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# Decomposition of three aerosol components using lidar-derived depolarization ratios at two wavelengths

Xiaoxia Shang<sup>1</sup>, Maria Filioglou<sup>1</sup>, Julian Hofer<sup>2</sup>, Moritz Haarig<sup>2</sup>, Qiaoyun Hu<sup>3</sup>, Philippe Goloub<sup>3</sup>, Sami Romakkaniemi<sup>1</sup>, and Mika Komppula<sup>1</sup>

<sup>1</sup>Finnish Meteorological Institute, Kuopio, Finland.

<sup>2</sup>Leibniz Institute for Tropospheric Research, Leipzig, Germany

<sup>3</sup>Univ. Lille, CNRS, UMR 8518 – LOA – Laboratoire d'Optique Atmosphérique, 59000 Lille, France

**Correspondence:** Xiaoxia Shang (xiaoxia.shang@fmi.fi)

**Abstract.** In this study, we present a novel algorithm using the lidar-derived particle linear depolarization ratios measured at two wavelengths for the decomposition of three aerosol components, to retrieve aerosol-type-specific backscatter fractions. This extended methodology builds upon well-developed polarization-based algorithms, e.g., POLIPHON (Polarization Lidar PHOtometer Networking) method, offers an added advantage for an almost unambiguous separation of three aerosol components, on the <sup>assumption</sup> condition that their ~~characteristic~~ depolarization ratios are different. And it <sup>assumes</sup> requires the proper knowledge of ~~characteristic~~ depolarization ratio and the backscatter-related Ångström exponent of each aerosol type. The mathematical relationship between particle linear depolarization ratios at two wavelengths for a mixture of two aerosol components has been derived and expressed as an equation. This equation is visualized as a curved <sup>area?</sup> ~~(line)~~, where the <sup>for a line?</sup> boundaries are determined by the characteristic depolarization ratios and the curvature is influenced by the characteristic backscatter-related Ångström exponents of both aerosol types. Moreover, the pair values of particle linear depolarization ratios of three aerosol components at two wavelengths must remain within the enclosed region predetermined by three boundary curves, and each curve is determined by the characteristics of any two of three types. Such characteristic curved relationships are more accurate than the common use of the ratio of the particle linear depolarization ratios. This novel algorithm has been applied to synthetic examples considering dust mixtures and to lidar observations of Arabian dust, Asian dust, and Saharan dust, so as to decompose coarse-mode dust (>1 μm in diameter), fine-mode dust (<1 μm in diameter), and spherical non-dust aerosols. The dust characteristics reported in numerous laboratory and field studies have been considered.

## 1 Introduction

Light detection and ranging (lidar) is a powerful instrument that provides vertical information of atmospheric aerosol and clouds from ground and space at high vertical resolution. Irregularly shaped particles induce strong depolarization of laser light. Polarization-based algorithms have been developed to separate the aerosol profiles of weakly light depolarizing (spherical, e.g., anthropogenic haze, biomass burning smoke, maritime) and strongly light depolarizing (non-spherical, e.g., volcanic ash, desert dust, pollen) particles (e.g., Shimizu et al., 2004; Tesche et al., 2009, 2011; Ansmann et al., 2011, 2012; Sugimoto and Lee, 2006; Nishizawa et al., 2007; Freudenthaler et al., 2009; Groß et al., 2011, 2012; Miffre et al., 2012; Nisantzi et al.,



2014; Shang et al., 2020). Such techniques have been primarily used for decoupling the particle backscatter coefficient profiles  
25 of, e.g., dust and non-dust particles (Teschke et al., 2009), ash and fine-mode particles (Ansmann et al., 2011; Marengo and  
Hogan, 2011), and pollen and non-depolarizing background aerosol (Shang et al., 2022). In addition, the POLIPHON (POLar-  
ization LIdar PHOtometer Networking) method (Ansmann et al., 2012) allows the retrieval of the particle number, surface area,  
and volume/mass concentration of fine mode and coarse mode particles, in synergy with sun-sky photometer measurements  
(one-step POLIPHON). The extended POLIPHON method, namely the two-step POLIPHON method, further allows the sep-  
30 aration of non-dust, fine mode, and coarse mode dust particle contributions of the above-mentioned optical and microphysical  
quantities (Mamouri and Ansmann, 2014, 2017). The two-step POLIPHON method comprises two subsequent phases similar  
to the one-step POLIPHON, and allows separating three aerosol components, as long as their characteristic depolarization ra-  
tios are distinct. However, to separate the backscatter coefficients of coarse mode dust in the first step, it requires an assumption  
about the spherical particle fraction to estimate the overall depolarization ratio for the residual aerosol (a mixture of non-dust  
35 and fine-dust with unknown mixing ratio). To date, POLIPHON has been utilized in many studies, to lidar observations ex-  
ploiting single-wavelength polarization measurements (Ansmann et al., 2019; Córdoba-Jabonero et al., 2018; Mamali et al.,  
2018; Haarig et al., 2019; Proestakis et al., 2024).

Most commonly, the 532 nm and 355 nm wavelengths have been used to perform depolarization ratio measurements.  
Most lidar stations in the European Aerosol Research Lidar Network (EARLINET, Pappalardo et al. (2014); <https://www.earlinet.org>,  
40 <https://www.earlinet.org>, last access: 10 October 2024) and the Raman and polarization lidar network (PollyNET, Baars et al. (2016);  
<https://polly.tropos.de>, last access: 10 October 2024) measure the particle linear depolarization ratios at 532 and/or 355 nm.  
The NASA Micro-Pulse Lidar Network (MPLNET, Welton et al. (2001); <https://mplnet.gsfc.nasa.gov>, last access: 10 October  
2024) provide polarization measurements at 532 nm. The space-borne lidars CALIOP (Cloud-Aerosol Lidar with Orthog-  
onal Polarization) onboard the CALIPSO (the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observation) (Winker  
45 et al., 2009), and ATLID (Atmospheric Lidar) in the ESA's EarthCARE (Cloud, Aerosol and Radiation Explorer; <https://earth.esa.int/eogateway/missions/earthcare>, last access: 10 October 2024) mission retrieve depolarization ratio at 532  
or 355 nm, respectively. Depolarization ratio observations at 1064 nm have been increasing the last years as well (Haarig et al.,  
2022; Hu et al., 2020). The Vaisala CL61 ceilometer, and the HALO Photonics Stream Line Pro scanning Doppler lidar  
(Pearson et al., 2009) also provide polarization observations at 910 nm and 1565 nm, respectively. The utilization of the multi-  
50 wavelength polarization lidar or a synergy of multiple lidars with the capability to provide concurrent depolarization ratio  
observations at various wavelengths allows the investigation of the spectral dependence on the depolarization ratios. This is an  
important aspect to characterize different aerosol types, such as dust (Haarig et al., 2017a, 2022) and pollen (Bohlmann et al.,  
2021; Filioglou et al., 2023). In particular, it could enable the distinction of non-spherical aerosol types.

In this study, we present a novel methodology (Sect. 2), using the particle linear depolarization ratios measured at two wave-  
55 lengths, to separate the particle backscatter coefficients of three aerosol components without introducing assumptions regarding  
the aerosol particle fractions as required in the POLIPHON method. The relationship between particle linear depolarization  
ratios at two wavelengths are investigated mathematically for mixtures of two and three aerosol components. Then, the method  
is applied to lidar observations of dust particles at different regions (Sect. 3).



## 2 Methodology

60 The particle linear depolarization ratio of the particle ensemble at wavelength  $\lambda$ , denoted as  $\delta_p(\lambda)$ , can be expressed by Eqs. 1–2 for an aerosol mixture of two or three externally mixed aerosol types (Shimizu et al., 2004; Tesche et al., 2009; Mamouri and Ansmann, 2014). In this context, each particle consists of a single aerosol type, and the calculation involves the aerosol backscatter coefficient ( $\beta_x$ ) and aerosol-type-specific characteristic depolarization ratio ( $\delta_x$ ), where the index  $x$  corresponds to each aerosol type ( $a$ , or  $b$ , or  $c$ ). *or to the mixture ( $x=p$ ) → this is used e.g. in line 71*

$$65 \quad \delta_p(\lambda) = \frac{\frac{\beta_a(\lambda)\delta_a(\lambda)}{\delta_a(\lambda)+1} + \frac{\beta_b(\lambda)\delta_b(\lambda)}{\delta_b(\lambda)+1}}{\frac{\beta_a(\lambda)}{\delta_a(\lambda)+1} + \frac{\beta_b(\lambda)}{\delta_b(\lambda)+1}} \quad (1)$$

$$\delta_p(\lambda) = \frac{\frac{\beta_a(\lambda)\delta_a(\lambda)}{\delta_a(\lambda)+1} + \frac{\beta_b(\lambda)\delta_b(\lambda)}{\delta_b(\lambda)+1} + \frac{\beta_c(\lambda)\delta_c(\lambda)}{\delta_c(\lambda)+1}}{\frac{\beta_a(\lambda)}{\delta_a(\lambda)+1} + \frac{\beta_b(\lambda)}{\delta_b(\lambda)+1} + \frac{\beta_c(\lambda)}{\delta_c(\lambda)+1}} \quad (2)$$

The aerosol backscatter fraction  $\phi_x$  (Eq. 3) is defined as the ratio of the backscatter coefficient of the aerosol type  $x$  ( $\beta_x$ ) to the total particle backscatter coefficient ( $\beta_p$ ). The sum of all aerosol backscatter fractions in the particle ensemble is equal to 1. *mixture*

$$\phi_x(\lambda) = \frac{\beta_x(\lambda)}{\beta_p(\lambda)} \quad (3)$$

70 The backscatter-related Ångström exponent ( $\tilde{A}_\beta$ ) between two wavelengths,  $\lambda_1$  and  $\lambda_2$ , can be expressed through Eq. 4 (the index  $x$  can be used for one aerosol type or for the particle ensemble), where parameter  $\eta$ , often referred as the backscatter color ratio, is a function of  $\tilde{A}_\beta$  and it is defined as follows:

$$\eta_x = \left(\frac{\lambda_1}{\lambda_2}\right)^{-\tilde{A}_{\beta,x}(\lambda_1,\lambda_2)} = \frac{\beta_x(\lambda_1)}{\beta_x(\lambda_2)}. \quad (4)$$

*particle* To apply the novel algorithm for the decomposition of two or three aerosol components, *proper* knowledge of the characteristic depolarization ratios ( $\delta_x$ ) and backscatter-related Ångström exponent ( $\tilde{A}_{\beta,x}$ ) of each aerosol type is *assumed* necessary. The fine and coarse mode dust optical properties have been measured and reported in many laboratory and field studies (Sakai et al., 2010; Järvinen et al., 2016; Freudenthaler et al., 2009; Burton et al., 2015). Due to the distinct depolarization ratios of fine and coarse mode dust, and spherical non-dust aerosols, these aerosols *types* become good candidates for validating the novel methodology. Atmospheric mineral dust is one of the most important aerosol types, playing a key role on several critical aspects of the Earth system. As stated in Adebisi et al. (2023), Castellanos et al. (2024), and references therein, many studies have been performed to investigate the dust properties. The size of mineral dust in the atmosphere ranges from less than  $0.1 \mu\text{m}$  to more than  $100 \mu\text{m}$  in diameter (Adebisi et al., 2023; Ryder et al., 2019; van der Does et al., 2018; Mahowald et al., 2014). Following the POLIPHON method, in this study, we consider two components of pure dust: fine-mode dust which covers the particle size spectrum up to  $1 \mu\text{m}$  in diameter, and coarse-mode dust with super-micrometer particles ( $>1 \mu\text{m}$  in diameter). *particles*



detailed below

input parameters

sections 2.1 and 2.3

85 The algorithm was applied to synthetic ~~examples considering dust mixture~~ in Sect. 2, and to lidar observations of dust  
in at different regions in Sect. 3, using the characteristics from Table 1. The characteristic depolarization ratios of coarse and  
fine mode dust at 355, 532, and 1064 nm are taken from the review study of Mamouri and Ansmann (2017) (see Table 1  
in that paper), which includes two laboratory studies (Sakai et al., 2010; Järvinen et al., 2016), and five field observations  
(Freudenthaler et al., 2009; Burton et al., 2015; Veselovskii et al., 2016; Haarig et al., 2017a; Hofer et al., 2017). The laboratory  
90 experiments to measure the airborne dust properties ~~are~~ challenging, and thus still limit, Sakai et al. (2010) measured  $\delta_x(532)$   
of several tropospheric aerosols using a laboratory chamber. For high number concentrations,  $\delta_{df}(532)$  of the fine-mode dust  
were found to be  $0.17 \pm 0.03$  for the Asian dust and  $0.14 \pm 0.03$  for the Saharan dust, whereas  $\delta_{dc}(532)$  of the coarse-mode  
dust were  $0.39 \pm 0.04$  to  $0.05$  for both. Järvinen et al. (2016) measured  $\delta_{dust}$  of various dust samples at 488 and 552 nm in a  
cloud chamber. They reported that the measured  $\delta_{dust}$  ranged from 0.03 to 0.36 and were strongly dependent on the particle  
95 size. Based on this study, Mamouri and Ansmann (2017) estimated  $\delta_{df}$  for fine-mode dust of around  $0.21 \pm 0.02$ ,  $0.16 \pm$   
 $0.02$ , and  $0.09 \pm 0.03$  for the laser wavelengths of 355, 532, and 1064 nm, respectively. Miffre et al. (2023) found that the  
dust depolarization ratios are mainly influenced by the particles' complex refractive index, when the strongly light-absorbing  
hematite is present, while its variations with size and shape are less significant. They also present measured  $\delta_{dust}$  values for  
finer and coarser size distributions of Arizona and Asian dust (see Table 1 in Miffre et al., 2023), which can not be used in this  
100 study as the used size distributions are different from other studies. Field measurements were also considered. Nevertheless,  
the reported characteristic depolarization ratios from field observations may still contain contributions from spherical particles  
within the mixture, potentially leading to an underestimation of the characteristic values. Moreover, certain vertical smoothing  
is always applied in the lidar retrievals, and layer-mean values are often reported, adding uncertainties on the lidar-derived  
characteristics of aerosol types. Burton et al. (2015) performed airborne measurements of dust plumes over the United States.  
105 For a dense dust layer of local North American dust, they found high  $\delta_p$  of  $0.24 \pm 0.05$ ,  $0.37 \pm 0.01$ ,  $0.38 \pm 0.01$  at 355,  
532, and 1064 nm, respectively. The corresponding  $\tilde{A}_\beta(532, 1064)$  <sup>was</sup>  $-0.09 \pm 0.04$ . For two transported Saharan dust layers,  
 $\tilde{A}_\beta(532, 1064)$  were found to be  $0.46 \pm 0.03$  and  $0.68 \pm 0.13$ . Veselovskii et al. (2016) observed that  $\delta_p(532)$  increased up to  
 $0.35 \pm 0.05$ , and  $\tilde{A}_\beta(355, 532)$  decreased to  $-0.7$ , during strong African dust episodes. Hofer et al. (2017) present an extreme  
dust event (probably with coarse mode dust dominant) with values of  $0.29 \pm 0.01$  or  $0.35 \pm 0.01$  for  $\delta_p(355)$  or  $\delta_p(532)$ , and  
110 values of  $-0.20 \pm 0.13$  or  $0.29 \pm 0.03$  for  $\tilde{A}_\beta(355, 532)$  or  $\tilde{A}_\beta(532, 1064)$ , respectively. Freudenthaler et al. (2009) reported  
 $0.31 \pm 0.03$  and  $0.27 \pm 0.04$  for  $\delta_p(532)$  and  $\delta_p(1064)$  over Morocco. Haarig et al. (2017a) highlighted maximum values of  
 $0.27$  for  $\delta_p(1064)$  measured over Barbados, which are almost equal to the coarse dust depolarization ratio. The characteristics  
of non-dust type can vary widely across regions and times. A review study of Proestakis et al. (2024) suggests a value of  
 $0.05 \pm 0.02$  at 532 nm for non-dust depolarization ratios (Teschke et al., 2009; Mamouri and Ansmann, 2014, 2016; Marinou  
et al., 2017; Proestakis et al., 2018). Here we consider  $0.05 \pm 0.02$  for all 3 wavelengths in the synthetic examples and cases  
where measurements are unavailable. However, such values may be adjusted if measurements become available. Laboratory  
measurements of dust  $\tilde{A}_\beta$  are still missing, thus values from lidar measurements are considered. Mamouri and Ansmann  
(2014) stated the extinction-related Ångström exponent between 355 and 532 nm to be  $-0.2$ ,  $1.5$ ,  $2.0$  for coarse dust, fine  
dust, and non-dust aerosols, respectively. Assuming the same lidar ratios at 355 and 532 nm, these values can be used for the





*coarse mixtures*

*fine*

**Table 1.** Input parameters used in the synthetic ~~cases~~ (Sect. 2) and case studies (Sect. 3): characteristic depolarization ratios ( $\delta$ ) at 355, 532 or 1064 nm, and backscatter-related Ångström exponent ( $\text{\AA}_\beta$ ) between 355 and 532 nm, or between 532 and 1064 nm, for coarse dust (dc), fine dust (df), and spherical non-dust (nd) aerosols. Typical values are considered from published studies (see text in Sect. 2). Values in parentheses are based on our assumptions.

Aerosol type (abbreviation)	$\delta(355)$	$\delta(532)$	$\delta(1064)$	$\text{\AA}_\beta(355, 532)$	$\text{\AA}_\beta(532, 1064)$
Coarse dust (dc)	$0.27 \pm 0.03$	$0.37 \pm 0.03$	$0.27 \pm 0.03$	$-0.2 (\pm 0.03)$	$0.3 \pm 0.03$
Fine dust (df)	$0.21 \pm 0.02$	$0.16 \pm 0.02$	$0.09 \pm 0.02$	$1.5 (\pm 0.03)$	$0.6 (\pm 0.03)$
Non-dust aerosol (nd)	$0.05 \pm 0.02$	$0.05 \pm 0.02$	$0.05 \pm 0.02$	$2.0 (\pm 0.03)$	$(1.5 \pm 0.03)$

120  $\text{\AA}_\beta(355, 532)$ . *We* The authors found no available value for  $\text{\AA}_\beta(532, 1064)$  of fine-mode dust in the literature. Nevertheless, several studies documented range of values of  $\text{\AA}_\beta$  for the dust layers including the coarse and fine mode dust. For example, Tesche et al. (2009) and Filioglou et al. (2020) found  $\text{\AA}_\beta(532, 1064)$  values of 0.0 to 0.7, or 0.1 to 0.6, respectively. The upper limit of such range values could be related to the fine-mode dust dominant dust mixture.

It should be emphasized that this paper focuses on presenting a novel methodology, and the investigation of the characteristics is beyond the scope. The characteristic values of the various aerosol types can be readily updated as more accurate values become available and new observations emerge in the field.

*optical properties*

## 2.1 Mixture of two aerosol ~~components~~

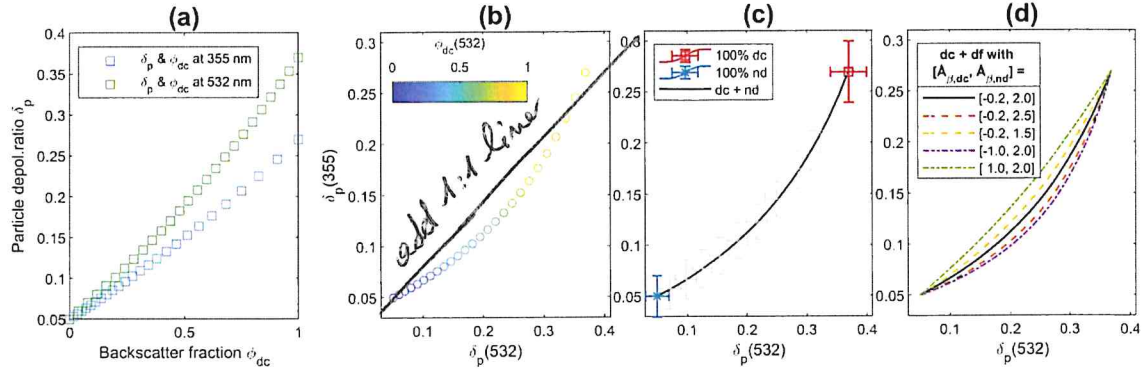
*but you already give a good literature review, so it is not fully out of scope*

As a first step, a two aerosol ~~component~~ mixture is considered assuming a strongly depolarizing and a weakly depolarizing aerosol types, with type denoted by the subscripts  $a$  and  $b$ . The characteristic depolarization ratios of the two aerosol types should be different (i.e.,  $\delta_a \neq \delta_b$ ). The total particle backscatter coefficient,  $\beta_p$ , is the sum of the backscatter coefficients of aerosols  $a$  and  $b$  ( $\beta_p = \beta_a + \beta_b$ ). The separation method using  $\delta_p$  ~~from~~ <sup>using</sup> one wavelength, initially developed by Shimizu et al. (2004) and thoroughly discussed in Tesche et al. (2009), is well known and has been widely utilized. In this section, we present an approach for cases where  $\delta_p$  at two wavelengths are available.

Using Eqs. 1 and 3, the  $\delta_p$  of the particle ensemble at wavelength  $\lambda_1$  (or  $\lambda_2$ ) can be expressed by Eq. 5 (or 6). A synthetic example is given in Fig. 1(a), using the characteristics of coarse dust and spherical non-dust aerosol from Table 1. Using Eqs. 3 (for wavelengths  $\lambda_1$  and  $\lambda_2$ ) and 4 (for aerosols  $a$  and  $b$ ), the relationships between the aerosol backscatter fractions at two wavelengths can be derived as Eqs. 7 and 8. Therefore, a scatter plot using  $\delta_p$  at two wavelengths can be generated, and linked to the backscatter fractions (an example is given in Fig. 1b). It is evident that the sum of  $\phi_a(\lambda_1)$  and  $\phi_b(\lambda_1)$  equals 1 (Eqs. 7–8). Also, the sum of the two aerosol backscatter fractions at  $\lambda_2$  is equal to 1 (Eq. 9). Eqs. 7–9 remain valid under the interchange

140 of  $\lambda_1$  and  $\lambda_2$ .

*optical properties*



**Figure 1.** Synthetic particle linear depolarization ratios ( $\delta_p$ ) for the aerosol mixture with two aerosol types: coarse dust (dc) and spherical non-dust aerosol (nd). (a)  $\delta_p$  against the coarse dust backscatter fraction ( $\phi_{dc}$ ) at 355 or 532 nm. (b) Relationship between  $\delta_p$  at 355 and 532 nm, with  $\phi_{dc}$  at 532 nm shown by color scales. (c) Theoretical characteristic curves of  $\delta_p$  at 355 and 532 nm for the dc and nd mixture, with uncertainties from Monte Carlo simulations (using parameters in Table 1). (d) Characteristic curves of  $\delta_p$  at 355 and 532 nm for dc and nd mixture, with different characteristic backscatter-related Ångström exponents ( $\tilde{A}_{\beta,dc}(355, 532)$  and  $\tilde{A}_{\beta,nd}(355, 532)$ ).

$$\delta_p(\lambda_1) = \frac{\frac{\phi_a(\lambda_1)\delta_a(\lambda_1)}{\delta_a(\lambda_1)+1} + \frac{\phi_b(\lambda_1)\delta_b(\lambda_1)}{\delta_b(\lambda_1)+1}}{\frac{\phi_a(\lambda_1)}{\delta_a(\lambda_1)+1} + \frac{\phi_b(\lambda_1)}{\delta_b(\lambda_1)+1}} \quad (5)$$

$$\delta_p(\lambda_2) = \frac{\frac{\phi_a(\lambda_2)\delta_a(\lambda_2)}{\delta_a(\lambda_2)+1} + \frac{\phi_b(\lambda_2)\delta_b(\lambda_2)}{\delta_b(\lambda_2)+1}}{\frac{\phi_a(\lambda_2)}{\delta_a(\lambda_2)+1} + \frac{\phi_b(\lambda_2)}{\delta_b(\lambda_2)+1}} \quad (6)$$

$$\phi_a(\lambda_1) = \frac{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2)}{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2) + \eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2)} \quad (7)$$

$$\phi_b(\lambda_1) = \frac{\eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2)}{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2) + \eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2)} \quad (8)$$

$$145 \quad \phi_a(\lambda_2) + \phi_b(\lambda_2) = 1 \rightarrow \text{Derefer for } \lambda_1 \rightarrow \text{assumed to be} \quad (9)$$

In the above-mentioned equations (Eqs. 5–9), eight variables are known: the particle linear depolarization ratios of the particle ensemble ( $\delta_p(\lambda_1)$ ,  $\delta_p(\lambda_2)$ ), and the characteristic depolarization ratios and the backscatter-related Ångström exponents ( $\delta_a(\lambda_1)$ ,  $\delta_b(\lambda_1)$ ,  $\delta_a(\lambda_2)$ ,  $\delta_b(\lambda_2)$ ,  $\tilde{A}_{\beta,a}$ ,  $\tilde{A}_{\beta,b}$ ) which are aerosol-type-dependent. Thus, the mathematical relationship between  $\delta_p(\lambda_1)$  and  $\delta_p(\lambda_2)$  can be derived and expressed through Eq. 10, without unknown parameters. Such a relationship relating to the wavelength dependency on the particle linear depolarization ratios is fixed for the mixture of two aerosol components. The two boundaries are determined by the  $\delta_x$  of the two aerosols. For the synthetic example in Fig. 1(b-d), the top-right (or left-bottom) boundary of the curve is determined by  $\delta_{dc}$  (or  $\delta_{nd}$ ) at 355 and 532 nm.  $\tilde{A}_{\beta,x}$  of both aerosol types impacts the curvature of the curve. Examples of characteristic curves using different  $\tilde{A}_{\beta,x}$  values are given in Fig. 1(d) to illustrate the curvature effect: higher  $\tilde{A}_{\beta,nd}$  or lower  $\tilde{A}_{\beta,dc}$  will result in a higher curvature while bending towards the right bottom



155 direction. A sensitively study on the synthetic example (Fig. 1) was performed based on the Monte Carlo approach. Six variables ( $\delta_{dc}(355)$ ,  $\delta_{dc}(532)$ ,  $\hat{A}_{\beta,dc}$ ,  $\delta_{nd}(355)$ ,  $\delta_{nd}(532)$ ,  $\hat{A}_{\beta,nd}$ ) are used, considering normal statistical distribution with their standard derivations (in Table 1). Results using 1000 draws/simulations are shown as gray error bars in Fig. 1(c).

$$\delta_p(\lambda_1) = \frac{\delta_a(\lambda_1)\eta_a[\delta_b(\lambda_1)+1][\delta_a(\lambda_2)+1][\delta_b(\lambda_2)-\delta_p(\lambda_2)] + \delta_b(\lambda_1)\eta_b[\delta_a(\lambda_1)+1][\delta_b(\lambda_2)+1][\delta_p(\lambda_2)-\delta_a(\lambda_2)]}{\eta_a[\delta_b(\lambda_1)+1][\delta_a(\lambda_2)+1][\delta_b(\lambda_2)-\delta_p(\lambda_2)] + \eta_b[\delta_a(\lambda_1)+1][\delta_b(\lambda_2)+1][\delta_p(\lambda_2)-\delta_a(\lambda_2)]} \quad (10)$$

160 It is concluded that the relationship between  $\delta_p$  at two wavelengths is not linear, thus, the common use of the ratio of  $\delta_p(\lambda_1)$  and  $\delta_p(\lambda_2)$  is less accurate than the characteristic curved relationship proposed in this study. Furthermore, these characteristic wavelength dependencies provide the potential application for aerosol typing.

Moreover, there are four independent equations from Eqs. 5–9, considering Eq. 10. Thus, the four unknowns ( $\phi_a(\lambda_1)$ ,  $\phi_b(\lambda_1)$ ,  $\phi_a(\lambda_2)$ ,  $\phi_b(\lambda_2)$ ) can be calculated as a unique solution.

## 2.2 Mixture of three aerosol components

165 As a following step, more complicated aerosol mixtures were considered in this section, assuming an aerosol population of three aerosol types (denoted with the subscript  $a$ ,  $b$  or  $c$ ). The characteristic depolarization ratios ( $\delta_x$ ) of all three types should be different. *and known*

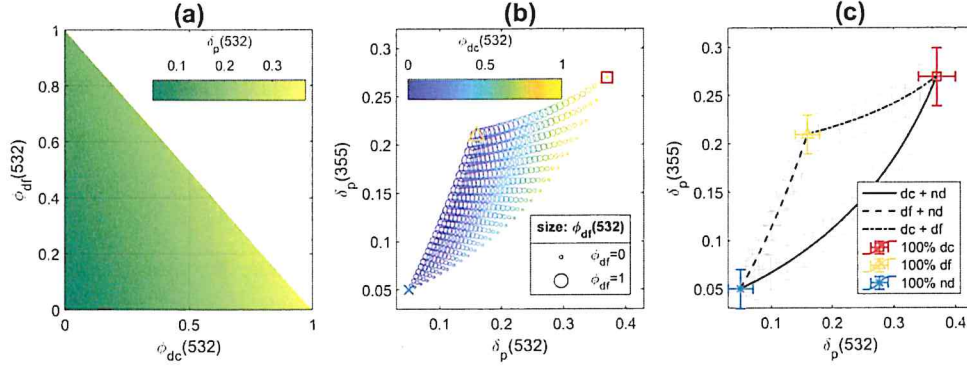
Using Eqs. 2 and 3,  $\delta_p$  of the particle ensemble at wavelength  $\lambda_1$  (or  $\lambda_2$ ) can be expressed by Eq. 11 (or 12). Synthetic examples are given in Fig. 2 for a three aerosol component mixture (coarse dust, fine dust, and spherical non-dust aerosol).  
 170  $\delta_p$  value of the particle ensemble depends on the share of each aerosol type (e.g., Fig. 2a). The pair values of  $\delta_p$  at two wavelengths must remain within the enclosed region predetermined by three boundary curves, and each curve is determined by the characteristics of any two of three types (e.g., using Eq. 10, see Fig. 1b-d). Similar sensitively study was performed based on the Monte Carlo approach, with results shown in Fig. 2(c), using the characteristic values and uncertainties of  $\delta_x$  and  $\hat{A}_{\beta,x}$  (in Table 1). The relationships between the aerosol backscatter fractions at two wavelengths can be derived as Eqs. 13–15, and  
 175 the sum of  $\phi_a(\lambda_1^i)$ ,  $\phi_b(\lambda_1^i)$ , and  $\phi_c(\lambda_1^i)$  is clearly equal to 1. *for  $i=1$  and  $i=2$*  The sum of the three aerosol backscatter fractions at  $\lambda_2$  is also equal to 1 (Eq. 16). Eqs. 13–16 remain valid under the interchange of  $\lambda_1$  and  $\lambda_2$ .

(\*)  
 I am not sure of this reasoning. Eg. 10 is a consequence of eq 5-9. What I see is a system of 6 equations and 4 unknowns



is unknown over the time





**Figure 2.** Synthetic particle linear depolarization ratios ( $\delta_p$ ) of the particle ensemble at 355 and 532 nm for the aerosol mixture with three aerosol types: coarse dust (dc), fine dust (df), and spherical non-dust aerosol (nd). (a)  $\delta_p$  at 532 nm for different backscatter fractions ( $\phi$ ) of coarse and fine dust. (b)  $\delta_p$  at 355 and 532 nm, with coarse dust backscatter fractions ( $\phi_{dc}$ ) shown by color scales, and fine dust backscatter fractions ( $\phi_{df}$ ) shown by marker sizes. (c) Theoretical characteristic curves of  $\delta_p$  at 355 and 532 nm for the two aerosol mixtures are in black lines, with uncertainties from Monte Carlo simulations (using parameters in Table 1). The characteristic values of  $\delta_{dc}$ ,  $\delta_{df}$ , and  $\delta_{nd}$  is shown as red square, yellow triangle, or blue cross, respectively.

$$\delta_p(\lambda_1) = \frac{\frac{\phi_a(\lambda_1)\delta_a(\lambda_1)}{\delta_a(\lambda_1)+1} + \frac{\phi_b(\lambda_1)\delta_b(\lambda_1)}{\delta_b(\lambda_1)+1} + \frac{\phi_c(\lambda_1)\delta_c(\lambda_1)}{\delta_c(\lambda_1)+1}}{\frac{\phi_a(\lambda_1)}{\delta_a(\lambda_1)+1} + \frac{\phi_b(\lambda_1)}{\delta_b(\lambda_1)+1} + \frac{\phi_c(\lambda_1)}{\delta_c(\lambda_1)+1}} \quad (11)$$

$$\delta_p(\lambda_2) = \frac{\frac{\phi_a(\lambda_2)\delta_a(\lambda_2)}{\delta_a(\lambda_2)+1} + \frac{\phi_b(\lambda_2)\delta_b(\lambda_2)}{\delta_b(\lambda_2)+1} + \frac{\phi_c(\lambda_2)\delta_c(\lambda_2)}{\delta_c(\lambda_2)+1}}{\frac{\phi_a(\lambda_2)}{\delta_a(\lambda_2)+1} + \frac{\phi_b(\lambda_2)}{\delta_b(\lambda_2)+1} + \frac{\phi_c(\lambda_2)}{\delta_c(\lambda_2)+1}} \quad (12)$$

$$\phi_a(\lambda_1) = \frac{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2)}{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2) + \eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2) + \eta_c(\lambda_1, \lambda_2)\phi_c(\lambda_2)} \quad (13)$$

$$180 \quad \phi_b(\lambda_1) = \frac{\eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2)}{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2) + \eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2) + \eta_c(\lambda_1, \lambda_2)\phi_c(\lambda_2)} \quad (14)$$

$$\phi_c(\lambda_1) = \frac{\eta_c(\lambda_1, \lambda_2)\phi_c(\lambda_2)}{\eta_a(\lambda_1, \lambda_2)\phi_a(\lambda_2) + \eta_b(\lambda_1, \lambda_2)\phi_b(\lambda_2) + \eta_c(\lambda_1, \lambda_2)\phi_c(\lambda_2)} \quad (15)$$

$$\phi_a(\lambda_2) + \phi_b(\lambda_2) + \phi_c(\lambda_2) = 1 \rightarrow \text{repeat for } \lambda_2 \rightarrow 7 \text{ equations} \quad (16)$$

It is possible to retrieve the six unknowns  $\phi_x(\lambda_i)$  (with  $x$  being  $a$ ,  $b$ , or  $c$ , and  $i$  being 1 or 2) using the six independent equations (Eqs. 11–16) with a unique mathematical solution. For the sake of simplicity, an aerosol-type-dependent term,  $Q_x(\lambda_i)$  <sup>has been</sup> introduced, which is based on the characteristic depolarization ratio ( $\delta_x$ ), as well as the particle linear depolarization ratio of the particle ensemble ( $\delta_p$ ), at a given wavelength (Eq. 17). For three aerosol types and depolarization ratios at two wavelengths, there are six  $Q_x(\lambda_i)$ . Thus, the Eq. 11 or 12 can be simplified as Eq. 18. The expressions of the aerosol backscatter fraction  $\phi_x(\lambda_i)$  can be mathematically derived using Eqs. 13–18. An example of the expression of  $\phi_a(\lambda_2)$  solution is given in Eq. 19. The solution equations for the other two types can apply the same equation, with the indices  $a$ ,  $b$ , and  $c$  interchanged

overdetermined? <sup>8</sup>  
has 7 equations (\*)





190 accordingly. The aerosol backscatter coefficient of one type can be easily calculated from the total backscatter coefficient using the backscatter fraction.

$$Q_x(\lambda_i) = \frac{\delta_p(\lambda_i) - \delta_x(\lambda_i)}{\delta_x(\lambda_i) + 1} \quad (17)$$

$$\phi_a(\lambda_i)Q_a(\lambda_i) + \phi_b(\lambda_i)Q_b(\lambda_i) + \phi_c(\lambda_i)Q_c(\lambda_i) = 0 \quad (18)$$

$$\phi_a(\lambda_2) = \frac{\eta_b Q_b(\lambda_1) Q_c(\lambda_2) - \eta_c Q_c(\lambda_1) Q_b(\lambda_2)}{\eta_a Q_a(\lambda_1) [Q_b(\lambda_2) - Q_c(\lambda_2)] + \eta_b Q_b(\lambda_1) [Q_c(\lambda_2) - Q_a(\lambda_2)] + \eta_c Q_c(\lambda_1) [Q_a(\lambda_2) - Q_b(\lambda_2)]} \quad (19)$$

*what if noise brings the data outside this region?*

### 195 2.3 Uncertainty study

Decomposition of two aerosol component mixture is well studied and reported in many studies. In this section, we present a sensitivity study and explore the uncertainties of the proposed methodology for the decomposition of three aerosol component mixture using particle depolarization ratios at two wavelengths.

*with different fractions of*

200 ~~In the simulation~~, synthetic data representing aerosol mixtures, which may include coarse dust, fine dust, and spherical non-dust aerosol, are utilized with characteristics from Table 1. The pair values of  $\delta_p$  of the aerosol mixture, with whichever the mixing ratio of the three components, should be inside the region bounded by the three characteristic curves. The uncertainties of both the type-specific ~~characteristics~~ *input parameters* and the measured  $\delta_p$  introduce uncertainties on the retrievals of the aerosol backscatter fractions. Here, we first focus on the uncertainty source of the type-specific characteristics and omit the uncertainty of the measured  $\delta_p$ , *to be examined thereafter*

205 Three representative cases are manually selected, with initial  $\delta_p$  values given in Table 2 and Fig. 3(a). The aerosol backscatter fractions can be calculated using Eq. 19, where there are two measured/initial parameters ( $\delta_p$  at 355 and 532 nm), and nine variables ( $\delta_{dc}(355)$ ,  $\delta_{dc}(532)$ ,  $\tilde{A}_{\beta,dc}$ ,  $\delta_{df}(355)$ ,  $\delta_{df}(532)$ ,  $\tilde{A}_{\beta,df}$ ,  $\delta_{nd}(355)$ ,  $\delta_{nd}(532)$ ,  $\tilde{A}_{\beta,nd}$ ). The ideal results without introducing uncertainties are given as "Reference results" in Table 2. A Monte Carlo simulation was conducted involving 10000 draws based on normal distributions of nine variables (Table 1). For each draw, the aerosol backscatter fractions of three components are calculated, resulting the distributions shown in Fig. 3(b-d). The statistical parameters are given in Table 2, where skewness is a measure of the asymmetry of the distribution, and kurtosis is a measure of the flatness of the distribution compared to a normal distribution. The retrieved  $\phi_x$  distributions are also presented as ternary plots in Fig. 3(e), where the color scale represent the frequency of occurrences. We can easily identify areas where there is a greater accuracy/confidence for the  $\phi_x$  retrievals with darker color.

215 For case 1, the pair values of  $\delta_p$  locate in the middle of the enclosed characteristic region. The retrieved backscatter fractions are closer in shape to a Gaussian distribution than the other two cases. The values are reasonably between 0 to 1.  $\delta_p(355)$  and  $\delta_p(532)$  of case 2 are located inside the error bars of the characteristic curve of coarse dust and non-dust aerosol. Thus, for this

*representative of what?  
 the best one, with negative  $\Phi$ , is also unphysical  
 so it cannot be "representative"!*

*(\*)*

*a purely mathematical statistical confidence.  
 Physically, the third case cannot have any*

**Table 2.** Parameters for the uncertainty study. Three cases with different initial particle linear depolarization ratios ( $\delta_p$ ) of the particle ensemble at 355 and 532 nm are used. Reference results are calculated using Eq. 19 without introducing uncertainties. Statistical parameters of retrieved aerosol backscatter fraction  $\phi_x$  of coarse dust (dc), fine dust (df), and non-dust aerosol (nd) are given after Monte Carlo simulations.

	Initial $\delta_p$		Reference results	Monte Carlo results			
	$\delta_p(355)$	$\delta_p(532)$		Mean	Standard deviation	Skewness	Kurtosis
Case 1	0.16	0.19	$\phi_{dc}(532)$	0.33	0.09	0.53	13.63
			$\phi_{df}(532)$	0.42	0.15	-1.78	51.61
			$\phi_{nd}(532)$	0.25	0.07	3.31	107.97
Case 2	0.18	0.28	$\phi_{dc}(532)$	0.74	0.14	1.84	95.39
			$\phi_{df}(532)$	0.08	0.20	-0.96	119.17
			$\phi_{nd}(532)$	0.19	0.08	-0.62	92.74
Case 3	0.10	0.30	$\phi_{dc}(532)$	1.01	0.38	57.08	4527.20
			$\phi_{df}(532)$	-0.46	0.59	-53.35	3906.65
			$\phi_{nd}(532)$	0.45	0.24	36.50	2010.26

$\delta_p$  pair, it is possible that the mixture contains only coarse dust and non-dust aerosol, or contains three aerosol components. For example, a small part of simulated values of  $\phi_{df}$  distribution in Fig. 3(c) is negative due to the uncertainties. In case 3, the pair values of  $\delta_p$  are far away from the characteristic region, only un-physical values (always below 0) were derived for  $\phi_{df}$  (Fig. 3d), and a big portion of  $\phi_{dc}$  are bigger than 1. This case is clearly not a mixture of above mentioned three aerosol components. It could contain other depolarizing particles, e.g., pollen, in the mixture.

As a second step, we concentrate on the ~~random uncertainties~~ <sup>observational uncertainty</sup> on the measured  $\delta_p$ . Reference values of  $\phi_{dc}$ ,  $\phi_{df}$ , and  $\phi_{nd}$  of three cases in Table 2 are used here as inputs. Note that it is purely a mathematical problem, as the system can be solved regardless of whether the values are physically meaningful (e.g., case 3).  $\delta_p(355)$  and  $\delta_p(532)$  are derived using Eqs. 11–15, and they exactly match the initial values. We added several relative uncertainty levels on both  $\delta_p(355)$  and  $\delta_p(532)$  from 0 % to 30 %, and performed Monte Carlo simulations using 10000 draws for each level, considering normal statistical distributions. The uncertainties (including bias and standard deviations) and relative uncertainties on the retrieved  $\phi_x$  for three cases are shown in Fig. 4, and they increase as the uncertainties on  $\delta_p$  increase. Such uncertainties on  $\phi_x$  range from 0.02 to 0.18 when considering typical relative uncertainties on the  $\delta_p$  of 5–10 %. There is the demand of well characterized lidar systems to deliver high-quality depolarization ratios.

### 3 Case studies of mineral dust

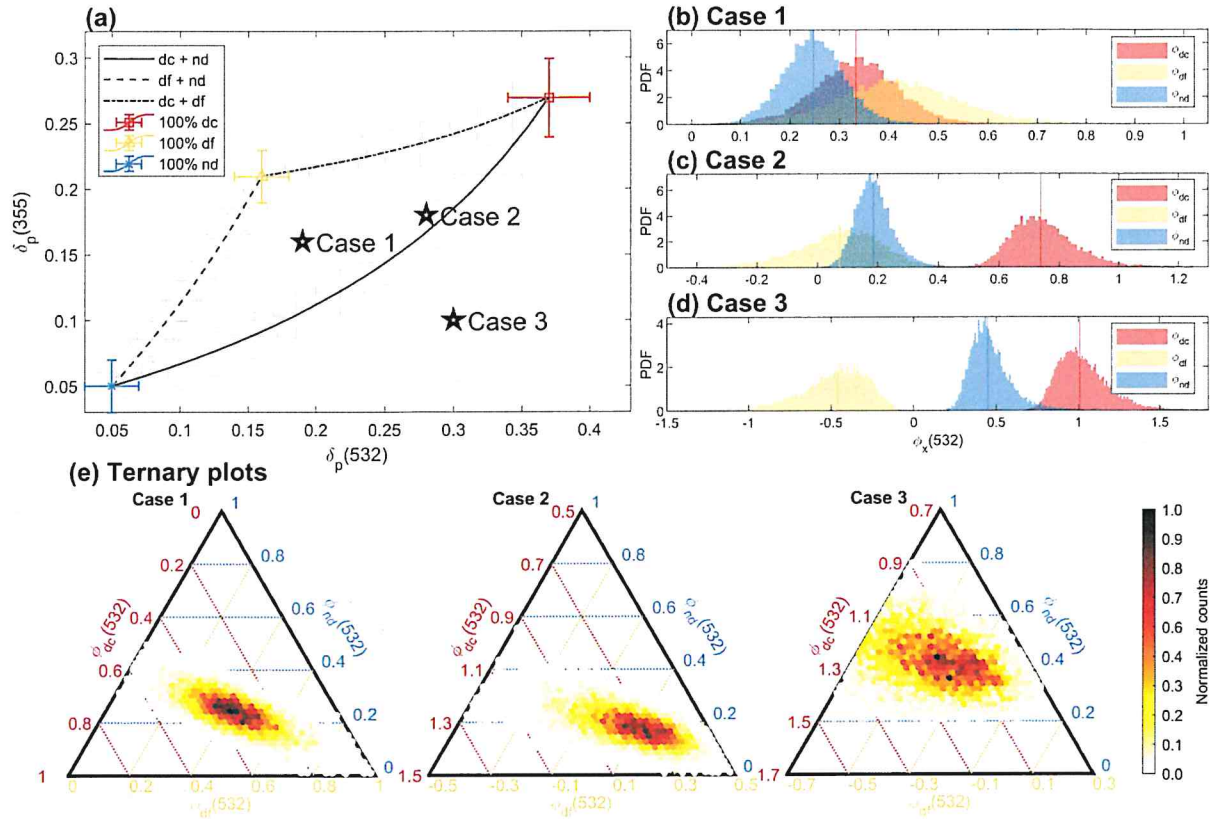
In this section, the algorithm was applied to lidar observations of dust at different regions.

As your retrieval has also a non-dust component, I would reformulate this sentence as follows:  
 "... to lidar observations of aerosols in different dust-affected regions"

This can be better elaborated, citing the average and the best available  $\delta_p$  measurement uncertainties in the literature,

and explaining better what efforts and challenges exist to have accurate  $\delta_p$  observations



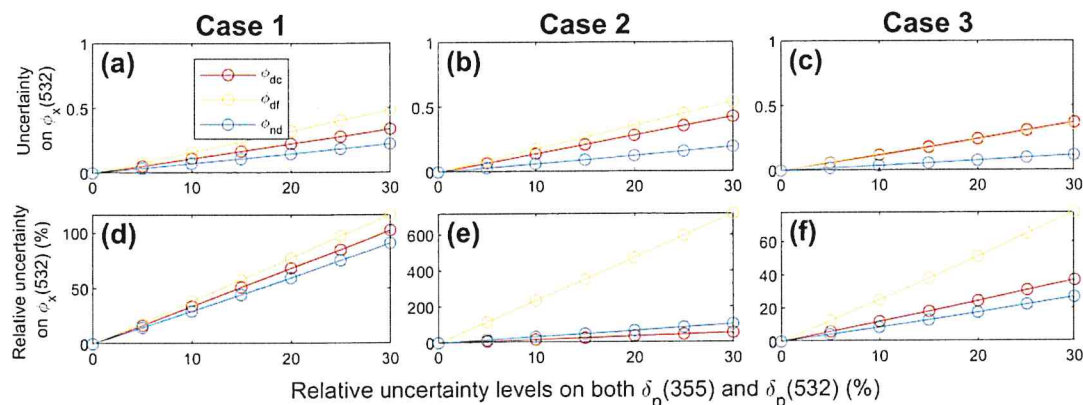


**Figure 3.** (a) Theoretical characteristic curves of  $\delta_p$  at 355 and 532 nm for the 2 aerosol mixtures are in black, with uncertainties from Monte Carlo simulations (using parameters in Table 1). The characteristic  $\delta_x$  of coarse dust (dc), fine dust (df), or spherical non-dust (nd) aerosol are shown as red square, yellow triangle, or blue cross, respectively. (b-d) Probability density function (PDF) estimates of the backscatter fractions ( $\phi_x$ ) of dc, df, and nd aerosol, for each case. Monte Carlo approach was applied. (e) Ternary plots of characteristic  $\phi_x$  for 3 cases, with normalized counts shown as color.

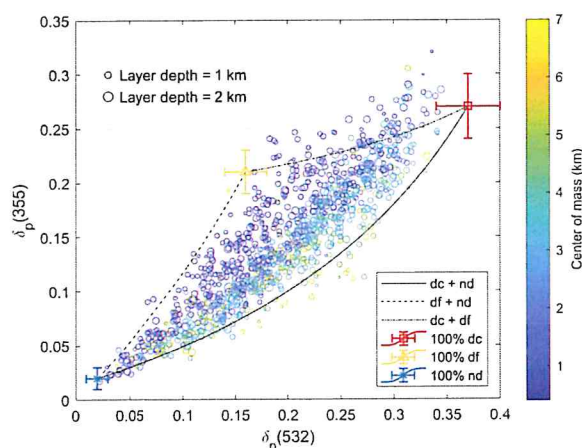
### 3.1 Arabian dust

235 Filioglou et al. (2020) reported the aerosol particle properties of Arabian dust over a rural site in the United Arab Emirates, during the 1 year measurement campaign between March 2018 and February 2019, within the framework of the Optimization of Aerosol Seeding In rain enhancement Strategies (OASIS) project. Among 1130 night-time aerosol particle layers,  $\delta_p$  at both 355 and 532 nm are available for 1063 layers. These layer-mean  $\delta_p$  are plotted in Fig. 5, with center mass of the layers shown by color scale, and layer depths shown by marker sizes.

240 The measurement site is a receptor of frequent dust events, three possible aerosol types are assumed to be present in these layers: coarse and fine dust (with characteristics in Table 1), and the spherical non-dust aerosols with anthropogenic and/or marine origin. From the lidar measurements, the mean values of the depolarization ratios for the non-dust aerosols ( $\delta_{nd}$ ) are



**Figure 4.** Estimated uncertainties (a–c) and relative uncertainties (d–f) on the retrieved backscatter fractions ( $\phi_x$ ) at 532 nm of coarse dust (dc), fine dust (df), or spherical non-dust (nd) aerosols, against the applied relative uncertainties on the particle linear depolarization ratios at both 355 and 532 nm ( $\delta_p(355)$  and  $\delta_p(532)$ ). Monte Carlo approach was applied.



**Figure 5.** Scatter plot of layer-mean particle linear depolarization ratios ( $\delta_p$ ) of the particle ensemble at 355 and 532 nm of Arabian dust layers observed over United Arab Emirates. The altitude of the center of mass of the layers are shown by color scale, and layer depths shown by marker sizes. Theoretical characteristic curves of  $\delta_p$  at 355 and 532 nm for the two aerosol mixtures are in black lines. Characteristic  $\delta_x$  of coarse dust (dc), fine dust (df), or spherical non-dust (nd) aerosol is shown as red square, yellow triangle, or blue cross, respectively.

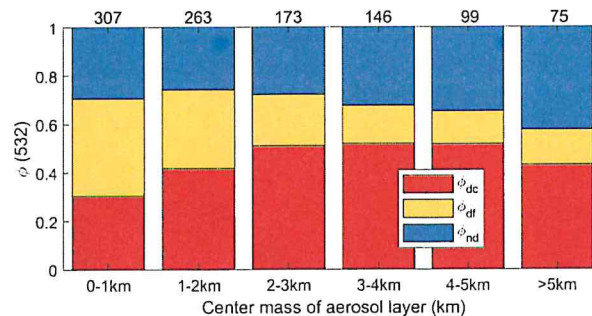
(355, 532)

derived as  $0.02 \pm 0.01$  at both 355 and 532 nm.  $\hat{A}_{\beta, nd}$  is assumed as 2 (cf., Table 1). The majority of the cases are well within the boundaries defined by the characteristic values of the three-aerosol-component method. A few  $\delta_p$  pairs are above the characteristic curve of coarse and fine dust. This could be an indication that the  $\delta_x$  at 355 nm for pure Arabian dust (for both coarse and fine mode) may have slightly higher values. It may also be that the commonly reported layer-mean values which are

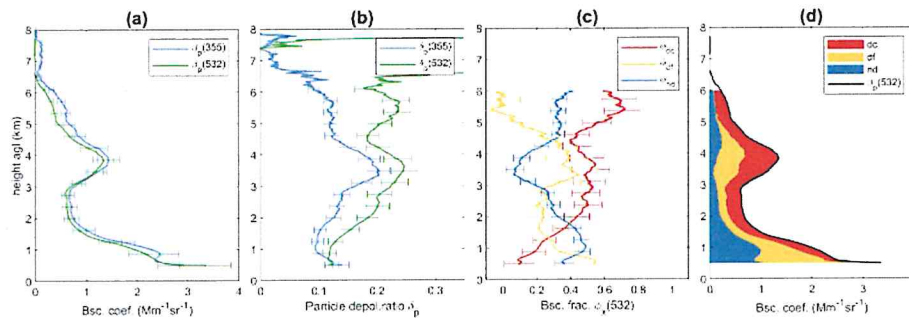
use these higher values determined experimentally  
as new  $\delta_{cd}$  and  $\delta_{fd}$  (\*)

(\*) Interesting result worth discussing in the paper  
This figure suggests that dust with a high center of mass is coarse (and dust mixed with non-dust) and dust with a lower center of mass is fine.





**Figure 6.** Height-dependent aerosol backscatter fractions ( $\phi_x(532)$ ) of coarse dust (dc), fine dust (df), and non-dust (nd) aerosol, for Arabian dust layers observed over United Arab Emirates. Layer numbers are given on the top.



**Figure 7.** An example of lidar-derived optical profiles (time-averaged at 00:10–01:09 on 4 August 2018 over United Arab Emirates). (a) Particle backscatter coefficients and (b) particle linear depolarization ratio ( $\delta_p$ ) at 355 and 532 nm. (c) The retrieved backscatter fractions ( $\phi$ ) of coarse dust (dc), fine dust (df), and non-dust (nd) aerosols at 532 nm, with uncertainties (shown by error bars) calculated using Monte Carlo approach following method in Sect. 2.3. (d) Separation of 3 aerosol backscatter coefficients at 532 nm.

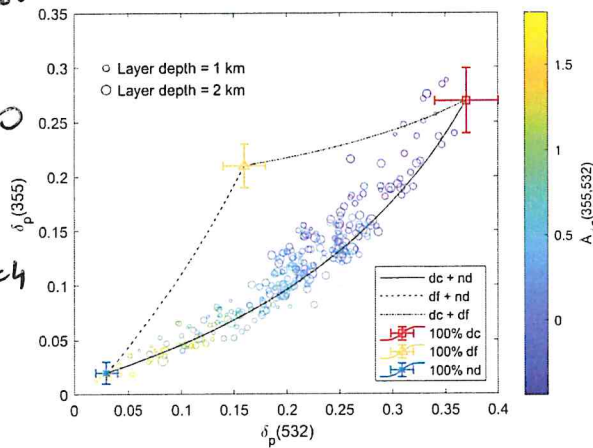
test this with the data before averaging (\*)  
 often calculated using smoothed optical parameters may lower the true characteristic value of dust particles. To this direction, measuring the characteristics of pure dust particles, e.g., in laboratory experiments, or on the field, would be beneficial.

The aerosol backscatter fractions of the three aerosol components are calculated using Eq. 19.  $\delta_p$  pairs located outside the region may result in negative or values above one for  $\phi_x$ . To avoid introducing a bias, these negative or above one values are included in the analysis, as a large dataset is utilized. Final values of  $\phi_x(532)$  are grouped using the center mass of aerosol layers and shown in Fig. 6. The non-dust aerosol contribution is increasing the higher the aerosol layer is in the atmosphere and at the same time the fine dust contribution is decreasing. Coarse dust contributes more at heights between 2 to 5 km, which is in line with Fig. 7 of Filioglou et al. (2020) where higher  $\delta_p$  at 532 nm has been detected. An example of vertical profiles is given in Fig. 7. The fine dust and the non-dust aerosols dominant the lowest layer below 1.5 km. The lofted layer between 3 and 4.5 km presents enhanced  $\delta_p$ , containing mainly coarse and fine dust. A higher disparity between  $\delta_p$  at 355 and 532 nm was found for an upper layer between 5 and 6 km, revealing a mixture of coarse dust and non-dust aerosol particles.

as also seen from Fig. 5!



$\tilde{A}$  is generally associated to particle size  
 large p. = geom. optics  $\Rightarrow \tilde{A} = 0$   
 fine p.  $\Rightarrow \tilde{A} = 1 \div 2$   
 molecules (Rayleigh sc.)  $\Rightarrow \tilde{A} = 4$   
 So this result is rather expected!



**Figure 8.** Scatter plot of layer-mean particle linear depolarization ratios ( $\delta_p$ ) of the particle ensemble at 355 and 532 nm of Central Asian dust layers observed over Dushanbe. The layer-mean backscatter-related Ångström exponents ( $\tilde{A}_{\beta,p}$ ) are shown by color scale, and the layer depths by marker sizes. Theoretical characteristic curves of  $\delta_p$  at 355 and 532 nm for the 2 aerosol mixtures are in black. Characteristic  $\delta_x$  of coarse dust (dc), fine dust (df), or spherical non-dust (nd) aerosols are shown as red square, yellow triangle, or blue cross, respectively.

### 3.2 Asian dust

Central Asia is one of the hot spot regions facing significant environmental challenges and climate-change effects. Hofer et al. (2020) presented a dense data set of lidar observations for a Central Asian site during the 18 month campaign from March 2015 to August 2016, at Dushanbe, Tajikistan, in the framework of the Central Asian Dust EXperiment (CADEX) project. They found broad distributions of optical properties of the 276 aerosol layers, reflecting the occurrence of very different aerosol conditions with aerosol mixtures consisting of mineral dust, soil dust, and anthropogenic pollution.

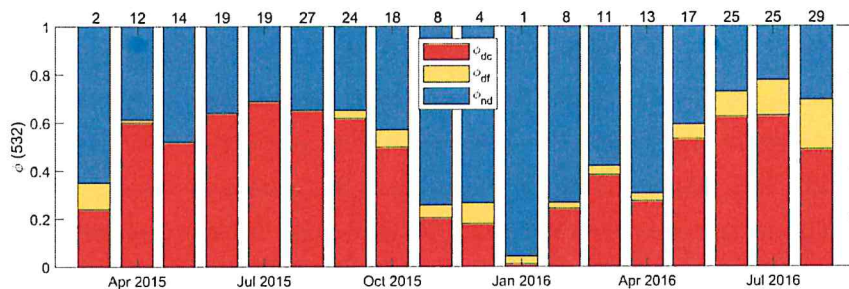
Layer mean  $\delta_p$  at 355 and 532 nm are shown in Fig. 8, with the layer mean  $\tilde{A}_{\beta,p}$  shown by color scale, and the layer depths by marker sizes. As already discussed in Hofer et al. (2020), with decreasing extinction-related Ångström exponents, the  $\delta_p$  at two wavelengths increase. For the aerosol component separations, we considered three aerosol types in those layers: coarse and fine dust (with characteristics in Table 1), and non-dust aerosols. Hofer et al. (2020) derived the mean values of  $\delta_{nd}$  as  $0.02 \pm 0.01$  or  $0.03 \pm 0.01$  at 355 or 532 nm, respectively.  $\tilde{A}_{\beta,nd}$  is assumed as 2 (cf., Table 1). The pair values of  $\delta_p$  are mostly located close to the characteristic curve of coarse dust and non-dust aerosol. The aerosol backscatter fractions are calculated (Eq. 19) and shown in Fig. 9, as time series. <sup>largest</sup> Highest dust contributions were found during the summer season, with coarse (or fine) dust contributes 61 % (or 8 %) on the backscatter coefficients at 532 nm. During spring and autumn, dust (including coarse and fine mode) and non-dust aerosols have nearly equal contributions. Only during winter months, non-dust (e.g., urban haze) dominates with 75 % on the backscatter coefficients.

Hu et al. (2020) documented 1 month East Asia dust aerosol observations over Kashi, China, in April 2019. The dust particles originate <sup>↓</sup> mainly from the Taklamakan desert. The measured  $\delta_p$  of dust layers <sup>were</sup> are about  $0.28\text{--}0.32 \pm 0.07$ ,  $0.36 \pm 0.05$ , and

"highest" could refer to higher altitude, whereas here you refer to larger contributions

these are usually the same thing. do you mean local vs. transported dust?





**Figure 9.** Monthly means of aerosol backscatter fractions ( $\phi_x(532)$ ) of coarse dust (dc), fine dust (df), and non-dust (nd) aerosol, for Central Asian dust layers observed over Dushanbe. Layer numbers are given on the top.

0.31  $\pm$  0.05 at 355, 532, and 1064 nm, respectively. These  $\delta_p$  are higher than the typical values of Asian dust in the literature (Murayama et al., 2004; Dieudonné et al., 2015; Hofer et al., 2017). The reason could be linked to the fact that observations were near the dust source region, and there would be a large fraction of coarse and giant dusts particles. They described four representative cases with six dust layers. The  $\delta_p$  values of two pure dust layers are 0.32 at 355 nm and 0.31 at 1064 nm, which are higher than the characteristic depolarization ratios of coarse dust (0.27 at 355 nm and 0.27 at 1064 nm in Table 1). For the four polluted dust layers, two of them have higher  $\delta_p$  at 355 nm and 1064 nm compared to the  $\delta_{dc}$ . Those values make the application of the algorithm unsuitable, as the  $\delta_p$  pairs locate outside the characteristic region, hence, the results would yield some un-physical values (below zero or above one as the fraction). The characteristic depolarization ratios of Taklamakan desert dust need to be determined, especially at wavelengths 355 and 1064 nm. The inclusion of giant dust particles may have impact on the characteristic depolarization ratios of coarse dust type when performing the decomposition.

### 3.3 Saharan dust

Many research studies have explored the geometric and optical characteristics of Saharan dust layers through lidar observations (e.g., Groß et al., 2011; Ansmann et al., 2003; Groß et al., 2015; Szczepanik et al., 2021). In this section, available lidar observations of the Saharan dust depolarization ratios at all three classical lidar wavelengths (355, 532 and 1064 nm) are considered. The small and spherical particles affect the back-scattering at shorter wavelengths more effectively than at longer wavelengths, whereas longer wavelengths are more sensitive to large particles.

Haarig et al. (2022) (referred as Ha22 further on) reported two case studies of Saharan dust layers observed over Leipzig, Germany. In the first pure-dust case in February 2021, Saharan dust plumes reached the observation station in less than 2 d after emission, exhibiting  $\delta_p$  of 0.242  $\pm$  0.024, 0.299  $\pm$  0.018 and 0.206  $\pm$  0.010 at 355, 532 and 1064 nm, respectively. In the second polluted-dust case in March 2021, the dust spent about 1 week in transportation, and the dust plume mixed with European haze. Such dust layers have  $\delta_p$  of 0.174  $\pm$  0.041, 0.298  $\pm$  0.016 and 0.242  $\pm$  0.007 at 355, 532 and 1064 nm, respectively. Haarig et al. (2017a) (referred as Ha17) documented the lidar observations in Saharan dust layers over Barbados in the summer seasons of 2013 and 2014, in the framework of the Saharan Aerosol Long-range Transport and Aerosol-Cloud-



Interaction Experiment (SALTRACE).  $\delta_p$  for long-range-transported (after approximately 1 week transport over the tropical Atlantic) Saharan dust layers were found to be  $0.252 \pm 0.030$ ,  $0.280 \pm 0.020$ ,  $0.225 \pm 0.022$  at 355, 532 and 1064 nm, respectively. Hu (2018) (referred as Hu18) described two cases of lidar measurements of long-range-transported Saharan dust observed at ATOLL observatory in Lille, France. The value ranges of  $\delta_p$  were 0.25–0.26 (0.25–0.27), 0.25–0.28 (0.24–0.26), 0.17–0.21 (0.20–0.22) at 355, 532, 1064 nm for the first case in March 2017 (or the second case in October 2017), respectively.

The pair values of  $\delta_p$  of these cases are presented in Fig. 10 to investigate the aerosol mixing states. We assume that there are coarse dust (dc), fine dust (df), and non-dust (nd) aerosols in the mixture, with characteristic values of  $\delta_x$  and  $\text{\AA}_{\beta,x}$  as given in Tables 1. The characteristics of background non-dust aerosols for these cases are different, but here we consider them as the same for the simplification. The two cases of Ha22 are located well on the characteristic curves of dc & df, or dc & nd, respectively, for  $\delta_p$  pairs both at 532 & 355 nm (Fig. 10a), and at 532 & 1064 nm (Fig. 10b). In the first case, dust plumes were directly transported towards to the station, thus, only dust (both coarse and fine mode) is contained within the observed plume. In the second case,  $\delta_p$  reveal the impact of aerosol pollution mixed into the dust layers after the transportation, and it seems that the remaining dust are mainly coarse mode. The other three cases of Ha17 and Hu18 are mostly located around the characteristic curve of dc & df considering  $\delta_p$  pairs at 355 & 532 nm (Fig. 10a), or located inside the enclosed characteristic region of three types regarding  $\delta_p$  pairs at 532 & 1064 nm (Fig. 10b). It should be noted that the values reported by Ha17 are the average over 21 individual cases of long-range-transported dust.

Apart from the first case of Ha22, all cases were long-range-transported dust. Results reveal that coarse dust contribute a lot in these layers. The dust particle size distribution can change quickly because of the dry deposition (e.g., gravitational settling). However, observations have consistently shown that coarse dust, or even giant dust, are able to transport much farther than previously expected, and can have longer atmospheric lifetime (e.g., Mallios et al., 2021; Ryder et al., 2018, 2019; van der Does et al., 2018; Denjean et al., 2016).

## 4 Conclusions

Polarization-based algorithms have been developed and widely used for the decomposition of two aerosol components. The two-step POLIPHON method allows separating three aerosol components under the assumption about the spherical particle fraction. The measurements of depolarization ratios at multiple wavelengths from a single or multiple lidars have become increasingly common, with availability continuing to expand. In this study, we present an extended methodology, using the particle linear depolarization ratios measured at two wavelengths, for the decomposition of three aerosol components, to retrieve the aerosol-type-specific backscatter fractions. This algorithm can be utilized for an almost unambiguous separation of aerosol components, on the condition that their characteristic depolarization ratios are different. And it requires the proper knowledge of characteristic depolarization ratios and backscatter-related Ångström exponent of each aerosol type. Therefore, laboratory and modeling studies, or for a layer with only one aerosol component in atmospheric conditions, to characterize pure particles would be beneficial, and increase the accuracy for the retrievals. Furthermore, a good characterization of the lidar system is necessary to provide the depolarization ratio with a small uncertainty. The relationship between particle

use your equations to assess what max. bias and uncertainty are needed for this method  
 QUANTIFY THE REQUIRED BIAS AND UNCERTAINTY