Reviewer #2

The authors provide CH4 retrieval and emission quantification methods for the MethaneAIR imaging spectrometer based on a matched filter and integrated mass enhancement method. The manuscript is well written and provides interesting results. The manuscript does not have a code and data availability section. I have some comments on the methodology that should be addressed for me to recommend the paper for publication.

Thank you for the positive comments and the very careful review.

Introduction

L20ff: The grouping of methane imagers based on 1600 nm and 2300 nm windows is a bit arbitrary. I would argue that the main difference between AVIRIS and MAMAP-2D instruments are the difference in spatial and spectral resolution.

We agree, and that is indeed the rationale for the split between 1600 and 2300 nm instruments in the text, as mentioned in e.g. "*First, we have the spectrometers sampling the entire solar spectrum ($\sim$400--2500\,nm) with a relatively coarse spectral sampling between 5 and 10\,nm, and a relatively high spatial resolution (a few meters in the case of some airborne instruments)*".

We have now emphasized the typically coarser spatial sampling of instruments relying on the 1650 nm band for methane retrievals: "*The second group of methane-sensitive spectrometers sample a narrow spectral window around the 1650\,nm methane absorption, with a sub-nanometer spectral sampling, and a typically coarser spatial sampling*".

L40f: Please define area sources. Is a landfill already an area source?

Definition added to the first sentence of the Introduction, as "*...methane emissions from small infrastructure elements, also known as point sources*"

L47ff: Maybe already explain here why CO2-proxy retrievals are less precise than matched filters.

Clarification added as "*Also, the normalization of the retrieved methane column density by the per-pixel XCO$_2$ proxy increases the 1-σ error of the resulting XCH$_4$ maps, which may lead to higher plume detection limits.*"

Method

Figure 1: Instead of arbitrary spectra for CH4, CO2 and H2O, it would be nice show spectra for typical atmospheric concentrations.

Figure and caption have been updated to include the column concentrations for each gas.

L86ff: Foote et al. (2020) introduces an albedo correction term to remove systematic errors in XCH4 plumes due to deviations between the mean spectrum and the local spectrum. The systematic errors are likely to introduce systematic errors in the emission estimates. I think it is necessary to test if the albedo correction affects the results.

We would argue that MethaneAIR's high spectral resolution enables a better decoupling of methane and surface reflectance/albedo than what is possible with coarser spectral resolution instruments, such as the AVIRIS-NG spectrometer used by Foote et al.. This would make the albedo correction less relevant. Also, the topic of the impact of surface albedo on the matched-filter retrieval is already tackled by the discussion around Fig. 3. For this reason, we prefer not to make a relatively

major extension to the study by implementating and evaluating Foote's albedo correction in our retrieval.

This clarification has been added: *"We expect that MethaneAIR's high spectral resolution enables a better decoupling of methane and surface reflectance in the retrieval than what is usually found in coaser spectral resolution retrievals \citep{AYASSE2018386}."*

L95: How do you account for varying observation angles and surface elevation during data acquisition?

This has been clarified as *"In the case of the target spectrum $\vec{k}$, this is calculated at high spectral resolution from pre-computed transmittance spectra stored in a look-up table (LUT). For that, we interpolate the LUT considering the mean value of the sun zenith angle and the ground-to-sensor distance within each data granule, whereas a per-column view zenith angle is used in order to account for across-track gradients in the observation angle. It must be stated that local gradients in surface elevation are not accounted for by this approach."*

L101f: The small number of samples also affect the mean vector. Did you test the effect of computing the mean vector for a larger sample on your retrieval?

No, we didn't, but we expect the largest effect to be on the covariance matrix.

L114f: Kuhlmann et al. (2024, https://doi.org/10.5194/egusphere-2024-3494) identified CH4 emissions from vent stack in Romania using AVIRIS-NG that were not visible in high-resolution images. How many plumes did you reject, because they are not linked to any infrastructure, and do you see the possibility that you miss such sources in your analysis?

Thanks to MethaneAIR's high spectral resolution, the large majority of the plumes we derived from MethaneAIR where clear enough to have confidence in the detection, making the need for cross-checking with very high resolution imagery to be very small.

This paragraph reads now: *"the candidate plumes identified through a first screening based on visual inspection are compared with the input spectral radiance data at the continuum of the 1650\,nm absorption feature to discard false positives due to surface patterns(e.g. clouds). However, thanks to MethaneAIR's high spectral resolution, the large majority of the plumes we derived from MethaneAIR were clear enough to have confidence in the detection, making the need for cross-checking with very high resolution imagery very small."*

L113: Do you use the plume length or the square root of the detectable plume area as length scale

Information added as *"where the plume length L is approximated by the square root of the detectable plume."*

L128ff: Effective wind speed also depends on emission height and vertical mixing. Maasakkers et al. (2022) derive their empirical equation for a landfill, which I would assume, emits near the surface, while emissions from oil and gas can be elevated from vent stacks or on top of processing facilities. How do you account for this in your method?

Thanks for this interesting point. The height of the source may indeed have an impact on the IME model, but in general there is no information on source height that we could use to contrain an IME model with this dependency during the operational processing.

We have specified in the text that the IME model from Maasakkers et al. was derived for surface-level emissions (*"which was proposed by \citet{bram_landfills} for GHGSat for surface-level emissions (landfills in their case)"*).

L139f: Please provide more information about the DI method.

The following lines have been included in a new section *"2.4 Reference plume quantification methods"*:

"For the DI method, we calculate the fluxes along rectangular boxes around the source of interest. First, we compute the flux for each pixel along the chosen rectangular box. We then determine the gradient of XCH$_4$ and multiply it by the wind vector at each pixel. Based on Green's theorem, we sum all the fluxes to obtain the total flux for a given rectangle. By repeating this calculation for rectangles of different sizes around the source, we obtain a statistical estimate of the flux around the source of interest. In other words, we sample the flux spatially across the observing region using the DI method. Unlike the IME method, we neither sum all the pixels within the plume nor use an effective wind speed."

L143ff: Section 2.4 does not provide enough information to judge the accuracy of the end-to-end simulator. I would assume that it does not include systematic errors in the plume, which might explain why Figure 5 shows good agreement between retrieval and input. I suggest to either remove the end-to-end simulator from the manuscript or provide more details including a more detailed analysis, which should be quite interesting.

The following paragraph has been added to provide more information about the simulation approach: *"The spatially-distributed \dx\ values from the simulated plumes were converted into per-pixel plume transmittance spectra with the same LUTs used for the generation of the $\vec{k}$ spectrum, which is an input to the \dx\ retrieval. With this approach of using the same radiative transfer scheme for the forward simulations and for the \dx\ retrieval, we avoid introducing uncontrolled systematic errors in the end-to-end simulation framework (e.g. as from different gas vertical profiles)."*

Results

Figure 2: Please add a (rough) scale to the image.

A scale bar has been added,

L182ff / Figure 4: I really would like to see the difference between proxy and matched filter (as in Fig. 5). Do you find systematic differences between the methods, in particular inside the plume, what might be the reason, and how would they affect your emission estimate?

Fig. 4 has been updated to show the difference map, and these lines have been added to the main text *"Two small clusters of pixels with systematic offsets can be seen in the difference map, at pixel coordinates (10, 60) and (10, 40) corresponding to the larger plume in the subset. However, these enhancements are close to the noise level and have a different sign, leading to an almost zero offset when aggregated to calculate the IME and, subsequently, Q."*

L198ff: (see my previous comment on the end-to-end simulator)

Please, see reply to **L143ff.**

L207ff: Please provide more information how the DI method has been implemented in this study. Following Chulakadabba et al. (2023), the DI method sums over all pixels along rectangular for difference from the source location to the edge of the detectable plume (except for subtracting the background, which would be about zero for the matched filter). This isn't much different from the IME method, which sums over all pixels in the detectable plume, while excluding the background (which is close to zero).

The main difference between IME and DI method seems to be the effective wind speed. What wind speed is used for the DI method and how does compare to effective wind speed used with the IME method? Would the differences vanish if the same data source (GEOS-FP or HRRR) for the wind speed is used for both methods?

Please, see reply to **L139f** regarding the description of the DI method.

We fully agree with the reviewer in that variations in wind speed data will proportionally affect Q estimates because of the linear relationship between U10 and Q in the IME model (Eq. 2). In this study, our intention was not to evaluate the IME or DI formulations per-se, but to show the validity of our basic IME+GEOS-FP implementation for the estimation of flux rates from the large dataset of plumes detected from the matched-filter output. The DI model constrained with HRRR winds offers an accurate Q estimation framework (although less practical for the processing of large datasets) that we took as a reference for the evaluation of our IME-based Q estimates.

This is discussed in the text as *"each method was constrained with different wind data: the IME-based method is run with GEOS-FP data, as this is the configuration that we apply for the processing of the large plume datasets derived in this work, whereas the DI method is constrained with HRRR wind data, as this is the configuration that potentially provides the most accurate reference for intercomparison with the IME approach"*

L223f: It would interesting do discuss the potential for systematic errors inside the plume here (see my previous comment).

Please, see reply to **L182ff / Figure 4.**

L226f: I do not see why the detection limit should not always increase with wind speed. However, detection limit can depend on other factors such as turbulence.

Clarification added as: *"which implies that the probability of plume detection is not always inversely proportional to wind speed, but in some cases there is an optimal wind speed for plume detection: low-to-moderate winds enabling the development of a plume covering several pixels with \dx\ values above the noise level."*

L238f: What is the uncertainty of the emission rates from the controlled releases?

The caption of Fig. 8 has been updated as *"The metered flux rates correspond to 30-second averages. Error bars in the y-axis represent the 1-sigma error for the IME Q estimates from MethaneAIR, and error bars in the x-axis represent the standard deviation in the metered flux rate values in the 30-second window."*

Figure 8: Why is the RMSE measured in ppb?

Thanks for pointing this out, the legend has been corrected to kg/h (also in Fig. 6)

L280ff: Does the wind speed vary spatially and temporally in the campaign area during data acquisition? I expect that would affect the detection limit during the campaign.

We agree. A clarification has been added as "The GEOS-FP wind product shows average wind speeds of about 3.5\,m/s for RF06, whereas stronger winds of about 5\,m/s are reported in GEOS-FP during the MX025 flights, with a standard deviation of 0.5\,m/s in both cases. The stronger winds may have led to higher detection limits for the MX025 campaign. We have not analyzed spatial and temporal variations of wind speed during data acquisition for each campaign in depth, but such changes would also have an impact on plume detections in each campaign"

Figure 12: Do you see a dependency of flux rates on wind speed?

We would need a more careful analysis, but from a simple representation of the data included in Fig. 12, we do not see a depency of the flux rate estimates on u10 (see figure below).
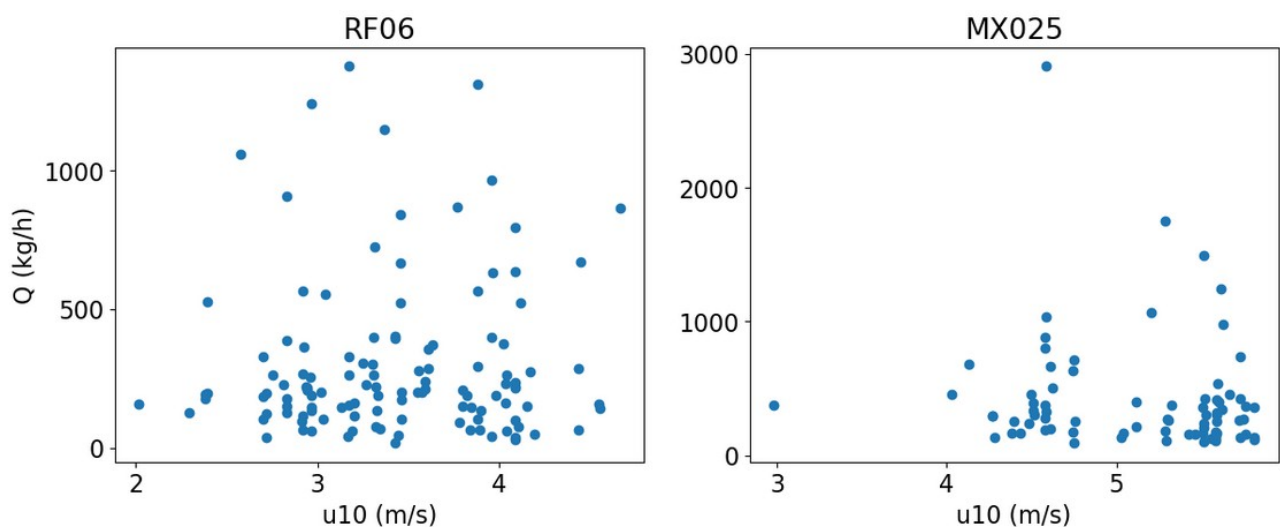
L292: Does the albedo change between the campaigns?

This line has been rephrased as "As mentioned earlier in this work, the detection of a plume in a \ dx\ map depends on several factors, including the wind speed, the retrieval noise (driven by at-sensor radiance and local variability in the surface albedo), and the modification of \dx\ gradients by neighboring sources."

L292f: It is unclear what do you mean with "enhanced spatial variability of ΔXCH4".

The "enhanced spatial variability of ΔXCH4" has been rephrased as "the modification of \dx\ gradients by neighboring sources"

Conclusions

L312f: Please specify why a computationally efficient retrieval would improve the detection limit.

Sentence rephrased as "Our goal was to implement a \dx\ retrieval which was both computationally-efficient and able to maximize the probability of plume detection"

L332: I suggest adding that a major advantage is minimizing the number of false positives.

Statement added as ", with a minimum rate of false positives"