Response to Referee

We sincerely appreciate your thoughtful and exhaustive comments and suggestions, which significantly help us to improve the quality of the manuscript.

However, I made a big mistake in my understanding of the tropopause as defined by the World Meteorological Organization, which made my algorithm wrong and on which a large part of the whole article is based. So, we will adjust the whole article by removing the part of modification to the definition of WMO and adding the long term trend analysis of the tropopause.

We would like to express our sincere gratitude to the referee for your exceptionally informative, constructive, and detailed comments. We would appreciate it if you could give us your valuable comments for the revised manuscript.

General comment

I have read this manuscript, and unfortunately, it falls short in terms of quality and presentation. What is worse, it seems to be built on a set of misunderstandings on what tropopause is, apparently, a lack of knowledge of the existing literature and research performed on it. The lack of discussion in the Introduction of the existing work in the field and even the doubtful use of some papers to support some statements (or not citing them) is another issue of concern here. I develop all this below, and because of it, I consider that this manuscript must be rejected for publication, not in this journal, but in any other in its current form. I do not like to be so categorical, but this manuscript presents serious flaws in this case.

First, as evident from the work presented, the title of the manuscript is grandiloquent, overstating, and not representative of the work presented here, which is, at best, a small study on how different statistics give different results. The fact that is applied to the tropopause is a minor detail. It does not exist any dilemma in the scientific community on what it is the tropopause or how to define it, and high-resolution radiosondes,

mentioned in the title as if they were a key part of the work, are not compared against other radiosondes, so it is not possible to establish here anything from them. Also, it has been proved that in some cases, the vertical resolution of the radiosonde data compared to IGRA, which they mention here, does not impact the final statistics on tropopause. At least this previous work should be cited in the text: Antuña et al. (2006) https://doi.org/10.5194/angeo-24-2445-2006

The authors try to propose better tropopause "definitions" that accommodate the high-resolution radiosonde data. However, they never study if they are seeing tropospheric and stratospheric air masses, and their reasoning to support their criteria as valid is not backed by anything and obviates all the existing literature on the complex structure of the tropopause, their inversion layer, multiples tropopauses, latitudinal transport of air masses, and regional characteristics. Even their split in different regions does not follow the usual practice in the community, which makes any potential intercomparison hard.

Some parts of the manuscript contain incorrect statements, and the presentation presents flaws in some parts. These problems with the quality of the manuscript submitted undermine confidence in the quality of the work presented here.

Response: These criticisms were invaluable, and I recognized my mistakes and reworked the entire manuscript, removing the section on improvements in the definition of WMO and adding a study of long-term trends in tropopause heights.

Specific comments

1. Line 32: It is hard to understand the selection of the work by Xian and Homeyer (2019) to establish in a paper what tropopause is in the atmosphere. With all the due respect to their work, their study is one more in a large existing literature about the tropopause, and is cherry-picked here. One would reasonably expect that the first paper to be cited to explain what is the tropopause is a review paper, a seminal work or book, such as the definition in the Encyclopedia of Atmospheric Sciences,

or a paper such as Fueglistaler et al. (2009) or Gettelman et al. (2011).

Response: Amended as suggested.

Line 31: "... The tropopause, marking the boundary between the turbulent troposphere

and the stably stratified stratosphere, is a "gate" for exchange of energy, air masses,

water vapor and so-called very short lived substances (Fueglistaler, 2009)."

2. Line 45: "defining" the tropopause does not lack a universal approach. The

tropopause has a definition given by the WMO. What can be different is the

separation between a tropospheric and a stratospheric regime. Obviously, different

characteristics of the troposphere and stratosphere produce a transition between

both layers that is different from the tropopause thermal definition, but this does

not mean that the tropopause does not have a definition.

Response: This part has been removed.

3. It is important that the authors make a clear difference here between the

characteristics that define the layer that separates the troposphere and the

stratosphere regimes and the transition layer itself. This can be done by clarifying

that the tropopause has a definition, but many "criteria" can be used to separate the

tropospheric and stratospheric characteristics. The dynamic criterion (usually

based on Potential Vorticity fields) does not fail at midlatitudes but in the tropics,

where potential vorticity isolines get vertical. Actually, the authors make the point

correctly in line 107. If they are going to talk about the different criteria in a

manuscript that intends to deal with the determination of the tropopause, one would

also expect a complete overview of it, mentioning the e90 by Prather et al. and the

different PV values tested by Hoinka.

Response: Amended as suggested. We have added citations and a short note.

Line 51: "...and the dynamic tropopause (WMO, 1985; Hoinka, 1998), typically

defined by potential vorticity (PV) thresholds of 1.5–4 potential vorticity unit (PVU) (Turhal et al., 2024), is less reliable in regions of low absolute potential vorticity, such as the tropics, and sometimes in mid-latitudes where strong anticyclonic flow prevails (Hoerling et al., 1991)."

4. Line 47: It is important to include citations to the different criteria to determine the tropopause for those unfamiliar with the topic. One of the best for the CPT is the paper by Gettelman et al. (2000), which began to make popular the topic. For the dynamical tropopause, the combination of the WMO (1985) technical report and the paper by Hoinka (1998) give the necessary information.

Response: For the CPT we have added a reference: Highwood and Hoskins, 1998. For the dynamical tropopause, amended as suggested.

Line 49: "...The cold point tropopause (CPT) get the tropopause via the minimum temperature in the vertical temperature profile, which is unsuitable for extratropical regions (Highwood and Hoskins, 1998), and the dynamic tropopause (WMO, 1985; Hoinka, 1998), typically defined by potential vorticity (PV) thresholds of 1.5–4 potential vorticity unit (PVU) (Turhal et al., 2024), is less reliable in regions of low absolute potential vorticity, such as the tropics, and sometimes in mid-latitudes where strong anticyclonic flow prevails (Hoerling et al., 1991)."

5. It is also important to note that the WMO definition (as anyone thermal) fails in polar regions, because of the low vertical gradient that exists in those regions during parts of the year, contrary to what the authors state in lines 49-50. And line 49 should read "The tropopause definition (WMO, 1957), which is thermodynamic..."

Response: Amended as suggested.

Line 54: "However, the tropopause definition (WMO, 1957), which is thermodynamic, proposed by the World Meteorological Organization offers a more robust global

approach (though it may occasionally fail in polar regions), providing reliable TH estimates from various datasets (Hoffmann and Spang, 2022)."

6. Line 51: The upward trend in the tropopause is not recent. The first report on it, already cited by the authors, is from 2003, and the existing data for this trend is from radiosonde data and goes back to 1958 (Seidel and Randel, 2006). I would cite here one of my papers, contemporaneous to the one of Seidel and Randel, Añel et al. (2006).

Response: Amended as suggested.

Line 70: "...More and more evidence suggests an upward trend in TH under a changing climate (Santer et al., 2003; Sausen and Santer, 2003; Seidel and Randel, 2006; Añel et al., 2006)."

7. Lines 54-57: It is hard to understand how this manuscript does not include a citation to the paper by Meng et al. (2021) https://doi.org/10.1126/sciadv.abi8065, which is one of the most recent discussing the tropopause rise from radiosondes.

Response: Amended as suggested.

Line 74: "...Meny et al. (2021) reported a TH increase of 50–60 m/decade (2001–2020) in the Northern Hemisphere based on radiosonde data."

8. Line 58: You should cite here the papers for IGRA: Durre et al. (2006, 2018), which you already include in the list of references.

Response: Amended as suggested.

Line 77: "...It is worthwhile to note that these radiosonde-related studies use data from the Integrated Global Radiosonde Archive (IGRA), a global dataset with coarse vertical resolution (approximately 300 to 400 m) (Durre et al., 2006, 2018),..."

9. Line 63: It is unclear what the authors want to say here. A couple of sentences before, they say that radiosonde data (IGRA) suffers from vertical resolution problems; now, here, they say that radiosonde data have greater vertical resolution. Do you refer now here to "raw" radiosonde data and not the soundings included in IGRA? Please clarify.

Response: Amended as suggested.

10. Line 70: "tropopause also exits as inversions". It is unclear what you want to say or imply with this sentence fragment. Please clarify.

Response: Amended as suggested. We delete it.

11. Line 78: it is unnecessary to clarify that ERA5 is the sucessor to ERA-Interim, please, delete it.

Response: Amended as suggested.

12. Line 94: quite self-serving, but if you talk about studying the tropopause structure from radiosonde data, you are probably missing the only study that is important to cite (jointly with the Birner et al. (2006) paper on the TIL), the one that studies its global structure until the third tropopause level: Añel et al. (2008) Climatological features of global multiple tropopause events (https://doi.org/10.1029/2007JD009697).

Response: Amended as suggested.

Line 106: "...tropopause structure (Birner, 2006; Seidel and Randel, 2006; Añel et al., 2008; Sunilkumar et al., 2017)..."

13. Line 100: Using a previously published paper to cite three different data sources is far from being the best practice. Instead, you should provide the exact data repositories for the datasets that you use. Following the better current standards on data citation, at least they should have a DOI. It would be great if they had it.

Response: Acquiring globally representative high-resolution radiosonde data

necessitates integration of multiple observational sources, as no single dataset provides

complete spatial coverage. URL links are available in the Data availability section of

the manuscript.

Line 115: "...Following Guo et al. (2021) and Zhang et al. (2022), we utilized a high-

vertical-resolution radiosonde (HVRRS) dataset spanning 2000 to 2023 (24 years),

compiled from multiple sources including the China Meteorological Administration

(CMA), the National Oceanic and Atmospheric Administration (NOAA) of the United

States, the German Deutscher Wetterdienst (Climate Data Center), the Centre for

Environmental Data Analysis (CEDA) of the United Kingdom, the Global Climate

Observing System (GCOS) Reference Upper-Air Network (GRUAN), and the

University of Wyoming."

14. Line 105: again, no several methods exist to define the tropopause. Maybe to

separate the troposphere from the stratosphere.

Response: This part has been removed.

15. It is Ertel's Potential Vorticity, not Rossby-Ertel. Rossby's formalism does not

contain the features later developed by Ertel (conservation) that make the EPV a

tracer that can separate stratosphere and troposphere air masses.

Response: Thanks for the correction. This section was not included after the revised

manuscript.

16. Lines 111 and 114: I am being picky here, but the WMO definition does not contain

the quotation marks used by the authors here, but the terms "first tropopause" and

"second tropopause" are given in italics. I think that the right way to do it would

be to put the full definition between the quotation marks and not only these two

terms.

Response: Amended as suggested.

17. Lines 150-152: I understand the argumentation by the authors; however, the statement "are likely to be more consistent with previous research." what do you mean by this? With what previous research? Why? This sounds like a willingness more than a scientific fact, and no previous research is cited to support such a statement. Then you say, "and understanding of the tropopause." This statement is baseless. Here, in these soundings, the authors do not check what the troposphere or the stratosphere is. For example, in Fig. 1a,b, have you checked if the air mass between the WDM and the MV or C-F is of stratospheric or tropospheric origin? Guessing that the WDM is not a valid tropopause is not enough; if you are stating it, you should prove it, for example, with PV and ozone fields. This station is located around the subtropical jet stream, a region prone to the occurrence of multiple tropopauses (see Añel et al. 2008), and where the tropospheric and stratospheric air masses mix along several km in the vertical. You can not simply state that the WDM is a not valid tropopause when, for January, the tropopause can appear in the region of this sounding at levels so low as 200 hPa (see Añel et al. (2008) again, e.g., Fig.4), and in a latitude where the latitudinal entrainment of midlatitudes stratospheric air under the tropical tropopause makes hard to define the change between the tropospheric and stratospheric air masses. See Wang and Polvani (2011) and Añel et al. (2012).

Response: Thanks for the criticism, this part of my argument is insufficiently supported. The revised manuscript no longer contains that image and its interpretation of its contents.