



# Enabling Fast Greenhouse Gas Emissions Inference from Satellites with GATES: a Graph-Neural-Network Atmospheric Transport Emulation System

Elena Fillola<sup>1,2\*</sup>, Raul Santos-Rodriguez<sup>2</sup>, Rachel Tunnicliffe<sup>1</sup>, Jeffrey N. Clark<sup>2</sup>, Nawid Keshtmand<sup>1</sup>, Anita Ganesan<sup>3</sup>, Matthew Rigby<sup>1</sup>

<sup>1</sup>School of Chemistry, University of Bristol, Bristol, UK

<sup>2</sup>School of Engineering Mathematics and Technology, University of Bristol, Bristol, UK

<sup>3</sup>School of Geographical Sciences, University of Bristol, Bristol, UK

Correspondence to: Elena Fillola (elena.fillolamayoral@bristol.ac.uk)

**Abstract.** Atmospheric observation-based “inverse” greenhouse gas flux estimates are increasingly important to evaluate national inventories. A dramatic improvement in “top-down” flux inference is expected in the coming years due to the rapidly growing number of measurements from space. However, many well-established inverse modelling techniques face significant computational challenges scaling to modern satellite datasets, particularly those that rely on Lagrangian Particle Dispersion Models (LPDM) to simulate atmospheric transport. Here, we introduce GATES (Graph-Neural-Network Atmospheric Transport Emulation System), a data-driven LPDM emulator which outputs source-receptor relationships (“footprints”) using only meteorology and surface data as inputs, approximately 1000x times faster than an LPDM. We demonstrate GATES’s skill in estimating footprints over South America and integrate it into an emissions estimation pipeline, evaluating Brazil’s methane emissions using GOSAT (Greenhouse Gases Observing Satellite) observations for 2016 and 2018 and finding emissions that are consistent in space and time with the physics-driven estimate. This work highlights the potential of machine learning-based emulators like GATES to overcome a key bottleneck in large-scale, satellite-based inverse modeling, accelerating greenhouse gas emissions estimation and enabling timely, improved evaluations of national GHG inventories.

## 1 Introduction

Reducing greenhouse gas (GHG) emissions is essential for mitigating climate change, with carbon dioxide (CO<sub>2</sub>) and methane (CH<sub>4</sub>) being two of the most significant contributors. International agreements such as the Global Methane Pledge, with over 150 participating countries, reflect the commitment to address this challenge, by aiming for a 30% reduction in emissions by 2030, compared to 2020 levels (European Commission and United States of America, 2021). However, significant uncertainties persist in the inventory-based (“bottom-up”) reports of national methane emissions, which will be used to evaluate progress (Saunio et al., 2020, 2025). “Top-down” or “inverse” estimates of GHG emissions can be used to evaluate and improve these self-reported national emissions inventories and are therefore seen as a valuable tool for supporting international climate agreements (e.g., (Leip et al., 2018)). These methods use atmospheric concentration observations to quantify surface fluxes, with atmospheric chemical transport models providing the link between these two quantities.

Until recently, top-down studies primarily relied on in situ atmospheric observations from individual stations or networks (e.g., (Bergamaschi et al., 2018)). Increasingly, CH<sub>4</sub> and CO<sub>2</sub> flux estimates are being derived using satellite data, reflecting the expansion of space-based instruments (e.g., (Ganesan et al., 2017; Scarpelli et al., 2022; Tunnicliffe et al., 2020; Western et al., 2021; Worden et al., 2023)), which can provide valuable insights into regions previously under-sampled by in situ data. National emissions estimates have been derived using data from instruments such as GOSAT (Greenhouse gases Observing SATellite, launched 2009 (Parker et al., 2020)) using regional (Ganesan et al., 2017; Tunnicliffe et al., 2020; Western et al., 2021) or global (Alexe et al., 2015; Feng et al., 2023; Maasakkers et al., 2019) chemical transport models. Current global instruments, like TROPOMI (Tropospheric Monitoring Instrument, launched 2017 (Veefkind et al., 2012)) have over 100 times the observation density of GOSAT, and recently launched and upcoming satellites (e.g. CO2M, MethaneSAT) will continue to grow the volume of available observations (Jacob et al., 2022). Higher data density increases the spatial and



temporal resolution at which fluxes can be inferred providing the opportunity to better understand the processes driving observed changes in global atmospheric CO<sub>2</sub> and CH<sub>4</sub> abundance.

This rapid growth in data volume, from in situ-based datasets (~1000s of observations per month in a continental region) to satellite-based (~10,000s to 100,000s of observations per month in a continental region), is leading to scaling issues for many traditional approaches to flux inference. One of the most common families of top-down methods for national scale emissions estimation employs Lagrangian Particle Dispersion Models (LPDMs), which use archived meteorological state estimates to simulate the movement of hypothetical gas particles backwards in time from a measurement point to the surface in the surrounding region. The advantage of using LPDMs for GHG flux inference is that LPDMs directly calculate the high-resolution sensitivity, or “footprint” (Fig. 1a), of a mole fraction measurement to upwind fluxes. This contrasts with Eulerian models, which simulate concentrations in a 3D atmospheric grid rather than using individual particles, and do not directly calculate source-receptor relationships. To be useful in top-down inference, Eulerian model outputs require additional processing to derive sensitivities of observations to fluxes, such as performing ensembles of perturbed flux runs (e.g., (Baker, 2006a; Bousquet, 2000; Peters et al., 2005)) or deriving adjoint model code (e.g., (Baker, 2006b; Kaminski et al., 1999)). However, a major disadvantage of LPDMs is that they require one run for each observation (several core-minutes, depending on set-up), leading to high computational burdens for large datasets. Studies show that increasing the number of simulated particles and extending their simulation time reduces statistical errors in the transport model, but these improvements also come at the expense of even greater resource demands (Pisso et al., 2019; Vojta et al., 2022). Although LPDMs are easily parallelizable with high performance clusters allowing for multiple simulations to run simultaneously, the overall computational cost remains substantial and will likely be a barrier in the use of LPDM-based methods for applications involving planned space-based GHG measurements.

The satellite community has recognized computational capacity as a key limitation in applying greenhouse gas measurements and inverse modelling to support policy (Joint CEOS-CGMS Working Group on Climate - Greenhouse Gas Task Team., 2024). To be able to conduct computationally-feasible studies with Lagrangian methods, researchers sometimes need to coarsen the dense satellite observations, averaging measurements in space (Thompson et al., 2025) and time (Tunnicliffe et al., 2020). Several recent studies have proposed methods for interpolating or emulating footprints (see below) but none have addressed the challenging problem of emulating satellite footprints at continental scales. In this study, we present GATES (Graph-Neural-Network Atmospheric Transport Emulation System), a new method for footprint emulation that addresses previous limitations, offering high computational efficiency for satellite data whilst retaining sufficient accuracy over large scales for regional-scale flux inference. Section 2 provides background on LPDMs and previous emulation approaches, and Section 3 presents the architecture of the machine learning model. In Section 4 we describe the generation of LPDM footprints in our case study region, South America, and detail the inputs, dataset and training approach. In Section 5 we show and evaluate the outputs of GATES, and most importantly we demonstrate its application in a previously studied top-down inference pipeline to estimate Brazil’s methane emissions.

## 2 Background and problem statement

### 2.1 Lagrangian Particle Dispersion Models

To calculate the sensitivity of a mole fraction measurement to surface fluxes using LPDMs, thousands of virtual particles are released from a set of 3D coordinates (latitude, longitude, height) and transported backwards in time for a number of days. The model records whenever these particles are near the surface (within 40m in the simulations used here), creating an aggregated 2D “influence footprint” that indicates the contribution of a unit surface flux at a particular location to the observed mole fraction. When applied to in situ measurements, the LPDM is initialized using the site coordinates and the inlet height. Satellites, on the other hand, take column-averaged measurements of GHG mole fractions, so instead, a number of 3D releases are run from different heights in the atmosphere, and then averaged using a kernel (e.g. Ganesan et al. (2017)). This means that LPDM runs for satellite footprints are more computationally expensive than for in-situ footprints.



85 Here, we emulate the UK Met Office LPDM NAME (Numerical Atmospheric-dispersion Modelling Environment (Jones et al., 2007)), with a similar setup to those used by Tunnicliffe et al. (2020) and Ganesan et al. (2017), who run NAME for GOSAT observations to infer methane emissions. ~~Thousands of~~ particles are simulated travelling backwards for 30 days from the location and time of the satellite measurement, from a range of heights defined by the pressure levels of the XCH4 product. Particles are recorded as interacting with the surface whenever they are below 40m above ground level. The sensitivities for  
90 each vertical level are averaged into a single **2D footprint**, weighted by the corresponding GOSAT averaging kernel and pressure weight. See Ganesan et al. (2017) for more details on the set-up. Other examples of well-known LPDMs that have been applied to similar applications are the FLEXible PARTicle Dispersion Model (FLEXPART (Pisso et al., 2019)) and the Stochastic Time-Inverted Lagrangian Transport Model (STILT, (Fasoli et al., 2018)).

## 95 2.2 Meteorology

LPDMs are usually driven by a meteorological reanalysis product. Here, our NAME simulations use the Met Office Unified Model (UM) global analysis fields to simulate particle dispersion. The global model has a resolution of 3 hours and 25 km up to July 2014, 17 km from then until July 2017 and 12 km thereafter, with 59 vertical levels up to 29 km (Met Office, 2025a, b). NAME also uses static fields (i.e. not time dependent) of surface characteristics, including orography, a sea-land mask, and  
100 a land surface type map with nine categories (including different types of trees and grasslands, urban, bare soil and ice (Essery et al., 2001)), at a resolution of  $0.156^\circ \times 0.234^\circ$ .

## 2.3 Problem statement

Summarised mathematically, an LPDM  $f$  produces a footprint  $\mathbf{y}_t^\varphi$  by modelling backwards particle dispersion from a set of  
105 coordinates  $\varphi$  at time  $t$ . For this, it uses static information  $\boldsymbol{\omega}$  including topography and land-use maps, and a time series of 3D meteorological features, starting at time  $t$  ( $\mathbf{x}^t$ ) and extending backwards in time from  $t$  for a number of steps  $N$  with separation  $\Delta t$ . The meteorological input time series can therefore be defined as  $\mathbf{x}^{t:t-N\Delta t} = [\mathbf{x}^t, \mathbf{x}^{t-\Delta t}, \dots, \mathbf{x}^{t-N\Delta t}]$ , and the LPDM summarized as  $\mathbf{y}_t^\varphi = f(\varphi, \mathbf{x}^{t:t-N\Delta t}, \boldsymbol{\omega})$ . The LPDM setup described here uses  $\Delta t = 3h$ , and  $N = 240$ , which equates up to tracking particles backwards in time for 30 days.

110 Our goal is to develop an efficient emulator  $\Phi$  that can accurately recreate footprints produced by the LPDM in orders of magnitude less time and potentially using only a subset of the full LPDM inputs. Thus, the emulator predicts a footprint as  $\hat{\mathbf{y}}_t^\varphi = \Phi(\varphi, \tilde{\mathbf{x}}, \tilde{\boldsymbol{\omega}})$  where  $\tilde{\mathbf{x}} \subseteq \mathbf{x}^{t:t-N\Delta t}$  and  $\tilde{\boldsymbol{\omega}} \subseteq \boldsymbol{\omega}$ .

## 115 2.4 Previous ML approaches

The urgent need for scalable LPDM-based inverse methods was previously addressed by Roten et al. (2021), Fasoli et al. (2018), Cartwright et al. (2021) and others, who derived modest gains in computational efficiency through interpolation-based approaches. More complex machine learning (ML) methods such as those developed by Fillola et al. (2023) and He et al., (2024) introduced proof-of-concept emulators of LPDM footprints for surface sites using meteorological fields as inputs. One  
120 of these studies (Fillola et al., 2023) used a set of individual regressors to emulate the footprint value at each grid-cell for in-situ observation towers, but only estimated these values for part of the footprint, within  $\sim 100$  km of the measurement site. Therefore, to perform flux inversions, the emulated footprints had to be nested within a low-resolution LPDM simulation. The emulator developed in (He et al., 2024) focuses on emulating high-resolution in-situ footprints ( $400 \times 400$  km<sup>2</sup> domain at 1 km resolution) for an urban sensor network (Dadheech et al., 2024). To constrain their convolutional neural network architecture,  
125 one of the key inputs was a Gaussian plume, a simplified footprint approximation calculated using the meteorology at the measurement site. While this approach is effective for local-scale dispersion, it is unlikely to be suitable for national or continental transport ( $\sim 1000$ – $5000$  km) because the assumptions underpinning the Gaussian plume model (such as constant wind speed and homogeneous atmospheric conditions) only hold over  $\sim 10$  km spatial scales.



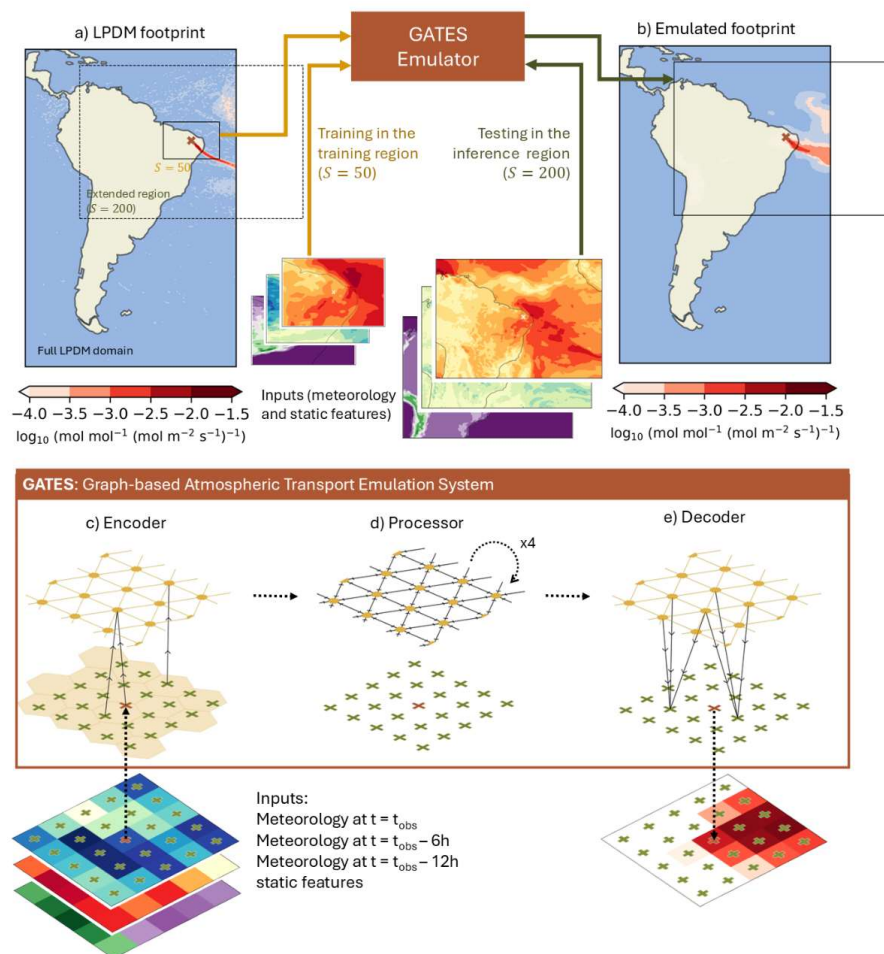
### 3 Model Architecture

130 The Graph-Neural-Network Atmospheric Transport Emulation System (GATES) is a ML-driven emulator of regional LPDM-  
derived satellite observation footprints using meteorological and topographical inputs. The architecture of GATES builds on  
that of Keisler, (2022) and Deepmind’s Graphcast (Lam et al., 2023), who developed weather forecasting models using Graph  
Neural Networks (GNNs) with an encoder-processor-decoder structure. This architecture achieved breakthroughs in  
deterministic weather forecasting, sometimes outperforming the reference physical models (Lam et al., 2023), as well as  
135 effectively learning complex systems based on Partial Differential Equations (PDEs), like fluid dynamics and diffusion (Pfaff  
et al., 2020; Sanchez-Gonzalez et al., 2020). Many of these systems are designed to learn a one-step forward model, predicting  
system quantities at time  $t+1$  given the current state (and often previous states too). Unlike these previous studies, GATES is  
trained to return **time-integrated** 2D GHG measurement footprints without requiring information about the intermediate model  
timesteps.

140 As inputs, GATES takes a subset of the meteorology that drives the LPDM, reducing input/output overhead and memory  
requirements compared to running the LPDM: we provide a number of snapshots of the state of the atmosphere at the time of  
the satellite measurement and before, including variables like wind direction, wind speed and planetary boundary layer height,  
as a latitude-longitude grid and at selected vertical levels. These inputs are complemented with time-independent variables,  
145 including the latitude-longitude **coordinates of a node**, its distance from the measurement, the surface height above sea level,  
and the main landcover type.

Figure 1 shows a schematic of the **architecture** of GATES. Graph Neural Networks represent data as a graph, composed of  
nodes and connecting edges. In GATES, each coordinate in the latitude-longitude grid is treated as a node, with the inputs at  
150 that location considered its attributes. In the encoder (Fig. 1e), this input grid is encoded in a lower-resolution regular triangular  
mesh, which acts as an internal abstract feature space. This mesh, built with the h3 library (Uber Technologies Inc, 2024),  
divides the domain into hexagons with an average area of 1770km<sup>2</sup>, and with mesh nodes placed ~40km from each other. We  
place edges between each node in the lat-lon grid and its closest node in the mesh, so that each mesh node receives a Multi-  
Layer Perceptron (MLP) encoding of the distance-weighted mean of the local features. MLPs are simple feedforward neural  
155 networks composed of multiple layers of linear transformations and non-linear transformation functions, which here are used  
to update node and edge features based on local information. In the processor (Fig. 1f), each node in the mesh is connected to  
its six adjacent nodes, and the whole mesh is updated in multiple message-passing rounds. Each message-passing GNN block  
(Battaglia et al., 2018) first uses an MLP to update the features of the edges in the mesh using information from the adjacent  
nodes, and then another MLP to update each node based on its adjacent features. In the decoder (Fig. 1g), a final MLP maps  
160 the mesh-node features back to the original latitude-longitude grid, outputting the footprint (Fig. 1b).

GATES is inherently flexible because it operates through local, node-wise computations. At every stage (encoding, processing  
and decoding) the model learns to update each node based only on its neighbours’ features, rather than relying on a regular  
grid or fixed input dimensions. Traditional architectures such as Convolutional Neural Networks (CNNs), on the other hand,  
165 require inputs to be defined on uniform, fixed-sized grids, where emulation depends on the resolution and dimensions of the  
training domain. With GATES, training and inference can be done at different resolutions, geometries or domain sizes, without  
needing to retrain or modify the architecture.



**Figure 1: GATES model schematic and architecture.**

Top: (a) Example of an LPDM-generated footprint (~20 mins to generate on a single CPU) showing the sensitivity of a satellite measurement to fluxes from the surrounding domain. (b) Corresponding GATES-emulated footprint (~1.5s to generate). Both (a) and (b) are shown over the full LPDM domain and resolution ( $0.352^\circ \times 0.234^\circ$ ,  $\approx 33 \times 25$  km in mid-latitudes) used in (Tunncliffe et al., 2020). In (a), the solid-line box corresponds to the training region, a square of size  $50 \times 50$  grid-cells centered around the coordinates of the satellite measurement. The solid-line box in (b) corresponds to the inference region, a  $200 \times 200$  grid-cell square over which footprints were emulated. When this area escapes the original footprint domain, as above, the added space is filled with zeros and ignored in evaluation (here shown as whitespace inside the boxes). Bottom: Architecture of the graph and emulator, demonstrated for a square domain of size  $5 \times 5$ . GATES is composed of (c) an encoder, (d) a processor, and (e) a decoder. The black solid arrows indicate the flow of information. The inputs are represented as node attributes on a latitude-longitude grid (crosses) centered around the measurement point (red cross). (c) In the encoder, local regions of the inputs are mapped into nodes in the abstract feature space (yellow hexagons), arranged as an triangular mesh. Each mesh-node is connected with edges to its six neighbors (yellow lines). (d) In the processor, each mesh-node is updated using message-passing from the neighboring nodes. Four independent message-passing blocks are learned. (e) The decoder maps the latent space back to the original latitude-longitude grid of the same resolution as the inputs, outputting the footprint value at each node.



#### 4 GATES in practice: Emulating GOSAT footprints over South America

185 To demonstrate the model, we train GATES to emulate NAME footprints for GOSAT observations over South America, as presented in (Tunnicliffe et al., 2020). GATES is trained and validated using data from 2014 to 2016, and emissions are derived for 2016 and 2018 (the year 2018 was chosen to demonstrate the performance of the GATES-based inversion as it is separated in time from the data used in the training and validation set). The footprints aggregate the surface interactions of particles transported for the 30 days leading up to the satellite measurement at a resolution of  $0.352^\circ$  longitude  $\times$   $0.234^\circ$  latitude ( $\approx$  190  $33 \times 25$  km in mid latitudes), constrained to a domain that covers the whole South American continent ( $60.98^\circ$  S to  $22.32^\circ$  N and  $91.33^\circ$  W to  $24.8^\circ$  W with a grid of size  $190 \times 357$ ). Each footprint takes about  $\sim 20$  core-minutes to be generated on a high-performance cluster.

##### 4.1 Inputs: meteorology and topography

195 This version of the emulator takes as main inputs nine physical variables at seven vertical levels in the atmosphere (see Table 1 for all the variables and levels used). The meteorology is interpolated linearly from its 3-hourly resolution  $t$ , as well as any required previous timesteps up to  $t - \tilde{N}\Delta t$ . In the application described here,  $\tilde{N} = 2$  and  $\Delta t = 6h$ , so that the meteorological input to each footprint is composed of the weather state at  $t$ , six hours and twelve hours before. This is a small subset of the full NAME input meteorology, which usually requires  $\sim 15$  meteorological variables at 50 atmospheric levels at over 200 timesteps. We also provide the model with information from the static fields NAME uses to describe topography (orography and landcover type), as well as two variables with the x- and y- coordinates of each grid-cell with respect to the measurement coordinates (so that the grid-cell with the satellite observation is  $[0,0]$ ) and a variable with the Euclidean distance from each grid-cell to the measurement coordinates. Each input is a 2D field of the same resolution and domain as the corresponding footprint.

| Variable name                   | Description                                                               | Vertical levels                             |
|---------------------------------|---------------------------------------------------------------------------|---------------------------------------------|
| x-wind                          | At $t=t_{\text{obs}}$ , $t=t_{\text{obs}-6h}$ and $t=t_{\text{obs}-12h}$  | 100m, 660m, 1.7km, 3.2km, 6.4km, 12km, 18km |
| y-wind                          |                                                                           |                                             |
| Upward air velocity             |                                                                           |                                             |
| Air temperature                 |                                                                           |                                             |
| Air pressure                    |                                                                           |                                             |
| Wind speed                      |                                                                           | 100m, 6.4km, 18km                           |
| Wind direction                  |                                                                           |                                             |
| Boundary layer thickness        |                                                                           | Surface variables (0m)                      |
| Surface air pressure            |                                                                           |                                             |
| Latitude                        | Not time-dependent                                                        |                                             |
| Longitude                       | Not time-dependent                                                        |                                             |
| Distance from measurement point | Not time-dependent, Euclidean distance in x-y grid (not on earth surface) |                                             |
| x-coordinate                    | Not time-dependent                                                        |                                             |
| y- coordinate                   | Not time-dependent                                                        |                                             |
| Height above sea level          | Not time-dependent                                                        |                                             |
| Main landcover type             | Not time-dependent                                                        |                                             |

205 **Table 1 – Input variables provided to the emulator.** In total, there are (2 atmospheric surface variables + 7 atmospheric variables  $\times$  7 levels)  $\times$  3 timesteps + 2 topography variables + 5 constant variables = 160 input features.



## 210 4.2 Preparing the dataset

GATES is designed to be LPDM domain agnostic: instead of emulating footprints over the whole LPDM domain, which tends to be sparse, GATES emulates footprints on a square domain of  $S \times S$  grid cells centred around the measurement coordinates  $\phi$ . The meteorology and static fields are cropped to the same area for each corresponding footprint.

215 For this South America application, GATES is first trained on a square (in latitude/longitude space) of size  $S=50$  grid cells centered around the satellite measurement. Subsequently, footprints are emulated over a square of  $S=200$  grid-cells ( $\sim 6000 \times 5000$  km; see the training and inference regions in Fig 1, panels a and b). We find that training in the smaller domain is not only more computationally efficient, but that the model performs better than training on the  $S=200$  domain, likely because the wider domain is mostly sparse. We choose to define our inference region as  $S=200$  as our preliminary tests suggest  
220 this size of domain doesn't introduce substantial error in the simulated mole fractions, compared to simulations using a larger region. When using the emulated footprints in the inference emissions pipeline, we fill the rest of the full LPDM domain with zeros.

We split our dataset into training, validation, and test sets using distinct time periods, to imitate deployment conditions and to  
225 avoid the high autocorrelations in meteorological fields from polluting the evaluation results. We use the first two years to train the model (2014-2015, 11165 samples), validate on January, February and March of 2016 (4314 footprints), and evaluate the outputs for the remaining months of 2016, as well as the whole of 2018 (36671 footprints, 16945 from 2016 and 15412 from 2018). The validation set was used to tune model hyperparameters, and to calibrate the bias correction. Figure A1 shows the spatial and seasonal distribution of the datasets used.

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## 4.3 Training details

### 4.3.1 Data normalization

During training, footprints are log-transformed and shifted by the minimum value in the training dataset, so that all non-zero  
235 values in the original footprints  $\mathbf{y}$  remain strictly positive in the transformed footprints  $\mathbf{y}'$ . The zero values are maintained as such. This helps tackle the footprints' strong exponential distributions, with values decaying quickly with distance from the measurement point. The emulated footprints on the test set are returned to the original space for evaluation. All inputs are standardized (zero mean and unit variance). Each atmospheric variable is standardized per atmospheric level (where relevant) and across all different input timesteps.

### 240 4.3.2 Model parameters

All neural networks in the GNN are MLPs with two hidden layers of size 16 and an output layer size of 64, except the decoder MLP, which has only one hidden layer and an output size of 1 (as a single value is predicted at each node). All MLPs use Relu (Nair et al., 2010) as the activation function and are followed by a LayerNorm (Ba et al., 2016) layer (except the decoder's MLP, which outputs the footprint value).

### 245 4.3.3 Loss function

The loss function  $L$  weights mean squared error (MSE) by the footprint value, which applies stronger penalties for mispredicting areas with higher relevance. It first calculates the pixel-by-pixel squared error between the predictions and the true footprints (both in the transformed space, i.e.  $\hat{\mathbf{y}}'$  and  $\mathbf{y}'$  respectively), and then weights it by a linear transformation  $g()$  of the original footprint  $\mathbf{y}$ , before taking the mean across the footprint. For each batch, we average the loss from all the footprints  
250 uniformly.



$$L = \ell(\hat{\mathbf{y}}, \mathbf{y}') = \frac{1}{S^2} \sum_{i=1}^S \sum_{j=1}^S g(\mathbf{y}(i, j)) \times (\hat{\mathbf{y}}(i, j) - \mathbf{y}'(i, j))^2$$

Where

$$g(\mathbf{y}) = w\mathbf{y} + a$$

255

Here, we use  $w = 1000$  and  $a = 0.5$ . This training objective was minimized with the ADAMW (Lam et al., 2023; Loshchilov and Hutter, 2019) **optimizer** and a learning rate of  $5 \times 10^{-5}$ , using a batch size of 5.

#### 4.4 Thresholding and bias correcting the footprints

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Following inference, the near-zero background values below a calculated threshold are set to zero, imitating approaches from precipitation modelling (Schmidli et al., 2006). The footprints are also bias-corrected by applying quantile mapping (Met Office, 2018). This bias correction is necessary to avoid the model's tendency to underpredict, likely caused by the sparsity of the outputs. The calibration of the threshold and the quantile mapping are both done using the **validation set**, transformed back to the original data space.

##### 4.4.1 Output thresholding

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A “footprint threshold” is defined on the validation set such that the threshold exceedance frequency matches **the above-zero frequency in the LPDM-generated footprints** (Schmidli et al., 2006). In the test dataset, all values under this threshold are set to zero.

##### 4.4.2 Bias correction

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After thresholding, the distribution is corrected using quantile mapping. This technique maps the cumulative distribution function (CDF) of the emulated data to that of the true data, applying a transformation function  $T(x)$ . We define  $T(x)$  using the CDF of the true data in the validation set,  $F_{LPDM}(x)$ , and the CDF of the emulated data  $F_{EM}(x)$  as **follows**:

$$T(x) = F_{LPDM}^{-1}(F_{EM}(x))$$

Once  $T(x)$  is defined on the validation set, it is applied to the footprints emulated by the test set ( $\mathcal{Y}_{test}$ ) to produce the corrected footprints ( $\mathcal{Y}'_{test}$ ):

275

$$\mathcal{Y}'_{test} = T(\mathcal{Y}_{test})$$

#### 4.5 Hardware and time requirements

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We train and run the model on a 32GB NVIDIA V100 GPU. It takes 10h to fully train, including loading all the data and model into memory. For emulation, each footprint takes around 0.75 seconds to produce on the same V100 GPU (after an initial overhead to load the model and the input data), whereas a single footprint LPDM footprint takes ~20 minutes. GATES can therefore generate footprints 1000x faster than the physics-based simulation. The model has **~250k parameters**, which is light in comparison to others (Keisler's has 6.7M (Keisler, 2022), and Graphcast has 36.7M (Lam et al., 2023)) and enables easier and cheaper deployment.

285

Integrating the emulator in the emissions inference pipeline presents a significant speed-up. The inversion algorithm itself, which combines the observations, footprints and prior emissions to output updated emission fluxes takes 6–10 hours on a CPU, depending on the number of data points assimilated (**using a computationally expensive hierarchical Bayesian Markov Chain Monte Carlo inverse method, as outlined in Ganesan et al. (2014)**). A regional monthly inversion pipeline shown here (~1,500 footprints) using an LPDM would take 13 core-days. Here, a GATES-driven one takes 8–11 hours. GATES therefore provides a 40x speed-up on **national flux inference** and shifts the primary computational bottleneck to the inversion algorithm, which now dominates the runtime. Substantially higher overall inversion speed-ups would be obtained if a less expensive inverse

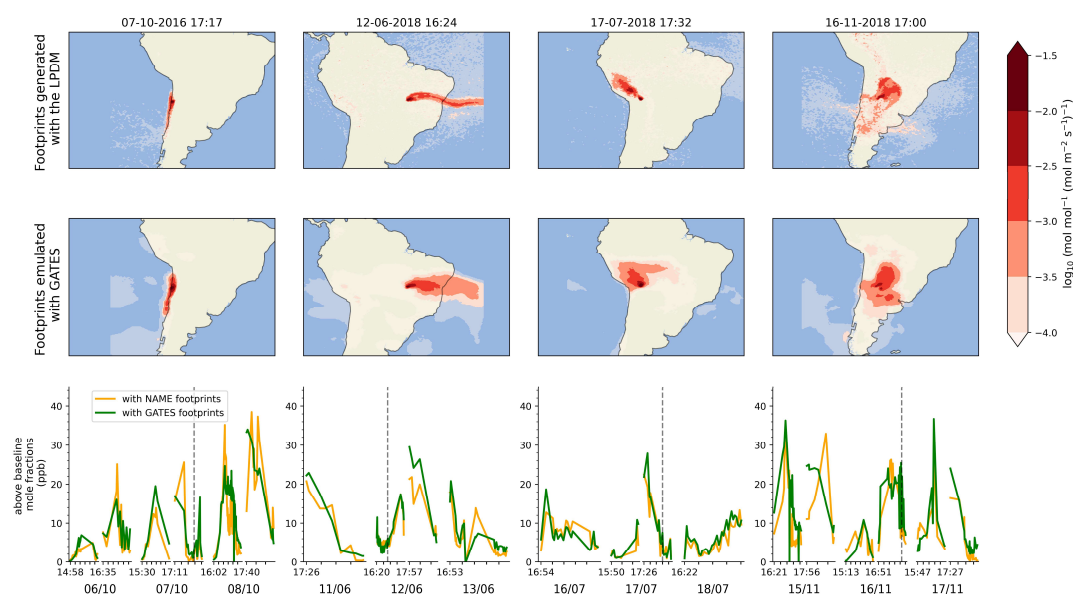
290



method was used. As noted in (Dadheech et al., 2024), the use of an efficient emulator has the added potential advantage that footprints do not need to be archived and can instead be produced on demand, substantially reducing storage requirements. Further speed-up to GATES is expected with software optimization in the future.

## 5 Evaluating GATES performance: footprints, predicted concentrations and inferred emissions

295 In this section we use a range of tests to evaluate the performance of the emulated footprints at three stages of the inversion pipeline: 1) metrics to compare the emulated footprints to the LPDM, 2) comparison of simulated methane column mole fractions over South America, and 3) comparison of Brazil's inferred methane emissions at monthly resolution for April-December 2016 and all of 2018. **Figure 2 shows four examples of LPDM footprints and their emulated counterparts, as well as the emulated methane mole fractions for those days.** We show that the monthly flux estimates using GATES are comparable to those obtained using LPDM footprints at national and sub-national scales.



**Figure 2: Example GATES outputs.** Four LPDM-generated footprints from the test dataset (top row) and their GATES-emulated counterparts (second row). **The bottom row shows modelled above-baseline mole fractions**, derived with the LPDM footprints (orange) and the GATES footprints (green). Each box shows the timeseries for three days with breaks between days indicated by wider gaps between the lines. Each tick mark corresponds to two minute intervals. For days where the satellite scans the continent multiple times, we indicate the time of the first measurement of each overpass. The dashed line indicates the date and time of the footprints shown in the corresponding top two rows. Mole fractions are calculated by convolving each footprint with a prior, producing the estimated methane contribution in ppb from each grid cell to that particular measurement, and summing over the domain to calculate the total expected contribution from local sources (i.e. above the background baseline).

The definition of all the metrics used can be found in Appendix B. We evaluate the footprints themselves using the Correlation of Coefficient between the predicted and the true values, both in the original data space and in the logged space. The correlation in the original space captures how well the model reproduces the overall magnitude of the footprints, whereas applying the metric in the logged space gives more weight to low-magnitude values, often more diffuse and challenging to model. To



quantify the spatial accuracy of the predicted footprints we use the metric Intersection over Union (IoU), which calculates the overlap between the predicted and true nonzero regions. The timeseries of simulated methane mole fractions is evaluated using standard metrics: the Coefficient of Correlation to assess the agreement between GATES and LPDM mole fractions; the Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) to quantify average and large errors, respectively; and the Mean Bias to indicate any systematic over- or underestimation in the predictions. The monthly emissions calculated with the inversion algorithm are evaluated using MAE and Mean Bias.

5.1 GATES-emulated footprints compared to the LPDM

Example emulated footprints (Fig. 2, middle row) and a set of goodness-of-fit metrics (Table 2) show that GATES captures well the overall shape and magnitude of the LPDM footprints over a range of meteorological regimes and locations in South America. However, the GATES outputs often tend to be somewhat smoother than the LPDM. This is primarily thought to be because the MSE loss function favours averaging in regions of high variability (similar smoothing effects have also been reported when using different architectures with MSE losses in LPDM emulation tasks (He et al., 2024). Moreover, since the LPDM is stochastic, the model outputs exhibit small-scale noise far from the measurement location, which is not reflected in the emulated footprints. However, this noise has little impact on receptor mole fraction predictions. The model's connected architecture may also contribute to the smoothing effect, as similar behavior has been observed in weather applications using similar machine learning model framework (Lam et al., 2023).

We evaluate the spatial agreement of the emulated footprints using Intersection over Union (IoU) and the accuracy of the predictions using the correlation of coefficient (see Appendix B for all metrics), averaging both scores across all footprints in the test dataset. In the near-field (training region,  $S=50$ , Box A in Fig. 1), GATES achieves a mean IoU score ( $\pm$  one standard deviation) of  $62\% \pm 23\%$  and a mean correlation of coefficient of  $0.70 \pm 0.13$ . Emulating the far field (full emulation domain,  $S=200$ , Box B in Fig. 1) is a more difficult task, as the particles become more dispersed further from the measurement point. It is also a prediction area unseen to GATES during training. There is an expected drop in performance, particularly in the IoU as the LPDM footprints become noisier (IoU of  $35\% \pm 12\%$ , correlation coefficient to  $0.68 \pm 0.13$ ). The drop in the correlation of coefficient is smaller as it is dominated by the large values very close to the measurement point.

We find that model performance is generally poorer in regions with more heterogeneous topography (see Fig. C1), with footprints near the Andes scoring lower across all metrics. Chemical transport models are known to struggle over complex terrains (Brioude et al., 2012), potentially leading to more variance in the outputs and more difficult footprints to emulate. In addition, the seasonal and spatial distribution of observations in the training data might also influence performance: there are fewer training footprints in some of the mountainous areas, which could limit the learning. In contrast, the July-August-September season, which has more training observations, consistently achieves better metric scores (Fig C1).

| Evaluation of footprints |                            |                                     |       |  |
|--------------------------|----------------------------|-------------------------------------|-------|--|
| Evaluation Size          | Coefficient of correlation | Coefficient of correlation (logged) | IoU   |  |
| $S = 50$                 | 0.703                      | 0.564                               | 62.2% |  |
| $S = 200$                | 0.684                      | 0.430                               | 35.0% |  |

| Evaluation of mole fractions |                            |                     |                      |                           |
|------------------------------|----------------------------|---------------------|----------------------|---------------------------|
| Evaluation Size              | Coefficient of correlation | MAE $ppb (10^{-9})$ | RMSE $ppb (10^{-9})$ | Mean Bias $ppb (10^{-9})$ |
| $S = 50$                     | 0.858                      | 2.01                | 3.28                 | 1.75                      |
| $S = 200$                    | 0.808                      | 2.89                | 4.40                 | 0.724                     |

Table 2. Evaluating GATES. Top: comparing footprints against the LPDM outputs. We show the mean score across footprints, averaged for the testing dataset, at the training region ( $S = 50$ ) and the inference region ( $S = 200$ ). Bottom: Evaluation of mole fraction timeseries, averaged across the testing dataset, also shown at the training and inference regions.



## 5.2 Evaluating simulated mole fractions

In the inversion pipeline, each footprint is convolved with an emissions field (element-wise multiplication of both 2D fields and then summation over the whole area) to calculate the modelled atmospheric column-averaged mole fraction at the satellite observation location and time. Here, we **convolve** both sets of footprints (emulated and LPDM-derived) with the emissions field from (Tunnicliffe et al., 2020), which includes anthropogenic (EDGAR (Emission Database for Global Atmospheric Research) v4.3.2 database (Janssens-Maenhout et al., 2019)), biomass burning (GFED (Global Fire Emissions Database) v4.1) and **wetland** (SWAMPS (Surface Water Microwave Product Series) (Schroeder et al., 2015)).

Figure 2 (bottom panel) show examples of the timeseries emulated with GATES and the LPDM, for twelve days across the testing dataset. The GATES-modelled measurements achieve a correlation coefficient of 0.81 with the LPDM-modelled data. The Mean Absolute Error (MAE) and Root Mean Squared Error (RMSE), of 2.89 ppb and 4.40 ppb respectively, are well below the estimated instrument GOSAT repeatability of 13 ppb (Parker et al., 2020). The errors between the two timeseries are approximately normally distributed, with a small tendency for GATES to overpredict (Mean Bias 0.72 ppb). 1.6% of the emulated mole fractions show an absolute error greater than 13 ppb. These footprints are often near large cities, where the calculated mole fractions are large and where the influence of emulation errors, particularly the above-mentioned smoothing, becomes more pronounced (see Fig. D1).

## 5.3 Inversion

Assessing the performance of the emulated footprints in a full methane flux inversion is key to ensuring that GATES is fit-for-purpose. Here, we follow a well-studied previous example, using GOSAT observations over and near Brazil (see (Tunnicliffe et al., 2020)) and an inversion set-up similar to (Western et al., 2021) and (Ganesan et al., 2014), who use a hierarchical Bayesian method to estimate monthly regional emissions. Brazil was chosen as a case study, because it is a large country where there are major and diverse CH<sub>4</sub> emissions from human and natural sources, which are not well understood (Tunnicliffe et al., 2020). We carry out this process for two inversion setups that are identical except for the footprints used: one uses the LPDM-generated footprints (those used in (Tunnicliffe et al., 2020)), the other uses the GATES-emulated footprints.

We find that the yearly flux estimates calculated with GATES are in good agreement with the more computationally expensive LPDM-powered estimates: the inversion using the LPDM footprints estimates Brazil's mean yearly emissions of methane to be  $41 \pm 5 \text{ Tg yr}^{-1}$  for 2016 and  $49 \pm 6 \text{ Tg yr}^{-1}$  for 2018, and the inversion using the GATES footprints estimates  $42 \pm 5 \text{ Tg yr}^{-1}$  and  $53 \pm 7 \text{ Tg yr}^{-1}$ , respectively (see Table 3 for the disaggregated metrics). Figure 3(a) shows the estimated monthly emissions for Brazil across the two years, where the Mean Absolute Error (only for the test months) is  $3.8 \text{ Tg yr}^{-1}$  in 2016 and  $6.3 \text{ Tg yr}^{-1}$  in 2018, which is comparable to the a posteriori emission uncertainties.

Figure 3(b) shows the difference between the derived emissions (posterior) and the initial estimate (prior) for 2018 for the two inversions, and Fig. 3(c) shows the difference between these adjustments. The fluxes are generally in good spatial agreement (Mean Absolute Error in the derived fluxes of  $0.003 \mu\text{mol m}^{-2} \text{ s}^{-1}$  compared to mean value of  $0.010 \mu\text{mol m}^{-2} \text{ s}^{-1}$  across the two years). Both inversions most notably increased the prior estimate in Brazil's east coast and in the Pantanal region on the border with Bolivia. Simulated methane concentrations based on the LPDM-derived posterior and the GATES-derived posterior both show a significantly improved fit to the observed GOSAT XCH<sub>4</sub> compared to the prior-based simulations (see Appendix E). The two posteriors show consistent corrections to the prior, with the GATES-based simulations showing only a small positive mean bias of 2.69 ppb relative to those from LPDM.

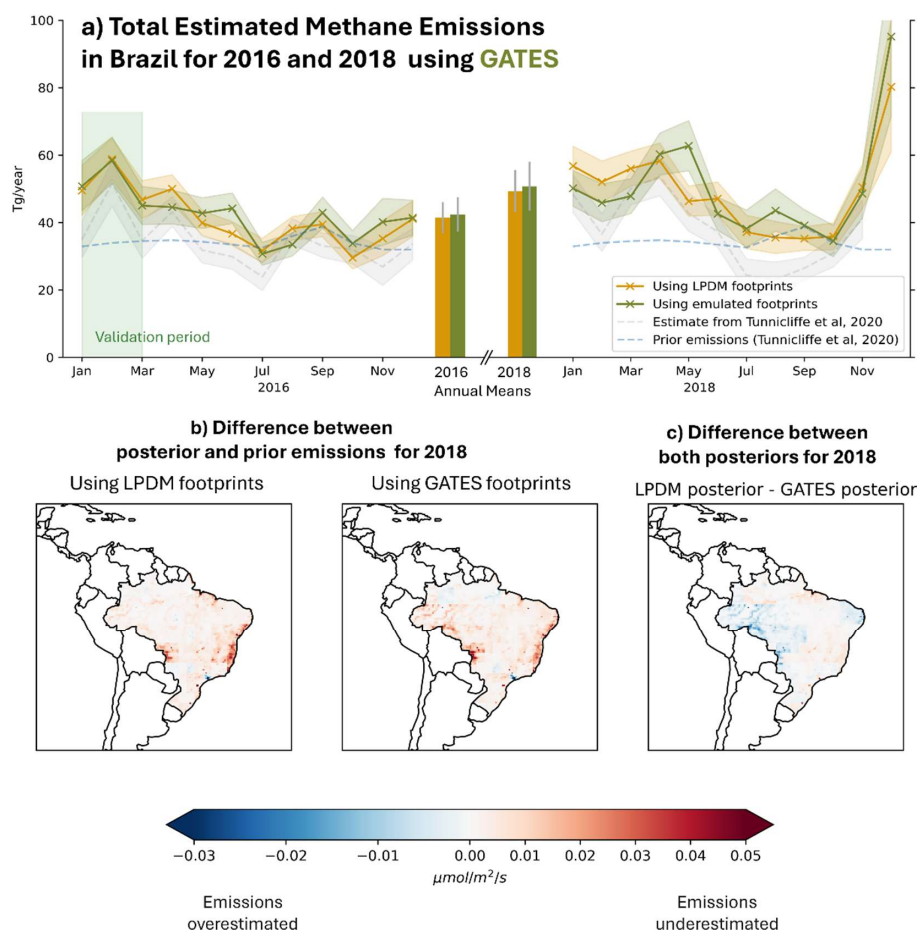
Overall, our flux estimates for Brazil are consistent within **uncertainties** with several previous studies that have used GOSAT and inversions based on LPDMs or Eulerian models (Janardana et al., 2020; Wilson et al., 2021). Whilst within uncertainties, the mean GATES and LPDM estimates are somewhat higher than that of Tunnicliffe et al. (2020). This difference occurs, despite the same satellite observations and LPDM because Tunnicliffe et al. (2020) also incorporated surface data from Ragged Point, Barbados, and used a different inverse method.



| Year                       | Mean yearly emissions ( $Tg\ yr^{-1}$ ) |                          | MAE ( $Tg$ )<br><i>For the monthly timeseries</i> | Mean Bias ( $Tg$ ) |
|----------------------------|-----------------------------------------|--------------------------|---------------------------------------------------|--------------------|
|                            | With LPDM<br>footprints                 | With GATES<br>footprints |                                                   |                    |
| 2016<br>(full year)        | $41.4 \pm 4.6$                          | $42.4 \pm 5$             | 3.17                                              | 0.94               |
| 2016<br>(test months only) | $38.0 \pm 4$                            | $39.3 \pm 4.6$           | 3.84                                              | 1.35               |
| 2018                       | $49.3 \pm 6$                            | $52.7 \pm 7.0$           | 6.26                                              | 1.44               |
| 2018<br>(excluding Dec)    | $46.5 \pm 5$                            | $46.7 \pm 5.7$           | 5.47                                              | 0.22               |

400 **Table 3 – Mean yearly methane emissions for Brazil in 2016 and 2018, estimated using the LPDM footprints and GATES emulated footprints, and mean errors between the two monthly timeseries.** We show that the Mean Absolute Error for the monthly timeseries is comparable to the uncertainty in the yearly estimates. Results are displayed for the full 2016 (Jan-Dec), the 2016 test set (April-Dec), the full 2018, and 2018 excluding Dec. December 2018 has <100 valid observations, and therefore the inferred emissions have very high uncertainties which is reflected in the annual mean. This month was also excluded from the analysis conducted by Tunnicliffe et al. (2020).

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**Fig. 3. Deriving methane emissions for Brazil, in time (top panel) and space (bottom panels).** (a) Estimated methane emissions, for 2016 and 2018. We compare the emissions estimates derived in an inversion using the LPDM footprints (yellow) with those emulated by GATES (green). The emissions inferred with the emulated footprints are well within the posterior inversion uncertainty of the emissions inferred with the traditional method. Note that we report the annual means (bars at the center of the plot) for the full 2016 (i.e. including the validation set January-March) to allow for like-for-like comparisons with 2018. We also show the monthly priors used by (Tunncliffe et al., 2020) and their derived emissions. (b) Difference between the inversion posterior and prior fluxes for 2018, using the LPDM footprints (left) and the GATES footprints (right). The difference highlights the areas that were underestimated or overestimated in the initial estimate. (c) Difference between the two posteriors for 2018. Blue shows the areas where the GATES posterior estimates higher emissions than the LPDM posterior, and red shows the opposite.



## 6 Discussion and Conclusions

We present GATES, a novel ML-driven approach to emulating LPDM footprints using graph neural networks. We demonstrate its use as a stand-alone application, but most importantly within the primary intended workflow, to infer GHG emissions using satellite mole fraction observations. The high consistency of the estimates of Brazil's methane emissions from the ML-enabled pipeline with those based on the physical model, at a fraction of the computational cost ( $>1000$  times faster), demonstrate the potential of this emulator to accelerate greenhouse gas estimations ~~evaluation~~.

One of the main limitations of GATES, as identified for similar GNNs in weather applications (Lam et al., 2023), is that the outputs tend to be smoother than the LPDM footprints. This is likely due to the use of an MSE-based loss function, which encourages less variance in the outputs rather than accurately reproducing fine-scale spatial details, particularly in areas of higher uncertainty. This effect can be observed in Fig. 2, especially in the second footprint, where the predicted plume is in the correct region and direction, but is broader than that of the LPDM. Smoother footprints may lead to higher inference errors in regions of more point-like sources, such as cities or oil and gas infrastructure (see Fig. S6).

Alternative architectures may help to improve future versions of GATES. GATES is a deterministic model, generating a single footprint for a set of inputs, whereas LPDMs are inherently probabilistic. This difference contributes to the smoothing effect, as GATES tends to predict an average outcome rather than generating multiple plausible outputs. Incorporating probability into the emulation would likely produce sharper outputs and contribute to a more rigorous quantification of uncertainty. Understanding uncertainty would also improve explainability, highlighting the areas where the model presents more variance. Further improvements to the architecture of the model could also increase its predicting capabilities, e.g. by integrating multi-meshes like (Lam et al., 2023) to capture dispersion at different scales, or adaptive mesh refinement (Pfaff et al., 2020) to encourage higher resolution predictions only around the footprint, or in complex geographies.

Here, we show GATES in application, using GOSAT data to infer emissions from Brazil, but we expect that it could be readily extended to other regions and instruments. As there are only minimal differences in the setup of LPDM simulations for retrievals of similar short-wave infrared satellites, GATES should also be readily applicable to several existing and upcoming mapping satellites (e.g., MethaneSat, TROPOMI, CO2M). The growing volume of space-based GHG measurements offers vast opportunities for improving emissions estimates. As these datasets continue to expand, ML approaches like GATES provide a promising avenue to leverage this data more efficiently, enhancing global efforts in tracking emissions at increasing temporal and spatial scales and with reduced latency.

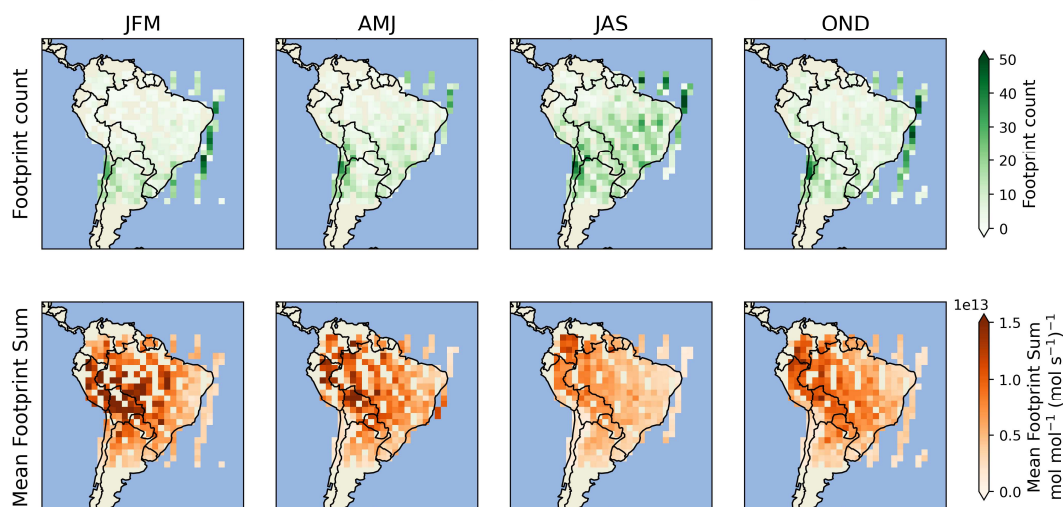


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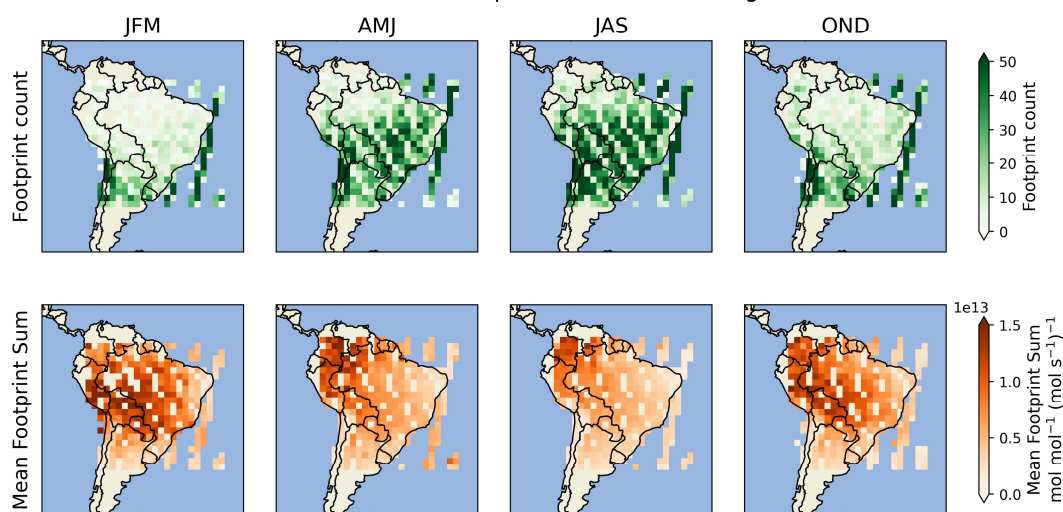
## Appendices

### Appendix A

Distribution of the data in space and time - Training Data



Distribution of the data in space and time - Testing data



455



**Fig. A1. Distribution in space and by season (see key below) of the footprint datasets, split in training (2014-2015, top panel) and validation and testing (2016 and 2018, bottom panel).** For each dataset, the count of samples in each  $2^\circ$  bin (**top subpanel**, green) shows seasonal variations in the data available, with more coverage in July-August-September, as well as spatial biases, with more observations in the southern regions and over the Atlantic. Note that although we train with footprints over the ocean, in the inversion only land observations are used, and we report metrics for those. **The bottom subpanels** show the mean sum of the footprints in that bin, over the spatial domain (the sensitivity in each grid cell is weighted by the area). Higher mean footprint sums indicate less particle dispersion, often due to slower winds or geographical barriers. For example, mean sums are higher near the Andes, where the high topography prevents the particles from advecting. (Key: JFM = January, February, March, AMJ = April, May, June, JAS = June, July, August, OND = October, November, December)



## Appendix B: Evaluation metrics

We use the metrics below to evaluate the model, where  $b_i$  is the true value and  $\hat{b}_i$  is the emulated value.

### 1. Pearson's Correlation Coefficient

$$r(\mathbf{b}, \hat{\mathbf{b}}) = \frac{\sum_{i=1}^n (b_i - \bar{b})(\hat{b}_i - \bar{\hat{b}})}{\sqrt{\sum_{i=1}^n (b_i - \bar{b})^2} \sqrt{\sum_{i=1}^n (\hat{b}_i - \bar{\hat{b}})^2}}$$

The correlation coefficient can be applied to the data in the native dataspace, or in the logged dataspace  $\left(r\left(\log(\mathbf{b}), \log(\hat{\mathbf{b}})\right)\right)$ .

### 2. Intersection Over Union, where B is a binary version of $\mathbf{b}$ ( $B_{i,j}=1$ if $\mathbf{b}_{i,j}>0$ , otherwise $B_{i,j}=0$ )

$$\text{IoU}(\mathbf{B}, \hat{\mathbf{B}}) = \frac{|\mathbf{B} \cap \hat{\mathbf{B}}|}{|\mathbf{B} \cup \hat{\mathbf{B}}|}$$

### 3. Mean Absolute Error

$$\text{MAE}(\mathbf{b}, \hat{\mathbf{b}}) = \frac{1}{n} \sum_{i=1}^n |b_i - \hat{b}_i|$$

### 4. Mean Squared Error

$$\text{MSE}(\mathbf{b}, \hat{\mathbf{b}}) = \frac{1}{n} \sum_{i=1}^n (b_i - \hat{b}_i)^2$$

### 5. RMSE

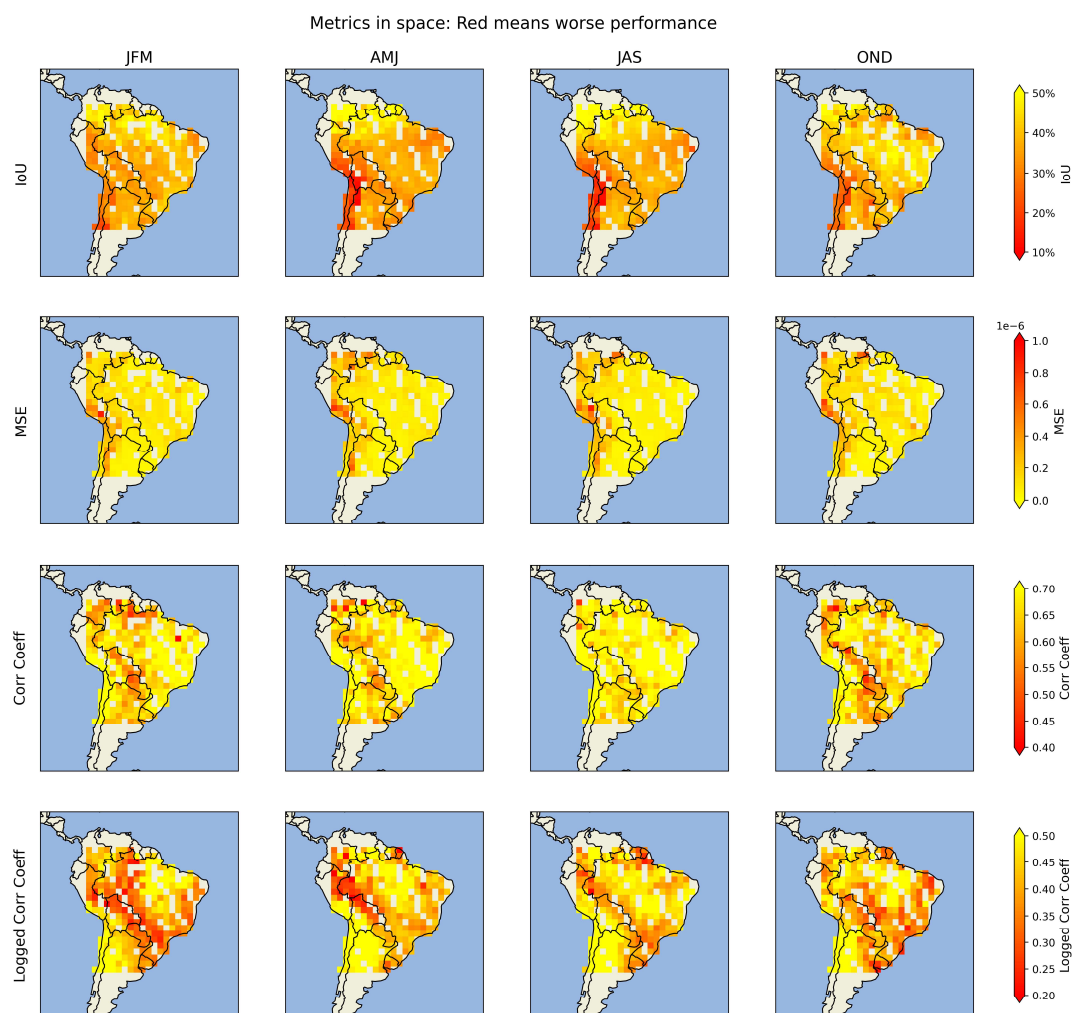
$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (b_i - \hat{b}_i)^2}$$

### 6. Mean Bias

$$\text{MBE}(\mathbf{b}, \hat{\mathbf{b}}) = \frac{1}{n} \sum_{i=1}^n (\hat{b}_i - b_i)$$



## Appendix C



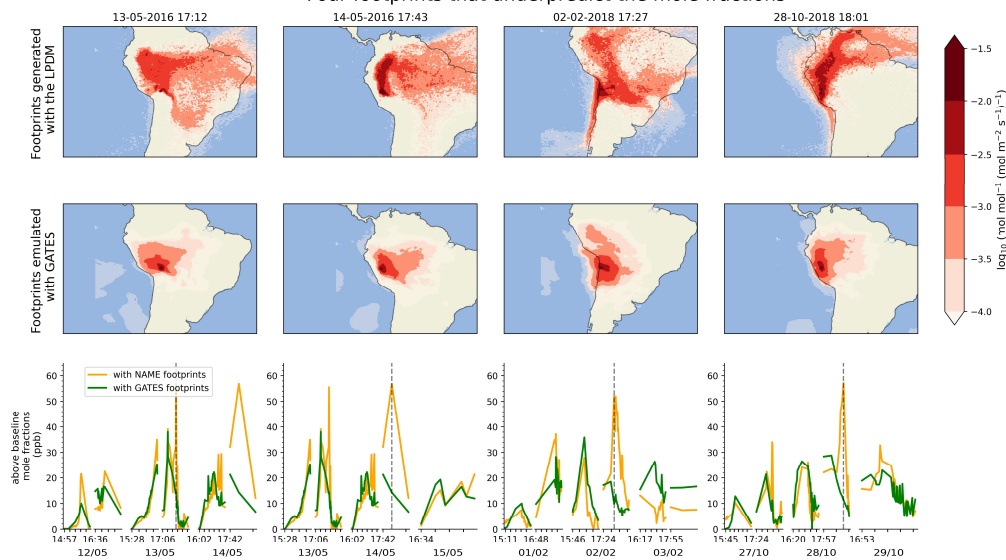
**Fig. C1. – Mean footprint metric scores disaggregated in space and time. Red indicates worse performance for that metric.** The footprints are binned by season (see key below) and by the coordinates of the satellite measurements in 2° bins, showing here the mean metrics for each bin in 2016 and 2018. (Key: JFM = January, February, March, AMJ = April, May, June, JAS = June, July, August, OND = October, November, December)



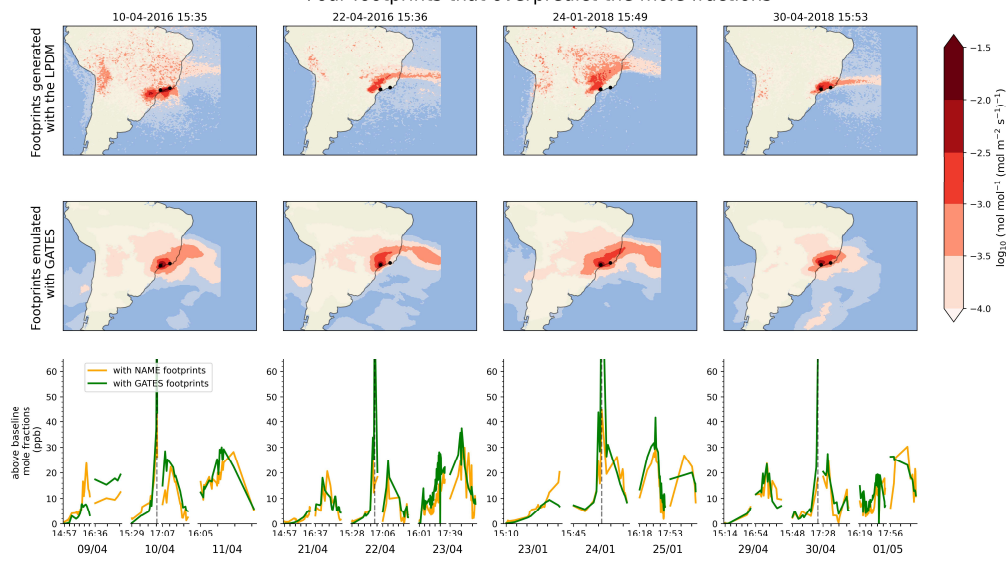
## Appendix D

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Four footprints that underpredict the mole fractions



Four footprints that overpredict the mole fractions





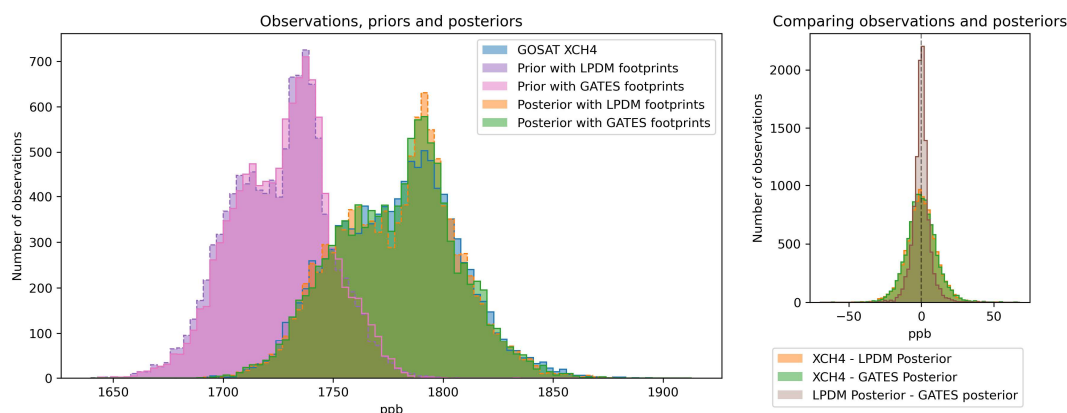
500 **Fig. D1. Two sets of footprints that lead to the largest errors in the emulated mole fractions, through underprediction (top panel) or overprediction (bottom panel).** In each panel, we show the LPDM footprint (top row), the GATES-emulated footprint (bottom row) and the derived mole-fraction timeseries, for the day of the footprint, the day before and the day after. **Top panel:** Footprints for measurements near the central Andes area accumulate higher errors than other areas (see figure C1), and for these four footprints GATES fails to emulate complex dispersion patterns from difficult meteorology and topography. The LDPM footprints capture dispersion over the Amazon basin, where  
505 estimated emissions are large, leading to a big difference between the two estimates. **Bottom panel:** The smoothing effect is particularly visible here, as sharp, narrow plumes in the LPDM footprints over or near Sao Paulo and Rio de Janeiro (black dots) are emulated to be wider and with softer edges. When convolved with the prior, the large emissions from the cities inflate the small errors in the GATES footprints, leading to overpredictions.



## 510 Appendix E: Comparing observations and posteriors

The LPDM footprints used here quantify the contribution of local emissions (i.e. from within the domain) to the modelled methane measurement. The sensitivity of the methane concentrations to contributions from outside the LPDM domain, called the a priori background mole fraction, is calculated using the ECMWF CAMS reanalysis database (Inness et al., 2019), convolved with a matrix of boundary sensitivities also produced using NAME. The inversion algorithm adjusts both the fluxes within the domain and the background concentrations so that there is a better fit between the modelled and the observed measurements.

The emissions derived from the inversion can be compared against the actual observations taken by GOSAT. In Fig. E1 (left panel), we show the distribution of prior modelled mole fractions (i.e. footprints  $\times$  prior fluxes + prior background) for 2018, calculated with the GATES footprints and the LPDM footprints. We also show the distribution of GOSAT XCH4 observations, and the posterior modelled mole fractions (i.e. footprints  $\times$  posterior fluxes + posterior background) derived with either set of footprints. Both posteriors fit the observations significantly better than the priors, with most of the improvement attributed to an increase in the background mole fractions. (Tunnicliffe et al., 2020) and (Thompson et al., 2025) also identify that adjusting the boundary together with the fluxes is key to obtaining well-fitting posteriors. The posteriors derived with either set of footprints are very similar, and show similar error distributions when compared to the observations (Fig. E1, right panel). The prior derived with GATES has a small bias to overpredict mole fractions, which translates into a small bias in the posteriors.



**Fig. E1.** Comparing the distributions of the GOSAT observations, prior and posterior mole fractions in 2018. **Left panel:** Distributions for a priori modelled methane mole fractions (purple and pink), GOSAT XCH4 observations (blue) and the posterior mole fractions (orange and green). We show the prior and posterior pair generated with the LPDM footprints (purple and orange respectively, dashed edges) and the posterior and prior pair generated with the GATES footprints (purple and green respectively, solid edges). Both posteriors fit the observations well. **Right panel:** Distribution of errors between the XCH4 observations and the mole fractions calculated from both sets of posteriors (in orange and green), and differences between the mole fractions derived with both posteriors (brown). Both posteriors show similar error patterns between the estimated emissions and the actual XCH4 observations. The errors between the two posteriors (brown) are normally distributed, with a small positive mean bias (2.69 ppb) which indicates a small overpredicting tendency in GATES.



### Code and data availability

The code used to implement, train and evaluate GATES will be made released as a free access, documented repository (currently available as a private repository [https://github.com/elenafillo/graphnet\\_LPDM\\_emulator](https://github.com/elenafillo/graphnet_LPDM_emulator), available under request for review). The trained model assessed above, together with a sample dataset for inference, will be also made available. The NAME III v7.2 transport model is available from the UK Met Office under license by contacting [enquiries@metoffice.gov.uk](mailto:enquiries@metoffice.gov.uk). A sample of the LPDM footprints generated with NAME can be found at (Fillola and Tunnicliffe, 2025). The UM meteorology in its original format is publicly available, hosted by the UK Centre for Environmental Data Analysis (CEDA) Archive, from July 2015 at [https://data.ceda.ac.uk/badc/name\\_nwp/data/global](https://data.ceda.ac.uk/badc/name_nwp/data/global) (Met Office, 2025a, b) under a UK Open Government Licence 3.0. Earlier dates are available on request from the Met Office. The meteorology can be extracted from its original format with the code at [https://github.com/elenafillo/extract\\_iris\\_met](https://github.com/elenafillo/extract_iris_met) (this code is currently being packaged and will be released as a Zenodo dataset with a DOI before publication). The software used for the inversion can be found at DOI <https://doi.org/10.5281/zenodo.6834888> (Rigby et al., 2022). The GOSAT XCH4 retrievals are located at <https://dx.doi.org/10.5285/18ef8247f52a4cb6a14013f8235cc1eb> (Parker et al., 2020).

### Author contribution

Conceptualization: EF, MR, RSR  
Methodology: EF, MR, RSR  
Investigation: EF  
Software: EF  
Data curation: EF, RT  
Visualization: EF  
Supervision: MR, RSR  
Writing – original draft: EF  
Writing – review & editing: EF, RSR, RT, JNC, NK, AG, MR

### Competing interests

The authors declare that they have no conflict of interest.

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