



Enhancing sea ice knowledge through assimilation of sea ice thickness from ENVISAT and CS2SMOS

Nicholas Williams¹, Yiguo Wang¹, and François Counillon¹²

¹Nansen Environmental and Remote Sensing Center, Bergen, Norway

²Bjerknes Centre for Climate Research, Bergen, Norway

Correspondence: Nicholas Williams (nicholas.williams@nerc.no)

Abstract. Arctic sea ice extent has declined significantly over the past two decades, opening up the Arctic to shipping and resource extraction while also impacting wildlife and local communities. This has led to an increasing need for skillful sea ice predictions. We focus on furthering the understanding of the role that sea ice thickness plays in the skilfulness of seasonal Arctic sea ice predictions. We look at how observations of sea ice thickness can improve both sea ice reanalyses and predictions.

5 We use the Norwegian Climate Prediction Model (NorCPM), which has previously assimilated ocean and sea ice concentration observations. We additionally assimilate two sea ice thickness products: CS2SMOS, and, for the first time in any study, ENVISAT. This allows us to produce a 2-decade reanalysis with sea ice thickness assimilation focusing on the Arctic Ocean. This reanalysis is then used to initialise and generate a series of year-long seasonal hindcasts for each season of the reanalysis. The reanalysis and hindcasts are compared to observations and other reanalyses to assess the impact of sea ice thickness obser-
10 vations. Assimilation of sea ice thickness data strongly improves the representation of sea ice thickness and volume, primarily in the central Arctic as well as the ice edge location. Although ENVISAT observations have greater uncertainties, the dataset still provides a useful impact on the model. For prediction, sea ice thickness initialisation reduces the model biases of thickness throughout the year as well as errors in the detrended anomalies. Ice thickness bias correction results in improvements in the representation of the ice edge location, i.e., the timing and extent of the summer melting. Thickness initialisation has
15 little improvements for detrended sea ice extent anomalies, but yields some skill in the Beaufort Sea and Central Arctic during summer. Overall, we show the impact of sea ice thickness assimilation has a positive effect on prediction skill in NorCPM.

1 Introduction

In the Arctic, both the atmosphere and ocean have undergone dramatic warming trends over the satellite era (Przybylak and Wyszyński, 2020; Steele et al., 2008), and continue to experience warming much faster than the rest of the globe (Cohen
20 et al., 2014), leading directly to sea ice loss (Dai et al., 2019). The sea ice loss in this region is having a strong impact on Arctic wildlife and habitats (Descamps et al., 2017). There are also wide-reaching effects on tourism, resource extraction and communities living in the Arctic (Arruda and Krutkowsky, 2017). This has led to increasing interest in the study of Arctic sea ice and, in particular, of seasonal predictions, which aim to predict the response of the sea ice to climate change and also predict internal variability. As the Arctic basin has warmed, the sea ice has not only retreated (Comiso et al., 2008; Stroeve



25 et al., 2014b), but also thinned (Nghiem et al., 2007; Giles et al., 2008; Kwok, 2018). Much of the Arctic sea ice has gone from being perennial year-round ice to seasonal ice, and an increase in the length of the melting season. Such radical change also influences internal variability, making seasonal Arctic sea ice prediction more challenging.

26 The field of seasonal Arctic sea ice prediction emerged and rapidly developed within the past two decades, focusing on identifying and improving our understanding of the physical properties of sea ice, in order to improve the prediction of Arctic
30 sea ice under a changing climate. This began with the first seasonal sea ice predictions using global climate models (GCM) and continued with prediction studies from a variety of research centres and institutes around the world (Wang et al., 2013; Chevallier et al., 2013; Peterson et al., 2015; Guemas et al., 2016; Bushuk et al., 2017; Kimmritz et al., 2019). The sea ice prediction network (SIPN) is at the centre of this field. The SIPN collects September sea ice extent (SIE) forecasts initialised
35 from June, July and August and September into the Sea Ice Outlook (SIO) report (Stroeve et al., 2014a; Bushuk et al., 2024). At present, over 30 different research groups of polar scientists contribute to the SIPN, using dynamical or statistical approaches to produce these predictions. Idealistic model experiments in GCMs estimate that sea ice area and extent in the Arctic could be predictable between 12-48 months in advance, though predictability beyond 36 months is dominated by atmospheric forcing and not the initial conditions (Blanchard-Wrigglesworth et al., 2011a, b). Sea ice thickness (SIT) may be predictable up to 2 years in advance (Holland et al., 2011), and can be important for SIE predictions up to 2 years ahead (Tietsche et al., 2014) in
40 an idealised framework.

41 The evolution of the Arctic sea ice is governed by the evolution of SIT distribution, and these changes come from two sources: dynamical and thermodynamical. Sea ice dynamics govern the movement of the sea ice either in space, or within
45 the thickness distribution (commonly known as ridging). Thermodynamic changes in the sea ice comprise of melting (lateral, bottom and top melt) and freezing (congelation and frazil ice formation). SIT therefore is a key variable for modelling the sea ice state. SIT observations can substantially improve reanalysis estimates of thickness, with smaller impacts on other model variables such as sea ice concentration (SIC) and sea ice drift (SID), which has been shown in a number of sea ice reanalysis studies using different observational sources of thickness (Xie et al., 2018; Fritzner et al., 2019; Williams et al., 2022), and freeboard (Sievers et al., 2023). For prediction of SIE, correct SIT initialisation and its advection through the Arctic is believed to be one of the key mechanisms for skill within the Arctic (Blanchard-Wrigglesworth et al., 2011b; Ordoñez et al., 2018;
50 Giese et al., 2021; Zhang et al., 2021; Min et al., 2023; Zhang et al., 2023), and has been shown recently for CryoSat-2 (CS2) observations when using the CICE model standalone (Sun and Solomon, 2024). This is particularly true during the growth season which has been shown to translate to improved skill in SIE during the summer melt season (Blockley and Peterson, 2018; Holland et al., 2019). Additional mechanisms identified as important in the Arctic for SIE prediction are initialisation, persistence and re-emergence of SIC (Blanchard-Wrigglesworth et al., 2011b; Ordoñez et al., 2018; Giese et al., 2021), ocean
55 heat transport (OHT), ocean heat content (OHC) and melt onset timing (Schröder et al., 2014; Serreze et al., 2016; Kwok, 2018; Zheng et al., 2021). The atmosphere, particularly wind, determines the dominant Arctic ocean currents of the Transpolar drift stream and the Beaufort Gyre, is also important but has a short memory, so its predictability can deteriorate quickly (Msadek et al., 2014; Serreze and Meier, 2019). Though several mechanisms have been identified in general, many are still



poorly understood. In this paper, we will focus on improving thickness initialisation, and in doing so, using a longer period of
60 SIT observations to study Arctic sea ice predictability.

In the past 15 years, significant work has been done on developing and producing new SIT observation datasets. At the forefront of this field are SIT datasets from CS2 (Laxon et al., 2013), available since October 2010, the combined CS2 and Satellite Moisture and Salinity (SMOS) dataset (Ricker et al., 2017) known as CS2SMOS. These datasets are the longest running available Arctic SIT observations, but until recently summer observations of SIT were not available due to the presence
65 of melt ponds, though this has now changed with the work of Landy et al. (2022) to produce a year-round CS2 thickness dataset. The launch of ICESat-2 in 2018 also led to a winter SIT dataset using laser observations (Petty et al., 2020). However, before these satellites were launched, there were the forerunner satellites of ICESat (Kwok et al., 2004) and ENVISAT (Louet and Bruzzi, 1999). As they were not primarily designed for SIT retrieval, the datasets have issues, particularly with spatial and temporal coverage, and also the instruments used. Monthly observations of SIT have been derived from ENVISAT for the
70 winter months not available during summer due to melt ponds, as with CS2 (Connor et al., 2009), which spans from October 2002 to 2012. In this work, we use the ENVISAT dataset to lengthen our reanalysis and increase the number of predictions possible for our statistical analysis.

In this study, we will investigate how assimilation of SIT observations from ENVISAT and CS2SMOS can first benefit our sea ice reanalysis and then summer Arctic sea ice predictions by using seasonal hindcasts (i.e. retrospective predictions)
75 started from 2003 to 2023. To our knowledge, ENVISAT SIT observations have not been assimilated before in a GCM, so this study will investigate their use and feasibility of inclusion for assimilation in GCMs for the first time. As we use ENVISAT observations, this also means we have a longer time series of SIT observations to assimilate, and thus a longer reanalysis and more hindcasts with which we can analyse, study and verify its usefulness within these fields. We investigate not only SIE/SIT predictions but also the prediction of the sea ice edge location using the integrated ice edge error (IIIE).

80 The paper is organised as follows. In Section 2, we outline the climate model, observations and experimental design. In Section 3, we outline the metrics and independent observations used for evaluating and validating the performance of the model. In Section 4.1, we show the results of the sea ice reanalysis from 2003 to 2023, including verification of the reanalysis with independent data from the Beaufort Gyre Exploration Project (BGEP) moorings. In Section 4.2, we show the results of the hindcast experiments. In Section 5, we discuss the key results and conclude this study.

85 2 NorCPM

We use the Norwegian Climate Prediction Model (NorCPM, Counillon et al., 2016; Wang et al., 2019), which combines the Norwegian Earth System Model (NorESM Bentsen et al., 2012) and the Ensemble Kalman Filter (EnKF, Evensen, 1994) data assimilation method. The version of NorCPM is as in Kimmritz et al. (2019), which contributed to the SIPN (Bushuk et al., 2024), but we are testing, in addition, a separate version that assimilates ice thickness data.



90 2.1 NorESM

The NorESM version used here is NorESM1-ME (Bentsen et al., 2013). It is based on the Community Earth System Model (CESM, Hurrell et al., 2013). However, the ocean component is replaced with an isopycnal coordinate ocean general circulation model (BLOM, Bentsen et al., 2012), and the Community Atmosphere Model (CAM4, Neale et al., 2010) with the original prescribed aerosol formulation is replaced by the atmospheric model CAM4-OSLO with a prognostic aerosol life cycle formulation using emissions and new aerosol-cloud interaction schemes (Kirkevåg et al., 2013). As in CESM1.0.4, NorESM1-ME uses the Los Alamos Sea Ice Model (CICE, Hunke et al., 2015) and the Community Land Model (CLM) (Lawrence et al., 2011). These are coupled using version 7 of the coupler designed for the CESM (Craig et al., 2012).

The atmosphere and land model has an approximately 2° finite volume grid, with horizontal resolutions of 1.9° in latitude and 2.5° in longitude, while the ocean and sea ice have approximately a $1^\circ \times 1^\circ$ horizontal resolution. BLOM uses 51 isopycnal layers plus 2 additional layers for the bulk mixed layer, with time-evolving thicknesses and densities. This version of NorESM is run with CMIP5 historical forcings (Taylor et al., 2012) and the RCP8.5 (Moss et al., 2010) beyond 2005. A similar version of NorCPM has contributed to CMIP6 Decadal Climate Prediction Project (Bethke et al., 2021). However, upgrading to CMIP6 forcings degraded NorCPM's baseline climate and hindcast performance (Bethke et al., 2021; Passos et al., 2023), and we use CMIP5 forcings in this study.

The sea ice model CICE uses five categories in its thickness distribution, optimal for representing the sea ice cover at reasonable computing power (Bitz et al., 2001). The horizontal transport of sea ice is solved using an incremental remapping scheme (Lipscomb and Hunke, 2004), and solving for the sea ice stresses using the elastic-viscous-plastic rheology (Hunke and Dukowicz, 1997). The one-dimensional vertical Bitz and Lipscomb model (Bitz and Lipscomb, 1999), is used to solve the thermodynamic equations, with melt pond, aerosol (Holland et al., 2012) and radiation transfer parameterisations (Briegleb and Light, 2007). Sea ice transported in thickness space is solved using a remapping scheme (Lipscomb, 2001).

2.2 Assimilation implementation

The EnKF is a sequential ensemble data assimilation (DA) method using Monte Carlo integration followed by a linear analysis update (Evensen, 1994). The method is multivariate and updates the model state variables based on their ensemble covariances with the observations. Specifically, we use a deterministic formulation of the EnKF (Sakov and Oke, 2008), which solves the analysis without needing to perturb the observations. The Deterministic EnKF outperforms the standard EnKF, particularly for small ensemble sizes (Sakov and Oke, 2008).

We assimilate the monthly average observations in the middle of the model month (i.e., the 15th day) and update the instantaneous model state based on all observations (Counillon et al., 2016; Kimmritz et al., 2019). The update of the model state during the assimilation is split into two steps: the ocean model variables and the model variable SIC are updated jointly by the assimilation of oceanic and SIC observations, and then the model variable SIC is again updated by the assimilation of SIT observations. The atmosphere and land components are not updated by the assimilation but adjusted dynamically via coupling in between the monthly assimilation cycles.



Assimilation of ocean temperature and salinity profiles, sea surface temperature (SST), and SIC observations are performed as described in Kimmritz et al. (2019). We employ anomaly-field assimilation, using a monthly reference climatology calculated from 1982 to 2016. We perform strongly coupled ocean-sea ice DA (Laloyaux et al., 2016; Kimmritz et al., 2018), in which both the ocean and sea-ice components are updated based on the observations from both components. Strongly coupled ocean-sea ice DA in NorCPM was shown to be more effective than weakly coupled DA (Kimmritz et al., 2018). We update the full ocean physics state vector in isopycnal coordinates (i.e., 3D temperature, salinity, velocities and layer thickness) and update the multicategory SIC in the sea ice state vector. The individual sea ice volume is changed proportionally so that the individual thickness category remains identical to that of the prior ensemble. This prevents the need to reshuffle ice to a different thickness category in the post-analysis, which proved to be optimal in an idealised twin experiment (Kimmritz et al., 2018). However, in Kimmritz et al. (2019), assimilation where carried out in 2 steps with SST and SIC updating the mixed layer depth ocean and the sea ice state, followed by assimilation of ocean profiles that update the full 3D ocean. This degraded performance in the lower latitudes where there are few profiles data to constrain the ocean interior. Therefore, we carry out a single assimilation step based on all observations products, which updates the full ocean and sea ice state jointly. This handled the degradation reported in Kimmritz et al. (2019) and has no impact on performance at high latitudes (not shown).

When assimilating SIT observations, we use full-field assimilation. In the first attempt, we tried to use anomaly-field assimilation. However, the assimilation impact of SIT was inconclusive, with no added skill for predictions (not shown). We, therefore, tried to correct for the SIT bias that can influence the variability. NorESM has a large SIT bias (Bentsen et al., 2012), and while assimilation of ocean and sea ice concentration observation reduces it partially, a large fraction remains. Bethke et al. (2021), compared two versions of NorCPM, one that updates only the ocean component and one that updates the ocean and sea ice components. The latter yields a strong reduction of the bias of SIT and provides enhanced predictions. Note also that it takes about ten years for the model to build the SIT bias again once assimilation is stopped (their Figure S15). As such, we see the current approach as a more effective way to constrain SIT bias. To update SIT, we update the individual multi-category sea ice fraction, which can change the sum of the ice fraction. However, as the prior assimilation of SIC observations has already constrained the ensemble close to the observed estimate, the subsequent SIT assimilation updates the individual fractions so that it complies with the observed ice thickness as well. We do not update the ocean component, as the covariances between SIT and the ocean are very small, and may cause more harm than benefit because of sampling error.

We use a series of ad-hoc techniques to handle issues related to sampling error, typically used in NorCPM (Counillon et al., 2016; Bethke et al., 2021). First, we used the R-factor (Sakov et al., 2012), which inflates the observation error by a factor of 2 for the update of the ensemble anomaly. We also use the K-factor formulation (Sakov et al., 2012), which inflates the observation error so that the analysis remains within m times the standard deviation of the ensemble ($m = 2$ in this study). This avoids producing too strong updates. Finally, we use a local analysis framework (Evensen, 2003), which only uses the local observations and limits the risk of spurious covariance. Tapering with a smooth distance-weighted Gaspari and Cohn function (Gaspari and Cohn, 1999) ensures continuity in the update. The localisation radius for the ocean variables is a function of latitude (Wang et al., 2017), and for the SIC and SIT observations we use a localisation radius of 800 km as used previously (Kimmritz et al., 2018; Massonnet et al., 2015).



Our DA implementation assumes the observation error to be independent. However, since observations of SST, SIC and SIT are gridded products, the observation error may be correlated due to heavy post-processing during data production. To mitigate 160 this fact, we only retain the nearest observation of each observation type in the local analysis (Counillon et al., 2016; Kimmritz et al., 2018). For the hydrographic profiles, all data within the local window are used (Wang et al., 2017).

2.3 Assimilated datasets

SST and SIC monthly average data are from the NOAA OISSTV2 dataset (Reynolds et al., 2007; Huang et al., 2021) available on a $1^\circ \times 1^\circ$ global grid. The data is originally produced as weekly fields, NOAA then produces monthly fields using a linear 165 interpolation of the weekly fields to daily fields then averaging those daily values over each month. The SST data are produced by combining both in-situ and satellite observations and SST's simulated by sea ice cover (Reynolds et al., 2007), where SST is derived using a quadratic relationship between SIC and SST at grid cells with sea ice cover. Monthly SST observation errors are estimated using the weekly error estimation provided by the dataset. We experience that error in SST tends to be very low and we imposed a minimum threshold of 0.1 °C. SIC observation errors are not provided with the dataset and thus we use 170 a 20% constant value (Kimmritz et al., 2019), which is the generally agreed upon value for the highest uncertainties in the summer melt season (Ivanova et al., 2015; Cavalieri and Parkinson, 2012; Comiso, 2017).

The temperature and salinity profile data from October 2003 to October 2021 are taken from EN4.2.1 dataset (Gouretski and Reseghetti, 2010; Good et al., 2013). The data from then onwards are from EN4.2.2 dataset (Gouretski and Cheng, 2020). The EN4 hydrographic dataset is split into different categories depending on its quality. In this study, we only use data in category 175 1 (i.e., the highest quality). Their associated observation errors are determined as in Wang et al. (2017).

For the SIT observations, we use two datasets: the ESA CCI dataset that includes SIT retrieved from ENVISAT (Connor et al., 2009), and the AWI CS2SMOS dataset (V2.6) (Ricker et al., 2018) that retrieves SIT from the SMOS satellite and the CS2 satellite. The ESA CCI dataset covers the period from October 2002 to April 2012, however we only use data up to March 180 2010 because the more accurate CS2SMOS product becomes available after this. For both datasets, data is only available outside the melt season between October and April. Melt ponds on top of sea ice make it challenging to identify leads, which is crucial for the estimation of freeboard and SIT (Laxon et al., 2013). Additionally, we do not use October or April data due to certain quality issues associated with the fringe months marking the change between the melting and growth seasons in the Arctic sea ice. The observation error is provided by the datasets.

2.4 Experiment design

185 In this work, we want to test the added value of SIT assimilation. For that, we have run several experiments. We use an ensemble model simulation without data assimilation and two reanalyses as follows:

FREE: a 30-member ensemble run without data assimilation and produced by selecting random states from a stable pre-industrial control run and integrating it from 1850 to December 2023 with CMIP5 historical forcings and with RCP8.5 beyond 2005.



190 **CTRL:** A 30-member reanalysis started in 1982 from FREE, using a similar setting as in Kimmritz et al. (2019); Bushuk et al. (2024). It assimilates hydrographic profiles, SST, and SIC data (section 2.3) with an anomaly-field assimilation framework.

+SIT: a 30-member reanalysis is branched off from CTRL on the 15th of October 2002. It assimilates SIT data (section 2.3) in addition to that assimilated in CTRL.

195 FREE allows us to disentangle the skill related to external forcings (Kimmritz et al., 2019). We use CTRL to compare the model with and without the assimilation of SIT data, while still assimilating the ocean and SIC observations.

Three sets of seasonal hindcasts (i.e., retrospective predictions) are created from FREE, CTRL and +SIT. They start on the 15th of January, April, July and October each year between 2003 and 2023 and run for 1 year with 10 members. This comprises 84 hindcasts in total (21 years and 4 hindcasts per year) for each set of hindcast experiments.

200 **3 Validation metrics and datasets**

We validate the reanalyses and hindcasts using their ensemble means. For the hindcast, we assess the performance for different start and lead months. Note that our hindcasts start in the middle of the month, but it has assimilated the monthly average of that month – e.g., our hindcast started on the 15th of April has assimilated April monthly average data. Lead month 1 starts after 15 days of model integration (e.g., May is lead month 1 of April-initialised prediction).

205 We define the SIE as the total sum of the area where the ensemble mean of SIC is at or above 15%.

3.1 Validation metrics

We use bias and bias-free root-mean-square error (bfRMSE), defined as

$$\text{bias} = \sum_{i=1}^N W_i(x_i - y_i), \quad (1)$$

$$210 \quad \text{bfRMSE} = \sqrt{\sum_{i=1}^N W_i(x_i - y_i)^2}, \quad (2)$$

where N is the total number of data points, W_i is a normalising area-based weight constant –i.e. when the metric is computed considering grid cells that do not have the same area. For point-wise bias and bfRMSE calculations, W_i is $\frac{1}{N}$. x_i is the model ensemble mean values, and y_i is the observed values, which are both anomalies from their respective climatology (model or observation). These are usually averaged either over time or space (where each grid cell is then weighted by its area). Note that 215 root-mean-square error (RMSE) is the quadratic sum of bias and bfRMSE.



We additionally use anomaly correlation coefficient (ACC) to test the variability of the reanalyses/hindcasts and the observations, defined as follows:

$$\text{ACC} = \frac{\sum_{i=1}^N x'_i y'_i}{\sqrt{\sum_{i=1}^N x'^2_i} \sqrt{\sum_{i=1}^N y'^2_i}}, \quad (3)$$

where x'_i and y'_i are model and observation values. For the reanalysis, we use the standard ACC and bfRMSE, but for the predictions, we use the detrended values – i.e. both time series are detrended before computing the metric. The reason is that the trend in reanalysis is part of the signal that one aims to represent and can be challenging due to discontinuity in the observation data set or drift in the system. In prediction, the trend is often removed as it is considered to be a trivial predictor (Bushuk et al., 2020). The statistical significance of the Pearson correlation coefficient is tested by using the Student's t-test with a significant level of 5% with degrees of freedom calculated as in Von Storch and Zwiers (2002).

225 The Degrees of Freedom for Signal (DFS) is calculated for each set of assimilated observations in the analysis to test the impact of their assimilation (Wahba et al., 1995; Cardinali et al., 2004).

$$\text{DFS} = \sum_{i=1}^L \frac{\partial x_a}{\partial y}, \quad (4)$$

where L is the total number of observations and x_a is the model posterior. DFS then effectively works by quantifying how much the analysis update is affected by the assimilated observations.

230 Finally, we use the Integrated Ice Edge Error (IIEE) to assess the error in the location of the ice edge (Goessling et al., 2016). It is defined as

$$\text{IIEE} = \int_A \max(c_x - c_y, 0) dA + \int_A \max(c_y - c_x, 0) dA, \quad (5)$$

where A is the area, $c = 1$ where the SIC is above 15% and 0 elsewhere, with subscripts x and y denoting the model and observations respectively. This works as essentially the sum of all areas where SIE is overestimated (first term on RHS of the 235 above equation) and underestimated (second term). The IIEE is a useful verification metric because it is conceptually simple. It is well verified with existing long-term SIC satellite data, is an important characteristic of the sea ice cover and is more useful to potential forecast users than total SIE (Goessling et al., 2016). In this study, we compute first IIEE for individual members and then take their mean.

3.2 Independent validation datasets

240 In the paper, a part of the validation will be carried out with the assimilated dataset. In the reanalysis, such data cannot be considered independent, but still represents a baseline verification (that DA works as expected).

We use observations of sea ice draft from the BGEP moorings for independent validation. BGEP includes upward-looking sonar (ULS) measuring instruments (Krishfield et al., 2014). There are a total of 4 moorings, 2 of which (A and B) have been in operation since August 2003, C was in operation until 2008, and D has been in operation since 2005. All moorings are located



245 in the Beaufort Sea (their location in the Arctic is shown in Figure 2c). The ULS instruments measured sea ice draft every 2 seconds before 2014, and every second after. The sea ice draft, which is the thickness of the sea ice under sea level, is found by subtracting the range measured by the ULS instrument from the known depth of the instrument. The draft measurements have a stated error of $+/- 5 - 10$ cm (Krishfield and Proshutinsky, 2006). To compare this data to our model monthly mean thickness, we first convert the sea ice draft into SIT using the method of Rothrock et al. (2008), and then average all the measurements 250 over each month to find the monthly mean thicknesses, which we can compare to the model. If there was missing data in a month, we discard the ULS data for that month for that mooring.

The Pan-Arctic Ice Ocean Modeling and Assimilation System (PIOMAS) reanalysis was first introduced in 2003 by Zhang and Rothrock (2003). PIOMAS is a coupled ice-ocean model that assimilates SST data in ice-free grid cells using optimal interpolation, and SIC using a relatively simple nudging technique which aims to move the model variables closer to their 255 observed counterparts by use of a weighting factor. PIOMAS has been substantially validated with a large number of SIT observations (Schweiger et al., 2011), so is often used as a comparison dataset for other SIT and sea ice volume datasets. The PIOMAS reanalysis is used for validation in this study.

4 Results

4.1 Reanalysis

260 In this section, we analyse our 21-year reanalyses over the period where satellite SIT observations are available.

We start by analysing the relative influence of each observation type in constraining errors in the system with the DFS (Section 3.1). The observations assimilated complement each other quite well and dominate in different regions (Figure 1). The ocean observations dominate in the sea ice-free regions of the Arctic. SIC assimilation is most impactful at the sea ice edge, where SIC shows the largest variability. SIT assimilation is mainly effective in the central Arctic, where the ice is thicker. 265 As expected, the SIT assimilation becomes more effective (higher DFS) when we switch over from assimilating ENVISAT to CS2SMOS. However, ENVISAT assimilation is still having a substantial impact in the central Arctic, where other observations are few.

We first verify performance against the SIT observations (Figure 2), which is assimilated in +SIT. We only present the validation against the CS2SMOS period due to the differing regional coverage between ENVISAT and CS2SMOS, but the 270 conclusions are similar for ENVISAT (not shown). FREE has a clear thick bias (up to 4 m), with the spatial pattern of the bias increasing as the ice gets thicker — largest close to the Canadian Arctic Archipelago (CAA). In CTRL, the biases in the central Arctic Ocean have been reduced, but there is still a thin strip of too-thick sea ice pushed against the CAA. In +SIT the thickness biases in the marginal seas surrounding the central Arctic have almost been completely removed, which showcases the influence of assimilating ice thickness data.

275 For bfRMSE, FREE features errors of around 20 cm in a majority of places, reaching errors up to 1 m close to the CAA. Surprisingly, the SIT bfRMSEs are increased in CTRL in much of the central Arctic compared to FREE. This suggests that the assimilation of SIC and ocean observations has led to increased bfRMSEs for SIT. However, as the bias is much larger than

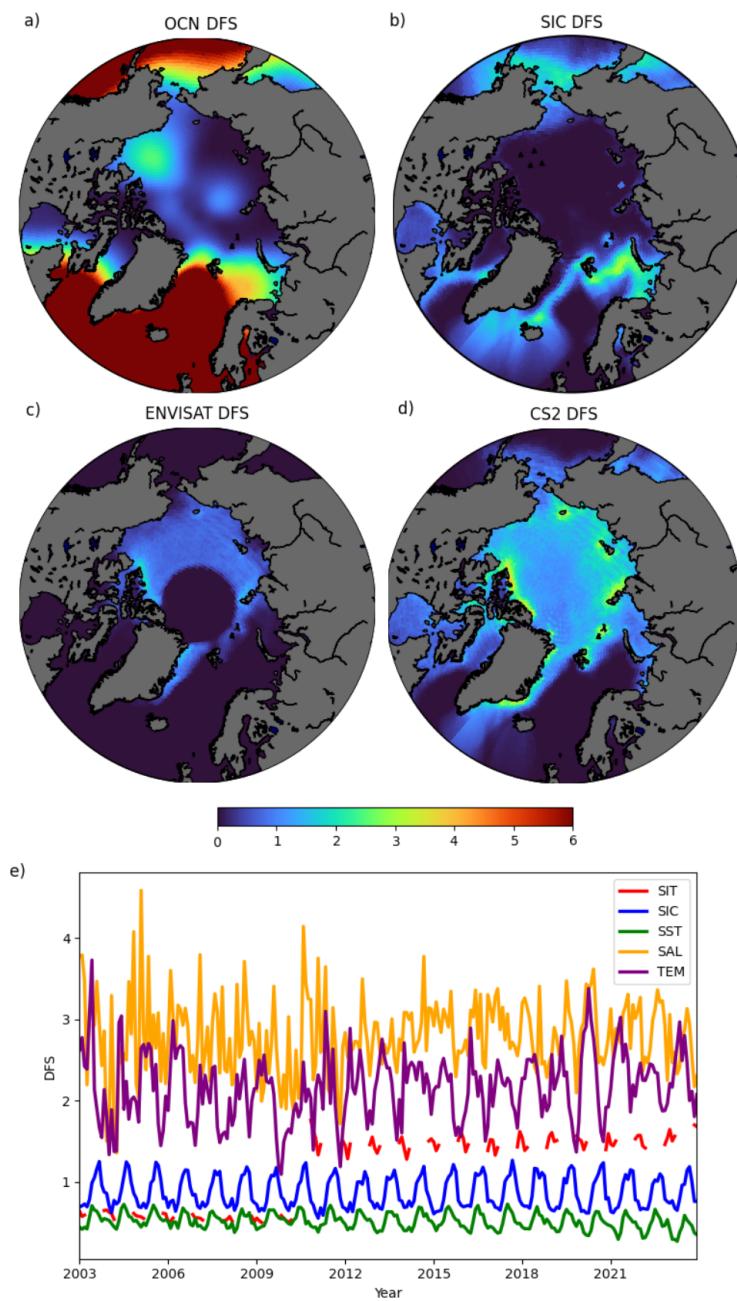


Figure 1. Top Left: Combined mean DFS of salinity, ocean temperature and sea surface temperature. Top Right: Mean DFS of SIC. Middle left: Mean DFS of ENVISAT SIT. Middle right: Mean DFS of CS2 SIT. Bottom: Pan-Arctic monthly mean DFS for each observation assimilated in our +SIT reanalysis. TEM refers to (ocean) temperature and SAL refers to salinity.

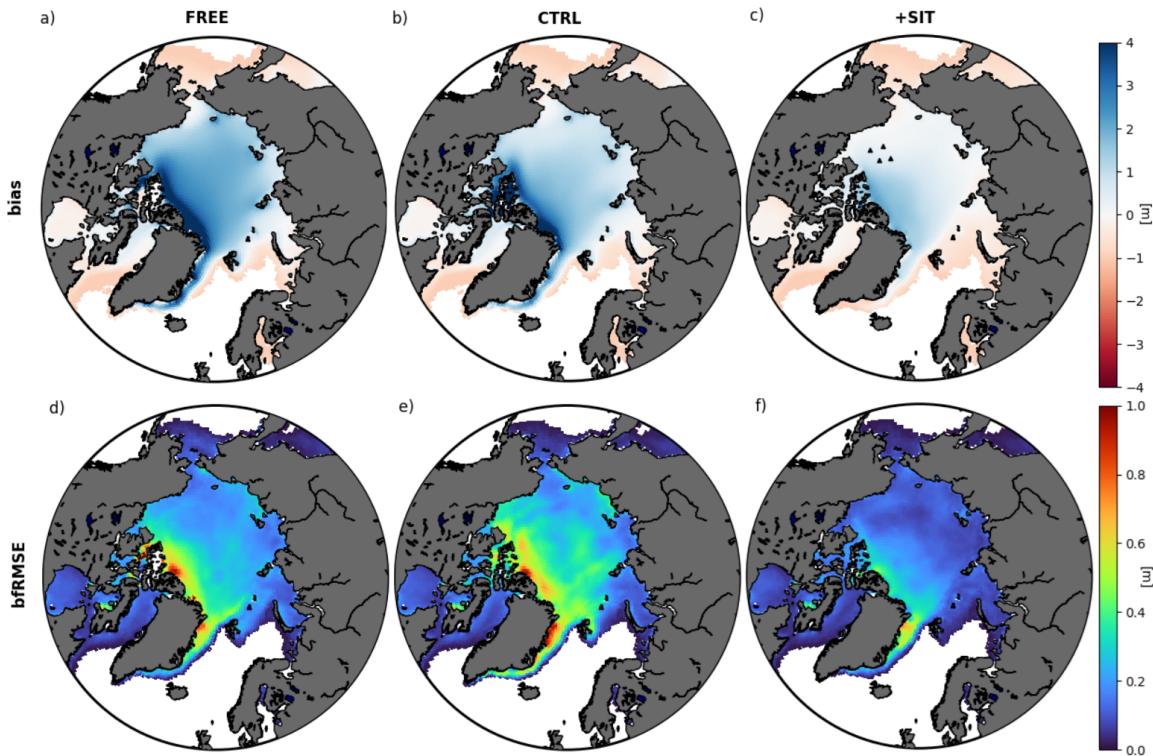


Figure 2. Bias (top row) and bfRMSE (bottom row) of SIT in each of our NorCPM experiments in comparison to SIT observations from CS2SMOS between 2010 and 2023. In panel (c) we also show the locations of the BGEP ULS moorings as black triangles.

bfRMSEs, the increased bfRMSEs result more from the evolution of the SIT bias in between and during the assimilation (the total RMSE is reduced). In the +SIT reanalysis, almost all grid cells feature low bfRMSE, especially in the central Arctic and

280 CAA. There remain higher errors in the Fram Strait – albeit weaker than for FREE and CTRL – that are typically driven by sea ice export. In this region, SIT observation errors are very large, and SIT assimilation effectiveness is reduced (Figure 1).

The previous comparison was done against assimilated observations of CS2SMOS, and we now compare with SIT derived from the independent BGEP moorings (Section 3.2). The moorings are all located in the Beaufort Gyre (Figure 2c), so do not provide an assessment over the whole pan-Arctic region. The comparison (Figure 3 and Table 1) is well in line with the 285 above CS2SMOS validation. FREE has the largest biases (as high as 1.5 m); CTRL has smaller biases than FREE due to ocean and SIC assimilation. +SIT has the smallest biases among the three reanalyses. FREE has bfRMSE from 0.06 m to 0.15 m, varying with the mooring and ACC around 0.7–0.8 as it captures the decreasing trends well with yearly data and the seasonal cycle with monthly outputs. The assimilation of the ocean and SIC data reduces bfRMSE (CTRL in Table 1) but yields a slight degradation of ACC at stations C and D. Assimilating SIT further reduces bfRMSE consistently with Figure 2 and improves 290 correlation (about 0.9). Overall, +SIT shows the best performance for all four moorings and performance is better during the CS2SMOS observations period than during the ENVISAT period.

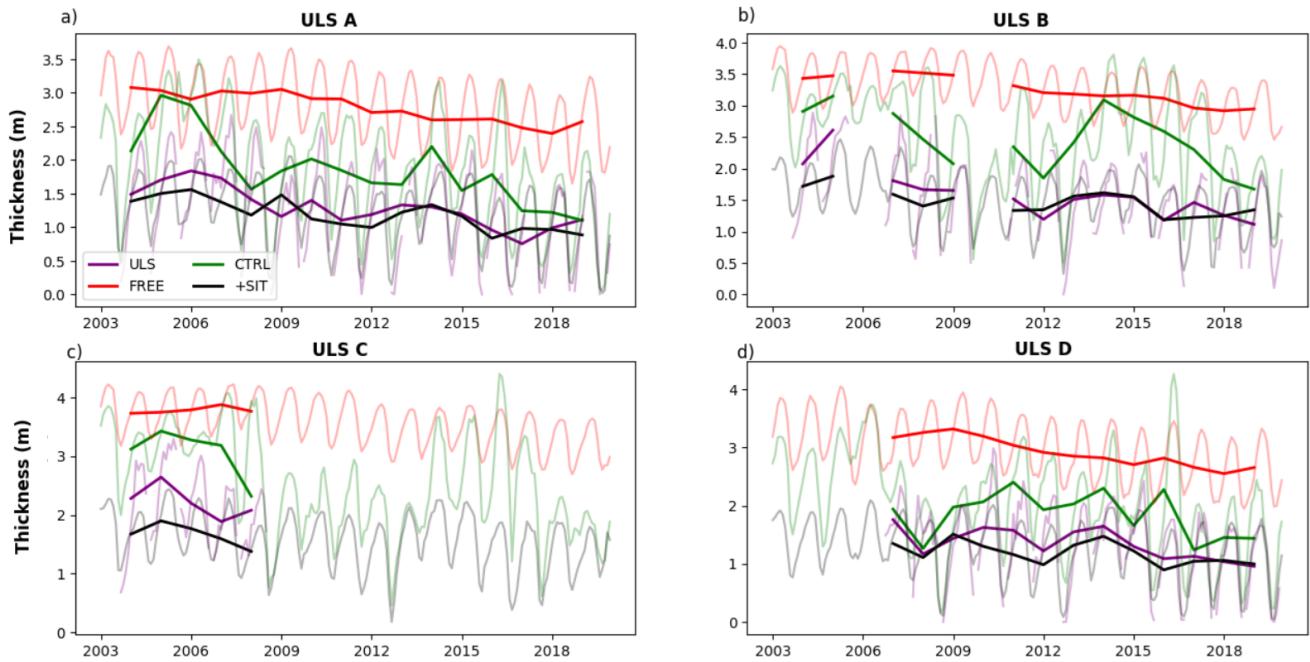


Figure 3. Yearly (thick line) and monthly (thin line) average sea ice thickness at ULS A (top left), B (top right), C (bottom left) and D (bottom right) and the respective SITs in our reanalyses during our experimental period. In some years, there are not enough observations from a BGEP ULS to formulate a yearly average, so these years are masked.

Table 1. Bias, ACC and bfRMSE for the SIT of BGEP ULS A, B, C and D in comparison with the FREE, CTRL and +SIT reanalyses. The statistics are based on monthly mean detrended data. The statistics with yearly data are given in brackets. The unit of bias and bfRMSE is the metre. The system with the best performance are highlighted in bold.

Metric	Experiment	ULS A	ULS B	ULS C	ULS D
Bias	FREE	1.51 (1.49)	1.51 (1.66)	1.03 (1.56)	0.43 (1.57)
	CTRL	0.96 (0.56)	0.62 (0.87)	0.58 (0.84)	0.34 (0.49)
	+SIT	0.08 (-0.1)	-0.14 (-0.11)	-0.37 (-0.55)	-0.22 (-0.15)
bfRMSE	FREE	0.11 (0.35)	0.13 (0.37)	0.15 (0.21)	0.06 (0.34)
	CTRL	0.08 (0.15)	0.06 (0.20)	0.11 (0.12)	0.05 (0.12)
	+SIT	0.03 (0.05)	0.03 (0.06)	0.08 (0.08)	0.04 (0.05)
ACC	FREE	0.87 (0.87)	0.77 (0.88)	0.73 (0.74)	0.80 (0.80)
	CTRL	0.85 (0.85)	0.79 (0.79)	0.55 (0.56)	0.76 (0.78)
	+SIT	0.92 (0.92)	0.91 (0.91)	0.87 (0.88)	0.89 (0.89)

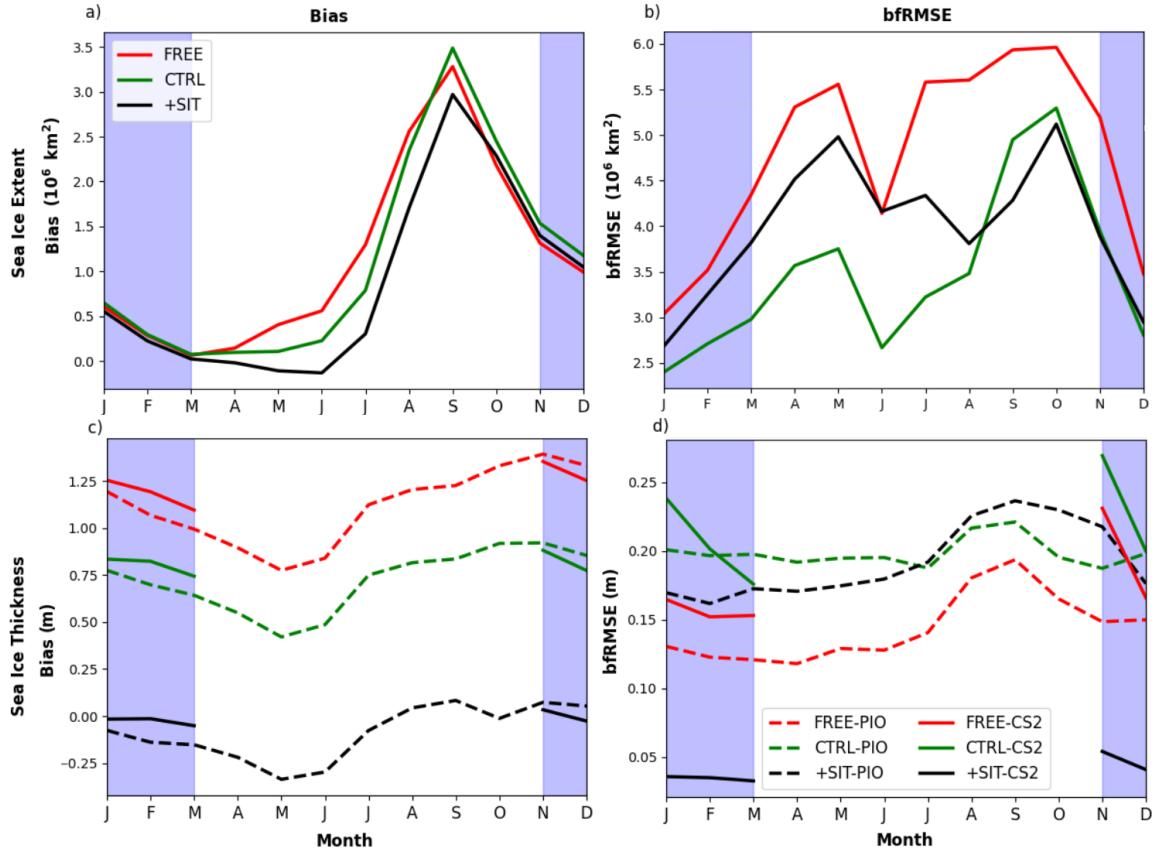


Figure 4. Bias (left-hand side) and bfRMSE (right-hand side) for SIE (top) and SIT (bottom) for FREE, CTRL and +SIT. SIC observations compared to SIC observations from NOAA, and the SIT from the PIOMAS reanalysis between 2003 and 2023 and CS2SMOS observations between 2010-2023. The blue-shaded area shows the time when SIT observations are assimilated.

We further analyse the seasonal variability of error of SIT and SIE (Figure 4). There is little difference between the reanalyses in the bias of SIE (Figure 4a) as we use an anomaly-field assimilation framework for ocean and SIC, which takes the climatology of FREE as an attractor. CTRL shows lower SIE bias than FREE in the ice-retreat season but slightly larger biases in the ice-advance season. SIE bias is substantially reduced in +SIT between April and September, and similar to FREE in the rest of the year. For bfRMSE of SIE (Figure 4b), +SIT and CTRL have lower errors than FREE, showing the positive impact of the assimilation of ocean and SIC data. However, the bfRMSE in SIT+ is larger than CTRL from January to August.

CTRL reduces the SIT bias compared to FREE uniformly throughout the year, and +SIT nearly removes entirely the SIT biases (Figure 4c), even outside of the assimilated season when compared to PIOMAS. The bfRMSE is slightly increased in CTRL compared to FREE, likely for the same reason explained above, i.e. bfRMSE being lower than bias can be misleading. bfRMSE in SIT+ is interesting because it is very low when computed against CS2SMOS (Figure 4d), but larger than FREE when computing bfRMSE against PIOMAS. PIOMAS tends to underestimate the interannual variability of SIT because it

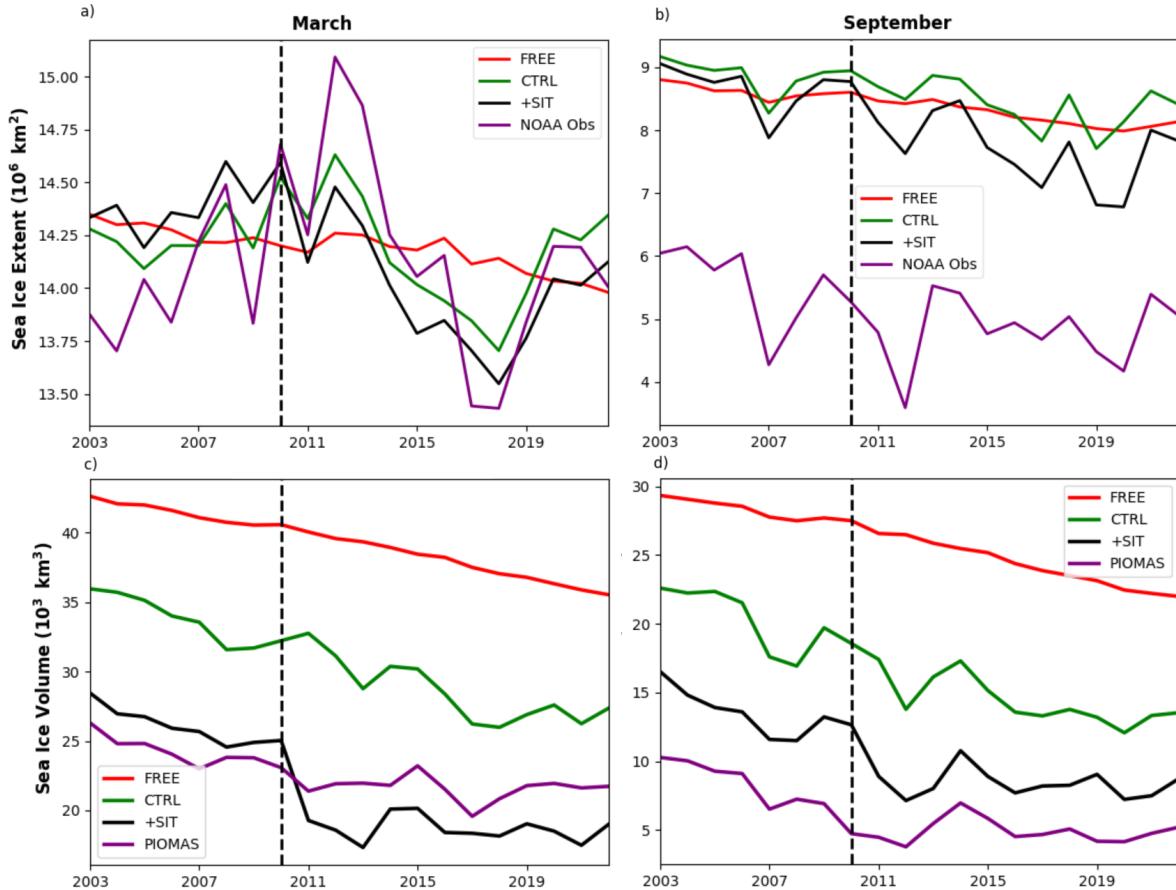


Figure 5. Arctic SIE (top) and SIV (bottom) in March (left-hand side) and September (right-hand side) for validation datasets and our experiments (FREE, CTRL and +SIT). SIC observations from NOAA, and the SIV from the PIOMAS reanalysis between 2003 and 2023. The dashed vertical lines split the whole period to the ENVISAT and C2SMOS eras.

overestimates the thickness of thin ice and underestimates the thickness of the thick ice (Schweiger et al., 2011; Wang et al., 2016). As such, the ensemble mean of FREE, which is nearly indistinguishable from the linear decline, compares favourably
 305 with PIOMAS for bfRMSE.

We then investigate the time evolution of the SIE and SIV throughout the reanalysis for March and September (Figure 5 and Table 2) when SIE reaches a maximum and minimum.

In March, FREE shows a weak decreasing trend in agreement with the observation but no year-to-year variability (as internal
 310 variability is not synchronised). CTRL shows good agreement with the assimilated NOAA observation estimate. Interannual variability is also much larger, implying that the individual members of CTRL are better constrained. +SIT also shows improved agreement with observations (amplitude of internal variability and ACC). The SIE bias is reduced from $7.4 \times 10^{10} \text{ km}^2$ to



Table 2. Bias, bfRMSE and ACC for the SIE and SIV in March and September in the FREE, CTRL and +SIT experiments. The unit of bias and bfRMSE in SIE (SIV) is km^2 (km^3). Observed SIE is computed from NOAA OISSTV2 and we use SIV computed from PIOMAS. The system with the best performance is highlighted in bold.

SIE		March			September		
Experiment	Bias	bfRMSE	ACC	Bias	bfRMSE	ACC	
FREE	6.5×10^{10}	9.8×10^{10}	0.1	3.3×10^{10}	2.4×10^{10}	0.6	
CTRL	7.4×10^{10}	2.2×10^{10}	0.8	3.4×10^{10}	3.9×10^{10}	0.7	
+SIT	2.3×10^{10}	2.9×10^{10}	0.6	2.9×10^{10}	3.8×10^{10}	0.8	
SIV		March			September		
Experiment	Bias	bfRMSE	ACC	Bias	bfRMSE	ACC	
FREE	1.6×10^{13}	2.1×10^{12}	0.8	1.9×10^{13}	2.4×10^{12}	0.7	
CTRL	0.7×10^{13}	3.25×10^{12}	0.8	1.0×10^{13}	3.3×10^{12}	0.9	
+SIT	-1.0×10^{12}	3.72×10^{12}	0.9	0.4×10^{13}	2.5×10^{12}	0.9	

2.3 $\times 10^{10}$ km^2 by the SIT assimilation. ACC and bfRMSE of SIE are slightly degraded compared to CTRL (albeit better than FREE). This primarily relates to a spurious increasing trend until 2010 during the ENVISAT SIT observation period (Figure 5a). The performance of ACC and bfRMSE for +SIT is comparable to CTRL in the C2SMOS era (not shown). All systems 315 capture the decreasing trend in SIV well. Interannual variability is stronger in CTRL than in FREE and even more pronounced in +SIT. Despite some visual agreement in CTRL, ACC and bfRMSE are not improved compared to FREE. +SIT reduces the bias but has a larger bfRMSE than CTRL when compared to PIOMAS. Still, ACC is improved, and Figure 4d suggests that PIOMAS underestimates interannual variability (quarrelling results for bfRMSE depending on whether we use C2SMOS or PIOMAS). +SIT has a strong discontinuity in 2010 during the transition between ENVISAT and C2SMOS.

320 In September, all systems have high positive SIE biases as a direct consequence of anomaly assimilation. The ensemble mean of FREE shows, again, nearly no interannual variability. CTRL and +SIT show higher ACC values than FREE. The agreement is better in +SIT, with ACC increasing from 0.7 to 0.8, and slightly reduced bfRMSE. +SIT better captures the amplitude of the peaks and, in particular, the minimum in 2007 and 2012. This shows a positive effect from the SIT assimilation, whereby a bias reduction in SIT at the end of winter leads to more grid cells becoming ice-free at the end of summer. For SIV, FREE 325 captures the trend well. CTRL and +SIT show a good agreement of interannual variability with PIOMAS, albeit with +SIT showing overall the best agreement. +SIT also reduces the bias effectively.

Finally, we investigate the mean climatology of IIEE (Section 3.1). The results (Figure 6) resemble the bias of SIE (Figure 4), which has the dominant contribution. However, +SIT and FREE had comparable SIE bias in summer, while for IIEE, SIT+ is superior, indicating it is not the sole contributor for IIEE. As such, FREE has the largest IIEE throughout the year, except 330 in September, October and November (where it is equal to CTRL, Figure 6). +SIT performs best for all months. It yields substantial improvement over FREE in the winter months (with some minor improvements over CTRL) and a substantial improvement over CTRL in the summer months. This implies that the location of the ice edge is most improved in summer by

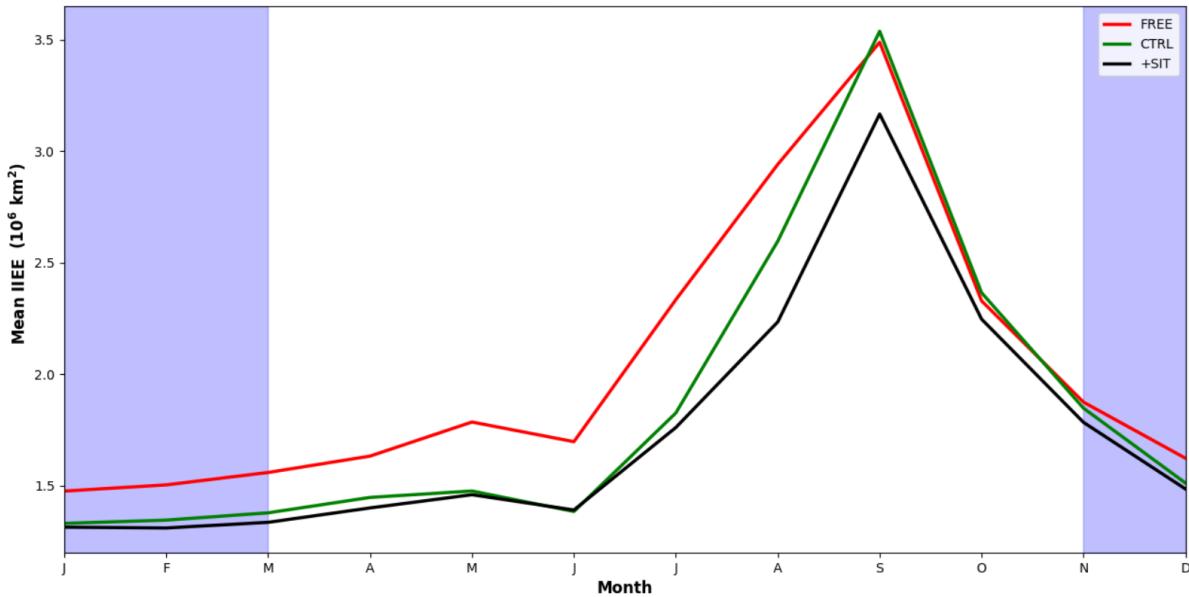


Figure 6. Ensemble mean of IIEE of three NorCPM experiments averaged over 2003-2023. The blue-shaded area shows the time when SIT observations are assimilated.

SIT assimilation. In winter, the location of the ice edge is controlled by the growth of new ice for which SIT plays a minor role, whereas in summer, the location of the ice edge is influenced by the melting of ice – i.e. when a grid cell becomes ice-free in summer (Section 5 for more detailed discussions) — for which the initial volume of ice is crucial. Thus, we can anticipate that SIT initialisation can bring added value to the prediction of the SIE minimum.

4.2 Prediction

We evaluate the prediction skill of our seasonal hindcasts for SIT, SIE, and IIEE using the metrics outlined in Section 3.1, and building on the reanalysis evaluation. For all quantities, we remove the trend that is highly predictable. The FREE experiment serves as a baseline for assessing skill driven by external forcings but shows minimal skill for detrended ACC (Kimmritz et al., 2019), so its results are not discussed here. Prediction skill and underlying mechanisms vary significantly by region (Bushuk et al., 2024). Our assessment spans both the pan-Arctic region and specific basins, following the approach of Bushuk et al. (2017). We compare the performance of CTRL and +SIT to highlight the role of SIT in improving predictability across different regions. We present the central Arctic, Beaufort Sea, Barents Sea, Bering Sea, and pan-Arctic regions as defined in, Bushuk et al. (2017), where the largest differences in SIE, SIT and IIEE skill between CTRL and +SIT are observed, but an assessment for other regions is also available in the supplementary material. Even if the time span of our experiment covers an

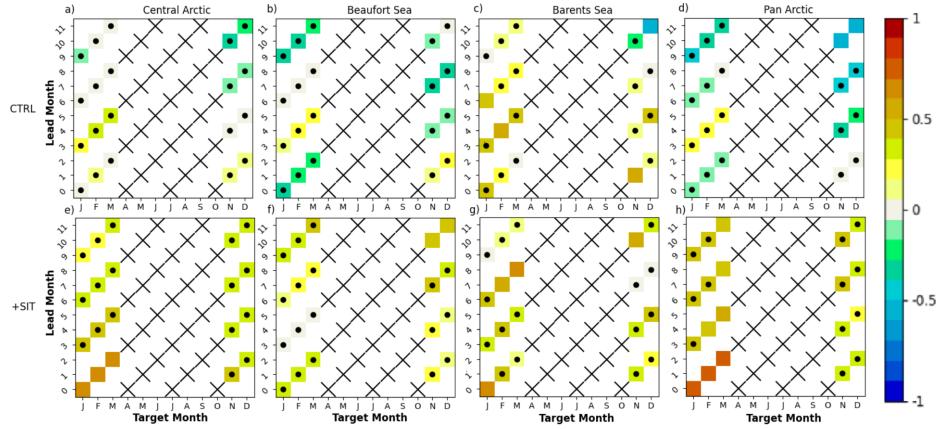


Figure 7. Detrended ACCs of our seasonal hindcasts for SIT from CTRL and +SIT with observations of SIT from CS2SMOS. The regions are defined by Bushuk et al. (2017).

unprecedentedly long period to assess the impact of SIT on seasonal predictions, the limited sample size of 21 hindcasts per season makes it challenging to perform the significance test of the differences between the systems.

4.2.1 Prediction of sea ice thickness

350 The assimilation of SIT observations improves detrended ACC and detrended bfRMSE of SIT prediction (Figure 7). In each region, ACCs of +SIT are positive and higher than the ones of CTRL, which are mostly not statistically significant (the top row of Figure 7). However, in most cases, ACC of +SIT does not pass the student's t-test due to the small sample size (the bottom row of Figure 7). Results are clearer with bfRMSE. +SIT shows lower bfRMSE than CTRL in almost all four regions and target months (Figure 8).

355 In the central Arctic, there is an overall improvement of detrended ACCs and bfRMSE for all lead months, but significant detrended ACCs +SIT are only found for +SIT in January-March. This coincides with times when detrended bfRMSE is also most reduced from CTRL. There is also a small reduction of detrended bfRMSE in winter. This suggests that the year-to-year anomaly of SIT can be predicted beyond 12 lead months.

360 In the Beaufort Sea, there is again an overall increase in detrended ACC (as for the central Arctic), but it is only significant in November-December, for hindcast initialised in January and March. Detrended bfRMSE is also strongly reduced for this hindcast. A clear improvement is also found in January-March for long lead times. It is somewhat surprising to see a degradation, in January for hindcasts started in October (at lead month 3), but an improvement for hindcasts started in March (at lead month 9). Both hindcasts assimilated the last SIT in March, but the October hindcast assimilated SIC and ocean observation from April to September in addition. This implies that the SIC assimilation degraded the accuracy of the SIT. Hence, we have 365 seen in Section 4.1, that CTRL reduces error compared to FREE, but still performs substantially poorer than SIT+ for SIT. This indicates that the persistence of SIT initialisation across summer is more accurate than using SIC for updating SIT.

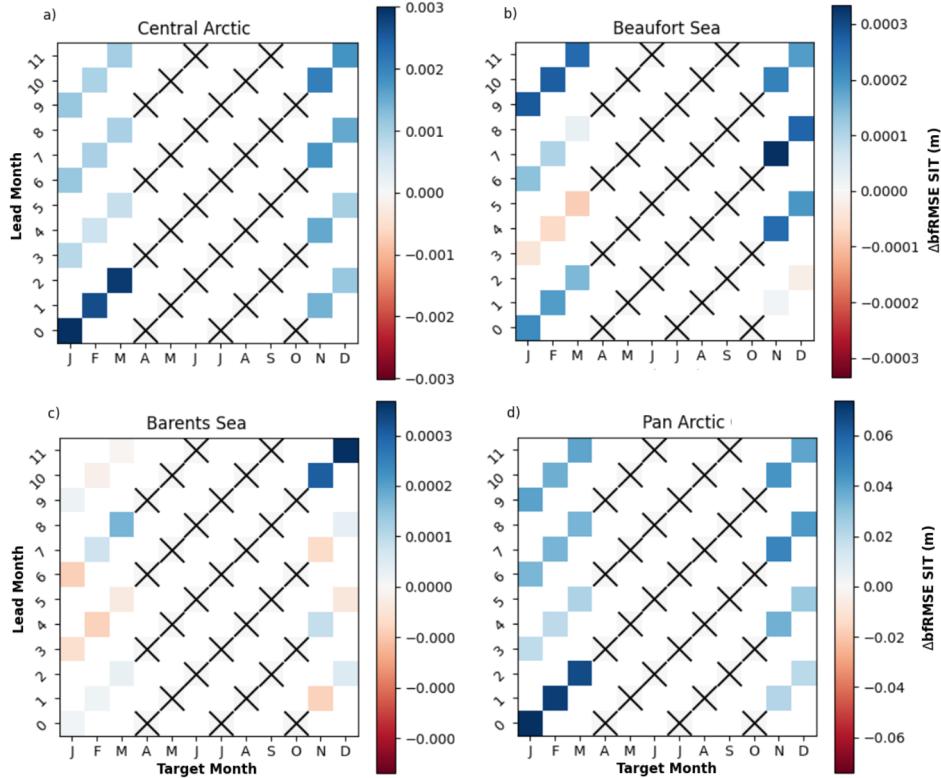


Figure 8. Differences in detrended bFRMSE of SIT from CTRL and +SIT experiments against observations from CS2SMOS. As Figure 7, we show bFRMSE only in four of the regions defined by Bushuk et al. (2017). Blue (red) colour indicates +SIT is better (worse) than CTRL.

The benefit is much less clear in the Barents Sea. For the July-initialised prediction, there was significant ACC up to lead month 8 in February-March. There is also a significant correlation associated with a strong reduction of bFRMSE at lead month 12 in December. This is associated with a good climatology for SIT, SIE and (possibly) SID in November, December and 370 January.

The pan-Arctic is the region for which we see the largest benefit from initialising SIT. The detrended ACC values are improved and the correlations are significant in January-March up to lead months 12. The associated detrended bFRMSE values are in agreement and also strongly reduced. Improvements in November-December are comparatively smaller than that of the later winter months, which can again be attributed to the lack of SIT observations in summer.

375 Overall, the SIT prediction results are quite promising and consistent with some previous studies (Blanchard-Wrigglesworth et al., 2011b, a). The impact is largest in the central Arctic and Beaufort Sea, where the observations are most accurate and where SIT anomalies persist longest. Our analysis did not assess prediction skills beyond 12 months lead time, but significant prediction skills of SIT were found to reach this limit — e.g. in the Beaufort and the Pan-Arctic.

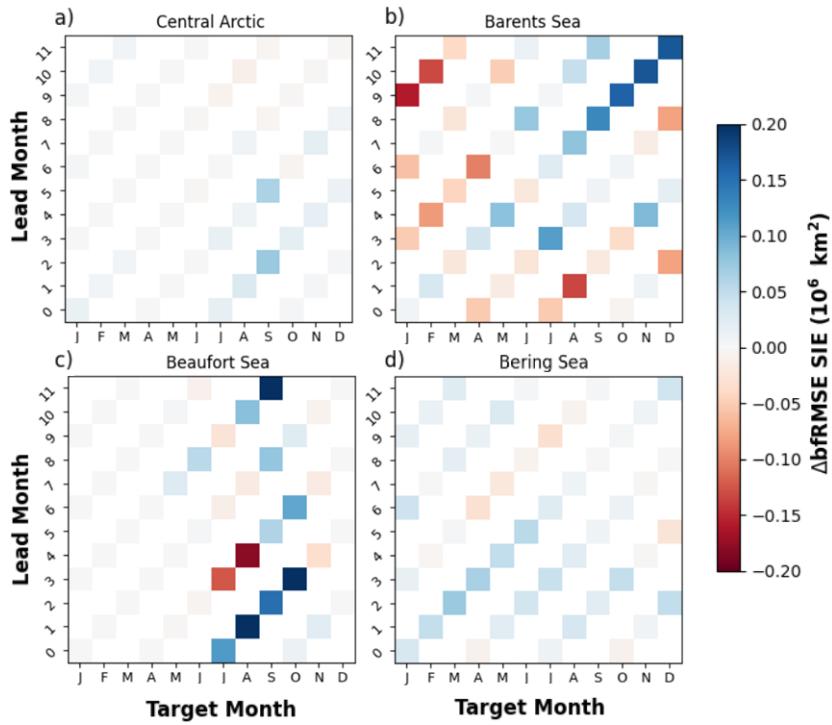


Figure 9. Difference in SIE detrended bfRMSE of CTRL and +SIT predictions computed with observations of SIE from NOAA in four Arctic regions. Blue (red) indicates that +SIT has lower (higher) bfRMSE than CTRL.

4.2.2 Prediction of sea ice extent and sea ice edge

380 For the predictions of SIE, we focus on bfRMSE and IIEE, as results from the ACC are less clear. ACC differences for detecting benefits from initialization can be problematic if the skill from the externally forced climate trend is high and the ACC differences are small – the normalisation step can yield misleading results (Smith et al., 2019).

The differences in bfRMSE between CTRL and +SIT are more nuanced than for SIT, as shown in Figure 9 and somewhat disappointing. In the central Arctic, there is little change except in the September SIE prediction for the April and July initialisations, which shows some improvements in +SIT. In the Barents Sea, the results mixed, with some improvements in predictions from January, but degradation in the other start months. In the Beaufort Sea, there are quite strong improvements around August-October for every lead time, but it does also appear to lead to some degradations in the months preceding. Finally, in the Bering Sea, improvements are more homogeneous for the first few months, with January initialised hindcast showing more substantial improvements. There are some improvements in bfRMSE in some other Pacific-side marginal regions.

390 As we did for the reanalysis, we investigate the IIEE of the hindcasts in Figure 10. The IIEE shows substantial improvement centered around September for all lead months, with improvement generally occurring between August to November. The result for the full RMSE of SIE looks very similar (not shown). As such, the location of the ice edge is improved primarily due

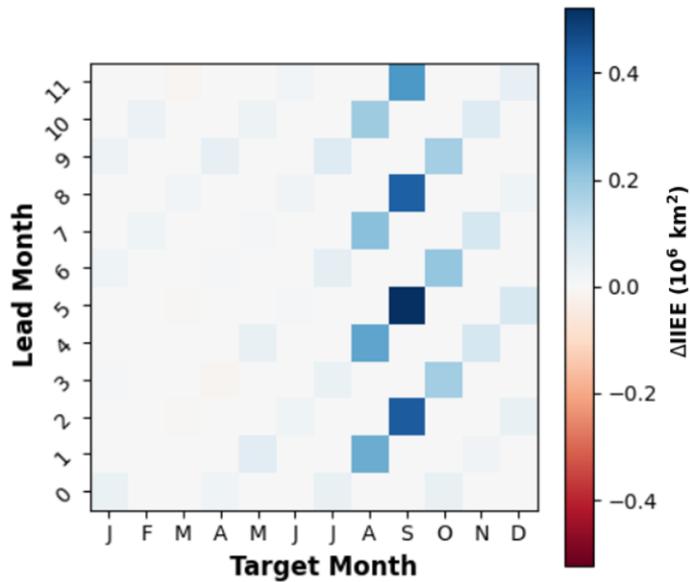


Figure 10. Difference of IIEE from CTRL and +SIT over the whole Arctic. Blue (red) means +SIT is better (worse) than CTRL.

to the bias changes in SIT, which improved the SIE bias during that period (Figure 4). In order to better exemplify that we will look in more detail at the Beaufort Sea has consistently shown the most positive results for predictions of SIE in our study so far.

We look at the SIE climatological mean of the hindcast in the different systems and for different start months in the Beaufort Sea (Figure 11). The +SIT system climatological minimum is in better agreement with the NOAA observations for each start month than the CTRL and FREE predictions. The improvements are largest during the melt season – even for the October initialised hindcast. This is in good agreement with the improvements we saw for the IIEE and confirms that the main reason for improvements in IIEE relates to improving the SIT bias that reduces the bias in SIE during the melting season.

5 Discussions and conclusions

In this study, we have used the NorCPM coupled global climate model to assimilate SIT data alongside SIC, SST and ocean profiles of temperature and salinity data. We compared the performance of our system that assimilated SIT in addition to the other datasets, to highlight the role of SIT in improving predictability across different regions. We first produced a reanalysis and then used this reanalysis to initialise seasonal hindcasts (+SIT). We validated our results not only using the standard metrics (bias, bfRMSE and ACC), but also IIEE, which provides unique insights on skill at the ice edge. We also measured our results against independent SIT measurements from the BGEP ULS moorings.

We evaluated the assimilation of ENVISAT and CS2SMOS SIT data into NorCPM. While ENVISAT has higher uncertainties than CS2SMOS, it extended the reanalysis period and improved SIT and ice edge estimates in the central Arctic, particularly

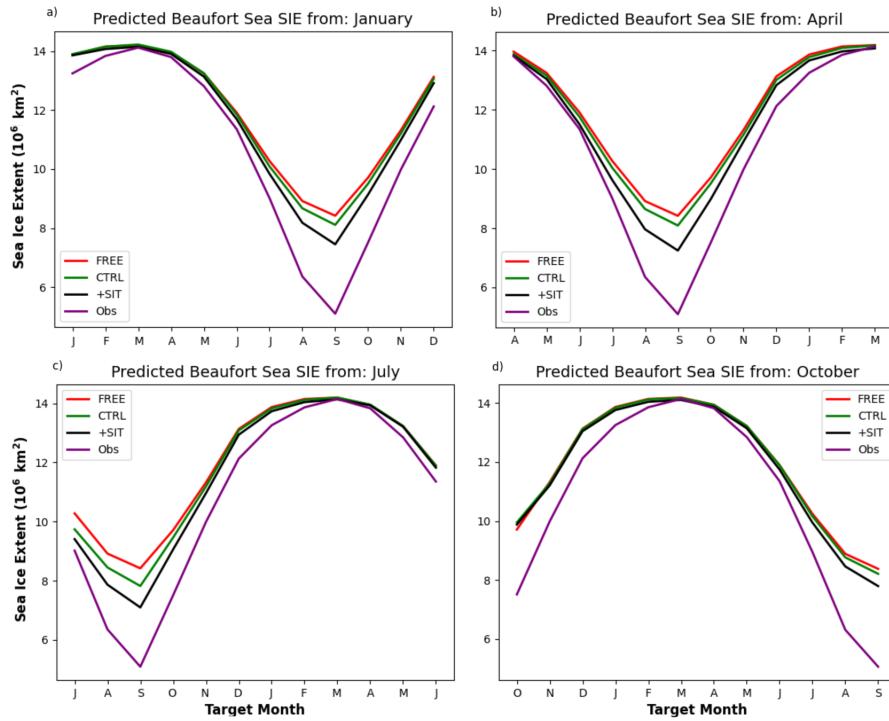


Figure 11. Climatological mean of SIE predictions from our NorCPM experiments and observations from NOAA in the Beaufort Sea. The region is as defined by Bushuk et al. (2017)

410 during the melt season. CS2SMOS provided more accurate data and greater reductions in biases, especially after 2010. Despite its limitations, ENVISAT data proved useful for reanalyses – highlighted by the DFS metrics that quantify the influence of each observational product – and provides meaningful observations in a period and location where observations are crucially lacking. We experienced some challenges in the transition period between ENVISAT and CS2SMOS, noticeable by discontinuities in the time series of SIE and SIV. It is because ENVISAT has a high uncertainty due to the instrumentation, which 415 disproportionately observes thicker ice (Louet and Bruzzi, 1999; Schwegmann et al., 2016; Tilling et al., 2018). There has been some initiatives to harmonize the two products by correcting for the bias in ENVISAT using CS2 and the period where the two products observational period overlapped between 2010–2012 (Tilling et al., 2019). Using a bias-corrected ENVISAT together with CS2 could lead to further improvements in reanalysis and prediction for SIT and SIE. There will also be a possibility in the future to assimilate a recently developed ice thickness dataset dating back to 1994 (Bocquet et al., 2024), substantially 420 lengthening the reanalysis by a further ten years and ensuring the consistency of the different sources of observations.

Our newest reanalysis +SIT showed substantial improvements compared to previous NorCPM versions (i.e., CTRL and FREE) with regard to ice thickness and ice volume. Bias and bfRMSE in SIT were both significantly reduced in +SIT, as our FREE and CTRL reanalyses have too thick ice all over the central Arctic and then large positive thickness biases in some places of up to 5 metres in comparison to CS2SMOS. The positive effects of the thickness assimilation in the +SIT reanalysis thus led



425 to improvements in the ice volume estimates. The improvements in the volume estimates are difficult to completely validate due to the lack of sea ice volume observations, but compared well with the PIOMAS reanalysis, which has been extensively validated with thickness measurements over a long period (Schweiger et al., 2011). The +SIT reanalysis also showed a reduced bfRMSE of SIV, highlighting that the assimilation does correct more than just the SIT bias. Validation with independent BGEP ULS measurements of SIT showed that the +SIT reanalysis had substantially smaller bias and bfRMSE than CTRL and FREE,
430 including during the ENVISAT period from 2003 to October 2010. The improvement in SIT also yielded improvement in SIE during the melting season and, therefore, also for IIEE.

We found that thickness prediction was substantially improved by the ice thickness assimilation across almost all regions. The largest part of the error reduction was from correcting model bias, which persisted throughout the year in good agreement with previous studies (Bushuk et al., 2017; Schröder et al., 2019). However, our results also showed that the SIT assimilation
435 improved the detrended bfRMSE up to 12 lead months, with the most notable improvement in the Pan-Arctic, Beaufort Sea and the central Arctic. Skill was not as clear in the Barents Sea. The results showed that we could predict SIT anomalies for at least up to a year in some regions. It would be interesting to extend the length of the hindcast to assess up to which time scale year-to-year anomalies of SIT are predictable. We could also clearly identify the detrimental impact of the lack of SIT observations during summer, highlighting the need to consider a product that extrapolates SIT estimate during that season – as
440 for example Landy et al. (2022).

Correcting the SIT bias and anomaly had a lower-than-expected impact on the Arctic SIE predictions. Correcting the SIT bias yielded improvements in the climatology of SIE in the melting season and, as a consequence for the IIEE metric. This improvement in late summer agreed with previous sea ice prediction studies with thickness initialisation (Bushuk et al., 2017; Schröder et al., 2019), which have found SIT assimilation can help to reduce thickness biases and thus improve SIE prediction.
445 The reason is that SIT reduced the positive bias in our model and, as a consequence, increased the area and the transition pace towards a sea ice minimum. However, if one removes the trend and the mean bias, the SIT brings some but little added value. Some skills were identified in the Beaufort during summer, central Arctic and Bering Sea. This was when and where NorCPM (CTRL) tends to perform the poorest compared to other dynamical models submitted to SIPN (Bushuk et al., 2024). Still, SIT assimilation also yielded some degradation in the other basins (e.g., Barents Sea). This was likely related to the discontinuity
450 in the observation period (summer observations missing and transition from ENVISAT to CS2SMOS). Furthermore, it should be remembered that even if our study covers an unprecedentedly long period (21 years), this is still too short to assess robustly year-to-year variability, especially considering the large trend in Arctic sea ice that can modulate internal variability.

Overall, this study advances the prediction capabilities of sea ice in NorCPM through additionally assimilating SIT data alongside SST, ocean profiles of salinity and temperature and SIC data. Here, we showed some improvements in SIT, SIE and
455 IIEE prediction using SIT initialisation. While the improvement of SIT was extended for the whole year and all lead time, SIE and IIEE were improved primarily during summer and in the central Arctic, where the improvement relates to a reduction of bias. We also found that the ENVISAT dataset can be useful for sea ice reanalyses and prediction (for monthly averages), which, to our knowledge, have been assimilated into a global climate model for the first time. Still, the SIT improvement on detrended SIE anomalies is lower than expected. As SIT plays an important role in the dynamics and thermodynamics of sea



460 ice, a possible reason may be that the sea ice model parameters used in this study have been calibrated to compensate for model bias. This can be bias in SIT, but also bias in the other components. A new ensemble-based parameter estimate was developed in NorCPM to tune model parameters efficiently (Singh et al., 2022, 2024). For our next steps, we aim to test the use of sea ice drift assimilation for refining three key sea ice parameters: air-ice stress, ocean-ice stress, and ice strength in a version of the model state that is sustained to a low level.

465 *Code and data availability.* During the revision phase, NorCPM data and scripts used in this study will be uploaded to the NIRD Research Data Archive which is the Norwegian long-term storage service for research data under the Open-Access license. EN4.2.1 and EN4.2.2 salinity and temperature profile data can be downloaded from <https://www.metoffice.gov.uk/hadobs/en4/download-en4-2-1.html>, NOAA SST and SIC data is available from <ftp://ftp.cdc.noaa.gov/Datasets/noaa.oisst.v2/>, ENVISAT ESA CCI SIT data is available from <http://catalogue.ceda.ac.uk/uuid/f4c34f4f0f1d4d0da06d771f6972f180>, C2SMOS v2.6 data is available from ftp://ftp.awi.de/sea_ice/product/cryosat2_smos/v206/,

470 PIOMAS data is available from <https://psc.apl.uw.edu/research/projects/arctic-sea-ice-volume-anomaly/data/>. BGEP ULS mooring data is available from the Woods Hole Oceanographic Institution website <https://www2.whoi.edu/site/beaufortgyre/data/mooring-data/>.

Author contributions. FC, YW and NW all wrote code pertaining to sea ice thickness assimilation in NorCPM and designed the experiments. NW conducted the experiments and produced the figures. NW produced the paper with assistance, feedback and edits from YW and FC.

Competing interests. The authors declare that they have no competing interests.

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