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1 May 16, 2025

2 To: Dr. Heng Dai, Editor of Hydrology and Earth System Sciences

Subject: Revision of Paper # EGUSPHERE-2024-4145

Dear Editor:

Upon the recommendation, we have carefully revised Paper # EGUSPHERE-2024-4145 entitled "Improving heat transfer predictions in heterogeneous riparian zones using transfer learning techniques" after considering all the comments made by the reviewers. The following is the point-point response to all the comments.

Response to Reviewer #1:

Overview:

This manuscript proposes a Deep Transfer Learning (DTL) approach to improve the accuracy of spatiotemporal temperature distribution predictions in heterogeneous riparian zones. Using transfer learning, the authors integrate analytical solution outputs for a homogeneous medium into a Deep Neural Network (DNN) and employ a 2D numerical model output for a heterogeneous medium as their synthetic data. They tested their approach by comparing the DTL to a DNN trained solely on synthetic data across various heterogeneous media and noise levels. Their findings indicate that the DTL model outperforms the DNN model in scenarios with limited training data and demonstrates greater robustness to data noise, which may have practical applications in riparian zone management.

The current version of the manuscript requires significant work. Essential information regarding the physical-based models used to train the DTL and DNNs is missing, as well as clarifications on the input and output variables of the machine learning models needed for testing and reproducing the work presented. Additionally, the authors should include the reasoning behind their sampling criteria and how it is linked to the physical process they are modeling, as well as highlight how their novel framework differs or adds from work done by previous authors. With the latter in mind, I cannot accept the manuscript in its current form.

Below, I have listed comments and suggestions, hoping they may help improve the manuscript's quality.

Reply: Thanks for your constructive comments. We have carefully revised Paper # EGUSPHERE-2024-4145.

Specific Comments:

The physics-based models need further clarification.

(1) The authors based their analytical and numerical models on previous work performed by Shi et al. (2023) and they present some of the equations and boundary conditions in the manuscript and the supplementary information. However, the manuscript does not clarify the actual domain of the system. Are they using the model's domain as the conceptual model presented in Figure 1? If so, why are the modeling results presented in a square? Is this an inset of the larger domain? If so, where is the inset located for the whole model? If it is not an inset, is the domain different from the one presented by Shi et al. (2023)? If so, why is its extent

shorter than that of the original study? A clear description of the conceptual model and its boundary conditions should be included in the main manuscript to aid in the understanding of the physical process.

Reply: Implemented. Please see Lines 98-115 and section S1-"Analytical solution of the 2D heat transfer process in homogeneous streambed" and S2-"Numerical solution of the 2D heat transfer process in heterogeneous streambed" in the Supplement.

Figure 1 is the schematic of the conceptual model illustrating heat transfer induced by surface water-groundwater interactions. Similar to Shi et al. (2023), the square domain used in this study represents a simplified case of the conceptual model. The groundwater flow model and heat transfer model are coupled through q_x and q_z , which are directly defined in the analytical model used in this study. Therefore, only the boundary conditions of the heat transfer model need to be considered in the analytical model. For heterogeneous scenarios (numerical model), the boundary conditions of groundwater flow model are applied to generate two-dimensional nonuniform flow fields, which are used to create fine-tuning and testing samples under heterogeneous streambed conditions. The settings of initial and boundary conditions are shown in Figure S2.

To improve simulation accuracy and avoid boundary effects in numerical model, the semi-infinite geometry size was replaced by a finite range, and two infinite element domains were added at x=1 m and z=1 m to represent the infinite boundary on the x- and z-directions, respectively. Therefore, the model's domain size does not influence the accuracy of either the analytical or numerical solutions, and Figure S1 further validates the accuracy of the proposed numerical model.

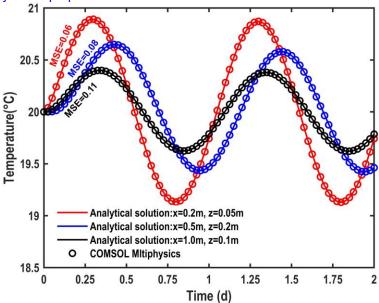
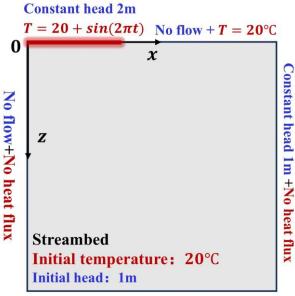


Figure S1. Comparison of temperature-time curves at three locations using the numerical solution (circle symbols) and the analytical solution of this study (solid curves).



No flow+No heat flux

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83 84 Figure S2. Conceptual model of 2D numerical model with streambed sediment, initial and boundary conditions. The red color zone represents the streambed with a half width of 0.32.

(2) Additionally, the groundwater flow model and its boundary conditions are not mentioned. Is this the same model as the one used in Shi et al. (2023)? This should be included and clarified in the manuscript for an integral understanding of the process that the data-driven models are trying to reproduce.

Reply: Implemented. Similar to Shi et al. (2023), the groundwater flow model and heat transfer model are coupled through q_x and q_z . In the analytical model, q_x and q_z are directly prescribed; therefore, only the boundary conditions of the heat transfer model need to be considered in the analytical model.

For heterogeneous scenarios (numerical model), the boundary conditions of groundwater flow model are applied to generate two-dimensional nonuniform flow fields, which are used to create fine-tuning and testing samples under heterogeneous streambed conditions. The settings of initial and boundary conditions are shown in Figure S2.

(3) Incidentally, part of the work looks into heterogeneity, and the authors present their heterogeneous fields. Nonetheless, there is no mention of which hydraulic conductivity value is used for the homogeneous case. The authors only mention variations in the Darcy's fluxes $(q_x \text{ and } q_z)$ in line 167. How are these fluxes calculated? What values are used for head gradients? Are the variations of these Darcy's fluxes related to boundary conditions or fluxes through the domain? I suggest including the Darcy flux equation and leaving the variations only to hydraulic conductivity to be consistent with the heterogeneous cases.

Reply: The groundwater flow model and heat transfer model are coupled through q_x and q_z . In the analytical solution, q_x and q_z are directly prescribed. For the homogeneous case, we use two pairs of q_x and q_z values-(0.2 m/d, 0.3 m/d) and (0.6 m/d, 0.9 m/d)-to represent variations in hydraulic conductivity. The corresponding mathematical expressions are as follows:

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$$q_x = -K_x \frac{\partial H}{\partial x}$$
 (1)
86 $q_z = -K_z \frac{\partial H}{\partial z}$ (2)

$$86 q_z = -K_z \frac{\partial H}{\partial z} (2)$$

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$$v_{x} = \frac{c_{w}}{c_{s}} q_{x} = -K_{x} \frac{c_{w}}{c_{s}} \frac{\partial H}{\partial x}$$

$$v_{z} = \frac{c_{w}}{c_{s}} q_{z} = -K_{z} \frac{c_{w}}{c_{s}} \frac{\partial H}{\partial z}$$
(4)

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$$v_{\rm z} = \frac{c_{\rm w}}{c_{\rm c}} q_{\rm z} = -K_{\rm z} \frac{c_{\rm w}}{c_{\rm c}} \frac{\partial H}{\partial z} \tag{4}$$

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$$C_s = (1 - \theta)\rho_s c_s + \theta \rho_w c_w \tag{5}$$

where H is the hydraulic head [L]; q_x and q_z are streambed water flux [LT-1] components of the streambed 90 on the x and z-axes, respectively; K_x and K_z are the hydraulic conductivities [LT-1] on the x and z-axes, 91 respectively; v_x and v_z are thermal front velocity [LT-1] components of the streambed on the x- and z-axes, 92 respectively; C_w is specific volumetric heat capacity [J/(m3·°C)] of water; C_s is specific volumetric heat 93 capacity [J/(m3·°C)] of streambed; ρ_s and ρ_w are densities [ML-3] of porous media and fluid, respectively; 94 95

 c_s and c_w are specific heat capacities [J/(kg \cdot °C)] of porous media and fluid, respectively. Please see section S1-"Analytical solution of the 2D heat transfer process in homogeneous streambed" in the Supplement.

(4) The authors only present the fields for hydraulic conductivity and absolute errors, and there is no plot of the temperature field they are trying to reproduce. Are these fields different from each other? How does the heterogeneous domain affect the temperature distributions? I suggest adding a figure with the temperature fields for the analytical and the numerical solutions so that the reader can understand how these fields vary throughout the domain and what the data-driven models are missing.

Reply: Implemented. The transient temperature field is plotted in Figure 8. As mentioned in Section 3.1, the transient temperature field consists of 100-time steps, resulting in 100 corresponding temperature field figures. In this study, we selected the temperature field at 0.5d (i.e., the 50th time step) as the reference field to calculate the absolute errors. We have added the reference temperature fields at 0.5d (i.e., the 50thtime step) in Figure 8 to further demonstrated how heterogeneous hydraulic conductivity affect the temperature distributions. Note that the selection of 0.5d is rather arbitrary for the demonstration purpose and can be replaced by other time steps.

With respect to the machine learning models

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127 128 (1) The authors mention in line 15 that this work "[proposes] a novel Deep Transfer Learning (DTL) approach [...] to improve the accuracy of spatiotemporal temperature distribution predictions." However, a similar approach has been explored in Zhang et al. (2023) for the prediction of hydraulic heads in heterogeneous aguifers. The authors should clearly specify the improvements or modifications made to the framework compared to Zhang et al. (2023), beyond the difference in application.

Reply: First, while Zhang et al. (2023) focused on one-dimensional groundwater flow, our study addresses heat transfer in two-dimensional heterogeneous riparian zones. This involves fundamentally different governing equations (convection-diffusion) than the groundwater flow equations in Zhang et al. (2023), more complex physical processes (coupled flow and heat transport), and significantly higher computational demands. Second, we incorporate physical constraints and impose penalties for violations of initial and boundary conditions in the pre-trained DNN model by implementing an enhanced loss function. This approach ensures that our model adheres to fundamental heat transfer principles. These innovations collectively advance the application of deep transfer learning in environmental modeling beyond what was presented in Zhang et al. (2023), with particular emphasis on heat transport processes in riparian zones and a systematic evaluation of model robustness under various uncertainties. Please see Lines 133-154.

- 129 (2) In line 222, the authors mention that they restricted the number of epochs in the model training. Is there
- 130 a reason why these models cannot be trained with different epochs until they reach the same convergence?
- 131 Also, what about the other hyperparameters of the DNN models (i.e., number of nodes, number of layers,
- 132 epochs, and activation functions, among others), have the authors considered testing a range of these
- 133 parameters to get the best set of DNN?
- 134 Reply: We limited the number of epochs during model training primarily to reduce computational cost and
- 135 prevent overfitting. In addition, we employed an early stopping strategy to prevent overfitting by monitoring
- 136 the validation loss during training, thereby ensuring the model's generalization ability. This training strategy
- is widely used in Wang et al. (2021), Zhang et al. (2023) and Wang et al. (2023), and their works have 137
- 138 demonstrated 3,000 epochs are sufficient for the DNN model to converge.
- 139 In addition, the other hyperparameters of the DNN models are selected after multiple trials. Results indicate
- 140 that the predictions of the two pre-trained models closely align with the analytical model, with average MSE
- 141 values of 1.2E-6 and 1.5E-6, respectively. This further demonstrates that the hyperparameters of the DNN
- 142 model are suitable.
- 143 144 Reference:
- 145 [1] Wang, N., Chang, H., and Zhang, D. (2021). Deep-learning-based inverse modeling approaches: A
- 146 subsurface flow example [J]. Journal of Geophysical Research: Solid Earth, 126, e2020JB020549.
- 147 [2] Zhang J, Liang X, Zeng L, et al. Deep transfer learning for groundwater flow in heterogeneous aquifers
- 148 using a simple analytical model [J]. Journal of Hydrology, 2023, 626: 130293.
- 149 [3] Wang, N., Chang, H., and Zhang, D. (2023). Inverse modeling for subsurface flow based on deep learning 150 surrogates and active learning strategies [J]. Water Resources Research, 59, e2022WR033644.
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- 152 (3) Part of using these data-driven approaches is leveraging the current available data to predict variables
- 153 that are difficult, expensive, or impractical to measure. With this in mind, the authors should be clear about 154
- what variables they are using as input to predict the temperature fields. Are they using the hydraulic heads and temperature of the stream? Are they using variables related to the geology of the site? Or are they using 155
- 156 temperature data from previous timesteps? All of this is important because if we were to use these models
- 157 to predict the temperature in a given field site, we would need to know what variables we should measure to
- 158 be able to have an accurate prediction.
- 159 Reply: Implemented. This study focuses on improving heat transfer predictions in a heterogeneous
- 160 streambed using a deep transfer learning approach. We are concerned with the spatiotemporal thermal
- distributions of the streambed. Therefore, we do not use previous hydraulic head, temperature, or geological 161
- 162 variables as input parameters. In this study, the input data consists of spatial locations (x, y) and time t, with dimensions of $100 \times 100 \times 100$. The output data is the corresponding temperature. We have clarified 163
- 164 that in the manuscript. Please see Lines 193-194.
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- 174 (4) Furthermore, the authors should link their sampling criteria to the physical process they are trying to
- reproduce with data-driven approaches. For instance, grabbing more than 50 samples in a 1-meter cross-
- section with some spaced less than 0.1 meters horizontally is impractical and inefficient. I suggest the authors
- approach the sampling criteria as they were placed in the field, and are tasked to maximize the location of
- their thermistors or other measuring devices. This reviewer believes this approach can benefit the scientific
- 179 community and add value to the manuscript.
- Reply: Implemented. We agree that linking our sampling approach to realistic field deployment scenarios would enhance the manuscript's practical relevance.
- In Section 3.3, our study deliberately evaluated various observation point densities (1, 5, 10, 20, 50, and 100)
- to analyze the minimum monitoring requirements for effective model performance. Our results demonstrate
- that the proposed PDTL model exhibits robust performance even with sparse data (fewer than 10 observation
- points), which outperforms the traditional DNN approach under heterogeneous streambed conditions and
- with observation noise. Please see Figures 5, 6, 7, 9, 11.
- To establish statistically sound sampling criteria, we employed random sampling with 200 realizations for
- each scenario, following established practices in field hydrology (Holmes et al., 2006; Ali et al., 2009). This
- approach ensures unbiased sampling where every possible measurement location has an equal chance of
- being selected, which is critical for comprehensive model evaluation. Similar sampling criteria have been
- widely adopted in many recent studies (Goswami et al., 2022; Zhang et al., 2023).

193 Reference:

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- 194 [1] Holmes, K. W., et al. (2006). Designs for marine remote sampling: a review and discussion of sampling
- methods, layout, and scaling issues, Task 2.1 Milestone Report Published by the Cooperative Research
- 196 Centre for Coastal Zone, Estuary and Waterway Management (Coastal CRC).
- 197 [1] Ali, G.A. and Roy, A.G. (2009), Revisiting Hydrologic Sampling Strategies for an Accurate Assessment of
- 198 Hydrologic Connectivity in Humid Temperate Systems. Geography Compass, 3: 350-374.
- 199 [1] Goswami, S., Kontolati, K., Shields, M.D.et al. Deep transfer operator learning for partial differential
- equations under conditional shift. Nature Machine Intelligence, 2022, 1155-1164.
- [2] Zhang J, Liang X, Zeng L, et al. Deep transfer learning for groundwater flow in heterogeneous aquifers using a simple analytical model [J]. Journal of Hydrology, 2023, 626: 130293.
- 204 (5) Consider including an additional paragraph or sentences that describe other approaches to create physics-informed machine learning models (e.g., Arcomano et al., 2022; M. Raissi et al., 2019; Maziar Raissi & Karniadakis, 2018; Yeung et al., 2022).
- 207 Reply: Implemented. We have added the paragraph to describe the physics-informed machine learning models. Please see Lines 65-69.

210 Reference:

- [1] Arcomano, T., Szunyogh, I., Wikner, A., Pathak, J., Hunt, B. R., & Ott, E. (2022). A hybrid approach to
- 212 atmospheric modeling that combines machine learning with a physics-based numerical model. Journal of
- Advances in Modeling Earth Systems, 14(3), e2021MS002712.
- 214 [2] Raissi, M., Perdikaris, P., & Karniadakis, G. E. (2019). Physics-informed neural networks: A deep learning
- framework for solving forward and inverse problems involving nonlinear partial differential equations. Journal
- of Computational Physics, 378, 686–707.
- 217 [3] Jiang, S., Zheng, Y., and Solomatin, D (2020). Improving Al system awareness of geoscience knowledge:
- 218 Symbiotic integration of physical approaches and deep learning, Geophysical Research Letters, 47, 733-745.

- [4] Kamrava, S., Sahimi, M., and Tahmasebi, P (2021). Simulating fluid flow in complex porous materials by integrating the governing equations with deep-layered machines, npj Computational Materials, 7, 127.
- [5] Arcomano, T., Szunyogh, I., Wikner, A., Pathak, J., Hunt, B. R., & Ott, E. (2022). A hybrid approach to
- atmospheric modeling that combines machine learning with a physics-based numerical model. Journal of
- Advances in Modeling Earth Systems, 14(3), e2021MS002712.
- [6] Yeung, Y.-H., Barajas-Solano, D. A., & Tartakovsky, A. M. (2022). Physics-informed machine learning method for large-scale data assimilation problems. Water Resources Research, 58(5), e2021WR031023.
- [7] Zhao, W. L., Gentine, P., Reichstein, M., et al (2019). Physics-constrained machine learning of evapotranspiration, Geophysical Research Letters, 46, 14496-14507.
- [8] Cho, K. and Kim, Y.(2022). Improving streamflow prediction in the WRF-Hydro model with LSTM networks. Journal of Hydrology, 605, 127297.
- 231 (6) I suggest the authors add more information in the discussion section. Where they highlight the importance 232 of their work and how it relates to other approaches. I suggest also highlighting the transferability of this 233 framework to other settings, as well as things that scientists should take into account.
- Reply: Implemented. We have highlighted the transferability of our framework to other settings in the discussion section. Please see Lines 308-322.
- 237 **Technical Corrections:**

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- 238 (1) Lines 17-20 are difficult to read and contain variables that are not previously defined
- 239 Reply: Implemented. We have reorganized Lines 17-20 and removed the variables that are not previously defined. Please see Line 18-24.
- 242 (2) The sentence in lines 22-23 is redundant, so consider removing it.
- 243 Reply: Implemented. We have removed Lines 22-23.
- 245 (3) Grammar in line 89 "Newly proposed demonstrates"
- 246 Reply: Implemented. We have revised the "newly proposed demonstrates" to "newly proposed approach demonstrates". Please see Line 92.
- 249 (4) In line 294 should be "centers" instead of "centres"
- 250 Reply: Implemented. We have revised the "centres" to "centers". Please see Line 326.
- 252 (5) What do you mean by "it is postulated that the thermal and hydraulic properties of the streambed maintain uniformity"? (Lines 98-99). Are you referring to the fact that these variables remain constant throughout the simulation? Please clarify.
- 255 **Reply:** Implemented. It has been rephrased to provide better clarification. In fact, we want to express that the thermal properties are homogeneous of the streambed. However, for hydraulic properties, i.e., hydraulic
- conductivity, we considered both the homogeneous and heterogeneous scenarios. Please see Lines 101-102.
- 260 (6) It should be "no heat flux boundary" in line 102.
- 261 Reply: Implemented. We have revised it to "no heat flux boundary". Please see Line 105.

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- 263 (7) I recommend collapsing equations (1a) through (1c) to a single equation with a subscript i that is later described.
- 265 Reply: Implemented. We have collapsed equations (1a) through (1c) to a single equation with a subscript *i*. Please see equation (1a).

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- (8) Line 144 states that "The hyperparameters θ_T for the fine-tuning model is acquired through the optimization of the loss function delineated by..." By definition, a hyperparameter cannot be estimated with model training. They are set by the user. I think that you mean "The parameters" instead of "The hyperparameters."
- 272 Reply: Implemented. We have revised the "hyperparameters θ_T " to "parameters θ_T ". Please see Lines 170.

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- 274 (9) Some variables, such as q_x and q_z , are not defined in the main manuscript. Since the manuscript should 275 be self-contained, these variables should be specified in the text.
- Reply: Implemented. We have defined q_x and q_z in the Supplement. Please see S1-"Analytical solution of the 2D heat transfer process in homogeneous streambed" in the Supplement.

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- 279 (10) Remember to add the units of the Mean Square Error (MSE) values.
- Reply: To mitigate the impact of dimensionality during the training process, the temperature field dataset is normalized to [-1,1], and the temperature field dataset becomes dimensionless. Please see Lines 120-126.

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283 (11) The text in Figures 5, 6, and 10 is difficult to read. Consider increasing the fonts. Also, include the units of the variables plotted.

285 Reply: Implemented. We have increased the fonts and units of the variables in Figures 5, 6, and 10. Please see Figures 5, 6, and 10.

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- 288 (12) Consider using the same y-scale for Figures 7, 9, and 11. This would aid in the comparison.
- 289 Reply: Implemented. We have used the same y-scale for Figures 7, 9, and 11 for better comparison. Please see Figure 7, 9, and 11.

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292 Response to Reviewer #2:

Overview:

The manuscript presents a novel Deep Transfer Learning (DTL) framework for improving the prediction of spatiotemporal temperature fields in heterogeneous riparian zones. The authors leverage analytical solutions in homogeneous domains to pre-train a DNN model, and subsequently fine-tune it for heterogeneous cases, thereby addressing the challenge of limited observational data. The study is well-motivated and addresses an important problem in hydrological modeling. The methodology is clearly described, and the results are well-documented through a series of comprehensive experiments. I find the manuscript suitable for publication in Hydrology and Earth System Sciences after minor revisions. Below are my specific comments and suggestions for improving the manuscript.

Reply: Thanks for your constructive comments. We have carefully revised Paper # EGUSPHERE-2024-4145.

General Comments:

(1) While the manuscript briefly mentions physics-informed neural networks (PINNs), a more direct comparison or a deeper discussion of how DTL differs from or complements PINNs would strengthen the manuscript. This would better situate the DTL approach within the broader landscape of hybrid modeling techniques.

Reply: Implemented. In the revised manuscript, we also integrate multiple loss functions considers the constraints of physical information and imposes penalties for initial and boundary conditions for the pretrained DNN model. Subsequently, the transfer learning technique is used to fine-tune the pre-trained model. Therefore, our model integrated the strength of PINNs and transfer learning technique .Please see Lines 133-154.

(2) The paper focuses on model performance but does not explore the interpretability of the DTL model. A short discussion on whether the transferred physical knowledge can be traced or interpreted in the model outputs would be beneficial. Furthermore, although the authors mention possible extensions to solute transport or other applications, this is not demonstrated or discussed in detail.

Reply: Implemented. In fact, we have discussed how the transferred physical knowledge impacts the parameters of deep learning model. Results indicate that the hydraulic conductivity primarily influences the parameters of the shallow layers in the DNN model. Please see Lines 196-202. Although a full interpretability analysis is beyond the current scope, we agree it is an important direction for future work and have noted this accordingly. Furthermore, we have discussed the extension of the proposed PDTL model to solute transport or other applications. Please see Lines 308-322.

(3) The authors acknowledge the limitation that analytical models assume regular geometries. This is an important point and could be expanded to discuss whether coordinate transformation, domain padding, or hybrid numerical-analytical datasets could mitigate this issue in future work.

Reply: Implemented. We have expanded this point in the discussion section. In future work, efforts should focus on improving the framework's ability to handle irregular spatial domains through coordinate transformations, domain padding, or hybrid numerical-analytical datasets, and on refining its extrapolation capability. Please see Lines 333-337.

- Specific Suggestions:
- 338 (1) Section 2.2: Clarify why the tanh activation function is used rather than alternatives like ReLU. This choice
- may influence convergence and generalization.
- Reply: Implemented. The tanh activation function was selected primarily due to its bounded and symmetric
- output range (-1 to 1), which helps in centering the data and can lead to faster convergence during training,
- especially when the inputs have been normalized. In our case, since the model learns from inputs that include
- both positive and negative physical feature, tanh facilitates smoother gradient flow across layers.
- Furthermore, the tanh activation function is widely used in hydrological problems, e.g., An et al. (2022), Zhang
- 345 et al. (2023).

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346 347 References:

- [1] An, Y., Yan, X., Lu, W. et al. An improved Bayesian approach linked to a surrogate model for identifying groundwater pollution sources. Hydrogeology Journal, 2022, 601-616.
- In [2] Zhang J, Liang X, Zeng L, et al. Deep transfer learning for groundwater flow in heterogeneous aquifers using a simple analytical model [J]. Journal of Hydrology, 2023, 626: 130293.
- 353 (2) Equation (2): Notation should be consistent with Equation (4). Clarify the definition of n (number of training samples).
- Reply: Implemented. We have incorporated the collocation points throughout the model domain, along with the physical information of the boundary and initial conditions to minimize the loss functions. Please see Equations (3a)-(3d).
- 359 (3) Consider including results for 200 observation points in the main figures, rather than relegating them to the Supplement, since these are discussed prominently in the text.
- Reply: Considering data acquisition in heterogeneous riparian zones is often time-consuming and costly, this study focuses on the performance of the proposed PDTL model under limited data availability. There is no significant difference between the PDTL and DNN model when the number of observation points increases to 200, therefore we relegate them to the Supplement.

Quarong Wang

- 366 If you have any further questions about this revision, please contact me.
- 367 Sincerely Yours,
- 368 Quanrong Wang, PhD, PG.
- 369 Professor and
- 370 Holder of Endowed CUG Scholar in Hydrogeology