



1 **GUST1.0: A GPU-accelerated 3D Urban Surface Temperature Model**

2 Shuo-Jun Mei^{1,2*}, Guanwen Chen^{1,2}, Jian Hang^{1,2}, Ting Sun³

3 ¹ School of Atmospheric Sciences, Sun Yat-sen University, and Southern Marine Science and
4 Engineering Guangdong Laboratory (Zhuhai), Zhuhai 519082, PR China

5 ² China Meteorological Administration Xiong'an Atmospheric Boundary Layer Key Laboratory,
6 Xiong'an, P.R. China

7 ³ Department of Risk and Disaster Reduction, University College London, London, UK

8 *Correspondence to:* Shuo-Jun Mei (meishj@mail.sysu.edu.cn)

9 **Abstract**

10 The escalating urban heat, driven by climate change and urbanization, poses significant threats to
11 residents' health and urban climate resilience. The coupled radiative-convective-conductive heat transfer
12 across complex urban geometries makes it challenging to identify the primary causes of urban heat and
13 develop mitigation strategies. To address this challenge, we develop a GPU-accelerated Urban Surface
14 Temperature model (GUST) through CUDA architecture. To simulate the complex radiative exchanges
15 and coupled heat transfer processes, we adopt Monte Carlo method, leveraging GPUs to overcome its
16 computational intensity while retaining its high accuracy. Radiative exchanges are resolved using a
17 reverse ray tracing algorithm, while the conduction-radiation-convection mechanism is addressed
18 through a random walking algorithm. The validation is carried out using the Scaled Outdoor
19 Measurement of Urban Climate and Health (SOMUCH) experiment, which features a wide range of
20 urban densities and offers high spatial and temporal resolution. This model exhibits notable accuracy in
21 simulating urban surface temperatures and their temporal variations across different building densities.
22 Analysis of the surface energy balance reveals that longwave radiative exchanges between urban surfaces
23 significantly influence model accuracy, whereas convective heat transfer has a lesser impact. To
24 demonstrate the applicability of GUST, it is employed to model transient surface temperature
25 distributions at complex geometries on a neighborhood scale. Leveraging the high computational
26 efficiency of GPU, the simulation traces 10^5 rays across 2.3×10^4 surface elements in each time step,
27 ensuring both accuracy and high-resolution results for urban surface temperature modeling.



28 1. Introduction

29 Urban overheating has become a pressing issue due to the combination effects of global warming,
30 heatwaves, and rapid urbanization ([Feng et al., 2023](#)). The Urban Heat Island (UHI) effect is
31 characterized by higher surface and air temperatures in urban areas than in surrounding rural areas, which
32 exacerbates the urban overheating ([Manoli et al., 2019](#)). It is estimated that more than 1.7 billion people
33 and 13,000 cities are facing urban overheating problems ([Tuholske et al., 2021](#)). Exposure to extreme
34 urban heat poses a significant threat to residents' health, contributing to increased mortality and morbidity
35 ([Ebi et al., 2021](#)). Identifying the main causes of hot urban surfaces is essential for developing effective
36 strategies to mitigate urban overheating.

37 Physics-based models are powerful tools for uncovering the urban thermal balance and identifying the
38 primary causes of urban heat ([Carmeliet and Derome, 2024](#)). They enable a quantitative evaluation of
39 the contribution of each process, such as conduction, radiation, and convection, to the overall thermal
40 balance. Urban surface temperatures are determined by the coupled heat transfer processes of conduction,
41 radiation, and convection ([Kravenhoff and Voogt, 2007](#)). These heat transfer processes in urban areas
42 differ from those in rural areas. First, urban materials typically have a lower heat capacity, allowing them
43 to heat up more quickly and reach higher temperatures ([Wang et al., 2018](#)). Secondly, the complex three-
44 dimensional geometry of urban environments leads to multiple reflections, which reduce urban albedo
45 and limit the longwave heat loss to sky ([Yang and Li, 2015](#)). Thirdly, the densely packed buildings
46 weaken the urban wind and thus reduce the convective transfer and further limit the heat loss ([Wang et](#)
47 [al., 2021](#)).

48 A well-designed urban surface temperature model needs to accurately capture these heat transfer
49 processes. Table 1 summarizes the models for urban surface temperatures and their schemes for
50 conduction, radiation, and convection. For heat conduction, 1D models are commonly used due to the
51 relatively thin walls of buildings in urban areas. For convective heat transfer, both parameterized
52 convective coefficients and CFD (Computational Fluid Dynamics) simulations are commonly used. CFD
53 simulations can better capture the spatial variations in air temperature in densely built urban areas, but
54 the computational cost is much higher. The key distinction among these models lies in their radiation



55 schemes, as radiation is the primary energy input into the thermal system of urban surfaces. Moreover,
56 simulating complex urban radiative transfer requires significant computational resources, necessitating
57 simplifications and parameterizations to make the simulation more applicable.

58 Table 1 shows that the radiosity method is widely used to solve the reflections. In the radiosity method,
59 the net longwave and shortwave radiation are solved by two main steps: 1) collecting luminous energy
60 from both the sun and the sky vault, and 2) distributing the reflected energy based on view factors. The
61 luminous energy is influenced by the shading pattern, which is solved by two main approaches in these
62 models: 1) Sunlit-shaded distributions method, which employs ray tracing to determine whether a surface
63 is illuminated; and 2) Flux reduction coefficients: where shading is accounted for by reducing the
64 irradiance at shaded points. The reflection and longwave exchange between urban surfaces are
65 determined by view factors, which can be calculated using three approaches: the analytical method, the
66 discrete transfer method, and the Monte Carlo ray tracing method.

- 67 • **The analytical method** uses analytical solutions of view factors by assuming urban surfaces are
68 composed of simple geometries.
- 69 • **The discrete transfer method (DTM)** uses ray tracing method to calculate view factors. The ray
70 direction is determined by dividing the hemisphere into equal segments. This method counts the
71 number of rays intersecting other surfaces.
- 72 • **The Monte Carlo Ray Tracing (MCRT)** is similar to DTM but differs by using rays that are
73 directed randomly. This method is suitable for calculating view factors in complex geometries, but
74 it requires a large number of rays.

75 The HTRDR-Urban adopted a different approach, using backward MCRT, to calculate the solar radiation
76 considering multiple reflections ([Schoetter et al., 2023](#)). The Monte Carlo method (MCM) has been
77 widely used to model solar radiation through the application of a ray tracing algorithm ([Kondo et al.,](#)
78 [2001](#)). Recently, its application has been extended to address conduction, convection, and radiation
79 problems ([Villefranque et al., 2022](#)). In backward MCRT, the energy of the incident light is divided into
80 a large number of photons. By tracking the path of these photons and counting the number of photons
81 absorbed, the net solar radiation reaching a given surface can be calculated. [Tregan et al. \(2023\)](#) proposed



82 a theoretical framework to solve linearized transient conduction-radiation problems with Robin's
83 boundary condition in complex 3D urban geometry. Based on this framework, [Caliot et al. \(2024\)](#)
84 developed a probabilistic model to simulate urban surface temperatures, using ray-tracing, walk-on-
85 sphere and double randomization techniques. Their model leverages advancements in computer graphics
86 for image synthesis and the Monte Carlo method (MCM), enabling it to effectively handle large and
87 complex 3D geometries.

88 The advantage of MCM is its ability to handle complex geometries and albedos, while the disadvantage
89 is its high computational cost. The low computational efficiency limits the application of MCM in real
90 urban configurations. Although some models in Table 1 are validated against field measurements, others
91 remain unvalidated. These models rely on various assumptions and parameterizations, and the lack of
92 validation limits their accuracy. Additionally, using field measurement data to validate numerical models
93 faces several challenges: 1) limited test points due to regulatory constraints and installation difficulties,
94 2) uncertainty in infrared imagery caused by varying view angles, and 3) heterogeneity in the optical and
95 thermal properties of building materials.

96 This study aims to develop a GPU-based Urban Surface Temperature (GUST) model to enhance the
97 computational speed of Monte Carlo Method. The absorption and reflection of longwave and shortwave
98 radiation on outdoor surfaces modeled using the reverse Monte Carlo ray tracing (rMCRT) algorithm.
99 The resulting shortwave and longwave radiation are then treated as heat flux boundary conditions for the
100 1D heat conduction model, which employs the Monte Carlo random walk method to calculate surface
101 temperatures. High spatial-temporal resolution surface temperature data from a scaled measurement
102 (SOMUCH) is employed to validate the parameterization and assumptions in this model.

103 The paper is organized as follows. Sect. 2 outlines the model structure and describes the algorithms used
104 for the submodels. Sect. 3 presents the validation and evaluation of the model by comparing it with
105 experimental data. Sect. 4 includes an example demonstrating how the model can be applied to complex
106 geometries. Sect. 5 discusses the applications, limitations, and future development of the model. Lastly,
107 Sect. 6 provides the conclusions.

108



Table 1. Overview of building-resolved models for urban surface temperature. The view factors are solved by both DTM (Discrete transfer method), analytical model, and Monte Carlo ray tracing method.

Model	Solar Irradiation	Reflections and longwave exchange	Conduction	Convection	Validation
HTRDR-Urban (Schoetter et al., 2023)	Backward Monte Carlo ray tracing	Backward Monte Carlo ray tracing	Monte Carlo random walking	Parameterized	N.A.
MUST (Yang and Li, 2013)	Sunlit-shaded distributions	Radiosity Method, DTM view factors	1D heat conduction	Parameterized	Thermal scanner and IRT (Voogt and Oke, 1998)
TUF-3D (Kravenhoff and Voogt, 2007)	Sunlit-shaded distributions	Radiosity Method, analytical view factors	1D heat conduction	Parameterized	Thermal scanner and IRT (Voogt and Oke, 1998)
SOLENE Microclimat (Imbert et al., 2018)	Sunlit-shaded distributions.	Radiosity Method, analytical view factors	1D heat conduction	Coupling CFD simulation	Thermographies measurement (Hénon et al., 2012)
Envi-Met (Eingrüber et al., 2024)	Flux reduction coefficients	Radiosity Method, DTM view factors	1D heat conduction	Coupling CFD simulation	Field measurements (Forouzandeh, 2021)
uDALES (Owens et al., 2024)	Sunlit-shaded distributions	Radiosity Method, DTM view factors	1D heat conduction	Coupling CFD simulation	N.A.
PALM (Resler et al., 2017)	Sunlit-shaded distributions	Radiosity Method, Analytical and DTM view factors	Empirical heat conductivity	Coupling CFD simulation	Field measurement (Resler et al., 2017)
MITRAS (Salim et al., 2018)	Meso-scale radiation scheme	Meso-scale radiation scheme (METRAS)	Force-restore method	Coupling CFD simulation	N.A.
OpenFOAM (Rodriguez et al., 2024)	Sunlit-shaded distributions	Radiosity Method, DTM view factor	1D heat-moisture diffusion.	Coupling CFD simulation	N.A.
FLUENT (Toparlar et al., 2015)	Sunlit-shaded distributions	Radiosity Method, DTM view factor	Shell conduction	Coupling CFD simulation	Field measurement (Toparlar et al., 2015)

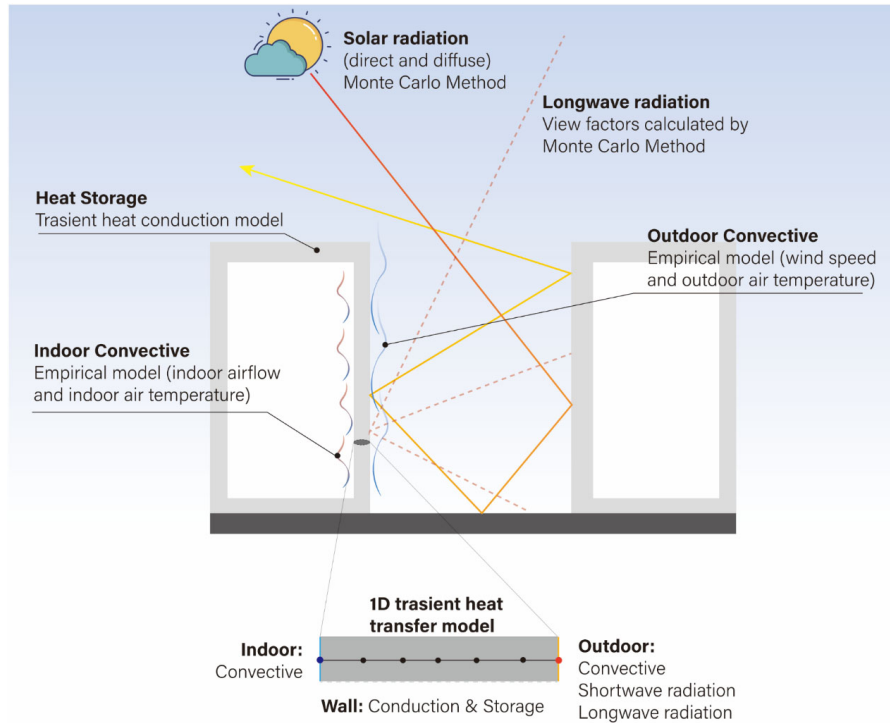


2. Model design

GUST aims to resolve the urban surface temperature by a transient heat conduction model, as illustrated in Fig.1. The convective and radiative heat transfer at urban surfaces is treated as boundary conditions for the 1D heat conduction model. For the outdoor side, the heat flux (q_{out}) is the sum of radiative (longwave q_l and solar q_s) and convective heat flux ($q_{c,out}$).

$$q_{out} = q_l + q_s + q_{c,out} \quad (1)$$

The absorbed solar radiation, q_s is the sum of direct solar irradiation ($q_{s,o}$) and diffuse solar irradiation ($q_{s,r}$), expressed by: $q_s = q_{s,o} + q_{s,r}$. The longwave radiation flux q_l includes the radiation between urban surfaces ($q_{l,urban}$) and between urban surfaces and the sky ($q_{l,sky}$), represented as $q_l = q_{l,urban} + q_{l,sky}$.



122

123 **Figure 1: The model design of GUST. In this model, 1D transient conductive heat transfer is considered for**
124 **urban surfaces the system (e.g., walls, roofs, and ground). They are composed of multiple layers where the**



125 thermal properties are uniform and isotropic. All urban surfaces are assumed to be opaque in this study.

126

127 2.1. Conduction sub-model

128 The Monte Carlo random walking method is used to solve the 1D heat conduction (Talebi et al., 2017).

129 Compared to finite volume method, this approach is insensitivity to the complexity of urban geometry

130 and boundary conditions (Villefranque et al., 2022; Caliot et al., 2024). In the present version, the heat

131 conduction along the wall span is neglected. The one-dimensional (1D) transient heat conduction

132 equation is:

$$133 \quad \frac{\partial}{\partial t} T = \alpha \frac{\partial^2 T}{\partial x^2} \quad (2)$$

134 where $\alpha = \frac{k}{\rho c_p}$ is the solid thermal diffusivity and k the thermal conductivity, ρ the density, c_p the

135 specific heat capacity. The ground, walls and roofs are composed of multiple layers. In the Monte Carlo

136 random walking method, the heat conduction equation is replaced by finite difference approximation as:

$$137 \quad T(x, t + \Delta t) = P_t T(x, t) + P_{x-} T(x - \Delta x, t + \Delta t) + P_{x+} T(x + \Delta x, t + \Delta t) \quad (3)$$

138 where $P_t = \frac{1}{1+2Fo}$ is defined as probability of time step; $P_{x-} = P_{x+} = \frac{Fo}{1+2Fo}$. where P_{x-} and P_{x+}

139 respectively represent the probabilities of stepping to the points $(x - \Delta x, t)$ and $(x + \Delta x, t)$. Here,

140 $Fo = \frac{k\Delta t}{\rho c_p (\Delta x)^2}$ These coefficients are nonnegative probabilistic values and

$$141 \quad P_t + P_{x-} + P_{x+} = 0 \quad (4)$$

142 The Monte Carlo random walking algorithm is schematically illustrated in Fig. 2. The core idea is that

143 particles walk by following rules:

144 1) Start a random walk at point x .

145 2) Generating a random number (R) between 0 and 1.

146 3) Determine walking direction by conditions



$$\begin{cases} 0 < R < P_{x-}: & x \rightarrow (x - \Delta x) \\ P_{x-} < R < (P_{x-} + P_{x+}): & x \rightarrow (x - \Delta x) \\ (P_{x-} + P_{x+}) < R: & x \rightarrow (x), T(i) = T(i) + T(x, t - \Delta t) \end{cases} \quad (5)$$

4) If the next point is not on the boundary repeat step 2 and 3 and if it is on the boundary, record $T(i) = T(i) + T$ at the boundary and go to step 1.

5) After N random walking, temperature at point x is calculated by

$$T(x) = \frac{T(i)}{N} \quad (6)$$

When a particle reaches a heat flux, convective or interface boundary, its movement follows the following rules.

1) Heat flux boundary

When the particle walks to the boundary of heat flux (q), it is bounced back and record the temperature

T_{hf} , which is calculate by $T_{hf} = \frac{q\Delta x}{k} + \frac{q}{2k}(\Delta x)^2$.

2) Convective boundary

The heat flux of a convective boundary is calculated by $q = h(T_w - T_a)$, where h is the heat transfer coefficient and T_w the wall temperature and T_a the air temperature. The wall temperature is calculated by

$$T_w = \frac{1}{1 + Bi} T(x - \Delta x) + \frac{Bi}{1 + Bi} T_a \quad (7)$$

Where $P_x = \frac{1}{1 + Bi}$, $P_a = \frac{Bi}{1 + Bi}$, $Bi = \frac{h\Delta x}{k}$. When the particle reaches the convective boundary, a new random number R was generated and moves as follows:

$$\begin{cases} 0 < R < P_x: & \rightarrow \text{bounced back} \\ P_x < R < 1: & \rightarrow \text{absorbed by air with } T(i) = T(i) + T_a \end{cases} \quad (8)$$

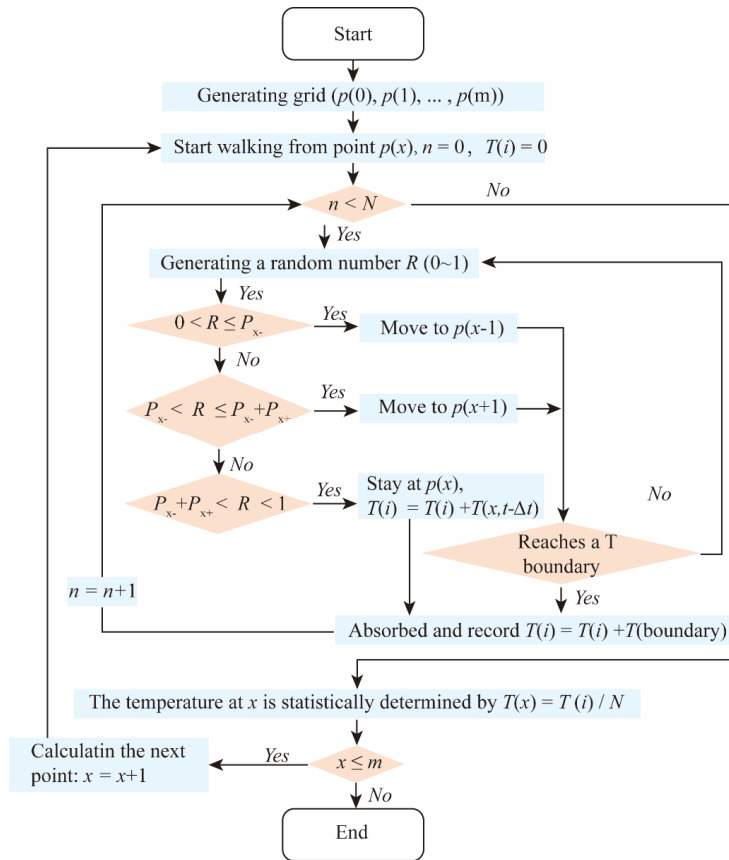
3) Interface between two layers

The interface between layers is flux continuity, i.e. the conductive fluxes are equal on both sides of the interface. The heat conductivities on left and right sides of the interface are k_A and k_B . The conductive



168 heat fluxes on both sides are equal, i.e., $-k_A \frac{dT}{dx} = -k_B \frac{dT}{dx}$. When a particle reaches the interface, it may
169 be reflected or move to the next layer. A new random number R is generated. The particle moves by
170 following

$$171 \quad \begin{cases} 0 < R < P_{x-} : & \rightarrow \text{bounced back to layer A} \\ P_{x-} < R < 1 : & \rightarrow \text{move to layer B} \end{cases} \quad (9)$$

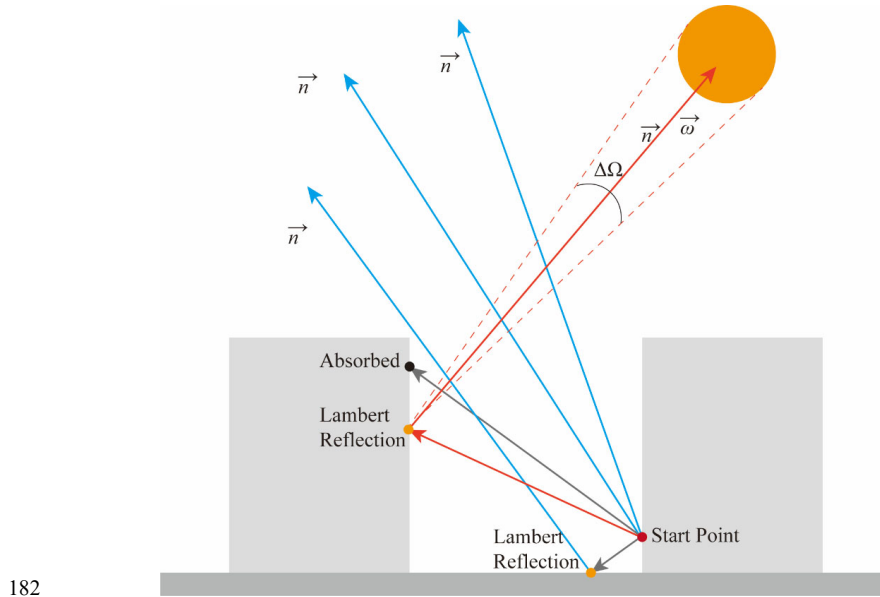


172
173 **Figure 2: Flowchart of the Monte Carlo random walking algorithm for 1D heat conduction. At each point,**
174 **the particle movement stops after N random walks. Each walk stops when particle either reaches a fixed**
175 **temperature boundary or remains stationary. Orange diamonds indicate decision points with two possible**
176 **outcomes (Yes/No).**



177 2.2. Solar radiation sub-model

178 The reverse Monte Carlo Ray Tracing (rMCRT) method is used to calculate the solar radiation q_s and
 179 longwave radiation q_l . The ray starts from the target points, instead of starting from the sky or sun in the
 180 ray tracing method (Caliot et al., 2024). This method ensures that enough photons reach the target point
 181 to obtain a statistical result.



182
 183 **Figure 3: Schematic illustration of the reverse MCM ray tracing method for calculating the directional and**
 184 **diffuse solar radiation.**

185 The procedure of reverse MCM is schematically explained in Fig. 3. In total, N photons leave the target
 186 point in random directions (\vec{r}), which is determined by the azimuth θ_a and incidence angle η_a . These
 187 angles are calculated by $\theta_a = 2\pi R_1$ and $\eta_a = \arccos(1 - 2R_2)$, where R_1 and R_2 are random
 188 numbers between 0 and 1.

189 When a photon reaches the surface, it can be absorbed or reflected via Lambert's law. To determine
 190 whether this photon is absorbed, a random number R_{ab} (ranging from 0 ~ 1) is generated. When $R_{ab} >$
 191 α_s (surface albedo), the photon is absorbed by the surface. When $R_{ab} < \alpha_s$, the photon is reflected. All
 192 surfaces are considered Lambertian and the direction of reflect solar beam is determined by the azimuth



193 θ_a and incidence angle η_a of that surface. At each reflection, θ_a and η_a are recalculated by
194 regenerating new random numbers.

195 When the photon reaches the “sky” in the direction of \vec{r} , its angle (θ_{ns}) with the reverse solar direction
196 $\vec{\omega}_{sun}$ is calculated. When $\theta_{ns} < \Delta\Omega_d$, that photon is marked as reaching the “Sun”, otherwise, that
197 photon is marked as reaching the “Sky”. The direct ($q_{s,o}$) and diffuse ($q_{s,r}$) solar radiation reaching the
198 target point can then be statistically determined by:

$$199 \quad q_{s,o} = \frac{\pi I_{s,o}}{\Delta\Omega_d N} \sum_{\theta_{ns} < \Delta\Omega_d} |\vec{\omega}_{sun} \cdot \vec{n}| \quad (10)$$

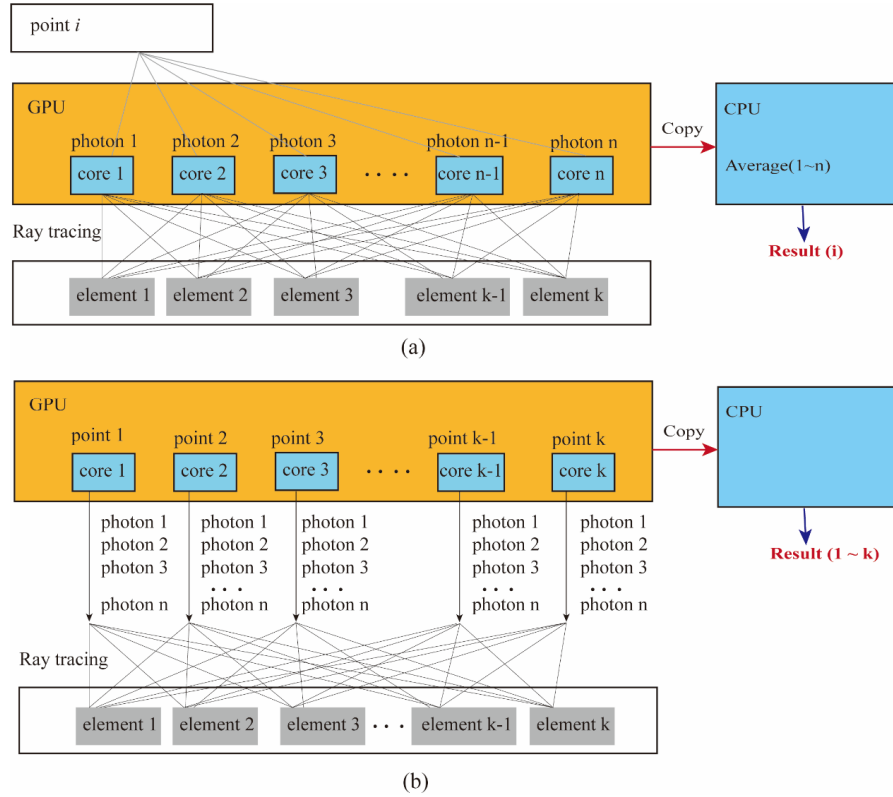
$$200 \quad q_{s,r} = \sum_{\theta_n > d\Delta\Omega_d} \frac{I_{s,r}}{N} \quad (11)$$

201 where $I_{s,o}$ and $I_{s,r}$ is the downward direction and diffuse solar radiation. The ratio between the
202 directional and diffuse solar radiation is calculated by the model proposed by (Reindl et al., 1990).

203 The rMCRT requires a large number of rays to achieve statistically reliable results. To accelerate the
204 simulation, the model is run in parallel on GPUs (Graphics Processing Units) using the CUDA® platform
205 (Yoshida et al., 2024). The advantage of GPUs is that they have a large number of cores, which enables
206 them to handle many parallel tasks simultaneously. GPUs are particularly well-suited for accelerating
207 MCRT, since each ray tracing operation is independent.

208 The GPU parallel computing is executed using two strategies, based on the number of elements and
209 points. As illustrated in Fig. 4, Strategy 1 calculates the radiative flux point by point, emitting n photons
210 for ray tracing simulation. Each photon is processed in a separate GPU core. Once the ray tracing process
211 is complete, the results from the GPU cores are copied to the CPU, where radiative flux at each point is
212 calculated. Strategy 2 calculates the radiative flux for all points simultaneously, with each GPU core
213 computing the flux for a single point. The ray tracing of n photons is performed iteratively on the GPU.

214 The advantage of Strategy 1 is the efficient utilization of GPU cores when the number of points and
215 elements is small. However, its disadvantage is that it requires a large amount of memory when the
216 number of points is large. In contrast, Strategy 2 requires significantly less memory and only transfers
217 data to the CPU once, making it highly efficient when the number of points and elements is large.



218

219 **Figure 4: Two strategies for GPU parallel computing. (a) The ray tracing is conducted point by point. For**
 220 **each point, n photons are emitted. Each GPU core calculates one photon. (b) The ray tracing is conducted**
 221 **for all points at one time. Each GPU core calculates one point. The ray tracing of n photons is performed**
 222 **iteratively within the GPU core.**

223 The space angle of the Sun ($\Delta\Omega_d$) and the number of photons (N) can significantly affect the accuracy of
 224 reverse MCM. To evaluate this influence, a series of test cases are conducted, in which the directional
 225 solar radiation at a ground point is calculated. The solar radiation on the open ground can be calculated
 226 theoretically, as there is no shading from buildings.

227 Figure 5 shows the errors of simulations using different values of N and $\Delta\Omega_d$. The simulation time of
 228 each case is also indicated in that figure. When the number of photons is increased from $N = 10^5$ to
 229 $N = 10^7$, the simulation time increases from 0.05s to 1.15s, which is an increase of 23 times. The



230 relatively slow increase in simulation time is a result of the parallel computing capabilities of the GPU.

231 In each scenario, the model was run 20 times to observe the difference between each run.

232 A small $\Delta\Omega_d$ reduce the photon number reaching the Sun, thus increasing the error, where the $\Delta\Omega_d$ is

233 calculated from a 2D angle θ as $\Delta\Omega_d = 2\pi(1 - \cos(\theta))$. For example, the error in cases with $\theta = 3^\circ$

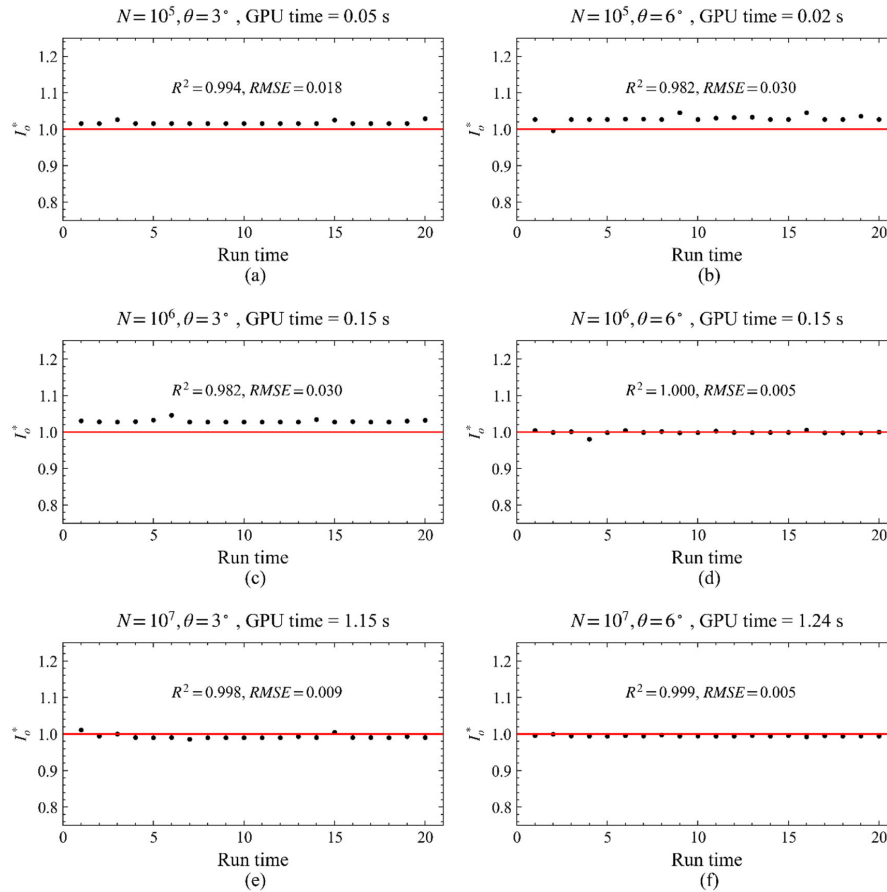
234 greater than that in cases with $\theta = 6^\circ$. A larger number of photons is needed to compensate for this error.

235 For example, the case with $\theta = 3^\circ$ and $N = 10^7$ shows acceptable accuracy. However, the case with

236 $\theta = 6^\circ$ shows a comparable accuracy when $N = 10^6$ and takes less simulation time.

237 In the subsequent simulations, $\theta = 6^\circ$ and $N = 10^6$ are applied to balance accuracy and simulation

238 time.



239



Figure 5: Numerical errors of directional solar radiation estimation using Monte Carlo method. The simulated solar radiation ($I_{o,sim}$) is normalized by the true value ($I_{o,true}$) and is expressed by ($I_o^* = \frac{I_{o,sim}}{I_{o,true}}$), where $I_o^* = 1.0$ represents an exact reproduction of the solar radiation. The test cases use different space angles of sun $\Delta\Omega_d = 2\pi(1 - \cos(\theta))$ and photon numbers (N). The red lines represent the true value, and dots represent the simulated data.

2.3. Longwave radiation sub-model

The view factors between the surfaces, as well as from the surfaces to the sky, are also calculated using the Monte Carlo ray tracing model, as illustrated in Fig. 6. The urban surfaces are divided into multiple triangular elements N_{ur} . The view factor from element S_i to element S_j , denoted as $F_{i,j}$, is calculated by emitting N photons from the centroid of element S_i . The algorithm then counts the number of photons $n_{i,j}$ that reach element S_j . Finally, the view factor $F_{i,j}$ is calculated by $F_{i,j} = n_{i,j}/N$. The sky view factor is also determined in this approach by treating the sky as an urban surface.

The longwave radiative heat exchange between the surfaces, as well as from the surfaces to the sky, is calculated by:

$$q_l = F_{i,sky}\epsilon(R_{l,lin} - \sigma T_i^4) + \epsilon\sigma \sum_{j=1}^{j=N_{ur}} F_{i,j}(T_j^4 - T_i^4) \quad (12)$$

where ϵ is the material emissivity, σ is Stefan–Boltzmann constant ($= 5.67 \times 10^{-8}$) ($\text{W m}^{-2} \text{K}^{-1}$), $R_{l,lin}$ is the downward longwave radiation from the sky, $F_{i,sky}$ is the sky view factor of element S_i . The surface temperature from the previous step (T_i and T_j) is used to calculate the longwave radiative heat exchange.

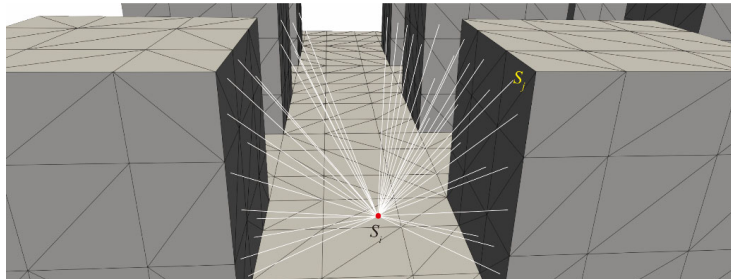


Figure 6: Schematic illustration of how view factors are calculated between urban surface elements.



2.4. Outdoor convective sub-model

GUST does not calculate urban airflow; instead, it uses empirical formulas to calculate the outdoor convective heat flux as follows:

$$q_{c,out} = U_f h_{out} (T_{w,out} - T_{a,out}) \quad (13)$$

where $T_{a,out}$ is the outdoor air temperature in the canopy layer, U_f is the wind speed, and convective heat transfer coefficient $h_{out} = 4.5 \left(\frac{W}{m^2 K} \right)$ is adopted.

The wind speed above the urban canopy layer (UCL) is calculated by a logarithm wind profile:

$$U(z) = \frac{u_*}{\kappa} \ln \left(\frac{z + z_0}{z_0} \right) \quad (14)$$

where $z_0 = 0.1H$ based on the estimation of ([Grimmond and Oke, 1999](#)).

The wind speed within the UCL is assumed to be uniform and is calculated by the model by Bentham and Britter ([Bentham and Britter, 2003](#)). This model estimates the in-canopy velocity (U_c) based on the frontal area density (λ_f) as follows:

$$\frac{U_c}{u_*} = \left(\frac{2}{\lambda_f} \right)^{0.5} \quad (16)$$

Here, the friction velocity (u_*) depends on the urban morphology and is estimated using the following functions ([Yuan et al., 2019](#)):

$$\begin{cases} u_* = 0.12U_{2H}, & \text{for } (\lambda_f > 0.4) \\ u_* = 6.7U_{2H}^3 - 6.4U_{2H}^2 + 1.7U_{2H} + 0.03, & \text{for } (\lambda_f < 0.4) \end{cases} \quad (17)$$

where U_{2H} is the wind speed at a height of $2H$ above the ground, and H is the building height.

The air temperature in UCL is assumed to be uniform and calculated by the urban canopy model ([Yuan et al., 2020](#)). This model estimates the in-canopy temperature based on the exchange velocity U_E and sensible heat flux $q_{c,out}$.

$$T_c = \frac{1}{D_c U_{2H} (1 - \lambda_p)} \left(1 - 0.12 \left(\frac{2}{\lambda_f} \right)^{0.5} \right) + T_{a,2H} \quad (18)$$



281 where $D_c = 17.183$, is a heat capacity constant of the air, $T_{a,2H}$ is the air temperature above the roof
282 level, λ_p is the plan area density. Bentham and Britter ([Bentham and Britter, 2003](#)) suggested that the
283 U_E can be calculated by:

$$284 \quad \frac{U_E}{u_*} = \left(\frac{U_{2H} - U_c}{u_*} \right)^{-1} \quad (19)$$

285 The $q_{c,out}$ is calculated by the temperature from previous time step.

286 **2.5. Indoor sub-model**

287 The indoor side uses a convective boundary condition given by $q_{in} = h_{in}(T_{w,in} - T_{a,in})$, where $T_{a,in}$ is
288 the indoor air temperature, $T_{w,in}$ is the wall temperature on indoor side. The indoor heat transfer
289 coefficient $h_{in} = 13.5 \frac{W}{m^2K}$ accounts for both natural convection and longwave radiative heat flux.

290 For air-conditioned rooms, the indoor air temperature is assumed to be constant at $T_{a,in} = 26$ °C. In
291 contrast, for naturally ventilated rooms, the indoor air temperature is assumed to be equal to the in-canopy
292 air temperature, represented as $T_{a,in} = T_c$.

293 **3. Model validation and assessment**

294 **3.1. SOMUCH measurement**

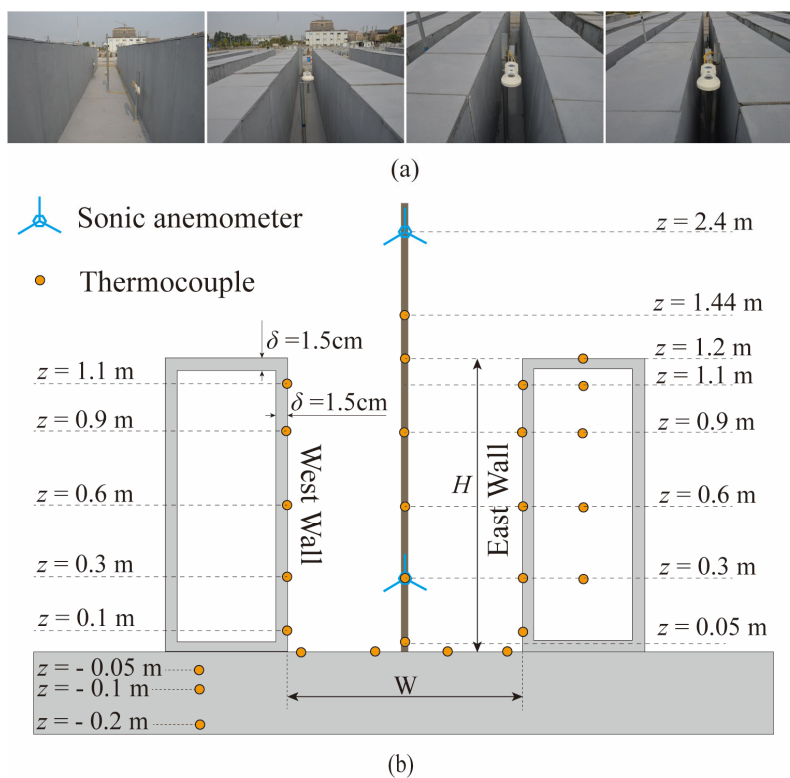
295 The model is validated by cross-compare with the SOMUCH measurement, which is a scale outdoor
296 field measurement conducted in Guangzhou, P.R. China (23°1' N, 113°25' E) ([Hang and Chen, 2022](#);
297 [Hang et al., 2025](#); [Wu et al., 2024](#)). This measurement provides a quality database for evaluating urban
298 climate models ([Hang et al., 2024](#); [Chen et al., 2025](#)). The campaign conducted from 29th Jan to 1st
299 Feb 2021 is used. In that campaign, both surface and air temperatures were measured at high resolution,
300 making it an ideal database for validating current models.

301 The geometry of the building blocks and measurement points are plotted in Fig. 7. In that measurement,
302 the urban buildings are modeled by hollow concrete blocks with a size of 0.5 m × 0.5 m × 1.2 m and a
303 thick of 0.015 m. The blocks are arranged to form street canyons with four different aspect ratios, i.e.,
304 H/W = 1, 2, 3, 6. Each row consists of 24 blocks and has a length of L = 12 m. In the experiment, the
305 surface and air temperatures are measured using thermocouples (Omega, TT-K-36-SLE, Φ0.127 mm and



306 TT-K- 30-SLE, $\Phi 0.255$ mm). The wind speeds inside and above the street canyon are measured using
307 sonic anemometers (Gill WindMaster). The incoming longwave and shortwave radiation are measured
308 using weather stations (RainWise PortLog). The thermal characteristics of the concrete and ground are
309 listed in Table 1.

310



311

312 **Figure 7: Photograph of the SOMUCH experiment (a). The geometry of concrete blocks and measurement**
313 **points in SOMUCH (b). The thermocouples are used to measure the surface temperature and air temperature.**

314 **The sonic anemometers are used to measure wind speed.**

315

316

317



Table 2. Thermal properties of the building material. The emissivity is for the longwave radiation and albedo is for the shortwave radiation.

Material	Density ρ (kg m ⁻³)	Conductivity k (W m ⁻¹ K ⁻¹)	Specific Heat Capacity c_p (J kg ⁻¹ K ⁻¹)	Emissivity ϵ	Albedo α
Concrete	2420	2.073	618	0.87	0.24

320

3.2. Cross comparison of the roof temperature

322 The surface temperature model is validated by cross-comparing with SOMUCH measurement. Many
 323 factors affect the accuracy of the model, including the radiation, convective and conduction. To
 324 separately investigate these factors, the temperatures at roofs are first validated because the total radiative
 325 flux of roof is only influenced by the incoming longwave and shortwave radiation. The shading effect of
 326 other blocks can be ignored as the block heights are uniform. Therefore, the accuracy of conductive and
 327 convective sub-models can be separately evaluated.

328 The accuracy of this model is quantitatively evaluated by two statistical parameters, the root mean square
 329 error (RMSE), and coefficient of determination (R^2). The RMSE and R^2 of u_x^* are calculated by:

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (O_i - P_i)^2} \quad (21)$$

$$R^2 = 1 - \frac{\sum_{i=1}^n (O_i - P_i)^2}{\sum_{i=1}^n (O_i - \overline{O_i})^2} \quad (22)$$

332 where O_i represents the measured values, P_i is the simulated values, $\overline{O_i}$ is the mean of the measured
 333 values, and n is the number of data points.

334 The wind speed at roof level is needed to calculate the outdoor convective flux of roofs. In SOMUCH
 335 measurement, the wind speed was measured above the roof and at a height of $2H$. The wind speed at
 336 roof level is estimated by a logarithm wind profile as:



$$U(z) = \frac{u_*}{\kappa} \ln \left(\frac{z + z_0}{z_0} \right) \quad (23)$$

where $z_0 = 0.1H$ based on the estimation of (Grimmond and Oke, 1999). The wind velocity at roof level ($z = H$) can be calculated by $\frac{U_H}{U_{2H}} = 0.787$. The outdoor air temperature, incoming shortwave and longwave radiation, are from the weather station ($z = 2H$).

For the indoor side, the radiative flux between indoor surfaces is ignored in this model. Only the convective flux is modeled. The convective velocity is assumed to be 3 m/s and CHTC is assumed to be 4.5 for indoor side. Data from the indoor measurement point at $H = 1.1$ m is used. That point is the nearest measurement point to the roof.

Figure 8(a) plotted the measurement data that was used to drive the model. Fig. 8(b) shows the roof surface temperatures from measurement and simulation. Generally, the roof surface temperatures are well reproduced by the model, because the R^2 is 0.99 and $RMSE$ is 1.28. The large discrepancy is found around noon. The model slightly overestimates the roof temperature. The comparison of roof temperatures shows that the conductive and convective sub-models are reliable.

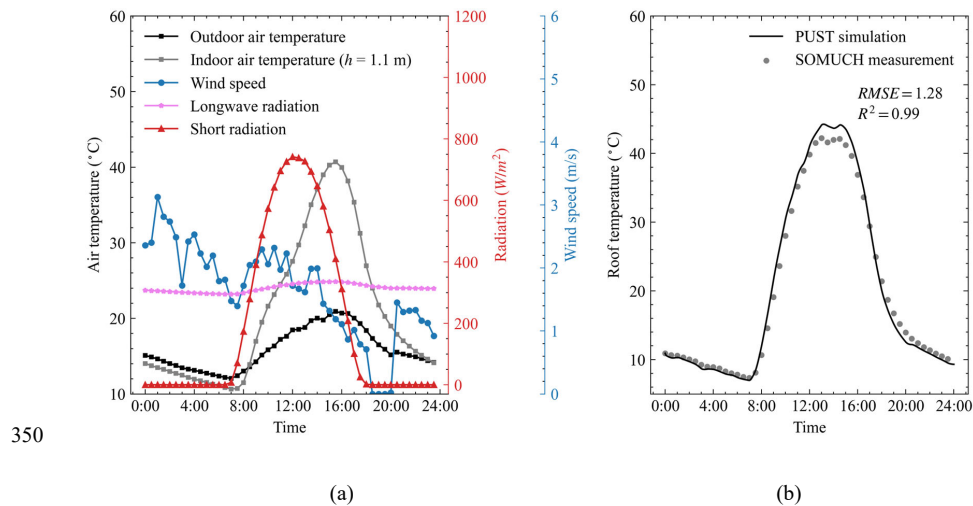


Figure 8: The weather data on the measurement date (measured on 29th Jan 2021) is plotted in (a). Comparison of the roof surface temperatures from simulation and measurement (b). The points represent measured data and lines represent the simulated data.



354 3.3. Cross comparison of the wall temperature

355 The temperatures at walls are more complicated than those at the roof because the buildings change the
356 radiative fluxes and wind speeds in street canyons. The radiative fluxes need to be accurately modelled
357 as they are the main energy input and have a large impact on the surface temperature. To avoid the
358 influence of air temperature and wind speed modeling, the canyon air temperature, wind speed, and
359 indoor temperature are from the measurement. The air temperatures are measured from multiple heights.
360 For the convective flux modelling, the nearest measured air temperatures are used. The wind speeds from
361 the sonic anemometer in the street canyon ($z = 0.3$ m) are used to calculate the convective flux at outdoor
362 side. The driving data are plotted in Appendix A.

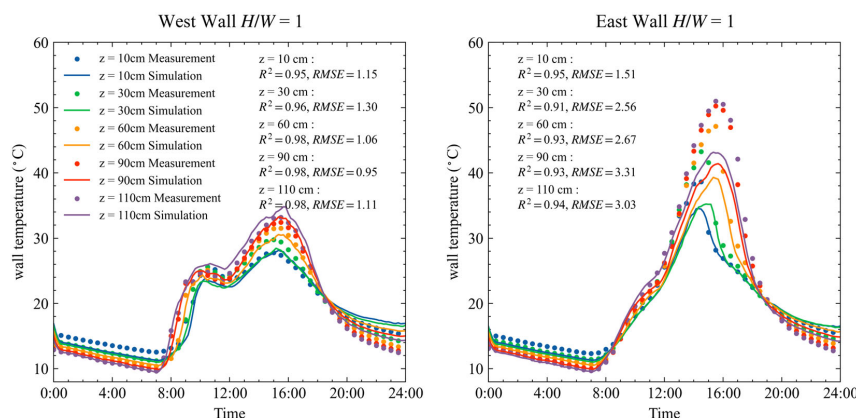
363 The east and west walls are defined by taking street canyon center as the origin point. The street direction
364 is tilted from north toward east by 25° . Therefore, the west and east walls are roughly defined to
365 distinguish them. The street orientation has been modeled in our model and will not cause additional
366 discrepancy.

367 Figure 9 shows the comparison of wall temperatures from simulation and measurement. The R^2 and
368 RMSE are calculated and marked in each sub-figure. Generally, the wall temperatures are well
369 reproduced, particularly their variation trend. The peak hours are well reproduced. For example, there
370 are two temperature peaks for the west wall. The first one is around 10:00 and the second is around 16:00.
371 Both simulation and measurement show the same occurring time. The accuracy of wall temperature
372 modeling varies from point to point. There are two main observations from the comparison of wall
373 temperatures.

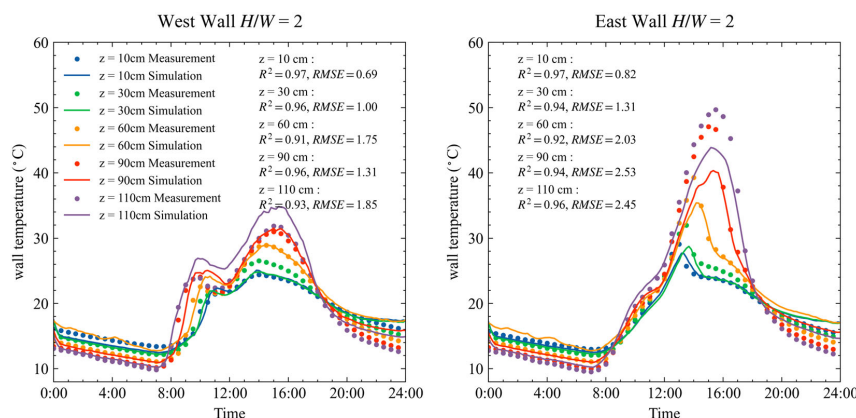
374 a) Accuracy Difference Between Walls: The temperatures on the east wall are modeled more accurately
375 than those on the west wall, as the model tends to underestimate the peak temperatures on the west wall.
376 For $H/W = 1$, the R^2 values for west wall temperatures range from 0.95 to 0.98, while those for east wall
377 temperatures range from 0.91 to 0.95. For $H/W = 2$, the R^2 values for the west and east wall temperatures
378 show only a slight difference. However, the RMSE values for the west wall, which range from 0.69°C to
379 1.85°C , are evidently lower than those for the east wall, which range from 0.82°C to 2.53°C . The R^2 and
380 RMSE values for $H/W = 3$ are comparable to those for $H/W = 2$.



b) Accuracy Difference Between Points: The underestimation of west wall temperature particularly pronounced at higher levels ($z = 90$ cm and 110 cm). At lower levels ($z = 10$ cm and 30 cm), temperatures are underestimated at night. The largest discrepancies occur at these lower levels in $H/W = 6$, with a minimum R^2 of 0.51 and a maximum RMSE of 1.98°C . The R^2 values suggest that wall temperatures at these levels are estimated poorly; however, the RMSE values do not appear abnormally high, reaching 2.53°C at $z = 90$ cm in $H/W = 2$. The main reason for this discrepancy is that wall temperatures in deep street canyons ($H/W = 6$) show only a slight increase compared to the air temperature, due to minimal sunlight penetration into the canyon. In these cases, wall temperatures can be highly sensitive to convective and longwave radiative fluxes.



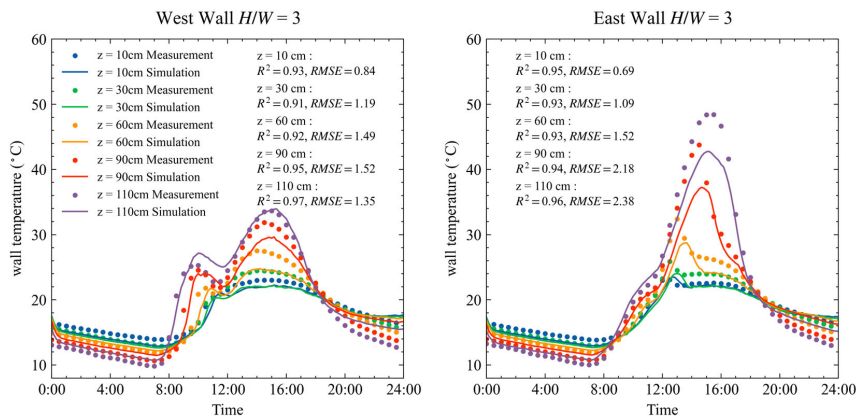
(a) $H/W = 1$





393

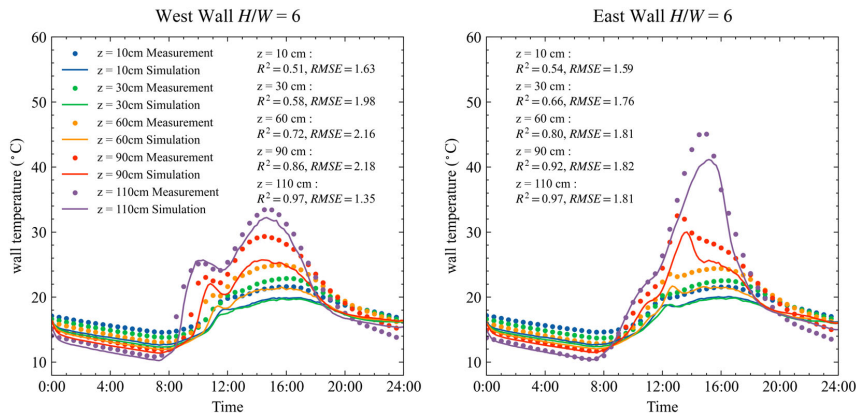
(b) $H/W = 2$



394

395

(c) $H/W = 3$



396

397

(d) $H/W = 6$

398 **Figure 9: Wall temperature comparison between the simulation and measurement results at street canyon**
399 **aspect ratio of $H/W = 1.0, 2.0, 3.0$, and 6.0 . Surface temperatures are measured on 29th Jan 2021. The root**
400 **mean square error (RMSE), and coefficient of determination (R^2) are calculate and plotted. The points**
401 **represent measured data and lines represent the simulated data.**

402



403 3.4. Cross comparison of the ground temperature

404 The surface temperatures of the ground are heavily influenced by heat storage. During the day, heat is
405 conducted to deeper layers and stored there. At night, this stored heat is released. Therefore, the initial
406 temperature field and boundary conditions are critical for accurately modeling surface temperatures. In
407 this study, an adiabatic boundary condition is applied at a depth of 0.5 m below the ground surface. The
408 soil material is divided into three layers with thicknesses of 0.2 m, 0.15 m, and 0.15 m. All three layers
409 are assumed to be made of concrete. The thermal properties in Table 1 are used. The underground
410 temperatures are measured by thermocouples with three depths of 5 cm, 10 cm, and 20 cm, as plotted in
411 Appendix A. In this study, we used only the measured underground temperatures at 0:00 to initialize the
412 underground temperature field. It is important to note that the available soil temperatures were measured
413 in open ground rather than under street canyons. This difference may lead to discrepancies in modeling
414 ground surface temperatures.

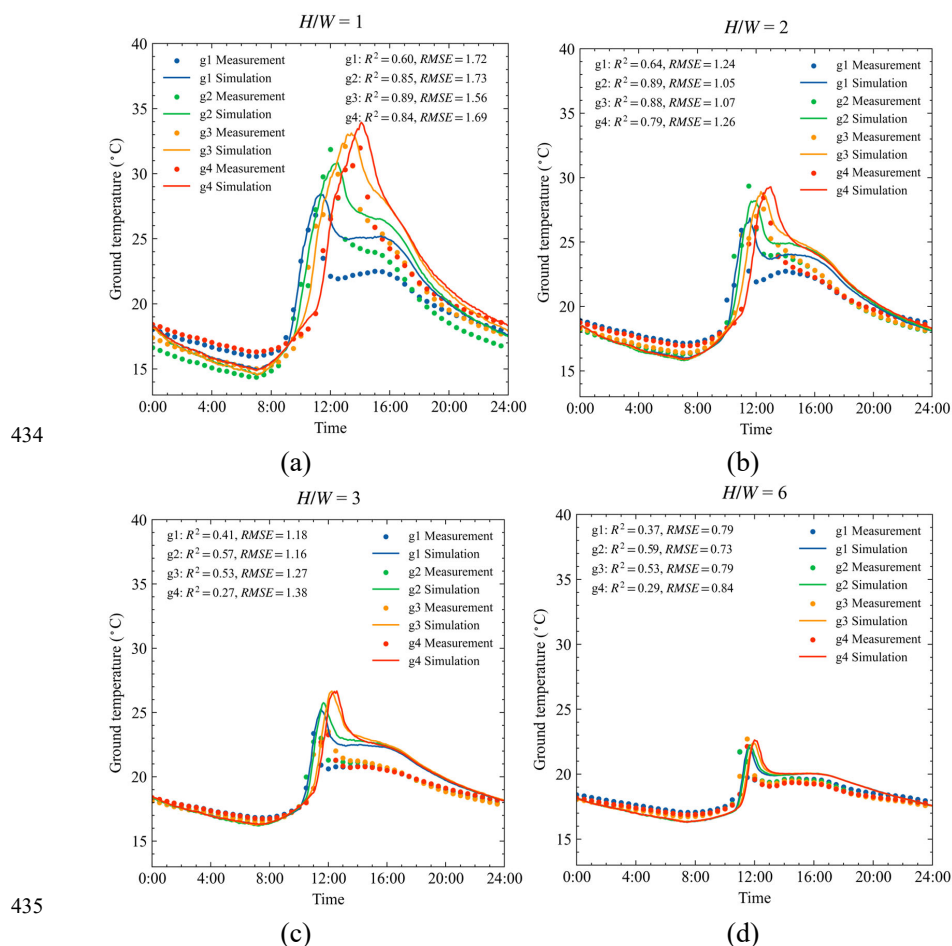
415 Figure 10 shows the ground surface temperatures from measurement and simulation. The ground surface
416 temperatures are measured at four locations: g1, which is close to west wall; g4, which is close to east
417 wall; and g2 and g3, which are situated in the middle of the streets. Generally, the temperature variations
418 are well reproduced by the model. For example, peak temperatures occur sequentially from g1 to g4 due
419 to the movement of the building's shadow. This phenomenon is observed in both simulations and
420 measurements.

421 The accuracy of ground temperatures is lower than that of the wall temperatures in terms of R^2 . For
422 example, in $H/W = 2$, the R^2 values for temperatures at the west wall range from 0.91 to 0.97, while
423 those at the ground range from 0.64 to 0.89. However, the ground temperatures can be considered better
424 modeled because the RMSE for ground temperatures is smaller than that for wall temperatures. Using
425 $H/W = 2$ as an example, the RMSE values for the west wall range from 0.69 to 1.85 °C, while those for
426 the ground range from 1.05 to 1.24 °C. This difference between the R^2 and RMSE values is due to the
427 ground temperature increase being much lower than that of the walls because of shading, particularly in
428 deep street canyons.

429 Uncertainties in the input data may also contribute to the discrepancies between simulation and



430 measurement. First, the thermal properties of soil can differ significantly from those of concrete blocks.
431 Secondly, the initial temperature is measured in surrounding area, rather than in street canyons. Thirdly,
432 since the same initial temperature field is used for all four points, the model is unable to reproduce the
433 differences between points at night.



436 **Figure 10: Ground temperature comparison between the simulation and measurement results at street canyon**
437 **aspect ratio of $H/W = 1.0, 2.0, 3.0$, and 6.0 . Surface temperatures are measured on 29th Jan 2021. The root**
438 **mean square error (RMSE), and coefficient of determination (R^2) are calculate and plotted. The points**
439 **represent measured data and lines represent the simulated data.**



3.5. Surface energy balance analysis

The surface temperature comparison indicates that model uncertainties arise from various factors. To identify the main factors impacting the model accuracy, the energy balance of wall surface is analyzed. The heat fluxes of shortwave (Q_K), longwave radiation (Q_L), convection (Q_H), and conduction (Q_G) of outer surface of walls satisfy the following equation:

$$Q_K + Q_L + Q_G + Q_H = 0 \quad (24)$$

Here, the longwave heat flux Q_L is divided into two parts as the heat exchange between wall to sky ($Q_{L,sky}$) and to other urban surfaces ($Q_{L,urban}$), expressed as $Q_L = Q_{L,sky} + Q_{L,urban}$. This analysis aims to determine whether it is necessary to model the longwave heat exchange between urban surfaces, which requires substantial computational resources.

Figure 11 shows the heat fluxes of walls in the simulation. The heat fluxes of east and west walls are averaged from five measurement points on each. Our previous study has demonstrated that the Monte Carlo ray tracing method has good accuracy in predicting solar radiation.

In all cases, longwave radiative heat exchange between urban surfaces plays an important role in the energy balance, particularly at high aspect ratios. The longwave radiative fluxes from sky only contribute a small amount of total longwave radiative flux in $H/W = 6$, as shown in Fig. 10(d). The shading effect of buildings creates heterogeneous surface temperatures within the urban canopy layer. The large temperature differences between surface elements contribute a large portion of the total heat flux. This highlights the necessity for accurate modeling of longwave heat exchange between urban surfaces, even though it demands significant computational resources.

The conductive heat flux also contributes a large portion of the total heat flux. It is negative in the morning and positive in the afternoon, meaning that heat is stored in the building block during the morning and released in the afternoon. In the reduced scale experiment, buildings were represented by airtight hollow concrete blocks. Due to the lack of ventilation, the indoor air temperature can rise to 40°C under an outdoor air temperature of 20°C, as shown in Appendix A. This indicates that the indoor air can also absorb, store, and release a considerable amount of heat. Therefore, accurately modeling indoor



air temperature is essential for effective surface temperature modeling.

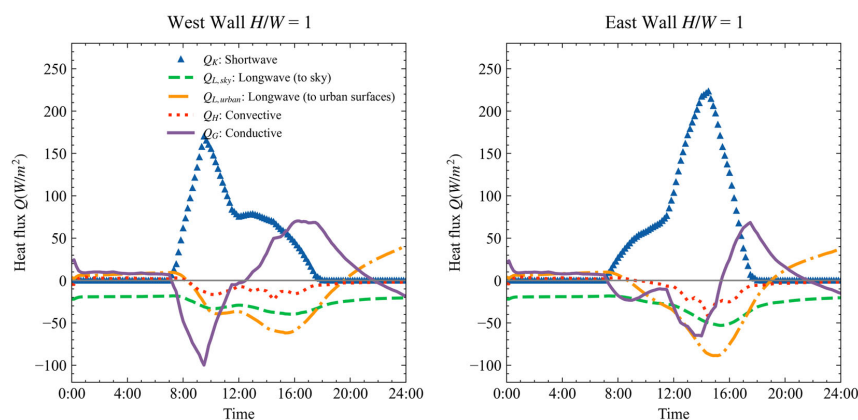
The convective contributes a smaller amount of the total heat flux. In high aspect ratio cases ($H/W = 3$

and 6), the convective heat fluxes are almost negligible. This is due to the weak wind in the deep street

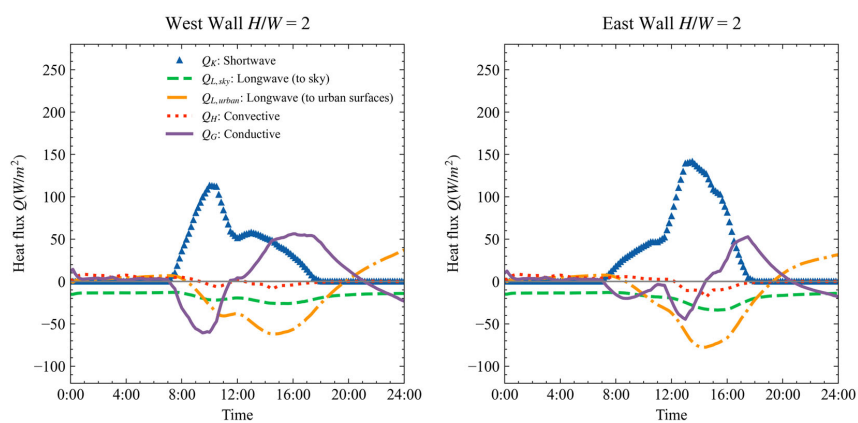
canyons. In this model, the surface convective heat flux is directly calculated from the wind speeds in

street canyons. This assumption may underestimate the convective flux, especially since natural

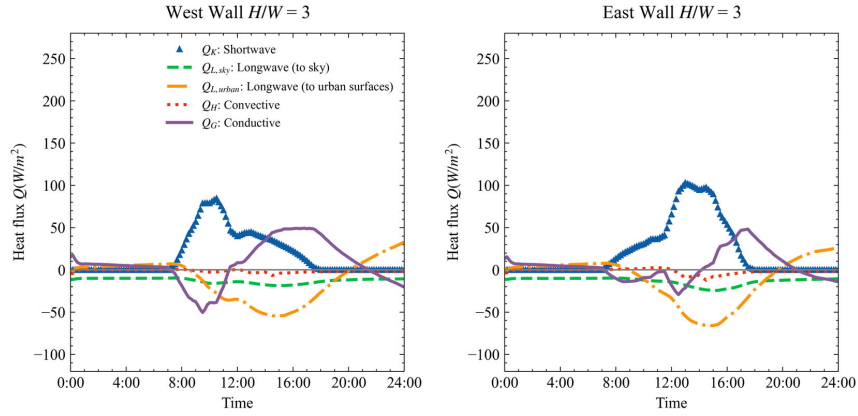
convection occurs under weak wind conditions (Fan et al., 2021).



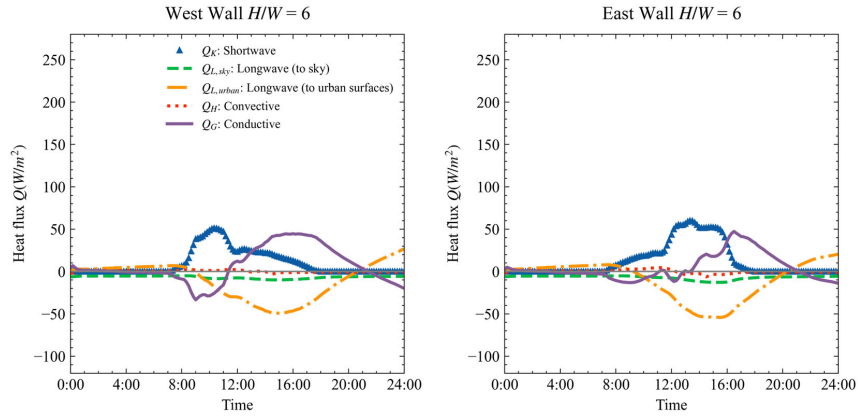
(a) $H/W = 1$



(b) $H/W = 2$



(c) $H/W = 3$



(d) $H/W = 6$

Figure 11: Diurnal heat fluxes from the simulation. The heat fluxes of shortwave (Q_K), longwave radiation (Q_L), convection (Q_H), and conduction (Q_G) are at the outer surface of walls.

4. Application to real urban configuration

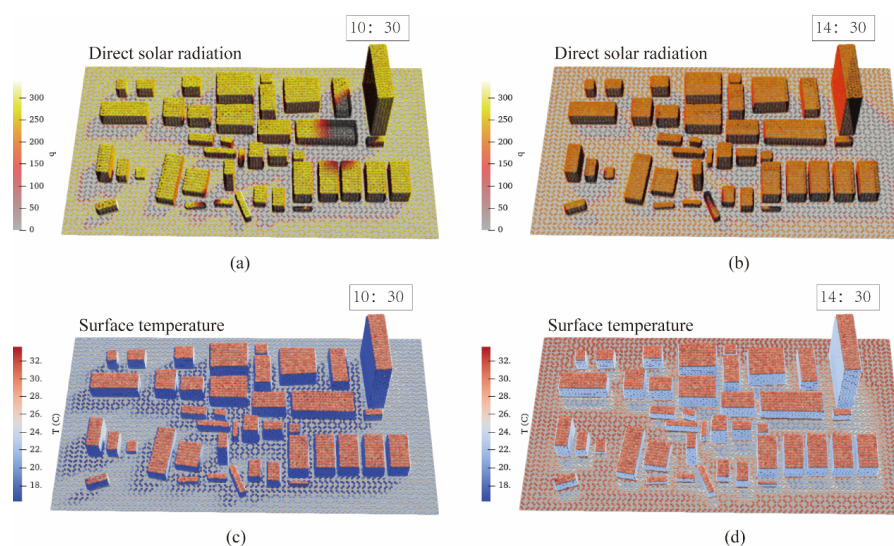
To show how this model can be implemented in complex geometries, a neighborhood with 40 buildings is modeled. The building geometries are constructed by *.stl* files with 2.3×10^4 triangular surface meshes. The surface temperatures are calculated on the grids. As a demonstration case, the complex



488 albedo of urban surfaces is ignored. A uniform albedo of 0.24 is used for all urban surfaces. The walls,
489 roofs, and ground are assumed to be constructed by three layers of concrete. The layer thickness of walls
490 and roofs is 10 cm. The total thickness of the ground is 35cm, with an adiabatic bottom boundary. The
491 buildings are assumed to be naturally ventilated, with the indoor and outdoor air temperatures being the
492 same. The thermal characteristics of concrete are assumed to be the same as in the SOMUCH experiment.

493 The surface temperatures are calculated in three steps: 1) calculate the solar radiative flux of each point
494 by rMCRT; 2) calculate the view factors between the elements using rMCRT; 3) calculate the surface
495 temperatures using Monte Carlo random walking. All three steps are processed in parallel on GPU. The
496 weather data measured on 29th Jan 2021 during the SOMUCH experiment is used as the driving input.
497 The surface temperatures are calculated from 0:00 to 24:00, with a time step of 30 minutes.

498 The simulation results are output in *.vtk* format and visualized using ParaView. Fig. 12 shows the direct
499 shortwave radiation and surface temperatures at 10:30 and 14:30. The movement of building shadows
500 and their impact on surface temperatures are clearly observed in these contours. These contours
501 demonstrate that this model can be applied to complex buildings in real urban areas.



502
503 **Figure 12: Radiation and temperature simulation results for complex building geometries. The direct**
504 **shortwave radiation at 10:30 (a) and 14:30 (b). The surface temperatures at 10:30 (c) and 14:30 (d).**



505 **5. Limitations and future work**

506 The first version focuses on the complex radiative exchange in densely built urban areas. The parameters
507 and assumptions are validated against the idealized scaled outdoor experiment, which uses homogeneous
508 building materials with consistent albedo and thermal characteristics. Glazing and green infrastructure
509 are not included in this experiment. The SOMUCH project is currently measuring the impact of glass
510 and green infrastructure. The next version will expand its capabilities to capture complex urban materials,
511 such as urban trees, green walls, and glass curtain walls, to better represent real urban configurations.
512 Other limitations include:

- 513 • All reflections are assumed to be Lambertian. While this assumption works well for the SOMUCH
514 measurements, where concrete is used for all urban surfaces, it may not fully capture the reflective
515 properties of other materials with different surface textures, such as glass or vegetation.
- 516 • The high-resolution wall temperature simulation still requires a significant amount of time to
517 complete, even with parallel computation on GPUs. This is due to the large number of rays ($N =$
518 10^6) required for accurate solar radiation modeling. For each point, the simulation takes about 1
519 second to finish. However, as the number of test points increases, the overall computational time
520 grows substantially.
- 521 • The dynamic indoor air temperature is not included in this model. It assumes that the indoor air
522 temperature is equal to the outdoor air temperature for a natural ventilated room. This assumption
523 may lead to discrepancies, particularly in situations where indoor temperatures differ from outdoor
524 conditions due to factors such as heat sources, insulation, or limited ventilation.
- 525 • The participation of the urban atmosphere is ignored in this study. In the scaled measurements,
526 longwave radiation travels much shorter distances to adjacent surfaces, which reduces the influence
527 of atmospheric effects compared to real-world urban environments.

528 **6. Conclusions**

529 This study introduces a GPU-accelerated Urban Surface Temperature model (GUST), which solves the
530 conduction-radiation-convection coupled heat transfer using Monte Carlo method. The GPU parallel
531 computing is adopted to address the large computational demands of Monte Carlo method. This model



532 is validated with a scaled outdoor experiment (SOMUCH), which has a high spatial and temporal
533 resolution.

534 The radiative heat flux is simulated using a reverse Monte Carlo Ray Tracing method, which allows for
535 the accurate reproduction of multiple reflections in high-density urban areas. The sensitivity test shows
536 that $10^5 \sim 10^6$ rays are required for each point to accurately model the shortwave radiation. This large
537 amount of ray tracing can only be achieved using GPU parallel computing. The Monte Carlo method is
538 also used to solve the couple heat transfer using random walking algorithms, which is suitable for GPU-
539 based coding.

540 The comparison with the SOMUCH experiment shows that the transient surface temperatures on roofs,
541 walls and the ground are well reproduced. A relatively large discrepancy is observed in cases with high
542 building density, where the wall temperatures are highly sensitive to convective and longwave radiative
543 fluxes. The surface energy balance analysis shows that longwave radiation exchange between urban
544 surfaces plays a critical role across all building densities. In contrast, convective heat flux only plays a
545 significant role in high-density cases. In future versions, the simulation of convective heat flux could be
546 improved by simulating urban airflow.

547 Lastly, this model is implemented to solve the surface temperatures on complex urban buildings, which
548 are composed of a total of 2.3×10^4 surface elements. The GPU allows simultaneous simulation of
549 heat transfer and view factors across all elements, enabling high-fidelity simulations in real urban
550 configurations with complex geometries. The current version focuses on the radiation-conduction-
551 convection coupled heat transfer coupled in complex geometries. Future developments will prioritize the
552 integration of complex glazing systems and green infrastructure in urban environments.

553

554 **Code availability**

555 The SOMUCH measurement data is available upon request. The development of GUST, model validation,
556 and visualization in this study were conducted using Python 3.8 with CUDA. The source code, supporting
557 data, and simulation results presented in this paper are archived on Zenodo at



558 <https://doi.org/10.5281/zenodo.15074365> (Mei, 2025). Users are requested to contact the corresponding
559 authors to obtain access to the code free of charge for research purposes under a collaboration agreement
560 (meishj@mail.sysu.edu.cn).

561

562 **Author contributions**

563 SM designed the study, developed the code, conducted the analysis. SM and GC prepared the manuscript
564 draft. GC and JH collected and shared SOMUCH measurements for the purpose of model validation. GC,
565 JH and TS supported the model implementation and data analysis. All have read and accepted the
566 manuscript for submission.

567

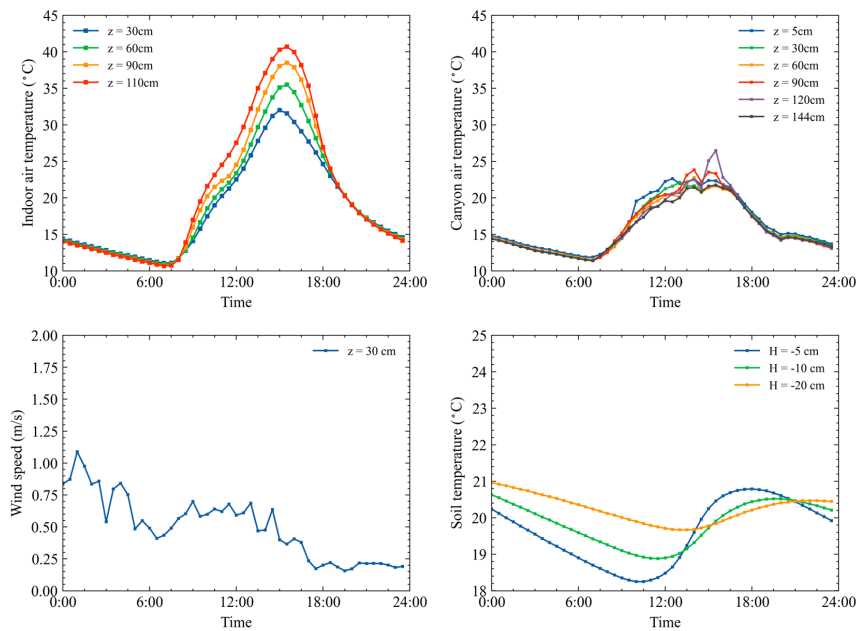
568 **Acknowledgement**

569 This research is supported by National Natural Science Foundation of China (Grant No. 42305076,
570 W2421048, U2442212), Natural Science Foundation of Guangdong Province, China (Grant No.
571 2024A1515010173) and Overseas Postdoctoral Talents 2023 Programme (Grant No. BH2023009). Dr.
572 Shuo-Jun Mei and Dr. Ting Sun are supported by an International Exchanges grant from the Royal
573 Society (Grant No. IEC\NSFC\242040) and National Natural Science Foundation of China (Grant No.
574 W2421048).

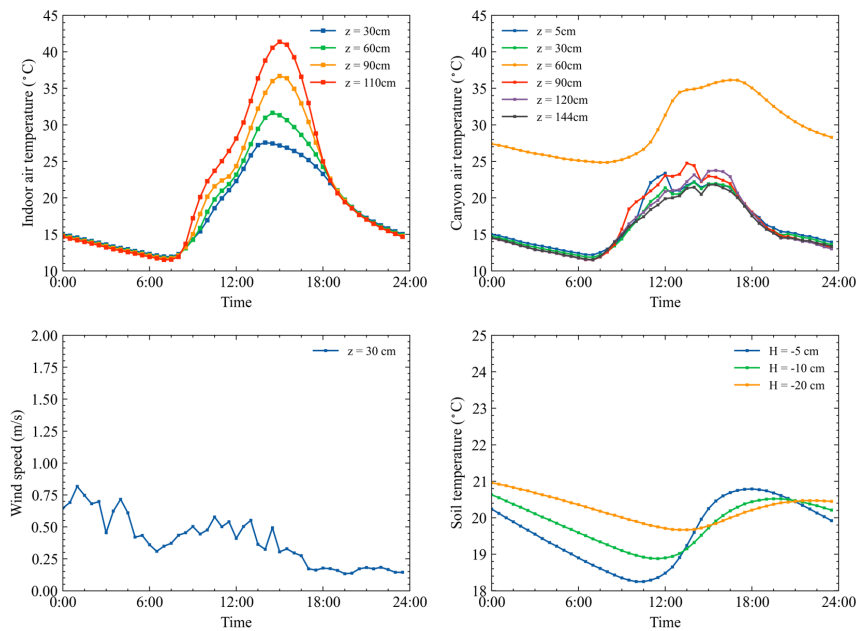
575

576 **Appendix A. Indoor and outdoor air temperatures in SOMUCH measurement**

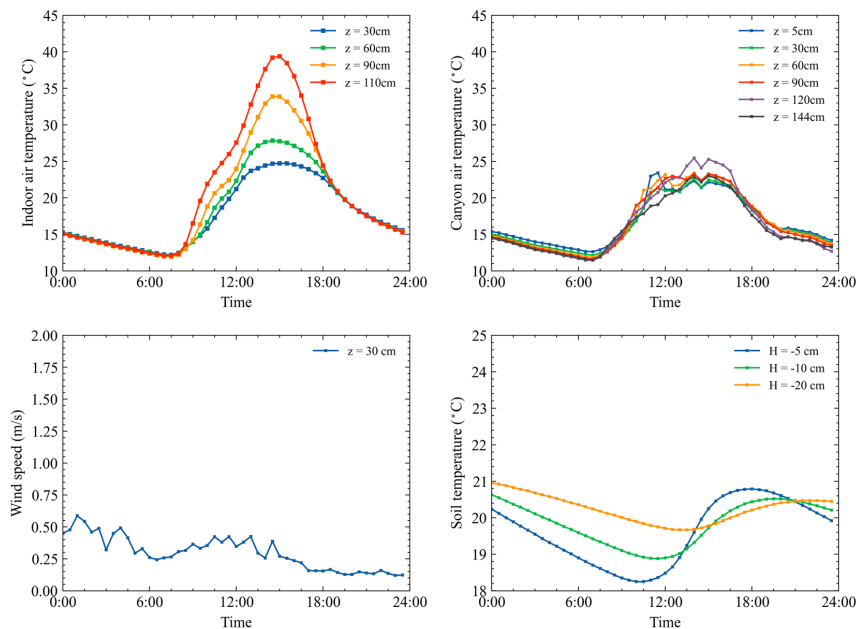
577 The indoor and outdoor air temperatures at different levels in the SOMUCH measurement are plotted in
578 Fig. A1. These air temperatures serve as input data for the validation cases.



(a) $H/W = 1$



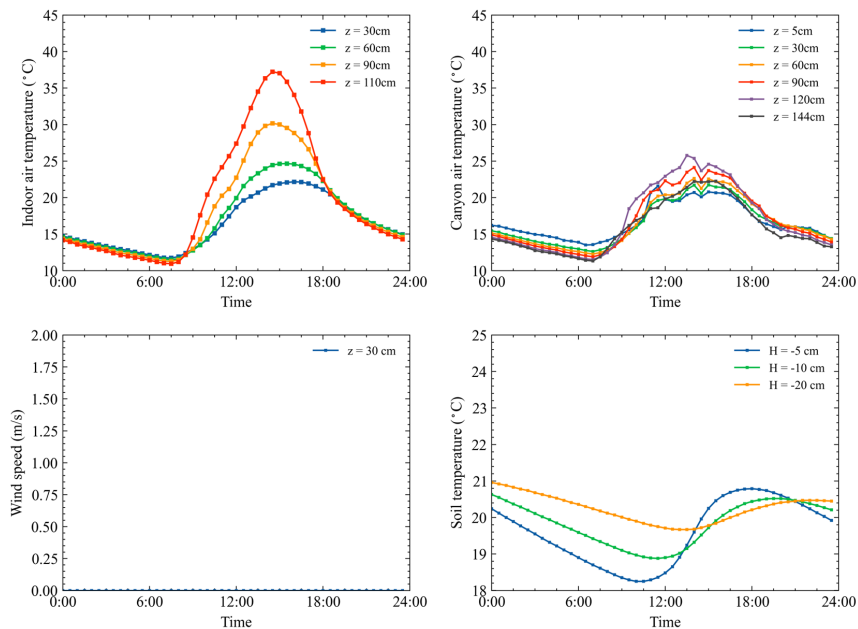
(b) $H/W = 2$



583

584

(c) $H/W = 3$



585

586

(d) $H/W = 6$



587 **Figure A1: Indoor, outdoor air temperatures, and wind speeds in street canyons that are measured on 29th**
588 **Jan 2021. The wind speeds in the street canyon of $H/W = 6$ were not measured because the sonic anemometer**
589 **cannot be installed in such a narrow street. The outdoor air temperatures measured at $z = 60$ cm in $H/W = 2$**
590 **are unusual, due to an instrument failure.**

591

592 **References**

- 593 Bentham, T. and Britter, R.: Spatially averaged flow within obstacle arrays, *Atmospheric Environment*,
594 37, 2037-2043, [https://doi.org/10.1016/S1352-2310\(03\)00123-7](https://doi.org/10.1016/S1352-2310(03)00123-7), 2003.
- 595 Caliot, C., d'Alençon, L., Blanco, S., Forest, V., Fournier, R., Hourdin, F., Retailleau, F., Schoetter, R.,
596 and Villefranche, N.: Coupled heat transfers resolution by Monte Carlo in urban geometry including
597 direct and diffuse solar irradiations, *International Journal of Heat and Mass Transfer*, 222, 125139,
598 <https://doi.org/10.1016/j.ijheatmasstransfer.2023.125139>, 2024.
- 599 Carmeliet, J. and Derome, D.: How to beat the heat in cities through urban climate modelling, *Nature*
600 *Reviews Physics*, 6, 2-3, 10.1038/s42254-023-00673-1, 2024.
- 601 Chen, G., Mei, S.-J., Hang, J., Li, Q., and Wang, X.: URANS simulations of urban microclimates:
602 Validated by scaled outdoor experiments, *Building and Environment*, 272, 112691,
603 <https://doi.org/10.1016/j.buildenv.2025.112691>, 2025.
- 604 Ebi, K. L., Capon, A., Berry, P., Broderick, C., de Dear, R., Havenith, G., Honda, Y., Kovats, R. S., Ma,
605 W., Malik, A., Morris, N. B., Nybo, L., Seneviratne, S. I., Vanos, J., and Jay, O.: Hot weather and
606 heat extremes: health risks, *The Lancet*, 398, 698-708, [https://doi.org/10.1016/S0140-](https://doi.org/10.1016/S0140-6736(21)01208-3)
607 [6736\(21\)01208-3](https://doi.org/10.1016/S0140-6736(21)01208-3), 2021.
- 608 Eingrüber, N., Domm, A. S., Korres, W., and Schneider, K.: Simulation of the heat mitigation potential
609 of unsealing measures in cities by parameterizing grass grid pavers for urban microclimate modelling
610 with ENVI-met (V5), *EGUsphere*, 2024, 1-25, 10.5194/egusphere-2024-697, 2024.
- 611 Fan, Y., Zhao, Y., Torres, J. F., Xu, F., Lei, C., Li, Y., and Carmeliet, J.: Natural convection over vertical
612 and horizontal heated flat surfaces: A review of recent progress focusing on underpinnings and
613 implications for heat transfer and environmental applications, *Physics of Fluids*, 33, 101301,
614 10.1063/5.0065125, 2021.
- 615 Feng, J., Gao, K., Khan, H., Ulpiani, G., Vasilakopoulou, K., Young Yun, G., and Santamouris, M.:
616 Overheating of Cities: Magnitude, Characteristics, Impact, Mitigation and Adaptation, and Future
617 Challenges, *Annual Review of Environment and Resources*, 48, 651-679,
618 <https://doi.org/10.1146/annurev-environ-112321-093021>, 2023.
- 619 Forouzandeh, A.: Prediction of surface temperature of building surrounding envelopes using holistic
620 microclimate ENVI-met model, *Sustainable Cities and Society*, 70, 102878,



- 621 <https://doi.org/10.1016/j.scs.2021.102878>, 2021.
- 622 Grimmond, C. S. B. and Oke, T. R.: Aerodynamic properties of urban areas derived from analysis of
623 surface form, *Journal of Applied Meteorology*, 38, 1262, 10.1175/1520-
624 0450(1999)038<1262:APOUAD>2.0.CO;2, 1999.
- 625 Hang, J. and Chen, G.: Experimental study of urban microclimate on scaled street canyons with various
626 aspect ratios, *Urban Climate*, 46, 101299, <https://doi.org/10.1016/j.uclim.2022.101299>, 2022.
- 627 Hang, J., Zeng, L., Li, X., and Wang, D.: Evaluation of a single-layer urban energy balance model using
628 measured energy fluxes by scaled outdoor experiments in humid subtropical climate, *Building and*
629 *Environment*, 254, 111364, <https://doi.org/10.1016/j.buildenv.2024.111364>, 2024.
- 630 Hang, J., Lu, M., Ren, L., Dong, H., Zhao, Y., and Zhao, N.: Cooling performance of near-infrared and
631 traditional high-reflective coatings under various coating modes and building area densities in 3D
632 urban models: Scaled outdoor experiments, *Sustainable Cities and Society*, 121, 106200,
633 <https://doi.org/10.1016/j.scs.2025.106200>, 2025.
- 634 Hénou, A., Mestayer, P. G., Lagouarde, J.-P., and Voogt, J. A.: An urban neighborhood temperature and
635 energy study from the CAPITOU experiment with the Solene model, *Theoretical and Applied*
636 *Climatology*, 110, 197-208, 10.1007/s00704-012-0616-z, 2012.
- 637 Imbert, C., Bhattacharjee, S., and Tencar, J.: Simulation of urban microclimate with SOLENE-
638 microclimat: an outdoor comfort case study, *Proceedings of the Symposium on Simulation for*
639 *Architecture and Urban Design*, Delft, Netherlands2018.
- 640 Kondo, A., Ueno, M., Kaga, A., and Yamaguchi, K.: The Influence Of Urban Canopy Configuration On
641 Urban Albedo, *Boundary-Layer Meteorology*, 100, 225-242, 10.1023/A:1019243326464, 2001.
- 642 Krayenhoff, E. S. and Voogt, J. A.: A microscale three-dimensional urban energy balance model for
643 studying surface temperatures, *Boundary-Layer Meteorology*, 123, 433-461, 10.1007/s10546-006-
644 9153-6, 2007.
- 645 Manoli, G., Fatichi, S., Schläpfer, M., Yu, K., Crowther, T. W., Meili, N., Burlando, P., Katul, G. G., and
646 Bou-Zeid, E.: Magnitude of urban heat islands largely explained by climate and population, *Nature*,
647 573, 55-60, 10.1038/s41586-019-1512-9, 2019.
- 648 Mei, S.-J.: GUST1.0: A GPU-accelerated 3D Urban Surface Temperature Model (1.0), Zenodo [dataset],
649 <https://doi.org/10.5281/zenodo.15074365>, 2025.
- 650 Owens, S. O., Majumdar, D., Wilson, C. E., Bartholomew, P., and van Reeuwijk, M.: A conservative
651 immersed boundary method for the multi-physics urban large-eddy simulation model uDALES v2.0,
652 *Geoscientific Model Development*, 17, 6277-6300, 10.5194/gmd-17-6277-2024, 2024.
- 653 Reindl, D. T., Beckman, W. A., and Duffie, J. A.: Diffuse fraction correlations, *Solar Energy*, 45, 1-7,
654 [https://doi.org/10.1016/0038-092X\(90\)90060-P](https://doi.org/10.1016/0038-092X(90)90060-P), 1990.
- 655 Resler, J., Krc, P., Belda, M., Jurus, P., Benesova, N., Lopata, J., Vlcek, O., Damaskova, D., Eben, K.,
656 Derbek, P., Maronga, B., and Kanani-Suhring, F.: PALM-USM v1.0: A new urban surface model



- integrated into the PALM large-eddy simulation model, *Geoscientific Model Development*, 10, 3635-3659, 10.5194/gmd-10-3635-2017, 2017.
- Rodriguez, A., Lecigne, B., Wood, S., Carmeliet, J., Kubilay, A., and Derome, D.: Optimal representation of tree foliage for local urban climate modeling, *Sustainable Cities and Society*, 115, 105857, <https://doi.org/10.1016/j.scs.2024.105857>, 2024.
- Salim, M. H., Schlünzen, K. H., Grawe, D., Boettcher, M., Gierisch, A. M. U., and Fock, B. H.: The microscale obstacle-resolving meteorological model MITRAS v2.0: model theory, *Geoscientific Model Development*, 11, 3427-3445, 10.5194/gmd-11-3427-2018, 2018.
- Schoetter, R., Caliot, C., Chung, T.-Y., Hogan, R. J., and Masson, V.: Quantification of Uncertainties of Radiative Transfer Calculation in Urban Canopy Models, *Boundary-Layer Meteorology*, 189, 103-138, 10.1007/s10546-023-00827-9, 2023.
- Talebi, S., Gharehbash, K., and Jalali, H. R.: Study on random walk and its application to solution of heat conduction equation by Monte Carlo method, *Progress in Nuclear Energy*, 96, 18-35, <https://doi.org/10.1016/j.pnucene.2016.12.004>, 2017.
- Toparlar, Y., Blocken, B., Vos, P., van Heijst, G. J. F., Janssen, W. D., van Hooff, T., Montazeri, H., and Timmermans, H. J. P.: CFD simulation and validation of urban microclimate: A case study for Bergpolder Zuid, Rotterdam, *Building and Environment*, 83, 79-90, <https://doi.org/10.1016/j.buildenv.2014.08.004>, 2015.
- Tregan, J. M., Amestoy, J. L., Bati, M., Bezian, J.-J., Blanco, S., Brunel, L., Caliot, C., Charon, J., Cornet, J.-F., Coustet, C., d'Alençon, L., Dauchet, J., Dutour, S., Eibner, S., El Hafi, M., Eymet, V., Farges, O., Forest, V., Fournier, R., Galtier, M., Gattepaille, V., Gautrais, J., He, Z., Hourdin, F., Ibarrart, L., Joly, J.-L., Lapeyre, P., Lavieille, P., Lecureux, M.-H., Lluc, J., Miscevic, M., Mourtaday, N., Nyffenegger-Péré, Y., Pelissier, L., Penazzi, L., Piaud, B., Rodrigues-Viguié, C., Roques, G., Roger, M., Saez, T., Terrée, G., Villefranque, N., Vourc'h, T., and Yaacoub, D.: Coupling radiative, conductive and convective heat-transfers in a single Monte Carlo algorithm: A general theoretical framework for linear situations, *PLoS One*, 18, e0283681, 10.1371/journal.pone.0283681, 2023.
- Tuholske, C., Caylor, K., Funk, C., Verdin, A., Sweeney, S., Grace, K., Peterson, P., and Evans, T.: Global urban population exposure to extreme heat, *Proceedings of the National Academy of Sciences of the United States of America*, 118, e2024792118, doi:10.1073/pnas.2024792118, 2021.
- Villefranque, N., Hourdin, F., d'Alençon, L., Blanco, S., Boucher, O., Caliot, C., Coustet, C., Dauchet, J., El Hafi, M., Eymet, V., Farges, O., Forest, V., Fournier, R., Gautrais, J., Masson, V., Piaud, B., and Schoetter, R.: The "teapot in a city": A paradigm shift in urban climate modeling, *Science Advances*, 8, eabp8934, doi:10.1126/sciadv.abp8934, 2022.
- Voogt, J. A. and Oke, T. R.: Effects of urban surface geometry on remotely-sensed surface temperature, *International Journal of Remote Sensing*, 19, 895-920, 10.1080/014311698215784, 1998.
- Wang, K., Li, Y., Li, Y., and Lin, B.: Stone forest as a small-scale field model for the study of urban climate, *International Journal of Climatology*, 38, 3723-3731, <https://doi.org/10.1002/joc.5536>, 2018.



- 694 Wang, W., Wang, X., and Ng, E.: The coupled effect of mechanical and thermal conditions on pedestrian-
695 level ventilation in high-rise urban scenarios, *Building and Environment*, 191, 107586,
696 <https://doi.org/10.1016/j.buildenv.2021.107586>, 2021.
- 697 Wu, Z., Shi, Y., Ren, L., and Hang, J.: Scaled outdoor experiments to assess impacts of tree
698 evapotranspiration and shading on microclimates and energy fluxes in 2D street canyons, *Sustainable*
699 *Cities and Society*, 108, 105486, <https://doi.org/10.1016/j.scs.2024.105486>, 2024.
- 700 Yang, X. and Li, Y.: Development of a Three-Dimensional Urban Energy Model for Predicting and
701 Understanding Surface Temperature Distribution, *Boundary-Layer Meteorology*, 149, 303-321,
702 10.1007/s10546-013-9842-x, 2013.
- 703 Yang, X. and Li, Y.: The impact of building density and building height heterogeneity on average urban
704 albedo and street surface temperature, *Building and Environment*, 90, 146-156,
705 <https://doi.org/10.1016/j.buildenv.2015.03.037>, 2015.
- 706 Yoshida, K., Miwa, S., Yamaki, H., and Honda, H.: Analyzing the impact of CUDA versions on GPU
707 applications, *Parallel Computing*, 120, 103081, <https://doi.org/10.1016/j.parco.2024.103081>, 2024.
- 708 Yuan, C., Adelia, A. S., Mei, S., He, W., Li, X.-X., and Norford, L.: Mitigating intensity of urban heat
709 island by better understanding on urban morphology and anthropogenic heat dispersion, *Building*
710 *and Environment*, 176, 106876, <https://doi.org/10.1016/j.buildenv.2020.106876>, 2020.
- 711 Yuan, C., Shan, R., Zhang, Y., Li, X.-X., Yin, T., Hang, J., and Norford, L.: Multilayer urban canopy
712 modelling and mapping for traffic pollutant dispersion at high density urban areas, *Science of The*
713 *Total Environment*, 647, 255-267, <https://doi.org/10.1016/j.scitotenv.2018.07.409>, 2019.

714