



# Using NO<sub>x</sub> as quantitative fossil fuel CO<sub>2</sub> proxy in urban areas: challenges and benefits

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**Abstract.** Continuously monitoring local excess fossil fuel CO<sub>2</sub> concentrations remains challenging due to the absence of accurate, continuous <sup>14</sup>CO<sub>2</sub> measurements. Continuous estimates of fossil fuel CO<sub>2</sub> (ffCO<sub>2</sub>) are made by observing continuously measurable proxies that are co-emitted during fossil fuel combustion. This paper investigates the potential and challenges of using in situ NO<sub>x</sub> observations in urban areas to quantitatively estimate hourly ffCO<sub>2</sub> concentration enhancements, using observations at the ICOS pilot station in Heidelberg, Germany. The short atmospheric lifetime of NO<sub>x</sub> limits the use of the observed signal to a local area. Thus, a local background for NO<sub>x</sub> and ffCO<sub>2</sub> was approximated using the Stochastic Time-Inverted Lagrangian Transport (STILT) model and bottom-up emission estimates from the Netherlands Organisation for Applied Scientific Research (TNO). Using <sup>14</sup>CO<sub>2</sub> data from 185 hourly integrated flask samples between 2020 and 2021, mean ratios of local excess NO<sub>x</sub> (ΔNO<sub>x</sub>) to local excess ffCO<sub>2</sub> (ΔffCO<sub>2</sub>) concentrations of 1.40 ppb ppm<sup>-1</sup> for winter and 2.12 ppb ppm<sup>-1</sup> for summer were calculated. These ratios were applied to the ΔNO<sub>x</sub> time series to construct continuous ΔffCO<sub>2</sub> estimates. The uncertainty of the ΔNO<sub>x</sub>-based ΔffCO<sub>2</sub> record was estimated at 3.94 ppm. Comparisons with <sup>14</sup>CO<sub>2</sub>-based and ΔCO-based ΔffCO<sub>2</sub> estimates showed good agreement, while still demonstrating distinct behaviour for individual events. ΔNO<sub>x</sub> shows considerable potential as proxy for ΔffCO<sub>2</sub> and as useful addition to ΔCO-based estimates, as both proxies have different footprints due to their lifetimes. A key challenge remains in reliably determining the seasonal and diurnal cycle of average ΔNO<sub>x</sub> to ΔffCO<sub>2</sub> ratios.

## 1 Introduction

To derive top-down estimates of anthropogenic CO<sub>2</sub> emissions due to fossil fuel combustion from atmospheric concentration measurements, it is necessary to separate the recently added biospheric and fossil fuel CO<sub>2</sub> (ffCO<sub>2</sub>) signal (Ciais et al., 2015). The most direct method to derive these excess fossil fuel CO<sub>2</sub> concentrations (ΔffCO<sub>2</sub>, the term "excess concentration" is used to describe an enhancement of the measured concentration above a given background level) is by utilising <sup>14</sup>CO<sub>2</sub> measurements compared to a background site (Levin et al., 2003; Turnbull et al., 2006). However, at present, optical methods for continuous



$^{14}\text{C}$  measurements are just developing (Ling et al., 2025), and existing methods like accelerator mass spectrometry (AMS) and low level counting (LLC) work only on discrete samples and are labour intensive ~~as well as costly~~. Continuously measured species that are co-emitted in combustion processes, such as CO or  $\text{NO}_x$ , are a possible alternative for deriving high temporal resolution  $\text{ffCO}_2$  estimates (Turnbull et al., 2006; Levin and Karstens, 2007; Van Der Laan et al., 2010; Maier et al., 2024a). These have the advantage of lower-cost continuous measurements, are in part (CO and  $\text{NO}_2$ ) observable by satellite (Konovalov et al., 2016), and in urban areas can even outperform sparsely collected  $^{14}\text{C}$ -based estimates in inversion modelling (Maier et al., 2024b). However, they require adequate knowledge about the ratio of excess proxy concentrations to  $\Delta\text{ffCO}_2$ .

CO has already been widely studied as a proxy for  $\Delta\text{ffCO}_2$  (Gamnitzer et al., 2006; Levin and Karstens, 2007; Turnbull et al., 2015; Maier et al., 2024a). Using  $\text{NO}_x$  as a proxy has been the subject of considerably less study, with the majority of research conducted using satellite data and ratios derived from inventories (Lopez et al., 2013; Goldberg et al., 2019; Liu et al., 2020; Feng et al., 2024). A fundamental challenge of both proxies is that CO and  $\text{NO}_x$  emissions depend on fuel type and combustion parameters like e.g. combustion temperature, oxygen supply, and applied emission reduction systems. Accordingly, different emission sectors, like traffic, industry, and residential heating, have different average proxy to  $\text{ffCO}_2$  emission ratios, which also vary within the emission sectors. The use of  $\text{NO}_x$  is accompanied by additional challenges due to its atmospheric chemistry and its relatively short atmospheric lifetime, which is on the order of hours (Beirle, 2004). This implies that atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios can vary by station and reflect the composition of fossil fuel sources present in each station's footprint. These features can also be an advantage, as it gives the  $\text{NO}_x$  signal a more localised nature and generally a low background (Goldberg et al., 2019). Furthermore, the combination of multiple proxies can provide better constraints on fossil fuel emissions and enable attribution of emissions to source sectors (Super et al., 2020; Jaschke, 2021).

This study characterises the potential and challenges of using  $\text{NO}_x$  concentration excesses ( $\Delta\text{NO}_x$ ) from in situ observations as a proxy for  $\Delta\text{ffCO}_2$  in an urban setting, using Heidelberg as an example. As  $\text{NO}_x$  shows a much more localised signal than CO and  $^{14}\text{C}$ , the choice of a suitable and common background for all species is of **paramount** importance. In the absence of a suitable  $\text{NO}_x$  and  $^{14}\text{CO}_2$  measurement station to define a local background, we describe its construction based on forward simulations of European  $\text{NO}_x$  and  $\text{ffCO}_2$  emissions in the Stochastic Time-Inverted Lagrangian Transport model (STILT, Lin et al. (2003)) and discuss the associated additional uncertainties. Following the methodology of Maier et al. (2024a), the ratios of  $\Delta\text{NO}_x$  to  $\Delta\text{ffCO}_2$  concentrations obtained from in situ  $\text{NO}_x$  and flask-based  $^{14}\text{C}$  measurements are then analysed for diurnal and seasonal variation, to determine average atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios. With these,  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates are calculated and benchmarked against  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  estimates to assess the accuracy of the proxy. We investigate what share of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  uncertainty is due to the observation and background uncertainty and what is due to the inherent oversimplification of applying observation-based seasonally averaged  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios. The  $\Delta\text{NO}_x$ -based continuous  $\Delta\text{ffCO}_2$  record is compared to a  $\Delta\text{CO}$ -based record in order to analyse if and how the two proxies differ. Finally, both proxy-based  $\Delta\text{ffCO}_2$  records are compared to an independent  $^{14}\text{CO}_2$ -based  $\Delta\text{ffCO}_2$  record with fortnightly resolution for Heidelberg.



## 2 Methods

### 2.1 Site and data description

Heidelberg is a city with a population of approximately 160,000, situated in the densely populated Upper Rhine Valley in south-western Germany. The measurement site is located in the northern part of the city, within the university campus. The sampling intake for the measurements is located 30 m above ground on the roof of the Institute for Environmental Physics, approximately 100 m from a residential area and a high traffic road, with little traffic directly around the building. Thus, local emissions of CO<sub>2</sub> and NO<sub>x</sub> are predominantly attributable to traffic and residential heating. A combined heat and power station, with a chimney height of 120 m, is situated 500 m to the north of the site, while a cement plant is located approximately 7 km to the south. Moreover, the cities of Mannheim and Ludwigshafen, which are characterised by a high degree of industrialisation, are situated approximately 15 – 20 km to the north-west. These include a large coal-fired power plant and the BASF industrial complex. Furthermore, air masses originating from the southern part of the Rhine Valley frequently affect the station due to the predominant south-westerly winds, which are a consequence of the channelling effect of the Rhine Valley.

Continuous measurements of atmospheric CO<sub>2</sub> and CO concentrations are performed with a Cavity Ring-Down Spectroscopy (CRDS) gas analyser (Picarro G2401). The measurement protocol as well as the calibration are in accordance with the ICOS Atmosphere Station specifications Version 2.0 (ICOS RI, 2020). The data processing is performed via the ICOS Atmosphere Thematic Center (ATC) following Hazan et al. (2016). NO<sub>x</sub> concentrations are measured with an iterative cavity-enhanced DOAS (ICAD) instrument. The ICAD measures absorption spectra and determines *in situ* NO<sub>2</sub> concentration by fitting its characteristic absorption structures. NO<sub>x</sub> is measured by converting NO to NO<sub>2</sub> through the addition of ozone (Horbanski et al., 2019). An ICOS flask sampler is used to collect flask samples integrated over one hour (see Levin et al. (2020) for a description of the sampler). The flow of air into the flasks is controlled by mass flow controllers so that the final sample in the flask approximates a one hour average of the concentrations in the ambient air. The flask samples are measured for CO<sub>2</sub> and CO concentrations at the ICOS Flask and Calibration Laboratory (FCL, <https://www.icos-cal.eu/fcl>) with a gas chromatographic analysis system (GC) (Jordan and Damak, 2023). Subsequently, the CO<sub>2</sub> in the flasks is extracted and graphitized at the Central Radiocarbon Laboratory (CRL, <https://www.icos-cal.eu/crl>; Lux (2018)) for subsequent <sup>14</sup>C analysis with an accelerator mass spectrometer (AMS, Kromer et al. (2013)). Additionally, integrated CO<sub>2</sub> sampling using NaOH solution has been implemented at HEI station since the late 1970s. Fortnightly samples are collected between 19:00 and 7:00 local time and analysed for <sup>14</sup>C at the CRL (Levin et al., 1980; Kromer and Münnich, 1992). In 2013 a second integrated sampling device for afternoon hours between 11:00 and 16:00 was added.

More than 600 flask samples were collected and analysed for <sup>14</sup>C in the years 2019 to 2021, covering a variety of atmospheric situations (Maier, 2023). The flasks were analysed following the same procedure as in Maier et al. (2024a). Accordingly, flasks with a modelled nuclear contamination from <sup>14</sup>CO<sub>2</sub> emissions of nuclear facilities above 2‰ were excluded to avoid high nuclear corrections with uncertainties exceeding typical <sup>14</sup>C uncertainties. NO<sub>x</sub> measurements are available from 18.12.2019 on. Multiple periods of one to four weeks in March, June, July, and October 2020, as well as March and July in 2021, were excluded due to instrument outages or maintenance. NO<sub>x</sub> data is available for 246 of the flask sampling periods. In the following,



all times are given in local time, as we expect this to be better suited than UTC to capture and explain the patterns of human behaviour and diurnal cycles, that affect the emission ratios.

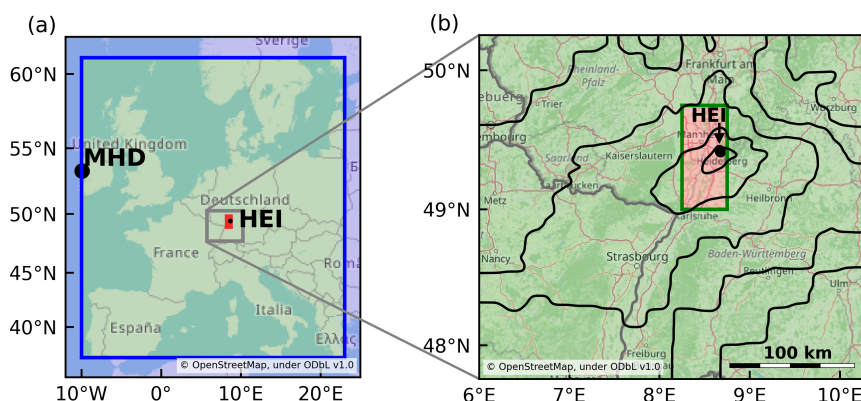
## 90 2.2 Construction of a suitable background

To calculate the excess concentration of a species, the background concentration must be subtracted from the measured concentration. For estimating  $^{14}\text{C}$ - or  $\text{CO}$ -based  $\text{ffCO}_2$  excess concentrations, the marine sector of the ICOS station at Mace Head (MHD), located on the west coast of Ireland, is a suitable choice for assessing European background conditions, due to the prevailing westerlies (Maier et al., 2023, 2024a). Maier et al. (2023) investigated the additional  $\text{ffCO}_2$  uncertainties that arise from the approximation of the European background concentrations based on the clean air sector in MHD and quantified these at 0.28 ppm. However, due to atmospheric chemistry, the lifetime of  $\text{NO}_x$  is on the order of hours (Beirle, 2004), and thus removal of  $\text{NO}_x$  from the atmosphere becomes important on scales larger than the immediate vicinity of the measurement site. This prevents the use of MHD as a  $\text{NO}_x$  background station. Exploiting the co-emission link between  $\text{ffCO}_2$  and  $\text{NO}_x$  requires that the excess concentrations contain information about the same emissions. In order to derive coherent excess concentrations for  $\text{NO}_x$  and  $\text{ffCO}_2$ , allowing to determine local atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  concentration ratios, it is necessary to choose the same background boundary for both species. Otherwise, if the determined  $\text{ffCO}_2$  excess concentrations are influenced by emissions from a larger area than the  $\text{NO}_x$  excess concentrations, the correlation between them would be generally weaker because of the heterogeneous spatial distribution of emissions. This would lead to a higher uncertainty of the derived  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates (see Sect. 2.3). The background boundary should therefore be close enough to the measurement station that, to a first approximation,  $\text{NO}_x$  removal from the atmosphere can be neglected (i.e.  $\text{NO}_x$  can be approximated to be transported as a conservative tracer). At the same time, to ensure a good signal-to-noise ratio, the background boundary should be far enough that the derived excess concentrations still contain most of the measured concentration signal. Thus, balancing these requirements, the location of the background boundary will depend on the  $\text{NO}_x$  lifetime and mean travel time to the station.

To differentiate between the excess concentrations in relation to MHD and in relation to the local background, the following nomenclature will be used: local excess concentrations are indicated by the symbol " $\Delta$ " preceding the species name, whereas excess concentrations relative to MHD are indicated by the abbreviation "ex." in the index. Equation 1 postulates that the measured concentration of a species (e.g.  $\text{NO}_x$ ,  $\text{CO}_2$  or  $^{14}\text{CO}_2$ ) at the station (meas.) is composed of a concentration contribution from the European background  $\text{BG}_{\text{EU/MHD}}$ , a concentration contribution from the European domain  $\text{EU}_{\text{contr.}}$ , and a local concentration contribution  $\Delta\text{species}$ . Figure 1 illustrates the spatial division of the different domains for the case of Heidelberg.

$$115 \text{ meas.} = \text{BG}_{\text{EU/MHD}} + \text{EU}_{\text{contr.}} + \Delta\text{species} = \text{BG}_{\text{EU/MHD}} + \text{species}_{\text{ex.}} \quad (1)$$

For  $\text{NO}_x$  we can expect the contribution from outside Europe to be 0 due to the atmospheric chemistry, and need only subtract the concentration contributions of the European domain from the measured  $\text{NO}_x$  concentrations to obtain  $\Delta\text{NO}_x$  for the local domain, as shown in Eq. (2). For  $^{14}\text{C}$ -based  $\text{ffCO}_2$ , as excess concentrations are derived relative to MHD ( $\text{ffCO}_{2,\text{ex.}}$ ) (Maier et al., 2023), the local excess concentration can also be calculated by subtracting the concentration contributions from



**Figure 1.** Division of the station catchment area into different domains, for the case of HEI, according to Eq. (1): European background  $BG_{MHD/EU}$  (blue shaded area), contribution from the European domain  $EU_{contr.}$  (green shaded area) and local domain  $\Delta_{species}$  (red shaded area). (b) The contour lines illustrate the mean simulated travel time of air masses to HEI for DJF 2019/20. The location of HEI and MHD is indicated.

120 the European domain, as shown in Eq. (3).

$$\Delta NO_x = \text{meas.} - EU_{contr.} \quad (2)$$

$$\Delta ffCO_2 = ffCO_{2,ex.} - EU_{contr.} \quad (3)$$

Thus, while formally the background for the determination of local excess concentrations includes the European background, in the context of this method only the contribution of the European domain needs to be determined. Therefore, in the following, when we refer to the local background, this concerns the contribution from the European domain.

### 2.2.1 Setting the local background boundaries

The atmospheric chemistry of  $NO_x$  involves multiple different processes, with several reactions being dependent on solar radiation, temperature, and concentrations of ozone and radicals (see Kenagy et al. (2018) for an overview). These in turn depend on  $NO_x$  concentrations themselves, thus introducing feedback loops (Valin et al., 2013). Consequently, the lifetime of  $NO_x$  varies considerably with the atmospheric conditions, resulting in significant spatial and temporal variations. Daytime lifetime estimates range from 2 h to 11 h in summer and 18 h to 2 days in winter (Martin et al., 2003; Liu et al., 2016; Romer et al., 2016; Kenagy et al., 2018). Lifetime estimates for Germany have been derived by Beirle et al. (2003) and Beirle (2004). From these, we assume typical  $NO_x$  lifetimes of 6 h for summer, 20 h for winter, and 16 h for the intermediate seasons, with an uncertainty of  $\pm 2h$  for the typical  $NO_x$  lifetimes, based on the range of estimates.

Figure 1 (b) illustrates the spatial distribution of simulated mean travel times to Heidelberg in the Rhine Valley for the winter months (DJF) of 2019/2020. These were simulated with the Stochastic Time-Inverted Lagrangian Transport (STILT) model, driven by meteorological fields from the Weather Research and Forecast (WRF) model (Nehrkorn et al., 2010) with



a horizontal resolution of 2 km. The WRF simulations are based on hourly, 0.25° resolution meteorological fields from the European Centre for Medium-Range Weather Forecast (ECMWF) Reanalysis v5 (ERA5; Hersbach et al. (2020)). The mean winter travel times already exceed 15 h or 20 h at distances of 100 to 200 km. On this timescale, the majority of the emitted NO<sub>x</sub> contribution from the European domain will not contribute significantly to the observations at the station due to its short atmospheric lifetime of a few hours to a day. Therefore, in most meteorological situations, the observed NO<sub>x</sub> concentration only provides information on a close vicinity around the station.

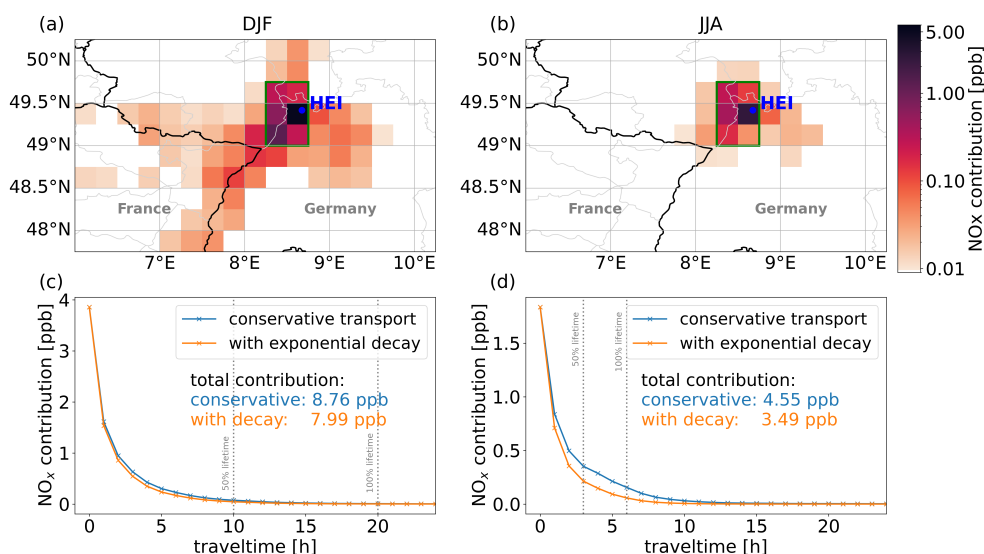
For the determination of the location of the local background boundaries, the WRF-STILT model was used to calculate time-resolved (hourly) and gridded footprints (with a horizontal resolution of ca. 1 km) for the HEI observation site within the Rhine Valley domain (47.75° N to 50.25° N and 6° E to 10.25° E indicated as grey rectangle in Fig. 1 (a)). These footprints describe the sensitivity of the HEI observation site on upwind surface fluxes within the Rhine Valley. They have been simulated by releasing 100 particles per hour from the Heidelberg site and calculating the particle trajectories backward in time. The footprints are mapped with high-resolution NO<sub>x</sub> and ffCO<sub>2</sub> fluxes from the TNO inventory (Dellaert et al., 2019; Denier van der Gon et al., 2019) to get the NO<sub>x</sub> (and ffCO<sub>2</sub>) contribution from each grid cell. The simulations incorporate the most basic atmospheric NO<sub>x</sub> chemistry through an exponential lifetime approach. The time-resolved and gridded footprints were multiplied by a factor  $e^{-\frac{T}{\lambda}}$ , where T is the travel time of the air mass and  $\lambda$  is the assumed atmospheric lifetime of NO<sub>x</sub>, to describe the atmospheric decay of NO<sub>x</sub> along the footprint.

Each grid cell contributes a specific share of the total simulated NO<sub>x</sub> concentration for HEI, which depends on the emission of that grid cell, the sensitivity of the footprint to the grid cell, and the travel time from the grid cell to the station. This is referred to as the NO<sub>x</sub> contribution of that grid cell, with the sum of all contributions being equal to the total simulated NO<sub>x</sub> concentration. We analysed the spatial distribution of the NO<sub>x</sub> contributions for HEI to identify a suitable location of the local background. For the mean simulated NO<sub>x</sub> contributions shown in Fig. 2 (a) & (b), the NO<sub>x</sub> contribution maps of the high-resolution domain were aggregated to a coarser resolution of 0.25°, which is used for simulating the European contributions (see Sect. 2.2.2).

The Heidelberg grid cell and the ones directly surrounding it have by far the highest NO<sub>x</sub> contributions. Therefore, the boundary for the background was chosen as indicated by the green border in Fig. 2 (a) and (b) (49° N, 49.75° N, 8.25° E and 8.75° E), encompassing six grid cells next to Heidelberg to cover most NO<sub>x</sub> contributions while still considering modest travel times. The domain defined by these boundaries will subsequently be referred to as the "local" domain and extends about 30 km to the West of HEI and about 40 km to the North and the South. The domain between these boundaries and the European background is referred to as the "European" domain. In summer (JJA) 86.1% of the simulated NO<sub>x</sub> contributions from the Rhine Valley (79.5% for ffCO<sub>2</sub>) originate from within the local domain and in winter (DJF) 77.8% (80.8% for ffCO<sub>2</sub>). Thus, the NO<sub>x</sub> and ffCO<sub>2</sub> excess concentrations relative to this background still contain most of the measured signal from the Rhine Valley.

To further investigate NO<sub>x</sub> contributions with respect to the air mass travelling times within the local domain, Fig. 2 (c) and (d) show the winter and summer distributions of the mean NO<sub>x</sub> contributions, with and without the exponential decay, based on simulations of the high-resolution model. For the winter months, 99.8% of the NO<sub>x</sub> contributions have a travel time less





**Figure 2.** (a) Mean simulated NO<sub>x</sub> contributions for winter and (b) summer months in 2020 on a 0.25° grid. The blue dot indicates the location of Heidelberg. The green rectangle shows the chosen boundary for the local background. (c) Simulated mean NO<sub>x</sub> contributions from the local domain as a function of their travel time for winter and (d) summer months in 2020. The vertical dotted lines indicate 50% and 100% of the lifetime of NO<sub>x</sub>, respectively. The results as for a conservative transport without decay are displayed in blue. The results obtained with the exponential decay applied are shown in orange.

than the typical NO<sub>x</sub> winter lifetime and 98% have a travel time less than half of it. In the summer months, this is still true for 97.1% and 86.7% respectively. The difference between the NO<sub>x</sub> concentrations simulated with and without the exponential decay shows that assuming conservative transport within the local domain introduces a bias on the order of 1 ppb (0.77 ppb for winter, 1.06 ppb for summer). The assumption of conservative transport leads to an underestimation of ~ 10% on the average winter NO<sub>x</sub> signal of 8.76 ppb and a more significant underestimation of ~ 25% on the average summer signal of 4.55 ppb. For winter, the overall underestimation and travel times are small enough that the assumption of conservative transport is deemed acceptable. For summer however, travel times are of the same order as the atmospheric lifetime, resulting in a significant underestimation. The effects of this are discussed in Sect. 2.3.

### 2.2.2 Determination of the local background concentrations

To calculate the local background concentrations, the STILT model was driven with coarser, 0.25° resolution meteorological fields from the ECMWF Integrated Forecasting System (IFS). Again, 100 particles were released each hour from the HEI site and their back-trajectories were calculated for 10 days or until they left the European model domain (32° N to 74° N, 16° W to 36° E). The resulting footprints are mapped with European NO<sub>x</sub> and ffCO<sub>2</sub> emissions from TNO, but with the emissions



inside the local domain set to 0, so that only emissions from the European domain were propagated to the HEI station. Due to the seasonal change in  $\text{NO}_x$  lifetime, the model was run three times with  $\text{NO}_x$  lifetimes of 6, 16, and 20 h to produce hourly resolved background concentrations for summer, spring/autumn, and winter respectively. Season changes were assigned based on the temperatures observed at the station: months with mean temperatures below  $10^\circ\text{C}$  were assigned as winter, months with  
190 over  $19^\circ\text{C}$  as summer, and the remaining months as spring/autumn.

Previous studies revealed that the STILT and TNO modelling framework shows a remarkable capability to model synoptic concentration changes for HEI station (Maier et al., 2022). However, the STILT model and the TNO emission inventory are imperfect and subject to uncertainties, thus the timing and the absolute value of the modelled local background concentrations should not be considered accurate on the hourly timescale. Thus, a rolling Gaussian smooth was applied on the modelled local  
195 background concentrations with a window size of 24 h and standard deviation of 3 h.

Figure 3 displays an example week, showing the modelled local background concentration time series, i.e. the contribution from the European domain and the measured concentrations for  $\text{ffCO}_2$  and  $\text{NO}_x$ . The modelled local background concentrations are predominantly lower than the measured concentrations. Comparing the two shows different situations with varying influence from the local domain (excess between measured data and local background). In a few cases the simulated back-  
200 ground concentrations do exceed the real measurements, resulting in negative local excess concentrations, but only for 1.7%, with only 0.1% outside a  $1\sigma$  range from 0 ppb. The average simulated contributions from the European domain for 2020 and 2021 were 1.49 ppb for  $\text{NO}_x$  and 2.93 ppm for  $\text{ffCO}_2$ , with standard deviations of 1.5 ppb and 2.8 ppm respectively. This corresponds on average to approximately 10% of the total measured  $\text{NO}_x$  concentration and 25% of the  $\text{ffCO}_{2, \text{ex}}$  concentration calculated from  $^{14}\text{CO}_2$  measurements.

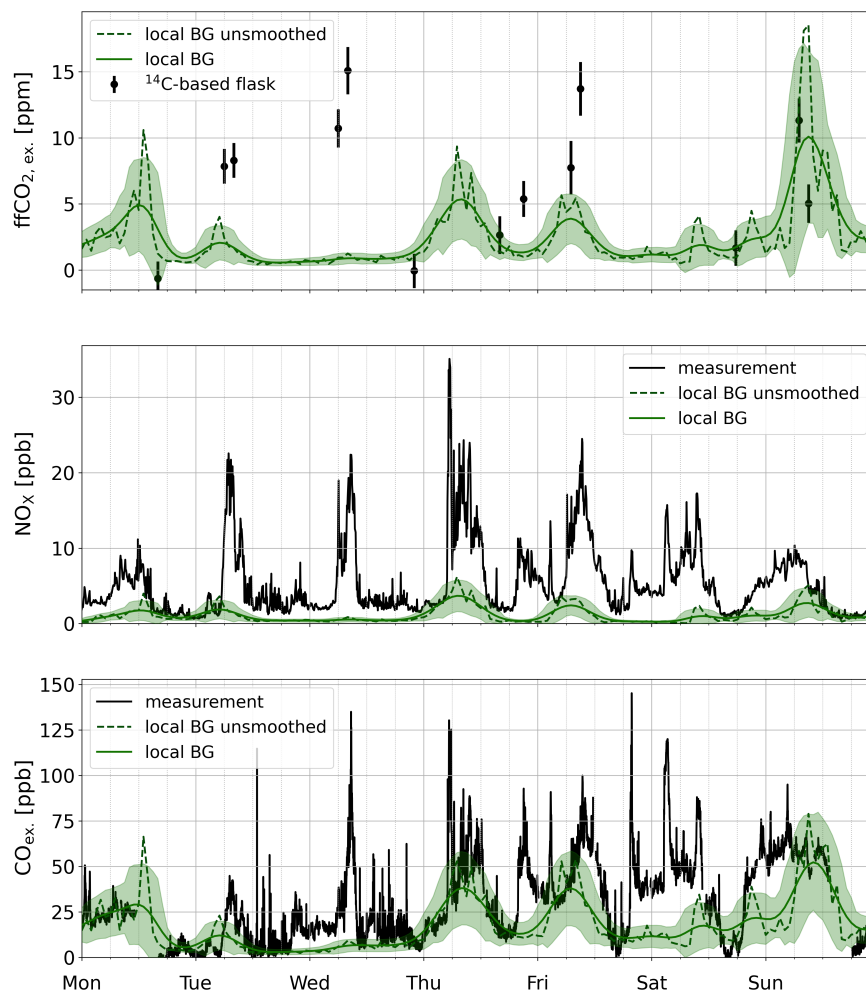
### 205 2.2.3 Assessing the uncertainty of the local background concentrations

The additional uncertainty related to the modelled local background concentration can be separated into three main contributions: the uncertainties of the emissions from the TNO inventory, the errors of the transport model, and the uncertainty of the lifetimes used in the exponential decay.

The uncertainties of the emissions from the TNO inventory were approximated as 40% for  $\text{ffCO}_2$ , 47% for CO and 45% for  
210  $\text{NO}_x$ , based on the uncertainties of the national emissions and their spatial distribution (I. Super, personal communication, based on Super et al. (2024)). Since a relative change of the emissions propagates linearly through the transport model, these relative uncertainties were directly applied to the simulated background to calculate the corresponding emission-related uncertainty.

As an approximation for the errors of the transport model and their impact on the simulated background, the main factor was assumed to be temporal misalignment of the simulated and "true" background. The standard deviation of the unsmoothed data  
215 over a 6 h window was used to assess the possible impact of such a shift and to estimate the corresponding uncertainty. The median of this background uncertainty is about 30% for the modelled  $\text{NO}_x$  and  $\text{ffCO}_2$  concentrations. This time-dependent estimate of transport uncertainty has the advantage of yielding higher uncertainties for periods with strong fluctuations in the simulated concentrations, mirroring the limited reliability of the simulated background concentrations. When averaging over





**Figure 3.** Measured concentrations (in black) and simulated background (in dashed green) from 13.04.2020 until 19.04.2020 for Heidelberg station. The solid green curve shows the background concentrations after the Gaussian smooth, with its  $1\sigma$  confidence interval according to the combined uncertainties from emission-, model transport- and lifetime-uncertainties. Please refer to main text for a detailed explanation. **For the interested reader, CO is also shown here.** (Continuous CO concentrations for MHD were calculated by a NOAA fit (Thoning et al., 1989) through weekly flasks from MHD (Petron et al., 2023).)

longer periods, the temporal misalignment should average out. This contribution to the background uncertainty is therefore  
220 mainly important when looking at individual hours.

To assess the impact of the  $\text{NO}_x$  lifetime uncertainties on the  $\text{NO}_x$  background, the modelled background concentration  $B$  at a certain hour can be regarded as a "mean" air mass with some initial concentration  $E$  and a travel time  $T$ . The dependency of the background concentration  $B$  on the lifetime  $\lambda$  can then directly be described by Eq. 4, where  $c$  is the contribution with



a travel time of 0 h.

225 
$$B = E * \exp(-T/\lambda) + c \quad (4)$$

As the background was simulated for 6, 16, and 20 h lifetimes (and additionally for 18 h and 24 h), the unknown parameters  $E$ ,  $T$  and  $c$  can be determined analytically. The lifetime-dependent change in the modelled  $\text{NO}_x$  concentration can thus be calculated analytically, without running the model. For the assumed uncertainty of 2 h of the seasonally dependent lifetime this yields a lifetime-related background uncertainty of 40% for 6 h, 11% for 16 h, and 7% for 20 h lifetime.

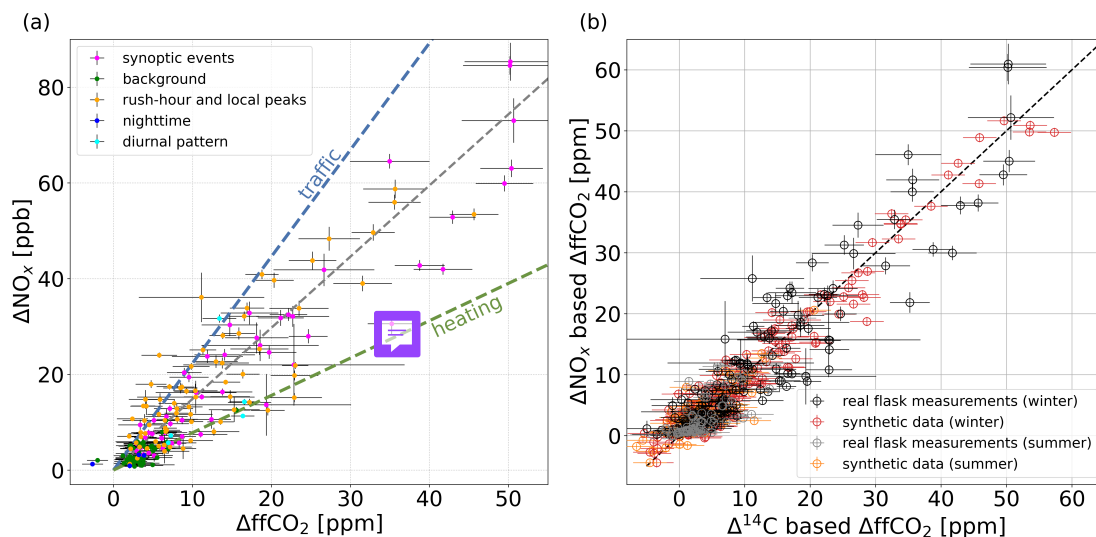
230 Assuming the three uncertainty components are independent, the resulting uncertainties for the simulated background concentrations are on average about 60% for  $\text{NO}_x$  and 50% for  $\text{ffCO}_2$ . They are shown as shaded uncertainty range of the modelled local background concentrations in Fig. 3. The uncertainty analysis of the modelled background concentrations conducted here is incomplete. It could be enhanced through an ensemble approach, utilising alternative transport models, meteorological driver data, and emission inventories. However, this is beyond the scope and intention of this exploratory work. We acknowledge the  
235 inherent limitation of using modelled local background concentrations, while recalling that these account for only 10% of the measured  $\text{NO}_x$  and 25% of the  $\text{ffCO}_2$  signals.

### 2.3 Construction of a $\Delta\text{NO}_x$ -based $\Delta\text{ffCO}_2$ record

To construct continuous hourly  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates, the hourly  $\Delta\text{NO}_x$  record is divided by an average atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio. The local excess concentrations  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$  are determined with respect to the simulated local background  
240 concentration according to Eq. (2) and (3). For each  $^{14}\text{CO}_2$  flask analysis we calculated a  $\text{ffCO}_{2,\text{ex}}$  concentration relative to a marine  $^{14}\text{CO}_2$  background record from MHD using Eq. (3) from Maier et al. (2023), which includes corrections for  $^{14}\text{C}$  contamination from nuclear facilities and biospheric respiration. Please refer to Maier et al. (2023) for more details and for the construction of the marine  $^{14}\text{CO}_2$  background. Following Maier et al. (2024a), a weighted total least-squares regression was applied to determine mean atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios.

245 By design, this method is insensitive to systematic shifts and scaling in the determination of  $\Delta\text{NO}_x$ , as long as the sampled flasks are representative of the conditions at the station. This is because such systematic biases affect the determination of the  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio and the continuous  $\Delta\text{NO}_x$  record on which the ratio is applied in the same way, and therefore cancel each other out in the calculation of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates. However, the statistical variability around a mean bias still has an effect. A mean bias is corrected for by the method, as described above, but the variability of that bias results in an effectively  
250 higher variability in the observed  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios and therefore a higher uncertainty in the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates. This would be, for example, a mean bias caused by  $\text{NO}_x$  removal from the atmosphere in the local domain, with variability due to the variability of atmospheric conditions leading to different levels of removal.

Returning to the underestimation of  $\Delta\text{NO}_x$  in the summer months due to significant removal of  $\text{NO}_x$  from the atmosphere within the local domain (see Sect. 2.2.1), the mean bias caused by this underestimation has no effect on the estimation of  
255  $\Delta\text{ffCO}_2$  as just stated. However, the variability of the underestimation increases the uncertainty of the derived ratio and  $\Delta\text{ffCO}_2$  concentrations. From the concentration contributions simulated with the high resolution model, we estimated this additional



**Figure 4.** (a) Scatter plot of the local  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$  concentrations for all valid flask measurements. The colour of each data point indicates the sampling situation. The dashed grey line represents the weighted total least-squares regression line. The blue and green lines show the average TNO inventory emission ratios for the traffic and heating sector in the vicinity of Heidelberg. (b) Comparison between  $\Delta\text{NO}_x$ - and  $^{14}\text{C}$ -based local  $\Delta\text{ffCO}_2$  concentrations for the summer (grey circles) and winter (black circles) flasks. Synthetic data (red circles for winter data and orange circles for summer data) was generated by assuming a constant summer and winter ratio respectively.

uncertainty for the  $\Delta\text{ffCO}_2$  estimates at approximately 0.4 ppm using a Monte Carlo approach. Given that this is much lower than the typical 1.5 ppm uncertainty of  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  estimates, the choice of background is still deemed appropriate for the **summer months**, although a higher uncertainty for the  $\Delta\text{NO}_x$ -based estimates is to be expected.

## 260 3 Results

### 3.1 $\Delta\text{NO}_x / \Delta\text{ffCO}_2$ ratios from flask samples

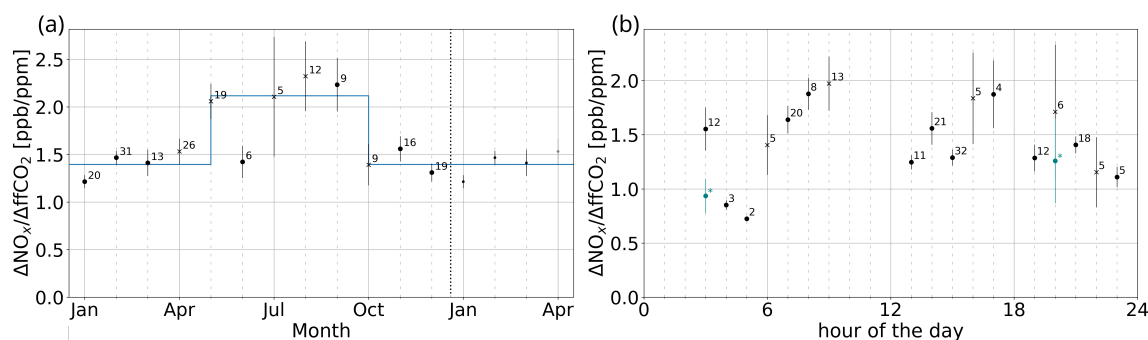
Figure 4 (a) shows the local  $\Delta\text{NO}_x$  enhancements against the  $^{14}\text{C}$ -based local  $\Delta\text{ffCO}_2$  enhancements. The flask samples were collected under a range of different atmospheric conditions and at different times of the day to be representative of the mix of conditions encountered at the station. While there are some very small or negative and some very high ratios, most ratios  
265 fall within the expected range for a mix of traffic and heating emissions for Heidelberg. Flasks with a ratio uncertainty of over 100% were excluded from the determination of the mean  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio (but included in the determination of the uncertainty of the resulting  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates). As outlined in Maier et al. (2024a), an error-weighted regression through the data was used to obtain unbiased estimates of the mean atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios.



The regression over all the flasks collected in 2020 and 2021 yields an average ratio of  $1.49 \pm 0.04$  ppb ppm<sup>-1</sup>, with an  $R^2$  value of 0.84. Due to the temporal changes in atmospheric chemistry and the mix of emissions, a seasonal and diurnal cycle of the atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio is expected. In Fig. 5 monthly and hourly derived atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios are shown. The monthly atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios clearly indicate two different ratios for winter (October to April) and summer (May to September). For all winter samples, the regression yields an average atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio of  $1.40 \pm 0.04$  ppb ppm<sup>-1</sup> with an  $R^2$  value of 0.86, while for all summer samples a higher ratio of  $2.12 \pm 0.13$  ppb ppm<sup>-1</sup> with an  $R^2$  value of 0.55 is found. The weaker correlation for the summer flasks is related to the overall smaller signal strength; if for the winter period only flasks in the same concentration range as the summer period ( $\Delta\text{ffCO}_2 < 19$  ppm) would be used, the  $R^2$  value would drop to 0.63.

Dividing the samples into summer and winter retains a sufficient number of samples per season, ensuring the regression remains resilient against non-representative ratios obtained from single flasks. However, if only a small number of flasks are available, for example in June where only background conditions were sampled or for specific hours of the day, the regression can be heavily biased by a single observation with a non-representative ratio (see Fig. 5). Therefore, we refrained from deducing a diurnal cycle even though a certain structure is visible.

The data was also analysed for any dependency on wind direction and speed, but no relevant correlation was found.



**Figure 5.** (a) Seasonal cycle with ratios calculated by separate regression for each month. The number next to each data point indicates the number of measurements in that month. Values denoted by a cross instead of a circle have an associated  $R^2$  value of less than 0.5. The blue line illustrates the ratios calculated by two regressions over a summer period from May to September, and a winter period from October to April. (b) Diurnal cycle with ratios calculated by separate regression for each hour of the day. The number indicates the number of measurements in that hour. Values denoted by a cross instead of a circle have an associated  $R^2$  value of less than 0.5. For three hours there is only one flask available, these were therefore excluded from this analysis. For hours 3 and 20 there is a second value shown with a teal coloured circle representing an alternative ratio under exclusion of three flasks from a single synoptic event for hour 3 and one traffic-signal flask for hour 20.

### 3.2 Uncertainty of the $\Delta\text{NO}_x$ -based $\Delta\text{ffCO}_2$ record

Following Maier et al. (2024a), the uncertainty of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates was estimated by comparison to the <sup>14</sup>C-based  $\Delta\text{ffCO}_2$  estimates (see Fig. 4 (b)). A regression through this data unsurprisingly results in a slope of 1, as the flask were



used to derive the average summer and winter ratios. The distribution of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates around the 1:1 line is caused by the uncertainties of the measurements and the background estimation, as well as the neglected spatio-temporal variability of the atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios on sub-seasonal time scales. The root-mean-square-deviation (RMSD) between the  $\Delta\text{NO}_x$ - and  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  can be used to estimate the uncertainty of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record. As the RMSD is  
290 dependent on the range of  $\Delta\text{ffCO}_2$  concentrations, the normalised RMSD (NRMSD) was calculated by dividing the RMSD by the mean  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  concentrations. The (N)RMSD over all flasks is 3.94 ppm (46%), while it is 4.45 ppm (41%) for the winter period and 2.46 ppm (73%) for the summer period.

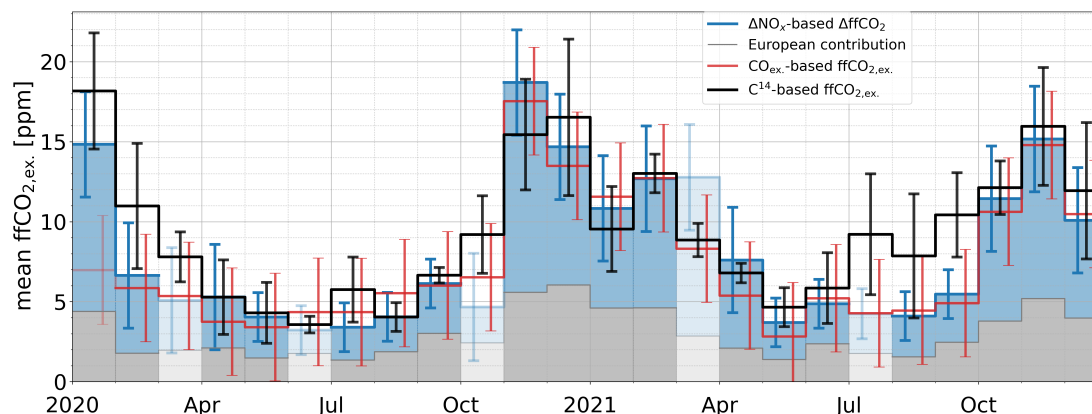
In order to assess which share of this uncertainty can be attributed to the measurement and background uncertainties and how much is due to the neglected variability of the  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios, a synthetic data experiment was performed analogue to  
295 the procedure in Maier et al. (2024a). With this, an uncertainty of 2.65 ppm (31%) over all flasks and 3.00 ppm (28%) or 1.93 ppm (57%) for the winter or summer periods, respectively, can be attributed to the measurement and background uncertainties. Assuming these to be independent of the ratio variability, the uncertainty of the  $\Delta\text{ffCO}_2$  concentrations due to the ratio variability can be estimated through Gaussian error propagation. An uncertainty of 2.91 ppm (34%) over all flasks can therefore be attributed to the ratio variability. This results in an uncertainty of 3.29 ppm (30%) in winter and 1.52 ppm (45%)  
300 in summer.

### 3.3 Comparison with $\text{CO}_{\text{ex}}$ - and $^{14}\text{C}$ -based $\text{ffCO}_{2,\text{ex}}$ records

We compared the constructed  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record with a  $^{14}\text{C}$ -based  $\text{ffCO}_{2,\text{ex}}$  record from fortnightly integrated radiocarbon samples and a  $\text{CO}_{\text{ex}}$ -based  $\text{ffCO}_{2,\text{ex}}$  record to investigate the similarities and differences between the records. Note that the ratio for CO was determined by Maier et al. (2024a) for the years 2019 and 2020 and applied here for the years  
305 2020 and 2021. The integrated radiocarbon samples are completely independent of the flask measurements used to derive the  $\Delta\text{NO}_x/\Delta\text{ffCO}_2$  ratio and therefore allow for a meaningful evaluation of the  $\Delta\text{NO}_x$ -based estimates.

Maier et al. (2024a) estimated an uncertainty of 3.95 ppm (39%) for the  $\text{CO}_{\text{ex}}$ -based  $\text{ffCO}_{2,\text{ex}}$  estimates and attributed 2.07 ppm (20%) to the background and measurement uncertainty. Consequently, an uncertainty of 3.36 ppm (33%) can be attributed to the  $\frac{\text{CO}_{\text{ex}}}{\text{ffCO}_{2,\text{ex}}}$  ratio variability. While the background and measurement uncertainty for the  $\text{CO}_{\text{ex}}$ -based record is  
310 smaller than for the  $\Delta\text{NO}_x$ -based record (even without considering the additional uncertainty of the European domain  $\text{ffCO}_2$  contribution), the relative uncertainty due to the ratio variability is almost identical for both proxies, although for CO no seasonally varying ratio was applied.

Figure 6 shows a comparison of monthly  $\text{ffCO}_{2,\text{ex}}$  means for the years 2020 and 2021. The local  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates and the  $\text{ffCO}_2$  contribution from the European domain are shown as blue and grey columns, which when stacked  
315 together give the composite  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex}}$  estimates relative to MHD. The  $\text{CO}_{\text{ex}}$ - and  $^{14}\text{C}$ -based estimates are shown as red and black lines, respectively. The monthly mean  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex}}$  concentrations are on average about 0.6 ppm higher than the  $\text{CO}_{\text{ex}}$ -based estimates and 1.1 ppm lower than the  $^{14}\text{C}$ -based. The  $\Delta\text{NO}_x$ - and  $\text{CO}_{\text{ex}}$ -based monthly mean  $\text{ffCO}_{2,\text{ex}}$  concentrations generally show a good agreement with each other and with the  $\text{ffCO}_{2,\text{ex}}$  concentrations from the integrated samples. A majority of the higher differences between the records are in months with low data coverage of one proxy



**Figure 6.** Mean monthly  $\text{ffCO}_{2,\text{ex.}}$  concentration estimates for Heidelberg estimated through independent proxies. The grey bars give the  $\text{ffCO}_2$  contribution from the European domain (see Sect. 2.2). Stacked upon this, the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  concentrations are shown in blue. The total height of this column represents the  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex.}}$  estimate relative to MHD. The blue error bars for  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex.}}$  report the uncertainty of the excess concentration relative to MHD, including the uncertainty of the  $\text{ffCO}_2$  background. Mean monthly  $^{14}\text{C}$ -based  $\text{ffCO}_{2,\text{ex.}}$  concentrations based on fortnightly integrated  $^{14}\text{C}$  samples are shown in black with their uncertainties. These were calculated by averaging the  $\text{ffCO}_{2,\text{ex.}}$  from the day and night time integrated  $^{14}\text{C}$  samples (calculated according to the methods described in Maier et al. (2023)), assuming that they represent the day and night halves of the day respectively.  $\text{CO}_{\text{ex.}}$ -based  $\text{ffCO}_{2,\text{ex.}}$  relative to MHD is shown in red with the uncertainty of 3.95 ppm estimated by Maier et al. (2024a). Periods with low data coverage are indicated in transparent. In January 2020, the CO data coverage is only 15%. For  $\text{NO}_x$ , the data coverage is low in March (63%), June (42%) and October (16%) 2020, as well as March (46%) and July (18%) 2021.

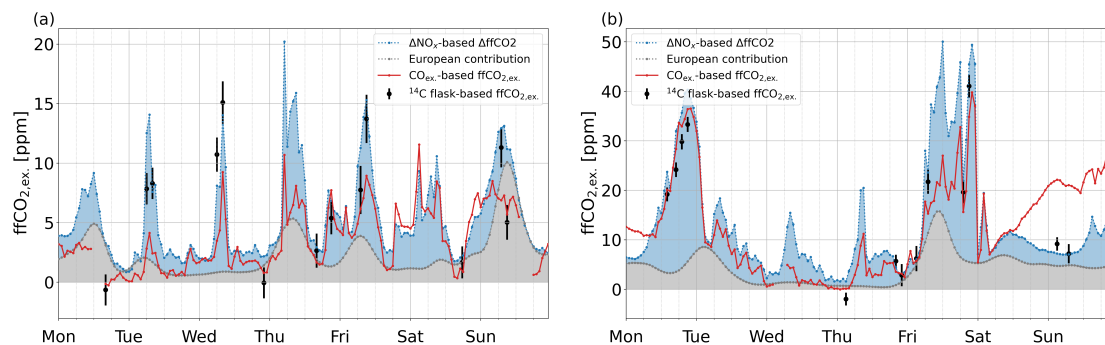
and are overall well within the uncertainties of the records. A more notable discrepancy is observed between the integrated samples and the proxy based records for the months of July through September 2021, which should warrant further investigation into the reasons for this.

Two example weeks of proxy-based  $\text{ffCO}_{2,\text{ex.}}$  estimates are shown in Fig. 7 to further compare the  $\Delta\text{NO}_x$ - and  $\text{CO}_{\text{ex.}}$ -based records. The  $^{14}\text{C}$ -based flask estimates generally agree well with the proxy-based estimates. On average, the  $\text{CO}_{\text{ex.}}$ -based estimates are 0.3 ppm lower than the  $\Delta\text{NO}_x$ -based. The  $\Delta\text{NO}_x$ -based estimates for the rush hour peaks are mostly higher than for the  $\text{CO}_{\text{ex.}}$ -based which is often corroborated by the  $^{14}\text{C}$ -based estimates. On multiple occasions the  $\text{CO}_{\text{ex.}}$  and  $^{14}\text{C}$ -based  $\text{ffCO}_{2,\text{ex.}}$  records reach lower than the  $\Delta\text{NO}_x$ -based record, partly below the modelled contribution from the local background. Figure 7 (b), on the other hand, shows a situation at the end of the week with prevailing winds from the east where the  $\text{CO}_{\text{ex.}}$ -based estimates are substantially higher compared to the  $\Delta\text{NO}_x$ - and  $^{14}\text{C}$ -based. As the  $\text{CO}_{\text{ex.}}$ -based record uses smoothed MHD measurements as background for CO, in the minority of cases where air masses are not originating from the Atlantic, this can lead to an over- or understated background, as illustrated here. At the same time, the constructed local background utilises a smooth over the modelled data, averaging out minima and high peaks. The determination of the  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio accounts





for this on some scale, as it uses the same background. Still, in situations that are not well represented by the available flasks, this can have a relevant impact. For example, on the 13 April 2020, a background problem is obvious, whereby the composite  
335  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex}}$  estimate is substantially higher than the  $\text{CO}_{\text{ex}}$ - and  $^{14}\text{C}$ -based estimates. While the problems of both backgrounds are reflected in their uncertainties, this needs to be considered when analysing individual events.



**Figure 7.** Example weeks of proxy based  $\text{ffCO}_{2,\text{ex}}$  records.  $\text{CO}_{\text{ex}}$ -based excess  $\text{ffCO}_2$  relative to MHD is shown in red. The grey bars give the  $\text{ffCO}_2$  contribution from the European domain. Stacked upon this, the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  concentrations are shown in blue. The total height of this column represents the  $\Delta\text{NO}_x$ -based  $\text{ffCO}_{2,\text{ex}}$  estimate relative to MHD. Additionally, the black data points show  $^{14}\text{C}$ -based  $\text{ffCO}_{2,\text{ex}}$  estimates from flasks. (a) 13.04.2020 - 19.04.2020, (b) 01.02.2021 - 07.02.2021. Note that (a) and (b) have different y scales.

## 4 Discussion

The co-emission of  $\text{NO}_x$  and  $\text{ffCO}_2$  makes  $\Delta\text{NO}_x$  a potential proxy for continuous  $\Delta\text{ffCO}_2$  estimates. The feasibility of such an approach in an urban environment, acknowledging the challenges involved, is demonstrated in our study. The comparison  
340 to two independent  $\text{ffCO}_{2,\text{ex}}$  records shows in general a good agreement with the  $\Delta\text{NO}_x$ -based estimates and validates this approach for the example of Heidelberg. In the following, we critically discuss the benefits and challenges of  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimation.

### 4.1 Challenges of a $\Delta\text{NO}_x$ -based proxy approach

The key challenges of the method lie in determination of coherent  $\text{NO}_x$  and  $\text{ffCO}_2$  excess concentration, i.e. in the determination  
345 of an appropriate background, and the robust determination of atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios with their seasonal and diurnal cycles.

The relatively short atmospheric lifetime of  $\text{NO}_x$  means that the observed  $\text{NO}_x$  concentrations provide information only about the immediate vicinity of the observation station. To utilise the correlation of  $\text{NO}_x$  and  $\text{ffCO}_2$ , it is crucial to ensure that the observed  $\text{NO}_x$  and  $\text{ffCO}_2$  signals pertain to the same catchment area. Therefore, determining an appropriate local  $\text{NO}_x$  and  $\text{ffCO}_2$  background is of paramount importance for the quantitative use of  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates. In an urban context,  
350 this would ideally be accomplished by a measurement network with up- and downwind measurements of  $^{14}\text{CO}_2$  and  $\text{NO}_x$ ,



allowing direct, measurement-based calculation of excess concentrations. As such a network was not available in the case of Heidelberg, the STILT model and TNO emission inventory were used to simulate background concentrations for a region of about 40 km x 80 km around Heidelberg. This required the consideration of the short atmospheric lifetime of  $\text{NO}_x$ , which was taken into account through a very simplistic exponential decay approach, with different lifetimes for each season. Consequently, this model approach introduced additional uncertainties through the uncertainties of the emission inventory, the transport model, and the lifetimes used for the exponential decay of  $\text{NO}_x$ . This is reflected in the higher background uncertainties of 40% for  $\text{NO}_x$  and 30% for  $\text{ffCO}_2$ . As described in Sect. 2.3, the choice of the background per se is not as crucial with regard to its absolute value, because the method used intrinsically accounts for shifts and scaling of the background. However, it is crucial for limiting the analysis to a region where the atmospheric chemistry of  $\text{NO}_x$  still allows for an adequate observation of the correlation between  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$ , which is necessary to obtain low uncertainties. Given that the estimated uncertainties of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates are comparable to those of the  $\text{CO}_{\text{ex}}$ -based estimates, we conclude that the choice of background was sufficient.

The atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios are influenced by the atmospheric chemistry of  $\text{NO}_x$  and the changing shares of emission sectors due to their different emission ratios. This leads to distinct seasonal and diurnal cycles in the atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios (see Fig. 5). The observed cycles generally agree qualitatively with the emission ratios from the inventory. However, we found that for lower numbers of available flasks, average ratios for individual months or hours can be highly influenced by individual flasks and are not necessarily representative, especially in summer. Therefore, only two different ratios for summer at  $2.12 \pm 0.13$  ppb ppm<sup>-1</sup> and winter at  $1.40 \pm 0.04$  ppb ppm<sup>-1</sup> were applied for the estimation of  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$ . These ratios are mostly influenced by the afternoon and rush hour, as more flasks were sampled during these times and these flasks generally measured the highest excess concentrations.

In particular, the neglected diurnal ratio variability should be further investigated, as this is one of the major sources for the overall uncertainty of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record. One possible approach which we tested, would be to take the basic shape of the diurnal cycle from the inventory and fit this to the observed ratios for the individual hours. However, applying this method actually increased the uncertainty of the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates by 50% to 6 ppm. This is not entirely surprising, considering that the inventory describes emission ratios, whereas our method requires mean atmospheric ratios. The difference between these is non trivial, especially at night and in the morning, as this depends on atmospheric conditions and the dynamics of the planetary boundary layer. By restricting this approach to afternoon hours only (11:00 to 16:00), a 2% improvement in the uncertainty can be achieved. Just restricting the original analysis to the afternoon and deriving a mean afternoon ratio already leads to a 3% improvement in the uncertainty. Consequently, a better quantitative determination of the diurnal cycle requires either more radiocarbon measurements for ratio determination, or an advanced atmospheric model to translate the inventory emission ratios into atmospheric concentration ratios, provided that the shape of the diurnal cycle from the inventory is correct.

The summer samples show a lower correlation between  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$ , as well as considerably higher relative uncertainties than the winter. This reflects the lower signal strength in summer and the higher variability due to the shorter



385 atmospheric  $\text{NO}_x$  lifetime compared to winter. Overall, the method is therefore in general strongest on a winter afternoon and much more limited in its significance in summer.

Determining robust  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios also requires a representative data set on which the ratios are determined. The typical range of the continuous  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  estimates (0–20 ppm) is lower than that of the  $^{14}\text{C}$ -based flask estimates (2–35 ppm), suggesting that the flasks used to derive the  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio are not necessarily representative of the complete record. This originates from a sampling bias of the flask samples, which were disproportionately sampled during situations with high  $\text{ffCO}_2$  concentrations and during daytime. In light of the uncertainties of the  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  estimates and the analysis costs, this is still a reasonable sampling approach. However, this should be kept in mind when using and interpreting the  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record.

## 4.2 Benefits of a $\Delta\text{NO}_x$ -based proxy approach

395 Despite all these challenges, the  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$  concentrations show a strong correlation with  $R^2$  values over 0.8, especially in winter. This allows the determination of robust seasonal ratios with relatively small uncertainties. When combined with a more advanced transport and chemistry model, they can provide valuable information for validating emission inventories.

A main cause of the challenges, the short atmospheric lifetime of  $\text{NO}_x$ , is also a reason for a benefit of using  $\Delta\text{NO}_x$  as a  $\Delta\text{ffCO}_2$  proxy due to the local nature of the  $\text{NO}_x$  signal. The  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record relative to the local background combined with the  $\text{CO}_{\text{ex}}$ -based  $\text{ffCO}_{2,\text{ex}}$  record relative to MHD allow the calculation of the local share of  $\text{ffCO}_2$ . As a result of the way in which the  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratio is determined, the distribution of  $\text{ffCO}_2$  into the local signal and background is calibrated by the flasks used for determining the ratio. Consequently, it is largely influenced by the local  $\text{ffCO}_2$  background. In a scenario where a more complex and precise background with sparse temporal resolution is used, e.g. a measured  $^{14}\text{C}$ -based  $\text{ffCO}_2$  background or a highly complex model that is only evaluated for the sample times of the flasks, the above introduced simpler method can be used to effectively upscale the background and determine the local share of  $\text{ffCO}_2$  on a high temporal resolution.

405 Furthermore, the comparison of the  $\Delta\text{NO}_x$ - and  $\text{CO}_{\text{ex}}$ -based records showed that while they generally produce similar records, there are also distinctly different structures for individual events. Where the two proxies show differing  $\text{ffCO}_{2,\text{ex}}$ , no single proxy systematically agrees better with the  $^{14}\text{C}$ -based flask data, highlighting that the two records offer distinct and complementary information. This calls for further studies on inverse modelling of  $\text{ffCO}_2$  emissions with multiple proxies, leveraging the different sensitivities of the proxies to the near and far field and to different emission sectors. This in turn opens up opportunities for spatial and sectoral attribution of emissions.

## 5 Conclusions

$\Delta\text{NO}_x$  shows considerable potential as a proxy for  $\Delta\text{ffCO}_2$  in an urban context, as shown here for the case of Heidelberg. Even with a simple approach to account for its atmospheric chemistry and ratio variability, a strong correlation between  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$  is observed, allowing the construction of a high temporal resolution  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$  record with uncertainties comparable to the use of  $\text{CO}$  as a proxy.



For this, a local background was modelled with the STILT model and TNO emission inventory to derive coherent  $\Delta\text{NO}_x$  and  $\Delta\text{ffCO}_2$  excess concentrations. Two different ratios for summer at  $2.12 \pm 0.13 \text{ ppb ppm}^{-1}$  and winter at  $1.40 \pm 0.04 \text{ ppb ppm}^{-1}$  were obtained through an error-weighted regression and applied to a continuous  $\Delta\text{NO}_x$  record for the estimation of  $\Delta\text{NO}_x$ -based  $\Delta\text{ffCO}_2$ . A comparison with the  $^{14}\text{C}$ -based  $\Delta\text{ffCO}_2$  from the flasks was used to estimate the uncertainty of the  $\Delta\text{NO}_x$ -based estimates at about 4 ppm. Approximately 2.6 ppm could be attributed to the measurement and background uncertainties, while about 3 ppm were attributed to the ratio variability. This is comparable with the uncertainties for  $\text{CO}_{\text{ex}}$ -based estimates in Heidelberg (Maier et al., 2024a). Moreover, the  $\Delta\text{NO}_x$ -based estimates are overall in good agreement with independent  $\text{CO}_{\text{ex}}$ - and fortnightly  $^{14}\text{C}$ -based estimates. Concurrently, they display distinctive structures that indicate a potential information gain from incorporating a  $\Delta\text{NO}_x$ -based record into model simulations. The extent to which the method can be applied to other stations represents an exciting avenue for further research.

One of the key challenges of the method is the short atmospheric lifetime of  $\text{NO}_x$ . This mandates the careful identification of an appropriate, common background to determine the excess concentrations of  $\text{NO}_x$  and  $\text{ffCO}_2$ . The pronounced seasonal and diurnal cycle of atmospheric  $\frac{\Delta\text{NO}_x}{\Delta\text{ffCO}_2}$  ratios necessitates a representative and comprehensive set of flask measurements to ensure its accurate and robust determination. As a consequence, the summer months present a particularly challenging period, given that the lifetime is shortest at this time and the predominantly low signals result in a less favourable signal-to-noise ratio. Urban measurement networks with up- and downwind sampling of  $^{14}\text{CO}_2$  and  $\text{NO}_x$  provide the ideal setup to accommodate these challenges through direct background measurements and short travel times over the city.

In turn, when these challenges are adequately addressed, the short lifetime of  $\text{NO}_x$  can also provide benefits, such as insights into the local share of  $\text{ffCO}_2$ . In conclusion, while this work highlights the potential of constructing proxy based  $\Delta\text{ffCO}_2$  records, it also reiterates the importance of systematic  $^{14}\text{C}$  measurements to provide the necessary constraints on the changing ratios between the proxies and  $\text{ffCO}_2$ .

*Data availability.* The flask results and  $\text{NO}_x$  data from Heidelberg can be found in TBA.

Temporarily available for review at <https://heibox.uni-heidelberg.de/d/35770e17796944948e83/>



440 *Author contributions.* HJ designed the study with contributions from SH, IL, and FM. FM and CR performed the flask sampling. SH and  
AJ provided the flask measurements. DP provided the NO<sub>x</sub> measurements. FM conducted the modelling. HJ evaluated the data. HJ and SH  
wrote the manuscript with contributions from all co-authors.

*Competing interests.* The authors declare that they have no conflict of interest.

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## 455 References

- Beirle, S.: Estimating source strengths and lifetime of Nitrogen Oxides from satellite data, PhD, University of Heidelberg, Heidelberg, <https://doi.org/10.11588/heidok.00005225>, 2004.
- Beirle, S., Platt, U., Wenig, M., and Wagner, T.: Weekly cycle of NO<sub>2</sub> by GOME measurements: a signature of anthropogenic sources, *Atmospheric Chemistry and Physics*, 3, 2225–2232, <https://doi.org/10.5194/acp-3-2225-2003>, 2003.
- 460 Ciais, P., Crisp, D., Denier Van Der Gon, H., Engelen, R., Heimann, M., Janssens-Maenhout, G., Rayner, P., and Scholze, M.: Towards a European Operational Observing System to Monitor Fossil CO<sub>2</sub> Emissions. Final Report from the Expert Group, European Commission: Joint Research Centre, ISBN 978-92-79- 53482-9, <https://doi.org/10.2788/350433>, 2015.
- Dellaert, S., Super, I., Visschedijk, A., and Denier van der Gon, H.: High resolution scenarios of CO<sub>2</sub> and CO emissions, Tech. rep., CHE deliverable D4.2, <https://www.che-project.eu/sites/default/files/2019-05/CHE-D4-2-V1-0.pdf>, 2019.
- 465 Denier van der Gon, H., Kuenen, J., Boleti, E., Muntean, M., Maenhout, G., Marshall, J., and Haussaire, J.-M.: Emissions and natural fluxes Dataset, Tech. rep., CHE deliverable D2.3, <https://www.che-project.eu/sites/default/files/2019-01/CHE-D2-3-V1-0.pdf>, 2019.
- Feng, S., Jiang, F., Wang, H., Liu, Y., He, W., Wang, H., Shen, Y., Zhang, L., Jia, M., Ju, W., and Chen, J. M.: China's Fossil Fuel CO<sub>2</sub> Emissions Estimated Using Surface Observations of Coemitted NO<sub>2</sub>, *Environmental Science & Technology*, <https://doi.org/10.1021/acs.est.3c07756>, 2024.
- 470 Gamnitzer, U., Karstens, U., Kromer, B., Neubert, R. E. M., Meijer, H. A. J., Schroeder, H., and Levin, I.: Carbon monoxide: A quantitative tracer for fossil fuel CO<sub>2</sub>?, *Journal of Geophysical Research: Atmospheres*, 111, <https://doi.org/10.1029/2005JD006966>, 2006.
- Goldberg, D. L., Lu, Z., Oda, T., Lamsal, L. N., Liu, F., Griffin, D., McLinden, C. A., Krotkov, N. A., Duncan, B. N., and Streets, D. G.: Exploiting OMI NO<sub>2</sub> satellite observations to infer fossil-fuel CO<sub>2</sub> emissions from U.S. megacities, *Science of The Total Environment*, 695, 133 805, <https://doi.org/10.1016/j.scitotenv.2019.133805>, 2019.
- 475 Hazan, L., Tarniewicz, J., Ramonet, M., Laurent, O., and Abbaris, A.: Automatic processing of atmospheric CO<sub>2</sub> and CH<sub>4</sub> mole fractions at the ICOS Atmosphere Thematic Centre, *Atmospheric Measurement Techniques*, 9, 4719–4736, <https://doi.org/10.5194/amt-9-4719-2016>, publisher: Copernicus GmbH, 2016.
- Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot, J., Bonavita, M., De Chiara, G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R., Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R. J., Hólm, E., Janisková, M., Keeley, S., Laloyaux, P., Lopez, P., Lupu, C., Radnoti, G., De Rosnay, P., Rozum, I., Vamborg, F., Villaume, S., and Thépaut, J.: The ERA5 global reanalysis, *Quarterly Journal of the Royal Meteorological Society*, 146, 1999–2049, <https://doi.org/10.1002/qj.3803>, 2020.
- 480 Horbanski, M., Pöhler, D., Lampel, J., and Platt, U.: The ICAD (iterative cavity-enhanced DOAS) method, *Atmospheric Measurement Techniques*, 12, 3365–3381, <https://doi.org/10.5194/amt-12-3365-2019>, 2019.
- ICOS RI: ICOS Atmosphere Station Specifications V2.0 (editor: O. Laurent), ICOS ERIC, <https://doi.org/10.18160/GK28-2188>, 2020.
- Jaschke, C.: Potentials and Limitations of Proxy to Fossil Fuel CO<sub>2</sub> Ratios – a Case Study at the ICOS Station near Karlsruhe, Master's thesis, University of Heidelberg, Heidelberg, 2021.
- Jordan, A. and Damak, F.: ICOS CAL - Quality Control Report 2022, <https://doi.org/10.18160/SA0X-SF4Z>, medium: Portable Document
- 490 Format (PDF) Publisher: ICOS CAL Version Number: 1.0, 2023.





- Kenagy, H. S., Sparks, T. L., Ebben, C. J., Wooldrige, P. J., Lopez-Hilfiker, F. D., Lee, B. H., Thornton, J. A., McDuffie, E. E., Fibiger, D. L., Brown, S. S., Montzka, D. D., Weinheimer, A. J., Schroder, J. C., Campuzano-Jost, P., Day, D. A., Jimenez, J. L., Dibb, J. E., Campos, T., Shah, V., Jaeglé, L., and Cohen, R. C.: NO<sub>x</sub> Lifetime and NO<sub>y</sub> Partitioning During WINTER, *Journal of Geophysical Research: Atmospheres*, 123, 9813–9827, <https://doi.org/10.1029/2018JD028736>, 2018.
- 495 Konovalov, I. B., Berezin, E. V., Ciais, P., Broquet, G., Zhuravlev, R. V., and Janssens-Maenhout, G.: Estimation of fossil-fuel CO<sub>2</sub> emissions using satellite measurements of "proxy" species, *Atmospheric Chemistry and Physics*, 16, 13 509–13 540, <https://doi.org/10.5194/acp-16-13509-2016>, 2016.
- Kromer, B. and Münnich, K. O.: Co2 Gas Proportional Counting in Radiocarbon Dating — Review and Perspective, in: *Radiocarbon After Four Decades*, edited by Taylor, R. E., Long, A., and Kra, R. S., pp. 184–197, Springer, New York, NY, ISBN 978-1-4757-4249-7, [https://doi.org/10.1007/978-1-4757-4249-7\\_13](https://doi.org/10.1007/978-1-4757-4249-7_13), 1992.
- 500 Kromer, B., Lindauer, S., Synal, H.-A., and Wacker, L.: MAMS – A new AMS facility at the Curt-Engelhorn-Centre for Archaeometry, Mannheim, Germany, *Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms*, 294, 11–13, <https://doi.org/10.1016/j.nimb.2012.01.015>, 2013.
- Levin, I. and Karstens, U.: Inferring high-resolution fossil fuel CO<sub>2</sub> records at continental sites from combined 14CO<sub>2</sub> and CO observations, *Tellus B: Chemical and Physical Meteorology*, 59, 245, <https://doi.org/10.1111/j.1600-0889.2006.00244.x>, 2007.
- 505 Levin, I., Münnich, K. O., and Weiss, W.: The Effect of Anthropogenic CO<sub>2</sub> and 14C Sources on the Distribution of 14C in the Atmosphere, *Radiocarbon*, 22, 379–391, <https://doi.org/10.1017/S003382220000967X>, 1980.
- Levin, I., Kromer, B., Schmidt, M., and Sartorius, H.: A novel approach for independent budgeting of fossil fuel CO<sub>2</sub> over Europe by 14CO<sub>2</sub> observations, *Geophysical Research Letters*, 30, <https://doi.org/10.1029/2003GL018477>, 2003.
- 510 Levin, I., Karstens, U., Erritt, M., Maier, F., Arnold, S., Rzesanke, D., Hammer, S., Ramonet, M., Vítková, G., Conil, S., Heliasz, M., Kubistin, D., and Lindauer, M.: A dedicated flask sampling strategy developed for Integrated Carbon Observation System (ICOS) stations based on CO<sub>2</sub> and CO measurements and Stochastic Time-Inverted Lagrangian Transport (STILT) footprint modelling, *Atmospheric Chemistry and Physics*, 20, 11 161–11 180, <https://doi.org/10.5194/acp-20-11161-2020>, 2020.
- Lin, J. C., Gerbig, C., Wofsy, S. C., Andrews, A. E., Daube, B. C., Davis, K. J., and Grainger, C. A.: A near-field tool for simulating the up-stream influence of atmospheric observations: The Stochastic Time-Inverted Lagrangian Transport (STILT) model, *Journal of Geophysical Research: Atmospheres*, 108, <https://doi.org/10.1029/2002JD003161>, 2003.
- 515 Ling, Q., Zhou, Y., Chen, D., Varricchio, L., Detti, A., Bartalini, S., and Guan, Z.: Laser spectroscopy applied in radiocarbon dating with the bomb peak, *Optics Express*, 33, 7830, <https://doi.org/10.1364/OE.554129>, 2025.
- Liu, F., Beirle, S., Zhang, Q., Dörner, S., He, K., and Wagner, T.: NO<sub>x</sub> lifetimes and emissions of cities and power plants in polluted background estimated by satellite observations, *Atmospheric Chemistry and Physics*, 16, 5283–5298, <https://doi.org/10.5194/acp-16-5283-2016>, 2016.
- 520 Liu, F., Duncan, B. N., Krotkov, N. A., Lamsal, L. N., Beirle, S., Griffin, D., McLinden, C. A., Goldberg, D. L., and Lu, Z.: A methodology to constrain carbon dioxide emissions from coal-fired power plants using satellite observations of co-emitted nitrogen dioxide, *Atmospheric Chemistry and Physics*, 20, 99–116, <https://doi.org/10.5194/acp-20-99-2020>, 2020.
- 525 Lopez, M., Schmidt, M., Delmotte, M., Colomb, A., Gros, V., Janssen, C., Lehman, S. J., Mondelain, D., Perrussel, O., Ramonet, M., Xueref-Remy, I., and Bousquet, P.: CO, NO<sub>x</sub> and <sup>13</sup>CO<sub>2</sub> as tracers for fossil fuel CO<sub>2</sub>: results from a pilot study in Paris during winter 2010, *Atmospheric Chemistry and Physics*, 13, 7343–7358, <https://doi.org/10.5194/acp-13-7343-2013>, 2013.



- Lux, J. T.: A new target preparation facility for high precision AMS measurements and strategies for efficient  $^{14}\text{CO}_2$  sampling, PhD, University of Heidelberg, Heidelberg, <https://doi.org/10.11588/heidok.00024767>, 2018.
- 530 Maier, F.: Estimating fossil fuel carbon dioxide (ffCO<sub>2</sub>) emissions in the Rhine Valley metropolitan region from local atmospheric observations in Heidelberg, PhD, University of Heidelberg, Heidelberg, 2023.
- Maier, F., Gerbig, C., Levin, I., Super, I., Marshall, J., and Hammer, S.: Effects of point source emission heights in WRF–STILT: a step towards exploiting nocturnal observations in models, *Geoscientific Model Development*, 15, 5391–5406, <https://doi.org/10.5194/gmd-15-5391-2022>, 2022.
- 535 Maier, F., Levin, I., Gachkivskyi, M., Rödenbeck, C., and Hammer, S.: Estimating regional fossil fuel CO<sub>2</sub> concentrations from  $^{14}\text{CO}_2$  observations: challenges and uncertainties, *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 381, 20220 203, <https://doi.org/10.1098/rsta.2022.0203>, 2023.
- Maier, F., Levin, I., Conil, S., Gachkivskyi, M., Denier van der Gon, H., and Hammer, S.: Uncertainty in continuous  $\Delta\text{CO}$ -based  $\Delta\text{ffCO}_2$  estimates derived from  $^{14}\text{C}$  flask and bottom-up  $\Delta\text{CO}$  /  $\Delta\text{ffCO}_2$  ratios, *Atmospheric Chemistry and Physics*, 24, 8205–8223, <https://doi.org/10.5194/acp-24-8205-2024>, 2024a.
- 540 Maier, F., Rödenbeck, C., Levin, I., Gerbig, C., Gachkivskyi, M., and Hammer, S.: Potential of  $^{14}\text{C}$ -based vs.  $\Delta\text{CO}$ -based  $\Delta\text{ffCO}_2$  observations to estimate urban fossil fuel CO<sub>2</sub> (ffCO<sub>2</sub>) emissions, *Atmospheric Chemistry and Physics*, 24, 8183–8203, <https://doi.org/10.5194/acp-24-8183-2024>, 2024b.
- Martin, R. V., Jacob, D. J., Chance, K., Kurosu, T. P., Palmer, P. I., and Evans, M. J.: Global inventory of nitrogen oxide emissions constrained by space-based observations of NO<sub>2</sub> columns, *Journal of Geophysical Research: Atmospheres*, 108, <https://doi.org/10.1029/2003JD003453>, 2003.
- 545 Nehr Korn, T., Eluszkiewicz, J., Wofsy, S. C., Lin, J. C., Gerbig, C., Longo, M., and Freitas, S.: Coupled weather research and forecasting–stochastic time-inverted lagrangian transport (WRF–STILT) model, *Meteorology and Atmospheric Physics*, 107, 51–64, <https://doi.org/10.1007/s00703-010-0068-x>, 2010.
- 550 Petron, G., Crotwell, A., Crotwell, M., Dlugokencky, E., Madronich, M., Moglia, E., Neff, D., Thoning, K., Wolter, S., and Mund, J.: Atmospheric Carbon Monoxide Dry Air Mole Fractions from the NOAA GML Carbon Cycle Cooperative Global Air Sampling Network, 1988–2022, <https://doi.org/10.15138/33BV-S284>, version: 2023-08-28, 2023.
- Romer, P. S., Duffey, K. C., Wooldridge, P. J., Allen, H. M., Ayres, B. R., Brown, S. S., Brune, W. H., Crounse, J. D., De Gouw, J., Draper, D. C., Feiner, P. A., Fry, J. L., Goldstein, A. H., Koss, A., Misztal, P. K., Nguyen, T. B., Olson, K., Teng, A. P., Wennberg, P. O., Wild, R. J., Zhang, L., and Cohen, R. C.: The lifetime of nitrogen oxides in an isoprene-dominated forest, *Atmospheric Chemistry and Physics*, 16, 7623–7637, <https://doi.org/10.5194/acp-16-7623-2016>, 2016.
- 555 Super, I., Denier van der Gon, H. A. C., van der Molen, M. K., Dellaert, S. N. C., and Peters, W.: Optimizing a dynamic fossil fuel CO<sub>2</sub> emission model with CTDAS (CarbonTracker Data Assimilation Shell, v1.0) for an urban area using atmospheric observations of CO<sub>2</sub>, CO, NO<sub>x</sub>, and SO<sub>2</sub>, *Geoscientific Model Development*, 13, 2695–2721, <https://doi.org/10.5194/gmd-13-2695-2020>, 2020.
- 560 Super, I., Scarpelli, T., Droste, A., and Palmer, P. I.: Improved definition of prior uncertainties in CO<sub>2</sub> and CO fossil fuel fluxes and its impact on multi-species inversion with GEOS-Chem (v12.5), *Geoscientific Model Development*, 17, 7263–7284, <https://doi.org/10.5194/gmd-17-7263-2024>, 2024.
- Thoning, K. W., Tans, P. P., and Komhyr, W. D.: Atmospheric carbon dioxide at Mauna Loa Observatory: 2. Analysis of the NOAA GMCC data, 1974–1985, *Journal of Geophysical Research: Atmospheres*, 94, 8549–8565, <https://doi.org/10.1029/JD094iD06p08549>, 1989.



- 565 Turnbull, J. C., Miller, J. B., Lehman, S. J., Tans, P. P., Sparks, R. J., and Southon, J.: Comparison of  $^{14}\text{CO}_2$ , CO, and SF<sub>6</sub> as tracers for recently added fossil fuel CO<sub>2</sub> in the atmosphere and implications for biological CO<sub>2</sub> exchange, *Geophysical Research Letters*, 33, <https://doi.org/10.1029/2005GL024213>, 2006.
- Turnbull, J. C., Sweeney, C., Karion, A., Newberger, T., Lehman, S. J., Tans, P. P., Davis, K. J., Lauvaux, T., Miles, N. L., Richardson, S. J., Cambaliza, M. O., Shepson, P. B., Gurney, K., Patarasuk, R., and Razlivanov, I.: Toward quantification and source sector identification
- 570 of fossil fuel CO<sub>2</sub> emissions from an urban area: Results from the INFLUX experiment, *Journal of Geophysical Research: Atmospheres*, 120, 292–312, <https://doi.org/10.1002/2014JD022555>, 2015.
- Van Der Laan, S., Karstens, U., Neubert, R., Van Der Laan-Luijkx, I., and Meijer, H.: Observation-based estimates of fossil fuel-derived CO<sub>2</sub> emissions in the Netherlands using  $\delta^{14}\text{C}$ , CO and  $^{222}\text{Rn}$ , *Tellus B: Chemical and Physical Meteorology*, 62, 389, <https://doi.org/10.1111/j.1600-0889.2010.00493.x>, 2010.