

Enhancing Urban Pluvial Flood Modelling through Graph Reconstruction of Incomplete Sewer Networks

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Abstract.

This work presents an efficient graph reconstruction-based approach for generating physical sewer models from incomplete information, addressing the challenge of representing sewer drainage effect in urban pluvial flood simulation. The approach utilizes graph-based topological analysis and hydraulic design constraints to derive gravitational flow directions and nodal invert elevations in decentralized sewer networks with multiple outfalls. By incorporating linearized programming formulation to solve reconstruction problems, this approach can achieve high computational efficiency, enabling application to city-scale sewer networks with thousands of nodes and links. Tested in Yinchuan, China, the approach integrates with a 1D/2D coupled hydrologic-hydrodynamic model and accurately reproduces maximum inundation depths ($R^2 = 0.95$) when the complete network layout and regulated facilities are available. Simplifications, such as adopting road-based layouts and omitting regulation facilities, can degrade simulation performance for extreme rainfall events compared to calibrated equifinal methods. However, design rainfall analysis demonstrates that the physical reconstruction approach can reliably outperform equifinal methods, achieving reduced variation and higher accuracy in simulating inundation areas. However, proper configuration of regulated facilities and network connectivity remains crucial, particularly for simulating local inundation during extreme rainfall. Thus, it is recommended to integrate the proposed algorithm with targeted field investigations to further improve urban pluvial flood simulation performance in data-scarce regions.

1 Introduction

Global climate ~~changes and intense human activities significantly alter climatic backgrounds~~ change and intensified human activities have significantly altered climatic conditions and surface environments, leading to an increase in the frequency and magnitude of urban pluvial floods ~~induced by excessive rainfalls and outdated drainage systems designed for past situations~~ , particularly where rainfall exceeds the design capacity of drainage systems (Rosenzweig et al., 2018). As representative ~~man-made drainage~~ infrastructure, sewer networks can effectively mitigate pluvial flood risks by ~~rapidly~~ transporting rainwater to downstream sites such as river channels and detention ponds (Wang et al., 2022). However, its performance can be inherently insufficient and gradually deteriorate due to ~~improper outdated~~ design and poor maintenance (Tran et al., 2024), ~~further causing~~

~~overflow and exacerbating potentially resulting in system overflow and exacerbated~~ surface floods during extreme rainfall
25 (Schmitt and Scheid, 2020). Thus, ~~an accurate representation of the sewer drainage effect accurately modeling the drainage effects of sewer networks~~ is essential for urban pluvial flood simulation and risk attribution (Luan et al., 2024).

However, detailed sewer network information may not always be readily available and its implementation in hydraulic models requires laborious work with high uncertainty (Montalvo et al., 2024), ~~yielding multiple simplified approaches~~. ~~As a result, various simplified approaches have been developed~~ to approximate the ~~sewer drainage effect~~. ~~Most approaches assume~~
30 ~~effect of sewer drainage~~. These approaches typically introduce a term of sewer-induced mass loss during ~~the rainfall-runoff process in specified simulations within specific~~ regions, such as ~~road areas and inlet areas roads and inlets~~ (Li et al., 2020; Xing et al., 2021, 2019). However, ~~they ignore the spatiotemporal distribution of hydraulic head at rainwater inlets and therefore fail to simulate the phenomenon of node overflow due to overload~~. ~~Thus such approaches fail to explicitly consider the relative difference in hydraulic heads between sewer networks and surface water, and thus are incapable of capturing critical processes~~
35 ~~such as overflow caused by system overload~~. To address these limitations, Montalvo et al. (2024) proposes a physics-based approach ~~which approximates the effects of the actual sewer network by designing a corresponding virtual one with open-access data and local regulations (Reyes-Silva et al., 2023)~~ that designs a representative virtual sewer network using publicly available datasets and local design standards. This approach ~~can establish a~~ enables the development of a physical sewer hydraulic model and allow for the simulation of the bidirectional interaction between the ground surface and the sewer system and therefore
40 ~~gives with bidirectional interactions between surface and sewer flows, thereby offering~~ a more comprehensive understanding of urban pluvial flood process.

~~representation of sewer drainage processes~~. The virtual network ~~generation (VNG) proposed in this study closely follows the steps of sewer network design (SND)~~, encompassing two main components for both water distribution and urban drainage networks (Duque et al., 2016): ~~design (VND) consists mainly of two steps:~~

- 45 – **Layout Definition:** ~~This step establishes~~. This step determines the geometric connections and hydraulic directions between nodes in the sewer network. ~~Various algorithms have been developed, including graph theory-based modelling (Bakhshipour et al., 2019; Kim et al., 2021), surface elevation-driven~~ Typical algorithms include surface-elevation-driven delineation (Blumensaat et al., 2012; Duque et al., 2022), ~~and street network-guided graph theory-based modeling (Bakhshipour et al., 2019; Kim et al., 2021), and street network-guided~~ configuration (Chegini and Li, 2022; Reyes-Silva et al., 2023). Most existing work ~~simplifies assumes~~ the target system ~~with as~~ a centralized layout ~~where with~~
50 a single outfall ~~node is present (Hesarkazzazi et al., 2022), allowing the use (Hesarkazzazi et al., 2022), facilitating the application of tree-based algorithms solutions~~ such as the minimum spanning tree (Reyes-Silva et al., 2023) and the Steiner minimal tree (Machine Hsie and Huang, 2019). However, this simplification ignores the rich topological structures of ~~real-world~~ decentralized networks with potential cycles and forests (Bakhshipour et al., 2019). ~~Additionally Furthermore,~~
55 most approaches assume that ~~the direction of gravity flow follows the surface slope, which is not always accurate, especially in flat areas or with gravitational flow direction aligns with surface gradients—an assumption that may not hold in flat urban areas or in the presence of~~ inaccurate elevation data (Hesarkazzazi et al., 2022; Dunton and Gardoni, 2024).

– **Hydraulic Design**. This step determines the sizes and slopes of pipes, as well as the necessary configuration of rain-water treatment facilities ~~where the goal is to fulfill~~, with the objective of satisfying the design discharge requirement estimated by the ~~rational method (Wang and Wang, 2018; Reyes-Silva et al., 2023). Most approaches solve the corresponding problem using mathematical programming, including Rational Method (Wang and Wang, 2018; Reyes-Silva et al., 2023).~~ To achieve this, most approaches formulate the design task as an optimization problem and employ mathematical programming techniques such as linear programming (Swamee and Sharma, 2013), mixed-integer linear programming (Safavi and Geranmehr, 2017), nonlinear programming (Li and Matthew, 1990), and multi-objective programming (Bakhshipour et al., 2021). However, it requires significant computational efforts ~~are required~~ to obtain global optima ~~, especially for in~~ nonlinear or integer cases. Thus, approximate approaches such as piecewise linearization (Elimam et al., 1989), evolutionary algorithms (Wang et al., 2017; Bakhshipour et al., 2021), and topological-driven prediction-correction (Sitzenfrei et al., 2020; Chegini and Li, 2022) are proposed to alleviate the computational burden related with optimization procedures. Nevertheless, a trade-off between approximation-based solution quality and computational efficiency still exists for large-scale cases (Yu et al., 2024).

~~While SND and VNG share similar workflows, they serve fundamentally different purposes. SND~~ Considering previous achievements in VND, this study further proposes a Virtual Network Reconstruction (VNR) approach to improve the physical realism of sewer representations in urban pluvial flood simulation. While VND optimizes network design for ~~cost and performance,~~ economic cost and drainage performance, ~~whereas VNG aims to reconstruct existing networks with incomplete information.~~ VNR estimates the most possible network properties constrained by partially known information. Although existing tools such as SWMManywhere (Dobson et al., 2025) have offered practical solutions for high-quality VND using publicly available datasets, certain discrepancies between virtual and real networks still inevitably exist due to inherent assumptions and simplifications, such as predefined road alignments for network topology, river proximity for outfall location, and ideal hydraulic design using the Rational Method. These discrepancies can potentially alter hydrological connectivity and lead to undesirable performance in flood simulation (Tran et al., 2024). Thus, in order to enhance the physical realism of virtual networks, additional efforts should be devoted to incorporating partially known information as constraints of network generation. This leads to a ~~key-critical~~ critical challenge: while basic network attributes like terminal nodes, spatial layout, and pipe sizes can be possibly ~~obtained through identified and easily adjusted through existing VND toolsets,~~ field surveys and engineering drawings, ~~critical key~~ hydraulic parameters such as flow directions and invert elevations often remain unknown ~~. These parameters are essential for accurate flood simulation but challenging to estimate or hard to achieve efficient estimation~~ at city scale. ~~To address~~ To bridge this gap, we ~~propose a graph reconstruction approach that combines partial topological~~ present our VNR approach that integrates partial network information with surface elevation data to ~~better represent~~ derive the most possible hydraulic parameters, thereby reducing simulation uncertainty of sewer drainage effects in urban flood modeling, ~~thereby reducing simulation uncertainty.~~

In the remainder of this paper, we first describe the proposed workflow for ~~sewer network reconstruction~~ VNR (Sect. 2) along with the corresponding 1D/2D coupled hydrologic-hydrodynamic model ~~employed~~ for urban pluvial flood simulation (Sect. 3) and then conduct a comparative analysis of ~~the reconstructed models' flood simulation~~ performance under varying

levels of information completeness during reconstruction, taking into account factors such as regulated facility removal and road-based layout simplification (Sect. 4).

95 2 Graph-based sewer network reconstruction

2.1 Graph representation of sewer networks

~~We represent sewer networks as graphs to leverage graph theory for topological analysis, providing a foundation for the reconstruction process. Given the spatial distribution of pipes, The necessary inputs of sewer network reconstruction include the sewer network layout with specified outfalls and corresponding digital elevation model (DEM). For convenience of topological~~
 100 ~~analysis, we represent~~ the sewer network ~~can be abstracted~~ as an undirected graph $G = (V, E)$ where $V = \{v_i\}$ and $E = \{e_{i,j}\}$ represent the sets of nodes and links, respectively ~~(Shi et al. (2023))~~. ~~When link directions are specified, e.g., by~~ (Shi et al., 2023). ~~Then we can specify the link directions as related~~ gravitational flow directions ~~, and convert~~ the original undirected graph ~~can be converted into to~~ the corresponding directed form $G_D = (V, E_D)$ where $E_D = \{\vec{e}_{i,j}\}$ represents the set of directed links evaluated as follows:

$$105 \quad \vec{e}_{i,j} = \begin{cases} 1, & v_j \in \mathcal{N}_{G_D}(v_i) \\ 0, & v_j \notin \mathcal{N}_{G_D}(v_i) \end{cases}, \forall v_j \in \mathcal{N}_G(v_i) \quad (1)$$

where $\mathcal{N}_{G_D}(v_i)$ and $\mathcal{N}_G(v_i)$ represent the neighboring nodes of node v_i in G_D and G .

~~According to the number of directed links pointed from/to~~ For one node v_i , its out-degree $d_{\text{out},i}$ and in-degree $d_{\text{in},i}$ can be defined as ~~follows~~ the number of directed links pointed from/to it:

$$d_{\text{out},i} = \sum_{v_j \in \mathcal{N}_G(v_i)} \vec{e}_{i,j}, d_{\text{in},i} = \sum_{v_j \in \mathcal{N}_G(v_i)} \vec{e}_{j,i}, \quad (2)$$

110 ~~Besides these basic topological~~ In addition to these basic attributes, some useful structures can be derived from the graph representation. Considering the potential cycles in the geometric layout of G , ~~the cycle basis we identify the set of simple cycles~~ $\mathcal{C} = \{C_k\}$ ~~can be identified such that every cycle in G can be expressed as the sum of cycles in $\mathcal{C}$ (Paton (1969))~~ defined as the set of closed paths where no node appears twice (Johnson, 1975). For a cycle $C_k \in \mathcal{C}$, we group its internal nodes and links into the corresponding sets denoted by CV_k and CE_k , respectively. ~~Thus, Then~~ its out-degree $dC_{\text{out},k}$ and in-degree
 115 $dC_{\text{in},k}$ can be ~~further~~ defined as follows:

$$dC_{\text{out},k} = \sum_{v_i \in CV_k} \sum_{v_j \in \mathcal{N}_G(v_i) \setminus CV_k} \vec{e}_{i,j}, dC_{\text{in},k} = \sum_{v_i \in CV_k} \sum_{v_j \in \mathcal{N}_G(v_i) \setminus CV_k} \vec{e}_{j,i} \quad (3)$$

where $\mathcal{N}_G(v_i) \setminus CV_k$ represents the difference set between $\mathcal{N}_G(v_i)$ and CV_k , i.e., the set of nodes that are neighboring nodes of v_i but not in C_k .

According to Eq. 3, we define a cycle C_k as an "island" if the sum of its in-degree and out-degree is equal to 1 and further
 120 denote the set of nodes located in the islands of G as $\text{ISD}(G)$:

$$\text{ISD}(G) = \bigcup_{C_k} C_k \quad \text{s.t.} \quad dC_{\text{out},k} + dC_{\text{in},k} = 1 \quad (4)$$

In addition to general properties, we also consider some ~~sewer-specific~~ sewer-related hydraulic characteristics for the convenience of the following analysis. For a node ~~v_i~~ $v_i \in V$, we include it in the set of outfalls (denoted as $\mathcal{O}$) if its out-degree is 0 and in-degree is 1, or in the set of sources (denoted as $\mathcal{S}$) if its in-degree is 0 and out-degree is 1:

$$125 \quad \mathcal{O} = \left\{ v_i \mid v_i \in V, d_{\text{out},i} = 0, \underline{d_{\text{in},i} = 1} \right\}, \mathcal{S} = \left\{ v_i \mid v_i \in V, \underline{d_{\text{out},i} = 1}, d_{\text{in},i} = 0 \right\} \quad (5)$$

During practical usage, the set of sources can be derived as the difference set between the set of predefined outfalls and the set of nodes whose in-degree and out-degree are summed to 1.

~~We~~ To allow for hydraulic simulation, we also attach the invert elevation attribute to v_i (denoted as z_i) which can be initialized as follows:

$$130 \quad z_i^{(0)} = z_{g,i} - D_{\min} \quad (6)$$

where $z_i^{(0)}$ is the initial value of z_i ; $z_{g,i}$ is the surface elevation at the location of v_i ; $D_{\min}$ is the minimum allowable cover depth and set as $D_{\min} = 0.6$ m by default (~~MOHURD (2021)~~) (MOHURD, 2021).

By comparing invert elevations of neighboring nodes, link directions can be initialized as follows:

$$\vec{e}_{i,j}^{(0)} = \begin{cases} 1, & z_i^{(0)} \geq z_j^{(0)} \\ 0, & z_i^{(0)} < z_j^{(0)} \end{cases} \quad (7)$$

135 Fig. 1 shows an illustrative example of a simple sewer system in its graph representation with aforementioned properties.

2.2 Gravitational flow direction derivation

Since flow direction initialization using Eq. 7 does not consider the necessary topological constraints for a feasible layout of the sewer network (Fig. 2), it may produce an unfeasible or unreasonable layout and therefore needs further correction (~~Reyes-Silva et al. (2023)~~) (Reyes-Silva et al., 2023).

140 In order to maintain flow directions as intact as possible during correction, we formulate the following 0-1 programming problems with linear constraints:

$$\min_{e_{ij}} \sum_{\vec{e}_{i,j}} \left| \vec{e}_{i,j} - \vec{e}_{i,j}^{(0)} \right| \quad (8a)$$

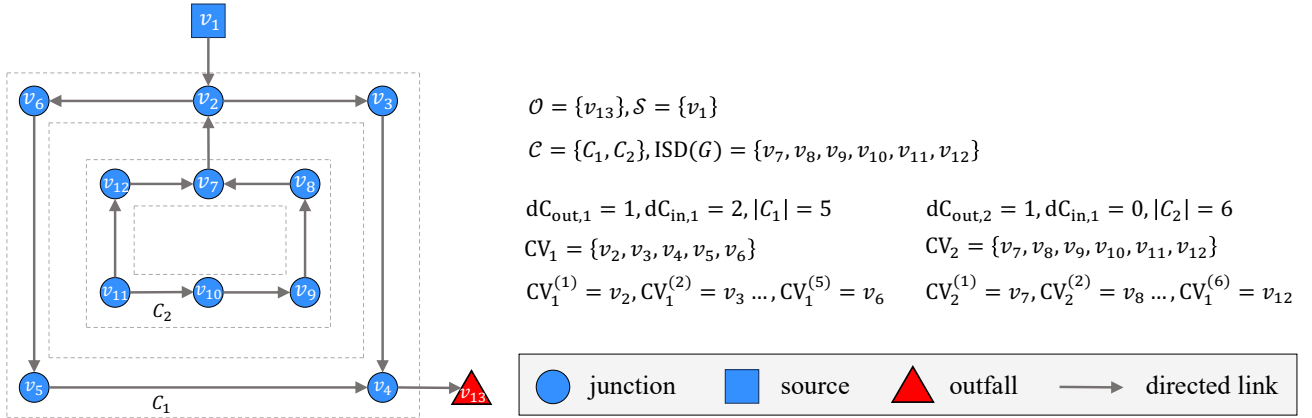
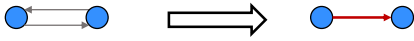
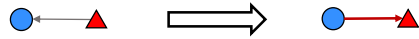


Figure 1. Graph representation of the sewer network.

Constraint 1: unique direction



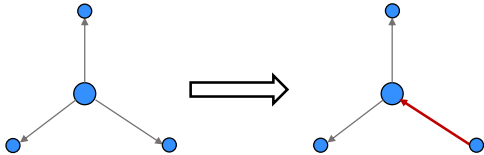
Constraint 2: zero out-degrees at outfalls



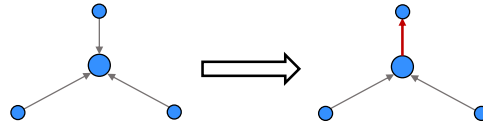
Constraint 3: known flow directions



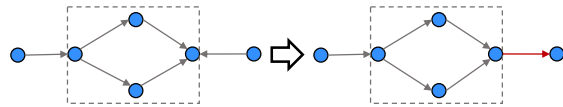
Constraint 4: strictly positive in-degrees at nodes that are neither sources nor situated in an island



Constraint 5: strictly positive out-degrees at non-outfall nodes



Constraint 6: strictly positive out-degrees of cycles



Constraint 7: no recirculation inside the cycles

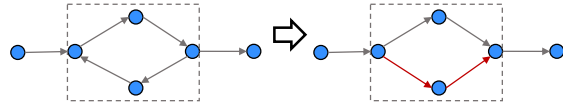


Figure 2. Topological constraints for a feasible sewer network.

$$\begin{aligned}
& \left\{ \begin{aligned}
& \vec{e}_{i,j} = 1 - \vec{e}_{j,i} & (8b) \\
& \vec{e}_{i,j} = 1, \forall v_j \in \mathcal{O} & (8c) \\
& \vec{e}_{i,j} = \vec{e}_{i,j}^*, \forall \vec{e}_{i,j} \in \mathcal{E}_D^* & (8d) \\
& d_{in,i} \geq 1, \forall v_i \notin \underline{\text{IS}} \cup \text{ISD}(G) & (8e) \\
& d_{out,i} \geq 1, \forall v_i \notin \mathcal{O} & (8f) \\
& dC_{out,k} \geq 1, \forall C_k \in \mathcal{C} & (8g) \\
& \vec{e}_{CV_k^{(|C_k|)}, CV_k^{(1)}} + \sum_{i=1}^{|C_k|-1} \vec{e}_{CV_k^{(i)}, CV_k^{(i+1)}} \leq |C_k| - 1, \forall C_k \in \mathcal{C} & (8h)
\end{aligned} \right.
\end{aligned}$$

145 where $|C_k|$ is the number of nodes in C_k ; $\mathcal{E}_D^*$ is the set of links with known directions (denoted by $\vec{e}_{i,j}^*$); $\vec{e}_{CV_k^{(|C_k|)}, CV_k^{(1)}} + \sum_{i=1}^{|C_k|-1} \vec{e}_{CV_k^{(i)}, CV_k^{(i+1)}}$ is the sum of consecutively connected direction values along C_k .

The rationale for each constraints-constraint can be summarized as follows (cf. Fig. 2):

- Eq. 8b: No bi-directional links between consecutive nodes
- Eq. 8c: Outfalls must have zero out-degree
- 150 – Eq. 8d: Preserves known link directions
- Eq. 8e: Non-inlet-Non-source and non-island nodes must have positive in-degrees (Eq. 4)
- Eq. 8f: Non-outfall nodes must have positive out-degrees
- Eq. 8g: Cycles must have positive out-degrees for flow passage
- Eq. 8h: No recirculation within cycles

155 Prior to optimization, pipes are discretized into 50 m segments following common inlet spacing (MOHURD, 2021). This ensures uniform link lengths for objective evaluation and provides computational elements with inlets at endpoints for surface-sewer exchange in hydraulic simulation.

2.3 Nodal invert elevation derivation

Corrected gravitational flow directions pave the way for the derivation of nodal invert elevation prepared for downstream hydraulic simulation. Based on invert elevation initialized by Eq. 6, further adjustment is needed to keep the slopes of links within the range of minimum and maximum allowable slopes (Safavi and Geranmehr, 2017).

160 In order to achieve the least deviation from initial results considering sewer construction costs proportional to excavation depth (Swamee and Sharma, 2013; Machine Hsie and Huang, 2019), we introduce the following nonlinear optimization problem to estimate the invert elevation of nodes:

Table 1. Slope constraints with respect to different sizes according to Standard for Design of Outdoor Wastewater Engineering (MOHURD, 2021).

Diameter [mm]	Minimum slope	Maximum slope
300	0.002	0.41
400	0.0015	0.28
500	0.0012	0.21
600	0.001	0.16
800	0.0008	0.11
1000	0.0006	0.08
1200	0.0006	0.06
1400	0.0005	0.05
> 1500	0.0005	0.05

$$\begin{aligned}
 & \min_{z_i} \sum_{z_i} |z_i - z_i^{(0)}| \\
 & \text{s.t.} \quad \begin{cases} i_{i,j} \leq -i_{\min,i,j}, & \forall \vec{e}_{i,j} = 1 \\ i_{i,j} \geq -i_{\max,i,j}, & \forall \vec{e}_{i,j} = 1 \end{cases}
 \end{aligned} \tag{9}$$

where $i_{i,j}$ is the slope of $\vec{e}_{i,j}$; $i_{\min,i,j}$, $i_{\max,i,j}$ are the minimum and maximum allowable slopes required for $\vec{e}_{i,j}$ according to Table 1 summarized from the Standard for Design of Outdoor Wastewater Engineering (MOHURD, 2021), considering both explicitly stated slope limits and those derived from velocity constraints (Swamee and Sharma, 2013).

For simplicity but without loss of generality, $i_{i,j}$ is estimated using the invert elevation of two consecutive nodes, ensuring the linearity of constraints for the above optimization problem:

$$i_{i,j} = -\frac{1}{d_{i,j}} z_i + \frac{1}{d_{i,j}} z_j \tag{10}$$

It should be also noted that Eq. 10 can be also extended to the case of multiple consecutive nodes and corresponding slope estimator still remains in the form of the linear combination of nodal invert elevation (see Appendix A for details), which maintains the linearity of constraints in the original optimization problem.

2.4 Computational efficiency considerations

The objective functions of Eq. 8 and Eq. 9 are expressed ~~in the form of the~~ as the sum of absolute deviations and can be further reduced into an equivalent linear form as follows (~~Wagner (1959); Giangrande et al. (2013)~~ Wagner, 1959; Giangrande et al., 2013), thus ensuring their solution efficiency for large-scale applications.

Without loss of generality, for minimizing the summation of absolute values:

$$180 \quad L = \sum_{i=1}^N |k_i x_i - b_i| \quad (11)$$

where k_i, b_i are fixed numbers with respect to N decision variables x_i , we can introduce auxiliary decision variables $z_i = |k_i x_i - b_i|$ constrained by:

$$\begin{cases} z_i \geq k_i x_i - b_i \\ z_i \geq -k_i x_i + b_i \\ z_i \geq 0 \end{cases} \quad (12)$$

Thus, the original unconstrained nonlinear problem can be reformulated into an equivalent linear one with additional constraints:

$$185 \quad \begin{aligned} & \min_{x_i, z_i} \sum_{i=1}^N z_i \\ & \text{s.t.} \quad \begin{cases} z_1 \geq k_1 x_1 - b_1, z_1 \geq -k_1 x_1 + b_1, z_1 \geq 0 \\ \dots, \dots \\ z_N \geq k_N x_N - b_N, z_N \geq -k_N x_N + b_N, z_N \geq 0 \end{cases} \end{aligned} \quad (13)$$

Furthermore, if additional constraints are present with Eq. 11, they can be added directly to the reformulated problem (Eq. 13) without loss of equivalence. This reformulation strategy has been used in previous research (Giangrande et al., 2013) and thus can be easily extended to our work for efficient sewer network reconstruction (Eq. 8 and Eq. 9).

190 [In terms of solving the reformulated linear programming problems, we select the open-source Computational Infrastructure for Operations Research \(COIN-OR\) branch-and-cut solver \(CBC\) \(Forrest and Lougee-Heimer, 2005\) through its Python interface in PuLP \(Mitchell et al., 2011\).](#)

3 AUTOSHED: A 1D/2D coupled hydrologic-hydrodynamic model

Given the sewer network reconstructed from incomplete information, we further adopt a 1D/2D coupled hydrologic-hydrodynamic model named AUTOSHED to simulate the pluvial flood process in the urbanized area. AUTOSHED delineates the whole simulation domain into multiple triangular-shaped units (TSUs). For each unit, AUTOSHED uses the Rain-on-Grid approach, also known as the Fully Hydrodynamic Approach (Hall, 2015; Chen and Huang, 2024; Perrini et al., 2024), and performs sequential hydrologic-hydrodynamic computations for surface runoff generation and routing, respectively.

3.1 Surface runoff generation and routing

200 The surface runoff generation scheme is mainly built upon the core module of the Surface Urban Energy and Water Balance Scheme (SUEWS) (Järvi et al., 2011) and Tsinghua Integrated Hydrological Modeling System (THIHMS) (Ni et al., 2008) except for overland and channel flow routing. Each TSU is divided into impervious and pervious parts according to the empirical impervious ratio α_{imp} derived from the ~~corresponding land use types in the unit using unit land use statistic by~~ area-weighted averaging, ~~which is also known as the mosaic method (Cao et al., 2020; Krebs et al., 2014).~~ For the impervious part, surface runoff ΔS_{imp} is equal to rainfall. For the pervious part, surface runoff ΔS_{p} equals rainfall minus vegetation interception, building interception and soil infiltration, parameterized using leaf area index, building footprint ratio and soil properties (Järvi et al., 2011; Ni et al., 2008). ~~The (Cao et al., 2020; Krebs et al., 2014).~~ And the total surface runoff ΔS_{sr} is calculated as the area-weighted sum of ΔS_{p} and ΔS_{imp} : ~~runoff from the impervious and pervious parts. Details of methodologies for rainfall-runoff simulation can be found in the work of (Ni et al., 2008) and (Järvi et al., 2011).~~

$$210 \quad \Delta S_{\text{sr}} = \alpha_{\text{imp}} \Delta S_{\text{imp}} + (1 - \alpha_{\text{imp}}) \Delta S_{\text{p}}$$

After obtaining total surface runoff, a well-balanced formulation of 2D shallow water equations (SWEs) (Song et al., 2011) is adopted to simulate the subsequent surface routing process:

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{E}}{\partial x} + \frac{\partial \mathbf{G}}{\partial y} = \mathbf{S}$$

where

$$215 \quad \frac{\partial}{\partial t} \begin{bmatrix} h \\ hu \\ hv \end{bmatrix}, \underline{\mathbf{E}} = \frac{\partial}{\partial x} \begin{bmatrix} hu \\ hu^2 + g(h^2 - z_b^2)/2 \\ huv \end{bmatrix}, \underline{\mathbf{G}} = \frac{\partial}{\partial y} \begin{bmatrix} hu \\ huv \\ hv^2 + g(h^2 - z_b^2)/2 \end{bmatrix}, \underline{\mathbf{S}} = \begin{bmatrix} \Delta S_{\text{sr}} - q_{\text{sd}} \\ -g(h + z_b) \frac{\partial z_b}{\partial x} - gh \frac{n^2 u \sqrt{u^2 + v^2}}{h^{4/3}} \\ -g(h + z_b) \frac{\partial z_b}{\partial y} - gh \frac{n^2 v \sqrt{u^2 + v^2}}{h^{4/3}} \end{bmatrix} \quad (14)$$

where h is the water depth; u, v are the depth-averaged velocity components in the x- and y-directions; z_b is the bed elevation; g is the gravitational acceleration; q_{sd} is the mass loss term caused by sewer drainage; S_{fx}, S_{fy} are the friction slopes in the x- and y-directions which can be parameterized by the Manning formulae:

$$S_{fx} = \frac{n^2 u \sqrt{u^2 + v^2}}{h^{4/3}}, S_{fy} = \frac{n^2 v \sqrt{u^2 + v^2}}{h^{4/3}}$$

220 where n is the empirical Manning coefficient initially derived from initialized as n_0 by land use types using the mosaic method and further increased at TSUs intersected with buildings using according to the intersected area ratio of TSUs with buildings (denoted as b_f) by the building roughness method (Schubert and Sanders, 2012) ÷

$$n = n_0 + (0.5 - n_0) \cdot b_f$$

where n, n_0 are the final and initial estimates of the empirical Manning coefficient and b_f is the intersected building area ratio at the TSU.

Considering the significance of topography in simulating pluvial flood, AUTOSHED utilizes a sloping bottom model to define the bed elevation at three vertices of each TSU (Begnudelli and Sanders, 2006), thereby achieving the second-order spatial accuracy in surface topography representation. AUTOSHED uses the finite volume method to solve the above 2D SWEs where the MUSCL reconstruction is used for estimating flow variables at the midpoints of unit edges, the HLLC approximate Riemann solver is used for evaluating mass and momentum fluxes across edges, the two-stage explicit Runge-Kutta approach is used for updating flow variables, where the maximum roughness is set as $0.5 \text{ s/m}^{1/3}$. Details of methodologies on for solving 2D SWEs can be found in the work of Song et al. (2011). The modules of surface runoff generation and routing are implemented in C++ and CUDA (Computed Unified Device Architecture), which can leverage many-core parallel capacity of the graphics processing units to significantly boost the computation performance of refined coupled hydrologic-hydrodynamic simulation with millions of units (Lacasta et al. (2014)).

3.2 Sewer flow simulation and its coupling with surface flow

In the TSU with rainwater inlets, vertical linkages are established for bidirectional coupling between the surface flow and the sewer flow. A modified form of the 1D Saint-Venant equations is introduced to represent simulate the sewer flow process using a node-link approach (Rossman and Huber (2017))(Rossman and Huber, 2017):

$$\begin{cases} \frac{\partial H}{\partial t} = \frac{Q_{1D-2D} + \sum Q_{nl}}{A_{as}} \\ \frac{\partial Q}{\partial t} = 2U \frac{\partial A}{\partial t} + U^2 \frac{\partial A}{\partial x} - gA \frac{\partial H}{\partial x} - gAS_f \end{cases} \quad (15)$$

where H is the total nodal hydraulic head of water; Q is the flow rate; U is the flow velocity; A is the cross-sectional area; A_{as} is the node assembly surface area consisting of node's storage surface area and half the surface area of connected links (Rossman (2015))(Rossman, 2015); S_f is the friction slope parameterized by the Manning formula; Q_{nl} are the flow contributed by neighboring links in the sewer system; Q_{1D-2D} is the flow sourced from the mass-exchange mass source term exchanged between the surface flow and the sewer flow.

Considering the complexity in flow exchange between the surface and underground sewer system (Dai et al. (2023)), AUTOSHED follows previous research works and adopts the weir/orifice-based empirical formulae to parameterize Q_{1D-2D} at each inlet (Buttinger-Kreuzhuber et al. (2022)). Assuming Q_{1D-2D} is positive when water flows from the TSU to the linked inlet, the corresponding parameterization formulae can be summarized as follows:-

$$250 \quad Q_{1D-2D} = \begin{cases} \frac{2}{3}c_w P \sqrt{2g} h_{2D}^{1.5}, & H_{1D} < z_{bc} \\ c_{o,s} A \sqrt{2g} [h_{2D} - (H_{1D} - z_{bc})]^{0.5} & z_{bc} \leq H_{1D} < z_{bc} + h_{2D} - A/P \\ c_{w,s} P \sqrt{2g} h_{2D} [h_{2D} - (H_{1D} - z_{bc})]^{0.5} & z_{bc} + h_{2D} - A/P \leq H_{1D} < z_{bc} + h_{2D} \\ -c_{w,s} P \sqrt{2g} h_{2D} [(H_{1D} - z_{bc}) - h_{2D}]^{0.5} & z_{bc} + h_{2D} \leq H_{1D} < z_{bc} + h_{2D} + A/P \\ -c_{o,s} A \sqrt{2g} [(H_{1D} - z_{bc}) - h_{2D}]^{0.5} & H_{1D} \geq z_{bc} + h_{2D} + A/P \end{cases}$$

where H_{1D} , h_{2D} and z_{bc} are the total hydraulic head at the inlet, the water depth at the TSU and the center bed elevation at the TSU, respectively; A and P are the inlet's area and perimeter, respectively; c_w , $c_{w,s}$ and $c_{o,s}$ are discharge coefficients for the free weir, the submerged weir, and the orifice equations, respectively. By default, AUTOSHED sets $c_w = 0.56$, $c_{w,s} = 0.11$ and $c_{o,s} = 0.2$ (Rubinato et al. (2017)) and $A = 0.3375 \text{ m}^2$, $P = 2.4 \text{ m}^2$ assuming that each inlet is rectangular whose size is

255 $0.45 \text{ m} \times 0.75 \text{ m}$ according to field investigation. Considering that one TSU can be linked with multiple inlets, we have:-

$$q_{sd} = \frac{1}{A_T} \sum_{i=1}^N Q_{1D-2D}^{(i)}$$

where A_T is the total area of the TSU, N is the total number of linked inlets and $Q_{1D-2D}^{(i)}$ is the sewer drainage rate at the i -th inlet derived from Eq. B1 and further constrained by the water availability of both the TSU and the inlet (Buttinger-Kreuzhuber et al. (2022)):-

$$260 \quad Q_{1D-2D}^{(i)} = \min \left(\frac{\min(h_{2D} A_T, V_{as})}{\Delta t} \frac{Q_{1D-2D}^{(i)}}{\sum_{i=1}^N Q_{1D-2D}^{(i)}}, Q_{1D-2D}^{(i)} \right)$$

where V_{as} is the water volume at the inlet assembly determined by A_{as} and H_{1D} ; Δt is the coupling time step evaluated as the minimum value between the timesteps of the [Details of methodologies for solving 1D Saint-Venant equations under regulation can be found in Rossman \(2015\)](#) and 2D solvers (Chen et al. (2018)):-

In order to solve Eq. 15 jointly with Eq. 14, AUTOSHED utilizes the 1D routing portion of the Storm Water Management Model (SWMM) 5.1.015 (Rossman (2015)) and implements communication routines for 1D/2D state variables such as water depth and hydraulic head (Eq. B1) via interface functions by compiling SWMM as a dynamic link library (Leandro and Martins (2016)):-

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In addition to unregulated nodes and links, we also account for the controlling effects of pump stations and wastewater treatment plants using Type 4 pumps (whose flow rate changes linearly with the inlet node depth until the maximum pumping capacity is reached) and nodes with limited maximum inflows in SWMM, respectively (Rossman (2015)) [corresponding surface-sewer flow coupling scheme is given in Appendix B.](#)

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3.3 Study area and data

The study area is the main city zone of Yinchuan (CYC), Ningxia Hui autonomous region, situated in the northwestern part of China, covering an area of 137.15 km². Despite being located in an arid region with an average annual rainfall of 189 mm and annual evaporation of 1825 mm, CYC has experienced several flood disasters due to increasing extreme rainfall events in recent years (~~Lu et al. (2024)~~)([Lu et al., 2024](#)). According to local documents, most of the drainage system in CYC is the combined sewer system, and therefore its drainage capacity is largely constrained by downstream wastewater treatment plants (WTPs) due to restrictive environmental regulations, which may result in overflow at rainwater inlets and further amplify the surface inundation risks.

In order to establish the urban pluvial flood model for scenario analysis, we collect multi-source geographical datasets listed as follows:

- 5 m digital elevation model ([DEM](#), Fig. 3 (a)) generated from the stereo images of ZiYuan-3 satellite. [Following common practices of DEM preprocessing in urban flood simulation, we delete the inaccurately measured building roof elevation from the original product \(Chen and Huang, 2024\) and lower the surface elevation of grids containing roads by 0.2 m \(Liu et al., 2022\) to improve the representation of hydrological connectivity in DEM.](#)
- 10 m land use map (Fig. 3 (b)) collected from the European Space Agency (ESA) WorldCover 2021 product (~~Zanaga et al. (2022)~~)([Zanaga et al., 2022](#)) and covers tree, grassland, cropland, built-up and bareland area in the study area.
- Building footprint (Fig. 3 (a)) and road network layers (Fig. 3 (b)) downloaded via the application programming interface of the Baidu map. Considering potential underestimation of impervious area identified from remote sensing datasets (~~Weng (2012)~~)([Weng, 2012](#)), we further modify the land use type as built-up area at pixels intersected with buildings and roads.
- Sewer network layout and corresponding attribute of pipeline sizes (Fig. 4 (a)) digitized from investigation and design documents authorized by the local government. It should be noted that when detailed information is unavailable, previous research would generate a virtual sewer network from the street network (~~Montalvo et al. (2024)~~)([Montalvo et al., 2024](#)). In order to investigate potential effects induced by such simplification, we further create a road-based sewer network by identifying pipes intersected with the major roadway zone and then performing necessary reconnections at pipes broken intermediately (Fig. 4 (b)). Here we define the term of "major road" (Fig. 3 (b)) as the union of the primary, secondary, tertiary and trunk roads and then generate corresponding roadway zones by buffering road centerlines with the width evaluated from The Design of Urban Road Engineering (CJJ 37—2012).

The formula of the designed rainfall in CYC is also collected based on local rainfall statistics:

$$q = \frac{551.4(1 + 0.584 \lg P)}{(t + 11)^{0.669}} \quad (16)$$

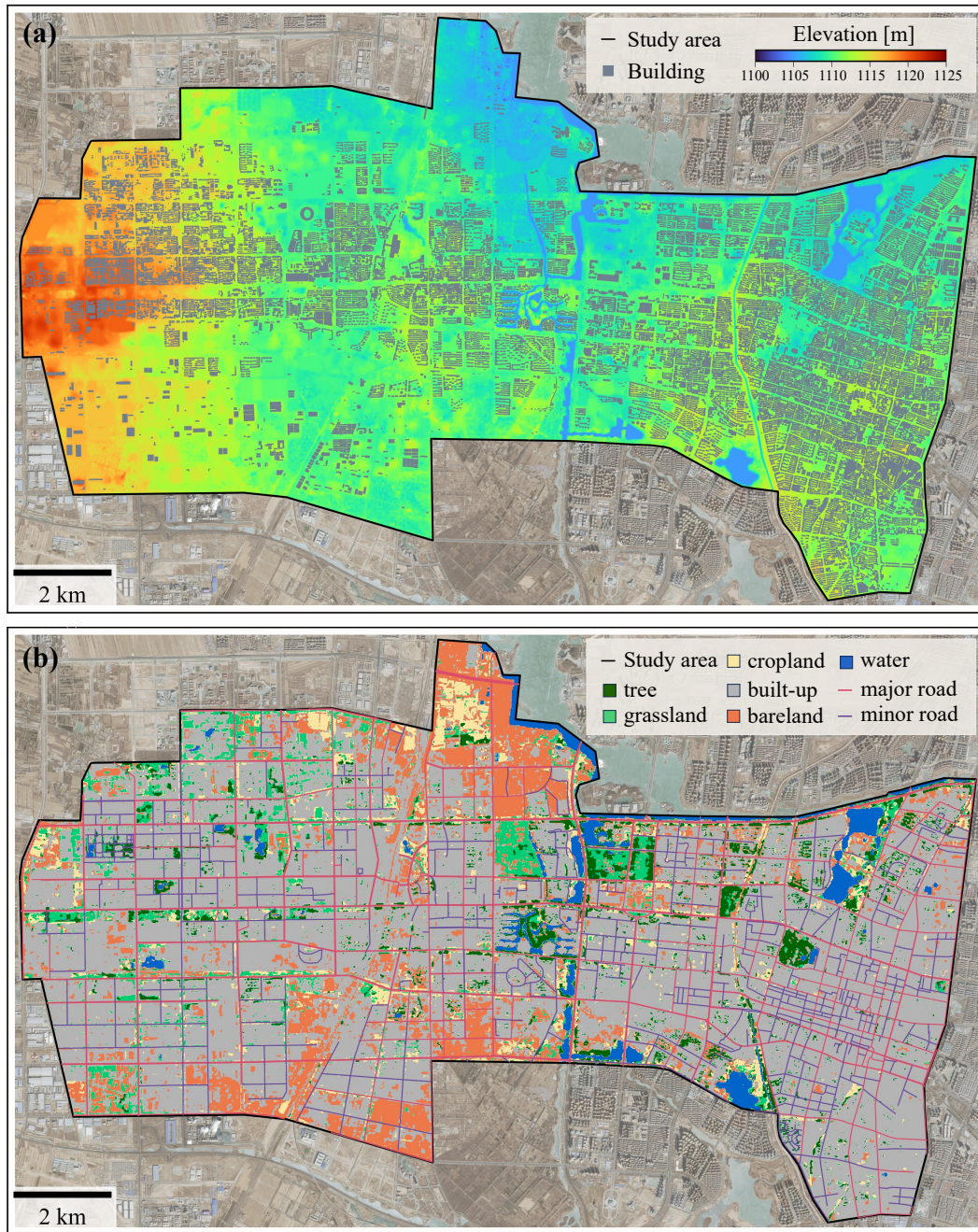


Figure 3. Geographical datasets in the study area. (a) Digital elevation model. (b) Land use map and road networks. Basemaps are provided by derived from ESRI World Imagery (Credit: Esri, TomTom, Garmin, FAO, NOAA, USGS, © OpenStreetMap contributors, and the GIS User Community).

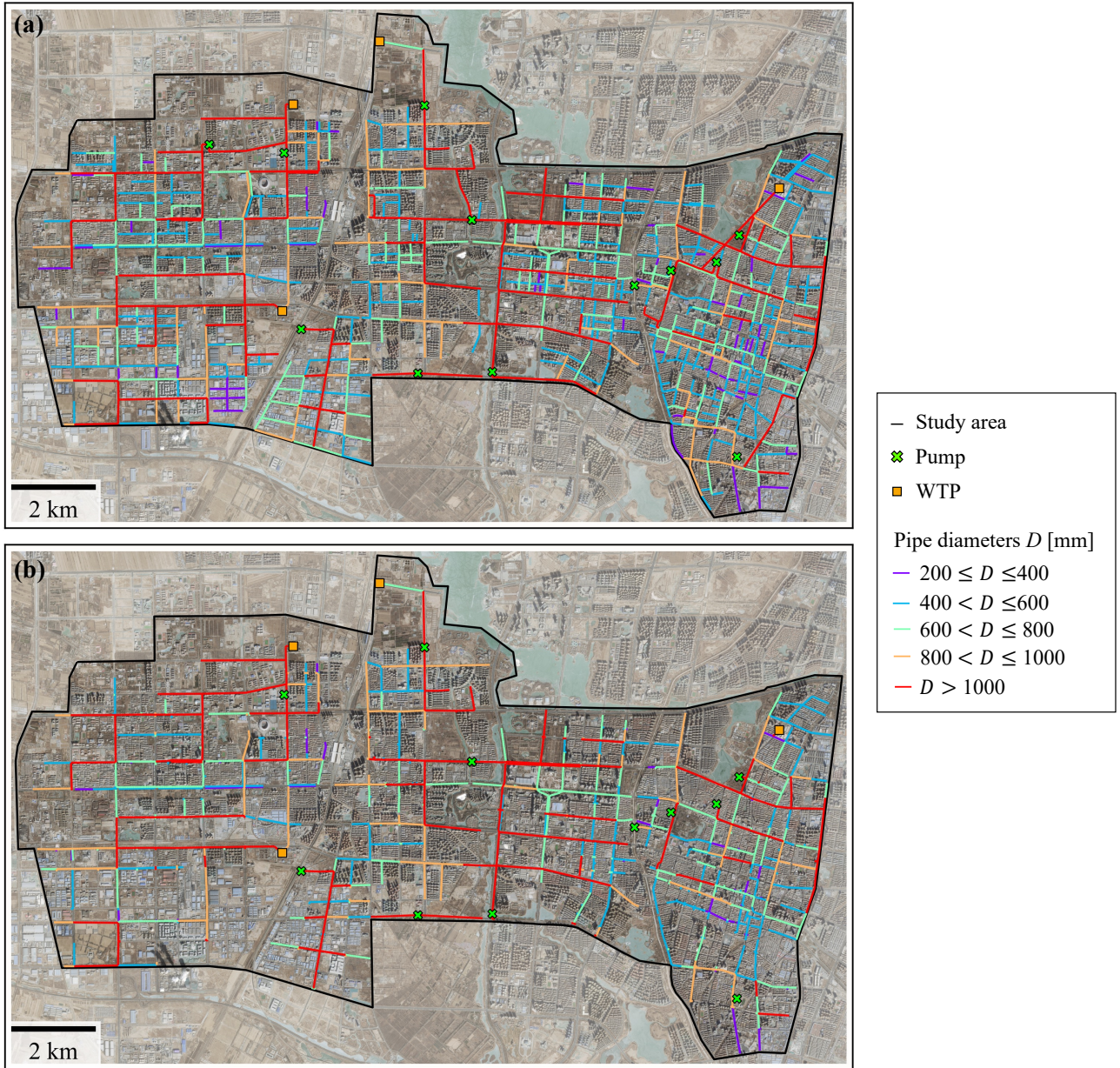


Figure 4. Sewer network in the study area. (a) Complete sewer network digitized from the local document. (b) Simplified sewer network filtered within major roadway zone. Basemaps are ~~provided by~~ derived from [ESRI World Imagery](#) (Credit: [Esri](#), [TomTom](#), [Garmin](#), [FAO](#), [NOAA](#), [USGS](#), © [OpenStreetMap contributors](#), and the [GIS User Community](#)).

where q is the rainfall intensity, $L/(s \cdot ha)$; P is the return period; t is the rainfall duration, min.

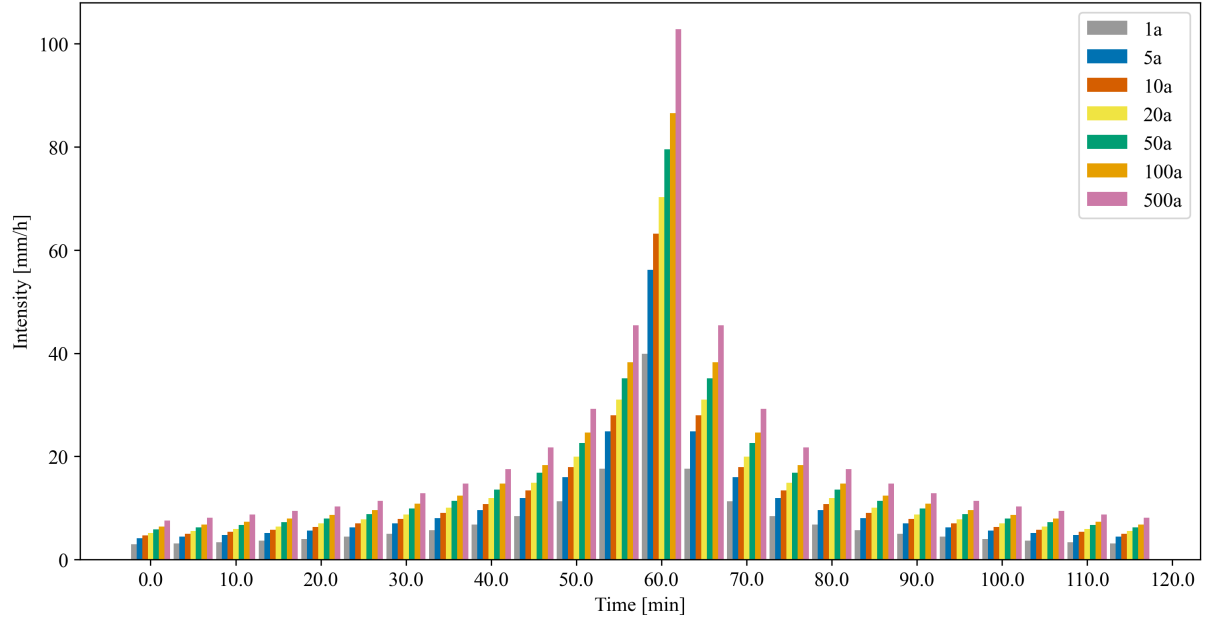


Figure 5. 2-hour design rainfall scenarios with varying return periods (1a, 5a, 10a, 20a, 50a, 100a and 500a).

Seven designed rainfalls with return years of 1a, 5a, 10a, 20a, 50a, 100a, and 200a are selected for the scenario analysis where each rainfall event lasts for 2 h (Fig. 5), followed by an additional 2 h period without any precipitation.

3.4 Baseline configurations

Four ~~Five~~ baselines are selected for the comparison of the performance between the proposed approach (denoted as the FSR approach) and other approximation methods:

- Full-Sewer-reconstruction-No-controls (FSN) which uses the same reconstruction approach but ignores the existence of regulated facilities such as pump stations and wastewater treatment plants. To be specific, regulated facilities located at outflow and intermediate points are configured as free outfalls and uncontrolled junctions, respectively.
- Road-based-Sewer-reconstruction-No-controls (RSN) which uses the same reconstruction approach but adopts the layout of sewers filtered by the major roadway zone (Fig. 4 (b)) and ignores the existence of regulated facilities.
- Road-based-Sewer-reconstruction-with-Controls (RSC) which uses the reconstructed sewer network from RSN and further incorporates regulated facilities at corresponding locations.
- Road-Drainage Approximation (RDA, Xing et al. (2021); Li et al. (2023)) (Xing et al., 2021; Li et al., 2023) which subtracts the mass at a uniform rate i_d from the roadway zone buffered from road centerlines using widths evaluated by The Design of Urban Road Engineering (CJJ 37—2012).

- No-Drainage Approximation (NDA) which ignores the drainage effects of the sewer network.

According to whether a sewer hydraulic module is reconstructed for simulation with AUTOSHED, we can further classify the above approximation methods into two categories: physical approaches (including FSR, FSN~~and RSN~~), RSN and RSC, and equifinal ones (including RDA and NDA), meaning similar flood simulation results can be achieved by different methods with appropriate parameters of drainage effects (Dobson et al., 2025).

4 Performance Analysis: From Graph Reconstruction to Urban Flood Simulation

4.1 Sewer network reconstruction performance

According to the layout of the digitized sewer network (Fig. 4(a)), gravitational flow directions are initialized by surface elevation (Eq. 7) and then estimated by solving 0-1 programming problems (Eq. 8). For simplicity, Fig. 6 summarizes the corresponding results for the initialized and reconstructed directions of the complete sewer network with 11 outfall points consisting of wastewater treatment plants and pumping stations. The directions of 359 in 908 pipes are reversed to satisfy the topological constraints. The majority of modified pipes are located in the southern part of the study area and exhibit a pattern of cyclic structures over a relatively flat areas, posing challenges on the direct identification of dominant flow directions and thus necessitating the incorporation of additional topological constraints (Eq. 8b-Eq. 8h) for rational reconstruction.

According to reconstructed flow directions, nodal invert elevation is further derived from values initialized by a constant cover depth (Eq. 6) and the slope distributions before / after adjustment are summarized in Fig. 6. The initial slopes of both complete and simplified sewer network exhibit a relatively symmetric distribution centered on 0, indicating adverse slopes in nearly half a number of links due to nearly reversed 40% pipes in the previous step. After reconstruction using Eq. 9, slope distributions are shifted into strictly positive ones where the majority of slopes are around 0.001. Additionally, the simplified sewer network shares a similar pattern in the slope distribution with the complete one except for minor increases around 0 because its layout is slightly modified due to aforementioned reconnection of broken pipes in Sect. 3.3. Thus, it can be concluded that the proposed reconstruction approach is robust to empirical simplification of the sewer network layout following road networks and can be stably extended to cases using street-based network generation.

Owing to linearized programming formulation used in the process of gravitational flow directions and nodal invert elevation reconstruction (Sect. 2.4), 1D sewer hydraulic models can be built from prepared geographical datasets in ~~a few minutes, resulting in 8242 links and 8131 inlets~~ (33 seconds on a local desktop using a single core of Intel(R) Core(TM) i7-14700KF CPU and 400 MB RAM occupancy. According to reconstructed sewer networks initialized with a uniform spacing of 50 m ~~;(cf. Sect. 2.2)in~~, FSR/FSN and RSN/RSC models have 8242 links and 8131 inlets, 5268 links and 5188 inlets~~in RSN, respectively~~. Furthermore, the entire study area is discretized into 7222150 TSUs with a median area of 18.2 m² for surface runoff generation and routing computation.

Table 2. Calibrated parameters of the AUTOSHED model.

Land use type	Impervious ratio [m ² /m ²]	Manning coefficient [s/m ^{1/3}]
tree	0.05	0.06
grassland	0.05	0.08
cropland	0.05	0.08
built-up	1.0	0.015
bareland	0.4	0.04
water	1.0	0.02

4.2 Model calibration and evaluation

To facilitate the comparison of pluvial flood simulation performance using different approaches, we first calibrate the model parameters with a severe storm hitting CYC on 11 July 2022 (denoted as the 20220711 storm). This storm brings an average total rainfall of 57.8 mm and a peak intensity of 44.5 mm/h, resulting in 31 inundated points reported by the local government, of which 18 are recorded with corresponding maximum waterlogging depth. Considering its representativeness as disastrous torrential events and data availability, we use the information of recorded maximum waterlogging depth to calibrate the ~~parameters~~ parameters in the aforementioned model and related approximation approaches for the sewer drainage effect.

For AUTOSHED, the main physical parameters include the empirical impervious ratio α_{imp} and the Manning coefficient n estimated from ~~the types of land use~~ land use types. Considering the dominance of the built-up area and attempts to avoid possible parameter equifinality between physical process such as soil infiltration and sewer drainage, we perform simple tests of model performance using recommended empirical values of corresponding parameters from the ~~Technical~~ Technical Specification for Construction and Application of Mathematical Model of Urban Flooding Prevention and Control System (DB11/T 2074-2022) and finalize the values of parameters in Table. 2 without exhaustive search. Fig. 8 shows the inundation map simulated by AUTOSHED with the sewer hydraulic module reconstructed from the FSR approach under the 20220711 storm.

The coefficient of determination (R^2) is used to quantify the overall performance of the models using different parameters:

$$R^2 = 1 - \frac{\sum_{i=1}^N (\hat{h}_i - h_i)^2}{\sum_{i=1}^N (h_i - \mu_h)^2} \quad (17)$$

where $N = 18$ is the number of inundated points with known maximum depth, $\hat{h}_i$ and h_i are the maximum depth simulated and observed, μ_h is the mean of the observed maximum depth.

According to Fig. 9 (a), the FSR approach achieves an R^2 of 0.95, which indicates good agreement between the simulated and observed values and thus consolidates the physical background for further comparison. In addition, we further examine the performance of the FSR approach with varying inlet spacings (denoted as ILS) from 30 m to 100 m. According to Fig. 9 (b), the FSR approach demonstrates relatively robust performance with R^2 ranging from 0.85 to 0.95 where ILS of 50 m achieves

370 the highest NSE. It is worth noting that increasing ILS leads to both underestimation and overestimation, such as P5 and P2 in Fig. 9 (b), highlighting the dual role of rainwater inlets in either alleviating surface inundation through drainage or contributing to it when overloaded.

Based on calibrated parameters of the physical model, we further use the grid search strategy to optimize the most possible equivalent drainage rate i_d used in the RDA method when detailed sewer network information is unavailable. Specifically, we
375 set the possible range of i_d according to the local design drainage standard and perform simulations with $i_d = 2.5, 5.0, 7.5, 10.0, 12.5, 15.0$ mm/h. According to Fig. 9 (bc), $i_d = 2.5$ mm/h achieves the highest R^2 and thus selected as the final value of drainage rate for further scenario analysis.

4.3 Extreme rainfall analysis: both local inlets and global regulation matter

After calibrating the AUTOSHED model integrated with reconstructed sewer hydraulic modules, we now delve deeper into
380 understanding how the proposed graph reconstruction-based approach performs compared to simplified alternatives across different rainfall scenarios and varying levels of available information. The aforementioned 20220711 storm event, with an average total rainfall exceeding the 500-year return period threshold (40.8 mm), highlights its extremity in an arid region. According to Fig. 9, when information on regulated facilities and detailed layouts is unavailable, simplified physical approaches, such as FSN, RSC and RSN, exhibit relatively lower accuracy than calibrated equifinal ones, which approximate limited
385 drainage capacities during extreme rainfall using a small equivalent drainage rate.

Considering physical approaches incorporate drainage effects at rainwater inlets, we further investigate the relationship between simulation error in maximum inundation depth and the distances to the nearest inlets, denoted as D_f for the complete sewer network and D_s for the simplified one (see Sect. 3.3), respectively. As illustrated in Fig. 10, simulation error variability decreases as D_f and D_s increase, with the maximum absolute value of deviations remaining less than 5 cm for distances
390 exceeding 30 m, where local microtopography predominantly influences the inundation. Furthermore, NDA can underestimate the maximum inundation depths at points such as P8 and P18, suggesting the occurrence of potential overflows surrounding nearby rainwater inlets due to insufficient drainage capacity under extreme rainfall.

To assess differences in simulated sewer drainage performance, we further summarize accumulated discharges at rainwater inlets and conduct two steps of comparisons according to available information.

395 – **Effects of neglecting regulation:** when neglecting the information of regulated facilities, FSN ~~significantly underestimates maximum inundation depths~~ can significantly underestimate the maximum inundation depth at points such as P2 ~~and P9 in Fig. 10,~~ compared to FSR(Fig. 10)-. This mainly results from overestimated inflows ($\Delta \sum Q_{1D-2D} > 0$) at surrounding inlets, as seen at P2 in Fig. 11 (a) and (e). ~~However, FSN also overestimates~~ Similar phenomenon of overestimation can also be observed when comparing RSN with RSC whereas with greatly decreased magnitude since road-based simplification reduces the rainwater collected into the sewer system and thus alleviates the drainage burden. However,
400 when regulated facilities are deleted, FSN can also overestimate the maximum inundation depths at certain points such as P1 and P3 (Fig. 10), which may seem counterintuitive. Analysis of P1's nearby inlets reveals lower inflows using

FSN, compared to FSR, particularly at IL1 (Fig. 11 (b) and (f)), causing model overestimation of surrounding maximum inundation depth. After tracking accumulated discharges at downstream inlets with respect to IL1, we further locate the drainage bottleneck at one pump station PM1. As illustrated in Fig. 11 (d), its removal can significantly increase inflows at upstream inlets, further ~~raising~~increasing water heads at adjacent sewer nodes and consequently reducing upstream inlet drainage capacities due to backwater effects.

- **Impact of network simplification:** when approximating the sewer layout through major roads, RSN generally overestimates the maximum water depths at inundated points within 30 m of rainwater inlets compared to FSN (Fig. 10), driven by intensified overflows from excessive surface water flowing through a single drainage pathway, as seen at P1 in Fig. 12 (a) and (c). However, some inundated points like P13 and P18, where surrounding inlets are removed, may also exhibit underestimated maximum water depths. This occurs because these inlets initially contribute to surface overflows in FSN-based simulations, as evidenced by the underestimation of maximum water depth in Fig. 10 when NDA is adopted. In particular, we can also observe the overestimation of maximum water depths at certain flood points without removing local inlets during simplification, such as P2 and P4 with $\Delta D = 0$ in Fig. 10. Examining the simulated total discharges at rainwater inlets near P2 (Fig. 12 (b) and (d)) reveals that increased local inflows are outweighed by amplified upstream overflows, thus exacerbating downstream inundation conditions.

In summary, while physical approaches simplified through major roads can yield a similar pipe slope distribution (Sect. 4.1), achieving accurate simulation of maximum inundation depths still requires the proper configuration of regulated facilities and drainage pathways. Otherwise, equifinal methods, flexible in parameter calibration, can offer better performance, especially when observational data are available.

4.4 Design rainfall analysis: physical approaches outperform but require more complete information

In order to assess whether equifinal approaches always exhibit comparable or even better performance with physical counterparts, we further conduct design rainfall scenario analysis. The Probability of Detection (POD), False Alarm Rate (FAR), Critical Success Index (CSI) and Bias (BIAS) are selected to evaluate the model performance in inundation area simulations (McGrath et al. (2018))(McGrath et al., 2018), using results from the FSR approach as the reference:

$$\text{POD} = \frac{\text{TP}}{\text{TP} + \text{FN}} \quad (18)$$

$$\text{FAR} = \frac{\text{FP}}{\text{TP} + \text{FP}} \quad (19)$$

$$\text{CSI} = \frac{\text{TP}}{\text{TP} + \text{FN} + \text{FP}} \quad (20)$$

$$430 \quad \text{BIAS} = \frac{\text{TP} + \text{FP}}{\text{TP} + \text{FN}} \quad (21)$$

where TP (True Positive) represents areas correctly identified as inundated, FN (False Negative) represents areas incorrectly classified as not inundated, and FP (False Positive) represents areas incorrectly classified as inundated, with FSR used as the reference. An area is considered inundated when its maximum depth exceeds 15 cm per local regulations.

In terms of detecting potential inundated areas, all approaches show only minor variations with high POD values ranging
 435 between 0.85 and 0.95. The NDA and RDA approaches even slightly outperform FSN, RSC and RSN under extreme rainfall conditions, aligning with previous results in Sect. 4.3. As rainfall return periods decrease, FAR values of the RSC, RSN, NDA and RDA approaches gradually increase, with the latter two showing much more significant variations. This indicates that the performance of the equivalent drainage rate i_d calibrated by a single event still has a high uncertainty when applied to ~~varying rainfall scenarios~~ rainfall scenarios with varying intensities. Therefore, while the ~~difference~~ differences in PODs are minimal,
 440 dramatically higher FARs of equifinal approaches widen the overall performance gap, as measured by CSI, especially for rainfall events with return periods below 50 years. Regarding BIAS, physical approaches that adopt virtual-reconstructed networks but without controls ~~consistently underestimate~~ exhibit a consistent underestimation of the total inundated area ~~, leading to with~~ BIAS values less than 1. In contrast, other equifinal approaches tend to overestimate the inundated area. Specifically, RDA and NDA can overestimate the total inundated area by more than 8% and 10% for rainfall events with return periods less than 100
 445 years, respectively. Thus, a constant equivalent drainage rate is insufficient to achieve an accurate simulation of sewer drainage effects under diverse rainfall conditions, while physical approaches can also yield biased estimation of the inundated area if regulated facilities are not properly configured.

From the perspective of water balance, total inundated areas (or volumes) are closely related to the volume of rainwater drained outside the system. Thus, we further compare the ~~simulated~~ discharge processes at ~~outflow points using outfalls~~
 450 simulated by different physical approaches (Fig. 14). Being the solution reconstructed from the most detailed information, FSR clearly ~~demonstrates~~ reveals the insufficient drainage capacities at most ~~outflow points~~ outfalls, such as OF1. When regulated facilities are excluded but sewer layout remains unchanged, FSN ~~yields~~ demonstrates significantly higher discharges, especially at major outflow points such as OF2 and OF3 with peak flows over 300% higher, thereby leading to an underestimation of total inundated areas ~~. When (Fig. 13). When the~~ sewer layout is further simplified ~~through by the~~ major roads, the simulated outflows ~~generally decrease by~~ decrease by approximately 27% due to ~~less rainwater entering~~ reduced inlets that collect
 455 rainwater into the sewer system. This attribution can be further supported by the improved alignment of outflow hydrographs between RSN and RSC, which exhibit fewer truncations during peak flows under regulated conditions when compared to FSR and FSN. This indicates an alleviation of drainage deficiency due to reduced rainwater inflow. However, certain outflow points, such as ~~OF2, still show substantially increased discharges. Comparing the~~ OF3, still yield substantially higher discharges with
 460 simplified road networks. Comparison of layouts used in FSN and RSN reveals that a ~~major main~~ major main pipe, measuring 6.8 m × 2.6 m (near OF1 and OF8, cf. Fig. 15) is found to be removed during simplification, blocking the drainage pathway that divides the corresponding upstream rainwater to the northern outflow points such as OF1 and OF8, eventually magnifying the inflow

to OF3. Thus, for real urban environments with complicated sewer layouts due to practical factors such as multistage construction, direct geometric simplification through major roads may remove some critical connectivity inside a graph-like drainage system and thus fail to accurately represent the drainage effects of the sewer network due to topological incompleteness.

4.5 Outlook and limitation

The proposed graph reconstruction-based approach offers an efficient solution for generating physical sewer models using available data on sewer layouts and surface elevation, which can be obtained from local surveys (Xing et al., 2022), engineering drawings (Lyu et al., 2018), or open source software such as SWMManywhere (Dobson et al., 2025). Given the significant influence of network topology and regulation facilities on inundation simulation results (as discussed in Sect. 4.3 and 4.4), in addition to the aforementioned data sources, it is imperative to further implement intelligent surveying systems targeting relevant critical components such as inlets and outfalls. These data can then be integrated with the proposed reconstruction algorithm to achieve more reliable pluvial flood modeling. In particular, outfall identification still remains a difficult task, especially for decentralized sewer networks in relatively flat urban areas, challenging the applicability of existing topography-driven approaches (Dobson et al., 2025) and motivating the need for user-defined configurations according to prior knowledge of the area (Reyes-Silva et al., 2023). In addition, it should be acknowledged that considering inherent quality issues of multi-source geographical datasets, mathematical programming procedures in the proposed approach may occasionally fail because of infeasible configurations such as over-elevated outfalls and dangling pipelines. While introducing data cleaning procedures may help alleviate such issues and streamline the downstream reconstruction process, it also necessitates the trade-off between algorithm robustness and accuracy owing to embedded assumptions during quality control, which deserves further investigations. In addition to related cleaning functions implemented in existing packages like SWMManywhere (Dobson et al., 2025), we propose leveraging the built-in functionality of irreducible inconsistent subset (IIS) computation within our optimization-based framework, which can be steadily accessed in solvers such as Gurobi (<https://docs.gurobi.com/projects/optimizer>). This tool can help identify the specific constraints responsible for infeasibility and thus support the spatial pinpointing of ill-conditioned sewer elements that over-constrain the optimization and may require further correction or elimination. In summary, additional integration with other existing tools will further enhance the practicality of the proposed reconstruction method and facilitate a more realistic representation of drainage effects in urban pluvial flood simulation.

5 Conclusions

In this work, we present a graph reconstruction-based approach for building a physical sewer hydraulic model, leveraging incomplete information and surface elevation model while adhering to design guidelines. In contrast to conventional optimal-design-based approaches, our approach seeks to reconstruct the most possible sewer network with related hydraulic properties, such as gravitational flow direction and nodal invert elevation, constrained by minimal deviation from the initial status based on available information. The resulting mathematical programming problems can be equivalently transformed into corresponding linearized formulations, ensuring their computational efficiency for large-scale applications. We apply the proposed approach

495 to Yinchuan’s main city zone, characterized by multiple outfalls consisting of wastewater treatment plants and pump stations, yielding the following key insights:

- The reconstructed sewer hydraulic module integrated into a 1D/2D coupled hydrologic-hydrodynamic model achieves high accuracy in simulating maximum inundation depths, with an R^2 of 0.95. A comparison with road-based layout simplifications further demonstrates the robustness of our approach in reconstructing sewer hydraulic properties, as the
500 simplified model maintains a similar distribution of pipe slopes.
- While equifinal approaches ease parameter calibration by encapsulating complex sewer drainage processes into equivalent drainage rates, the proposed reconstruction approach can reliably achieve superior performance in simulating inundated areas across various rainfall scenarios. This improvement stems from its physically grounded structure in simulating bidirectional interaction between the ground surface and the sewer system, indicating that physical reconstruction is
505 preferable to approximate sewer drainage effects in operational applications.
- The completeness of available information has non-negligible effects on the simulated hydraulic performance of reconstructed sewer networks. Simplifications involving road-based layouts and regulation facility removal lead to complex deviation patterns in local maximum inundation depths and outflow hydrographs, with both overestimations and underestimations arising from the combined effects of surface microtopography, sewer connectivity modification and regulation
510 facility operation.

In conclusion, we provide an efficient sewer reconstruction approach that improves the simulation and understanding of sewer drainage effects during urban pluvial floods, accounting for varying levels of information completeness. However, uncertainties persist in reconstructed physical models when detailed information on regulated facilities and drainage pathways is lacking. Thus, future research will focus on integrating advanced techniques, such as data assimilation [and intelligent surveying](#)
515 [system](#), with reconstructed physical models to augment the realism of sewer drainage process representation.

Code and data availability. Landuse (<https://worldcover2021.esa.int/download>). DEM and sewer network information are not publicly available due to the privacy reasons. The [snapshot of the source code and compiled application](#) for ~~end-to-end~~ sewer reconstruction ~~will be open~~
~~onee has been archived on Zenodo~~ (<https://doi.org/10.5281/zenodo.15522608>). And the ~~manuscript up-to-date version~~ is ~~aecepted~~ [available at: https://github.com/LIIC-mmmd/ASHED_sewerReconstruction](#).

520 **Appendix A: Slope estimation using multiple points**

Given a path consisting of K points $p = \{v_1, \dots, v_K\}$ with corresponding elevation values $z = \{z_1, \dots, z_K\}$, its slope can be derived from the estimated coefficient of ordinary least squares regression through the coordinates (v_r, z_r) :

$$i_p = \frac{\sum_{r=1}^K (d_r - \mu_d)(z_i - \mu_z)}{\sum_{r=1}^K (d_r - \mu_d)^2} = \frac{\sum_{r=1}^K d_r z_r - K \mu_d \mu_z}{\sum_{i=1}^K d_r^2 - K \mu_d^2} \quad (\text{A1})$$

where d_r is the distance from v_1 to v_r along the path ($d_1 = 0$), μ_d and μ_z is the mean value of $\{d_r\}_{r=1,\dots,K}$ and $\{z_r\}_{r=1,\dots,K}$.

Eq. A1 can re-written by using z_r as pivot variables:

$$\begin{aligned} i_p &= \frac{\sum_{r=1}^K d_r z_r - K \mu_d \mu_z}{\sum_{i=1}^K d_r^2 - K \mu_d^2} \\ &= \frac{K \sum_{r=1}^K d_r z_r - (\sum_{r=1}^K d_r) \cdot (\sum_{r=1}^K z_r)}{K \sum_{r=1}^K d_r^2 - (\sum_{r=1}^K d_r)^2} \\ &= \sum_{k=1}^K \frac{\left(K d_k - \sum_{r=1}^K d_r \right)}{K \sum_{r=1}^K d_r^2 - \left(\sum_{r=1}^K d_r \right)^2} z_k \end{aligned} \quad (\text{A2})$$

Thus, i_p can be expressed as a linear combination of z_r . When $K = 2$, i.e., only two points are involved in the slope estimation, we can simplify Eq. A2 into Eq. A3:

$$i_p = -\frac{1}{d_2} z_1 + \frac{1}{d_2} z_2 \quad (\text{A3})$$

Appendix B: Bidirectional surface-sewer flow coupling scheme

In AUTOSHED, the surface flow and sewer flow are bidirectionally linked via the mass source term Q_{1D-2D} which can be parameterized as follows (Buttinger-Kreuzhuber et al., 2022):

$$Q_{1D-2D}^* = \begin{cases} \frac{2}{3} c_w P \sqrt{2g} h_{2D}^{1.5}, & H_{1D} < z_{bc} \\ c_{o,s} A \sqrt{2g} [h_{2D} - (H_{1D} - z_{bc})]^{0.5}, & z_{bc} \leq H_{1D} < z_{bc} + h_{2D} - A/P \\ c_{w,s} P \sqrt{2g} h_{2D} [h_{2D} - (H_{1D} - z_{bc})]^{0.5}, & z_{bc} + h_{2D} - A/P \leq H_{1D} < z_{bc} + h_{2D} \\ -c_{w,s} P \sqrt{2g} h_{2D} [(H_{1D} - z_{bc}) - h_{2D}]^{0.5}, & z_{bc} + h_{2D} \leq H_{1D} < z_{bc} + h_{2D} + A/P \\ -c_{o,s} A \sqrt{2g} [(H_{1D} - z_{bc}) - h_{2D}]^{0.5}, & H_{1D} \geq z_{bc} + h_{2D} + A/P \end{cases} \quad (\text{B1})$$

Here we assume Q_{1D-2D}^* is positive when water flows from the TSU to the linked inlet. H_{1D} , h_{2D} and z_{bc} are the total hydraulic head at the inlet, the water depth at the TSU and the center bed elevation at the TSU, respectively; A and P are the inlet's area and perimeter, respectively; c_w , $c_{w,s}$ and $c_{o,s}$ are discharge coefficients for the free weir, the submerged weir, and the orifice equations, respectively. By default, AUTOSHED sets $c_w = 0.56$, $c_{w,s} = 0.11$ and $c_{o,s} = 0.2$ (Rubinato et al., 2017).

and $A = 0.3375 \text{ m}^2$, $P = 2.4 \text{ m}$ assuming that each inlet is rectangular whose size is $0.45 \text{ m} \times 0.75 \text{ m}$ according to field investigation.

540 After examining the links between TSUs and inlets, we find that each TSU is linked with at most one inlet and thus have:

$$q_{sd} = \frac{Q_{1D-2D}}{A_T} \quad (B2)$$

where A_T is the total area of the TSU, and Q_{1D-2D} is the sewer drainage rate at the inlet derived from Eq. B1 and further constrained by the water availability of both the TSU and the inlet (Buttinger-Kreuzhuber et al., 2022):

$$Q_{1D-2D} = \begin{cases} \min\left(\frac{h_{2D}A_T}{\Delta t}, Q_{1D-2D}^*\right), & H_{1D} < z_{bc} + h_{2D} \\ \max\left(-\frac{V_{as}}{\Delta t}, Q_{1D-2D}^*\right), & H_{1D} \geq z_{bc} + h_{2D} \end{cases} \quad (B3)$$

545 where V_{as} is the water volume at the inlet assembly determined by A_{as} and H_{1D} ; Δt is the coupling time step evaluated as the minimum value between the timesteps of the 1D and 2D solvers (Chen et al., 2018).

Notably, Eq. B2 and Eq. B3 can ensure strict mass balance during surface-sewer flow coupling since it is straightforward to prove:

- The total exchange mass is the same between the surface and sewer network

$$550 \quad q_{sd}A_T\Delta t = Q_{1D-2D}\Delta t \quad (B4)$$

- The total exchange mass does not exceed the available water in the surface when water flows from the TSU to the inlet, i.e., $H_{1D} < z_{bc} + h_{2D}$,

$$Q_{1D-2D}\Delta t = \min(h_{2D}A_T, Q_{1D-2D}^*) \leq h_{2D}A_T \quad (B5)$$

- The total exchange mass does not exceed the available water in the sewer network when water flows from the inlet to the TSU, i.e., $H_{1D} \geq z_{bc} + h_{2D}$,

$$555 \quad Q_{1D-2D}\Delta t = \max(-V_{as}, Q_{1D-2D}^*) \geq -V_{as} \quad (B6)$$

In order to jointly solve surface-sewer flow equations coupled with Eq. B2, AUTOSHED utilizes the 1D routing portion of the Storm Water Management Model (SWMM) 5.1.015 (Rossman, 2015) and implements communication routines for 1D/2D state variables such as water depth and hydraulic head (Eq. B1) via interface functions by compiling SWMM as a dynamic link library (Leandro and Martins, 2016).

560

In addition to unregulated nodes and links, we also account for the controlling effects of pump stations and wastewater treatment plants using Type 4 pumps (whose flow rate changes linearly with the inlet node depth until the maximum pumping capacity is reached) and nodes with limited maximum inflows in SWMM, respectively (Rossman, 2015).

Author contributions. RL conceived the idea and implement the algorithm. JL and JS collected the data. RL, TS, JL, FT, and GN conducted
565 the analysis. RL drafted the manuscript and all authors reviewed and edited the manuscript.

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570 References

- Bakhshipour, A. E., Bakhshizadeh, M., Dittmer, U., Haghighi, A., and Nowak, W.: Hanging Gardens Algorithm to Generate Decentralized Layouts for the Optimization of Urban Drainage Systems, *Journal of Water Resources Planning and Management*, 145, 04019034, [https://doi.org/10.1061/\(ASCE\)WR.1943-5452.0001103](https://doi.org/10.1061/(ASCE)WR.1943-5452.0001103), 2019.
- Bakhshipour, A. E., Hespen, J., Haghighi, A., Dittmer, U., and Nowak, W.: Integrating Structural Resilience in the Design of Urban Drainage
575 Networks in Flat Areas Using a Simplified Multi-Objective Optimization Framework, *Water*, 13, <https://doi.org/10.3390/w13030269>, 2021.
- Begnudelli, L. and Sanders, B. F.: Unstructured Grid Finite-Volume Algorithm for Shallow-Water Flow and Scalar Transport with Wetting and Drying, *Journal of Hydraulic Engineering*, 132, 371–384, [https://doi.org/10.1061/\(ASCE\)0733-9429\(2006\)132:4\(371\)](https://doi.org/10.1061/(ASCE)0733-9429(2006)132:4(371)), 2006.
- Blumensaat, F., Wolfram, M., and Krebs, P.: Sewer model development under minimum data requirements, *Environmental Earth Sciences*,
580 65, 1427–1437, <https://doi.org/10.1007/s12665-011-1146-1>, 2012.
- Buttinger-Kreuzhuber, A., Konev, A., Horváth, Z., Cornel, D., Schwerdorf, I., Blöschl, G., and Waser, J.: An integrated GPU-accelerated modeling framework for high-resolution simulations of rural and urban flash floods, *Environmental Modelling & Software*, 156, 105480, <https://doi.org/https://doi.org/10.1016/j.envsoft.2022.105480>, 2022.
- Cao, X., Lyu, H., Ni, G., Tian, F., Ma, Y., and Grimmond, C.: Spatial Scale Effect of Surface Routing and Its Parameter Upscaling for Urban Flood Simulation Using a Grid-Based Model, *Water Resources Research*, 56, e2019WR025468, <https://doi.org/https://doi.org/10.1029/2019WR025468>, e2019WR025468 2019WR025468, 2020.
- 585 Chegini, T. and Li, H.-Y.: An algorithm for deriving the topology of belowground urban stormwater networks, *Hydrology and Earth System Sciences*, 26, 4279–4300, <https://doi.org/10.5194/hess-26-4279-2022>, 2022.
- Chen, W., Huang, G., Zhang, H., and Wang, W.: Urban inundation response to rainstorm patterns with a coupled hydrodynamic model: A case study in Haidian Island, China, *Journal of Hydrology*, 564, 1022–1035, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2018.07.069>,
590 2018.
- Chen, Z. and Huang, G.: Numerical simulation study on the effect of underground drainage pipe network in typical urban flood, *Journal of Hydrology*, 638, 131481, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2024.131481>, 2024.
- Dai, S., Hou, J., Jin, S., Zhang, K., Hou, J., and Liu, G.: Discharge coefficients formulae of grate inlets of complicated conditions for urban floods simulation and urban drainage systems design, *Journal of Hydrology*, 625, 130089, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2023.130089>, 2023.
- 595 Dobson, B., Jovanovic, T., Alonso-Álvarez, D., and Chegini, T.: SWMManywhere: A workflow for generation and sensitivity analysis of synthetic urban drainage models, anywhere, *Environmental Modelling & Software*, 186, 106358, <https://doi.org/https://doi.org/10.1016/j.envsoft.2025.106358>, 2025.
- 600 Dunton, A. and Gardoni, P.: Generating network representations of small-scale infrastructure using generally available data, *Computer-Aided Civil and Infrastructure Engineering*, 39, 1143–1158, <https://doi.org/https://doi.org/10.1111/mice.13137>, 2024.
- Duque, N., Duque, D., and Saldarriaga, J.: A new methodology for the optimal design of series of pipes in sewer systems, *Journal of Hydroinformatics*, 18, 757–772, <https://doi.org/10.2166/hydro.2016.105>, 2016.
- Duque, N., Bach, P. M., Scholten, L., Fappiano, F., and Maurer, M.: A Simplified Sanitary Sewer System Generator for Exploratory Modelling
605 at City-Scale, *Water Research*, 209, 117903, <https://doi.org/https://doi.org/10.1016/j.watres.2021.117903>, 2022.

- Elimam, A. A., Charalambous, C., and Ghobrial, F. H.: Optimum Design of Large Sewer Networks, *Journal of Environmental Engineering*, 115, 1171–1190, [https://doi.org/10.1061/\(ASCE\)0733-9372\(1989\)115:6\(1171\)](https://doi.org/10.1061/(ASCE)0733-9372(1989)115:6(1171)), 1989.
- Forrest, J. and Lougee-Heimer, R.: CBC User Guide, chap. Chapter 10, pp. 257–277, INFORMS, <https://doi.org/https://doi.org/10.1287/educ.1053.0020>, 2005.
- 610 Giangrande, S. E., McGraw, R., and Lei, L.: An Application of Linear Programming to Polarimetric Radar Differential Phase Processing, *Journal of Atmospheric and Oceanic Technology*, 30, 1716 – 1729, <https://doi.org/10.1175/JTECH-D-12-00147.1>, 2013.
- Hall, J.: Direct Rainfall Flood Modelling: The Good, the Bad and the Ugly, *Australasian Journal of Water Resources*, 19, 74–85, <https://doi.org/10.7158/13241583.2015.11465458>, 2015.
- Hesarkazzazi, S., Hajibabaei, M., Bakhshipour, A. E., Dittmer, U., Haghighi, A., and Sitzenfrei, R.: Generation of optimal (de)centralized
615 layouts for urban drainage systems: A graph-theory-based combinatorial multi-objective optimization framework, *Sustainable Cities and Society*, 81, 103 827, <https://doi.org/https://doi.org/10.1016/j.scs.2022.103827>, 2022.
- Johnson, D. B.: Finding All the Elementary Circuits of a Directed Graph, *SIAM Journal on Computing*, 4, 77–84, <https://doi.org/https://doi.org/10.1137/0204007>, 1975.
- Järvi, L., Grimmond, C., and Christen, A.: The Surface Urban Energy and Water Balance Scheme (SUEWS): Evaluation in Los Angeles and
620 Vancouver, *Journal of Hydrology*, 411, 219–237, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2011.10.001>, 2011.
- Kim, S. E., Seo, Y., Hwang, J., Yoon, H., and Lee, J.: Connectivity-informed drainage network generation using deep convolution generative adversarial networks, *Scientific Reports*, 11, 1519, <https://doi.org/10.1038/s41598-020-80300-6>, 2021.
- Krebs, G., Kokkonen, T., Valtanen, M., Setälä, H., and Koivusalo, H.: Spatial resolution considerations for urban hydrological modelling, *Journal of Hydrology*, 512, 482–497, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2014.03.013>, 2014.
- 625 Lacasta, A., Morales-Hernández, M., Murillo, J., and García-Navarro, P.: An optimized GPU implementation of a 2D free surface simulation model on unstructured meshes, *Advances in Engineering Software*, 78, 1–15, <https://doi.org/https://doi.org/10.1016/j.advengsoft.2014.08.007>, 2014.
- Leandro, J. and Martins, R.: A methodology for linking 2D overland flow models with the sewer network model SWMM 5.1 based on dynamic link libraries, *Water Science and Technology*, 73, 3017–3026, <https://doi.org/10.2166/wst.2016.171>, 2016.
- 630 Li, D., Hou, J., Xia, J., Tong, Y., Yang, D., Zhang, D., and Gao, X.: An Efficient Method for Approximately Simulating Drainage Capability for Urban Flood, *Frontiers in Earth Science*, 8, <https://doi.org/10.3389/feart.2020.00159>, 2020.
- Li, D., Hou, J., Shen, R., Li, B., Tong, Y., and Wang, T.: Approximation method for the sewer drainage effect for urban flood modeling in areas without drainage-pipe data, *Frontiers in Environmental Science*, 11, <https://doi.org/https://doi.org/10.3389/fenvs.2023.1134985>, 2023.
- 635 Li, G. and Matthew, R. G. S.: New Approach for Optimization of Urban Drainage Systems, *Journal of Environmental Engineering*, 116, 927–944, [https://doi.org/10.1061/\(ASCE\)0733-9372\(1990\)116:5\(927\)](https://doi.org/10.1061/(ASCE)0733-9372(1990)116:5(927)), 1990.
- Liu, L., Sun, J., and Lin, B.: A large-scale waterlogging investigation in a megacity, *Natural Hazards*, 114, 1505–1524, <https://doi.org/https://doi.org/10.1007/s11069-022-05435-3>, 2022.
- Lu, Y., Zhai, G., and Zhou, S.: An integrated Bayesian networks and Geographic information system (BNs-GIS) ap-
640 proach for flood disaster risk assessment: A case study of Yinchuan, China, *Ecological Indicators*, 166, 112 322, <https://doi.org/https://doi.org/10.1016/j.ecolind.2024.112322>, 2024.

- Luan, G., Hou, J., Wang, T., Zhou, Q., Xu, L., Sun, J., and Wang, C.: Method for analyzing urban waterlogging mechanisms based on a 1D-2D water environment dynamic bidirectional coupling model, *Journal of Environmental Management*, 360, 121024, <https://doi.org/https://doi.org/10.1016/j.jenvman.2024.121024>, 2024.
- 645 Lyu, H., Ni, G., Cao, X., Ma, Y., and Tian, F.: Effect of Temporal Resolution of Rainfall on Simulation of Urban Flood Processes, *Water*, 10, <https://doi.org/https://doi.org/10.3390/w10070880>, 2018.
- Machine Hsie, M.-Y. W. and Huang, C. Y.: Optimal urban sewer layout design using Steiner tree problems, *Engineering Optimization*, 51, 1980–1996, <https://doi.org/10.1080/0305215X.2018.1560436>, 2019.
- McGrath, H., Bourgon, J.-F., Proulx-Bourque, J.-S., Nastev, M., and Abo El Ezz, A.: A comparison of simplified conceptual models for rapid
650 web-based flood inundation mapping, *Natural Hazards*, 93, 905–920, <https://doi.org/10.1007/s11069-018-3331-y>, 2018.
- Mitchell, S., OSullivan, M., and Dunning, I.: Pulp: a linear programming toolkit for python, The University of Auckland, Auckland, New Zealand, 65, 25, 2011.
- MOHURD: Standard for Design of Outdoor Wastewater Engineering, GB 50014-2021, Ministry of Housing and Urban-Rural Development of the People's Republic of China, Beijing, China, in Chinese, 2021.
- 655 Montalvo, C., Reyes-Silva, J., Sañudo, E., Cea, L., and Puertas, J.: Urban pluvial flood modelling in the absence of sewer drainage network data: A physics-based approach, *Journal of Hydrology*, 634, 131043, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2024.131043>, 2024.
- Ni, G.-H., Liu, Z.-Y., Lei, Z.-D., Yang, D.-W., and Wang, L.: Continuous Simulation of Water and Soil Erosion in a Small Watershed of the Loess Plateau with a Distributed Model, *Journal of Hydrologic Engineering*, 13, 392–399, [https://doi.org/https://doi.org/10.1061/\(ASCE\)1084-0699\(2008\)13:5\(392\)](https://doi.org/https://doi.org/10.1061/(ASCE)1084-0699(2008)13:5(392)), 2008.
- 660 Paton, K.: An algorithm for finding a fundamental set of cycles of a graph, *Commun. ACM*, 12, 514–518, <https://doi.org/10.1145/363219.363232>, 1969.
- Perrini, P., Cea, L., Chiaravalloti, F., Gabriele, S., Manfreda, S., Fiorentino, M., Gioia, A., and Iacobellis, V.: A Runoff-On-Grid Approach to Embed Hydrological Processes in Shallow Water Models, *Water Resources Research*, 60, e2023WR036421, <https://doi.org/https://doi.org/10.1029/2023WR036421>, e2023WR036421 2023WR036421, 2024.
- 665 Reyes-Silva, J. D., Novoa, D., Helm, B., and Krebs, P.: An Evaluation Framework for Urban Pluvial Flooding Based on Open-Access Data, *Water*, 15, <https://doi.org/https://doi.org/10.3390/w15010046>, 2023.
- Rosenzweig, B. R., McPhillips, L., Chang, H., Cheng, C., Welty, C., Matsler, M., Iwaniec, D., and Davidson, C. I.: Pluvial flood risk and opportunities for resilience, *WIREs Water*, 5, e1302, <https://doi.org/https://doi.org/10.1002/wat2.1302>, 2018.
- Rossman, L. A.: Storm Water Management Model User's Manual Version 5.1, U.S. Environmental Protection Agency, 2015.
- 670 Rossman, L. A. and Huber, W.: Storm Water Management Model Reference Manual Volume II – Hydraulics, US Environmental Protection Agency: Washington, DC, USA, 2, 190, 2017.
- Rubinato, M., Martins, R., Kesserwani, G., Leandro, J., Djordjević, S., and Shucksmith, J.: Experimental calibration and validation of sewer/surface flow exchange equations in steady and unsteady flow conditions, *Journal of Hydrology*, 552, 421–432, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2017.06.024>, 2017.
- 675 Safavi, H. and Geranmehr, M. A.: Optimization of sewer networks using the mixed-integer linear programming, *Urban Water Journal*, 14, 452–459, <https://doi.org/10.1080/1573062X.2016.1176222>, 2017.
- Schmitt, T. G. and Scheid, C.: Evaluation and communication of pluvial flood risks in urban areas, *WIREs Water*, 7, e1401, <https://doi.org/https://doi.org/10.1002/wat2.1401>, 2020.

- Schubert, J. E. and Sanders, B. F.: Building treatments for urban flood inundation models and implications for predictive skill and modeling efficiency, *Advances in Water Resources*, 41, 49–64, <https://doi.org/https://doi.org/10.1016/j.advwatres.2012.02.012>, 2012.
- Shi, X., Liu, Z., Carlos, V., and Jia, H.: The role of graph-based methods in urban drainage networks (UDNs): review and directions for future, *Urban Water Journal*, 20, 1095–1109, <https://doi.org/10.1080/1573062X.2023.2252807>, 2023.
- Sitzenfrei, R., Wang, Q., Kapelan, Z., and Savić, D.: Using Complex Network Analysis for Optimization of Water Distribution Networks, *Water Resources Research*, 56, e2020WR027929, <https://doi.org/https://doi.org/10.1029/2020WR027929>, e2020WR027929
2020WR027929, 2020.
- Song, L., Zhou, J., Guo, J., Zou, Q., and Liu, Y.: A robust well-balanced finite volume model for shallow water flows with wetting and drying over irregular terrain, *Advances in Water Resources*, 34, 915–932, <https://doi.org/https://doi.org/10.1016/j.advwatres.2011.04.017>, 2011.
- Swamee, P. K. and Sharma, A. K.: Optimal design of a sewer line using Linear Programming, *Applied Mathematical Modelling*, 37, 4430–4439, <https://doi.org/https://doi.org/10.1016/j.apm.2012.09.041>, 2013.
- Tran, V. N., Ivanov, V. Y., Huang, W., Murphy, K., Daneshvar, F., Bednar, J. H., Alexander, G. A., Kim, J., and Wright, D. B.: Connectivity in urban landscapes can cause unintended flood impacts from stormwater systems, *Nature Cities*, 1, 654–664, <https://doi.org/https://doi.org/10.1038/s44284-024-00116-7>, 2024.
- Wagner, H. M.: Linear Programming Techniques for Regression Analysis, *Journal of the American Statistical Association*, 54, 206–212, <https://doi.org/10.1080/01621459.1959.10501506>, 1959.
- Wang, J., Liu, J., Mei, C., Wang, H., and Lu, J.: A multi-objective optimization model for synergistic effect analysis of integrated green-gray-blue drainage system in urban inundation control, *Journal of Hydrology*, 609, 127 725, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2022.127725>, 2022.
- Wang, Q., Savić, D. A., and Kapelan, Z.: GALAXY: A new hybrid MOEA for the optimal design of Water Distribution Systems, *Water Resources Research*, 53, 1997–2015, <https://doi.org/https://doi.org/10.1002/2016WR019854>, 2017.
- Wang, S. and Wang, H.: Extending the Rational Method for assessing and developing sustainable urban drainage systems, *Water Research*, 144, 112–125, <https://doi.org/https://doi.org/10.1016/j.watres.2018.07.022>, 2018.
- Weng, Q.: Remote sensing of impervious surfaces in the urban areas: Requirements, methods, and trends, *Remote Sensing of Environment*, 117, 34–49, <https://doi.org/https://doi.org/10.1016/j.rse.2011.02.030>, remote Sensing of Urban Environments, 2012.
- Xing, Y., Liang, Q., Wang, G., Ming, X., and Xia, X.: City-scale hydrodynamic modelling of urban flash floods: the issues of scale and resolution, *Natural Hazards*, 96, 473–496, <https://doi.org/10.1007/s11069-018-3553-z>, 2019.
- Xing, Y., Shao, D., Yang, Y., Ma, X., and Zhang, S.: Influence and interactions of input factors in urban flood inundation modeling: An examination with variance-based global sensitivity analysis, *Journal of Hydrology*, 600, 126 524, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2021.126524>, 2021.
- Xing, Y., Shao, D., Liang, Q., Chen, H., Ma, X., and Ullah, I.: Investigation of the drainage loss effects with a street view based drainage calculation method in hydrodynamic modelling of pluvial floods in urbanized area, *Journal of Hydrology*, 605, 127 365, <https://doi.org/https://doi.org/10.1016/j.jhydrol.2021.127365>, 2022.
- Yu, X., Wu, Y., Meng, F., Zhou, X., Liu, S., Huang, Y., and Wu, X.: A review of graph and complex network theory in water distribution networks: Mathematical foundation, application and prospects, *Water Research*, 253, 121 238, <https://doi.org/https://doi.org/10.1016/j.watres.2024.121238>, 2024.
- Zanaga, D., Van De Kerchove, R., Daems, D., De Keersmaecker, W., Brockmann, C., Kirches, G., Wevers, J., Cartus, O., Santoro, M., Fritz, S., et al.: ESA WorldCover 10 m 2021 v200, <https://doi.org/https://doi.org/10.5281/zenodo.7254221>, 2022.

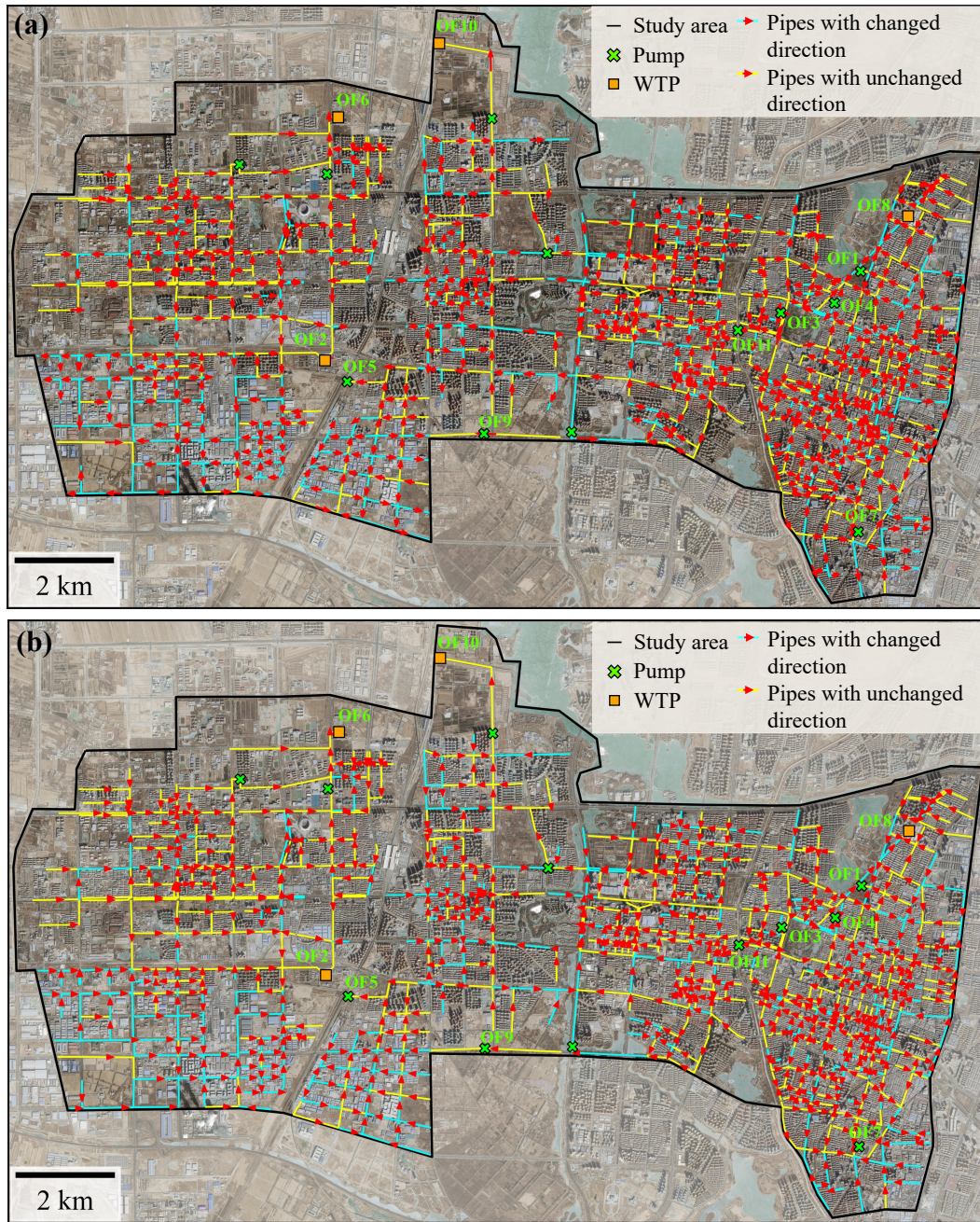


Figure 6. Comparison of initial and reconstructed gravitational flow directions of the complete sewer network in the study area. (a) Flow directions initialized by surface elevation. (b) Flow directions reconstructed from topological constraints. Basemaps are provided by derived from ESRI World Imagery (Credit: Esri, TomTom, Garmin, FAO, NOAA, USGS, © OpenStreetMap contributors, and the GIS User Community).

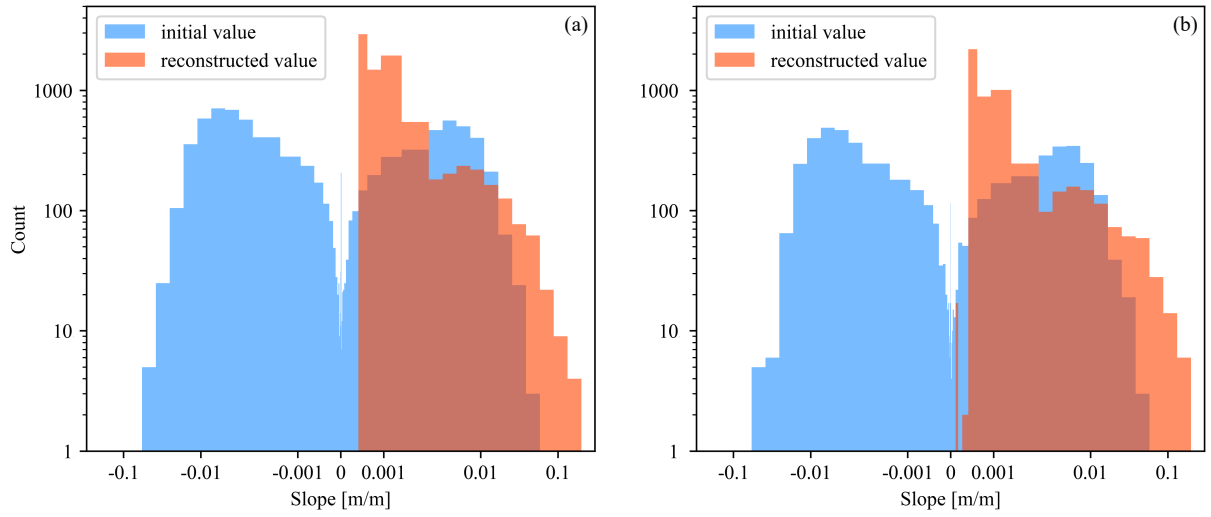


Figure 7. Comparison of initial and reconstructed sewer slope distributions. (a) Complete sewer network used in the FSR and FSN approaches. (b) Road-based sewer network used in the RSN and RSC approach.

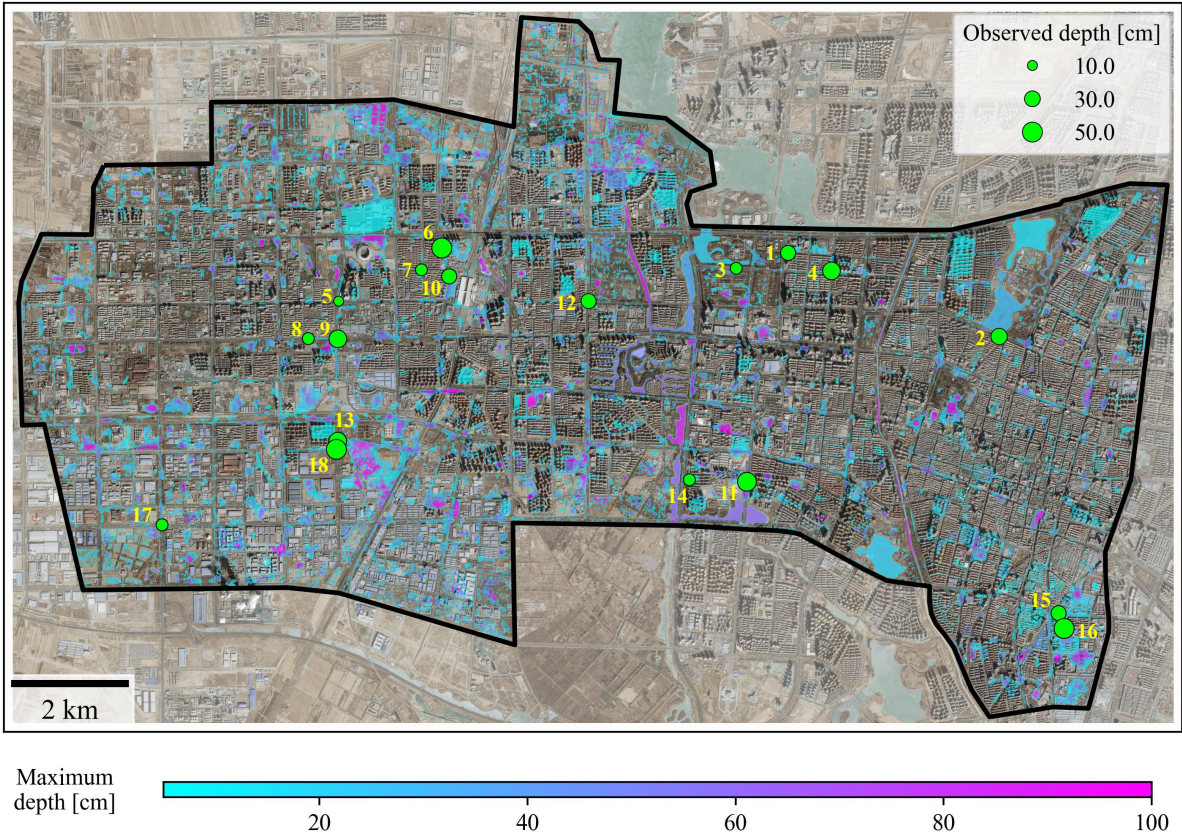


Figure 8. Maximum inundation depth map simulated by the FSR approach under the 20220711 storm. The basemap is provided by Basemaps are derived from ESRI World Imagery (Credit: Esri, TomTom, Garmin, FAO, NOAA, USGS, © OpenStreetMap contributors, and the GIS User Community).

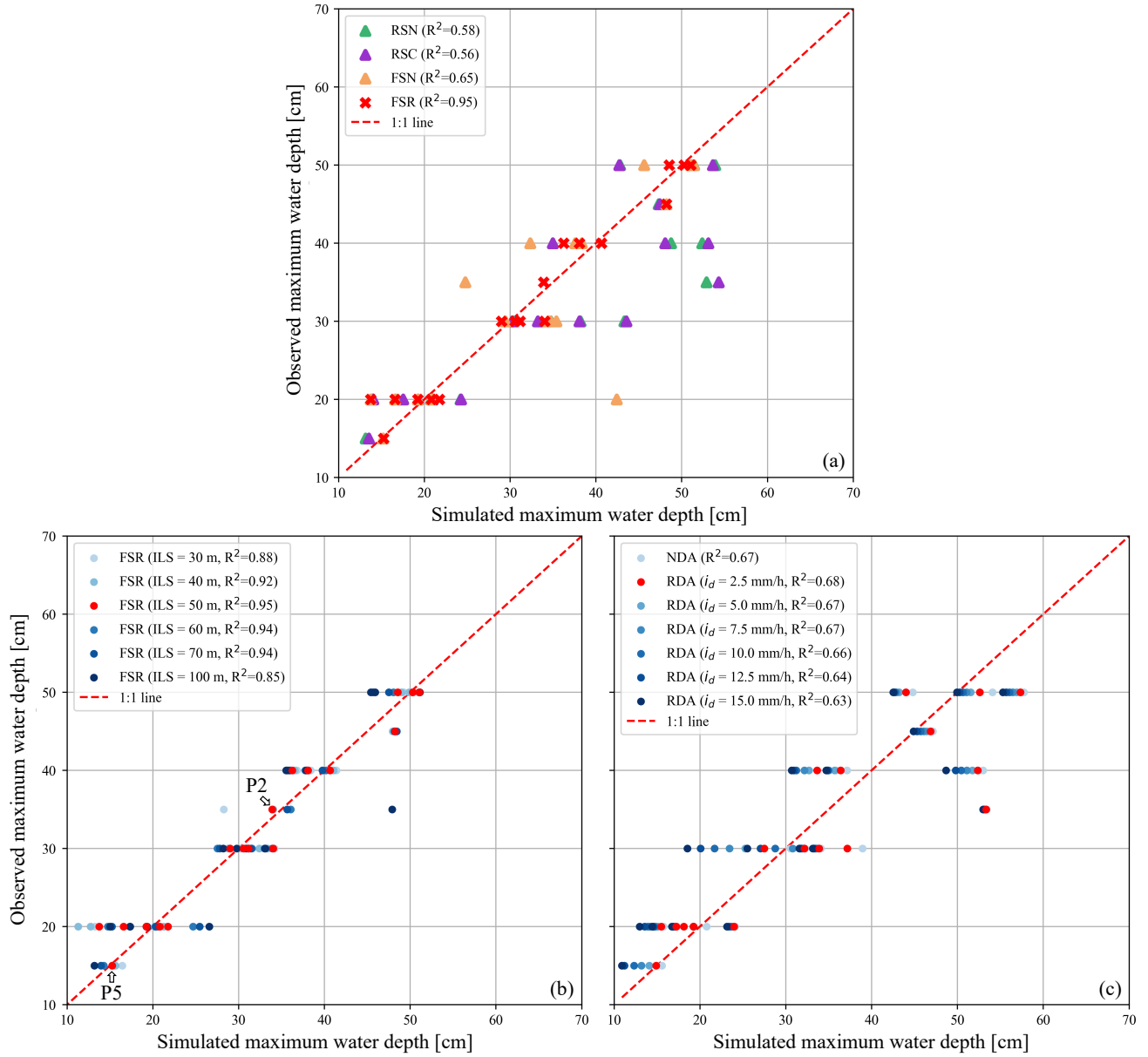


Figure 9. Simulation performance of the maximum inundation depth at inundated points using different approximation methods and parameters. The index of inundated points follow Fig. 8.

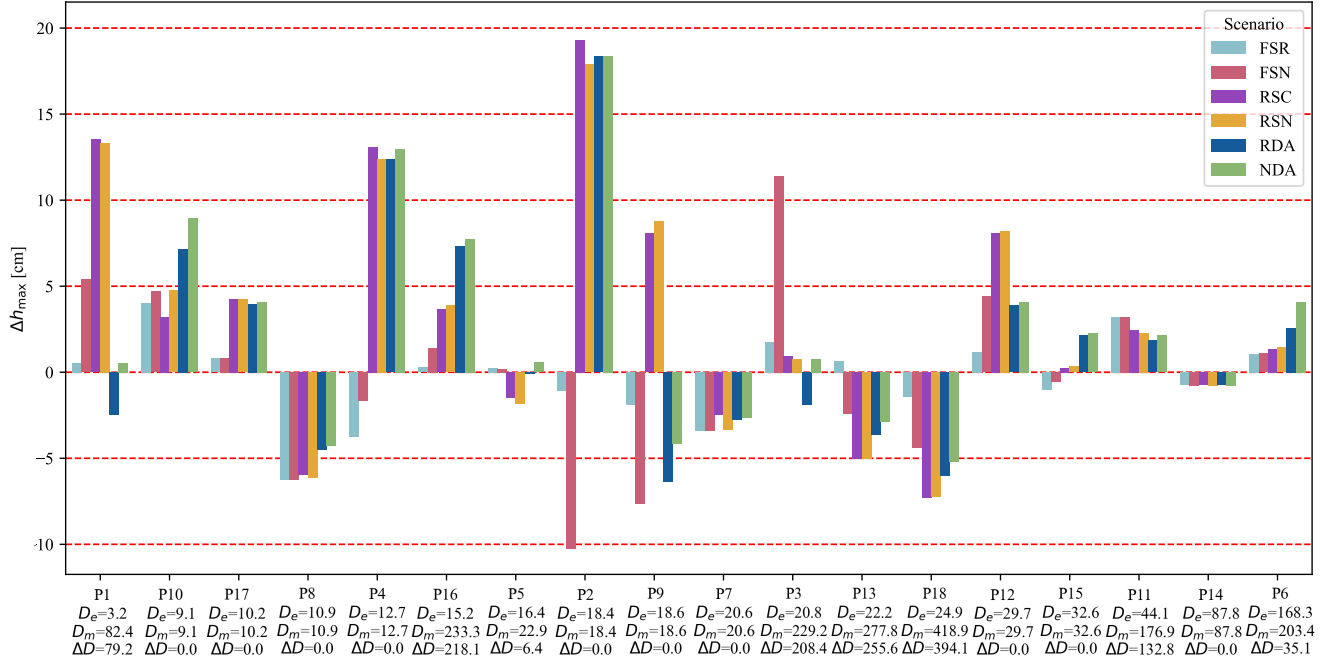


Figure 10. Simulation error of maximum inundation depth at inundated points where $\Delta h_{\max}$ stands for the simulated depth minus observed ones and D_f and D_s are the distances to the closest rainwater inlet of the complete sewer network used in the FSR, FSN approach and the simplified sewer network used in the RSN approach. $\Delta D = D_s - D_f$. The index of inundated points follow Fig. 8.

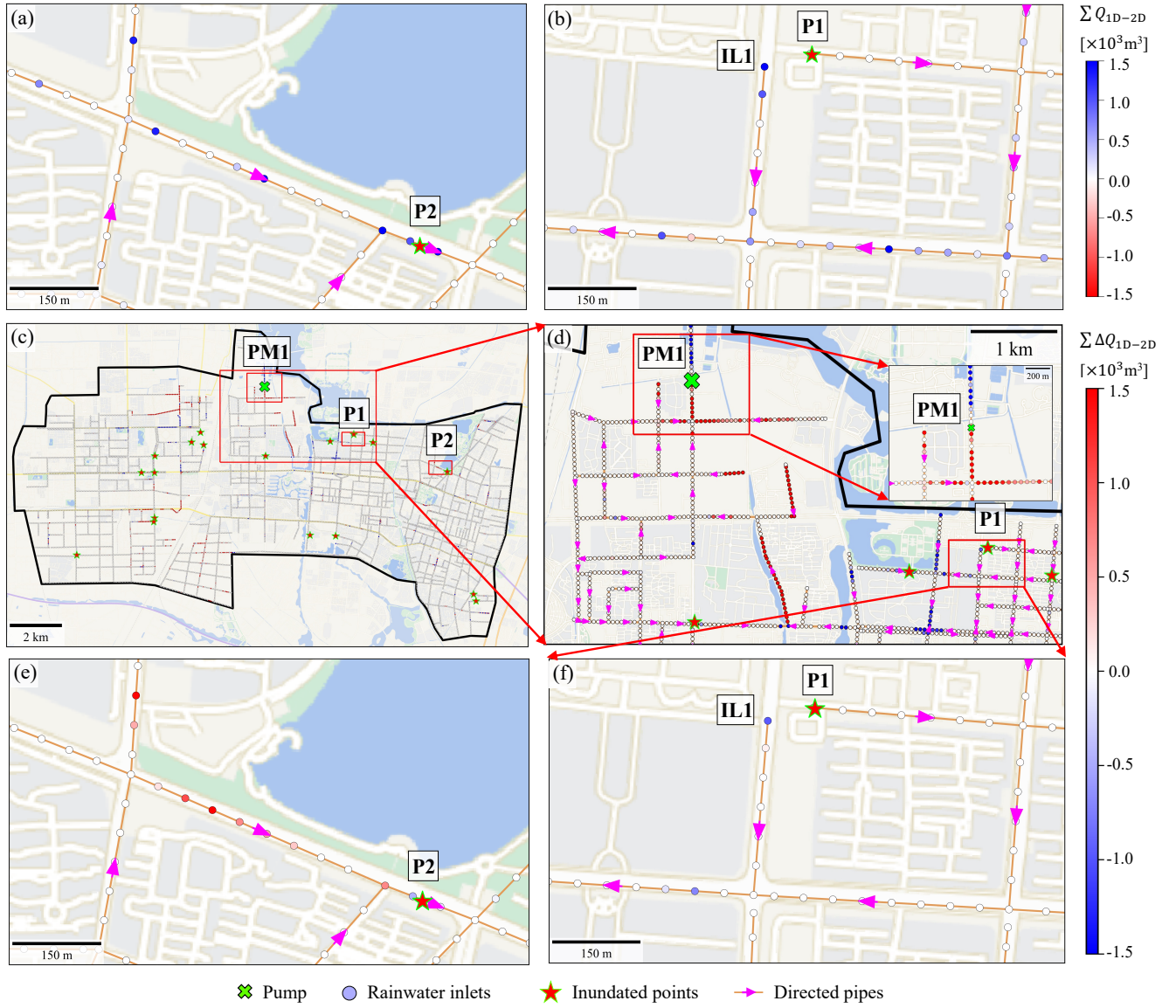


Figure 11. Comparison of accumulated discharges ($\sum Q_{1D-2D}$) at rainwater inlets during the 20220711 storm where positive values indicate inflows. (a)-(b). FSN simulated discharges. (c-f) Simulated discharge differences ($\sum \Delta Q_{1D-2D}$) between FSN and FSR defined by FSN minus FSR. Basemaps are provided by Tianditu (<https://map.tianditu.gov.cn/>).

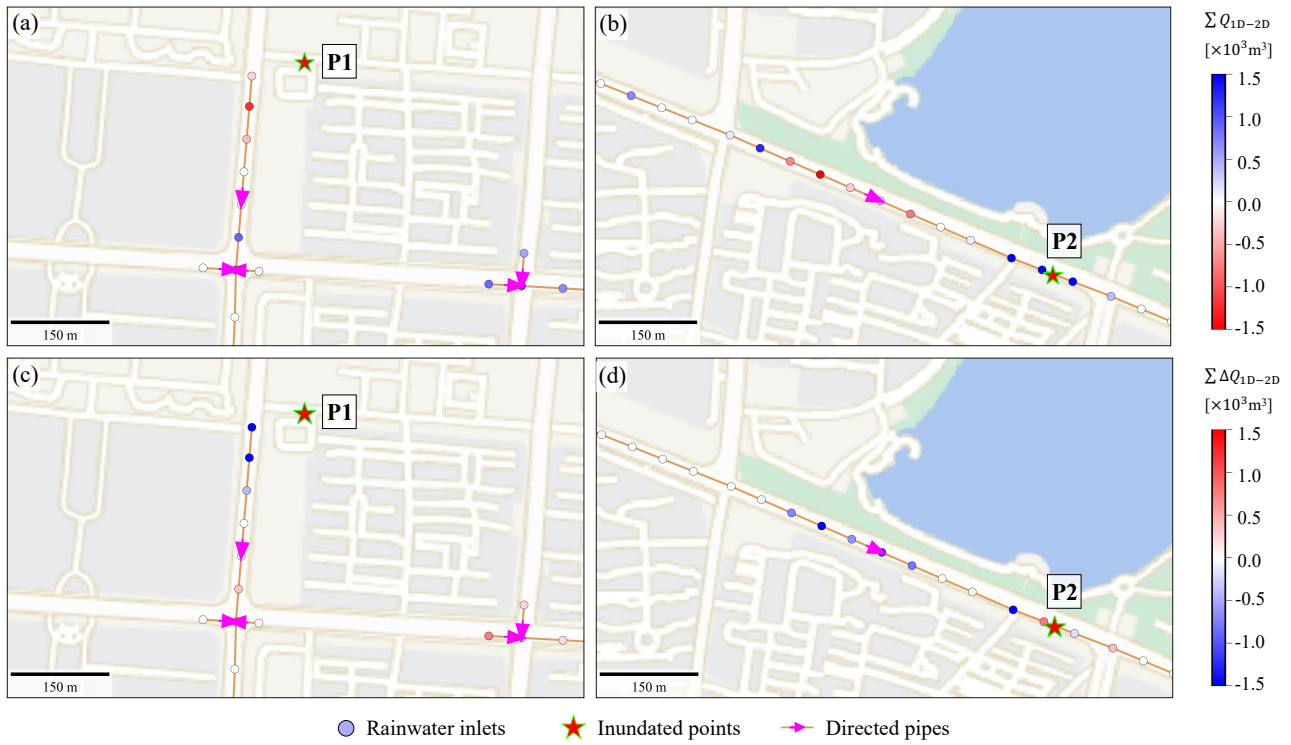


Figure 12. Comparison of accumulated discharges at rainwater inlets during the 20220711 storm. (a)-(b) RSN simulated discharges. (c)-(d) Simulated discharge differences between RSN and FSN defined by RSN minus FSN. Basemaps are provided by Tianditu (<https://map.tianditu.gov.cn/>).

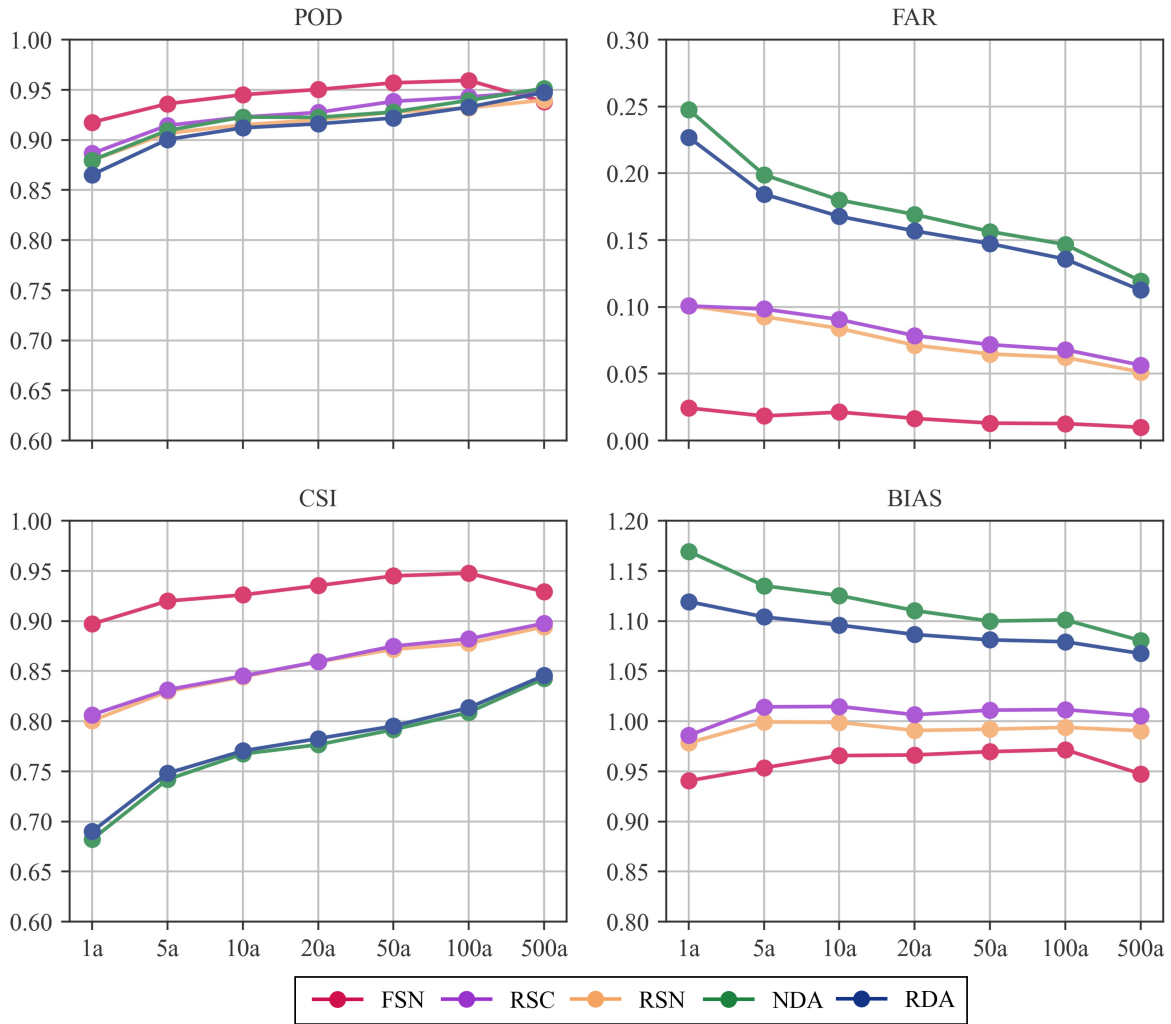


Figure 13. Comparison of simulated inundation area under design rainfall scenarios using different approximation methods.

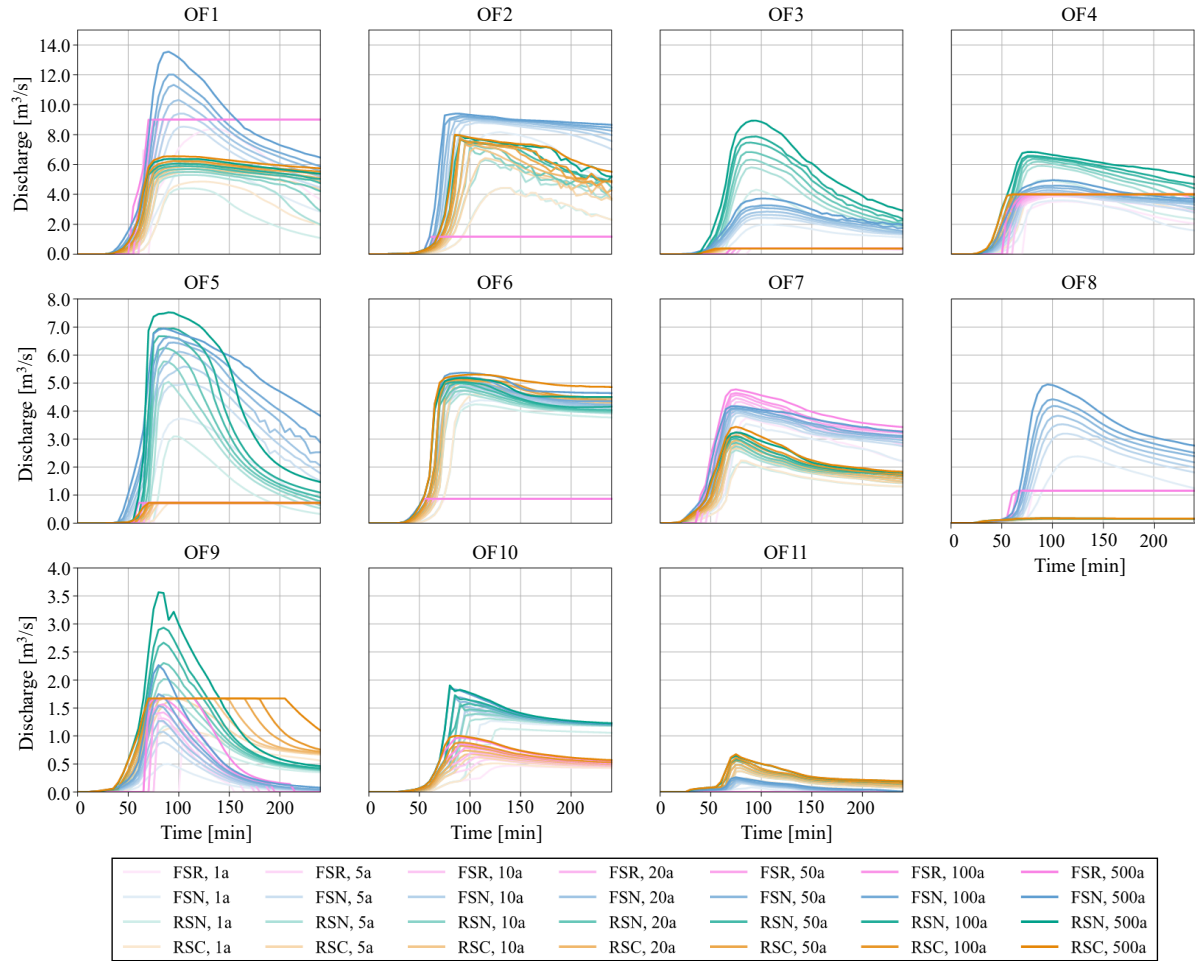


Figure 14. Comparison of simulated outflow processes under design rainfall scenarios using different approximation methods.

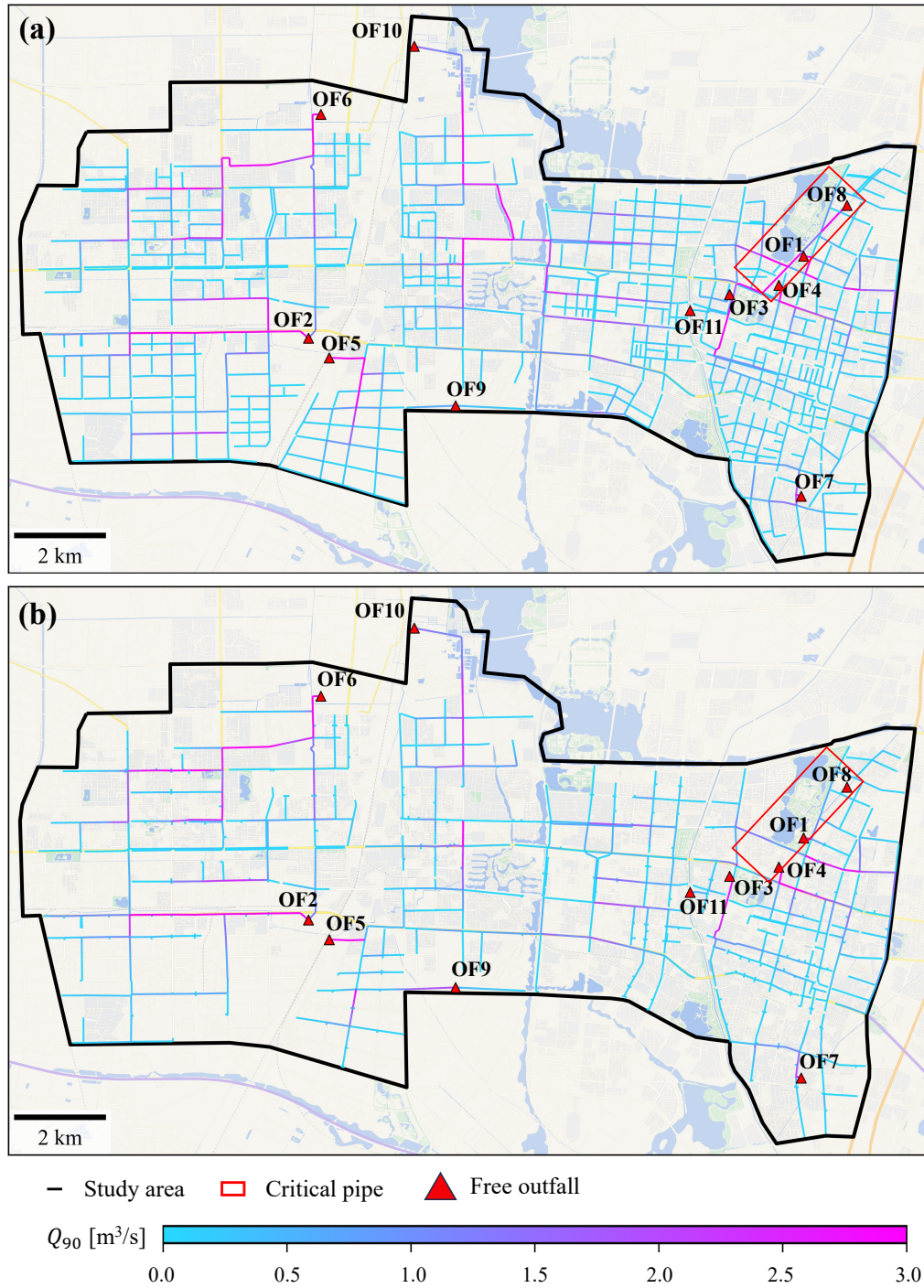


Figure 15. Comparison of simulated flows at 90 percentiles (Q_{90}) of pipes under design rainfall scenarios using physical approaches with/without network simplification. (a) FSN approach. (b) RSN approach. Basemaps are provided by Tianditu (<https://map.tianditu.gov.cn/>).