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2 **M2 Monthly and annual mode 1 and mode 2 internal tide atlases from altimetry**
3 **data and MIOST: focus on the Indo-Philippine Archipelago and the region off the**
4 **Amazon shelf.**

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12 **Abstract**

13 The M2 MIOST24 (Multivariate Inversion of Ocean Surface Topography 2024) internal tide atlases are
14 available in annual (MIOST24a) and monthly (MIOST24m) regional versions for modes 1 and 2 in the Indo-
15 Philippine archipelago and the region off the Amazon shelf. They are derived from 25 years (1993-2017,
16 period 1) of sea level anomalies (SLA) from altimetry observations. Compared to MIOST22, MIOST24
17 incorporates M2 modes 1 and 2 wavelengths based on monthly stratification profiles from GLORYS12v1
18 (1993-2020). The differences between MIOST24a and MIOST22a lead to RMSE (Root Mean Square Error) of
19 up to 3 cm, reflecting amplitude changes, while the RMSE between MIOST24a and HRET (High-Resolution
20 Empirical Tide) indicate both amplitude and phase differences. MIOST24m highlights significant monthly
21 variability of M2 internal tides in the Indo-Philippine archipelago and off the Amazon shelf. In the Amazon
22 region, the internal tide propagates far offshore from March to June but is blocked closer to the coast from
23 August to December. For both regions, mode 1 monthly variability is mainly phase-related, while mode 2 is
24 more amplitude-dependent. Variance reductions of SLA show that MIOST24m outperforms MIOST24a,
25 MIOST22a and HRET on period 1 in the two regions of interest, and on the Amazon region in period 2 (2018-
26 2023). Monthly atlases are therefore recommended to correct the internal tides of the SLA used to derive
27 them. All these results support the development of an improved MIOST24 global atlas.

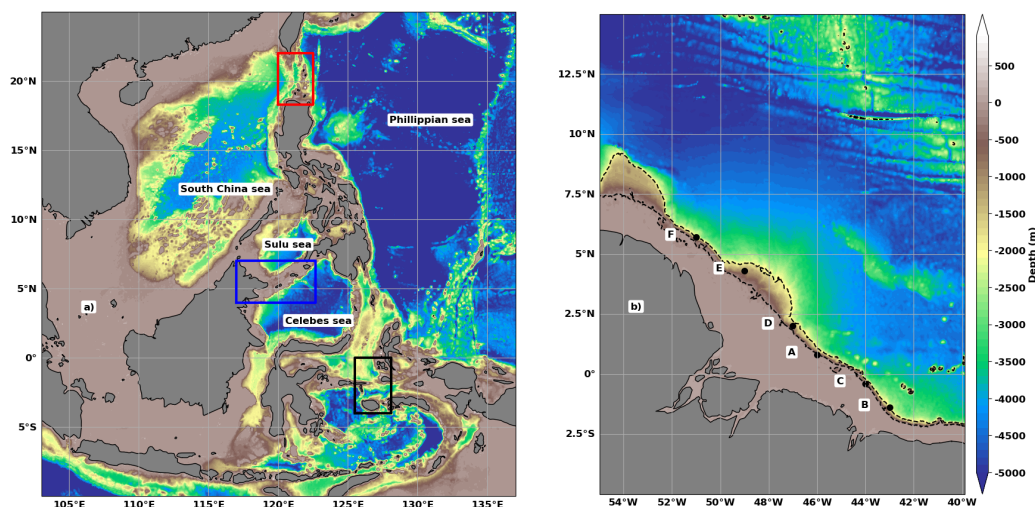
28 **Introduction**

29 Since the early 1990s and the launch of the TOPEX/Poseidon mission, spatial altimetry has provided an
30 independent source of measurements of ocean surface topography. These measurements are essential for a
31 better understanding of ocean surface dynamics, deep ocean circulation and their impact on climate
32 (Escudier et al., 2017). Significant progress has been made in the processing and reprocessing of altimetry
33 data (Dibarboure et al. 2011, Ablain et al., 2015, Pujol et al., 2016, Pujol et al., 2023). Today, more than 30
34 years of observations are available. They can be used directly or indirectly (model constraints, data
35 assimilation) to generate global atlases of barotropic tides (Stammer et al., 2014, Carrere et al., 2016, Lyard
36 et al., 2020, Lyard et al., 2024, Desai and Ray, 2014, Egbert and Erofeeva, 2002) and baroclinic tides, also
37 known as internal tides (Dushaw et al., 2011; Dushaw, 2015, Zhao et al., 2012, Ray and Zaron, 2016; Zaron et
38 al., 2019, Ubelmann et al., 2022). In turn, these tidal atlases are used as geophysical corrections in the Data
39 Unification and Altimeter Combination System (DUACS) chain to compute the Sea Level Anomaly (SLA) along
40 the altimeter tracks (L3 product) and on regular horizontal grids (L4 product).



41 Internal tide (IT) atlases have been included in the geophysical corrections of the altimetry dataset since
 42 the transition from version DT2018 to DT2021 in the DUACS processing chain (Sanchez-Roman et al., 2021;
 43 Lievin et al., 2020; Faugere et al., 2022). The internal tide model currently used as a reference in DUACS is
 44 HRETv8.1 (High-Resolution Empirical Tide 8.1, HRET in the rest of the paper) by Zaron (2019). Several global
 45 atlases exist as described in (Carrère et al., 2021), such as those by Zhao (Zhao et al., 2012, 2018, 2019, 2021)
 46 or MIOST (Multivariate Inversion of Ocean Surface Topography; Ubelmann et al., 2021, 2022). The MIOST
 47 atlas of Ubelmann et al. (2022), like the Zhao atlases, uses mode 1 and 2 theoretical internal tide wavelengths'
 48 climatologies to extract the internal tide signal from the altimetric SLA. For the 2022 version of the MIOST
 49 atlas, Ubelmann et al. (2022) use the first Rossby deformation radius climatology from Chelton et al. (1998)
 50 as an approximation of the mode 1 wavelength and divide it by two to approximate the mode 2 wavelength.
 51 These approximations are not always accurate because each baroclinic mode has characteristics influenced
 52 by ocean stratification (Gerkerma et al., 2004). Moreover, the climatology of Chelton et al. (1998) is based
 53 on a very different period from the 1993 - 2017 period of the altimetry data used by Ubelmann et al. (2022),
 54 which could lead to inaccuracies in the location and amplitude of internal tides. The first objective of this
 55 study is to propose a 2024 version of MIOST IT atlas based on more appropriate mode 1 and 2 wavelengths,
 56 thus overcoming the deficiencies of the wavelengths prescribed in Ubelmann et al. (2022).

57 The second objective of this study concerns the monthly variability of the internal tide and the relevance
 58 of replacing the HRET internal tide atlas with monthly atlases in the DUACS chain. Altimetry-derived internal
 59 tide atlases only include the stationary (or coherent, or phase-lock) part of the internal tides. The coherent
 60 and incoherent (non-stationary) internal tides both vary with stratification and the interactions of the internal
 61 tides with the ocean circulation, including mesoscale eddies (Tchilibou et al., 2020; Duda et al., 2018; Dunphy
 62 et al., 2014). This variability is not considered in annual atlases such as HRET, which use the altimetry
 63 database as a single set. Zhao (2021) builds subsets of altimetry data over the four meteorological seasons
 64 and shows that seasonal atlases perform better in tropical regions but with some limitations. In this study,
 65 we extend the question of internal tide variability to the monthly scale, focusing on the M2 wave in the Indo-
 66 Philippine archipelago (Figure 1a) and the region of the Amazon shelf in the tropical Atlantic (Figure 1b).



67
 68 **Figure 1:** Bathymetric depth (in m) in the Indo-Philippine archipelago (a) and the region off the Amazon shelf
 69 (b). The major internal tide generation areas are indicated by red (Luzon Strait), blue (Sulu Island Chain) and
 70 black (Seram Sea) boxes for the Indo-Philippine archipelago and by the letters A-F for the Amazon shelf-
 71 break.



72 These two tropical regions are chosen because they are hotspots of M2 internal tide generation and the
73 site of high M2 internal tide variability (Jan et al.,2008; Muller et al.,2012; Ray and Zaron 2011, Niwa and
74 Hibiya 2001, 2004 and 2014, Arbic et al.,2012; Nugroho et al., 2018; Zhao and Qui 2023; Pickering et al.,2015;
75 Rainville et al.,2013; Tchilibou et al., 2022; Assene et al., 2024). In addition, the Indo-Philippine archipelago
76 is a transit zone between the Pacific and Indian Oceans (Sprintall et al., 2014; Hurlburt et al., 2011), and the
77 tide-induced mixing there affects the coupled ocean-atmosphere system and thus the global climate system
78 (Koch-Larrouy et al., 2010). More details on these two regions can be found in Nugroho (2018) and Tchilibou
79 et al. (2022). The paper is divided into 5 sections. In section 1 we give an overview of HRET, compare the
80 wavelengths' bases of the 2022 and 2024 versions of MIOST-IT, and present the altimetry data and how they
81 are organized to derive the annual (classical) and monthly atlases. In section 2, the annual atlases of MIOST-
82 IT 2022 and 2024 are compared qualitatively with HRET. The efficiency of the monthly atlases in correcting
83 for internal tides in the altimetry data is analyzed in section 4, and the paper is concluded in section 5.

84 **1- Internal tide atlases and data:**

85

86 In this section, we describe the different internal tide atlases developed within the study (MIOST24) as
87 well as the datasets used for computation, and the other atlases used for comparison (MIOST22 and
88 HRET).

89

90

91 **1.1- HRET**

92

93 HRET (for HRETv8.1; Zaron 2019) is an empirical atlas of internal tides at the M2, S2, K1 and O1 frequencies,
94 developed from the analysis of the 1993 to 2017 (25 years) exact repeat mission altimetry data (Topex, Jason
95 1 to 3, ERS, Envisat, Saral AltiKa and the GEOSAT follow-on). The method used to construct the HRET internal
96 tide atlas involves a local two-dimensional Fourier analysis of the along-track data, and a least-squares fit by
97 a second-order polynomial. HRET is provided on a horizontal grid of 0.05°X0.05° (1/20°) and includes modes
98 1 and 2. A mask is applied in the regions where the amplitude of the internal tides is very noisy.

99

100 **1.2- MIOST22 and MIOST24 mode 1 and 2 wavelengths for M2:**

101

102 MIOST is an empirical atlas of internal tides obtained by a single inversion that simultaneously separates
103 mesoscale and internal tides (modes 1 and 2) from altimetry observations (Ubelmann et al., 2022). The
104 2022 and 2024 versions of MIOST-IT atlases are hereafter referred to as MIOST22 and MIOST24. The
105 suffixes 'a' and 'm' are used to distinguish between annual (e.g. MIOST24a) and monthly (e.g. MIOST24m)
106 MIOST atlases.

107

108 In MIOST, mesoscales are expressed as a reduced wavelet basis. Internal tides are defined by a plane-
109 wave basis according to the dispersion relation (e.g. Rainville et Pinkel, 2006) given in Equation 1, where f
110 is the Coriolis parameter, λ_n , C_n and ω are the wavelength, eigenspeed and pulsation of the internal tides
111 of mode n , respectively.

112

113

$$\lambda_n = \frac{2\pi C_n}{\sqrt{\omega^2 - f^2}}, (1)$$

114 As mentioned in the introduction, for MIOST22 the wavelength of mode 1 corresponds to the first Rossby
115 deformation radius and the wavelength of mode 2 is half the wavelength of mode 1. For MIOST24, mode 1
116 and 2 wavelengths are determined independently by solving the eigenvalue equation (Eq 2; Gill, 1982) with
117 the boundary conditions $\phi_n(0) = \phi_n(H) = 0$, where H is the ocean depth and $\phi_n(z)$ the modal vertical
118 structure.

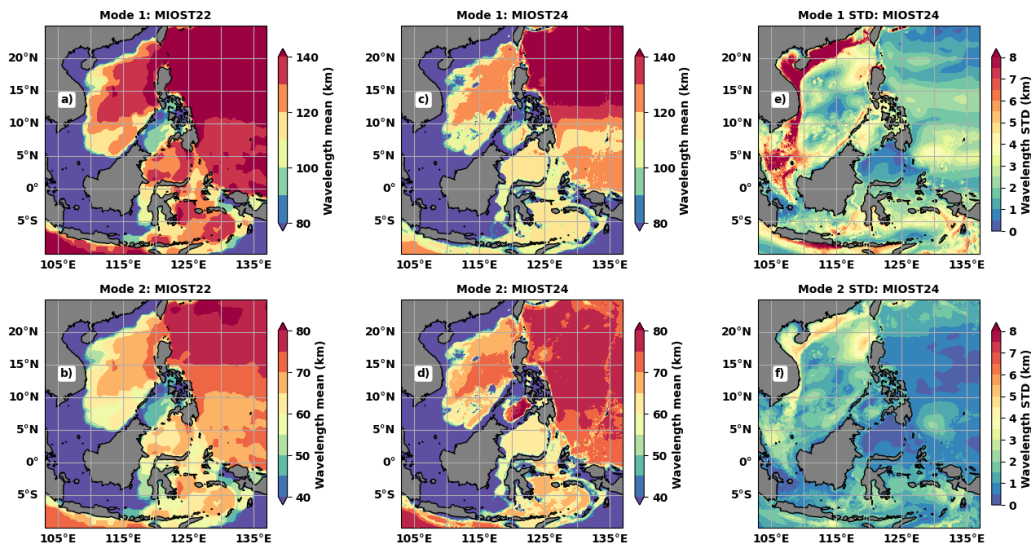


119

$$\frac{\partial^2 \phi_n(z)}{\partial z^2} + \frac{N(z)^2}{C_n^2} \phi_n = 0, (2)$$

120 The $N(z)$ stratification profiles required for equation 2 are computed from the 1993 - 2020 monthly
 121 climatologies of the potential temperature and salinity fields from the GLORYS12v1 reanalysis
 122 (<https://doi.org/10.48670/moi-00021>, last accessed 30/07/2024). GLORYS12v1 is a global CMEMS
 123 (Copernicus Marine Environment Monitoring Service) product with a horizontal resolution of $1/12^\circ$ and 50
 124 levels. It is based on an eddy-resolving NEMO platform assimilating along tracks altimetric SLA, satellite sea
 125 surface temperature observations and in situ vertical temperature and salinity profiles (Argo, moorings, etc.).
 126 The GLORYS12v1 reanalyses are used as they are to calculate $N(z)$ and derive the monthly mode 1 and 2
 127 wavelengths of the M2 internal tides required for MIOST24m. The MIOST24a atlas requires annual
 128 wavelengths, obtained using $N(z)$ derived from the annual mean of GLORYS12v1 fields. The annual
 129 wavelengths used for MIOST22a and MIOST24a and the standard deviations of the monthly wavelengths
 130 used for MIOST24m are shown in Figure 2 for the Indo-Philippine Archipelago and Figure 3 for the region off
 131 the Amazon shelf.

132 In the Indo-Philippine archipelago, the annual mode 1 (Figures 2a and 2c) and mode 2 (Figures 2b and 2d)
 133 M2 wavelengths used for MIOST22 (Figures 2a and 2b) are generally larger than those used for MIOST24
 134 (Figure 2c and 2d). The differences can be up to 10 km and are quite pronounced south of the Philippine Sea,
 135 in the South China Sea, in the Celebes Sea and the Banda Sea. Only in the Sulu Sea do MIOST24 wavelengths
 136 exceed those of MIOST22. The simplified approximation that the wavelength of mode 2 is half the one of
 137 mode 1, used for MIOST22, implies that the spatial distributions of the two modes are equivalent (Figure 2a
 138 and 2b). We assume that the locations of the maximum wavelengths in mode 1 also correspond to the
 139 locations of the longest wavelengths in mode 2, and similarly for the locations of the shortest wavelengths.
 140 This is not the case when looking at the MIOST24 wavelength maps for modes 1 (Figure 2c) and 2 (Figure 2d).
 141 In the Sulu Sea, the mode 2 wavelengths of MIOST22 are about 50 km, *i.e.* among the shortest, while in
 142 MIOST24 they are of the order of 80 km, *i.e.* the highest.



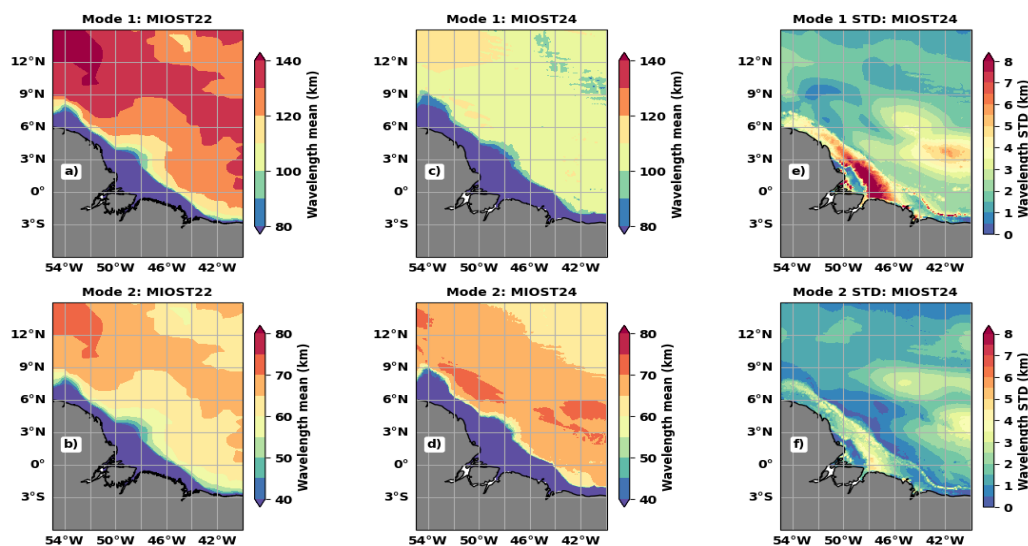
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144 **Figure 2:** M2 wavelengths values (a-d, in km) and standards deviations (e-f, in km) in the Indo-Philippine
 145 archipelago: (a) mode 1 and (b) mode 2 annual values used for MIOST22a, (c) mode 1 and (d) mode 2 annual
 146 values used for MIOST24a, standard deviation of (e) mode 1 and (f) mode 2 monthly wavelengths used for
 147 MIOST24m.



148 Off the Amazon shelf, the M2 wavelengths of MIOST22 and MIOST24 show differences in both spatial
 149 distribution and values (Figure 3). In MIOST22, mode 1 (Figure 3a), and mode 2 (Figure 3b), the wavelength
 150 gradient is positive from offshore to about 7°N. Thereafter the wavelengths decrease slightly. In MIOST24
 151 the structures are more homogeneous (Figure 3c and 3d). Outside the continental shelf, mode 1 wavelengths
 152 (Figure 3c) are mostly between 100 and 110 km, while they exceed 120 km in MIOST22 (Figure 3a). For mode
 153 2 (Figure 3d), the dominant structure corresponds to wavelengths between 65 and 70 km, while in MIOST22
 154 the space bounded by this structure also includes a short-wavelength zone between 60 and 65 km (Figure
 155 3c). As in the Indo-Philippine archipelago, there is no direct relationship between the spatial distributions of
 156 mode 1 and 2 annual wavelengths in MIOST24. This confirms that the wavelength characteristics are specific
 157 to each mode.

158



159

160 **Figure 3:** As Figure 2 for the region off the Amazon shelf.

161 The differences between the wavelengths of MIOST22 and MIOST24 reflect the differences between the
 162 stratifications and therefore between the climatological eigenspeed used in each case. According to Equation
 163 1, a velocity difference of 0.1 m/s corresponds to 4 to 5 km shift in the wavelengths for the latitudes of
 164 interest here, between 10°S and 20°N. We have found differences of up to 0.5 m/s between the eigenspeed
 165 of MIOST22 and MIOST24 (not shown). Despite the differences with the MIOST22 wavelengths, we remain
 166 confident about the MIOST24 wavelengths as they are close to those used by Zhao (2018), which is based on
 167 the same method but on the stratification from the World Ocean Atlas 2013 climatology.

168 The standard deviations of the monthly M2 wavelengths used to derive the MIOST24m atlases are shown
 169 for modes 1 and 2 in the last column of Figures 2 and 3. In both regions, the M2 wavelength variation over
 170 the year is up to 5 km for mode 1 (Figures 2e and 3e) and 3 km (Figures 2f and 3f) for mode 2 in the deep
 171 ocean. On the continental shelves the M2 wavelength variation is up to 8 km for mode 1 and 5 km for mode
 172 2. In the Luzon Strait (Figure 2), wavelength variations are more pronounced in the western part, which opens
 173 to the South China Sea, than in the eastern part, which opens to the Philippine Sea. Wavelengths are relatively
 174 stable in the Celebes Sea (Figure 2), with monthly variations of less than 2 km for mode 1 and less than 1 km
 175 for mode 2. Outside the continental shelf, wavelengths vary more in the eastern part of the Amazon region
 176 (Figure 3). The wavelength variability would also have been biased if the mode 2 wavelengths had been taken



177 to be half the mode 1 wavelength as in MIOST22. For example, south of the Philippine Sea, mode 1
178 wavelengths vary between 1 and 4 km (Figure 2e), while mode 2 (Figure 2f) is relatively stable (less than 1
179 km). In addition, for the boxes in Figure 1a and the region off the Amazon shelf, the spatial means of monthly
180 wavelengths have been plotted and presented in the Appendix to illustrate further the annual cycle of mode
181 1 and 2 wavelengths.

182 **1.3- Database organization for annual and monthly atlases:**

183 In this study, we use Level 3 along-track data with a resolution of 1 Hz (about 7 km), processed according
184 to the DT2024 protocol (Kocha et al., 2023) and available on Copernicus website (see link in Data availability).
185 The HRET correction is reintroduced to obtain an SLA with the full internal tide signal. As in MIOST22, data
186 are from the Topex/Poseidon, Jason-1, Jason-2, Jason-3, Sentinel-3A, Sentinel-3B, Saral/AltiKa, Cryosat-2,
187 ERS-1, ERS-2, Envisat, Geosat Follow-On and HY-2A altimetry missions. The altimetry SLAs are selected from
188 1993 to 2023 and divided into two periods. The MIOST24a and MIOST24m atlases are derived from the SLA
189 over "period 1" between January 1993 and December 2017, as are MIOST22 and HRET. The "period 2" from
190 January 2018 to December 2023 is used for validation as independent measurements. The validation consists
191 of an inter-comparison of the levels of altimetry residual SLA after applying the internal tide corrections using
192 either the HRET, MIOST22 or MIOST24 atlases.

193 The 25 years of SLA data from period 1 are used as a single set to derive the annual MIOST24a atlas
194 (stationary part over 25 years). Period 1 and 2 SLA data are divided into monthly subsets to derive the
195 MIOST24m atlas and to validate the four atlases. Due to tidal aliasing in the altimetry observations and the
196 low repeatability of the satellites, the monthly subsets are formed by overlapping the month in question by
197 15 days on each side. For example, the SLA subset data for April is defined with SLAs from 16 March to 15
198 May. Finally, the monthly time series covers about 4 years (1500 days) of observations (60 days per year over
199 25 years), which is a minimum for separating the S2 and M2 harmonics for the Topex/Poseidon and Jasons
200 missions, whose reference orbit has a period of 9.92 days. After analysis of the altimetry data, the MIOST24a
201 and MIOST24m M2 atlases are produced on $1/20^\circ$ horizontal grids, the same resolution as HRET, while
202 MIOST22 was produced on a $1/10^\circ$ grid. The HRET mask is applied to the MIOST atlas to harmonize the
203 comparisons.

204 **2- MIOST24a M2 atlas, comparison with MIOST22 and HRET:**

205
206 This section compares the annual M2 atlas MIOST24a with the annual M2 atlases MIOST22a and HRET.
207 First, the internal tide amplitude maps M2 are compared. Then, considering the amplitudes (A, A_m), and
208 phases (φ, φ_m), the Root Mean Square Error (RMSE) between MIOST24 and MIOST22 or MIOST24 and HRET
209 is calculated according to equation 3 for a more complete quantification of the distance between the atlases.
210 Equation 3 can be rewritten as equation 4, where the terms on the right indicate the contribution of the
211 amplitude differences to the RMSE (Ac) and the contribution of the phase differences to the RMSE (Pc). The
212 phase differences contribute more to the RMSE when the ratio of the second term to the first term on the
213 right is greater than 1 ($Pc / Ac > 1$, in equation 5). This ratio is referred to as the rate of the contributions
214 to the RMSE (Rc) and is evaluated for locations with amplitude differences greater than 3 mm, more precisely
215 $(A - A_m)^2 > 0.1$, and this is to avoid noise effects on the ratio.

$$216 \quad RMSE = \sqrt{\frac{1}{2} |Ae^{i\varphi} - A_me^{i\varphi_m}|^2}, \quad (3)$$

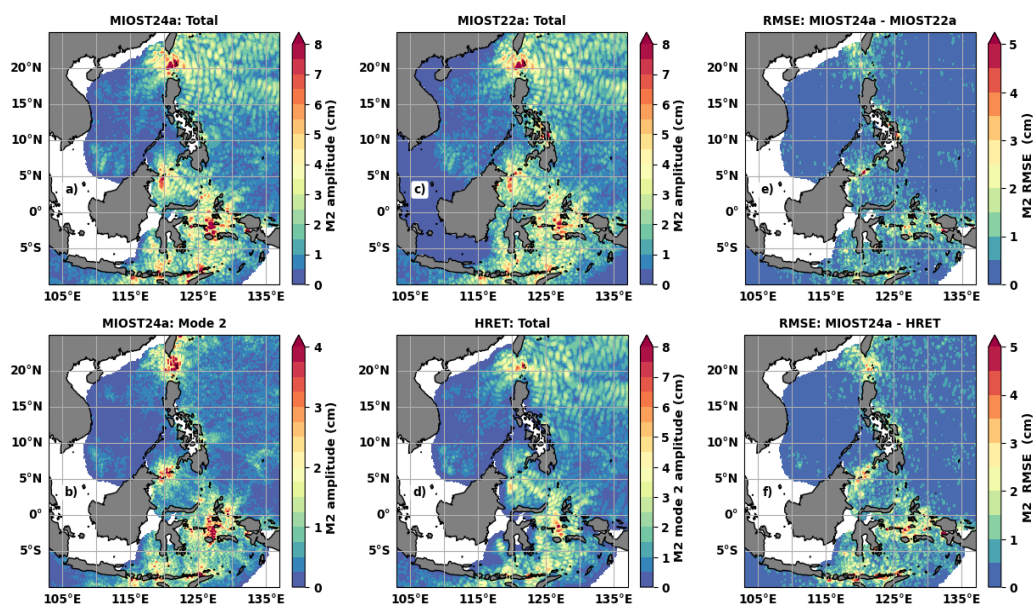
$$217 \quad 2RMSE^2 = (A - A_m)^2 + 2AA_m (1 - \cos(\varphi - \varphi_m)), \quad (4)$$

$$218 \quad Rc = Pc / Ac = 2AA_m (1 - \cos(\varphi - \varphi_m)) / (A - A_m)^2, \quad (5)$$



219 The amplitudes of the total internal tides (including mode 1 and 2) and mode 2 internal tides, as obtained
 220 for MIOST24a, are shown in Figures 4a and 4b, respectively, for the Indo-Philippine archipelago. Three main
 221 areas stand out for their maximum amplitude of more than 8 cm for the total internal tides and more than 4
 222 cm for mode 2: the Luzon Strait, the Sulu Island chain and the Serem Sea. These are the main sources of
 223 internal tides in this part of the ocean. Once generated, the internal tides propagate through the various seas
 224 of the archipelago. From the Luzon Strait, the intrusion of the internal tides is stronger to the east in the
 225 Philippine Sea compared to the west in the South China Sea (Figure 4a).

226 MIOST24a (Figure 4a) agrees with MIOST22a (Figure 4c) and HRET (Figure 4d) in the spatial distribution of
 227 the M2 internal tide amplitude. Compared to the latter two atlases, MIOST24a shows stronger amplitudes
 228 and well-defined small-scale structures, because mode 2 is better defined in MIOST24a. On the RMSE maps,
 229 the differences between MIOST24a and MIOST22a are 1-2 cm south of 5°N and around Luzon Strait (Figure
 230 4e). For the same locations, the RMSE between MIOST24a and HRET (Figure 4f) increases to 3 cm and non-
 231 zero RMSE marks are more visible in the Philippine Sea. The spatial mean of R_c is 1.36 for the RMSE between
 232 MIOST24a and MIOST22a, indicating that the atlases differ mainly by their phases. For HRET, the spatial mean
 233 of R_c is 1.06, thus amplitudes and phases contribute equally to the differences between MIOST24a and HRET.

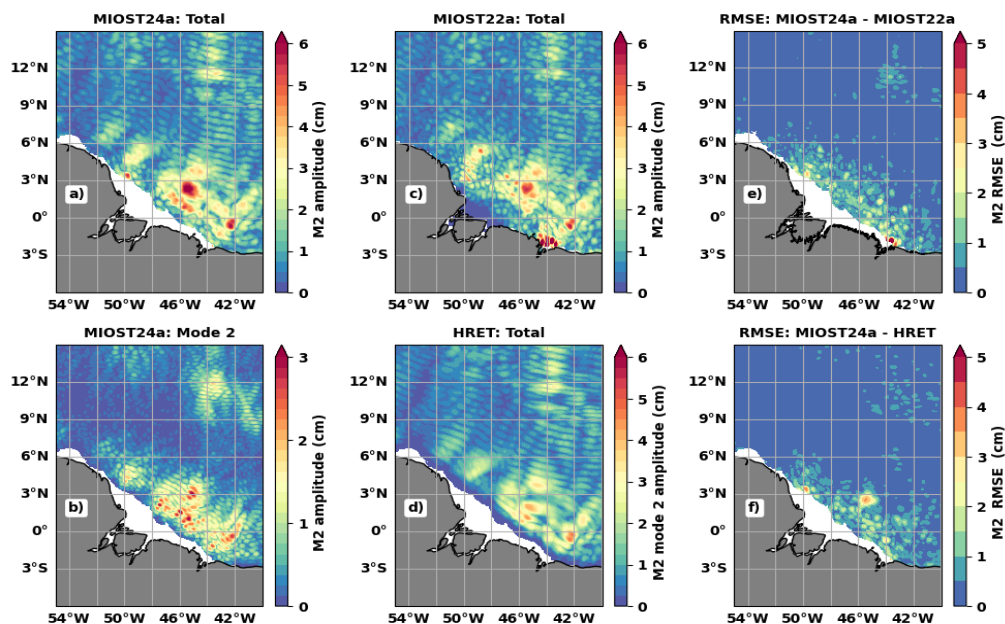


234
 235 **Figure 4:** Amplitude (a-d, in cm) and RMSE (e-f, in cm) of the M2 internal tides in the Indo-Philippine
 236 Archipelago. Amplitudes are shown for (a) MIOST24a total internal tides, (b) MIOST24a mode 2 internal tides,
 237 (c) MIOST22a total internal tides and (d) HRET total internal tides. The RMSE is computed for (e) MIOST22a
 238 and (f) HRET against MIOST24a. White corresponds to the HRET mask applied to MIOST24 to facilitate
 239 comparison.

240 In the region off the Amazon shelf (Figure 5), MIOST24a is also characterized by offshore propagation of
 241 internal tides. Two lines of maximum internal tides are distinguishable south of 2.5°N (Figure 5a), and the
 242 third is less clear. Mode 2 from the Amazon shelf-break can be seen following these lines (Figure 5b). Again,
 243 the amplitude of the M2 internal tides is stronger in MIOST24a, but the atlas matches MIOST22a (Figure 5c)
 244 and HRET (Figure 5d), even if the latter shows smoother structures. As in the Indo-Philippine archipelago, the
 245 RMSEs between MIOST24a and the other two atlases are mostly lower than 2 cm but exceed 3 cm at a few
 246 locations (Figures 5e and 5f). The MIOST24a atlas differs more from MIOST22a (Figure 5e) and HRET (Figure



247 5f) in the first 100 to 200 km from the shelf break. The RMSEs are characterized by small scale structures in
 248 this zone where the mode 2 amplitude is maximum. This suggests that the RMSEs reflect the changes
 249 associated with improved mode 2 in MIOST24. The spatial means of R_c are 1.35 and 0.69 for the RMSE
 250 between MIOST24a and MIOST22a and HRET, respectively. In this region, the phase differences are dominant
 251 between MIOST22a and MIOST24a, while the amplitude differences are dominant between MIOST24a and
 252 HRET.



253

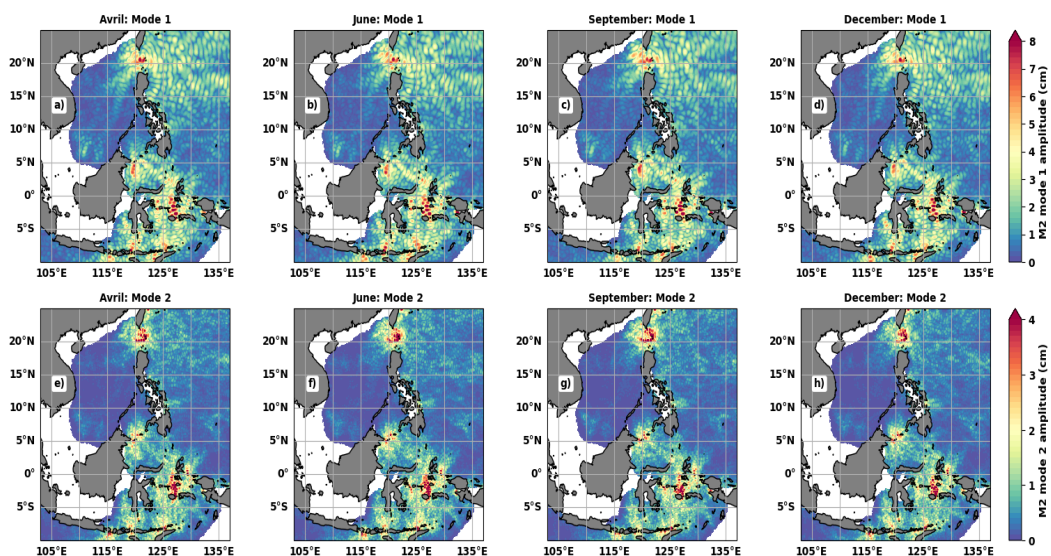
254 **Figure 5:** As Figure 4 for the region off the Amazon shelf.

255 **3- MIOST24m M2 atlases, the monthly variability of the internal tide:**

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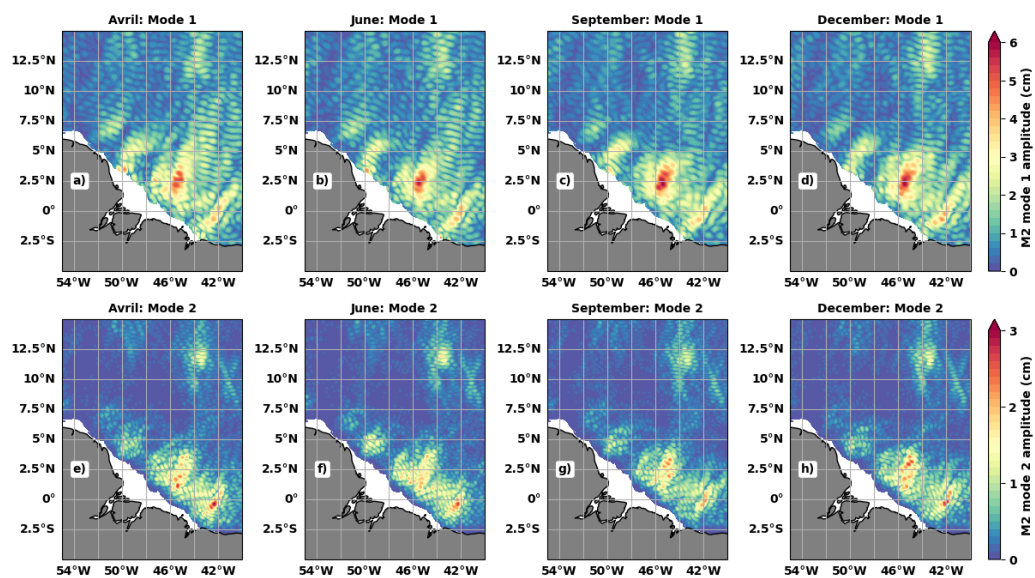
257 As a reminder, the MIOST24m monthly atlases are derived from the monthly climatology of M2
 258 wavelength (Section 1.2) and monthly subsets of the altimetry data (Section 1.3). Monthly mode 1 and 2
 259 atlases for April, July, September and December have been selected to illustrate the different propagation
 260 situations and changing amplitudes of internal tides that occur throughout the year. The RMSE is calculated
 261 between the monthly atlases MIOST24m and the annual atlas MIOST24a. The annual cycles of the spatial
 262 mean of the RMSE and R_c are used to investigate the monthly variability of the M2 internal tide.

263 In the Indo-Philippine archipelago (Figure 6), the propagation of the mode 1 internal tides towards the
 264 Philippine Sea is most pronounced in the early months of the year, such as April (Figure 6a) and in December
 265 (Figure 6d). For the rest of the year, the structure of the internal tides is distorted quite rapidly, as in June
 266 (Figure 6b) and September (Figure 6c). In the South China Sea and the rest of the archipelago, the amplitude
 267 and trajectories of the internal tides vary. Mode 2 variability is more characterized by amplitude variations
 268 (Figure 6 e-h). In the first half of the year in the region off the Amazon shelf (Figure 7), the internal tides of
 269 mode 1 propagate freely from the Amazon shelf-break towards the open ocean, as in April (Figure 7a) and
 270 June (Figure 7b). In the second half of the year, mode 1 has difficulty crossing 5°N, as in September (Figure
 271 7c) and December (7d). The amplitude variations of mode 2 (Figure 7 e-h) are also easily distinguishable in
 272 this region.



273

274 **Figure 6:** MIOST24m M2 mode 1 (top) and mode 2 (bottom) amplitudes (in cm) for Avril (a and e), June (b
275 and f), September (c and g) and December (d and h).



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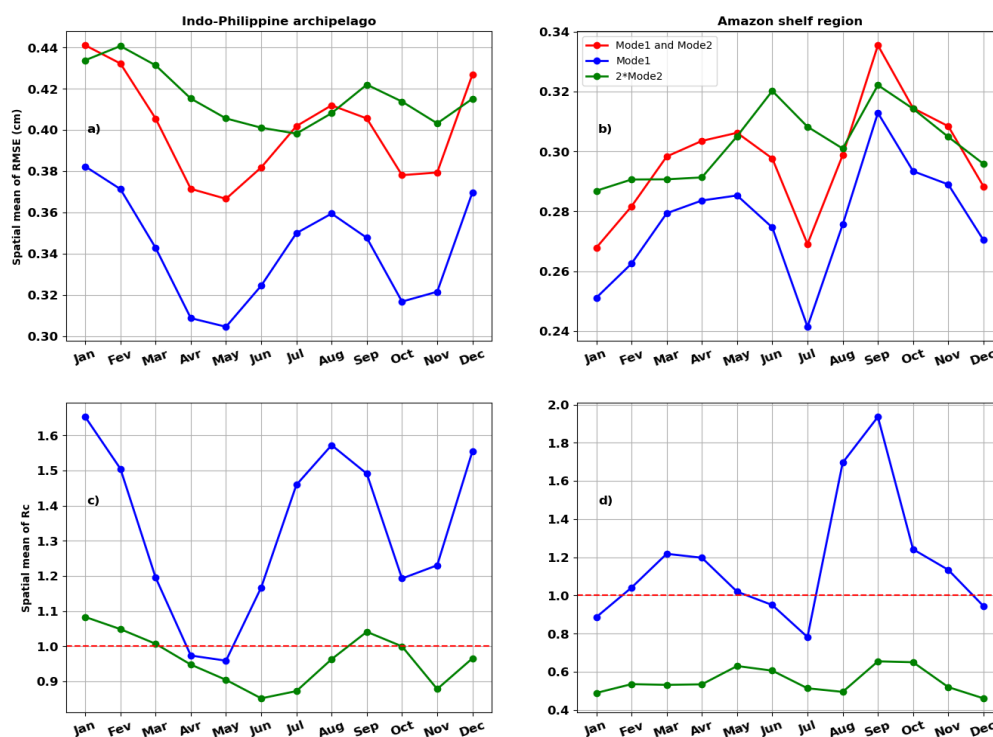
277 **Figure 7:** As Figure 6 for the region off the Amazon shelf.

278 The annual cycles of the spatial mean of monthly RMSE (Figure 8) of the total internal tides (in red), mode
279 1 (in blue) and mode 2 internal tides (in green) confirm that the internal tides are not constant throughout
280 the year. For the two regions of interest, the annual cycle of the spatial mean of the RMSE of the total internal
281 tides is like that of the mode 1 internal tides. The largest discrepancies between the annual MIOST24a atlas
282 and the monthly MIOST24m atlases of the total and mode 1 internal tides occur in January, August and
283 December in the Indo-Philippine archipelago (Figure 8a). Monthly and annual atlases are closest in May



284 (Figure 8 a). The annual cycle of the spatial mean of the RMSE for Mode 2 is consistent with that of mode 1,
285 although there is a one-month lag between the maximum peaks of mode 1 and mode 2 (Figure 8a).

286 Off the Amazonian shelf (Figure 8b), the annual cycle of the spatial mean of the RMSE of the total and mode
287 1 internal tide is bimodal, with the minimum of July dividing the year into two parts. For mode 2, the RMSE
288 is relatively constant between January and April, so on average mode 2 internal tides barely vary during these
289 months. From April to December, the RMSE cycle is bimodal as for mode 1, with peaks in June and September.
290 The bimodal shape of the annual cycle of the spatial mean of the RMSE is consistent with the behavior of the
291 M2 amplitudes during the year, as partially shown in Figure 7. It is also reminiscent of the distinction made
292 by Tchilibou et al, 2022, which separates the MAMJJ (March to July) months of high internal tides coherence
293 from the ASOND (August to December) months of high internal tides incoherence due to the increase of the
294 eddy kinetic energy.



295 **Figure 8:** Annual cycle of the spatial mean of (top) the monthly RMSE (in cm) and (bottom) the monthly rate
296 of the contributions to the RMSE (R_c) in the Indo-Philippine Archipelago (a and c) and the region off the
297 Amazon shelf (b and d). The RMSE is calculated for the total internal tide (modes 1 and 2, in red), mode 1 (in
298 blue) and mode 2 (in green). Note that the RMSE for mode 2 has been multiplied by 2 to improve visibility.
299 The rate of the contributions to the RMSE (R_c) is evaluated following equation 5 and for locations with
300 amplitude differences greater than 3 mm.
301

302 The monthly spatial mean of R_c for mode 1 is greater than 1 for most of the year, except for April and May
303 in the Indo-Philippine Archipelago (Figure 8c) and especially for July in the region off the Amazon shelf (Figure
304 8d). The latter months are those with the lowest RMSE (Figure 8a-b). Thus, the RMSEs between the monthly
305 MIOST24m and annual MIOST24a mode 1 atlases express differences in amplitude for the month with the
306 minimum RMSE, but in general over the year, differences in phase and therefore in the internal tides
307 structures between the atlases. For Mode 2, R_c indicates that the RMSE reflects that amplitude differences



308 predominate over phase differences in the two regions. Except, of course, for January, February and
 309 September in the Indo-Philippine archipelago, for which the RMSE is maximum (Figure 8a).

310 Examples of the annual cycle of the M2 internal tides amplitude are shown in the Appendix. These cycles
 311 are not identical to those of the RMSE, as the approach is different. However, they confirm that using
 312 altimetry data and MIOST provides access to the monthly variability of the internal tide. In the next section,
 313 we will test the effectiveness of monthly atlases in removing the internal tides from altimetry observations.

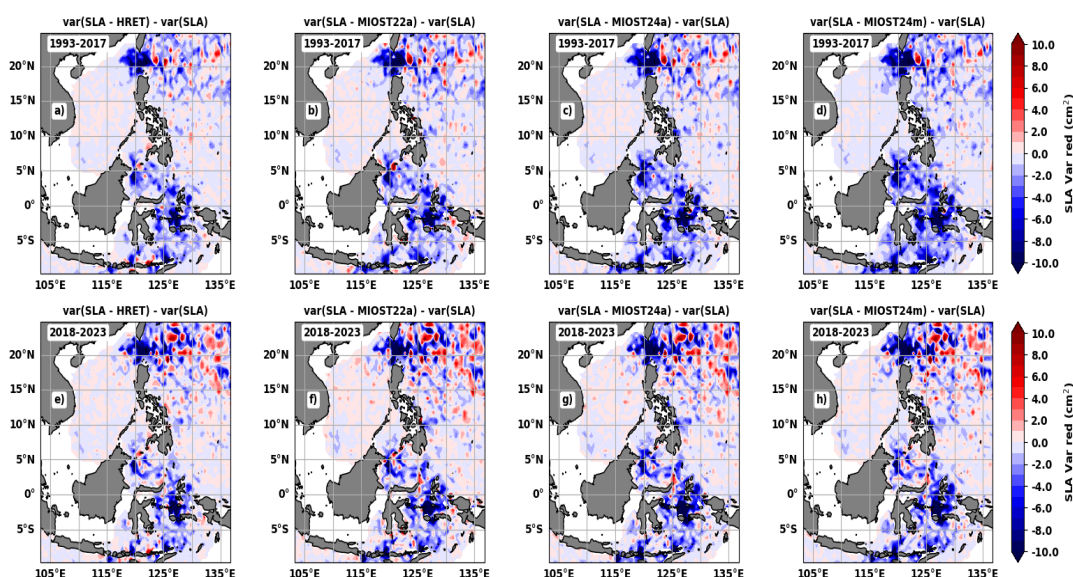
314 **4- Impact of internal tide correction in altimetric data: comparison between monthly and annual**
 315 **atlases.**

316
 317 The variance reduction is a way of measuring how much an internal tide atlas removes or corrects the
 318 internal tides in the altimetric SLA. In equation 6, the variance reduction is defined as the difference between
 319 the variance of the SLA corrected with the M2 internal tide prediction and the variance of the uncorrected
 320 SLA. In this way, a negative value of the variance reduction means that the internal tide atlas has helped to
 321 reduce the variance of the SLA. On the other hand, a positive value of the variance reduction means that the
 322 internal tide atlas had the opposite effect to what was expected and increased the variance of the SLA.

323
$$\text{variance reduction} = \text{var}(SLA - M2 \text{ prediction}) - \text{var}(SLA), (6)$$

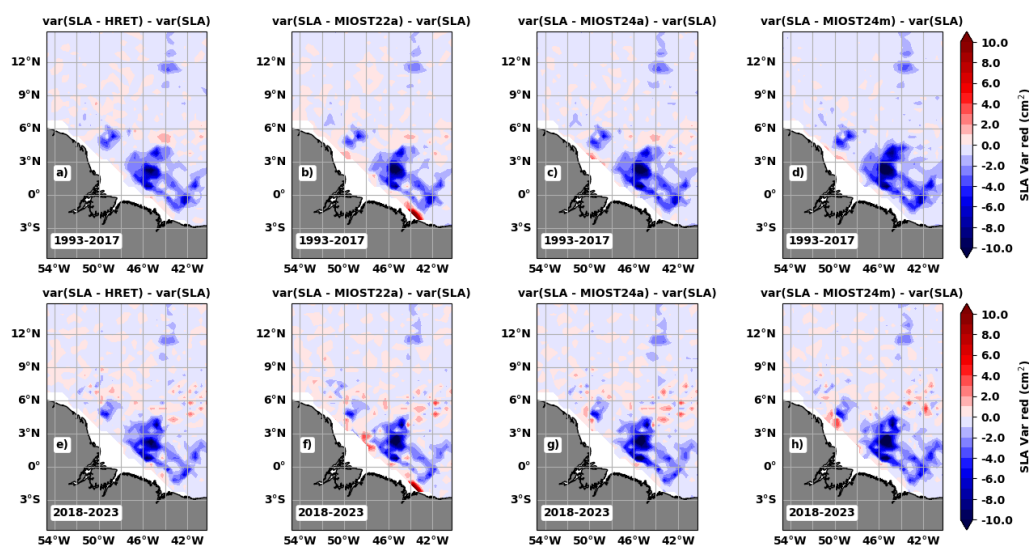
324 The annual M2 HRET, MIOST22a, MIOST24a and the monthly M2 MIOST24m atlases are each used in turn
 325 as the M2 correction in equation 6, and the monthly variance reductions are calculated in pixels of 0.5° x
 326 0.5°. As the main objective is to test the robustness of the monthly atlases, the variance reductions are
 327 estimated each month on monthly subsets (see section 1.2) of the altimetry data from period 1 (1993-2017)
 328 and period 2 (2018-2023). Examples of variance reduction maps are shown for September only. The atlases
 329 are then classified according to the annual cycles of the spatial mean of the monthly variance reduction.

330



331

332 **Figure 9:** SLA variance reduction (in cm²) in the Indo-Philippine archipelago during September for period 1
 333 (a-d, 1993-2017) and period 2 (e-h, 2018-2023).



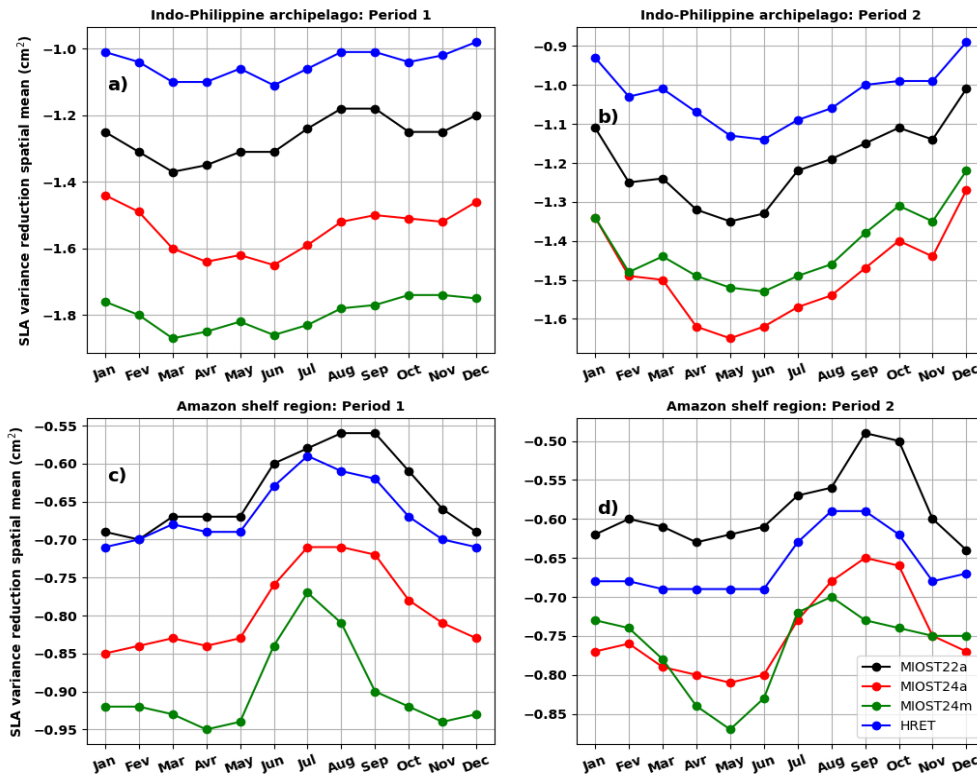
334

335 **Figure 10:** As Figure 9 for the region off the Amazon shelf.

336 In September (Figure 9), as in other months of the year (not shown), the four atlases performed particularly
 337 well around the internal tide generation zones in the Indo-Philippine archipelago, including the Luzon Strait
 338 and the entire area south of 10°N (Figure 6). In the Amazon region (Figure 10), the beneficial effects of the
 339 atlases in reducing the SLA variance are noticeable in the areas and beams of maximum amplitude of the
 340 internal tides previously shown in Figure 7. Some areas, such as the Philippine Sea (Figure 9) and the Amazon
 341 shelf-break (Figure 10 b and f), present a local increase in variance due to the internal tides atlases. Compared
 342 to period 1 (Figure 9 a-d and Figure 10 a-d), this negative effect of the atlases is more pronounced in period
 343 2 (Figure 9 e-h and Figure 10 e-h). However, in period 2 the atlases still perform well at the locations where
 344 the internal tides are generated and along their main trajectories. This indicates that in period 2 the atlases
 345 have more difficulty in correcting the incoherent internal tide.

346 In both regions, the MIOST24m atlas has the best internal tide correction in period 1 (Figure 11 a-b),
 347 followed by the MIOST24a atlas. The atlases that eliminate the least variance in period 1 are HRET for the
 348 Indo-Philippine archipelago (Figure 11a) and MIOST22a (Figure 11b) for the region off the Amazon shelf. The
 349 positions of MIOST24a and MIOST24m are reversed in period 2 in the Indo-Philippine archipelago (Figure
 350 11c), with MIOST24a being slightly better for most months. In the Amazon region (Figure 11d), the MIOST24m
 351 atlas outperforms the other atlases between March and June and again between August and November. The
 352 positions of MIOST22a and HRET in period 1 are unchanged in period 2.

353 It is not surprising that the MIOST24 atlases performed better than HRET and MIOST22a in period 1, the
 354 variance reductions are indeed calculated on the same dataset used to obtain the MIOST24 atlases. However,
 355 the fact that the two MIOST24 atlases perform better on independent period 2 data shows that the
 356 wavelengths' change from MIOST22 to MIOST24 has a positive impact on the internal tide correction in the
 357 altimetry data. Regarding the use of monthly atlases to correct internal tides in altimetric SLA, our results
 358 show that they are appropriate and indicated when applied to the data used to construct them. On an
 359 independent dataset, the monthly atlas remains effective at the generation site and on the main trajectories of
 360 the internal tide, but it may struggle to correct the internal tides on the secondary trajectories associated
 361 with the incoherence of the internal tide. Finally, MIOST22a is the least efficient atlas in the Amazon region
 362 because it increases the variance of the SLA along the coast, and in the open ocean it is better than HRET but
 363 not than the MIOST24 atlases.



364

365 **Figure 11:** Spatial mean of monthly variance reduction (in cm^2) in (left) the Indo-Philippine Archipelago and
366 (right) the region off the Amazon shelf in (top) period 1 (1993-2017) and (bottom) period 2 (2018-2023). The
367 variance reduction was calculated according to equation 6, using either M2 prediction from the MIOST22a
368 (black), HRET (blue), MIOST22a (red) and MIOST24m (green) atlases.

369

5- Conclusion.

370

371 This study presents the M2 MIOST24 (MIOST 2024) internal tide atlas for modes 1 and 2 in the Indo-
372 Philippine archipelago and the region off the Amazon shelf, derived from 25 years (1993-2017) of altimetric
373 SLA and compared with the existing atlases MIOST22 (version 2022, Ubelmann et al., 2022) and HRET (Zaron,
374 2019). The latest is currently used as the reference atlas for correcting internal tides in altimetry data. The
375 improvement of M2 wavelengths is the distinguishing feature between MIOST24 and MIOST22. MIOST24
376 uses the M2 wavelengths of modes 1 and 2 obtained after solving the vertical mode equations constrained
377 by the stratification of the 1993-2020 monthly climatologies from the GLORYS12v1 reanalyses, whereas
378 MIOST22 used the first Rossby deformation radius climatology of Chelton et al. (1998) as an approximation
379 of the mode 1 wavelength, then divided the mode 1 wavelength by 2 to obtain the mode 2 wavelengths. The
380 MIOST24a annual atlas is produced by averaging the GLORYS12v1 monthly reanalyses and using the altimetry
381 data as a set. In contrast, the MIOST24m monthly atlases are derived from GLORYS12v1 monthly reanalyses
382 and subsets of altimetry data, defined with a 15-day overlap in each of the months adjacent (see section 1.3)
383 to the month of interest. The differences between MIOST24, MIOST22 and HRET, the monthly variability of
384 the internal tide and the relevance of using a monthly atlas to correct for the internal tide in altimetry data
385 are discussed.

386



387 The RMSE calculated between M2 atlases of MIOST24a and MIOST22a and between MIOST24a and HRET
388 reaches 3 cm at certain locations in the Indo-Philippine archipelago and the Amazon region, highlighting
389 internal tide estimates that were certainly biased in previous atlases. The spatial mean of the rate of
390 contributions to the RMSE (R_c), defined as the ratio between the contribution of phase differences to the
391 RMSE and the contribution of amplitude differences to the RMSE, shows that the differences between
392 MIOST24a and MIOST22a are mostly explained in the two regions of interest by the phase differences
393 between the two atlases. This means that the differences between the internal tide patterns of MIOST24a
394 and MIOST22a are greater than the differences between the amplitudes of these atlases. This is not surprising
395 as the M2 internal tide structures are better represented in MIOST24a thanks to the improved wavelengths
396 of modes 1 and 2 in MIOST24. The differences between HRET and MIOST24a are related to both amplitude
397 and phase differences. This is because the internal tide amplitudes are larger in MIOST24a and HRET is a
398 smoothed atlas.

399 The amplitude maps of the MIOST24m atlas and the monthly RMSE calculated between MIOST24a and
400 MIOST24m confirm that the M2 internal tides vary over the year. In the Indo-Philippine archipelago, mode
401 1 internal tides generated in the Luzon strait propagate strongly towards the Philippine Sea in the early
402 months of the year (such as April) and in December. In other months, such as June and September, the
403 internal tide structure deforms rapidly. In the South China Sea and the rest of the archipelago, the amplitude
404 and trajectories of the internal tides show significant monthly variability. The total (including modes 1 and 2)
405 internal tide atlases for January and August are the least close to the annual atlas, whereas May is the closest.
406 Mode 2 atlases are distinguished by their amplitude, being furthest from the annual atlas in February and
407 September and closest in July. Overall, for this region, the variability of the monthly atlases has yet to be
408 linked to changes in stratification, seasonal cycles of currents (Sprintall et al., 2019) and seasonal cycles of
409 cyclonic and anticyclonic eddies (Hao et al., 2021), this is beyond the scope of this study and needs special
410 future dedicated study to be revealed.

411 In the Amazon region, our results on the monthly variability of M2 internal tides are in good agreement with
412 those of Tchilibou et al. (2022): from March to June the internal tides propagate far offshore, whereas from
413 August to December the propagation seems to stop at about 5°N. Tchilibou et al (2022) have shown that this
414 is the result of the interaction between internal tides and the mesoscale, which is stronger in the fall season.
415 The RMSE between MIOST24a and MIOST24m allows us to find the bimodal variation MAMJJ (March to July)
416 and ASOND (August to December) of Tchilibou et al. (2022) for mode 1 and the total internal tide, and to
417 show that mode 2 remains relatively stable until April before following the bimodal cycle of mode 1.

418 The annual cycle of the spatial mean of R_c suggests that, in the Indo-Philippine archipelago and the region
419 off the Amazon shelf, for mode 1, the main differences between the annual and monthly atlases result from
420 changes in the phase (*e.i.* the spatial distribution of the M2 internal tides). For mode 2, the annual and
421 monthly atlases are characterized by differences in the internal tide amplitude. The results from these two
422 regions illustrate that altimetry can be used, to some extent at least, to study the monthly variability of the
423 internal tides. In a few years, the monthly atlases could be re-evaluated with longer data series and limiting
424 the overlap of the data from the surrounding months, which may improve furthermore the present results.

425 The last part of the study is devoted to the quantification of the new internal tide correction in the altimetry
426 data : to date, annual atlases (HRET, MIOST22a or MIOST24a) are used instead of monthly atlases
427 (MIOST24m), which are more accurate in terms of the internal tide variability. Variance reductions were
428 calculated for the period (1993-2017, period 1) used to derive the MIOST24 atlases and for an independent
429 period (2018-2023, period 2). For both regions, MIOST24m is the atlas that best corrects the internal tide
430 signal in period 1 altimetry data. In period 2, MIOST24a is better in the Indo-Philippine archipelago, while
431 MIOST24m is better in the region off the Amazon shelf depending on the season. As MIOST24m is not always
432 the best atlas for period 2 in both regions, it is more judicious to choose between annual and monthly atlases
433 depending on the objectives. Monthly atlases are recommended if they are to be applied to the same



434 database from which they were derived as they reflect a specific seasonal variability which can have strong
 435 annual variations. On independent data, monthly atlases should work well around the internal tides
 436 generation sites and along their main trajectories. Beyond these locations, the performance of the monthly
 437 atlases is conditioned by changes in the secondary trajectories reflecting the incoherence of the internal tide.
 438 The annual atlas, on the other hand, may underestimate the correction around the generation sites, but
 439 make a less degraded correction along the secondary trajectories of the internal tide.

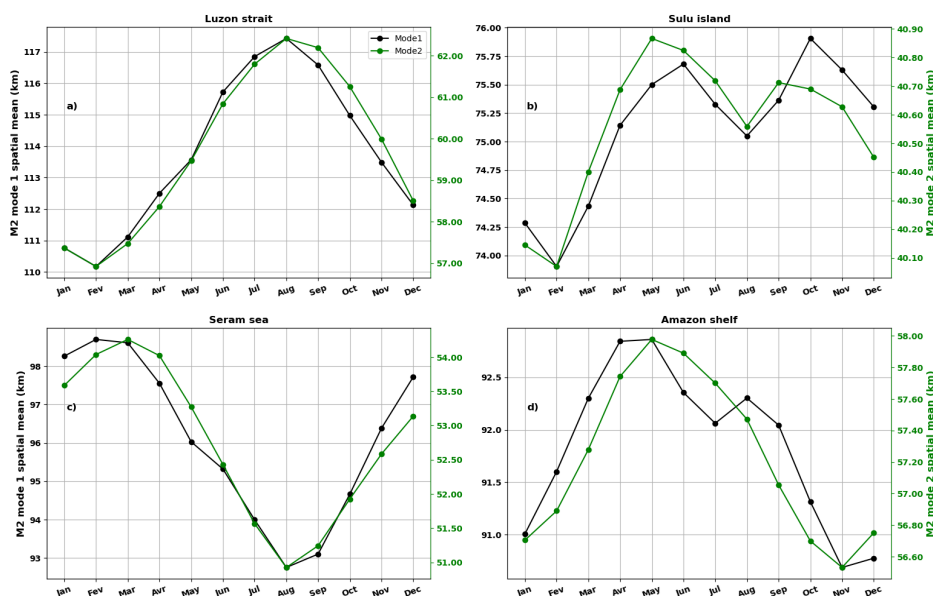
440 In general, the new MIOST24 M2 atlases extract internal tides from altimetric data better than MIOST22
 441 and HRET for the Indo-Philippine and Amazon regions. The results of MIOST24 are encouraging and justify
 442 the development of a global version of the annual MIOST24 atlas for the M2 wave as well as for the N2, S2,
 443 K1 and O1 waves. The new MIOST24 atlas could incorporate satellite data beyond 2017. Initially, the new
 444 global atlas will only include the classic nadir missions described in this article. In a second phase, tests could
 445 be carried out to incorporate 2D observations from the new SWOT (Surface Water and Ocean Topography)
 446 KaRIn mission to improve the spatial resolution of the atlases and its impact on the mode 2 descriptions.

447

448 **Appendix:**

449 **A.1- Example of an annual cycle of mode 1 and 2 M2 wavelengths**

450 The curves of the spatial averages of the monthly M2 wavelengths of mode 1 (in black) and mode 2 (in
 451 green) are shown in Figure A1. The spatial means are calculated in the Luzon Strait (Figure A1a), Sulu Island
 452 Chain (Figure A1b) and Seram Sea (Figure A1c) boxes as shown in Figure 1. The Amazon region is treated as
 453 a box because internal tides generation occurs over almost the entire shelf break, although it is dominant in
 454 the six locations shown in Figure 1. The annual cycles of mode 1 and 2 M2 wavelengths are in phase in the
 455 Luzon Strait (Figure A1a). Mode 1 increases by an average of 7 km between February (when it is lowest) and
 456 September (when it is highest). For mode 2, the variation is about 5 km. In the Sulu Island chain (Figure A1b)
 457 and for mode 1, a first peak is observed in June and a second peak in October. Although the cycle of mode 2
 458 is close to that of mode 1, the monthly variations remain small (less than 1 km, Figure A1b green curve) and
 459 agree with Figure 2f.



460



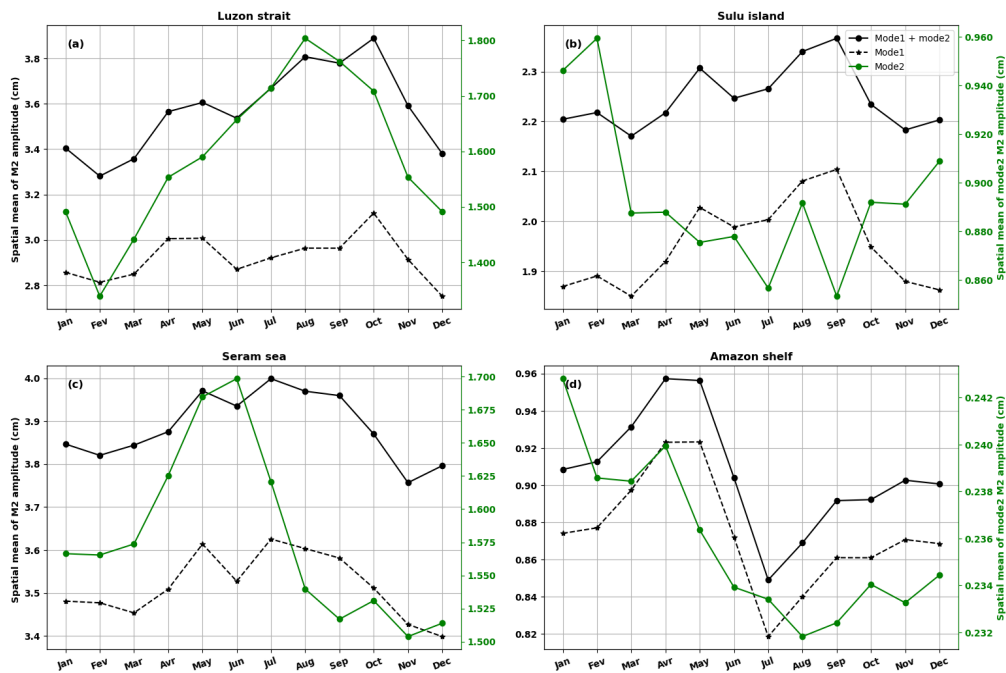
461 **Figure A1:** Annual cycle of mode 1 (black) and mode 2 (green) M2 internal tide wavelengths in the Luzon Strait (a), the Sulu Island chain (b), the Serem Sea (c) and the Amazon region (d). The right vertical axis (green) corresponds to mode 2.

464 The annual cycle of M2 wavelengths in the Seram Sea (Figure A1c) is opposite to that observed in the Luzon Strait. The longest wavelengths are observed in March and the shortest in August, representing a variation of more than 4 km for mode 1 and about 3 km for mode 2 (Figure A1c). In the Amazon region (Figure A1d), there are variations of about 2 km for mode 1 and 2 wavelengths, which are the longest between April and May and the shortest in November. However, the spatial mean is certainly influenced by variations in the eastern part of the basin and reduced by small variations in the western part of the basin (Figures 3e and 3f).

470 A.2- Annual cycle of M2 internal tide amplitude

471 The annual cycles of the internal tide amplitude M2 are obtained by averaging, as above, the amplitudes of the monthly MIOST24m atlases in the Luzon Strait, the Sulu Island Chain and the Serem Sea for the Indo-Philippine archipelago, and the entire Amazon region. The annual cycles of M2 internal tide amplitudes are represented by black, dashed black and green curves for total tide (mode 1 and 2), mode 1 and 2, respectively.

475 In the Luzon Strait (Fig. A.2a), the amplitude of the internal tides reaches its maximum in October. This maximum of about 4 cm follows a relative maximum of 3.6 cm that occurs in spring (April-May), giving the annual cycle a bimodal appearance. The amplitude of mode 2 is maximum in August and minimum in February. The apparent bimodality of mode 1 could be related to the combination in our Luzon Box of the annual antiphase cycles of the M2 internal tides propagating eastward in the Pacific (Philippine Sea) and westward in the South China Sea, as described in Zhao and Qui (2023). The intense eastward flow in winter and spring is expected to contribute to the relative maximum, while the intense westward flow in summer and autumn helps to increase the mean amplitude to the absolute maximum.



483



484 **Figure A2:** Annual cycle of M2 internal tidal amplitudes in the Luzon Strait (a), the Sulu Island Chain (b), the
485 Serem Sea (c) and the Amazon region (d). In black is the total amplitude including modes 1 and 2, dashed
486 black is mode 1, green is mode 2 and the vertical axis on the right (green) corresponds to mode 2.

487 In the Sulu Island chain, the annual cycle is bimodal for the total internal tides and mode 1 (Figure A2b).
488 The peaks occur in May and September and are at almost identical levels. The amplitude of mode 2 remains
489 relatively constant, as do the wavelengths of this mode. It cannot be excluded that the shape of the annual
490 cycle of mode 1 in this part of the ocean is related to seasonal divergences in the propagation of internal
491 tides towards the Sulu and Celebes Seas, as observed in Figure 6. In the Seram Sea, the amplitudes of the
492 total and mode 1 internal tide reach their maximum in July, one month later than the mode 2 maximum
493 (Figure A2c). In the second half of the year, the amplitude of the internal tides decreases. The annual cycle is
494 closer to monomodal, although the first maximum for mode 1 occurs in May.

495 In the Amazon region (Fig. A2d), the internal tides (total and mode 1) are highest between April and May
496 and lowest in July. The distribution of the monthly RMSE in Figure 8b and Tchilibou et al. (2022) is somewhat
497 recovered. The M2 amplitudes are very strong between March and June when the internal tides propagate
498 freely. The weak amplitudes between August and December form a second block of variation. The spatial
499 averages of the mode 2 M2 internal tide amplitude vary between 0.235 and 0.245 cm in the Amazon region.
500 This variation is quite negligible and could be explained by possible compensation for what happens in the
501 different internal tide generation sites. For example, in Figure 7, the transition from April to September is
502 characterized by a decrease in mode 2 amplitude around site B and an increase in amplitude around sites A
503 and E.

504 All the annual cycles presented confirm that MIOST and altimetry provide some access to the annual
505 variability of the internal tide. However, the cycles presented are sensitive to the area in which the spatial
506 averaging was carried out. They cannot be considered strictly as the annual cycle of the internal tides in these
507 regions. This is one of the reasons why we have not discussed these cycles in the main part of the paper and
508 have not attempted to establish the links between these cycles and variations in ocean stratification and
509 circulation. The main objective of our study remains the production of annual and monthly atlases of internal
510 tides. To gain a better understanding of the annual internal tidal cycles, further studies should be carried out,
511 for example using a high-resolution model that would allow a focus on the locations where internal tides are
512 generated.

513 **Authors contributions:** This work is part of DUACS-RD and marée-SWOT/SALP projects funded by the CNES
514 at CLS. MT's work and analyses are supervised by LC. Conceptualization: MT, LC, SB. MT wrote the paper with
515 contributions from all co-authors.

516 **Data availability:** Level 3 along-track altimetric data are available on Copernicus website :
517 https://data.marine.copernicus.eu/product/SEALEVEL_GLO_PHY_L3_MY_008_062/description. The
518 GLORYS12v1 reanalysis is available at <https://doi.org/10.48670/moi-00021>.

519 **Competing interests:** The contact author has declared that none of the authors has any competing interests

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