

[..*]A Multivariate Analysis of Atmospheric Drivers for Western European Heatwaves[..[†]]

Aytaç Paçal^{1,2}, Birgit Hassler¹, Katja Weigel^{2,1}, Miguel-Ángel Fernández-Torres³, Gustau Camps-Valls⁴, and Veronika Eyring^{1,2}

¹Deutsches Zentrum für Luft- und Raumfahrt (DLR), Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany

²University of Bremen, Institute of Environmental Physics (IUP), Bremen, Germany

³Department of Signal Theory and Communications, Universidad Carlos III de Madrid (UC3M), Leganés, Madrid, Spain

⁴Image Processing Laboratory (IPL), Universitat de València (UV), Paterna, València, Spain

Correspondence: Aytaç Paçal (aytac.pacal@dlr.de)

Abstract. Understanding the dynamics of heatwaves is critical for accurate climate risk assessment. Traditional definitions, based solely on surface temperature thresholds, [..³]can detect heatwaves but cannot be used to analyze the complex, multivariate nature [..⁴]that causes them. We apply a spatiotemporal Variational Autoencoder (VAE) [..⁵]to ERA5 reanalysis data to identify compact representations of multivariate, year-round heatwave patterns over Western Europe. Focusing on 5 key atmospheric variables (e.g., circulation, humidity, temperature, geopotential height, cloud cover, stream function, and radiation), we extract [..⁶]11-day heatwave samples from ERA5 reanalysis data over the North Atlantic, centered on near-surface temperature extremes in Western Europe. The VAE was trained on [..⁷]heatwave samples from 1941 [..⁸]to 1990 and evaluated using samples from 2001 [..⁹]to 2022[..¹⁰], effectively clustering heatwave events by season [..¹¹]and identifying 10 known dynamical regimes, such as summer blocking highs and winter omega blocks. The VAE model captures the interplay and temporal evolution between different atmospheric variables in their contributions to heatwaves over Western Europe. Notably, recent summer heatwaves form a distinct cluster within the latent space, pointing to a shift in atmospheric dynamics consistent with climate change. Composite anomaly maps further show coherent pre-onset patterns across variables. These results demonstrate the [..¹²]utility of VAEs for extracting physically meaningful, multivariate representations of heatwave dynamics from [..¹³]reanalysis data, highlighting changes in their atmospheric drivers over recent decades.

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15 1 Introduction

Extreme events and heatwaves [..¹⁴]pose a significant threat to both the environment and human health [..¹⁵](López-Bueno et al., 2021; Mora et al., 2017a). Extreme events refer to rare and intense meteorological phenomena, [..¹⁶]whereas heatwaves are characterized by exceptionally high temperatures [..¹⁷]that persist over several days. Since the effects of climate change intensify with the increased amount of human-induced greenhouse gases in the atmosphere (Lynas et al., 2021), the frequency and intensity of hot (cold) extremes increase (decrease) globally (IPCC, 2021). [..¹⁸]On average, the intensity of hot extremes increases approximately linearly with global warming, while the frequency of rare hot extremes increases more rapidly (IPCC, 2021; Li et al., 2021; Fischer and Knutti, 2014; Kharin et al., 2018; Fischer et al., 2021; Skinner et al., 2025). These trends are projected to continue even at the lowest projected global warming scenario [..¹⁹](IPCC, 2021).

Currently, 30% of the global population is exposed to deadly climatic conditions, which are projected to increase up to 75% under the current greenhouse gas emissions scenarios [..²⁰]

(Mora et al., 2017b, a; King and Harrington, 2018). The growing severity of extreme events also [..²¹]impacts the environment, infrastructure, and economy [..²²](Yuan et al., 2024; Dosio et al., 2018; IPCC, 2021). Recent heatwaves in Europe (2003, 2010, 2015, and 2018) caused damages that amounted to 0.3-0.5% of European gross domestic product (GDP) (García-León et al., 2021). Globally, the annual cost of extreme weather events is estimated at US\$143 billion (Newman and Noy, 2023). Looking ahead, global cumulative GDP losses could reach 16-22% by the end of the century if the current 3°C warming trajectory continues (Burke et al., 2015; Newell et al., 2021; Kotz et al., 2024; World Economic Forum, 2024). Therefore, identifying and characterizing heatwaves is crucial to effectively mitigating and adapting to their impacts. Since extreme temperature events, including heatwaves, [..²³]are by definition rare occurrences at the tails of temperature distributions (McPhillips et al., 2018), percentile and block maxima methods have been widely used for their detection (Zhang et al., 2011; Huang et al., 2016; Alaya et al., 2020; Li et al., 2021; IPCC, 2021). Russo and Domeisen (2023) [..²⁴]demonstrated that historically unprecedented extreme heatwaves have increased 10-fold in recent years, using cumulative indices for their identification rather than indices relying on temporal averages, as cumulative indices are more reliable for comparing events with different [..²⁵

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40]durations. Brunner and Voigt (2024) found that seasonal running windows commonly used to define extreme thresholds can introduce systematic biases and underestimate the frequency of extreme events. However, the definition of an extreme depends on the application, and there is no standard definition for heatwaves (Barriopedro et al., 2023; Boni et al., 2023). Many existing indices rely solely on temperature, which [..²⁶]allows detection but provides only limited information to capture the full complexity of these events (Perkins, 2015; McPhillips et al., 2018; Barriopedro et al., 2023). The complex nature of heatwaves, however, requires more sophisticated analysis methods. Multiple atmospheric processes and local drivers play an essential role in the occurrence of heatwaves, and a multidimensional approach considering the tails of high-dimensional, multivariate probability distributions, whose shape and structure are themselves changing due to non-stationary climate dynamics, is required for defining and studying heatwaves (Sardeshmukh et al., 2015; Domeisen et al., 2022; Barriopedro et al., 2023; Camps-Valls et al., 2025).

Machine learning (ML) and deep learning (DL) methods are frequently [..²⁷]employed in climate science, as they can [..²⁸]uncover complex relationships in multivariate and high-dimensional climate datasets (Reichstein et al., 2019; Zhu et al., 2023; Salcedo-Sanz et al., 2023; Camps-Valls et al., 2025). For instance, Ronco et al. (2023) employed explainable machine learning models, including random forests and gradient boosting, to predict human displacement induced by floods, storms, and landslides from global observational data. Machine learning methods help discover physical processes from data and improve numerical simulations (Heuer et al., 2024; Debeire et al., 2025). Unsupervised approaches such as autoencoders and clustering can extract dynamical regimes from high-dimensional climate fields, advancing physical understanding beyond traditional linear methods (Lai et al., 2025; Behrens et al., 2022). ML and DL techniques rely on high-quality and reliable labeled data (Camps-Valls et al., 2025). However, a [..²⁹]significant limitation for extreme events and heatwaves is precisely the lack of high-quality and labeled datasets (Prabhat et al., 2021; Lacombe et al., 2023). One potential solution is to use unsupervised learning methods where the model learns patterns from data autonomously. Unsupervised learning methods help identify complex data patterns without relying on predefined labels or thresholds (Kingma and Welling, 2019). In Paçal et al. (2023), the Gaussian Mixture Model (GMM), an unsupervised learning approach that models data as a combination of multiple Gaussian distributions, was applied to characterize extreme temperature events. By representing daily maximum temperatures as a bimodal rather than a traditional unimodal distribution, the study found that extreme temperature events will become significantly more frequent under future global warming levels and revealed regional differences not captured by conventional methods. Another example of an unsupervised learning method is the Variational Autoencoder (VAE), which is composed of an encoder [..³⁰]that reduces the dimensionality of the input data to a latent space and a decoder [..³¹]that reconstructs the input data from that latent space (Kingma and Welling, 2019). Recent advances in artificial intelligence for climate extremes have highlighted the importance of unsupervised learning models like GMMs and

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VAEs for both detecting anomalies and uncovering the mechanisms behind rare and compound events, especially when labeled data is scarce or absent (Materia et al., 2024).

70 VAEs are [..³²] primarily developed as generative models, capable of learning complex data distributions and generating realistic synthetic samples (Kingma and Welling, 2019). Beyond generative tasks, VAEs have also been widely applied in anomaly detection [..³³] across various domains, including network security, risk management, health monitoring, and computer vision (Pang et al., 2021; Nassif et al., 2021; Albuquerque Filho et al., 2022). Among other applications, autoencoders and VAEs have been applied to learn spatiotemporal regularities from video data (Hasan et al., 2016; Fan et al., 2020). VAEs
75 and clustering methods [..³⁴] such as GMMs [..³⁵] have been used to identify regimes in the latent space and analyze their dynamical behavior [..³⁶] in climate science [..³⁷] (Lindhe et al., 2021; Happé et al., 2024; Paçal et al., 2023). Spuler et al. (2024) introduced the RMM-VAE, a probabilistic machine learning method that combines variational autoencoders with clustering to identify circulation regimes targeted to local impact variables. Happé et al. (2024) applied a 3D variational autoencoder to heatwave events from the KNMI-LENTIS dataset over western Europe, showing that the latent space
80 captures physically interpretable circulation regimes and that heatwaves are best represented in a probabilistic framework.

Building on these previous applications, our study extends Happé et al. (2024) to a multivariate and year-round analysis of European heatwaves using reanalysis data. This study aims to understand how heatwaves develop [..³⁸], what contributes to their evolution, and how recent heatwaves are represented in relation to the heatwaves from the historical baseline. In contrast to Happé et al. (2024), who focused on heatwave samples extracted from the KNMI-LENTIS dataset over
85 Western Europe, we (i) include nine atmospheric variables from the ERA5 reanalysis dataset to assess their contribution to heatwave evolution, (ii) analyze spatiotemporal samples over a larger window (± 5 days around the onset, i.e., 11 days in total) to characterize build-up and decay processes better, (iii) train on 11-day multivariate ERA5 heatwave samples that cover the full year with standardized anomalies, and (iv) assess generalization with an explicit historical-to-recent evaluation. To this end, we first [..³⁹] train a spatiotemporal VAE [..⁴⁰] on multivariate reanalysis heatwave samples [..⁴¹] from
90 the historical period of 1941-1980. Then, we cluster and analyze the latent space representation of [..⁴²] recent heatwaves (2000-2022) in Western Europe. Section 2 describes the data and methodology followed in this research. Section 3 provides the results for the heatwave cluster analysis. Finally, the main results are summarized and discussed in Section 4.

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provides a promising frameworkfor characterizing complex climate extremes

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2 Data and Methods

2.1 Data Sources and Preprocessing

95 We used the ERA5 reanalysis dataset (Hersbach et al., 2017; Soci et al., 2024) to detect and ⁴³understand heatwave dynamics. We focused only on atmospheric variables, as shown in Table 1, ⁴⁴including those used in Happé et al. (2024) as well as additional variables relevant to heatwave dynamics identified in previous studies, such as geopotential height at 500 hPa (z500) as it captures mid-tropospheric circulation patterns and has been shown to better reproduce temperature anomalies associated with European heatwaves than sea-level pressure (Jézéquel et al., 2018; Domeisen et al., 2022; Rousi
100 et al., 2022; Barriopedro et al., 2023; Kim and Seo, 2023; Tian et al., 2024). All data was accessed via the German Climate Computing Center (DKRZ) data catalog (Hersbach et al., 2017). We aggregated the hourly data in GRIB (General Regularly-distributed Information in Binary form) file format for each variable into daily values using variable-specific temporal operators, such as daily maxima for temperature and daily means for pressure fields, as shown in Table 1. The resulting dataset comprises daily observations from 1940 to 2022 for the North Atlantic region, ⁴⁵spanning from 75°W to 60°E ⁴⁶and from 30°N
105 to 75°N on a 0.7° grid, as shown in Figure 2. ⁴⁷ERA5 data was regridded from its native 0.25° resolution to 0.7° to ensure direct comparability with Happé et al. (2024), where this resolution corresponds to the native grid of the EC-Earth3 model. Furthermore, this coarser resolution also reduces the very high dimensionality of the multivariate input while retaining the large-scale circulation patterns. Although ERA5’s native resolution is finer, the reconstruction loss of the variational autoencoder emphasizes large-scale circulation patterns while smoothing out small-scale variability. Retaining the native
110 0.25° grid would therefore not provide additional benefit while substantially increasing computational cost. Since ERA5 data is provided in hourly resolution, we first applied the temporal aggregation operators listed in Table 1 to convert the hourly ERA5 fields to daily values. From these daily fields, we then computed the 1941–1980 ⁴⁸climatological mean and standard deviation using a 15-day moving window centered on each calendar day⁴⁹, which we used to standardize the variables and remove seasonal variability. The 15-day climatological window is a common choice for smoothing day-to-
115 day noise while preserving seasonal variations. This approach is consistent with other studies on extreme-event detection (Sulikowska and Wypych, 2020). We used this period to calculate the climatology, as it precedes the stronger warming trends after 1980 in Europe (Elguindi et al., 2013; Reid et al., 2016). The standardized daily anomalies were then used for all subsequent analyses.

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Table 1. Overview of the atmospheric variables used for heatwave characterization in this study. The temporal operator refers to the daily aggregation method applied to each variable during preprocessing^[.50], converting the hourly frequency to a daily frequency. Heatwave samples for training and analysis, ^[.51] comprising all nine variables (multivariate), are extracted from the broader North Atlantic region, centered temporally around the onset dates. (*) 2-meter temperature (*t2m*) is used to identify heatwave onset dates specifically from the Western Europe subregion. Regions are shown in Figure 2.

Short Name	Long Name	Temporal operator
msl	Mean sea level pressure	Mean
r	Relative humidity	Mean
ssr	Surface net solar radiation	Sum
stream250	Stream function at 250 hPa	Mean
t2m*	2-meter temperature	Max
tcc	Total cloud cover	Mean
u10	10-meter U wind component	Mean
v10	10-meter V wind component	Mean
z500	Geopotential height at 500 hPa	Mean

2.2 Heatwave Identification

120 We followed the methodology proposed by Happé et al. (2024) to identify ^[.52] heatwave onset dates over Western Europe and extract heatwaves from the extended North Atlantic region. The identification process consists of three main steps: (1) threshold-based detection of anomalies at the grid-point level, (2) clustering of spatially and temporally contiguous anomalous grid cells, and (3) extraction of multivariate spatiotemporal samples suitable for model training. The overall workflow for heatwave onset detection and sample extraction is illustrated in Figure 1.

125 The first step involves detecting anomalies at the level of individual grid cells. We focused only on land grid cells in the Western Europe subregion, extending from 10°W to 55°E and from 35°N to 55°N (see the blue shaded area in Figure 2). Then, we used daily maximum 2-meter temperature data from the ERA5 reanalysis dataset. For each grid cell, we calculated the 90th percentile threshold for each calendar day using a multiyear 15-day moving window centered on each calendar day over the historical baseline period from 1941 to 1980. We identified anomalies each day by comparing the temperature to the

130 corresponding threshold. This approach captured relative temperature anomalies while accounting for seasonality and regional climate norms. The result was a binary mask indicating whether or not a grid cell experienced a day of anomalous heat. A value of 1 for a grid cell marks exceedance of the local threshold, while 0 represents climatologically typical conditions.

Subsequently, during the second step, we applied the Generalized Density-Based Spatial Clustering of Applications with Noise (GDBSCAN) algorithm to detect heatwave events (Sander et al., 1998), using a minimum cluster size of 21 cells across

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space and time, as suggested by Happé et al. (2024). This procedure identified 2565 unique heatwave onset dates, between 1941 and 2022, from the land grid cells over Western Europe, as shown in Figure 2.

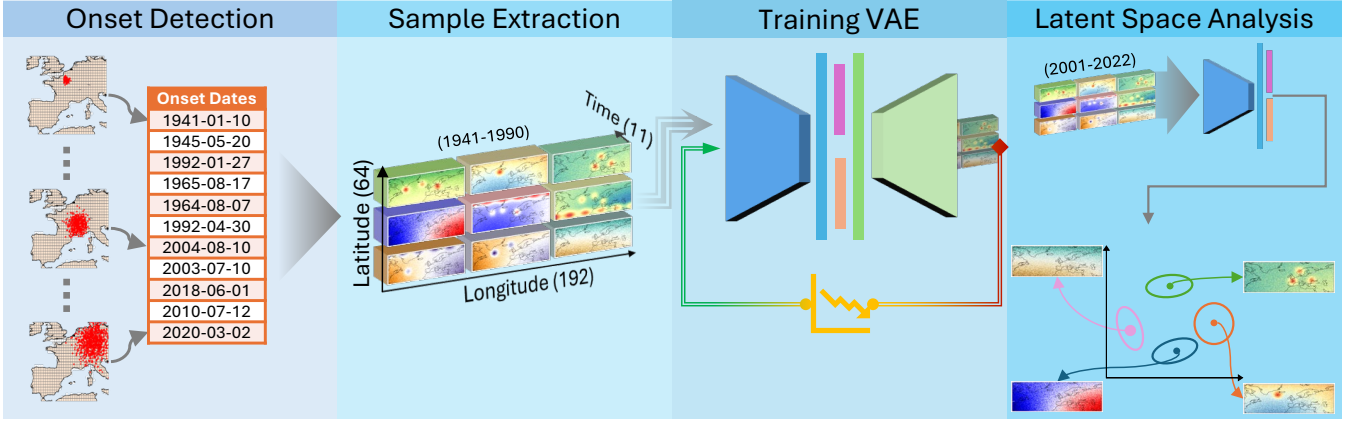


Figure 1. Workflow illustration of the heatwave onset detection and sample extraction process. Detected onset dates over Western Europe are used to extract [\[..⁵³\]](#) 11-day multivariate heatwave samples from the North Atlantic region, centered on [the onset of each event\[..⁵⁴\]](#). Samples from 1941–1990 are used to train a Variational Autoencoder (VAE) that learns compact representations of the spatiotemporal structure of heatwaves. Subsequently, samples from 2001 [\[..⁵⁵\]](#) to 2022 are encoded into the latent space to analyze the evolution and dynamics of recent heatwave events.

Finally, the last step involves extracting heatwave samples using these onset dates, where we fixed 11-day windows centered on each onset. The 11-day window [\[..⁵⁶\]](#) encompasses the five days [\[..⁵⁷\]](#) preceding the onset, the onset day itself, and the [\[..⁵⁸\]](#) subsequent five days, similar to Rouges et al. (2023). We focused on nine different atmospheric variables (multivariate), as listed in Table 1. In the first step, we only used land grid cells over Western Europe to define heatwave onset dates. However, the heatwave samples used for training the model and analyses cover a broader spatial domain, namely the extended North Atlantic region, to capture large-scale atmospheric conditions as shown with the hatched gray box in Figure 2. This framing (spatiotemporal) captures both the build-up and evolution of heatwave conditions, enabling the VAE model to learn characteristic patterns associated with the heatwaves.

[\[..⁵⁹\]](#) Compared to Happé et al. (2024), our setup differs in several ways. We focused on the ERA5 reanalysis dataset to extract heatwave samples, rather than the KNMI-LENTIS. Furthermore, we extracted [\[..⁶⁰\]](#) heatwave samples from the whole year, [\[..⁶¹\]](#) which avoids a fixed definition of summer. This makes our approach more general and independent of

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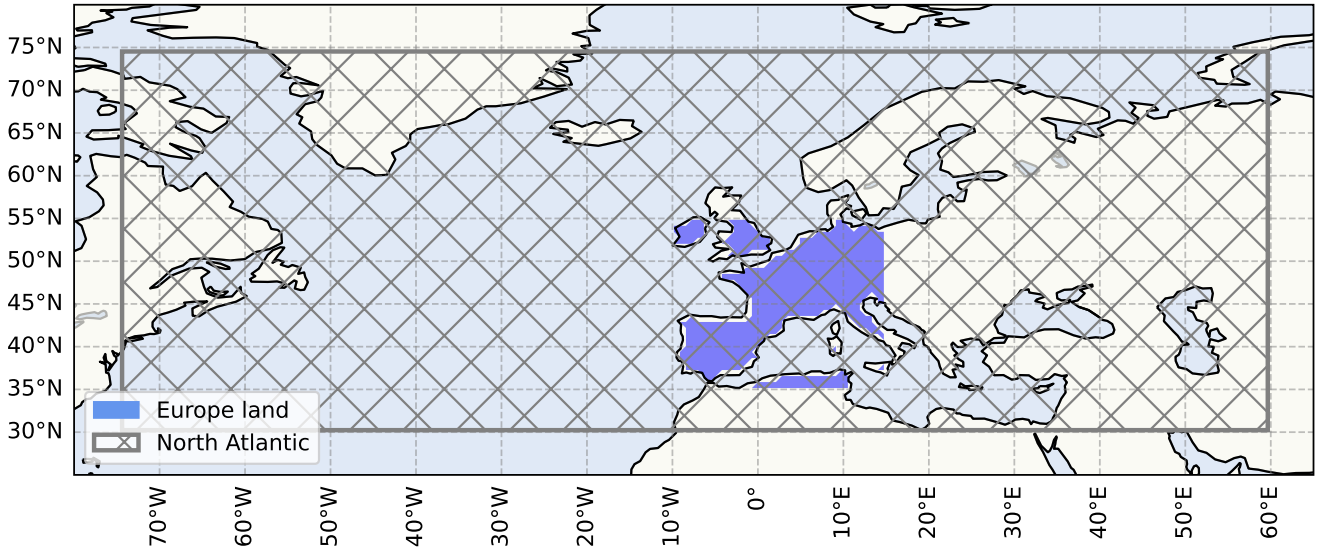


Figure 2. Geographical domains used to identify heatwave onset dates and train the VAE model. The shaded blue area represents the Western Europe land grid cells used to identify heatwave onset dates based on hot grid points derived from ERA5 temperature fields. These onset dates are then used to extract 11-day heatwave samples, centered on the onset dates, from the broader North Atlantic region (indicated by the hatched gray box), covering the nine variables (multivariate) listed in Table 1. These multivariate heatwave samples are used for training and analysis.

[..⁶²] a definition of "summer" (Wang et al., 2021). [..⁶³] Additionally, the data is standardized, [..⁶⁴] allowing us to analyze both summer heatwaves and [..⁶⁵] anomalous heat during colder months, [..⁶⁶] such as warm spells or winter heatwaves. This approach [..⁶⁷], in turn, allows for more heatwave samples from the ERA5 reanalysis dataset to [..⁶⁸] be used for training the VAE model. An additional difference between our approach and the method applied in [..⁶⁹] Happé et al. (2024) is that we [..⁷⁰] utilized additional atmospheric variables to investigate their [..⁷¹] impact on the occurrence of [..⁷²] heatwaves and to analyze large-scale atmospheric patterns. We also [..⁷³] incorporated timesteps before the onset of heatwaves (Rouges et al., 2023), which allows us to identify atmospheric patterns that build up to and persist during the progression of heatwaves.

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The Variational Autoencoder (VAE) is an unsupervised machine learning method that [..⁷⁴] utilizes neural networks to generate a latent space representation of the input data[..⁷⁵], enabling the reconstruction of the original input data (Kingma and Welling, 2019). VAEs have been widely and successfully used in anomaly detection, image recognition, and generative modeling (Pang et al., 2021). VAEs consist of an encoder network and a decoder network. The encoder network takes an input, x , such as an image, and compresses it to a latent space representation. This latent space is represented by a probability distribution, generally by a Gaussian. The decoder then takes the representation from the latent space and reconstructs the input, $\hat{x}$. The main goal of VAE is to approximate the reconstructed output as closely as possible to the original input by minimizing the reconstruction loss between the output and input. A VAE[..⁷⁶], therefore, [..⁷⁷] summarizes complex, high-dimensional data into a low-dimensional embedding. This low-dimensional latent space compresses the input data[..⁷⁸], allowing for the discovery of hidden patterns within the data. It can be further analyzed using visualization techniques and clustering algorithms to identify patterns and regimes in the data (Happé et al., 2024; Lindhe et al., 2021). The reconstruction produced by the VAE can be interpreted as a learned climatological baseline or ‘normal state,’ against which deviations can be studied. We focused on using latent space to understand the atmospheric patterns underlying different heatwave types. Similar latent space approaches have been successfully applied in climate research (Behrens et al., 2022; Oliveira et al., 2022; Shamekh et al., 2023; Mooers et al., 2023; Camps-Valls et al., 2025).

We consider a 3D convolutional neural network architecture for our VAE model to learn multivariate spatiotemporal representations of heatwaves in an unsupervised manner (see Table A1 in the Appendix for the description of the VAE architecture and more details on the training process). [..⁷⁹] We also experimented with hybrid architectures combining 2D convolutional encoder (decoder) layers to capture spatial features, followed (preceded) by LSTM (Long Short-Term Memory) layers to capture temporal information. However, these configurations produced unstable or less coherent reconstructions, likely because the LSTM struggled to capture the complex spatiotemporal dynamics of heatwave events when applied after a spatially compressed representation by 2D convolutional encoders. The 3D convolutional setup proved more robust and effective for representing the coupled spatiotemporal dynamics of heatwaves, consistent with findings from other studies employing 3D architectures for climate and geophysical data (Happé et al., 2024; Szwarcman et al., 2024).

Each heatwave sample consisted of 9 climate variables for 11 days on a 64×192 spatial grid (North Atlantic, see hatched gray region in Figure 2), resulting in input tensors with the shape (9, 11, 64, 192). [..⁸⁰] The model was trained on heatwave

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samples from [..⁸¹] 1941 to 1990, validated on samples from 1991 to 2000, and tested on samples from 2001 to 2022, resulting in [..⁸²] 1,408, 320, and 928 [..⁸³] samples, respectively.

[..⁸⁴] This split enables an out-of-distribution setting where the test years reflect recent climate conditions that differ from the historical baseline because recent decades exhibit non-stationary warming and circulation changes (Chitsaz et al., 2023; Rouges et al., 2023). Because the 1941–1980 baseline precedes the strong post-1980 warming trend (Elguindi et al., 2013; Reid et al., 2016; IPCC, 2021), this choice naturally leads to more detected heatwave events in recent decades. However, our goal is not to quantify frequency changes but to characterize the structural and dynamical patterns of heatwaves. The model focuses on circulation-related variability rather than long-term thermodynamic shifts. To assess robustness against non-stationarity, we also trained a version of the VAE using random train (0.8)/validation(0.05)/test(0.15) splits across the whole 1941–2022 period. While this approach provides a smoother latent space as expected, the resulting latent space (Figure A8) shows consistent seasonal clustering, confirming that the identified heatwave types are not artifacts of temporal trends. By training the model on historical heatwave samples, the [..⁸⁵] VAE learns an internal representation of typical patterns over time, capturing the complex spatial and temporal relationships between the different climate-relevant variables. This allows the model to learn a low-dimensional representation of extreme multivariate events in the latent space.

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⁸⁴removed: After training the VAE model, we evaluated its ability to reconstruct the climate variables. Table 2 summarizes the R^2 scores obtained for each meteorological variable individually and the overall score across all variables for the test period (2001-2022). The model demonstrates good reconstruction skill, with an overall R^2 of 0.7235. Notably, the highest R^2 values are achieved for geopotential height ($z500$) and mean sea level pressure (msl), while relatively lower scores are observed for 2-meter temperature ($t2m$) and 10-meter wind components ($u10$ and $v10$). Similarly, Jézéquel et al. (2018) showed that geopotential height ($z500$) better captures temperature anomalies associated with European heatwaves. The relatively lower R^2 scores for 2-meter temperature ($t2m$) and 10-meter wind components ($u10$ and $v10$) can be attributed to higher spatiotemporal variability in near-surface fields, influenced by local surface conditions, which are difficult for the model to capture accurately, considering the coarse spatial resolution of

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[⁸⁶..⁸⁷][⁸⁸..⁸⁹][⁹⁰..⁹¹][⁹²..⁹³][⁹⁴..⁹⁵][⁹⁶..⁹⁷][⁹⁸..⁹⁹][¹⁰⁰..¹⁰¹][¹⁰²..¹⁰³][¹⁰⁴..¹⁰⁵][¹⁰⁶..¹⁰⁷][¹⁰⁸..]

Once the model was trained, we evaluated the latent space by encoding heatwave samples from the test period (2001–2022), which includes 928 heatwave events. After passing the data through the encoder, each event was mapped to a point in the 128-dimensional latent space. To uncover distinct types of heatwaves, we first reduced the dimension of the latent space to 2-dimension using t-distributed stochastic neighbor embedding (t-SNE), which is a statistical method to visualize high-dimensional data (van der Maaten and Hinton, 2008), and then applied GMM clustering to the latent vectors. GMM is an unsupervised learning method that probabilistically clusters data points into different Gaussian components. This technique identifies the [¹⁰⁹..¹¹⁰] underlying groups or clusters of heatwave events in the latent space. Each cluster corresponds to a distinct type of heatwave event [¹¹⁰..¹¹¹] characterized by similar atmospheric conditions. We extracted the centroids for each GMM cluster to interpret the resulting clusters. [¹¹¹..¹¹²] For interpretation, we do not reconstruct the cluster centroid directly through the decoder, since the stochastic nature of the VAE means that latent positions and cluster centers can vary slightly across runs. Instead, we retrieve the 100 heatwave samples closest to each cluster centroid in the latent space [¹¹²..¹¹³] and compute composite maps of the nine climate-relevant variables [¹¹³..¹¹⁴] (Happé et al., 2024). This approach produces spatial patterns that are more stable and physically consistent, because neighboring samples in latent space already share

⁸⁶removed: Overall R^2 score and per channel for samples in the test subset. The evaluation is based on the input data structured as 928 samples with nine channels, each covering 11 timesteps and a spatial grid of 64×192 points.

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⁸⁹removed: 2-meter temperature (*t2m*)

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⁹¹removed: 10-meter zonal wind (*u10*)

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similar structures (Kingma and Welling, 2019). This process ¹¹⁴enables us to analyze the spatial patterns associated with each cluster and the conditions described by these variables, ¹¹⁵culminating in the heatwave onset (Rouges et al., 2023). A potential concern is that averaging might partially cancel features if events are spatially shifted. To assess this, we tested composite maps with different sample sizes ($N = \{1, 5, 10, 25, 50, 100\}$). Patterns remain consistent for $N > 5$, while the single-sample composite differs, as expected, since the 1-sample map corresponds to an individual event and cluster centers (see Appendix Figure A9-A14). Due to the stochastic nature of the method, the position of the heatwave sample assigned as the cluster center in the latent space may not be stable. These tests confirm that the composite maps are therefore more reliable in capturing robust spatial signals representative of each heatwave cluster.

220 3 Results

3.1 Identification of heatwaves

Figure 3 shows the annual number of heatwave events in Western Europe identified in the ERA5 reanalysis dataset from 1940 to 2022. We observe a gradual increase in heatwave frequency starting in the 1980s, which becomes especially pronounced after the mid-1990s. ¹¹⁶Over the past two decades, annual heatwaves have frequently exceeded 40 events, culminating in a peak of 55 events in 2021, the highest value within the analyzed period. These findings are consistent with other studies, ¹¹⁷which have shown that heatwaves ¹¹⁸are becoming more frequent (Coumou and Rahmstorf, 2012; Rahmstorf and Coumou, 2011; Perkins-Kirkpatrick and Lewis, 2020; Fischer et al., 2021; IPCC, 2021; Wang et al., 2024; Huntingford et al., 2024). While the overall trend indicates an increase in the frequency of heatwaves, we also find occasional declines in annual counts. These lower counts can be attributed to interannual climate variability and varying meteorological conditions for heatwave formation (Perkins-Kirkpatrick et al., 2017).

After training the VAE model, we ¹¹⁹evaluated its reconstruction performance for all climate variables across the training, validation, and test subsets (Table 2). The model achieves overall R^2 scores of 0.76, 0.73, and 0.72 for the train, validation, and test data, respectively, indicating stable performance and good generalization without signs of overfitting. The highest reconstruction skill is obtained for geopotential height ($z500$) and mean sea level pressure (msl). This agrees with Jézéquel et al. (2018), who found that geopotential height better represents temperature anomalies associated with European heatwaves. Near-surface variables such as 2-meter temperature ($t2m$) and 10-meter wind components ($u10$, $v10$) show lower scores, reflecting their higher spatiotemporal variability influenced by local surface conditions, which are difficult for the model to capture accurately, considering the coarse spatial resolution of the data and the smoothing of small-scale variability due to the reconstruction loss.

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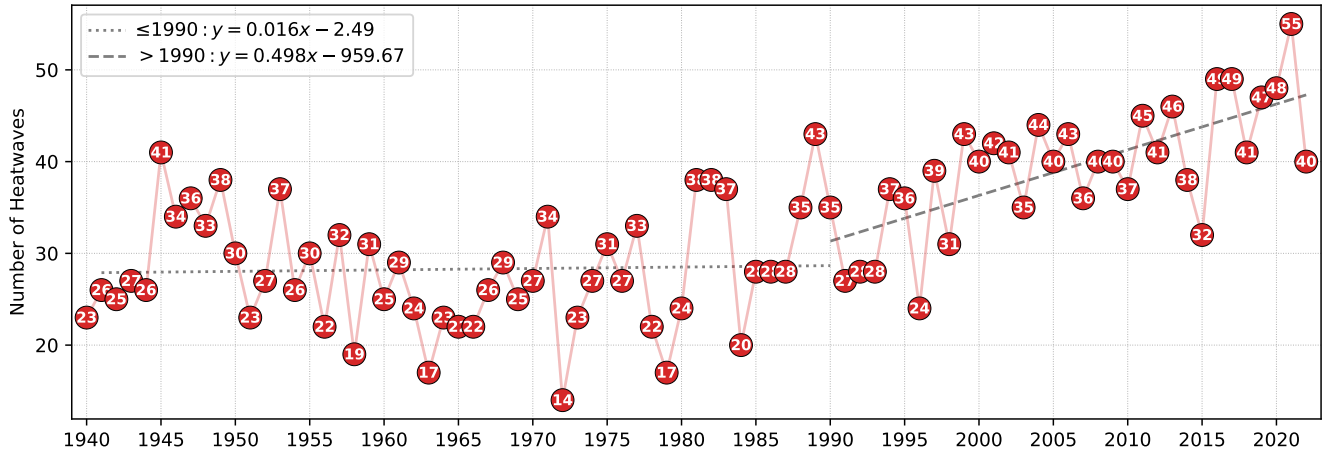


Figure 3. Number of detected heatwave events per year in Western Europe, from 1940 to 2022, identified by the GDBSCAN algorithm (Sander et al., 1998) in ERA5 reanalysis data using the grid cells that exceed the 90th percentile with respect to the 1941-1980 daily maximum temperature climatology. This period precedes the stronger warming trends after 1980 in Europe (Elguindi et al., 2013).

Table 2. R^2 scores for training, validation, and test subsets. The evaluation is based on input data structured into 1408, 320, and 928 samples for the training, validation, and testing sets, respectively, each with nine channels covering 11 days on a 64×192 grid.

Channel	Train R^2	Validation R^2	Test R^2
2-meter temperature (<i>t2m</i>)	0.7187	0.6705	0.6163
10-meter zonal wind (<i>u10</i>)	0.6863	0.6466	0.6416
10-meter meridional wind (<i>v10</i>)	0.7010	0.6613	0.6567
Total cloud cover (<i>tcc</i>)	0.7391	0.7167	0.7100
Surface solar radiation (<i>ssr</i>)	0.7371	0.7205	0.7139
Relative humidity (<i>r</i>)	0.7889	0.7716	0.7722
Stream function (<i>stream250</i>)	0.8060	0.7819	0.7753
Mean sea level pressure (<i>msl</i>)	0.8222	0.8041	0.8027
Geopotential height (<i>z500</i>)	0.8463	0.8269	0.8226
All variables	0.7606	0.7333	0.7235

240 Then, we analyzed the latent space representation of heatwave samples. Each multivariate heatwave sample was encoded into a 128-dimensional latent space by the VAE. As an intermediate processing step, we first used Principal Component Analysis (PCA) to reduce the dimensionality of all heatwave samples from 1941-2022 to 50 components^[.120]. Then, we applied the t-SNE algorithm to ^[.121]all heatwave samples to reduce them to two dimensions for visualization of the latent

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space. This two-step approach is recommended by van der Maaten and Hinton (2008) for t-SNE visualizations of high-dimensional latent space to reduce the number of dimensions and help to ensure efficiency and robustness (Pedregosa et al., 2011). Because these steps involve stochasticity, we fixed the random seed to 42 (Adams, 1979) for PCA, t-SNE, and GMM to ensure consistency across visualization runs.

Figure 4 shows the t-SNE projections for training (1941-1990), validation (1991-2000), test (2001-2022), and combined (1941-2022) samples. During training (from 1941 to 1990, characterized by heatwaves), the VAE was exposed to a larger set of heatwave patterns, which were encoded into a latent space. This spread suggests that there was a broad diversity in training examples. The validation period shows a consistent distribution with the training periods, suggesting that the model generalizes well with the validation data (1991-2000). Interestingly, the latent space for the test period (2001-2022) shows a ring-like structure with fewer samples in the center and an accumulation toward the positive values of the first component (see Figure 4c). This shift compared to previous periods might imply that the nature of heatwaves has changed compared to historical periods. As heatwaves become more frequent and extreme (Perkins-Kirkpatrick and Lewis, 2020; Fischer et al., 2021; IPCC, 2021; Russo et al., 2015; Lhotka and Kysely, 2022; Paçal et al., 2023), the VAE encodes these heatwave samples, which are underrepresented in the training period, into regions of the latent space not occupied by training heatwave samples. This subtle drift is more pronounced in the combined panel in Figure 4d, which suggests a change in heatwave characteristics for the most recent period (2001-2022).

We fitted multiple GMM components to the latent space to identify different clusters of heatwaves. After testing the GMM fits with the Bayesian Information Criterion (BIC) scores and cluster stability across different random initializations, we found that four clusters provide the most robust grouping of test samples (see Figure A3 in the Appendix for BIC scores across different components for training, validation, and test periods). While the BIC scores favor simpler models for training and validation sets, the test set exhibits a clear minimum score at four components. This balances model complexity and fits well, as BIC values steadily increase beyond four across all datasets. We color-coded heatwave sample representations in the latent space to interpret these clusters according to their corresponding seasons. As shown in Figure 4f, some clusters are dominated by heatwaves happening at specific seasons (e.g., Cluster #2 with mostly June-July-August (JJA) events), indicating that the model distinguishes between heatwave patterns that align with different seasonal characteristics. While some of this separation could also emerge from individual variables such as air temperature, using multiple variables provides a more complex representation of the atmospheric conditions associated with each cluster. This seasonal structure emerges even though the input data were deseasonalized and standardized. Clusters #2 and #3 in Figure 4f, respectively, correspond to nearly the same heatwave samples as those shown in the three-component clustering (see Figure A2 in the Appendix). Since the samples correspond mostly to JJA months in the latent space represented on the right side of the t-SNE plots, this also suggests that these heatwave samples were not very frequent historically, as this aggregation is clearly outside of training pe-

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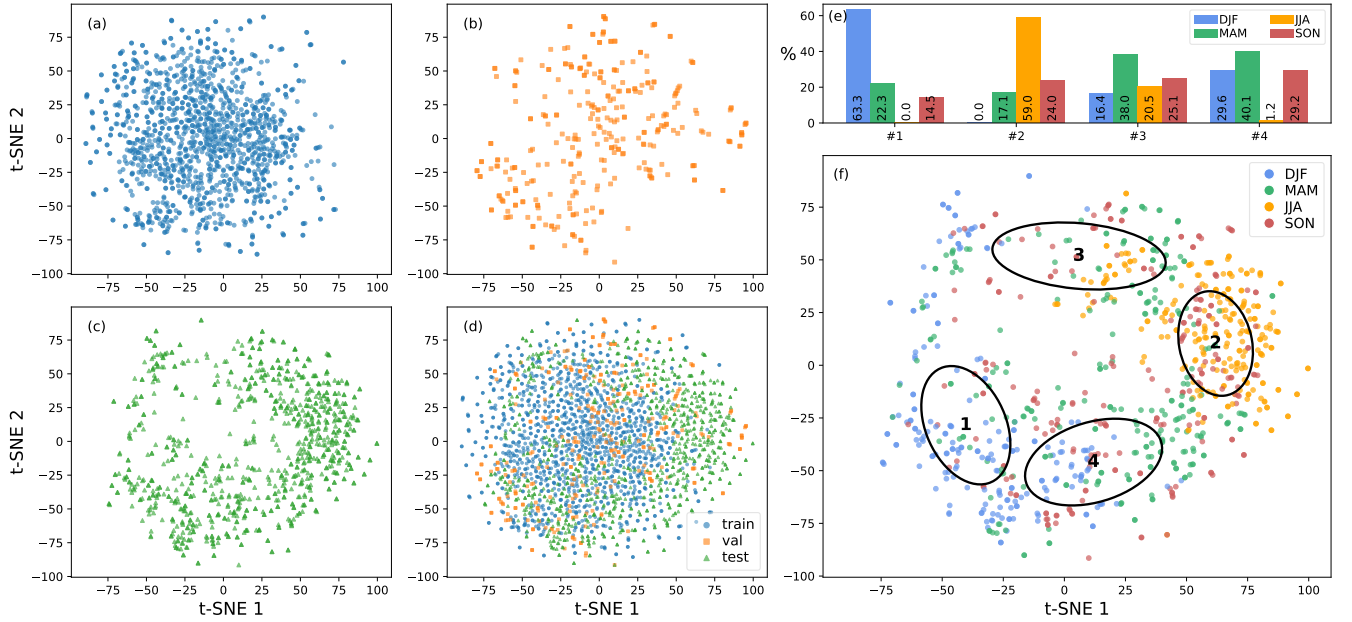


Figure 4. t-SNE representation of the latent space for (a) training (1941–1990), (b) validation (1991–2000), (c) test (2001–2022), and (d) the full period (1941–2022). (e) shows the seasonal distribution of samples within each cluster. (f) displays the t-SNE projection of test-period heatwave samples colored by the season of onset, with ellipses representing the four Gaussian Mixture Model components. Each point corresponds to an individual heatwave event.

275 rioid samples, as shown in the combined panel in Figure 4. Since four components in Figure 4f provide the possibility of a more detailed analysis for heatwave samples within cluster #1, i.e., those corresponding to December-January-February (DJF) winter months, while having a similar cluster #2 and #3 as in the three-cluster case (see [...¹²⁸]Figure A2 in the Appendix), we chose four GMM components for our further analysis. Similarly, Happé et al. (2024) found that four clusters were optimal for their latent space analysis. Our identified clusters represent then the following seasons: cluster #1 represents DJF (Section 3.2), cluster #2 represents JJA (Section 3.3), clusters #3 and #4 represent transition seasons March–April–May (MAM) or September–October–November (SON) (Section 3.4). To further investigate whether the clustering reflects only seasonal differences or distinct dynamical regimes, we examined the standardized mean anomaly of each variable within the four clusters (Figure 5). For each variable, we computed the mean standardized anomaly values over all heatwave samples in a cluster. These mean values represent the typical anomaly structure captured by each cluster. Although the clusters align broadly with seasonal timing, their multivariate structures differ beyond temperature intensity. For instance, Cluster #1, representing mainly winter events, exhibits on average weaker positive temperature anomalies but enhanced warm advection (positive v10 values) and reduced solar input (low ssr) (Spanjers et al., 2025). Cluster #2 shows strong positive t2m, r, and z500 anomalies typical of intense summer heatwaves (Vautard et al., 2023). Clusters #3 and #4 show mixed

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transition season features, one dominated by high solar radiation and the other by stronger pressure anomalies (Träger-
 290 Chatterjee et al., 2013; Boboc et al., 2025). These differences suggest that the latent space clustering captures distinct
 dynamical configurations, rather than just temperature variability.

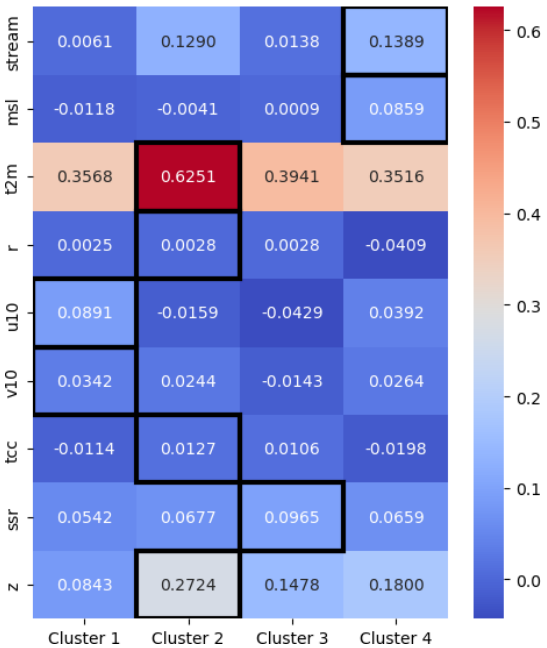


Figure 5. Mean standardized anomaly values for each variable, averaged over all heatwave samples in each latent cluster. The values summarize the typical anomaly patterns represented by the four clusters. Black boxes represent the highest value for each variable.

To analyze the atmospheric patterns before and during heatwaves, we constructed composite representations of heatwave samples for each cluster by selecting the closest 100 samples (in latent space) to each GMM cluster centroid, similar to the procedures described by Rouges et al. (2023) and Happé et al. (2024). Since the entire process, i.e., the encoding of
 295 heatwave samples to the latent space by the VAE, the dimensionality reduction via t-SNE, and the GMM clustering, contains randomness, a single sample may be sensitive to random fluctuations. The composite maps provide a more stable representation of atmospheric conditions for each cluster by averaging over the closest samples in the latent space. The anomalies of each variable are displayed for the North Atlantic region (as shown in Figure 2) for each of the eleven analyzed days (five days [.129
]before the onset of the heatwave; the onset day of the heatwave, indicated with a broader frame around the graphs; and five
 300 days after the onset of the heatwave), and all four identified clusters. The results are shown in Figures 7 to 15.

To assess the physical relevance of our VAE-based clustering, we selected several major European heatwaves that have been extensively studied in the literature as case studies. Russo et al. (2015) identified and ranked the top ten most severe European heatwaves between 1950 and 2014, highlighting events such as the 2003 Western European and 2010 Russian heatwaves as

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the most severe. ^[..¹³⁰] Lhotka and Kysely (2022) expanded on this work by providing an updated catalog of major heatwaves up to 2021. Following these studies, we selected the 2003, 2010, and 2018 heatwaves as case studies to examine whether the VAE latent space captures the known dynamical features of these benchmark events. Due to differences in detection methods, the exact onset dates of heatwaves in our dataset do not always align with those reported in the literature. Therefore, for each target heatwave date defined by ^[..¹³¹] Lhotka and Kysely (2022) (“target date” in Figure 6), we identified the temporally closest matching event in our dataset (“closest date” in Figure 6). We then extracted the ten nearest neighbors in the latent space around each closest date to construct composite anomaly maps. This ^[..¹³²] procedure allows us to ^[..¹³³] place these historically significant heatwaves within the structure of the learned latent space and to compare the resulting anomaly patterns directly with those documented in the literature. As shown in Figure 6, the resulting geopotential height at 500 hPa (z_{500}) anomaly maps exhibit similar patterns to those reported by ^[..¹³⁴] Lhotka and Kysely (2022). In particular, the 2010 ^[..¹³⁵] heatwave shows the characteristic strong positive z_{500} anomalies over western Russia, the 2003 ^[..¹³⁶] event exhibits the ridge over central Europe, and the 2018 heatwave ^[..¹³⁷] displays height anomalies over Scandinavia^[..¹³⁸]. These spatial features closely match the patterns reported in Figure 3 ^[..¹³⁹] of Lhotka and Kysely (2022), demonstrating that the VAE organizes these events in a way that is consistent with established dynamical interpretations.

3.2 Cluster #1

Using the composite maps, we found that four heatwave clusters provide distinct atmospheric patterns for heatwaves in different seasons. In Figures 7 and 8, cluster #1 shows a similar pattern to the UK High cluster in Happé et al. (2024) and the omega block in Rouges et al. (2023) for the onset day of the heatwaves. While Happé et al. (2024) found this UK high pattern in summer (JJA) months and Rouges et al. (2023) found this pattern in extended summer (May to September) months, we detected that heatwaves, not just in summer, but also in winter months, show this or a similar pattern.

The positive anomalies over the British Isles and Western Europe, characteristic of this pattern, ^[..¹⁴²] persist $t-5$ days before the heatwave and ^[..¹⁴³] gradually spread into the Mediterranean. Similarly, the geopotential height at 500 hPa (z_{500}) exhibits positive anomaly values centered over Western Europe before the onset of the heatwave, as shown in Figure 15, in line with findings from both Tomczyk et al. (2019) and Leach et al. (2021), who associated winter heatwaves over Europe with positive anomalies of geopotential height. Rouges et al. (2023) classified European heatwaves into five distinct types based on daily

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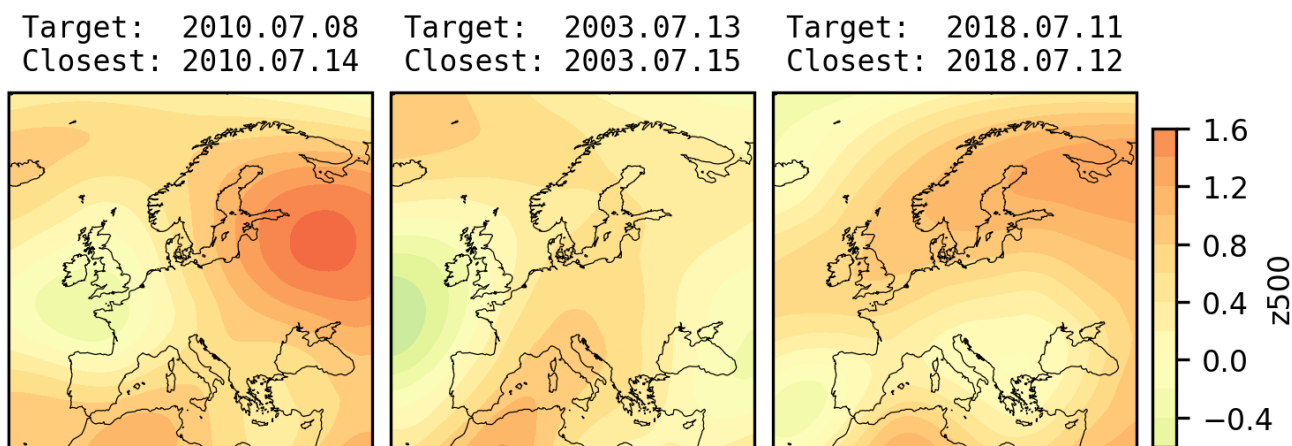


Figure 6. Geopotential height at 500 hPa ($z500$) anomaly maps for three historically significant European heatwaves: 2010, 2003, and 2018. The *target dates* correspond to the heatwave onset dates defined by [..¹⁴⁰]Lhotka and Kysely (2022), while the *closest dates* refer to the temporally nearest matching events detected in our dataset using the GDBSCAN algorithm. For each event, composite maps are constructed by averaging the ten latent space neighbors closest to the selected onset date. The spatial domain in this figure is cropped to match that used by [..¹⁴¹]Lhotka and Kysely (2022), for consistency, although other figures in this study use a broader domain.

mean 2-meter temperature anomalies and geopotential height anomalies at 500 hPa[..¹⁴⁴], characterizing the western Europe cluster as a temperature anomaly spread across France and the British Isles, with its circulation pattern similar to an omega-type blocking pattern. This pattern is analogous to our identified cluster #1. As the extreme event progresses (the days after the onset), these geopotential height at 500 hPa ($z500$) anomalies begin to disperse eastward across the North Atlantic, as shown in cluster #1 in Figure 15. Tomczyk et al. (2019) also [..¹⁴⁵]demonstrated this in their study: [..¹⁴⁶]anomalies in geopotential height begin to develop over the North Atlantic and move towards Europe, where they [..¹⁴⁷]intensify as they traverse the continent. This pattern of dispersion is also evident in Figure 11: the positive maximum temperature anomalies associated with winter heatwaves are initially concentrated over Western Europe, gradually weakening and dissipating similarly, following the onset of the heatwave events in cluster #1. These patterns are also consistent with findings from previous studies where heatwaves in north-west Europe are typically found to be related to blockings (Carril et al., 2008; Zschenderlein et al., 2020). This blocking is also accompanied by a positive (negative) anomaly in the zonal wind ($u10$) component at the north (south), and a dipole structure with positive (negative) anomalies to the west (east) in the meridional wind ($v10$) (see cluster #1 in Figures 13 and 14). Together, these features point to a blocking structure with enhanced atmospheric stagnation, consistent with an anti-cyclonic flow (Kautz et al., 2022), and advection of warm-moist air from the Atlantic (Spanjers et al., 2025). This

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blocking system helps to create and maintain unusually warm weather as it is associated with clear skies, as shown in cluster #1 in Figures 10 and 12. The lack of cloud cover, indicated by negative anomalies in the total cloud cover (*tcc*) variable, for cluster #1 over Southern Europe and the Mediterranean in Figure 12, allows more solar radiation to reach the Earth's surface, especially during the build-up of the heatwaves (days $t - 5$ to day 0), where these negative anomalies are more pronounced. The positive anomalies in surface net solar radiation (*ssr*), as shown in Figure 10, become more distinct especially after the heatwave event has started, creating a feedback loop that brings further warm and dry air into the region, as shown with negative relative humidity (*r*) anomalies located over Europe in Figure 9 during the onset. During the days after the onset, the negative anomaly for relative humidity tends to move eastward towards the Middle East.

Notably, while previous studies have linked these atmospheric circulation patterns to summer heatwaves, our clustering, which encompasses year-round heatwave data, reveals that similar patterns also manifest during winter events.

3.3 Cluster #2

Cluster #2, which corresponds to mostly summer heatwaves, as shown in Figure 4f, exhibits a similar atmospheric pattern to the southern European cluster (SE) in Rouges et al. (2023). As shown in Figure 7, stream function at 250 hPa (*stream250*) shows a broad negative anomaly over the North Atlantic, expanding from Greenland to Scandinavia, while a larger positive anomaly block is observed from the central North Atlantic to Russia from $t - 5$ days before the heatwave onset. Similarly, a continuous ridge pattern in geopotential height at 500 hPa (*z500*) is detectable. It is accompanied by a positive anomaly in zonal wind component, as shown in Figure 13, up to $t + 3$ days, and positive anomalies in the meridional wind component, especially from $t - 1$ days in the build-up period of heatwaves, as shown in Figure 14. These anomalies point towards a larger heat transfer from lower latitudes to Europe. Positive anomalies in geopotential height at 500 hPa (*z500*) over the Subtropical North Atlantic region start $t - 5$ days before the onset, and later sweep into Central Europe during the progression of heatwaves. This finding is similar to [..¹⁴⁸]those reported by Tomczyk et al. (2019), who showed that the occurrence of warm spells in winter months is associated with positive anomalies of geopotential height at 500 hPa (*z500*) over Central Europe. After the onset, the positive anomaly ridge in stream function at 250 hPa (*stream250*), stretching from central North Atlantic to Russia, surrounds the North Atlantic trough, and extends to North America through to the Arctic during the progression of heatwaves, as seen in cluster #2, from $t = 0$ to $t + 5$, in Figure 7, while the negative anomalies over North Atlantic dissipates. A persistent negative mean sea level pressure (*msl*) anomaly occurs over the British Isles during the build-up period of these heatwaves, where it later gives place to a positive anomaly over Russia up to $t + 3$ days, as shown in Figure 8. As these persistent patterns start to dissipate after the [..¹⁴⁹]onset of the heatwave, cloud-free skies and a stagnant atmosphere [..¹⁵⁰]prevail. This is indicated by expanding negative anomalies in total cloud cover (*tcc*) over Europe and Russia, and near-zero wind speed anomalies, as shown in Figures 12 and 13-14, respectively. The positive anomalies in relative humidity (*r*) over the North Atlantic during

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the build-up period of heatwaves [..¹⁵¹] gradually spread into Western Europe, as the zonal wind component [..¹⁵²] exhibits positive anomalies during the same time. This brings more humid and warm air to Europe, creating the positive anomalies in relative humidity (r) over Western Europe on the onset date, and merging with the anomalies over the Middle East during the heatwave, as shown in Figure 9. Simultaneously, positive temperature anomalies propagate northeast towards central Europe as the heatwave progresses, as shown in Figure 11. On the other hand, a clear negative anomaly pattern over the North Atlantic in 2-meter temperatures ($t2m$) is observed during the build-up and progression of the heatwaves [..¹⁵³]. This negative anomaly pattern over the North Atlantic is consistent with results described by Krüger et al. (2023), Bischof et al. (2023), and Lipfert et al. (2024), [..¹⁵⁴] who showed that colder-than-usual North Atlantic sea surface temperatures (SSTs) [..¹⁵⁵] with a negative tendency [..¹⁵⁶] are associated with persistent negative anomalies. These conditions promote a deep North Atlantic trough and the subsequent formation of a European ridge, which in turn favors stronger and longer-lasting heatwaves as well as a shift toward positive [..¹⁵⁷] summer temperature anomalies over Europe (Krüger et al., 2023). These different atmospheric mechanisms help [..¹⁵⁸] explain why the latent space representations of summer heatwave samples (see Figure 4) are [..¹⁵⁹] distinctly clustered and separate from the rest of the dataset. As heatwaves intensify and high temperatures rise more rapidly in Europe and other mid-latitude regions (Perkins-Kirkpatrick and Lewis, 2020; Bischof et al., 2023; Paçal et al., 2023), these events diverge from the historical distribution learned by the VAE. Since the test data is unseen during training, such extreme events are encoded differently in the latent space.

3.4 Clusters #3 and #4

Clusters #3 and #4 primarily correspond to heatwaves in the transition seasons, occurring mainly during MAM or SON. Although both occur mainly during MAM and SON, they represent different dynamical regimes. Cluster #3 is dominated by enhanced solar radiation, while Cluster #4 is linked to stronger large-scale pressure anomalies. Similarly, autumn heatwaves are associated with high-pressure anomalies over western and southern Europe, leading to persistent warm conditions (Boboc et al., 2025). Träger-Chatterjee et al. (2013) found that enhanced solar irradiation during late winter and spring is associated with the development of warm conditions in the coming months. Even though it is not possible to assign these clusters to certain seasons as we could do with the first two clusters, cluster #4 shows some similarities in anomaly patterns in certain variables with cluster #1, such as (1) 2-meter temperature ($t2m$), where both show a negative–positive–negative anomaly tripole across the North Atlantic–Europe–Russia domain; (2) mean sea level pressure (msl), where both show negative anomalies closer to Arctic while having positive anomalies over Europe, (3) stream function at 250 hPa ($stream250$), where

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400 both show negative anomalies over Greenland with positive anomalies over Europe. These similarities could explain why the GMMs in Figures A2 and 4f, with three or four components, consistently identify the same seasonal clusters (#2 and #3), while clusters #1 and #4 are either merged or separated depending on the number of components. Four components are used in our study to better understand the differences [..¹⁶⁰]in the characteristics of heatwave clusters.

Although clusters #3 and #4 are both associated with transition seasons, they exhibit nearly opposite atmospheric anomaly patterns in several key climate variables. For instance, in Figure 15, cluster #3 displays a positive geopotential height at 500 hPa ($z500$) anomaly over Greenland and negative anomalies over the North Atlantic extending into Scandinavia, [..¹⁶¹]a pattern consistent with Greenland blocking events which are known to cause European heatwaves (Kornhuber et al., 2017). Conversely, cluster #4 shows the opposite, i.e., negative anomalies over Greenland and positive anomalies over the North Atlantic–Scandinavia sector. This creates a contrasting tripole structure during the heatwave build-up phase, which then evolves into opposite-sign anomalies over Scandinavia as the events progress. Likewise, the zonal ($u10$) and meridional ($v10$) wind component anomalies show opposing dipole structures between the two clusters, as shown in Figure 13 and 14. Cluster #3 shows a positive meridional wind ($v10$) anomaly over the Canaries, $t - 5$ days before the onset, and slowly becomes more prominent as the anomaly expands towards Europe during the event’s progress. Since this positive anomaly of wind becomes more prominent as the onset date approaches, increasing wind anomalies enhance the advection of warm air from the south, as shown in Figure 11.

On the other hand, the wind components for cluster #4 exhibit anti-cyclonic flow with positive (negative) anomalies over the western North Atlantic (Canaries) during the build-up shown in Figures 13 and 14, which carries warm air through the North Atlantic, as shown in temperature anomalies in Figure 11. Cluster #3 is characterized by an elongated trough in stream function at 250 hPa ($stream250$) extending from the east coast of Canada towards Scandinavia, with a ridge over Greenland. Conversely, cluster #4 exhibits an inverse pattern with a trough over Greenland, and two ridges are located over the central North Atlantic and Scandinavia, as shown in Figure 7, showing similarities with the North Atlantic Low cluster in Hap   et al. (2024). This elongated trough in cluster #3 persists across all analyzed heatwave time steps, while the ridge over the central North Atlantic in cluster #4 dissolves as the event progresses. Furthermore, while heatwave cluster #3 is accompanied by positive relative humidity (r) anomalies over the Eastern subtropical North Atlantic during the build-up and over Europe following the onset, cluster #4 exhibits negative relative humidity (r) anomalies over Central Europe and Russia (see Figure 9). Recent studies also highlight that the accelerated decline of Arctic sea ice since the 2000s has contributed to a shift toward a dipole-like atmospheric circulation mode, [..¹⁶²]resulting in more heatwaves in Europe (Zhang et al., 2020; Lee et al., 2025). These enhance warm air advection from the North Atlantic and favor soil drying over Europe, supporting the contrasting atmospheric variable anomalies observed between clusters #3 and #4.

430 4 Discussion & Conclusions

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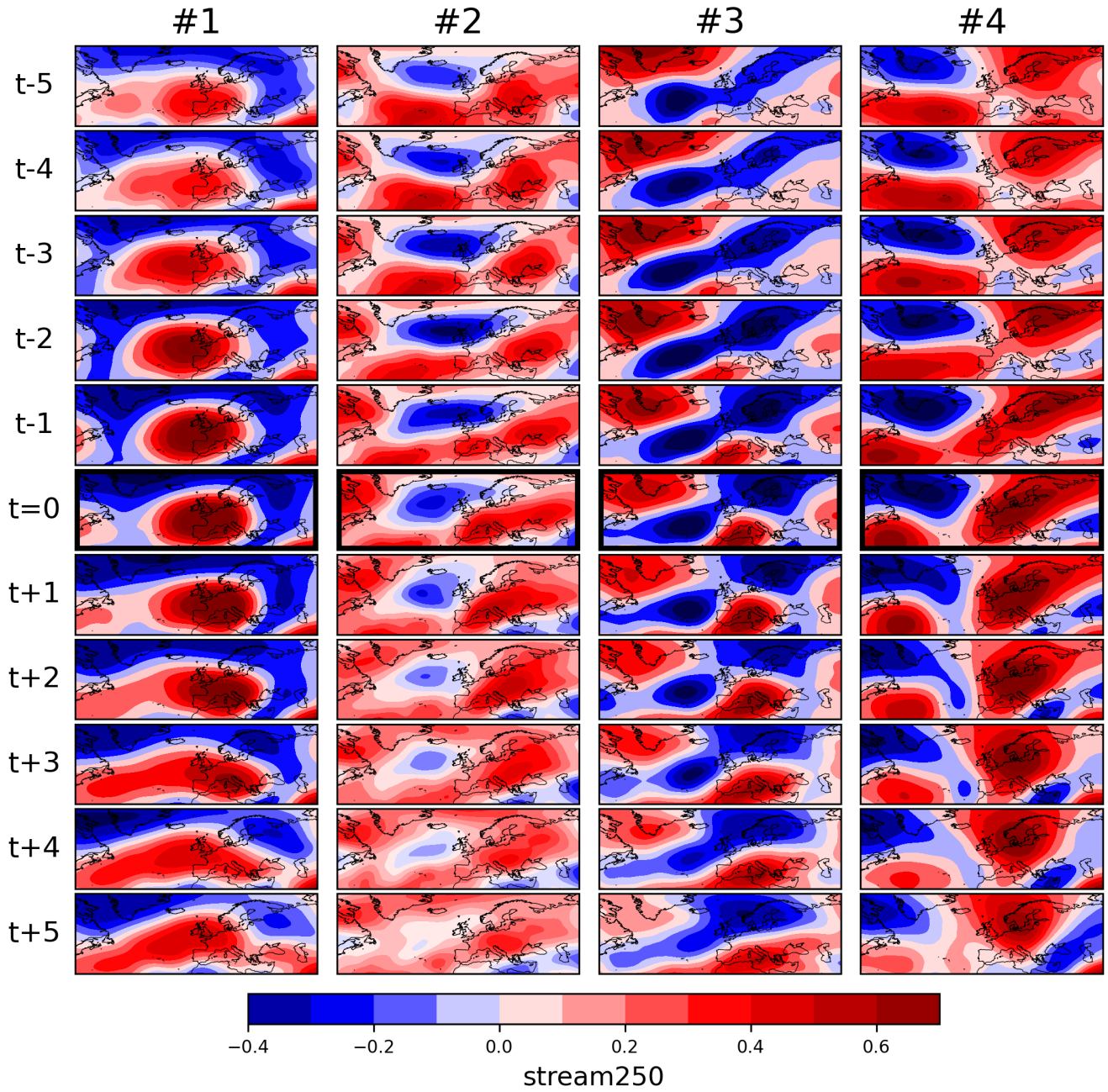


Figure 7. Composite map for standardized stream function anomaly at 250 hPa ($stream250$) across $t \pm 5$ days for each GMM cluster identified in Figure 4f. Rows show cluster #1 to #4, and each row corresponds to the cluster average of the $n=100$ heatwave samples closest to the respective GMM centroids. Time progresses from top to bottom, centered on the heatwave onset date ($t = 0$), as shown in the sixth row, and is emphasized with a broader frame.

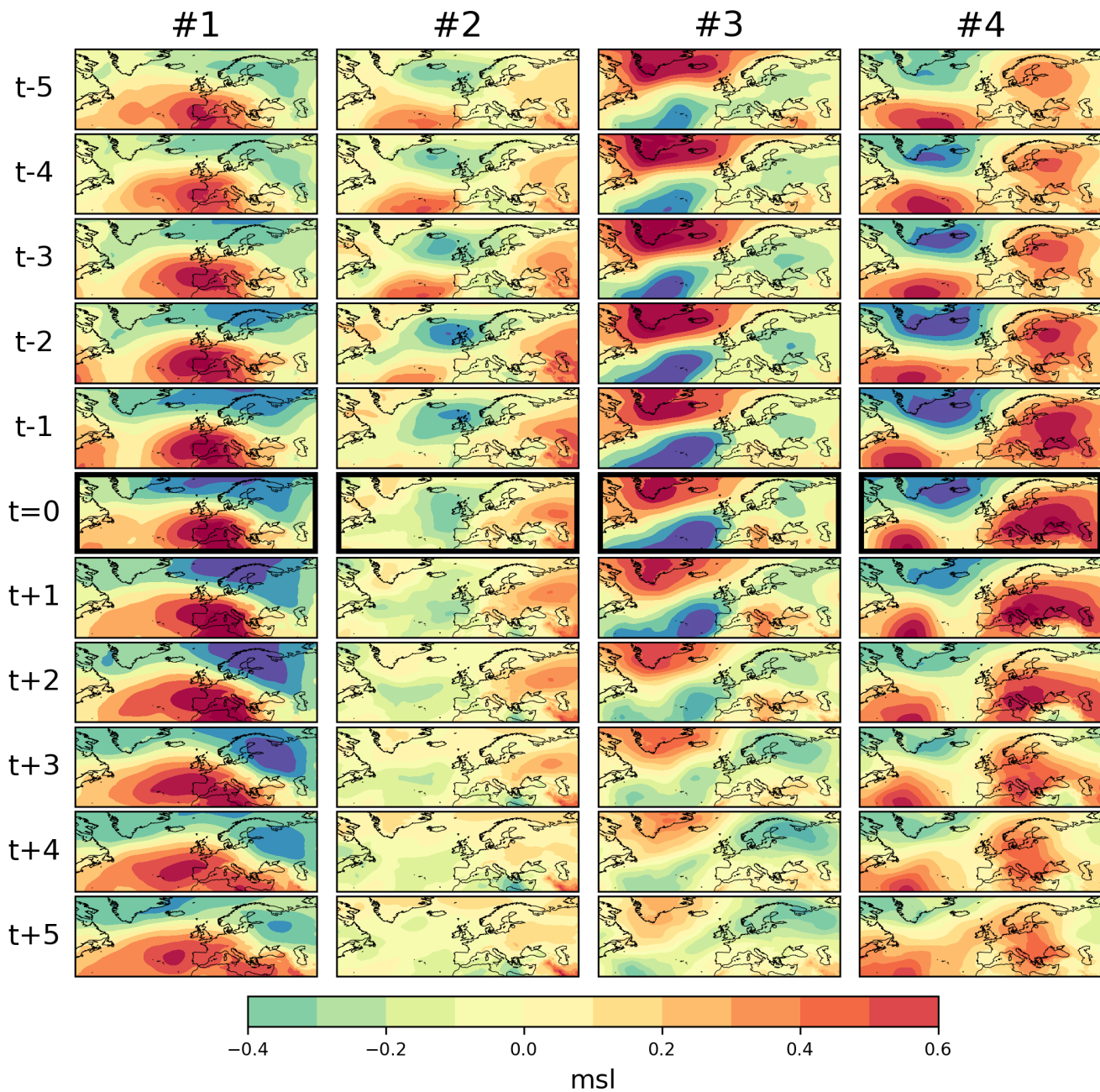


Figure 8. Same as Figure 7, but for standardized mean sea level pressure (*msl*) anomaly.

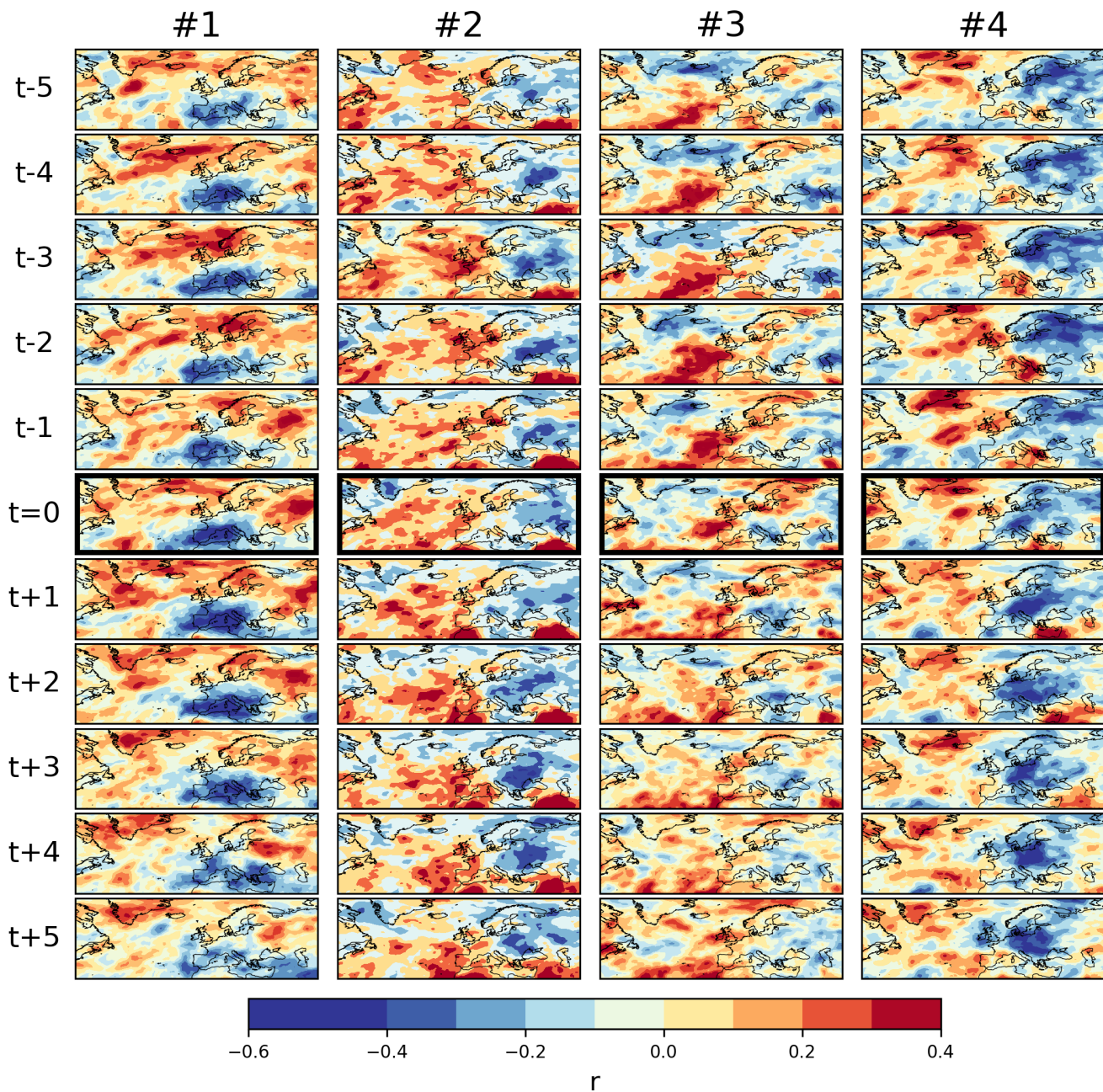


Figure 9. Same as Figure 7, but for standardized relative humidity (r) anomaly.

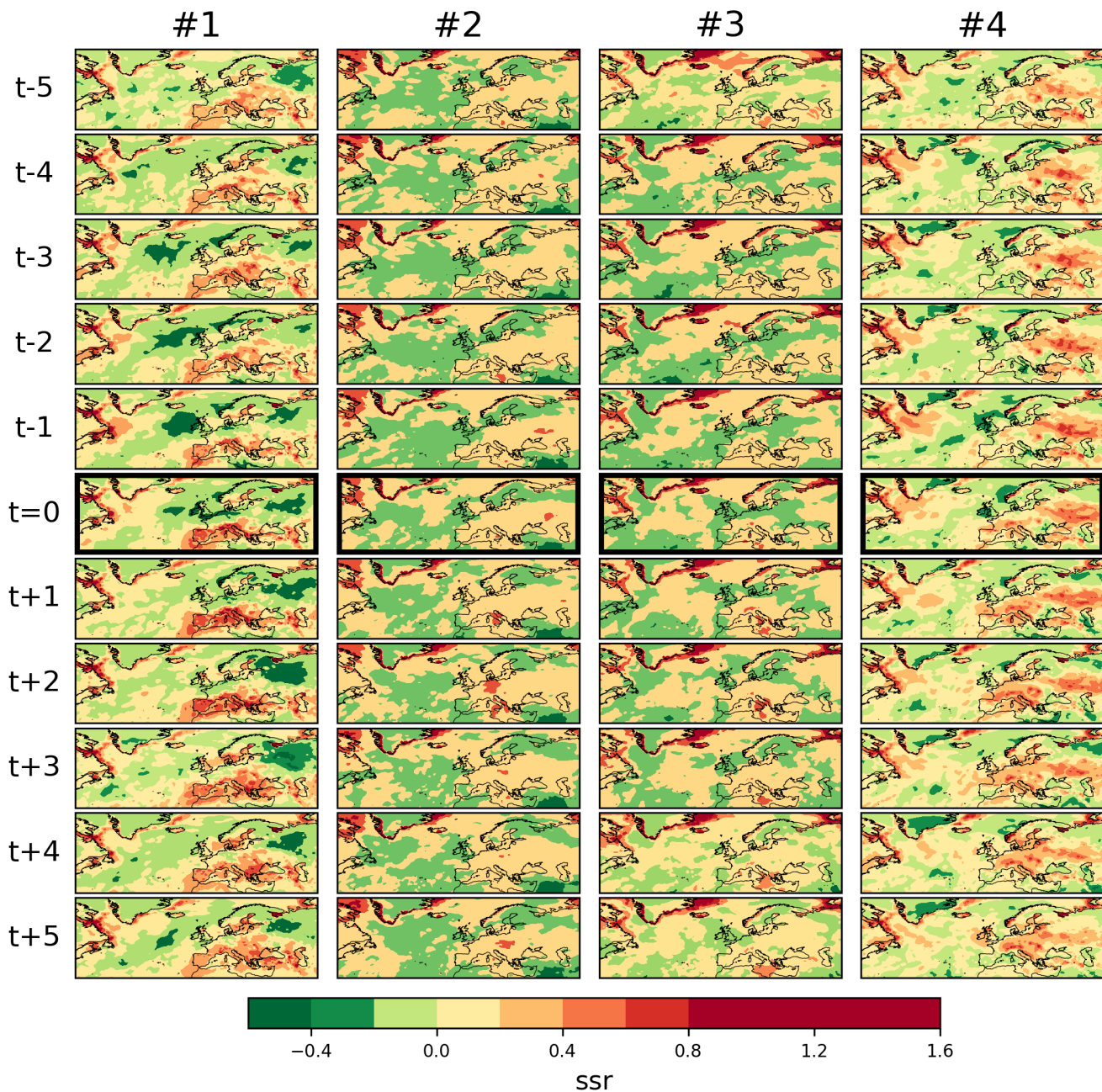


Figure 10. Same as Figure 7, but for standardized sum surface net solar radiation (ssr) anomaly.

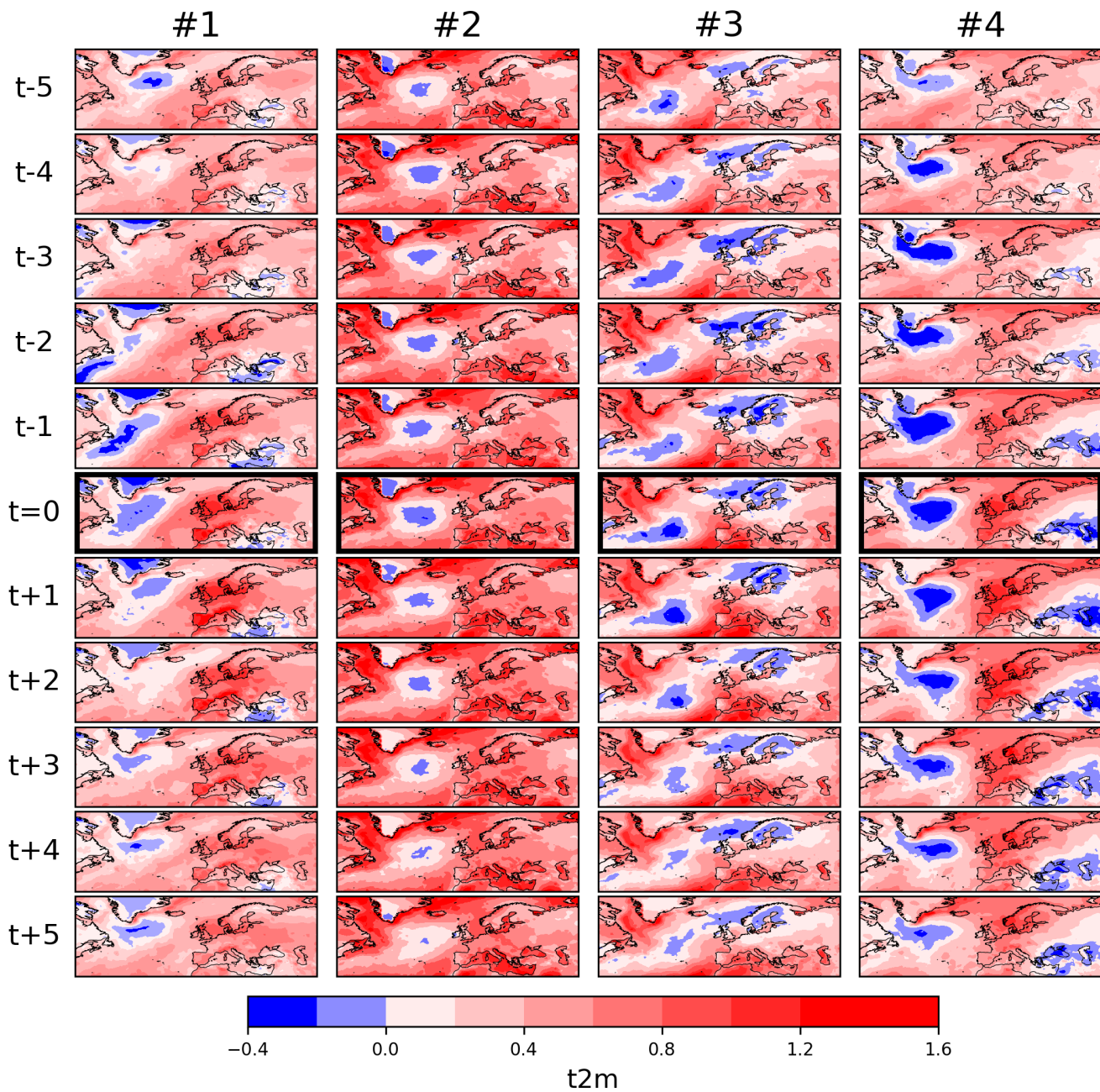


Figure 11. Same as Figure 7, but for standardized maximum 2-meter temperature ($t2m$) anomaly.

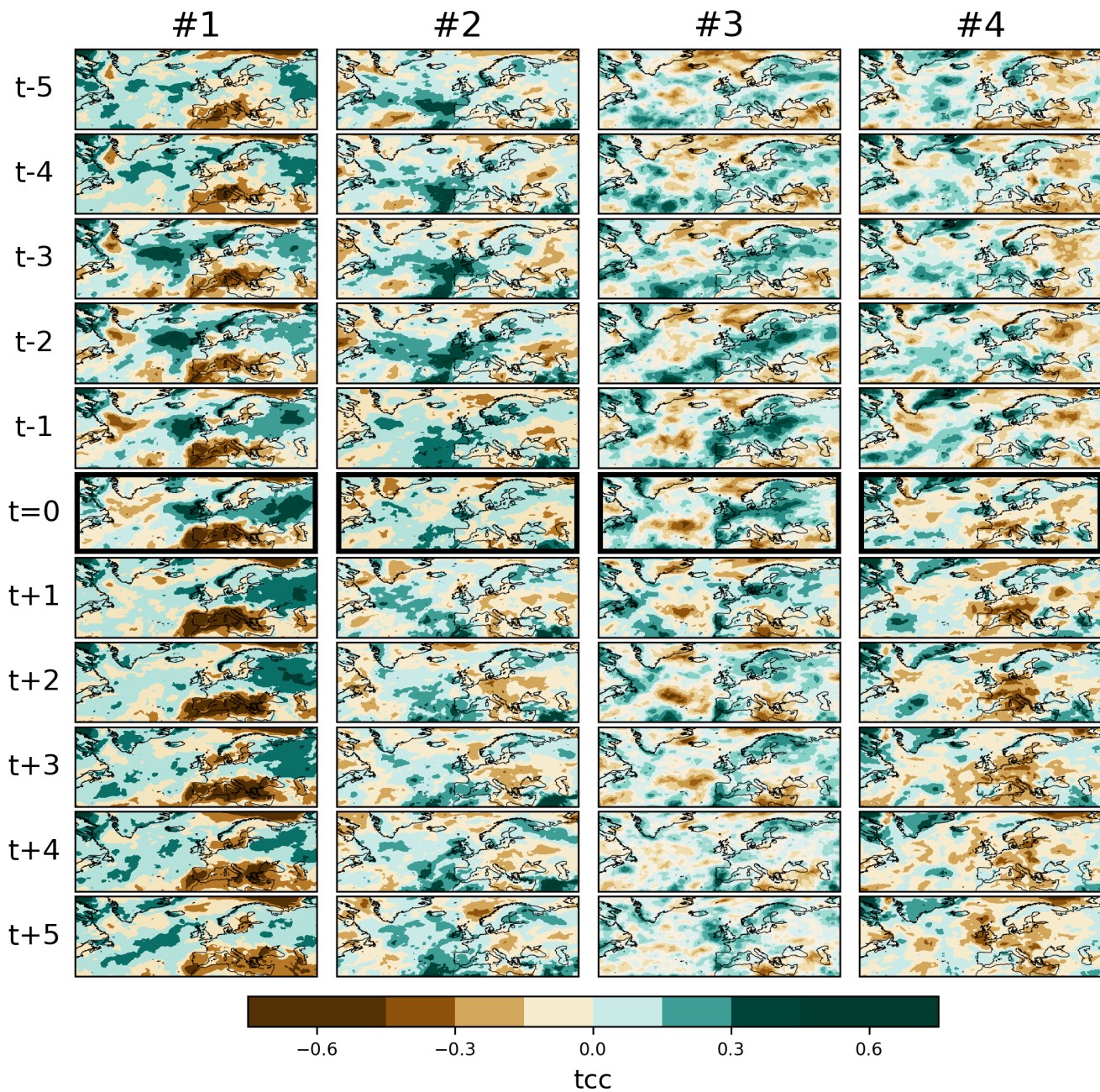


Figure 12. Same as Figure 7, but for standardized total cloud cover (*tcc*) anomaly.

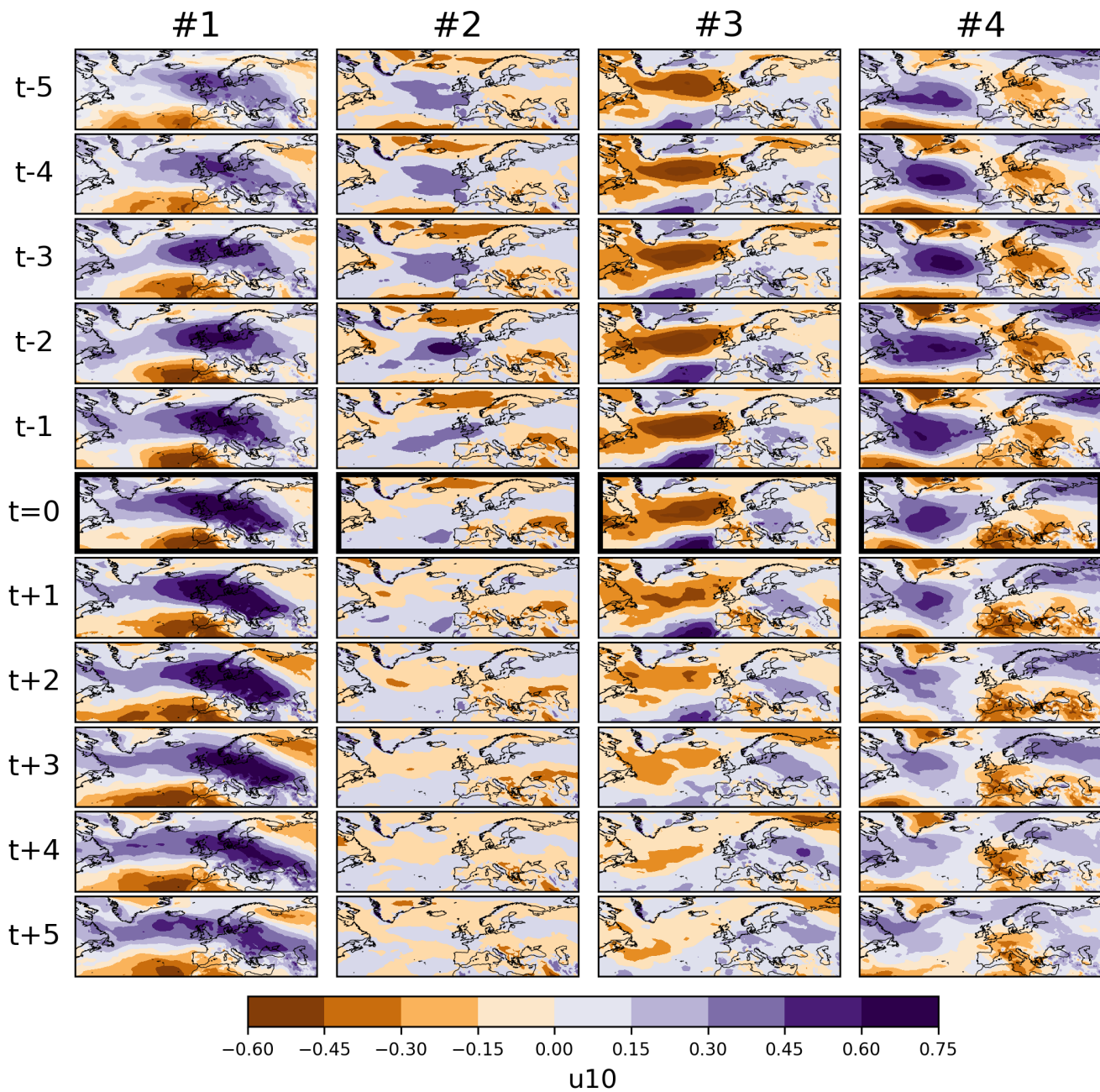


Figure 13. Same as Figure 7, but for standardized 10-meter U wind component ($u10$) anomaly.

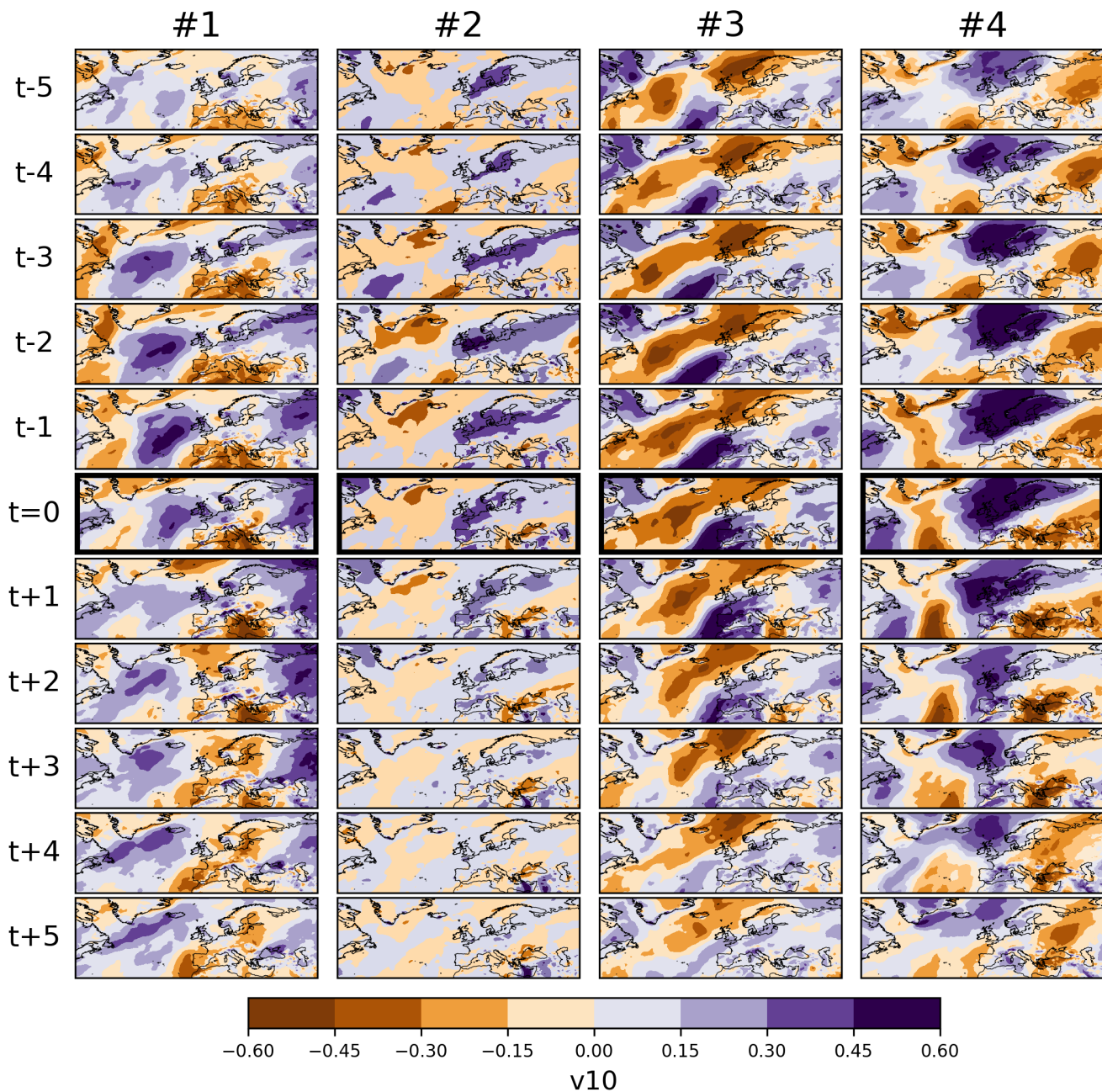


Figure 14. Same as Figure 7, but for standardized 10-meter V wind component ($v10$) anomaly.

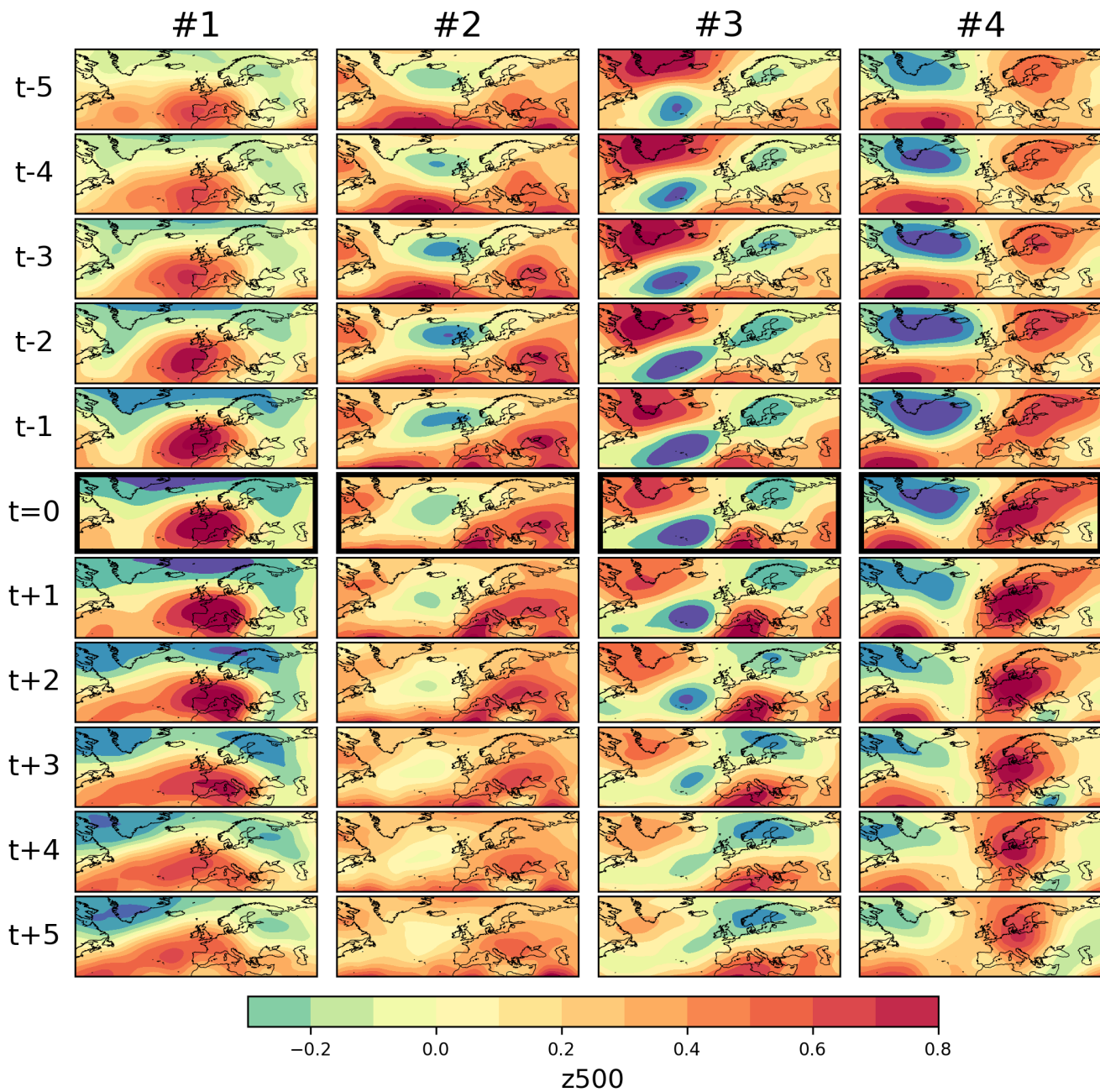


Figure 15. Same as Figure 7, but for standardized geopotential height at 500 hPa (z_{500}) anomaly.

[..¹⁶³] Heatwaves are expected to intensify and occur more frequently, particularly in Western Europe, where recent extremes have exceeded model projections. (Perkins-Kirkpatrick and Lewis, 2020; Russo and Domeisen, 2023; Schielicke and Pfahl, 2022; Paçal et al., 2023; Vautard et al., 2023; Patterson, 2023; McKinnon et al., 2024; Kornhuber et al., 2024). However, these dynamics are not yet fully understood due to the complex interactions between multivariate spatiotemporal variables and the limited availability of labeled data, making unsupervised learning a promising approach (Van Oldenborgh et al., 2022; Barriopedro et al., 2023; Ruff et al., 2021). This study aims to [..¹⁶⁴] investigate the interplay and temporal evolution [..¹⁶⁵] of different atmospheric variables in their contributions to heatwaves [..¹⁶⁶] in Western Europe. To [..¹⁶⁷] achieve this, we [..¹⁶⁸] employed a Variational Autoencoder (VAE) and interpreted the different data clusters, identified by a Gaussian Mixture Model (GMM), in the latent space. [..¹⁶⁹] Our work builds directly on Happé et al. (2024), [..¹⁷⁰] but extends it in several important ways. While their study focused on summer heatwaves in the KNMI-LENTIS ensemble dataset, our analysis uses ERA5 reanalysis data [..¹⁷¹], encompasses nine variables, spans all seasons, and incorporates a longer heatwave sample window (11 days). We also analyze historical and recent periods separately to reveal how heatwave dynamics have changed under warming. These patterns were subsequently analyzed to gain a deeper understanding of the development and progression of heatwaves across all seasons, including summer, winter, and transition periods. By training the VAE on year-round heatwave samples, we were able to capture a comprehensive view of atmospheric dynamics associated with various heatwave events. Our VAE analysis identified several distinct heatwave regimes from the ERA5 dataset, each associated with characteristic atmospheric patterns and seasonal preferences. [..¹⁷²]

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¹⁷²removed: Understanding the dynamics of heatwaves is important as they are projected to intensify and become more frequent (Perkins-Kirkpatrick and Lewis, 2020; Russo and Domeisen, 2023; Schielicke and Pfahl, 2022; Paçal et al., 2023). This is particularly relevant for Western Europe, where temperature extremes have increased faster than the projections of the climate model (Vautard et al., 2023; Patterson, 2023; McKinnon et al., 2024; Kornhuber et al., 2024). However, these dynamics are not yet fully understood due to the complex interactions between multivariate spatiotemporal variables and their responses to climate change (Van Oldenborgh et al., 2022; Barriopedro et al., 2023). Since finding labeled and high-quality data for anomaly detection is challenging, unsupervised learning methods allow for automatically distinguishing heatwaves (Ruff et al., 2021).

¹⁷³removed: We used GDBSCAN to detect heatwave events and a VAE to analyze and cluster the detected events based on their latent space representations (Happé et al., 2024). VAEs compress high-dimensional multivariate input data into a low-dimensional latent space while preserving essential features, allowing for efficient reconstruction of the input data (Kingma and Welling, 2019; Lindhe et al., 2021). The reconstruction produced by the VAE can be interpreted as a learned climatological baseline or ‘normal state,’ against which deviations can be studied. We focused on using latent space to understand the atmospheric patterns underlying different heatwave types. Similar latent space approaches have been successfully applied in climate research (Behrens et al., 2022; Oliveira et al., 2022; Shamekh et al., 2023; Mooers et al., 2023; Camps-Valls et al., 2025).

While we [..¹⁷⁴] trained the VAE model with year-round heatwave samples from ERA5, the composite [..¹⁷⁵] maps of the
 450 resulting heatwave clusters reveal atmospheric patterns consistent with previous studies, [..¹⁷⁶] which typically considered
 only summer months [..¹⁷⁷] (Carril et al., 2008; Horton et al., 2015; Rouges et al., 2023; Krüger et al., 2023; Bischof et al.,
 2023; Happé et al., 2024). We observed a similar pattern in Cluster #1 to the UK High cluster described by Happé et al.
 (2024) and the omega block reported by Rouges et al. (2023), although our analysis considered year-round heatwave
 samples. In contrast, those studies focused only on summer events. As explained before, our choice of four Gaussian
 455 components for our analyses enables a more nuanced analysis of heatwave regimes and enhances the interpretability of the
 latent space. Each of the four identified groups captures distinct atmospheric conditions in different variables analyzed, with
 well-defined patterns leading to the onset of the heatwave and their subsequent progression, as illustrated in the composite
 anomaly maps in Figures 7-15. For example, anomalies in relative humidity (r) in Figure 9 highlight contrasting patterns
 between seasonal heatwaves: Cluster #1, associated with winter heatwave samples, exhibits a pronounced negative relative
 460 humidity (r) anomaly over Western Europe and the Mediterranean, whereas cluster #2, dominated by summer heatwaves,
 shows a positive relative humidity (r) anomaly following the onset. This distinction is consistent with previous studies, [..¹⁷⁸
] which indicate that humid summer heatwaves are highly dangerous and are [..¹⁷⁹] intensifying under climate change (Russo
 et al., 2017; Dong et al., 2024; Wang et al., 2024). The total cloud cover (tcc) shows a distinct negative anomaly starting from
 $t - 5$ days and strengthening during the progression of winter heatwaves over Southern Europe, causing a positive anomaly
 465 in surface net solar radiation (ssr) a couple of days later, which brings more heat to Western Europe, as seen in cluster #1
 (Figure 10). Meanwhile, positive anomalies in total cloud cover (tcc) are observed before the onset of summer heatwaves in
 cluster #2 [..¹⁸⁰]. Still, they gradually transition into negative anomalies in total cloud cover (tcc) over Central Europe as the
 heatwave evolves (Figure 12). [..¹⁸¹] Despite the data being standardized, the VAE organizes heatwave samples into clusters
 that align with seasonal differences, suggesting [..¹⁸²] that seasonal signals are embedded in the atmospheric patterns of the
 470 test period. [..¹⁸³] Heatwave samples corresponding to summer months are separated in the learned representation, reflecting
 distinct atmospheric conditions unprecedented in the training period. [..¹⁸⁴] This suggests that parts of the changes in latent
 space are [..¹⁸⁵] due to a changing seasonal cycle of [..¹⁸⁶] atmospheric variables related to heatwaves. This [..¹⁸⁷] finding

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aligns with previous studies, which [..¹⁸⁸] have shown that climate change [..¹⁸⁹] impacts seasonal cycles (Wang et al., 2021; Paçal et al., 2023).

475 [..¹⁹⁰]

This study highlighted the potential of machine learning methods to improve our understanding of heatwaves. By using a VAE, we uncovered a data-driven classification of heatwave events that not only aligns with known atmospheric circulation regimes from previous studies but also reveals their seasonal and dynamical characteristics from several days before the onset of the heatwave until several days after.

480 Our results showed that the VAE’s latent space effectively captures key atmospheric patterns [..¹⁹¹] previously linked to extreme heat events, such as blocking highs, omega blocks, and persistent ridges, similar to those identified by Happé et al. (2024) and Rouges et al. (2023). Furthermore, we observed that recent summer heatwaves form a distinct cluster separated from the historical distribution of events. This separation is consistent with the increasing intensity and changing nature of heatwaves under anthropogenic climate change (IPCC, 2021). The VAE’s ability to detect these shifts in the latent space
485 without supervision suggests that unsupervised learning techniques can be a powerful tool for monitoring climate change (Behrens et al., 2022; Shamekh et al., 2023; Mooers et al., 2023; Camps-Valls et al., 2025).

Despite these promising results for identifying heatwaves and their underlying atmospheric conditions, several limitations of the current approach must be acknowledged. First, we adopt a percentile-based threshold for detecting heatwave sample onset dates using 2-meter temperature anomalies over Western Europe. However, there is no universally accepted definition of heatwaves (Barriopedro et al., 2023; Boni et al., 2023). Alternative heatwave indices could yield different heatwave samples and thus different atmospheric patterns. Second, while we used variables related to atmospheric heatwaves, other potentially relevant drivers of heatwave dynamics may not be represented. As a result, the clusters we identify should be interpreted as emerging from the chosen subset of variables rather than from the full spectrum of processes affecting heatwaves. In addition, ERA5 itself has known uncertainties (Soci et al., 2024). Future work could
490 [..¹⁹²] improve this by also analyzing other variables to capture additional feedback processes. Third, the VAE is trained on historical heatwaves (1941–1990) and tested with recent heatwaves. While this was a deliberate choice to investigate how recent heatwaves differ from historical heatwaves, it assumes that the latent representation learned from the historical period can adequately model unprecedented patterns arising from climate change. Furthermore, the VAE approach

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¹⁹⁰removed: Despite these promising results for identifying heatwaves and their underlying atmospheric conditions, several limitations of the current approach must be acknowledged. The VAE approach, an unsupervised machine learning method, introduces some uncertainty due to the choices in model architecture. Key hyperparameters (such as the dimensionality of the latent space, learning rate, batch size, and the number of layers) can significantly influence training outcomes and the structure of the latent space. In addition, dimensionality reduction using PCA and t-SNE, followed by clustering with GMM, further affects how heatwave events are grouped, as all of these steps involve stochastic elements. To address these, we fixed the random seed to 42 (Adams, 1979) for PCA, t-SNE, and GMM steps to ensure consistency across visualization runs. Finally, by constructing composite maps of atmospheric patterns by averaging the 100 latent samples closest to each GMM cluster centroid, we reduced randomness and provided a more stable and representative depiction of the atmospheric conditions associated with each cluster.
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introduces some uncertainties due to the choices in model architecture. Key hyperparameters (such as the dimensionality of the latent space, learning rate, batch size, and the number of layers) can significantly influence training outcomes and the structure of the latent space. In addition to this, dimensionality reduction using PCA and t-SNE, followed by clustering with GMM, further influences how heatwave events are grouped in the latent space, as all these steps involve stochastic elements. Finally, the VAE reconstructions tend to smooth out extremes, and the use of composite maps that average 100 nearest latent samples, while reducing randomness and providing a more stable representation of atmospheric conditions, may mask variability within clusters. These limitations highlight that the VAE clustering approach is one possible data-driven analysis of atmospheric dynamics associated with heatwaves, rather than a definitive classification.

An open question concerns whether the atmospheric patterns identified before heatwave onsets also appear during periods without subsequent temperature extremes. We computed the mean bias between the composite fields of the summer cluster center and 11-day running window samples from all summer days from 2015 to 2021 for each variable. This approach tests whether these circulation patterns exclusively arise before the heatwaves. Our preliminary results did not show a clear predictive signal, suggesting that these large-scale configurations can occur without always leading to a heatwave. Future work could investigate the potential predictive value and improve understanding of the physical mechanisms linking circulation anomalies to heatwave development. Another possible approach could be to enhance the model's ability to analyze ^[.193] various types of extreme events by ^[.194] incorporating additional variables, such as soil moisture, vegetation indices, or extreme indices. Furthermore, applying the VAE model to CMIP6 climate simulations (Eyring et al., 2016) to evaluate how well climate models capture historical heatwave patterns compared to reanalysis data could provide valuable insights on model biases and help to bridge the gap between observational and model-based understanding of extreme events in a warming climate (Domeisen et al., 2022; Kornhuber et al., 2024; Barriopedro et al., 2023; Brunner and Voigt, 2024). These insights are ^[.195] particularly relevant for climate change adaptation and mitigation efforts (IPCC, 2021), as heatwaves pose serious risks to both environmental systems and human health (Mora et al., 2017b).

Code and data availability. Python and bash scripts to process and extract heatwave samples from ERA5 reanalysis data, to construct, train, and test the VAE model, and to produce all figures of this manuscript are accessible in the following GitHub repository: https://github.com/EyringMLClimateGroup/pacal25esd_UnderstandingHeatwaves_VAE. ERA5 data are provided by the ECMWF and accessed from DKRZ (Hersbach et al., 2017).

Author contributions. AP conceptualized the study with the help of BH, KW, and VE. AP developed the code, conducted the analysis, and generated all figures. MAFT and GCV supported the development of the machine learning approach and provided feedback. AP drafted the manuscript with the help of BH and KW. All authors contributed to the interpretation of results and the writing of the manuscript.

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Competing interests. The authors declare that they have no conflict of interest.

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540 **Appendix: Details for the Variational Autoencoder**

VAEs, like other deep learning models, require ^[..¹⁹⁹] [several](#) design choices to be made before training. These hyperparameters determine how the model performs, such as how the model adjusts its parameters during each training iteration (learning rate), how many samples it uses in each iteration (batch size), and how complex the internal representations are (hidden layer size and latent space size). Since these settings strongly affect the performance of the model reconstruction, we conducted a grid search over a range of hyperparameters, including learning rates ([0.0001, 0.001, 0.01]), batch sizes ([8, 16, 32, 64]), hidden layer dimensions ([64, 128, 256]), and latent space sizes ([64, 128, 256]). [The model performance improves substantially with increasing hidden dimension, as shown in Figure A1.](#) Based on the model’s performance on the unseen validation data, we selected a learning rate of 0.001, a batch size of 32, a hidden layer size of 256, and a latent space size of 128. These choices provided a good balance between reconstruction accuracy, [latent-space simplicity](#), and computational efficiency.

550 The encoder processes the input with four layers of 3D convolutions with Max Pooling layers across the variable, time, and spatial dimensions (See Table A1). Likewise, Happé et al. (2024) used a similar architecture and latent space size. By using 3D convolutions, the model captures interactions across time and space simultaneously. It gradually reduces the spatiotemporal heatwave data in the encoder. From the encoded representation, the model estimates the parameters of a latent distribution using the reparameterization trick (Kingma and Welling, 2019). Sampling from this distribution yields a 128-dimensional latent vector that serves as the compressed representation of each heatwave event. The decoder, consisting of four layers of 3D transposed convolutions with corresponding unpooling operations to recover the original input dimensions, reconstructs

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the heatwave sample from its latent space representation. By minimizing the reconstruction loss between the original input and the decoder output, the model learns to optimize its parameters. The encoder-decoder architecture is symmetric and fully convolutional, preserving spatiotemporal locality throughout the encoding and decoding process, as described in Table A1.

Table A1. Architecture of the VAE model. Each row shows the layer name, the output tensor size after the operation, the number of input and output filters (where applicable), the convolution or transpose convolution kernel size, the applied padding, and the stride. The output has dimensions corresponding to variables (9), days (11), latitude (64), and longitude (192). The encoder compresses the input, and fully connected (FC) layers map the flattened encoder output to the latent space. In VAEs, the latent space is sampled from a Gaussian distribution. Two separate FC layers generate the mean (FC_μ) and standard deviation (FC_σ) vectors that parameterize the latent Gaussian distribution. After sampling from the latent space, the data is reshaped and passed into the decoder to reconstruct the input.

Layer name	Output size	Filters	Kernel size	Padding	Stride
Input	$9 \times 11 \times 64 \times 192$	-			
Conv3D ₁	$32 \times 11 \times 64 \times 192$	$9 \rightarrow 32$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxPool3D ₁	$32 \times 9 \times 32 \times 96$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
Conv3D ₂	$64 \times 9 \times 32 \times 96$	$32 \rightarrow 64$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxPool3D ₂	$64 \times 7 \times 16 \times 48$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
Conv3D ₃	$128 \times 7 \times 16 \times 48$	$64 \rightarrow 128$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxPool3D ₃	$128 \times 5 \times 8 \times 24$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
Conv3D ₄	$256 \times 5 \times 8 \times 24$	$128 \rightarrow 256$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxPool3D ₄	$256 \times 3 \times 4 \times 12$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
Flatten	36864				
FC_μ	128	$36864 \rightarrow 128$			
FC_σ	128	$36864 \rightarrow 128$			
Unflatten	36864	$128 \rightarrow 36864$			
Reshape	$256 \times 3 \times 4 \times 12$				
MaxUnpool3D ₄	$256 \times 5 \times 8 \times 24$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
ConvTranspose3D ₄	$128 \times 5 \times 8 \times 24$	$256 \rightarrow 128$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxUnpool3D ₃	$128 \times 7 \times 16 \times 48$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
ConvTranspose3D ₃	$64 \times 7 \times 16 \times 48$	$128 \rightarrow 64$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxUnpool3D ₂	$64 \times 9 \times 32 \times 96$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
ConvTranspose3D ₂	$32 \times 9 \times 32 \times 96$	$64 \rightarrow 32$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$
MaxUnpool3D ₁	$32 \times 11 \times 64 \times 192$		$3 \times 2 \times 2$	$0 \times 0 \times 0$	$1 \times 2 \times 2$
ConvTranspose3D ₁	$9 \times 11 \times 64 \times 192$	$32 \rightarrow 9$	$3 \times 3 \times 3$	$1 \times 1 \times 1$	$1 \times 1 \times 1$

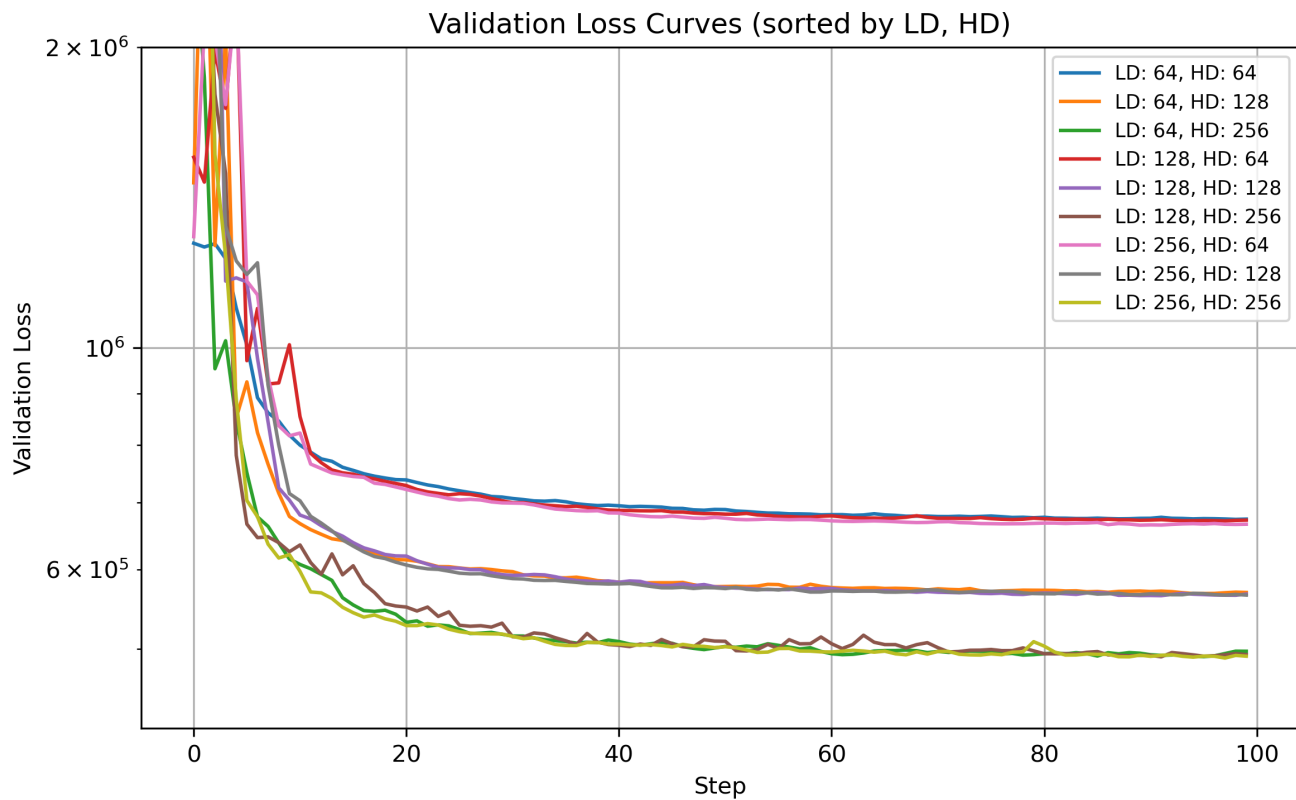


Figure A1. Validation loss curves for combinations of latent dimension (LD) and hidden dimension (HD). Each line shows the validation loss over training steps for a specific pair of LD and HD values. Higher-dimensional representations substantially improve reconstruction accuracy.

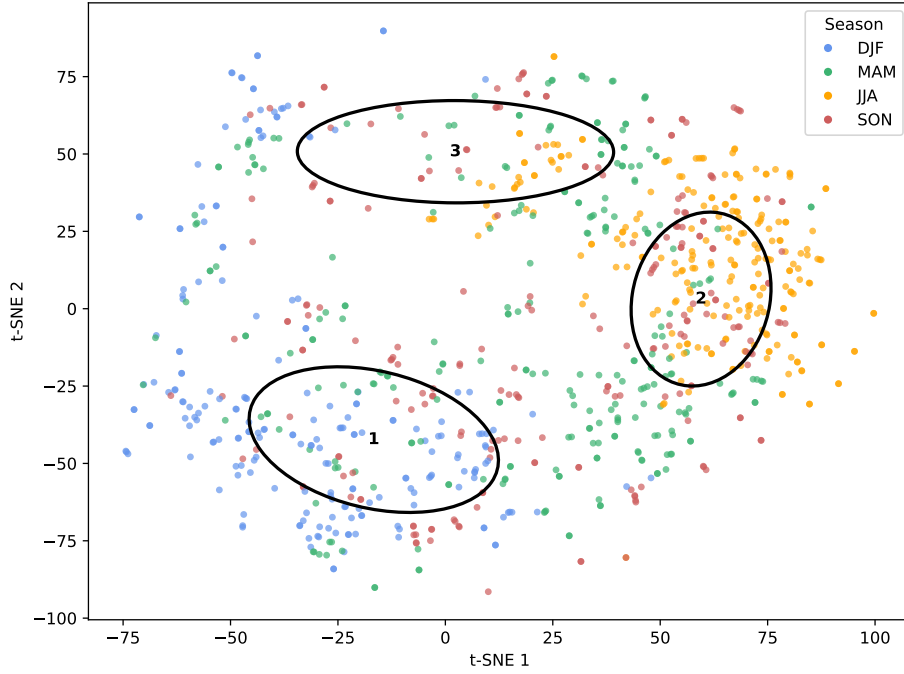


Figure A2. t-SNE representation of the latent space with three corresponding GMM components. Each point represents a heatwave sample. Colors represent the seasons in which the sample onset dates are located.

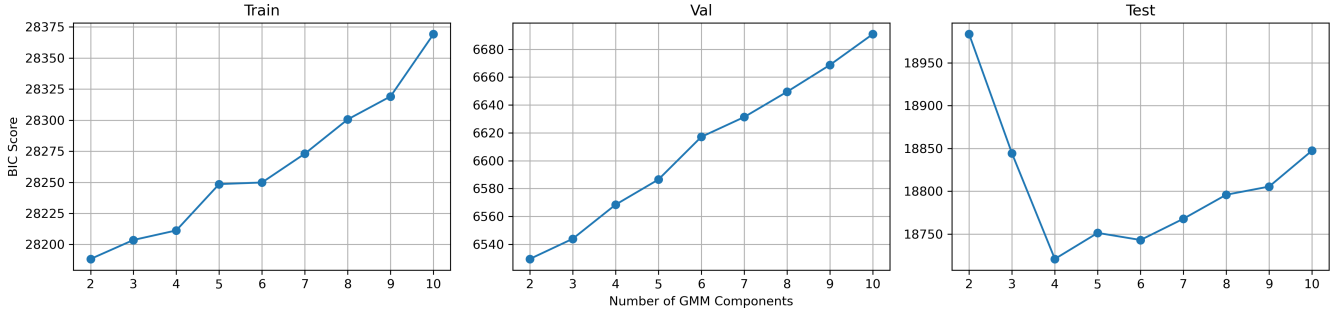


Figure A3. Bayesian Information Criterion (BIC) scores for GMM clustering across 2 to 10 components. Each panel shows the BIC scores for a different dataset split: (left) training period (1941–1990), (middle) validation period (1991–2000), and (right) testing period (2001–2022). The test set shows a clear minimum BIC score at four components, suggesting this is the optimal number of clusters under the BIC criterion. In contrast, the training and validation sets [\[...²⁰⁰\]](#) exhibit steadily increasing BIC scores with [\[...²⁰¹\]](#) the addition of components, favoring simpler models. Despite these differences, the four-component model provides a balance between underfitting and overfitting across all periods.

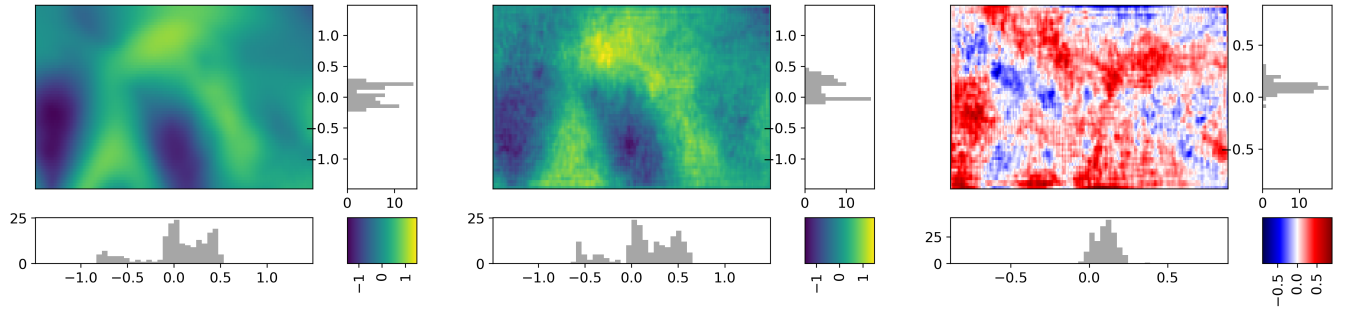


Figure A4. Geopotential height at 500 hPa for a random sample (left), its VAE reconstruction (middle), and the resulting reconstruction bias (right), each averaged over the time dimension. The histograms below and to the right of each panel show the distributions of longitudinal and latitudinal values, respectively.

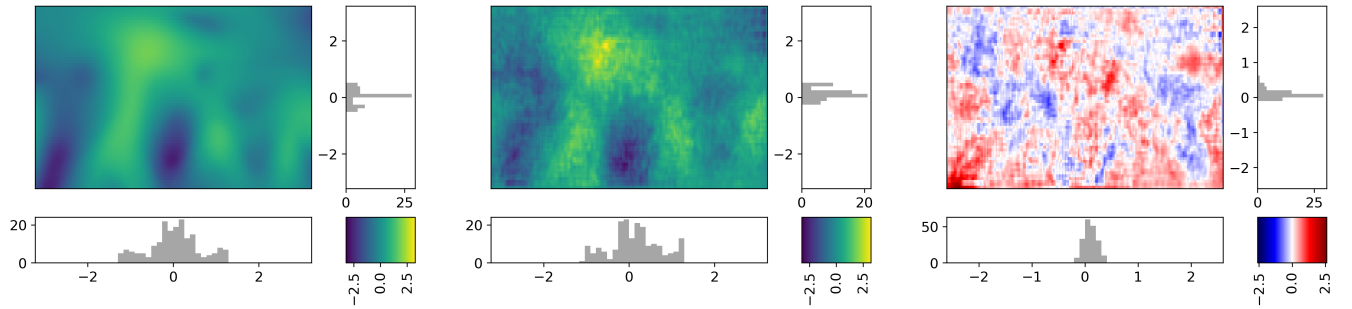


Figure A5. Geopotential height at 500 hPa for a random sample (left), its VAE reconstruction (middle), and the resulting reconstruction bias (right), each shown at the onset date. The histograms below and to the right of each panel show the distributions of longitudinal and latitudinal values, respectively.

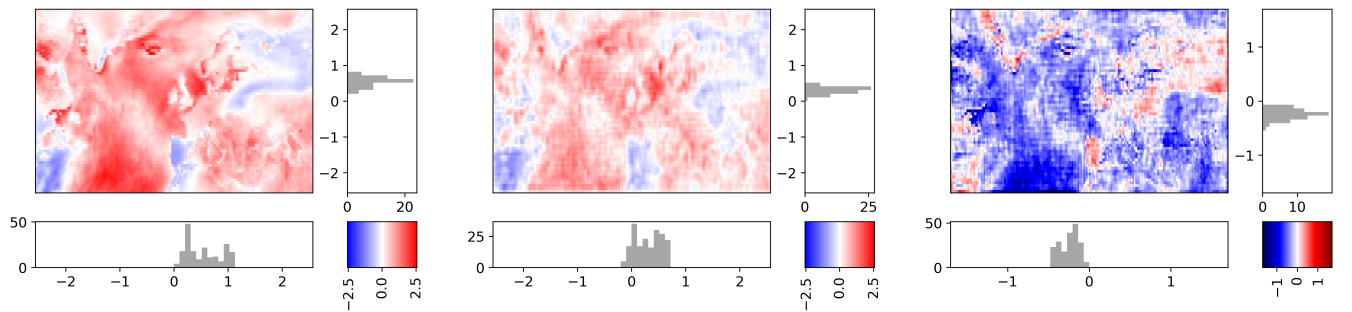


Figure A6. 2-meter temperature for a random sample (left), its VAE reconstruction (middle), and the resulting reconstruction bias (right), each averaged over the time dimension. The histograms below and to the right of each panel show the distributions of longitudinal and latitudinal values, respectively.

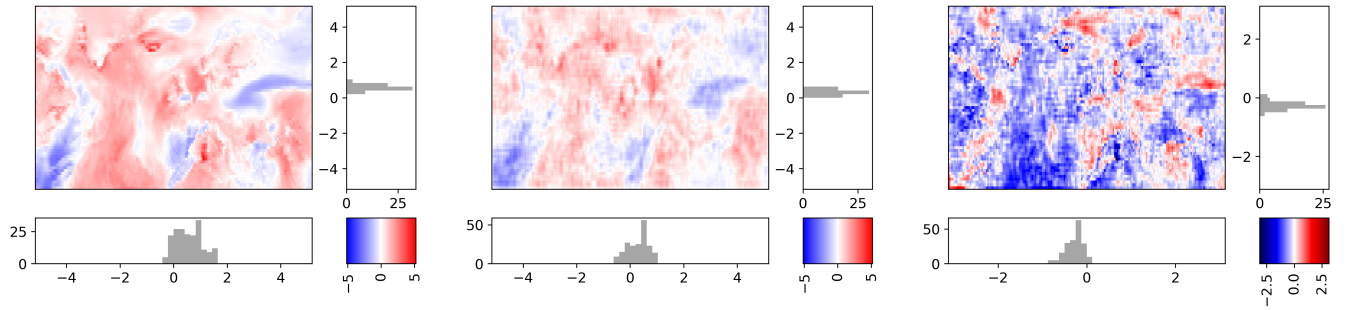


Figure A7. 2-meter temperature for a random sample (left), its VAE reconstruction (middle), and the resulting reconstruction bias (right), each shown at the onset date. The histograms below and to the right of each panel show the distributions of longitudinal and latitudinal values, respectively.

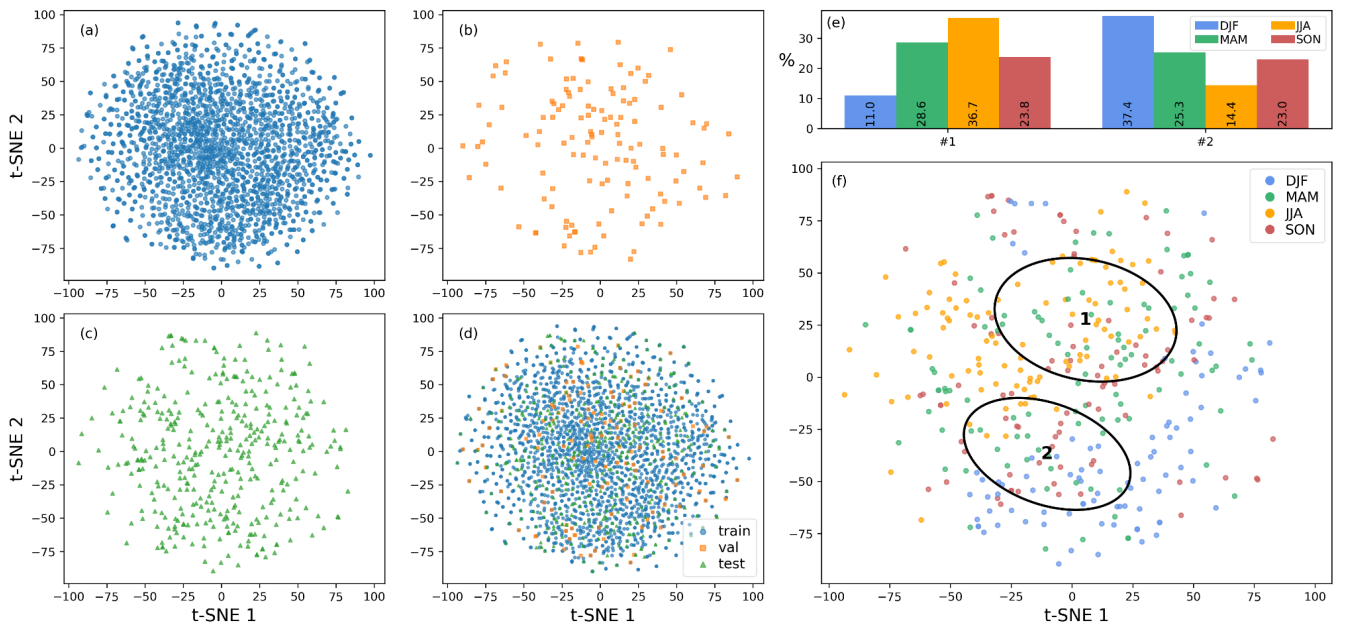


Figure A8. t-SNE representation of the latent space with random-split data (0.8/0.05/0.15). Following our workflow (testing with more than two components), a 2-component GMM provided the best fit, as it was closest to a single Gaussian distribution and thus better captured the smooth latent space structure. While this approach provides a smoother latent space, summer heatwaves still accumulate more closely together. This confirms that the clustering is not simply an artifact in the time series but reflects consistent structural patterns across periods.

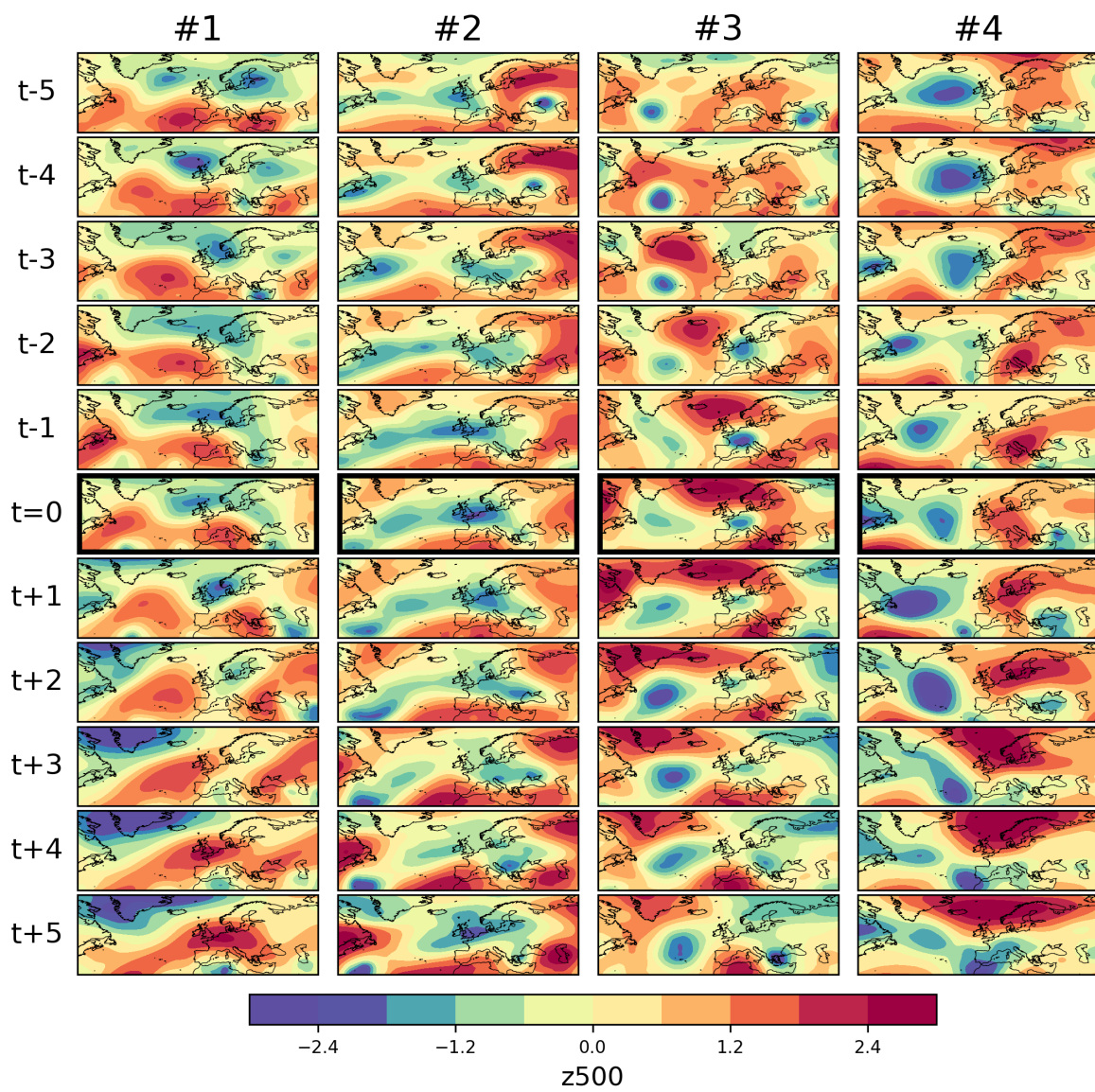


Figure A9. 1-sample composite map.

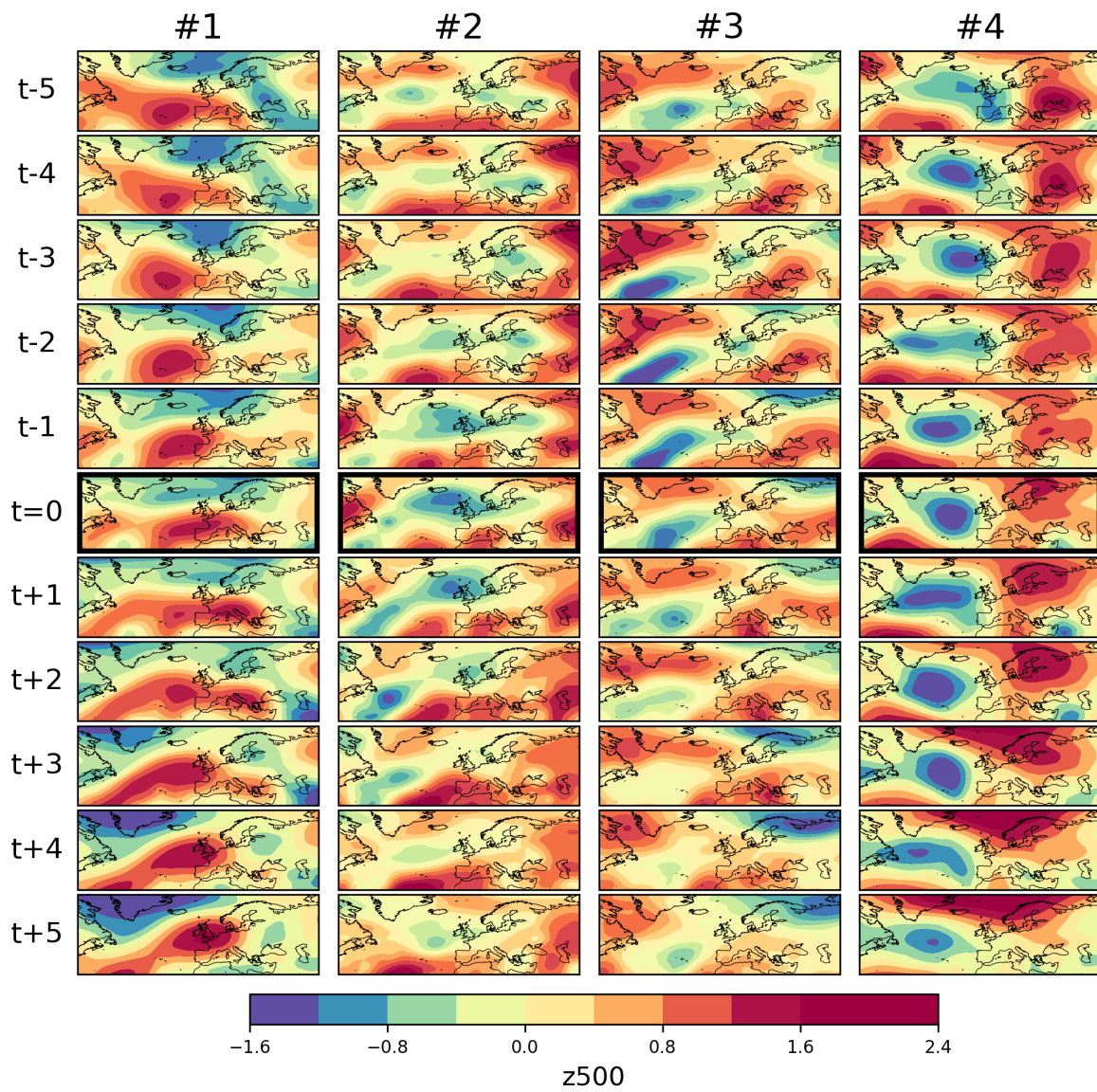


Figure A10. 5-sample composite map.

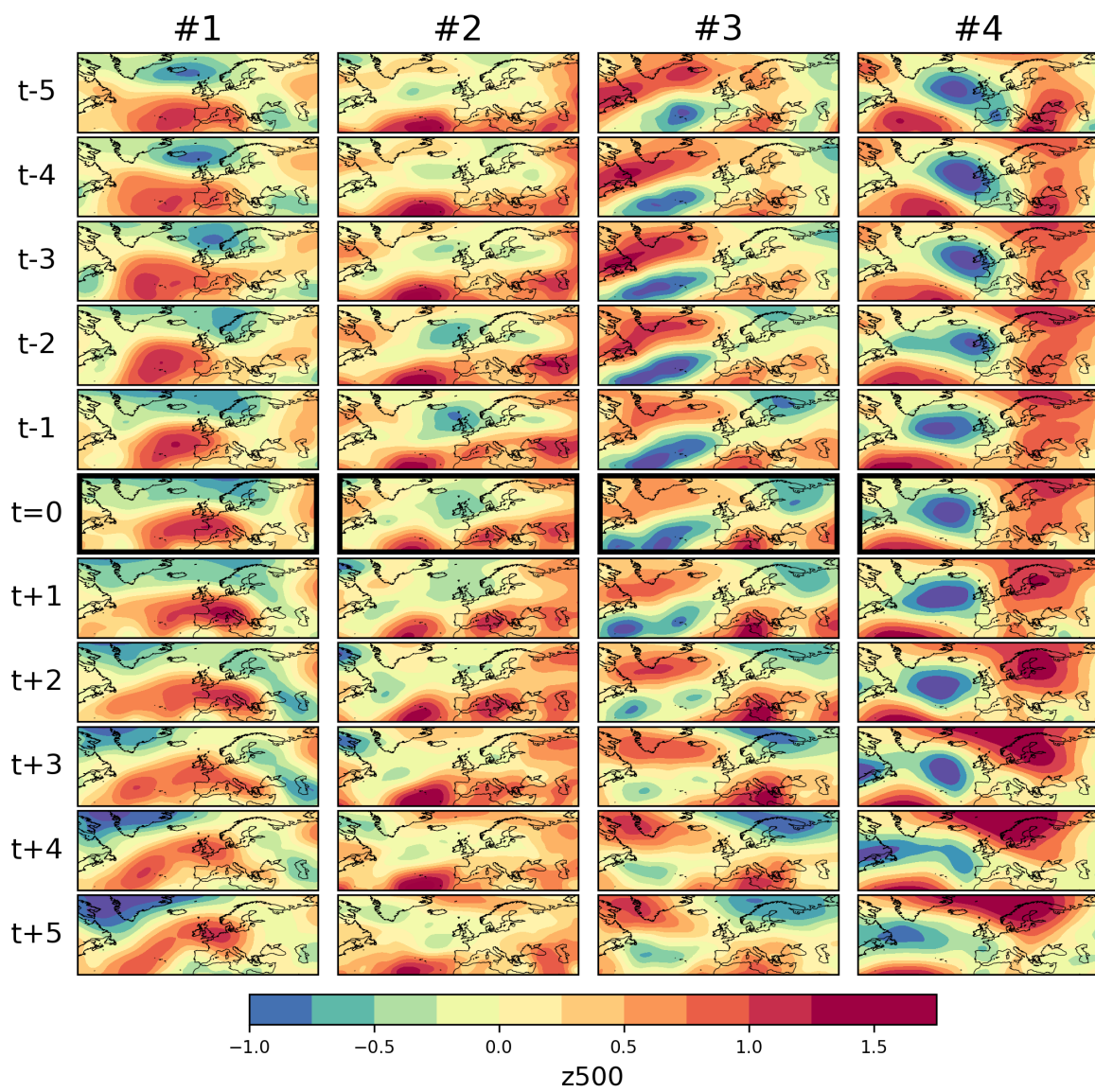


Figure A11. 10-sample composite map.

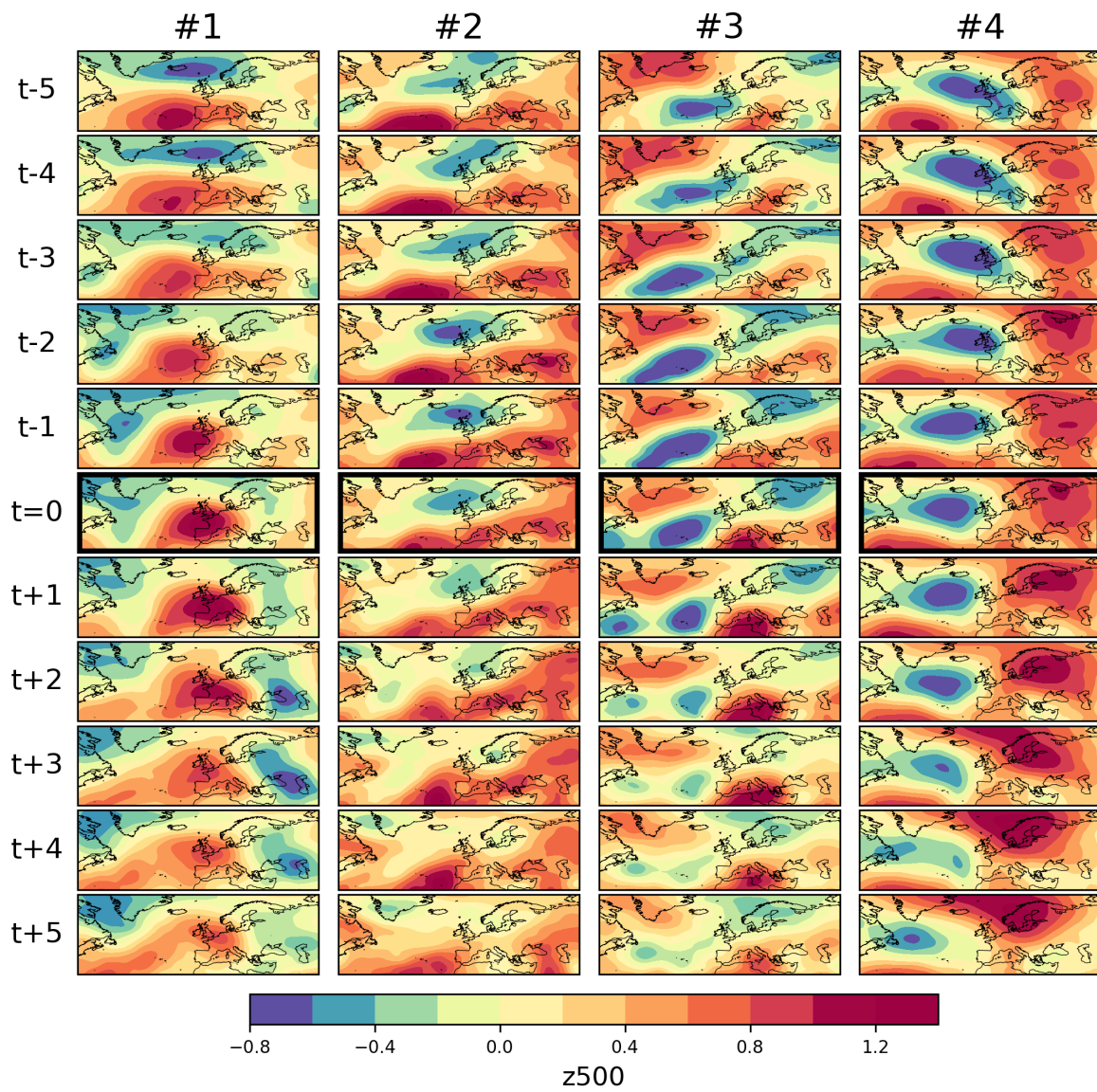


Figure A12. 20-sample composite map.

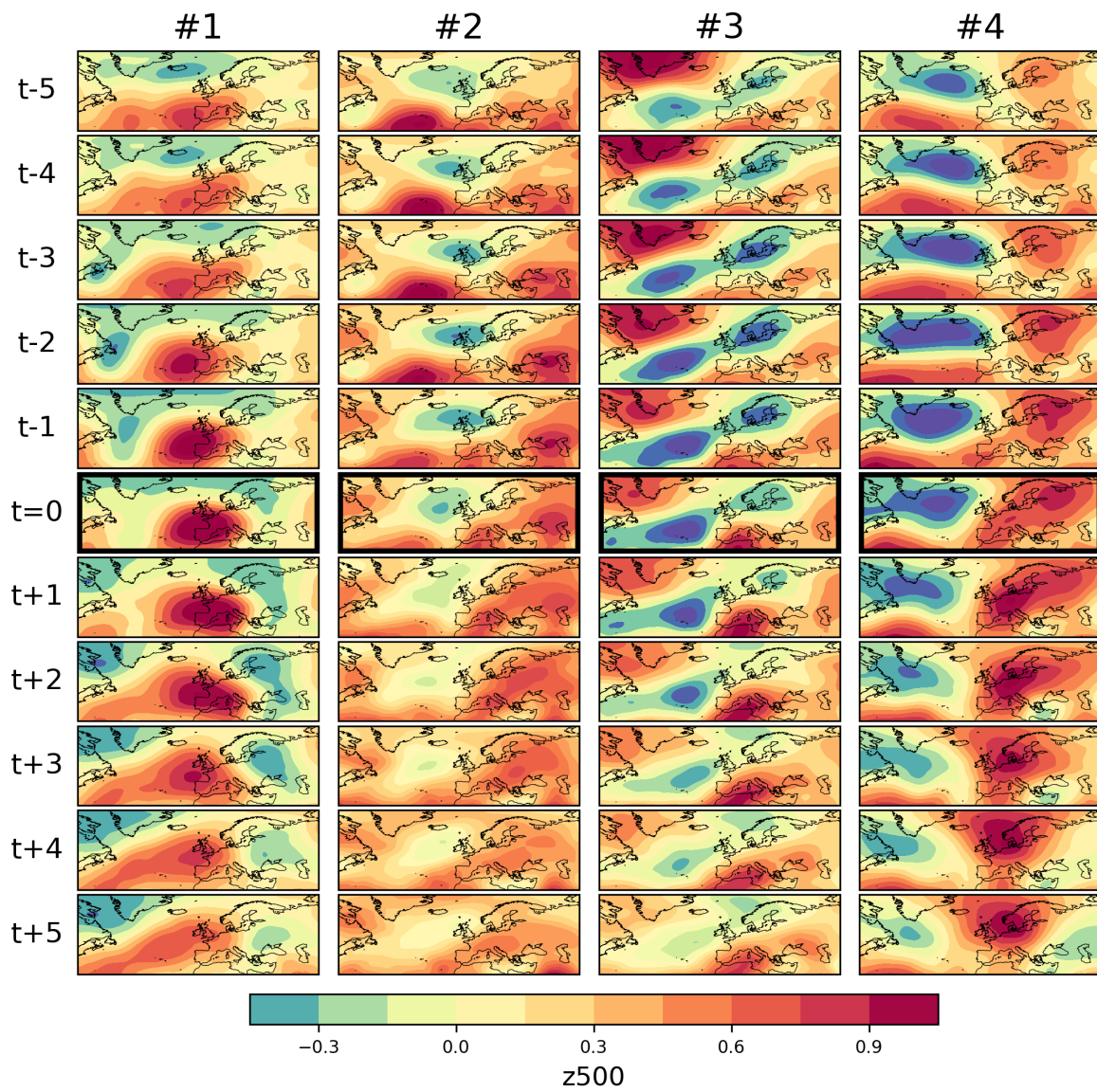


Figure A13. 50-sample composite map.

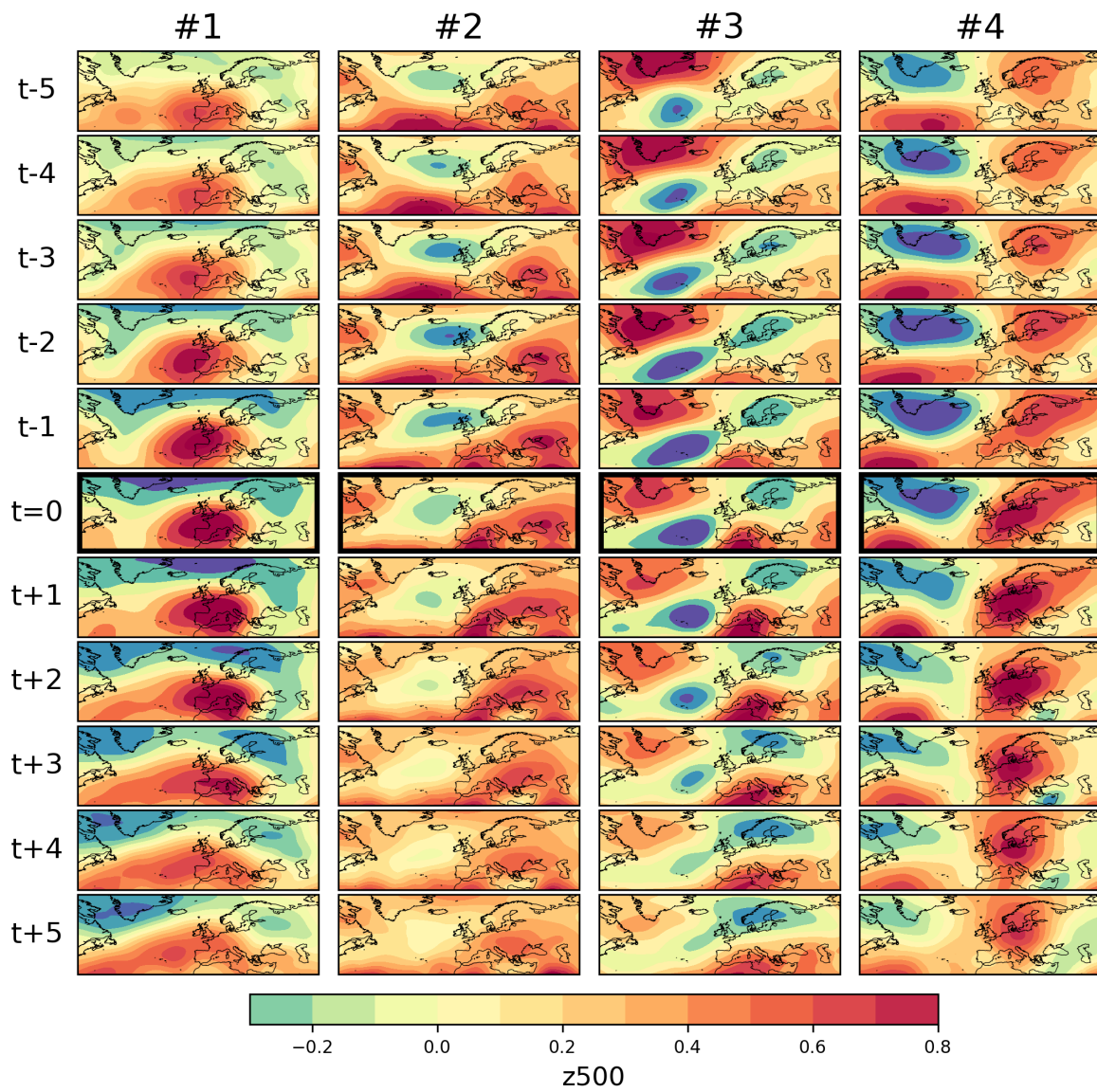


Figure A14. 100-sample composite map.

References

- Adams, D.: The Hitch Hiker's guide to the Galaxy, Pan original, Pan Books, London, ISBN 978-0-330-25864-7, 1979.
- 565 Alaya, M. A. B., Zwiers, F., and Zhang, X.: An Evaluation of Block-Maximum-Based Estimation of Very Long Return Period Precipitation Extremes with a Large Ensemble Climate Simulation, *Journal of Climate*, 33, 6957–6970, <https://doi.org/10.1175/JCLI-D-19-0011.1>, 2020.
- Albuquerque Filho, J. E. D., Brandão, L. C. P., Fernandes, B. J. T., and Maciel, A. M. A.: A Review of Neural Networks for Anomaly Detection, *IEEE Access*, 10, 112 342–112 367, <https://doi.org/10.1109/ACCESS.2022.3216007>, 2022.
- 570 Barriopedro, D., García-Herrera, R., Ordóñez, C., Miralles, D. G., and Salcedo-Sanz, S.: Heat Waves: Physical Understanding and Scientific Challenges, *Reviews of Geophysics*, 61, e2022RG000 780, <https://doi.org/https://doi.org/10.1029/2022RG000780>, 2023.
- Behrens, G., Beucler, T., Gentine, P., Iglesias-Suarez, F., Pritchard, M., and Eyring, V.: Non-Linear Dimensionality Reduction With a Variational Encoder Decoder to Understand Convective Processes in Climate Models, *Journal of Advances in Modeling Earth Systems*, 14, e2022MS003 130, <https://doi.org/https://doi.org/10.1029/2022MS003130>, 2022.
- 575 Bischof, S., Pilch Kedzierski, R., Hänsch, M., Wahl, S., and Matthes, K.: The Role of the North Atlantic for Heat Wave Characteristics in Europe, an ECHAM6 Study, *Geophysical Research Letters*, 50, e2023GL105 280, <https://doi.org/https://doi.org/10.1029/2023GL105280>, 2023.
- Boboc, L., Dima, M., Vaideanu, P., and Ionita, M.: Trends and variability of heat waves in Europe and the association with large-scale circulation patterns, *Weather and Climate Extremes*, 49, 100 794, <https://doi.org/10.1016/j.wace.2025.100794>, 2025.
- 580 Boni, Z., Bienkowska, Z., Chwałczyk, F., Jancewicz, B., Marginean, I., and Serrano, P. Y.: What is a heat(wave)? An interdisciplinary perspective, *Climatic Change*, 176, 129, <https://doi.org/10.1007/s10584-023-03592-3>, 2023.
- Brunner, L. and Voigt, A.: Pitfalls in diagnosing temperature extremes, *Nature Communications*, 15, 2087, <https://doi.org/10.1038/s41467-024-46349-x>, 2024.
- Burke, M., Hsiang, S. M., and Miguel, E.: Global non-linear effect of temperature on economic production, *Nature*, 527, 235–239, <https://doi.org/10.1038/nature15725>, 2015.
- 585 Camps-Valls, G., Fernandez-Torres, M. Á., Cohrs, K.-H., Höhl, A., Castelletti, A., Pacal, A., Robin, C., Martinuzzi, F., Papoutsis, I., Prapas, I., Pérez-Aracil, J., Weigel, K., Gonzalez-Calabuig, M., Reichstein, M., Rabel, M., Giuliani, M., Mahecha, M. D., Popescu, O.-I., Pellicer-Valero, O. J., Ouala, S., Salcedo-Sanz, S., Sippel, S., Kondylatos, S., Happé, T., and Williams, T.: Artificial intelligence for modeling and understanding extreme weather and climate events, *Nature Communications*, 16, 1919, <https://doi.org/10.1038/s41467-025-56573-8>, 2025.
- 590 Carril, A. F., Gualdi, S., Cherchi, A., and Navarra, A.: Heatwaves in Europe: areas of homogeneous variability and links with the regional to large-scale atmospheric and SSTs anomalies, *Climate Dynamics*, 30, 77–98, <https://doi.org/10.1007/s00382-007-0274-5>, 2008.
- Chitsaz, F., Gohari, A., Najafi, M. R., Zareian, M. J., and Haghighi, A. T.: Heatwave Duration and Heating Rate in a Non-Stationary Climate: Spatiotemporal Pattern and Key Drivers, *Earth's Future*, 11, e2023EF003 995, <https://doi.org/10.1029/2023EF003995>, <https://onlinelibrary.wiley.com/doi/pdf/10.1029/2023EF003995>, 2023.
- 595 Coumou, D. and Rahmstorf, S.: A decade of weather extremes, *Nature Climate Change*, 2, 491–496, <https://doi.org/10.1038/nclimate1452>, 2012.
- Debeire, K., Bock, L., Nowack, P., Runge, J., and Eyring, V.: Constraining uncertainty in projected precipitation over land with causal discovery, *Earth System Dynamics*, 16, 607–630, <https://doi.org/10.5194/esd-16-607-2025>, publisher: Copernicus GmbH, 2025.

- 600 Domeisen, D. I. V., Eltahir, E. A. B., Fischer, E. M., Knutti, R., Perkins-Kirkpatrick, S. E., Schär, C., Seneviratne, S. I., Weisheimer, A., and Wernli, H.: Prediction and projection of heatwaves, *Nature Reviews Earth & Environment*, <https://doi.org/10.1038/s43017-022-00371-z>, 2022.
- Dong, J., Brönnimann, S., Hu, T., Cheng, X., Liu, Y., and Peng, J.: Trends of the Intra-Annual Onset and End of Humid Heatwaves in the Northern Hemisphere, *Earth's Future*, 12, e2024EF005163, <https://doi.org/https://doi.org/10.1029/2024EF005163>, 2024.
- 605 Dosio, A., Mentaschi, L., Fischer, E. M., and Wyser, K.: Extreme heat waves under 1.5 °C and 2 °C global warming, *Environmental Research Letters*, 13, 054006, <https://doi.org/10.1088/1748-9326/aab827>, 2018.
- Elguindi, N., Rauscher, S. A., and Giorgi, F.: Historical and future changes in maximum and minimum temperature records over Europe, *Climatic Change*, 117, 415–431, <https://doi.org/10.1007/s10584-012-0528-z>, 2013.
- Eyring, V., Bony, S., Meehl, G. A., Senior, C. A., Stevens, B., Stouffer, R. J., and Taylor, K. E.: Overview of the Coupled Model Intercomparison Project Phase 6 (CMIP6) experimental design and organization, *Geoscientific Model Development*, 9, 1937–1958, <https://doi.org/10.5194/gmd-9-1937-2016>, 2016.
- 610 Fan, Y., Wen, G., Li, D., Qiu, S., Levine, M. D., and Xiao, F.: Video anomaly detection and localization via Gaussian Mixture Fully Convolutional Variational Autoencoder, *Computer Vision and Image Understanding*, 195, 102920, <https://doi.org/10.1016/j.cviu.2020.102920>, 2020.
- 615 Fischer, E. M. and Knutti, R.: Detection of spatially aggregated changes in temperature and precipitation extremes, *Geophysical Research Letters*, 41, <https://doi.org/10.1002/2013GL058499>, 2014.
- Fischer, E. M., Sippel, S., and Knutti, R.: Increasing probability of record-shattering climate extremes, *Nature Climate Change*, 11, 689–695, <https://doi.org/10.1038/s41558-021-01092-9>, 2021.
- García-León, D., Casanueva, A., Standardi, G., Burgstall, A., Flouris, A. D., and Nybo, L.: Current and projected regional economic impacts of heatwaves in Europe, *Nature Communications*, 12, 5807, <https://doi.org/10.1038/s41467-021-26050-z>, 2021.
- 620 Happé, T., Wijnands, J. S., Fernández-Torres, M. Á., Scussolini, P., Muntjewerf, L., and Coumou, D.: Detecting Spatiotemporal Dynamics of Western European Heatwaves Using Deep Learning, *Artificial Intelligence for the Earth Systems*, 3, e230107, <https://doi.org/10.1175/AIES-D-23-0107.1>, 2024.
- Hasan, M., Choi, J., Neumann, J., Roy-Chowdhury, A. K., and Davis, L. S.: Learning Temporal Regularity in Video Sequences, 2016.
- 625 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot, J., Bonavita, M., De Chiara, G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R., Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R., Hólm, E., Janisková, M., Keeley, S., Laloyaux, P., Lopez, P., Lupu, C., Radnoti, G., de Rosnay, P., Rozum, I., Vamborg, F., Villaume, S., and Thépaut, J.-N.: Complete ERA5 from 1940: Fifth generation of ECMWF atmospheric reanalyses of the global climate, *Copernicus Climate Change Service (C3S) Climate Data Store (CDS)*, <https://doi.org/10.24381/cds.143582cf>, accessed on 15-JUN-2023. Data distribution by the German Climate Computing Center (DKRZ), 2017.
- 630 Heuer, H., Schwabe, M., Gentile, P., Giorgetta, M. A., and Eyring, V.: Interpretable Multiscale Machine Learning-Based Parameterizations of Convection for ICON, *Journal of Advances in Modeling Earth Systems*, 16, e2024MS004398, <https://doi.org/10.1029/2024MS004398>, <https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/2024MS004398>, 2024.
- 635 Horton, D. E., Johnson, N. C., Singh, D., Swain, D. L., Rajaratnam, B., and Diffenbaugh, N. S.: Contribution of changes in atmospheric circulation patterns to extreme temperature trends, *Nature*, 522, 465–469, <https://doi.org/10.1038/nature14550>, 2015.

- Huang, W. K., Stein, M. L., McInerney, D. J., Sun, S., and Moyer, E. J.: Estimating changes in temperature extremes from millennial-scale climate simulations using generalized extreme value (GEV) distributions, *Advances in Statistical Climatology, Meteorology and Oceanography*, 2, 79–103, <https://doi.org/10.5194/ascmo-2-79-2016>, 2016.
- 640 Huntingford, C., Cox, P. M., Ritchie, P. D. L., Clarke, J. J., Parry, I. M., and Williamson, M. S.: Acceleration of daily land temperature extremes and correlations with surface energy fluxes, *npj Climate and Atmospheric Science*, 7, 1–10, <https://doi.org/10.1038/s41612-024-00626-0>, 2024.
- IPCC: Climate Change 2021: The Physical Science Basis, Contribution of Working Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change, Cambridge University Press (In Press), edited by V. Masson-Delmotte, P. Zhai, A. Pirani, S.L. Connors, C. Péan, S. Berger, N. Caud, Y. Chen, L. Goldfarb, M.I. Gomis, M. Huang, K. Leitzell, E. Lonnoy, J.B.R. Matthews, T.K. Maycock, T. Waterfield, O. Yelekçi, R. Yu, and B. Zhou, 2021.
- 645 Jézéquel, A., Yiou, P., and Radanovics, S.: Role of circulation in European heatwaves using flow analogues, *Climate Dynamics*, 50, 1145–1159, <https://doi.org/10.1007/s00382-017-3667-0>, 2018.
- Kautz, L.-A., Martius, O., Pfahl, S., Pinto, J. G., Ramos, A. M., Sousa, P. M., and Woollings, T.: Atmospheric blocking and weather extremes over the Euro-Atlantic sector – a review, *Weather and Climate Dynamics*, 3, 305–336, <https://doi.org/10.5194/wcd-3-305-2022>, 2022.
- 650 Kharin, V. V., Flato, G. M., Zhang, X., Gillett, N. P., Zwiers, F., and Anderson, K. J.: Risks from Climate Extremes Change Differently from 1.5°C to 2.0°C Depending on Rarity, *Earth’s Future*, 6, 704–715, <https://doi.org/10.1002/2018EF000813>, 2018.
- Kim, J.-Y. and Seo, K.-H.: Physical mechanisms for the dominant summertime high-latitude atmospheric teleconnection pattern and the related Northern Eurasian climates, *Environmental Research Letters*, 18, 104 022, <https://doi.org/10.1088/1748-9326/acfa13>, 2023.
- 655 King, A. D. and Harrington, L. J.: The Inequality of Climate Change From 1.5 to 2°C of Global Warming, *Geophysical Research Letters*, 45, 5030–5033, <https://doi.org/https://doi.org/10.1029/2018GL078430>, 2018.
- Kingma, D. P. and Welling, M.: An Introduction to Variational Autoencoders, *Foundations and Trends® in Machine Learning*, 12, 307–392, <https://doi.org/10.1561/22000000056>, 2019.
- Kornhuber, K., Petoukhov, V., Karoly, D., Petri, S., Rahmstorf, S., and Coumou, D.: Summertime Planetary Wave Resonance in the Northern and Southern Hemispheres, *Journal of Climate*, <https://doi.org/10.1175/JCLI-D-16-0703.1>, 2017.
- 660 Kornhuber, K., Bartusek, S., Seager, R., Schellnhuber, H. J., and Ting, M.: Global emergence of regional heatwave hotspots outpaces climate model simulations, *Proceedings of the National Academy of Sciences*, 121, e2411258 121, <https://doi.org/10.1073/pnas.2411258121>, 2024.
- Kotz, M., Levermann, A., and Wenz, L.: The economic commitment of climate change, *Nature*, 628, 551–557, <https://doi.org/10.1038/s41586-024-07219-0>, 2024.
- 665 Krüger, J., Kjellsson, J., Kedzierski, R. P., and Claus, M.: Connecting North Atlantic SST Variability to European Heat Events over the Past Decades, *Tellus A: Dynamic Meteorology and Oceanography*, 75, <https://doi.org/10.16993/tellusa.3235>, 2023.
- Lacombe, R., Grossman, H., Hendren, L., and Lüdeke, D.: Improving extreme weather events detection with light-weight neural networks, <https://doi.org/10.48550/arXiv.2304.00176>, 2023.
- 670 Lai, C.-Y., Hassanzadeh, P., Sheshadri, A., Sonnewald, M., Ferrari, R., and Balaji, V.: Machine Learning for Climate Physics and Simulations, *Annual Review of Condensed Matter Physics*, 16, 343–365, <https://doi.org/10.1146/annurev-conmatphys-043024-114758>, 2025.
- Leach, N. J., Weisheimer, A., Allen, M. R., and Palmer, T.: Forecast-based attribution of a winter heatwave within the limit of predictability, *Proceedings of the National Academy of Sciences*, 118, e2112087 118, <https://doi.org/10.1073/pnas.2112087118>, 2021.

- Lee, D. Y., Yeh, S.-W., Lee, Y.-H., Cai, W., Wang, G., and Yang, Y.-M.: The emergence of a dipole-like mode in Arctic atmospheric circulation conducive to European heat waves, *Communications Earth & Environment*, 6, 1–9, <https://doi.org/10.1038/s43247-025-02020-x>, 2025.
- Lhotka, O. and Kysely, J.: The 2021 European Heat Wave in the Context of Past Major Heat Waves, *Earth and Space Science*, 9, e2022EA002 567, <https://doi.org/https://doi.org/10.1029/2022EA002567>, 2022.
- Li, C., Zwiers, F., Zhang, X., Li, G., Sun, Y., and Wehner, M.: Changes in Annual Extremes of Daily Temperature and Precipitation in CMIP6 Models, *Journal of Climate*, 34, 3441–3460, <https://doi.org/10.1175/JCLI-D-19-1013.1>, 2021.
- Lindhe, A., Ringqvist, C., and Hult, H.: Variational Auto Encoder Gradient Clustering, <https://doi.org/10.48550/arXiv.2105.06246>, 2021.
- Lipfert, L., Hand, R., and Brönnimann, S.: A Global Assessment of Heatwaves Since 1850 in Different Observational and Model Data Sets, *Geophysical Research Letters*, 51, e2023GL106 212, <https://doi.org/https://doi.org/10.1029/2023GL106212>, 2024.
- Lynas, M., Houlton, B. Z., and Perry, S.: Greater than 99% consensus on human caused climate change in the peer-reviewed scientific literature, *Environmental Research Letters*, 16, 114 005, <https://doi.org/10.1088/1748-9326/ac2966>, 2021.
- López-Bueno, J. A., Navas-Martín, M. A., Linares, C., Mirón, I. J., Luna, M. Y., Sánchez-Martínez, G., Culqui, D., and Díaz, J.: Analysis of the impact of heat waves on daily mortality in urban and rural areas in Madrid, *Environmental Research*, 195, 110 892, <https://doi.org/10.1016/j.envres.2021.110892>, 2021.
- Materia, S., García, L. P., van Straaten, C., O, S., Mamalakis, A., Cavicchia, L., Coumou, D., de Luca, P., Kretschmer, M., and Donat, M.: Artificial intelligence for climate prediction of extremes: State of the art, challenges, and future perspectives, *WIREs Climate Change*, 15, e914, <https://doi.org/10.1002/wcc.914>, 2024.
- McKinnon, K. A., Simpson, I. R., and Williams, A. P.: The pace of change of summertime temperature extremes, *Proceedings of the National Academy of Sciences*, 121, e2406143 121, <https://doi.org/10.1073/pnas.2406143121>, 2024.
- McPhillips, L. E., Chang, H., Chester, M. V., Depietri, Y., Friedman, E., Grimm, N. B., Kominoski, J. S., McPhearson, T., Méndez-Lázaro, P., Rosi, E. J., and Shafiei Shiva, J.: Defining Extreme Events: A Cross-Disciplinary Review, *Earth’s Future*, 6, 441–455, <https://doi.org/https://doi.org/10.1002/2017EF000686>, 2018.
- Mooers, G., Pritchard, M., Beucler, T., Srivastava, P., Mangipudi, H., Peng, L., Gentine, P., and Mandt, S.: Comparing storm resolving models and climates via unsupervised machine learning, *Scientific Reports*, 13, 22 365, <https://doi.org/10.1038/s41598-023-49455-w>, 2023.
- Mora, C., Counsell, C. W., Bielecki, C. R., and Louis, L. V.: Twenty-Seven Ways a Heat Wave Can Kill You, *Circulation: Cardiovascular Quality and Outcomes*, 10, e004 233, <https://doi.org/10.1161/CIRCOUTCOMES.117.004233>, 2017a.
- Mora, C., Dousset, B., Caldwell, I. R., Powell, F. E., Geronimo, R. C., Bielecki, C. R., Counsell, C. W. W., Dietrich, B. S., Johnston, E. T., Louis, L. V., Lucas, M. P., McKenzie, M. M., Shea, A. G., Tseng, H., Giambelluca, T. W., Leon, L. R., Hawkins, E., and Trauernicht, C.: Global risk of deadly heat, *Nature Climate Change*, 7, 501–506, <https://doi.org/10.1038/nclimate3322>, 2017b.
- Muntjewerf, L., Bintanja, R., Reerink, T., and van der Wiel, K.: The KNMI Large Ensemble Time Slice (KNMI–LENTIS), *Geoscientific Model Development*, 16, 4581–4597, <https://doi.org/10.5194/gmd-16-4581-2023>, 2023.
- Nassif, A. B., Talib, M. A., Nasir, Q., and Dakalbab, F. M.: Machine Learning for Anomaly Detection: A Systematic Review, *IEEE Access*, 9, 78 658–78 700, <https://doi.org/10.1109/ACCESS.2021.3083060>, 2021.
- Newell, R. G., Prest, B. C., and Sexton, S. E.: The GDP-Temperature relationship: Implications for climate change damages, *Journal of Environmental Economics and Management*, 108, 102 445, <https://doi.org/10.1016/j.jeem.2021.102445>, 2021.
- Newman, R. and Noy, I.: The global costs of extreme weather that are attributable to climate change, *Nature Communications*, 14, 6103, <https://doi.org/10.1038/s41467-023-41888-1>, 2023.

- Oliveira, D. A. B., Diaz, J. G., Zadrozny, B., Watson, C. D., and Zhu, X. X.: Controlling Weather Field Synthesis Using Variational Autoencoders, in: IGARSS 2022 - 2022 IEEE International Geoscience and Remote Sensing Symposium, pp. 5027–5030, <https://doi.org/10.1109/IGARSS46834.2022.9884668>, 2022.
- Pang, G., Shen, C., Cao, L., and Hengel, A. V. D.: Deep Learning for Anomaly Detection: A Review, *ACM Computing Surveys*, 54, 1–38, <https://doi.org/10.1145/3439950>, 2021.
- Patterson, M.: North-West Europe Hottest Days Are Warming Twice as Fast as Mean Summer Days, *Geophysical Research Letters*, 50, e2023GL102757, <https://doi.org/https://doi.org/10.1029/2023GL102757>, 2023.
- Paçal, A., Hassler, B., Weigel, K., Kurnaz, M. L., Wehner, M. F., and Eyring, V.: Detecting Extreme Temperature Events Using Gaussian Mixture Models, *Journal of Geophysical Research: Atmospheres*, 128, e2023JD038906, <https://doi.org/https://doi.org/10.1029/2023JD038906>, 2023.
- Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel, M., Prettenhofer, P., Weiss, R., Dubourg, V., Vanderplas, J., Passos, A., Cournapeau, D., Brucher, M., Perrot, M., and Duchesnay, E.: Scikit-learn: Machine Learning in Python, *Journal of Machine Learning Research*, 12, 2825–2830, 2011.
- Perkins, S. E.: A review on the scientific understanding of heatwaves—Their measurement, driving mechanisms, and changes at the global scale, *Atmospheric Research*, 164–165, 242–267, <https://doi.org/10.1016/j.atmosres.2015.05.014>, 2015.
- Perkins-Kirkpatrick, S. E. and Lewis, S. C.: Increasing trends in regional heatwaves, *Nature Communications*, 11, 3357, <https://doi.org/10.1038/s41467-020-16970-7>, 2020.
- Perkins-Kirkpatrick, S. E., Fischer, E. M., Angélib, O., and Gibson, P. B.: The influence of internal climate variability on heatwave frequency trends, *Environmental Research Letters*, 12, 044005, <https://doi.org/10.1088/1748-9326/aa63fe>, 2017.
- Prabhat, Kashinath, K., Mudigonda, M., Kim, S., Kapp-Schwoerer, L., Graubner, A., Karaismailoglu, E., von Kleist, L., Kurth, T., Greiner, A., Mahesh, A., Yang, K., Lewis, C., Chen, J., Lou, A., Chandran, S., Toms, B., Chapman, W., Dagon, K., Shields, C. A., O’Brien, T., Wehner, M., and Collins, W.: ClimateNet: an expert-labeled open dataset and deep learning architecture for enabling high-precision analyses of extreme weather, *Geoscientific Model Development*, 14, 107–124, <https://doi.org/10.5194/gmd-14-107-2021>, 2021.
- Rahmstorf, S. and Coumou, D.: Increase of extreme events in a warming world, *Proceedings of the National Academy of Sciences*, 108, 17905–17909, <https://doi.org/10.1073/pnas.1101766108>, 2011.
- Reichstein, M., Camps-Valls, G., Stevens, B., Jung, M., Denzler, J., Carvalhais, N., and Prabhat: Deep learning and process understanding for data-driven Earth system science, *Nature*, 566, 195–204, <https://doi.org/10.1038/s41586-019-0912-1>, 2019.
- Reid, P. C., Hari, R. E., Beaugrand, G., Livingstone, D. M., Marty, C., Straile, D., Barichivich, J., Goberville, E., Adrian, R., Aono, Y., Brown, R., Foster, J., Groisman, P., H  laou  t, P., Hsu, H.-H., Kirby, R., Knight, J., Kraberg, A., Li, J., Lo, T.-T., Myneni, R. B., North, R. P., Pounds, J. A., Sparks, T., St  bi, R., Tian, Y., Wiltshire, K. H., Xiao, D., and Zhu, Z.: Global impacts of the 1980s regime shift, *Global Change Biology*, 22, 682–703, <https://doi.org/https://doi.org/10.1111/gcb.13106>, 2016.
- Ronco, M., T  rraga, J. M., Mu  oz, J., Piles, M., Marco, E. S., Wang, Q., Espinosa, M. T. M., Pons  rre, S., and Camps-Valls, G.: Exploring interactions between socioeconomic context and natural hazards on human population displacement, *Nature Communications*, 14, 8004, <https://doi.org/10.1038/s41467-023-43809-8>, 2023.
- Rouges, E., Ferranti, L., Kantz, H., and Pappenberger, F.: European heatwaves: Link to large-scale circulation patterns and intraseasonal drivers, *International Journal of Climatology*, 43, 3189–3209, <https://doi.org/https://doi.org/10.1002/joc.8024>, 2023.
- Rousi, E., Kornhuber, K., Beobide-Arsuaga, G., Luo, F., and Coumou, D.: Accelerated western European heatwave trends linked to more-persistent double jets over Eurasia, *Nature Communications*, 13, 3851, <https://doi.org/10.1038/s41467-022-31432-y>, 2022.

Ruff, L., Kauffmann, J. R., Vandermeulen, R. A., Montavon, G., Samek, W., Kloft, M., Dietterich, T. G., and Müller, K.-R.: A Unifying
750 Review of Deep and Shallow Anomaly Detection, *Proceedings of the IEEE*, 109, 756–795, <https://doi.org/10.1109/JPROC.2021.3052449>, 2021.

Russo, E. and Domeisen, D. I. V.: Increasing Intensity of Extreme Heatwaves: The Crucial Role of Metrics, *Geophysical Research Letters*,
50, e2023GL103 540, <https://doi.org/10.1029/2023GL103540>, 2023.

Russo, S., Sillmann, J., and Fischer, E. M.: Top ten European heatwaves since 1950 and their occurrence in the coming decades, *Environ-
755 mental Research Letters*, 10, 124 003, <https://doi.org/10.1088/1748-9326/10/12/124003>, 2015.

Russo, S., Sillmann, J., and Sterl, A.: Humid heat waves at different warming levels, *Scientific Reports*, 7, 7477,
<https://doi.org/10.1038/s41598-017-07536-7>, 2017.

Salcedo-Sanz, S., Pérez-Aracil, J., Ascenso, G., Del Ser, J., Casillas-Pérez, D., Kadow, C., Fister, D., Barriopedro, D., García-Herrera,
R., Giuliani, M., and Castelletti, A.: Analysis, characterization, prediction, and attribution of extreme atmospheric events with machine
760 learning and deep learning techniques: a review, *Theoretical and Applied Climatology*, <https://doi.org/10.1007/s00704-023-04571-5>, 2023.

Sander, J., Ester, M., Kriegel, H.-P., and Xu, X.: Density-Based Clustering in Spatial Databases: The Algorithm GDBSCAN and Its Appli-
cations, *Data Mining and Knowledge Discovery*, 2, 169–194, <https://doi.org/10.1023/A:1009745219419>, 1998.

Sardeshmukh, P. D., Compo, G. P., and Penland, C.: Need for Caution in Interpreting Extreme Weather Statistics, *Journal of Climate*, 28,
9166–9187, <https://doi.org/10.1175/JCLI-D-15-0020.1>, 2015.

765 Schielicke, L. and Pfahl, S.: European heatwaves in present and future climate simulations: a Lagrangian analysis, *Weather and Climate
Dynamics*, 3, 1439–1459, <https://doi.org/10.5194/wcd-3-1439-2022>, 2022.

Shamekh, S., Lamb, K. D., Huang, Y., and Gentile, P.: Implicit learning of convective organization explains precipitation stochasticity,
Proceedings of the National Academy of Sciences, 120, e2216158 120, <https://doi.org/10.1073/pnas.2216158120>, 2023.

Skinner, C. B., Touma, D., Barlow, M., Singh, D., and King, T.: The spatial extent of heat waves has changed over the past four decades,
770 *Communications Earth & Environment*, 6, 662, <https://doi.org/10.1038/s43247-025-02661-y>, publisher: Nature Publishing Group, 2025.

Soci, C., Hersbach, H., Simmons, A., Poli, P., Bell, B., Berrisford, P., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Radu, R., Schepers, D.,
Villaume, S., Haimberger, L., Woollen, J., Buontempo, C., and Thépaut, J.: The ERA5 global reanalysis from 1940 to 2022, *Quarterly
Journal of the Royal Meteorological Society*, <https://doi.org/10.1002/qj.4803>, 2024.

Spanjers, B., Beutner, E., Coumou, D., and Schaumburg, J.: Increased persistence of warm and wet winter weather in recent decades in
775 north-western Europe, *Communications Earth & Environment*, 6, 760, <https://doi.org/10.1038/s43247-025-02588-4>, publisher: Nature
Publishing Group, 2025.

Spuler, F. R., Kretschmer, M., Kovalchuk, Y., Balmaseda, M. A., and Shepherd, T. G.: Identifying probabilistic weather regimes targeted to
a local-scale impact variable, *Environmental Data Science*, 3, e25, <https://doi.org/10.1017/eds.2024.29>, 2024.

Stefanon, M., D’Andrea, F., and Drobinski, P.: Heatwave classification over Europe and the Mediterranean region, *Environmental Research
780 Letters*, 7, 014 023, <https://doi.org/10.1088/1748-9326/7/1/014023>, 2012.

Sulikowska, A. and Wypych, A.: Summer temperature extremes in Europe: how does the definition affect the results?, *Theoretical and
Applied Climatology*, 141, 19–30, <https://doi.org/10.1007/s00704-020-03166-8>, 2020.

Szwarcman, D., Guevara, J., Macedo, M. M. G., Zadrozny, B., Watson, C., Rosa, L., and Oliveira, D. A. B.: Quantizing reconstruction
losses for improving weather data synthesis, *Scientific Reports*, 14, 3396, <https://doi.org/10.1038/s41598-024-52773-2>, publisher: Nature
785 Publishing Group, 2024.

- Tian, Y., Kleidon, A., Lesk, C., Zhou, S., Luo, X., Ghausi, S. A., Wang, G., Zhong, D., and Zscheischler, J.: Characterizing heatwaves based on land surface energy budget, *Communications Earth & Environment*, 5, 1–9, <https://doi.org/10.1038/s43247-024-01784-y>, 2024.
- Tomczyk, A. M., Sulikowska, A., Bednorz, E., and Pótrolniczak, M.: Atmospheric circulation conditions during winter warm spells in Central Europe, *Natural Hazards*, 96, 1413–1428, <https://doi.org/10.1007/s11069-019-03621-4>, 2019.
- 790 Träger-Chatterjee, C., Müller, R. W., and Bendix, J.: Analysis of extreme summers and prior late winter/spring conditions in central Europe, *Natural Hazards and Earth System Sciences*, 13, 1243–1257, <https://doi.org/10.5194/nhess-13-1243-2013>, publisher: Copernicus GmbH, 2013.
- van der Maaten, L. and Hinton, G.: Visualizing Data using t-SNE, *Journal of Machine Learning Research*, 9, 2579–2605, <http://jmlr.org/papers/v9/vandermaaten08a.html>, 2008.
- 795 Van Oldenborgh, G. J., Wehner, M. F., Vautard, R., Otto, F. E. L., Seneviratne, S. I., Stott, P. A., Hegerl, G. C., Philip, S. Y., and Kew, S. F.: Attributing and Projecting Heatwaves Is Hard: We Can Do Better, *Earth’s Future*, 10, e2021EF002 271, <https://doi.org/https://doi.org/10.1029/2021EF002271>, 2022.
- Vautard, R., Cattiaux, J., Happé, T., Singh, J., Bonnet, R., Cassou, C., Coumou, D., D’Andrea, F., Faranda, D., Fischer, E., Ribes, A., Sippel, S., and Yiou, P.: Heat extremes in Western Europe increasing faster than simulated due to atmospheric circulation trends, *Nature*
- 800 *Communications*, 14, 6803, <https://doi.org/10.1038/s41467-023-42143-3>, 2023.
- Wang, C., Li, Z., Chen, Y., Li, Y., Ouyang, L., Zhu, J., Sun, F., Song, S., and Li, H.: Changes in Global Heatwave Risk and Its Drivers Over One Century, *Earth’s Future*, 12, e2024EF004 430, <https://doi.org/https://doi.org/10.1029/2024EF004430>, 2024.
- Wang, J., Guan, Y., Wu, L., Guan, X., Cai, W., Huang, J., Dong, W., and Zhang, B.: Changing Lengths of the Four Seasons by Global Warming, *Geophysical Research Letters*, 48, e2020GL091 753, <https://doi.org/https://doi.org/10.1029/2020GL091753>, 2021.
- 805 World Economic Forum: The Cost of Inaction: A CEO Guide to Navigating Climate Risk, <https://www.weforum.org/publications/the-cost-of-inaction-a-ceo-guide-to-navigating-climate-risk/>, in collaboration with Boston Consulting Group (BCG), 2024.
- Yuan, X., Chen, X., Ochege, F. U., Hamdi, R., Tabari, H., Li, B., He, B., Zhang, C., De Maeyer, P., and Luo, G.: Weakening of global terrestrial carbon sequestration capacity under increasing intensity of warm extremes, *Nature Ecology & Evolution*, pp. 1–10, <https://doi.org/10.1038/s41559-024-02576-5>, 2024.
- 810 Zhang, R., Sun, C., Zhu, J., Zhang, R., and Li, W.: Increased European heat waves in recent decades in response to shrinking Arctic sea ice and Eurasian snow cover, *npj Climate and Atmospheric Science*, 3, 1–9, <https://doi.org/10.1038/s41612-020-0110-8>, 2020.
- Zhang, X., Alexander, L., Hegerl, G. C., Jones, P., Tank, A. K., Peterson, T. C., Trewin, B., and Zwiers, F. W.: Indices for monitoring changes in extremes based on daily temperature and precipitation data, *WIREs Climate Change*, 2, 851–870, <https://doi.org/10.1002/wcc.147>, 2011.
- 815 Zhao, Y., Strebel, D., Derome, D., Esau, I., Li, Q., and Carmeliet, J.: Using clustering to understand intra-city warming in heatwaves: insights into Paris, Montreal, and Zurich, *Environmental Research Letters*, 19, 064 002, <https://doi.org/10.1088/1748-9326/ad456f>, 2024.
- Zhu, J.-J., Yang, M., and Ren, Z. J.: Machine Learning in Environmental Research: Common Pitfalls and Best Practices, *Environmental Science & Technology*, 57, 17 671–17 689, <https://doi.org/10.1021/acs.est.3c00026>, 2023.
- Zschenderlein, P., Pfahl, S., Wernli, H., and Fink, A. H.: A Lagrangian analysis of upper-tropospheric anticyclones associated with heat
- 820 waves in Europe, *Weather and Climate Dynamics*, 1, 191–206, <https://doi.org/10.5194/wcd-1-191-2020>, 2020.