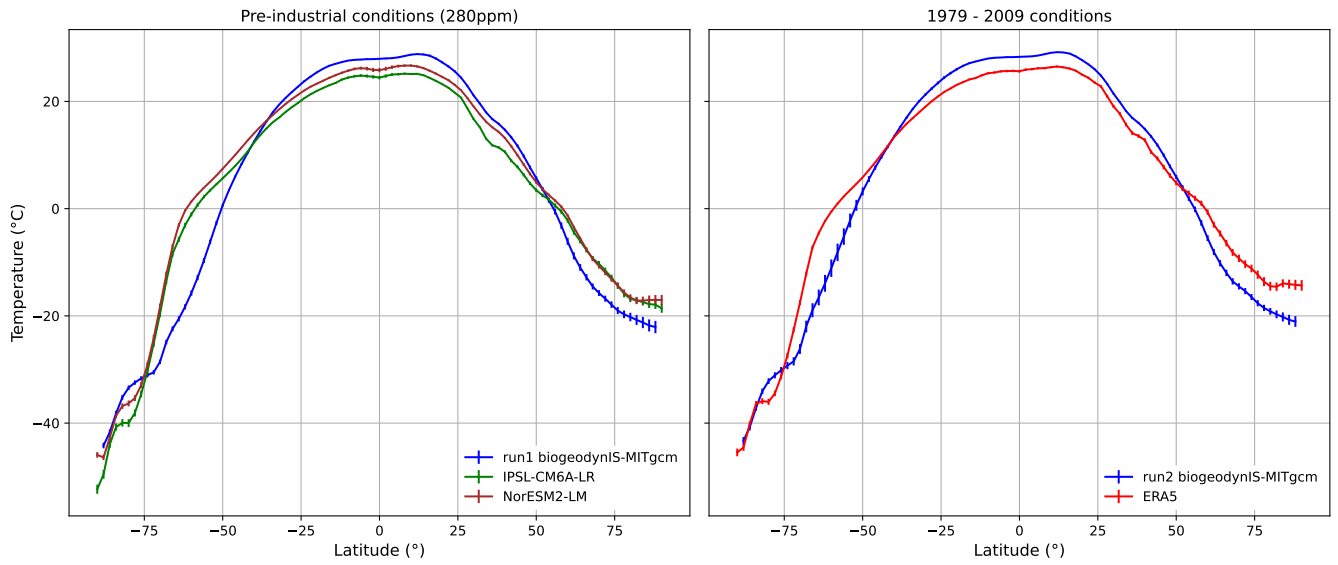
### 3.2 *biogeodyn-MITgcmIS* evaluation

To evaluate if our coupling setup correctly reproduces the modern Earth climate, we examined several diagnostics of the dynamical behavior of atmosphere, ocean, vegetation and cryosphere.

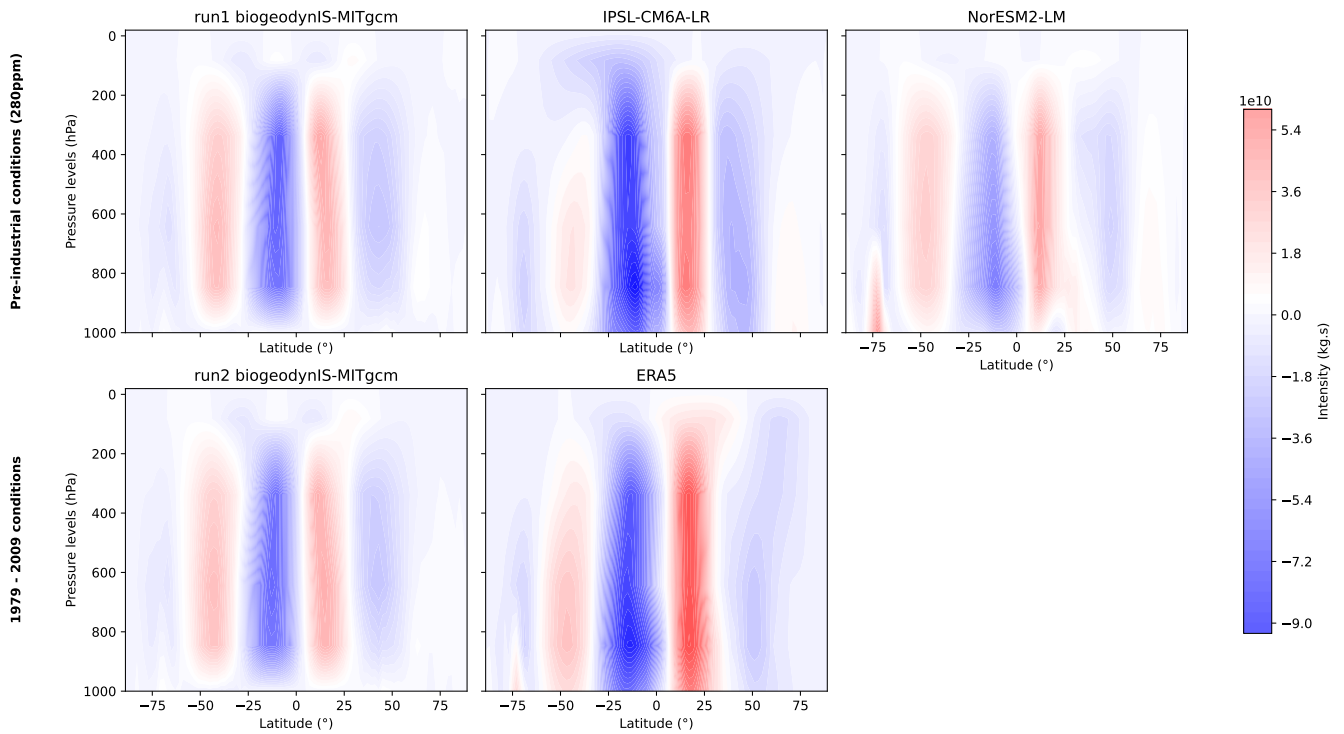
#### 425 3.2.1 Atmosphere

In Table 2 global mean values of the relevant variables, calculated from the last 30 simulated years, are listed, together with the reanalysis data and the climatology values from the two CMIP models. The global mean SAT of 13.92 13.78 °C in run1 is intermediate between the two CMIP values, and close to the real data of 13.7 °C (NOAA National Centers for Environmental Information, 2024) because of our tuning procedure. However, the global mean SAT of 16.39 15.9 °C in run2 is larger than  
430 the ERA5 value. This depends on the Earth Climate Sensitivity (ECS), which is 5.4°C in our model This corresponds to an Earth System Sensitivity (ESS) of 6.8°C, which is in the range of values obtained by other CMIP-class models, from 3 to 10 °C (Haywood et al., 2020). Excluding the ice sheet formation, the MITgem coupled setup gives an Equilibrium Climate Sensitivity of approximately 4 °C, i.e., in the highest range of CMIP6 values (Nijssse et al., 2020; Zelinka et al., 2020).

More in detail, if we look at the SAT zonal profile as shown in Fig. 3, we can make common remarks for the two runs  
435 concerning the polar regions. The overall behaviour is well reproduced in our simulations, except the temperature at the south



**Figure 3.** Zonal annual mean surface air temperature for the two *biogeodyn-MITgcmIS* simulations, CMIP models and ERA5.



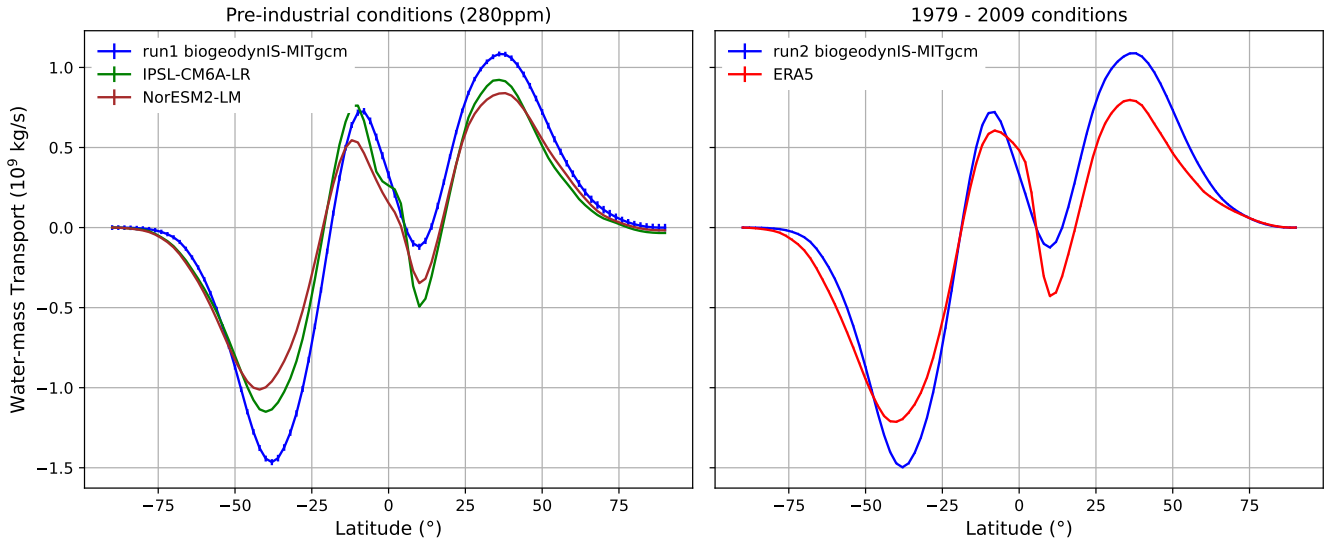
**Figure 4.** Atmospheric overturning cells for the two *biogeodyn-MITgcmIS* simulations, CMIP models and ERA5.

polar region around 60S, which is around 10°C higher lower in *biogeodyn-MITgcmIS* compared to the CMIP6 models and the ERA5 values, as also shown in Fig. A1. This is due to the southern hemisphere sea ice extent, which is higher than in CMIP models and observations, probably because our setup does not include dynamical but only thermodynamical effects. Fig. A1 also shows that SAT over ice sheets is higher than in CMIP models and observations. The difference in the north polar region is mainly located in Greenland. This can be due to the coarser resolution of the Coupled MITgcm coupled Setup (2.8°), which underestimates the elevation of Antarctica and Greenland, hence giving higher temperatures than observations and CMIP models, where the ice sheet elevation is fixed to observed values.

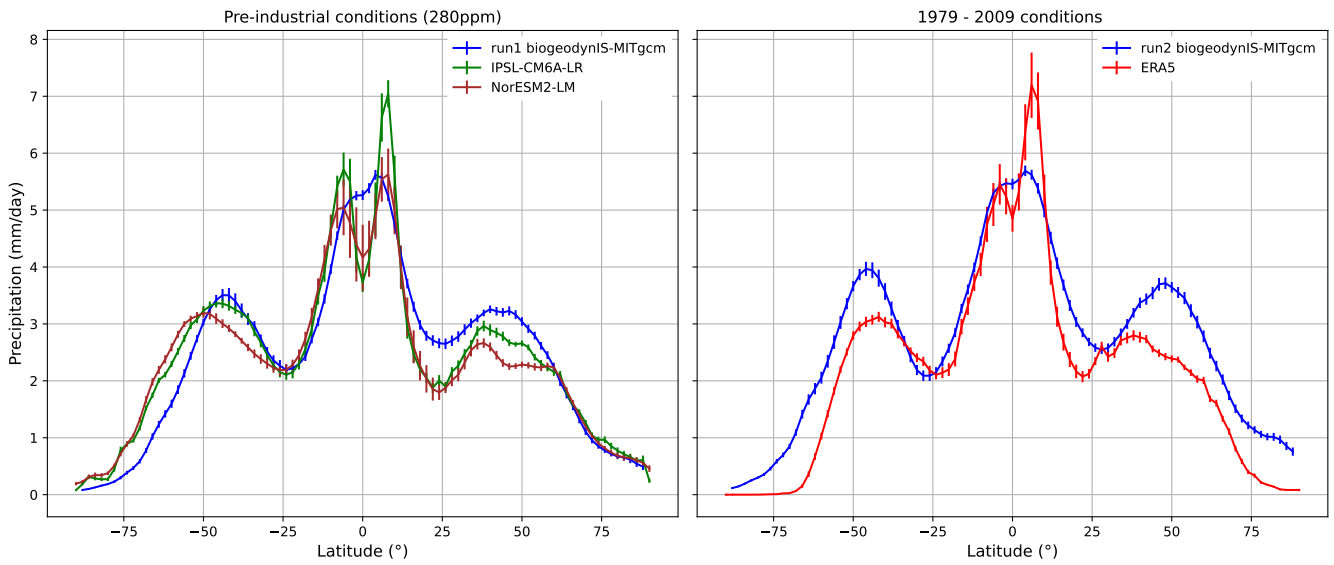
Another important feature to be checked regarding the atmosphere dynamics is the model capability to correctly reproduce the Hadley cells, as shown in Fig. 4. The comparison is shown in Figure 4. In run2, our model gives rise to a weaker positive overturning cell near the Equator, as also seen by Ruggieri et al. (2024) where the 8-layer SPEEDY module is coupled with the NEMO ocean. However, from run1 we see that the positive overturning cells reconstructed by NorESM2-LM are similarly weak, despite a number of vertical layers in the atmosphere that is larger than the 5 layers in SPEEDY-MITgcm. In run1, SPEEDY gives cells with similar extent as the IPSL-CM6A-LR model, which has a state-of-the-art atmospheric module with 75 levels, while there is an additional positive south polar cell in the NorESM2-LM model. The lower branch of the positive Hadley cell is less intense than that in IPSL-CM6A-LR and ERA5. This feature has direct consequences on southward transport of water mass in the tropics, as shown in Fig. 5, which in our setup is indeed weaker than observations and CMIP models. In contrast, the transport towards the southern polar region turns out to be larger in our simulations due to the comparatively intense Ferrel cell in the southern hemisphere. In addition, the mean zonal wind in our simulations, shown in Fig. A2, agrees with ERA5 and NorESM2-LM the two CMIP models, with a slightly lower intensity of the jet stream in the northern hemisphere. Despite these limitations, it is important to note that the total water mass  $E - P$  shows only a small imbalance in our simulations with respect to the control runs of the two CMIP models, as reported in Table 2.

As we can see in Fig. 6, while the precipitation peak at the ITCZ is correctly reproduced in our simulations, at a mean latitude of approximately 6°N (Marshall et al., 2014) that corresponds to the ascending branch of the Hadley cells, the precipitation intensity at ITCZ is underestimated due to weak Hadley overturning cells. In addition, our simulations do not capture the decrease in precipitation intensity at the Equator, as also observed in Ruggieri et al. (2024). The precipitation is in general overestimated in *biogeodyn-MITgcmIS* with respect to observations in subtropics and the extratropics, with peaks occurring at higher latitudes. However, the SPEEDY module captures the overall precipitation pattern in both runs (see Fig. A3), with localised maximum anomalies of around 5 mm/day in the equatorial region.

The heat transport at TOA in Fig. 7 shows that *biogeodyn-MITgcmIS* closely follows the overall pattern in both runs, except for a slightly stronger southward total heat transport at approximately 40°S and 40°N. Across the Equator, the atmospheric heat transport (dotted lines) is southward in our simulations and in ERA5, correctly compensating for the northward ocean heat transport driven by the AMOC, as described in Marshall et al. (2014). In contrast, the CMIP models do not show this compensation across the Equator despite their finer vertical resolution in the atmosphere, as can be seen in the inset of Fig. 7. Moreover, as shown in Table 2, the energy budget  $R_t$  at the top of the atmosphere (TOA) is almost closed in *biogeodyn-MITgcm* run1 and within the range of CMIP models (Lembo et al., 2019). In run2, the TOA imbalance increases due to forcing

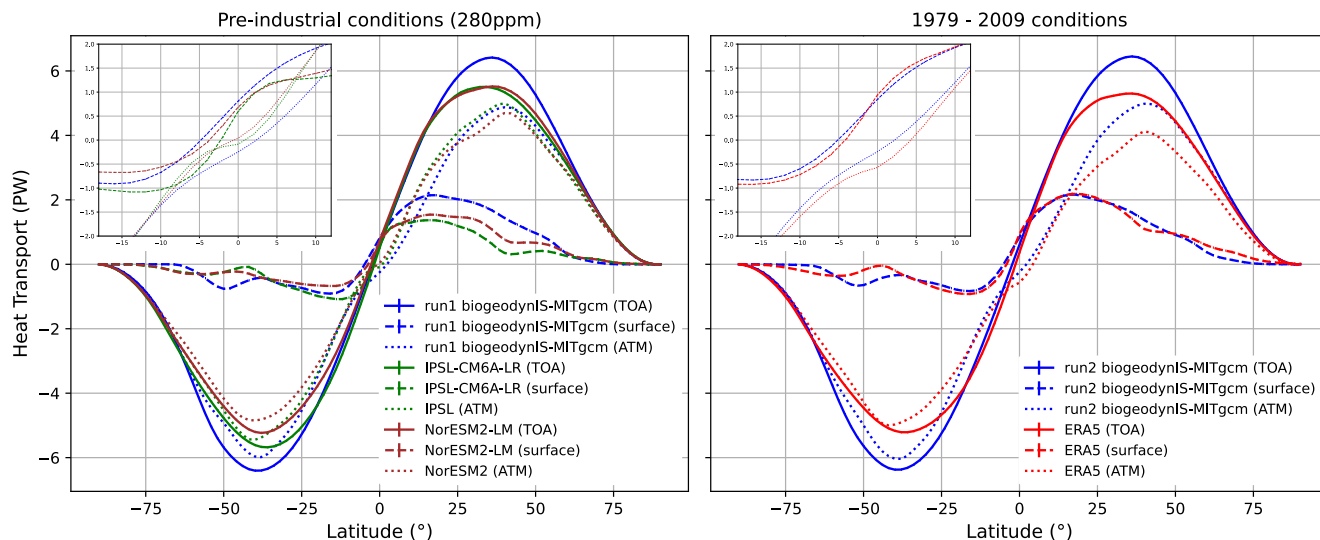


**Figure 5.** Northward water-mass transport in the atmosphere for the two *biogeodyn-MITgcmIS* simulations, CMIP models and ERA5. Data are plotted using the Carissimo correction (Carissimo et al., 1985).



**Figure 6.** Zonal annual mean precipitation in mm/day for the two *biogeodyn-MITgcmIS* simulations, CMIP models and ERA5.

conditions. The *biogeodyn-MITgcmIS* coupled system has not a closed energy budget  $R_t$  at the top of the atmosphere (TOA), as shown in Table 2. This is mainly due to the fact that the energy used for ice sheet growth is not included in this diagnostics. As further confirmation, during the first MITgcm iteration before running the ice sheet model,  $R_t$  is indeed comparable to the



**Figure 7.** Northward heat transport at the top of the atmosphere (solid lines) and at the ocean surface (dashed lines). Their difference gives the heat transport in the atmosphere (dotted lines). The insets show a zoom of the tropical region.

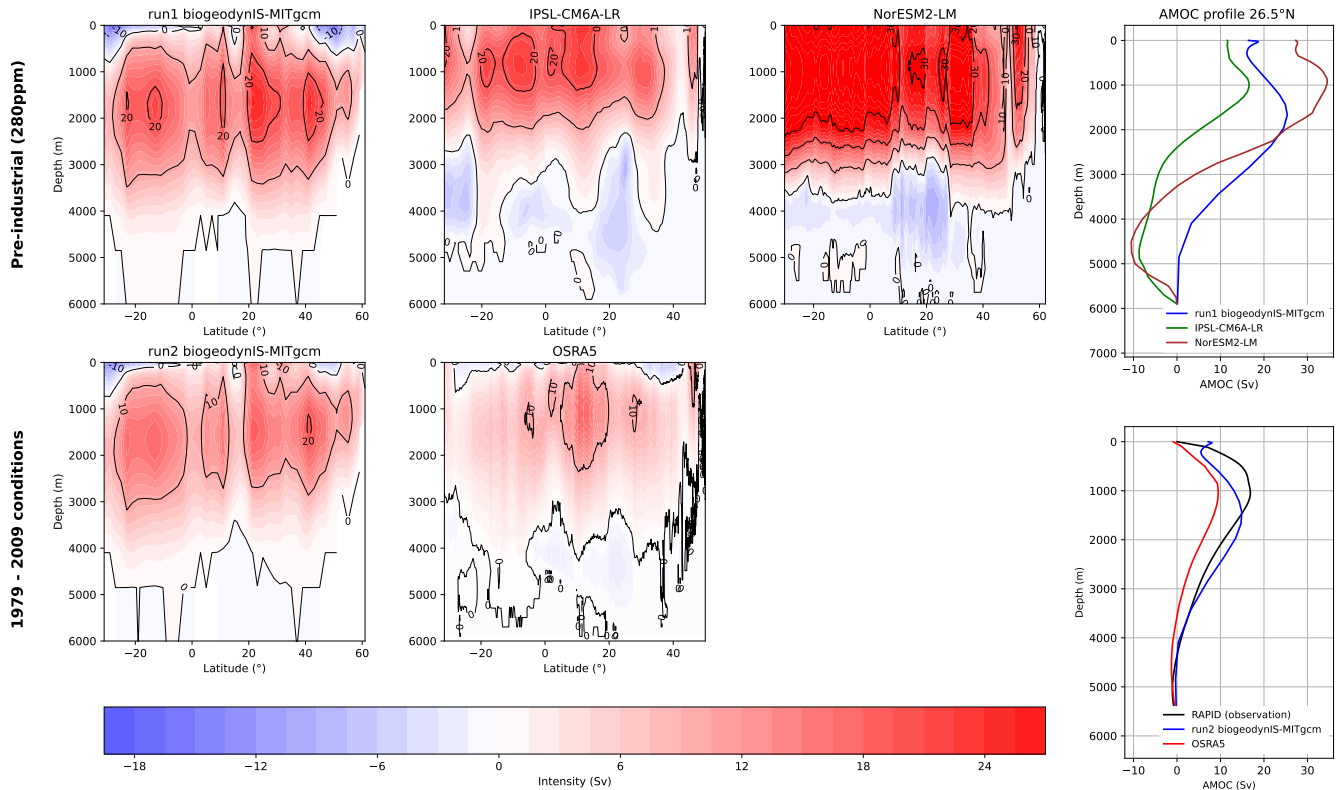
values obtained by the CMIP models and ERA5 (see also other present-day simulations performed with the MITgcm coupled setup in Brunetti and V  rard (2018)).

### 3.2.2 Ocean

In order to assess the capacity of *biogeodyn-MITgcmIS* to correctly represent the ocean dynamics, we looked at the sea surface temperature (SST) and salinity (SSS), the sea ice extent, the water-mass budget, the AMOC profile and the heat transport at the surface.

As shown in Table 2, SST in *run1* of *biogeodyn-MITgcmIS* *run1* simulations is in between the two CMIP models, whereas it is higher than in OSRA5 being consistent with SAT. Sea ice extent in our *run1* simulation is lower in the northern hemisphere (NH) than in the southern hemisphere (SH), in contrast to NorESM2-LM results. Note that the NorESM2-LM model simulates a pre-industrial climate with less SH sea ice (with an extent of  $6.9 \cdot 10^6$  km<sup>2</sup>) compared to ERA5 (with approximately  $8.7 \cdot 10^6$  km<sup>2</sup>), even though ERA5 reflects a climate state with a higher atmospheric CO<sub>2</sub> content.

For *run2*, the values of sea ice extent in *biogeodyn-MITgcmIS* are differ from those in ERA5 (lower in the northern hemisphere and higher in the southern hemisphere), due to the starting values obtained in the pre-industrial run. However, lower than those in ERA5, especially in the southern hemisphere, due to higher surface temperatures. We observe that the sea ice extent obtained in our simulations, which is shown in Fig. A4, is in good agreement with that in Ruggieri et al. (2024), obtained with SPEEDY-NEMO for the period 1979-2014.



**Figure 8.** AMOC intensity for the two *biogeodyn-MITgcmIS* simulations, CMIP models and OSRA5. The vertical profile at  $26.5^{\circ}\text{N}$  of the AMOC is added on the right with the addition of the RAPID observations.

490 Our two simulations show a reduction in **the** sea ice extent with increasing atmospheric  $\text{CO}_2$  concentrations, ~~along with a~~  
 consistent decrease in salinity due to enhanced water dilution. The total extent of sea ice in our run1 simulation is larger than  
 in NorESM2-LM, which explains a higher value of salt concentration. It is comparable to that of IPSL-CM6A-LR, which,  
 however, shows an imbalance in the water budget of  $E - P = -7 \cdot 10^{-8} \text{ kg m}^{-2} \text{ s}^{-1}$  and a slightly lower value of salinity.

The ocean heat transport (OHT) in Fig. 7 (dashed lines) shows a larger amount of heat towards the northern polar region  
 495 compared to CMIP models, explaining why our setup produces less sea ice there. The bulk of the OHT is dominated by the  
 Ekman transport in the subtropical gyres. As mentioned before, the AMOC effect is to increase heat transport across the Equator  
 (Marshall et al., 2014), which is of around 0.7 PW in all models. It is important to note that the surface energy imbalance  
 $F_s$  of **run1** in our simulations is very low ( $|F_s| \leq 0.1 \text{ W/m}^2$ , see Table 2), because **it is they are** run close to equilibrium. In  
 contrast,  $F_s = 2.48 \text{ W/m}^2$  in **run2** and ~~the observations give~~  $F_s = 7 \text{ W/m}^2$  in **the observations**, reflecting forced conditions.  
 500 Although they represent control runs, the two CMIP simulations exhibit values larger than  $0.1 \text{ W/m}^2$ , indicating that they are  
 not fully equilibrated.

As shown in Fig. 8, the AMOC produced by our coupled setup for run1 has a clockwise (positive) overturning cell with intensity comparable to the cell obtained by IPSL-CM6A-LR, which however develops at lower depths. The positive overturning cell in NorESM2-LM has a higher intensity than both *biogeodyn-MITgcmIS* and IPSL-CM6A-LR. For run2, the AMOC intensity produced by OSRA5 exhibits a maximum at the Tropics, while in our coupled setup there are several regions of high intensity. In both, there is a weak anticlockwise (negative) overturning cell at depths higher than 4 km. Right panels in Fig. 8 show vertical profiles at 26.5°N of the AMOC streamfunction. The two blue curves correspond to the *biogeodyn-MITgcmIS* simulations and show that there is a decrease in the intensity of the AMOC positive cell as the CO<sub>2</sub> concentration increases. This behavior is expected (Caesar et al., 2018) and demonstrates the ability of *biogeodyn-MITgcmIS* to produce consistent results. It is important to note that the two CMIP models exhibit strong negative values around 4500 m that are not appearing in the observations. A similar pattern is also observed in another class of CMIP models described in Valdes et al. (2017), even in present-day simulations. However, *biogeodyn-MITgcmIS* shows the maximum of the positive cell around 1500 m, whereas it should be around 1000 m according to the RAPID measurements. This discrepancy may be related to the fact that the MITgcm ocean module includes only 25 vertical levels, compared to 75 in the two CMIP models.

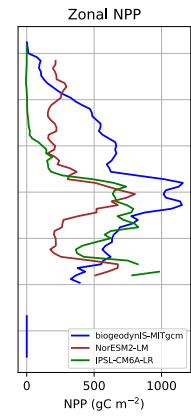
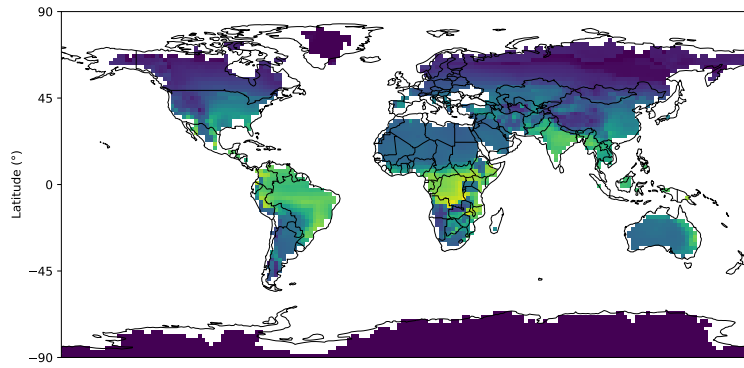
### 515 3.2.3 Vegetation

In this section, we evaluate the capacity of the coupled system to correctly reproduce the present-day vegetation and to assess its performance against models with dynamical vegetation.

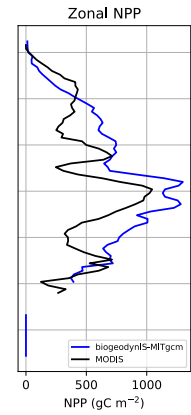
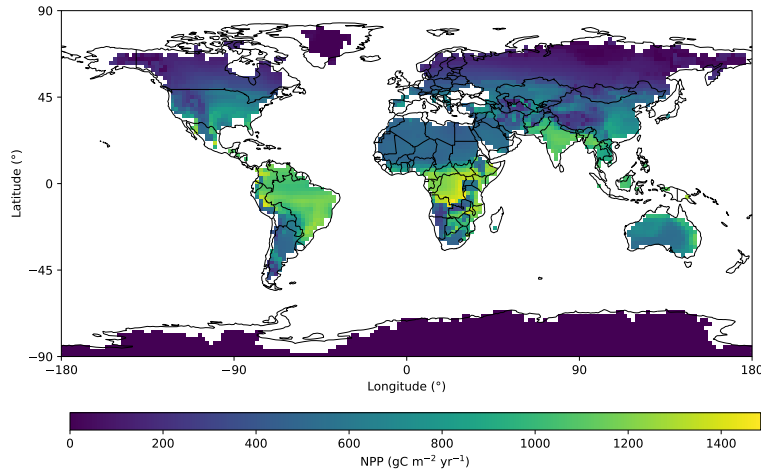
As shown in Fig. 9C, the *biogeodyn-MITgcmIS* simulations run2 gives rise to a good representation of the major biomes. They both Run2 displays the boreal forest, which, following the biome classification used in Kaplan et al. (2003) and Haywood et al. (2010), corresponds to cool mixed forests, evergreen and deciduous taiga (see the legend at the bottom of in Fig. 9C). They It also displays the Amazon rainforest by returning the tropical evergreen forest biome, which has a larger extent for higher CO<sub>2</sub> values. Both simulations include and the desert biome, whose extent reduces with increased atmospheric CO<sub>2</sub> content (Norby et al., 2005), although the latter is smaller than expected in observations. This is directly linked to the excess of precipitation produced by the SPEEDY module at these latitudes (Fig. 6) in North Africa (Fig. A3). Major differences between run1 and run2 are the emergence of tropical savanna in South America and Africa in run2, the loss in run2 of shrub tundra at high latitudes, which has been replaced by deciduous taiga, temperate grassland or montane forest. In Greenland, run2 shows an increase in cushion forb and lichen, and the appearance of prostrate shrub tundra, which was not present in run1. Run2 shows an expansion of temperate grassland across North America and Russia.

Maps and The zonal profiles of the Net Primary Production (NPP) distribution for run1 and run2 are shown in the right panels of Fig. 9A,B. The zonal profiles are compared to those of CMIP models and the MODIS dataset. Our simulations reproduce the general pattern by correctly displaying an increase in the equatorial region. However, they fail to capture the decrease at 10° and -25° latitude, as shown by MODIS. It is important to note that there is a difference in NPP intensity between run1 and run2. This is mainly explained by the increase of CO<sub>2</sub> concentration, precipitation and temperature, as shown in Figs. 3 and 6. The two CMIP models show different behaviors. NorESM2-LM captures quite well the decrease at 10° and -25°, as well as the increase in the equatorial region, despite lower intensities than MODIS. IPSL-CM6A-LR does not show vegetation at

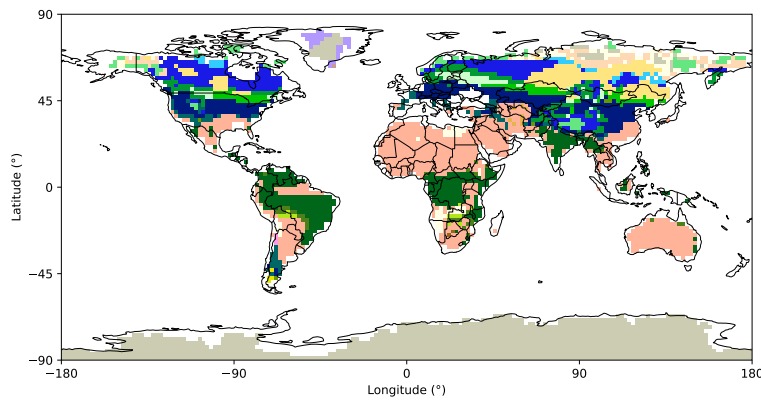
**A run1: pre-industrial conditions (280ppm)**



**B run2: 1979 - 2009 conditions**

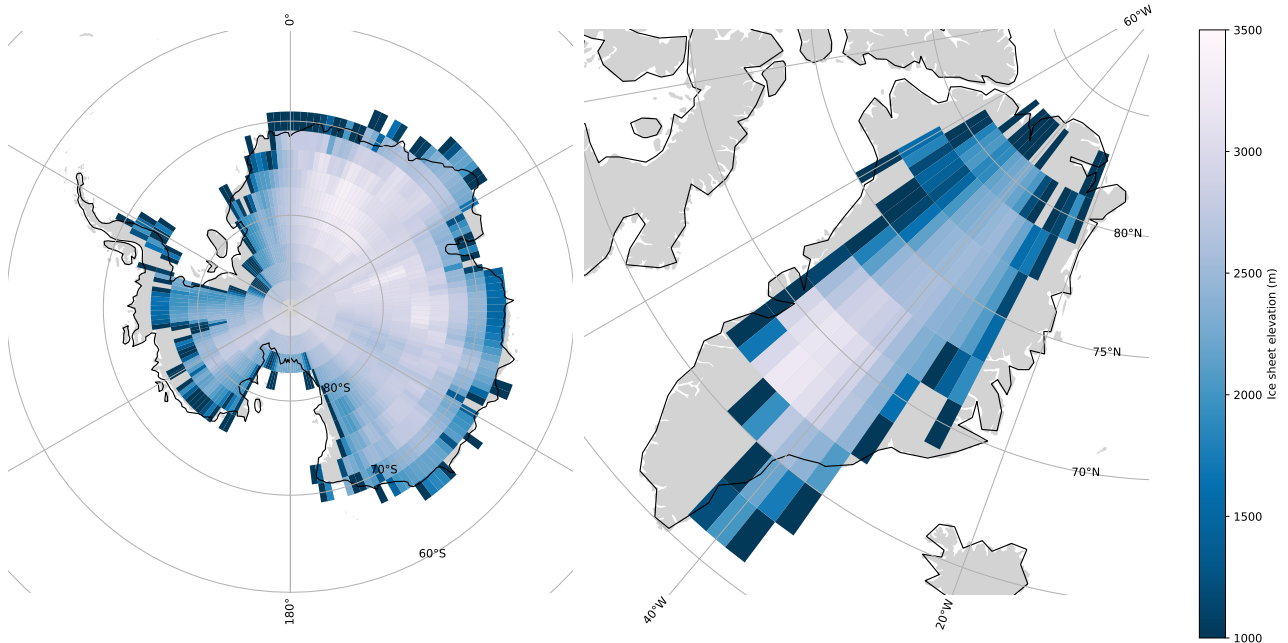


**C**



- 1: tropical evergreen forest
- 2: tropical semi-deciduous forest
- 3: tropical deciduous forest/woodland
- 4: temperate deciduous forest
- 5: temperate conifer forest
- 6: warm-temperate mixed forest
- 7: cool mixed forest
- 8: cool conifer forest
- 9: cold mixed forest
- 10: evergreen taiga/montane forest
- 11: deciduous taiga/montane forest
- 12: tropical savanna
- 13: tropical xerophytic shrubland
- 14: temperate xerophytic shrubland
- 15: temperate sclerophyll woodland
- 16: temperate broad-leaved savanna
- 17: open conifer woodland
- 18: boreal parkland
- 19: tropical grassland
- 20: temperate grassland
- 21: desert
- 22: steppe tundra
- 23: shrub tundra
- 24: dwarf-shrub tundra
- 25: prostrate shrub tundra
- 26: cushion-forb, lichen
- 27: barren (soil)
- 28: inundated.

**Figure 9.** NPP distribution for *biogeodyn-MITgcmIS* run1 (A) and run2 (B) (left panels), and zonal NPP profile (right panels) for all models and the MODIS dataset; C. Biomes distribution in *biogeodyn-MITgcmIS* run2.



**Figure 10.** Map of the region where ice sheets form with *biogeodyn-MITgcmIS*, showing ESPG:3031 and ESPG:3413 projections for Antarctica and Greenland, respectively.

latitudes higher than 25°N, as ORCHIDEE does not include high-latitude biomes such as tundra (Dinh et al., 2024). The two dynamical vegetation models do not capture all the trends in the NPP pattern, even with more sophisticated land modules than the one used in our setup. This is confirmed by the correlation analysis shown in Fig. A5. the Pearson correlation coefficient and slope values obtained in our two simulations and the two CMIP models when assessed against the MODIS observations, as shown in Fig. A5. Both *biogeodyn-MITgcmIS* runs are evaluated against MODIS due to the lack of observational data in the pre-industrial era. For both runs of our setup, the correlation coefficient  $r$  is close to 0.8 and the slope values are close to 1 one when the results of run2 are plotted against MODIS, confirming a broad agreement with observations. with an increase in slope in run2. In contrast, The correlations of the results of run1 against the two CMIP models are around 0.6. exhibit lower slope values, and IPSL-CM6A-LR also shows a lower  $r$  value. This emphasizes that, even without online dynamical vegetation, our setup successfully captures global-scale vegetation features and remains consistent with different climate conditions.

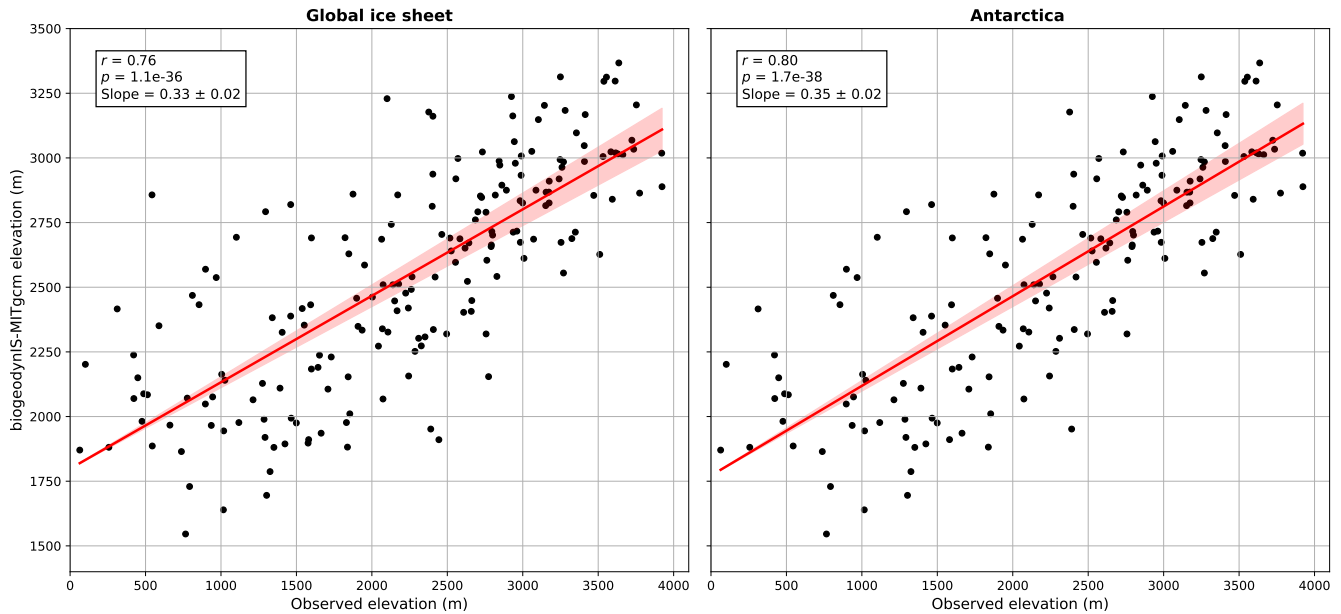
### 3.2.4 Ice sheet

The performance of *MITgcmIS* is evaluated against present-day observations using the BedMachine datasets. Since there are no observational data available for the pre-industrial period, and the two CMIP models do not include dynamical ice sheets, both *biogeodyn-MITgcmIS* simulations are run 1 is assessed using the same set of present-day observations. We also compared the resulting climate in run1 with that obtained by starting from fixed present-day ice sheets (from ETOPO2) and same vegetation,

and found that the resulting climatic attractors are essentially the same, with very small differences in terms of temperature and precipitation, as shown in Fig. A6, demonstrating the ability of our procedure to reconstruct first-order processes in ice sheets. As mentioned in Sec. 3.1.1, evaluating the SMB produced for Antarctica is a prerequisite to calibrate the Glen's law parameter using the total ice sheet volume in our setup. The reason is that the volume is strongly sensitive to both net SMB and the Glen's law coefficient; without a good estimate of SMB, the correct volume can be achieved for the wrong reasons. Thus, we calibrated the Glen's law parameter based on the first iteration of run1. To this end, we tested a range of  $\alpha$  values that yield different Antarctic volumes (Tab. A1), while maintaining a similar surface elevation profile. We selected  $\alpha = 1.2 \cdot 10^{-15} \text{ Pa}^{-3} \text{ s}^{-1}$  as a compromise, as it produces a volume within 10% of the observed value and surface elevations consistent with observations. For the simulation at 280 ppm (run1), we obtained a SMB of approximately  $1500 \text{ Gt yr}^{-1}$ . This SMB value can be compared with the ensemble mean of SMB values for Antarctica obtained from a comparison of Regional Climate Models (RCMs) in Mottram et al. (2021). In that study, the ensemble mean over the grounded ice sheet is estimated at  $2073 \pm 306 \text{ Gt/yr}^{-1}$ . Although the value obtained in our simulation is slightly lower than the ensemble mean reported in Mottram et al. (2021), as well as lower than the values obtained by all individual models in that comparison, it is important to consider that the spatial smoothing applied to obtain  $2.8^\circ$  resolution in our simulations implies a different representation of the Antarctic continent compared to models with higher resolutions (25-50 km). Additionally, there are known simplifications in the description of the ice sheet in *MITgcmIS*, as discussed in Sec. 2.4, and limitations in the representation of snow processes in the land module. Therefore, even if our value is slightly lower than those obtained from RCMs, it remains within the same order of magnitude.

The ice sheets obtained in both runs **run1** are shown in Fig. 10. The Antarctica ice sheet does not change significantly from one run to the other, in both height and extent. However, the Greenland ice sheet decreases strongly in height and extent when the  $\text{CO}_2$  content increases. A The total volume of is  $24.5 \cdot 10^6 \text{ km}^3$ , of which  $22.0 \cdot 10^6 \text{ km}^3$  in Antarctica and  $2.5 \cdot 10^6 \text{ km}^3$  in Greenland. is formed in run1 compared to  $22.5 \cdot 10^6 \text{ km}^3$  in run2 (Tab. ??). For Antarctica, there is a difference of 6% for run1 and 8% for run2 compared to the observed volume (after smoothing to the same spatial resolution) of  $22.9 \cdot 10^6 \text{ km}^3$ . Hence, in both runs in **run1** the ice sheet volume is of the same order as the observed volume ( $22.9 \cdot 10^6 \text{ km}^3$ , after smoothing to the same spatial resolution) (Morlighem et al., 2022; Morlighem, 2022). as the observations, with a decrease in run2 that corresponds to a total freshwater flux in 145 years of approximately 0.37 Sv, with a rate in Greenland of  $1.6 \cdot 10^{-3} \text{ Sv yr}^{-1}$ , and nearly two times smaller in Antarctica. These values are much smaller than those typically used in hosing experiments (e.g.,  $0.1\text{-}0.5 \text{ Sv yr}^{-1}$  in Jackson et al. (2023)), but they overestimate the melting rates reconstructed by a comprehensive survey in Greenland by one order of magnitude (Mouginot et al., 2019).

This overall agreement with observations (**BedMachine dataset**) is reflected in a statistically significant Pearson correlation coefficients  $r$  of 0.76 and 0.80 for the surface elevation of both ice sheets and Antarctica only 0.84/0.81 in surface elevation between the ice sheets formed in *MITgcmIS* run1/run2 and BedMachine, respectively, as shown in Fig. 11, and detailed for Antarctica in Fig. ???. However, the slope values of 0.33 and 0.35 for both ice sheets and Antarctica only, respectively, are lower than 1.0.44 and 0.39 for run1 and run2, respectively, are lower than 1. This means that the model tends to underestimate the largest ice sheet heights and to overestimate the smallest ones on the edges. This pattern is evident in Fig. A7, particularly in



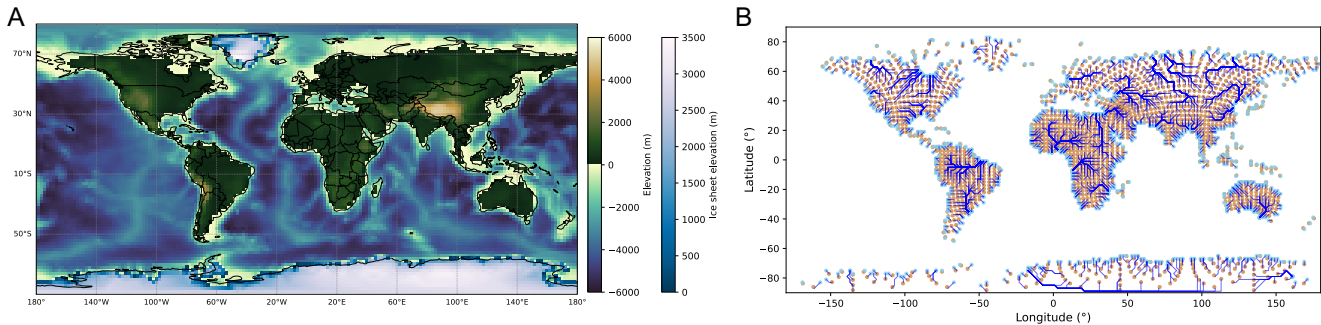
**Figure 11.** Correlations in surface elevation between the ice sheets formed in run1 and BedMachine.

West Antarctica. In contrast, conclusions about Greenland are more uncertain due to the limited pixel coverage. Overall, we observe that Antarctica in *MITgcmIS* agrees more closely with observations than Greenland, which shows a strong sensitivity to an increase of atmospheric  $\text{CO}_2$  content.

If we examine the histograms in the right panels of Fig. A7, we observe that *MITgcmIS* can reproduce both low and high ice sheet elevations over Greenland, albeit for a low number of grid points. For Antarctica, the histograms they support the conclusions discussed above. The excess accumulation in West Antarctica is also reported in Xie et al. (2022), which uses an ice sheet model of similar complexity. In addition, analogous biases in ice thickness are also observed in more sophisticated models, such as in Quiquet et al. (2018), which underestimates the ice thickness in central Antarctica of around 300-400 m. The fact that *MITgcmIS* does not correctly capture the peak of ice sheet elevation in central Antarctica can be attributed to the model's coarse spatial resolution, confirming the role played by spatial resolution in ice sheet models (Rückamp et al., 2020). In addition, it is important to consider uncertainties related to bedrock elevation, isostatic adjustment, and measurements of the ice sheet thickness. Nevertheless, we can conclude that our model reproduces the first-order characteristics of the ice sheets reasonably well, and shows a consistent behavior between run1 and run2.

### 3.2.5 Runoff

The final topography obtained in run1 is shown in Fig. 12A. The topography includes the ice sheets formed by iterating the asynchronous coupling procedure five times (Fig. 1). By applying *pysheds* to this topography, the drainage basins and the corresponding main rivers are identified, resulting in the runoff routing map shown in Fig. 12B. In this way, each land point is



**Figure 12.** A. Topography with ice sheet elevation obtained in run1; B. Runoff routing map for the corresponding topography.

associated with an ocean point corresponding to the relevant river mouth. The main river paths can be clearly recognised, such as the Amazon, Congo, Nile or Yangtze rivers.

### 605 3.3 The Permian-Triassic case

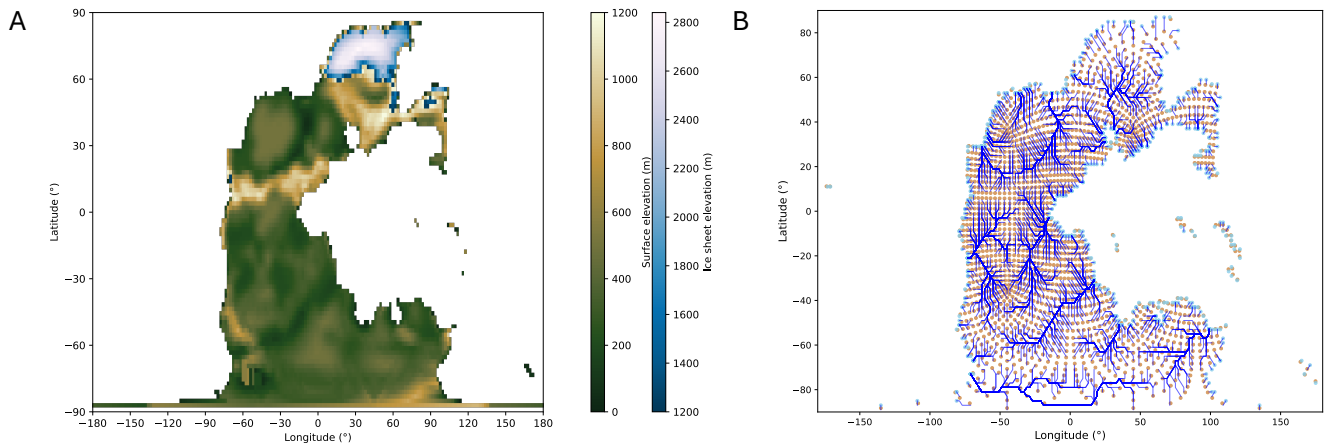
We now demonstrate how the asynchronous procedure can be applied to a very different continental configuration. As an example, we consider the Permian-Triassic bedrock paleogeography as reconstructed by PANALEISIS (Vérard, 2019). Three alternative climatic steady states have been identified for this paleogeography by Ragon et al. (2024), with mean surface air temperatures (SAT) higher than present-day values. However, the so-called cold state, with an average SAT of around 17°C and a meridional overturning circulation characterised by a negative cell (i. e., flowing from north to south at the surface), corresponds to climate conditions where a small ice cap can develop in the Northern Hemisphere. Therefore, we applied our procedure to investigate this possibility.

We find that a small ice cap can indeed develop in the Northern Hemisphere in the cold state, as shown in the resulting topography in Fig. 13A. The associated runoff routing map is also shown in Fig. 13B. Global annual values of the main climatic variables, listed in Table 3, fall within the same range as those reported by Ragon et al. (2024), with slightly lower SAT and higher sea ice extent, indicating that this climatic state can be represented by the same attractor. The ice sheet extends in the north polar region with a volume of 7.8 million km<sup>3</sup>, corresponding to approximately -20 m of sea-level change relative to a climate state without ice sheets, and -65 m relative to the present-day value. Interestingly, this value falls within the range of eustatic variations in the Early Triassic reconstructed by global stratigraphic data (Haq, 2018; Simmons et al., 2020).

Regarding the vegetation cover, the main differences in NPP distribution relative to Ragon et al. (2024) occur at high latitudes, as shown in Fig. 14, due to the southward migration of temperate forests and the disappearance of tundra in regions covered by the ice sheet.

**Table 3.** Global annual mean values averaged over the last 30 years, and associated standard deviations derived from interannual variability. The acronyms in the table are: surface air temperature (SAT), top-of-the-atmosphere budget ( $R_t$ ), ocean surface budget ( $F_s$ ), evaporation minus precipitation ( $E - P$ ), sea surface temperature (SST) and sea surface salinity (SSS).

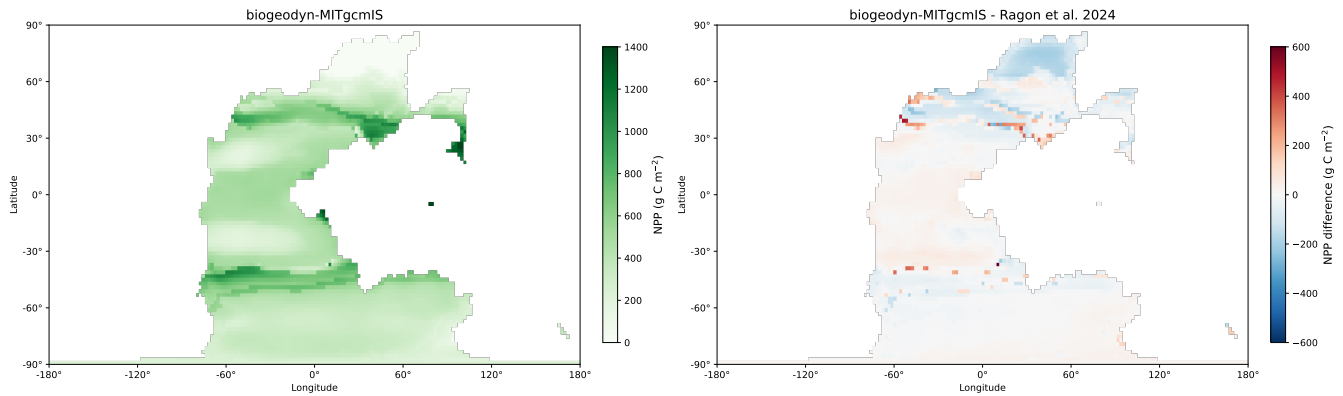
	Ragon et al., 2024	biogeodyn-MITgcmIS
SAT ( $^{\circ}\text{C}$ )	$17.20 \pm 0.09$	$17.06 \pm 0.09$
$R_t$ ( $\text{W m}^{-2}$ )	$-0.3 \pm 0.2$	$-0.3 \pm 0.2$
$F_s$ ( $\text{W m}^{-2}$ )	$0.07 \pm 0.03$	$0.1 \pm 0.2$
Sea ice extent ( $10^6 \text{ km}^2$ )	$34.3 \pm 0.4$	$36.1 \pm 0.3$
$E - P$ ( $10^{-8} \text{ kg m}^{-2} \text{ s}^{-1}$ )	$0 \pm 2$	$0 \pm 1$
SST ( $^{\circ}\text{C}$ )	$21.11 \pm 0.04$	$21.14 \pm 0.05$
SSS (psu)	$38.19 \pm 0.05$	$38.79 \pm 0.02$
Ice sheet volume ( $10^6 \text{ km}^3$ )	–	7.8
Ice sheet extent ( $10^6 \text{ km}^2$ )	–	5.0



**Figure 13.** A. Permian-Triassic topography with ice sheet elevation obtained using *biogeodyn-MITgcmIS* (the bedrock elevation used to start the simulation can be found in Ragon et al., 2024); B. Runoff routing map for the corresponding topography.

### 3.4 Future developments

In this paper, we have described how the implemented offline coupling framework successfully reproduces the large-scale climate and its major components, giving results comparable to those of two CMIP6 models for the pre-industrial climate, and demonstrating its capability to represent deep-time climates. However, further improvements are possible, some of which we discuss below.



**Figure 14.** NPP distribution map obtained with *biogeodyn-MITgcmIS* and the difference with the cold state in Ragon et al. 2024.

The atmospheric module is currently based on a previous version of SPEEDY with five vertical levels, while a newer version with eight levels is now available (Kucharski et al., 2013). This updated version has recently been coupled with the NEMO  
 630 ocean model (Ruggieri et al., 2024), providing a good representation of both climatology and the main modes of internal variability. A further improvement would be to directly implement the offline coupling with BIOME4 on the MITgcm cubed-sphere grid, thereby eliminating interpolation errors, as discussed in Sec. 2.6.

Regarding the ice sheet model, we plan to provide the option of performing both online and offline coupling with the MITgcm dynamical kernel. This upgrade requires an enhancement of the land module within MITgcm. While incorporating a detailed  
 635 land surface scheme, such as the one used in the JULES model (Wiltshire et al., 2020) would constitute a major improvement, we plan to follow a different approach, as only selected processes need to be represented at coarse spatial resolutions. As mentioned in the Methods section, the current two-layer land module in MITgcm lacks representations of processes such as heat conduction in snow, meltwater refreezing and retention, and snow compaction. All of these can significantly affect the ablation and accumulation in the surface mass balance, which is currently underestimated in our simulations. Using  
 640 the open-source snowpack model described in Essery (2015) could be a viable option. In future iterations of *MITgcmIS*, sliding and basal heat balance could easily be implemented – this would allow study of nonlinear processes that occur over continental and millennial scales, such as binge-purge oscillations (MacAyeal, 1993). Furthermore, incorporating a dynamical ice sheet model would lead to a more consistent energy budget across the different model components. However, due to the slow temporal evolution of ice sheets starting from bedrock conditions, a spin-up phase using offline coupling will always be necessary, since  
 645 the Coupled MITgcm Setup cannot be run on timescales of hundreds of thousands of years due to computational costs.

## 4 Conclusions

In summary, the *biogeodyn-MITgcmIS* coupled setup provides a good representation of large-scale features of the present-day climate with reasonably low computational costs. Atmosphere and ocean dynamics broadly agree well with observations,

giving a model performance comparable to CMIP6-class models. Coupling with the BIOME4 vegetation model reproduces the  
650 main biomes, with results similar to those obtained using CMIP6 models with dynamical vegetation. Moreover, the vegetation  
cover obtained with *biogeodyn-MITgcmIS* exhibits coherent behavior under increasing CO<sub>2</sub> concentrations. The ice sheet  
component, *MITgcmIS*, reproduces reasonably well the surface mass balance, as well as the global volume and the thickness  
of Antarctica and Greenland ice sheets, considering its coarse spatial resolution. An upgrade of the land module and the  
development of an online ice sheet module could address some of the limitations of the current version and are planned for  
655 future development.

For now, this new tool, which consistently describes the global-scale coupled dynamics of the ocean, atmosphere, vege-  
tation, and ice over multimillennial timescales with relatively low computational costs, allows for a new range of climate  
investigations. Climatic steady states and their basin boundaries, including the position of tipping points at the global scale  
elements (McKay et al., 2022), like the Atlantic Overturning Meridional Circulation, ice sheets, Amazon rainforest, and sea  
660 ice extent, can be studied with a our modelling framework that allows for the consistent evolution of all these interacting com-  
ponents at the global scale. An additional advantage is that *biogeodyn-MITgcmIS* is adaptable to different modelling setups,  
as each module can be removed if needed. Furthermore, by changing the coupling frequency, both equilibrium and transient  
simulations can be performed. We expect that the proposed model will contribute to the investigation of the climate system on  
Earth, for both present-day and past continental configurations, as well as on idealised scenarios and exoplanet research.

665 *Code and data availability.* The BedMachine data for Antarctica and Greenland can be accessed through the NASA National Snow and  
Ice Data Center at <https://nsidc.org/data/explore-data>. Data for the isostatic correction are available from the U.S. National Science Foun-  
dation Arctic Data Center at <https://arcticdata.io/catalog/view/doi:10.18739/A2280509Z>. The sea ice extent data can be downloaded from  
the National Snow and Ice data Center Sea Ice Index at <https://nsidc.org/data/g02135/versions/3#anchor-data-access-tools>. The MODIS  
TERRA data for the NPP can be obtained at <https://modis.gsfc.nasa.gov/data/dataproduct/>. The RAPID data from the RAPID/MOCHA/WBTS  
670 project are available from <https://rapid.ac.uk/>. CMIP6 model data can be freely downloaded on the ESGF nodes (for example [https://  
esgf-node.ipsl.upmc.fr/search/cmip6](https://esgf-node.ipsl.upmc.fr/search/cmip6)). ERA5 and OSRA5 datasets are accessible via the Copernicus Climate Data Store at the following  
link: <https://cds.climate.copernicus.eu/datasets>. *MITgcm* is open source and archived on <https://github.com/MITgcm/MITgcm>, the vegeta-  
tion model BIOME4 is available from <https://github.com/jedokaplan/BIOME4>, *pysheds* from <https://github.com/mbartos/pysheds>.

The current version of *biogeodyn-MITgcmIS* is available from the project website <https://doi.org/10.5281/zenodo.18723952> under the  
675 license Creative Commons Attribution 4.0 International. The exact version of the model used to produce the results used in this paper  
is archived on <https://doi.org/10.5281/zenodo.18723952> under DOI:10.5281/zenodo.18723952 (Moinat et al., 2025), as are input data and  
scripts to run the model and produce the plots for all the simulations presented in this paper (Moinat et al., 2025).

*Author contributions.* MB planned the study and acquired funding. DNG implemented the main part of the *MITgcmIS* code with support  
from LM. FF and CV implemented the hydrology component. LM ran the simulations with the help of MB, and made the plots. LM and MB  
680 analysed the simulation results. LM, MB and DNG wrote the manuscript. All authors reviewed the paper.

*Competing interests.* The authors declare that they have no conflict of interest.

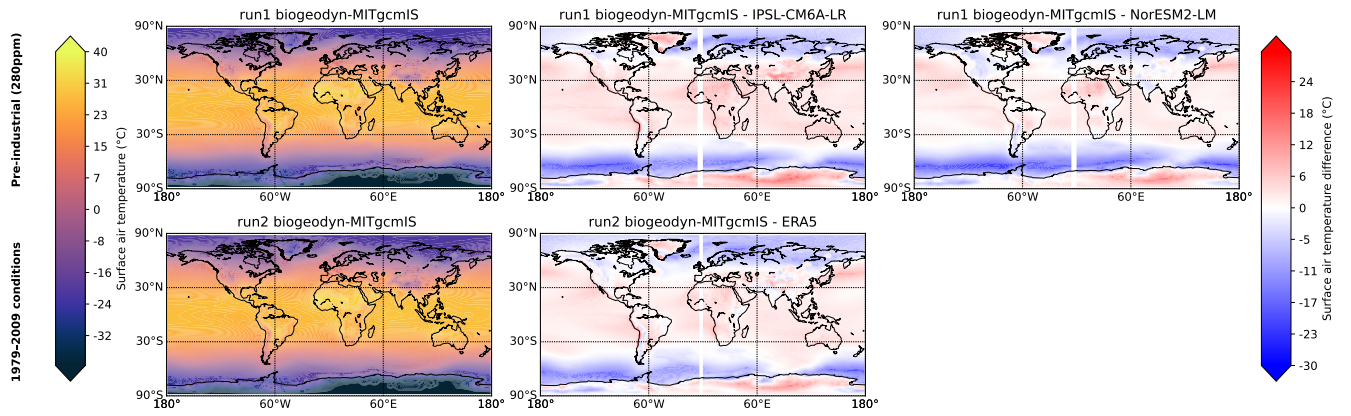
*Acknowledgements.* We are grateful to Jean-Michel Campin for solving an issue with the TOA budget. LM, FF, CV and MB acknowledge the financial support from the Swiss National Science Foundation (Sinergia Project No. CRSII5\_213539), and useful discussions with the Sinergia team. LM, FF, CV and MB thank the pan-EUROpean BIoGeodynamics network (EUROBIG) COST Action (CA23150, <https://www.cost.eu/actions/CA23150>) and, in particular, Taras Gerya for inspiring discussions on biogeodynamics. LM acknowledges the financial support from the EUROBIG COST Action (CA23150). DNG acknowledges support from the Natural Environment Research Council (Project Nos. NE/X005194/1, NE/X01536X/1).

## Appendix A: Appendix A

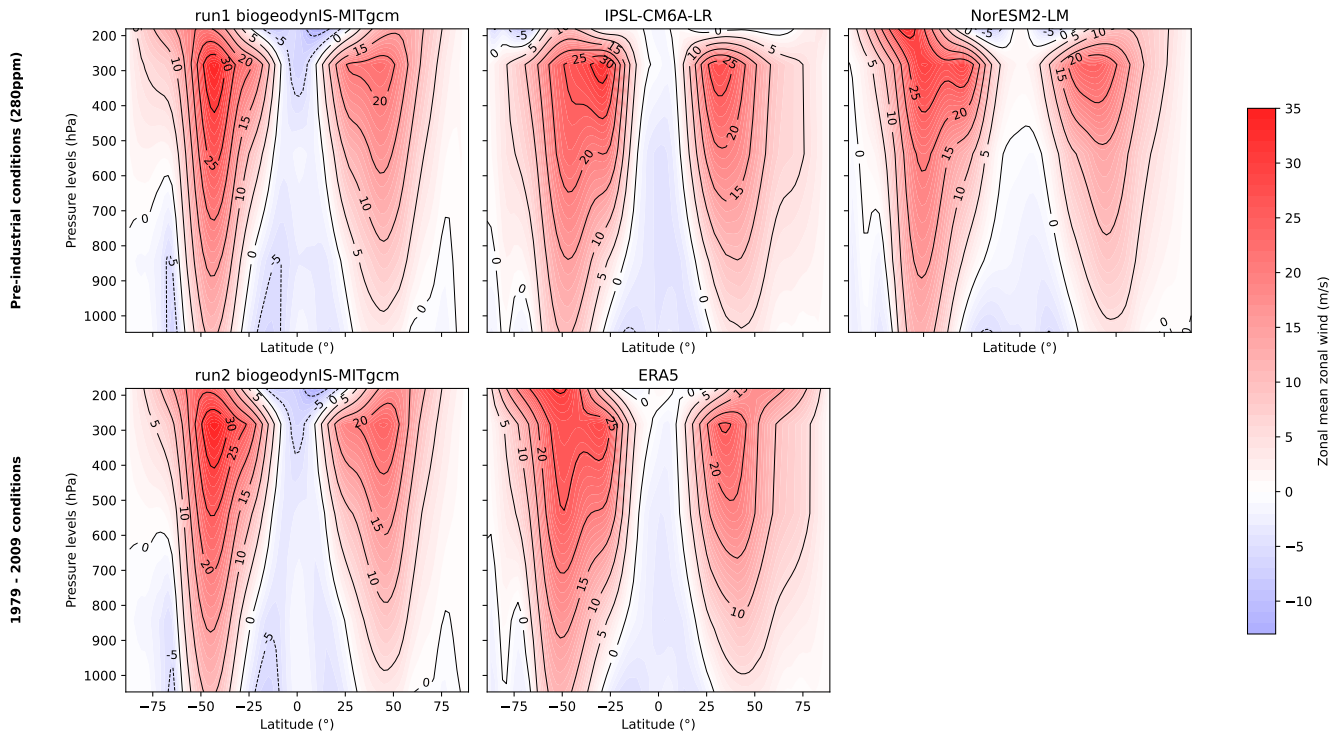
Additional table and figures, mentioned in the main text, are shown in this Appendix.

**Table A1.** Glen's law parameter and corresponding ice sheet volume produced in Antarctica by *MITgcmIS*.

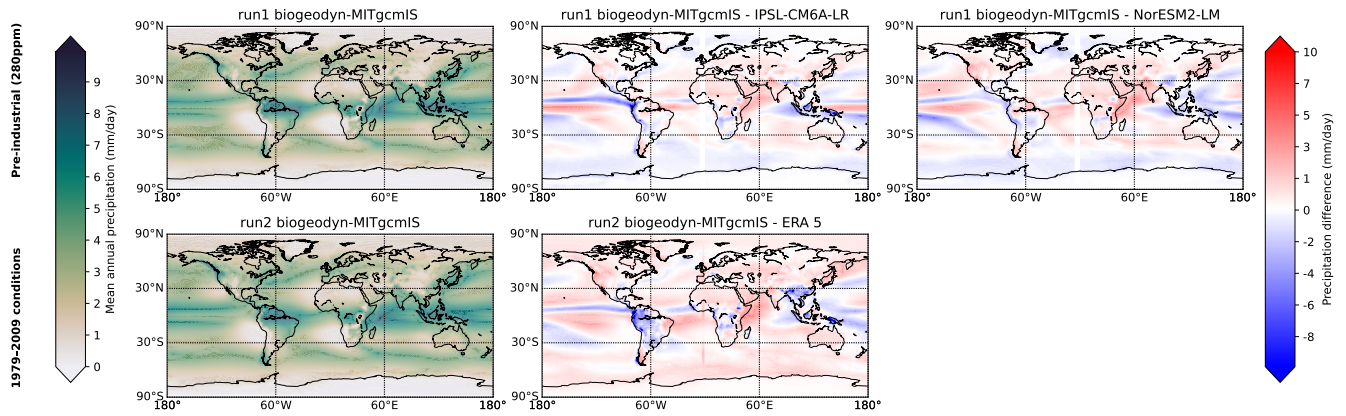
Glen's parameter ( $10^{-15} \text{ Pa}^{-3} \text{ s}^{-1}$ )	Antarctica volume ( $10^6 \text{ km}^3$ )
0.2	23.2
0.4	21.7
0.6	21.0
1.2	19.3
1.7	18.6
2.5	17.8
3.2	17.2



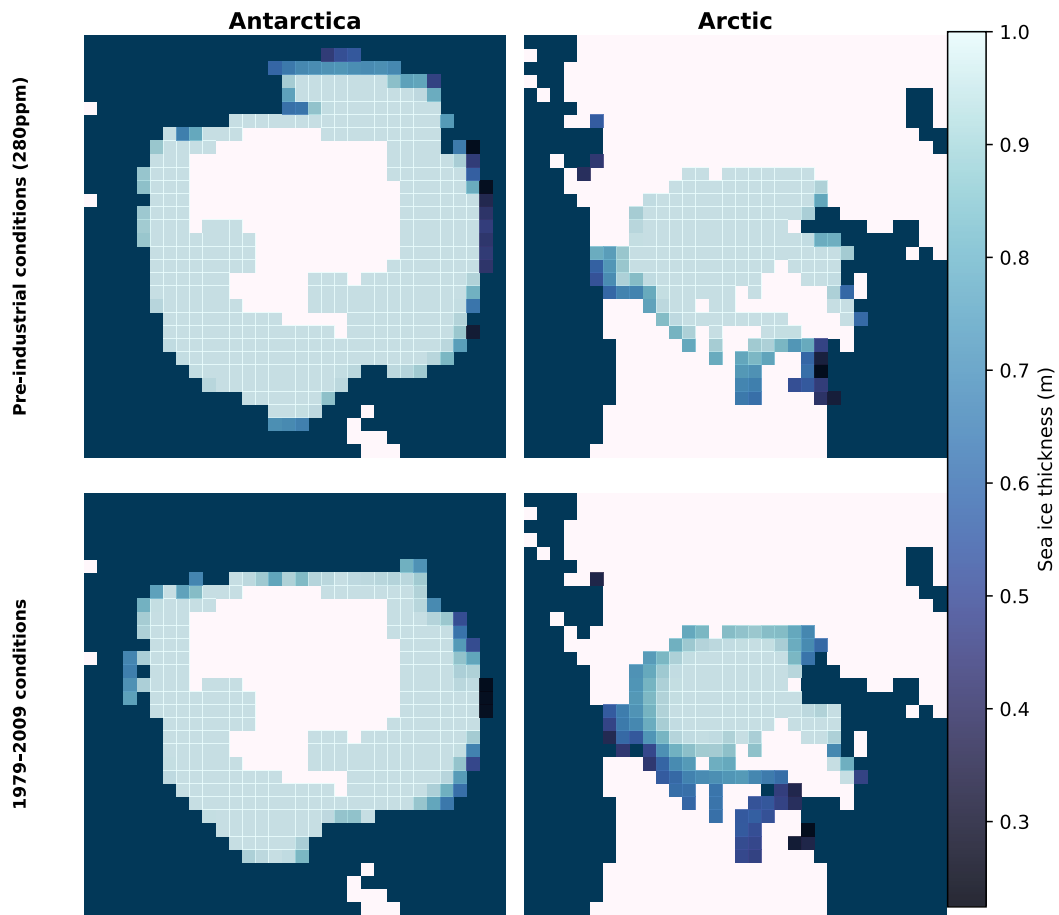
**Figure A1.** Climatology of surface air temperature for the two *biogeodyn-MITgcmIS* simulations and the corresponding anomaly maps with respect to CMIP models and ERA5.



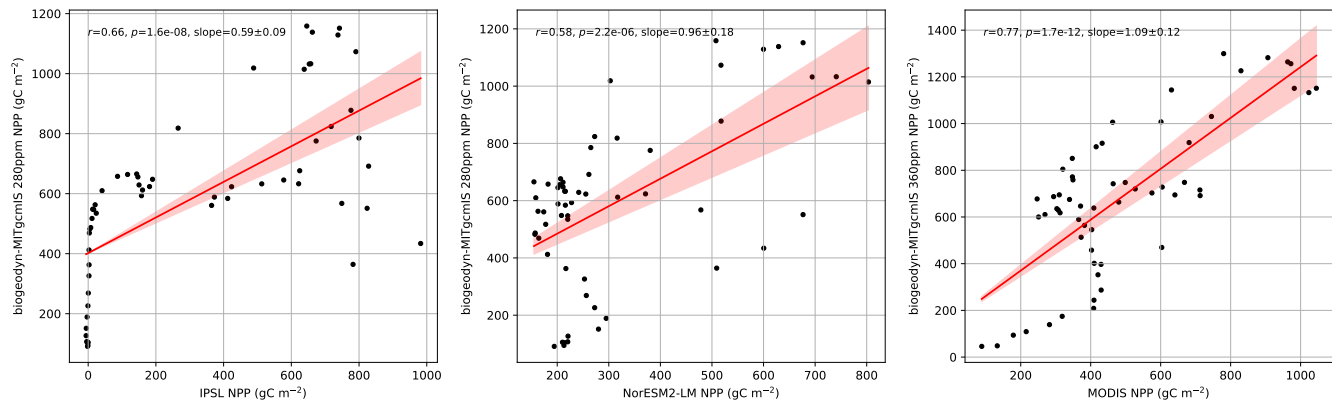
**Figure A2.** Zonal annual mean of zonal wind for the two *biogeodyn-MITgcmIS* simulations, CMIP models and ERA5.



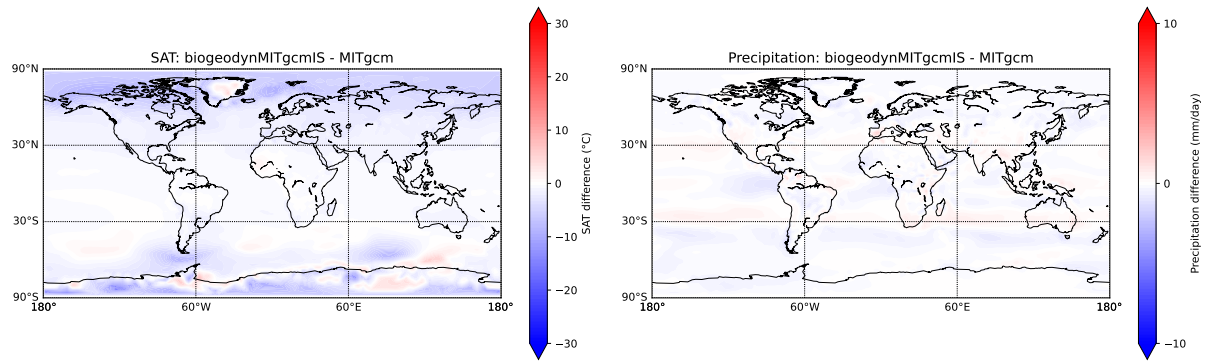
**Figure A3.** Climatology of precipitation for the two *biogeodyn-MITgcmIS* simulations and the corresponding anomaly maps with respect to CMIP models and ERA5.



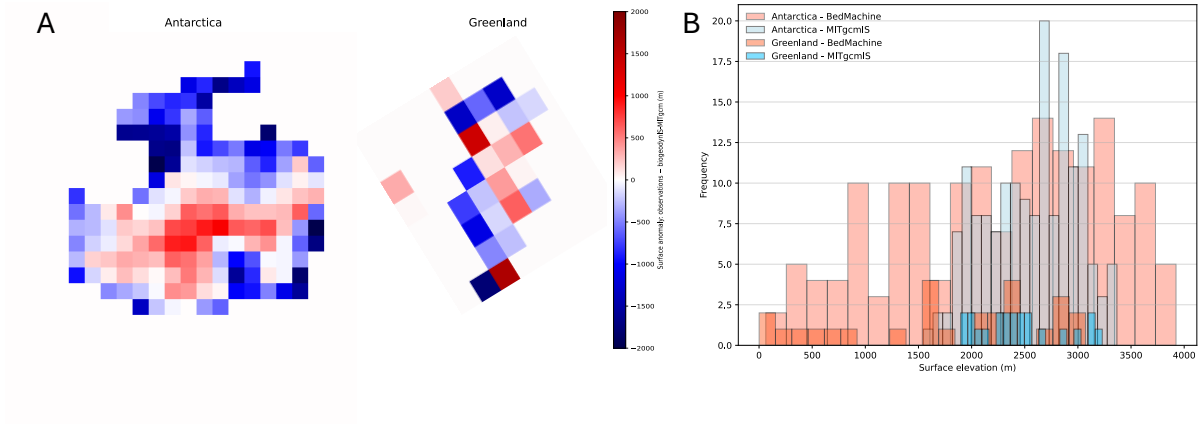
**Figure A4.** Annual mean sea ice thickness and extent in the polar regions for the two *biogeodyn-MITgcmIS* simulations on the cubed-sphere grid.



**Figure A5.** Linear regression (with corresponding  $r$ ,  $p$  and slope values) of NPP obtained with *biogeodyn-MITgcmIS* run1 against the CMIP models, and with *biogeodyn-MITgcmIS* run2 against the MODIS dataset.



**Figure A6.** Maps of surface air temperature and precipitation for the difference between *biogeodyn-MITgcmIS* run1 and the simulation started from ETOPO2. Scales are the same as in the anomaly maps in Figs. A1 and A3.



**Figure A7.** A. Anomaly maps of surface elevation (BedMachine minus the *MITgcmIS* simulation where ice sheets form). B. Histograms of surface elevation where ice sheets form in *MITgcmIS* simulations (blue) and in the BedMachine observations (orange).

690 **References**

- Ackermann, L., Danek, C., Gierz, P., and Lohmann, G.: AMOC Recovery in a Multicentennial Scenario Using a Coupled Atmosphere-Ocean-Ice Sheet Model, *Geophysical Research Letters*, 47, e2019GL086810, <https://doi.org/https://doi.org/10.1029/2019GL086810>, e2019GL086810 10.1029/2019GL086810, 2020.
- Adcroft, A., Campin, J.-M., Hill, C., and Marshall, J.: Implementation of an atmosphere ocean general circulation model on the expanded  
695 spherical cube, *Monthly Weather Review*, 132, 2845–2863, <https://doi.org/10.1175/MWR2823.1>, 2004.
- Allen, B. J., Hill, D. J., Burke, A. M., Clark, M., Marchant, R., Stringer, L. C., Williams, D. R., and Lyon, C.: Projected future climatic forcing on the global distribution of vegetation types, *Philosophical Transactions of the Royal Society B: Biological Sciences*, 379, 20230011, <https://doi.org/10.1098/rstb.2023.0011>, 2024.
- Balaji, V., Maisonnave, E., Zadeh, N., Lawrence, B. N., Biercamp, J., Fladrich, U., Aloisio, G., Benson, R., Caubel, A., Durachta, J., Foujols,  
700 M.-A., Lister, G., Mocavero, S., Underwood, S., and Wright, G.: CPMIP: measurements of real computational performance of Earth system models in CMIP6, *Geoscientific Model Development*, 10, 19–34, <https://doi.org/10.5194/gmd-10-19-2017>, 2017.
- Bartos, M.: pysheds: simple and fast watershed delineation in python, <https://doi.org/10.5281/zenodo.3822494>, 2020.
- Boers, N., Ghil, M., and Rousseau, D.-D.: Ocean circulation, ice shelf, and sea ice interactions explain Dansgaard, Ål̈oeschger cycles, *Proceedings of the National Academy of Sciences*, 115, E11 005–E11 014, <https://doi.org/10.1073/pnas.1802573115>, 2018.
- 705 Boucher, O., Denvil, S., Levvasseur, G., Cozic, A., Caubel, A., Foujols, M.-A., Meurdesoif, Y., Cadule, P., Devilliers, M., Ghattas, J., Lebas, N., Lurton, T., Mellul, L., Musat, I., Mignot, J., and Cheruy, F.: IPSL IPSL-CM6A-LR model output prepared for CMIP6 CMIP historical, <https://doi.org/10.22033/ESGF/CMIP6.5195>, 2018.
- Braithwaite, R. J.: Air Temperature and Glacier Ablation — A Parametric Approach, Ph.D. thesis, McGill University, ph.D. thesis, *Interdisciplinary Studies in Glaciology*, 1977.
- 710 Brovkin, V., Brook, E., Williams, J. W., Bathiany, S., Lenton, T. M., Barton, M., DeConto, R. M., Donges, J. F., Ganopolski, A., McManus, J., et al.: Past abrupt changes, tipping points and cascading impacts in the Earth system, *Nature Geoscience*, 14, 550–558, <https://doi.org/10.1038/s41561-021-00790-5>, 2021.
- Brunetti, M. and Ragon, C.: Attractors and bifurcation diagrams in complex climate models, *Phys. Rev. E*, 107, 054 214, <https://doi.org/10.1103/PhysRevE.107.054214>, 2023.
- 715 Brunetti, M. and V erard, C.: How to reduce long-term drift in present-day and deep-time simulations?, *Climate Dynamics*, 50, 4425–4436, <https://doi.org/10.1007/s00382-017-3883-7>, 2018.
- Brunetti, M., V erard, C., and Baumgartner, P. O.: Modeling the Middle Jurassic ocean circulation, *Journal of Palaeogeography*, 4, 371–383, <https://doi.org/https://doi.org/10.1016/j.jop.2015.09.001>, 2015.
- Brunetti, M., Kasparian, J., and V erard, C.: Co-existing climate attractors in a coupled aquaplanet, *Climate Dynamics*, 53, 6293–6308,  
720 <https://doi.org/10.1007/s00382-019-04926-7>, 2019.
- Caesar, L., Rahmstorf, S., Robinson, A., Feulner, G., and Saba, V.: Observed fingerprint of a weakening Atlantic Ocean overturning circulation, *Nature*, 556, 191–196, <https://doi.org/10.1038/s41586-018-0006-5>, 2018.
- Carissimo, B. C., Oort, A. H., and Haar, T. H. V.: Estimating the Meridional Energy Transports in the Atmosphere and Ocean, *Journal of Physical Oceanography*, 15, 82 – 91, [https://doi.org/10.1175/1520-0485\(1985\)015<0082:ETMETI>2.0.CO;2](https://doi.org/10.1175/1520-0485(1985)015<0082:ETMETI>2.0.CO;2), 1985.
- 725 Claussen, M.: On coupling global biome models with climate models, *Climate Research*, 4, 203–221, 1994.

- Claussen, M., Mysak, L., Weaver, A., Crucifix, M., Fichefet, T., Loutre, M.-F., Weber, S., Alcamo, J., Alexeev, V., Berger, A., et al.: Earth system models of intermediate complexity: closing the gap in the spectrum of climate system models, *Climate dynamics*, 18, 579–586, 2002.
- 730 Copernicus Climate Change Service: ORAS5 global ocean reanalysis monthly data from 1958 to present, <https://doi.org/10.24381/cds.67e8eeb7>, accessed on 12-MAR-2025, 2021.
- Cuffey, K. M. and Paterson, W. S. B.: *The physics of glaciers*, Academic Press, 2010.
- de Noblet-Ducoudré, N., Claussen, M., and Prentice, C.: Mid-Holocene greening of the Sahara: first results of the GAIM 6000 year BP Experiment with two asynchronously coupled atmosphere/biome models, *Climate Dynamics*, 16, 643–659, <https://doi.org/10.1007/s003820000074>, 2000.
- 735 Dinh, T. L. A., Goll, D., Ciais, P., and Lauerwald, R.: Impacts of land-use change on biospheric carbon: an oriented benchmark using the ORCHIDEE land surface model, *Geoscientific Model Development*, 17, 6725–6744, <https://doi.org/10.5194/gmd-17-6725-2024>, 2024.
- Drótos, G., Bóday, T., and Tél, T.: On the importance of the convergence to climate attractors, *The European Physical Journal Special Topics*, 226, 2031–2038, <https://doi.org/10.1140/epjst/e2017-70045-7>, 2017.
- Drüke, M., von Bloh, W., Petri, S., Sakschewski, B., Schaphoff, S., Forkel, M., Huiskamp, W., Feulner, G., and Thonicke, K.: CM2Mc-LPJmL v1.0: biophysical coupling of a process-based dynamic vegetation model with managed land to a general circulation model, *Geoscientific Model Development*, 14, 4117–4141, <https://doi.org/10.5194/gmd-14-4117-2021>, 2021.
- 740 Essery, R.: A factorial snowpack model (FSM 1.0), *Geoscientific Model Development*, 8, 3867–3876, <https://doi.org/10.5194/gmd-8-3867-2015>, 2015.
- ETOPO: 15 Arc-Second Global Relief Model, <https://doi.org/10.25921/fd45-gt74>, 2022.
- 745 ETOPO2: 2-minute Gridded Global Relief Data (ETOPO2) v2, <https://doi.org/10.7289/V5J1012Q>, 2006.
- Eyring, V., Bony, S., Meehl, G. A., Senior, C. A., Stevens, B., Stouffer, R. J., and Taylor, K. E.: Overview of the Coupled Model Intercomparison Project Phase 6 (CMIP6) experimental design and organization, *Geoscientific Model Development*, 9, 1937–1958, <https://doi.org/10.5194/gmd-9-1937-2016>, 2016.
- Ferreira, D., Marshall, J., and Rose, B.: Climate Determinism Revisited: Multiple Equilibria in a Complex Climate Model, *Journal of Climate*, 24, 992 – 1012, <https://doi.org/10.1175/2010JCLI3580.1>, 2011.
- 750 Ferreira, D., Marshall, J., Ito, T., and McGee, D.: Linking Glacial-Interglacial States to Multiple Equilibria of Climate, *Geophysical Research Letters*, 45, 9160–9170, <https://doi.org/10.1029/2018GL077019>, 2018.
- Fetterer, F., Knowles, K., Meier, W., and Savoie, M.: Sea Ice Index, <https://doi.org/10.7265/N5QJ7F7W>, updated daily. [Indicate subset used], 2002.
- 755 Gent, P. R. and McWilliams, J. C.: Isopycnal mixing in ocean circulation models, *Journal of Physical Oceanography*, 20, 150–160, [https://doi.org/10.1175/1520-0485\(1990\)020<0150:IMIOCM>2.0.CO;2](https://doi.org/10.1175/1520-0485(1990)020<0150:IMIOCM>2.0.CO;2), 1990.
- Goldberg, D. N. and Heimbach, P.: Parameter and state estimation with a time-dependent adjoint marine ice sheet model, *The Cryosphere*, 7, 1659–1678, <https://doi.org/10.5194/tc-7-1659-2013>, 2013.
- Greve, R. and Blatter, H.: *Glacial Isostasy*, pp. 185–201, Springer Berlin Heidelberg, Berlin, Heidelberg, ISBN 978-3-642-03415-2, [https://doi.org/10.1007/978-3-642-03415-2\\_8](https://doi.org/10.1007/978-3-642-03415-2_8), 2009.
- 760 Hansen, J., Russell, G., Rind, D., Stone, P., Lacis, A., Lebedeff, S., Ruedy, R., and Travis, L.: Efficient Three-Dimensional Global Models for Climate Studies: Models I and II, *Monthly Weather Review*, 111, 609 – 662, [https://doi.org/10.1175/1520-0493\(1983\)111<0609:ETDGMF>2.0.CO;2](https://doi.org/10.1175/1520-0493(1983)111<0609:ETDGMF>2.0.CO;2), 1983.

- Haq, B. U.: Triassic eustatic variations reexamined, *GSA Today*, 28, 4–9, <https://doi.org/10.1130/GSATG381A.1>, 2018.
- 765 Hawkins, E., Smith, R. S., Allison, L. C., Gregory, J. M., Woollings, T. J., Pohlmann, H., and de Cuevas, B.: Bistability of the Atlantic overturning circulation in a global climate model and links to ocean freshwater transport, *Geophysical Research Letters*, 38, <https://doi.org/https://doi.org/10.1029/2011GL047208>, 2011.
- Haxeltine, A. and Prentice, I. C.: BIOME3: An equilibrium terrestrial biosphere model based on ecophysiological constraints, resource availability, and competition among plant functional types, *Global Biogeochemical Cycles*, 10, 693–709, <https://doi.org/https://doi.org/10.1029/96GB02344>, 1996.
- 770 Haywood, A. M., Dowsett, H. J., Otto-Bliesner, B., Chandler, M. A., Dolan, A. M., Hill, D. J., Lunt, D. J., Robinson, M. M., Rosenbloom, N., Salzmann, U., and Sohl, L. E.: Pliocene Model Intercomparison Project (PlioMIP): experimental design and boundary conditions (Experiment 1), *Geoscientific Model Development*, 3, 227–242, <https://doi.org/10.5194/gmd-3-227-2010>, 2010.
- Haywood, A. M., Tindall, J. C., Dowsett, H. J., Dolan, A. M., Foley, K. M., Hunter, S. J., Hill, D. J., Chan, W.-L., Abe-Ouchi, A., Stepanek, C., Lohmann, G., Chandan, D., Peltier, W. R., Tan, N., Contoux, C., Ramstein, G., Li, X., Zhang, Z., Guo, C., Nisancioglu, K. H., Zhang, Q., Li, Q., Kamae, Y., Chandler, M. A., Sohl, L. E., Otto-Bliesner, B. L., Feng, R., Brady, E. C., von der Heydt, A. S., Baatsen, M. L. J., and Lunt, D. J.: The Pliocene Model Intercomparison Project Phase 2: large-scale climate features and climate sensitivity, *Climate of the Past*, 16, 2095–2123, <https://doi.org/10.5194/cp-16-2095-2020>, 2020.
- Herrington, A. R. and Poulsen, C. J.: Terminating the Last Interglacial: The Role of Ice Sheet, Climate Feedbacks in a GCM Asynchronously Coupled to an Ice Sheet Model, *Journal of Climate*, 25, 1871 – 1882, <https://doi.org/10.1175/JCLI-D-11-00218.1>, 2011.
- 780 Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., Nicolas, J., Peubey, C., Radu, R., Rozum, I., Schepers, D., Simmons, A., Soci, C., Dee, D., and Thépaut, J.-N.: ERA5 monthly averaged data on single levels from 1940 to present, <https://doi.org/10.24381/cds.f17050d7>, accessed on 12-MAR-2025, 2023.
- Hock, R. and Holmgren, B.: A distributed surface energy-balance model for complex topography and its application to Storglaciären, Sweden, *Journal of Glaciology*, 51, 25–36, <https://doi.org/10.3189/172756505781829566>, 2005.
- 785 Hoffman, P. F. and Schrag, D. P.: The snowball Earth hypothesis: testing the limits of global change, *Terra Nova*, 14, 129–155, <https://doi.org/https://doi.org/10.1046/j.1365-3121.2002.00408.x>, 2002.
- Holden, P. B., Edwards, N. R., Fraedrich, K., Kirk, E., Lunkeit, F., and Zhu, X.: PLASIM–GENIE v1.0: a new intermediate complexity AOGCM, *Geoscientific Model Development*, 9, 3347–3361, <https://doi.org/10.5194/gmd-9-3347-2016>, 2016.
- 790 Hou, Y., Guo, H., Yang, Y., and Liu, W.: Global Evaluation of Runoff Simulation From Climate, Hydrological and Land Surface Models, *Water Resources Research*, 59, e2021WR031817, <https://doi.org/https://doi.org/10.1029/2021WR031817>, 2023.
- Jackson, L. C., Alastrué de Asenjo, E., Bellomo, K., Danabasoglu, G., Haak, H., Hu, A., Jungclaus, J., Lee, W., Meccia, V. L., Saenko, O., Shao, A., and Swingedouw, D.: Understanding AMOC stability: the North Atlantic Hosing Model Intercomparison Project, *Geoscientific Model Development*, 16, 1975–1995, <https://doi.org/10.5194/gmd-16-1975-2023>, 2023.
- 795 Kaplan, J.: *Geophysical Applications of Vegetation Modeling*, Doctoral thesis (compilation), Department of Biology, ISBN 91-7874-089-4, 2001.
- Kaplan, J. O., Bigelow, N. H., Prentice, I. C., Harrison, S. P., Bartlein, P. J., Christensen, T. R., Cramer, W., Matveyeva, N. V., McGuire, A. D., Murray, D. F., Razzhivin, V. Y., Smith, B., Walker, D. A., Anderson, P. M., Andreev, A. A., Brubaker, L. B., Edwards, M. E., and Lozhkin, A. V.: Climate change and Arctic ecosystems: 2. Modeling, paleodata-model comparisons, and future projections, *Journal of Geophysical Research: Atmospheres*, 108, <https://doi.org/https://doi.org/10.1029/2002JD002559>, 2003.
- 800

- Kirschvink, J. L.: Late Proterozoic Low-Latitude Global Glaciation: The Snowball Earth, in: *The Proterozoic Biosphere: A Multidisciplinary Study*, edited by Schopf, J. W. and Klein, C., pp. 51–52, Cambridge University Press, Cambridge, UK, 1992.
- Kucharski, F., Molteni, F., King, M. P., Farneti, R., Kang, I.-S., and Feudale, L.: On the Need of Intermediate Complexity General Circulation Models: A „SPEEDY“ Example, *Bulletin of the American Meteorological Society*, 94, 25 – 30, <https://doi.org/10.1175/BAMS-D-11-00238.1>, 2013.
- 805 Lan, X., Tans, P., and Thoning, K. W.: Trends in globally-averaged CO<sub>2</sub> determined from NOAA Global Monitoring Laboratory measurements, <https://doi.org/10.15138/9N0H-ZH07>, <https://doi.org/10.15138/9N0H-ZH07>, version Monday, 05-May-2025 16:38:58 MDT, 2025.
- Large, W. G. and Yeager, S. G.: Diurnal to decadal global forcing for ocean and sea-ice models: The data sets and flux climatologies, Technical note, National Center for Atmospheric Research (NCAR), Boulder, CO, <https://doi.org/10.5065/D6KK98Q6>, 2004.
- 810 Lembo, V., Lunkeit, F., and Lucarini, V.: TheDiaTo (v1.0) – a new diagnostic tool for water, energy and entropy budgets in climate models, *Geoscientific Model Development*, 12, 3805–3834, <https://doi.org/10.5194/gmd-12-3805-2019>, 2019.
- Lenton, T. M., Held, H., Kriegler, E., Hall, J. W., Lucht, W., Rahmstorf, S., and Schellnhuber, H. J.: Tipping elements in the Earth’s climate system, *Proceedings of the National Academy of Sciences*, 105, 1786–1793, <https://doi.org/10.1073/pnas.0705414105>, 2008.
- 815 Levitus, S.: *Climatological Atlas of the World Ocean*, NOAA Professional Paper 13, U.S. Government Printing Office, Washington, D.C., 1982.
- Lucarini, V. and Bódai, T.: Edge states in the climate system: exploring global instabilities and critical transitions, *Nonlinearity*, 30, R32–R66, <https://doi.org/10.1088/1361-6544/aa6b11>, 2017.
- Lucarini, V. and Bódai, T.: Global stability properties of the climate: Melancholia states, invariant measures, and phase transitions, *Nonlinearity*, 33, R59, <https://doi.org/10.1088/1361-6544/ab86cc>, 2020.
- 820 Lucarini, V., Serdukova, L., and Margazoglou, G.: Lévy noise versus Gaussian-noise-induced transitions in the Ghil–Sellers energy balance model, *Nonlinear Processes in Geophysics*, 29, 183–205, <https://doi.org/10.5194/npg-29-183-2022>, 2022.
- M. Haywood, A., Valdes, P. J., Sellwood, B. W., and Kaplan, J. O.: Antarctic climate during the middle Pliocene: model sensitivity to ice sheet variation, *Palaeogeography, Palaeoclimatology, Palaeoecology*, 182, 93–115, [https://doi.org/https://doi.org/10.1016/S0031-0182\(01\)00454-0](https://doi.org/https://doi.org/10.1016/S0031-0182(01)00454-0), 2002.
- 825 MacAyeal, D.: *EISMINT: Lessons in ice-sheet modeling*, 1997.
- MacAyeal, D. R.: Binge/purge oscillations of the Laurentide Ice Sheet as a cause of the North Atlantic’s Heinrich events, *Paleoceanography*, 8, 775–784, <https://doi.org/https://doi.org/10.1029/93PA02200>, 1993.
- Madsen, M. S., Yang, S., Aðalgeirsdóttir, G., et al.: The role of an interactive Greenland ice sheet in the coupled climate-ice sheet model EC-Earth-PISM, *Climate Dynamics*, 59, 1189–1211, <https://doi.org/10.1007/s00382-022-06184-6>, 2022.
- 830 Marshall, J., Adcroft, A., Hill, C., Perelman, L., and Heisey, C.: A finite-volume, incompressible Navier Stokes model for studies of the ocean on parallel computers, *Journal of Geophysical Research: Oceans*, 102, 5753–5766, <https://doi.org/10.1029/96JC02775>, 1997a.
- Marshall, J., Hill, C., Perelman, L., and Adcroft, A.: Hydrostatic, quasi-hydrostatic, and nonhydrostatic ocean modeling, *Journal of Geophysical Research: Oceans*, 102, 5733–5752, <https://doi.org/10.1029/96JC02776>, 1997b.
- 835 Marshall, J., Adcroft, A., Campin, J.-M., and Hill, C.: Atmosphere–ocean modeling exploiting fluid isomorphisms, *Monthly Weather Review*, 132, 2882–2894, <https://doi.org/10.1175/MWR2835.1>, 2004.
- Marshall, J., Donohoe, A., Ferreira, D., and McGee, D.: The ocean’s role in setting the mean position of the Inter-Tropical Convergence Zone, *Climate Dynamics*, 42, 1967–1979, <https://doi.org/10.1007/s00382-013-1767-z>, 2014.

- McKay, D. I. A., Staal, A., Abrams, J. F., n, R., Sakschewski, B., Loriani, S., Fetzer, I., Cornell, S. E., Rockström, J.,  
840 and Lenton, T. M.: Exceeding 1.5°C global warming could trigger multiple climate tipping points, *Science*, 377, eabn7950,  
<https://doi.org/10.1126/science.abn7950>, 2022.
- Merdith, A. S., Williams, S. E., Collins, A. S., Tetley, M. G., Mulder, J. A., Blades, M. L., Young, A., Armistead, S. E., Cannon, J., Zahirovic,  
S., and Müller, R. D.: Extending full-plate tectonic models into deep time: Linking the Neoproterozoic and the Phanerozoic, *Earth-Science  
Reviews*, 214, 103477, <https://doi.org/https://doi.org/10.1016/j.earscirev.2020.103477>, 2021.
- 845 Moat, B. I., Smeed, D. A., Rayner, D., Johns, W. E., Smith, R., Volkov, D., Elipot, S., Petit, T., Kajtar, J., Baringer, M. O., and Collins,  
J.: Atlantic meridional overturning circulation observed by the RAPID-MOCHA-WBTS (RAPID-Meridional Overturning Circulation  
and Heatflux Array-Western Boundary Time Series) array at 26N from 2004 to 2023 (v2023.1a), [https://doi.org/10.5285/33826d6e-801c-  
b0a7-e063-7086abc0b9db](https://doi.org/10.5285/33826d6e-801c-b0a7-e063-7086abc0b9db), 2025.
- Moinat, L., Kasparian, J., and Brunetti, M.: Tipping detection using climate networks, *Chaos: An Interdisciplinary Journal of Nonlinear  
850 Science*, 34, 123161, <https://doi.org/10.1063/5.0230848>, 2024.
- Moinat, L., Franziskakis, F., V  rard, C., Goldberg, D. N., and Brunetti, M.: Repository for: biogeodyn-MITgcmIS (v1): a biogeodynamical  
tool for exploratory climate modelling], <https://doi.org/10.5281/zenodo.18723952>, 2025.
- Molteni, F.: Atmospheric simulations using a GCM with simplified physical parametrizations. I: Model climatology and variability in multi-  
decadal experiments, *Climate Dynamics*, 20, 175–191, <https://doi.org/10.1007/s00382-002-0268-2>, 2003.
- 855 Moreno-Parada, D., Alvarez-Solas, J., Blasco, J., Montoya, M., and Robinson, A.: Simulating the Laurentide Ice Sheet of the Last Glacial  
Maximum, *The Cryosphere*, 17, 2139–2156, <https://doi.org/10.5194/tc-17-2139-2023>, 2023.
- Morlighem, M.: MEaSURES BedMachine Antarctica, Version 3, <https://doi.org/10.5067/FPSU0V1MWUB6>, accessed: 2025-03-21, 2022.
- Morlighem, M., Williams, C., Rignot, E., An, L., Arndt, J. E., Bamber, J., Catania, G., Chauch  , N., Dowdeswell, J. A., Dorschel, B., Fenty,  
I., Hogan, K., Howat, I., Hubbard, A., Jakobsson, M., Jordan, T. M., Kjeldsen, K. K., Millan, R., Mayer, L., Mouginot, J., No  l, B.,  
860 O’Cofaigh, C., Palmer, S. J., Rysgaard, S., Seroussi, H., Siegert, M. J., Slabon, P., Straneo, F., van den Broeke, M. R., Weinrebe, W.,  
Wood, M., and Zinglensen, K.: IceBridge BedMachine Greenland (IDBMG4, Version 5), <https://doi.org/10.5067/GMEVBWFLWA7X>,  
accessed: 2025-04-103, 2022.
- Mottram, R., Hansen, N., Kittel, C., van Wessem, J. M., Agosta, C., Amory, C., Boberg, F., van de Berg, W. J., Fettweis, X., Gossart, A., van  
Lipzig, N. P. M., van Meijgaard, E., Orr, A., Phillips, T., Webster, S., Simonsen, S. B., and Souverijns, N.: What is the surface mass balance  
865 of Antarctica? An intercomparison of regional climate model estimates, *The Cryosphere*, 15, 3751–3784, [https://doi.org/10.5194/tc-15-  
3751-2021](https://doi.org/10.5194/tc-15-3751-2021), 2021.
- Mouginot, J., Rignot, E., Bj  rk, A. A., van den Broeke, M., Millan, R., Morlighem, M., No  l, B., Scheuchl, B., and Wood, M.: Forty-  
six years of Greenland Ice Sheet mass balance from 1972 to 2018, *Proceedings of the National Academy of Sciences*, 116, 9239–9244,  
<https://doi.org/10.1073/pnas.1904242116>, 2019.
- 870 Muntjewerf, L., Petrini, M., Vizcaino, M., Ernani da Silva, C., Sellevold, R., Scherrenberg, M. D. W., Thayer-Calder, K.,  
Bradley, S. L., Lenaerts, J. T. M., Lipscomb, W. H., and Lofverstrom, M.: Greenland Ice Sheet Contribution to 21st Century  
Sea Level Rise as Simulated by the Coupled CESM2.1-CISM2.1, *Geophysical Research Letters*, 47, e2019GL086836,  
<https://doi.org/https://doi.org/10.1029/2019GL086836>,  
<https://doi.org/10.1029/2019GL086836>, 2020.
- Nijssen, F. J. M. M., Cox, P. M., and Williamson, M. S.: Emergent constraints on transient climate response (TCR) and equilibrium climate sensi-  
875 tivity (ECS) from historical warming in CMIP5 and CMIP6 models, *Earth System Dynamics*, 11, 737–750, [https://doi.org/10.5194/esd-  
11-737-2020](https://doi.org/10.5194/esd-11-737-2020), 2020.

- NOAA National Centers for Environmental Information: Monthly Global Climate Report for Annual 2023, <https://www.ncei.noaa.gov/access/monitoring/monthly-report/global/202313>, <https://doi.org/10.25921/C00672>, published online January 2024, retrieved April 25, 2025, 2024.
- 880 Norby, R. J., DeLucia, E. H., Gielen, B., Calfapietra, C., Giardina, C. P., King, J. S., Ledford, J., McCarthy, H. R., Moore, D. J. P., Ceulemans, R., Angelis, P. D., Finzi, A. C., Karnosky, D. F., Kubiske, M. E., Lukac, M., Pregitzer, K. S., Scarascia-Mugnozza, G. E., Schlesinger, W. H., and Oren, R.: Forest response to elevated CO<sub>2</sub> is conserved across a broad range of productivity, *Proceedings of the National Academy of Sciences*, 102, 18 052–18 056, <https://doi.org/10.1073/pnas.0509478102>, 2005.
- Paxman, G. J. G., Austermann, J., and Hollyday, A.: Total isostatic response to the complete unloading of the Greenland and Antarctic Ice  
885 Sheets, *Scientific Reports*, 12, 11 399, <https://doi.org/10.1038/s41598-022-15440-y>, 2022.
- Plach, A., Nisancioglu, K. H., Le clec'h, S., Born, A., Langebroek, P. M., Guo, C., Imhof, M., and Stocker, T. F.: Eemian Greenland SMB strongly sensitive to model choice, *Climate of the Past*, 14, 1463–1485, <https://doi.org/10.5194/cp-14-1463-2018>, 2018.
- Pohl, A., Donnadieu, Y., Le Hir, G., Ladant, J.-B., Dumas, C., Alvarez-Solas, J., and Vandenbroucke, T. R. A.: Glacial onset predated Late Ordovician climate cooling, *Paleoceanography*, 31, 800–821, <https://doi.org/https://doi.org/10.1002/2016PA002928>, 2016.
- 890 Prentice, C., Guiot, J., Huntley, B., Jolly, D., and Cheddadi, R.: Reconstructing biomes from palaeoecological data: a general method and its application to European pollen data at 0 and 6 ka, *Climate Dynamics*, 12, 185–194, <https://doi.org/10.1007/BF00211617>, 1996.
- Quiquet, A., Dumas, C., Ritz, C., Peyaud, V., and Roche, D. M.: The GRISLI ice sheet model (version 2.0): calibration and validation for multi-millennial changes of the Antarctic ice sheet, *Geoscientific Model Development*, 11, 5003–5025, <https://doi.org/10.5194/gmd-11-5003-2018>, 2018.
- 895 Ragon, C., Lembo, V., Lucarini, V., V  rard, C., Kasparian, J., and Brunetti, M.: Robustness of Competing Climatic States, *Journal of Climate*, 35, 2769 – 2784, <https://doi.org/10.1175/JCLI-D-21-0148.1>, 2022.
- Ragon, C., V  rard, C., Kasparian, J., and Brunetti, M.: Alternative climatic steady states near the Permian–Triassic Boundary, *Scientific Reports*, 14, 26 136, <https://doi.org/10.1038/s41598-024-76432-8>, 2024.
- Ragon, C., V  rard, C., Kasparian, J., Nowak, H., Kustatscher, E., and Brunetti, M.: Comparison between plant fossil assemblages and  
900 simulated biomes across the Permian-Triassic Boundary, *Frontiers in Earth Science*, 13, <https://doi.org/10.3389/feart.2025.1520846>, 2025.
- Rose, B. E.: Stable “Waterbelt” climates controlled by tropical ocean heat transport: A nonlinear coupled climate mechanism of relevance to Snowball Earth, *Journal of Geophysical Research: Atmospheres*, 120, 1404–1423, <https://doi.org/10.1002/2014jd022659>, 2015.
- R  ckamp, M., Goelzer, H., and Humbert, A.: Sensitivity of Greenland ice sheet projections to spatial resolution in higher-order simulations: the Alfred Wegener Institute (AWI) contribution to ISMIP6 Greenland using the Ice-sheet and Sea-level System Model (ISSM), *The  
905 Cryosphere*, 14, 3309–3327, <https://doi.org/10.5194/tc-14-3309-2020>, 2020.
- Ruggieri, P., Abid, M. A., Garc  a-Serrano, J., et al.: SPEEDY-NEMO: performance and applications of a fully-coupled intermediate-complexity climate model, *Climate Dynamics*, 62, 3763–3781, <https://doi.org/10.1007/s00382-023-07097-8>, 2024.
- Salzmann, U., Haywood, A. M., Lunt, D. J., Valdes, P. J., and Hill, D. J.: A new global biome reconstruction and data-model comparison for the Middle Pliocene, *Global Ecology and Biogeography*, 17, 432–447, <https://doi.org/https://doi.org/10.1111/j.1466-8238.2008.00381.x>,  
910 2008.
- Schoof, C. and Hewitt, I.: Ice-Sheet Dynamics, *Annual Review of Fluid Mechanics*, 45, 217–239, <https://doi.org/https://doi.org/10.1146/annurev-fluid-011212-140632>, 2013.
- Scotese, C. R.: An Atlas of Phanerozoic Paleogeographic Maps: The Seas Come In and the Seas Go Out, *Annual Review of Earth and Planetary Sciences*, 49, 679–728, <https://doi.org/https://doi.org/10.1146/annurev-earth-081320-064052>, 2021.

- 915 Seland, Ø., Bentsen, M., Olivié, D., Toniazzo, T., Gjermundsen, A., Graff, L. S., Debernard, J. B., Gupta, A. K., He, Y.-C., Kirkevåg, A., Schwinger, J., Tjiputra, J., Aas, K. S., Bethke, I., Fan, Y., Griesfeller, J., Grini, A., Guo, C., Ilicak, M., Karset, I. H. H., Landgren, O., Liakka, J., Moseid, K. O., Nummelin, A., Spensberger, C., Tang, H., Zhang, Z., Heinze, C., Iversen, T., and Schulz, M.: Overview of the Norwegian Earth System Model (NorESM2) and key climate response of CMIP6 DECK, historical, and scenario simulations, *Geoscientific Model Development*, 13, 6165–6200, <https://doi.org/10.5194/gmd-13-6165-2020>, 2020.
- 920 Sellwood, B. W. and Valdes, P. J.: Jurassic climates, *Proceedings of the Geologists' Association*, 119, 5–17, [https://doi.org/https://doi.org/10.1016/S0016-7878\(59\)80068-7](https://doi.org/https://doi.org/10.1016/S0016-7878(59)80068-7), 2008.
- Simmons, M., Miller, K., Ray, D., Davies, A., van Buchem, F., and Gréselle, B.: Phanerozoic Eustasy, in: *The Geologic Time Scale 2020*, edited by Gradstein, F. M., Ogg, J. G., Schmitz, M. D., and Ogg, G. M., chap. 13, pp. 357–400, Elsevier, <https://doi.org/10.1016/B978-0-12-824360-2.00013-9>, 2020.
- 925 Smith, R. S., Mathiot, P., Siahahan, A., Lee, V., Cornford, S. L., Gregory, J. M., Payne, A. J., Jenkins, A., Holland, P. R., Ridley, J. K., and Jones, C. G.: Coupling the U.K. Earth System Model to Dynamic Models of the Greenland and Antarctic Ice Sheets, *Journal of Advances in Modeling Earth Systems*, 13, e2021MS002520, <https://doi.org/https://doi.org/10.1029/2021MS002520>, e2021MS002520 2021MS002520, 2021.
- Tsai, V. C. and Ruan, X.: A simple physics-based improvement to the positive degree day model, *Journal of Glaciology*, 64, 661–668, <https://doi.org/10.1017/jog.2018.55>, 2018.
- 930 Valdes, P. J., Armstrong, E., Badger, M. P. S., Bradshaw, C. D., Bragg, F., Crucifix, M., Davies-Barnard, T., Day, J. J., Farnsworth, A., Gordon, C., Hopcroft, P. O., Kennedy, A. T., Lord, N. S., Lunt, D. J., Marzocchi, A., Parry, L. M., Pope, V., Roberts, W. H. G., Stone, E. J., Tourte, G. J. L., and Williams, J. H. T.: The BRIDGE HadCM3 family of climate models: HadCM3@Bristol v1.0, *Geoscientific Model Development*, 10, 3715–3743, <https://doi.org/10.5194/gmd-10-3715-2017>, 2017.
- 935 Vérard, C.: Panalexis: towards global synthetic palaeogeographies using integration and coupling of manifold models, *Geological Magazine*, 156, 320–330, <https://doi.org/10.1017/S0016756817001042>, 2019.
- Wake, L. and Marshall, S.: Assessment of current methods of positive degree-day calculation using in situ observations from glaciated regions, *Journal of Glaciology*, 61, 329–344, <https://doi.org/10.3189/2015JoG14J116>, 2015.
- Willeit, M., Ganopolski, A., Robinson, A., and Edwards, N. R.: The Earth system model CLIMBER-X v1.0 – Part 1: Climate model description and validation, *Geoscientific Model Development*, 15, 5905–5948, <https://doi.org/10.5194/gmd-15-5905-2022>, 2022.
- 940 Wiltshire, A. J., Duran Rojas, M. C., Edwards, J. M., Gedney, N., Harper, A. B., Hartley, A. J., Hendry, M. A., Robertson, E., and Smout-Day, K.: JULES-GL7: the Global Land configuration of the Joint UK Land Environment Simulator version 7.0 and 7.2, *Geoscientific Model Development*, 13, 483–505, <https://doi.org/10.5194/gmd-13-483-2020>, 2020.
- Winton, M.: A reformulated three-layer sea ice model, *Journal of Atmospheric and Oceanic Technology*, 17, 525–531, [https://doi.org/10.1175/1520-0426\(2000\)017<0525:ARTLSI>2.0.CO;2](https://doi.org/10.1175/1520-0426(2000)017<0525:ARTLSI>2.0.CO;2), 2000.
- 945 Wunderling, N., von der Heydt, A. S., Aksenov, Y., Barker, S., Bastiaansen, R., Brovkin, V., Brunetti, M., Couplet, V., Kleinen, T., Lear, C. H., Lohmann, J., Roman-Cuesta, R. M., Sinet, S., Swingedouw, D., Winkelmann, R., Anand, P., Barichivich, J., Bathiany, S., Baudena, M., Bruun, J. T., Chiessi, C. M., Coxall, H. K., Docquier, D., Donges, J. F., Falkena, S. K. J., Klose, A. K., Obura, D., Rocha, J., Rynders, S., Steinert, N. J., and Willeit, M.: Climate tipping point interactions and cascades: a review, *Earth System Dynamics*, 15, 41–74, <https://doi.org/10.5194/esd-15-41-2024>, 2024.

- Xie, Z., Dommenget, D., McCormack, F. S., and Mackintosh, A. N.: GREB-ISM v1.0: A coupled ice sheet model for the Globally Resolved Energy Balance model for global simulations on timescales of 100 kyr, *Geoscientific Model Development*, 15, 3691–3719, <https://doi.org/10.5194/gmd-15-3691-2022>, 2022.
- 955 Zelinka, M. D., Myers, T. A., McCoy, D. T., Po-Chedley, S., Caldwell, P. M., Ceppi, P., Klein, S. A., and Taylor, K. E.: Causes of Higher Climate Sensitivity in CMIP6 Models, *Geophysical Research Letters*, 47, e2019GL085782, <https://doi.org/https://doi.org/10.1029/2019GL085782>, e2019GL085782 10.1029/2019GL085782, 2020.
- Zhu, F. and Rose, B. E. J.: Multiple Equilibria in a Coupled Climate,ÄiCarbon Model, *Journal of Climate*, 36, 547 – 564, <https://doi.org/10.1175/JCLI-D-21-0984.1>, 2023.