



# Impact of reduced non-Gaussianity on analysis and forecast accuracy by assimilating every-30-second radar observation with ensemble Kalman filter: idealized experiments of deep convection

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**Abstract.** This study investigates the impact of very high frequency data assimilation on analysis and forecast accuracy with the local ensemble transform Kalman filter for idealized deep convection. Previous studies showed that assimilating every 30 seconds data from Phased Array Weather Radar (PAWR) alleviates the problem of strongly non-Gaussian error probability distribution due to rapid nonlinear evolution of deep convection in real-world cases. This study aims to understand better the pure impact of non-Gaussian distribution and performs perfect model observing system simulation experiments with radar reflectivity every 5 minutes and 30 seconds. The idealized experimental settings have unique advantage in verifications for unobserved variables since it was unclear in the previous studies with real-world data. The results show that every 30 seconds data assimilation contributes to a significant improvement of the analysis accuracy, particularly for vertical velocity associated with strong convection, although the impact on the forecast accuracy is limited. We also find a significant reduction in the non-Gaussianity of first guess ensemble. The impact of assimilation frequency on reducing non-Gaussianity is enhanced when the uncertainty in background wind or stability is included in the initial ensemble perturbation.

## 1 Introduction

The use of convection-permitting numerical weather prediction (NWP) models is now becoming a standard practice for short-range precipitation forecast. It is complementary to nowcasting based on simple extrapolation of the precipitation image motion or optical flow. The forecast by NWP models is expected to provide a better representation of precipitation than the forecast by optical flow for a lead time beyond a few hours (Sun et al., 2014; Clark et al., 2016).

Important information on precipitation in convection-permitting NWP models is provided mainly by data assimilation of Doppler weather radars. Currently, most operational centers apply a variational data assimilation method at a 1-hour interval, with radar reflectivity incorporated through latent heat nudging (Gustafsson et al., 2018). Alternatively, the ensemble Kalman filter (EnKF) has also been extensively studied because of its low implementation cost without the need for adjoint models. As EnKF favors sequential data assimilation with a shorter interval than the window length of four-dimensional variational data assimilation (4D-Var) (Fertig et al., 2007), it is common to perform data assimilation cycles with the same frequency as the available observation, typically 5 minutes for most current operational weather radars (Schraff et al., 2016).



The non-Gaussianity of error probability distribution is a major problem for the convective scale EnKF with radar data. Here, the strong non-Gaussianity can be caused by nonlinear observation operators and rapid nonlinear evolution of state variables. The non-Gaussianity makes the analysis based on the EnKF suboptimal (Lei et al., 2010). In this study, we are motivated to investigate the impact of non-Gaussianity on analysis and forecast accuracy with convective-permitting NWP.

Assimilating radar data at an interval shorter than 5 minutes can mitigate the non-Gaussianity problem. Previous studies used the phased array weather radar (PAWR) in Japan with observation interval of 30 seconds. They assimilated PAWR data every 30 seconds using the local ensemble transform Kalman filter (LETKF) to capture the rapid growth of localized intense thunderstorms in metropolitan areas of Japan (Miyoshi et al., 2016b, a; Maejima et al., 2017; Honda et al., 2022; Miyoshi et al., 2023). Other studies also performed high-frequency data assimilation with different phased array radar systems (Kuster et al., 2015; Wu et al., 2018; Huang et al., 2020; Stratman et al., 2020; Huang et al., 2022; Palmer et al., 2022).

Some studies have demonstrated the advantage of frequent data assimilation with an interval of less than 5 minutes. Xue et al. (2006) discussed the possible use of the Collaborative Adaptive Sensing of the Atmosphere (CASA) radar system with a frequent observation mode, showing improved analysis accuracy of dynamical variables by assimilating radar data with 1 or 2-minute intervals. Maejima and Miyoshi (2020) studied the impact of changing the window size of the four-dimensional LETKF in the real case observed by Osaka PAWR and reported the advantage of assimilation interval of less than 3 minutes. Maejima et al. (2022) performed an observing system simulation experiment (OSSE) for a hypothetical network of PAWR in western Japan and showed that the assimilation of radar observation every 30 seconds is more effective than the case with every 5 minutes in predicting the observed heavy rain distribution. Ruiz et al. (2021) investigated the non-Gaussianity by assimilating the Osaka PAWR data using the LETKF with 1000 members and showed significant reduction of non-Gaussianity and differences of the analysis mean value of vertical winds by the assimilation interval of 30 seconds compared with 1, 2 and 5 minutes. However, the previous studies used real-world data without sufficient verification data for unobserved variables. Additionally, in real-world cases, it is difficult to distinguish the effect of non-Gaussianity from other factors which may degrade the analysis and forecast performances, such as the errors in the model physics and observation operators, limited observation coverage, and multi-scale background error structure.

In this study, we perform a series of idealized OSSEs to investigate the impact of assimilating radar observation at very high frequency on the non-Gaussianity, the analysis accuracy for the variables which are not directly observed, and the accuracy of extended ensemble precipitation forecast. We carefully design the OSSEs as simple as possible, so that we exclude complex factors other than non-Gaussianity. The findings of this study would provide insights into future designs on convection-permitting NWP with radar data assimilation, even though every 30 seconds radar data assimilation is a very limited practice at this moment. The investigation on non-Gaussianity would be useful in relation to future studies on non-Gaussian data assimilation methods.

This paper is organized as follows. Section 2 describes idealized OSSEs with the assimilation of radar reflectivity every 30 seconds. Section 3 shows the results of the experiments in terms of analyses and extended ensemble forecasts, followed by an investigation on the impact on 30 seconds data assimilation on the non-Gaussianity of the ensemble perturbation and its



impact on the analysis fields. Section 4 discusses the influence of larger-scale uncertainty based on the results of additional experiments. Section 5 provides a conclusion.

## 60 2 Methodology

### 2.1 Overall experimental design

We first describe the overall strategy of the OSSEs in this study. We focus on the impact of assimilating radar observation with a very high frequency on the non-Gaussian characteristics of the background error of state variables and the accuracy of analysis and extended forecast. Therefore, in the first set of experiments, we exclude other factors which we usually have in  
65 real-world applications and significantly affect the performance of data assimilation.

First, we perform perfect-model OSSEs, in which the nature run is generated by the same model as the one used in data assimilation experiments. We also use the same observation operator for generating synthetic observations to be assimilated and for the verification purpose in the observation space.

Second, we study the ideal case of a single deep convection triggered by a warm bubble in a conditionally unstable atmo-  
70 sphere. This simplifies the causal relationship between the evolutions of hydrometeors and winds. This causal relationship is often complex with multi-scale interactions in the real world. In addition, we assume only convective-scale uncertainty in the initial ensemble by perturbing only warm bubbles while using the same vertical profiles for the initialization of each member.

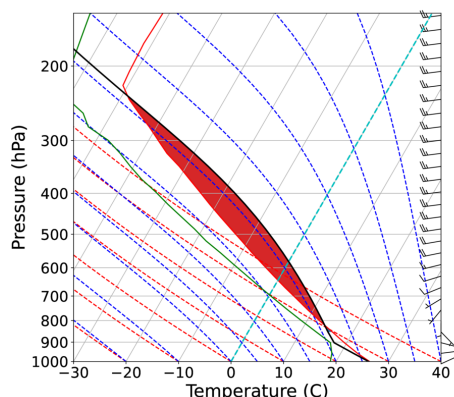
Third, we use a large ensemble size for ensemble data assimilation to reduce the effect of sampling error. Also, inflation methods are not applied such as additive or multiplicative covariance inflation, relaxation to prior spread (RTPS), and relaxation  
75 to prior perturbation (RTPP), even though these applications might improve the analysis accuracy. This would exclude modifications to the ensemble perturbations and help focus on the impact of analysis frequency on non-Gaussianity of ensemble perturbation.

In addition to this highly idealized set of OSSEs, we also perform complementary experiments with more realistic settings, which apply perturbations in the thermal and wind background vertical profiles. This is closer to a real-world data assimilation  
80 problem where the first guess has uncertainty not only at a convective scale but also at larger scales.

### 2.2 Model and the nature run

In this study, we use the Scalable Computing for Advanced Library and Environment Regional Model (SCALE-RM; Nishizawa et al. (2015)) as a NWP model. The SCALE-RM employs a single-moment 6-category cloud microphysics parameterization of Tomita (2008), a Smagorinsky-type subgrid-scale turbulence parameterization of Smagorinsky (1963), and the level 2.5  
85 closure of Mellor-Yamada Nakanishi-Niino type boundary layer parameterization (Nakanishi and Niino, 2004). Radiation and convective cloud parameterizations are not used in the experiments of this study.

We simulate the development of a deep convective cloud with a following idealized setting. The computational domain is 3-dimensional and has a  $160 \text{ km} \times 160 \text{ km}$  horizontal extent with a 16 km model top. The grid spacing is regular, 1 km



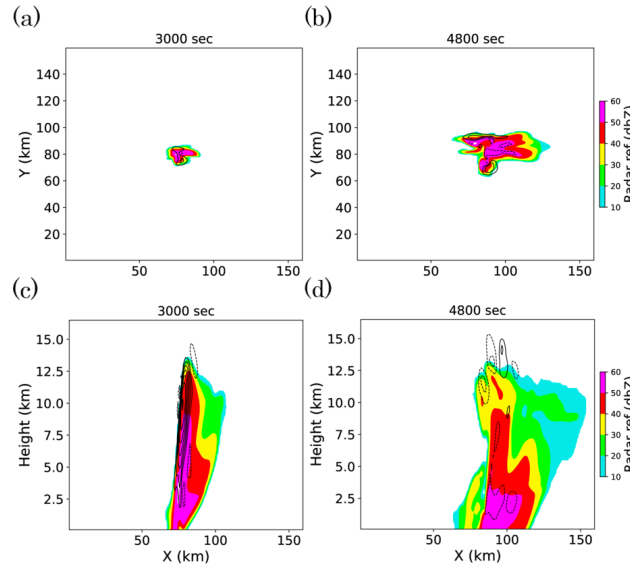
**Figure 1.** A skew-T plot of background atmospheric thermal profile of the experiment. The red shaded area corresponds to the convective available potential energy (CAPE). The profile of horizontal wind is shown on the right side of the figure.

horizontally and 200 m vertically. Lateral boundary conditions are periodic in both the X and Y directions. Vertical profiles  
90 of horizontal wind, temperature, and specific humidity are prescribed to set the initial condition. To trigger a convective cell,  
a warm bubble is imposed near the center of the domain. The center of the warm bubble is 75 km from western and southern  
boundary of the domain and 3 km height from the surface. The warm bubble has a positive temperature anomaly with a 3-  
dimensional Gaussian shape, with horizontal and vertical length scales of 25 km and 1.5 km, respectively. With these settings,  
we first performed a single forecast to create a time series of model state variables which is considered the truth. We hereafter  
95 call it the "nature run".

Figure 1 shows the skew-T plot of the vertical profile of the initial background state of the atmosphere. It has convection  
available potential energy (CAPE) of  $1655 \text{ J kg}^{-1}$  and a strong westerly wind shear. Figure 2 shows the time evolution of the  
nature run in radar reflectivity calculated by the observation operator, which is described in the next section. The warm bubble  
triggers an intense deep convective cell that reaches the maximum cloud top height in about an hour. Then the area of strong  
100 reflectivity starts to unfold and eventually evolves to two major cells, while the entire system moves eastward.

### 2.3 Data assimilation system and the synthetic observations

We use the data assimilation system known as the SCALE-LETKF, which is the combination of the LETKF with the SCALE-  
RM. The SCALE-LETKF for radar data assimilation was developed and utilized in previous studies (Miyoshi et al., 2016a, b;  
Maejima et al., 2017; Amemiya et al., 2020; Honda et al., 2022). The SCALE-LETKF directly assimilates radar reflectiv-  
105 ity using the observation operator obtained by the radar simulator using the same particle size distribution settings with the  
microphysics scheme of the model (Amemiya et al., 2020). The SCALE-LETKF was implemented for successful real-time  
demonstrations of 30-second refresh NWP in 2020 with 50 ensemble members (Honda et al., 2022) and in 2021 during Tokyo  
Olympic and Paralympic games with 1000 ensemble members (Miyoshi et al., 2023).



**Figure 2.** Radar reflectivity (color shades) and vertical velocity (thin black contours with an interval of  $5 \text{ m s}^{-1}$ ) of the nature run at (a,b) 2 km height level and (c,d) the vertical cross section along  $Y = 80 \text{ km}$  (horizontal black lines in a,b). The snapshots at (a,c) 50 minutes and (b,d) 80 minutes from the initial time are shown.

Synthetic observation is generated from the time series of the nature run every 30 seconds. In this study, we assume that the radar reflectivity is observed throughout the domain, at every grid point of 1 km interval both horizontally and vertically. For simplicity, the scanning geometry and the attenuation effect depending on the radar location are not considered. The assimilation or Doppler velocity is also not considered. Radar reflectivity is calculated from the density and hydrometeor mixing ratios of the nature run using the same observation operator used in the SCALE-LETKF, adding random errors from the Gaussian distribution with the standard deviation of 5.0 dBZ.

Following the method of Aksoy et al. (2009), reflectivity values below 10 dBZ are adjusted to 5 dBZ and considered as 'no-precipitation' signals, separated from 'precipitation' signals which are equal to or above 10 dBZ. The localization with an approximate Gaussian function of Gaspari and Cohn (1999) is applied, with horizontal length scales of 4 km and 2 km for precipitation and no-precipitation observations, respectively. The vertical length scale is set to 2 km for both of them. These settings are the same with Ruiz et al. (2021). We use 100 members for all experiments, which we consider large enough for this study. We set the threshold of the number of members which has a 'precipitation' signal at a grid point for the observed radar reflectivity to be assimilated. In this study, the lower limit is set to 1 for both 'precipitation' and 'no-precipitation' observations. We also set the upper limit of the number of observations assimilated at a grid point to 100, which is equal to the ensemble size.

We perform data assimilation experiments with three different configurations, namely, (i) 5-minute 3D-LETKF (hereafter called 5MIN-3D), which uses only the reflectivity observed every 5 minutes, (ii) 5-minute 4D-LETKF (hereafter called 5MIN-



4D), which uses observations of every 30 seconds within the 5-minute time window from the previous to the current analysis time, and (iii) 30-second 3D-LETKF (hereafter called 30SEC), which assimilates the observation every 30 seconds. The 5MIN-4D case does not use temporal localization, setting the same weight to all observations in a time window. Therefore, the 5MIN-4D and 30SEC use the same observation information in total, while they differ in the assimilation frequency.

## 130 2.4 Initial ensemble perturbation

The design of initial ensemble perturbation is crucially important for the data assimilation with the LETKF, as it largely determines the characteristics of the multi-scale and multi-variable background error covariance. In this study, as mentioned above, we simplify the problem by setting the idealized initial perturbation. We use the same vertical profile with that of the nature run, to initialize the state variables of all the members. We perturb the location and intensity of the warm bubble, with  
 135 a spatial scale comparable to the size of the convective cell. Further, we add the small random band-pass-filtered potential temperature perturbation over the entire domain. With these initial perturbations, the first guess ensemble at the first data assimilation cycle is expected to have strongly non-Gaussian perturbations with a spatial structure at a convective scale. The parameters used for these perturbations are summarized in Table 1.

	Variable	Perturbation type	mean and standard deviation
Warm bubble	Potential temperature	Maximum intensity	Mean: 1 K Std. dev. : 0.2K
		Center location	Mean: 75 km in X and Y Std. dev. : 25 km in X and Y
Whole domain	Potential temperature	Additive noise	Mean: 0 K Std. dev. : 0.2 K (domain average) 3-D bandpass filter: 4 km - 40 km

**Table 1.** The initial perturbation properties.

## 2.5 Verification methods

140 For each of the three experiments, we perform data assimilation cycles for 50 minutes from the initial time (corresponding to figures 1a - 1c) and evaluate the analysis. We also perform a 30-minute ensemble forecast from the analysis ensemble at that time step.

We compare the performances of the analyses and extended forecasts among different data assimilation settings. We particularly focus on the non-Gaussianity of first guess ensemble vertical velocity and the accuracy of analysis mean vertical velocity  
 145 in comparison with the nature run, as it is thought to be one of the most difficult variables to properly estimate from radar observation (Fabry and Meunier, 2020), and has been shown to have a strong sensitivity to the data assimilation interval in the real-world case (Ruiz et al., 2021). For extended forecasts, we mainly evaluate the ensemble mean accumulated surface



precipitation, as it is the most important forecast variable in practice. To quantify the non-Gaussianity of a univariate probability distribution, we use the Kullback–Leibler divergence (KLD) against the Gaussian distribution having the same mean and variance. As we calculate the KLD from the ensemble of finite size, we approximate it by kernel density estimation. Suppose that we have a standardized ensemble of a variable  $x_k$  ( $k = 1 \dots K$ ). The estimated probability density using Gaussian kernel is,

$$p(x) = \frac{1}{Kh} \frac{1}{\sqrt{2\pi}} \sum_{k=1}^K \exp\left(-\frac{(x - x_k)^2}{2h^2}\right), \quad (1)$$

where  $h$  is a kernel bandwidth, which is determined adaptively as follows.

$$h = 1.059 * K^{-0.2} \quad (2)$$

Then the KL divergence is calculated numerically as follows.

$$KLD(P||Q) \sim \sum_j^J p_j \ln \frac{p_j}{q_j}, \quad (3)$$

where  $p_j$  and  $q_j$  are the values at the center of each bin, for the estimated density  $p(x)$  and the normal distribution  $q(x)$  respectively.

## 3 Results

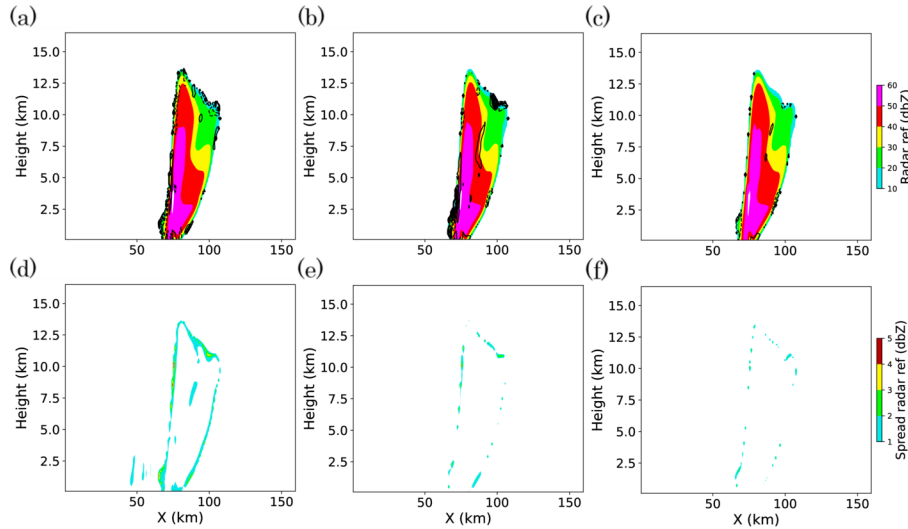
### 3.1 Analysis and first guess fields in reflectivity and vertical velocity

Figure 3 shows the analysis mean reflectivity at 00:50:00 for 5MIN-3D, 5MIN-4D, and 30SEC. The analysis ensemble mean reflectivity is closely similar to the nature run in all the cases. The ensemble spread of analysis reflectivity has at most 6.6 dBZ in the 5MIN-3D case and 3.2 dBZ in the 30SEC case. This simply reflects the total number of assimilated observations, with more observations leading to a smaller spread.

Figures 4a-4c compare the analysis mean vertical velocity and its deviation from the nature run. Note that the figures show the area between  $X = 60$  km and 100 km, which is narrower than Fig.3. The 5MIN-3D case underestimates the updraft near its maximum position. The 5MIN-4D has slight errors around the updraft, whereas the 30SEC case almost reproduces the true vertical velocity field. The largest error is located around the maximum of the updraft near 10 km height, and not large enough to change the structure of deep convection. The errors in the 5MIN-3D and 5MIN-4D cases are considered to be the remainders of the error in the first guess ensemble shown in Figures 4d and 4e.

Figures 4g-4i show the ensemble spread and the KL divergence in vertical velocity for each case. The case 5MIN-3D shows the largest spread and KL divergence in vertical velocity. The 5MIN-4D shows smaller values, though they are still significantly larger than those of 30SEC. In the case of 5MIN-3D and 5MIN-4D, large values of KL divergence are found near the location of the maximum updraft, the lower troposphere below the updraft, and in the right part of the figures ( $X = 95$  km,  $Z = 8$  km).





**Figure 3.** Vertical cross sections of (a-c) ensemble mean and (d-f) spread of analysis reflectivity at 00:50:00, for (a,d) 5MIN-3D, (b,e) 5MIN-4D, and (c,f) 30SEC cases respectively. Black contours in (a-c) indicate the difference between analysis mean and nature run, with contour interval of 0.5 dBZ.

The area below the updraft is thought to be associated with downdraft caused by precipitation in some members, and the right part may correspond to the border of the convective system. However, there are no significant differences of KL divergence around the area of the maximum updraft between 5MIN-4D and 30SEC cases.

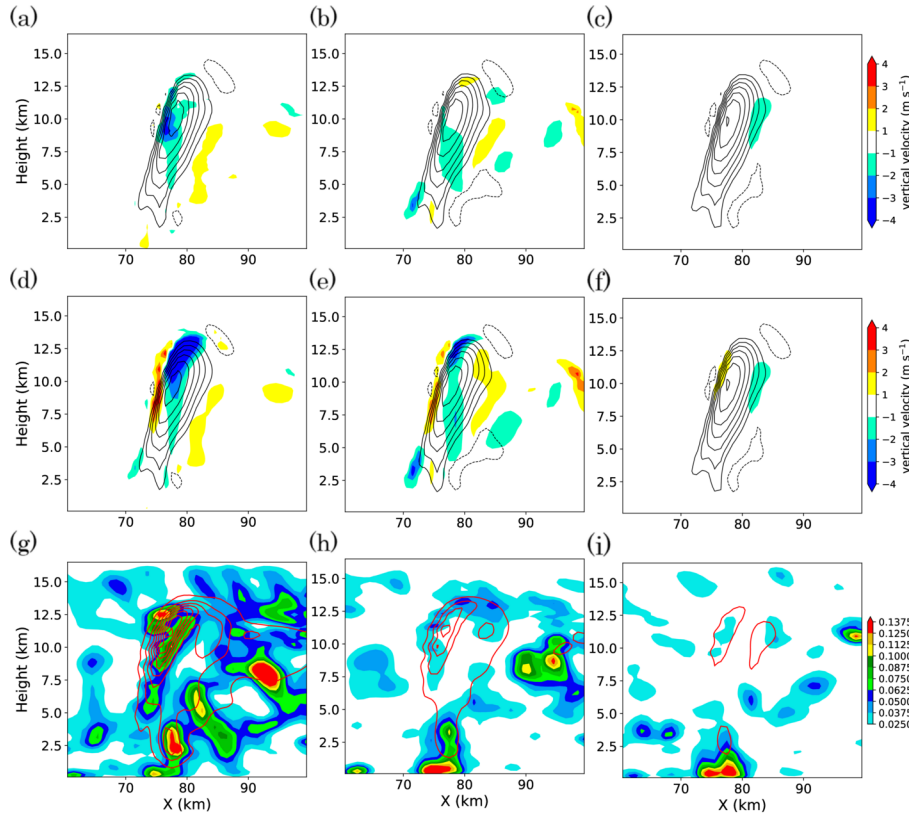
### 3.2 Forecast fields in reflectivity and surface precipitation rate

Figures 5a-5c show cross sections of the ensemble mean radar reflectivity of 30-minute forecasts from 00:50:00. The difference from the nature run is shown in black contours. The three cases show almost similar patterns of large reflectivity area. Some differences among the cases are found in the rear part of the precipitation system, where relatively low reflectivity remains below 4 km and around  $Y = 70$  to  $80$  km. The 30SEC case shows a higher accuracy in reflectivity in this part, although the difference is small. Figures 5d-5f show the accumulated surface precipitation for 30 minutes between 00:50:00 and 01:20:00 for each case. All of them show a common spatial pattern of error against the nature run. The difference among the cases is not as significant as the systematic error of the forecasts.

### 3.3 Non-Gaussianity and non-linearity

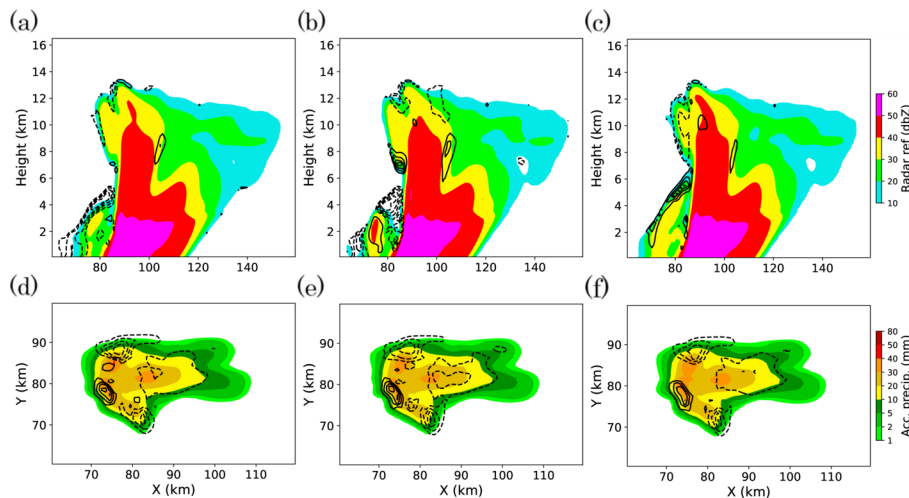
In this section, we examine the error probability distribution and discuss how it impacts on analysis accuracy. Figure 6 shows the example scatter plots between first guess ensemble of graupel mixing ratio and vertical velocity for each case. The blue markers correspond to the values of each of the 100 ensemble members, indicating the joint probability distribution, and the red markers indicate the nature run. They are extracted from the same grid point ( $X = 78$  km,  $Y = 80$  km,  $Z = 12.1$  km), where the



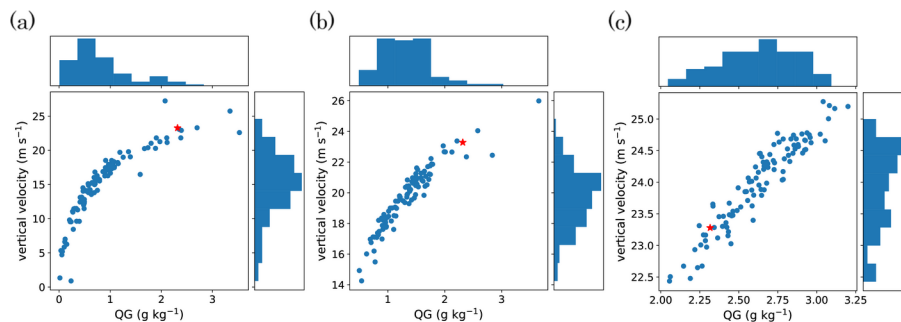


**Figure 4.** Vertical cross sections at  $Y = 80$  km of (a-c) analysis ensemble mean and deviation from the nature run, (d-f) first guess ensemble mean and deviation from the nature run, and (g-i) first guess ensemble spread and KL divergence, of vertical velocity at 00:50:00, for (a,d,g) 5MIN-3D, (b,e,h) 5MIN-4D, and (c,f,i) 30SEC cases respectively. Black contours in (a-f) indicate ensemble mean of vertical velocity with contour interval of  $5 \text{ m s}^{-1}$ . Red contours in (g-i) indicate first guess ensemble spread of vertical velocity with contour interval of  $0.5 \text{ m s}^{-1}$ .

5MIN-3D case shows large KL divergence of vertical velocity. The 5MIN-3D case shows the joint distribution with a bended shape, whereas the 5MIN-4D and 30SEC cases show the distribution that would be more fitted by a straight line. This is due to the difference in the ensemble spread as seen in Figures 4d-4f. The rapid error growth produces not only the non-Gaussianity in a single variable but also the nonlinearity in cross-variable relationships in the first guess ensemble. This may be the cause of the analysis error in state variables, as the LETKF calculates the analysis increment using the linear superposition of the ensemble perturbation of the first guess. That treatment is unable to estimate the optimal analysis increment value for both of the two variables when they have a nonlinear functional relationship. To quantify the occurrence of the joint distribution showing nonlinear relationship such as Figure 6a, we calculate the mutual information between the ensemble members of graupel and vertical velocity at every grid point, after removing the linear dependency. Figure 7 shows the cross section of the mutual information. Large values are found in the upper part of the main convective cell in the 5MIN-3D case, indicating

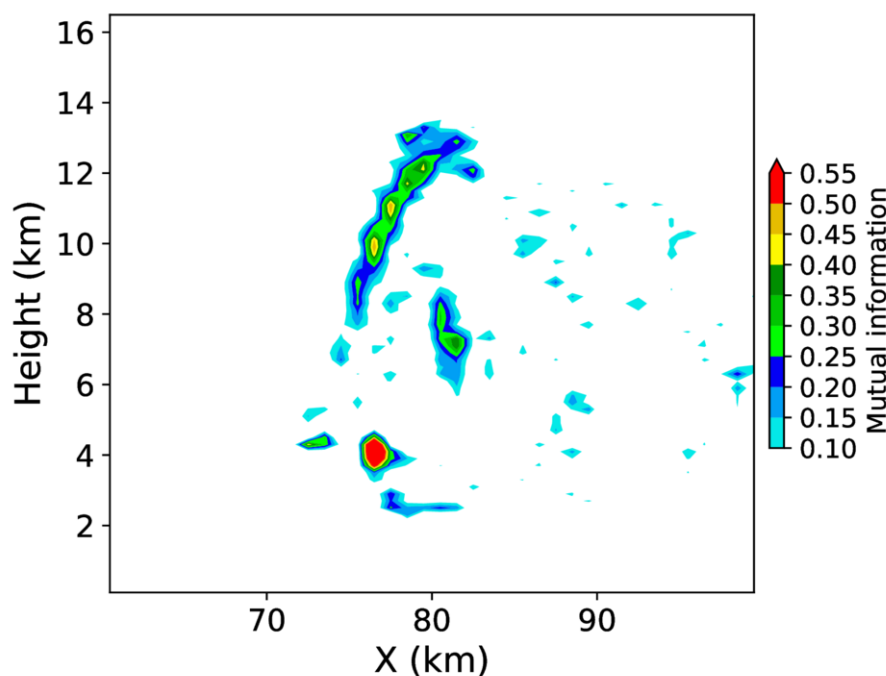


**Figure 5.** (a-c) Vertical cross sections at  $Y = 80$  km of ensemble mean radar reflectivity and (d-f) ensemble mean accumulated surface precipitation of 30 minutes forecast from 00:50:00. They are of (a,d) 5MIN-3D, (b,e) 5MIN-4D, and (c,f) 30SEC cases respectively. Black contours in (a-c) indicate difference from the nature run with contour interval of 5 dbz. Black contours in (d-f) indicate the difference from the nature run with contour interval of 2 mm.



**Figure 6.** The examples of scatter plots of 100 ensemble members between graupel mixing ratio (QG) and vertical velocity (W) for each of (a) 5MIN-3D, (b) 5MIN-4D, and (c) 30SEC cases. The blue dots indicate values of each ensemble member. The red star marker indicates the value of nature run. Histograms of QG and W are shown on the top and on the right of each panel, respectively.

strong nonlinear relationship between the two variables. This tendency of a strongly nonlinear joint distribution between the graupel mixing ratio and the vertical velocity may explain the larger error in analysis mean vertical velocity in Figure 4a.



**Figure 7.** Vertical cross section at  $Y = 80$  km of the mutual information between ensemble values of QG and W after removing linear dependency.

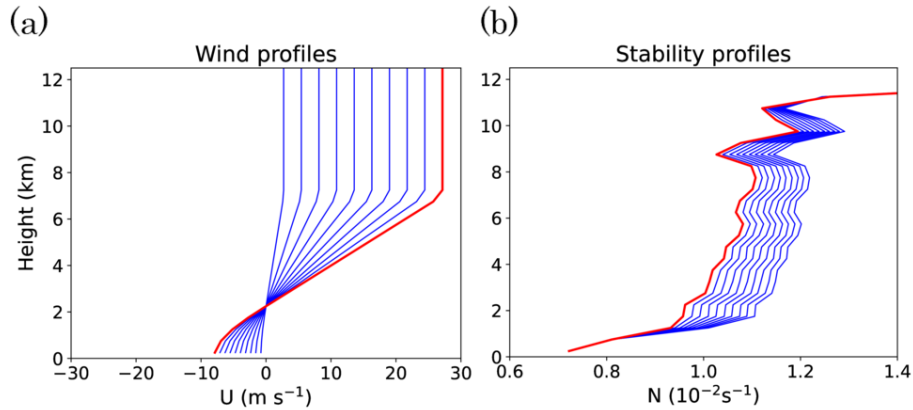
#### 4 Additional experiments in the presence of larger-scale errors

##### 205 4.1 Initial ensemble with perturbed background profiles

To extend the discussion in the previous sections to more realistic situations, we conduct additional experiments with background errors at a larger scale. We perform two additional experiments using the same observation data, one with perturbation in the background wind profile, and the other with perturbation in the background thermal profile. In both cases, 10 different background profiles for each 10 members of the ensemble are used to create a 100-member initial ensemble.

210 Figure 8 shows the 10 different wind and stability profiles used in each experiment, respectively. Both of those 10 sets include one true profile, indicating only 10 members have correct background wind or stability profile. The other 90 members are biased and are expected to have significant errors in the evolution at a convective scale.

The same LETKF setting is used in these additional experiments, although the previous setting includes parameters such as small localization scales, which may be suboptimal in the presence of background errors of a larger scale. Our purpose  
215 of these experiments is to find implications that help interpret the previous real-world experiment (Ruiz et al., 2021), which was performed with initial and boundary conditions downscaled from the parent model ensemble forecasts with considerable larger-scale uncertainty.



**Figure 8.** Background atmospheric profiles of (a) horizontal wind and (b) atmospheric stability (buoyancy frequency) used in the experiment in Sect. 4. Each panel shows 10 different profiles, which are randomly assigned to the initial condition of 100 members. Red curves indicate the profiles used for the nature run.

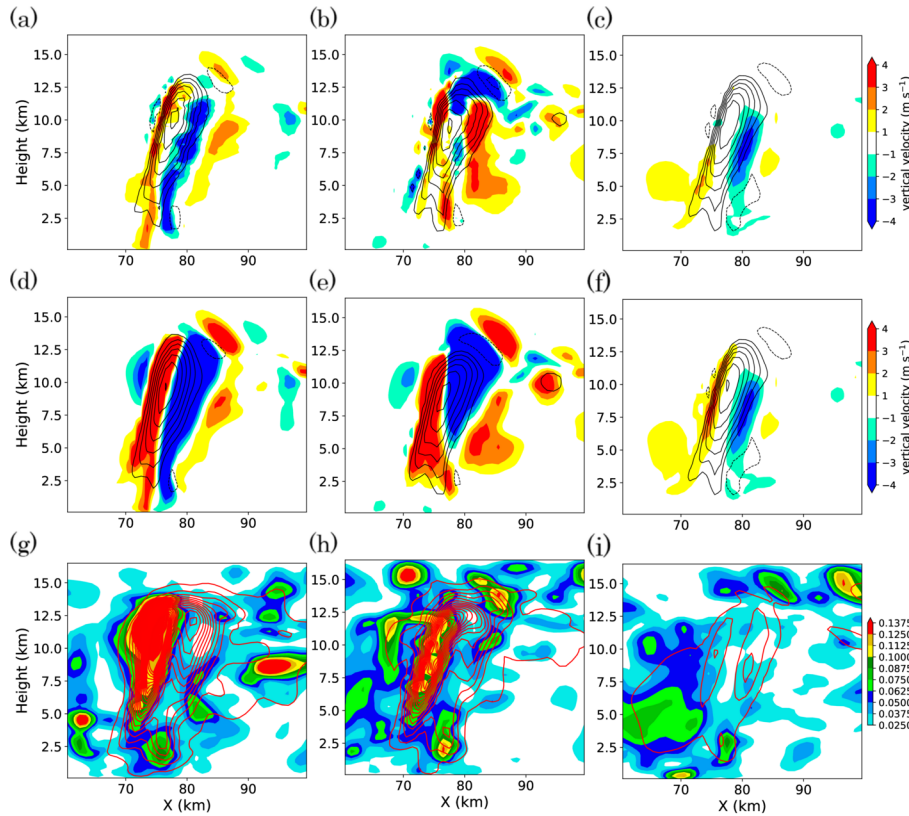
#### 4.2 Analysis and first guess in vertical velocity

Figures 9a-9c show the analysis mean, and 9d-9f show the first guess mean vertical velocity in the presence of background  
220 wind perturbation. As the ensemble includes members with weaker upper-level wind, they are expected to have convection location shifted to the left. Consequently, 5min-3D and 5MIN-4D cases have a significant dipole pattern of first-guess error in vertical velocity. Additionally, the location shift of the maximum updraft causes a skewed error distribution of vertical velocity in nearby grid points, causing high non-Gaussianity seen in Figures 9g and 9h. The analysis mean of 5MIN-3D has a remaining dipole-shaped error, whereas 5MIN-4D has larger errors with complex spatial pattern. This might be caused by the absence of  
225 temporal localization of 4D-LETKF, which assimilates all previous 5-minute observations with equal weight, leading to the suboptimal instantaneous field at the analysis time. The 30SEC case has significantly smaller first guess mean error and KL divergence, leading to smaller analysis mean error.

The results of perturbed stability experiment are more complicated. The first guess mean error in vertical velocity shown in Figures 10d-10f indicates a significant negative bias over the area of updraft in 5MIN-3D and 5MIN-4D cases. This is caused  
230 by members with less intense convection under weaker background instability. The KL divergence fields show large values in the upper part of the convection, implying a strongly non-Gaussian distribution among the ensemble. The analysis mean of the 5MIN-3D case has significant remaining negative error in the upper part. Although the background vertical velocity is expected to be correlated with reflectivity, the analysis mean error still remains especially in the upper part, indicating the possibility of a non-Gaussianity effect. On the other hand, the analysis mean vertical velocity of 5MIN-4D has a significantly smaller  
235 error than 5MIN-3D in the upper part, whereas it has somewhat larger negative errors in the lower troposphere. The 30SEC case has a smaller first guess error and KL divergence in the area of the updraft. However, the area of larger negative error behind it (around  $X = 70$  km) is found both in the first guess and the analysis mean fields. It might be a side effect of frequent



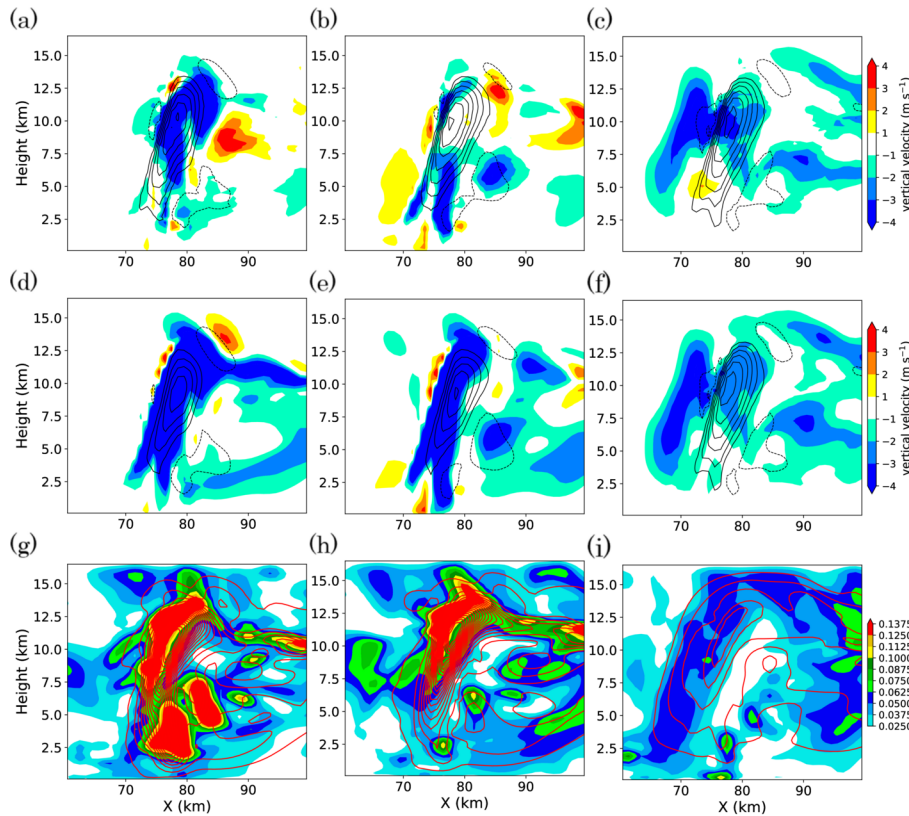
assimilation, possibly triggering artificial convection cells by accumulated unbalanced analysis increments. In summary, in this perturbed stability case, the comparison among different data assimilation frequencies has more complex features, and we have to consider other possible factors than non-Gaussianity, although 5MIN-3D still shows the largest analysis error.



**Figure 9.** Same with figure 4 but for the experiments with background wind perturbation. Purple contours in (g-i) indicate first guess ensemble spread of vertical velocity with contour interval of  $1 \text{ m s}^{-1}$ .

### 4.3 Forecast in surface precipitation rate

Finally, we compare the impact of frequent data assimilation on surface precipitation forecast in these experiments with perturbed background profiles. Figures 11a-11c show the accumulated surface precipitation for 30 minutes between 00:50:00 and 01:20:00 for each of the three cases with perturbed background wind. The common feature of forecast errors among these three cases is that the area of high precipitation is slightly shifted to the left in these figures, as we can see in the areas of large positive errors ( $X = 70\text{-}80 \text{ km}$ ,  $Y = 70\text{-}80 \text{ km}$ ). In contrast, the area around the peak of accumulated precipitation ( $X = 70\text{-}90 \text{ km}$ ,  $Y = 80\text{-}85 \text{ km}$ ) has negative errors. Compared to these common features, the differences among the three cases have a smaller spatial scale and less significant. Figures 11d-11f show those of the experiments with perturbed background stability. The common error patterns are the higher peak value ( $X = 80 \text{ km}$ ,  $Y = 80 \text{ km}$ ) and the smaller values in the surrounding area.



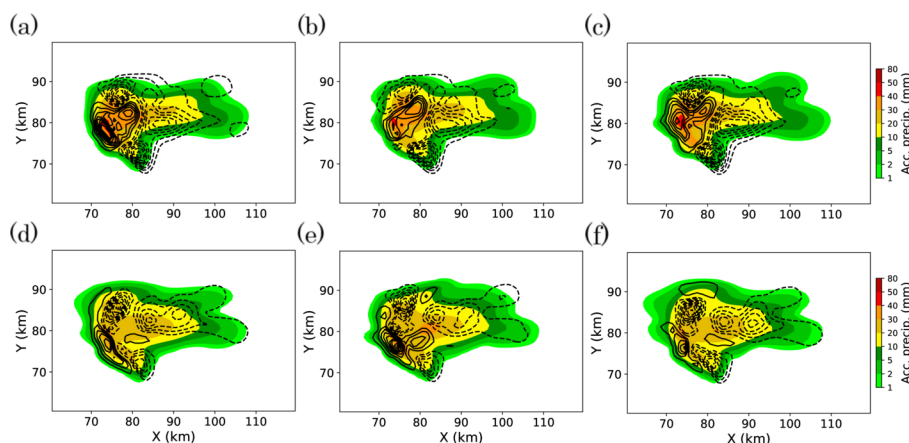
**Figure 10.** Same with figure 9 but for the experiments with background stability perturbation.

250 This is caused by weaker development of convection and concentration of precipitation in a smaller area. In these experiments, the difference among the cases with different data assimilation frequency is less significant than the common errors as well. In overall, in these experiments with perturbed background profiles, the ensemble mean precipitation forecasts have more realistic amplitude of errors than the case with the true profile. The wind and stability perturbations produce characteristic spatial patterns in the forecast error. Meanwhile, the difference among the three data assimilation methods does not cause significant  
255 differences in forecast precipitation, despite the difference in the analysis errors in vertical velocity fields.

## 5 Summary and discussions

In this study, the idealized experiments were conducted to examine the impact of assimilating radar reflectivity every 30 seconds on the non-Gaussianity of first-guess error distribution and the analysis and forecast accuracy. The experiments were carefully designed so that we can focus on convective scale errors. We excluded other factors such as errors in the forecast  
260 model and the observation operator, uncertainties in background vertical profiles of atmospheric variables, and modifications on the background error covariance in the EnKF such as covariance inflation.





**Figure 11.** Ensemble mean 30-minute accumulated surface precipitation of forecasts from 00:50:00, of the experiments with (a-c) background wind and (d-f) background stability perturbation. They are of (a,d) 5MIN-3D, (b,e) 5MIN-4D, and (c,f) 30SEC cases respectively. Black contours indicate the difference from the nature run with contour interval of 2 mm.

We performed perfect-model OSSEs of an idealized supercell development from a warm bubble. Synthetic radar reflectivity observation data was created from the time series of the nature run every 30 seconds. We compared the analyses produced by the data assimilation cycles with three different manners, namely, 5-minute 3D-LETKF (5MIN-3D), 5-minute 4D-LETKF (5MIN-4D), and 30-second 3D-LETKF (30SEC). We found a significant reduction of the non-Gaussianity for vertical velocity in 30SEC compared to other cases, along with the reduction of the ensemble spread. We also found the improvement of the analysis accuracy for vertical velocity in 30SEC. The impact was larger when compared with 5MIN-3D. Smaller but still significant differences were found when compared to 5MIN-4D.

The significant difference between the cases was found mostly in the upper part of the main convective cell, where the vertical velocity has the largest value. In contrast, the dynamical variables in the lower levels that mainly control the evolution of the supercell system did not change significantly. The ensemble mean reflectivity and surface accumulated precipitation of 30-minute forecast from the analysis ensemble did not show significant differences between the cases.

We further examined the first guess ensemble where significant non-Gaussianity is found. We compared the joint distribution between graupel mixing ratio and vertical velocity among the three cases and found a significant difference in the relationship between the two variables. In 5MIN-3D, not only the non-Gaussianity of the background error of a single variable but also the nonlinearity in the approximate relationship between the two variables was found, whereas in 30SEC they were significantly reduced. We suggested the possibility that the LETKF under this nonlinearity causes the analysis error in vertical velocity.

We concluded that assimilating radar reflectivity every 30 seconds indeed has a significant impact on the analysis accuracy for unobserved variables, and that it could be caused by the joint non-Gaussian background error probability density of multiple variables. However, at the same time, we also found that the importance of the analysis accuracy improvement is not significant for short-period precipitation forecasting, as it does not essentially change the evolution of the convective system itself. The





30-minute forecast of 5MIN-3D already showed a highly accurate precipitation forecast, suggesting that radar reflectivity of every 5 minutes is sufficient in the idealized setting of this study, where errors from the model and observation operator, and the uncertainty in larger-scale atmospheric fields are all ignored. Therefore, where the impact of non-Gaussianity is considered separately, it is likely to be less significant than other factors.

We further performed a similar comparison under more realistic situations where we have uncertainty at a larger scale. To mimic realistic settings, 10 different background profiles were used to create a 100-member initial ensemble. In the two experiments, background wind and stability profiles were perturbed, respectively. These experiments showed a more significant difference between assimilation frequencies of 5 minutes and 30 seconds in first guess vertical velocity. The biases in background profiles caused larger deviations among first guess members and thus large non-Gaussianity during 5-minute integration. On the other hand, the 30SEC case has significantly reduced non-Gaussianity. It produced significantly smaller analysis errors than 5MIN-3D. However, in these experiments, we also found more complex features in first guess and analysis errors which we did not find in the previous experiment. First, the analysis error of 5MIN-4D has patterns that are significantly different from those of 5MIN-3D. This might be caused by 4D-LETKF method which attempts to optimize the time series within the window instead of the instantaneous analysis value. Second, we found some patterns in first guess and analysis error in 30SEC which were not seen in the others. This was supposed to be caused by frequent data assimilation and possibly driven by the accumulation of unbalanced analysis increment.

The findings in these additional experiments may provide more insights into the interpretation of previous studies. For example, in the experiment using the Osaka PAWR data (Ruiz et al., 2021), they found a significant difference in first guess mean vertical velocity not only in magnitude but also in structure (their figures 2a and 2d). The situation may be explained by the case shown in Figure 10, indicating that the large uncertainty in background thermal profile might cause a large difference in analysis vertical velocity field.

We changed nothing in the LETKF when we performed the experiments with perturbed background profiles, for comparison with the previous studies. However, assimilating the observation only with a small localization scale was inefficient in constraining larger-scale fields and did not improve the forecast accuracy, which is supposed to be mostly driven by larger-scale atmospheric states. We can consider more advanced approaches to deal with this problem. Some studies proposed methods of multi-scale data assimilation using a single observation data source (Zhang et al., 2009; Miyoshi and Kondo, 2013; Fabry, 2022). The application of those methods to frequent radar data assimilation problems will be examined in future studies.

Data assimilation methods without the assumption of Gaussianity, such as particle filters (van Leeuwen et al., 2019), are another potential approach to deal with the problem of non-Gaussianity. Particle filters can avoid the error caused by linear superposition when the errors in the state variables have nonlinear relationships, as seen in Figure 6a. Therefore, this approach has the potential to improve the analysis accuracy in such situations.

*Code and data availability.* The SCALE-LETKF code is available on Zenodo: <https://doi.org/10.5281/zenodo.13906038> (Amemiya et al., 2024). All the code and data to reproduce the figures in this study are available on request from the corresponding author.



315 *Author contributions.* A. Amemiya was responsible for conceptualization, formal analysis, methodology, investigation, visualization, and writing. T. Miyoshi was responsible for the project administration, investigation, and review and editing of the manuscript.

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