



1 **Unraveling the Impact of Heterogeneity and Morphology on Light**

2 **Absorption Enhancement of Black Carbon-Containing Particles**

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15



16 Abstract

17 Black carbon (BC) is a strong climate forcer, but considerable uncertainty remains in
18 estimating its radiative impact, largely due to persistent gaps between observed and
19 modeled light absorption enhancement (E_{abs}). In this study, we employed a Centrifugal
20 Particle Mass Analyzer and Single Particle Soot Photometer tandem system to
21 characterize mass ratio (M_{R} , coating-to-BC) and morphology of BC-containing
22 particles in Hangzhou, China. Fortunately, low, medium, and high E_{abs} values were
23 observed during a single field campaign. Results show that the uniform core-shell Mie
24 model overestimated E_{abs} especially in clean conditions (low E_{abs}). A morphology-
25 dependent correction scheme was developed to improve optical property estimates of
26 BC in the “transition state.” This improved model better reproduces measured E_{abs} in
27 different pollution conditions and reveals that the concentrations of particle chemical
28 composition affect the M_{R} threshold defining this state. Our findings highlight the need
29 to account for real-world particle complexity in climate-relevant BC modeling.

30 1 Introduce

31 Black carbon (BC) is a strongly light-absorbing aerosol that effectively absorbs
32 solar radiation, warms the atmosphere, and contributes to direct radiative forcing
33 (DRF)(Bond and Bergstrom, 2006; Seinfeld, 2008). According to IPCC assessments,
34 the global effective DRF of BC ranges from -0.28 to 0.41 W/m^2 (Szopa et al., 2021).
35 Most climate models(Bauer et al., 2013; Chen et al., 2024; Stier et al., 2005; Wang et
36 al., 2023; Zhang et al., 2025) use Mie theory to estimate BC light absorption
37 enhancement (E_{abs}), assuming a uniform core-shell structure where BC core is fully
38 coated by coating materials. This approach predicts a monotonic increase in E_{abs} with
39 the coating-to-core mass ratio (M_{R}), often reaching values up to ~ 2 , consistent with
40 laboratory results (Peng et al., 2016). However, field observations commonly report
41 lower E_{abs} values, typically around 1.4 and sometimes as low as 1.09 (Cappa et al., 2012;
42 Huang et al., 2024). This discrepancy mainly stems from the oversimplified
43 assumptions in Mie theory, which fail to capture the real atmospheric complexity in BC
44 size distribution, morphology, and mixing state (Wang et al., 2021c). These limitations
45 introduce considerable uncertainty in assessing the radiative impacts of BC. Therefore,
46 improving our understanding of the mechanisms controlling BC E_{abs} and its
47 atmospheric evolution is essential for reducing uncertainties in BC DRF estimates and
48 enhancing the accuracy of climate model projections.

49 Previous studies have explored the discrepancies in BC E_{abs} from various
50 perspectives. A recent particle-resolved model study reveals that particle-to-particle
51 heterogeneity in M_{R} significantly influences E_{abs} (Fierce et al., 2020). Traditional
52 spherical core-shell models tend to overestimate E_{abs} , especially for partially coated
53 particles with low M_{R} . However, M_{R} heterogeneity alone cannot explain low E_{abs} under
54 high M_{R} conditions (Huang et al., 2024). Atmospheric BC particles also vary in
55 morphology. Fresh BC exhibit a branched structure that collapses into compact shapes
56 with reduced light absorption cross-sections during aging (Moteki and Kondo, 2007;
57 Romshoo et al., 2024; Li et al., 2024). Early aging stage feature uneven coatings, while
58 aged particles show BC core either encapsulated or located near the particle surface.



These configurations further influence E_{abs} . Recent studies suggest that the proportion of non-spherical BC particles and the position of the BC core may be key factors contributing to low E_{abs} , leading to an overestimation by core-shell model (Huang et al., 2024; Chen et al., 2024; Zhang et al., 2022). Thus, due to M_R heterogeneity and the morphological complexity, the mechanisms driving BC E_{abs} remain poorly understood, necessitating further research into relevant physical and chemical processes.

In this study, a suite of state-of-the-art instruments were employed to simultaneously capture the magnitude and dynamic evolution of M_R and morphology of BC-containing particles in Hangzhou, China. Fortunately, field measurements directly revealed the coexistence of high, medium, and low E_{abs} under high bulk-averaged M_R conditions. Further, the influences of M_R and morphology of BC-containing particles on E_{abs} are quantified to reconcile the discrepancies between models and observations under different E_{abs} conditions. Subsequently, an improved model for "transition-state" BC-containing particles was developed to reproduce the observed E_{abs} under varying E_{abs} and bulk-averaged M_R conditions. This study underscores the importance of simultaneously considering M_R heterogeneity and morphology of BC-containing particles in predicting E_{abs} . These findings contribute to reducing the uncertainty in estimating the DRF of BC.

2 Methods

2.1 Overview of the field campaign and instrumentation

The field measurements were conducted at the Central Air Quality Assurance Monitoring Station (30.25°N, 120.24°E) in Hangzhou from 3th Sept., 2023 to 13th Oct., 2023. The sampling site is located just 100 meters from the Qiantang River in the western part of Hangzhou, with major traffic routes within 3 kilometers to the northeast and southwest of the station. The schematic of the instrumentation is provided in Fig. S1. Aerosols were sampled after passing through a $\text{PM}_{2.5}$ impactor and then dried through a diffusion dryer before reaching subsequent instruments. The mass of an BC-containing particle (M_p) and of the BC core (M_{BC}) can be simultaneously obtained by a Centrifugal Particle Mass Analyzer (CPMA, Cambustion) and a single-particle soot photometer (SP2, DMT Inc.) tandem system. In the CPMA-SP2 system, particles with known mass (M_p) selected by CPMA were injected into the SP2, and the M_p was set from 0.9 fg to 30 fg with a logarithmic evenly spaced distribution, divided into 10 M_p , specially 0.93 fg, 1.37 fg, 2.02 fg, 2.97 fg, 4.36 fg, 6.40 fg, 9.39 fg, 13.78 fg, 20.22 fg and 29.68 fg, then the mass of BC core was measure by SP2. The duration of one set point cycle was 1 hour, with each M_p point sampling for 5 minutes, and all M_p points was sampling for total of 50 minutes. The remaining 10 minutes were divided into 4 minutes for instrument stabilization and 6 minutes for measuring all BC-containing particles when the valve was switched to the single SP2 line. During further data analysis, particles with $M_p = 0.93$ fg and $M_p = 1.37$ fg exhibited excessively noisy scattering signals and were therefore excluded from subsequent statistical analysis. The SP2 was calibrated with size-resolved Aquadag aerosols to establish the correlation



101 between incandescence peak height and the mass of BC-containing particles (DMT,
102 2011) (Fig. S2c and d). As reported in previous studies (Liu et al., 2020; Liu et al., 2014;
103 Zhang et al., 2018), a correction factor of 0.75 was applied to the peak height during
104 calibration. The SP2 scattering signal was calibrated with polystyrene latex spheres
105 (PSL) of known sizes (210 nm, 270 nm and 310 nm) (Fig. S2b). Additionally, the
106 calibration of the scattering and the incandescence channels was performed before and
107 after the measurement campaign. The mass concentrations of non-refractive OA, nitrate,
108 sulfate, ammonium and chloride was measured by an aerosol chemical speciation
109 monitor (ACSM, Aerodyne Research Inc.).

110 The aerosol extinction coefficient and scattering (Fig. S3) at wavelength of 440
111 nm, 530 nm and 630 nm was measured by Multi-Wavelength Cavity Attenuated Phase
112 Shift Single-Scattering Albedo Monitor (CAPS-ALB) (Weber et al., 2022), the aerosol
113 absorption coefficient was the difference between extinction coefficient and scattering
114 coefficient. Meanwhile, the aerosol scattering coefficient at wavelength of 450 nm, 525
115 nm, and 635 nm was also measured by Nephelometer (Multi Wavelength Integrating
116 Nephelometer) (Schloesser, 2016). The slope of the scattering coefficient measured by
117 CAPS and Nephelometer at corresponding wavelength was close to 1 (Fig. S4),
118 indicating the all data are reliable for further analysis. Besides, before sampling, the
119 scattering coefficient of CAPS and Nephelometer at every wavelength was calibrated
120 using PSL spheres. The slope of the scattering coefficient measured by CAPS (or the
121 Nephelometer) and modeled by Mie theory was close to 1 (Fig. S5), indicating the
122 reliability of the CAPS and Nephelometer. The lower detection limit of the
123 Nephelometer at all three wavelengths was 0.3 Mm^{-1} with a 60-second integration time,
124 while that of the CAPS was 1 Mm^{-1} with 30-second integration time.

125 2.2 Mixing state and morphology of the particle-resolved BC-containing particles

126 The mixing state of single BC-containing particle can be represented by the mass
127 ratio of the BC coating to BC core without any assumptions,

$$M_R = (M_p - M_{BC})/M_{BC} \quad (1)$$

128 where M_p and M_{BC} were the mass and core of each BC-containing particle. Then M_R
129 was converted to the bulk-averaged M_R to compared the measured E_{abs} in bulk particles
130 by summing of total coating and core mass of BC-containing particles every hour,

$$\text{bulk average } M_R = \frac{\sum_i M_{R,i} \times M_{BC,i}}{\sum_i M_{BC,i}} \quad (2)$$

131 where i was the i^{th} single BC-containing particle. The data measured by CPMA-SP2
132 were corrected via several steps, including (1) correction of delay time, (2) multi-
133 charged particles and (3) collection efficiency (for details, see Text S1).

134 In CPMA-SP2, when knowing M_p and M_{BC} , the modeled scattering cross section
135 (C_{modeled}) of BC-containing particles can be derived using Mie theory (Wang et al.,
136 2021a). This calculation assumes a core-shell structure with BC having refractive index
137 of $2.26-1.26i$ (Liu et al., 2017; Zhao et al., 2020) and the coating with $1.48i$, along with
138 a coating density of 1.5 g cm^{-3} (Liu et al., 2015). The measured scattering cross section
139 (C_{measured}) is analyzed using the leading-edge-only (LEO) technique, which reconstructs



140 the distorted scattering signal when BC-containing particles passes through the SP2
141 laser beam, as widely described in previous studies (Liu et al., 2014; Zhang et al., 2016;
142 Brooks et al., 2019; Gao et al., 2007; Zhang et al., 2020). Note only particles with
143 successfully fitted LEO signals are considered in the optical property calculations.
144 Subsequently, C_{modeled} can be compared with C_{measured} to infer the morphological
145 characteristic of BC-containing particles (Liu et al., 2017; Liu et al., 2020). Further
146 details can be seen in Section 3.

147 2.3 The measured and modeled E_{abs}

148 The light absorption enhancement of BC-containing particles is defined as the ratio
149 of the mass absorption cross section (MAC) of the coated and uncoated BC-containing
150 particles,

$$E_{\text{abs_measured}} = \frac{MAC_{BC}}{MAC_{BC_core}} \quad (3)$$

151 where $E_{\text{abs_measured}}$ is the measured light absorption enhancement, and MAC_{BC_core} is the
152 mass absorption coefficient for uncoated BC particles. The value of MAC_{BC_core} was
153 obtained by extrapolating MAC_{BC} to the limit of bulk-averaged $M_R = 0$. The MAC_{BC_core}
154 at wavelength of 630 nm was 9.08 (Fig. S6).

155 The commonly used models for calculating the optical properties of BC-
156 containing particles include Core-shell Mie theory (Cappa et al., 2012), T-matrix (Wu
157 et al., 2020), and discrete dipole approximation (DDA) (Kahnert and Kanngießer, 2020).
158 Among them, T-matrix, and DDA fully account for the impact of morphology of BC-
159 containing particles by incorporating detailed three-dimensional parameters such as
160 fractal dimension and monomer number (Wu et al., 2020). In contrast, Core-shell Mie
161 theory relies solely on the BC core size (D_c) and coating thickness (D_p/D_c). Given the
162 measurement data available in this study, the Core-shell Mie theory was used to
163 calculate the E_{abs} of BC-containing particles in this study. The refractive index (RI) of
164 BC and its coatings are assumed to be $n=1.85+0.71i$ and $n=1.5+0i$ (Liu et al., 2015; Liu
165 et al., 2014). The size of BC core and coating thickness was directly measured by
166 CPMA-SP2 tandem system. For the uniform core-shell assumption, the M_R of every D_c
167 was equal to bulk-averaged M_R (Method), as described by Cappa et al. (2019) and Liu
168 et al. (2017). Then the particle-resolved Core-shell Mie theory was employed to
169 calculate the MAC_{BC} of individual BC-containing particles. After obtaining the
170 particle-resolved MAC, we can calculate the MAC of BC particle ensembles as

$$MAC_{BC} = \sum_{i=0}^n MAC_i \times \frac{[BC]_i}{[BC]} \quad (4)$$

171 where MAC_i and $[BC]_i$ are the particle-resolved MAC_{BC} and mass concentration of the
172 BC core, $[BC]$ is the mass concentration of BC particle ensembles, and n is the number
173 of M_p bins. Then, the E_{abs} of BC particle ensembles are calculated as the ratio of MAC_{BC}
174 to MAC_{BC_core} . Note that the MAC_{BC_core} here is calculated using the core-shell Mie
175 model when $D_p/D_c = 1$.

176 The morphology-dependent approach was based on the C_{measured} measured by SP2
177 and C_{modeled} by Core-shell Mie theory at wavelength of 1064 nm. The approach mainly
178 primarily focuses on calculating the optical properties of transition-state BC-containing



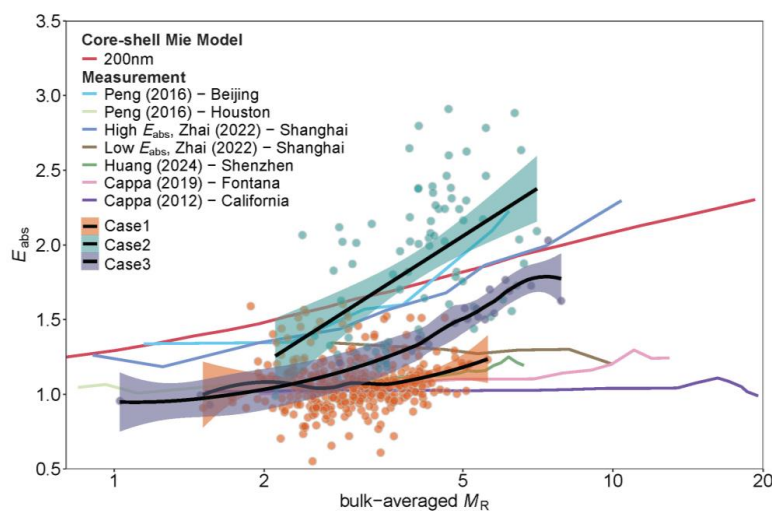
179 particles based on their morphology. In this study, we use the scattering cross-section
180 of transition-state BC-containing particles measured by SP2 at 1064 nm as a reference,
181 establish a mathematical relationship between the C_{measured} and M_R (Fig. 3d, e and f),
182 and use this relationship to calculate the MAC of this portion of BC-containing particles.
183 Then the bulk-averaged MAC was obtained by integrating the MAC of each BC-
184 containing particle.

185

186 3 Results and discussions

187 3.1 Direct observation of different E_{abs} .

188 The average $E_{\text{abs_measured}}$ during the sampling period in Hangzhou is 1.28, and the bulk-
189 averaged M_R is 3.32. Based on the measured E_{abs} , three scenarios were identified (Fig.
190 S7 and Fig. 1). Case 1 spans from September 3 to September 23, 2023, and from
191 October 1 to October 7, 2023. Case 2 covers the period from September 24 to
192 September 30, 2023, while Case 3 runs from October 8 to October 13, 2023. $E_{\text{abs_measured}}$
193 in Case 1 is relatively low, with an average value of 1.09. In contrast, the $E_{\text{abs_measured}}$ in
194 Case 2 and Case 3 is significantly higher, with average values of 1.84 and 1.55,
195 respectively.



196

197 **Figure. 1** Comparison of measured E_{abs} in different observation periods and with
198 previous studies (Peng et al., 2016; Cappa et al., 2012; Zhai et al., 2022; Cappa et al.,
199 2019; Huang et al., 2024). The black solid line represents the fitted smoothing curve of
200 bulk-averaged M_R and measured E_{abs} , with the shaded area indicating the 95%
201 confidence interval of the fit.

202

203 Some studies conducted in cities such as Beijing (Peng et al., 2016), Shanghai
204 (Zhai et al., 2022) have observed a notable increase in $E_{\text{abs_measured}}$. However, in cleaner
205 regions like Shenzhen (Huang et al., 2024), Houston (Peng et al., 2016) and California



(Cappa et al., 2012; Cappa et al., 2019), even when R_{BC} reached approximately 5, many studies reported minimal increases in $E_{abs_measured}$. Fortunately, our observations captured a wide range of $E_{abs_measured}$ values (0.92~1.84), encompassing high, medium, and low levels. In these three cases, $E_{abs_measured}$ showed markedly different evolution patterns during the aging of BC-containing particle populations (Fig. 1). Specially, in Case 1, $E_{abs_measured}$ remained almost unchanged with increasing bulk-averaged M_R . In Case 3, $E_{abs_measured}$ showed a significant increase as bulk-averaged M_R rose, while in Case 2, the increase in $E_{abs_measured}$ was even more pronounced for the same increment in bulk-averaged M_R . Besides, in Case 2, the E_{abs} calculated by the traditional core-shell Mie model ($E_{abs_uniform}$) closely matches the $E_{abs_measured}$, followed by Case 3, which shows a slightly lower level of consistency. However, in Case 1, the $E_{abs_uniform}$ predicted by the traditional core-shell Mie model is significantly higher than the $E_{abs_measured}$. In our subsequent analysis, we will address this discrepancy by exploring both heterogeneity of M_R and morphology.

3.2 Role of mixing state heterogeneity in E_{abs} and direct evidence of morphology of BC-containing particles with increasing coating thickness.

The measurement data were integrated and corrected to quantify the coating-to-black carbon mass ratio (M_R) and morphology of each black carbon-containing particle. The M_R is an important indicator reflecting the aging of BC (Zeng et al., 2024; Li et al., 2024; Liu et al., 2017). Fig. 2a and 2b illustrated significant differences in the normalized number distribution of BC-containing particles at $M_p = 4.35$ fg and 9.38 fg at different period. Specifically, during Case 2 and Case 3, the M_R presents a unimodal distribution, with the peak value increasing with increasing M_p . In contrast, during Case 1, the M_R exhibits a distinct bimodal distribution, and both peak positions shift toward higher M_R values as M_p increases. For example, when $M_p = 4.35$ fg, the two peaks occur at $M_R = 1$ fg and 4.2 fg, respectively, whereas at $M_p = 9.38$ fg, they shift to $M_R = 1.8$ fg and 8.0 fg, respectively. The standard deviation (SD) of $\log_{10}(M_R)$ was used to characterize the heterogeneity of M_R among individual BC-containing at each M_p . The results showed that the SD of Case 1 (0.63) was greater than that of Case 3 ($SD = 0.52$), followed by Case 2 ($SD = 0.48$). In contrast, the $E_{abs_measured}$ exhibited an opposite trend during three corresponding periods, indicating that the greater M_R heterogeneity of BC-containing particles leads to a lower $E_{abs_measured}$. This is further supported by the positive correlation between the difference in E_{abs} (modeled by the uniform core-shell Mie model and measured) and SD (Fig. 2d). In other words, the uniform core-shell model predicts a greater E_{abs} as M_R heterogeneity increases, which leads to a greater discrepancy between the measured and modeled E_{abs} . This discrepancy is primarily due to stems from the uniform core-shell model's simplified treatment of M_R heterogeneity in BC (Romshoo et al., 2024; Wang et al., 2021c).

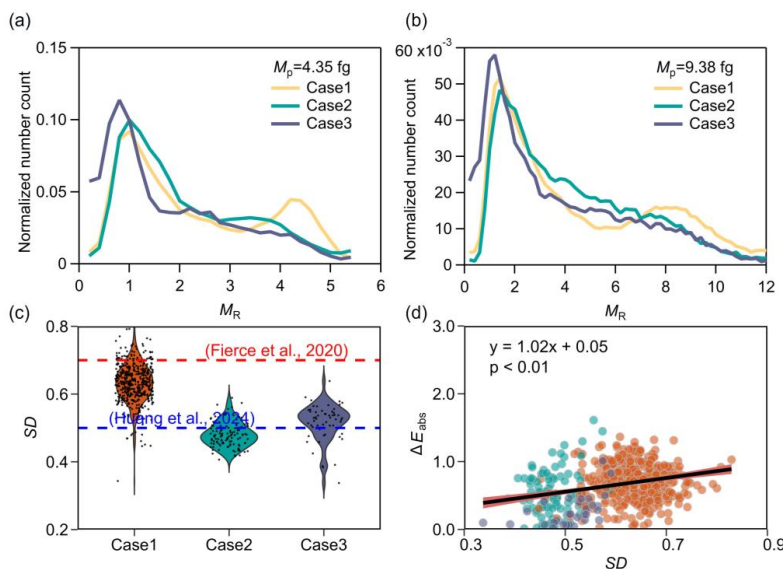
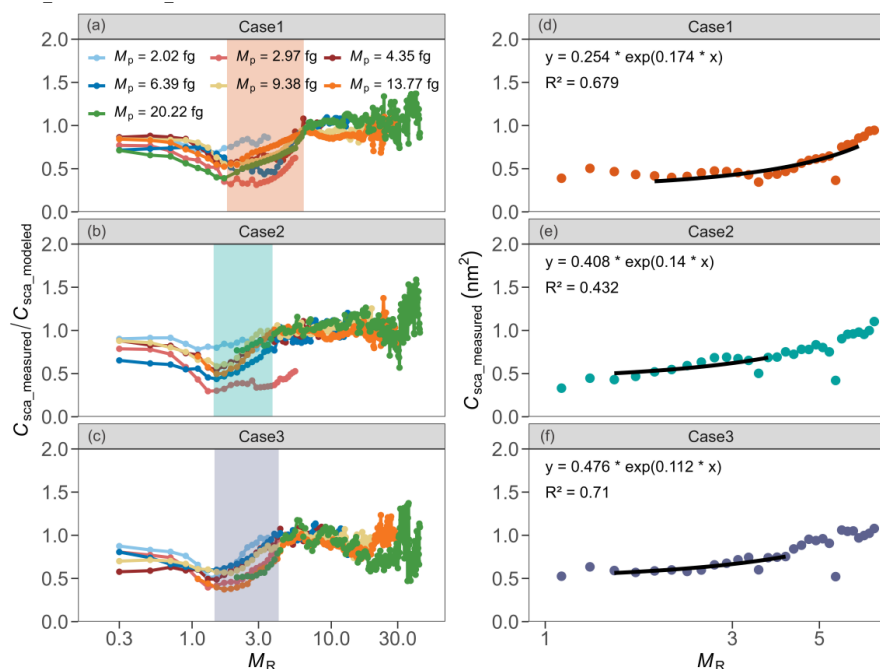


Figure. 2 Heterogeneity of BC-containing particles in different observation periods. The average M_R normalized number distribution of BC-containing particles at $M_p = 4.35$ fg (a) and $M_p = 9.38$ fg (b) during different cases. (c) Comparison of the average standard deviation (SD) of $\log_{10}(M_R)$ in this study with those reported by Huang et al. (2024) and Fierce et al. (2020), the SD characterizes the dispersion of M_R among individual BC-containing particles. (d) Linear fitting of ΔE_{abs} ($E_{abs_uniform} - E_{abs_measured}$) with the SD of $\log_{10}(M_R)$.

The SP2 can measure the scattering cross-section (C_{sca}) of single BC-containing particles, providing insights into their morphology. Fig. 3 presents the variation of the ratio $C_{sca_measured}/C_{sca_modeled}$ with M_R under different M_p . When M_R is relatively low, $C_{sca_measured}/C_{sca_modeled}$ is less than 1, suggesting that the BC core may exist in a fractal structure, remain bare, or are not fully embedded in the coating materials. Consequently, the measured C_{sca} is lower than that calculated by the core-shell Mie model. This observation aligns with the finding by Liu et al. (2017), who classified such BC-containing particles as externally mixed. As M_R increases, the ratio of $C_{sca_measured}/C_{sca_modeled}$ also increases, indicating the BC core becomes more compact and more thoroughly coated, transitioning toward a core-shell structure. Previous studies (Liu et al., 2017; Liu et al., 2020) have referred to BC in this aging stage as being in the “transition state”. However, the M_R criteria for the “transition state” vary across different periods: 1.43-3.78 in Case 2, 1.45-4.19 in Case 3, and higher range of 1.78-6.34 in Case1. This implies that under polluted conditions (Case 2 and Case 3), BC particles can form core-shell structure with less coating material. This can be attributed, on the one hand, to unfavorable meteorological conditions—particularly low wind speed (0.81 m/s)—which facilitated the accumulation and formation of secondary inorganics and organics, accelerating the heterogeneous aging of BC-containing particles. On the other hand, the presence of abundant pollutants originating from



271 Jiangsu and northern Zhejiang (Fig. S7 and Fig. S8) further contributed to this rapid
272 aging process. These factors explain why BC required less coating material to evolve
273 into a core-shell structure in Case 2 and Case 3 compared to Case 1. When M_R exceeds
274 the range associated with the transition state, BC-containing particles predominantly
275 adopt a spherical shape, as further confirmed by the steady ratio of
276 $C_{sca_measured}/C_{sca_modeled}$.



277 **Figure. 3** The morphology and measured optical properties of BC-containing particles
278 as a function of mass ratio (M_R). (a) – (c) show the ratio of measured to modeled
279 scattering cross-section during different cases. The shadows indicate the M_R ranges
280 corresponding to “transition-state” BC-containing particles. (d) – (f) present the
281 measured scattering cross-section as a function of M_R , along with fitted morphology-
282 dependent models representing the “transition-state” BC-containing particles.
283

284 3.3 The predicted E_{abs} during different period.

285 The complexity of BC in the atmosphere depends on various factors, including the
286 size, morphology of the BC core, coating amount, and the interaction between the BC
287 core and the coating. this study retrieves comprehensive multidimensional information
288 on single BC-containing particle, which is subsequently incorporated into the optical
289 model, as shown in Fig. 4. The bias between $E_{abs_uniform}$ and $E_{abs_measured}$ varies across
290 different periods, even when applying the same model input scheme. Specially, the
291 $E_{abs_uniform}$ closely aligns with $E_{abs_measured}$ during Case 2 and Case 3, with deviations
292 below 10%, whereas the deviation increases to as much as to 65% during Case 1,
293 primarily due to the higher M_R dispersion of BC-containing particles in this period. To
294 further investigate this discrepancy, we assume that all BC-containing particles adopt a



core-shell morphology and calculate the E_{abs} of each BC-containing particle based on the measured single-particle M_R . Subsequently, the E_{abs} of bulk BC-containing particles was determined (Method) and compared with $E_{\text{abs_measured}}$ to evaluate their consistency. The results show that for the Case 1, although the discrepancy between the measured and modeled values exhibits a decreasing trend, the average deviation remains as high as 38%. This finding is inconsistent with previous studies (Fierce et al., 2020), which suggest that the M_R heterogeneity of BC-containing particles can largely explain the overestimation of $E_{\text{abs_measured}}$ by the uniform core-shell model. The discrepancy arises because the M_R dispersion of BC-containing particles in that study was lower than the observed value (Fig. 2c) in the present study. However, for Case 2 and Case 3 with higher M_R heterogeneity of BC-containing particles, the error between the model and measured E_{abs} is almost negligible, with deviations below 10%, indicating that the core-shell Mie model can reproduce the observed E_{abs} during these periods. These findings further validate that the degree of M_R dispersion of BC-containing particles is a key factor in determining whether the core-shell Mie model overestimates the observed E_{abs} , and to what extent this overestimation occurs.

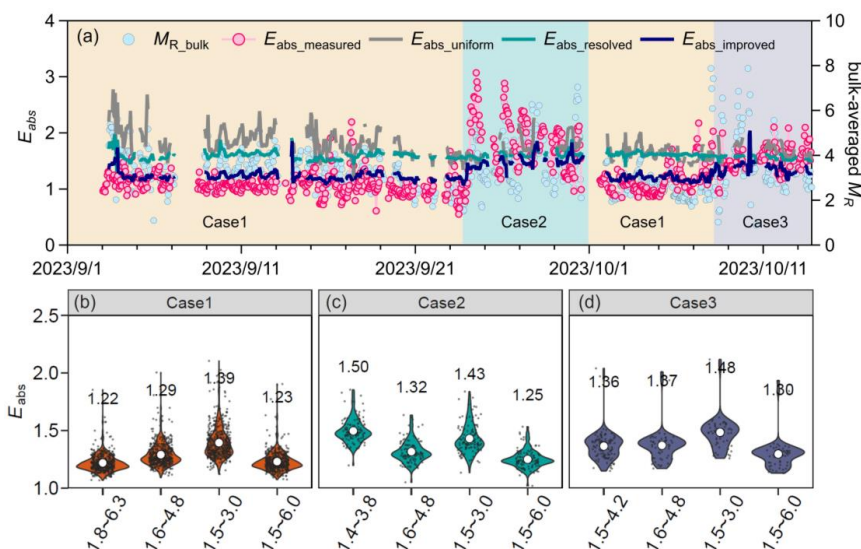


Figure. 4 Comparison of measured and modeled E_{abs} under various different model input schemes. (a) shows the time series of the E_{abs} during the observation period. (b) – (d) were the sensitivity of E_{abs} to the “transition state” range of BC-containing particles. The “transition state” range of 1.6~4.8 was the average value derived from Case 1, Case 2 and Case 3. The range of 1.5~3.0 and 1.5~6.0 was reported by Liu et al. (2017), and Liu et al. (2020), respectively.

The proportion of BC cores embedded in their coatings varies significantly due to differences in atmospheric conditions, which further leads to differences in E_{abs} . Under low non-volatile PM_{10} and low relative humidity (RH) conditions, the proportion of BC cores embedded in the coating was small, resulting in lower E_{abs} (Cappa et al., 2019). However, during the haze period in Beijing (Zeng et al., 2024), intense liquid-phase



chemical reactions produced a large number of inorganic substances, causing rapid aging of BC-containing particles, which significantly increased the degree of BC core embedding and led to higher E_{abs} . The essence of this differences lies in the fact that the BC core lacks sufficient coating material to form a core-shell structure. Therefore, the embedding pattern mainly occurs in the BC-containing particles with small M_R . The chemical composition of PM_{10} especially for nitrate during Case 2 and Case 3 was significantly higher than in Case 1 (Fig. S7), resulting in higher bulk-averaged M_R and E_{abs} for BC. However, during Case 1, the lower concentrations of chemical components of PM_{10} was unfavorable for the formation of BC coatings, thereby leading to lower bulk-averaged M_R and E_{abs} . Therefore, a larger proportion of BC-containing particles remain in a “transition” and externally mixed state (Fig. S9), for which the E_{abs} is considered negligible. Consequently, accurately quantifying the E_{abs} of “transition state” is essential for determine the bulk E_{abs} . To address this, a morphology-dependent approach was developed to calculate E_{abs} of BC-containing particles in the “transition state”, which was achieved by fitting the measured C_{sca} against M_R (Fig. 3d-3f). The improved model yielded an average E_{abs} of only 1.21 during Case 1. For Case 2 and Case 3, although the modeled E_{abs} ($E_{\text{abs_improved}}$) were slightly lower than $E_{\text{abs_measured}}$, the deviation remained within 20%. These findings suggest that the improved model effectively reconcile the E_{abs} of BC-containing particles under different atmospheric conditions.

In recent years, the application of particle-resolved models in multiple field observations has effectively improved the overestimation of observed E_{abs} by uniform core-shell Mie model (Fierce et al., 2020; Li et al., 2024; Jiang et al., 2025). Some studies have also considered the morphology of individual BC-containing particle and developed advanced models such as the electron-microscope-to-BC-simulation (EMBS) (Wang et al., 2021c; Wang et al., 2021b; Chakrabarty et al., 2006), thereby enhancing the accuracy of modeled BC E_{abs} . Although the improved model proposed in this study demonstrates better fitting performance especially under low PM_{10} concentrations conditions (clean periods, Case 1), its accuracy remains highly dependent on the classification of the “transition state.” During heavily polluted periods or in highly polluted regions (Case 2 and Case 3), the “transition state” is usually concentrated within a smaller M_R range, whereas under clean periods, it usually appears in a larger M_R range. If a uniform classification of “transition state” is applied, it will inevitably introduce errors in modeled BC E_{abs} (Fig. 4b, 4c and 4e). Moreover, considering only the M_R heterogeneity of BC-containing particle can effectively reproduce the observed BC E_{abs} in polluted environments. However, applying different model input schemes to varying atmospheric conditions would increase the complexity of radiation model. Therefore, a unified model input scheme that incorporates both M_R heterogeneity and morphology is recommended for all atmospheric conditions. This model input scheme allows for a more consistent representation of BC mixing state while focusing solely on how environmental variations influence the classification of the “transition state”. In summary, improvements to the model should not only account for the M_R heterogeneity, morphological differences of BC-containing particle but also incorporate the dynamic changes in environmental conditions to more accurately predict the optical



properties of BC-containing particles in different atmospheric environments, thereby reducing errors in assessing the climate effects of BC.

4 Conclusions

In this study, we employed the CPMA-SP2 tandem system to investigate the mass ratio of coating and core (M_R), and morphology of BC-containing particles in Hangzhou, China, and to assess how heterogeneity in M_R and morphology influence their E_{abs} under different atmospheric conditions. By dividing the observation into three representative scenarios (Case 1, Case 2, and Case 3), we observed significant differences in the measured E_{abs} , that were closely associated with the evolution and distribution of M_R and morphology characteristics. The findings indicate that both M_R heterogeneity and morphology play critical roles in modeling E_{abs} . During clean condition (Case 1), the uniform core-shell Mie model significantly overestimated E_{abs} , while during polluted periods (Case 2 and Case 3), model predictions were more consistent with the measured E_{abs} . To address these discrepancies, we developed a morphology-dependent correction scheme for the optical property calculation of BC in the "transition state" by incorporating M_R heterogeneity and morphology information. The improved model input method effectively reconciled the measured E_{abs} across varying pollution conditions, especially in clean environments dominated by externally mixed and partially coated BC-containing particles. Our results further show that environmental factors-such as the chemical composition of PM_{10} -not only influence the morphology and M_R distribution of BC-containing particles but also shift the threshold M_R range defining the "transition state". These findings underscore the limitations of uniform model input schemes under complex atmospheric conditions and demonstrate the value of a unified modeling framework that incorporates both M_R heterogeneity and particle morphology. Such improvement enables more accurate representation of BC mixing state and light absorption across diverse environmental settings, thereby reducing uncertainties in assessing the radiative forcing of BC-containing particles.

Data availability. The data are available from the link: <http://doi.org/10.6084/m9.figshare.29097263>.

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Competing interests. At least one of the (co-)authors is a member of the editorial board of *Atmospheric Chemistry and Physics*.

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