



# Kalman filter inversions on NO<sub>x</sub> and VOCs emissions in China using TROPOMI satellite observations

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**Abstract:** Kalman filter inversions with multipollutant may improve the accuracy of inversion results and model performance. A joint inversion of VOCs and NO<sub>x</sub> emissions was conducted using the HCHO and NO<sub>2</sub> column data from the TROPospheric Monitoring Instrument and the simulated sensitivities of VOCs and NO<sub>x</sub> from an air quality model from June to September 2019. The results showed that joint inversion results typically outperformed that of separate inversion in reducing model bias and error and regional variations of emission estimates under satellite data constraints. The inversed NO<sub>x</sub> emissions over China decreased from a priori by approximately 30%, and the inversed VOCs emissions over China increased from a priori by around 50%. Joint inversion results aligned more closely with satellite-observed NO<sub>2</sub> and HCHO columns, capturing the unique belt-like distribution of HCHO and stabilizing maximum NO<sub>2</sub> column at approximately 15molec/cm<sup>2</sup>. The accuracy of simulated ground-level ozone concentrations was enhanced by the joint inversion, with the mean bias decreased by 11.6µg/m<sup>3</sup> overall. Meanwhile, ozone sensitivities prevalently shifted towards NO<sub>x</sub>-limited conditions during summer after the joint inversion.

**Keywords:** Ozone modeling, Decoupled direct method, Kalman filter inversion, Satellite data, VOCs and NO<sub>x</sub> emissions



## 28 1. Introduction

29 Tropospheric ozone ( $O_3$ ), a secondary pollutant, is formed mainly through complex nonlinear photochemical reactions  
30 between  $NO_x$  and VOCs in sunlight. Investigating the nonlinear formation of  $O_3$  and its precursors is complex and difficult.  
31 Since 1990s, countries in Europe and North America have adopted scientific emission control measures for the  $O_3$   
32 precursors ( $NO_x$  and VOCs), resulting in significant decrease in the levels of  $O_3$  concentration (Jiang et al., 2020).  
33 Meanwhile,  $O_3$  precursor emissions from anthropogenic sources have increased significantly in Asia, particularly in China,  
34 along with accelerated urbanization and industrialization. The maximum daily 8h  $O_3$  concentration in summer has gradually  
35 increased, with an average growth rate of up to  $3.73\mu g/m^3$  per year in China overall from 2013–2019 (Li et al., 2020). The  
36 Chinese government has implemented various control measures to reduce  $NO_x$  and VOC emissions in alleviating  $O_3$   
37 pollution. With stringent emission control policies, the total amount of  $NO_x$  and VOC emissions from various sectors of  
38 anthropogenic sources in China were reduced significantly every year, which changes  $O_3$  control strategies simultaneously.  
39 Hence, it is important to have a refined, accurate, and responsive anthropogenic emission inventory.  
40 Earlier Chinese emission inventories were derived from a bottom-up statistical approach with continually updated local  
41 emission data. However,  $NO_x$  emissions have a relatively short lifetime and react quickly in the atmosphere, and the bottom-  
42 up inventories are mostly overestimated, even by a factor of approximately 2, compared to monitored or satellite-observed  
43  $NO_2$  data (Silver et al., 2020). In addition, there is also significant uncertainty occurred in the estimates of VOCs emissions,  
44 leading to inaccurate modeling of  $O_3$  concentrations (Lu et al., 2023). Furthermore, the bottom-up inventories rely on  
45 estimated emission activities to infer the spatial distribution, which can also generate significant uncertainties.  
46 A top-down approach is an alternative way to estimate emissions based on observed air pollutant concentrations and source  
47 characteristics, and can be scientifically and objectively validated and improved through in situ observations, satellite data,  
48 and inverse modeling. Inverse modeling is a mathematical method has been widely used to estimate emission inventory by  
49 minimizing the difference between modeled and observed concentrations (Trombetti et al., 2018). As early as the mid-  
50 1960s, meteorologists applied the least squares method as a basic principle to construct atmospheric inversion models to  
51 reduce the bias between models and observations (Smagorjnsky, 1983). Martin et al. (2003) used a mass balance approach  
52 to invert regional  $NO_x$  emission intensities in conjunction with changes in  $NO_2$  column concentrations from satellite data.  
53 However, since nonlinearity between  $NO_x$  emissions and  $NO_2$  concentrations, this inversion method might underestimate  
54  $NO_x$  emissions.  
55 Many studies have been using various inversion methods to estimate emission inventories in combination with highly  
56 spatially covered satellite observations. Gerbig et al. (2003) and Khattatov et al. (1999) conducted Bayesian-based



57 estimation of emission inventories using satellite data and simulated pollutant sensitivities. Müller en Stavrakou, (2005)  
58 proposed a method that can invert multiple chemical species simultaneously, considering the interactions between chemical  
59 species as one of interacted pollutant undergo changes. Jung et al. (2022), Sourì et al. (2020), and Wang et al. (2020)  
60 conducted several studies on joint inversion of multiple species such as NO<sub>x</sub> and VOCs, SO<sub>2</sub> and NO<sub>x</sub>, and CO and NO<sub>x</sub>  
61 emissions. However, the Jacobian matrix settings in previous studies incorporated only the sensitivities of multiple  
62 pollutant concentrations to self-emissions during inversion process, without considering the cross-sensitivities of species  
63 interactions. It is important to include interspecies interactions from chemical transport models to deal with the nonlinear  
64 relationships in the iterative inversions.

65 The selection of NO<sub>x</sub> and VOCs as focal precursors in this study is driven by their dominant roles in near-surface O<sub>3</sub>  
66 formation over China. While TROPospheric monitoring instrument (TROPOMI) provides observations for multiple ozone  
67 precursors (e.g., CO with lower retrieval uncertainty), NO<sub>2</sub> and HCHO offer superior diagnostic value for local emission  
68 adjustments due to their short atmospheric lifetimes (hours to days) and direct participation in rapid photochemical O<sub>3</sub>  
69 production. In contrast, CO (lifetime ~2 months) influences O<sub>3</sub> indirectly through atmospheric oxidation capacity  
70 modulation, exhibiting lagged and nonlinear effects.

71 The uncertainties in VOCs and NO<sub>x</sub> emission inventory in China pose a challenge for achieving relatively accurate  
72 predictions of O<sub>3</sub> levels. In this study, a discrete Kalman filter (DKF) inversion method of Tang et al. (2013) combined  
73 with the European TROPOMI satellite HCHO and NO<sub>2</sub> data was used to generate a top-down VOCs and NO<sub>x</sub> emission  
74 inventory. The cross-sensitivities of NO<sub>2</sub> and HCHO concentrations to NO<sub>x</sub> and VOC emissions computed by the  
75 Comprehensive Air Quality Model with Extensions (CAMx v7.10)-decoupled direct method (DDM) were also  
76 incorporated into the inversion framework. The joint DKF inversions allowed us quantify NO<sub>x</sub> and VOCs emissions  
77 simultaneously, providing more accurately O<sub>3</sub> precursor emissions to simulate the O<sub>3</sub> formation and its control strategy.

## 78 **2. Inverse modeling method and materials**

### 79 **2.1 TROPOMI NO<sub>2</sub> and HCHO column retrievals**

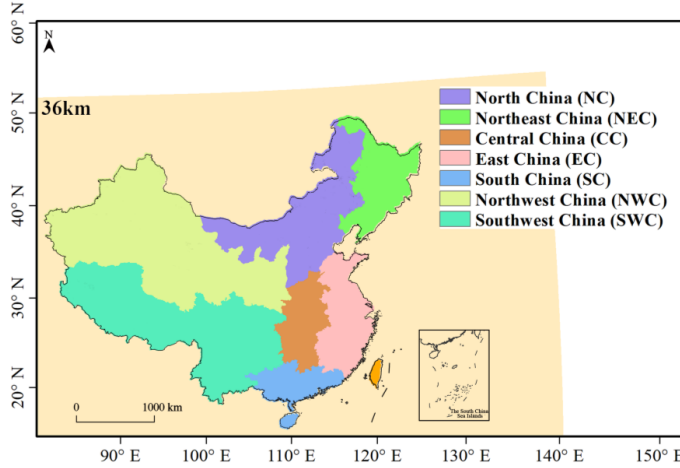
80 TROPOMI on the Sentinel-5 precursor, launched in October 2017, is to continue measuring atmospheric trace gas (e.g.,  
81 NO<sub>2</sub>, O<sub>3</sub>, and HCHO) from the ozone monitoring instrument (OMI) (Levelt et al., 2006), which is still operating after its  
82 launch in July 2004 (Veefkind et al., 2012). Like OMI, the TROPOMI satellite crosses the equator in a sun-synchronous  
83 polar orbit at approximately 13:30 local time with near-UV visible (270 to 500 nm) spectrometers. It has almost global  
84 daily coverage and a wavelength window from 405 to 465 nm. The ground pixel size of the TROPOMI data is



7 km × 3.5 km (5.5 km × 3.5 km after 6 August 2019). It has a higher spatial resolution than previous instruments, a signal-to-noise ratio improvement of approximately 1 to 5 times, and a slant-column density error for individual pixels 30% lower than that for OMI retrievals (20% after 6 August 2019). The TROPOMI data has been well validated and used for top-down emission estimates (Vigouroux et al., 2020). TROPOMI S-5P level 2 data products for NO<sub>2</sub> and HCHO from June to September 2019 were used in this study. Retrievals with quality assurance values greater than 0.7 were extracted and regridded to a resolution of 0.1° × 0.1° in molec./cm<sup>2</sup>, and remapped to matching the modeling grids (units converted to 10<sup>15</sup> molec./cm<sup>2</sup>).

## 2.2 Model settings

The CAMx model version 7.10 (ENVIRON, 2021) was used in this study. The model master grid (36 × 36 km) covered all provinces of China with longitudes of 57°E–161°E and latitudes of 1°N–59°N, with 20 vertical layers and the top height of approximately 20 km, and contained grids of 200 columns × 160 rows (**Fig. 1**). The meteorological data used for the simulations were obtained from the Weather Research and Forecast (WRF) v3.9.1.1 model (Skamarock et al., 2019). The modeled meteorological parameters were verified and demonstrated in the **Supplementary Note 3**. The chemical mechanism, SAPRC07 was chosen for the gas phase chemistry. Photolysis rates used in the CAMx model were calculated using O<sub>3</sub> column data from OMI. The emission inventory of China integrating CO<sub>2</sub> with air pollutants, as reported by Zhi et al. (2024) was chosen as the base emission inventory in this study. The emission data used outside of China was from the Regional Emission inventory in Asia, version 2.1 (REAS2.1; Kurokawa et al., 2019). The Sparse Matrix Operator Kernel Emissions (SMOKE) was used to facilitate the allocation of emissions by sector and the categorization of VOCs and particulate matter. The emissions from natural sources were modeled by the Model of Emissions of Gases and Aerosols from Nature (MEGAN) v3.1. (Guenther et al., 2019).



**Figure 1: 36 km × 36 km domain for the CAMx simulation (different regions shown in various colours).**

High-order DDM (Hakami et al., 2005) is a widely used method for the forward sensitivity analysis, and was used in this study to simulate changes in O<sub>3</sub> concentrations due to NO<sub>x</sub> and VOCs emission perturbations. This method effectively calculated semi-normalized sensitivity coefficients by solving sensitivity equations and the model equations simultaneously. It also has been used as one of the key methods for preparing emission reduction plans and state air quality implementation plans (Liao and Hou, 2015). The sensitivity factor  $S_{ij}^*$  is defined as

$$S_{ij}^* = S_{i,j}^{(1)} + S_{i,j}^{(2)} = P_{i,j} \frac{\partial C}{\partial p_{i,j}} + P_i \frac{\partial}{\partial p_i} \left( P_j \frac{\partial C}{\partial p_j} \right) =$$

$$P_{i,j} \frac{\partial C}{\partial (\epsilon_{i,j} p_{i,j})} + P_i \frac{\partial}{\partial \epsilon_{i,j}} \left( P_j \frac{\partial C}{\partial \epsilon_{j,j} p_{j,j}} \right) = \frac{C}{\partial \epsilon_{i,j}} + \frac{\partial^2 C}{\partial \epsilon_{i,j} \partial \epsilon_{j,j}} \quad (1)$$

where  $i$  and  $j$  are air pollutant types,  $S_{i,j}^{(1)}$  and  $S_{i,j}^{(2)}$  are the semi-normalized first- and second-order sensitivity coefficients,  $C$  is the pollutant concentration,  $P_{i,j}$  is the sensitivity parameter in the base case,  $p_{i,j}$  is the base value of source emissions, and  $\epsilon_{i,j}$  is the perturbation ratio (between 0 and 1).

## 2.3 Inverse modeling

### 2.3.1 Discrete Kalman filter

The Kalman filter theory developed by Kalman (1960) has been widely used from as early as 1983 when Cunnold et al. (1994) applied the Kalman filter to a 2D model to predict the atmospheric lifetime of freon-11 (CFC13). Haas - Laursen et al. (1996) then compared and tested various correction methods for the Kalman filter, showing that the adaptive iterative



approach gave the most accurate simulation results. Following that, a DKF using discrete recursive optimal linear filtering was conducted, directly using the sensitivities of pollutant concentrations to emissions to calculate the nonlinear relation between pollutants and sources through a multiple iteration algorithm (Gilliland and Abbitt, 2001; Prinn, 2013). Using the DKF method combined with satellite observations to derive top-down air pollutant emission inventories and to calculate their possible biases, has recently been performed (Napelenok et al., 2008; Tang et al., 2013). The DKF method is described as

$$\bar{E}_{i+1} = \bar{E}_i + G_i(\bar{C}_i^{obs} - \bar{C}_i^{mod}) \quad (2)$$

$$G_i = A_i S_i^T (S_i A_i S_i^T + R_i)^{-1} \quad (3)$$

$$A_{i+1} = A_i - G_i S_i A_i \quad (4)$$

where  $\bar{E}_{i+1}$  is the updated emission regulator,  $\bar{E}_i$  is the emission regulator at the time of the baseline simulation scenario,  $A_{i+1}$  is the updated emission-related covariance,  $A_i$  is the covariance on emissions at the time of the baseline simulation scenario,  $\bar{C}^{obs}$  and  $\bar{C}^{mod}$  are the observed (satellite data or station monitoring data) and modelled concentrations of an air pollutant respectively, the calculated  $G_i$  is the Kalman gain,  $S_i$  is the sensitivity of the pollutant to emissions at the time of the baseline simulation scenario, and  $R_i$  is the covariance of the observed data. Combining the equations gives

$$\bar{E}_{i+1} = \bar{E}_i + A_i S_i^T (S_i A_i S_i^T + R_i)^{-1} (\bar{C}_i^{obs} - \bar{C}_i^{mod} - S_i \bar{E}_i) \quad (5)$$

At observation correction step time step  $i$ , the inversion process corrects the predicted emissions ( $\bar{E}_i$ ) and the predicted emission covariance ( $A_i$ ) by taking the observations ( $\bar{C}^{obs}$ ) and inverts them to obtain the Kalman gain ( $G_i$ ), then generates the corrected emissions ( $\bar{E}_{i+1}$ ) and the corrected emission covariance ( $A_{i+1}$ ). The iteration stops when the regulation parameter is extremely close to the present value ( $\frac{\bar{E}_{i+1} - \bar{E}_i}{\bar{E}_i} < 0.01$ ).

### 2.3.2 Joint inversion for NO<sub>x</sub> and VOC emissions

Joint inversion considers multiple pollutants within a matrix framework, involving cross-sensitivity coefficients ( $S_{i,j}^{(2)}$ ) and incorporating both simulated ( $\bar{C}_i^{mod}$ ) and observed ( $\bar{C}_i^{obs}$ ) pollutant concentrations, as detailed in Eq. (6) to Eq. (8). The variables in Eq. (5) update as follows:

$$\bar{E}_{i+1} = \bar{E}_i + A_i S_{matrix}^T (S_{matrix} A_i S_{matrix}^T + R_i)^{-1} (\bar{C}_{matrix}^{obs} - \bar{C}_{matrix}^{mod} - S_{matrix} \bar{E}_i) \quad (6)$$

The detailed variables in Eq. (6) are as follows:



$$s_{matrix} = \begin{bmatrix} S_{NOx}^{NO_2(1,1)} & S_{VOC}^{NO_2(1,1)} \\ S_{NOx}^{NO_2(1,2)} & S_{VOC}^{NO_2(1,2)} \\ \vdots & \vdots \\ S_{NOx}^{HCHO(1,1)} & S_{VOC}^{HCHO(1,1)} \\ S_{NOx}^{HCHO(1,2)} & S_{VOC}^{HCHO(1,1)} \\ \vdots & \vdots \end{bmatrix} \quad (7)$$

$$c_{matrix} = \begin{bmatrix} NO_2^{(1,1)} \\ NO_2^{(1,1)} \\ \vdots \\ HCHO^{(1,1)} \\ HCHO^{(1,1)} \\ \vdots \end{bmatrix} \quad (8)$$

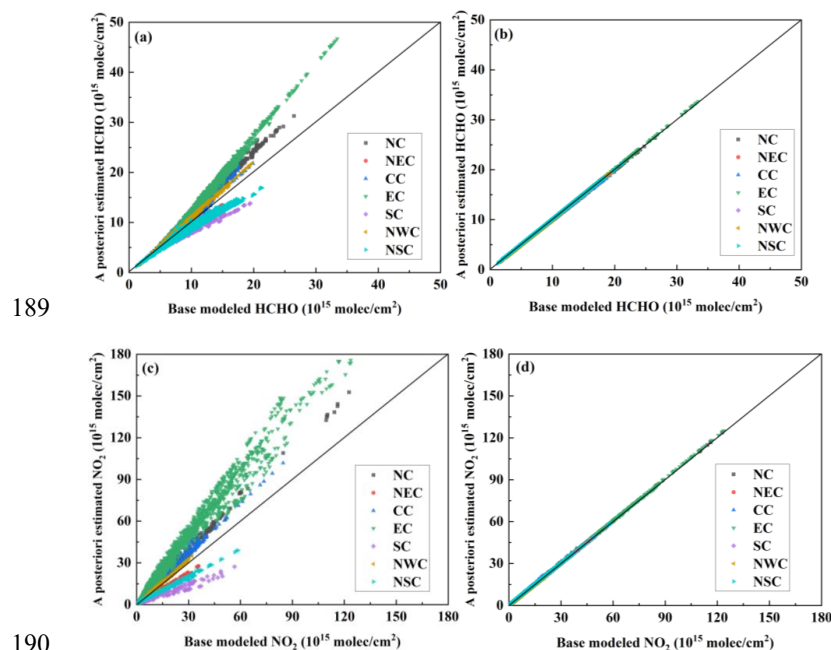
In  $s_{matrix}$  we considered the sensitivity of  $NO_2$  and HCHO concentrations to  $NO_x$  and VOC emissions  $S_{NOx}^{NO_2(1,1)}$  and  $S_{VOC}^{HCHO(1,1)}$  and the sensitivity of  $NO_2$  concentrations to VOC emissions  $S_{VOC}^{NO_2(1,1)}$  and HCHO concentrations to  $NO_x$  emissions  $S_{NOx}^{HCHO(1,1)}$ . In Eq. (7) and Eq. (8), (1,1) in the upper right corner indicates the first row and first column of the simulation grid. The joint inversion approach considered not only the nonlinear chemical feedbacks between  $NO_2$  concentration and  $NO_x$  emission and HCHO concentrations and VOCs emissions, respectively, but also the mutual influence between  $NO_2$  concentration and VOCs emission and HCHO concentration and  $NO_x$  emission, respectively. The emission-related covariance matrix  $A_i$  for the baseline simulation scenario followed a reference setting (H. Sourì et al., 2020), with a set of a priori error of 50% for  $NO_x$  emissions,  $\sigma_i^{ENOx}$ , 150% for VOCs emissions,  $\sigma_i^{EVOC}$ , and  $A_i = \sigma_i^{E^2}$ . An important assumption of the inversion methodology is that inconsistencies between satellite observations and model outputs arise mainly from emission inventories. Whereas the observed data covariance  $R_i$  can also introduce other errors, it ultimately limits only the extent to which the final inversion results are close to the observed values. The error  $\sigma_i^{obs}$  in the satellite data product includes instrumental errors and other uncertainties that were difficult to quantify. In this study, to prevent data instability,  $R_i = \text{Max}[\sigma_{min}^{obs}, \bar{c}_{matrix}^{obs} \times \chi^{obs}]^2$ , with  $\sigma_{min}^{obs}$  being a minimum value of  $0.8 \times 10^{15}$  molec./cm<sup>2</sup> and  $1.0 \times 10^{15}$  molec./cm<sup>2</sup> for the TROPOMI  $NO_2$  and HCHO column concentration, respectively.  $\chi^{obs}$  represents the satellite data uncertainty and was set to 35% for  $NO_2$  and 20% for HCHO column concentrations, respectively. It assumed that both covariance matrices were diagonal matrices. Since the satellite data used in this study were monthly averages, the correction factors were also monthly averages for each month from June to September 2019.

### 2.3.3 Pseudodata test

Before formally inverting the emission inventory with satellite data, a pseudodata test was performed to evaluate the effectiveness of the inversion approach and to ensure that the joint inversion was accurate within the study area. To determine the inversion performance more quickly for a given change in emissions, the pseudodata test was randomly



173 selected for 10 days (July 1<sup>st</sup> to July 10<sup>th</sup>) with the first 3 days as the model start-up and excluded from the calculation. The  
 174 principle of the pseudodata test was to add a known perturbation to the existing inventory, and the perturbation values for  
 175 the test varied randomly from 0.5 to 1.6 (**Table S1**). The simulated concentrations in the baseline scenario were used as  
 176 observed concentrations to invert the perturbed inventory, testing whether the inversion could restore the perturbed  
 177 inventory to its original values.  
 178 As previously mentioned, the pseudodata test also required the emission-related covariance matrix  $A_i$  and the observed  
 179 data covariance  $R_i$ . The a priori errors  $\sigma_i^{ENox}$  and  $\sigma_i^{EVOC}$  for all source regions were assumed to be consistent with the  
 180 formal inversion, setting at 50% and 150% respectively. The observed data covariance  $R_i$  was determined in the formal  
 181 inversion based on the uncertainty of the satellite data product. However, in the pseudodata test, the inversion was used the  
 182 simulated concentrations as the observed concentrations, and the overall process was fully controllable. Hence,  $\chi^{obs}$  was  
 183 therefore set to 0, and the  $\sigma_{min}^{obs}$  for the simulated  $NO_2$  and HCHO column concentrations were set to match the formal  
 184 inversion at  $0.8 \times 10^{15}$  molecules $\cdot$ cm $^{-2}$  and  $1 \times 10^{15}$  molecules $\cdot$ cm $^{-2}$  respectively.  
 185 The pseudodata test results for different regions showed in **Fig. 2**. The inversion approach successfully and simultaneously  
 186 reset the  $NO_x$  and VOCs emissions from the baseline scenario for each region within a few iterations. The corresponding  
 187  $NO_2$  and HCHO column concentrations were well reproduced, and the inversion converged closely to the original emission  
 188 adjustment factors, indicating that the inversion approach was feasible for this study (**Fig. S1**).







191 **Figure 2: Pseudodata analysis for region-based DKF inversion for HCHO (top) and NO<sub>2</sub> (bottom) column concentrations**

### 192 **3. Results**

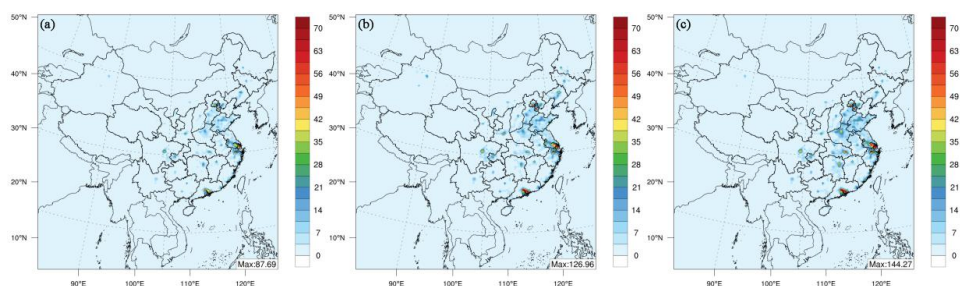
#### 193 **3.1 Comparisons of emission changes under satellite data constraints**

194 A quantitative analysis of NO<sub>x</sub> and VOCs emissions was conducted in different regions in China to assess the effects of  
 195 inversions on emission estimates (**Table 1**). The trends in NO<sub>x</sub> emissions varied across regions. In the North China (NC)  
 196 region, the NO<sub>x</sub> emissions decreased from a prior estimate of 622 tons to 428 tons after joint inversion (a reduction of  
 197 31.2%) and further to 412 tons after individual inversion (a reduction of 33.8%). However, in the Central China (CC)  
 198 region, despite the decrease in NO<sub>x</sub> emissions to 462 tons after individual inversion (a reduction of 34.5%), the emissions  
 199 increased to 1,029 tons after joint inversion (an increase of 45.9%), indicating that interaction between NO<sub>x</sub> and VOCs in  
 200 the inversion may lead to various estimates of emissions. In terms of VOCs emissions, the regional inversion produced  
 201 diverse results as well. In the NC region, the VOCs emissions slightly increased after joint inversion (787 tons, an increase  
 202 of 13.6%) but surged to 1,231 tons via individual inversion (an increase of 77.6%), which might have stemmed from the  
 203 diversity and complexity of VOCs emission sources. Overall, significant variations observed in both inversed NO<sub>x</sub> and  
 204 VOC emission estimates in different regions under different inversion approaches. The inversed NO<sub>x</sub> emissions over China  
 205 decreased from a priori by 39% and 17% via individual and joint inversions, respectively, and the inversed VOCs emissions  
 206 over China increased from a priori by 45% and 55% via individual and joint inversions, respectively.

207 **Table 1. A priori and a posteriori NO<sub>x</sub> and VOCs emissions in different regions in China**

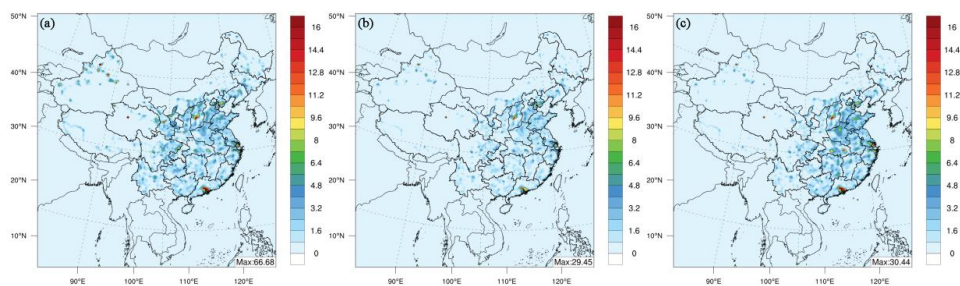
Region	NO <sub>x</sub> emissions			VOCs emissions		
	Posteriori (joint)	Posteriori (individual)	Priori	Posteriori (joint)	Posteriori (individual)	Priori
NC	428	412	622	787	1,231	693
CC	1,029	462	705	2,604	1,465	1,099
EC	1,408	846	1,172	4,634	3,929	3,059
SC	613	405	619	1,516	1,473	962
NWC	740	770	1,776	654	1,250	606
SWC	899	755	1,382	1,295	1,301	960
NEC	847	722	937	1,573	1,521	1,021

208 Spatial distribution analysis of VOCs emissions (**Fig.3**) showed that a priori VOCs emissions were concentrated  
 209 predominantly in densely populated areas such as the Beijing–Tianjin–Hebei (BTH) and its surrounding areas, the Yangtze  
 210 River delta (YRD), and the Pearl River delta (PRD). VOCs emissions in NC and EC regions increased substantially after  
 211 individual inversion. Urban VOCs emissions in CC and Eastern China (EC) significantly increased via joint inversion.



**Figure 3. Spatial distribution of (a) a priori, (b) individual inverted, and (c) joint inverted VOCs emissions with TROPOMI constraints**

In contrast, the spatial distribution of a priori  $\text{NO}_x$  emissions was more dispersed than that of VOCs emissions (**Fig.4**). There was a marked decrease in China's total  $\text{NO}_x$  emissions after individual inversion, while joint inversion has led a reduction of  $\text{NO}_x$  emissions mostly in Western China.



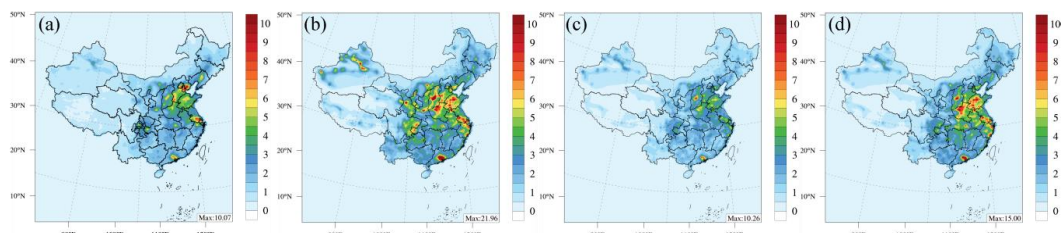
**Figure 4. Spatial distributions of (a) a priori, (b) individual inverted, and (c) joint inverted  $\text{NO}_x$  emissions with TROPOMI constraints**

### 3.2 Effects of inversed emissions on column concentrations

A comprehensive analysis of the  $\text{NO}_2$  and HCHO column concentrations in China was conducted. The modeled results of a priori emissions, individual inversed emissions, and joint inversed emissions were compared with the TROPOMI satellite data to assess the effects of different inversion approaches on column concentrations. The spatial distribution of  $\text{NO}_2$  column concentrations (**Fig. 5**) showed that modeled results by the a priori emissions significantly overestimated  $\text{NO}_2$  levels across central, eastern and northwestern China, with regional maxima up to twice the values observed by TROPOMI. In contrast, the  $\text{NO}_2$  column concentrations obtained through joint inversion showed a spatial distribution more consistent with TROPOMI, aligning with the range of observed concentrations and stabilizing at a maximum of approximately  $15 \text{ molec./cm}^2$ . However, there were slight overestimations persisted in Henan and Shandong Province, possibly due to the application of uniform emission adjustment coefficients in urban areas of the CC and EC regions. On the other hand, a

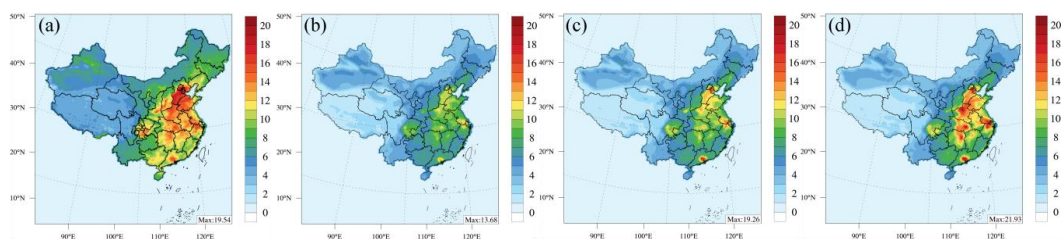


232 marked reduction in NO<sub>2</sub> column concentrations across China was led by the individual inversion, particularly pronounced  
233 in the BTH and the YRD regions.



234  
235 **Figure 5. Spatial distribution of tropospheric NO<sub>2</sub> column concentrations from (a) TROPOMI satellite data, (b) a priori**  
236 **emissions simulation, (c) individual inverted emissions simulation (d) joint inverted emissions simulation for June to September**  
237 **2019**

238  
239 The spatial distribution of the HCHO column concentrations (**Fig. 6**) showed that the HCHO levels observed by TROPOMI  
240 in central EC were considerably higher than those predicted by the a priori emissions, with most areas exceeding  
241 15molec./cm<sup>2</sup>, whereas the simulated values generally fell below 12molec./cm<sup>2</sup>. The simulated HCHO column  
242 concentrations were significantly increased by both individual and joint inversions, with the maximum value reaching  
243 approximately 19molec./cm<sup>2</sup> after individual inversion, closely matching the peak values from TROPOMI. However, a  
244 tendency towards underestimation remained across the overall distribution. Notably, the HCHO column concentrations in  
245 NC, CC, and EC regions yielded by the joint inversion closely resembled the satellite data, successfully capturing the belt-  
246 like distribution characteristic of the TROPOMI HCHO column. Although both individual and joint inversions have  
247 improved the a priori emission estimates, joint inversions have demonstrated a superior alignment with the TROPOMI  
248 observations.



249  
250 **Figure 6. Spatial distribution of tropospheric HCHO column concentrations from (a) TROPOMI satellite data, (b) a priori**  
251 **emissions simulation, (c) individual inverted emissions simulation (d) joint inverted emissions simulation for June to September**  
252 **2019**

253



### 254 3.3 Effects of inversed emissions on ground-level concentrations

255 The inverse modeling adjusted NO<sub>x</sub> and VOCs emissions to bring simulated tropospheric NO<sub>2</sub> and HCHO column  
256 concentrations closer to the TROPOMI satellite retrievals. To verify the accuracy of the inversed emission inventory and  
257 its performance on ground-level O<sub>3</sub> simulations, ground-monitoring data was used to validate the model outputs. A priori  
258 and a posteriori emissions-based simulations of ground-level O<sub>3</sub> concentrations were compared with observed data (**Fig.7**,  
259 NO<sub>2</sub> comparisons are in **Supplementary Note 4**). The joint inversed emission-based simulation significantly improved the  
260 modeled surface O<sub>3</sub> concentrations across China (**Fig. 7**), particularly in the NEC and CC regions, where a priori and  
261 individual inversed-based emission simulations substantially underestimated O<sub>3</sub> concentrations. The model performance  
262 of O<sub>3</sub> simulation in the NWC region improved insignificantly, possibly because the spatial distribution of emissions in the  
263 NWC region were concentrated in certain areas, while the adjustments were applied for the entire region.

264 The model performance statistics were shown in **Table 2**. The correlation coefficient (R) is generally high for both a priori  
265 and a posteriori emissions-based simulations. (More statistical results are in **Figs. S10 and S11**.) In most regions, the joint  
266 inversion outperformed the individual inversion and a priori simulation in terms of normalized mean bias (NMB) and  
267 normalized mean error (NME). Especially in the EC region, the joint inversion achieved NMB and NME values of 0.5%  
268 and 8.7%, respectively, significantly lower than the other two simulations, demonstrating the effectiveness of the joint  
269 inversion in reducing model bias and error. Moreover, the joint inversion simulation also showed significant reductions in  
270 mean bias (MB) and mean error (ME), indicating that the model predictions were very close to the actual observations.

271 The joint inversion simulation had lower root mean square error (RMSE) than that of the individual inversion and a priori  
272 simulation in most regions, showing better performance in improving model accuracy. The observation mean and the model  
273 mean served as an indicator for the model predictive precision. In various regions, the model mean derived from the joint  
274 inversion approach had a closer correspondence to the observation mean, particularly pronounced in the NC, EC, and SC  
275 regions of China, thereby reinforcing the advantage of the joint inversion approach in improving the model performance.

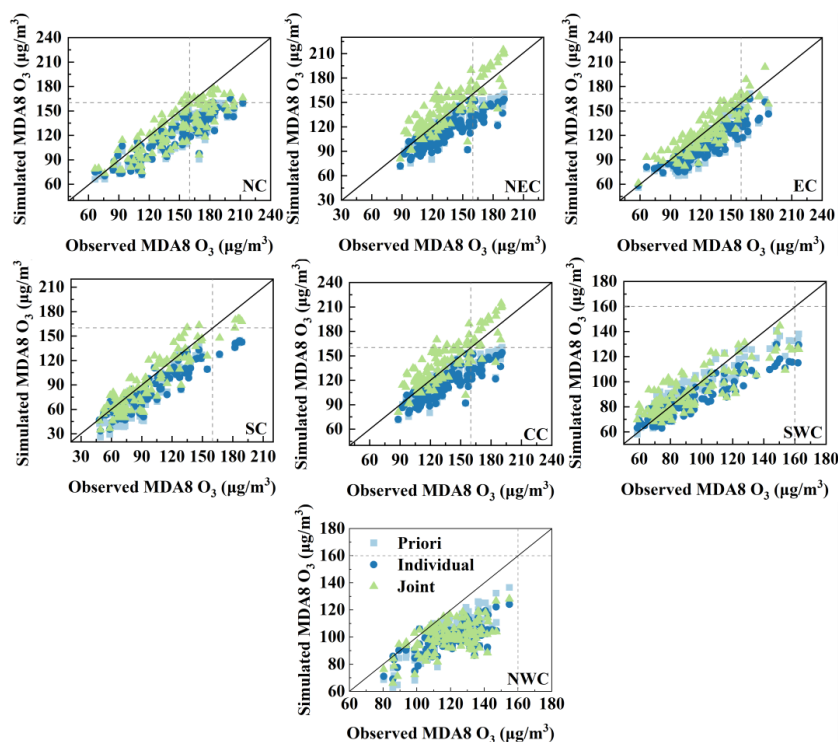


Figure 7. Simulated ground-level MDA8 O<sub>3</sub> concentrations by a priori, individual inversed, and joint inversed emissions against the ground monitored data at different regions in China



**Table 2. Model performance of simulated MDA8 O<sub>3</sub> concentrations against observations in different regions in China. (*R* – correlation, NMB – normalized absolute bias, NME – normalized absolute error, MB – mean bias, ME – mean error, RMSE – root mean square error, Obs. – observation mean, Mod. – model mean)**

		<i>R</i>	NMB (%)	NME (%)	MB (µg/m <sup>3</sup> )	ME (µg/m <sup>3</sup> )	RMSE (µg/m <sup>3</sup> )	Obs. (µg/m <sup>3</sup> )	Mod. (µg/m <sup>3</sup> )
Individual		0.79	-12.9	15.4	-13.2	15.6	19.5	100	87
Joint	NEC	0.79	-9.9	13.7	-10.2	14.0	17.8	100	90
a Priori		0.79	-13.9	15.6	-14.0	15.8	20.0	100	86
Individual		0.88	-17.7	18.3	-26.4	27.1	29.6	146	119
Joint	NC	0.86	-10.4	12.8	-16.3	19.4	22.3	146	129
a Priori		0.87	-17.9	18.0	-26.6	26.7	29.4	146	119
Individual		0.90	-13.9	14.3	-17.8	18.4	20.9	128	110
Joint	EC	0.89	0.5	8.7	0.2	11.0	13.3	128	128
a Priori		0.90	-13.5	13.9	-17.5	18.0	20.8	128	110
Individual		0.86	-15.8	16.8	-15.2	16.2	20.2	99	83
Joint	SC	0.86	-4.7	12.3	-3.7	11.6	14.2	99	95
a Priori		0.86	-17.9	18.4	-16.9	17.5	21.4	99	82
Individual		0.89	-15.4	15.5	-20.9	21.1	24.5	136	115
Joint	CC	0.89	5.9	10.7	8.0	14.5	17.3	136	144
a Priori		0.89	-12.7	13.0	-17.5	17.8	21.4	136	118
Individual		0.75	-17.1	17.2	-21.0	21.1	22.7	120	99
Joint	NWC	0.67	-15.6	15.9	-19.3	19.6	21.8	120	100
a Priori		0.77	-14.9	14.9	-18.1	18.2	20.2	120	102
Individual		0.93	-8.8	11.9	-9.0	11.6	14.6	94	85
Joint	SWC	0.90	-0.4	12.2	-1.1	11.3	14.4	94	93
a Priori		0.93	-1.4	9.0	-1.9	8.5	10.4	94	92

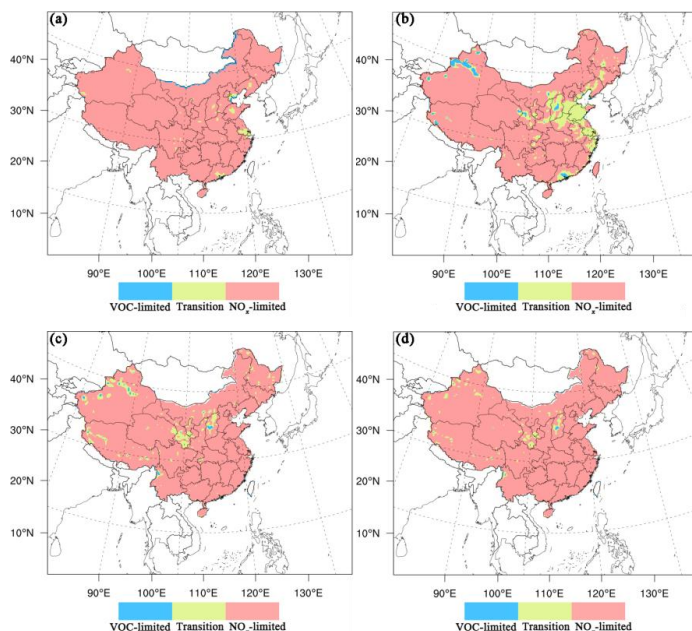
### 3.4 Effects of inversed emissions on O<sub>3</sub> sensitivities

To explore the effect of different inversion approaches on the O<sub>3</sub> sensitivities, the spatial distributions of the O<sub>3</sub> formation regimes derived from OMI satellite data and various inversion approach simulations were analysed for June to September 2019 (**Fig. 8**). OMI satellite-based O<sub>3</sub> sensitivity showed that most regions in China are predominantly NO<sub>x</sub>-limited for O<sub>3</sub> formation during the summer, with VOC-limited or transitional regime present in some key areas such as BTH, YRD, and PRD. This pattern is consistent with the findings from Wang et al. 2023.

In addition, the a priori emission simulation results shown in **Fig. 8b** illustrated a broader range of transitional regimes in NC and EC, especially in key areas such as BTH, YRD, and PRD, which was more extensive compared to those demonstrated by the satellite-based results in **Fig. 8a**. However, O<sub>3</sub> sensitivities simulated by the individual inversed (**Fig. 8c**) and the joint inversed (**Fig. 8d**) emissions showed significant differences compared to that from a priori emission simulation. Although some systematic noise in the central region of China were observed in both inversion simulations, the sensitivities indicated that most regions in China had shifted to NO<sub>x</sub>-limited regimes.



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297 **Figure 8. Spatial distributions of  $O_3$  sensitivities from (a) satellite data-derived, (b) a priori emissions, (c) individual inverted**  
298 **emissions, and (d) joint inverted emissions simulations for June–September 2019**

#### 299 4. Conclusion and discussion

300 The findings of this study offered critical insights into the effects of inversion approaches on the top-down  $NO_x$  and VOCs  
301 emission estimates, and the consequential influences on  $O_3$  sensitivity simulations in China. The analysis emphasized the  
302 significant regional variability in the a priori and a posteriori emission estimates, with the NC region demonstrating a  
303 substantial reduction in  $NO_x$  emissions, reaching 31.2% after joint inversion and further to 33.8% following individual  
304 inversion. However, contrasting results were observed in the CC region, where the joint inversion increased  $NO_x$  emissions  
305 by 45.9%, while the individual inversion decreased  $NO_x$  emissions by 34.4%. Although the NC region was observed a  
306 slight increase of VOCs emissions after the joint inversion, individual inversion led to a significant boost of VOCs emission  
307 estimates, indicating that various estimates of emissions may resulted in different inversion approaches, and the mutual  
308 influence of  $NO_x$  and VOCs cannot be neglected in the inversion process.

309 Overall, the inversion brought down  $NO_x$  emissions over China by approximately 30% and brought up VOCs emissions  
310 over China by around 50%. This  $NO_x$  reduction trend aligns with prior multi-species inversion studies, which consistently  
311 report decreasing  $NO_x$  emissions over eastern China (Qu et al., 2017; Souri et al., 2020; Wang et al., 2020). Satellite-





312 constrained inversions, including ours, show steeper declines than a priori inventories, especially in industrial hotspots like  
313 the North China Plain (NCP) and Yangtze River Delta. Notably, Wang et al. (2020) documented smaller national decreases  
314 (5.8%–6.5%) but similarly large localized drops (up to 40% in the NCP). Discrepancies emerge in central and western  
315 China: while our results show local NO<sub>x</sub> increases, Wang et al. (2020) reported 3%–8% decreases, potentially due to  
316 differences in a priori inventories or satellite data limitations (Qu et al., 2022). For VOCs, our inferred ~50% national  
317 increase is consistent with evidence of widespread underestimation in East Asia. Sourì et al. (2020) found a 25% post-  
318 inversion rise in the NCP, and Choi et al. (2022) reported a 47% total increase using hybrid inversion methods, supporting  
319 the robustness of VOCs underestimation.

320 The joint inversion simulation generally outperformed that of individual inversion in reducing model bias and error and  
321 improving the correlation coefficients between model predictions and observations. In EC, the joint inversion simulation  
322 achieved a NMB of 0.5% and a NME of 8.7% compared to the observed data, which were significantly lower than those  
323 of the individual inversion and a prior emission-based simulations. In addition, the joint inversion approach had a closer  
324 alignment with TROPOMI-observed NO<sub>2</sub> and HCHO column concentrations, effectively capturing the the belt-like  
325 distribution of HCHO, and with a stabilized maximum column concentration of approximately 15 molec./cm<sup>2</sup> for NO<sub>2</sub>. The  
326 model performance of ground-level O<sub>3</sub> concentration simulations were significantly enhanced by the joint inversion  
327 approach, especially in the regions like NEC and CC, where a priori emission-based simulations significantly  
328 underestimated O<sub>3</sub> levels. Furthermore, the O<sub>3</sub> formation regimes over China predominantly shifted towards NO<sub>x</sub>-limited  
329 conditions during the summer using inversed emissions.

330 Notwithstanding these findings, several limitations warrant consideration: (1) Satellite data uncertainties (coarse resolution  
331 masking urban sources; monthly TROPOMI averaging obscuring short-term variability) coupled with inversion sensitivity  
332 constraints; (2) Chemical interference (e.g., NH<sub>3</sub> uncertainty propagating NO<sub>x</sub> errors via nitrate chemistry); (3) Temporal  
333 and spatial mismatches in a priori inventory leading to biased adjustments; (4) Targeting total VOC emissions rather than  
334 individual species may affect model simulations of secondary organic aerosols, thereby impacting inversion accuracy.

335 To sum up, this study emphasized the critical role of inversion approaches in refining emission estimates and enhancing  
336 the accuracy of atmospheric models. Although the joint DKF inversion approach appears to offer several advantages over  
337 individual DKF inversion, it is crucial to continue exploring and refining these methods to address the remaining  
338 uncertainties and improve our understanding of air pollution dynamics. Furthermore, we quantitatively assess the causal  
339 impacts of these emission adjustments on regional O<sub>3</sub> sensitivity regime transitions. Future research could focus on  
340 integrating various observational data sources into the inversion process, such as satellite data, ground-based and aircraft





measurements, to further enhance the accuracy and reliability of inversion-derived emission estimates and their implications for air quality management and policy-making.

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### Code/Data availability

The data used in this study are available from the corresponding author upon request ([tangwei@craes.org.cn](mailto:tangwei@craes.org.cn)).

### Author contribution

XD and WT designed the research, analyzed data, and prepared the manuscript. CY provided TROPOMI HCHO and NO<sub>2</sub> satellite data. JH provided data modification suggestions. ZZ performed meteorological simulations. YY performed air quality model calculations. YL provided emission inventory calculations. MC and FM commented on the manuscript.

### Competing interests

The authors declare that they have no conflict of interest.

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